

# **Electromagnetic form factors of nucleon resonances within dynamical coupled channel model of meson production reactions**

Toru Sato

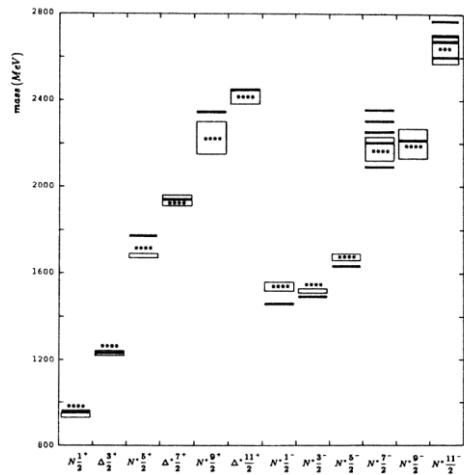
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Collaborators

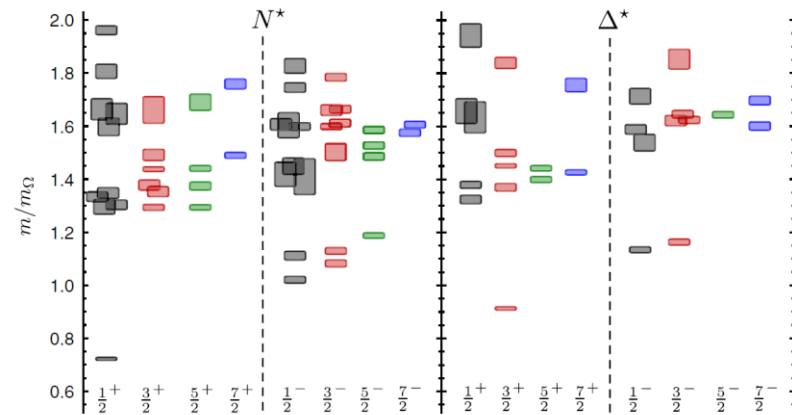
S. X. Nakamura(Osaka), H. Kamano(KEK), T. -S. H. Lee(ANL)

# Baryon excited states

Baryon excited states are predicted from quark models, SD,... LQCD

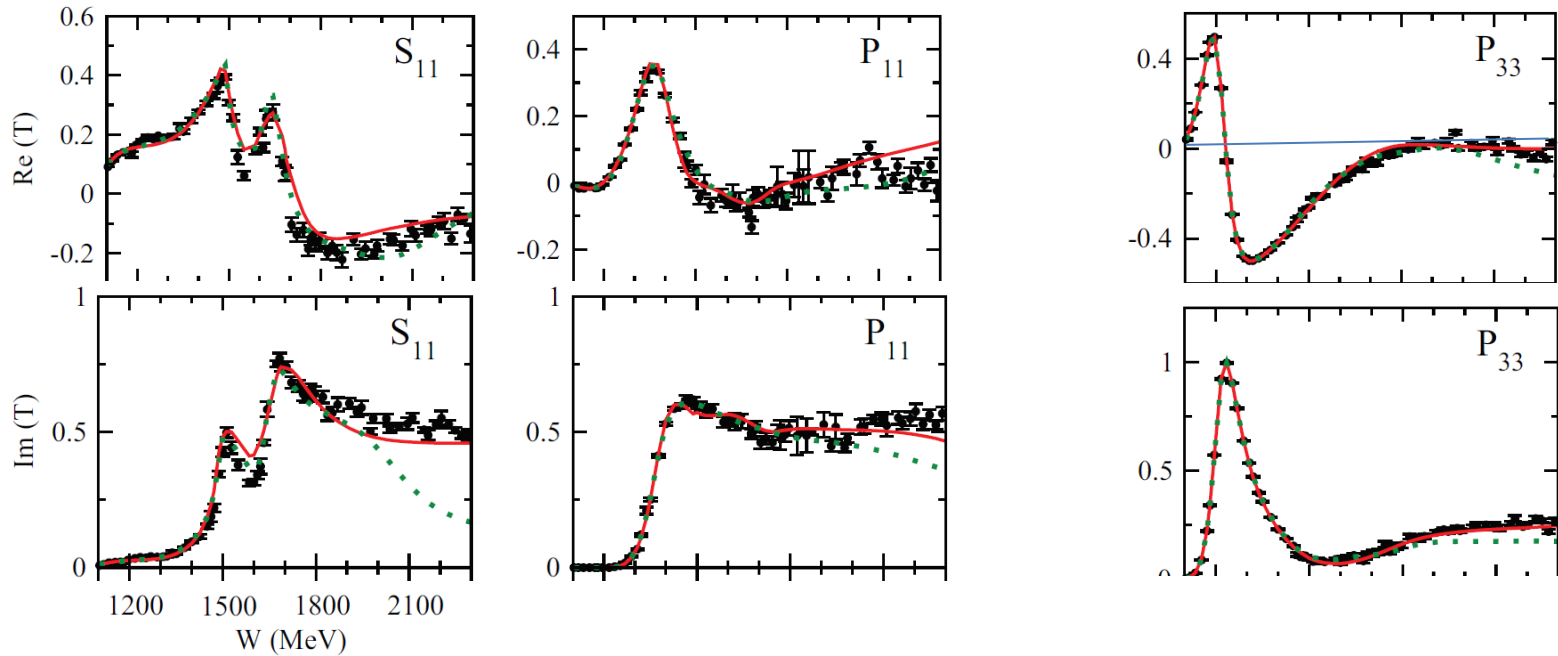


S. Capstic, N. Isgur PRD84(1984)



R. Edwards, et al. PRD84(2011)

# Excited states : resonances in meson-baryon scattering state

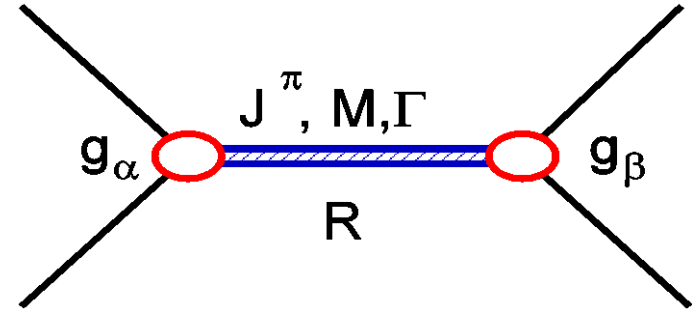


$N^*$ : large width, overlapping, inelastic resonances

- Reaction model (meson-baryon degrees of freedom)  
K-matrix approach, **dynamical reaction model**,...
- LQCD: scattering in box, effective potential

$\pi N \rightarrow \pi N, \eta N, KY, \omega N, \pi\pi N, \dots$   
 $\gamma^{(*)} N \rightarrow \pi N, \eta N, KY, \omega N, \pi\pi N, \dots$

**analysis of meson production reactions with  
Dynamical Coupled-Channels approach**



$$F_{em}(Q^2) = \langle N^* | J_{em}(Q^2) | N \rangle$$

- **partial wave amplitudes**
- **analytic continuation of amplitudes**

- **resonance spectrum (Mass, width and **transition form factor**)**
- **Role of reaction dynamics on the properties of excited states**

- Dynamical coupled channel approach(ANL-Osaka model)
- Transition form factor
- ◆ N-Delta transition Form factor : imaginary part of multipole amplitude
- ◆ Form factor from the residue at the resonance pole of amplitude
- ◆ Preliminary results from current DCC model

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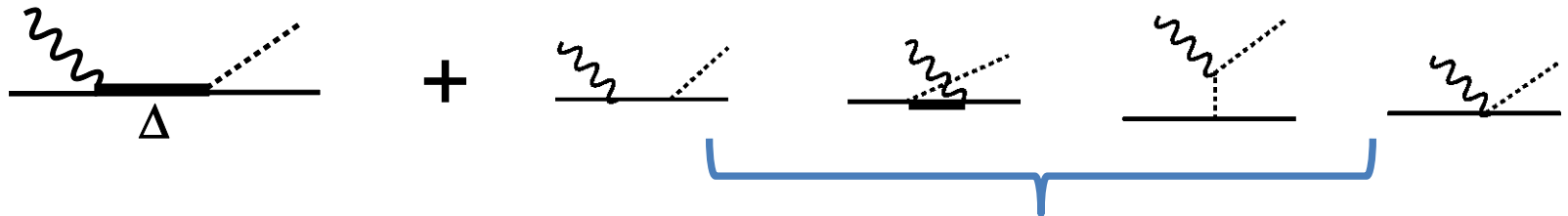
## Scattering amplitudes and unitarity

Phase relation among partial wave amplitudes is essential for the description of observables (polarization,...), unitarity plays important role.

Example: below two pion production threshold, phase of pion photoproduction amplitude is given by that of pion-nucleon elastic scattering. (Watson theorem)

$$T_{\gamma\pi}^{\alpha} = |T_{\gamma\pi}^{\alpha}| e^{i\delta_{\pi N}^{\alpha}}$$

Breit-Wigner resonant amplitude + non-resonant mechanisms does not work



Born diagrams (based on chiral Lagrangian)

Many meson-baryon channels open for  $W < 2\text{GeV}$

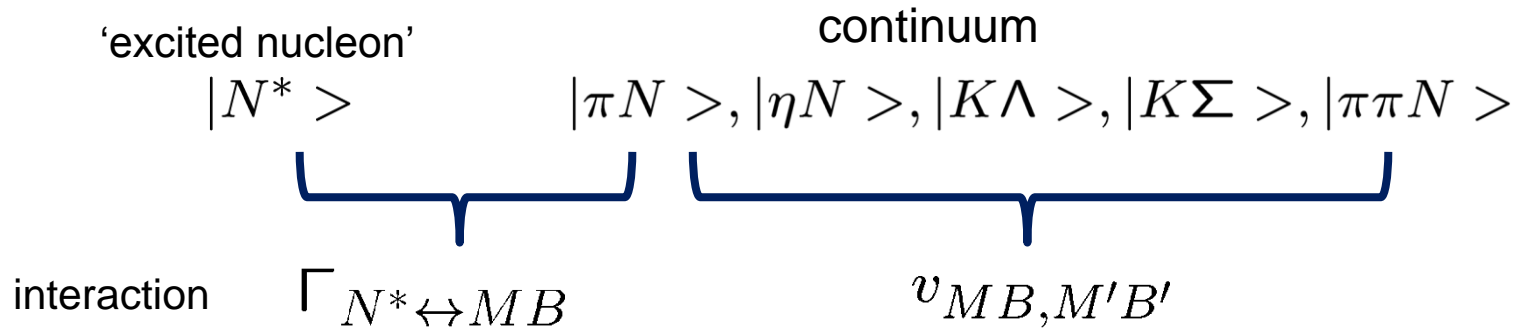
$$\pi N, \eta N, K\Lambda, K\Sigma, \pi\pi N, \omega N$$

Needs coupled channel approach with 2body+3body ( $\pi\pi N$ ) unitarity

$$\frac{T - T^{\dagger}}{i} = T^{\dagger}T$$

# Dynamical Coupled Channel Approach

start from Hamiltonian of meson-baryon system



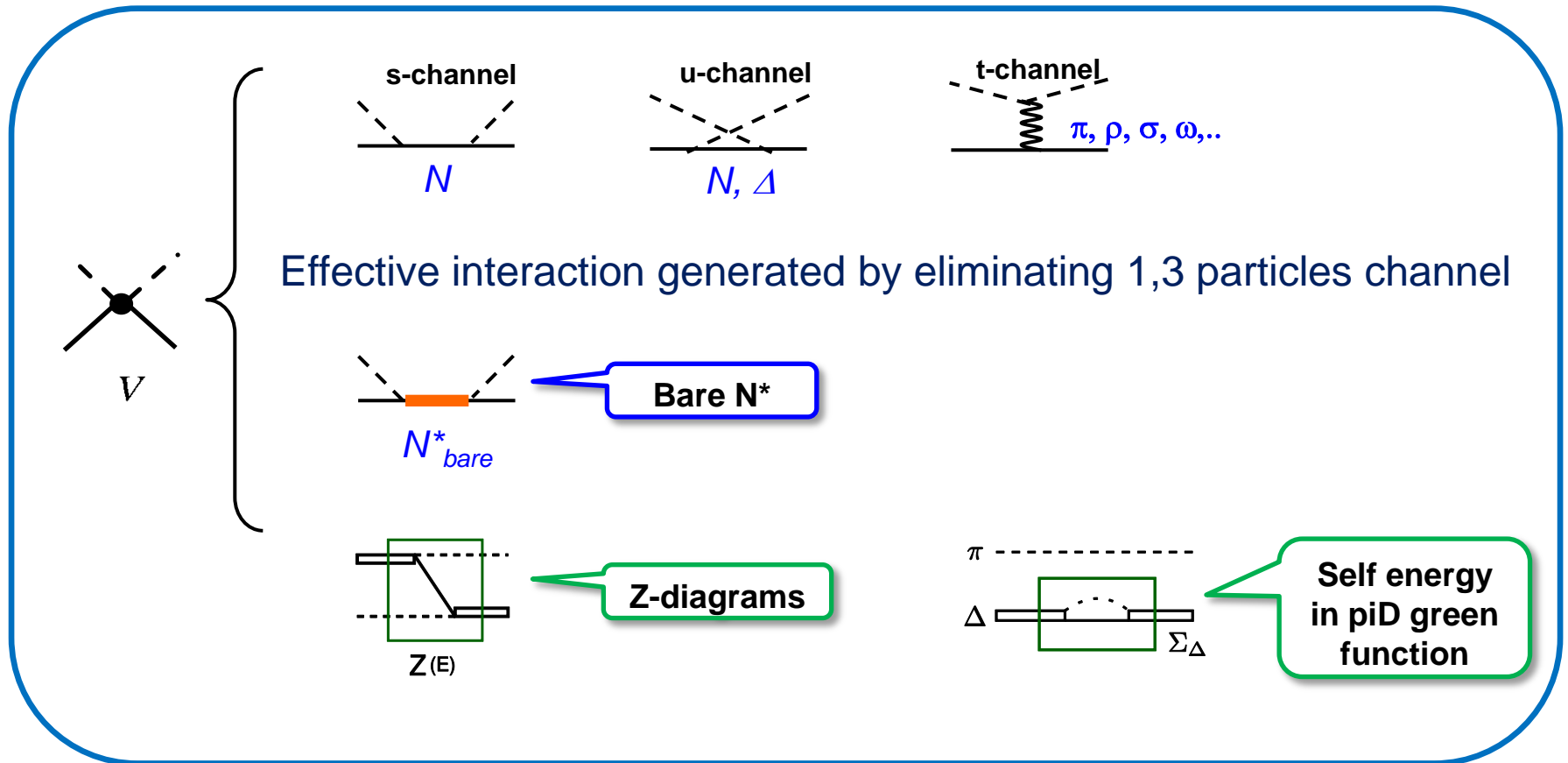
Hamiltonian  $\pi N \oplus \Delta \oplus \gamma N$



$$H = H_0 + v_{\pi N, \pi N} + v_{\pi N, \gamma N} + \Gamma_{\Delta \leftarrow \pi N} + \Gamma_{\Delta \leftarrow \gamma N} + (h.c.)$$



Building block of our model  $(\gamma^{(*)}N, \pi N, \eta N, \pi\Delta, \sigma N, \rho N, K\Lambda, K\Sigma, \dots)$



→ Solve scattering equation that satisfies two+three body unitarity

$$T_{\beta,\alpha}^{IJP}(k', k, W) = V_{\beta,\alpha}^{IJP}(k', k) + \sum_{\gamma} \int dq q^2 V_{\beta,\gamma}^{IJP}(k', q) G_{\gamma}^0(q, W) T_{\gamma,\alpha}^{IJP}(q, k, W)$$

$$\alpha, \beta, \gamma = (\gamma^{(*)}N, \pi N, \eta N, \underbrace{\pi\Delta, \sigma N, \rho N}_{\pi\pi N}, K\Lambda, K\Sigma, \dots)$$

each meson-exchange potential  $V$  contributes many partial waves

- partial waves,  $W$ -region, MB channels are related
- simultaneous analysis MB channels constrains model, but time consuming to fit data

Scattering amplitude can be rewritten as

$$T_{\alpha,\beta}(W) = t_{\alpha,\beta}^{nr}(W) + \sum_{i,j} \bar{\Gamma}_{\alpha,i}(W) \left[ \frac{1}{W - m_0 - \Sigma(W)} \right]_{ij} \bar{\Gamma}_{\beta,j}(W)$$

$\alpha, \beta$  Meson-Baryon channel

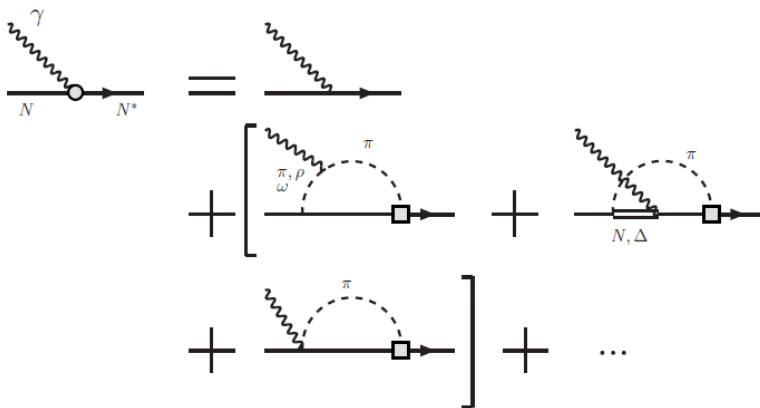
$i, j$  Resonances

$$\langle N_i^{*0} | \Sigma(W) | N_j^{*0} \rangle = \sum_{\alpha} \bar{\Gamma}(W)_{\alpha,i} G_{\alpha}^0(W) \Gamma(W)_{\alpha,j}$$



Non-trivial contribution of meson loop:

$$\bar{\Gamma}_{\gamma N \rightarrow \Delta}(E) = \Gamma_{\gamma N \rightarrow \Delta} + \int \bar{\Gamma}_{\Delta \rightarrow \pi N} G_{\pi N}^0(E) v_{\gamma\pi}$$



Core + Meson Cloud

- Dynamical coupled channel approach(ANL-Osaka model)
- Transition form factor
- ◆ N-Delta transition Form factor : imaginary part of multipole amplitude
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Delta(1232): isolated, elastic(BR~100% piN ) resonance

Sato, Lee PRC54(1996), PRC63(2001)

$\Delta + \pi N$ : fix model by analyzing  $(\pi N)$ ,  $(\gamma, \pi)$ ,  $(e, e' \pi)$

'Transition form factors' are presented by using the imaginary part of the multipole amplitudes at  $W=1.232$ , where piN phase shift of P33 channel goes through 90 degree.

$$G_M^* \sim \text{Im}[M_{1+}^{3/2}]$$

transition amplitude

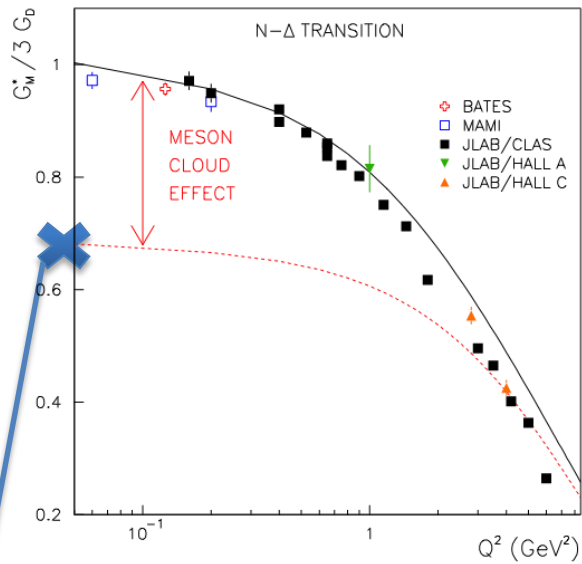
$$T_{\pi, \gamma}(W) = t_{\pi, \gamma}^{nr}(W) + \bar{\Gamma}_{\Delta \pi}(W) \left[ \frac{1}{W - m_0 - \Sigma_{\Delta}(W)} \right] \bar{\Gamma}_{\Delta \gamma}(W)$$

$$[\bar{\Gamma}_{\Delta, \gamma}^K]_{M1} = \sqrt{\frac{8\pi m_{\Delta} k \Gamma_{\Delta}}{3m_N q}} \times \text{Im}[M_{1+}^{3/2}]$$

$$\text{Similar relation : E2, C2} \leftrightarrow E_{1+}^{3/2}, S_{1+}^{3/2}$$

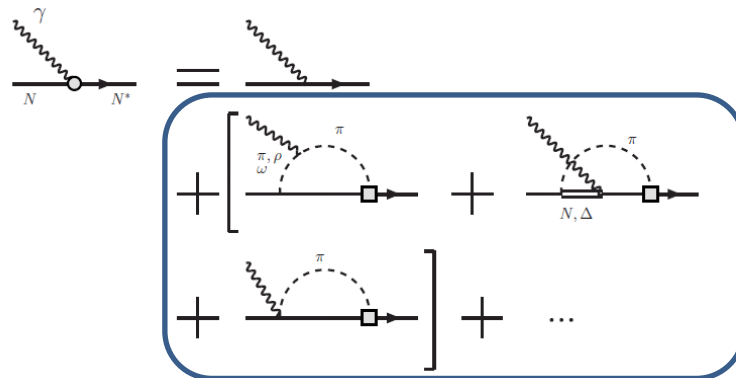
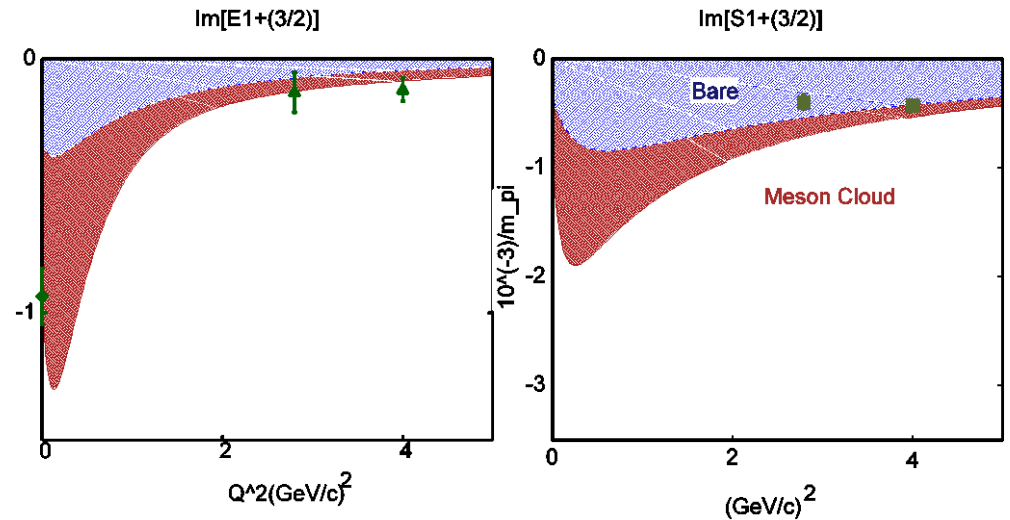
# $\gamma N \rightarrow \Delta(1232)$ (role of reaction dynamics)

M1: Magnetic dipole



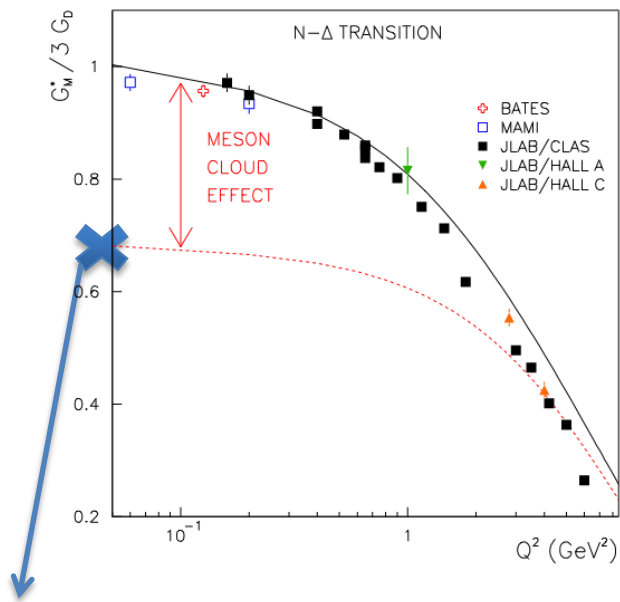
**Note:**  
Most of the available static hadron models give  $G_M(Q^2)$  close to "Bare" form factor.

Quadrupole transition E2,C2



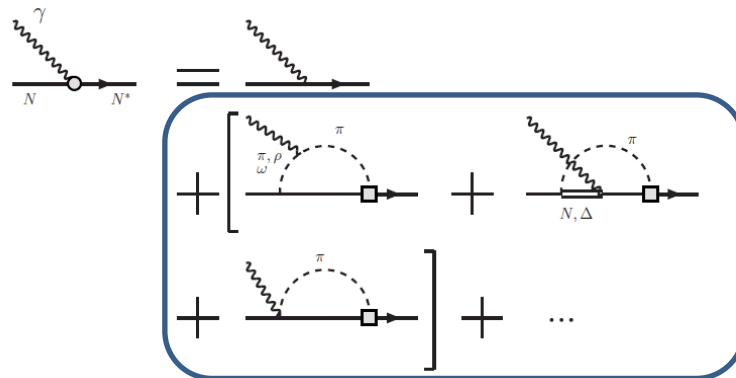
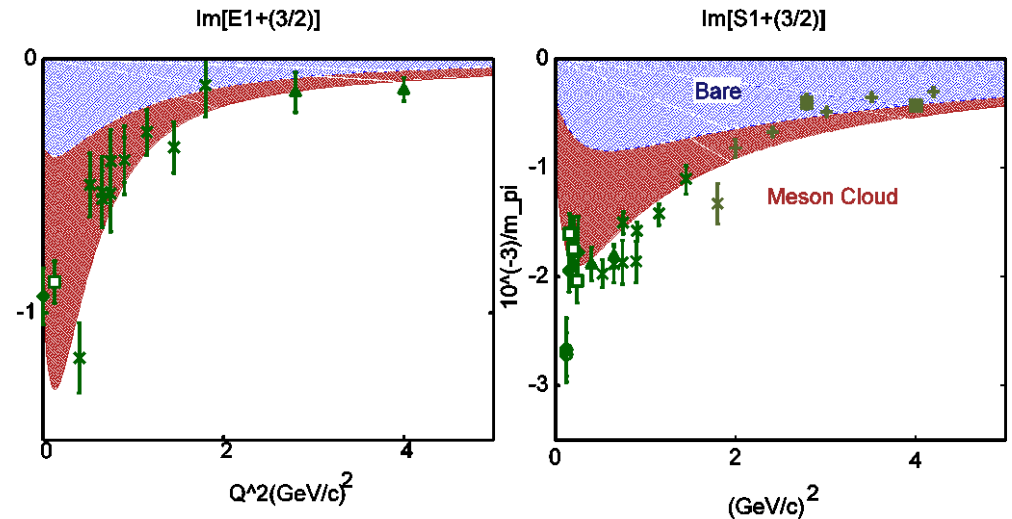
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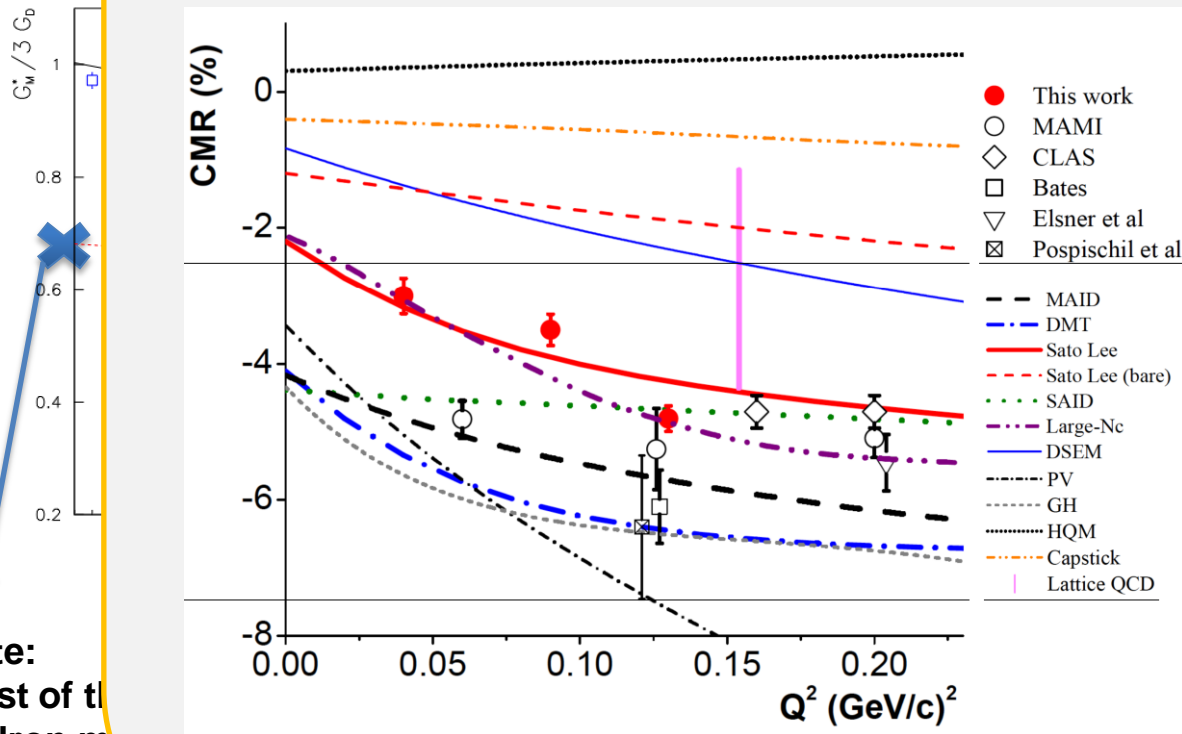
Phys. Lett. B760 (2016) 267, A. Blomberg et al.

M1:

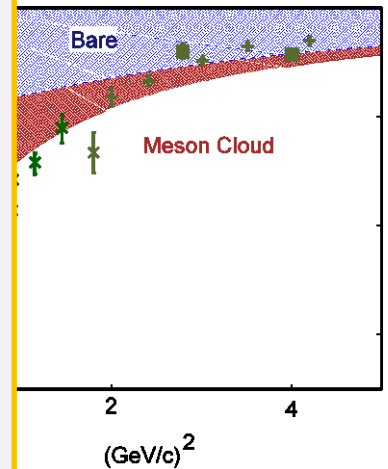
E2, C2

CMR = C2/M1

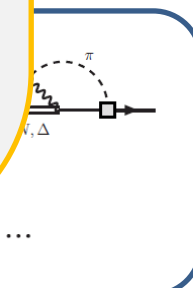
$G_M / 3 G_0$



$\text{Im}[S_{1+(3/2)}]$



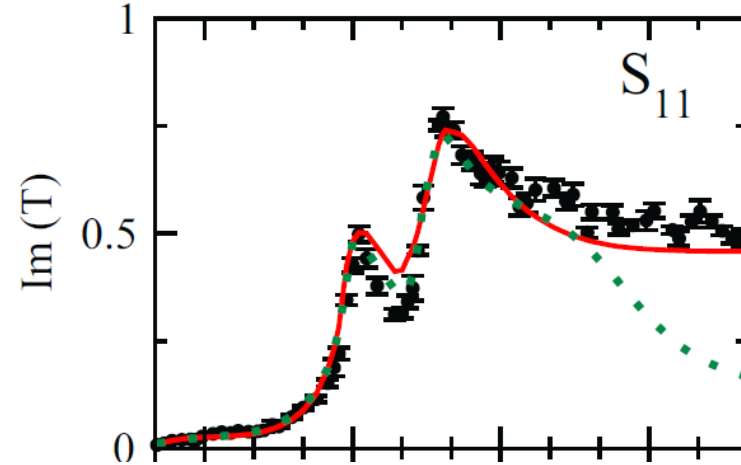
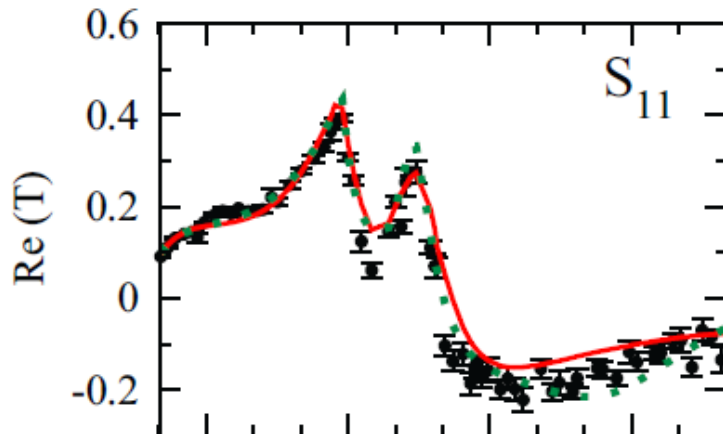
Note:  
Most of the  
hadron m  
close to "B"





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Calculating from factor from the imaginary part of the amplitudes does not work except Delta(1232)



$$T_{\beta,\alpha} = t_{\beta,\alpha}^{nr} + \bar{\Gamma}_{\beta,1} \left[ \frac{1}{W - m_0 - \Sigma} \right]_{11} \bar{\Gamma}_{\alpha,1} + \bar{\Gamma}_{\beta,1} \left[ \frac{1}{W - m_0 - \Sigma} \right]_{12} \bar{\Gamma}_{\alpha,2} \\ + \bar{\Gamma}_{\beta,2} \left[ \frac{1}{W - m_0 - \Sigma} \right]_{21} \bar{\Gamma}_{\alpha,1} + \bar{\Gamma}_{\beta,2} \left[ \frac{1}{W - m_0 - \Sigma} \right]_{22} \bar{\Gamma}_{\alpha,2}$$

Two resonances mix with each other through  $\Sigma$

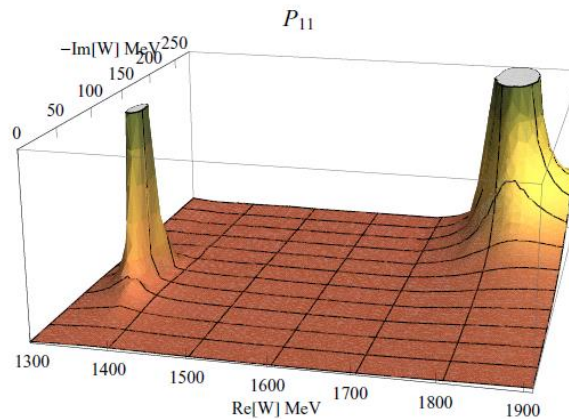
(In our previous report PRC80 (2009), we presented MC by using  $\bar{\Gamma}_{\gamma,1}$  at resonance energy)

## Extract resonance properties from pole of amplitude

$$T_{\alpha,\beta}(W) = t_{\alpha,\beta}^{nr}(W) + \sum_{i,j} \bar{\Gamma}_{\alpha,i}(W) \left[ \frac{1}{W - m_0 - \Sigma(W)} \right]_{ij} \bar{\Gamma}_{\beta,j}(W)$$

$$\sim \frac{\gamma_\alpha \gamma_\beta}{W - M + i\Gamma/2}$$

- Analytic continuation of  $T(W)$  on unphysical sheet by using contour deformation
- Pole can be found in the second term (non-resonant amplitude may have a pole)



Resonance Mass

(Single resonance case)

$$M - i\Gamma/2 = m_0 + \Sigma(M - i\Gamma/2)$$

Resonance Form Factor (complex number)

$$\langle N^* | j_{em} | N \rangle = \frac{1}{\sqrt{1 - d\Sigma/dW}} \bar{\Gamma}(M - i\Gamma/2)$$

$$|N^* \rangle = \frac{1}{\sqrt{1 - d\Sigma/dW}} [1 + G_0^\dagger (1 + t^{non-res}) \Gamma] |N_0^* \rangle$$

□ Dynamical coupled channel approach(ANL-Osaka model)

□ Transition form factor

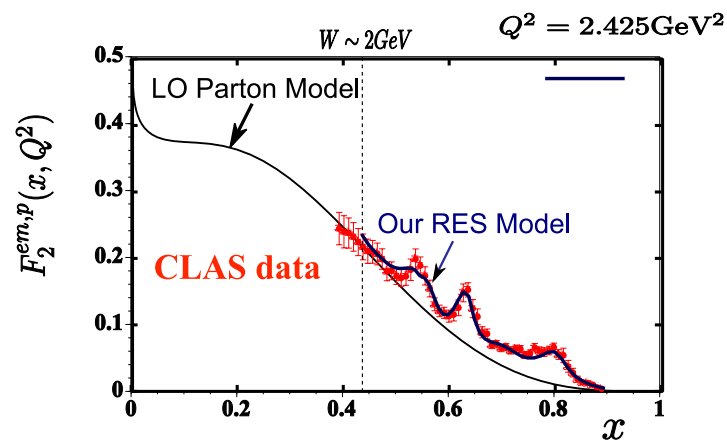
◆ N-Delta transition Form factor : imaginary part of multipole amplitude

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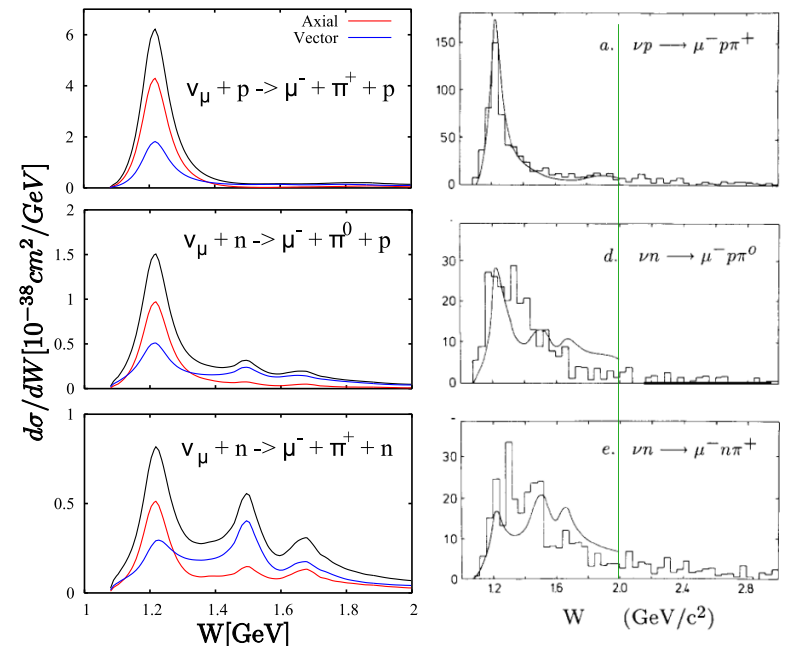
◆ Preliminary results from current DCC model

# models for meson production reactions

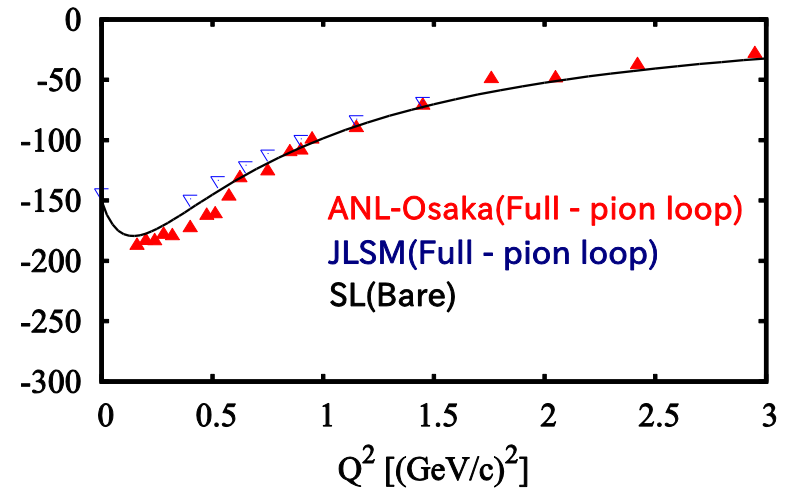
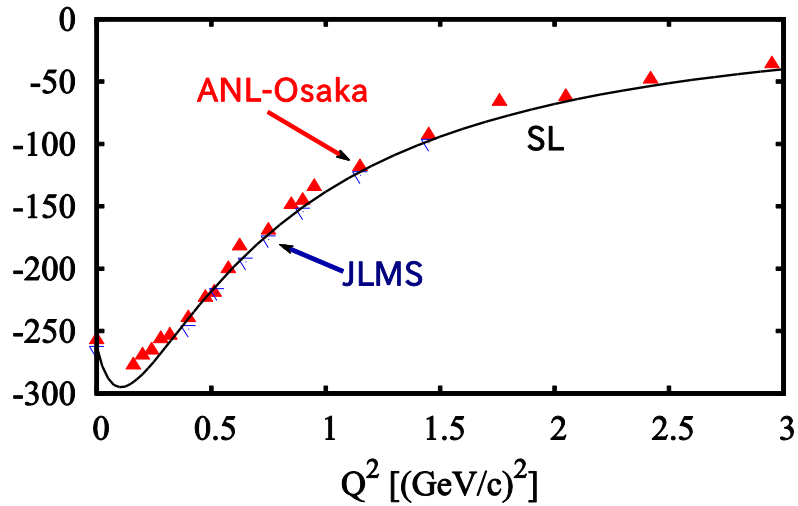
- JLSM model: B. Julia-Diaz et al. PRC76 (2007) (EBAC)
  - pion photo and electroproduction: B. Julia-Diaz PRC80(2009)
- tools to extract resonance information from the pole of amplitudes:
  - N.Suzuki et al. PRC79(2009),C82(2010)
- Grand fit model (Current): H.Kamano et al. PRC83(2013) (ANL-Osaka)
  - neutrino induced meson production reaction: S.Nakamura et al. PRC92 (2015)
  - pion photoproduction on neutron: H.Kamano et al. PRC94(2016)
  - electron scattering (preliminary results)



$E_{\nu}=40\text{GeV}$ , BEBC NP343, 285(1990)

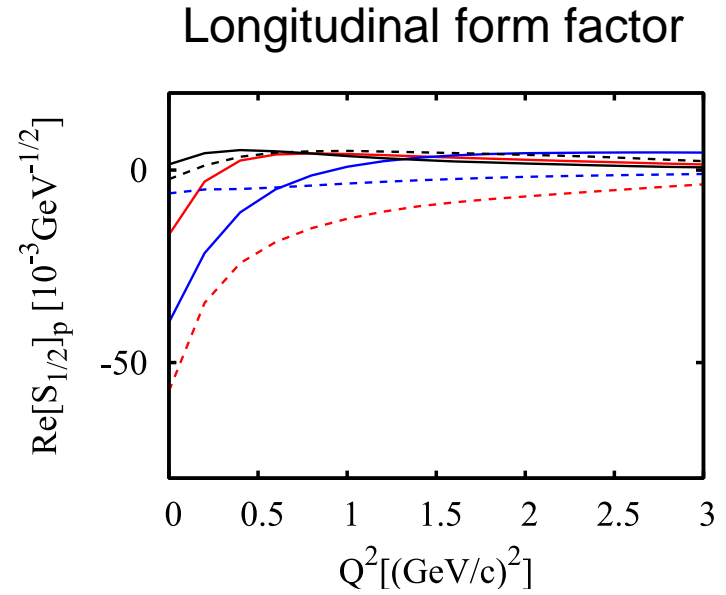
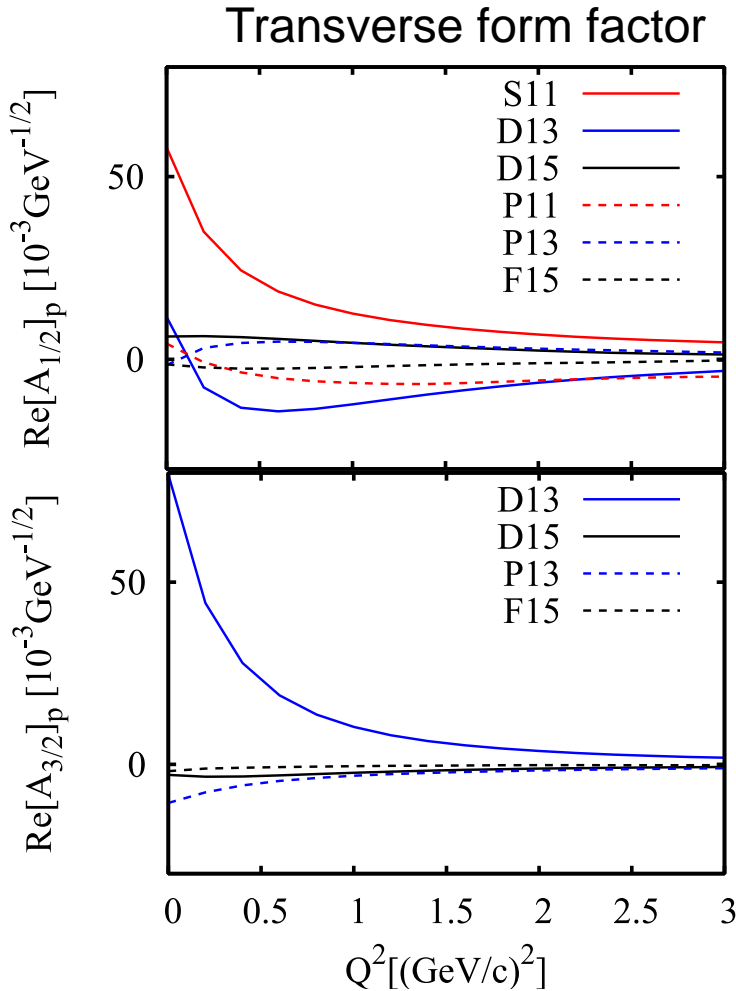


# Stability of extracted form factor of Delta(1232) $\text{Re}(A_{\{3/2\}})$



extracted  $A_{\{3/2\}}$ , pion loop contribution of three reaction models agree well

# Multipole dependence of meson loop contribution (Preliminary)



N1520

$$A_{3/2} = -\frac{\sqrt{3}}{2}[E_{2-} + M_{2-}]$$

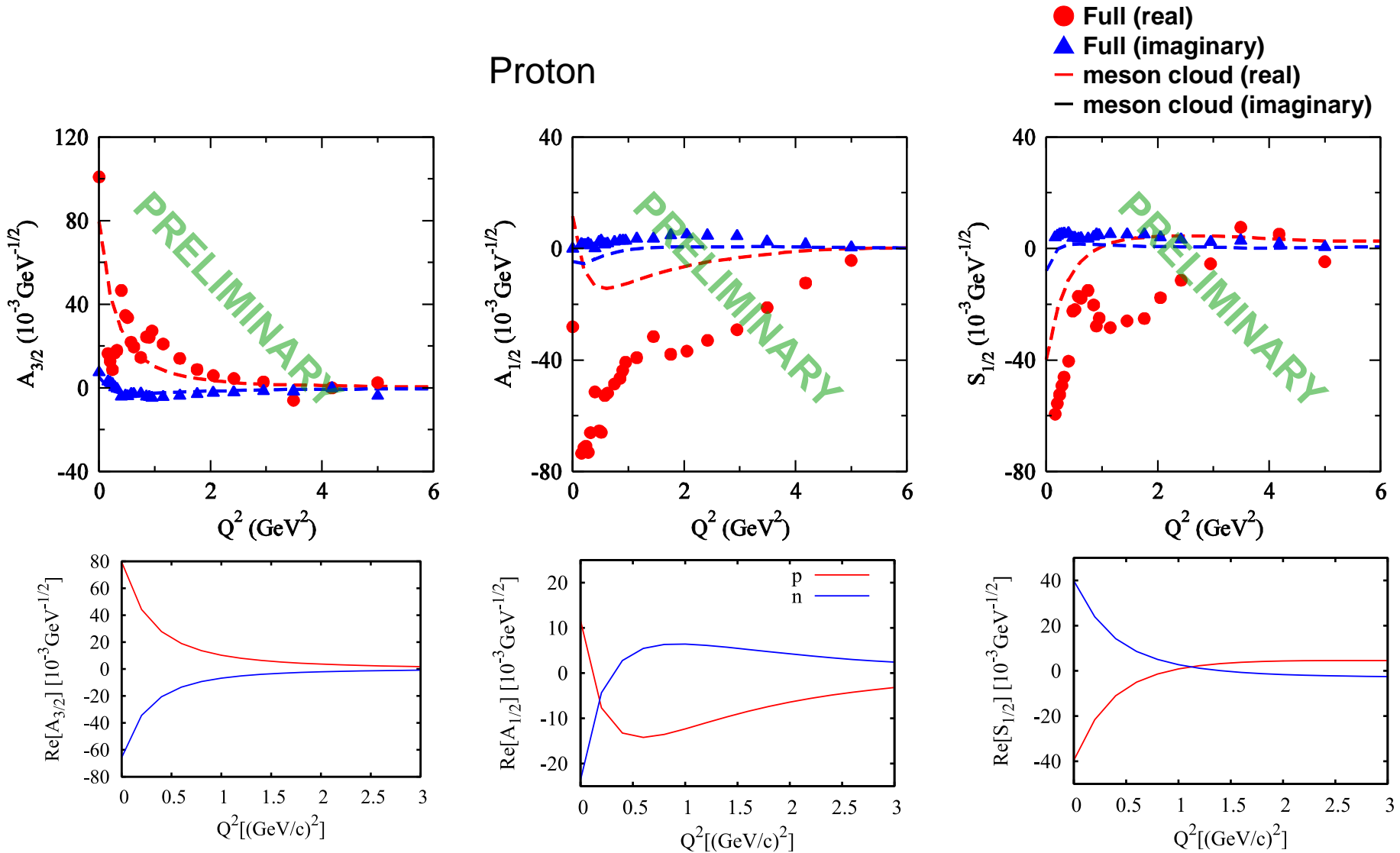
$$A_{1/2} = -\frac{1}{2}[E_{2-} - 3M_{2-}]$$

	T	L
S11(N1535 1/2-)	E1(E0+)	C1(S0+)
D13(N1520 3/2-)	E1(E2-),M2(M2-)	C1(S2-)
D15(N1675 5/2-)	E3(E2+),M2(M2+)	C3(S2+)
P11(N1440 1/2+)	M1(M1-)	C0(S1-)
P13(N1720 3/2+)	M1(M1+),E2(E1+)	C2(S1+)
F15(N1680 5/2+)	M3(M3-),E2(E3-)	C2(S3-)

larger meson loop for lower multipole



Proton

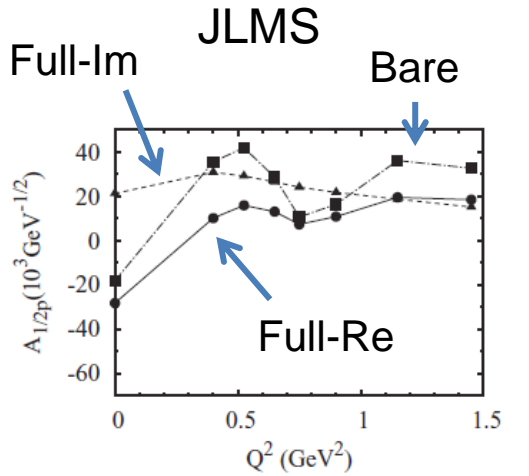


Meson-loop ~ iso-vector, interesting to study transition form factor of neutron

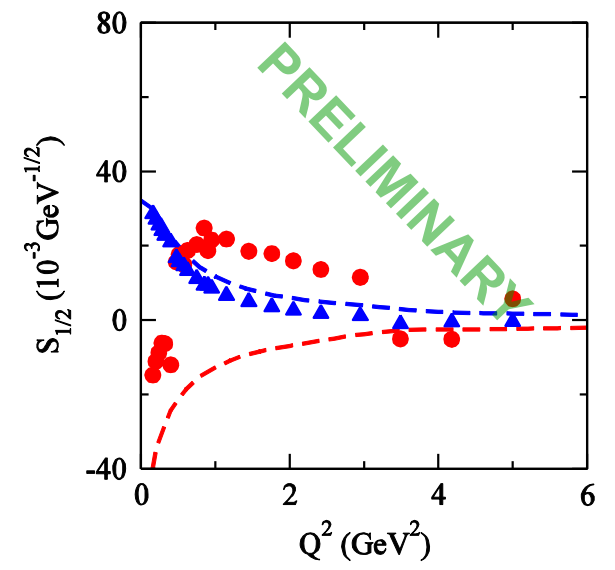
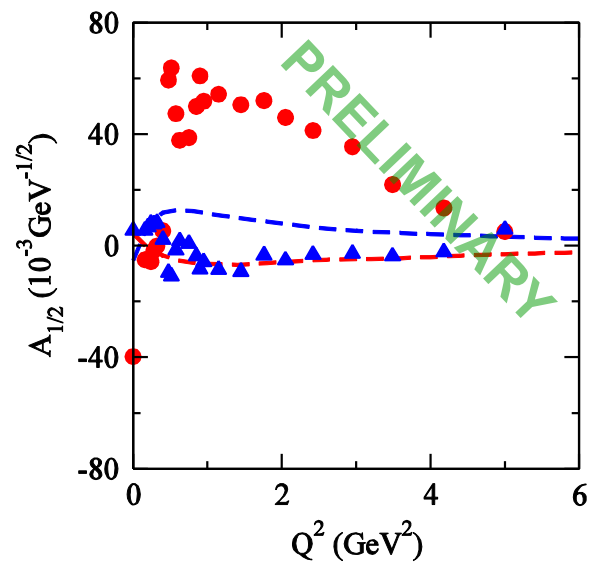
# N1440 1/2+ (proton)

## ANL-Osaka Current

- Full (real)
- ▲ Full (imaginary)
- meson cloud (real)
- meson cloud (imaginary)



Suzuki et al. PRC82 (2009)



Total Helicity amplitude at  $Q^2=0$

$$A_p^{1/2} = -40e^{-i8^\circ} (10^{-3} GeV^{-1/2})$$

$$A_n^{1/2} = 95e^{-i15^\circ} (10^{-3} GeV^{-1/2})$$

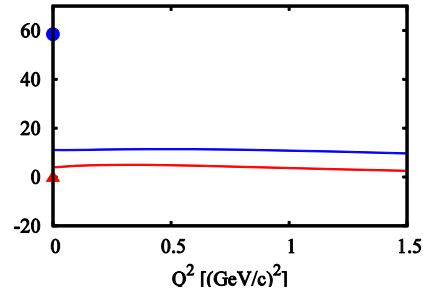
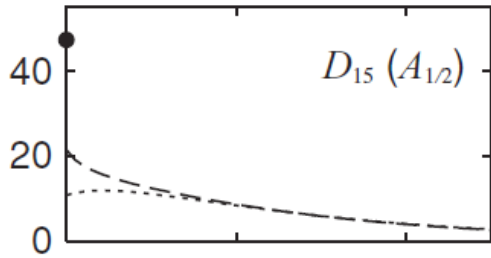
# N1675 5/2-(proton)

EBAC(JLMS)

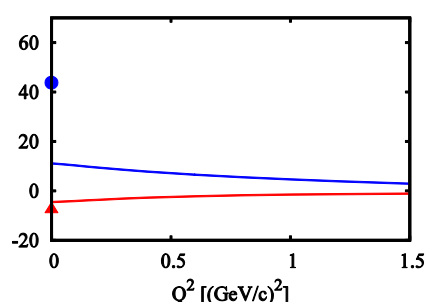
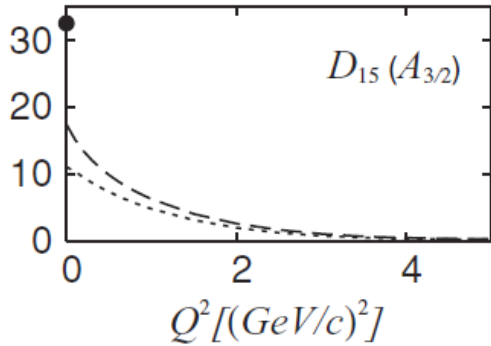
real W, not pole

Pole

D15



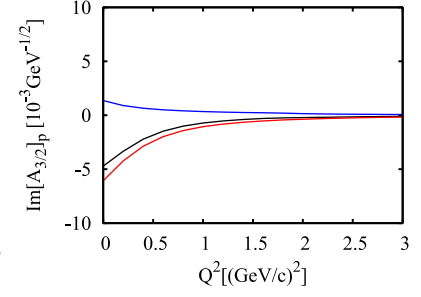
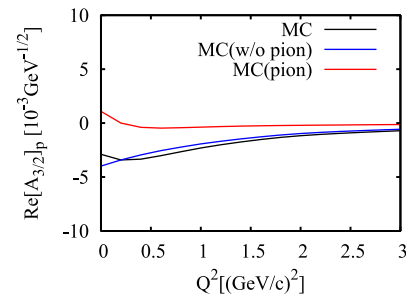
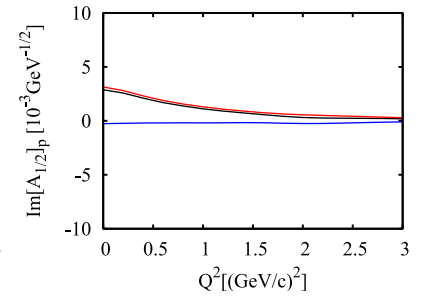
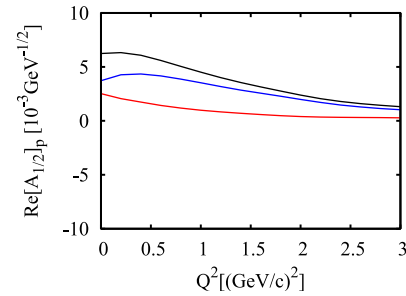
D15



ANL-Osaka Current

Re

Im



PRC77 (2008) B. Julia-Diaz et al.

$$A_{1/2p} = 8e^{i19^\circ}$$

$$A_{3/2p} = 49e^{-i12^\circ}$$

$$A_{1/2n} = -76e^{i3^\circ}$$

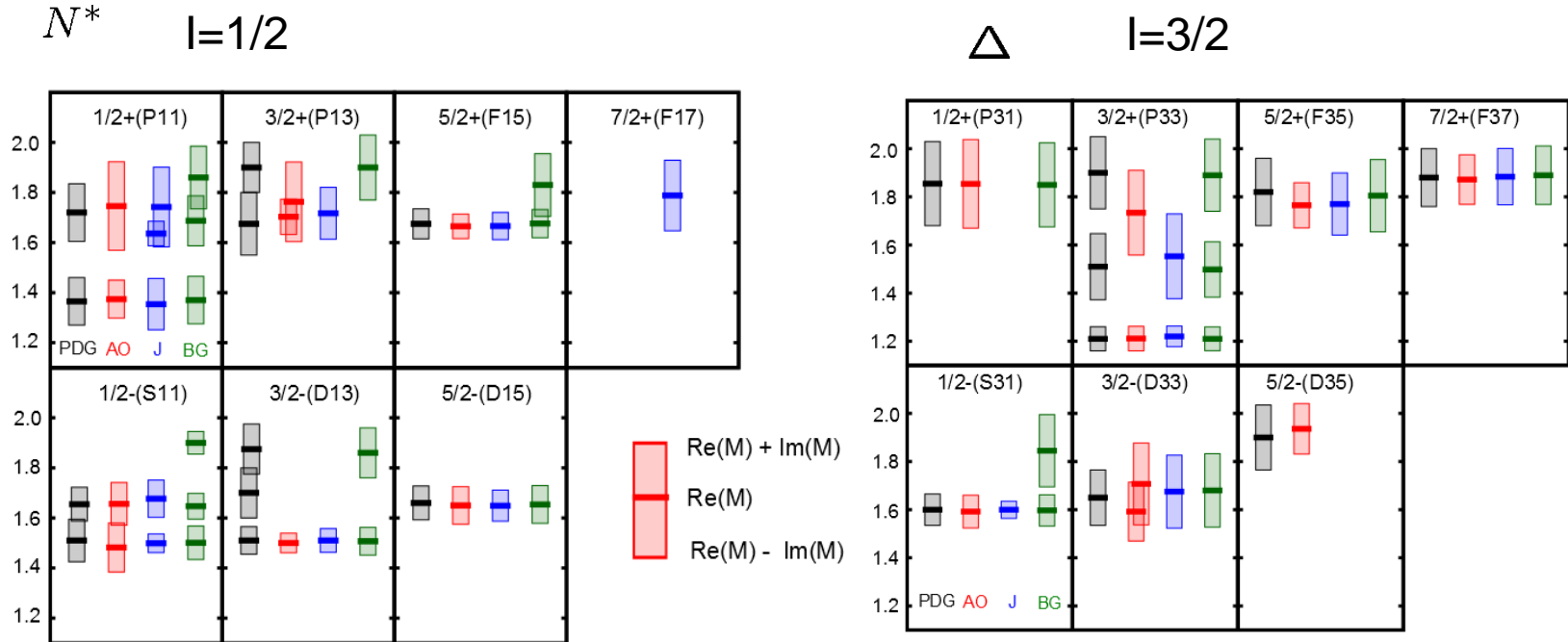
$$A_{3/2n} = -38e^{-i4^\circ}$$

## Summary

- ❑ We have investigated within a dynamical coupled channel model of pi-N and gamma-N reactions up to 2GeV
- ❑ The meson baryon channels included in calculations are  
 $\gamma N \pi N, \eta N, K\Lambda, K\Sigma \pi\pi N$  ( $\pi\Delta, \rho N$  and  $\sigma N$ )
- ❑ Pole positions and residues(coupling constants of N\*) are extracted by analytic continuation of the amplitudes.
- ❑ Qualitative feature of Meson loop effects: Q<sup>2</sup> dependence, multipole dep., iso-spin dep.

# Spectrum of nucleon resonances: pole of amplitude

$\text{Re}(M) < 2\text{GeV}$ ,  $\text{Width} < 0.4\text{GeV}$ , (AO only poles on the nearest sheet)



AO: Argonne-Osaka

J: Julich (model A: dynamical reaction model)  
EPJA(2013)**49**,44 D. Ronchen et al.

BG: Bonn-Gachina(K-matrix approach)  
EPJ A(2012)**48**,15 A.V.Anisovich et al.

PDG: 2012 3\*, 4\*

- AO agree with PDG for  $W < 2\text{GeV}$  (3\*, 4\*) except no 3rd P33, D13, additional 2nd D33, 2nd S31
- Pole positions of AO, Julich, Bonn-Gachina agree well only for the first  $N^*$

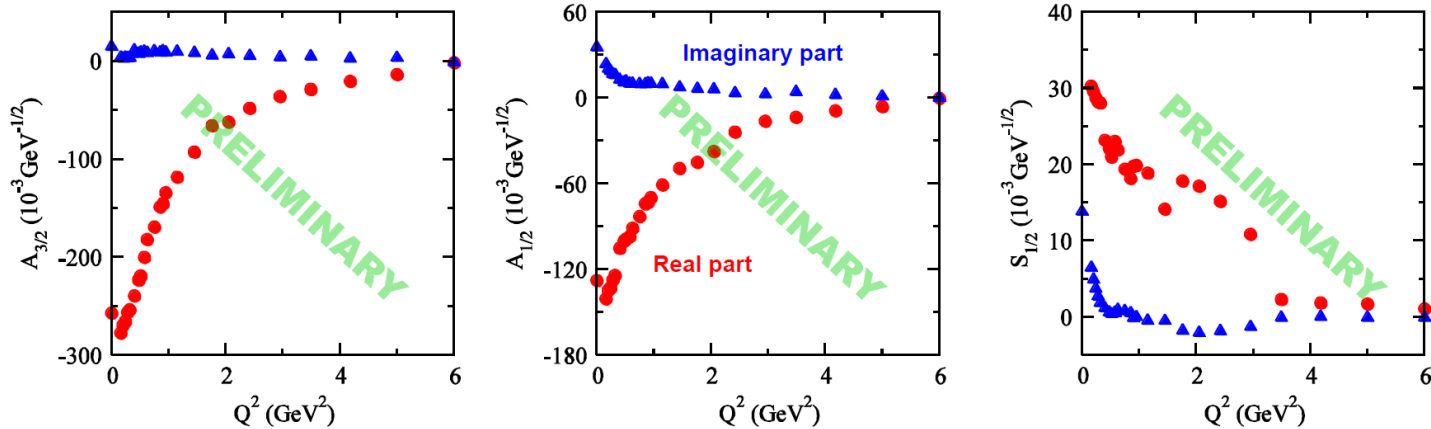
# Transition form factor of N\* and Delta

$$\langle \Delta | j_{em}(q) | N \rangle$$

Residue of helicity amplitude at resonance pole: complex number

form factors are determined at each  $Q^2$

$\gamma^{(*)} p \rightarrow \Delta(1232) 3/2^+$



$\gamma^{(*)} p \rightarrow N(1440) 1/2^+$

