

# Physics of $\nu$ -A

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# A Wake-up Call



INT 12/16



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GIESSEN

# GiBUU

## ■ Essential References:

1. Buss et al, Phys. Rept. 512 (2012) 1  
contains both the theory and the practical implementation of transport theory
2. Gallmeister et al., Phys.Rev. C94 (2016), 035502  
contains the latest changes in GiBUU2016
3. Mosel, Ann. Rev. Nucl. Part. Sci. 66 (2016) 171  
short review, contains some discussion of generators



# $\nu A$ Reaction

- General structure: **approximately** factorizes

full event (four-vectors of all particles in final state)

$$\text{initial interaction} \quad \times \quad \text{final state interaction}$$

$\approx$



Determines inclusive X-section



Determines the final state particles



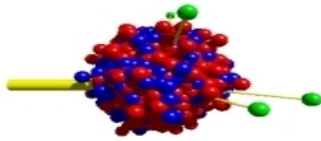
# A theory-based generator

- Aim: to construct the best possible consistent theory framework for inclusive reactions *and* full event simulations (NOT exclusive 1 particle out or coherent).

## Requirements:

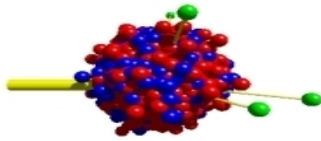
- Relativistically correct (Skyrme-like or RMF) momentum-dependent potentials, nuclear binding, approximately correct handling of collision terms
- Same potentials in initial state and final state interactions
- Final state interactions testable in many different reactions, such as  $p+A$ ,  $\pi+A$ ,  $A+A$ ,  $e+A$ ,  $\gamma+A$





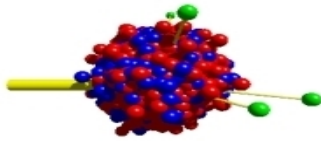
- ◎ **GiBUU : Quantum-Kinetic Theory and Event Generator**  
based on a BM solution of Kadanoff-Baym equations
- ◎ Physics content and details of implementation in:  
**Buss et al, Phys. Rept. 512 (2012) 1- 124**  
Mine of information on theoretical treatment of potentials,  
collision terms, spectral functions and cross sections, useful for  
any generator
- ◎ Code from [gibuu.hepforge.org](http://gibuu.hepforge.org), new version GiBUU 2016  
Details in Gallmeister et al, Phys.Rev. C94 (2016) no.3, 035502





- *Initial interaction*: can be any sophisticated model  
→ inclusive cross sections
- *Final state interaction*: propagates these outgoing particles through the nucleus using quantum-kinetic transport theory, fully relativistic → full event, four-vectors of all particles
- Initial and final interactions come from the same Hamiltonian:  
**CONSISTENCY** of inclusive and semi-inclusive  $X$ -sections





- The same groundstate for all processes!
  - Different from GENIE (NEUT), where different processes (QE, 2p2h, ...) are calculated within different models.
- Bound groundstate
  - Different from all generators, also from Nieves, Martini
- New in GiBUU 2016:
  - Better ground state: constant Fermi surface enforced, - 8 MeV binding for all nuclei, not tuned
  - new treatment of 2p2h, consistent with e-scattering





# Inclusive and Exclusive Modelling

- In quantum-kinetic theory the inclusive X-section emerges as time = 0 step for the time-development of the one-body phase-space distribution of all particles involved:

$$f(\mathbf{x}, 0, \mathbf{p}) = \frac{1}{(2\pi)^3} \int d\mathbf{s} e^{-i\mathbf{p}\cdot\mathbf{s}} \rho\left(\mathbf{x} - \frac{\mathbf{s}}{2}, \mathbf{x} + \frac{\mathbf{s}}{2}\right)$$

$$\mathcal{P}_h(\mathbf{p}, E) = g \int_{\text{nucleus}} d^3x f(\mathbf{x}, 0, \mathbf{p}) \Theta(E) \delta\left(E - m^*(\mathbf{x}, \mathbf{p}) + \sqrt{\mathbf{p}^2 + m^{*2}(\mathbf{x}, \mathbf{p})}\right)$$

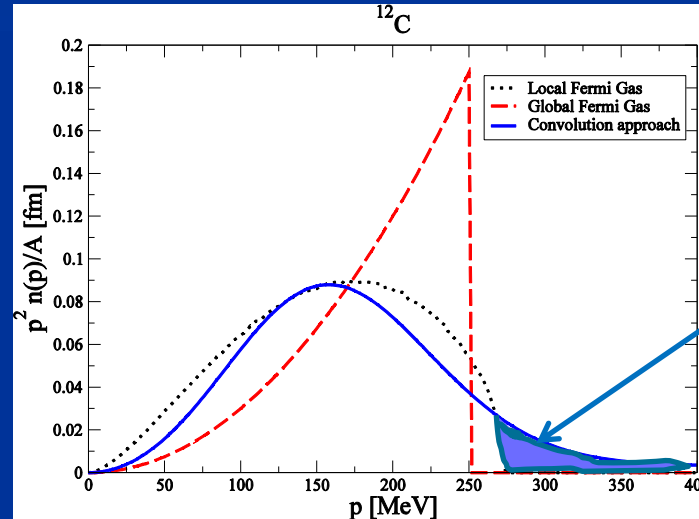
$$d\sigma_{\text{QE}}^{\nu A} = \int \frac{d^3p}{(2\pi)^3} dE \mathcal{P}_h(\mathbf{p}, E) f_{\text{corr}} d\sigma_{\text{QE}}^{\text{med}} P_{\text{PB}}(\mathbf{x}, \mathbf{p}) .$$



# Initial State Correlations

- GiBUU ground state: nucleons bound in momentum-dependent potential, obtained from EFT, momentum given by local Fermi gas, potential RMF or Skyrme

Energy-distribution smooth  
because of  $x$ -dependent  
Potential  $\rightarrow$  spectral function  
close to realistic, but no shell-  
effects



Alvarez-Ruso, Hayato, Nieves

True src contribution  
Very small effect on  
Inclusive cross sections

# GiBUU Ingredients: 2p-2h

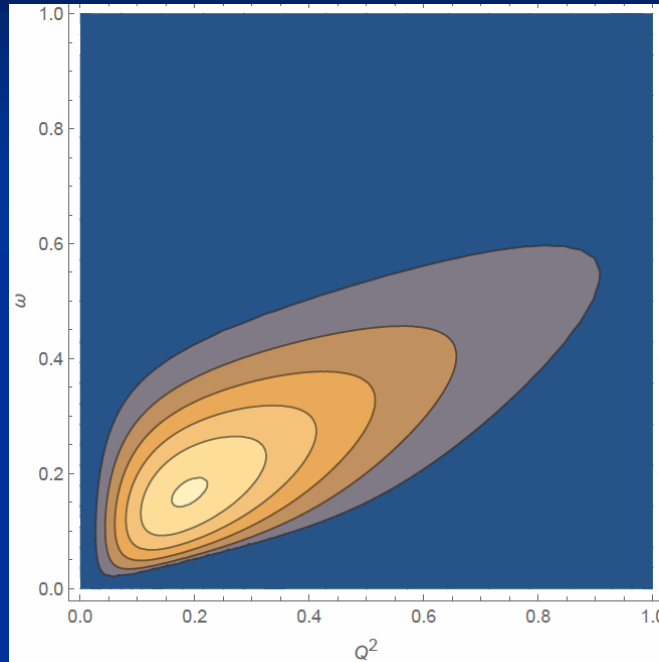
- **Assume:** 2p2h transverse, structure function  $W_1$  for electrons from experimental fit of **MEC contribution** by Bosted and Mamyan (arXiv:1203.2262) and Christy (priv. comm.) to world data for  $0 < W < 3.2$  GeV and  $0.2 < Q^2 < 5$  GeV<sup>2</sup>

$$\frac{d\sigma}{d\Omega dE'} = \frac{4\alpha^2}{Q^4} E'^2 2 \left( \frac{Q^2}{2\vec{q}^2} \cos^2 \frac{\theta}{2} + \sin^2 \frac{\theta}{2} \right) W_1(Q^2, \omega)$$

- Transverse assumption established around 1990, Ericsson, Marteau



# 2p2h $Q^2$ - $\omega$ Distribution for 2p2h



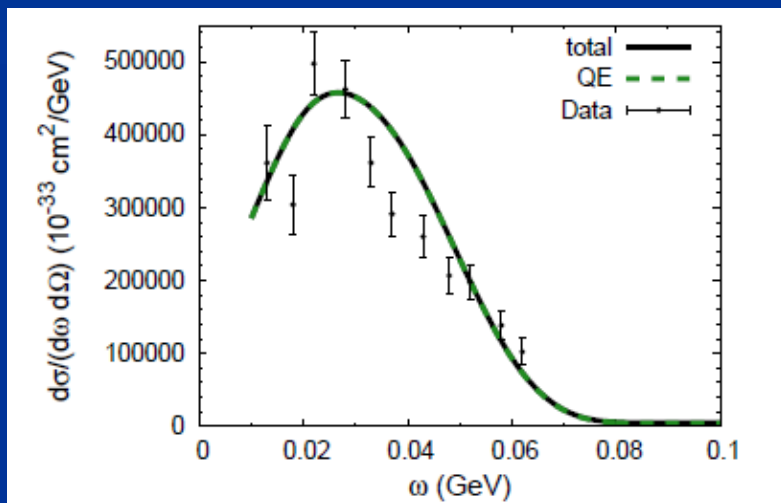
From:  
Bosted and Mamyan,  
Christy

$W_1$

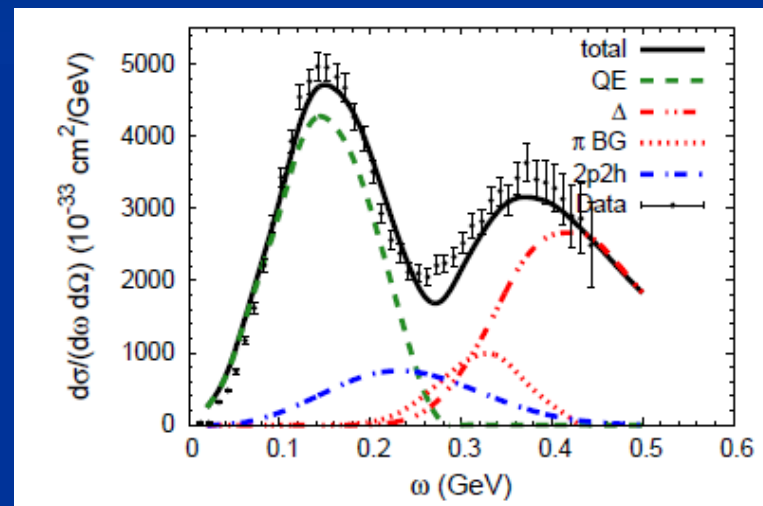


# Semi-inclusive QE Electron Scattering

- a necessary check for any generator development

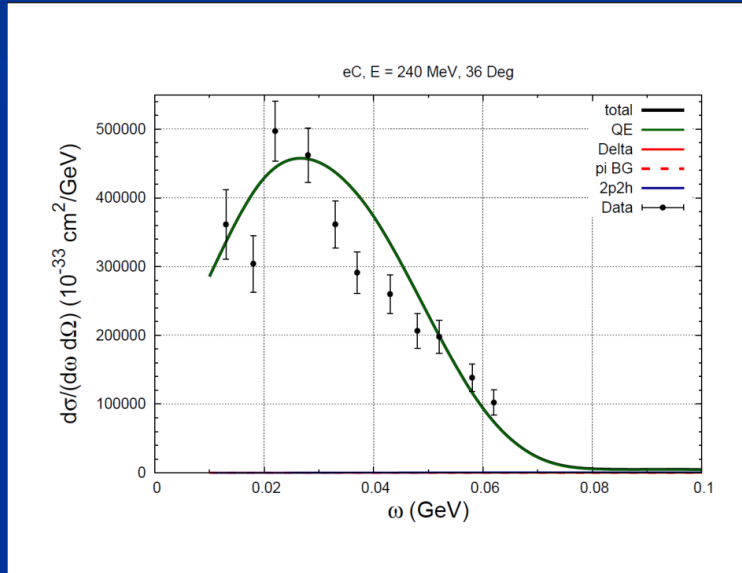


0.24 GeV, 36 deg,  $Q^2 = 0.02 \text{ GeV}^2$



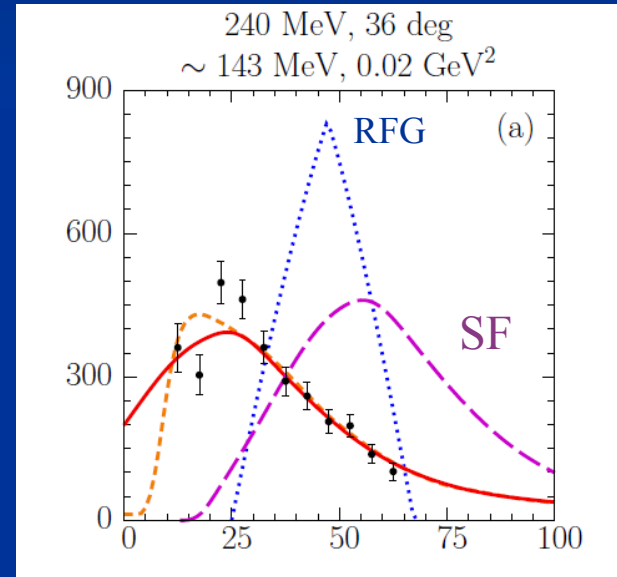
0.56 GeV, 60 deg,  $Q^2 = 0.24 \text{ GeV}^2$

# Test with Electron Data



GiBUU

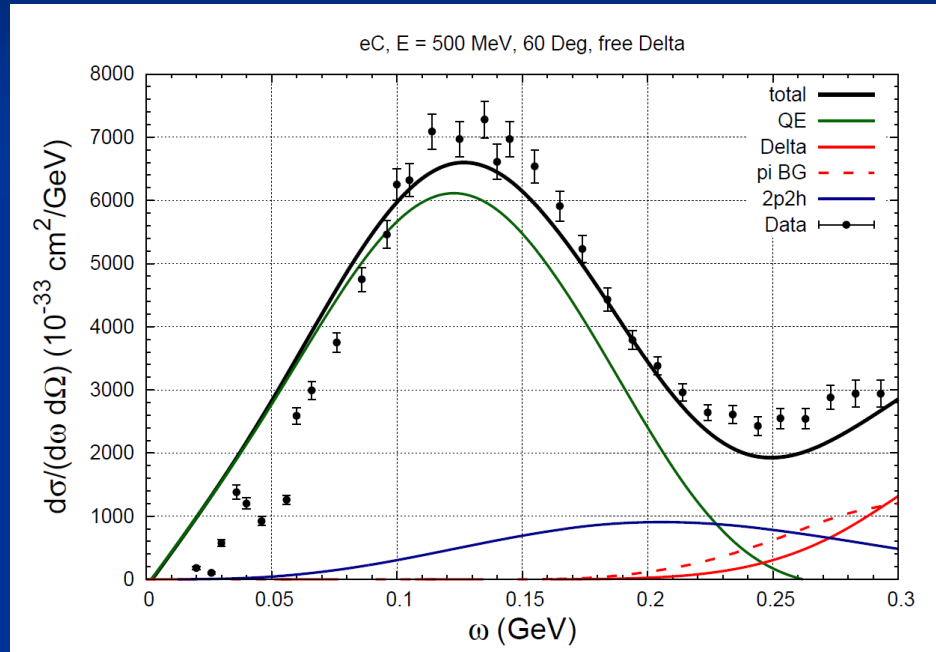
## Dramatic influence of fsi



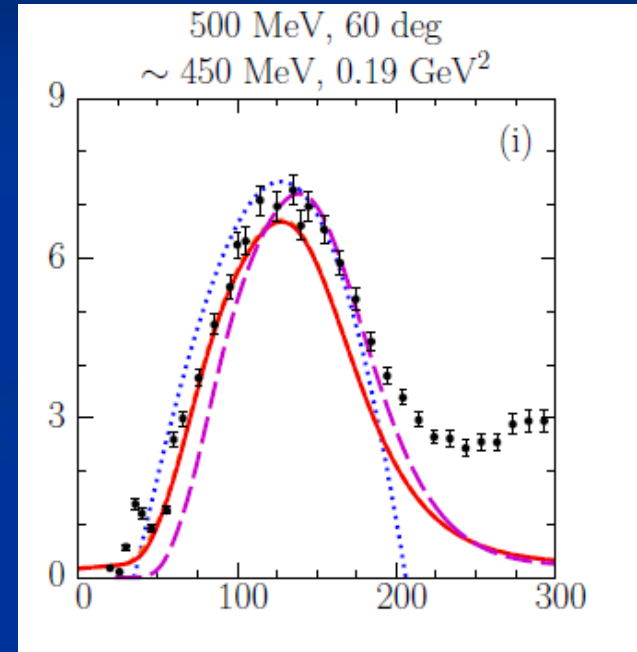
Ankowski, Benhar, Sakuda, PR D91 (2015) 03305



# Test with Electron Data



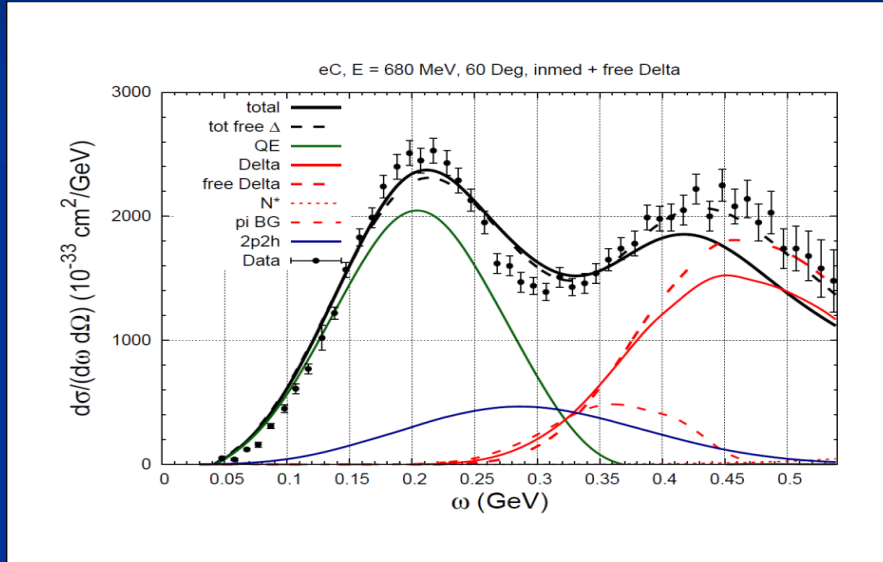
GiBUU 2016



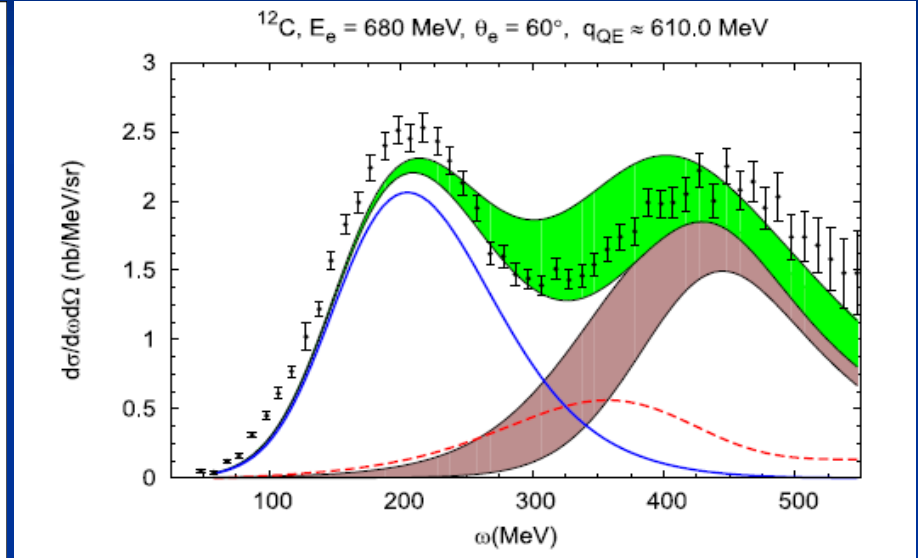
Ankowski, Benhar, Sakuta



# Test with Electron Data



GiBUU



M.V. Ivanov et al, J.Phys. G43 (2016) 045101, Scaling

Agreement with data, without explicit RPA or src!





# Now to (Anti-) Neutrinos

- QE, pion production, DIS straightforward
- 2p2h: purely transverse, use response from e

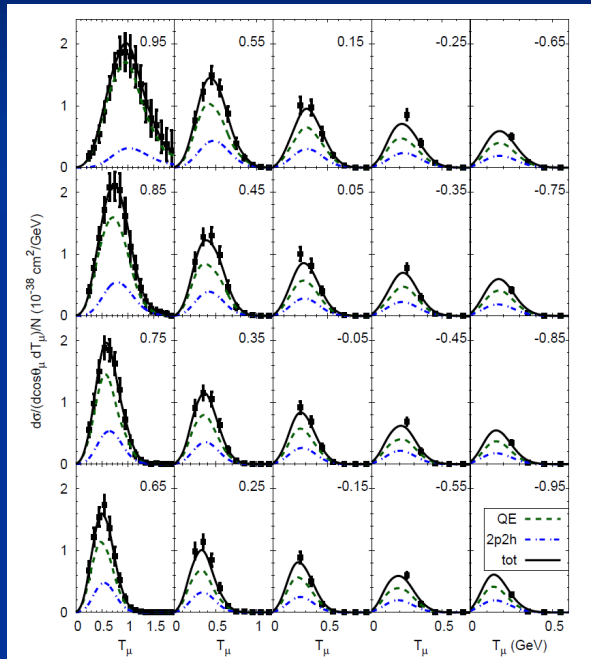
$$\begin{aligned} \frac{d\sigma}{d\Omega dE'} = & \frac{G^2}{2\pi^2} E'^2 \left[ \frac{Q^2}{\bar{q}^2} \left( G_M^2 \frac{\omega^2}{\bar{q}^2} + G_A^2 \right) R_{\sigma\tau}(T) \cos^2 \frac{\theta}{2} \right. \\ & + 2 \left( G_M^2 \frac{\omega^2}{\bar{q}^2} + G_A^2 \right) R_{\sigma\tau}(T) \sin^2 \frac{\theta}{2} \\ & \left. \pm 2 \frac{E+E'}{M} G_A G_M R_{\sigma\tau}(T) \sin^2 \frac{\theta}{2} \right] \end{aligned}$$

from: Martini et al.

$R_{\sigma\tau} \sim W_1$  from  
electron scattering

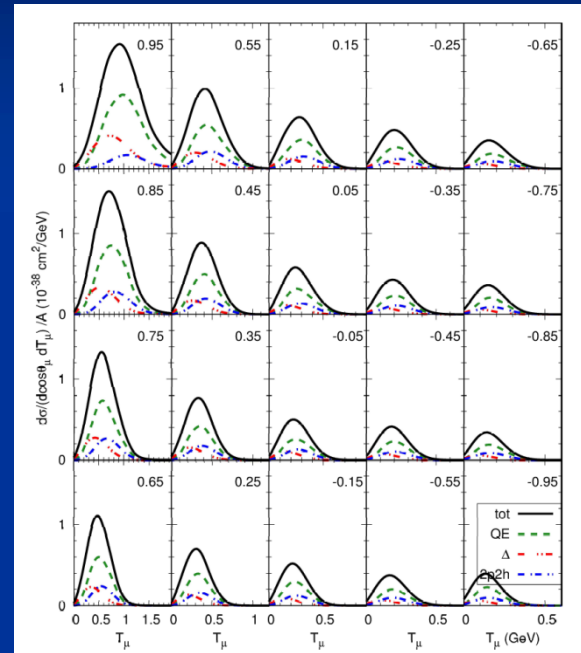
Same Response in  $V + A$  as in  $V \cdot A \sim W_1$   
from Walecka 1975

# Inclusive Lepton Kinematics



MiniBooNE C12 (QE + 2p2h)

Gallmeister et al.  
Phys. Rev. C94 (2016) no.3, 035502

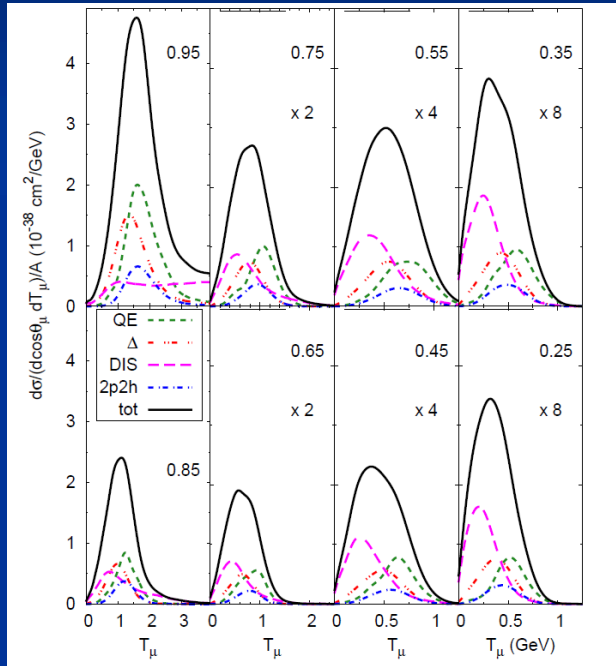


MicroBooNE Ar40 (fully inclusive)

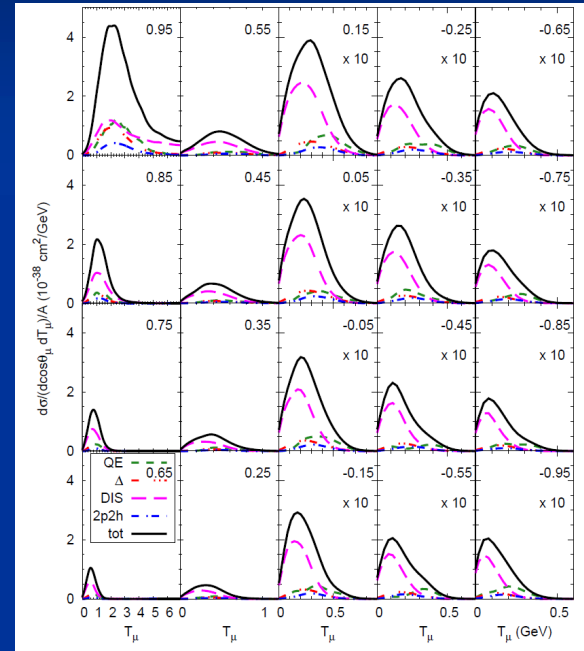
$2p2h \sim \Delta$



# Inclusive Lepton Kinematics



NOvA C12

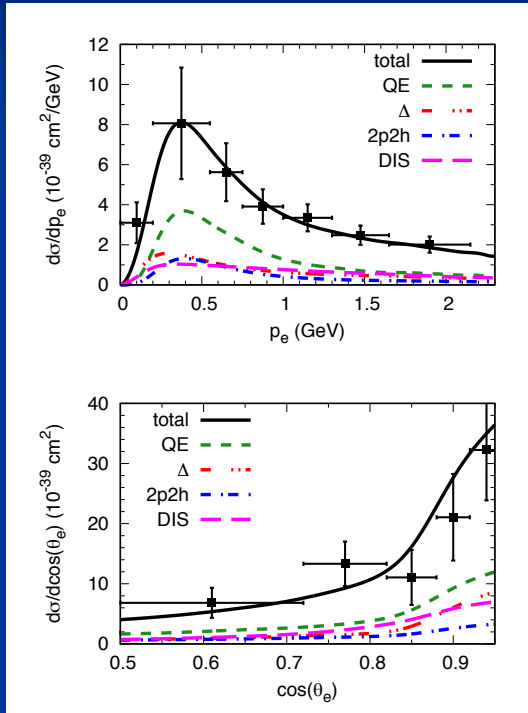


DUNE/LBNF Ar40

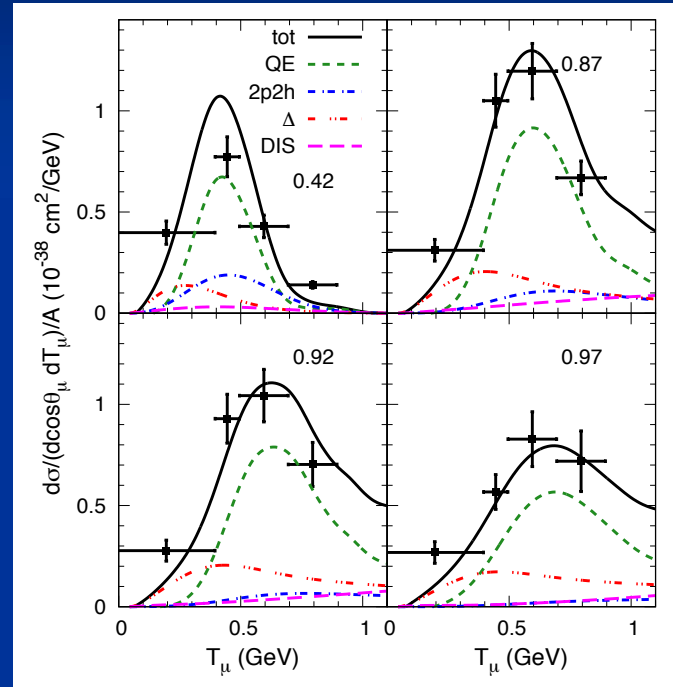
Gallmeister et al.  
Phys.Rev. C94 (2016) no.3, 035502



# Comparison with T2K Data



T2K,  $\nu_e$



T2K,  $\nu_\mu$



# Now to Final State Interactions

- Quantum-kinetic Transport Theory  
(Kadanoff-Baym, 60s, Botermans-Malfliet 90s)
- Basic object: not particle (as in MC generators),  
but single particle density matrix:

$$f(\mathbf{x}, 0, \mathbf{p}) = \frac{1}{(2\pi)^3} \int d\mathbf{s} e^{-i\mathbf{p}\cdot\mathbf{s}} \rho \left( \mathbf{x} - \frac{\mathbf{s}}{2}, \mathbf{x} + \frac{\mathbf{s}}{2} \right)$$

Here, for simplicity, given for on-shell particle, at time 0



# Quantum-kinetic Transport Theory

On-shell drift term

Off-shell transport term

Collision term

$$\mathcal{D}F(x, p) - \text{tr} \left\{ \Gamma f, \text{Re} S^{\text{ret}}(x, p) \right\}_{\text{PB}} = C(x, p) .$$

$$\mathcal{D}F(x, p) = \{p_0 - H, F\}_{\text{PB}} = \frac{\partial(p_0 - H)}{\partial x} \frac{\partial F}{\partial p} - \frac{\partial(p_0 - H)}{\partial p} \frac{\partial F}{\partial x}$$

$H$  contains  
mean-field  
potentials

Describes time-evolution of  $F(x, p)$

$$F(x, p) = 2\pi g f(x, p) \mathcal{P}(x, p)$$

Spectral function

Phase space distribution

KB equations with BM offshell term

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# Inclusive and Exclusive Modelling

- GiBUU takes the final state of the first, initial lepton-nucleus interactions and propagates it (i.e. all particles in it) through the nuclear volume.

$$F(x, p) = 2\pi g f(x, p) \mathcal{P}(x, p)$$

$$\mathcal{D}F(x, p) - \text{tr} \left\{ \Gamma f, \text{Re}S^{\text{ret}}(x, p) \right\}_{\text{PB}} = C(x, p)$$



# Transparency

- Transparency: integral measure of in-medium initial and final state effects
- Basic Definition:

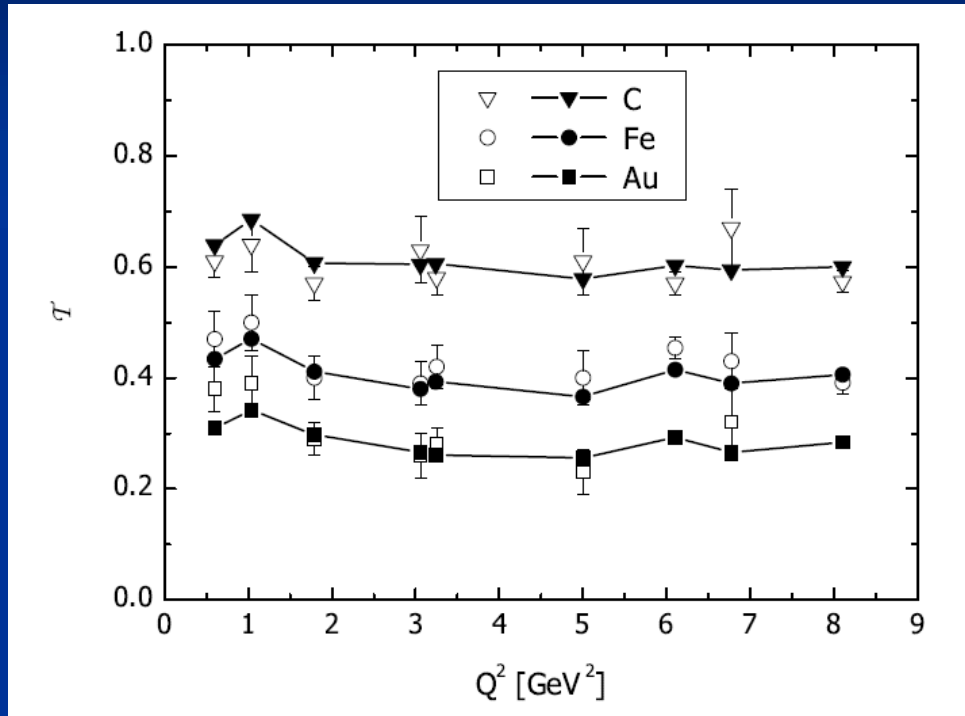
$$T = I/A * \sigma(A)/\sigma(N)$$

widely used in electron-A interaction physics  
and in in-medium physics





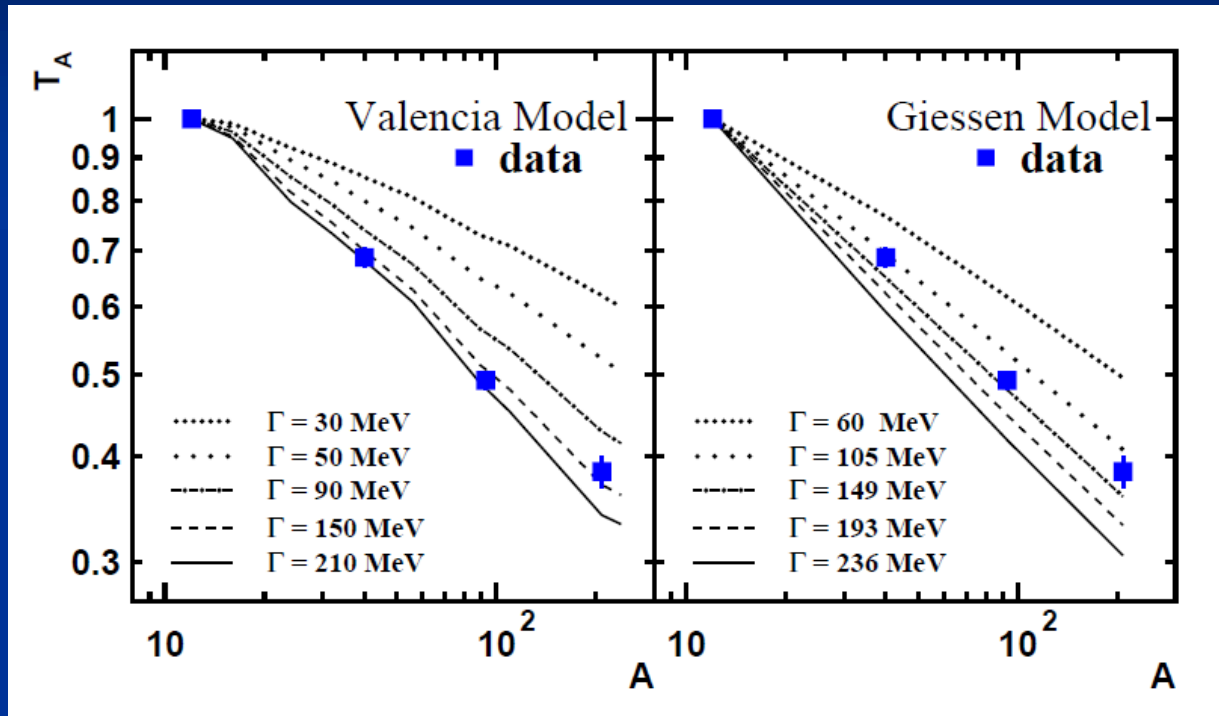
# Proton Transparency



GiBUU: full symbols  
Data: open symbols  
JLAB, SLAC

from: J. Lehr, Giessen thesis, 2003

# $\omega$ Meson Transparency



Transparency  $T$  gives integral information on in-medium width  $\Gamma$

Kotulla et al, Phys.Rev.Lett. 100 (2008) 192302

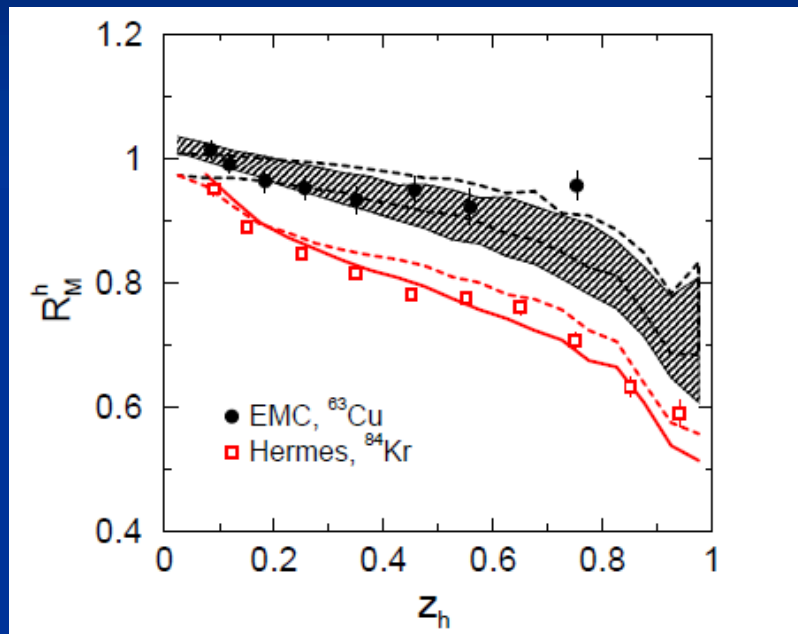
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# Hadron Transparency



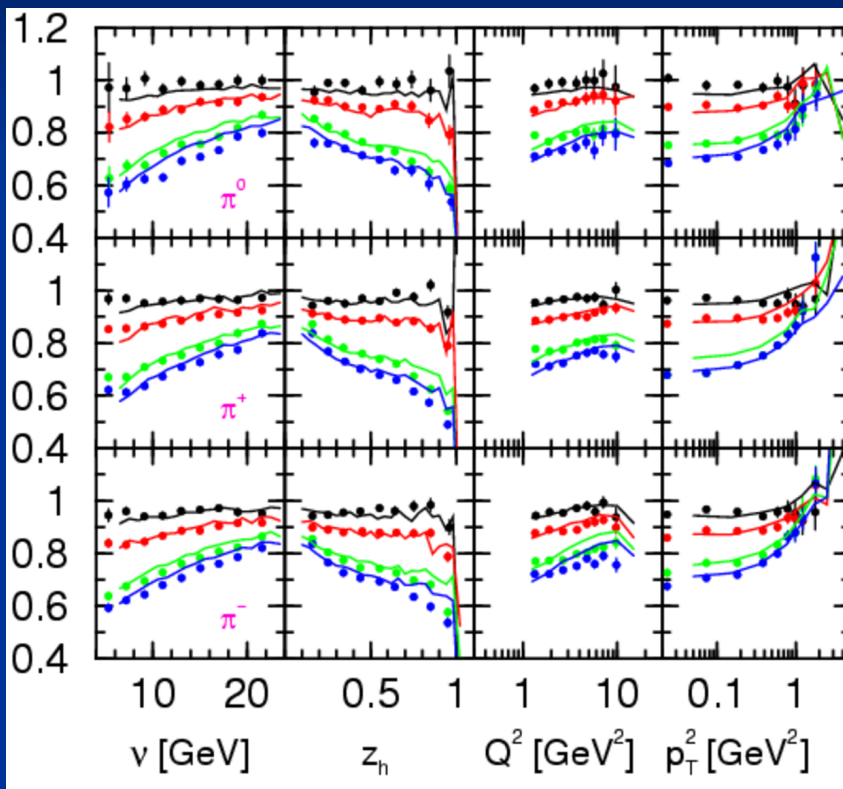
EMC: 200, 280 GeV leptons  
Hermes: 28 GeV

$$Z_h = E_h/v$$

Distribution contains  
Info on hadron formation  
times

# Hermes@27: A.Airapetian et al., NPB780(2007)1

Transparency T



$^2d_1$   
 $^4He_2$   
 $^{20}Ne_{10}$   
 $^{84}Kr_{36}$   
 $^{131}Xe_{54}$

For neutrinos:  
 get T distributions for  
 $T(E_h)$  and  $T(p_T^2)$   
 Possible without reconstruction



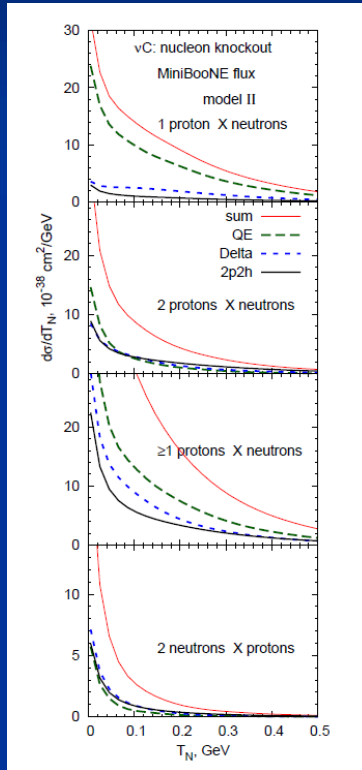
# Proton Tagging and Multi-Nucleons

- FSI cause ‚avalanche effect‘ : one nucleon kicks out other nucleons and loses energy
- 2 outgoing particles can come also from true, one-body QE (and  $\Delta N \rightarrow NN$ , pion absorption)



# Proton Tagging and Multi-Nucleons

Lalukulich et al., Phys.Rev. C86 (2012) no.1, 014614



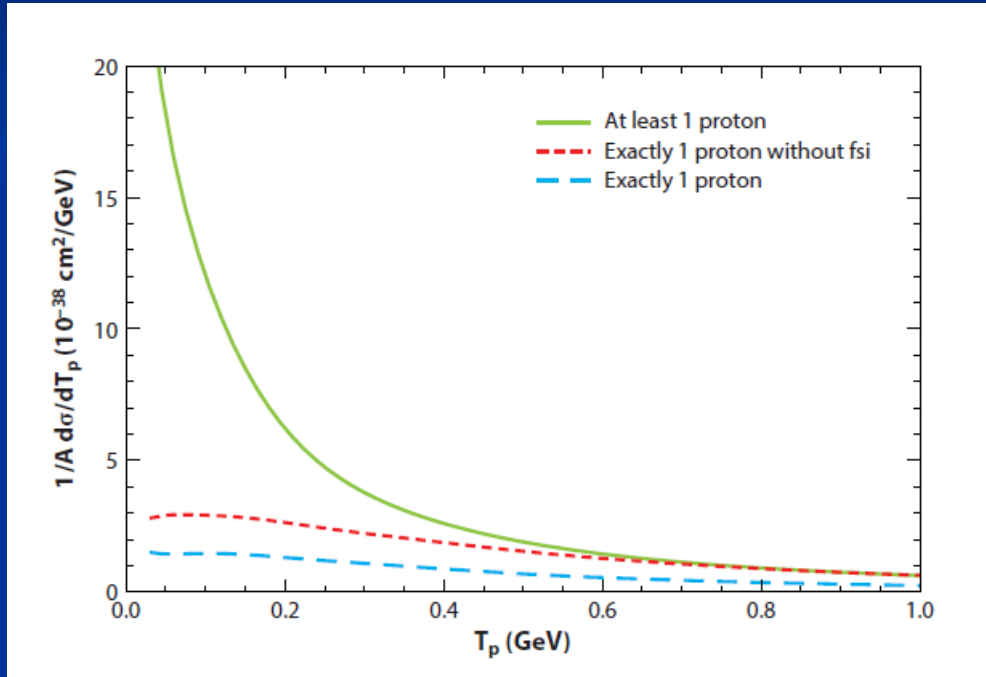
FSI cause ‚avalanche effect‘ : one nucleon kicks out other nucleons and loses energy

→ 2 outgoing particles can come also from true, one-body QE (and  $\Delta N$  → NN, pion absorption)

HOWEVER:

events with one nucleon out can come only from true QE

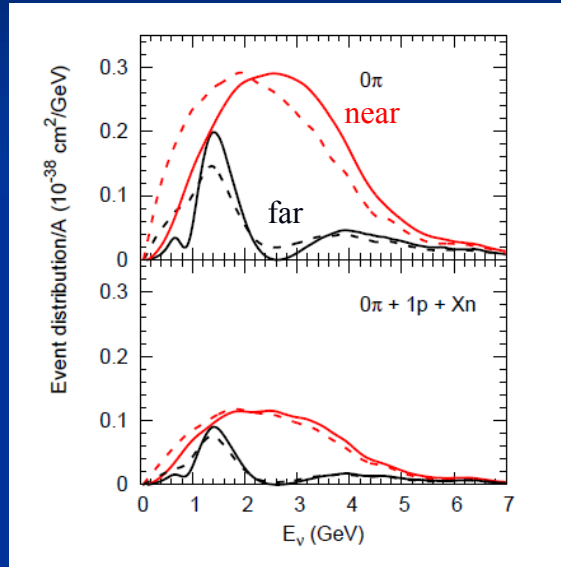
# Proton Spectrum



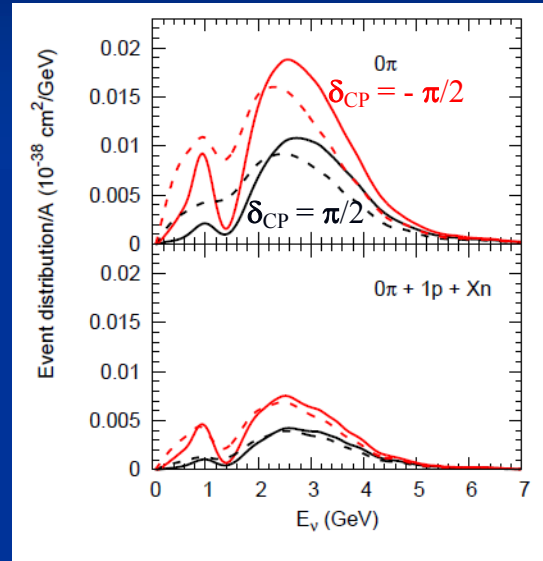
Transparencies contain integral  
Info on imaginary parts of  
self-energies  
Loss of flux only, no info on  
where the flux goes.

Spectra give the full story,  
essential for influence of  
experimental acceptance cuts

# Proton Tagging and Multi-Nucleons



Event rates at near (LBNF)  
and far detector (DUNE)



$\delta_{CP}$  sensitivity at DUNE

Mosel et al,  
Phys.Rev.Lett. 112 (2014) 151802

Solid: true E  
Dashed: reconstructed E

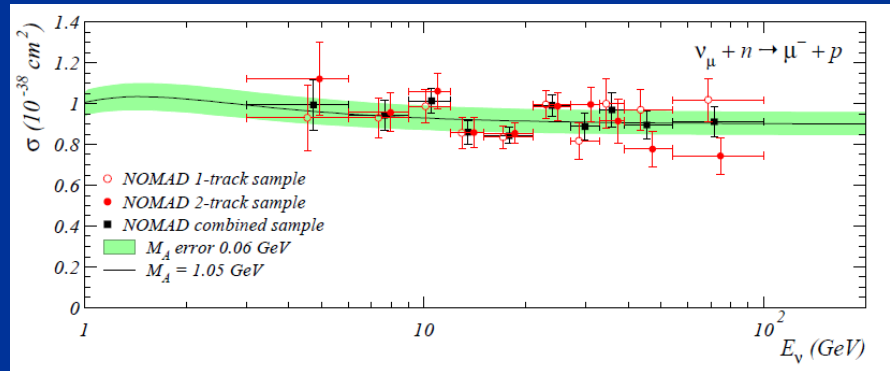


# CCQE in MiniBooNE and NOMAD

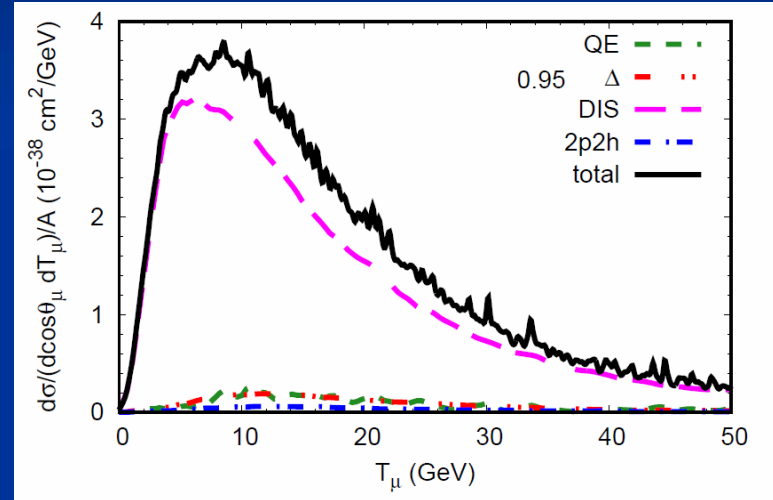
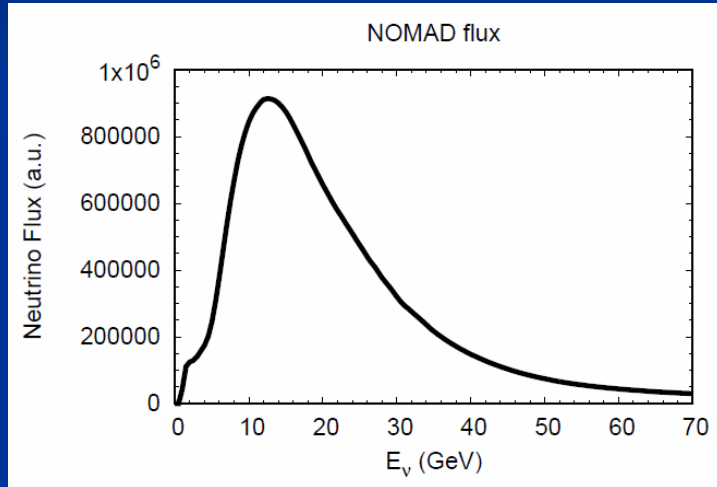
## ■ Different Event Selection

■ MiniBooNE:  $1\mu, 0\pi$

■ NOMAD:  $1\mu, 0\pi$  (1 track) +  $1\mu, 0\pi, 1p$  (two-track)



# NOMAD Event-Rates



QE and 2p2h are very small parts of the total interaction

# Summary I

## ■ Theory:

- State-of-the-art calculations of inclusive cross sections provide a necessary (but not sufficient) check for a full description of  $\nu A$  reactions
- Free-Space Monte Carlo Simulations miss the most important aspect of nuclei: potentials and binding!
- Quantum-kinetic Transport Theory is the (well established, and – in other fields of physics - widely used) method to deal with potentials and binding in non-equilibrium processes, allows for off-shell transport



# Summary II

## ■ Experiment:

- Give data with as little generator contamination as possible. No-go is, e.g., flux cuts to mimick lepton acceptance
- QE-events are experimentally indistinguishable from ‚stuck-pion‘ events - > give your cross section for these reabsorption events (as MB did!). Aim for consistency: use the same theory to calculate both the explicit and the reabsorbed pion events
- At DUNE (and MINERvA) DIS dominates the total event rate. It should give interesting info on  $W_3$  in medium (EMC effect for neutrinos)

