

Equation of state and neutrino-matter interactions from chiral effective field theory

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DFG



Bundesministerium
für Bildung
und Forschung



Main points

EOS is **well constrained by ab initio calculations** for
Neutron-rich conditions and nondegenerate conditions
especially interesting for proto-neutron star cooling and mergers

General EOS band based on nuclear physics and observations
neutron star radius 9.7-13.9 km for $M=1.4 M_{\text{sun}}$ ($\pm 18\%$)

Chiral EFT important for consistent neutrino-matter interactions

**Enhancement of neutrino bremsstrahlung at low densities,
important for inelastic scattering**

Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV



	NN	3N	4N
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N ² LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N ³ LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

include long-range pion physics

short-range couplings, fit to experiment once

systematic: can work to desired accuracy and obtain **error estimates**

consistent **electroweak interactions** and **matching to lattice QCD**

new developments in power counting, uncertainty quantification, **optimization** Ektröm, Forssen, Furnstahl,...

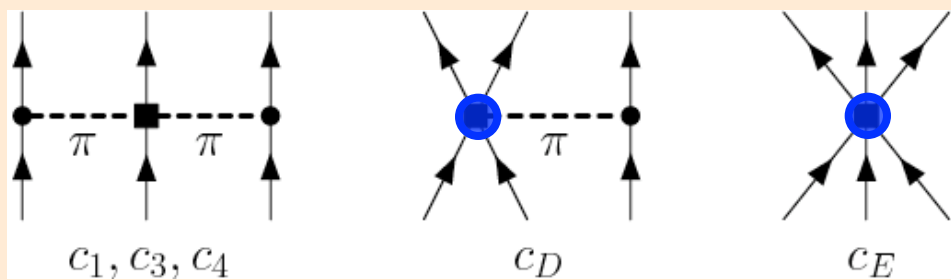
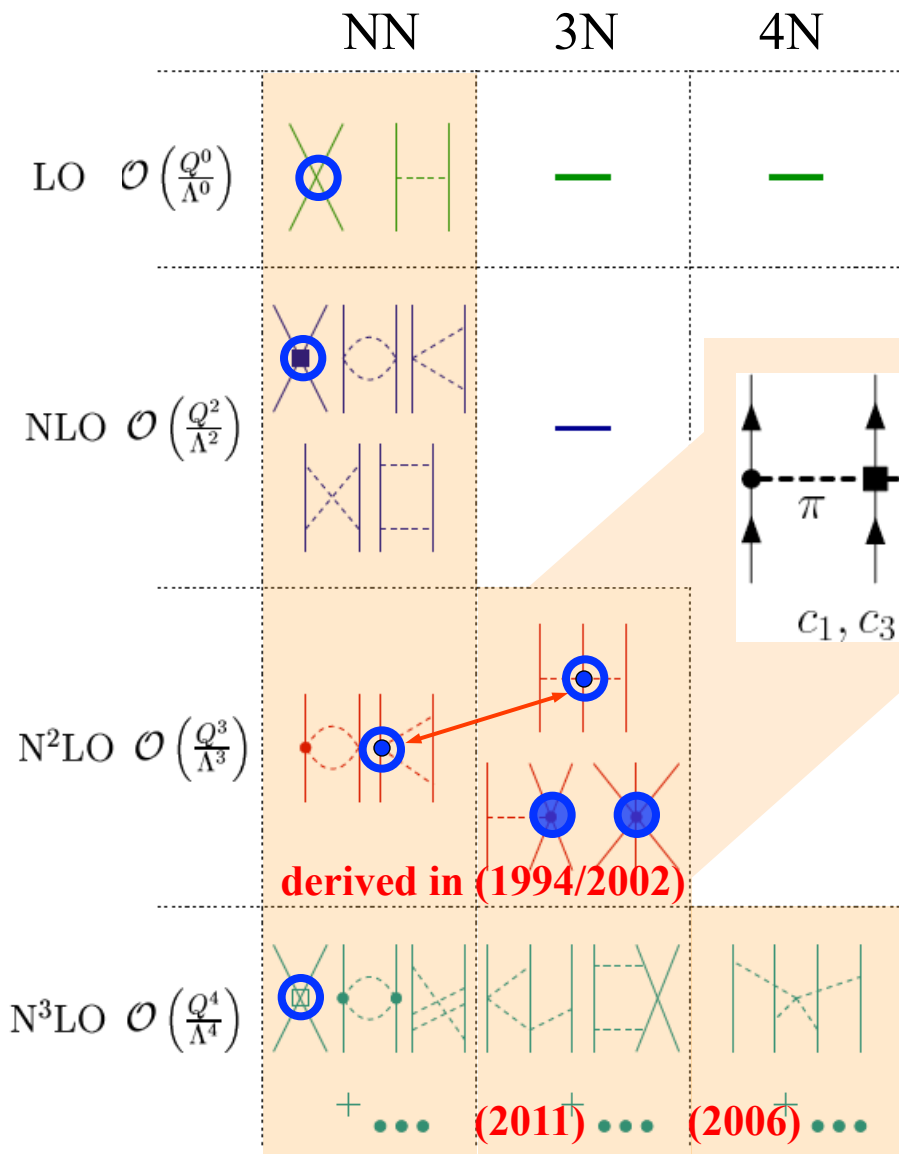
Weinberg, van Kolck, Kaplan, Savage, Wise, Bernard, Epelbaum, Kaiser, Machleidt, Meissner,...

Chiral effective field theory and many-body forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV

consistent NN-3N-4N interactions

3N,4N: **2 new couplings to N³LO**
+ no new couplings for neutrons



c_i from π N and NN

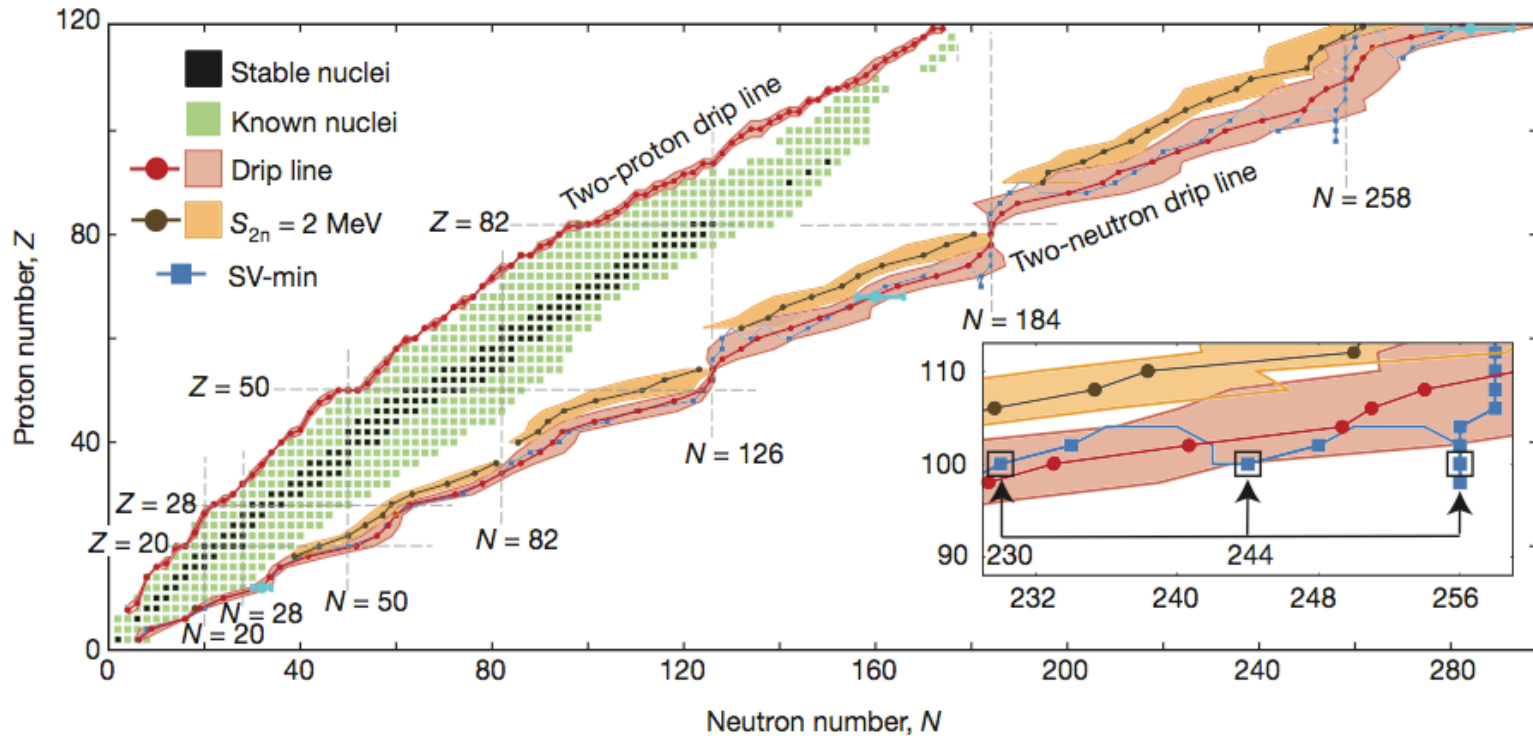
c_D, c_E fit to light nuclei only

Nuclei bound by strong interactions

doi:10.1038/nature11188

The limits of the nuclear landscape

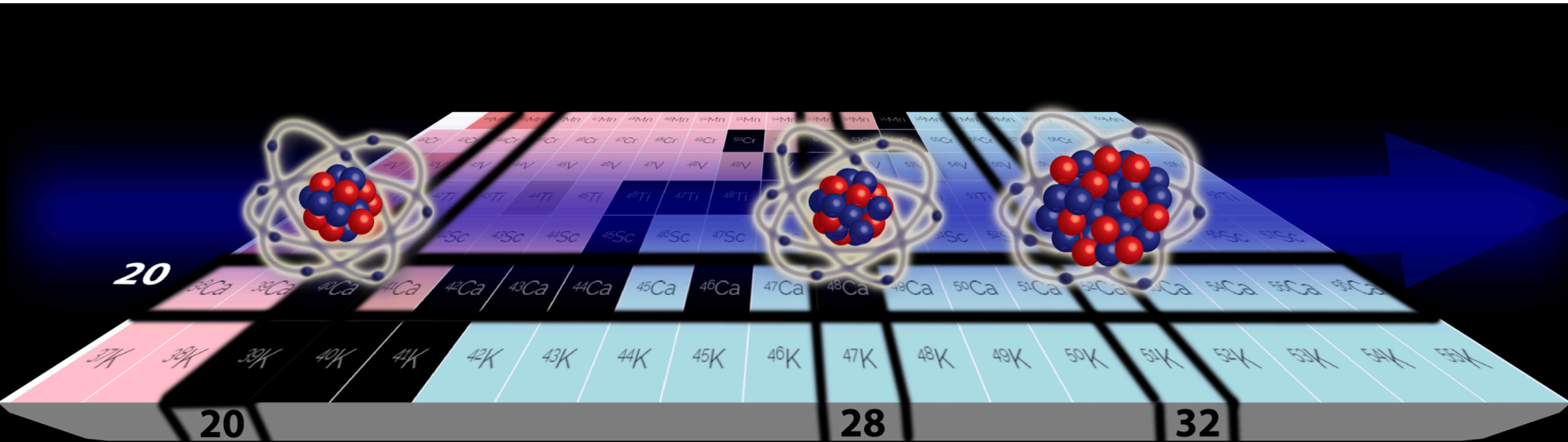
Jochen Erler^{1,2}, Noah Birge¹, Markus Kortelainen^{1,2,3}, Witold Nazarewicz^{1,2,4}, Erik Olsen^{1,2}, Alexander M. Perhac¹ & Mario Stoitsov^{1,2†}



How does the nuclear chart emerge from chiral EFT?

Future: Connect chiral EFT to Lattice QCD

Neutron-rich calcium isotopes



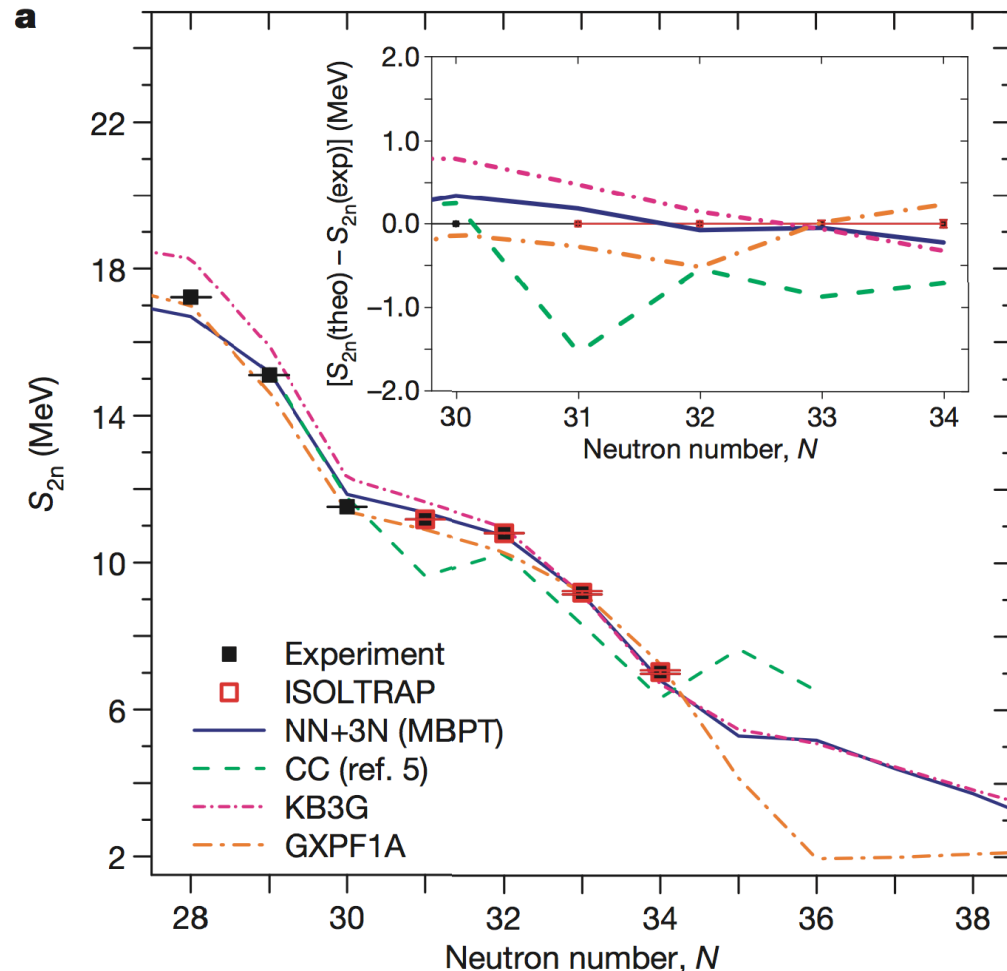
Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholtz¹, D. Beck², K. Blaum³, Ch. Borgmann³, M. Breitenfeldt⁴, R. B. Cakirli^{3,5}, S. George¹, F. Herfurth², J. D. Holt^{6,7}, M. Kowalska⁸, S. Kreim^{3,8}, D. Lunney⁹, V. Manea⁹, J. Menéndez^{6,7}, D. Neidherr², M. Rosenbusch¹, L. Schweikhard¹, A. Schwenk^{7,6}, J. Simonis^{6,7}, J. Stanja¹⁰, R. N. Wolf¹ & K. Zuber¹⁰

$^{53,54}\text{Ca}$ masses measured at ISOLTRAP/CERN using new MR-TOF mass spectrometer

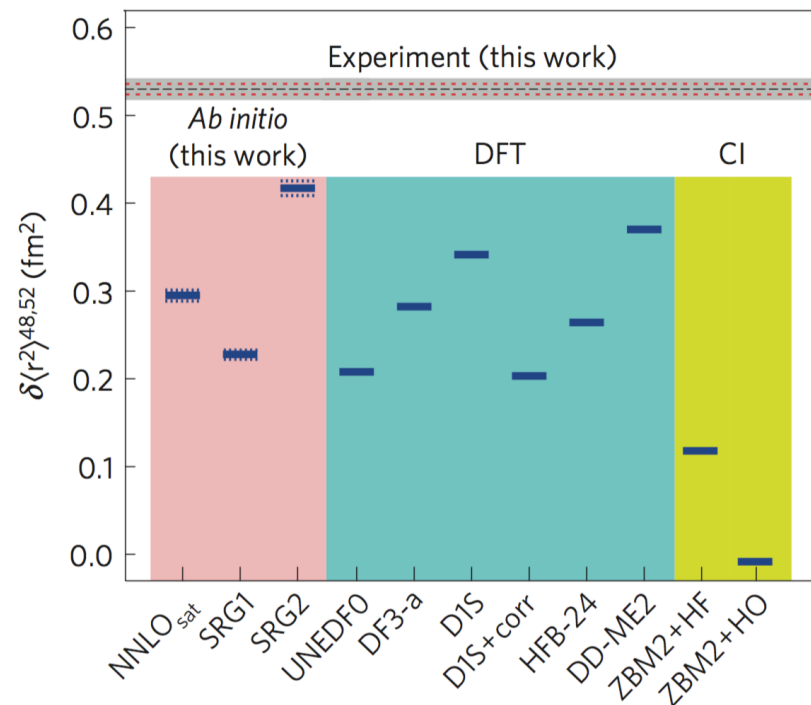
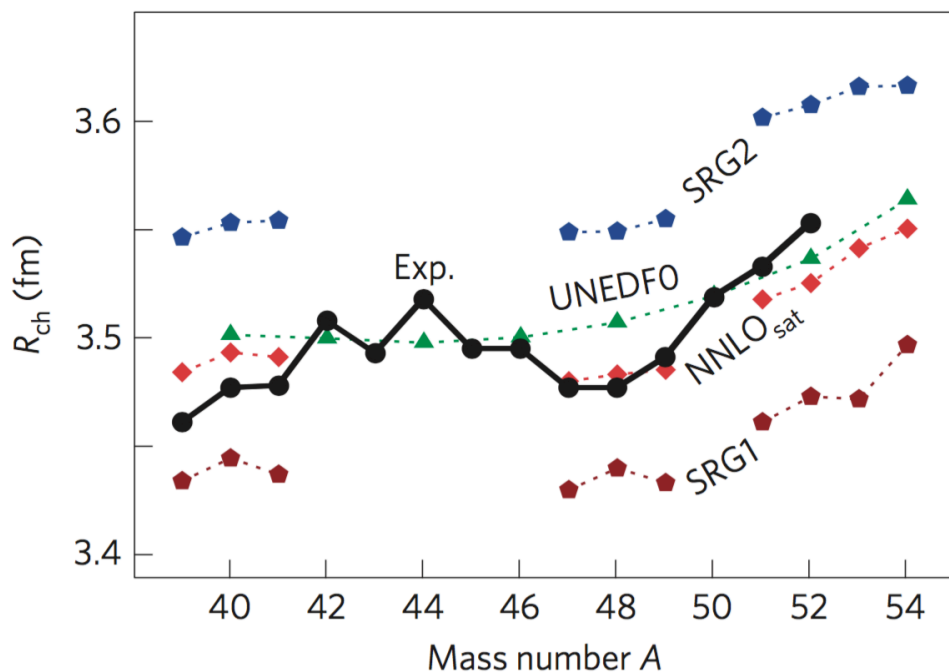
excellent agreement with theoretical NN+3N prediction

suggests $N=32$ shell closure



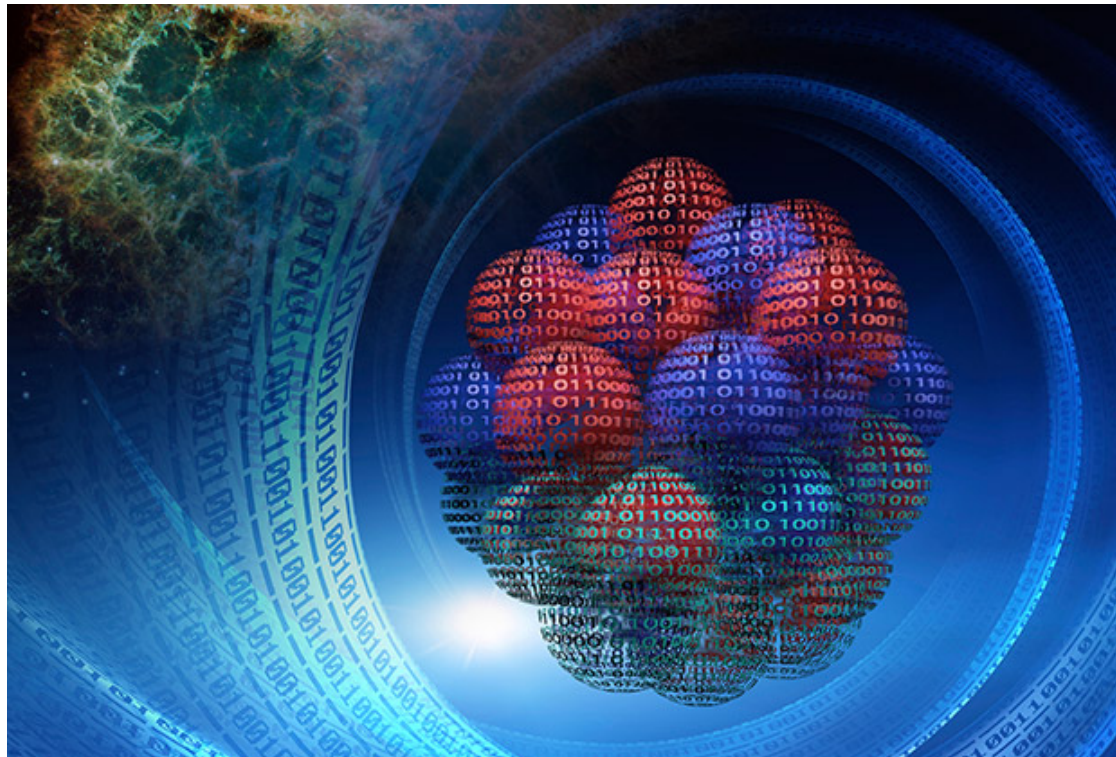
Unexpectedly large charge radii of neutron-rich calcium isotopes

R. F. Garcia Ruiz^{1*}, M. L. Bissell^{1,2}, K. Blaum³, A. Ekström^{4,5}, N. Frömmgen⁶, G. Hagen⁴, M. Hammen⁶, K. Hebeler^{7,8}, J. D. Holt⁹, G. R. Jansen^{4,5}, M. Kowalska¹⁰, K. Kreim³, W. Nazarewicz^{4,11,12}, R. Neugart^{3,6}, G. Neyens¹, W. Nörtershäuser^{6,7}, T. Papenbrock^{4,5}, J. Papuga¹, A. Schwenk^{3,7,8}, J. Simonis^{7,8}, K. A. Wendt^{4,5} and D. T. Yordanov^{3,13}



Neutron and weak-charge distributions of the ^{48}Ca nucleus

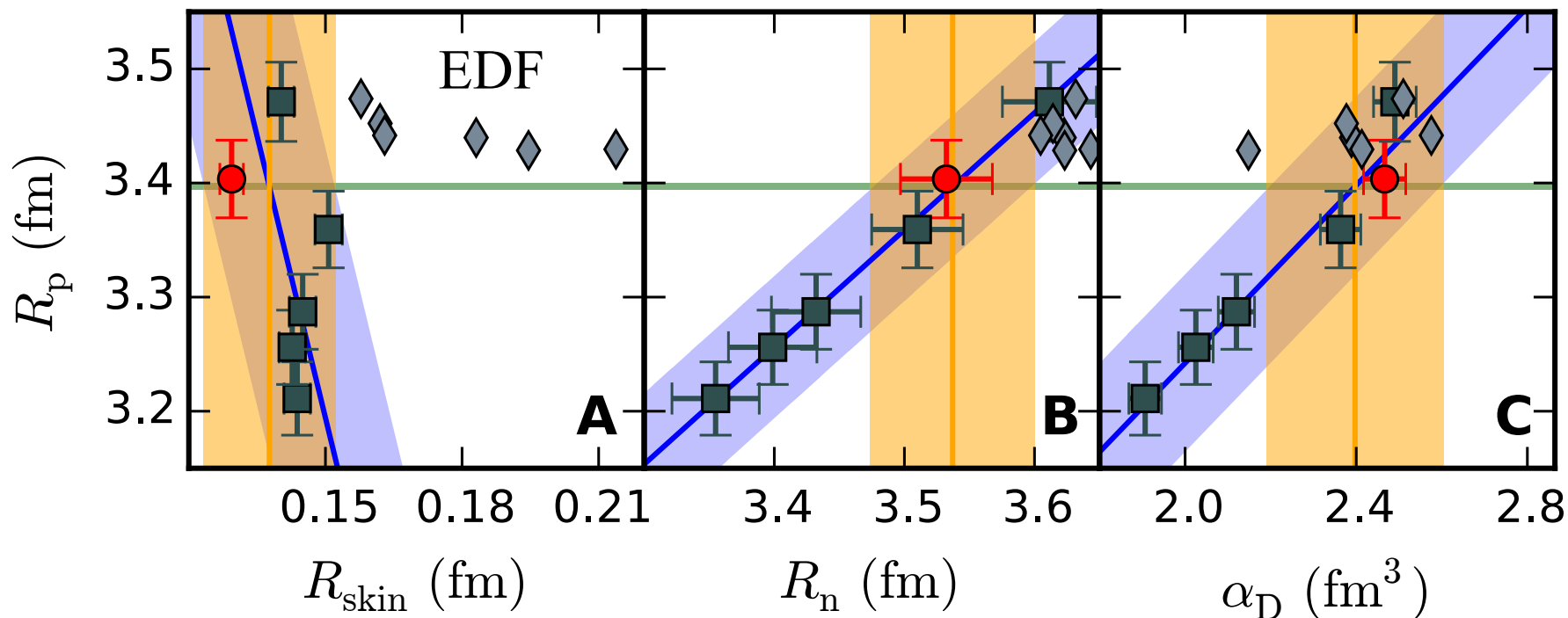
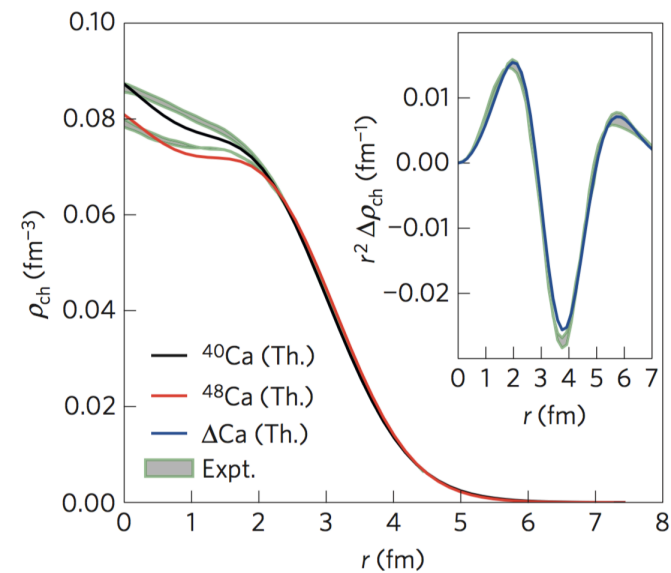
G. Hagen^{1,2*}, A. Ekström^{1,2}, C. Forssén^{1,2,3}, G. R. Jansen^{1,2}, W. Nazarewicz^{1,4,5}, T. Papenbrock^{1,2},
K. A. Wendt^{1,2}, S. Bacca^{6,7}, N. Barnea⁸, B. Carlsson³, C. Drischler^{9,10}, K. Hebeler^{9,10},
M. Hjorth-Jensen^{4,11}, M. Miorelli^{6,12}, G. Orlandini^{13,14}, A. Schwenk^{9,10} and J. Simonis^{9,10}



Neutron and weak-charge distributions of ^{48}Ca

ab initio calculations lead to charge distributions consistent with experiment

predict **small neutron skin**, dipole polarizability, and weak formfactor

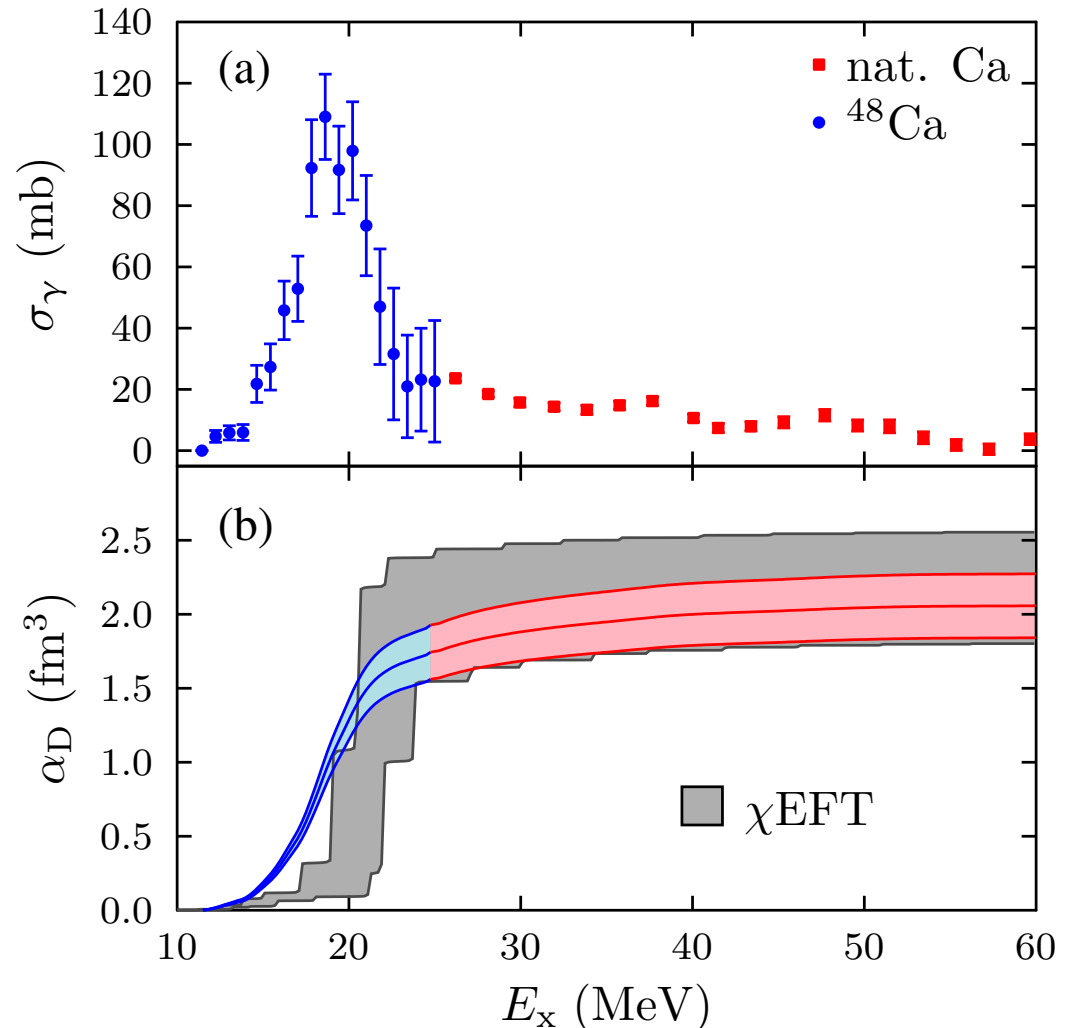


Dipole polarizability of ^{48}Ca

from photo-absorption cross section, measured at Osaka up to 25 MeV

Birkhan, von Neumann-Cosel, Richter, Tamii et al.

very similar to ^{40}Ca except for shift of giant dipole resonance

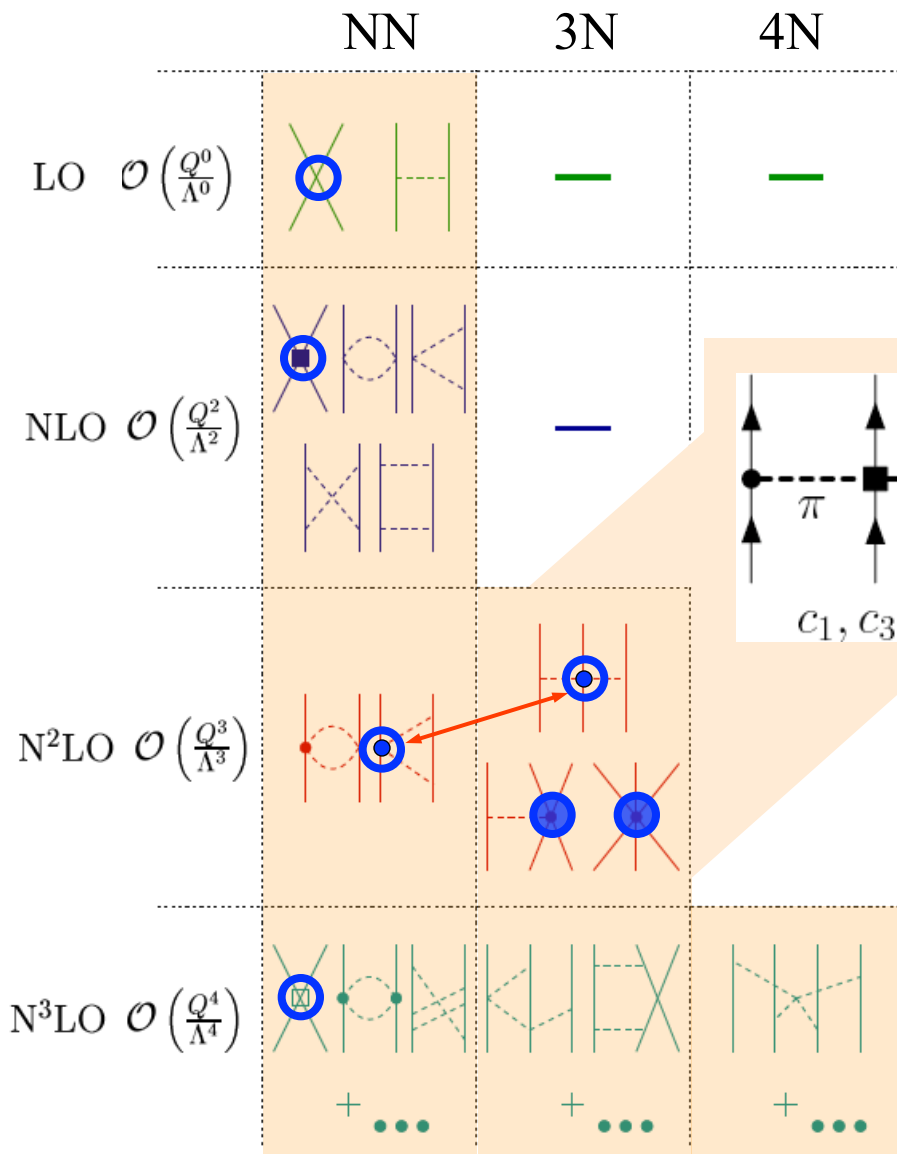


good agreement with
chiral EFT predictions

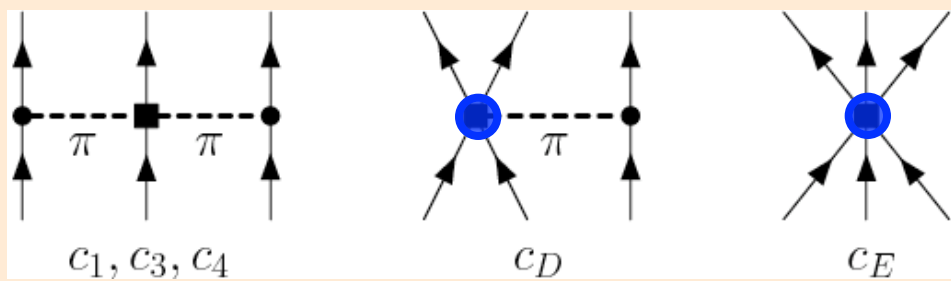
Miorelli, Bacca, Hagen et al.

Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV



c_D, c_E don't contribute for **neutrons** because of Pauli principle and pion coupling to spin, also for c_4
 Hebeler, AS (2010) for non/semi-local regulators

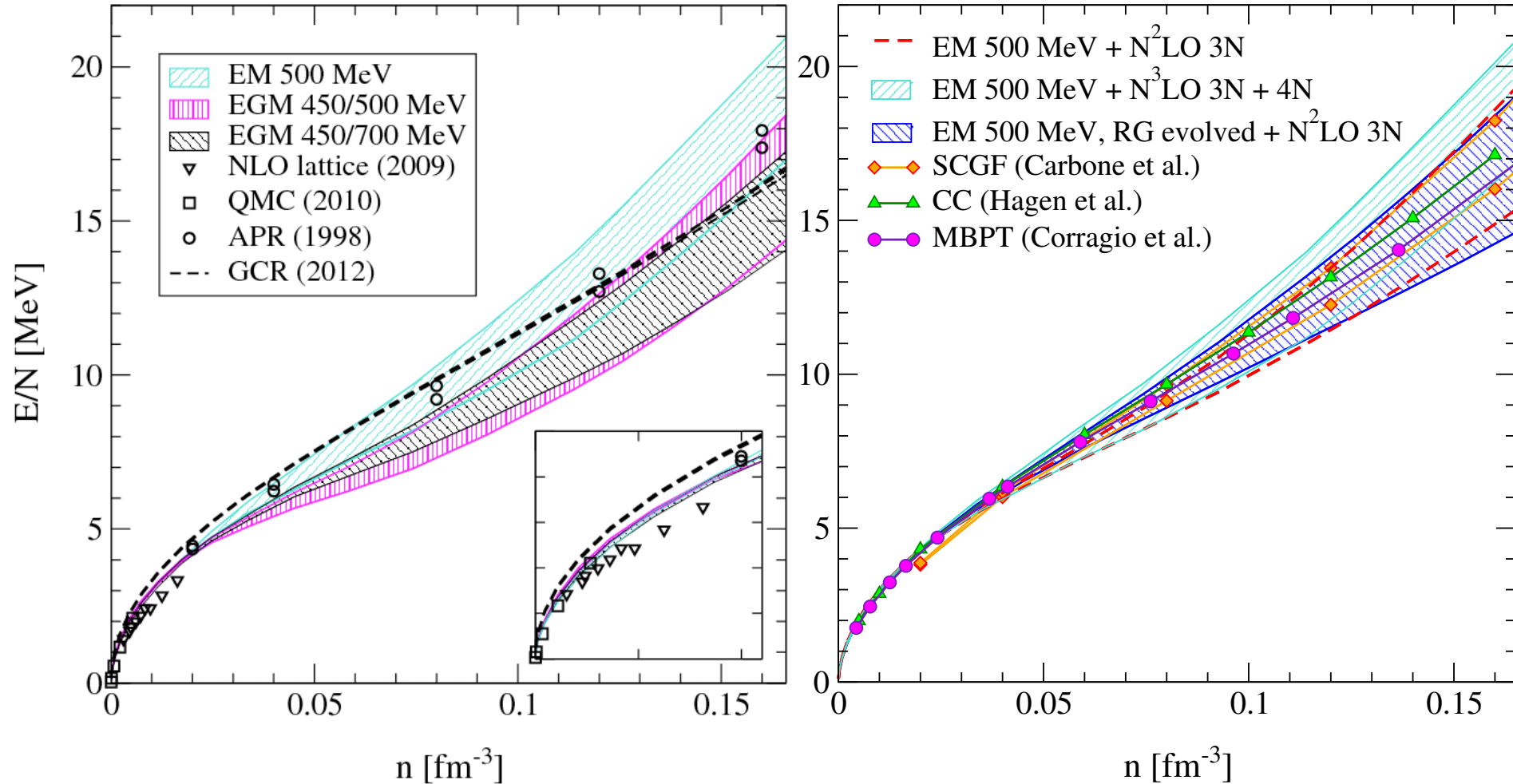


all 3- and 4-neutron forces are predicted to N³LO!

Complete N³LO calculation of neutron matter

first complete N³LO result [Tews, Krüger, Hebeler, AS, PRL \(2013\)](#)

includes uncertainties from NN, **3N (dominates)**, 4N

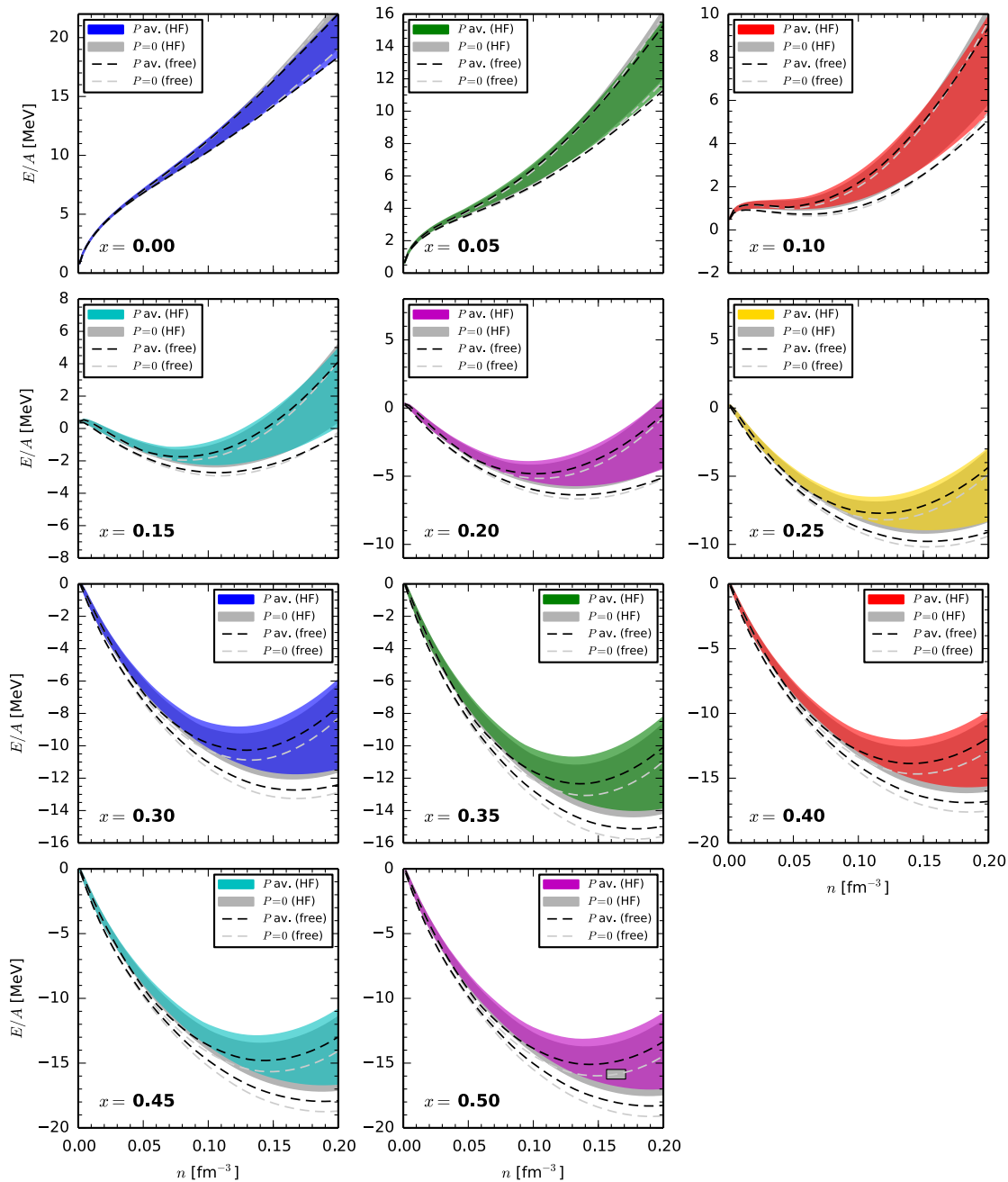
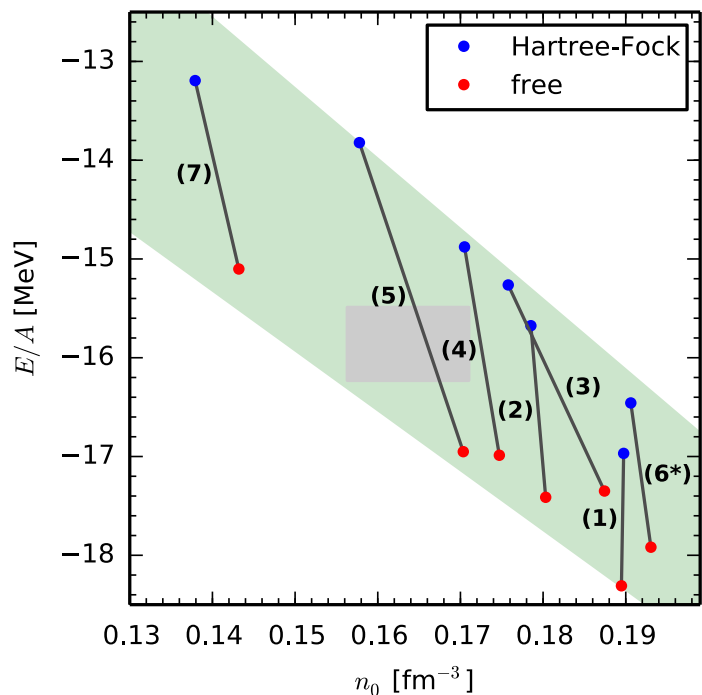


excellent agreement with other methods!

Nuclear forces and nuclear matter

asymmetric matter
with improved treatment
of 3N forces

Drischler, Hebeler, AS, PRC (2016)
see also Holt, Kaiser, Weise, Wellenhofer



Symmetry energy and pressure of neutron matter

neutron matter band predicts
symmetry energy S_v and
its density derivative L

comparison to experimental
and observational constraints

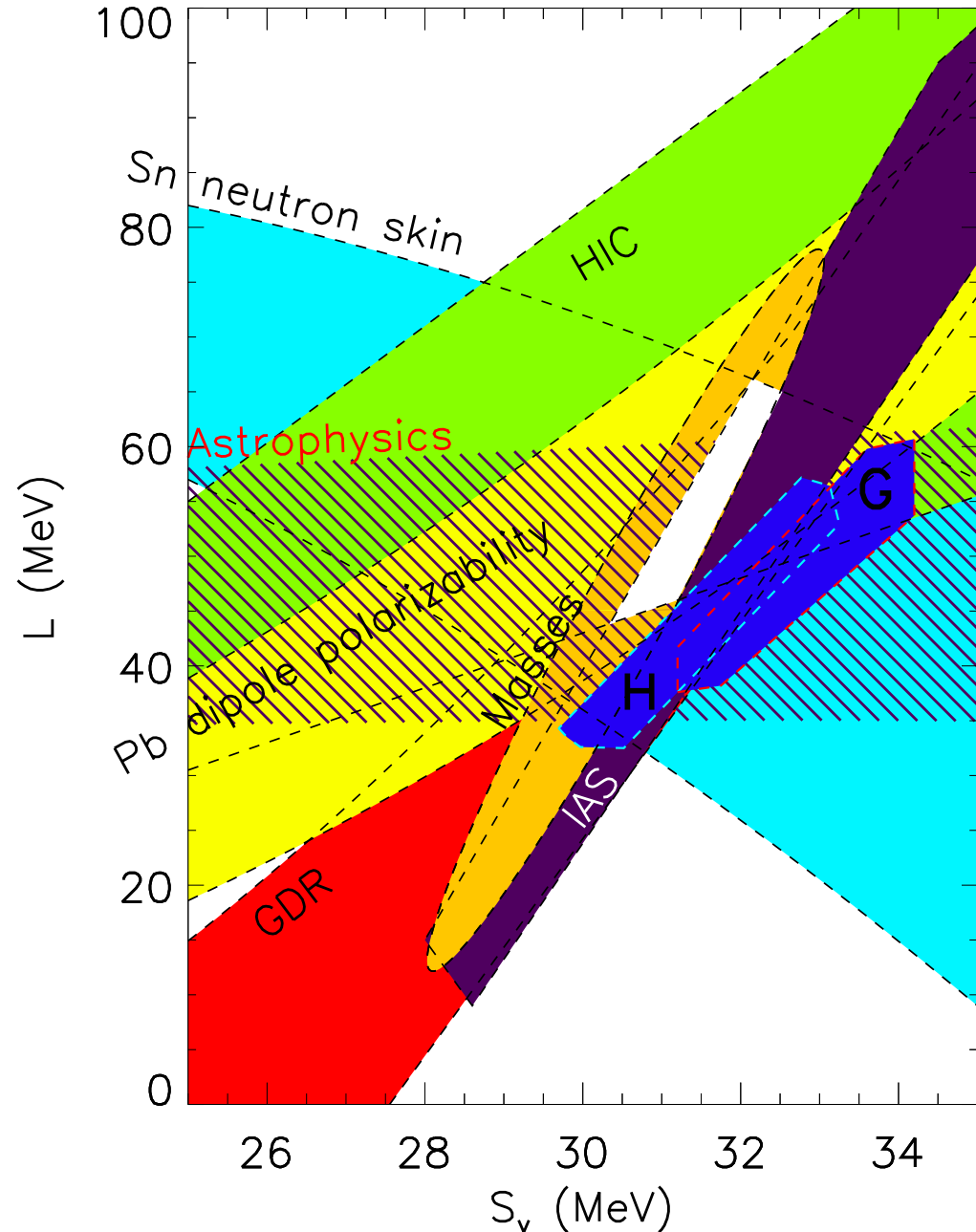
Lattimer, Lim, ApJ (2012), EPJA (2014)

neutron matter constraints

H: Hebeler et al. (2010)

G: Gandolfi et al. (2011)

provide tight constraints!



Symmetry energy and pressure of neutron matter

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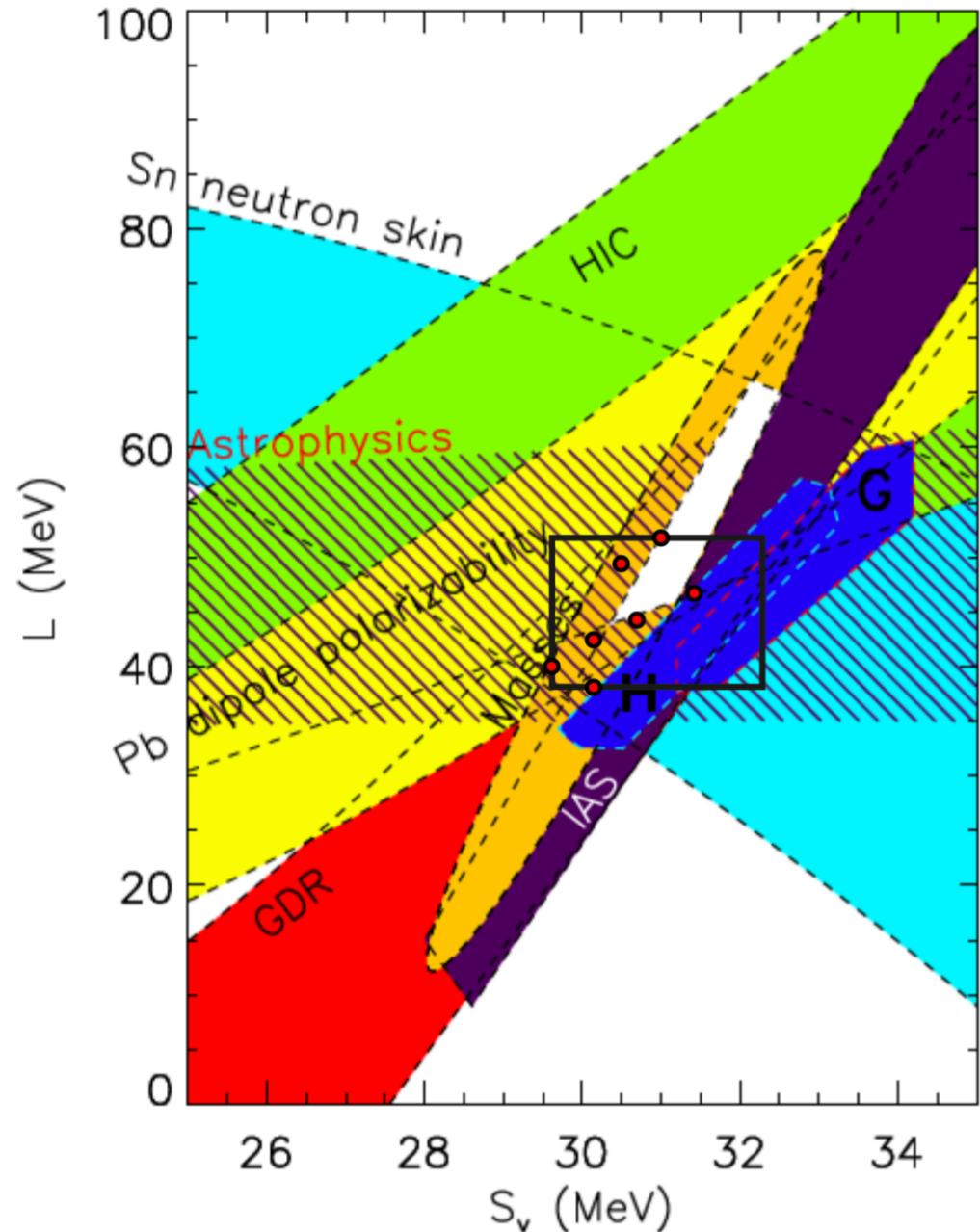
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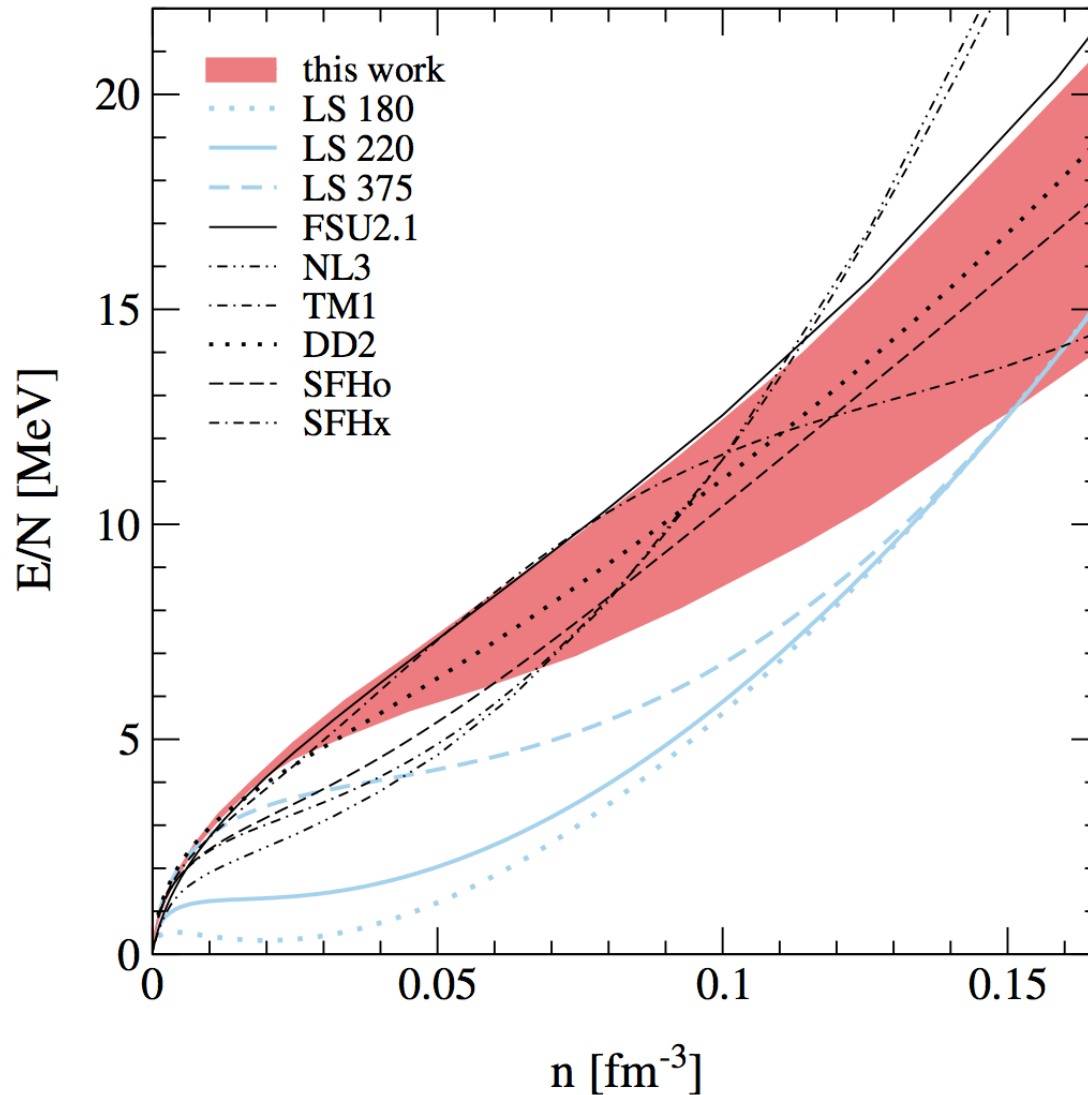
provide tight constraints!

from asymmetric matter
calculations Drischler



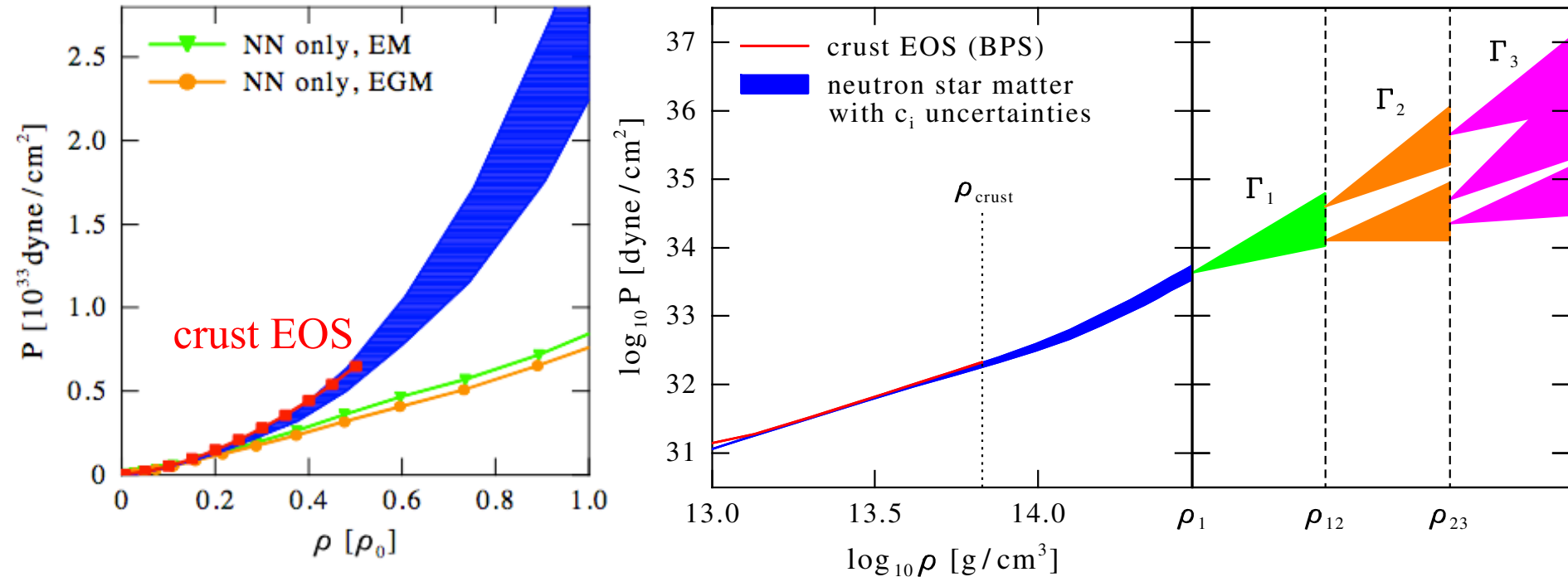
Comparisons to equations of state in astrophysics

many equations of state used in supernova simulations not consistent with neutron matter results



Impact on neutron stars Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

Equation of state/pressure for **neutron-star matter** (includes small $Y_{e,p}$)

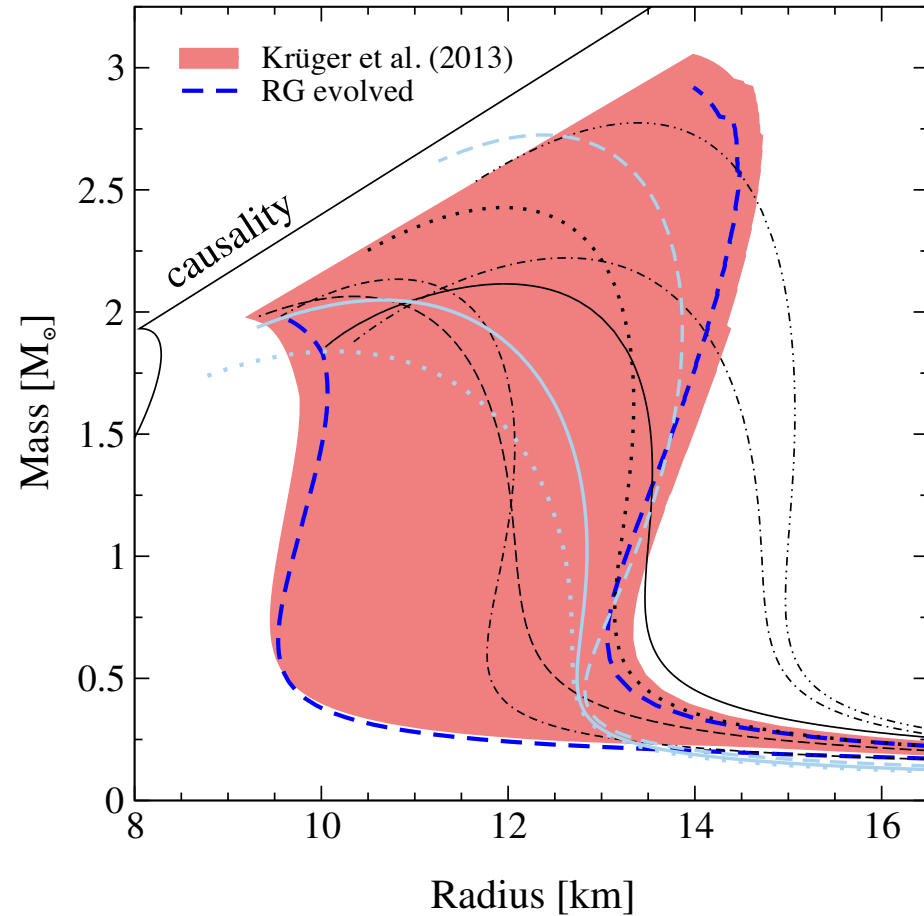
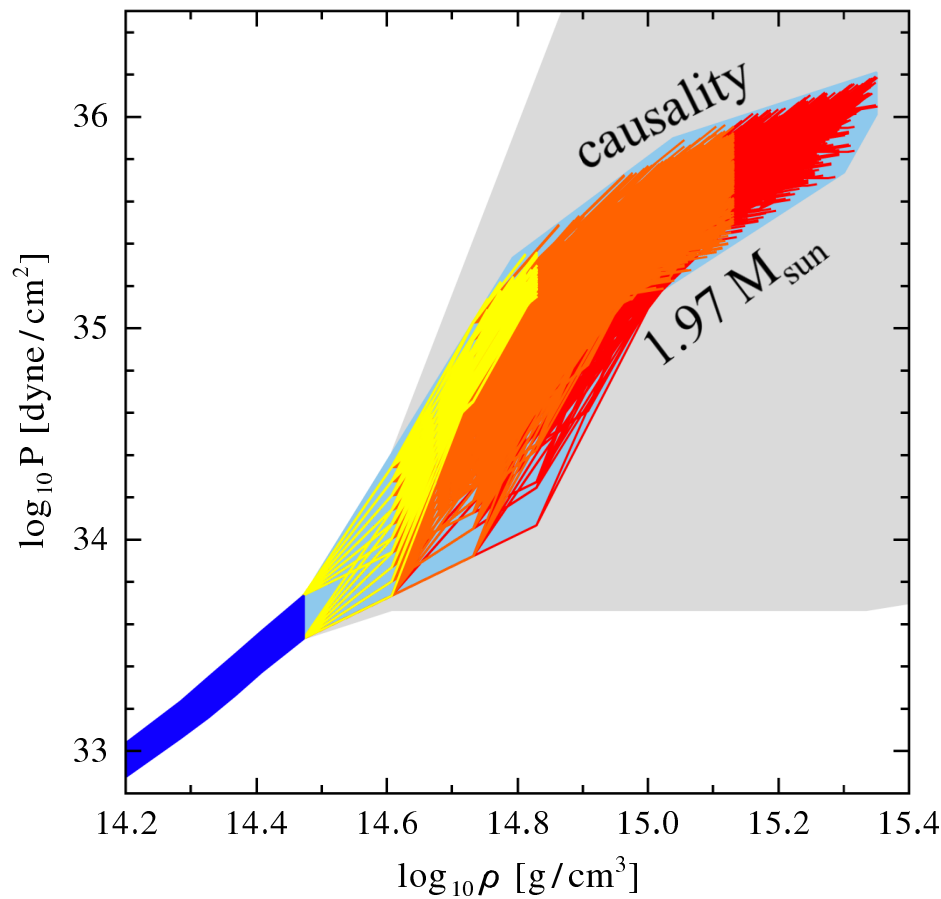


pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

extend uncertainty band to higher densities using piecewise polytropes
allow for soft regions

Impact on neutron stars Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

constrain high-density EOS by causality, require to support $2 M_{\text{sun}}$ star



low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

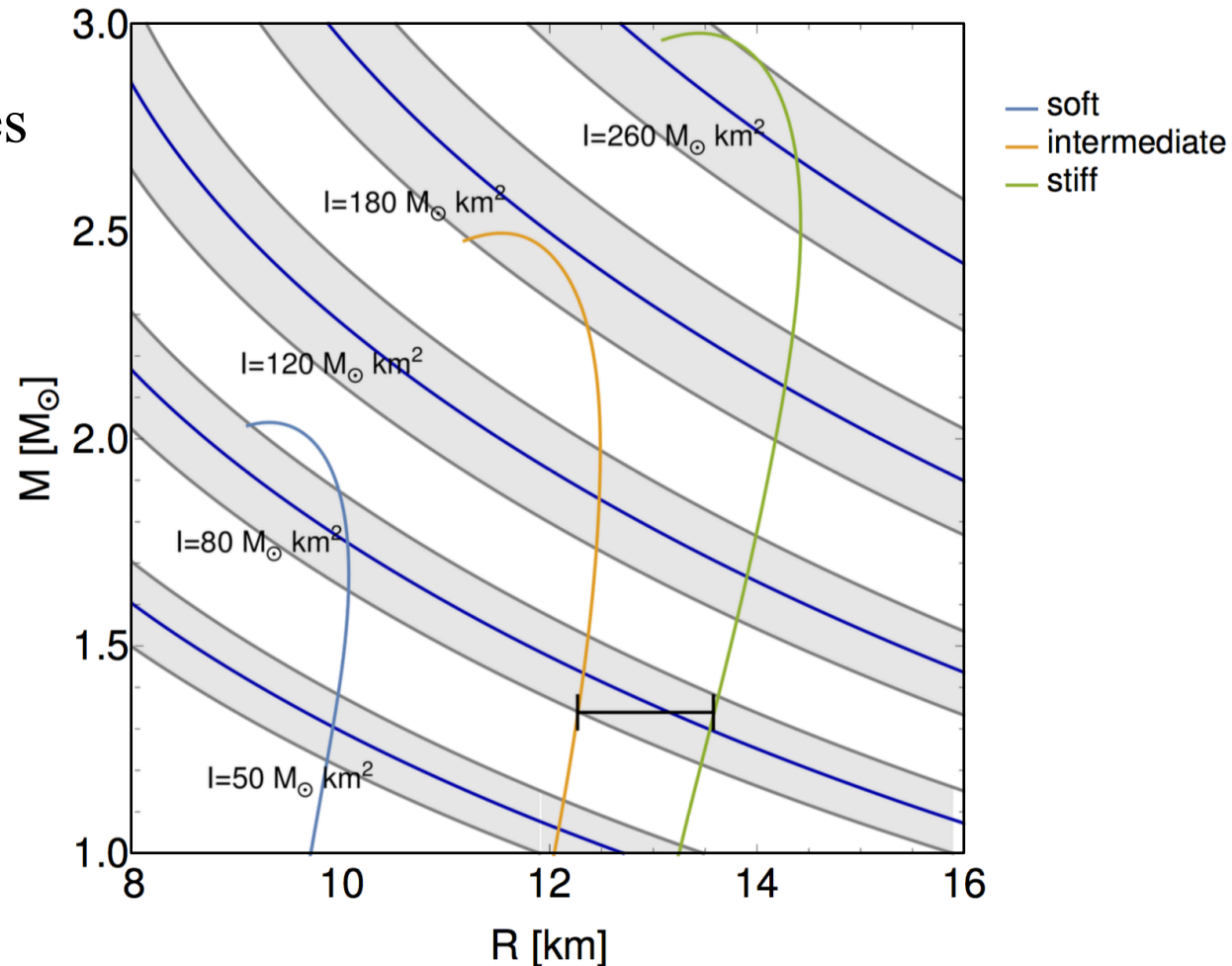
predicts neutron star radius: 9.7-13.9 km for $M=1.4 M_{\text{sun}}$ ($\pm 18\%$!)

Radius constraints from moment of inertia Svenja Greif et al., in prep.

candidate neutron star:

PSR J0737-3039 $M=1.35 M_{\text{sun}}$

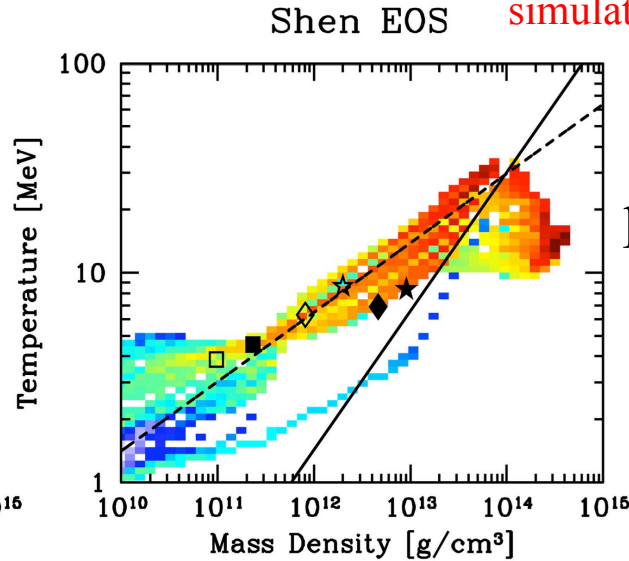
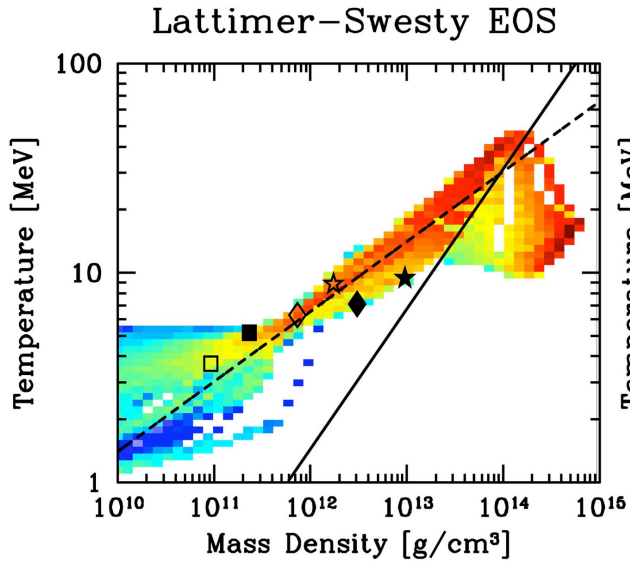
10% measurement of
moment of inertia reduces
radius range by 1/2



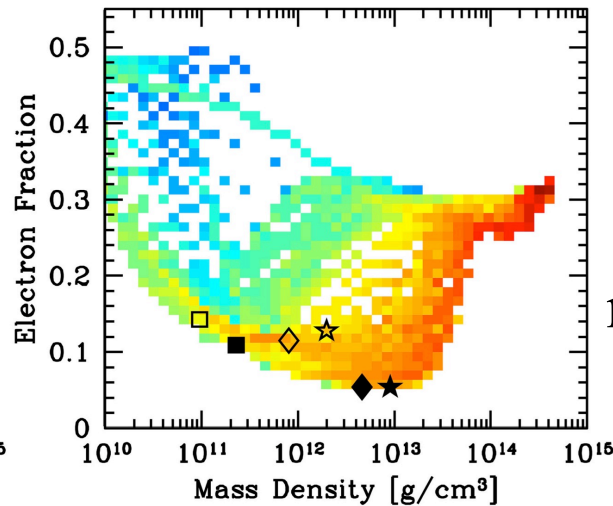
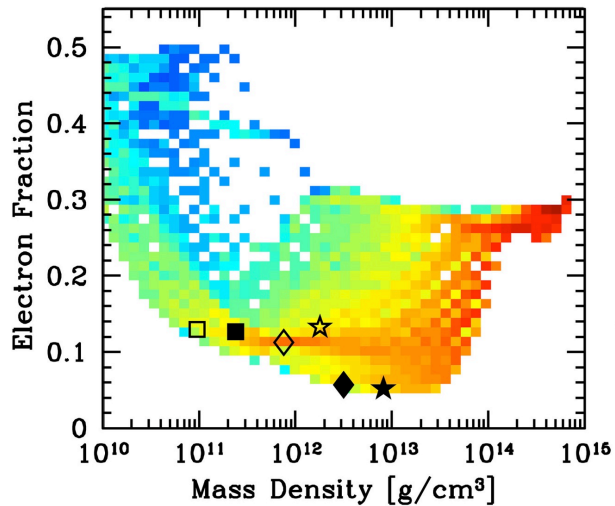
Relevant conditions in core-collapse supernovae

15 M_⊙ progenitor

S. Bacca et al., ApJ (2012)
simulations by M. Liebendörfer et al.



partially degenerate



neutron-rich

crucial densities below nuclear matter density $\sim 10^{13}$ - 10^{14} g/cm³
(high densities: neutrinos trap; low densities: few interactions)

Neutrino rates from chiral effective field theory

processes involving two nucleons play a special role [Friman,...](#) [Suzuki, Raffelt,...](#)

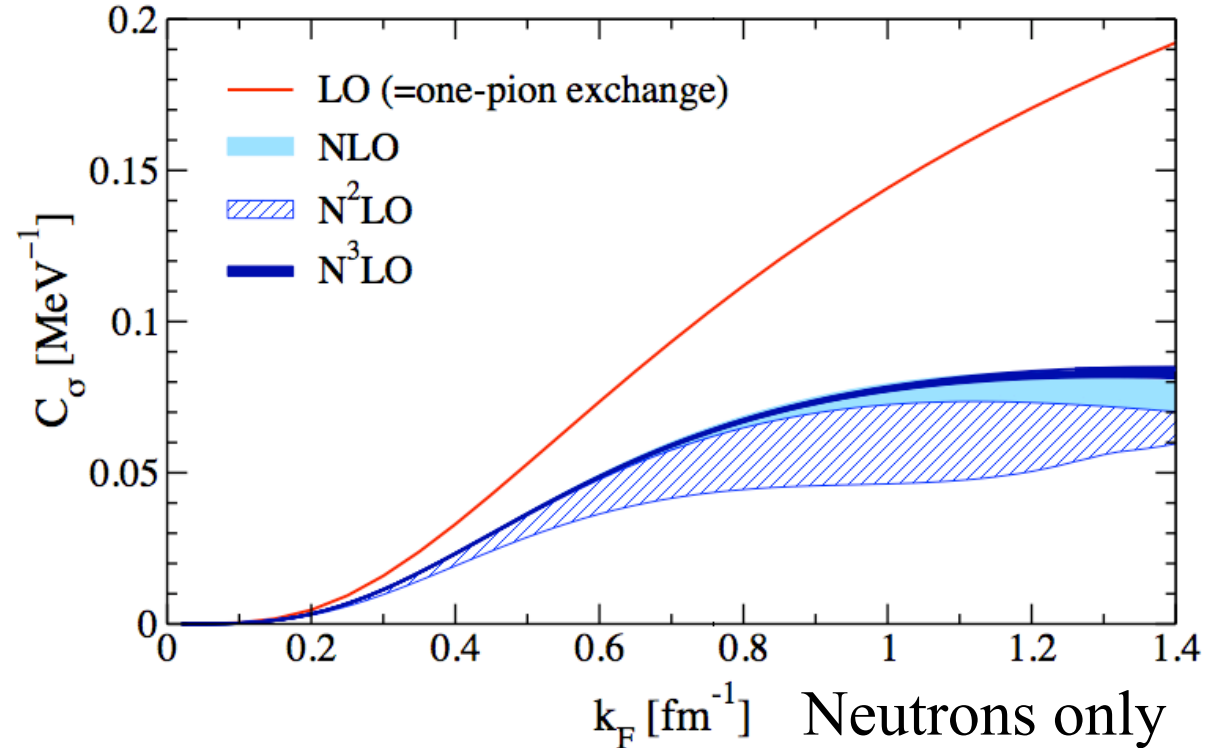
$NN \leftrightarrow NN\nu\bar{\nu}$ key for muon and tau neutrino production in supernovae
(and neutron stars crust and core cooling)

determined by spin relaxation time = rate of change of nucleon spin
through collisions

first neutrino rates
based on chiral EFT,
degenerate conditions

[Bacca et al. \(2009\)](#)

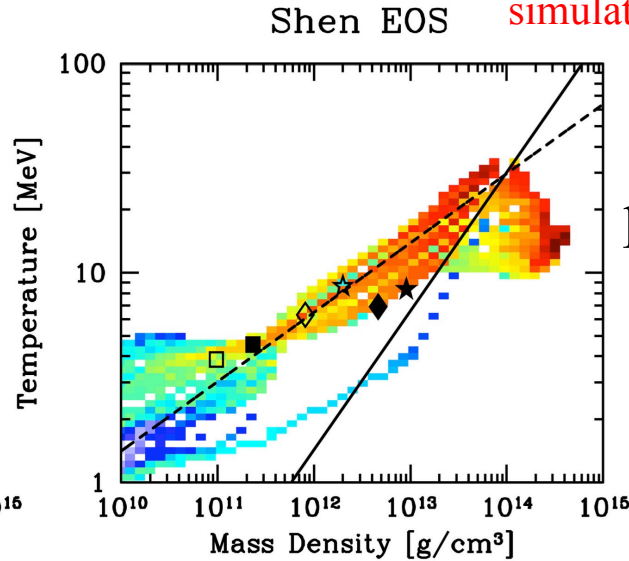
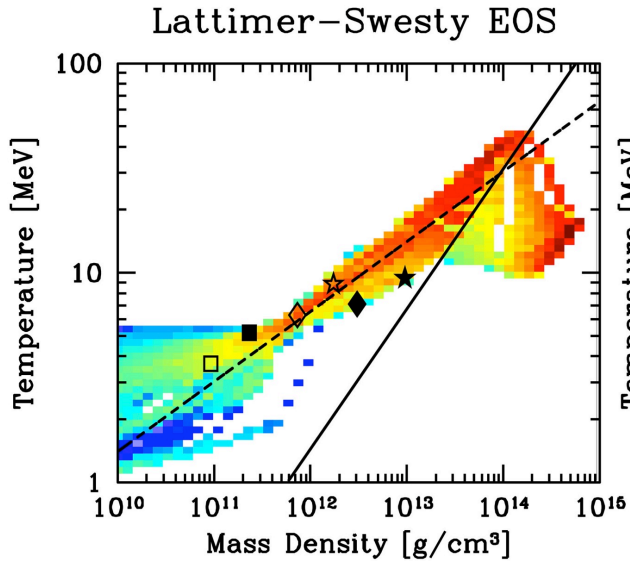
shorter-range interactions
reduce rates for neutrons



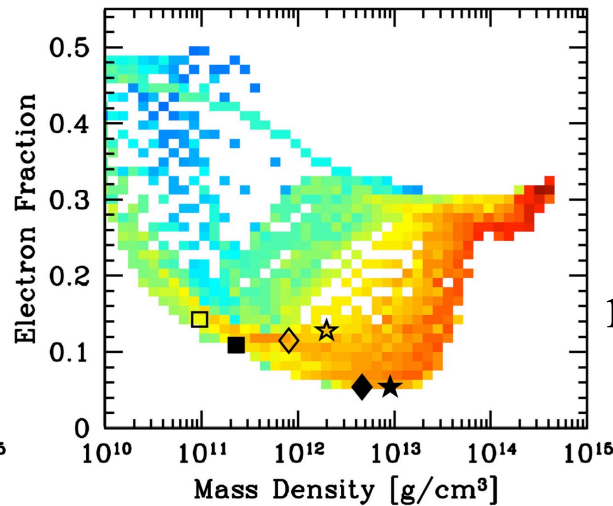
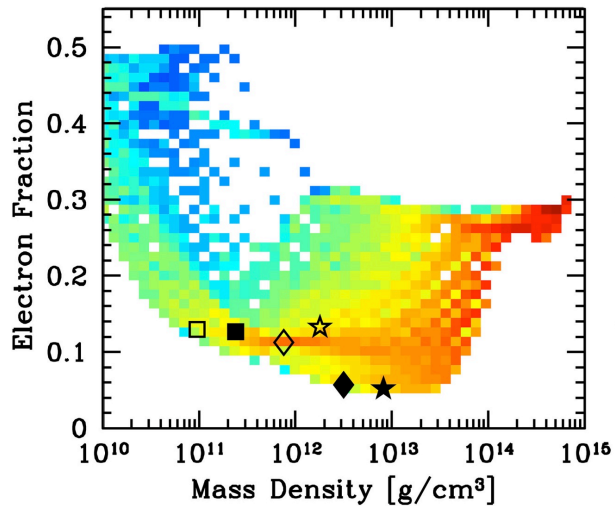
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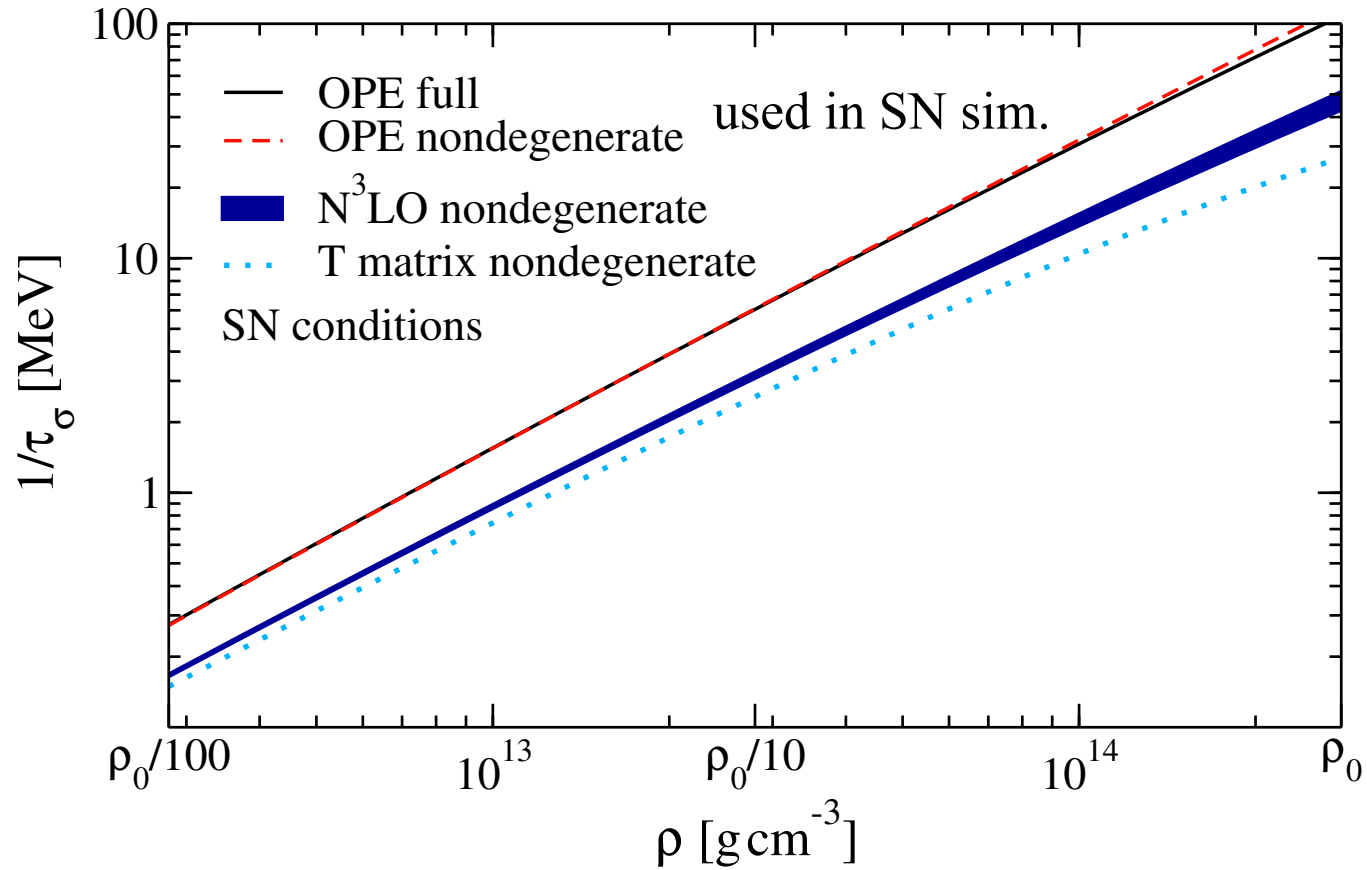


neutron-rich

crucial densities below nuclear matter density $\sim 10^{13}$ - 10^{14} g/cm^3
(high densities: neutrinos trap; low densities: few interactions)

Neutrino rates from chiral EFT S. Bacca et al., ApJ (2012)

neutrons only, arbitrary degeneracy



similar reduction along SN conditions

Energy transfer in neutrino scattering from nucleons Bartl et al., in prep.

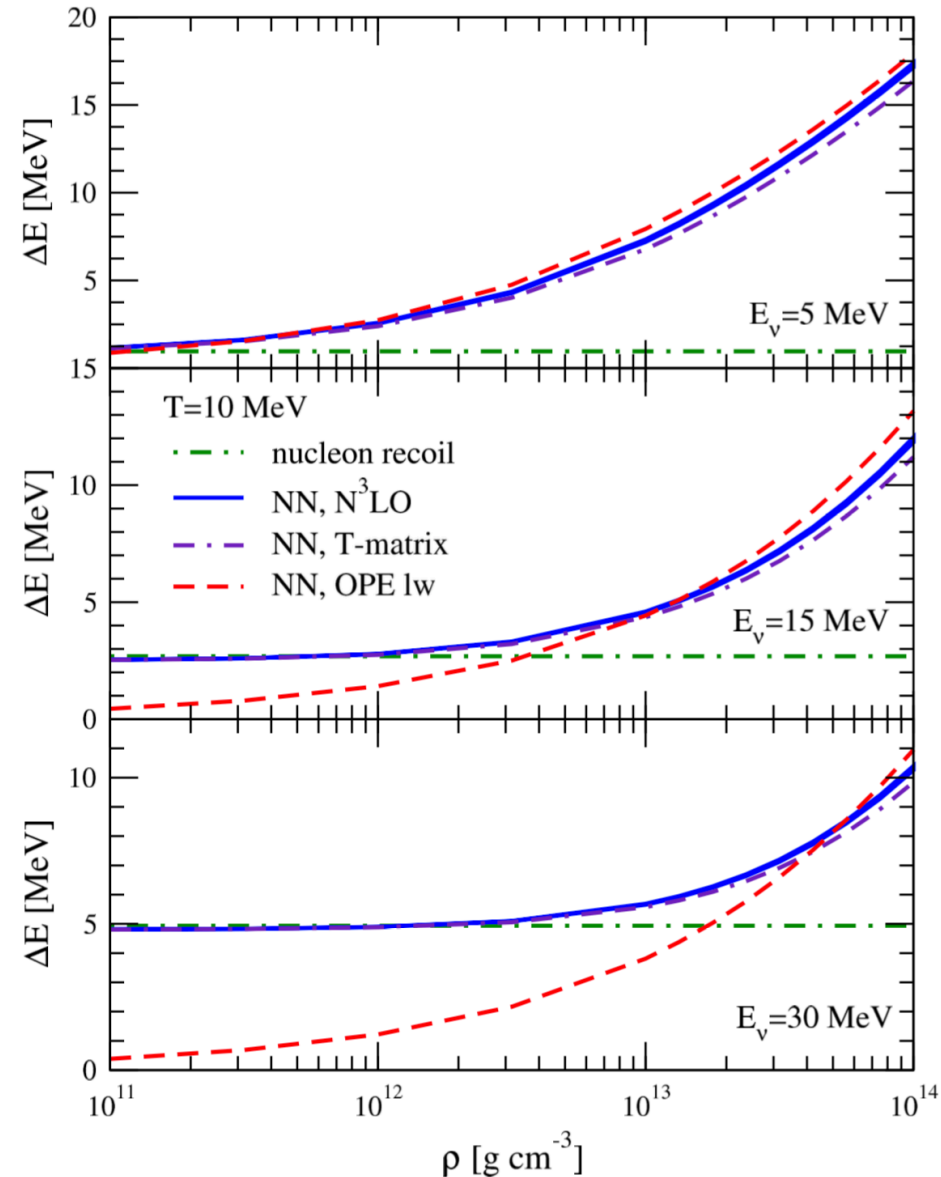
mean-square neutrino energy transfer in $\nu nn \leftrightarrow \nu nn$

$$(\Delta E)^2 = \frac{\int d\mathbf{p}'_\nu (E_\nu - E'_\nu)^2 \Gamma(E_\nu - E'_\nu, p_\nu - p'_\nu)}{\int d\mathbf{p}'_\nu \Gamma(E_\nu - E'_\nu, p_\nu - p'_\nu)}$$

leads to heating,
NN analogue of inelastic
excitations of nuclei
(but post-collapse)

energy transfer significant,
can dominate over recoil

not included in simulations

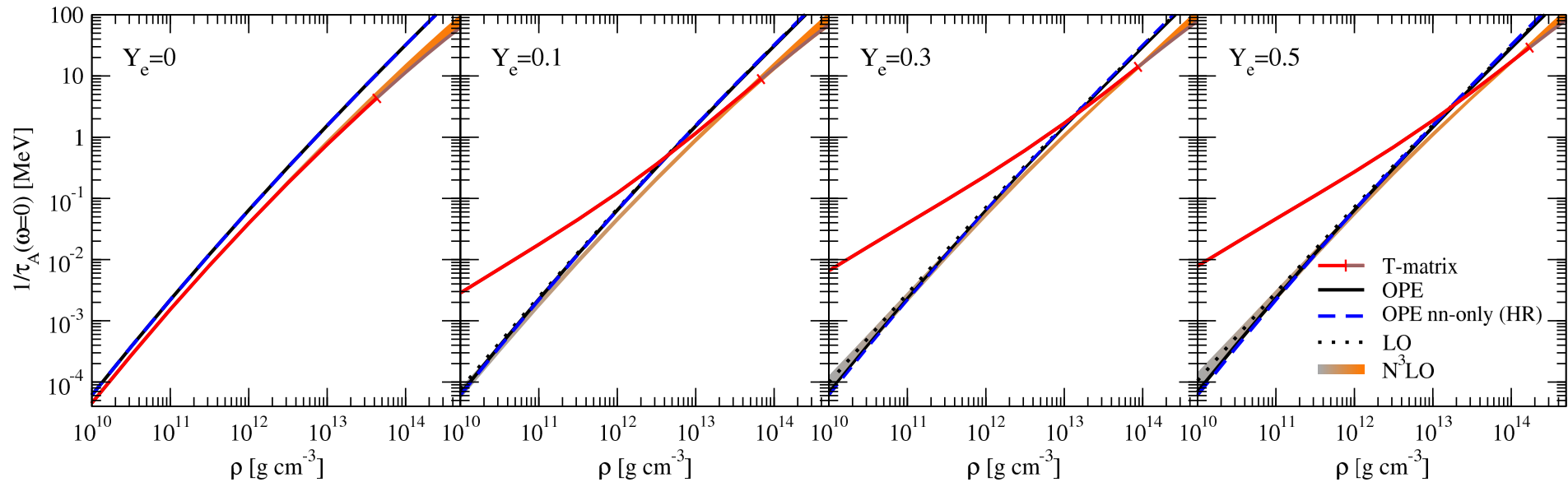


Neutrino bremsstrahlung in mixtures of neutron and protons

in mixtures also S-wave interactions enter: large scattering lengths!

lead to enhancement of bremsstrahlung at low densities for nonzero Y_e

Bartl, Pethick, AS, PRL (2015)

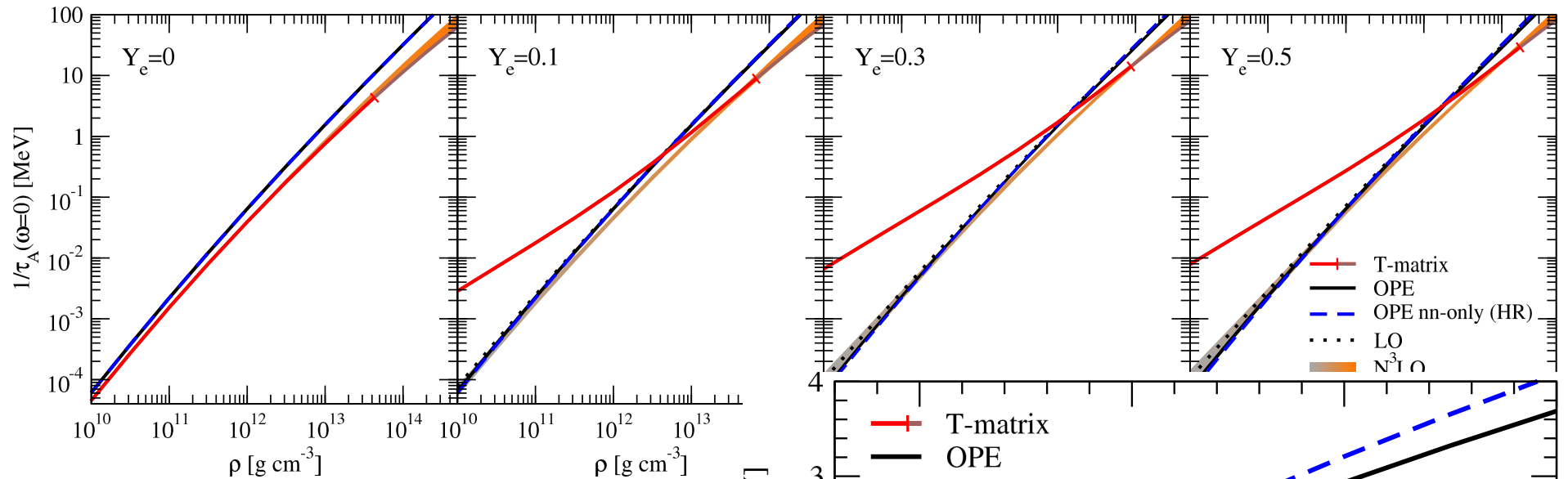


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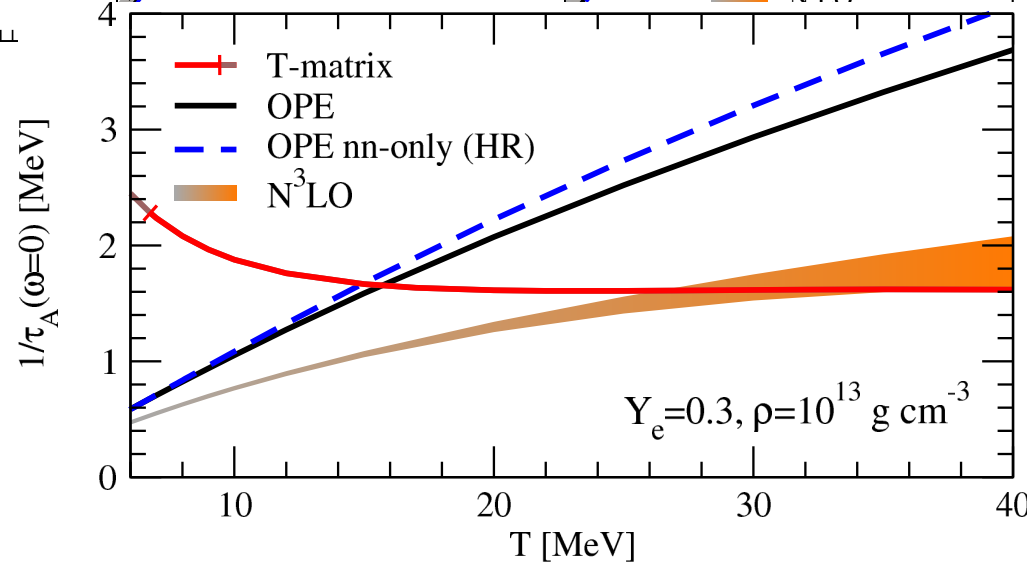
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same enhancement at low T

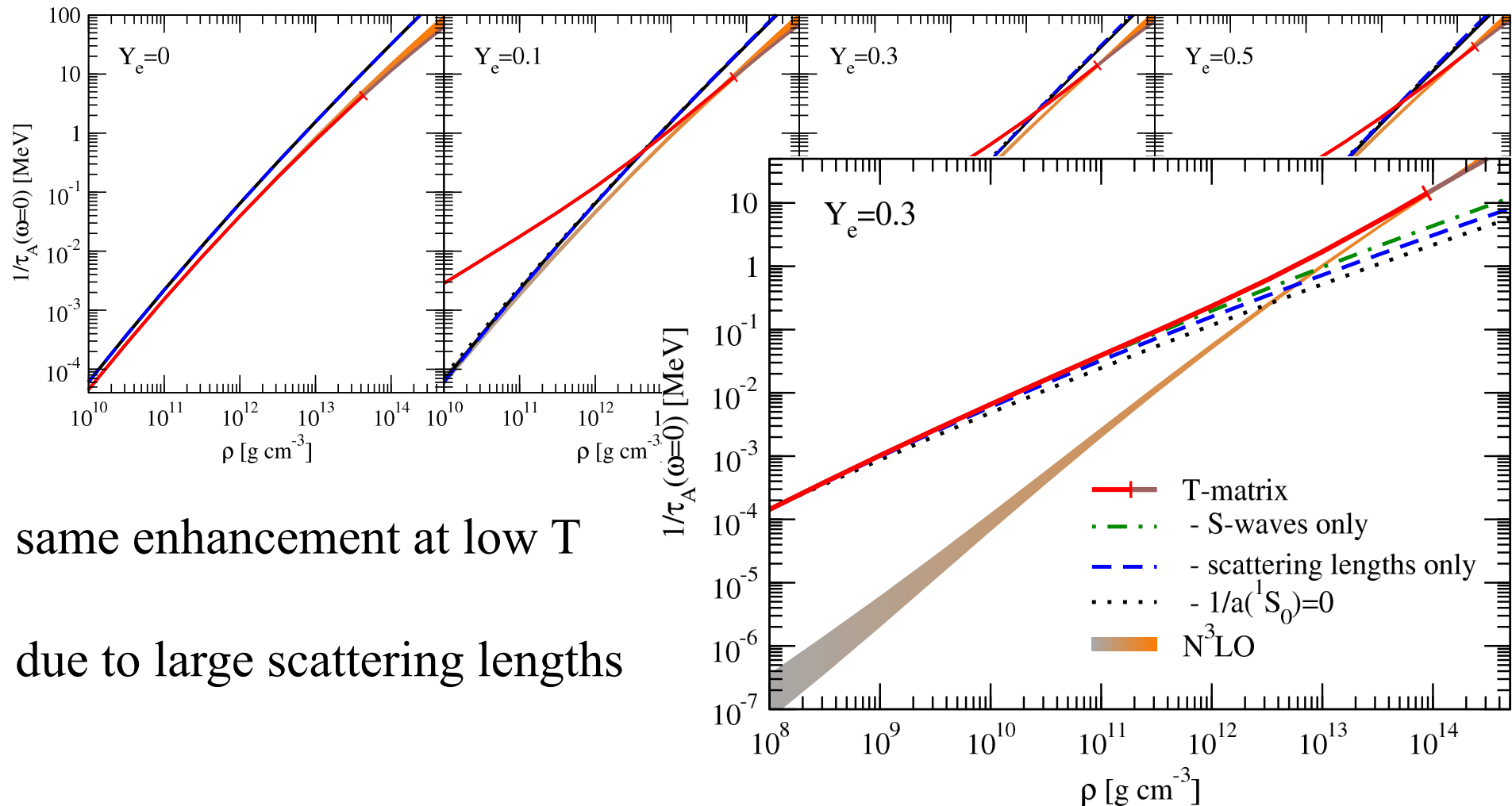


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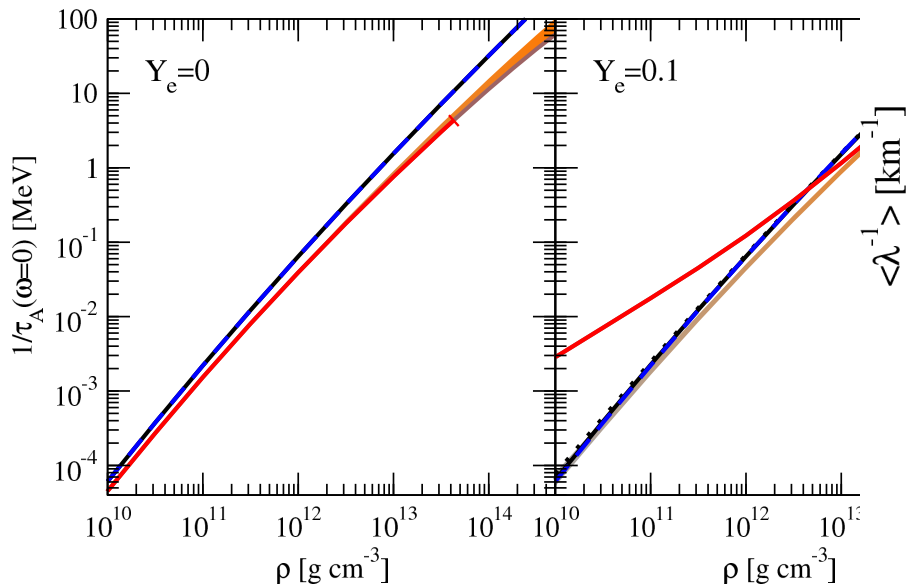
due to large scattering lengths

Neutrino bremsstrahlung in mixtures of neutron and protons

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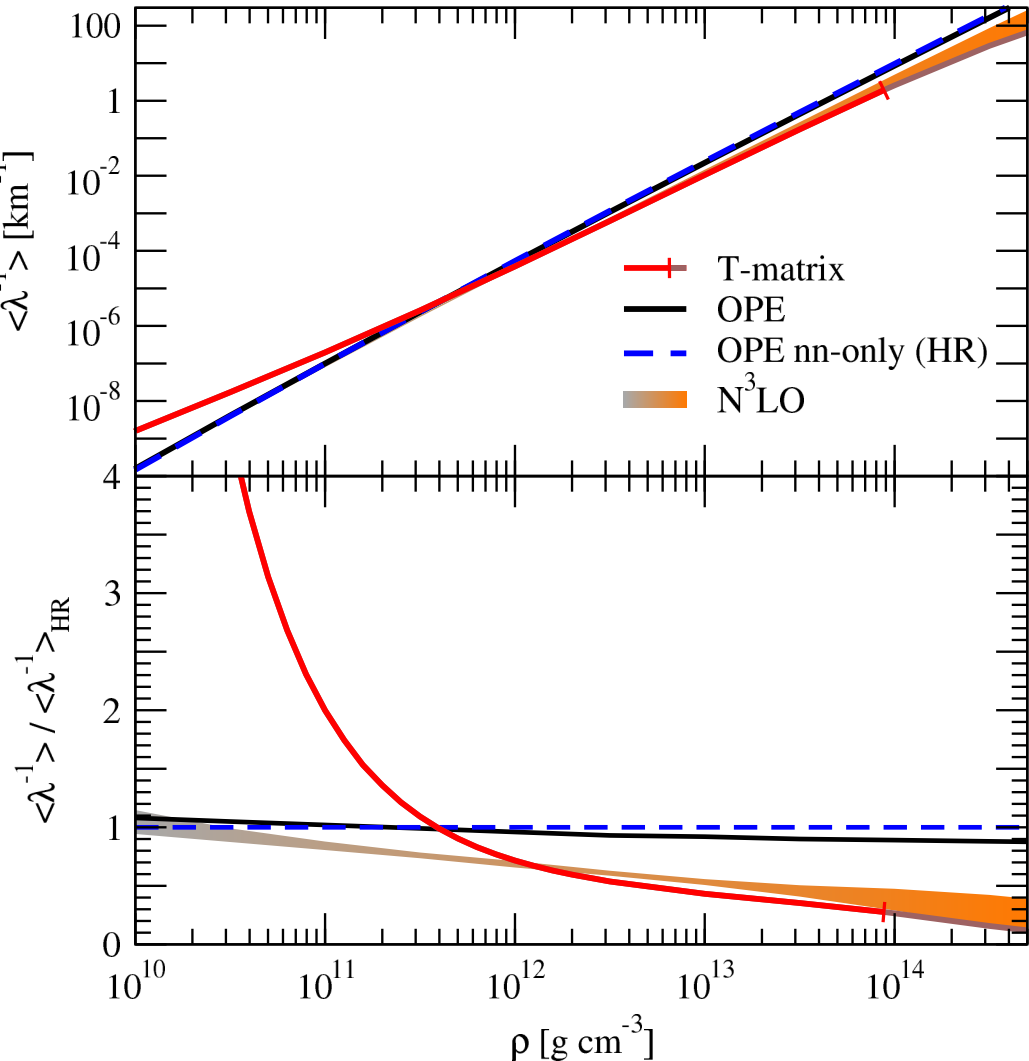
lead to enhancement of bremsstrahlung at low densities for nonzero Y_e

Bartl, Pethick, AS, PRL (2015)



same enhancement at low T

smaller enhancement of
inverse mf paths



Main points

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Neutron-rich conditions and nondegenerate conditions

General EOS band based on nuclear physics and observations
neutron star radius 9.7-13.9 km for $M=1.4 M_{\text{sun}}$ ($\pm 18\%$)

Chiral EFT important for consistent neutrino-matter interactions

Enhancement of neutrino bremsstrahlung at low densities

see talk by **Robert Bollig** on impact in simulations

important to explore inelastic scattering

Main results thanks to: **A. Bartl, C. Drischler, S. Greif, K. Hebeler, T. Krüger, J. Lattimer, C. Pethick, I. Tews**