

# Quarkonium-nucleus bound states

## — Chromopolarizability and color van der Waals forces



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**Modern Exotic Hadrons**  
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# Outline

- Motivation
- From models (1990) to a lattice simulation (2015)
- Other interesting bound states:  $D$ –nuclei,  $D^*\Delta$
- Experimental perspective
- EFT approach: polarizability & van der Waals forces
- Perspectives

# Collaborators

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- J. Haidenbauer
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- A. Sibirtsev
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- J. Tarrús-Castellá
- L. Tolos
- K. Tsushima
- A. Vairo
- A. Valcarce
- D. Wilson

# Charm in matter

- Understanding of the nuclear force, role of glue
- $J/\Psi$ ,  $\eta_c$ , ... : color polarizability, van der Waals force
- D-mesons in medium: chiral-symmetry restoration
- Charm hypernuclei
- Quark-gluon plasma

Experiments ongoing and underway:

LHC, RHIC, JLab @ 12 GeV, JPARC, Fair, NICA

# Charmonium in nuclear matter

## — an exotic nuclear state

Brodsky, Schmidt & de Téramond, PRL 64, 1011 (1990)

- Nucleons and charmonium have no valence quarks in common
- Interaction has to proceed via gluons – QCD van der Waals
- No Pauli Principle – no short-range repulsion
- Also, binding via D,D\* meson loop - interaction with nucleons

$$BE \sim 10 - 20 \text{ MeV}$$

GK, A. W. Thomas & K. Tsushima PLB 697, 136 (2011)  
K. Tsushima, D. Lu, GK & A. W. Thomas PRC 83, 065208 (2011)

**Nuclear-Bound Quarkonium**Stanley J. Brodsky and Ivan Schmidt<sup>(a)</sup>*Stanford Linear Accelerator Center, Stanford University, Stanford, California 94309*

Guy F. de Téramond

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(Received 25 September 1989)

We show that the QCD van der Waals interaction due to multiple-gluon exchange provides a new kind of attractive nuclear force capable of binding heavy quarkonia to nuclei. The parameters of the potential are estimated by identifying multigluon exchange with the Pomeron contributions to elastic meson-nucleon scattering. The gluonic potential is then used to study the properties of  $c\bar{c}$  nuclear-bound states. In particular, we predict bound states of the  $\eta_c$  with  ${}^3\text{He}$  and heavier nuclei. Production modes and rates are also discussed.

PACS numbers: 21.90.+f, 12.40.-y, 21.30.+y, 25.10.+s

**Variational calculation  
of binding energy**

$$V_{(c\bar{c})N}(r) = -\frac{\alpha}{r} e^{-\mu r}$$

TABLE I. Binding energies  $\epsilon = |\langle H \rangle|$  of the  $\eta_c$  to various nuclei, for unscreened and partially screened potentials; all masses are given in GeV. The data for  $\langle R_A^2 \rangle^{1/2}$  (in  $\text{GeV}^{-1}$ ) are from Ref. 10.

$A$	$\langle R_A^2 \rangle^{1/2}$	$\mu$	$m_{\text{red}}$	Unscreened		$\langle H \rangle$	Partially screened		
				$\alpha$	$\gamma$		$\alpha$	$\gamma$	$\langle H \rangle$
1	3.9	0.60	0.715	0.59		> 0	0.42		> 0
2	10.7	0.23	1.15	0.172		> 0	0.122		> 0
3	9.5	0.26	1.45	0.327	0.40	-0.019	0.231	0.24	-0.003
4	8.2	0.30	1.66	0.585	0.92	-0.143	0.414	0.62	-0.051
6	11.2	0.22	1.95	0.470	0.89	-0.128	0.332	0.61	-0.050
9	11.2	0.22	2.20	0.705	1.53	-0.407	0.499	1.07	-0.179

# Possible production processes

TABLE II. Kinematics for the production of  $\eta_c$ -nucleus bound states. All quantities are given in GeV.

Process	$\epsilon$	$p_{\text{c.m.}}$	$p_1^{\text{lab}}$
$\gamma^3\text{He} \rightarrow ({}^3\text{He} \eta_c)$	0.020	2.20	4.52
$pd \rightarrow ({}^3\text{He} \eta_c)$	0.020	2.48	7.64
$\bar{p} {}^4\text{He} \rightarrow ({}^3\text{H} \eta_c)$	0.020	1.48	2.30
$\gamma {}^4\text{He} \rightarrow ({}^4\text{He} \eta_c)$	0.120	2.24	3.96
$n {}^3\text{He} \rightarrow ({}^4\text{He} \eta_c)$	0.120	2.60	6.09
$dd \rightarrow ({}^4\text{He} \eta_c)$	0.120	2.71	9.51

## Comment on “Nuclear-Bound Quarkonium”

David A. Wasson

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### Smearing of the interaction over the nuclear volume

$$V_{(c\bar{c})A}(r) = \int d^3r' V_{(c\bar{c})N}(r - r')\rho_A(r')$$

$$\int d^3r' \rho_A(r') = A$$

$A$	$\epsilon$ [MeV]	$\langle r^2 \rangle^{1/2}$ [fm]
3	- 0.8	3.5
4	- 5.0	1.9
12	- 13	1.7
40	- 19	2.0
200	- 27	3.1

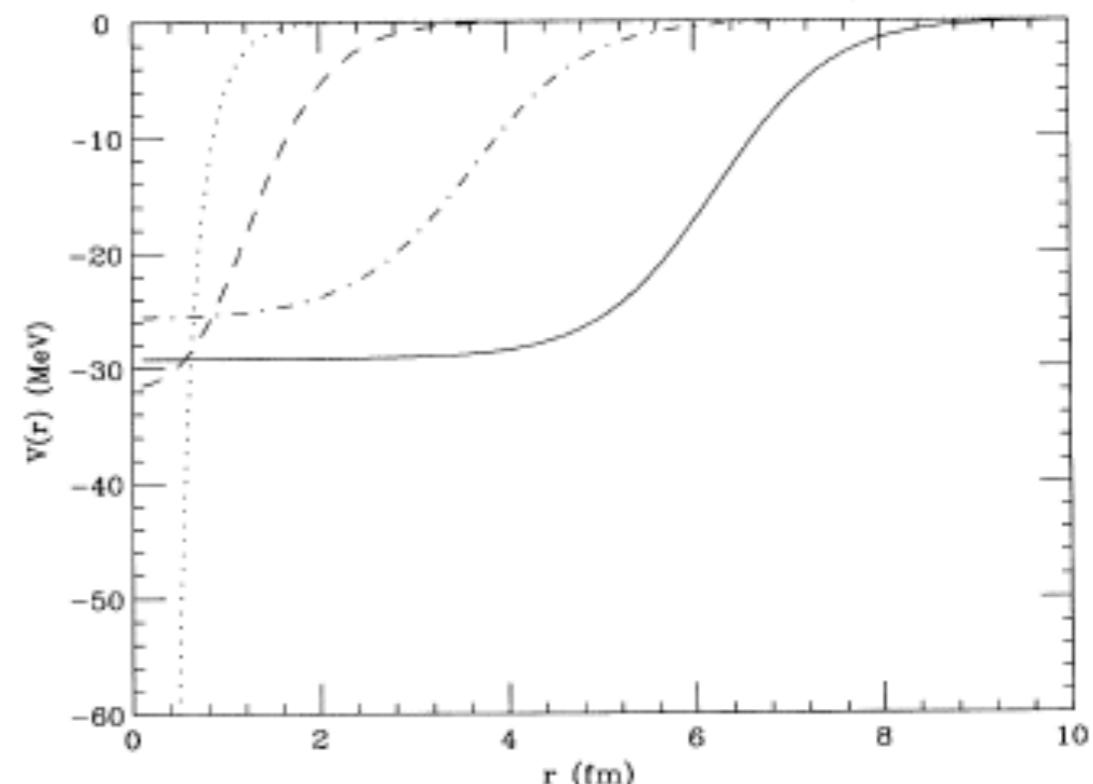


FIG. 1. Effective charmonium-nucleus potentials for various  $A$ . The dotted line is the  $A=1$  result given by Eq. (1) and the dashed line is the  $A=4$ , the dash-dotted line is the  $A=40$ , and the solid line is the  $A=200$  results predicted by Eq. (2).

## A QCD calculation of the interaction of quarkonium with nuclei

Michael Luke, Aneesh V. Manohar and Martin J. Savage

*Department of Physics 0319, University of California, San Diego, 9500 Gilman Drive, La Jolla, CA 92093-0319, USA*

### Binding to nuclear matter

$\Upsilon, \eta_c$  :  $\epsilon \simeq -2$  to  $-4$  MeV

$J/\Psi$  :  $\epsilon \simeq -8$  to  $-11$  MeV

$\psi'(2s)$  :  $\epsilon \simeq 700$  MeV

}

less reliable

# J/ $\Psi$ binding to nuclei

Generically: two independent mechanisms

- Second order stark effect – octet intermediate state  
van der Waals force
- D,D\* meson-loop – color singlet intermediate state  
D mesons interact with the nuclear mean fields

# Bhanot-Peskin theory

- van der Waals force (second order Stark effect)

J/ $\Psi$  as a small color electric dipole

$$\Delta m_\psi(\rho_B) = -\frac{1}{9} \int dk^2 \left| \frac{\partial \psi(k)}{\partial k} \right|^2 \frac{k}{k^2/m_c + \epsilon} \langle \alpha_s E^2 / \pi \rangle_N \frac{\rho_B}{2m_N}$$

$\psi(k)$  : charmonium wave function

$\rho_B$  : nuclear density

$m_c, m_N$  : masses charm quark and nucleon

$\epsilon = 2m_c - m_\psi$  : energy shift octet – charmonium

**Note:** intermediate state  
is noninteracting

# Numerical results

$$\langle \alpha_s E^2 / \pi \rangle_N = 0.5 \text{ GeV}^2$$

$\psi$  : Gaussian

$\langle r^2 \rangle$  : from Cornell potential model

$$\Delta m_\psi = -8 \text{ MeV}$$

at normal nuclear  
matter density

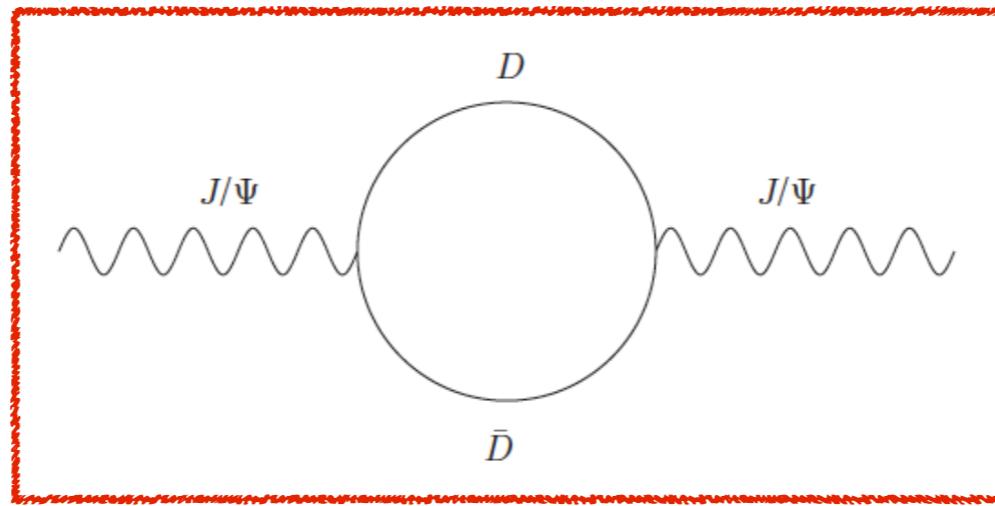
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Sibirtsev & Voloshin, PRD 71, 076005 (2005)

J/ $\Psi$  N cross section > 17 mb

$$\Delta m_\psi = -21 \text{ MeV}$$

# $D, D^*$ -meson loops



Calculate loop with effective Lagrangians

- need coupling constants & form factors
- need medium dependence of  $D$  masses

# Is $J/\psi$ -nucleon scattering dominated by the gluonic van der Waals interaction? <sup>1</sup>

Stanley J. Brodsky <sup>a</sup>, Gerald A. Miller <sup>a,2,b</sup>

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<sup>b</sup> National Institute for Nuclear Theory, Box 35150, University of Washington, Seattle, WA 98195-1560, USA

Received 17 July 1997

Editor: M. Dine

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## Abstract

The gluon-exchange contribution to  $J/\psi$ -nucleon scattering is shown to yield a sizeable scattering length of about -0.25 fm, which is consistent with the sparse available data. Hadronic corrections to gluon exchange which are generated by  $\rho\pi$  and  $D\bar{D}$  intermediate states of the  $J/\psi$  are shown to be negligible. We also propose a new method to study  $J/\psi$ -nucleon elastic scattering in the reaction  $\pi^+ d \rightarrow J/\psi pp$ . © 1997 Elsevier Science B.V.

# Hadron loops: General theorems and application to charmonium

T. Barnes<sup>1,2,\*</sup> and E. S. Swanson<sup>3,†</sup>

<sup>1</sup>*Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA*

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(Received 7 December 2007; published 14 May 2008)

TABLE III. Mass shifts (in MeV) and  $c\bar{c}$  probabilities for low-lying charmonium states due to couplings to two-meson continua. This one-loop estimate sets the unperturbed bare masses to the experimental values and assumes  $^3P_0$  model and SHO wave function parameters  $\gamma = 0.35$  and  $\beta = 0.5$  GeV and quark mass ratios  $r_n = m_n/m_c = 0.33/1.5$  and  $r_s = m_s/m_c = 0.55/1.5$ .

Bare $c\bar{c}$ state		Mass shifts by channel, $\Delta M_i$ (MeV)						$P_{c\bar{c}}$	
Multiplet	State	$DD$	$DD^*$	$D^*D^*$	$D_s D_s$	$D_s D_s^*$	$D_s^* D_s^*$	Total	
$1S$	$J/\psi(1^3S_1)$	-23	-83	-132	-21	-76	-123	-457	0.69
	$\eta_c(1^1S_0)$	0	-114	-105	0	-106	-98	-423	0.73
$2S$	$\psi'(2^3S_1)$	-27	-84	-126	-19	-70	-113	-440	0.51
	$\eta'_c(2^1S_0)$	0	-118	-103	0	-102	-94	-416	0.61
$1P$	$\chi_2(1^3P_2)$	-40	-105	-144	-33	-88	-111	-521	0.49
	$\chi_1(1^3P_1)$	0	-127	-148	0	-90	-130	-496	0.52
	$\chi_0(1^3P_0)$	-57	0	-196	-34	0	-172	-459	0.58
	$h_c(1^1P_1)$	0	-149	-130	0	-118	-107	-504	0.52

# $D, D^*$ in medium

## Light quarks in $D$ mesons

- quark condensate changes for nonzero temperature and baryon density
- quark-model: masses of the  $D$  mesons change

# Quark condensate at finite T

— model independent result\*

For low temperatures:

$$\frac{\langle \bar{q}q \rangle_T}{\langle \bar{q}q \rangle} = 1 - \frac{\Sigma_\pi}{m_\pi^2 f_\pi^2} \rho_s^\pi(T)$$

$$\simeq 1 - \frac{T^2}{8f_\pi^2}$$

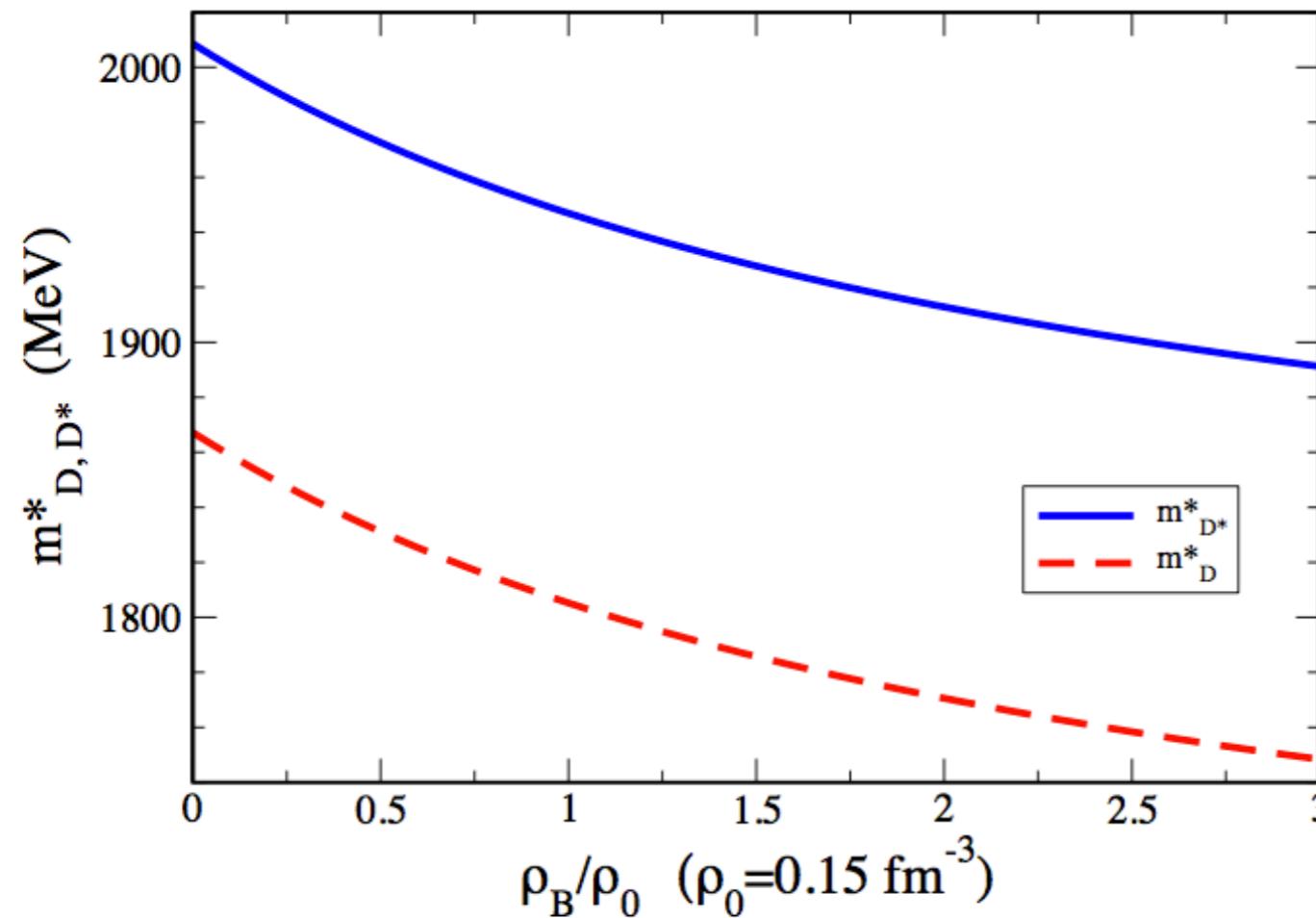
$$\Sigma_\pi = m_q \frac{dm_\pi}{dm_q}$$

$\rho_s^\pi(T)$  : scalar density  
of pions in medium

\* Gerber & Leutwyler (1989)

# D,D\* in medium

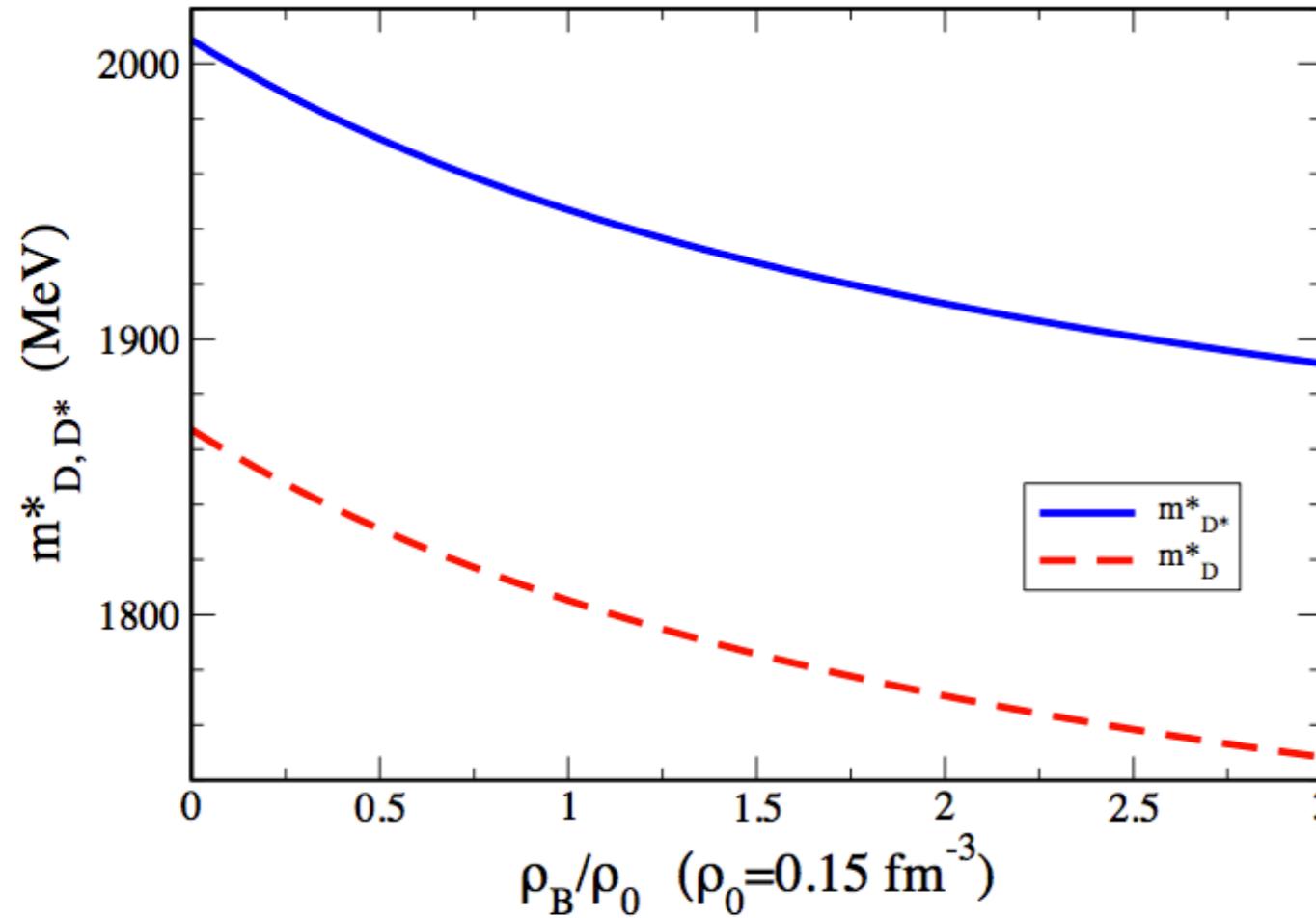
— QMC model



Low temperature and density:

# D,D\* in medium

— QMC model



Low temperature and density:

$$\langle \bar{q}q \rangle \simeq \left( 1 - \frac{T^2}{8f_\pi^2} - 0.3 \frac{\rho}{\rho_0} \right) \langle \bar{q}q \rangle_{\text{vac}}$$

# Effective Lagrangians

– SU(4) flavor symmetry for couplings

$$\mathcal{L}_{\psi DD} = ig_{\psi DD} \psi^\mu [\bar{D}(\partial_\mu D) - (\partial_\mu \bar{D}) D]$$

$$\mathcal{L}_{\psi DD^*} = \frac{g_{\psi DD^*}}{m_\psi} \varepsilon_{\alpha\beta\mu\nu} (\partial^\alpha \psi^\beta) \left[ (\partial_\mu \bar{D}^{*\nu}) D + \bar{D} (\partial_\mu D^{*\nu}) \right]$$

$$\begin{aligned} \mathcal{L}_{\psi D^* D^*} = & ig_{\psi D^* D^*} \left\{ \psi^\mu \left[ (\partial_\mu \bar{D}^{*\nu}) D_\nu^* - \bar{D}^{*\nu} (\partial_\mu D_\nu^*) \right] \right. \\ & + \left[ (\partial_\mu \psi^\nu) \bar{D}_\nu^* - \psi^\nu (\partial_\mu \bar{D}_\nu^*) \right] D^{*\mu} \\ & \left. + \bar{D}^{*\mu} [\psi^\nu (\partial_\mu D_\nu^*) - (\partial_\mu \psi^\nu) D_\nu^*] \right\} \end{aligned}$$

# J/Ψ in nuclear matter

J/Ψ self-energy:

$$i\Sigma_{\psi}^{D\bar{D}}(k^2) = -\frac{8}{3}g_{\psi D\bar{D}}^2 \int \frac{d^4q}{(2\pi)^4} F(q^2) \Delta_D(q) \Delta_{\bar{D}}(k-q)$$

$\Delta_D, \Delta_{\bar{D}}$  : propagators

$F(q^2)$  : form factors, extension of the mesons

Effective potential:

$$U_{\psi}(\rho_B) \equiv m_{\psi}^* - m_{\psi}$$

$$m_{\psi}^2 = \left(m_{\psi}^{(0)}\right)^2 + \Sigma_{\psi}^{D\bar{D}}(k^2 = m_{\psi}^2)$$

$$m_{\psi}^{*2} = \left(m_{\psi}^{(0)}\right)^2 + \Sigma_{\psi}^{*D\bar{D}}(k^2 = m_{\psi}^2)$$

# Structure of the mesons — form factors

$^3P_0$ — model

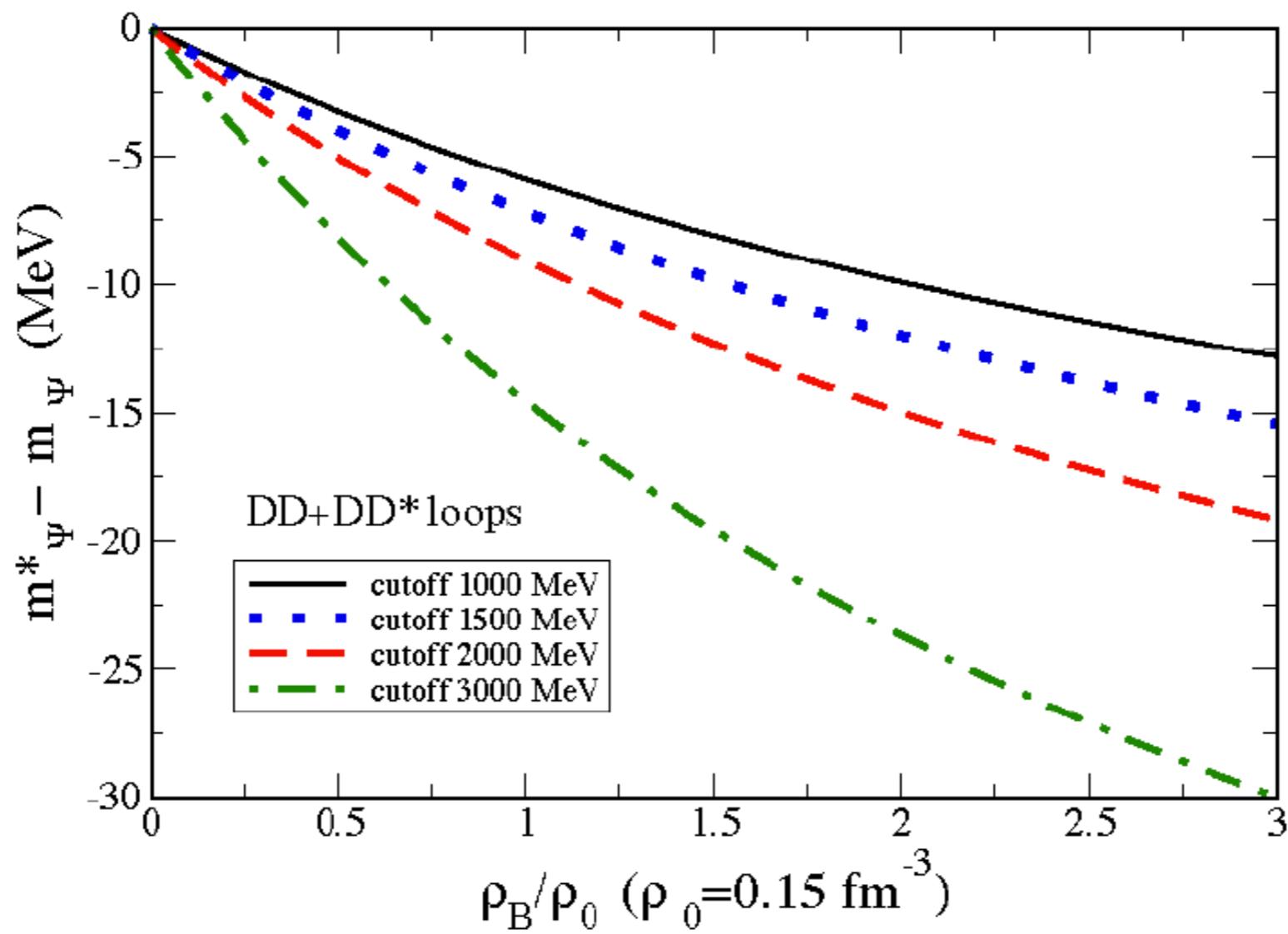
(E. Swanson)

$$F(q^2) = \gamma^2 \pi^{3/2} \frac{m_\psi^3}{\beta^3} \frac{2^6 r^3 (1 + r^2)^2}{(1 + 2r^2)^5} e^{-q^2/2\beta_D^2(1+2r^2)}, \quad r = \frac{\beta_\psi}{\beta_D}$$

Phenomenological

$$F(q^2) = \left[ \frac{\Lambda^2 + m_\psi^2}{\Lambda^2 + 4(q^2 + m_D^2)} \right]^2, \quad g_{\psi D\bar{D}} = 7.7$$

# J/ $\Psi$ in nuclear matter



# J/ $\Psi$ single-particle energies in nuclei

## — from Klein-Gordon equation

		$\Lambda_{D,D^*} = 1500 \text{ MeV}$	$\Lambda_{D,D^*} = 2000 \text{ MeV}$
		E (MeV)	E (MeV)
$^4_\Psi \text{He}$	1s	-4.19	-5.74
$^{12}_\Psi \text{C}$	1s	-9.33	-11.21
	1p	-2.58	-3.94
$^{16}_\Psi \text{O}$	1s	-11.23	-13.26
	1p	-5.11	-6.81
$^{40}_\Psi \text{Ca}$	1s	-14.96	-17.24
	1p	-10.81	-12.92
	1d	-6.29	-8.21
	2s	-5.63	-7.48
$^{90}_\Psi \text{Zr}$	1s	-16.38	-18.69
	1p	-13.84	-16.07
	1d	-10.92	-13.06
	2s	-10.11	-12.22
$^{208}_\Psi \text{Pb}$	1s	-16.83	-19.10
	1p	-15.36	-17.59
	1d	-13.61	-15.81
	2s	-13.07	-15.26

# Quarkonium-nucleus bound states from lattice QCD

S. R. Beane,<sup>1</sup> E. Chang,<sup>1,2</sup> S. D. Cohen,<sup>2</sup> W. Detmold,<sup>3</sup> H.-W. Lin,<sup>1</sup> K. Orginos,<sup>4,5</sup> A. Parreño,<sup>6</sup> and M. J. Savage<sup>2</sup>  
 (NPLQCD Collaboration)

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(Received 9 November 2014; published 11 June 2015)

Quarkonium-nucleus systems are composed of two interacting hadronic states without common valence quarks, which interact primarily through multigluon exchanges, realizing a color van der Waals force. We present lattice QCD calculations of the interactions of strange and charm quarkonia with light nuclei. Both the strangeonium-nucleus and charmonium-nucleus systems are found to be relatively deeply bound when the masses of the three light quarks are set equal to that of the physical strange quark. Extrapolation of these results to the physical light-quark masses suggests that the binding energy of charmonium to nuclear matter is  $B_{\text{phys}}^{\text{NM}} \lesssim 40 \text{ MeV}$ .

# Models

TABLE I. Estimates for the binding energies of charmonium to light nuclei and nuclear matter (in MeV) from selected models. A “\*” indicates the system is predicted to be unbound, while entries with center dots indicate that the system was not addressed.

Ref.	Binding energy (MeV)			Binding energy (MeV)	
	${}^3\text{He}$	$\eta_c$	${}^4\text{He}$	$\eta_c$	NM
[1]	19		140		*
[2]	0.8		5		27
[3]					10
[5]	*		*		9
[6]					5
[7]					5
[8]					18
					15.7



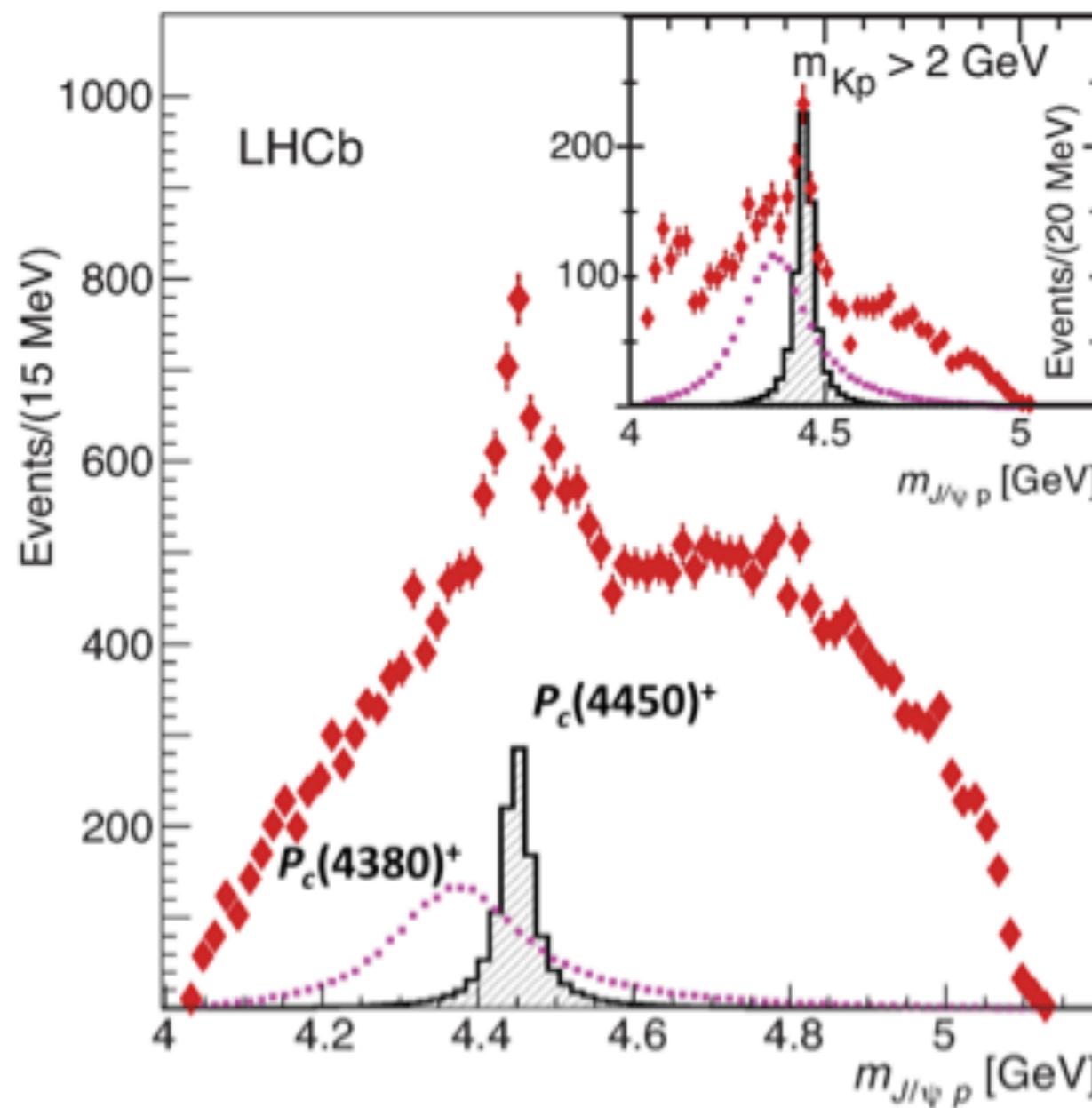
TABLE V. The binding energies (in MeV) of charmonium-nucleus systems calculated on the  $L = 24$  and  $32$  ensembles. The rightmost column shows the infinite-volume estimate, which, without results on the  $L = 48$  ensemble, is taken to be the binding calculated on the  $L = 32$  ensemble. The first and second sets of parentheses shows the statistical and quadrature-combined statistical plus systematic uncertainties, respectively.

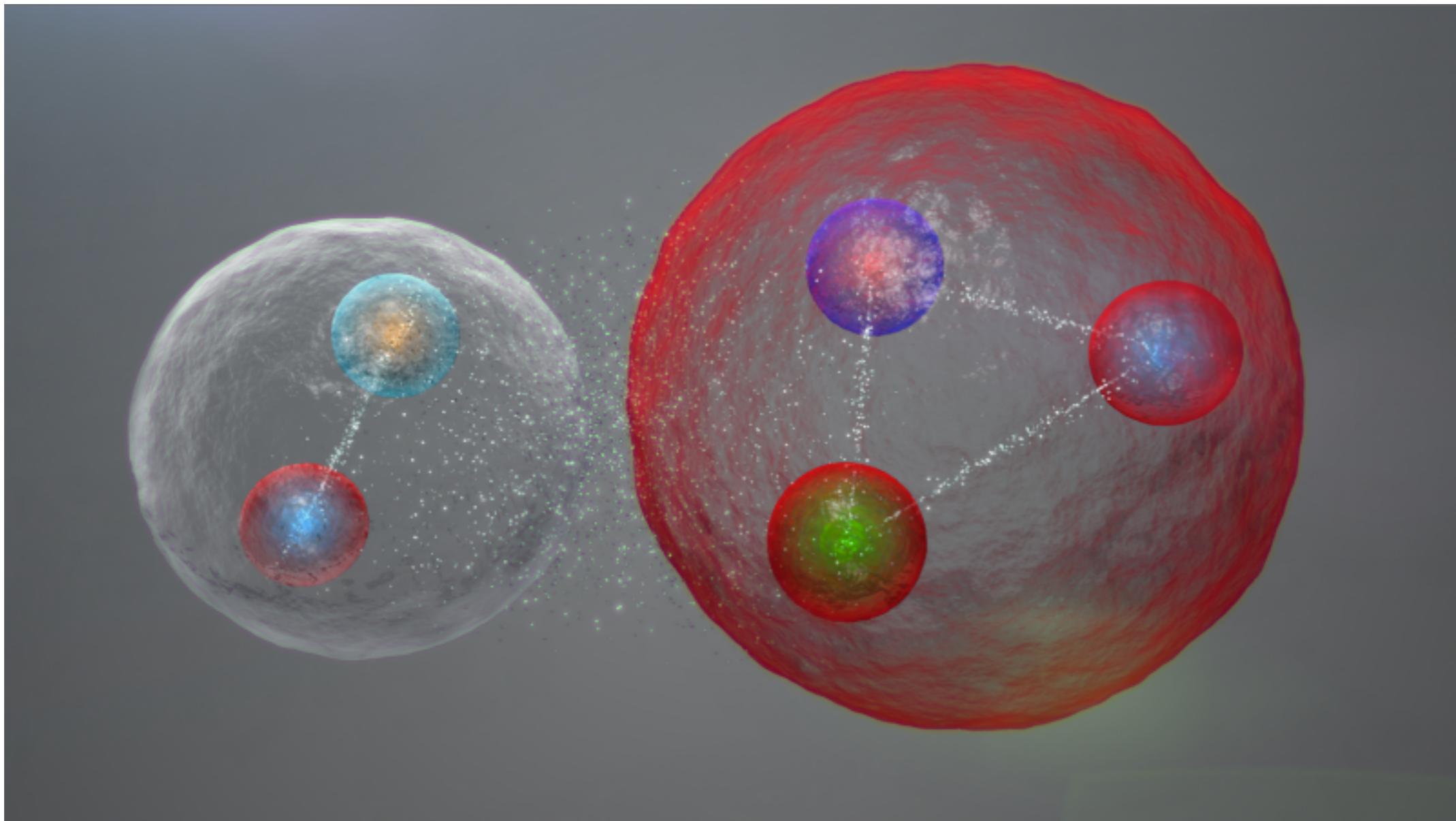
System	$24^3 \times 64$	$32^3 \times 64$	$L = \infty$
$N\eta_c$	17.9(0.4)(1.5)	19.8(0.7)(2.6)	19.8(2.6)
$d\eta_c$	39.3(1.3)(4.8)	42.4(1.1)(7.9)	42.4(7.9)
$p\bar{p}\eta_c$	37.8(1.1)(4.5)	41.5(1.0)(7.5)	41.5(7.6)
${}^3\text{He}\eta_c$	57.2(1.3)(8.3)	56.7(2.0)(9.4)	56.7(9.6)
${}^4\text{He}\eta_c$	70(02)(13)	56(06)(17)	56(18)
${}^4\text{He}J/\psi$	75.7(1.9)(9.4)	53(07)(18)	53(19)



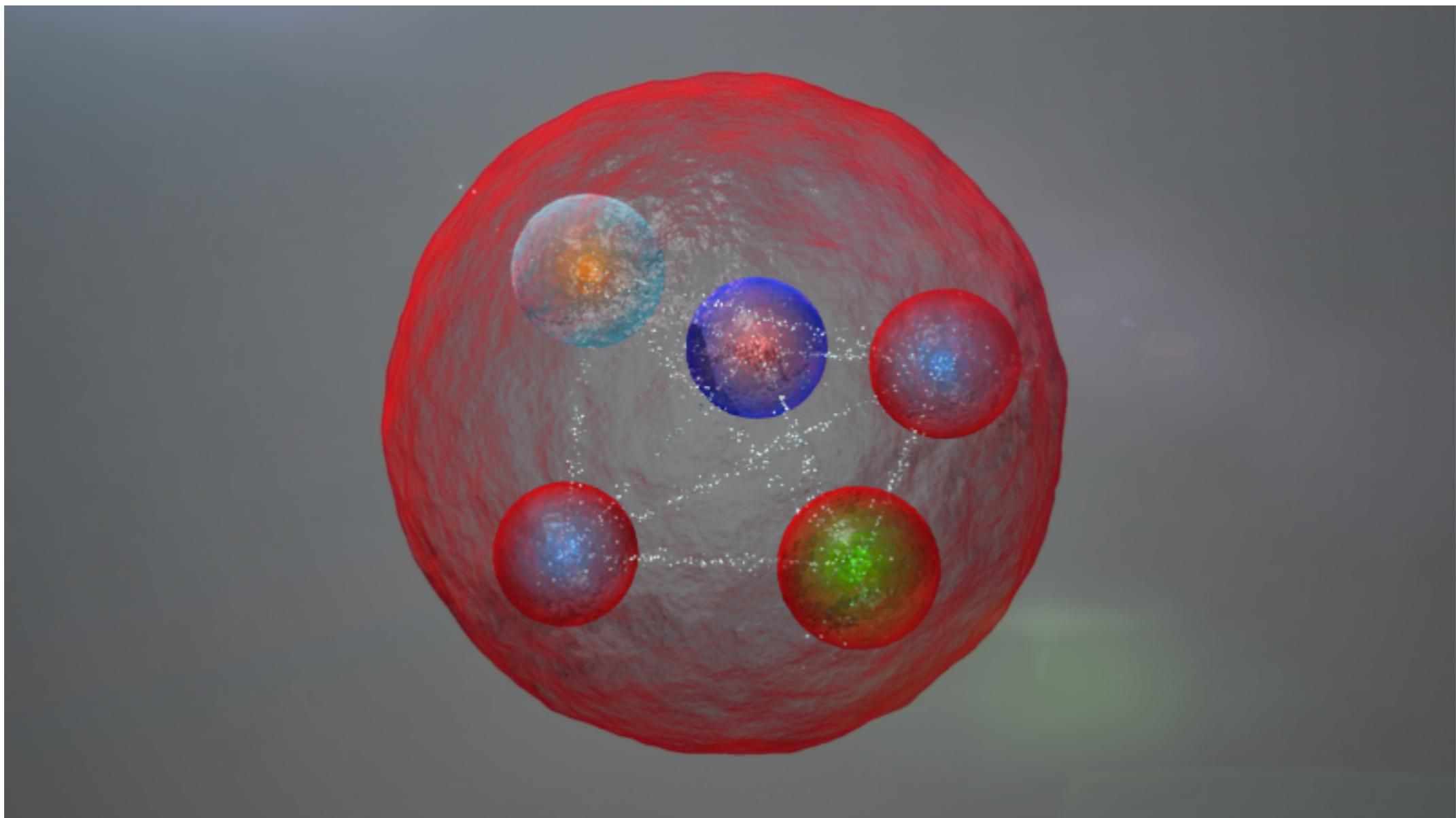
NPLQCD

# J/ $\Psi$ binding to proton?



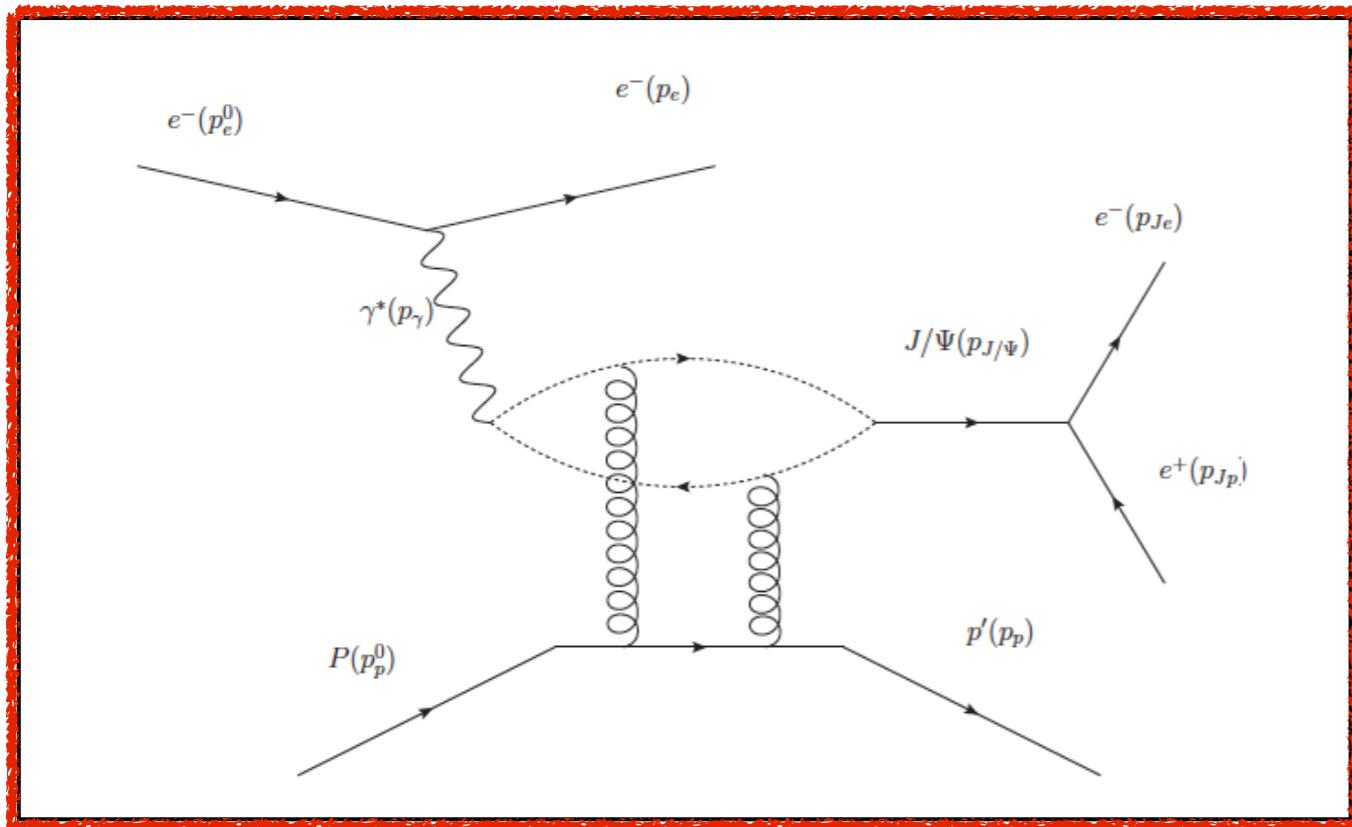


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# ATHENNA\* collaboration JLab @ 12 GeV

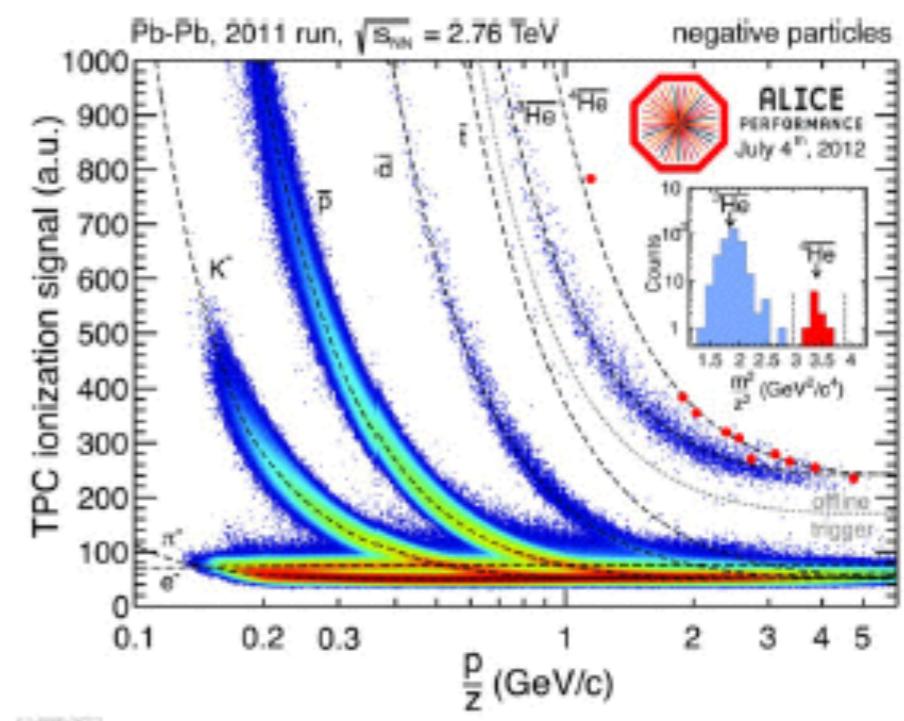
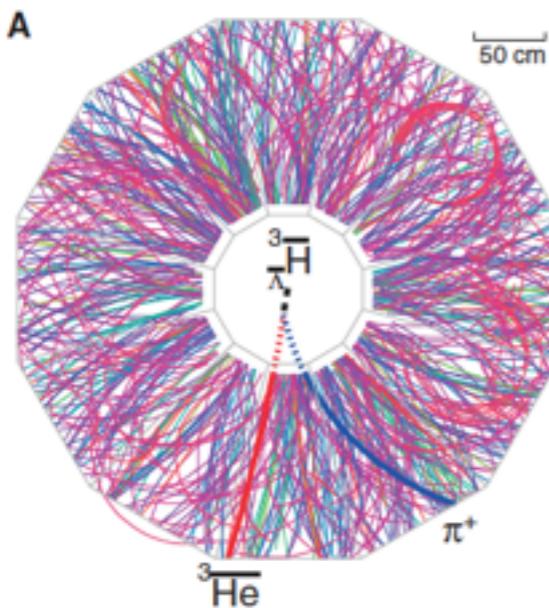
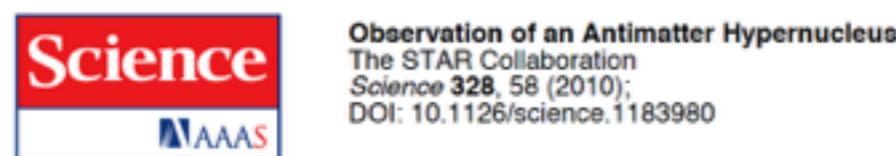


Z.-E. Meziani (Co-spokesperson/Contact)  
N. Sparveris (Co-spokesperson)  
Z. W. Zhao (Co-spokesperson)

\*A  $J/\Psi$  THreshold Electroproduction on the Nucleon and Nuclei Analysis

# How About coalescence at the LHC?

- Chances of a charmed hadron meeting one or two nucleons **not smaller** than of two antinucleons and one antihyperon meeting to form an antihypernucleus



Need to detect in coincidence  
the decay products

# D-mesons

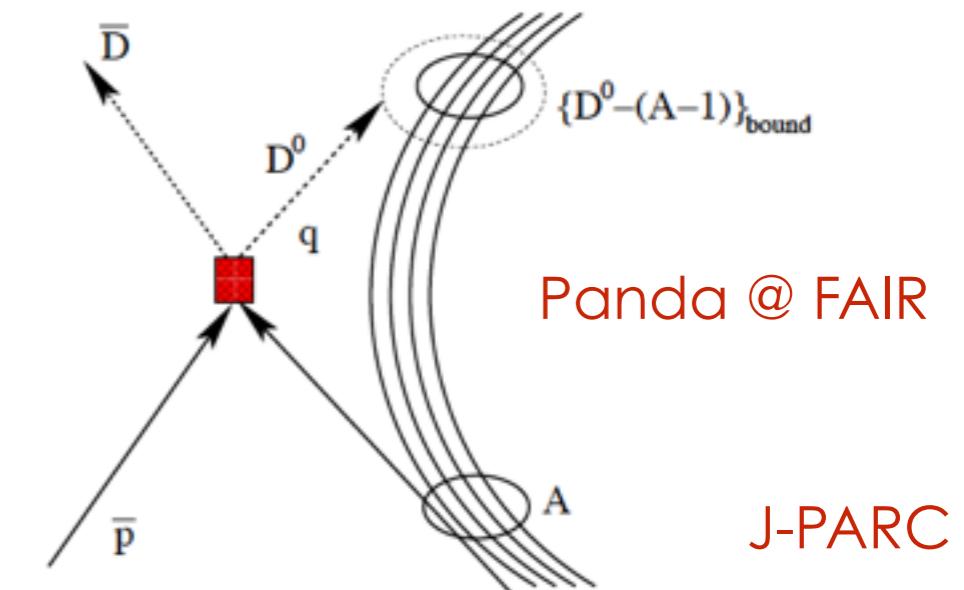
## — bound to nuclei

Quark-meson-coupling model  
- Hartree MFT\*, scalar + vector mean fields

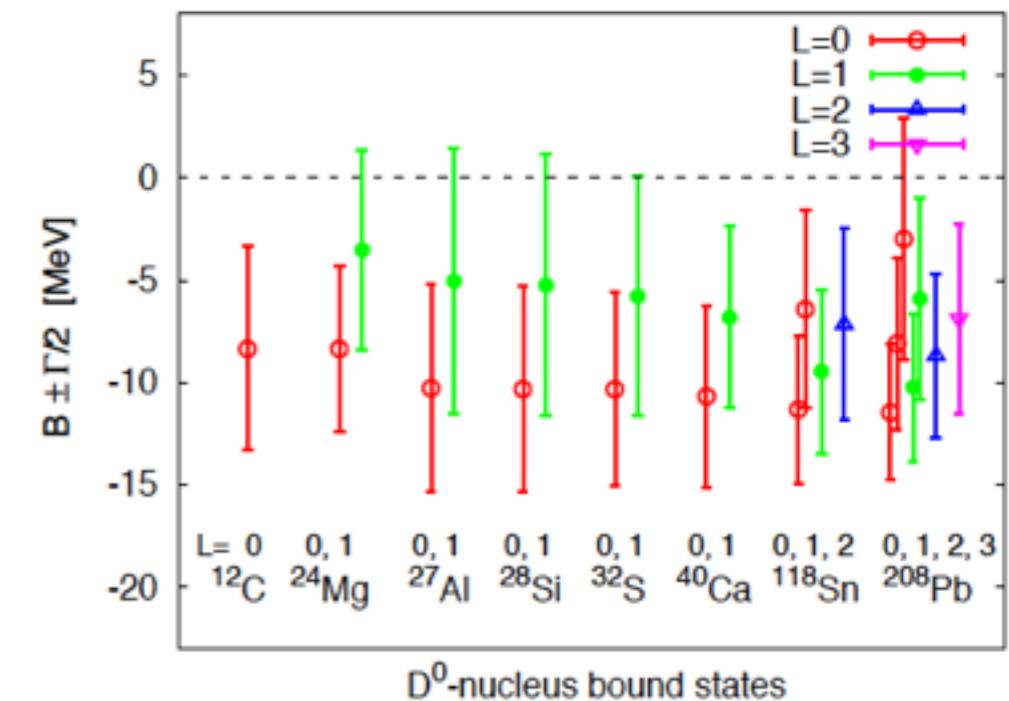
state	$\bar{D}^-$ $*V_{q\omega}$	$D^-$ $V_{q\omega}$	$D^-$ $V_{q\omega}$ No Coulomb	$\bar{D}^0$ $*V_{q\omega}$	$\bar{D}^0$ $V_{q\omega}$	$V_{q\omega}$
1s	-10.6	-35.2	-11.2	unbound	-25.4	-96.2
1p	-10.2	-32.1	-10.0	unbound	-23.1	-93.0
2s	-7.7	-30.0	-6.6	unbound	-19.7	-88.5

Review  
K. Saito et al. PPNP (2007)

\*Fock terms do not change much size of mean fields  
GK, K. Tsushima, T. Thomas



EFT HQSS  
- MFT, coupled channels



Review  
L. Tolos, Int. J. Mod. Phys. E (2013)

# $\text{DN}$ , $\text{D}\Delta$ states

## Chiral quark model\*

- constituent quarks
- confining potential
- OGE, OPE, OSE

Coupled channels - T. Caramés, A. Valcarce (2012)

	$T = 0$	$T = 1$	$T = 2$
$J = 1/2$	$N\bar{D} - N\bar{D}^*$	$N\bar{D} - N\bar{D}^* - \Delta\bar{D}^*$	$\Delta\bar{D}^*$
$J = 3/2$	$N\bar{D}^*$	$N\bar{D}^* - \Delta\bar{D} - \Delta\bar{D}^*$	$\Delta\bar{D} - \Delta\bar{D}^*$
$J = 5/2$		$\Delta\bar{D}^*$	$\Delta\bar{D}^*$

- In vacuum: very few DN bound states (Caramés & Valcarce)
- In medium: many become bound, combined effect of coupled channels and change of condensate

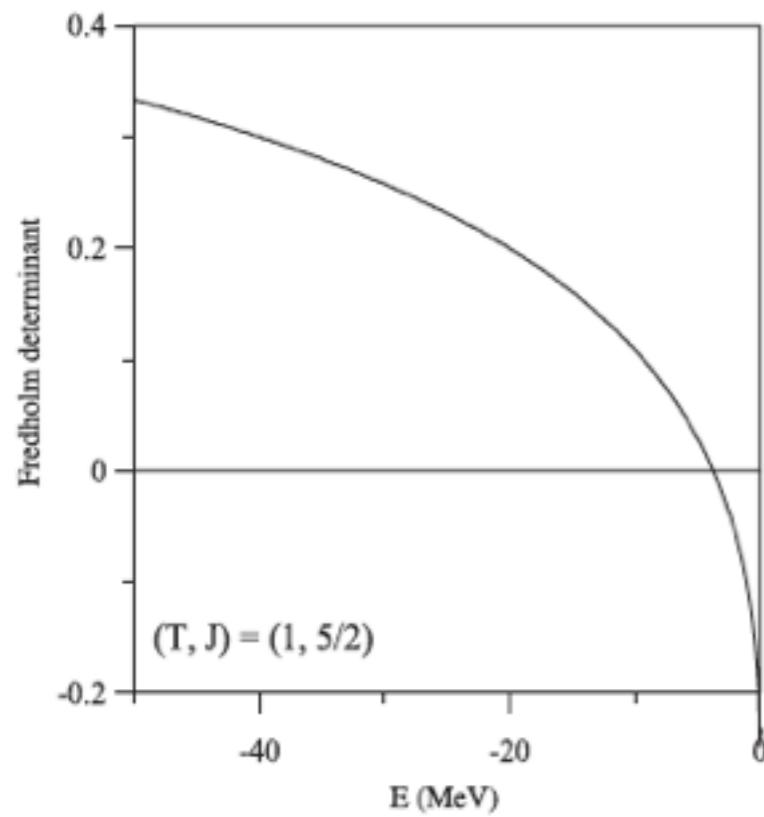
T. Caramés, C. E. Fontoura, GK, K. Tsushima, A. Valcarce (2015)

\*J. Vijande, F. Fernandez, A. Valcarce (2005)

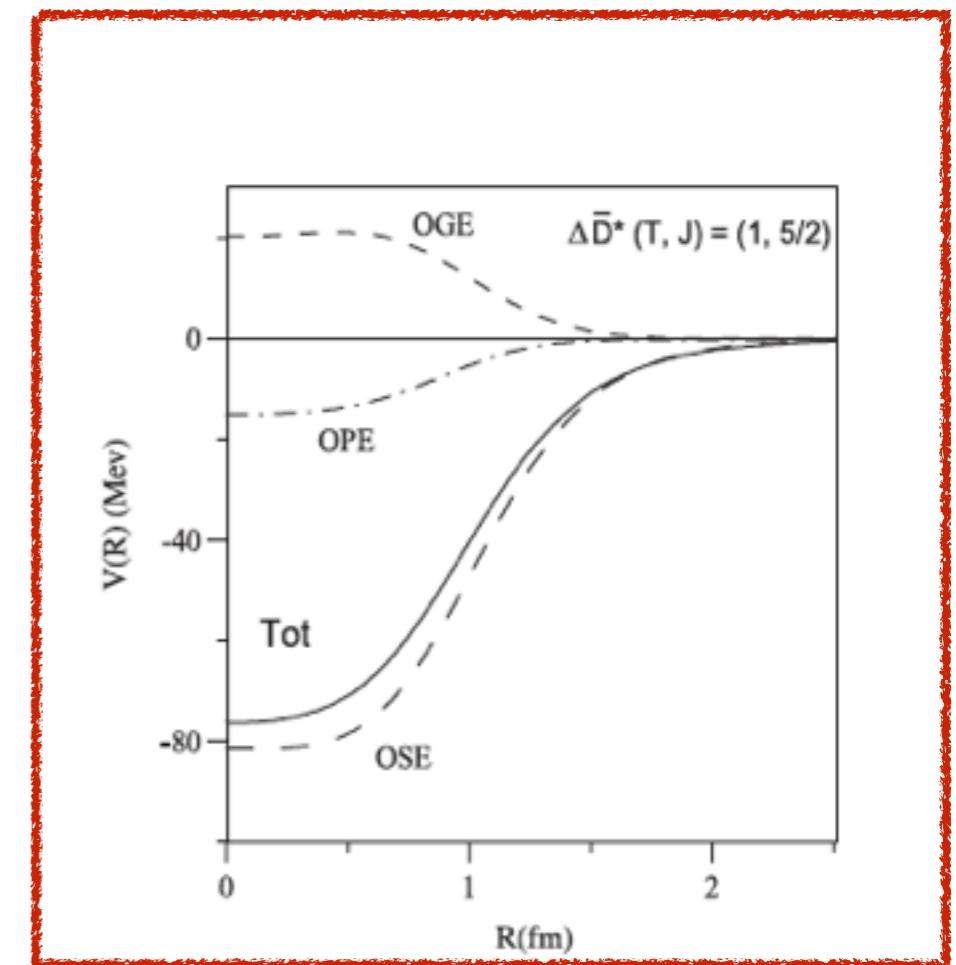
J. Segovia, A. M. Yasser, D. R. Entem, F. Fernandez (2008)

# $\bar{D}^* \Delta$ - an interesting molecular state

—  $(T, J^P) = (1, 5/2^-)$

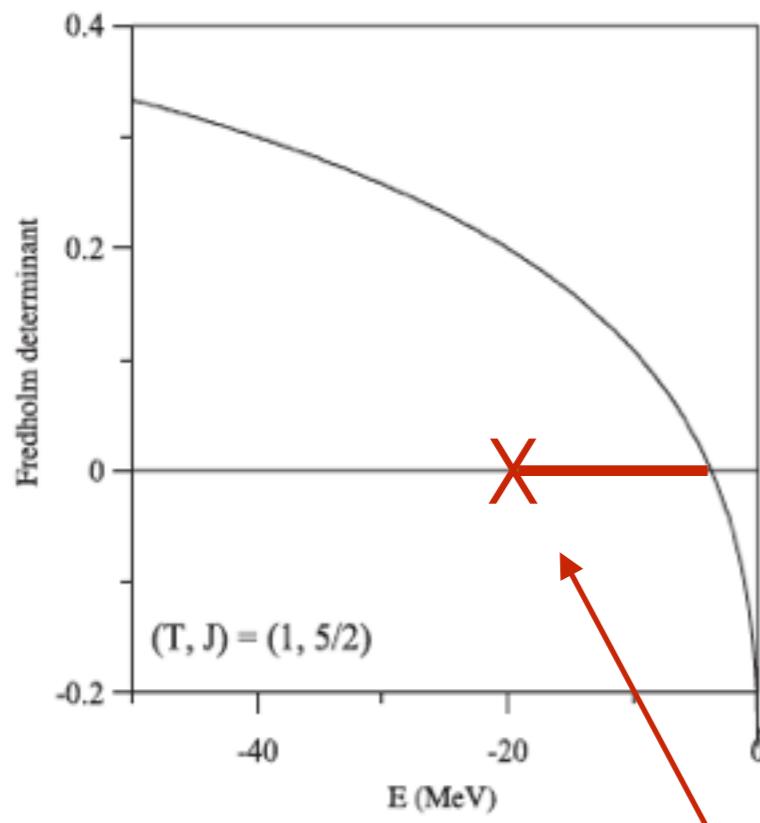


OSE dominates  
OGE & OPE cancel

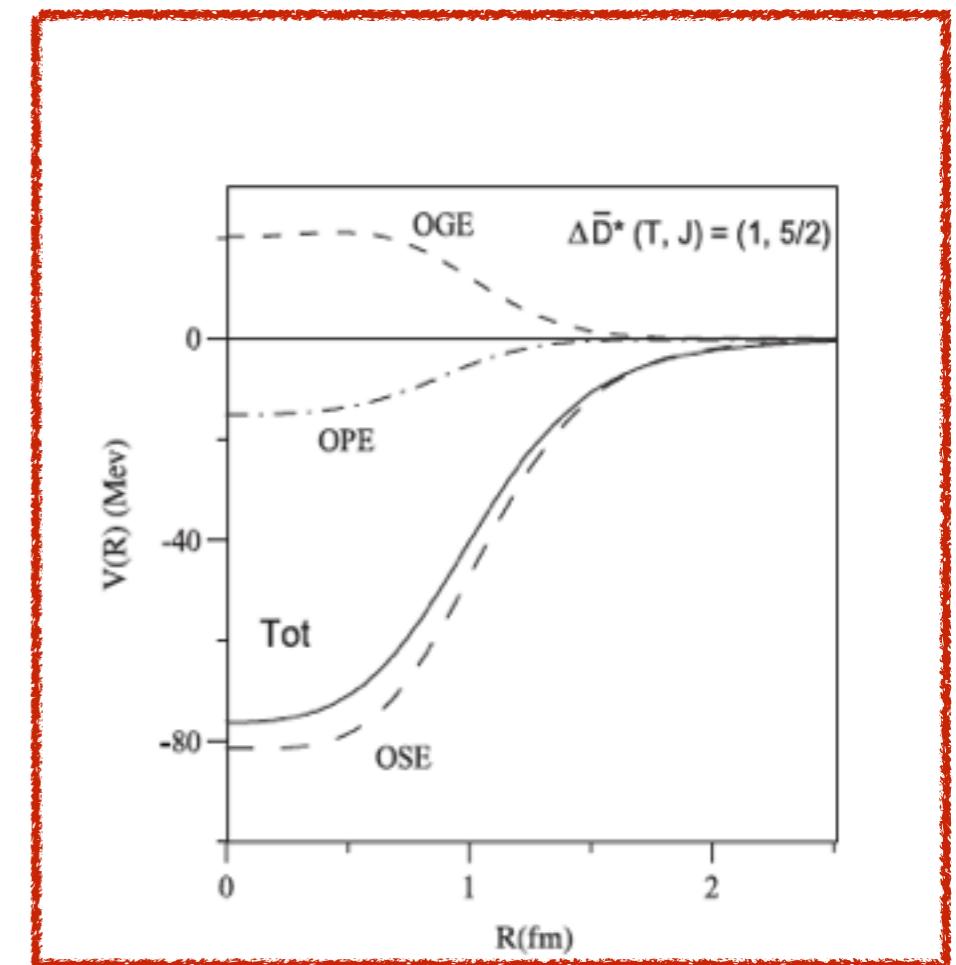


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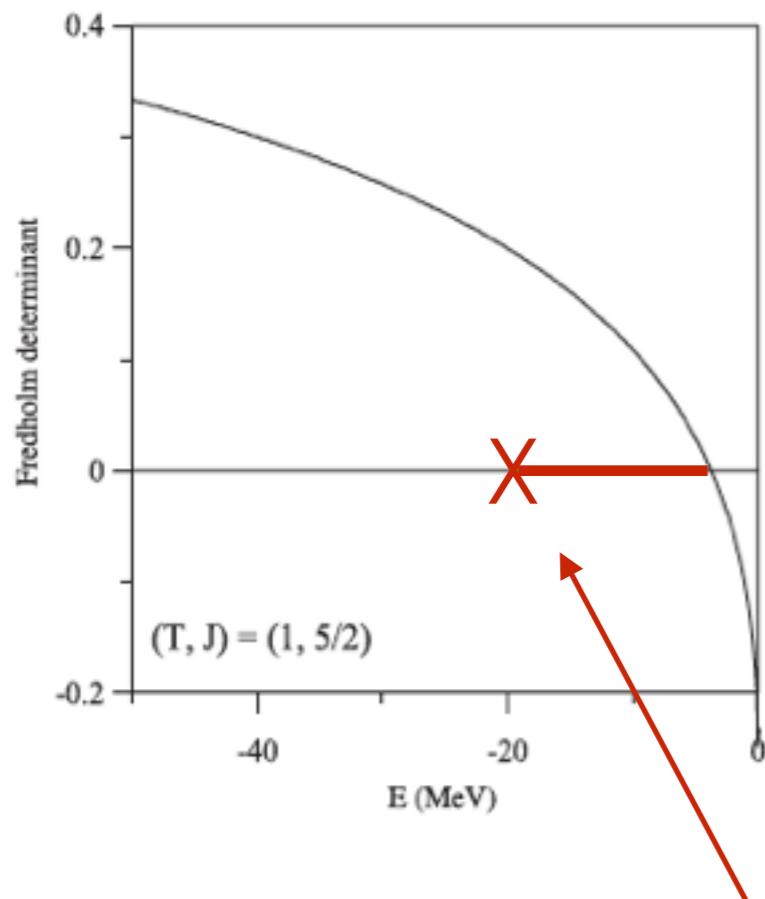


Drop of the condensate

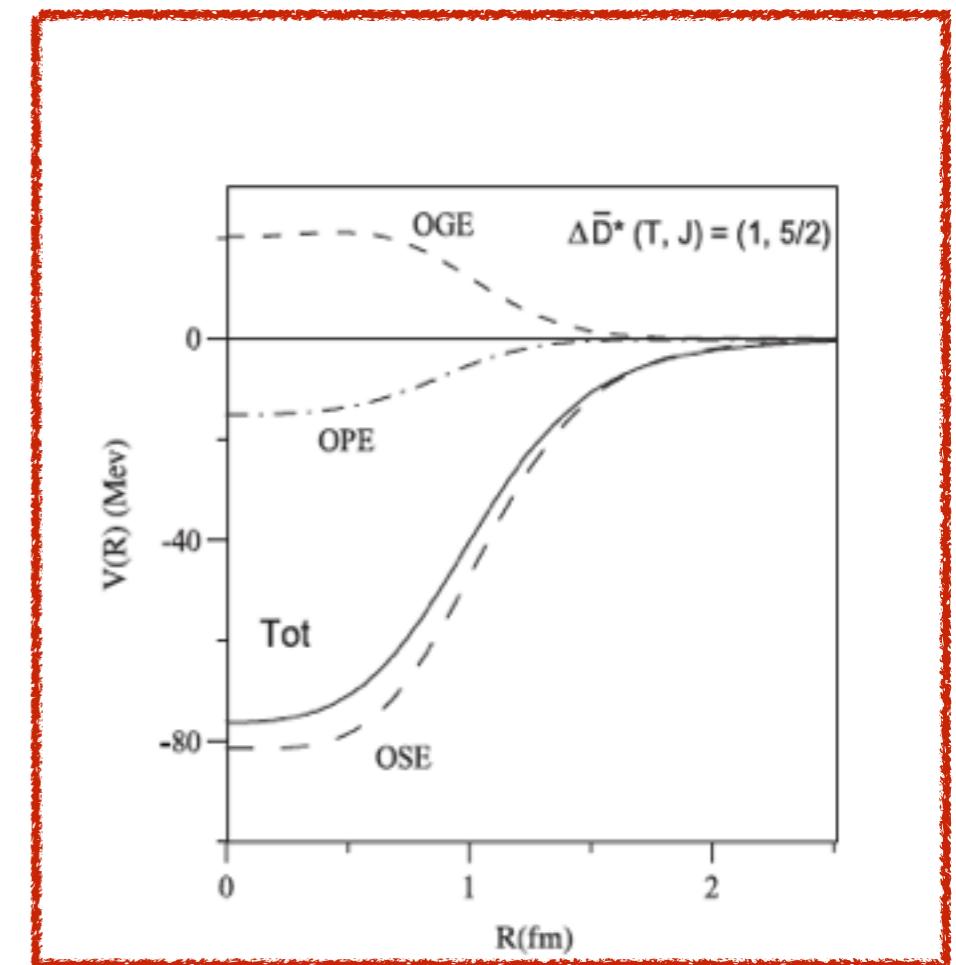
- OGE & OPE still cancel each other
- OSE, extended range, larger binding

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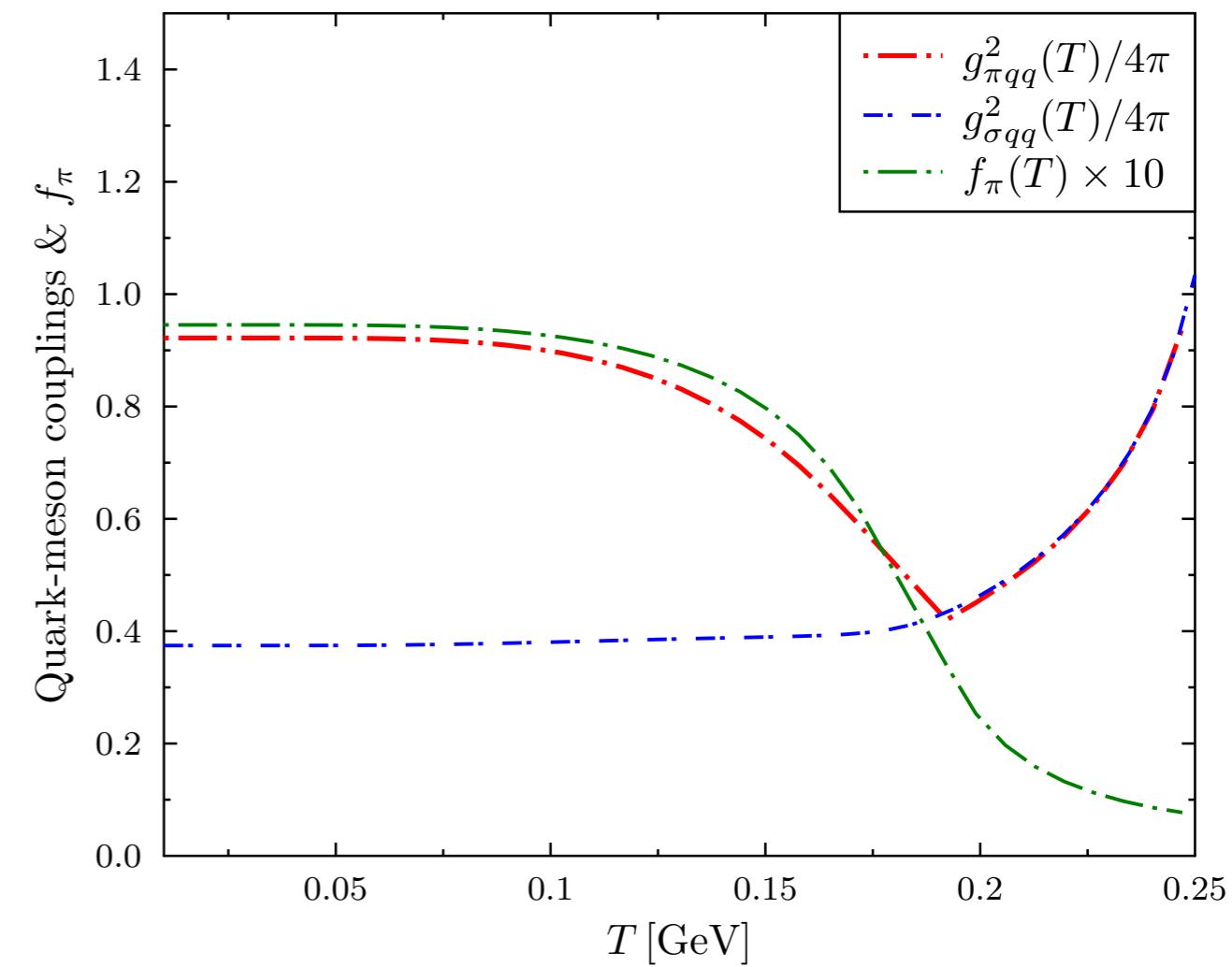
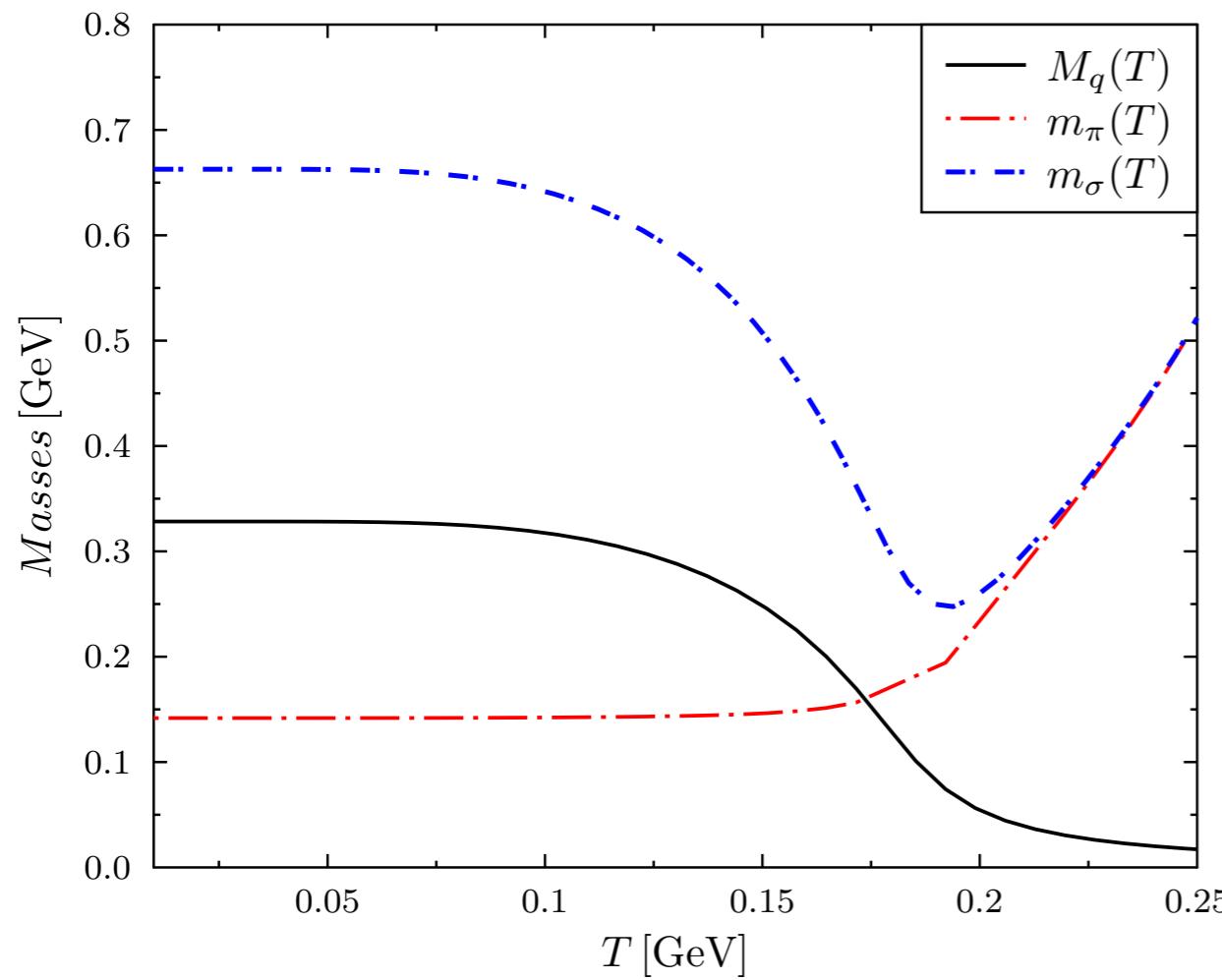
- OGE & OPE still cancel each other
- OSE, extended range, larger binding

Also,  $\Lambda_c(2940)^+$  as a  $D^*N$  bound state  
P. G. Ortega, D. Entem, F. Fernandez (2013)

# $\bar{D}^* \Delta$ - in medium

— ( $T, J^P$ ) =  $(1, 5/2^-)$

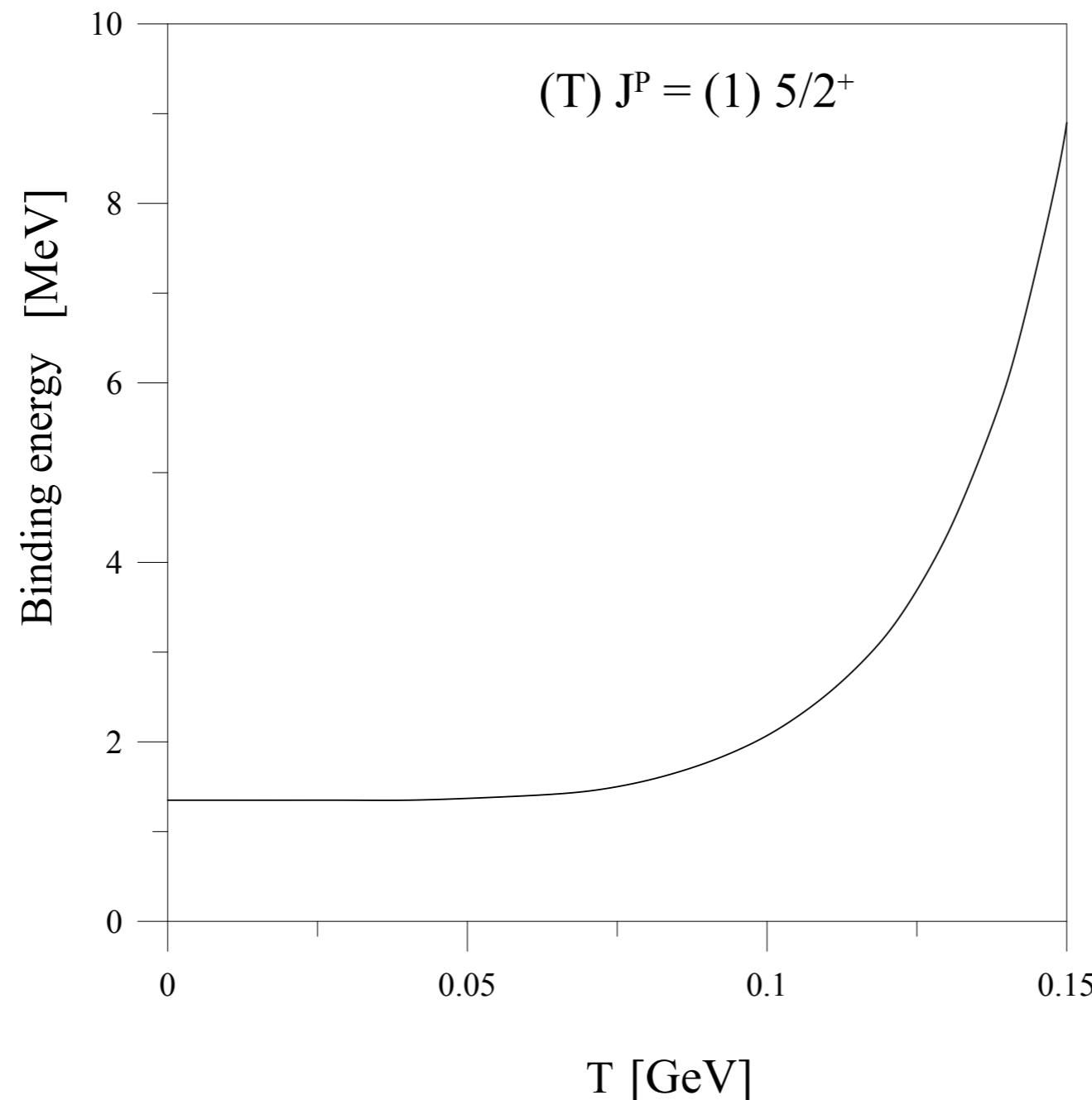
Input for the chiral quark model - NJL model



# $\bar{D}^* \Delta^-$ in medium

—  $(T, J^P) = (1, 5/2^-)$

Binding energy



Need crucial input  
— DN interaction

Need crucial input  
— DN interaction

— PANDA @ FAIR

Need crucial input  
— DN interaction

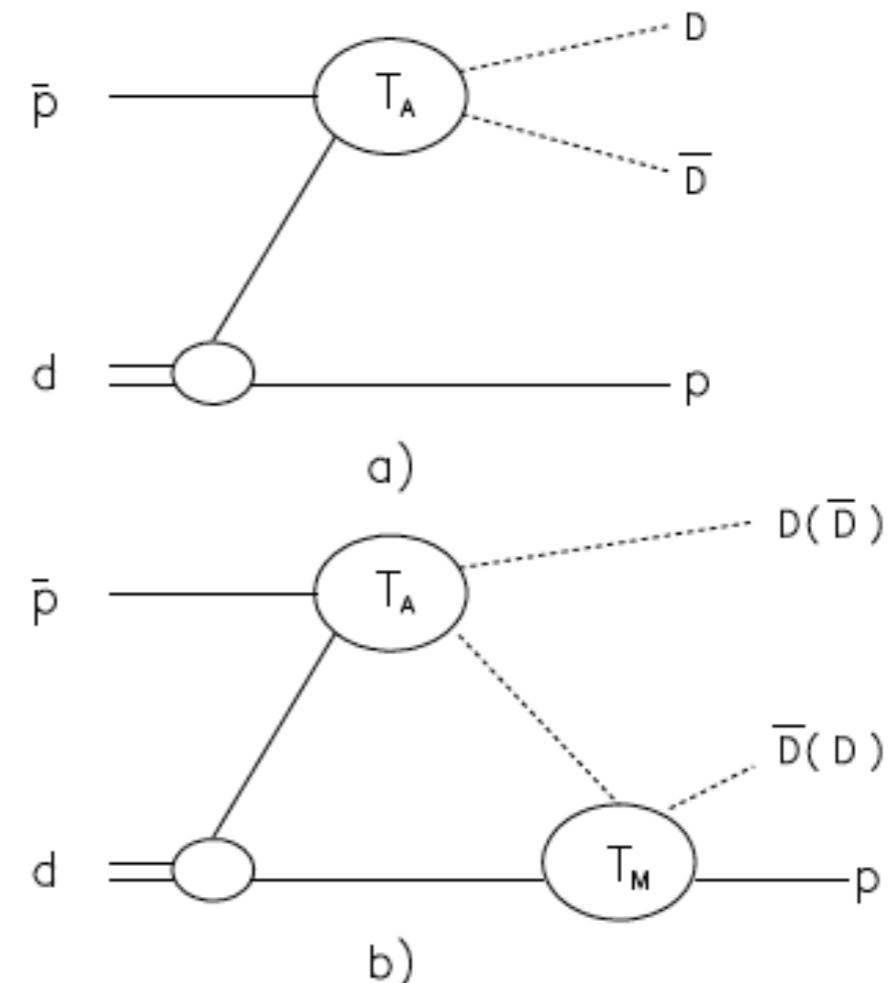
PANDA @ FAIR



# DN Experiment

- antiproton annihilation on the deuteron\*

Panda @ FAIR



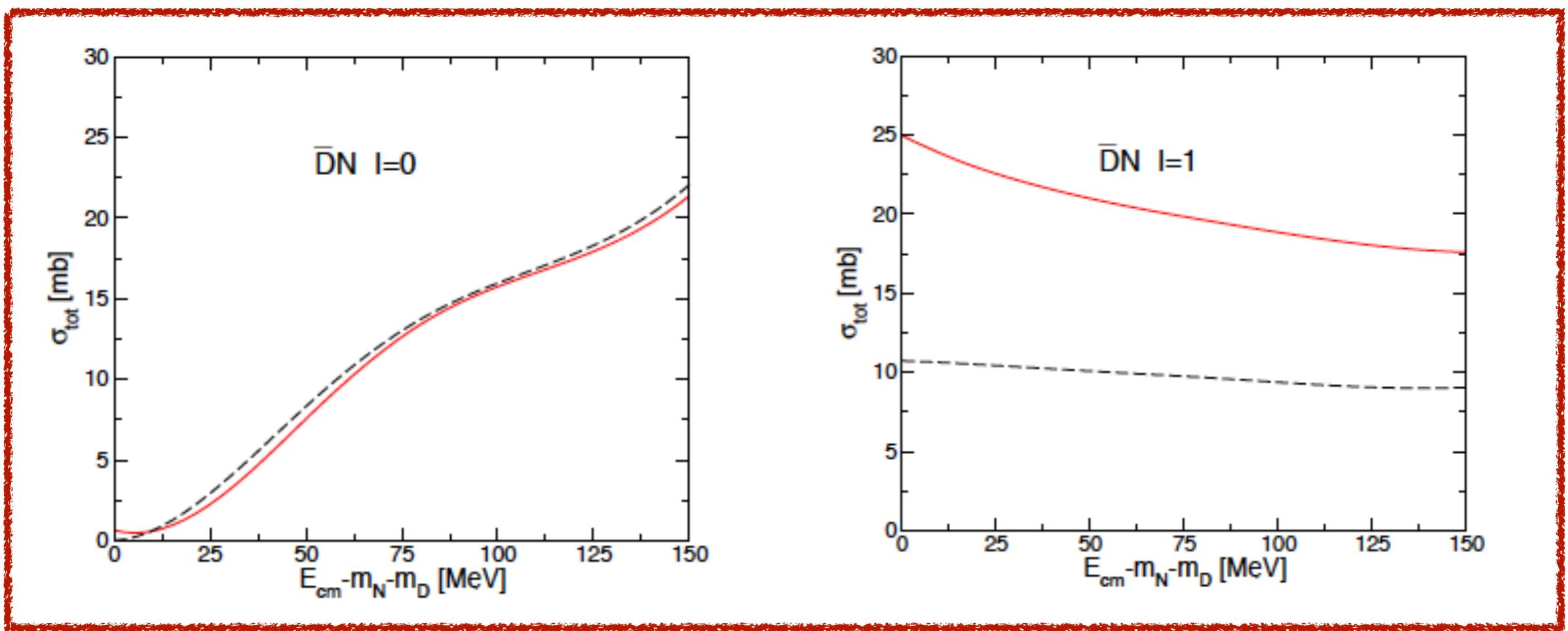
\* J. Haidenbauer, GK, U.-G. Meissner, A. Sibirtsev

1) Eur. Phys. J. A 33, 107 (2007)

2) Eur. Phys. J. A 37, 55 (2008)

# Predictions for the PANDA measurement

Use SU(4) symmetry for couplings:

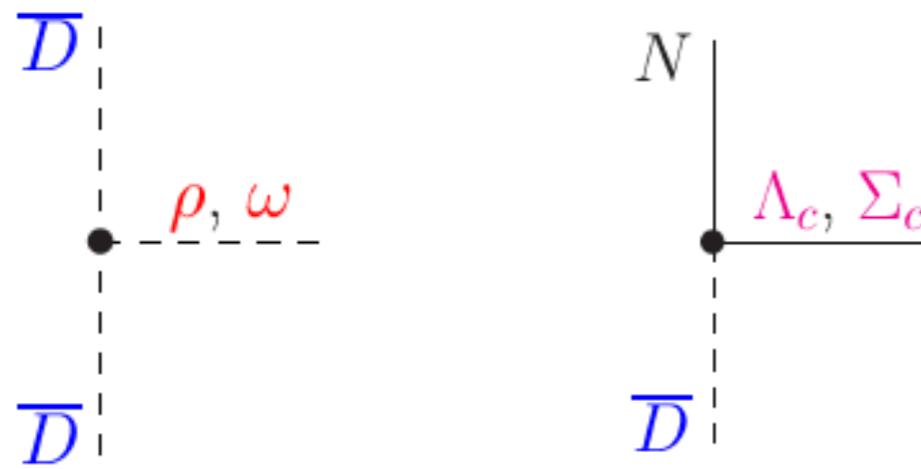


Similar magnitude to KN

# How good is SU(4) flavor symmetry for couplings ?

$$m_u < m_s \ll m_c$$

SU(4) symmetry:

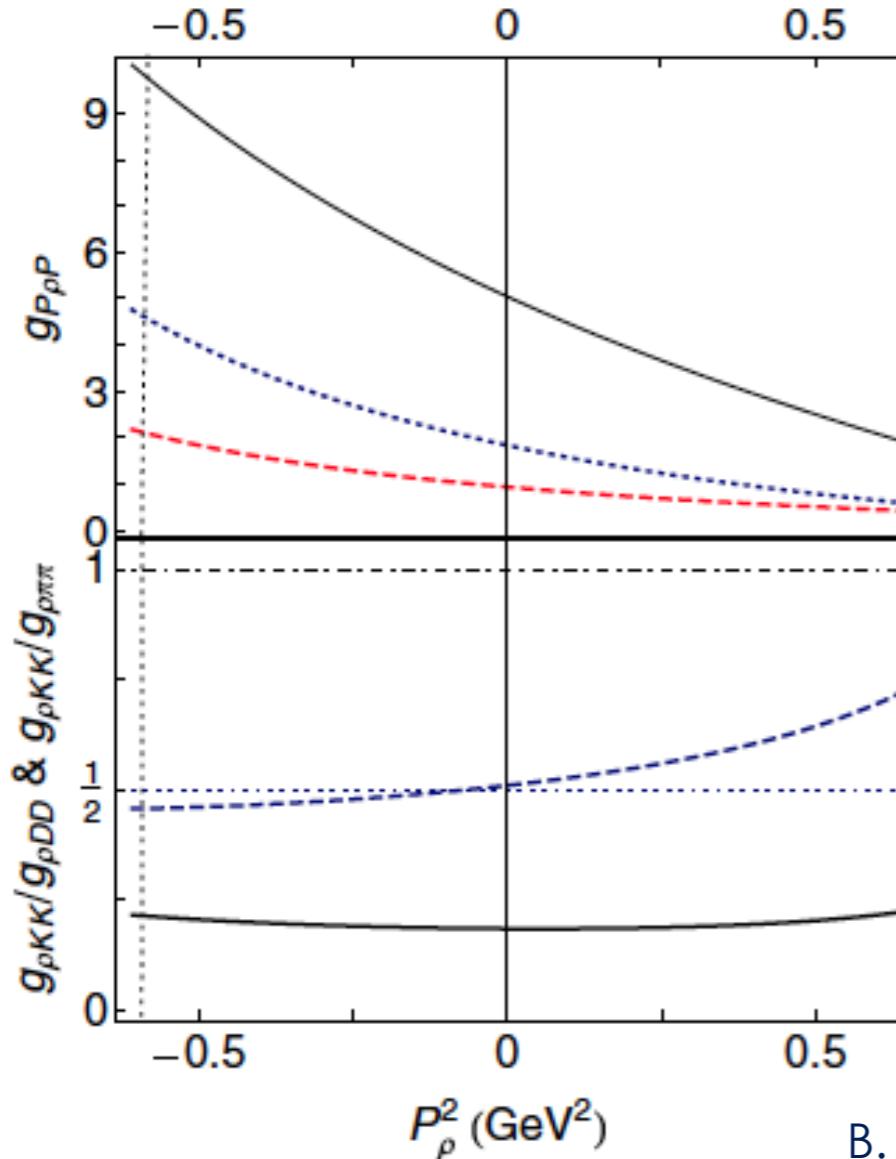


$$\boxed{g_{\bar{D}\rho\bar{D}} = g_{K\rho K} = \frac{1}{2}g_{\pi\rho\pi}}$$
$$g_{N\Lambda_c\bar{D}} = g_{N\Lambda K} = g_{NN\bar{\pi}}$$

# Coupling constants & Form factors

Dyson-Schwinger & Bethe-Salpeter equations:

- rainbow ladder, no free parameters (heavily constrained spectrum and e.w. decay constants)



$g_{K\rho K}/g_{D\rho D}$  —  $\sim 1/4 \rightarrow 400\% \text{ violation}$

$g_{K\rho K}/g_{\pi\rho \pi}$  - - -  $\sim 1/2 \rightarrow \text{SU}(4) \text{ OK}$

COUPLING LARGE, BUT FORM FACTORS ARE SOFT

- DN X-SECTION ONLY 5 TIMES LARGER THAN SU(4)

# On the other hand:

- Quark model +  ${}^3P_0$  decay

	$g_{\rho\pi\pi} / 2g_{\rho KK}$	$g_{\rho\pi\pi} / 2g_{\rho DD}$	$g_{\rho KK} / g_{\rho DD}$
SU(4) symmetric	1	1	1
SU(4) broken	1.05	1.28	1.22

SU(4) BREAKING: AT THE LEVEL OF 20% – 30%

# Quark model + ${}^3P_0$ decay

	$\frac{g_{NN\pi}}{g_{N\Lambda_s K}}$	$\frac{g_{NN\pi}}{g_{N\Lambda_c \bar{D}}}$	$\frac{g_{N\Lambda_s K}}{g_{N\Lambda_c \bar{D}}}$
SU(4) symmetric	1	1	1
SU(4) broken	1.07	1.20	1.12

SU(4) BREAKING: AT THE LEVEL OF 10% – 15%

# AdS/QCD hard wall model

$$\frac{g_{\rho\pi\pi}}{2g_{\rho KK}} = 1.08$$

$$\frac{g_{\rho\pi\pi}}{2g_{\rho DD}} = 1.78$$

$$\frac{g_{\rho KK}}{g_{\rho DD}} = 1.65$$

# QCD sum rules<sup>1</sup> & Lattice<sup>2</sup>

- Looked at SU(4) symmetry breaking  
within the charm sector only

$$g_{\rho DD} = g_{\rho D^* D^*} = g_{\pi D^* D}$$

- 1) M.E. Bracco, M. Chiapparini, F.S. Navarra, M. Nielsen, Prog. Part. Nucl. Phys. 67, 1019 (2012)
- 2) K.U. Can, G. Erkol, M. Oka, T. Takahashi, Phys. Lett. B 719 , 103 (2013)

# QCD sum rules

**Table 8**

SU(4) relations between the coupling constants (on the left column) and their violation (in percentage on the right column) found in QCDSR.

SU(4) relation	Violation
$g_{J/\psi DD} = g_{J/\psi D^* D^*}$	(7%)
$g_{\rho DD^*} = \frac{\sqrt{6}}{2} g_{J/\psi DD^*}$	(12%)
$g_{\rho DD} = \frac{\sqrt{6}}{4} g_{J/\psi DD}$	(17%)
$g_{\pi D^* D^*} = \frac{\sqrt{6}}{2} g_{J/\psi DD^*}$	(20%)
$g_{D^* D^* \rho} = \frac{\sqrt{6}}{4} g_{J/\psi D^* D^*}$	(20%)
$g_{DD\rho} = \frac{\sqrt{6}}{4} g_{J/\psi D^* D^*}$	(21%)
$g_{\rho D^* D^*} = \frac{\sqrt{6}}{4} g_{J/\psi DD}$	(25%)
$g_{\pi D^* D^*} = g_{\rho DD^*}$	(29%)
$g_{\rho DD} = g_{\rho D^* D^*}$	(36%)
$g_{D^* D\pi} = g_{D^* D^* \rho}$	(52%)
$g_{D^* D\pi} = \frac{\sqrt{6}}{4} g_{J/\psi D^* D^*}$	(62%)
$g_{D^* D\pi} = \frac{\sqrt{6}}{4} g_{J/\psi DD}$	(64%)
$g_{D^* D\pi} = g_{DD\rho}$	(70%)

# Lattice

Extrapolation to physical  
pion mass from

$m_\pi$  : 700, 570, 410, 300 MeV

$$g_{D^* D \pi} = 16.23(1.71)$$

$$g_{DD\rho} = 4.84(34)$$

$$g_{D^* D^* \rho} = 5.94(56)$$

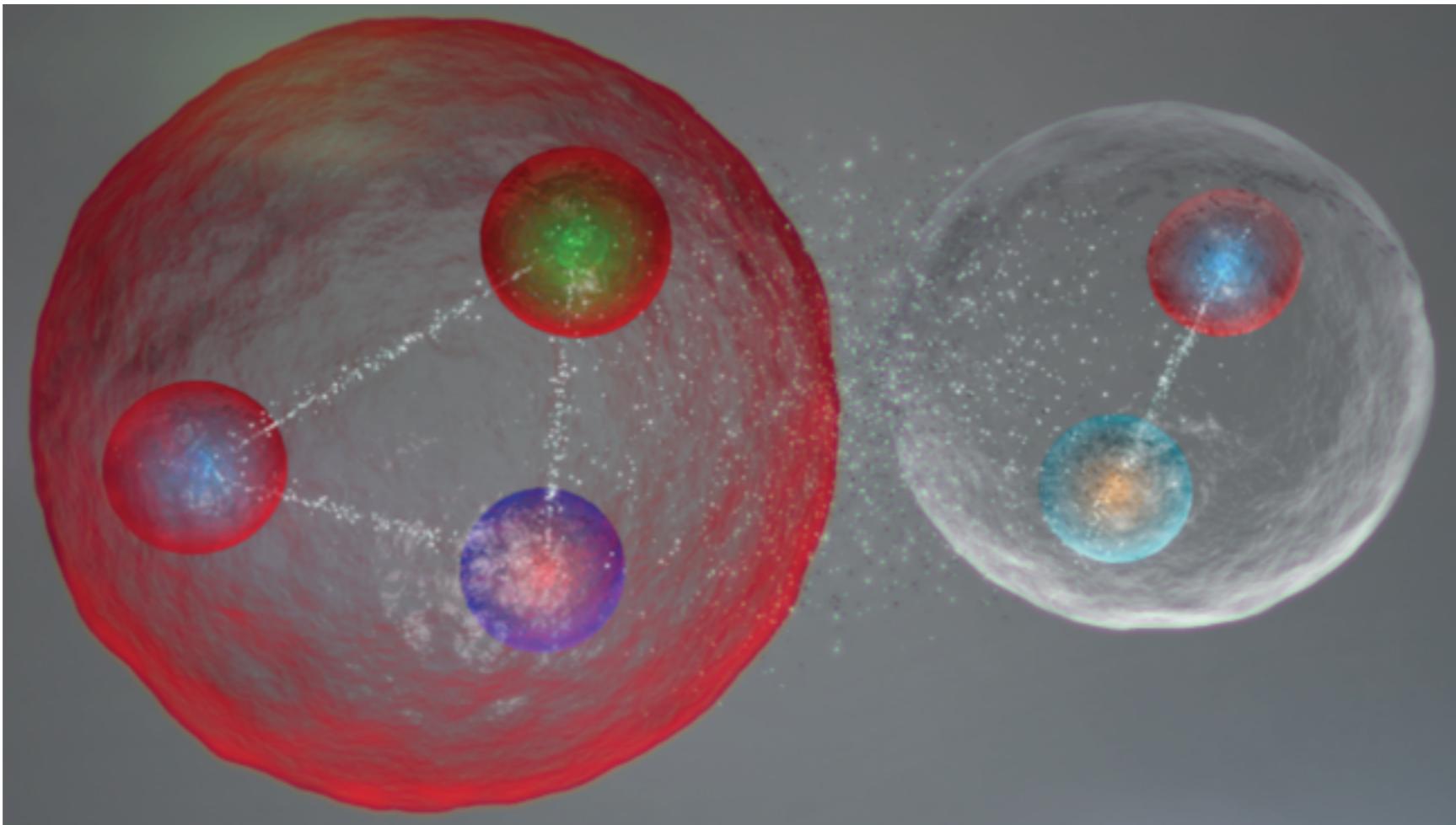
# Chromopolarizability & color van der Waals forces — an EFT perspective

Interactions between color neutral objects:

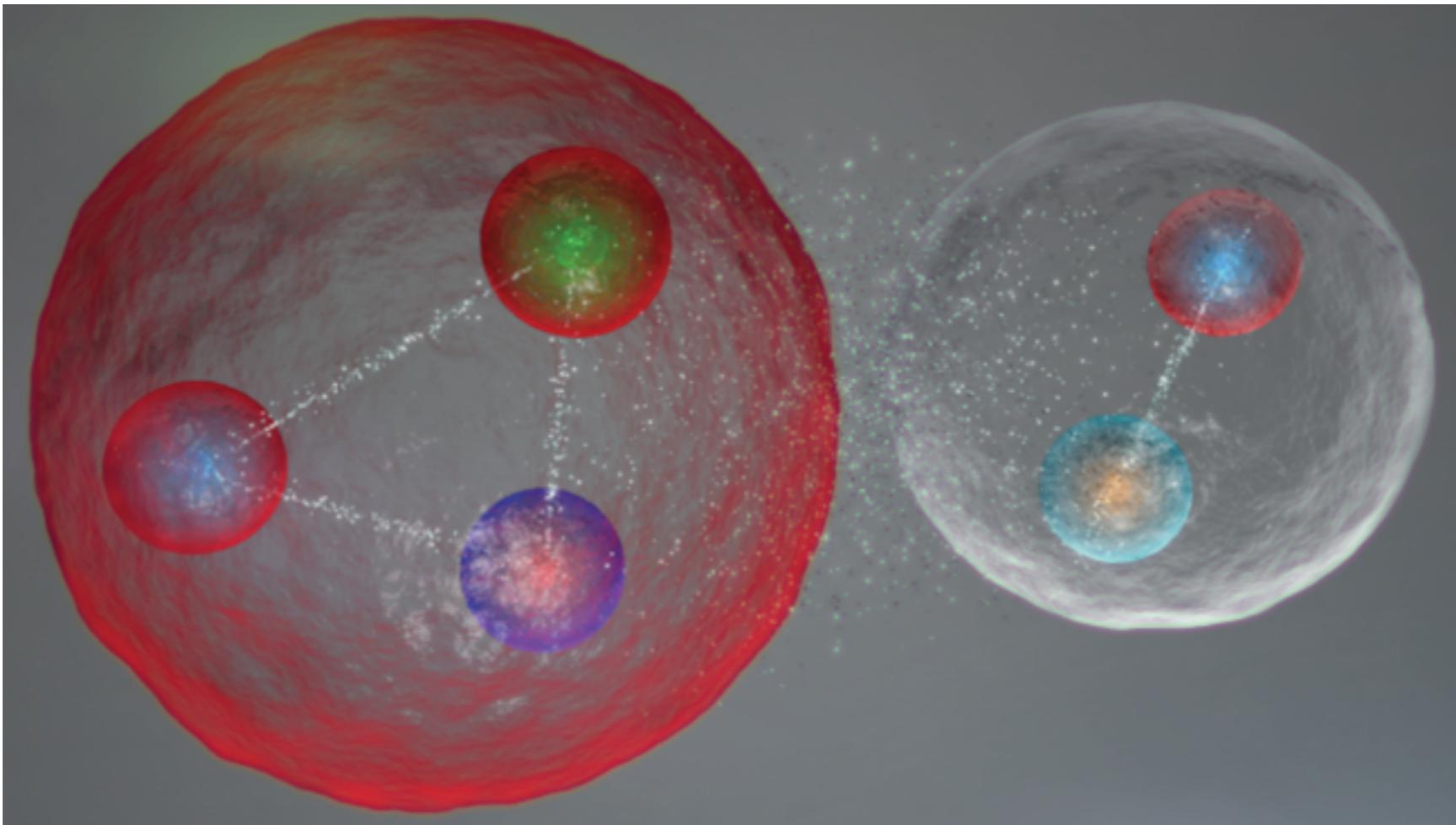
Via creation of instantaneous color dipole moments &  
gluon transitions in virtual color-octet intermediate state

— Polarizability —

Would like to treat this

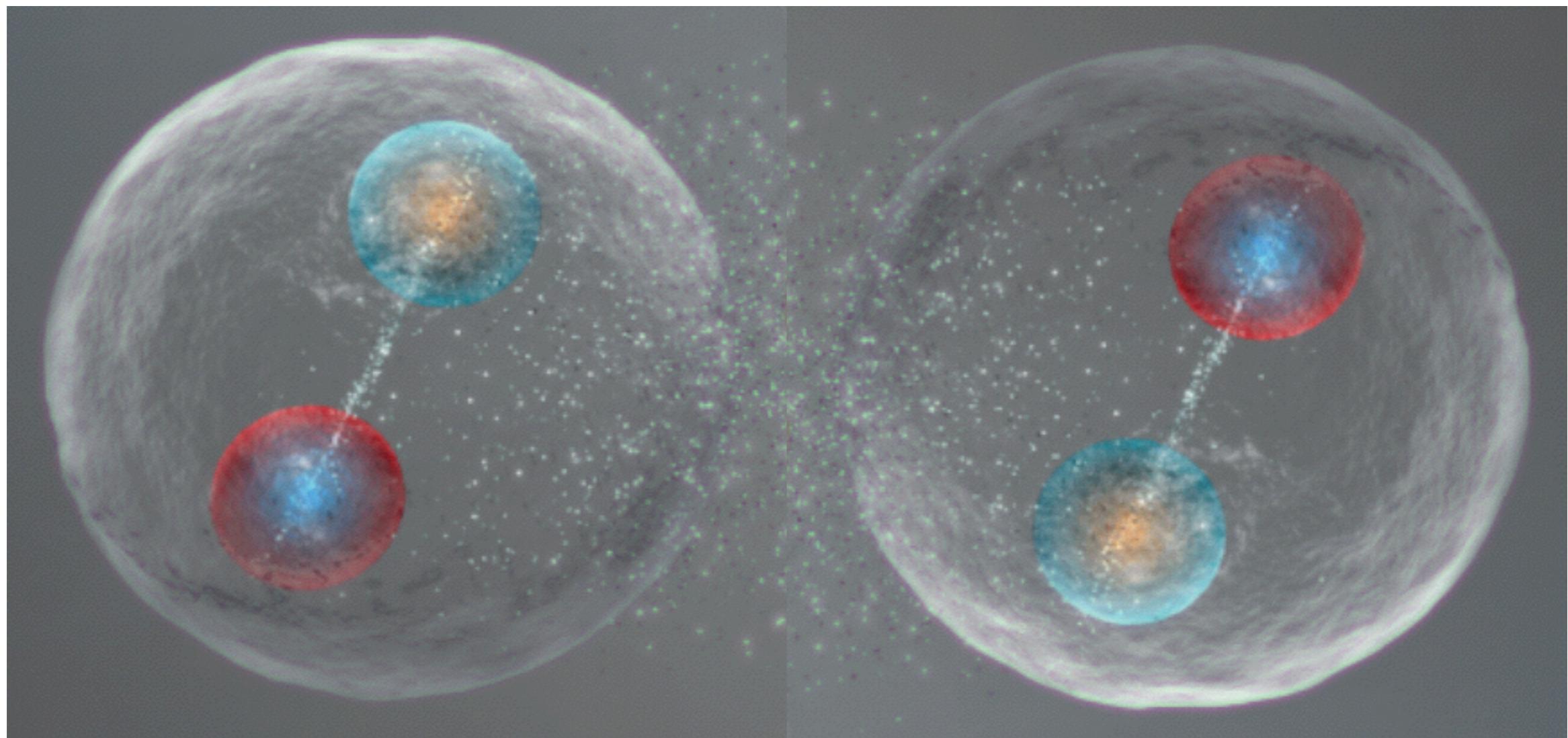


# Would like to treat this



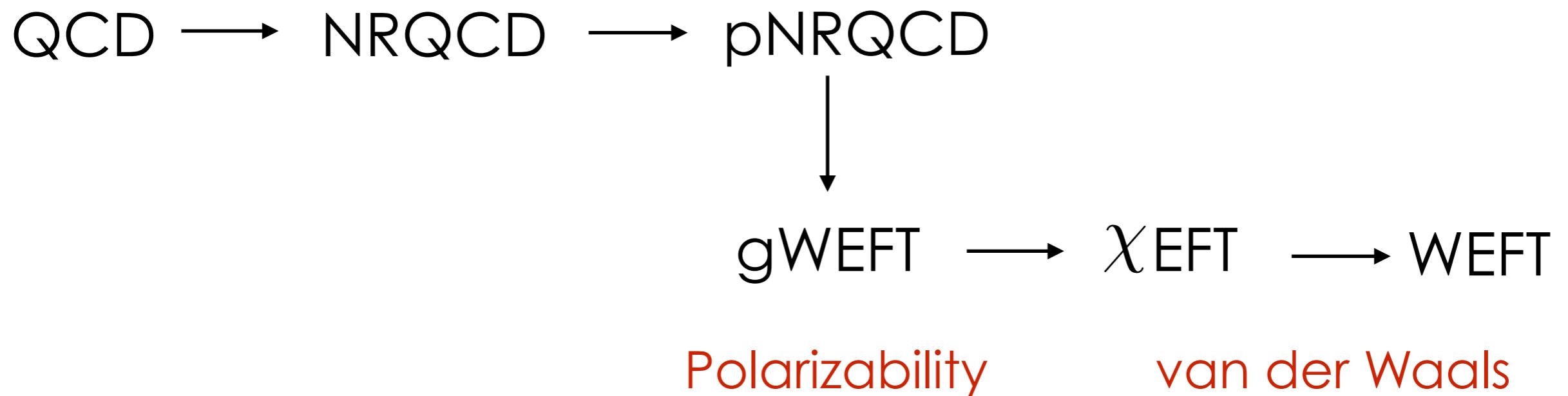
But will start with a simpler system ...

$$\eta_b - \bar{\eta}_b$$



# EFT approach

- Chromopolarizability of 1S bottomonium;  
use pNRQC (potential Nonrelativistic QCD)
- van der Waals force between two bottomonia;  
use QCD trace anomaly to match pNRQC to a chiral EFT



# Scales

$m$ : bottom mass,       $v$ : relative velocity

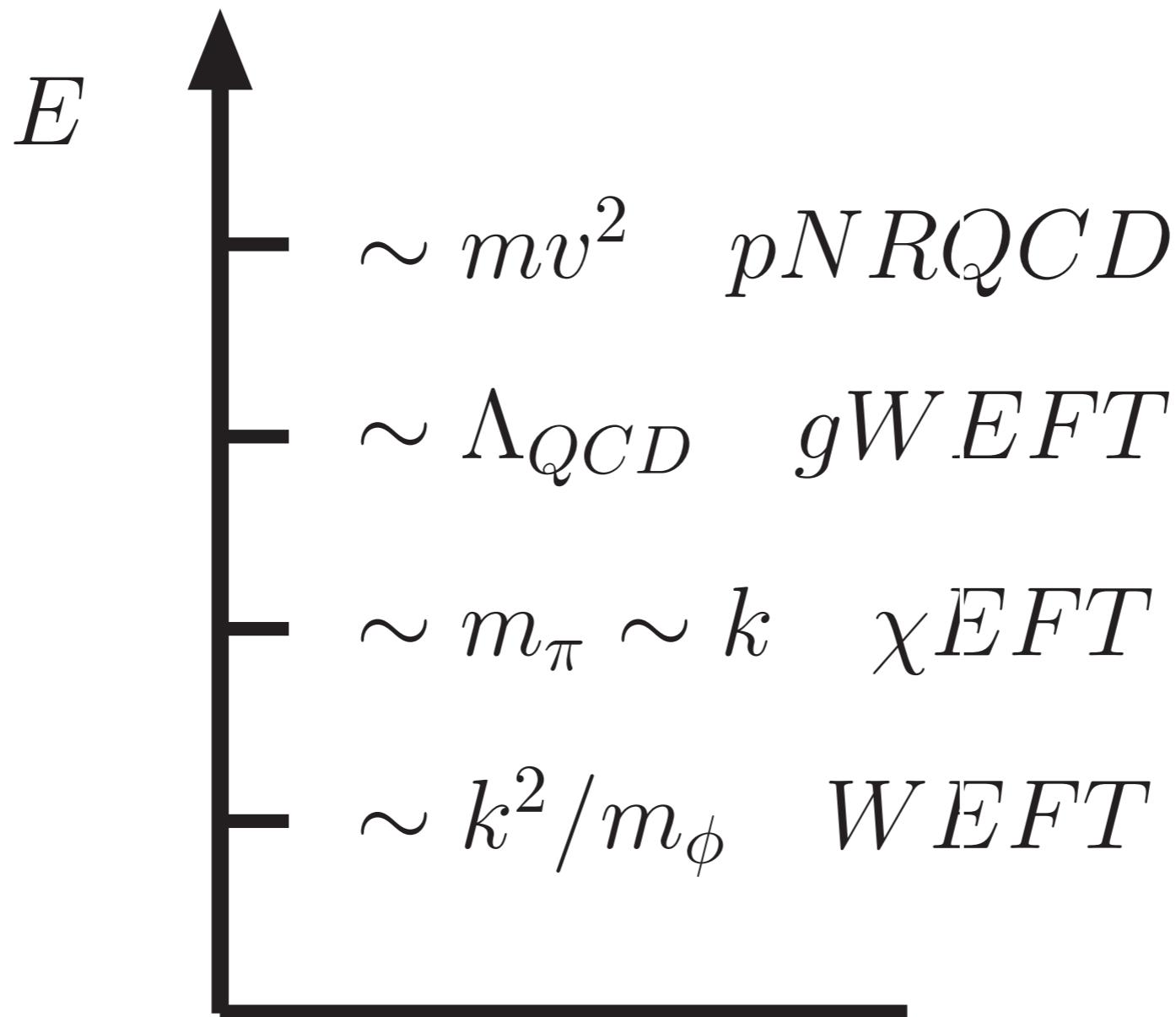
$$m \gg mv \gg mv^2 \gg \Lambda_{\text{QCD}}$$

QCD  $\longrightarrow$  NRQCD  $\longrightarrow$  pNRQCD  $\longrightarrow$  gWEFT

$m_\phi$ : mass bottomonium,       $r_{\phi\phi} \sim 1/m_\pi$ : relative distance

$$\mathbf{k}_{\phi\phi}^2/m_\phi = m_\pi^2/m_\phi \ll m_\pi$$

gWEFT  $\longrightarrow$  EFT  $\longrightarrow$  WEFT



Hierarchy of scales and the corresponding EFTs

# pNRQCD

$$\begin{aligned}\mathcal{L}_{\text{pNRQCD}} = & \int d^3r \text{Tr} [S^\dagger (i\partial_0 - h_s) S + O^\dagger (iD_0 - h_o) O] \\ & + g V_A(r) \text{Tr} [O^\dagger \mathbf{r} \cdot \mathbf{E} S + S^\dagger \mathbf{r} \cdot \mathbf{E} O] + \frac{g}{2} V_B(r) \text{Tr} [O^\dagger \mathbf{r} \cdot \mathbf{E} O + O^\dagger O \mathbf{r} \cdot \mathbf{E}] \\ & + \mathcal{L}_{\text{light}}\end{aligned}$$

$$\begin{aligned}h_s = & -\frac{\nabla_{\mathbf{r}}^2}{m} - \frac{\nabla_{\mathbf{R}}^2}{4m} + V_s(r)\,, & V_s(r) = & -C_F \frac{\alpha_s(r)}{r}\,, \\ h_o = & -\frac{\nabla_{\mathbf{r}}^2}{m} - \frac{D_{\mathbf{R}}^2}{4m} + V_o(r)\,, & V_o(r) = & \left(\frac{C_A}{2} - C_F\right) \frac{\alpha_s(r)}{r}\,, \\ & & V_A(r) = & 1\,, \\ & & V_B(r) = & 1\,,\end{aligned}$$

$$C_A=N_c=3,\,C_F=(N_c^2-1)/(2N_c)\text{ and }T_F=1/2$$

# Chromopolarizability



$$L_{\text{gWEFT}} = \int d^3 \mathbf{R} \left\{ \phi^\dagger(t, \mathbf{R}) \left[ i\partial_0 + E_\phi - \frac{\nabla_{\mathbf{R}}^2}{4m} + \frac{1}{2}\beta g^2 E_a^2 + \dots \right] \phi(t, \mathbf{R}) \right\} + \mathcal{L}_{\text{light}}$$

Chromopolarizability

$$\beta = -\frac{2V_A^2 T_F}{3N_c} \langle \phi | \mathbf{r} \frac{1}{E_\phi - h_o} \mathbf{r} | \phi \rangle$$

$$= -\frac{2V_A^2 T_F}{3N_c} \sum_l \int \frac{d^3 p}{(2\pi)^3} |\langle \phi | \mathbf{r} | \mathbf{p} l \rangle|^2 \frac{1}{E_\phi - \frac{\mathbf{p}^2}{4m}}$$

# Wave functions

Bound-state

$$\langle \mathbf{r} | \phi \rangle = \frac{1}{\sqrt{\pi a_0^3}} e^{-r/a_0} \quad a_0 = 1/(m\alpha_s)$$

Continuum octet\*

$$\langle \mathbf{r} | \mathbf{p} \cdot \mathbf{1} \rangle = e^{i(\pi/2 - \delta_1)} \sqrt{2\pi} \mathbf{p} \cdot \mathbf{r} \sqrt{\frac{\rho \left(1 + \frac{\rho^2}{a_0^2 |\mathbf{p}|^2}\right)}{a_0 |\mathbf{p}| \left(e^{\frac{2\pi\rho}{a_0 |\mathbf{p}|}} - 1\right)}} e^{i|\mathbf{p}||\mathbf{r}|} {}_1F_1 \left(2 + i\frac{\rho}{a_0 |\mathbf{p}|}; 4; -2|\mathbf{p}||\mathbf{r}|\right)$$

$$\rho = (N_c^2 - 1)^{-1}$$

\*N. Brambilla, M.A. Escobedo, J. Ghiglieri, A. Vairo JHEP 1112, 116 (2011)

# Result

## — sensitivity to bottom mass

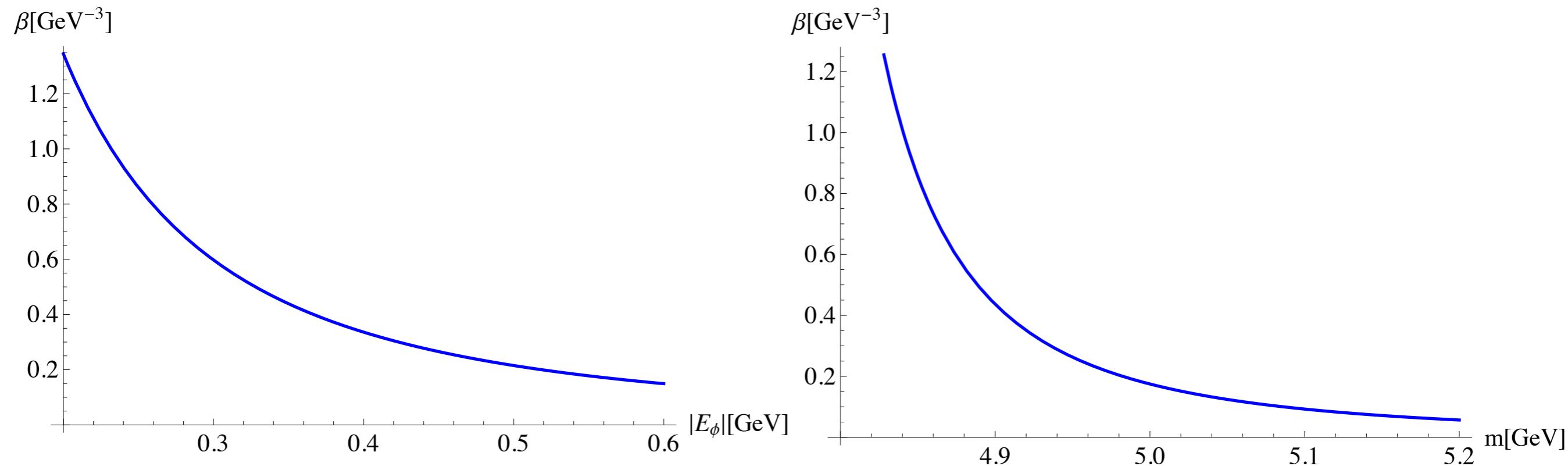


Figure 3. Plot of  $\beta$  from eq. (19). Left panel: plot as a function of the  $\phi$  binding energy for  $m = 5$  GeV. Right panel: plot as a function of the bottom mass fixing the binding energy as  $E_\phi = m_\phi - 2m$ .

# Numerical results

$$m = 5 \text{ GeV} \quad m_\phi = 9.4454 \text{ GeV} \quad \left\{ \begin{array}{l} \text{average of} \\ \eta_b \text{ & } \Upsilon_b(1S) \end{array} \right.$$

$$E_\phi = m_\phi - 2m = -0.555 \text{ GeV}$$

$$\alpha_s = \sqrt{\frac{4|E_\phi|}{C_F^2 m}} \approx 0.5$$

$$\beta = 0.175 \text{ GeV}^{-3}$$

$$\Upsilon(2S) \rightarrow \Upsilon(1S)\pi\pi$$

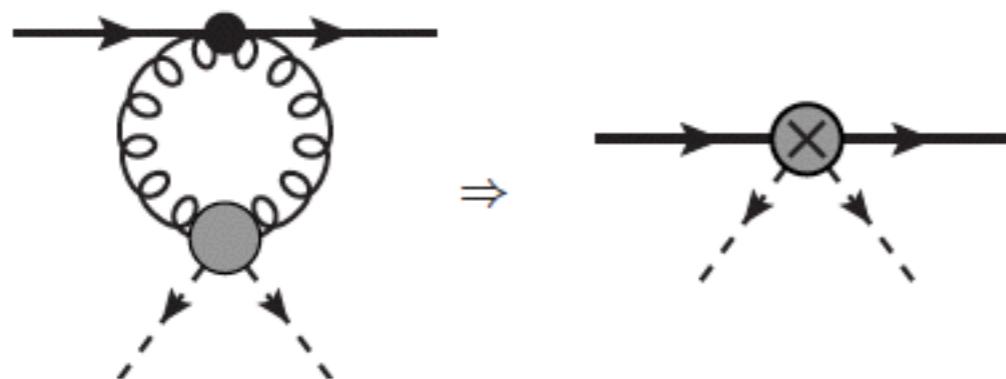
$$\beta_{\Upsilon-\Upsilon'} = 0.66 \text{ GeV}^{-3}$$

M.B. Voloshin, Mod. Phys. Lett A 19, 665 (2004)

We can obtain this value if we use  $m = 4.863 \text{ GeV}$

# van der Waals force

gWEFT  $\longrightarrow$   $\chi$ EFT  $\longrightarrow$  WEFT



QCD trace  
anomaly

$$g^2 \langle \pi^+(p_1) \pi^-(p_2) | E_a^2 | 0 \rangle = \frac{8\pi^2}{3b} \left( (p_1 + p_2)^2 \kappa_1 + m_\pi^2 \kappa_2 \right)$$

$$\kappa_1 = 1 - 9\kappa/4, \kappa_2 = 1 - 9\kappa/2 \quad b = \frac{11}{3}N_c - \frac{2}{3}N_f$$

$$\kappa = 0.186 \pm 0.003 \pm 0.006 \quad \leftarrow \quad \psi' \rightarrow J/\psi \pi^+ \pi^-$$

# Matching gWEFT $\longrightarrow$ $\chi$ EFT

$$\mathcal{L}_{\chi\text{EFT}}^\phi = \phi^\dagger \left( i\partial_0 - \frac{\nabla^2}{2m_\phi} \right) \phi$$

$$\mathcal{L}_{\chi\text{EFT}}^\pi = \frac{F^2}{4} (\langle \partial_\mu U \partial^\mu U^\dagger \rangle + \langle \chi^\dagger U + \chi U^\dagger \rangle)$$

$$U = e^{i\phi/F} = u^2, \quad \phi = \begin{pmatrix} \pi^0 & \sqrt{2}\pi^+ \\ \sqrt{2}\pi^- & -\pi^0 \end{pmatrix}$$

$$\chi = 2B\hat{m}\mathbf{1} \quad F = F_\pi = 92.419 \text{ MeV}$$

$$\mathcal{L}_{\chi\text{EFT}}^{\phi-\pi} = \phi^\dagger \phi \frac{F^2}{4} (c_{d0} \langle \partial_0 U \partial_0 U^\dagger \rangle + c_{di} \langle \partial_i U \partial^i U^\dagger \rangle + c_m \langle \chi^\dagger U + \chi U^\dagger \rangle)$$

$$\mathcal{A} = \frac{4\pi^2\beta}{b} (\kappa_1 p_1^0 p_2^0 - \kappa_2 p_1^i p_2^i + 3m_\pi^2)$$

$$\mathcal{A} = -c_{d0} p_1^0 p_2^0 + c_{di} p_1^i p_2^i - c_m m_\pi^2$$

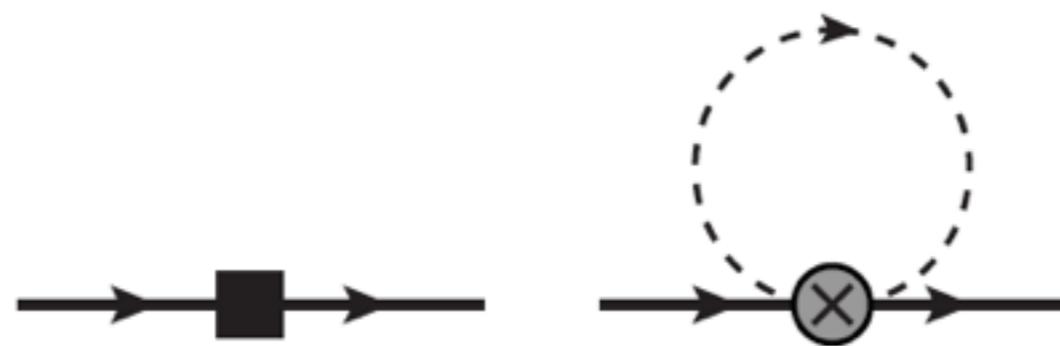
$$c_{d0} = -\frac{4\pi^2\beta}{b} \kappa_1$$

$$c_{di} = -\frac{4\pi^2\beta}{b} \kappa_2$$

$$c_m = -\frac{12\pi^2\beta}{b}$$

# Chiral correction bottomonium mass

## — leading chiral log



$$\delta m_\phi|_{\text{chiral log}} = -\frac{15}{8} \frac{\beta}{b} m_\pi^4 \log \frac{m_\pi^2}{\nu^2}$$

# van der Waals force

$$r_{\phi\phi} \sim 1/m_\pi$$

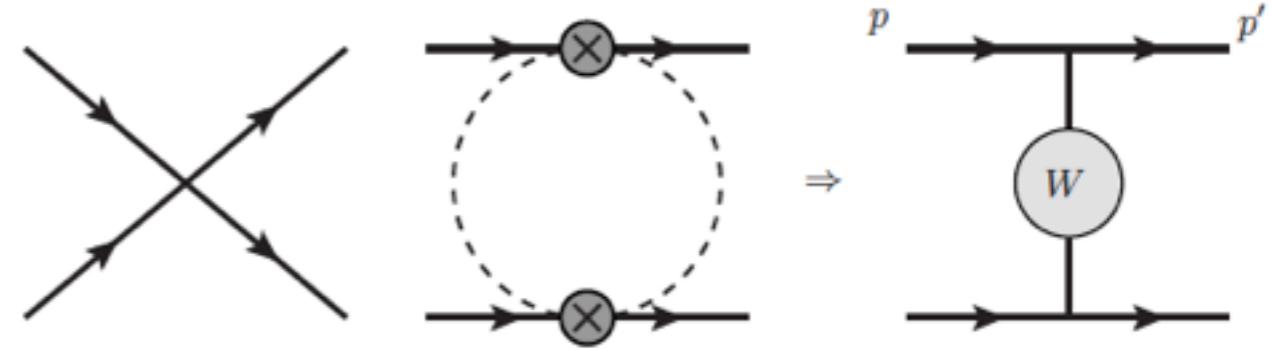
$$\mathbf{k}_{\phi\phi}^2/m_\phi = m_\pi^2/m_\phi \ll m_\pi$$

Relative motion at energies lower than pion mass  
— integrate out the pion

$$\chi\text{EFT} \longrightarrow \text{WEFT}$$

# Matching

$\chi$ EFT  $\longrightarrow$  WEFT

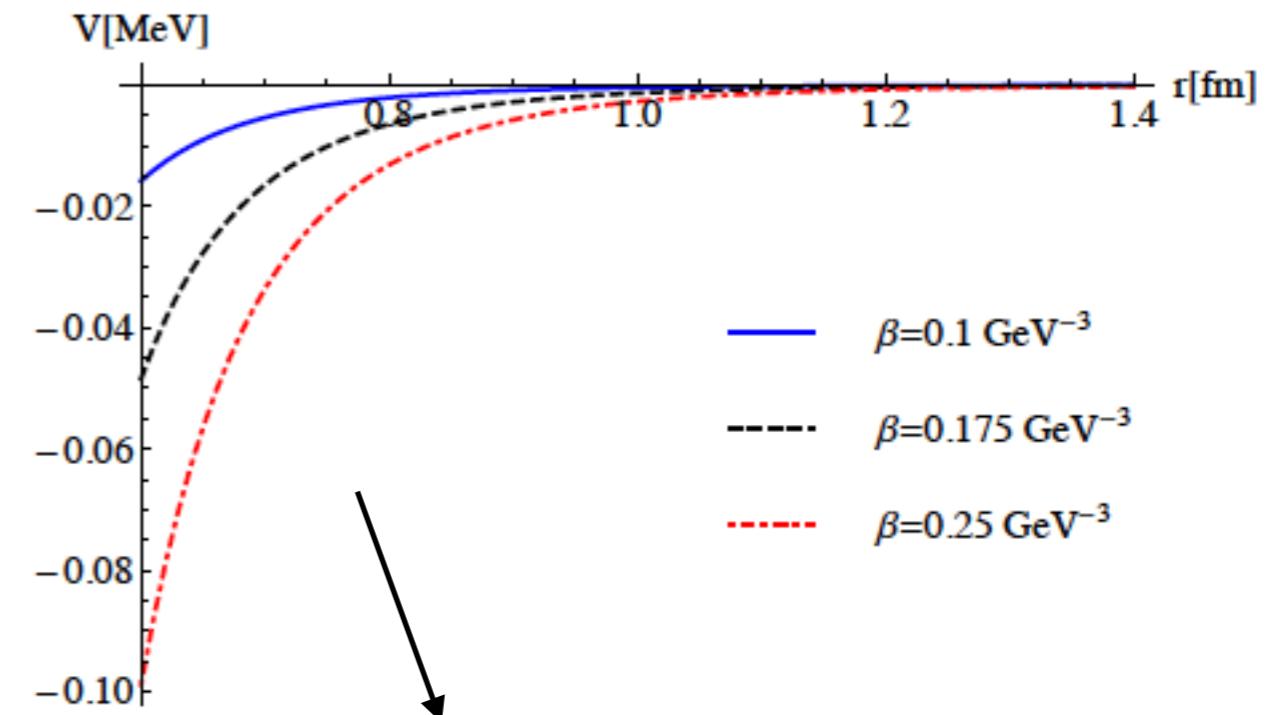
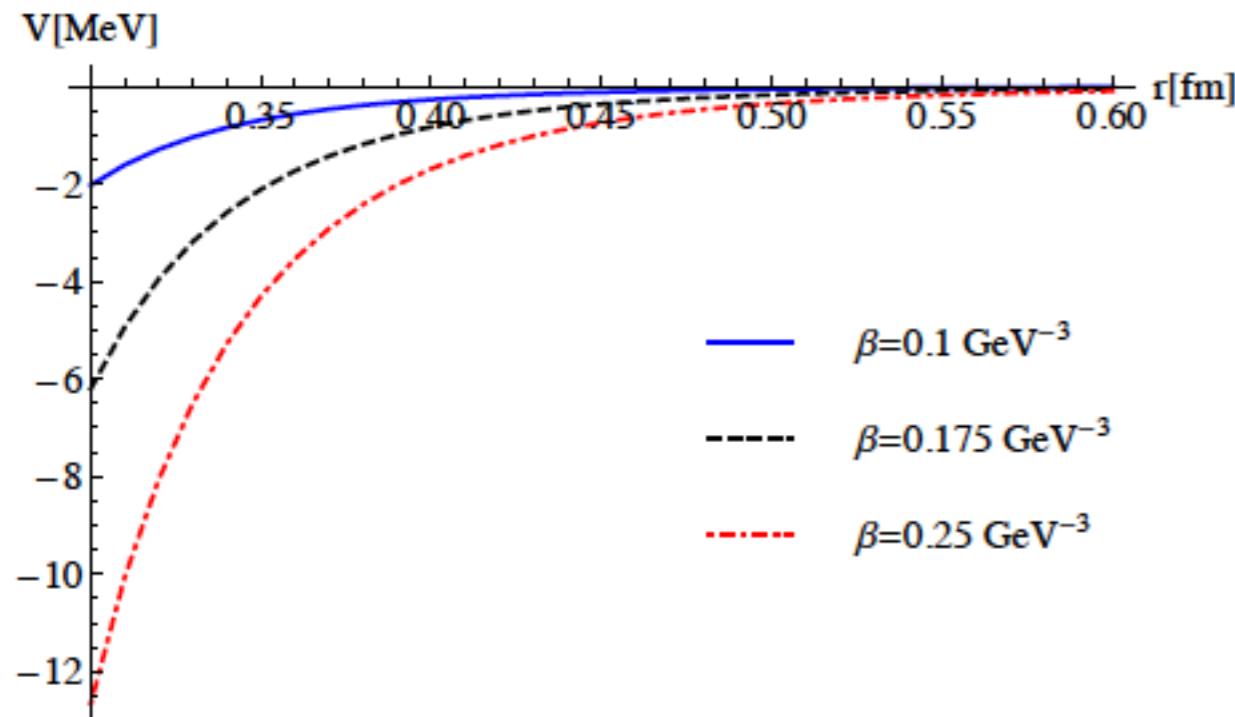


$$\begin{aligned}\mathcal{L}_{\text{WEFT}}^\phi &= \phi^\dagger \left( i\partial_0 - \frac{\nabla^2}{2m_\phi} \right) \phi, \\ L_{\text{WEFT}}^{\phi\phi} &= - \int d^3\mathbf{R}_1 d^3\mathbf{R}_2 \phi^\dagger \phi(t, \mathbf{R}_1) W(\mathbf{R}_1 - \mathbf{R}_2) \phi^\dagger \phi(t, \mathbf{R}_2)\end{aligned}$$

Long-range part:

$$\begin{aligned}W(r) &= -\frac{3\pi\beta^2 m_\pi^2}{8b^2 r^5} \left[ (4(\kappa_2 + 3)^2 (m_\pi r)^3 + (3\kappa_1^2 + 43\kappa_2^2 + 14\kappa_1\kappa_2) m_\pi r) K_1(2m_\pi r) \right. \\ &\quad \left. + 2(2(\kappa_2 + 3)(\kappa_1 + 5\kappa_2)(m_\pi r)^2 + (3\kappa_1^2 + 43\kappa_2^2 + 14\kappa_1\kappa_2)) K_2(2m_\pi r) \right]\end{aligned}$$

# Numerical result



$$W(r) = -\frac{3(3 + \kappa_2)^2 \pi^{3/2} \beta^2}{4b^2} \frac{m_\pi^{9/2}}{r^{5/2}} e^{-2m_\pi r}$$

Possible bound state?

$E_{\phi\phi} \sim 1 \text{ MeV}$

# Perspectives

- EFT for molecules, Born-Oppenheimer
- Help from the lattice
- Need experiments, e.g. DN

# Funding

