

A. [3 pts] Rank the batteries according to *absolute value of the potential difference across each battery*, from largest to smallest. Explain.

Because all batteries are assumed ideal and identical, the absolute value of the potential differences across all batteries are the same.

B. [5 pts] Is the brightness of bulb B *greater than, less than,* or *equal to* the brightness of bulb A? Explain. If either bulb does not light, state so explicitly.

Consider the (clockwise) loop starting at point X, containing battery 2, battery 3, and bulb B. Battery 2 provides a potential gain and battery 3 provides a potential drop of the same magnitude. For the sum of the potential differences around the loop to be zero, the potential difference across bulb B must be zero. This means **bulb B does not light**, whereas bulb A does because battery 1 sets a non-zero potential difference across it. Therefore the brightness of bulb B is **less than** that of bulb A.

C. [5 pts] Is the brightness of bulb D *greater than, less than,* or *equal to* the brightness of bulb A? Explain. If bulb D does not light, state so explicitly.

As above, battery 1 sets a potential difference across bulb A equal to that of one battery. Consider the (clockwise) loop starting at point Y, containing batteries 4, 6, and 5, and bulb D. Battery 4 provides a potential gain, while batteries 5 and 6 each provide a potential drop of the same magnitude. Thus from the bottom of bulb D to the top, there must be a gain in potential equal to that of one battery to make the sum of the potential differences zero. Since brightness is an indicator of potential difference across a bulb, the ranking by the brightness is the same as by potential difference. Thus the brightness of bulb D is **equal to** that of bulb A.

D. [4 pts] On the diagram for *circuit III* above, indicate the direction of the current through each of the batteries. Explain.

Current flows through a bulb from high potential to low. In the answer to part B, it was determined that the top of bulb D is at a higher potential than the bottom, so the current must flow down through bulb D. Series elements have the same current flowing through them, so the current through batteries 4 and 5 are also down. Battery 6 sets the top of bulb E at a higher potential than the bottom, so the current through bulb E is also down. Considering the junction at point Z, the current flows into the junction from battery 5 and bulb E, meaning the current through battery 6 is up.

E. [3 pts] Is the current through battery 6 *greater than*, *less than*, or *equal to* the current through battery 5? Explain.

Applying the results from part D to the junction at point Z, the current through battery 5 equals the current through battery 5 <u>plus</u> that through bulb E. Thus, the current through battery 6 is **greater than** the current through battery 5.