

Exotics 2020 from LHCb

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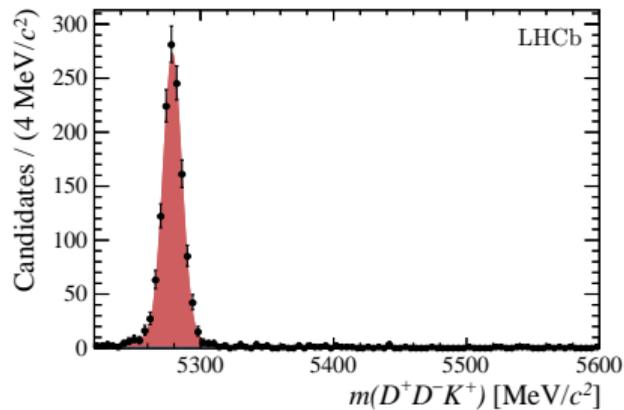


- 1 $X(2900)$ in $B^+ \rightarrow D^+ D^- K^+$
(in preparation)
- 2 $J/\psi J/\psi$ from LHCb
arXiv:2006.16957
- 3 Spin and parity of the vector-vector system
arXiv:2007.05501

$X(2900)$ in $B^+ \rightarrow D^+ D^- K^+$
(in preparation)

$B^+ \rightarrow D^+ D^- K^+$ reaction: [CERN seminar by Dan Johnson]

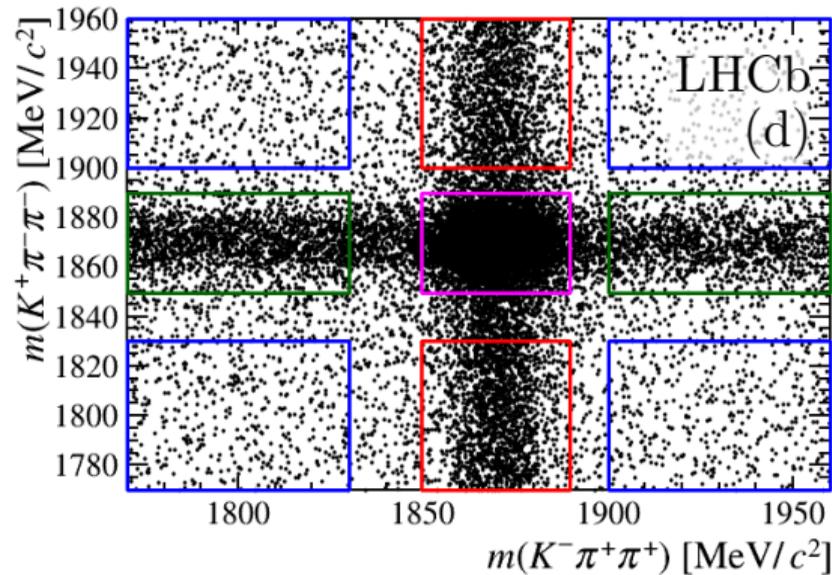
Preliminary



Clean topology, negligible background

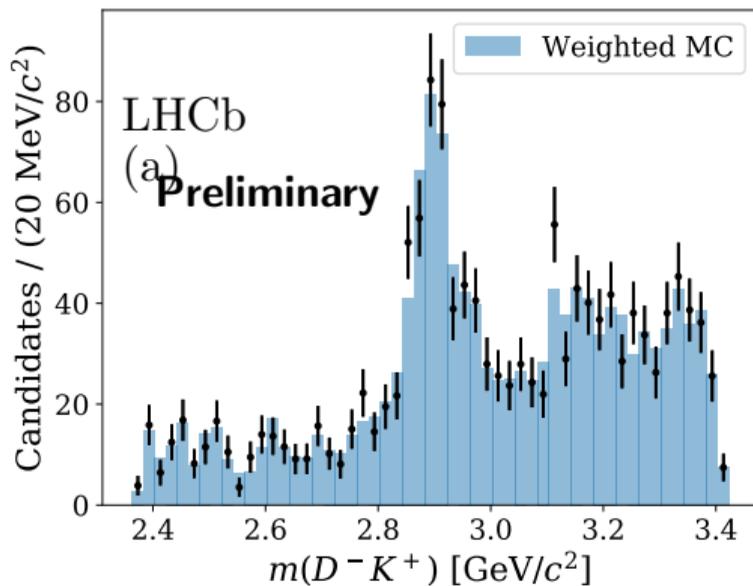
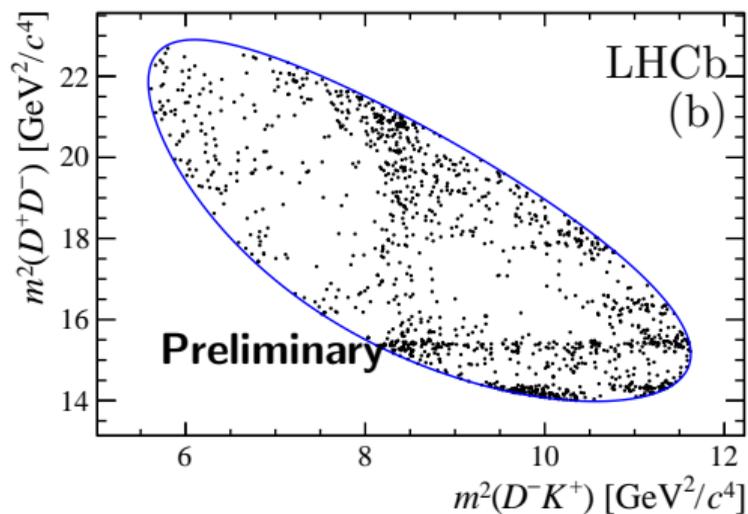
- B flights out of interaction point
- $D^\pm \rightarrow K^\mp \pi^\pm \pi^\pm$

9 fb^{-1} : Run 1 + Run 2 data



Dalitz plot for $B^+ \rightarrow D^+ D^- K^+$

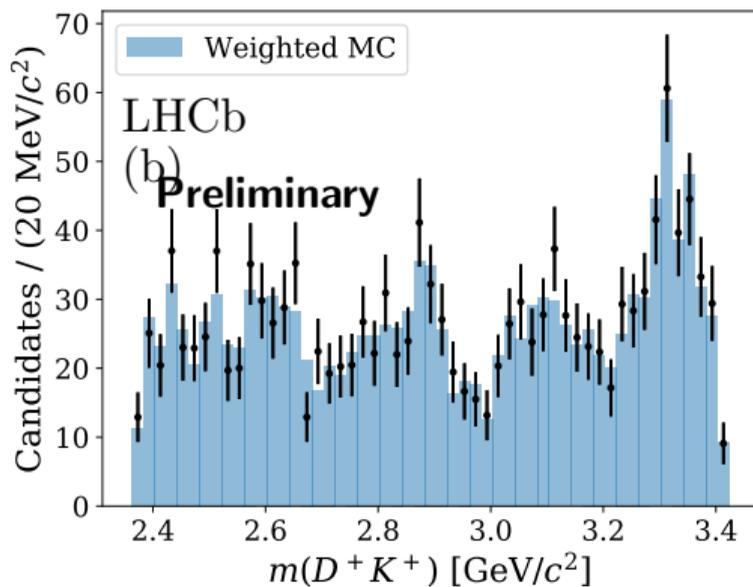
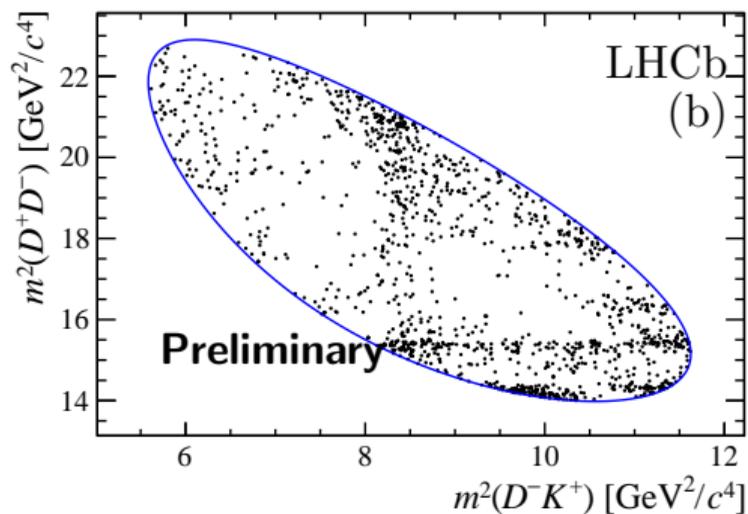
[LHCb (in preparation)]



- Horizontal lines are resonances in $D^+ D^-$
- Huge peak at 2.9 GeV in $D^- K^+$: $(\bar{c}d)(\bar{s}u)$
- Peaks in $D^+ K^+$: reflections?

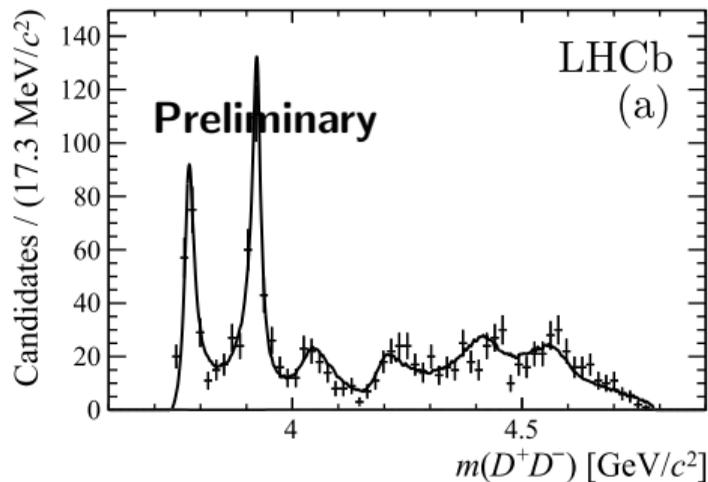
Dalitz plot for $B^+ \rightarrow D^+ D^- K^+$

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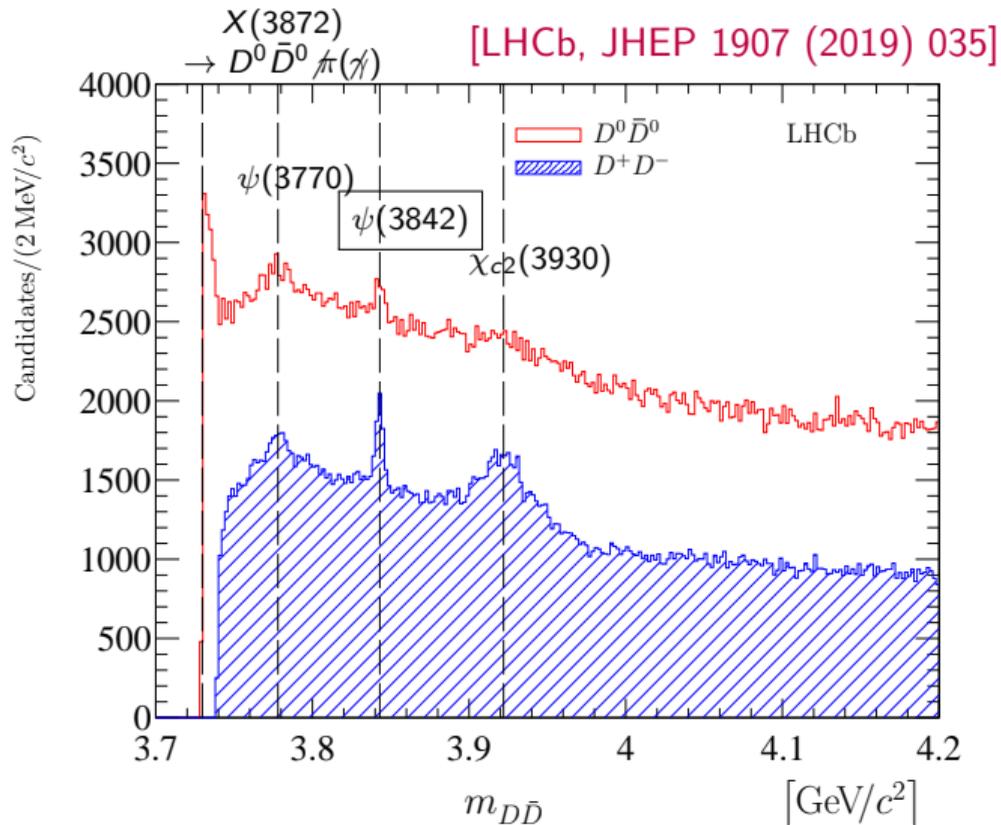
$D\bar{D}$ spectroscopy



Natural parity charmonia above D^+D^- threshold:

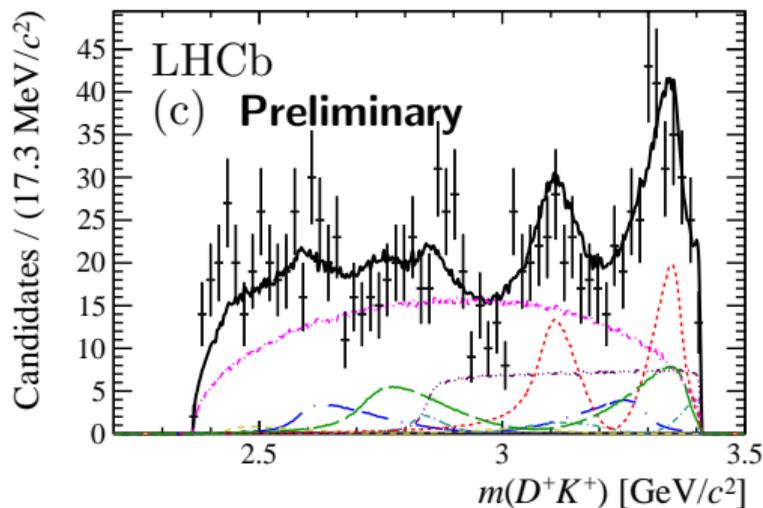
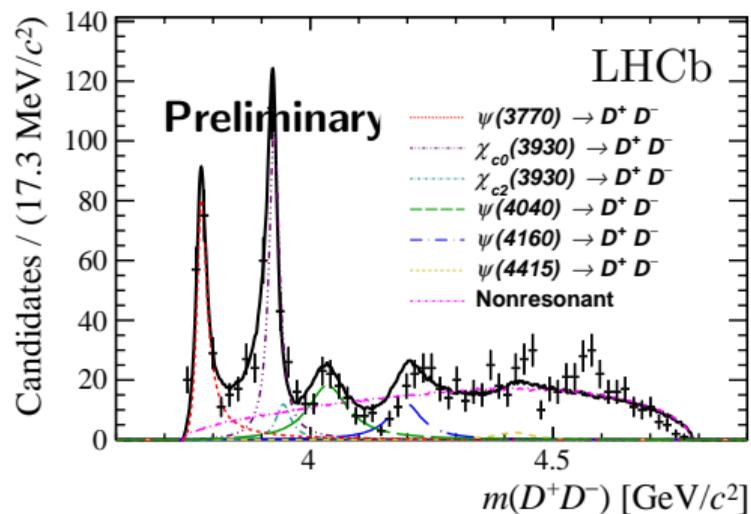
- $\psi(3770)$, $\chi_{c0}()$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$, $\psi(4415)$

Compare to inclusive DD spectra:



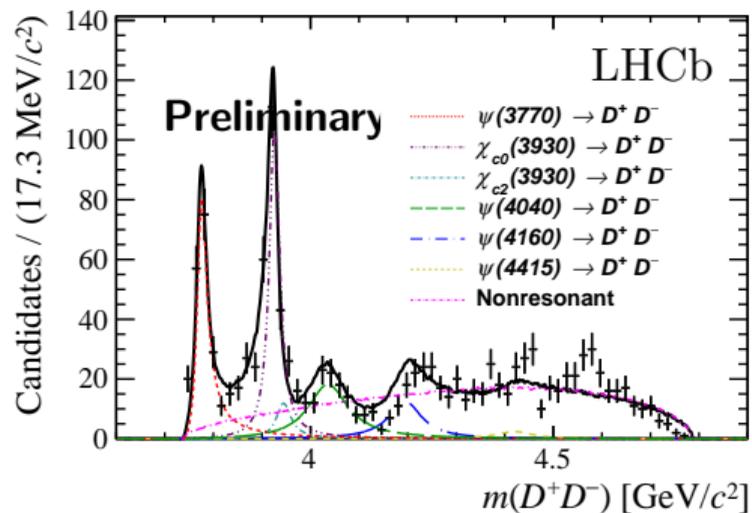
Fit with no exotics

[LHCb (in preparation)]

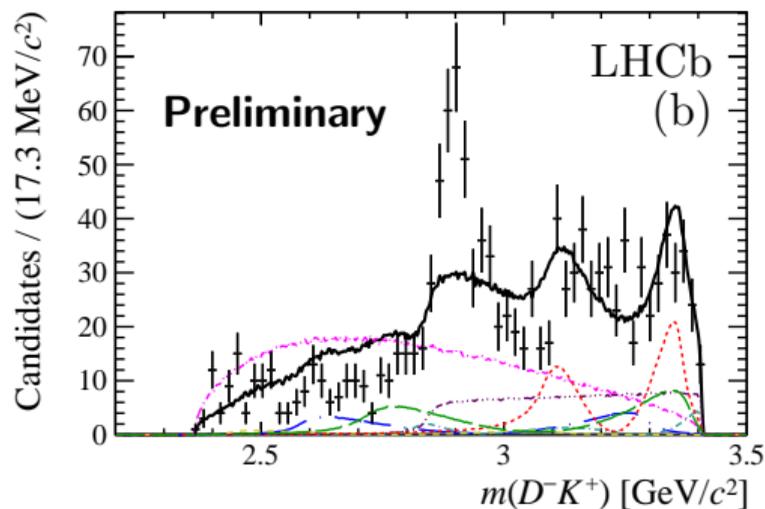


- One can get a "reasonable" description of D^+D^- and D^+K^+ ,
- the D^-K^+ projection has a clear additional structure

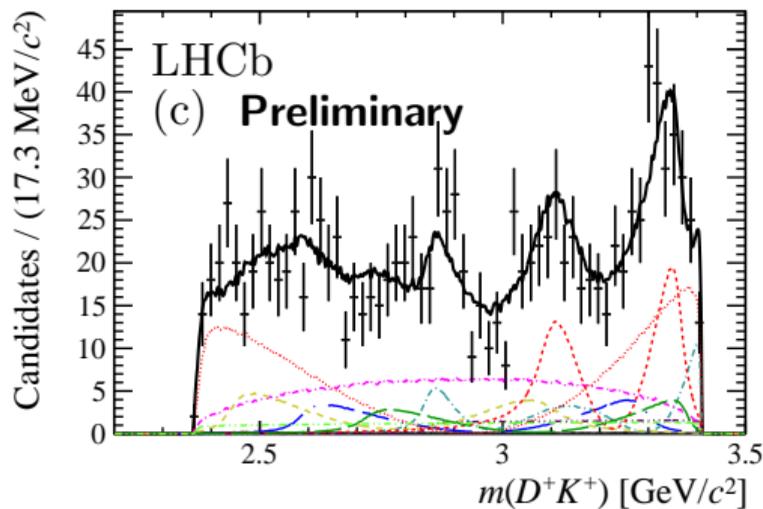
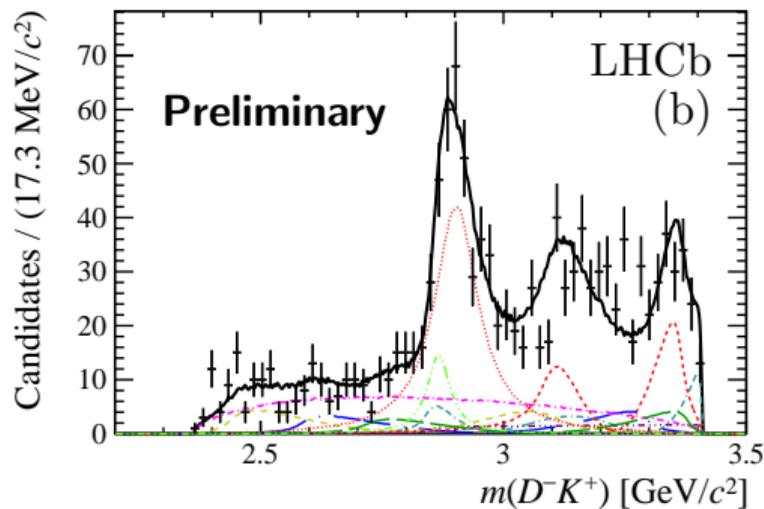
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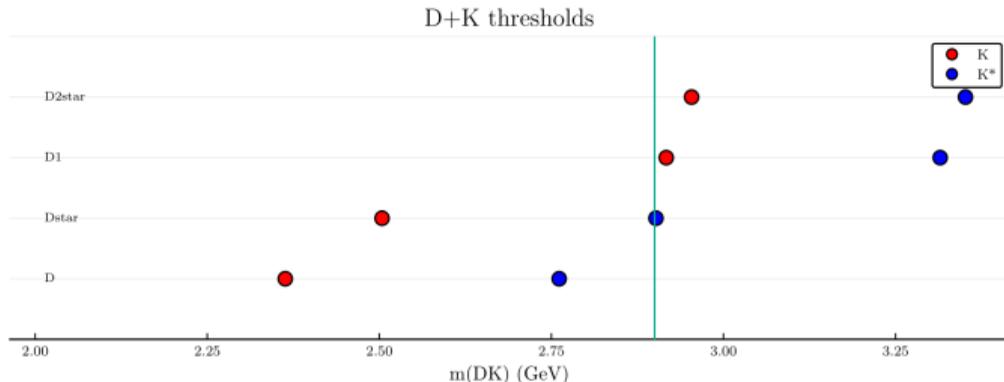
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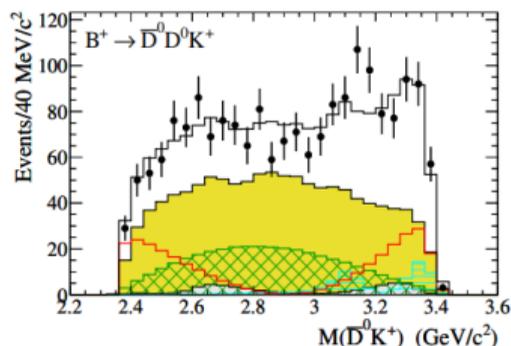
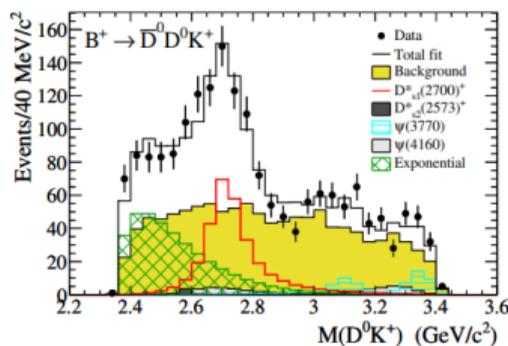
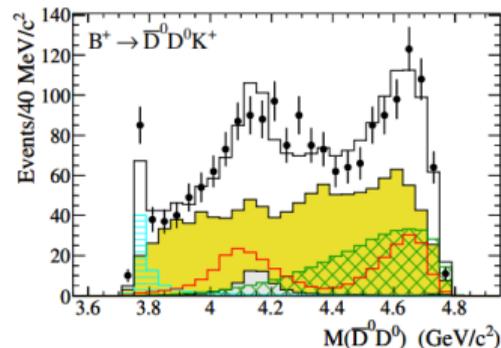
- $X_1(2900)$: $m = (2904 \pm 5 \pm 1) \text{ MeV}$, $\Gamma = (100 \pm 10 \pm 4) \text{ MeV}$
- $X_0(2900)$: $m = (2866 \pm 6 \pm 2) \text{ MeV}$, $\Gamma = (57 \pm 12 \pm 4) \text{ MeV}$

Some thoughts on $D^- K^+$ exotics

- Nearby thresholds: $D^* K^*$, $D_1 K$
- Isospin of $\bar{c}\bar{s}ud$ can be $I = 0$, and $I = 1$.
 - ▶ $\bar{c}\bar{s}uu$ would show up in $\bar{D}^0 K^+$
 - ▶ $\bar{c}\bar{s}dd$ would show up in $D^+ K^0$



$B^+ \rightarrow D^0 \bar{D}^0 K^+$ by BaBar



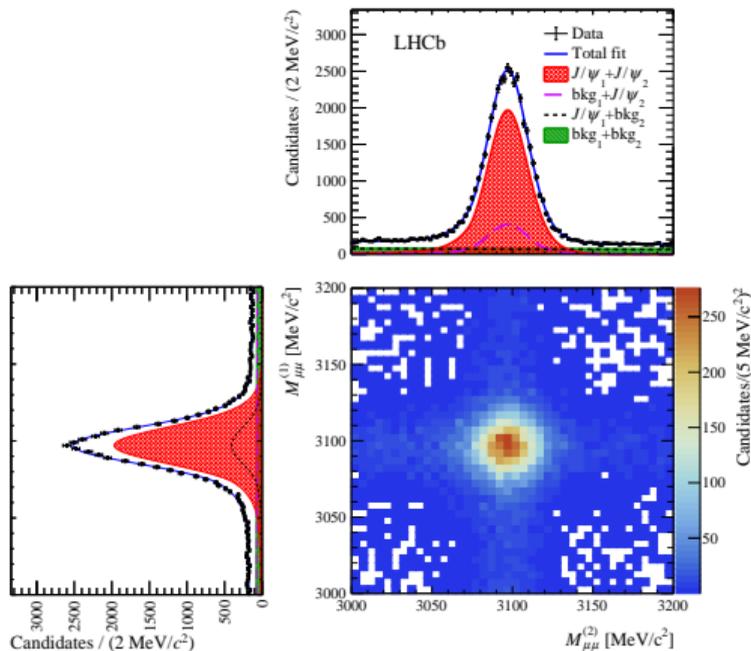
[Phys.Rev.D 91 (2015) 5, 052002].

There are many systems to look at in the $B \rightarrow DDK$ family

$J/\psi J/\psi$ from LHCb
arXiv:2006.16957

Observation of the prompt $J/\psi J/\psi$ pairs

[LHCb, 2006.16957]



- Full statistics: Run 1 + Run 2
- Inclusive: $pp \rightarrow J/\psi J/\psi X$ (4μ tracks from the same PV)
- $N_{J/\psi J/\psi} \approx 34 \text{ k}$ candidates
- Important kinematic variables: $m_{J/\psi J/\psi}$, $p_t(J/\psi J/\psi) = p_{t1} + p_{t2}$.

Understanding the background

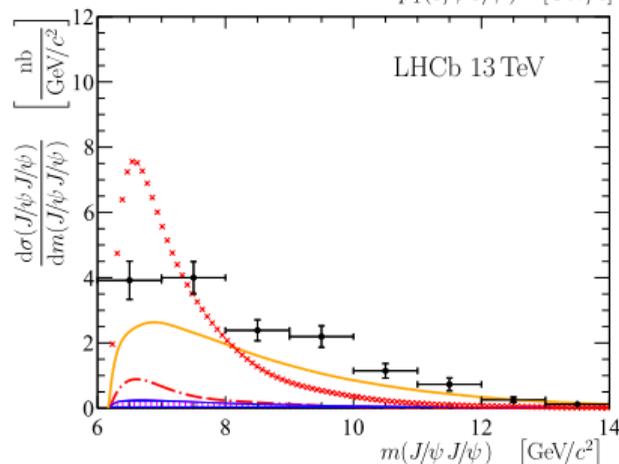
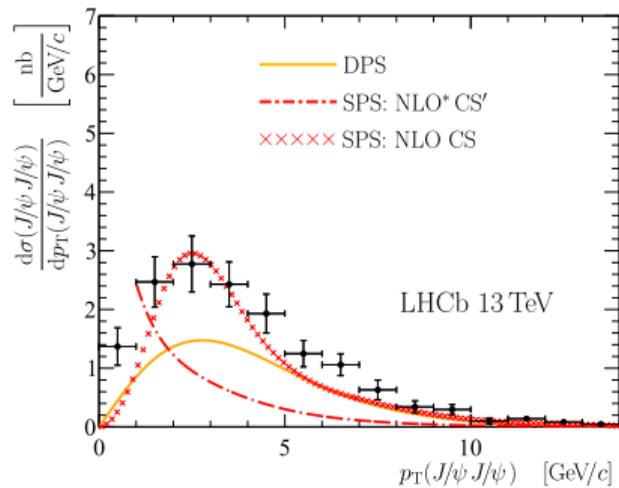
SPS, DPS [LHCb, JHEP 47, arXiv:1612.07451]

Single-parton scattering (SPS)

- $gg \rightarrow J/\psi J/\psi$: the $cc\bar{c}\bar{c}$ is produced in a single interaction of partons (gluons)
- Expected to dominate low masses
- Vanishes at high p_t

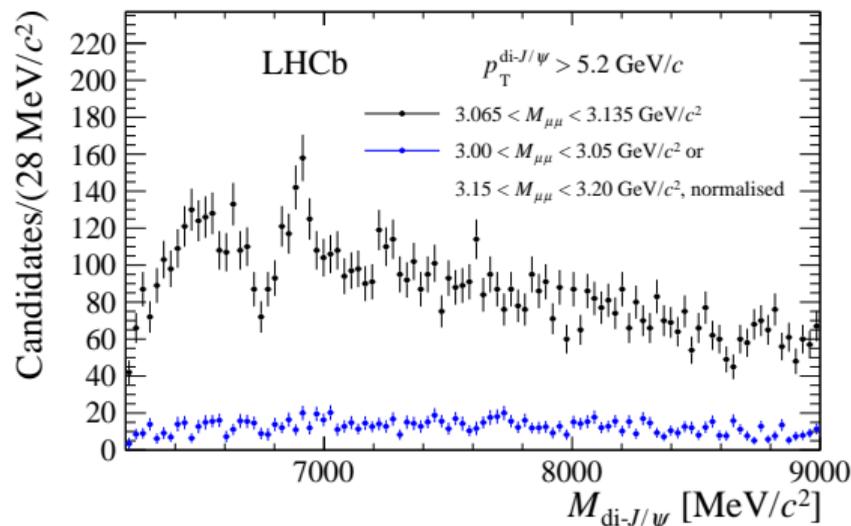
Double-parton scattering (DPS)

- $gg \rightarrow J/\psi$ twice: almost uncorrelated J/ψ .
- Expected to dominate at high masses
- Vanishes at high p_t



Spikes at the near-threshold region

[LHCb, 2006.16957]



Features

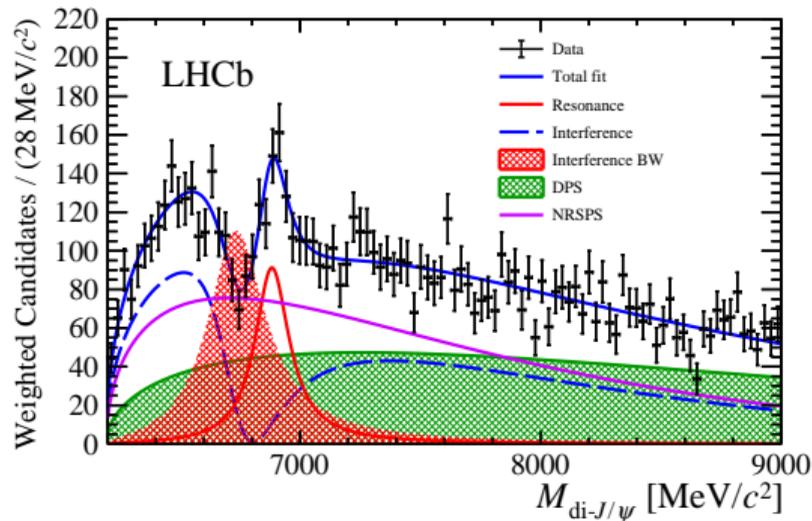
- Rapid start at threshold
- Sharp Deep at 6.8 GeV
- Peak at 6.9 GeV.
- Long continuous spectrum

- Fix DPS model at high energy, $> 10 \text{ GeV}$
- Release SPS shape and strength
- Add a couple of poles to the amplitude with BW functions

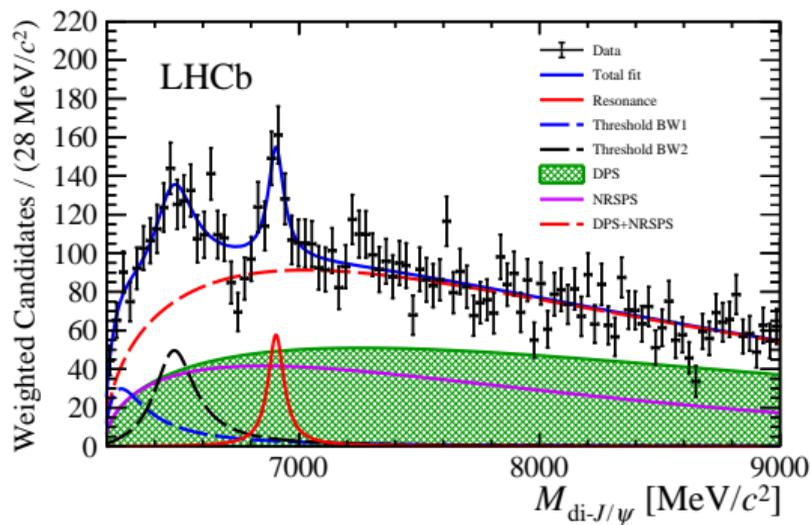
Two exaggerated models: interference, no interference

[LHCb, 2006.16957]

SPS: $gg \rightarrow J/\psi J/\psi$



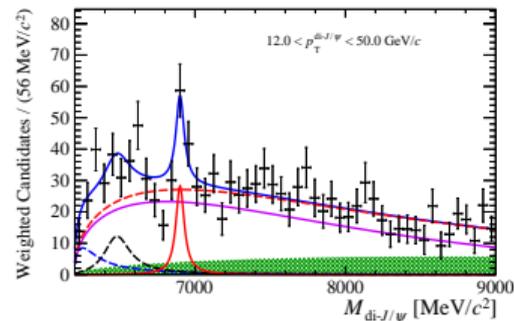
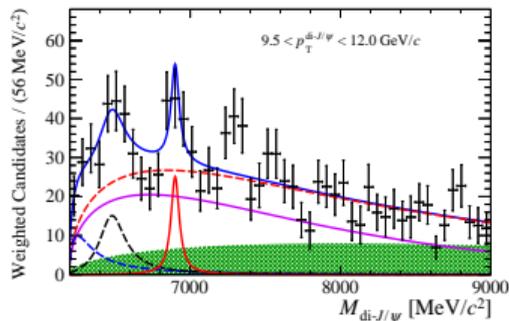
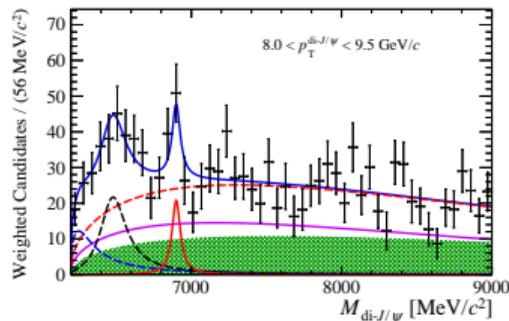
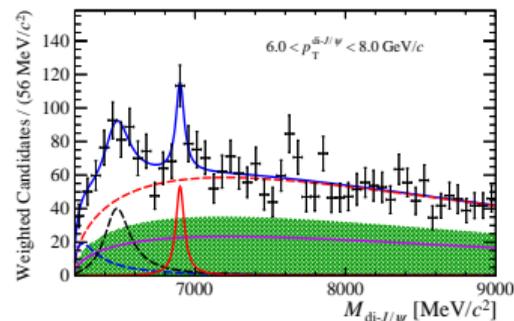
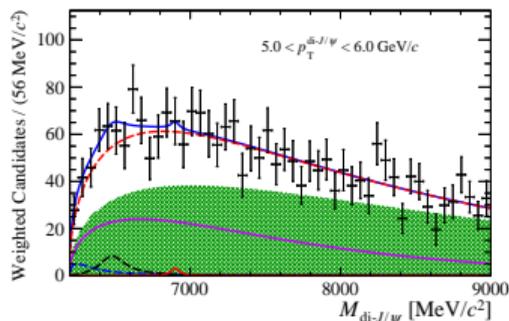
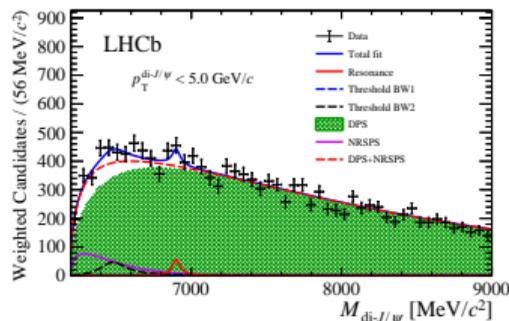
- NRSPS with constant phase fully coherent
- $M = (6886 \pm 11 \pm 11)$ MeV
 $\Gamma = (168 \pm 33 \pm 69)$ MeV



- Incoherent sum of components
- Threshold BWs are to adjust the lineshape.
- $M = (6906 \pm 11 \pm 7)$ MeV
 $\Gamma = (80 \pm 19 \pm 33)$ MeV

Simultaneous fit of $p_t(J/\psi J/\psi)$ bins

[LHCb, 2006.16957]

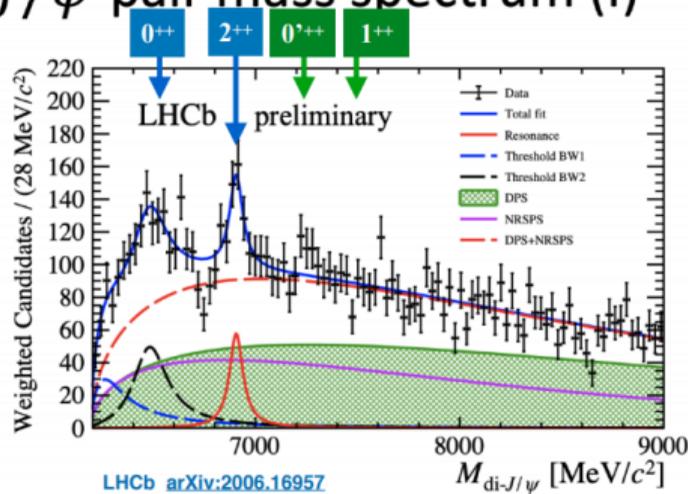


- the shape of DPS is determined separately for every bin
- Simulations fit: 7σ significance of the main peak

Some thoughts on the interpretations

- There are predictions for $T_{cc\bar{c}\bar{c}}$ e.g. [1911.00960], [1803.02522]
- Match the observation by adjusting overall scale
- The narrow widths are puzzling
- The dip is a mystery

J/ψ -pair mass spectrum (I)



[courtesy of L.Maiani, 2008.01637]

Measurements of the quantum numbers is critical

[1911.00960]

J^{PC}	$cc\bar{c}\bar{c}$		E^{th} [MeV]
	$N[(S_D, S_{\bar{D}})S, L]J$		
0^{++}	1[(1, 1)0, 0]0		5883
0^{++}	2[(1, 1)0, 0]0		6573
0^{++}	1[(1, 1)2, 2]0		6835
0^{++}	3[(1, 1)0, 0]0		6948
0^{++}	2[(1, 1)2, 2]0		7133
0^{++}	3[(1, 1)2, 2]0		7387
1^{+-}	1[(1, 1)1, 0]1		6120
1^{+-}	2[(1, 1)1, 0]1		6669
1^{+-}	1[(1, 1)1, 2]1		6829
1^{+-}	3[(1, 1)1, 0]1		7016
1^{+-}	2[(1, 1)1, 2]1		7128
1^{+-}	3[(1, 1)1, 2]1		7382
1^{--}	1[(1, 1)0, 1]1		6580
1^{--}	1[(1, 1)2, 1]1		6584
1^{--}	2[(1, 1)0, 1]1		6940
1^{--}	2[(1, 1)2, 1]1		6943
1^{--}	3[(1, 1)0, 1]1		7226
1^{--}	3[(1, 1)2, 1]1		7229
0^{*+}	1[(1, 1)1, 1]0		6596
0^{*+}	2[(1, 1)1, 1]0		6953
0^{*+}	3[(1, 1)1, 1]0		7236
1^{*+}	1[(1, 1)2, 2]1		6832
1^{*+}	2[(1, 1)2, 2]1		7130
1^{*+}	3[(1, 1)2, 2]1		7384
2^{*+}	1[(1, 1)2, 0]2		6246
2^{*+}	1[(1, 1)2, 2]2		6827
2^{*+}	1[(1, 1)0, 2]2		6827
2^{*+}	2[(1, 1)2, 0]2		6739
2^{*+}	3[(1, 1)2, 0]2		7071
2^{*+}	2[(1, 1)2, 2]2		7125
2^{*+}	2[(1, 1)0, 2]2		7126
2^{*+}	3[(1, 1)2, 2]2		7380
2^{*+}	3[(1, 1)0, 2]2		7380

Spin and parity of the vector-vector system

arXiv:2007.05501

$X \rightarrow J/\psi J/\psi$ amplitude

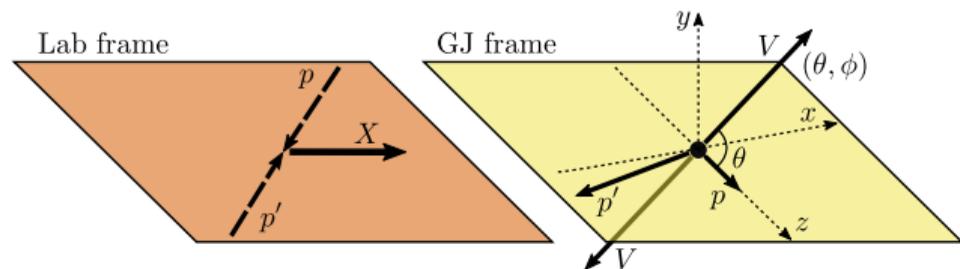
[MM, L. An, R. McNulty, 2007.05501]

Amplitude:

$$A_{\lambda_1, \lambda_2}^M = n_J d_{M, \lambda_1 - \lambda_2}^J(\theta) H_{\lambda_1, \lambda_2}(-1)^{1 - \lambda_2}$$

Differential width (intensity):

$$I(\theta) = \sum_M \rho_M \sum_{\lambda_1, \lambda_2} |A_{\lambda_1, \lambda_2}^M|.$$



Production by pp collision

- choose $z \uparrow \vec{n} \Rightarrow$ diagonal polarization matrix $\delta_{M, M'} \rho_M$

Intensity for the unpolarized decay

$$I(\theta) = n_J^2 \sum_{M, \lambda_1, \lambda_2} \rho_M |d_{M, \lambda_1 - \lambda_2}^J(\theta)|^2 |H_{\lambda_1, \lambda_2}|^2$$

What is no polarization $\rho_M = 1$ (quite likely in pp)?

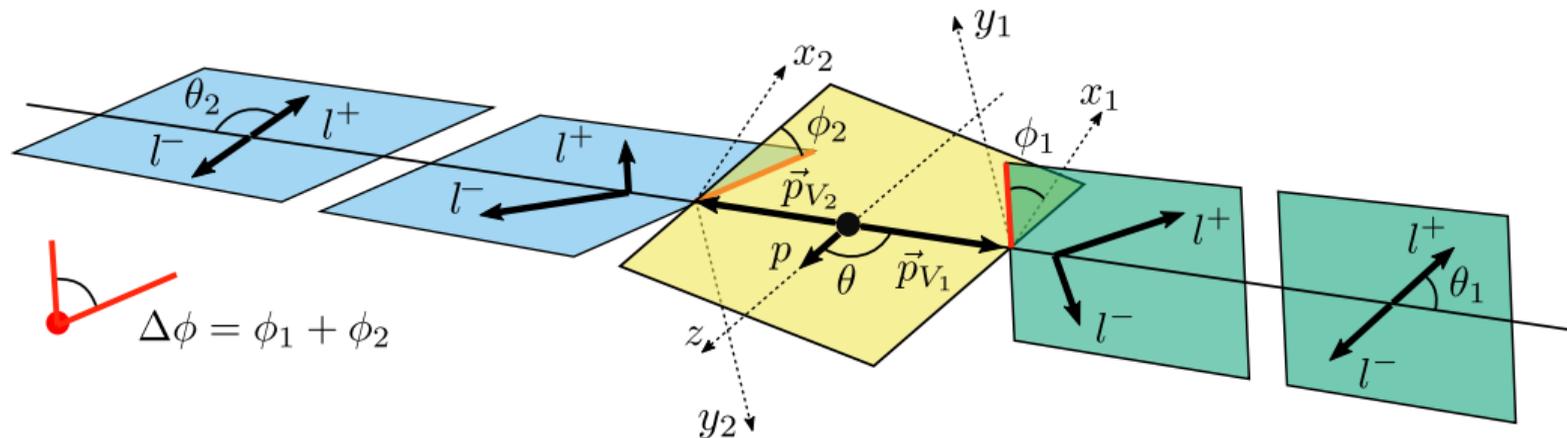
$$I(\theta) = n_J^2 \sum_{\lambda_1, \lambda_2} |H_{\lambda_1, \lambda_2}|^2$$

no J : explicit dependence on J disappears. What helps to determine J ?

- (a) Can helicity couplings tell us something?
- (b) Will the decays of J/ψ help?

Four-body decay angles

[MM, L. An, R. McNulty, 2007.05501]



- θ is the polar angle of $(J/\psi)_1$ with respect to the polarization direction
- (θ_1, ϕ_1) are the spherical angles of μ^+ in the $(J/\psi)_1$ helicity frame
- (θ_2, ϕ_2) are the spherical angles of μ^+ in the $(J/\psi)_2$ helicity frame

No polarization \Rightarrow no $z \Rightarrow$ no decay plane (pink) \Rightarrow only $\phi = \phi_1 + \phi_2$ matters.

$X \rightarrow V(\mu, \mu)V(\mu, \mu)$ amplitude

$$\begin{aligned} A_{\xi_1, \xi_2}^M &= n_J \sum_{\lambda_1, \lambda_2} d_{M, \lambda_1 - \lambda_2}^J(\theta) H_{\lambda_1, \lambda_2} (-1)^{1 - \lambda_2} \\ &\quad \times n_1 D_{\lambda_1, \xi_1}^{1*}(\phi_1, \theta_1, 0) \\ &\quad \times n_1 D_{\lambda_2, \xi_2}^{1*}(\phi_2, \theta_2, 0) \end{aligned}$$

- $\xi_i = \lambda_{\mu^+, i} - \lambda_{\mu^-, i}$ difference of muon helicities
- $\xi \in \{-1, 1\}$ since $\xi = 0$ is suppressed by $m_\mu/m_{J/\psi}$.

$$F^{(\mu\mu)} = \sum_{\xi \in \{-1, 1\}} \int d \cos \theta d_{\lambda, \xi}^1(\theta) d_{\lambda', \xi}^1(\theta) = \frac{1}{3} \begin{pmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{pmatrix}_{\lambda, \lambda'}$$

Helicity couplings

[Martin, Spearman (1970) book]

Reappearance of J

$$|\text{two part. state}; \lambda_1, \lambda_2\rangle = |\vec{p}, \lambda_1\rangle \otimes |-\vec{p}, \lambda_2\rangle (-1)^{j_2 - \lambda_2}$$

$$|JM; \lambda_1, \lambda_2\rangle = n_J \int \frac{d\Omega}{4\pi} D_{M\lambda}^{J*} |\text{two part. state}; \lambda_1, \lambda_2\rangle$$

$$H_{\lambda_1, \lambda_2} = \langle JM; \lambda_1, \lambda_2 | \hat{T} | JM \rangle$$

Parity

$$\mathcal{P} |JM; \lambda_1, \lambda_2\rangle = (-1)^J \eta_V^2 |JM; -\lambda_1, -\lambda_2\rangle.$$

Permutation $1 \leftrightarrow 2$

$$\mathcal{P}_{12} |JM; \lambda_1, \lambda_2\rangle = (-1)^J |JM; \lambda_2, \lambda_1\rangle.$$

\Rightarrow

$$H_{\lambda_1, \lambda_2} = (-1)^J \eta_X H_{-\lambda_1, -\lambda_2},$$

$$H_{\lambda_1, \lambda_2} = (-1)^J H_{\lambda_2, \lambda_1}.$$

Matrix of helicity couplings

$$H_{\lambda_1, \lambda_2} = \begin{pmatrix} h_{1,1} & h_{1,0} & h_{1,-1} \\ h_{0,1} & h_{0,0} & h_{0,-1} \\ h_{-1,1} & h_{-1,0} & h_{-1,-1} \end{pmatrix}$$

The same-color elements are connected by symmetries.

The symmetry relates the couplings

$$H_{\lambda_1, \lambda_2} = (-1)^J \eta_X H_{-\lambda_1, -\lambda_2},$$

$$H_{\lambda_1, \lambda_2} = (-1)^J H_{\lambda_2, \lambda_1}.$$

Four categories of possible helicity matrices:

group	$\eta_X(-1)^J, (-1)^J$	J^P	symmetry
<i>I</i>	+, +	0^+ , 2^+ , 4^+ , 6^+	symmetric, <i>S</i>
<i>II</i>	-, +	0^- , 2^- , 4^- , 6^-	symmetric, <i>S</i>
<i>III</i>	+, -	1^- , 3^- , 5^- , 7^-	antisymmetric, <i>A</i>
<i>IV</i>	-, -	1^+ , 3^+ , 5^+ , 7^+	antisymmetric, <i>A</i>

$$\begin{array}{cccc}
 H^{(I)} & H^{(II)} & H^{(III)} & H^{(IV)} \\
 \begin{pmatrix} b & a & c \\ a & d & a \\ c & a & b \end{pmatrix}_S & \begin{pmatrix} b & a & \\ a & & -a \\ & -a & -b \end{pmatrix}_S & \begin{pmatrix} & a & \\ -a & & -a \\ & a & \end{pmatrix}_A & \begin{pmatrix} & a & c \\ -a & & a \\ -c & -a & \end{pmatrix}_A
 \end{array}$$

a, b, c, d are still unknown coefficients, complex in general.

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<i>I</i>	+, +	0^+ , 2^+ , 4^+ , 6^+	symmetric, <i>S</i>
<i>II</i>	-, +	0^- , 2^- , 4^- , 6^-	symmetric, <i>S</i>
<i>III</i>	+, -	1^- , 3^- , 5^- , 7^-	antisymmetric, <i>A</i>
<i>IV</i>	-, -	1^+ , 3^+ , 5^+ , 7^+	antisymmetric, <i>A</i>

$$\boxed{0^+} \begin{pmatrix} b & & \\ & d & \\ & & b \end{pmatrix}_S$$

$$\boxed{0^-} \begin{pmatrix} b & & \\ & & \\ & & -b \end{pmatrix}_S$$

$$\boxed{1^+} \begin{pmatrix} & a & \\ -a & & a \\ & -a & \end{pmatrix}_A$$

a, b, c, d are still unknown coefficients, complex in general.

Landau-Yang theorem

"A massive particle with spin 1 cannot decay into two photons", wikipedia

Photons do not carry the longitudinal polarizarion $\Rightarrow H_{0,i} = H_{i,0} = 0$

$H^{(I)}$	$H^{(II)}$	$H^{(III)}$	$H^{(IV)}$
$\begin{pmatrix} b & a & c \\ a & d & a \\ c & a & b \end{pmatrix}_S$	$\begin{pmatrix} b & a & \\ a & & a \\ & -a & -b \end{pmatrix}_S$	$\begin{pmatrix} & a & \\ -a & & a \\ & a & \end{pmatrix}_A$	$\begin{pmatrix} & a & c \\ -a & & a \\ -c & -a & \end{pmatrix}_A$
$\begin{pmatrix} b & & \\ & d & \\ & & b \end{pmatrix}_S$	$\begin{pmatrix} b & & \\ & & \\ & & -b \end{pmatrix}_S$		$\begin{pmatrix} & a & \\ -a & & a \\ & -a & \end{pmatrix}_A$
0^+	0^-		1^+

No decay to two photons for 1^+ , and group-III: $1^-, 3^-, 5^-, \dots$

A comment on Higgs decay to ZZ: $J^P = 0^+$

The term in the SM lagrangian:

$$\mathcal{L}_{ZZH} = \frac{m_Z^2}{2v} Z_\mu Z^\mu H$$

Helicity amplitude:

$$A_{\lambda_1, \lambda_2}^{H \rightarrow ZZ} = \frac{m_Z^2}{2v} (\epsilon_1^*(\lambda_1) \cdot \epsilon_2^*(\lambda_2)).$$

Matrix of couplings:

$$H_{\lambda_1, \lambda_2} \Rightarrow \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + O(p^2)$$

First group: $b = -d = 1$.



Determination of the spin-parity

LLH comparison

- Only group can be determined without polarization
- Already something(!) - to distinguish 0^\pm , 1^\pm , 2^\pm .

Likelihood of hypothesis (model \mathcal{M}):

$$\text{LLH}_{\mathcal{M}} = - \sum_{e=1}^{N_{\text{ev}}} \log l(\tau_e | \mathcal{M}\{\hat{h}\}),$$

Test statistics :

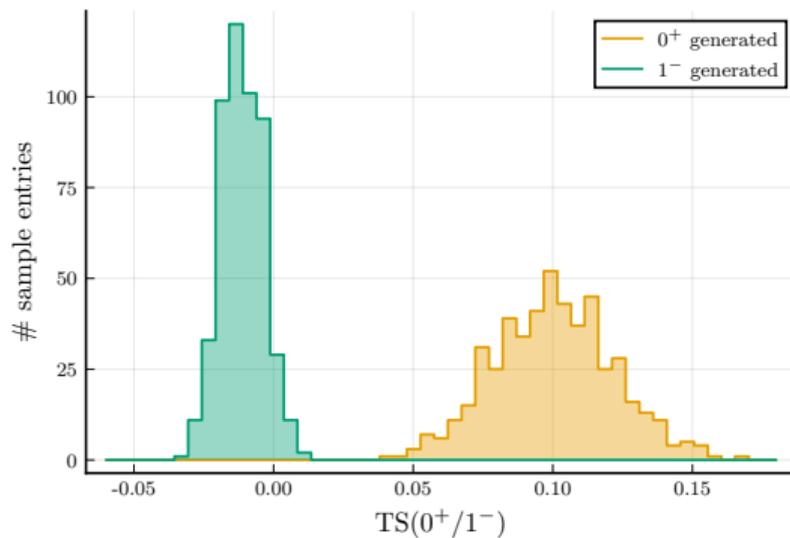
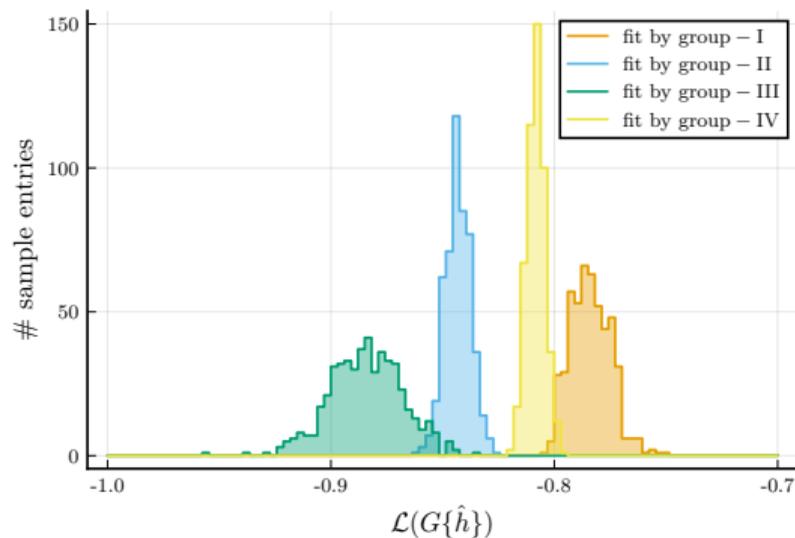
$$\text{TS}_{\mathcal{M},\mathcal{M}'} = \text{LLH}_{\mathcal{M}} - \text{LLH}_{\mathcal{M}'}$$

- parameters of the model are unknown couplings $\mathcal{M}\{h\}$
- evaluation of the LLH for the optimized values $\mathcal{M}\{\hat{h}\}$

Numerical result: $T_{cc\bar{c}}(0^{++}) \rightarrow J/\psi(\mu^+\mu^-)J/\psi(\mu^+\mu^-)$

fits of a sample with 500 events. 500 MC experiments.

[MM, L. An, R. McNulty, 2007.05501]



- The group-*I* has the highest likelihood (Yes!) $\Rightarrow J^P$ Natural, Even
- Width of distribution is due to the statistics
- LLH barely overlaps. TS separation is even better.

Net ϕ -dependence distinguishes naturality

$$\frac{2\pi}{N} \frac{dI}{d\phi} = 1 + \frac{h_{1,1} h_{-1,-1}^*}{2} \cos(2\phi),$$

$$\sum_{\lambda_1, \lambda_2} |H_{\lambda_1 \lambda_2}|^2 = 1$$

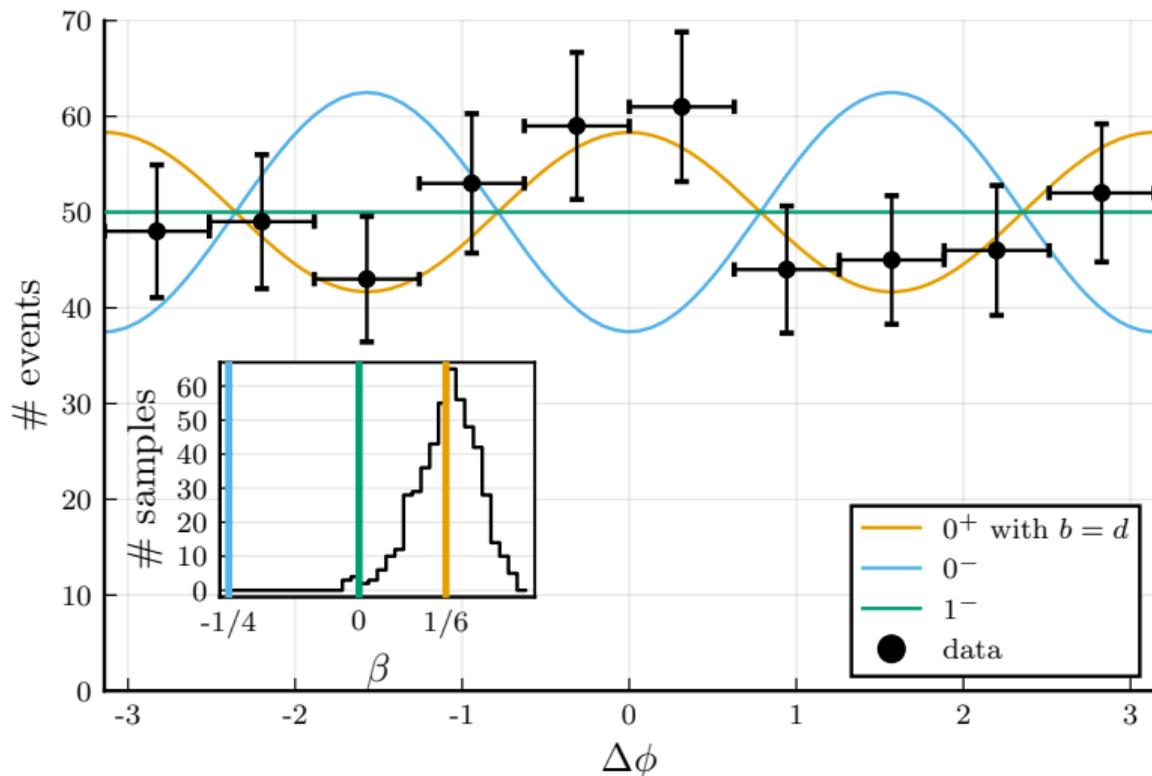
groups	$h_{1,1} h_{-1,-1}^*$	$dN/d\phi (2\pi/N)$
group-I	$ b ^2$	$1 + b ^2 \cos(2\phi)/2$
group-II	$- b ^2$	$1 - b ^2 \cos(2\phi)/2$
group-III	0	flat
group-IV	0	flat

- either fit $dN/d\phi$ or calculate the moment $\langle \cos(2\phi) \rangle$
- distinguish groups I vs II vs (III & IV)
- warning: b might be zero \Rightarrow works only if $\langle \cos(2\phi) \rangle \neq 0$

$T_{cc\bar{c}\bar{c}}(0^{++})$ ϕ distribution

[MM, L. An, R. McNulty, 2007.05501]

MS sample, 1000 events



Helicity matrix $H = \mathbb{I}/\sqrt{3}$,

$$h_{1,1}h_{-1,-1}^* = \frac{1}{3}$$

positive $\langle \cos(2\phi) \rangle$ moment,

$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \frac{1}{6} \cos(2\phi)$$

- Clearly different to the best one gets with other hypotheses

Summary: Exotics 2020

Two groundbreaking news from LHCb and it is not the end of the year yet

$X(2900)$ in $D^- K^+$ spectrum

- charm-strange molecule?
- tetraquark of "two generations"?
- kinematic effect

$T_{cc\bar{c}\bar{c}}$ First hints for the $cc\bar{c}\bar{c}$ tetraquarks

- How many states
- How the dip is produced
- How to treat interference with SPS
- Measurements of the quantum numbers are critical

Thank you for your attention

Thanks to LHCb colleagues
Thanks to Ronan and Liupan