

Dense matter from nuclear forces

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DARMSTADT



INT Program “The Phases of Dense Matter”

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DFG



Bundesministerium
für Bildung
und Forschung



Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV



	NN	3N	4N
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N ² LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N ³ LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

include long-range pion physics

short-range couplings, fit to experiment once

systematic: can work to desired accuracy and obtain **error estimates**

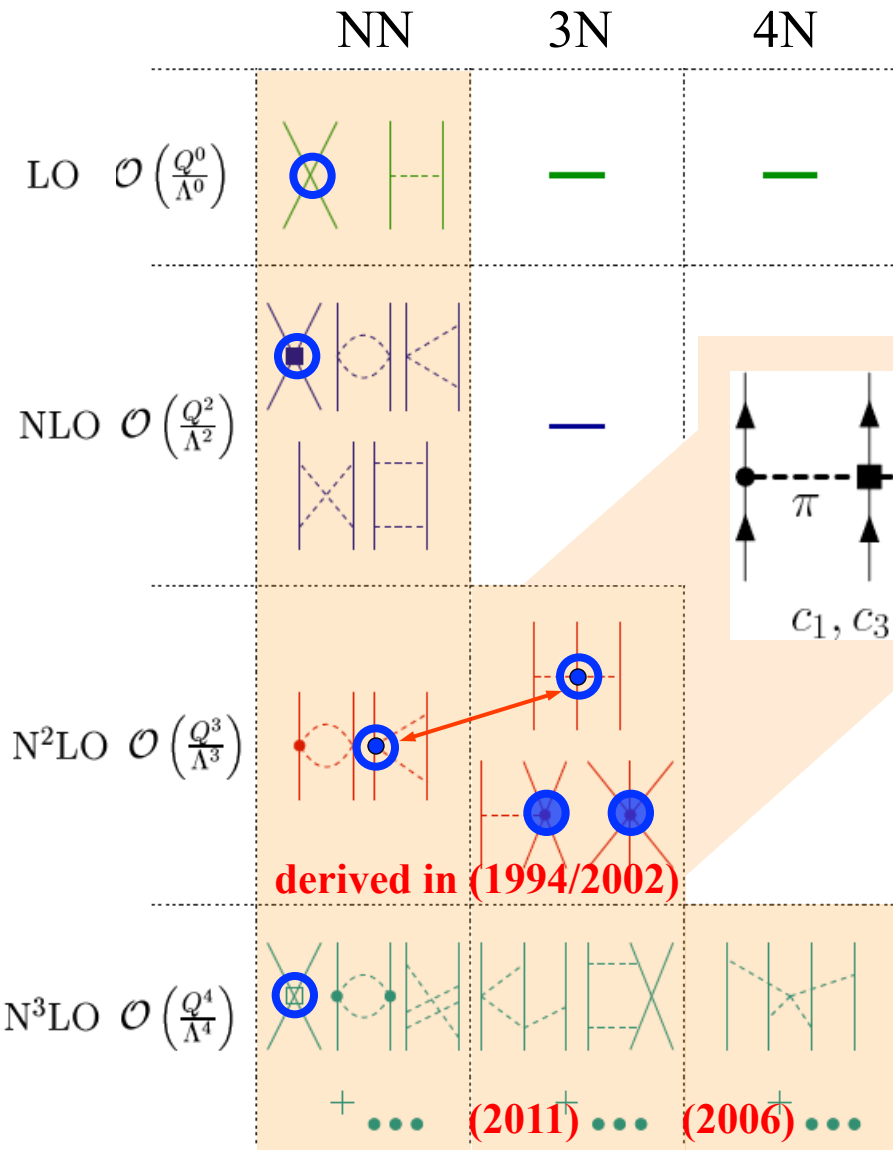
consistent **electroweak interactions** and **matching to lattice QCD**

new developments in power counting, uncertainty quantification, **optimization** Ektröm, Forssen, Furnstahl,...

Weinberg, van Kolck, Kaplan, Savage, Wise, Bernard, Epelbaum, Kaiser, Machleidt, Meissner,...

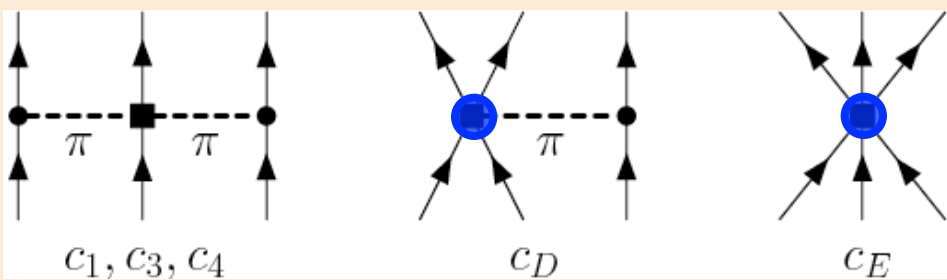
Chiral effective field theory and many-body forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV



consistent NN-3N-4N interactions

3N,4N: **2 new couplings to N³LO**
+ no new couplings for neutrons



c_i from π N and NN Meissner, LAT 2005

$$c_1 = -0.9_{-0.5}^{+0.2}, \quad c_3 = -4.7_{-1.0}^{+1.2}, \quad c_4 = 3.5_{-0.2}^{+0.5}$$

c_D, c_E fit to light nuclei only

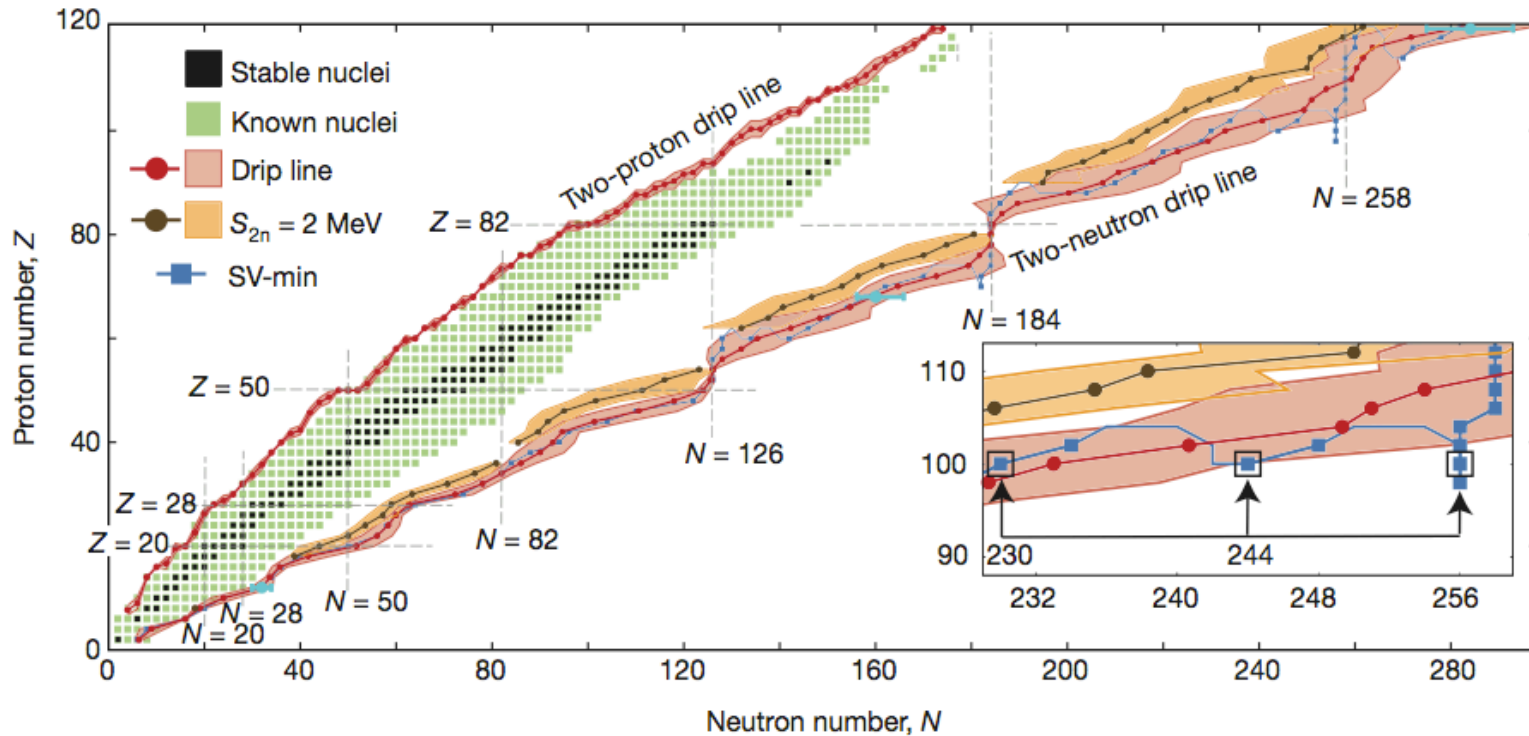
N²LOsat fit to nuclei up to $A=24$

Nuclei bound by strong interactions

doi:10.1038/nature11188

The limits of the nuclear landscape

Jochen Erler^{1,2}, Noah Birge¹, Markus Kortelainen^{1,2,3}, Witold Nazarewicz^{1,2,4}, Erik Olsen^{1,2}, Alexander M. Perhac¹ & Mario Stoitsov^{1,2†}



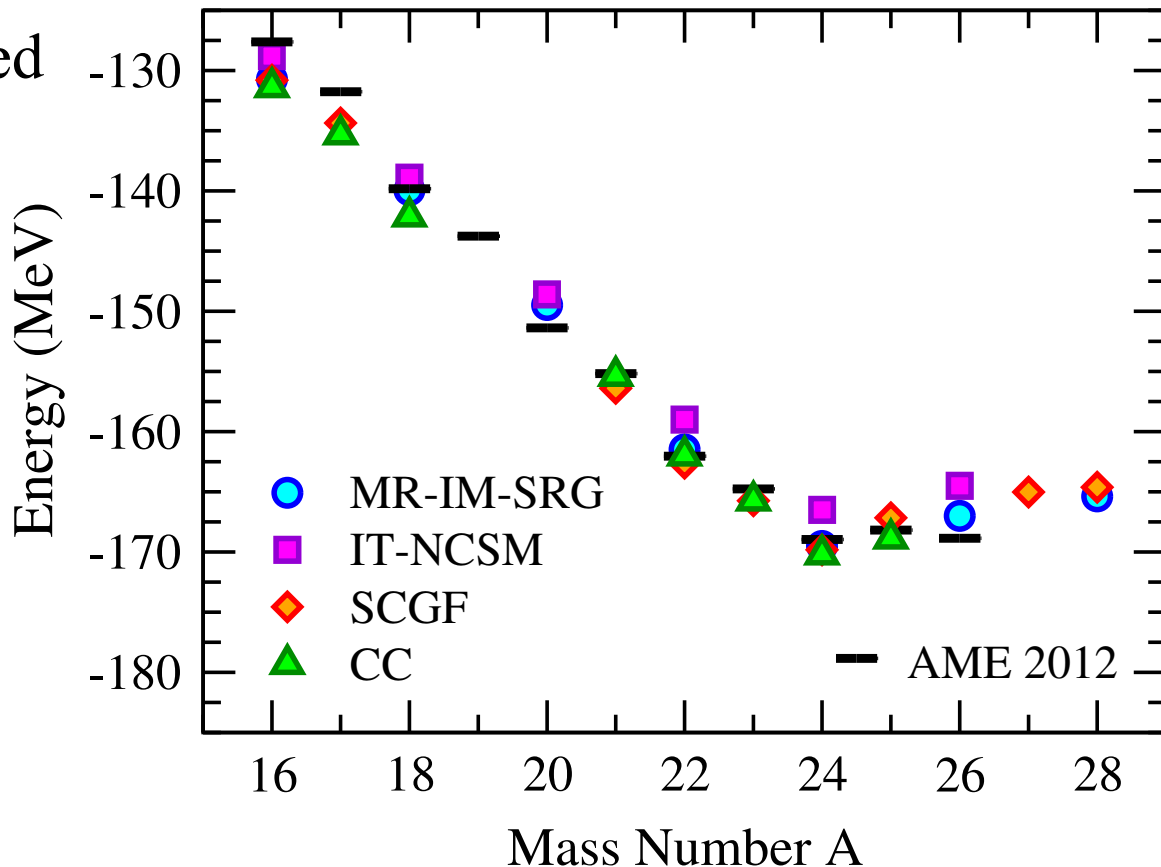
How does the nuclear chart emerge from chiral EFT?

Future: Connect chiral EFT to Lattice QCD

Ab initio calculations of neutron-rich oxygen isotopes

impact of **3N forces key for neutron dripline** Otsuka et al., PRL (2010)

based on **same** SRG-evolved
NN+3N interactions



using different many-body methods:

Coupled Cluster theory/CCEI Hagen et al., PRL (2012), Jansen et al., PRL (2014)

Multi-Reference In-Medium SRG and IT-NCSM Hergert et al., PRL (2013)

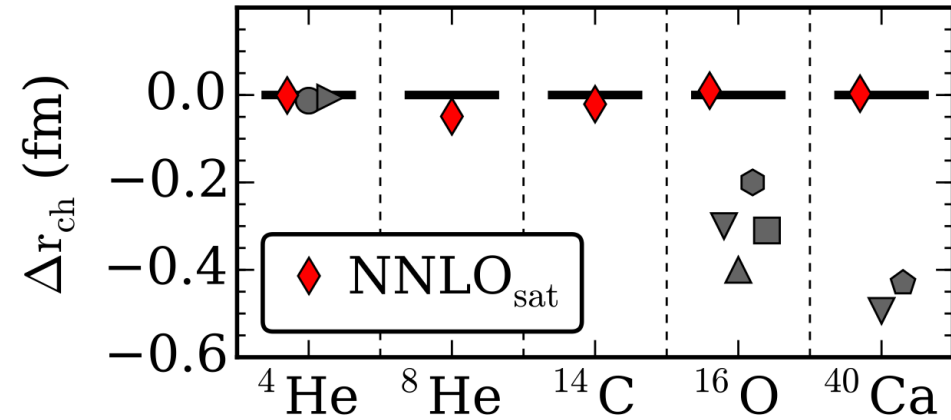
Self-Consistent Green's Function methods Cipollone et al., PRL (2013)

Resolution of radius problems

good saturation properties essential for radii

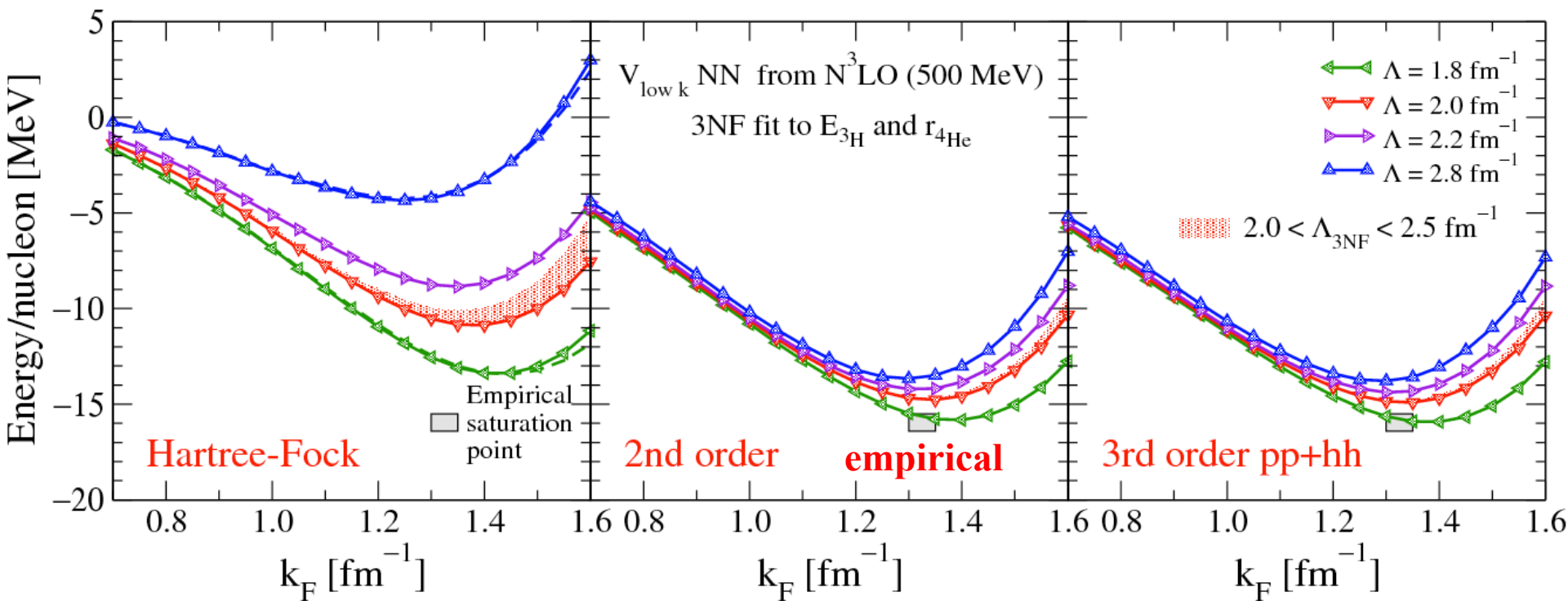
N^2LO_{sat} potential fit to nuclei up to $A=24$

Ekström et al., PRC (2015)



Nuclear forces and nuclear matter

chiral 3N forces fit to light nuclei predict nuclear matter saturation with theoretical uncertainties Hebel et al., PRC (2011), Bogner et al., NPA (2005)



Resolution of radius problems

good saturation properties essential for radii

N^2 LOsat potential fit to nuclei up to $A=24$

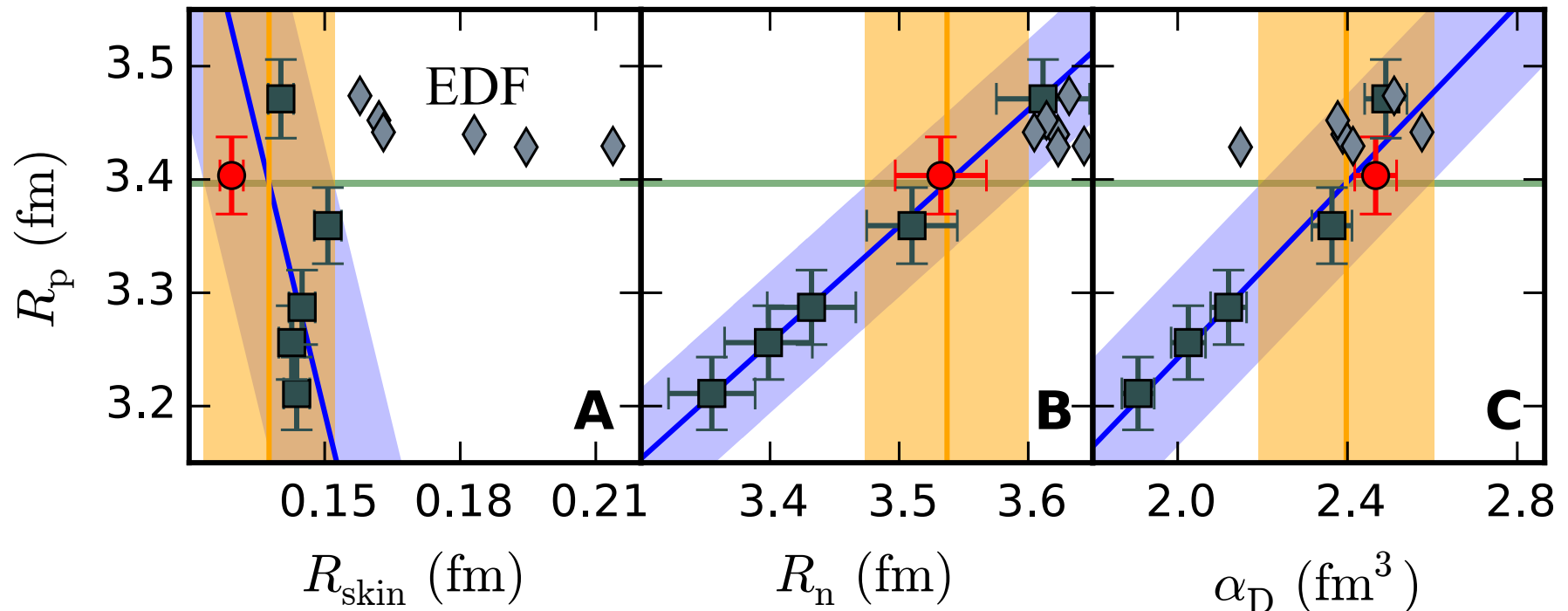
Ekström et al., PRC (2015)

NN+3N interactions that predict nuclear matter saturation

Hebeler et al., PRC (2011) only fit to light nuclei, but nonlocal 3N regulators

lead to radii consistent with experiment for ^{48}Ca Hagen et al., Nature Phys. (2015)

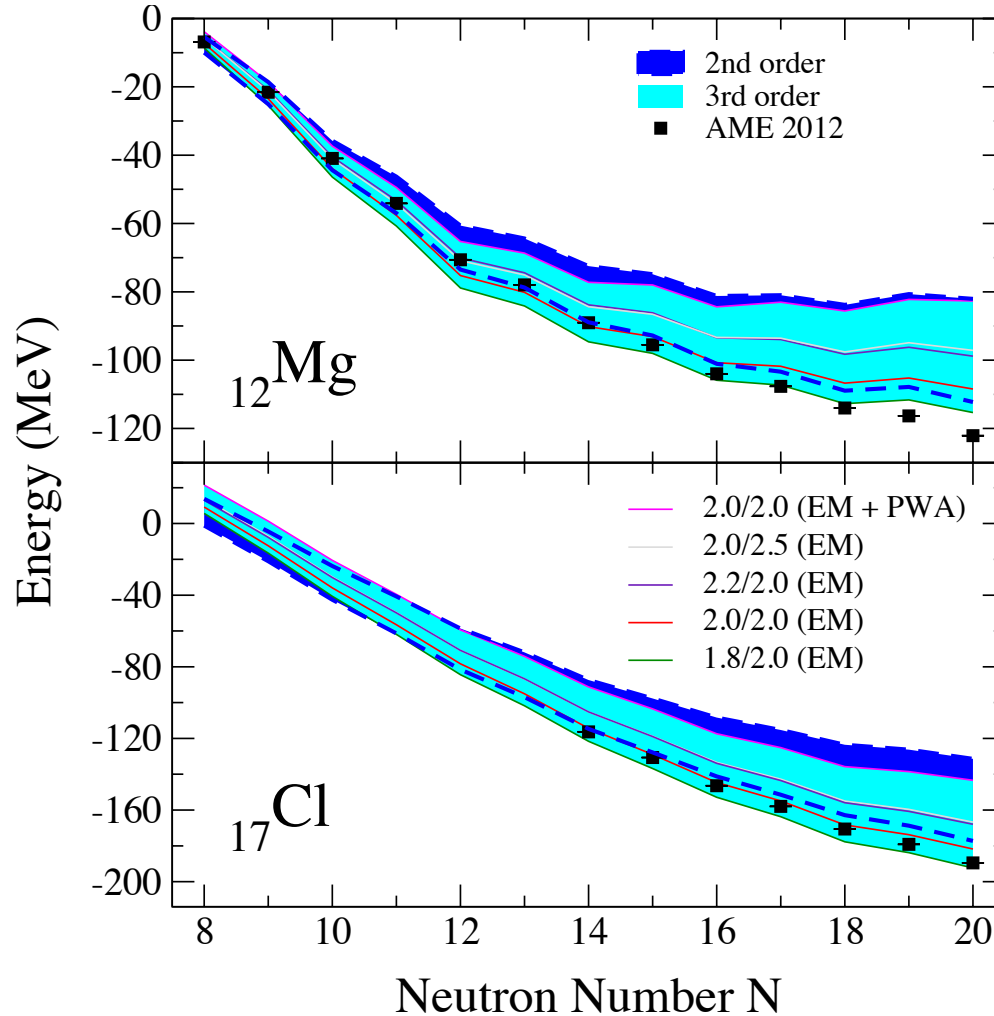
predict small neutron skin, dipole polarizability, and weak formfactor



Towards theoretical uncertainties Simonis et al., PRC (2016)

based on NN+3N interactions (sd shell)

that predict nuclear matter saturation within uncertainties

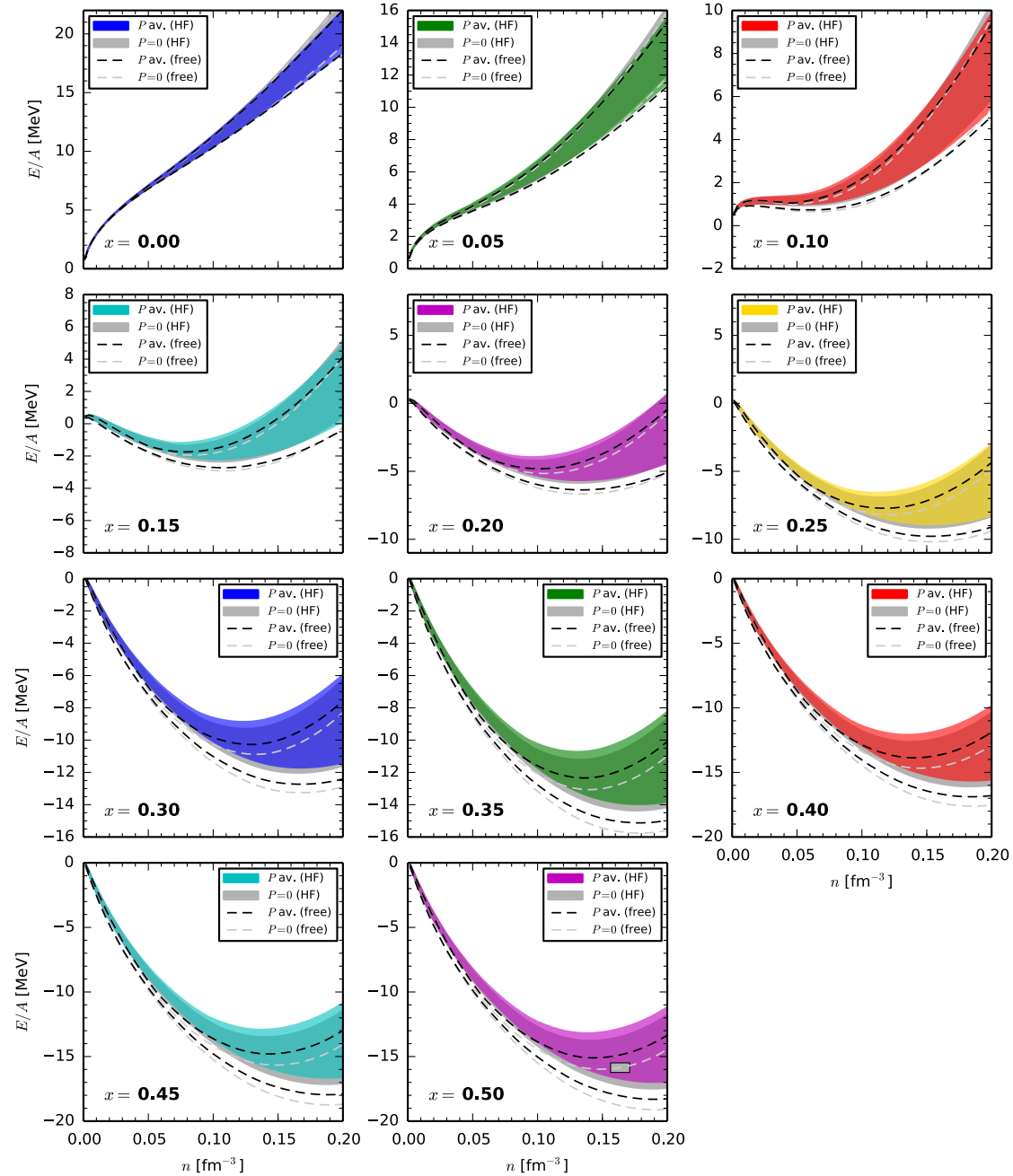
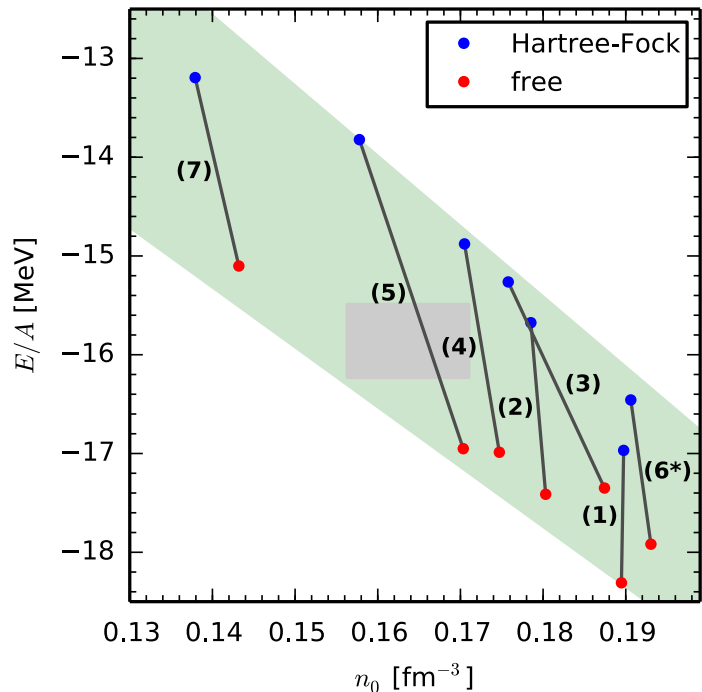


Theoretical uncertainties dominated by uncertainties in nuclear forces!

Nuclear forces and nuclear matter

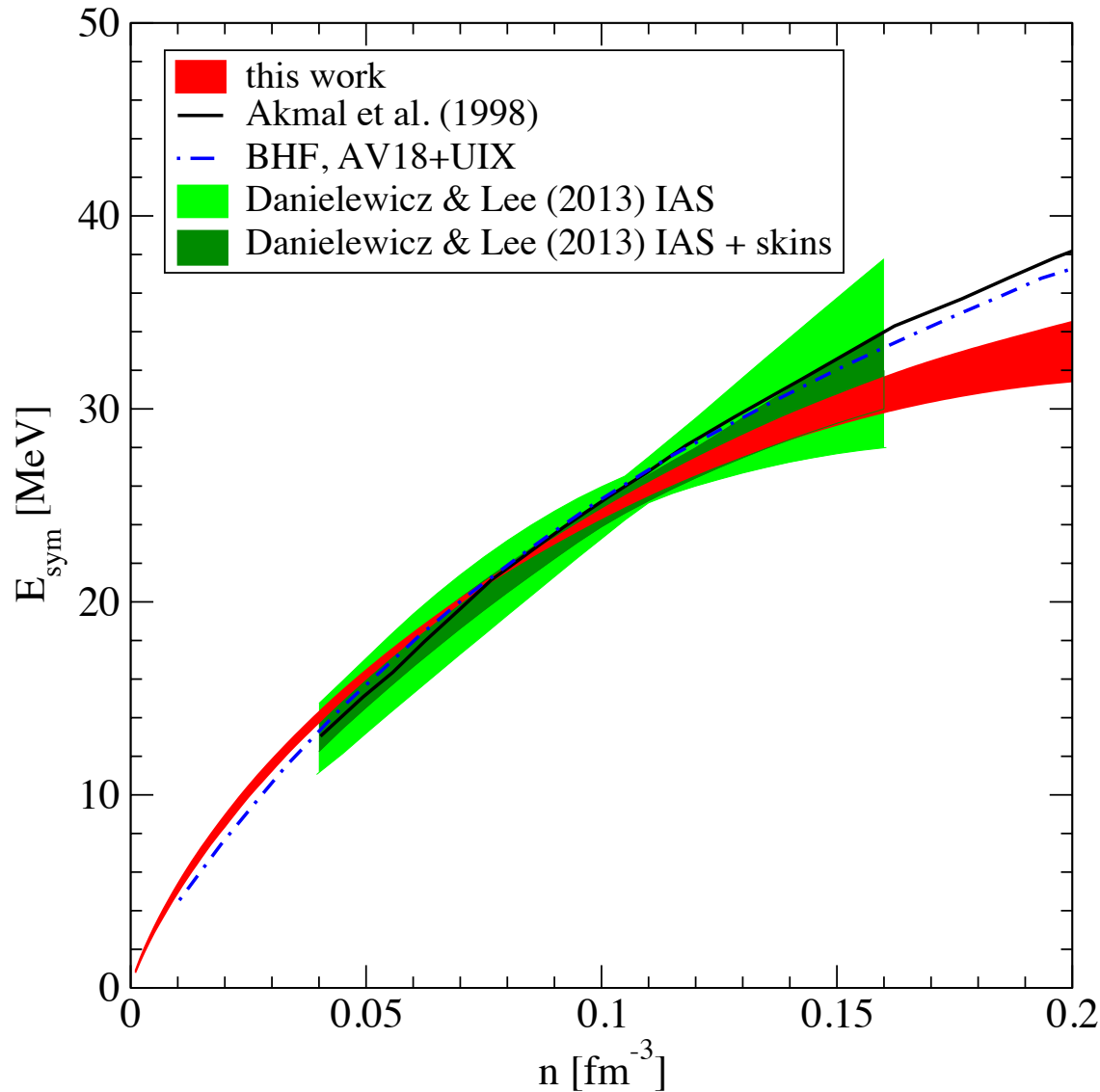
asymmetric matter
with improved treatment
of 3N forces

Drischler, Hebeler, AS, PRC (2016)
see also Holt, Kaiser, Weise, Wellenhofer

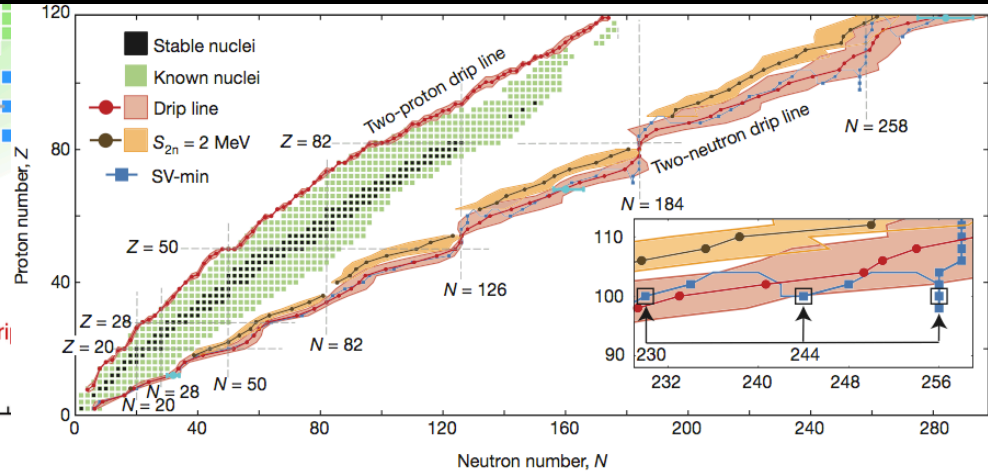
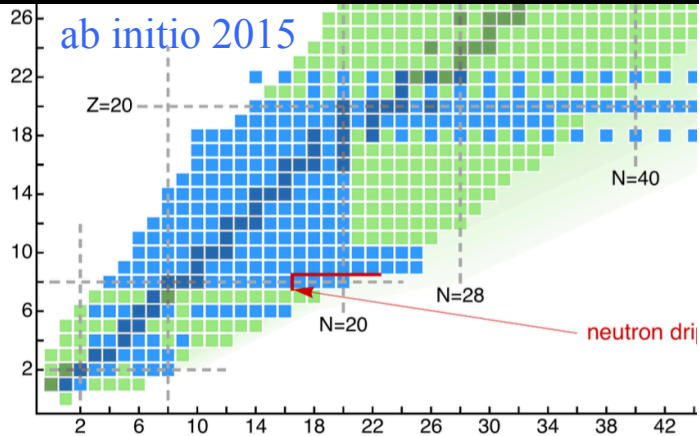
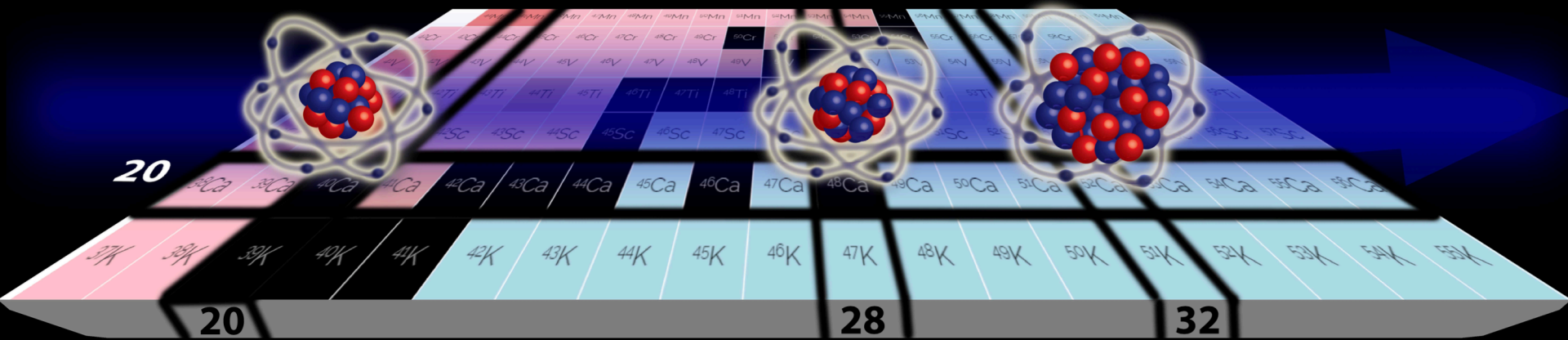


Calculations of asymmetric matter Drischler, Soma, AS, PRC (2014)

E_{sym} comparison with extraction from isobaric analogue states (IAS)
3N forces fit to ${}^3\text{H}$, ${}^4\text{He}$ properties only



Neutron-rich calcium isotopes



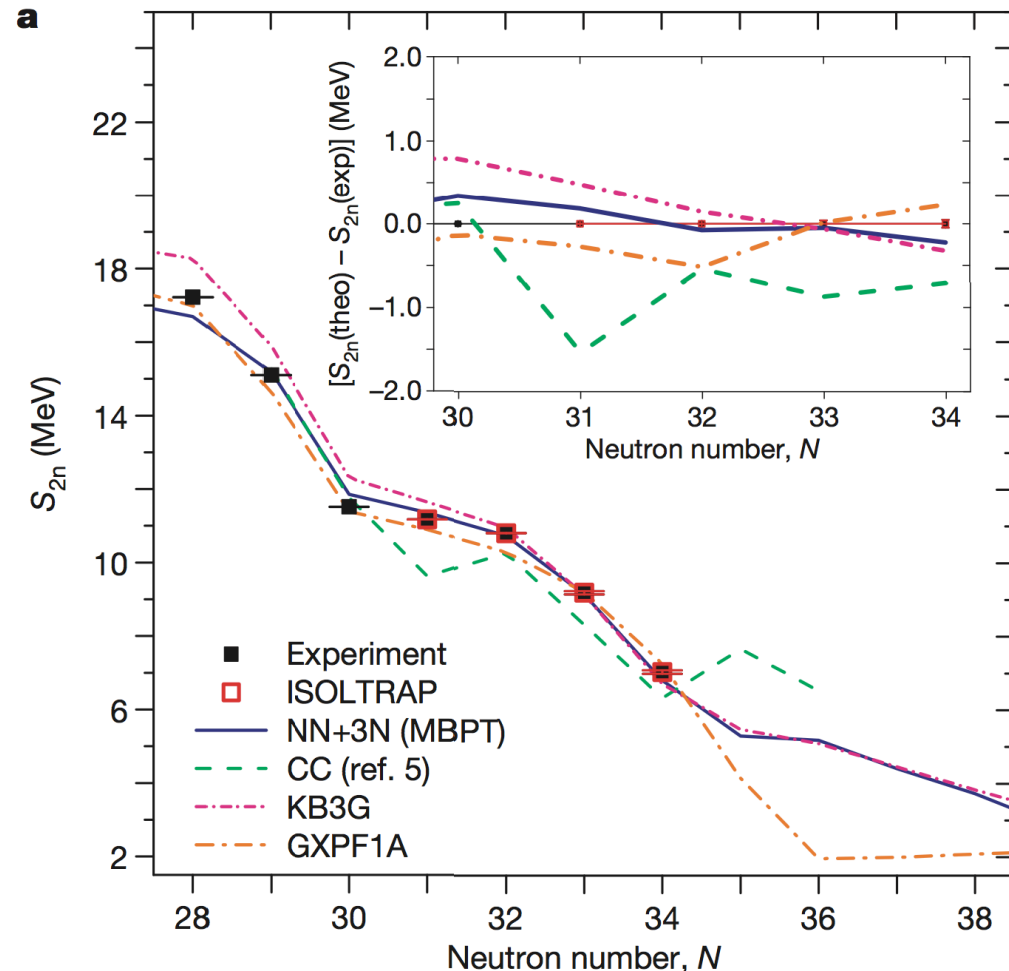
Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholtz¹, D. Beck², K. Blaum³, Ch. Borgmann³, M. Breitenfeldt⁴, R. B. Cakirli^{3,5}, S. George¹, F. Herfurth², J. D. Holt^{6,7}, M. Kowalska⁸, S. Kreim^{3,8}, D. Lunney⁹, V. Manea⁹, J. Menéndez^{6,7}, D. Neidherr², M. Rosenbusch¹, L. Schweikhard¹, A. Schwenk^{7,6}, J. Simonis^{6,7}, J. Stanja¹⁰, R. N. Wolf¹ & K. Zuber¹⁰

$^{53,54}\text{Ca}$ masses measured at ISOLTRAP/CERN using new MR-TOF mass spectrometer

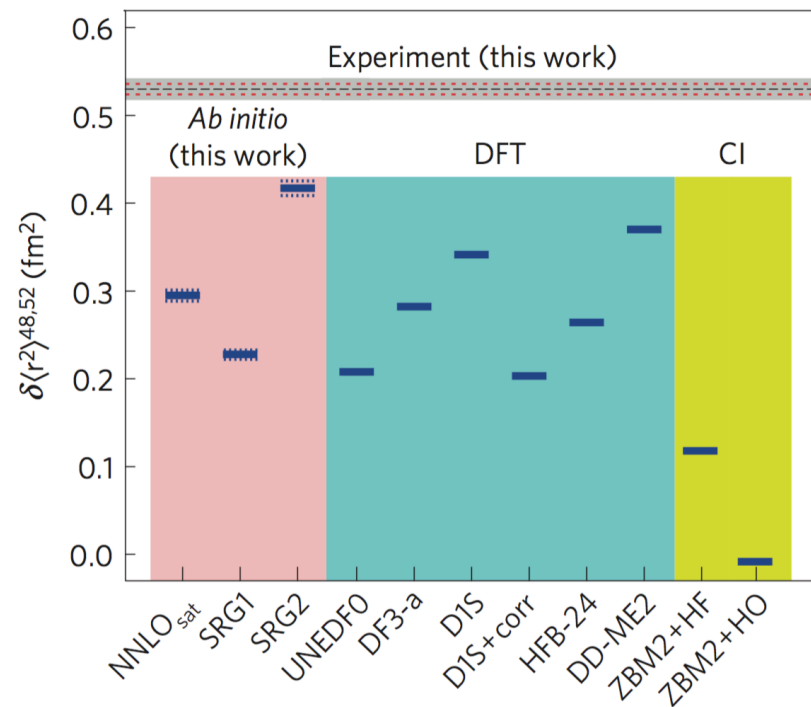
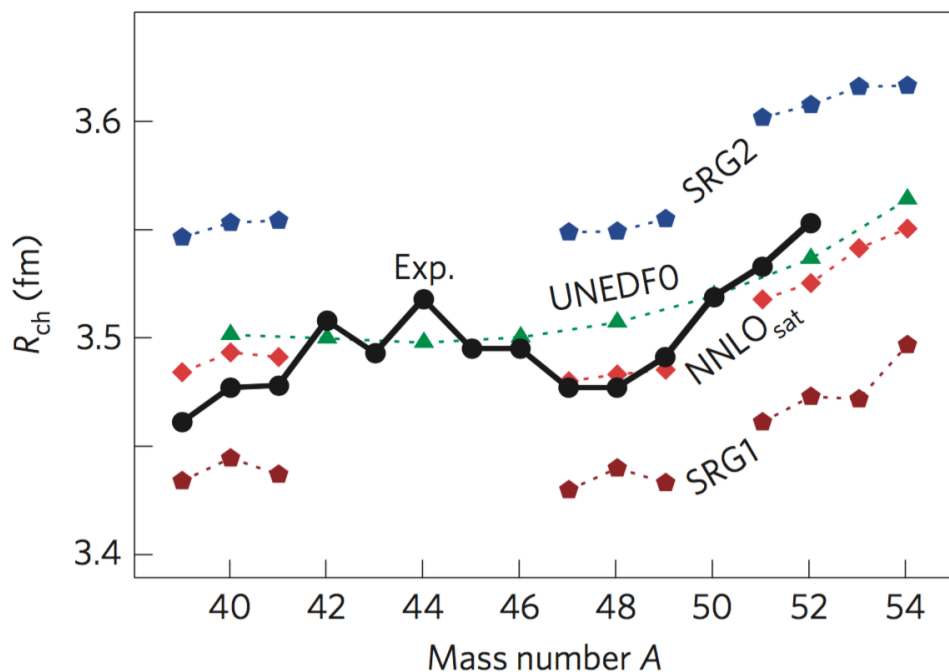
excellent agreement with theoretical NN+3N prediction

suggests $N=32$ shell closure



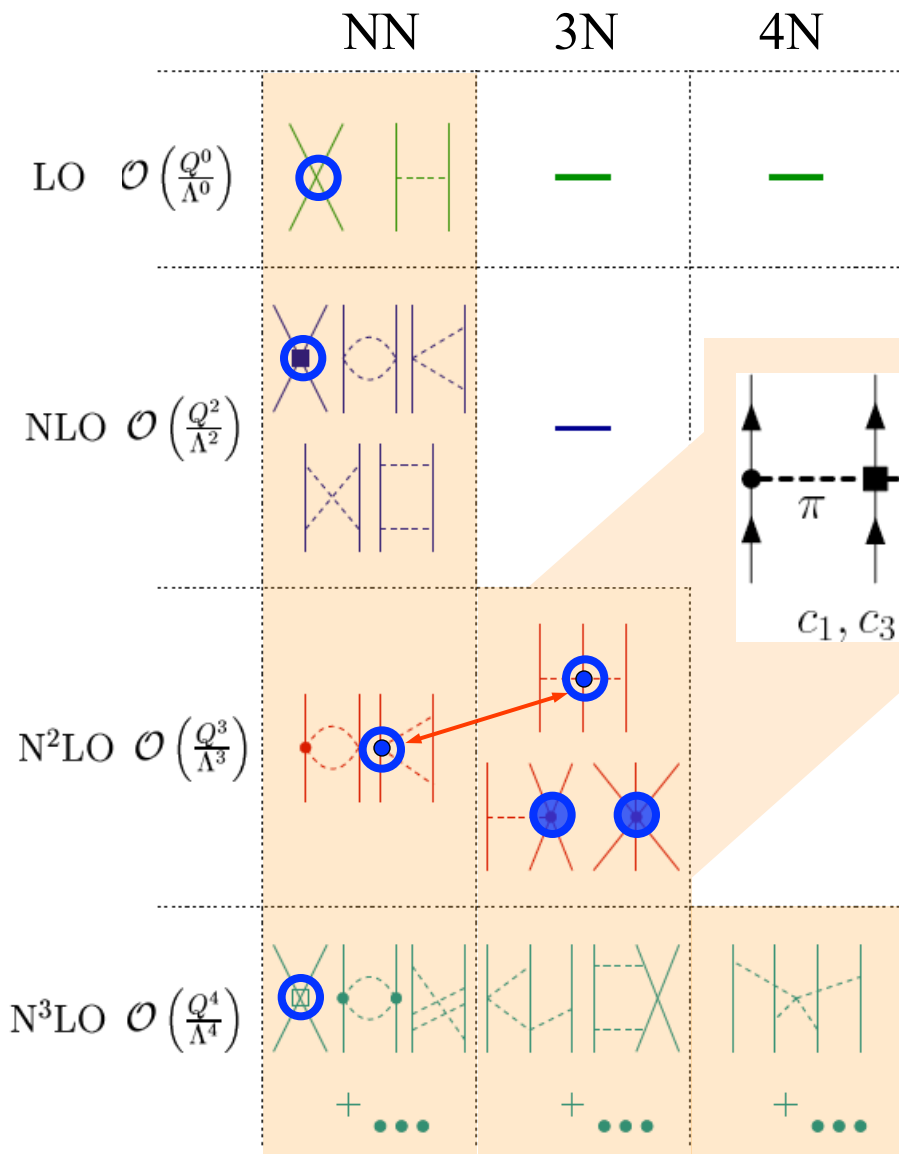
Unexpectedly large charge radii of neutron-rich calcium isotopes

R. F. Garcia Ruiz^{1*}, M. L. Bissell^{1,2}, K. Blaum³, A. Ekström^{4,5}, N. Frömmgen⁶, G. Hagen⁴, M. Hammen⁶, K. Hebeler^{7,8}, J. D. Holt⁹, G. R. Jansen^{4,5}, M. Kowalska¹⁰, K. Kreim³, W. Nazarewicz^{4,11,12}, R. Neugart^{3,6}, G. Neyens¹, W. Nörtershäuser^{6,7}, T. Papenbrock^{4,5}, J. Papuga¹, A. Schwenk^{3,7,8}, J. Simonis^{7,8}, K. A. Wendt^{4,5} and D. T. Yordanov^{3,13}

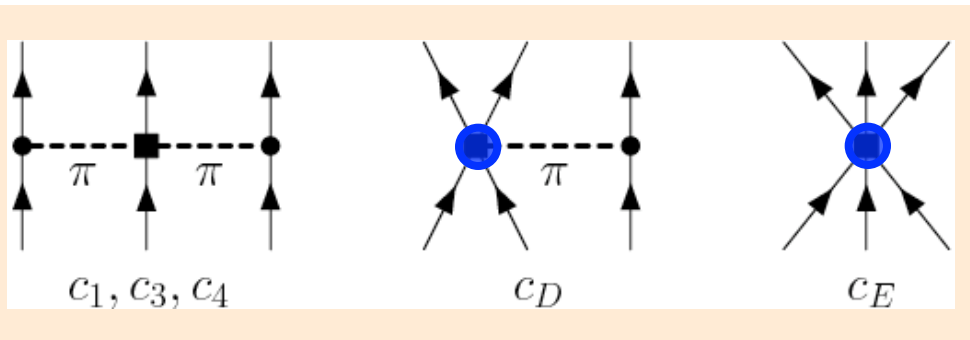


Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_b$ breakdown scale ~ 500 MeV



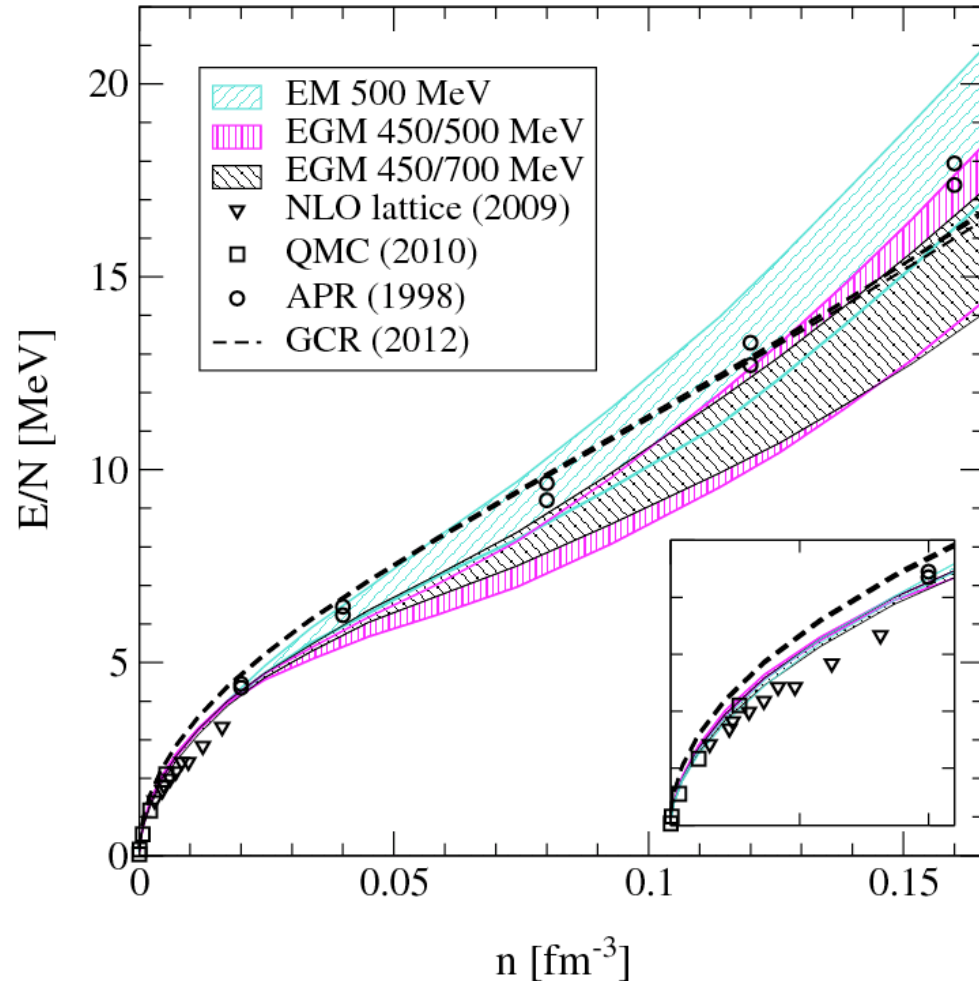
c_D, c_E don't contribute for **neutrons** because of Pauli principle and pion coupling to spin, also for c_4
 Hebeler, AS (2010) for non/semi-local regulators



all 3- and 4-neutron forces are predicted to N³LO!

Complete N³LO calculation of neutron matter

first complete N³LO result [Tews, Krüger, Hebeler, AS, PRL \(2013\)](#)
includes uncertainties from NN, 3N (dominates), 4N



good agreement with
Quantum Monte Carlo
calculations at low densities

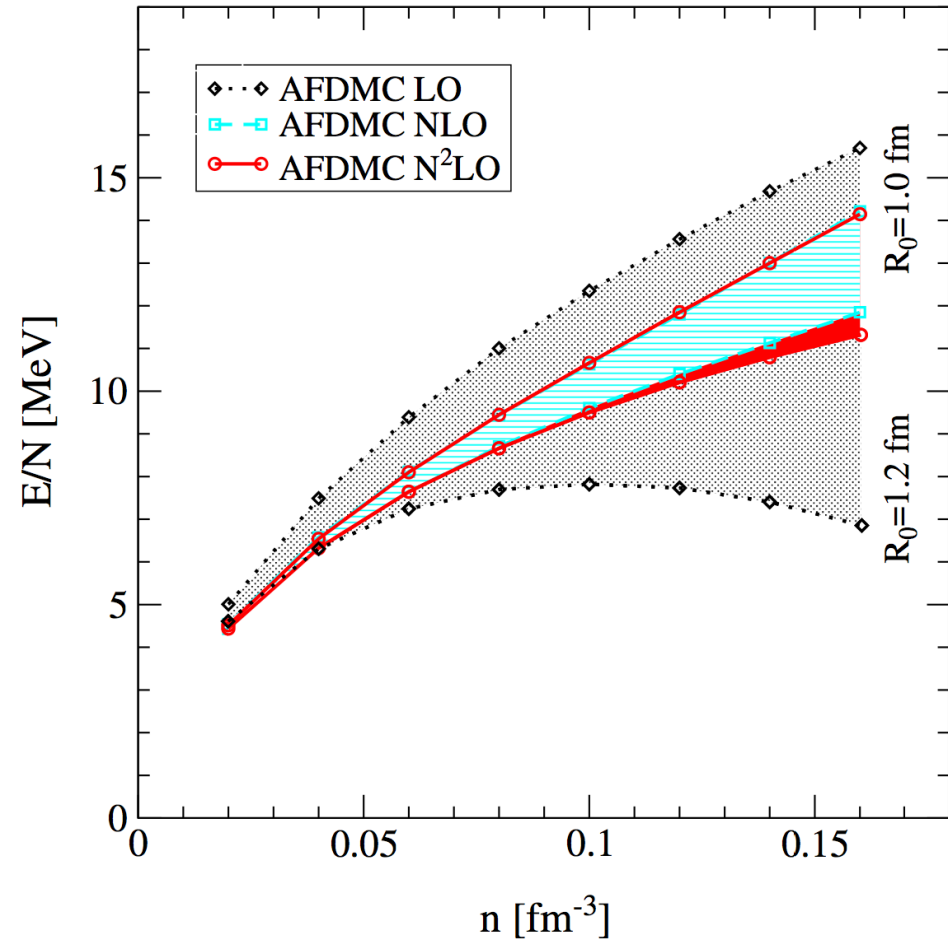
new QMC benchmarks with
local chiral potentials

[Gezerlis, Lynn, Tews et al.](#)

Quantum Monte Carlo for neutron matter Gezerlis, Tews et al., PRL (2013)

and PRC (2014)

based on new **local** chiral EFT potentials,
order-by-order convergence up to saturation density



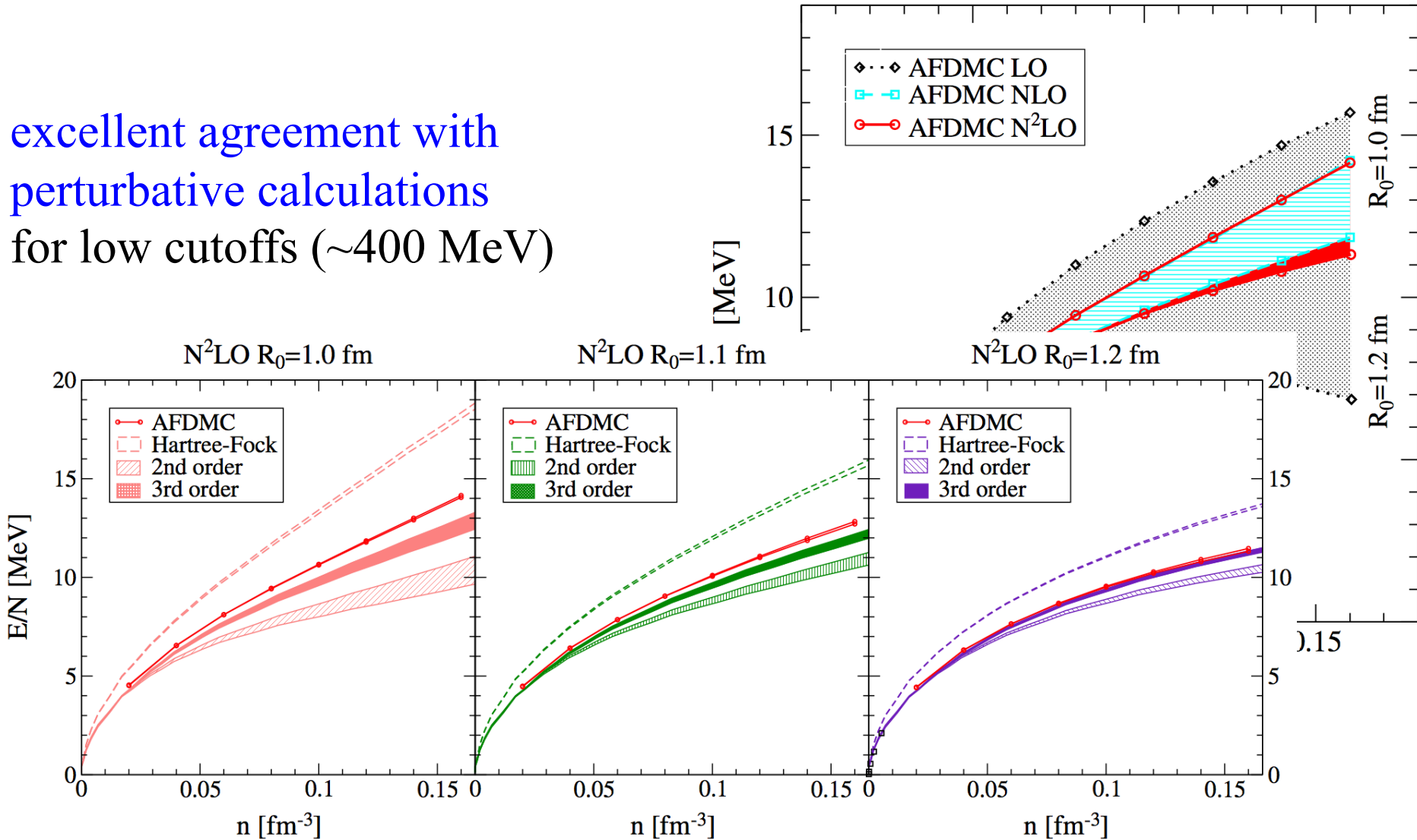
Quantum Monte Carlo for neutron matter Gezerlis, Tews et al., PRL (2013)

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and PRC (2014)

order-by-order convergence up to saturation density

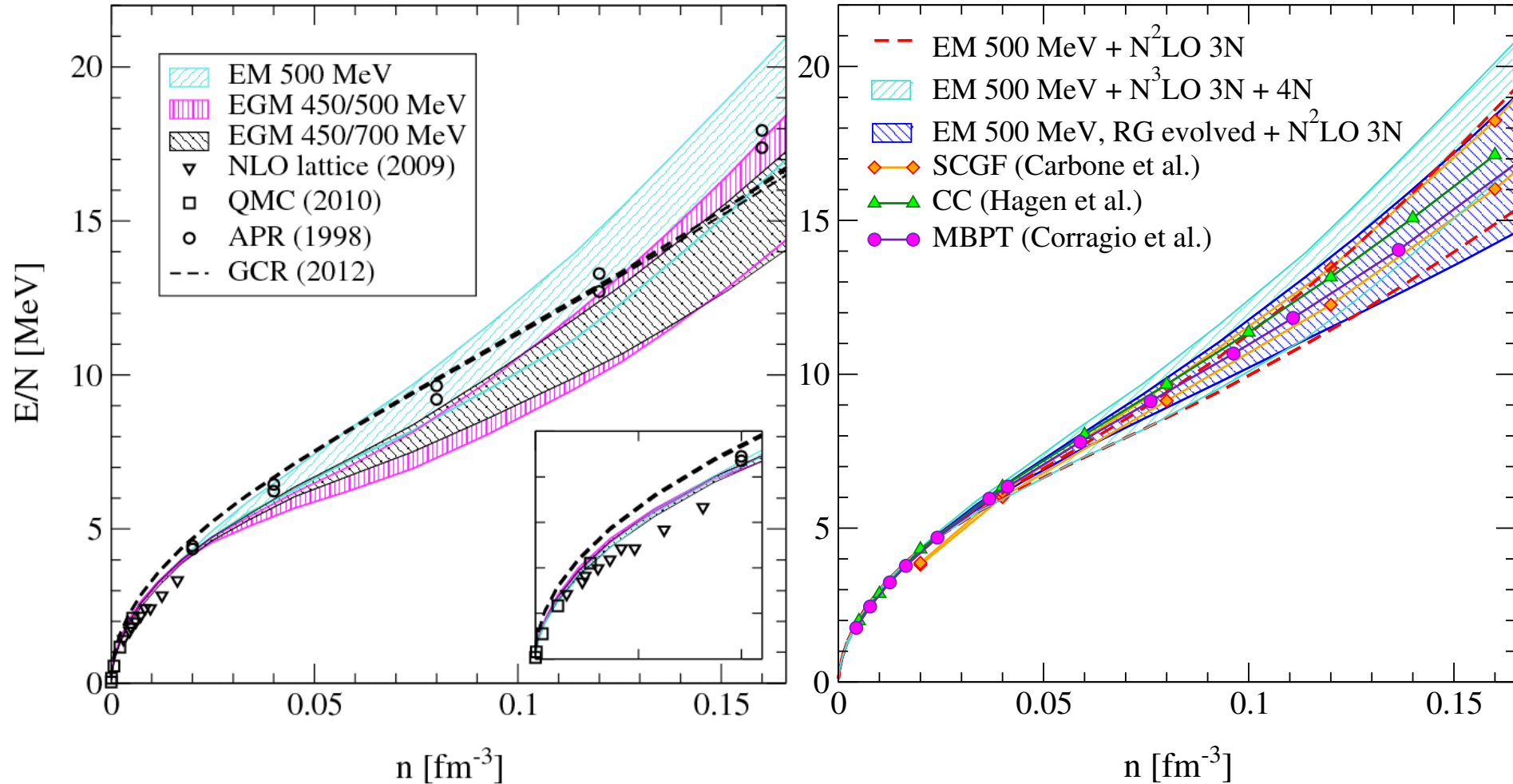
excellent agreement with
perturbative calculations
for low cutoffs (~ 400 MeV)



Complete N^3 LO calculation of neutron matter

first complete N^3 LO result [Tews, Krüger, Hebeler, AS, PRL \(2013\)](#)

includes uncertainties from NN, **3N (dominates)**, 4N

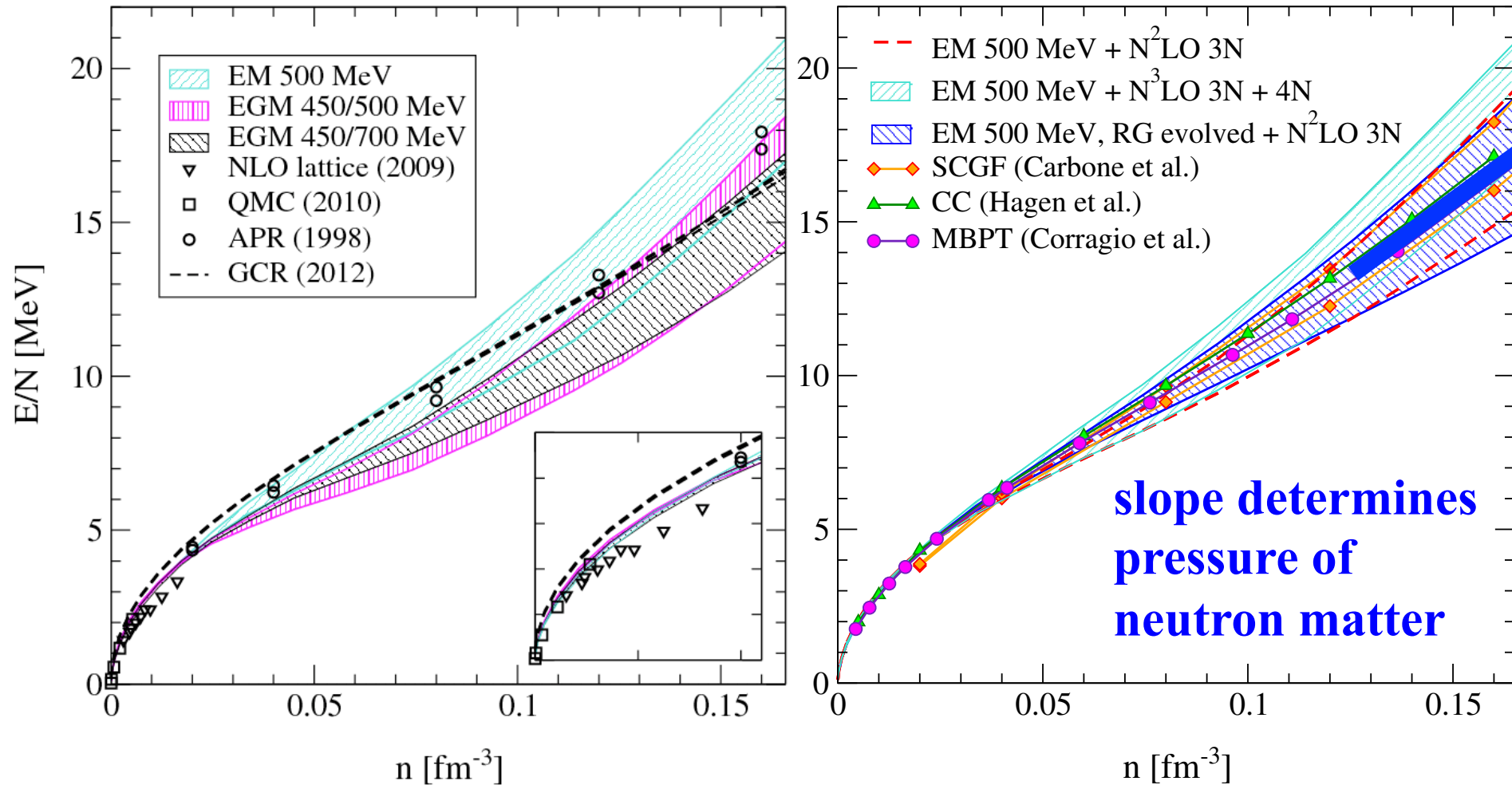


excellent agreement with other methods!

Complete N³LO calculation of neutron matter

first complete N³LO result Tews, Krüger, Hebeler, AS, PRL (2013)

includes uncertainties from NN, 3N (dominates), 4N



excellent agreement with other methods!

Symmetry energy and pressure of neutron matter

neutron matter band predicts
symmetry energy S_v and
its density derivative L

comparison to experimental
and observational constraints

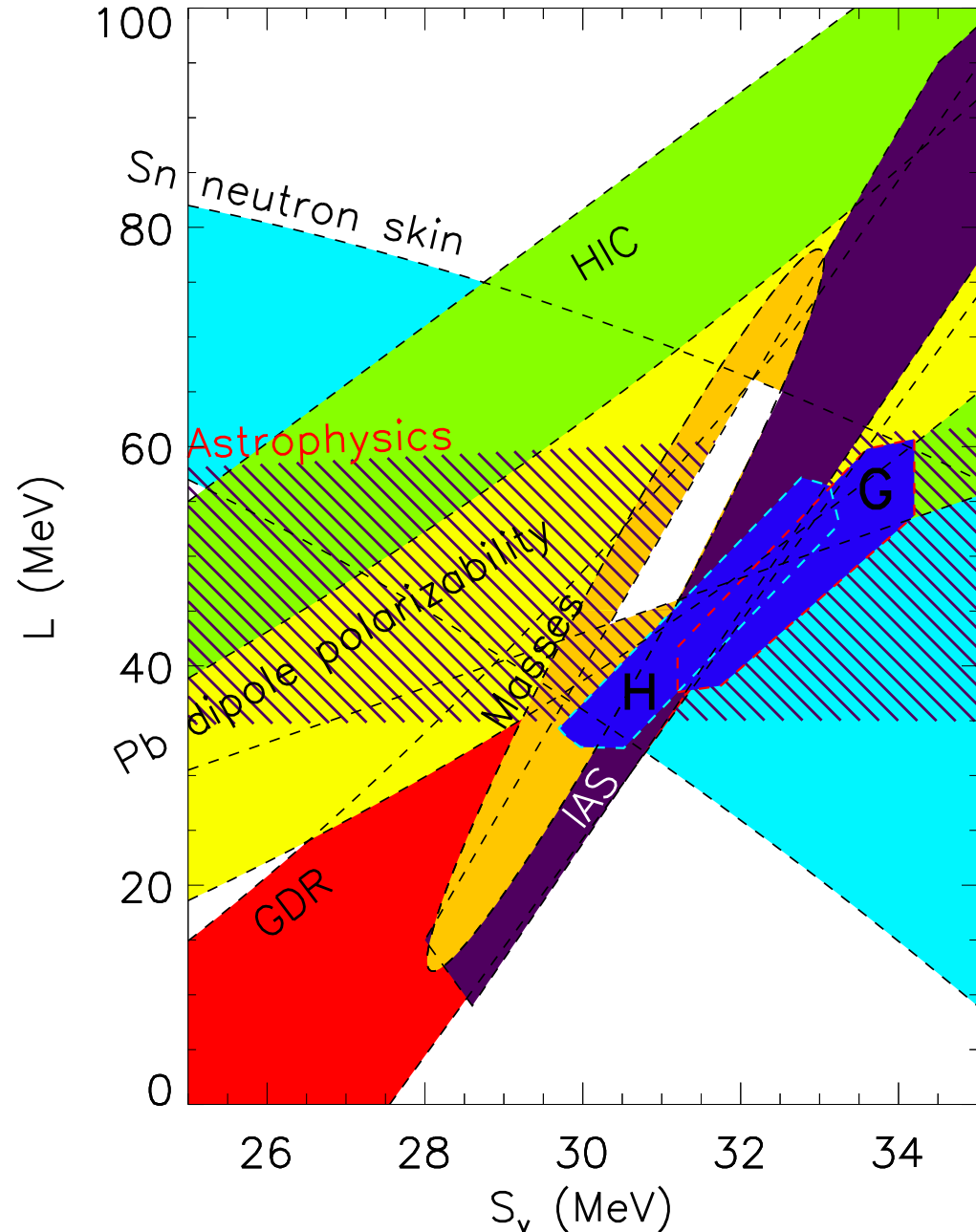
Lattimer, Lim, ApJ (2012), EPJA (2014)

neutron matter constraints

H: Hebeler et al. (2010)

G: Gandolfi et al. (2011)

provide tight constraints!

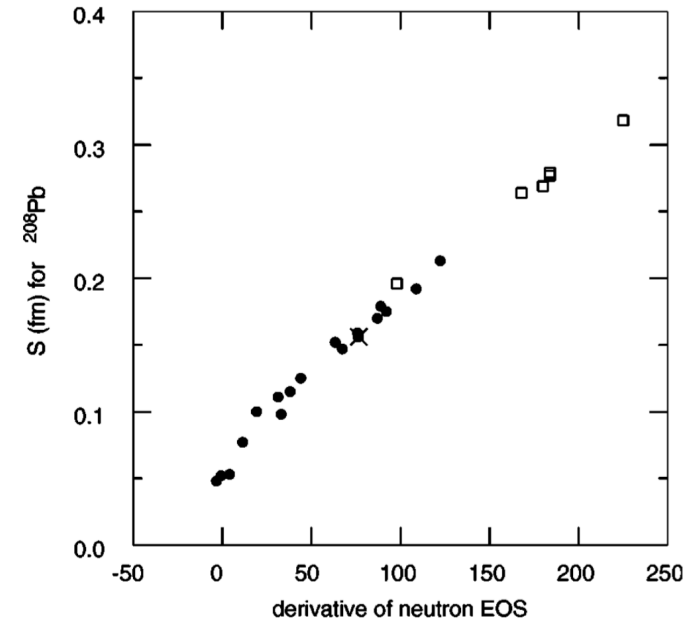
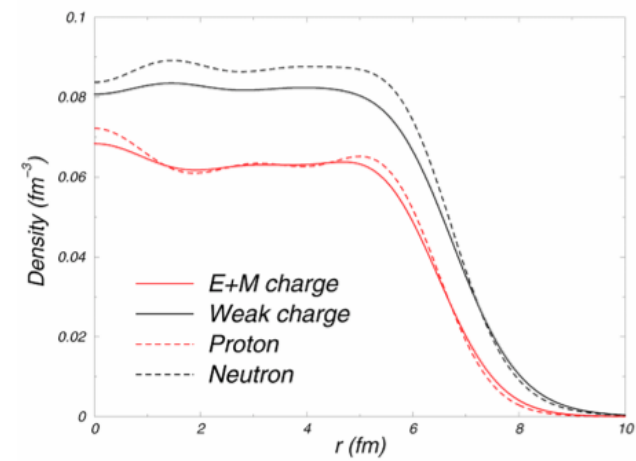


Neutron skin of ^{208}Pb

probes neutron matter energy/pressure,
neutron matter band predicts

neutron skin of ^{208}Pb : 0.17 ± 0.03 fm ($\pm 18\%$)

Hebeler, Lattimer, Pethick, AS, PRL (2010)



Brown (2000), Typel, Brown (2001)

Neutron skin of ^{208}Pb

probes neutron matter energy/pressure,
neutron matter band predicts

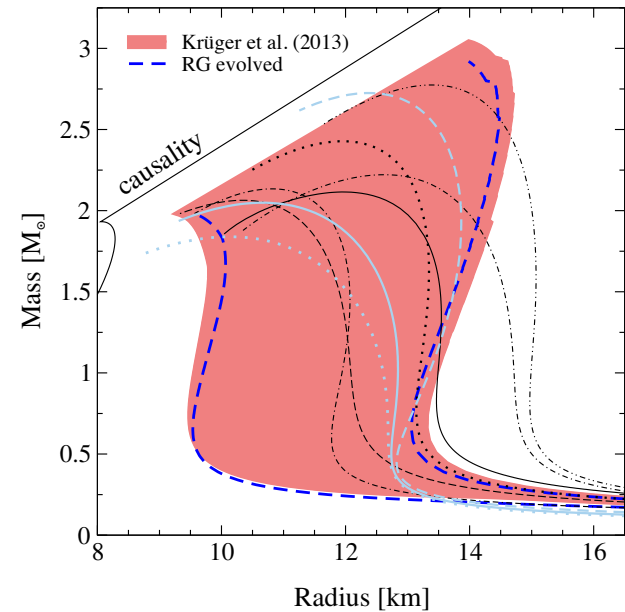
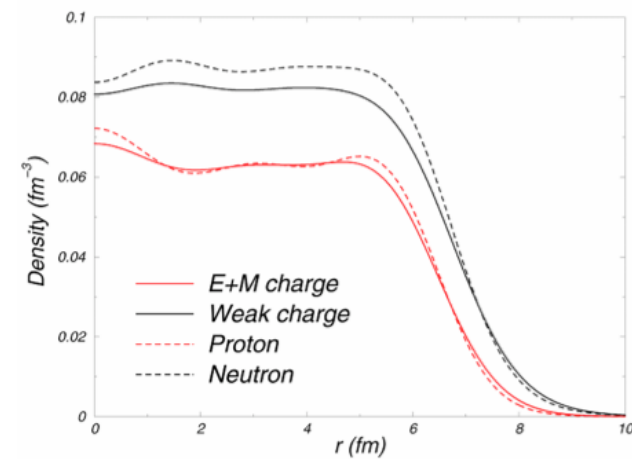
neutron skin of ^{208}Pb : 0.17 ± 0.03 fm ($\pm 18\%$)

Hebeler, Lattimer, Pethick, AS, PRL (2010)

same interactions lead to neutron star

radius: 9.7-13.9 km for $M=1.4 M_{\text{sun}}$ ($\pm 18\%$)

Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

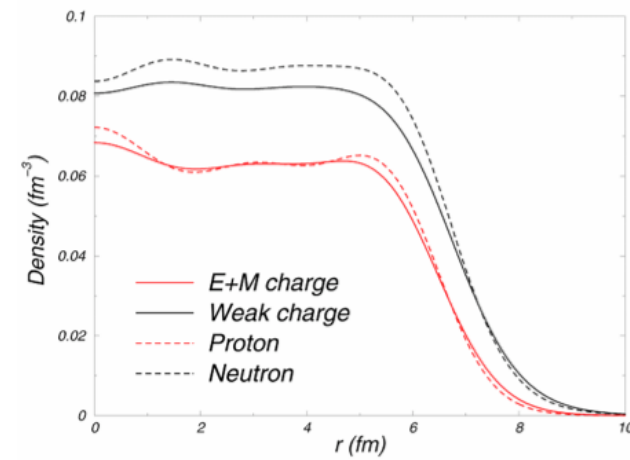


Neutron skin of ^{208}Pb

probes neutron matter energy/pressure,
neutron matter band predicts

neutron skin of ^{208}Pb : 0.17 ± 0.03 fm ($\pm 18\%$)

Hebeler, Lattimer, Pethick, AS, PRL (2010)



in agreement with extraction from dipole polarizability

$0.156 + 0.025 - 0.021$ fm Tamii et al., PRL (2011)

PREX: neutron skin from parity-violating electron-scattering at JLAB

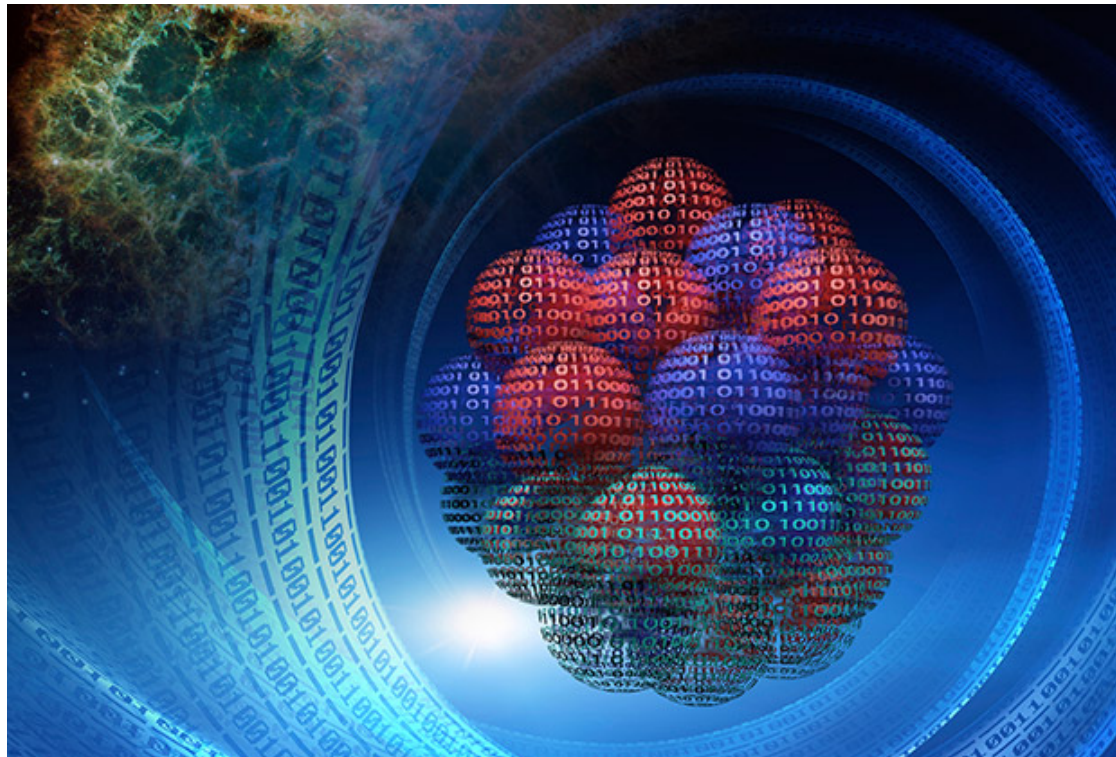
goal II: ± 0.06 fm Abrahamyan et al., PRL (2012)

MAMI: coherent pion photoproduction

$0.15 + 0.04 - 0.06$ fm Tabert et al., PRL (2014)

Neutron and weak-charge distributions of the ^{48}Ca nucleus

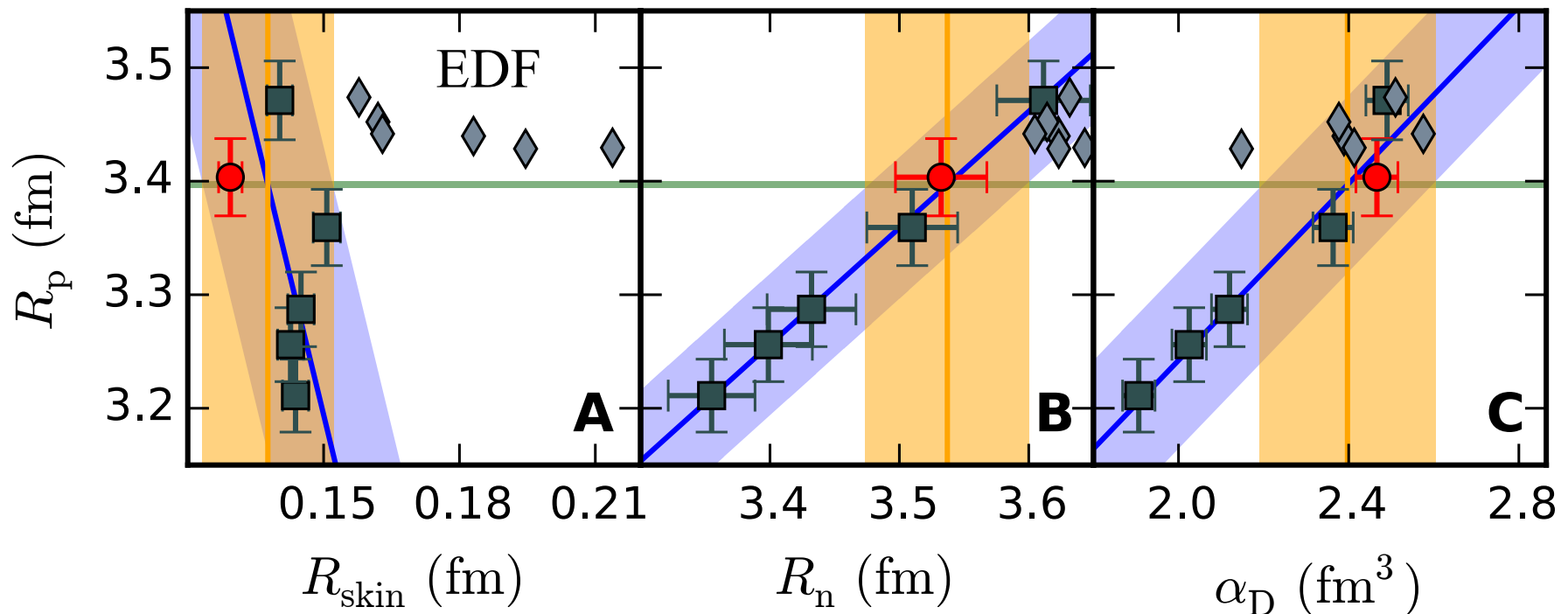
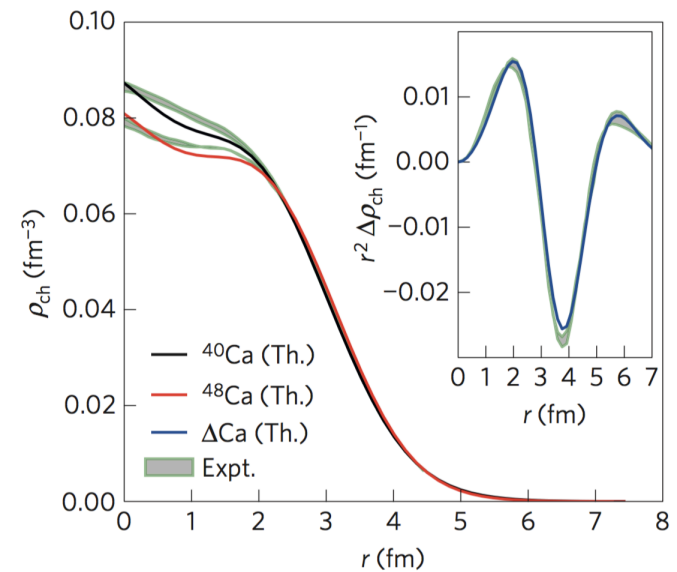
G. Hagen^{1,2*}, A. Ekström^{1,2}, C. Forssén^{1,2,3}, G. R. Jansen^{1,2}, W. Nazarewicz^{1,4,5}, T. Papenbrock^{1,2},
K. A. Wendt^{1,2}, S. Bacca^{6,7}, N. Barnea⁸, B. Carlsson³, C. Drischler^{9,10}, K. Hebeler^{9,10},
M. Hjorth-Jensen^{4,11}, M. Miorelli^{6,12}, G. Orlandini^{13,14}, A. Schwenk^{9,10} and J. Simonis^{9,10}



Neutron and weak-charge distributions of ^{48}Ca

ab initio calculations lead to charge distributions consistent with experiment

predict **small neutron skin**, dipole polarizability, and weak formfactor

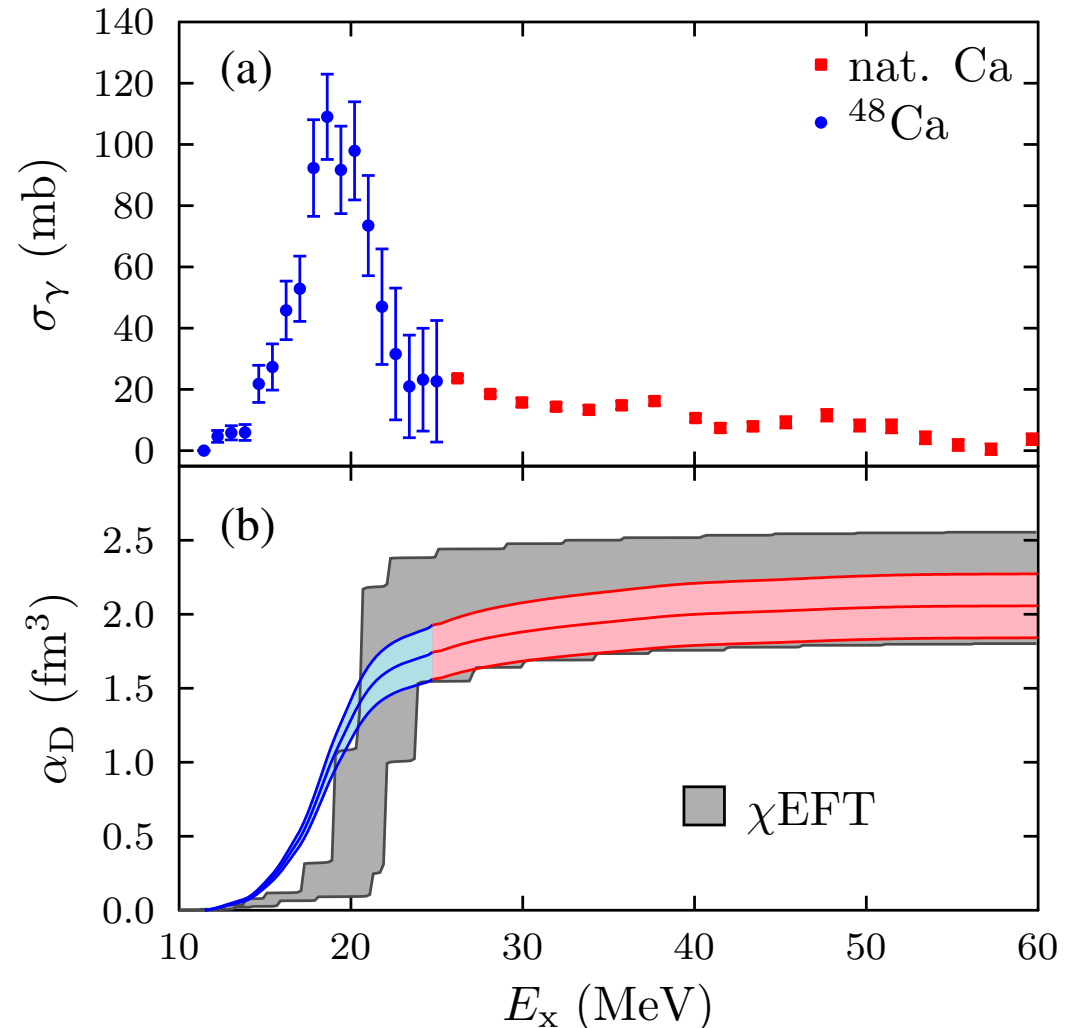


Dipole polarizability of ^{48}Ca

from photo-absorption cross section, measured at Osaka up to 25 MeV

Birkhan, von Neumann-Cosel, Richter, Tamii et al.

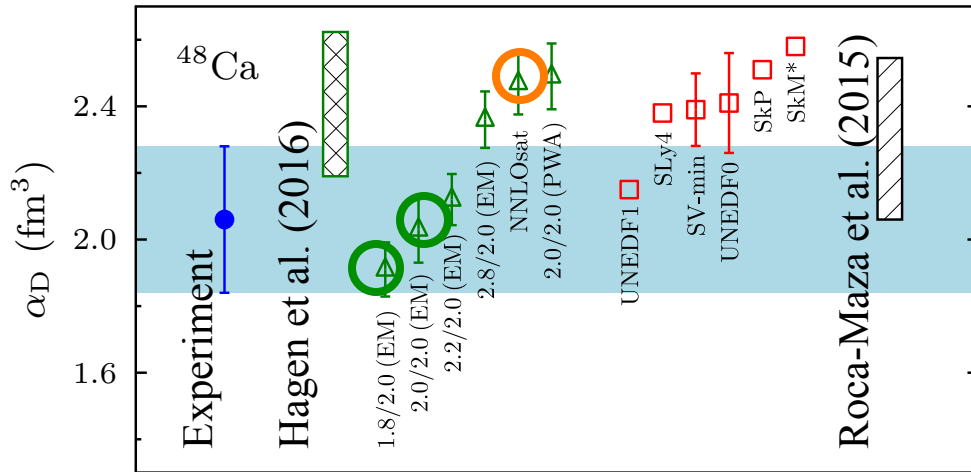
very similar to ^{40}Ca except for shift of giant dipole resonance



good agreement with
chiral EFT predictions

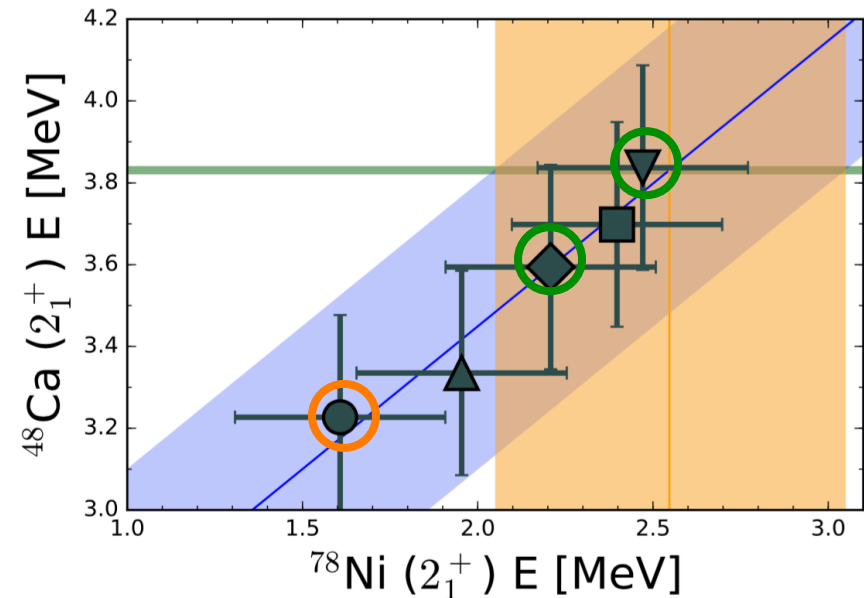
Miorelli, Bacca, Hagen et al.

Dipole polarizability of ^{48}Ca



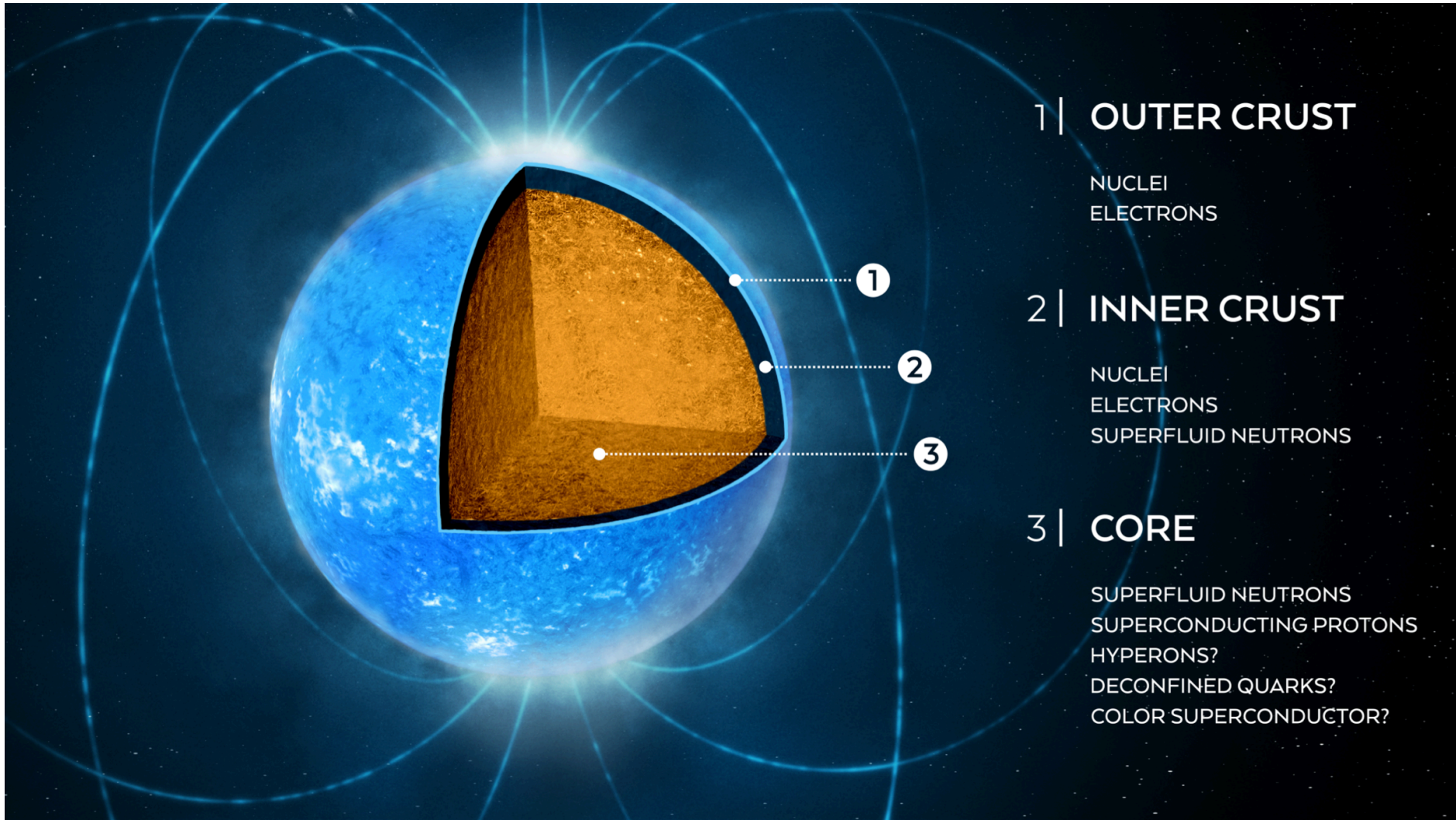
theory comparison gives
 $R_{\text{skin}} = 0.14\text{-}0.20$ fm

sensitive to
neutron matter properties
and strong shell closure



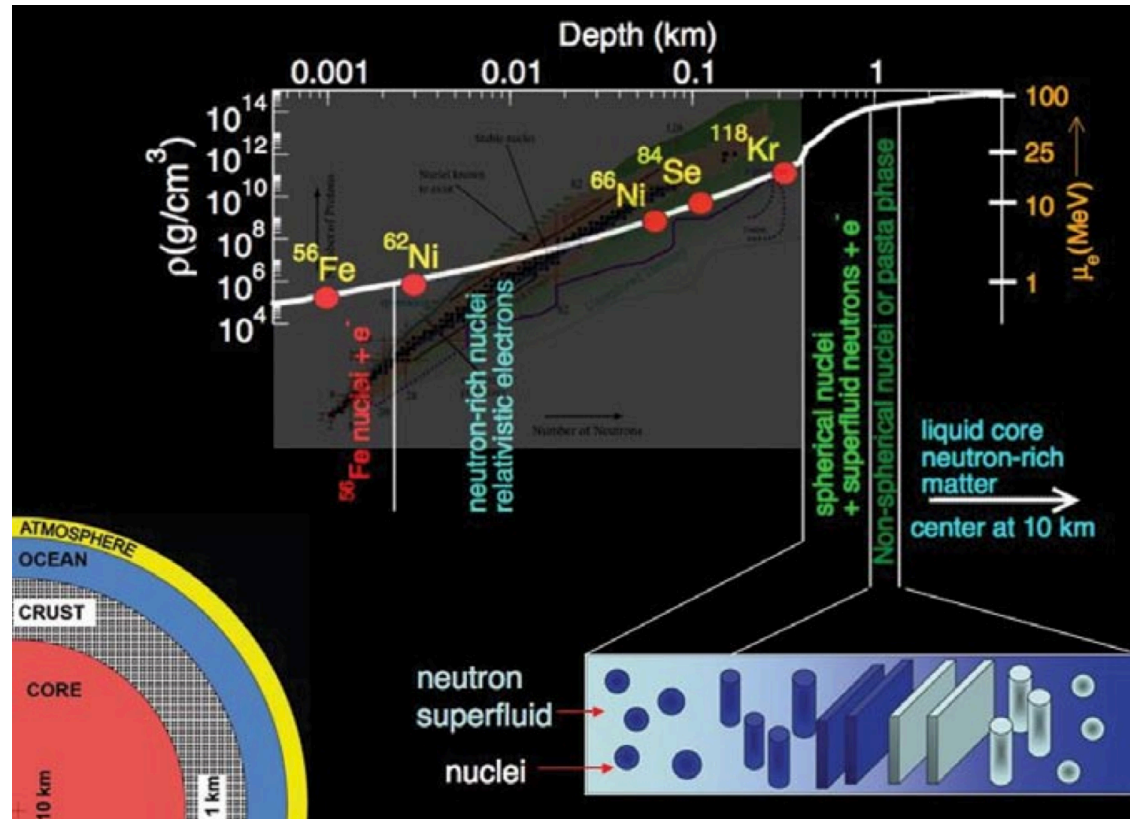
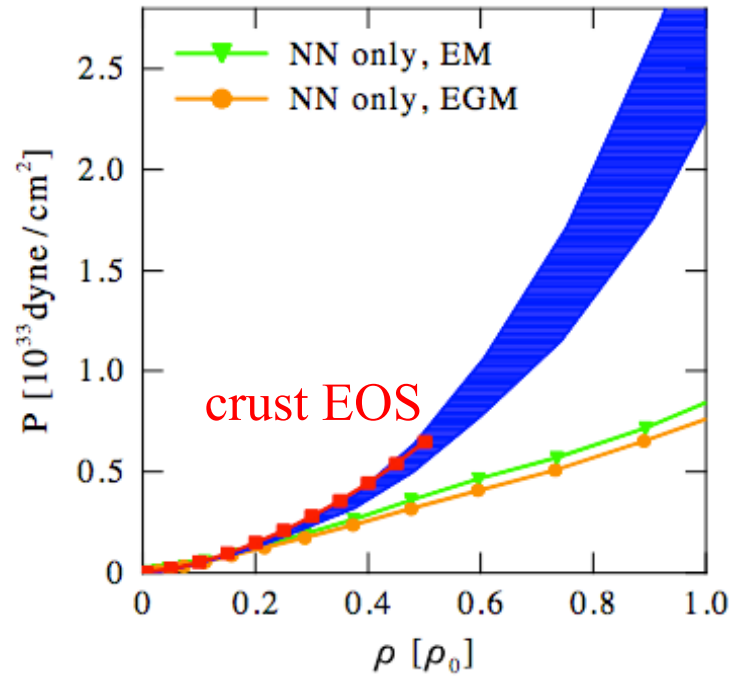
Hagen et al., 1605.01477

Neutron matter and neutron stars



Impact on neutron stars Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

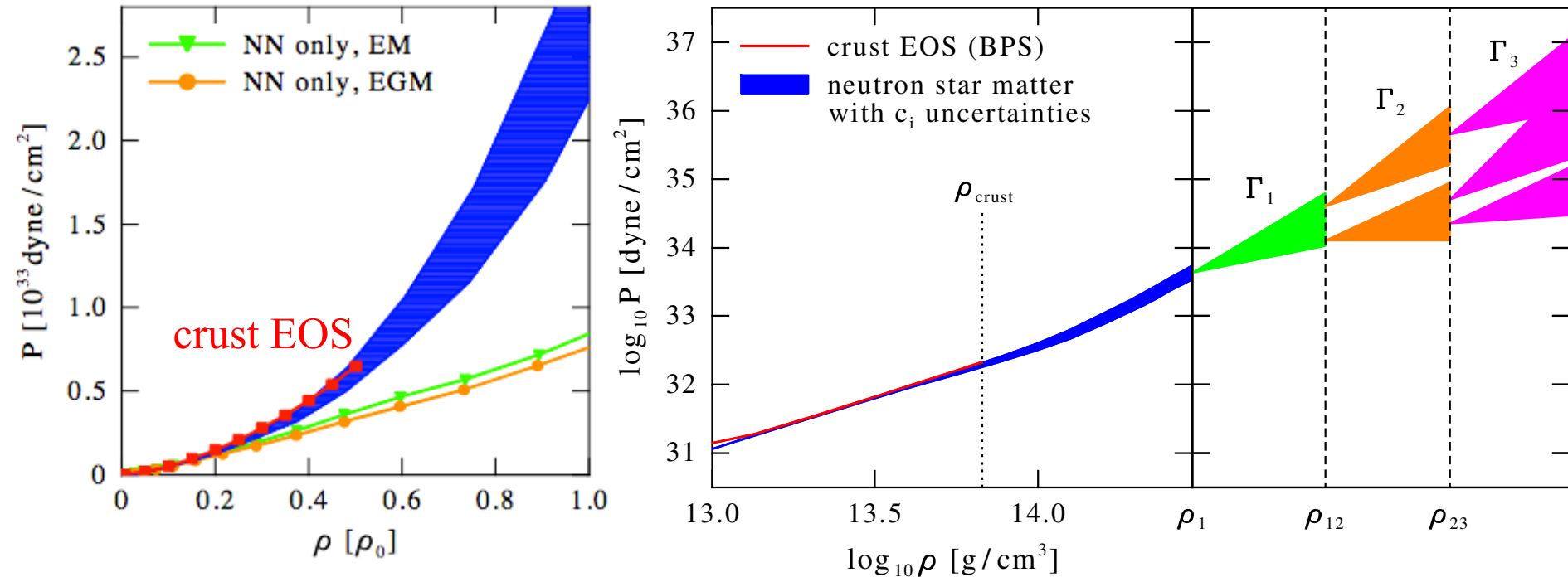
Equation of state/pressure for **neutron-star matter** (includes small $Y_{e,p}$)



pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

Impact on neutron stars Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

Equation of state/pressure for **neutron-star matter** (includes small $Y_{e,p}$)

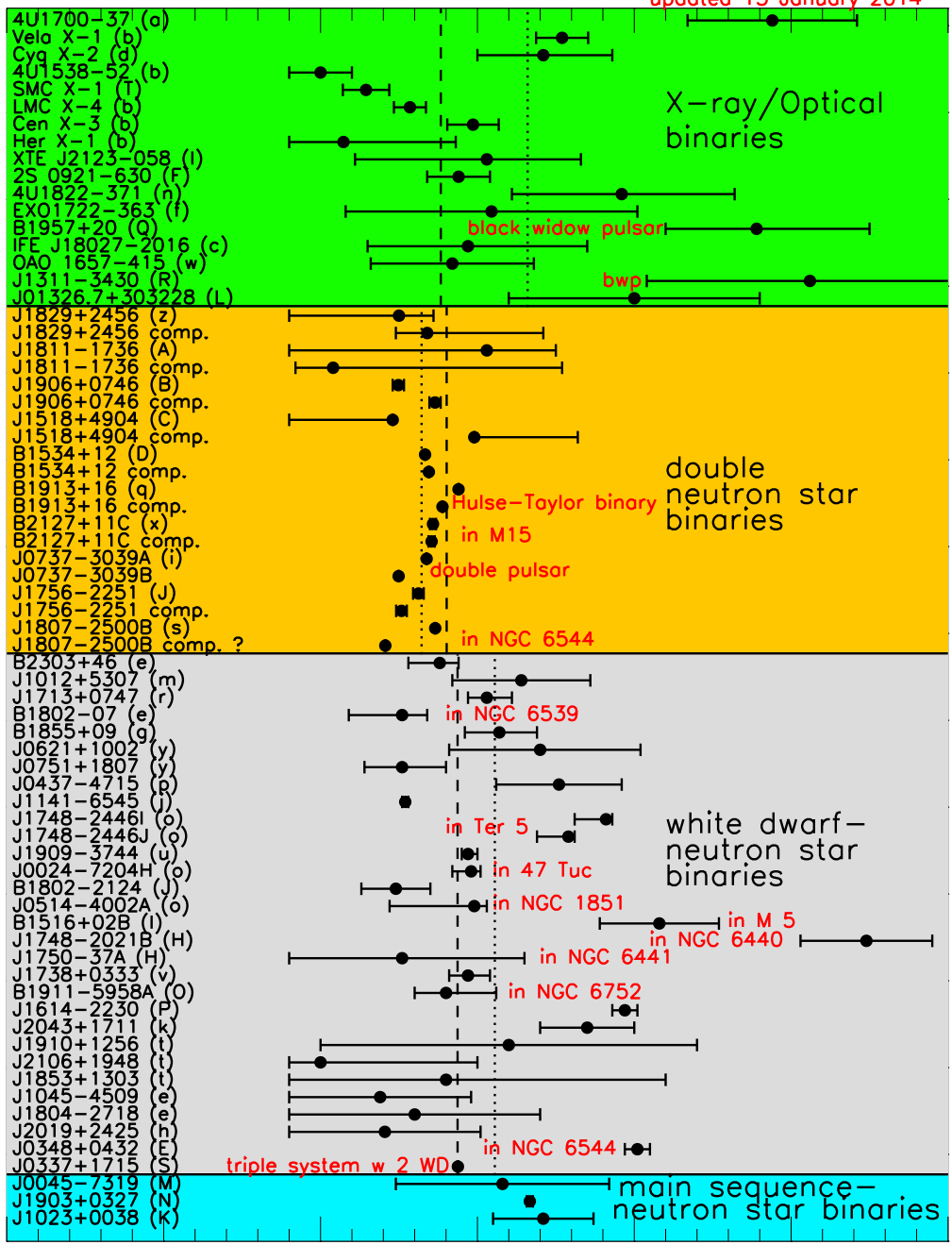


pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

extend uncertainty band to higher densities using piecewise polytropes
allow for soft regions

Chart of neutron star masses

from Jim Lattimer



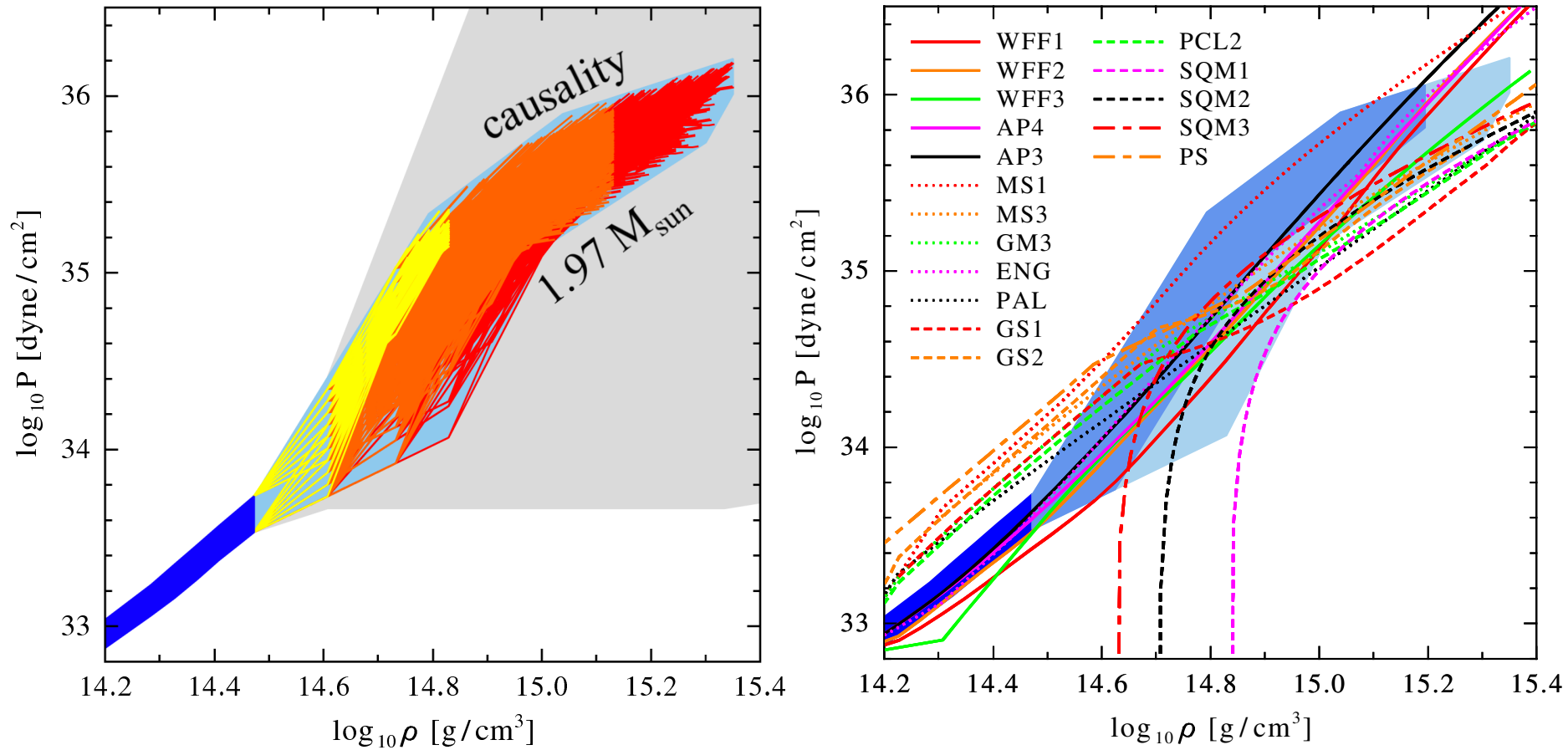
two $2 M_{\text{sun}}$ neutron stars observed

Demorest et al, Nature (2010),

Antoniadis et al., Science (2013)

Impact on neutron stars Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

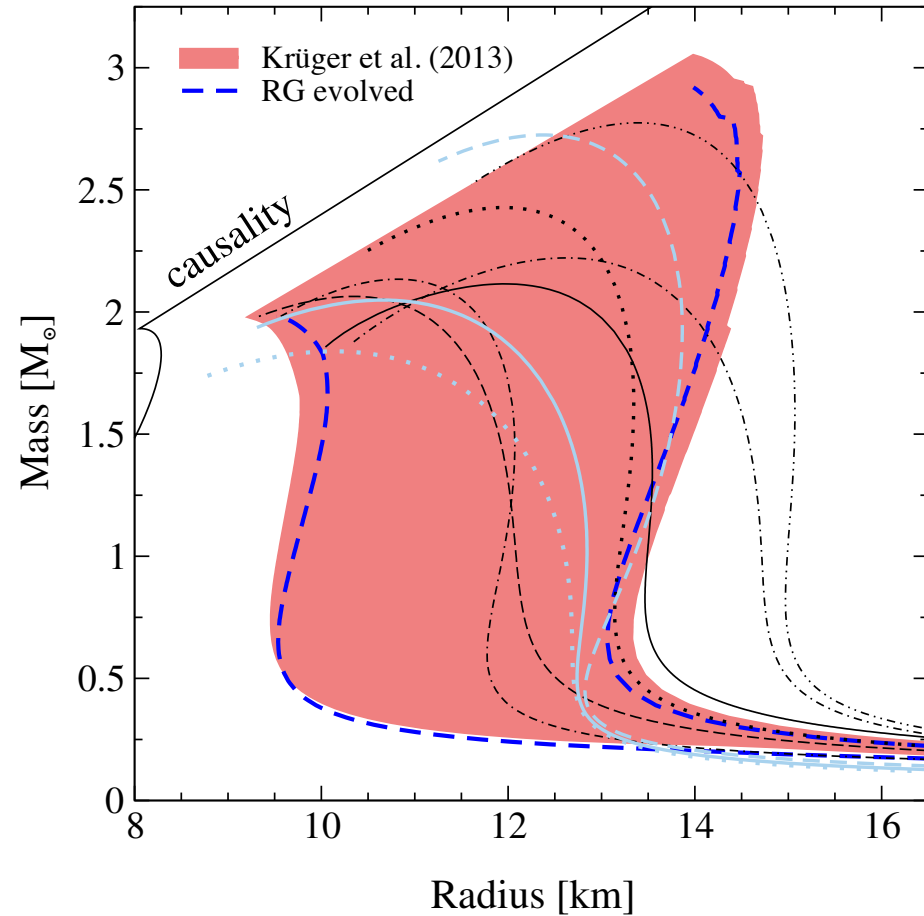
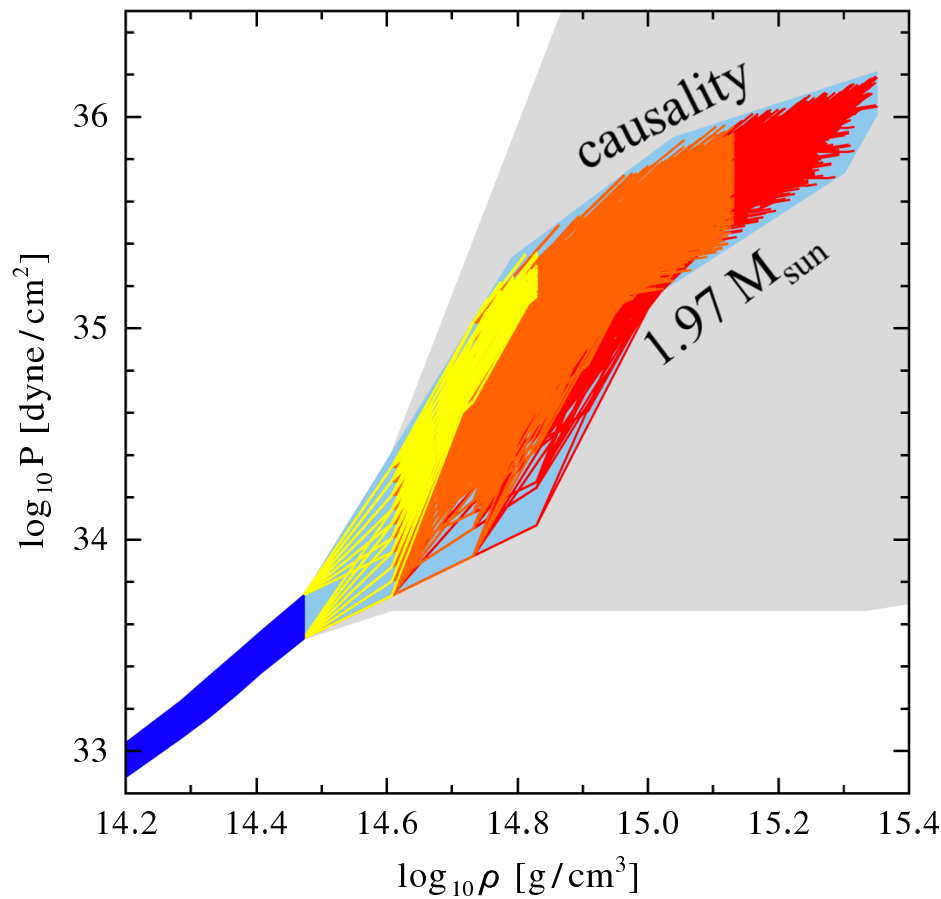
constrain high-density EOS by causality, require to support $2 M_{\text{sun}}$ star



low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

Impact on neutron stars Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

constrain high-density EOS by causality, require to support $2 M_{\text{sun}}$ star

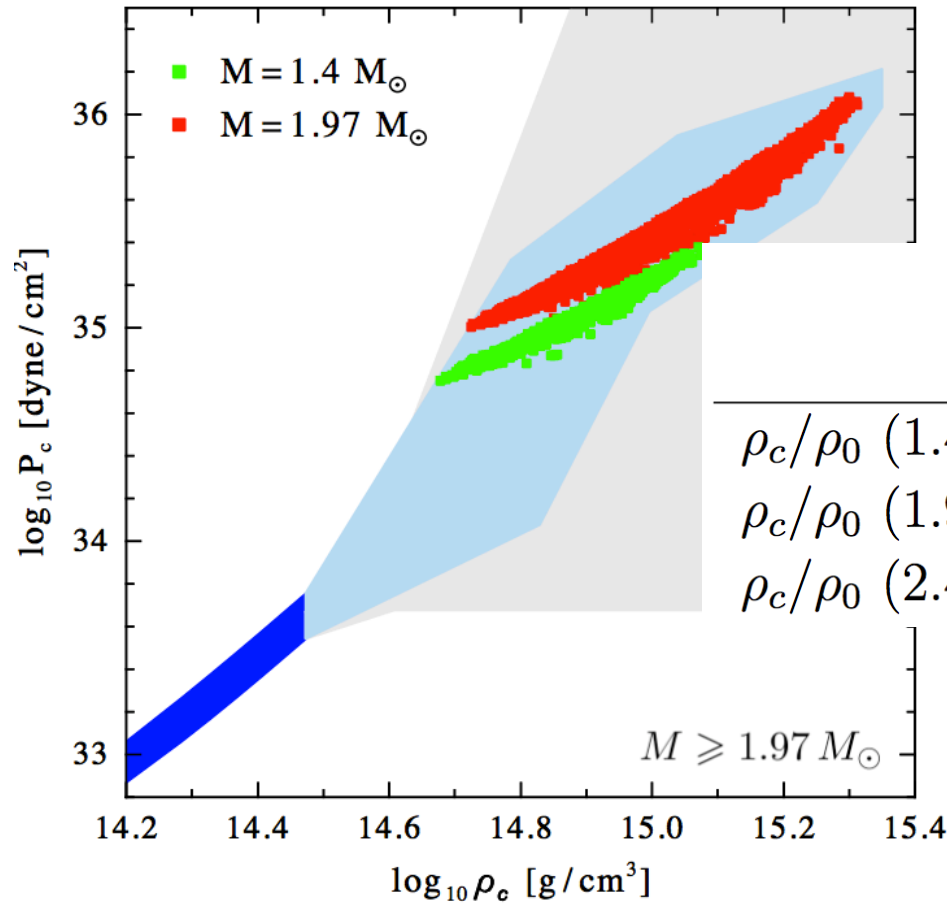


low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

predicts neutron star radius: 9.7-13.9 km for $M=1.4 M_{\text{sun}}$ ($\pm 18\%$!)

Impact on neutron stars Hebeler, Lattimer, Pethick, AS, PRL (2010), ApJ (2013)

constrain high-density EOS by causality, require to support $2 M_{\text{sun}}$ star



	$\widehat{M} = 1.97 M_{\odot}$		$\widehat{M} = 2.4 M_{\odot}$	
	min	max	min	max
$\rho_c / \rho_0 (1.4 M_{\odot})$	1.8	4.4	1.8	2.7
$\rho_c / \rho_0 (1.97 M_{\odot})$	2.0	7.6	2.0	3.4
$\rho_c / \rho_0 (2.4 M_{\odot})$			2.2	5.4

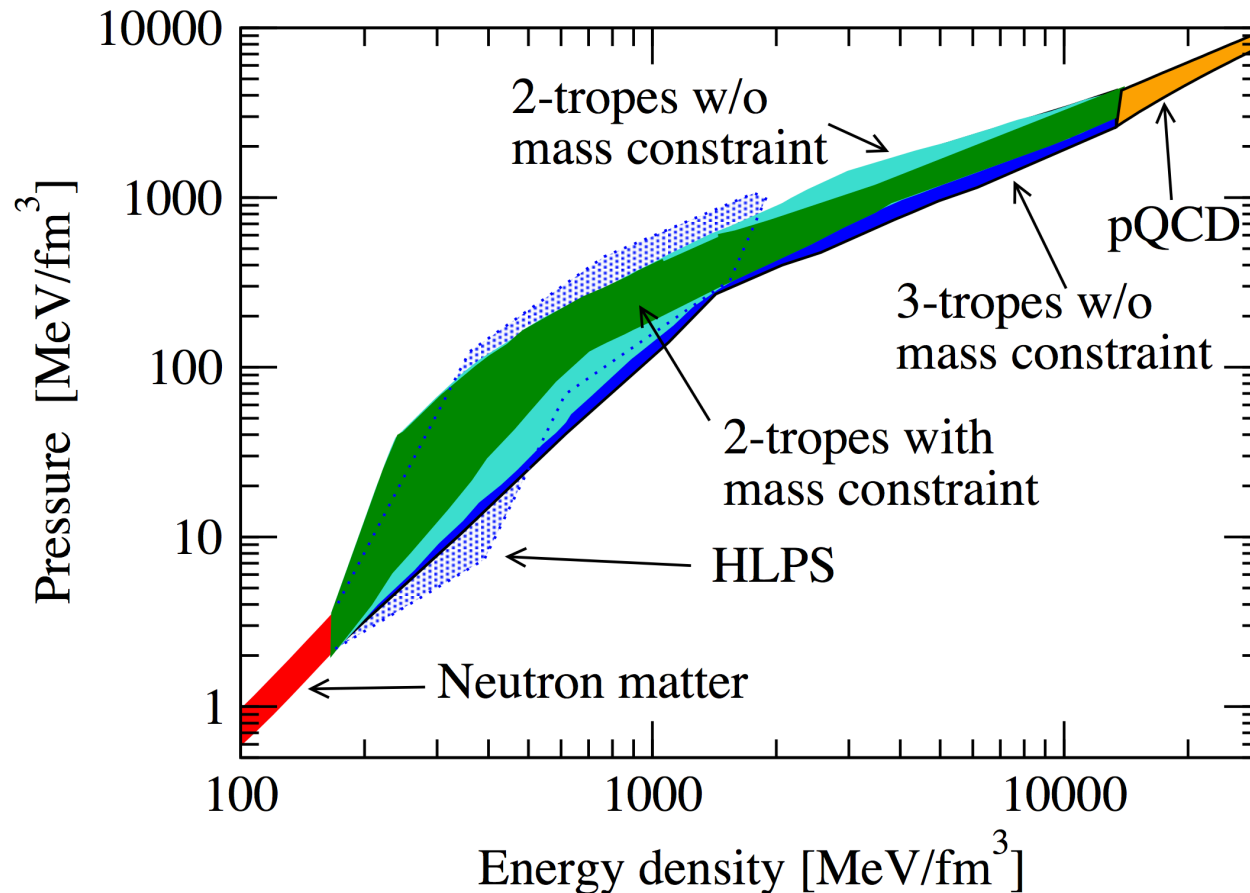
**central densities
for $1.4 M_{\text{sun}}$ star: 1.8-4.4 ρ_0**

not very high momenta!

Connecting the equation of state to pQCD calculations

recent $O(\alpha_s^2)$ calculation of quark matter in perturbative QCD provides constraint at very high densities

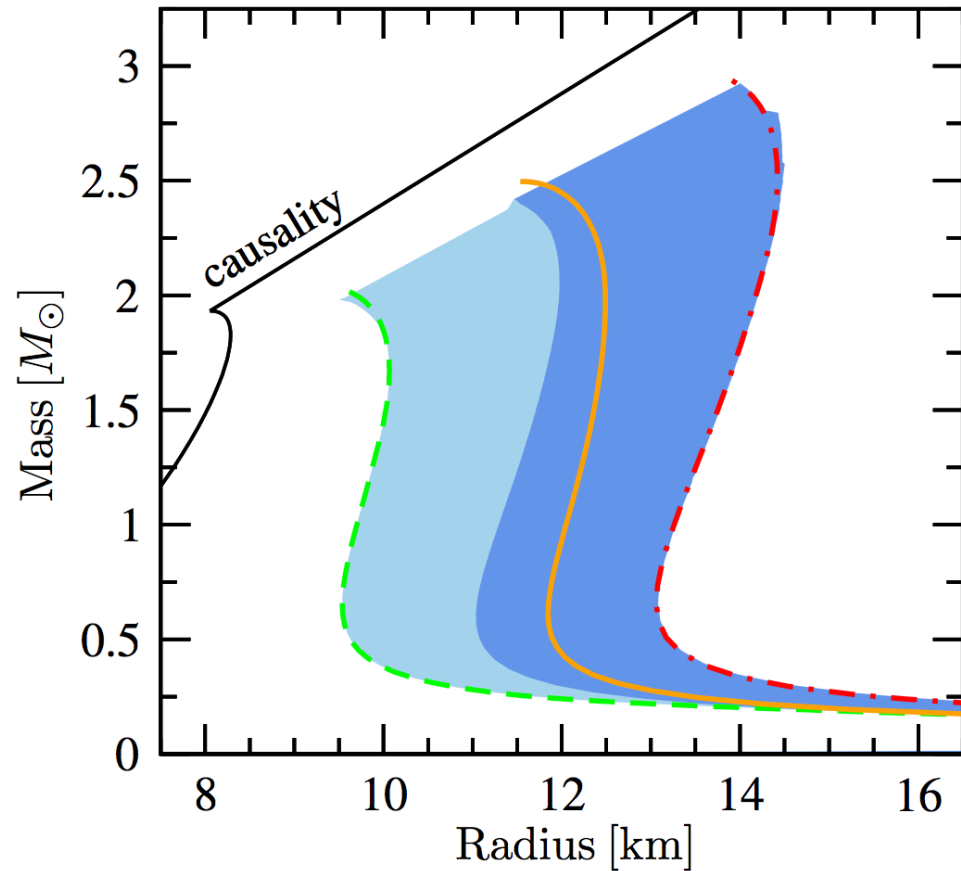
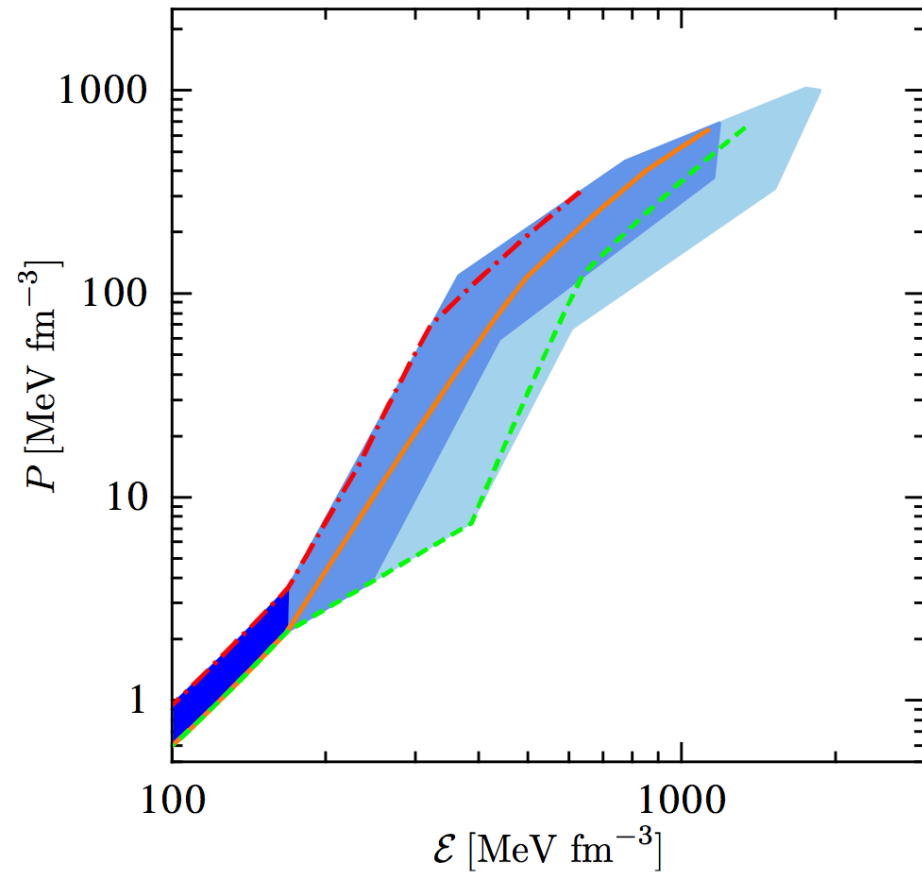
interpolating between **neutron matter calculations** and **pQCD** gives consistent EOS band [Kurkela et al., ApJ \(2014\)](#)



Representative equations of state

all EOS for cold matter in beta equilibrium should go through our band

constructed 3 representative EOS for users: **soft**, **intermediate**, **stiff**



Neutron-star mergers and gravitational waves

explore sensitivity to neutron-rich matter in neutron-star merger predictions for gravitational-wave signal, including NP uncertainties

Bauswein, Janka, PRL (2012)

Bauswein, Janka, Hebeler, AS, PRD (2012)

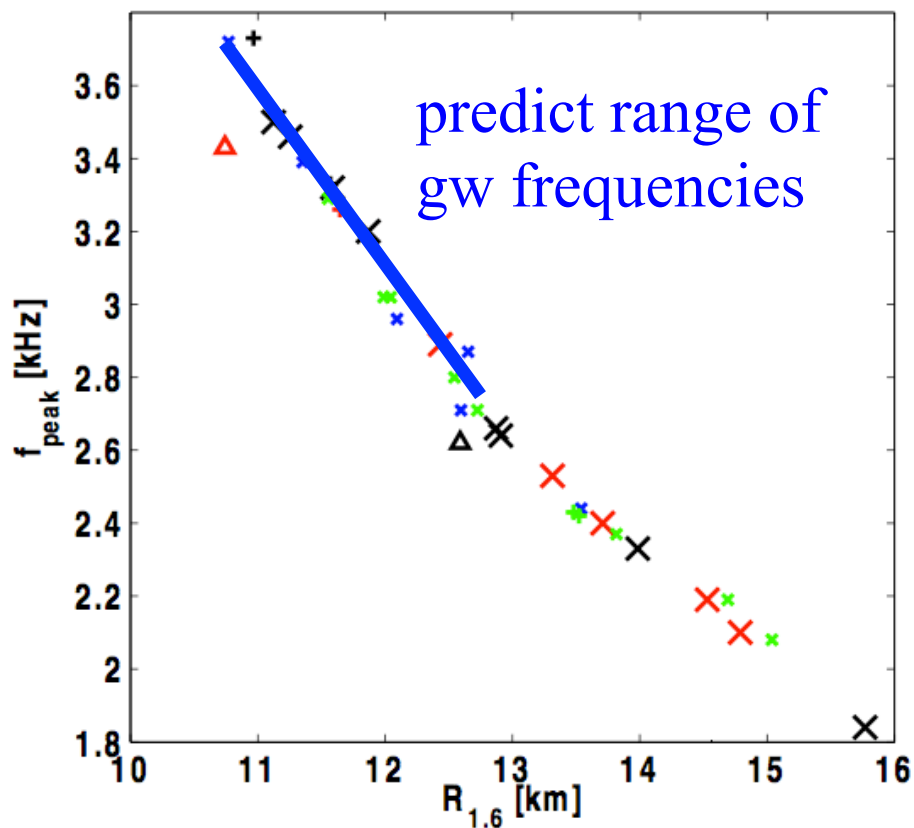
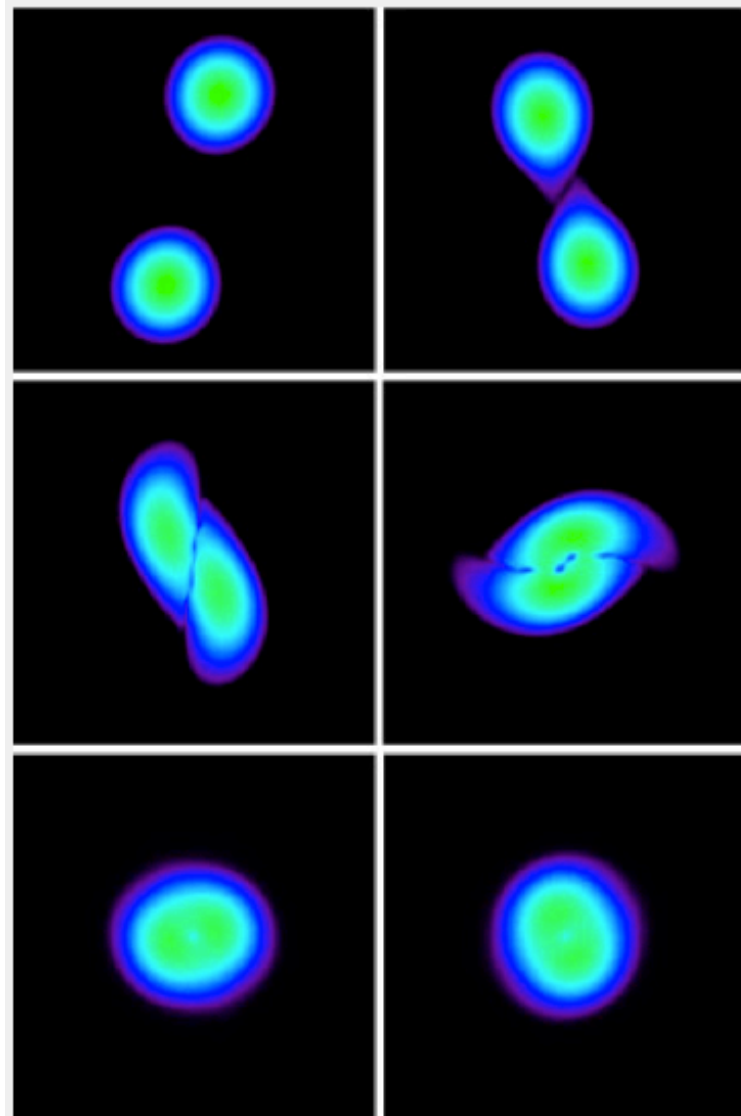


FIG. 10: Peak frequency of the postmerger GW emission versus the radius of a nonrotating NS with $1.6 M_{\odot}$ for different EoSs. Symbols have the same meaning as in Fig. 8.

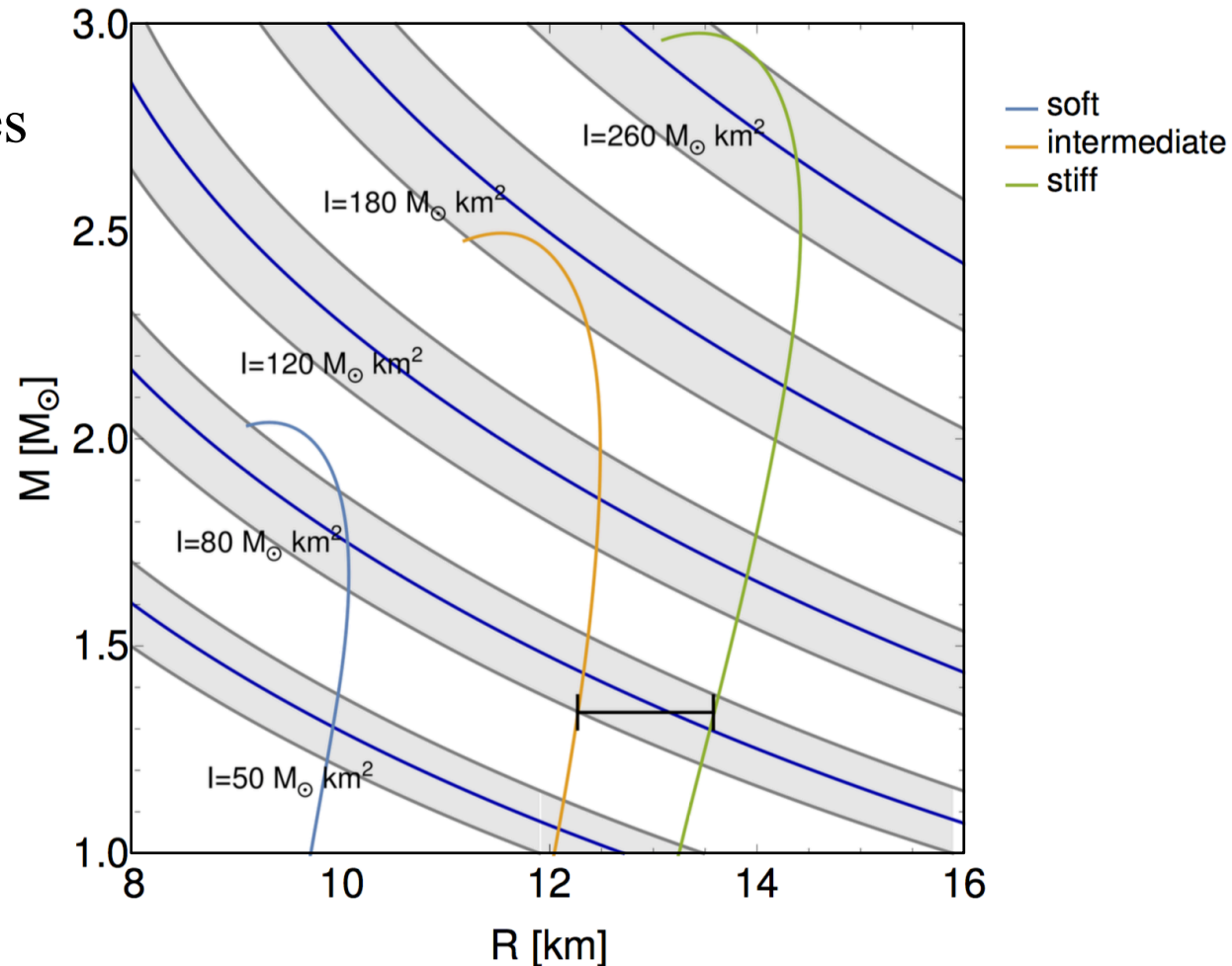


Radius constraints from moment of inertia Svenja Greif et al., in prep.

candidate neutron star:

PSR J0737-3039 $M=1.35 M_{\text{sun}}$

10% measurement of
moment of inertia reduces
radius range by 1/2



Summary

Chiral EFT interactions provide powerful constraints for dense matter: especially for neutron-rich matter up to around saturation density

Combined with heaviest neutron star observations limits radius to 9.7-13.9 km for $M=1.4 M_{\text{sun}}$

Can be further constrained with heavier neutron stars, extending EOS to higher densities, moment of inertia

Neutron-rich calcium isotopes present test-bench for nuclear forces: Energies, shell structure, charge radii
first constraints on neutron skin from ^{48}Ca dipole polarizability

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