

Precision QCD for New Physics Searches:

Working with heavy quarks at High Scales & High Orders

Fred Olness

SMU

Thanks to:

F. Lyonnet, E. Godat, A. Kusina,, I. Schienbein, K. Kovarik, J.Y. Yu, T. Jezo, J.G. Morfin, J.F. Owens, P. Nadolsky, M. Guzzi, V. Radescu, C. Keppel, B. Clark

The Key to Discovery: The Parton Model and Factorization

$$\sigma_{P\gamma \rightarrow c} = f_{P \rightarrow a} \otimes \hat{\sigma}_{a\gamma \rightarrow c}$$

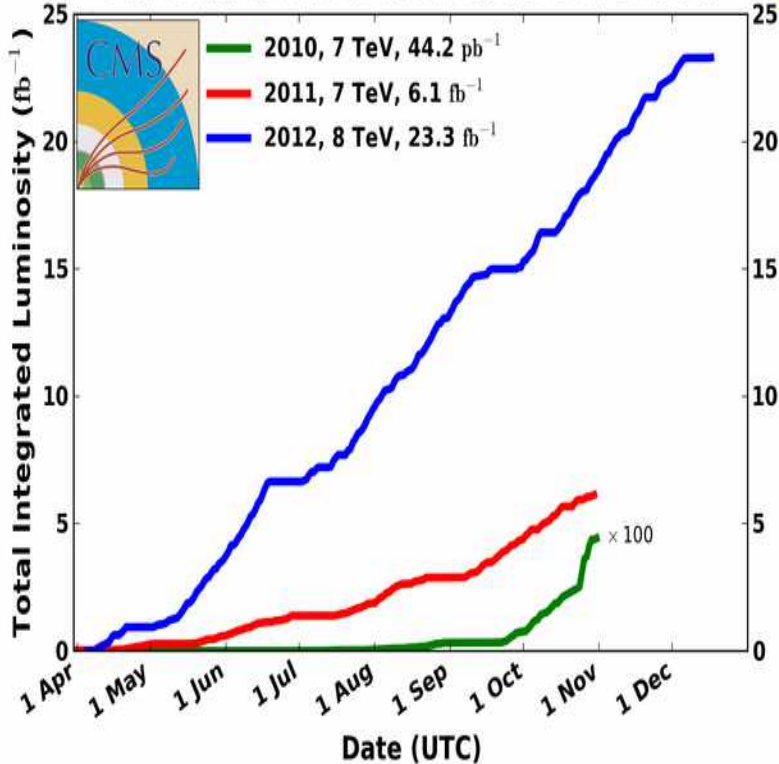
Experimental Observables

Theoretical Calculations

WHAT ABOUT PDF'S ???

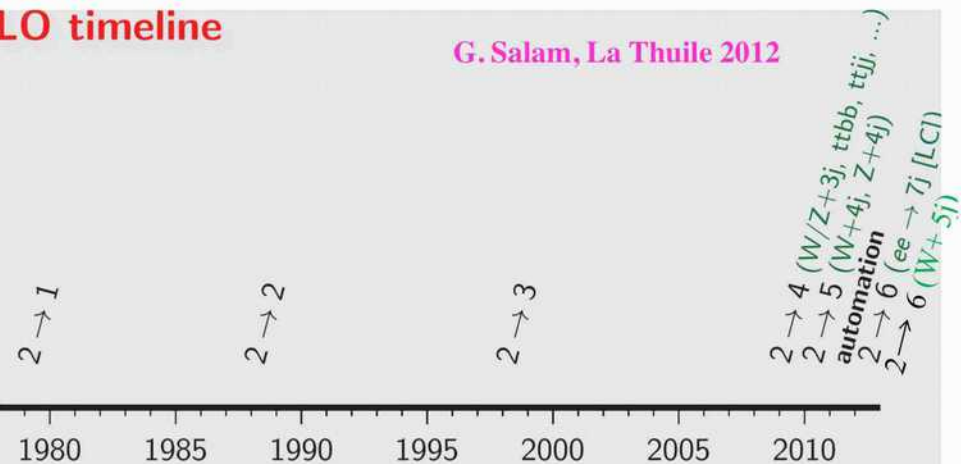
CMS Integrated Luminosity, pp

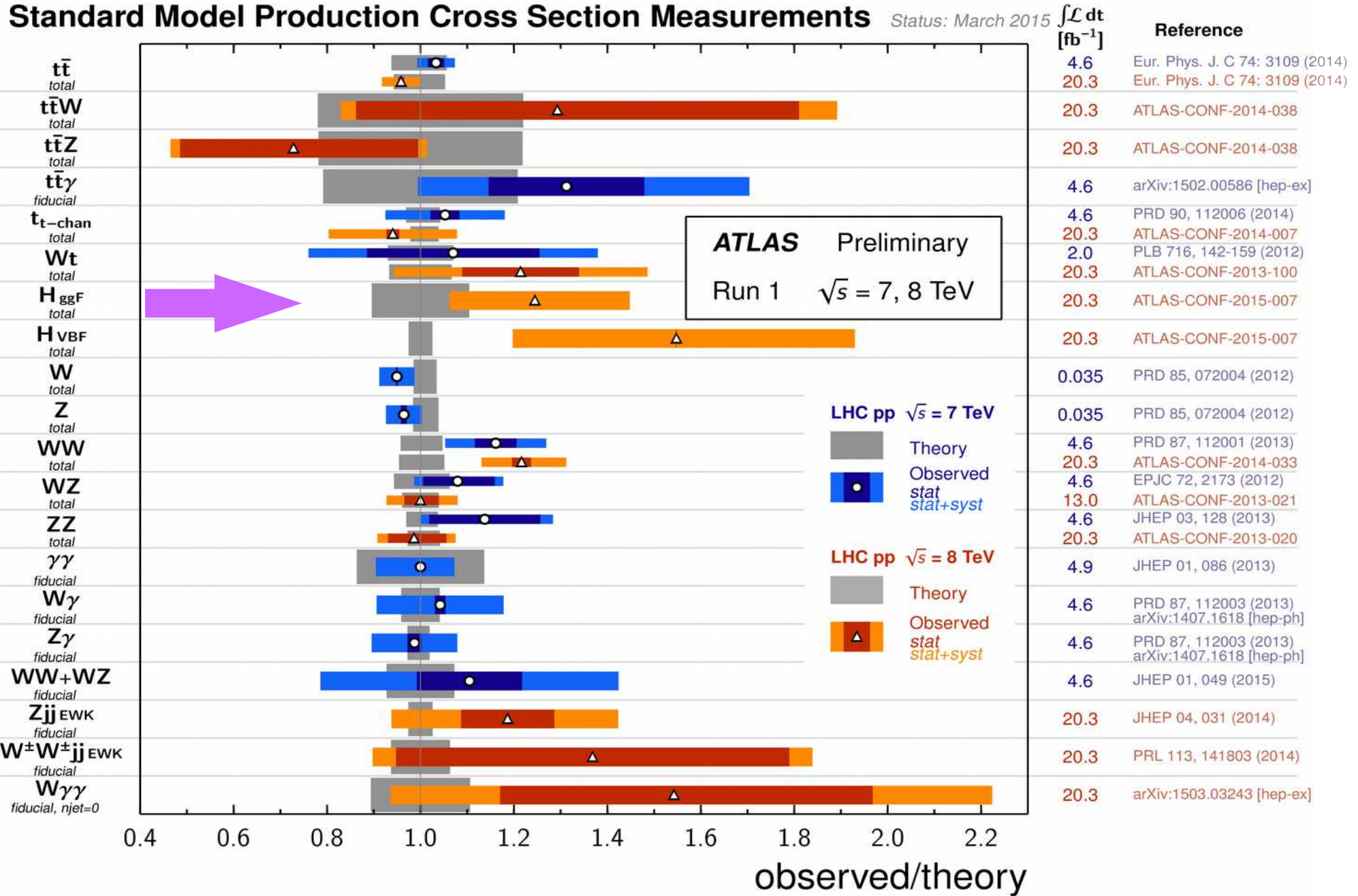
Data included from 2010-03-30 11:21 to 2012-12-16 20:49 UTC



NLO timeline

G. Salam, La Thuile 2012





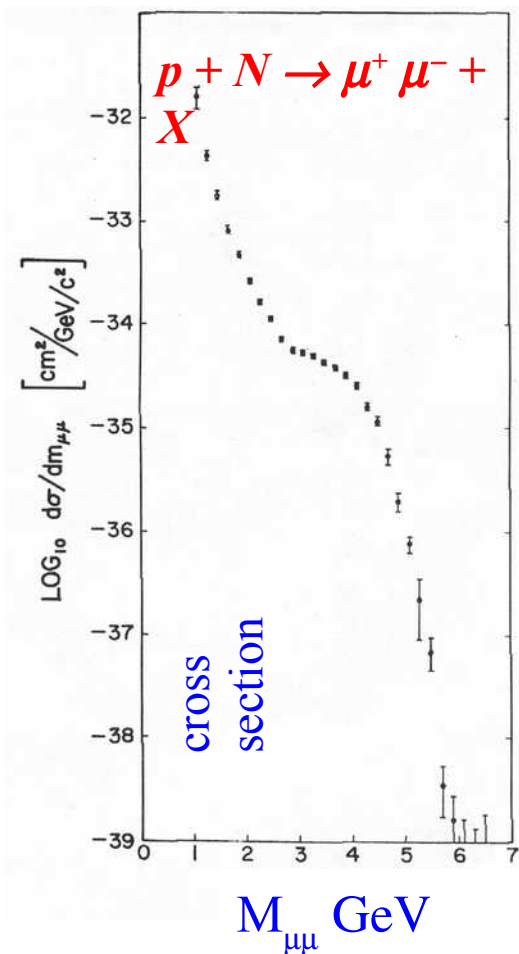
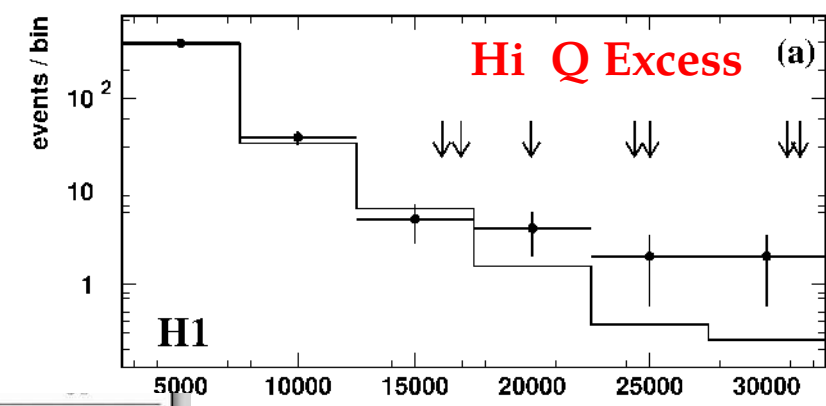
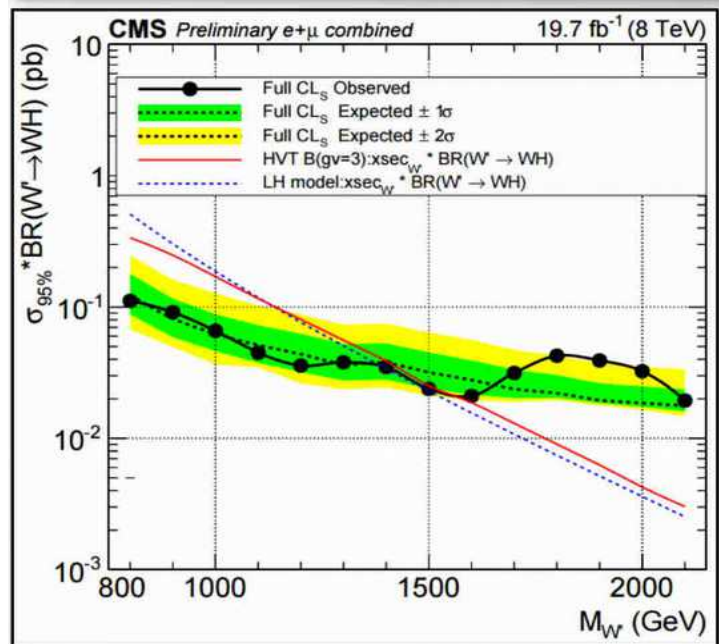
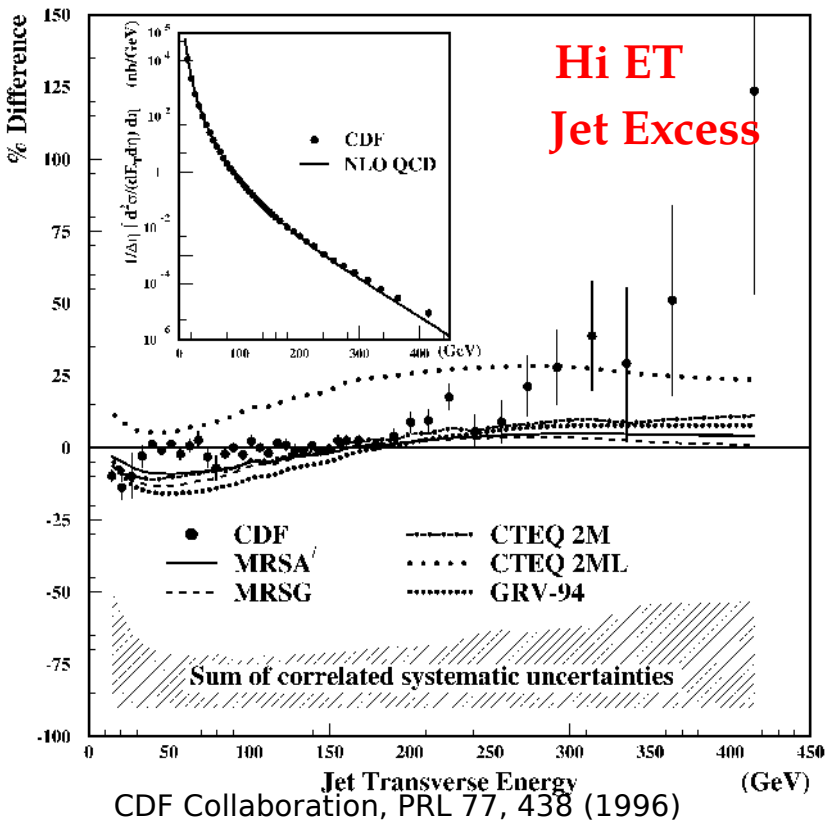
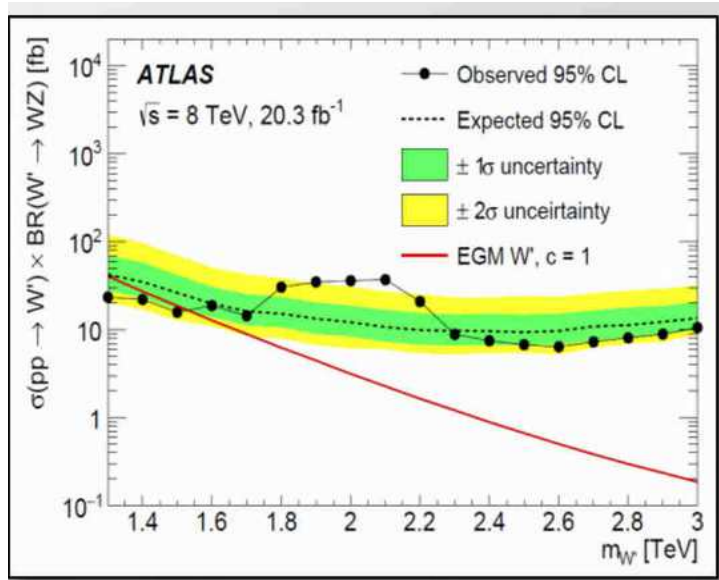
Much of theory error from PDFs

N^3 LO $gg \rightarrow H$

PDF error 2x of Theory Error

... things that go bump in the data ...

Can you find the Nobel Prize???



H1 Collaboration, ZPC74, 191 (1997)
ZEUS Collaboration, ZPC74, 207 (1997)

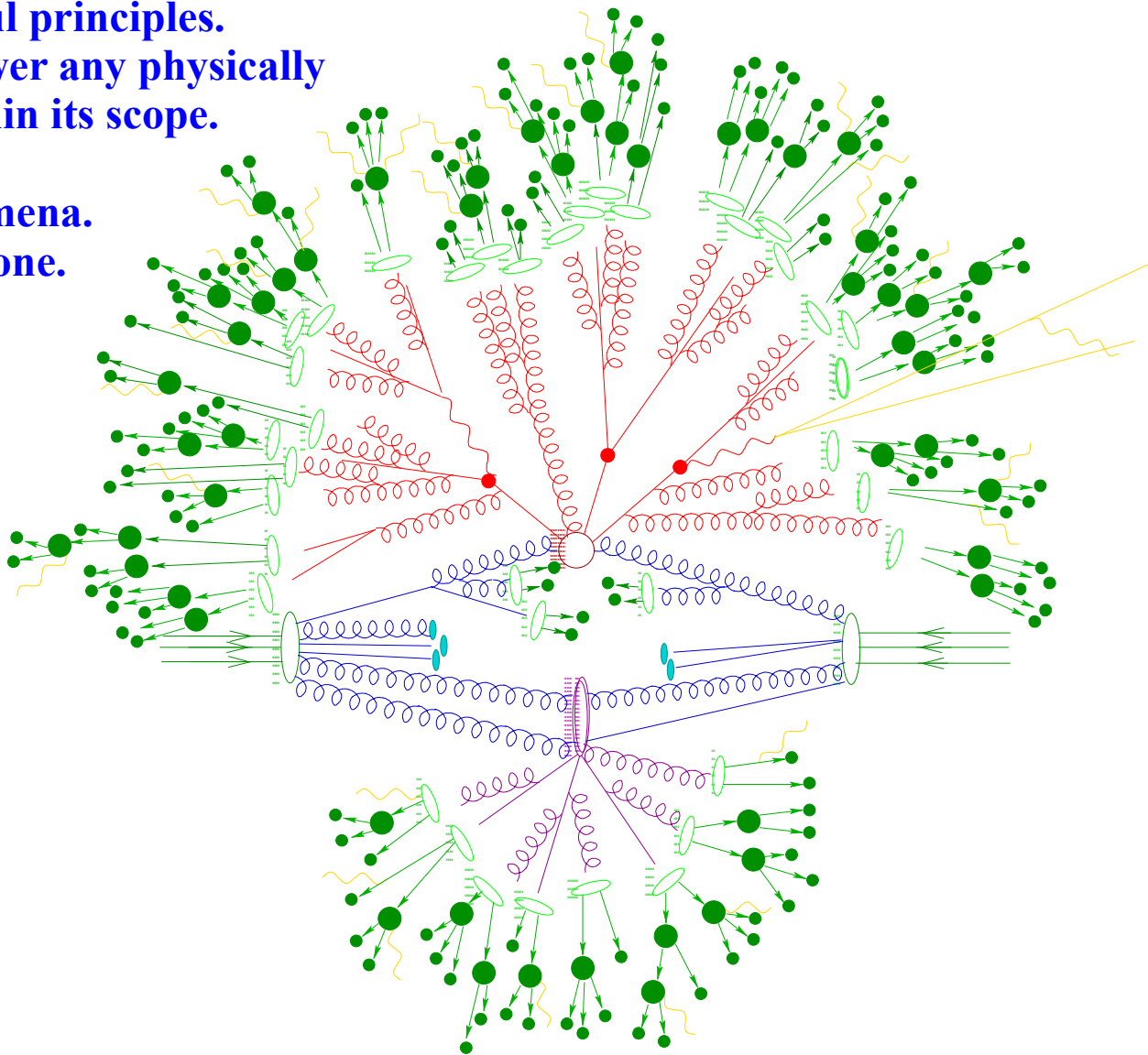
What QCD Tells Us About Nature – and Why We Should Listen

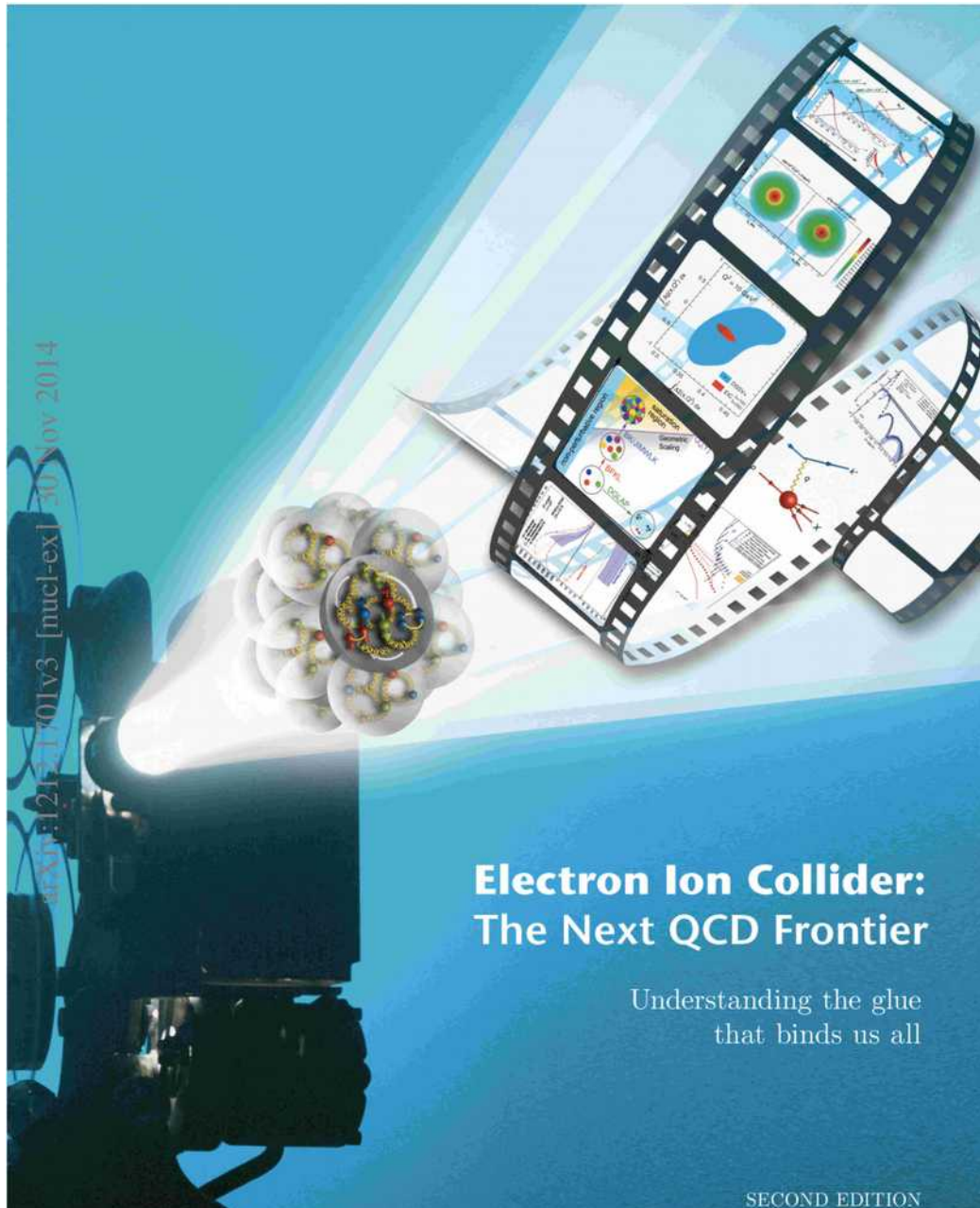
Frank Wilczek (*arXiv:hep-ph/9907340*)

QCD is our most perfect physical theory

- It embodies deep and beautiful principles.
- It provides algorithms to answer any physically meaningful question within its scope.
- Its scope is wide.
- It contains a wealth of phenomena.
- It has few parameters ... or none.
- It is true.
- It lacks flaws.

Lessons: The Nature of Nature
... alien, simple, beautiful, weird,
& comprehensible





Electron Ion Collider: The Next QCD Frontier

Understanding the glue
that binds us all

SECOND EDITION

arXiv:1211.701v3 [nucl-ex] 30 Nov 2014

<http://cern.ch/lhec>

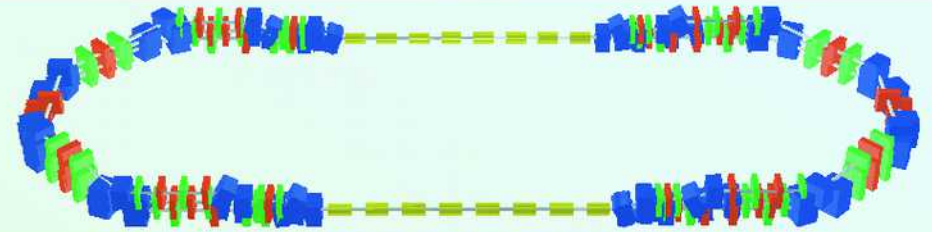
lhec.ws@cern.ch

Workshop on the LHeC

Electron-proton and electron-ion collisions at the LHC

24 June 2015 CERN

25-26 June 2015 Chavannes-de-Bogis, Switzerland



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2015 Long Range Plan for Nuclear Science 15 Oct 2015
 We recommend a high-energy high-luminosity polarized EIC as the highest priority for new facility construction following the completion of FRIB.

Expect the Unexpected

The CTEQ List of Challenges in Perturbative QCD

~1995

CTEQ

Welcome to the CTEQ List of Challenges in Perturbative QCD! Although QCD has successfully passed many tests, there are still areas where there are problems when comparing theory and experiment or where additional data or calculations are needed. Here is our current list of Challenges in Perturbative QCD. This is expected to be a dynamic list, so check back often. It is expected that existing entries will be periodically updated and that new entries will be added.

1. Direct photon production
2. Heavy quark production cross sections
3. Jet cross sections and x_T scaling
4. Determining the gluon distribution
5. Large- x behavior of parton distributions
6. Determining the flavor dependence of pdf's
7. Extracting Charged & Neutral Current Cross Sections

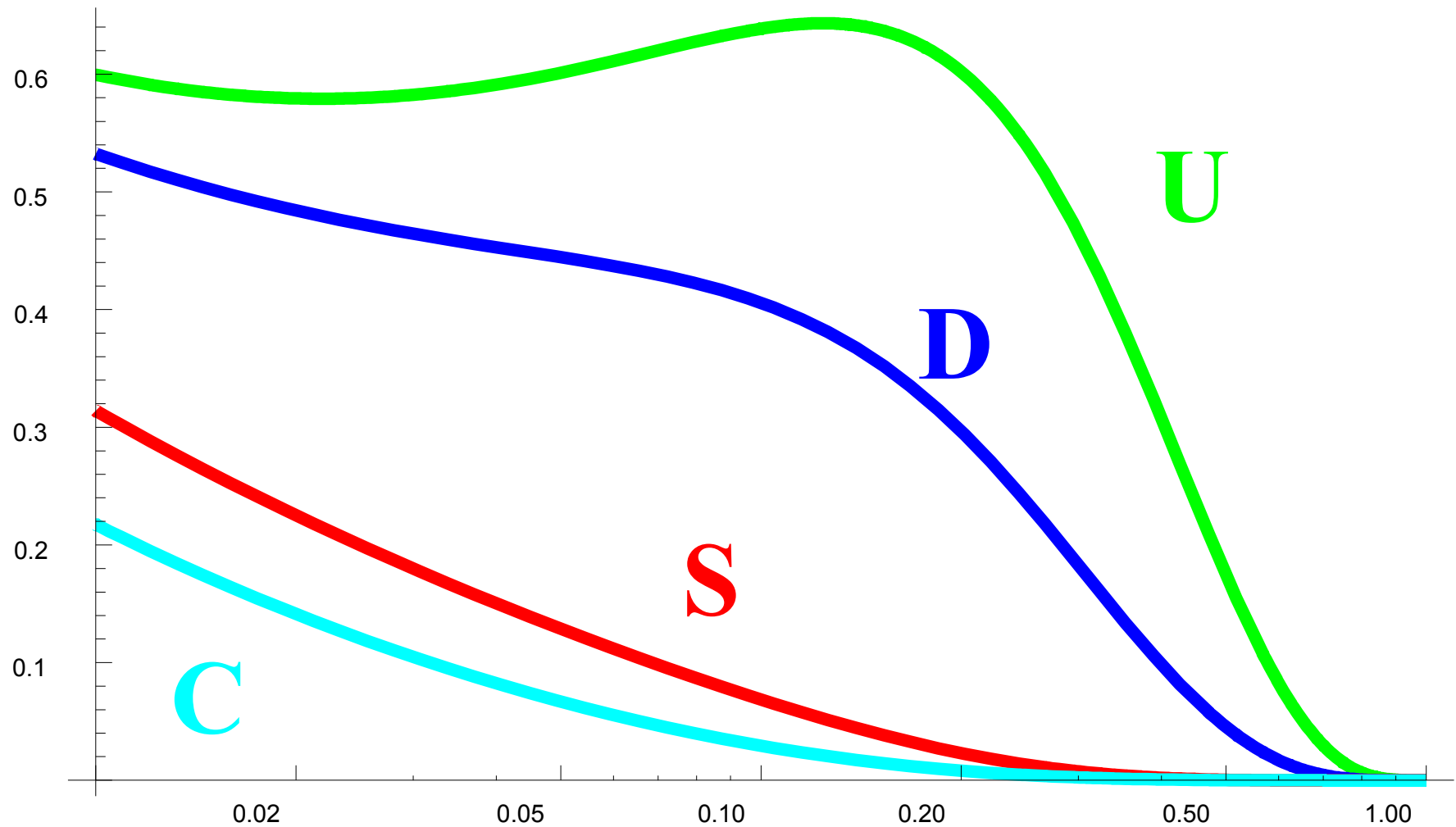
http://www.hep.fsu.edu/~owens/qcd/QCD_list.html

**1) Flavor Differentiation
& Nuclear Corrections**

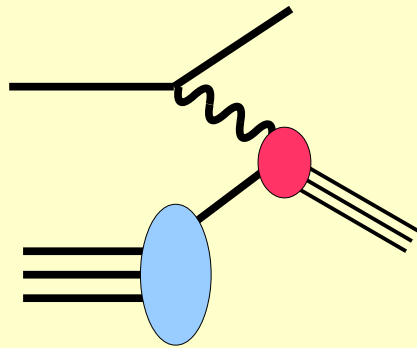
**2) Multi-scale problems:
Heavy Quarks**

**3) Hi-Order Corrections
& ACOT**

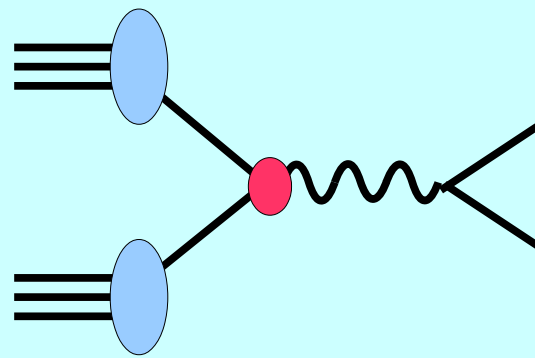
How do we differentiate flavors???



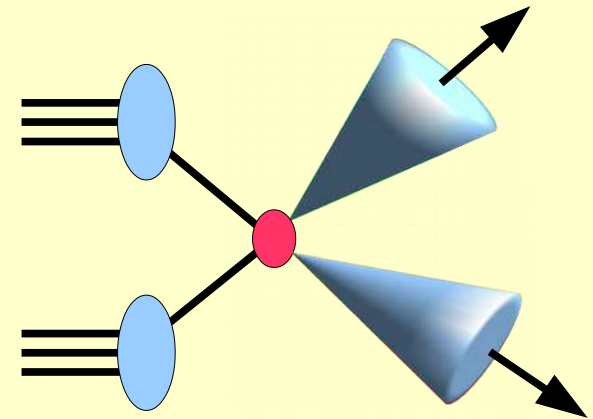
... why do we care about nuclear corrections



DIS Production



Drell-Yan



Jet Production

$$F_2^\nu \sim [d + s + \bar{u} + \bar{c}]$$

$$F_2^{\bar{\nu}} \sim [\bar{d} + \bar{s} + u + c]$$

$$F_3^\nu = 2 [d + s - \bar{u} - \bar{c}]$$

$$F_3^{\bar{\nu}} = 2 [u + c - \bar{d} - \bar{s}]$$

$$F_2^{\ell^\pm} \sim \left(\frac{1}{3}\right)^2 [d + s] + \left(\frac{2}{3}\right)^2 [u + c]$$

In particular, the DIS combinations have historically been particularly useful

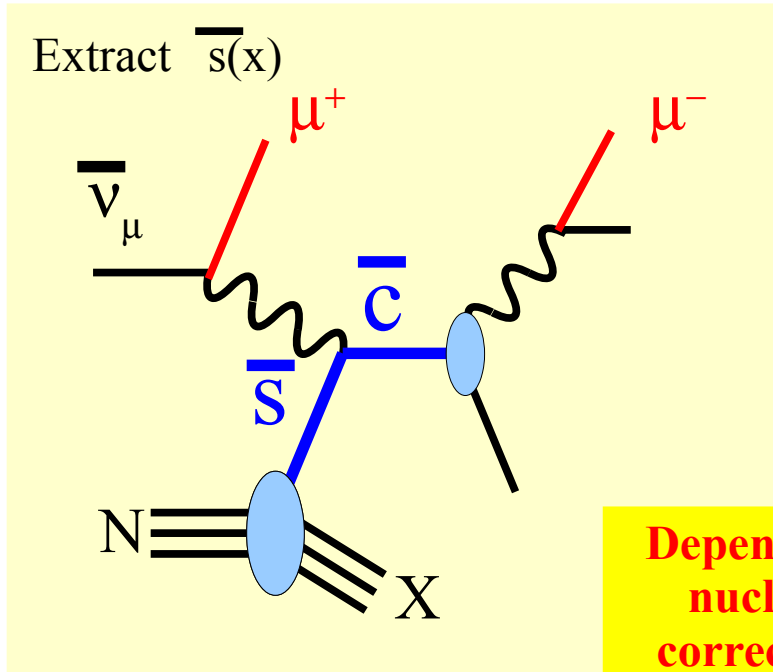
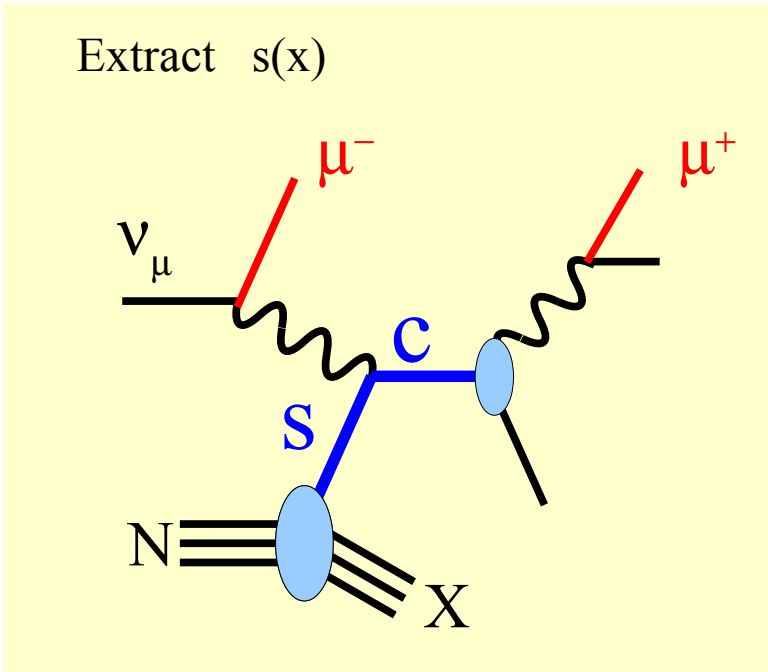
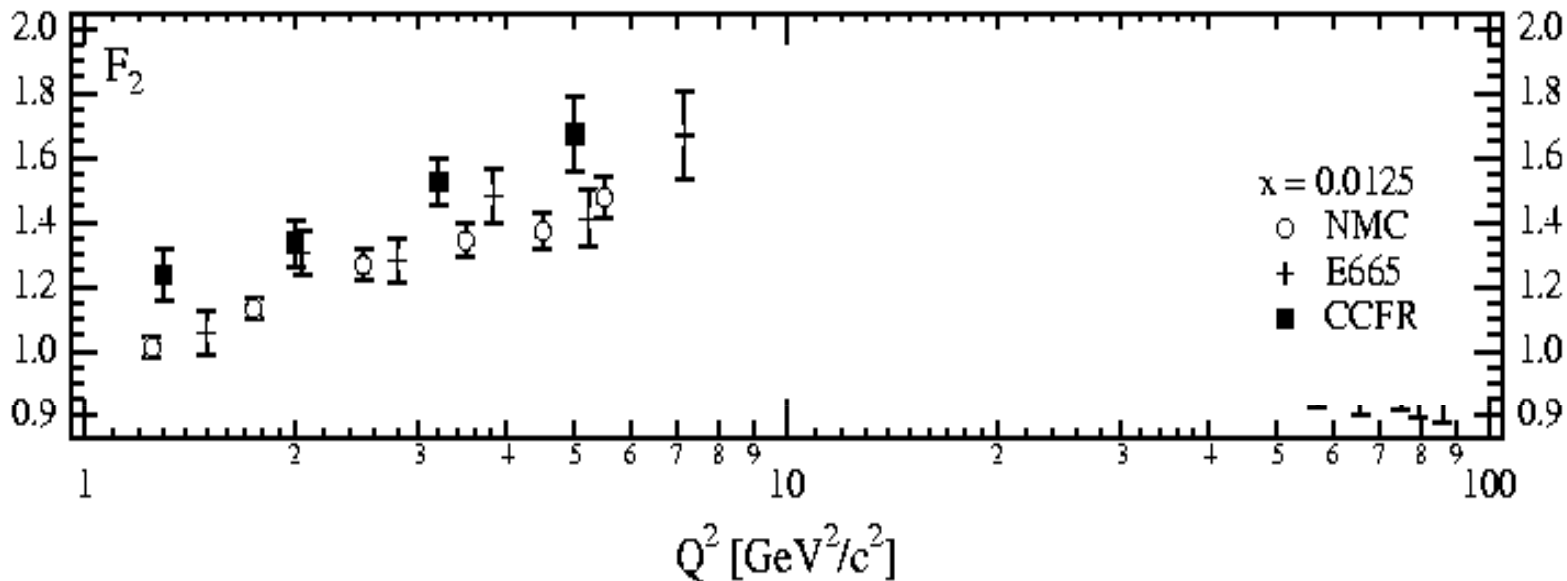
Different linear combinations – key for flavor differentiation

The ν -DIS data typically use heavy targets, and this requires the application of nuclear corrections

The CTEQ List
of Challenges in
Perturbative QCD

~1995

CTEQ

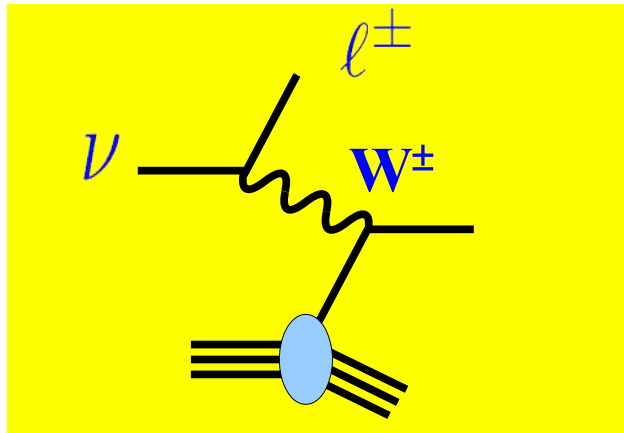
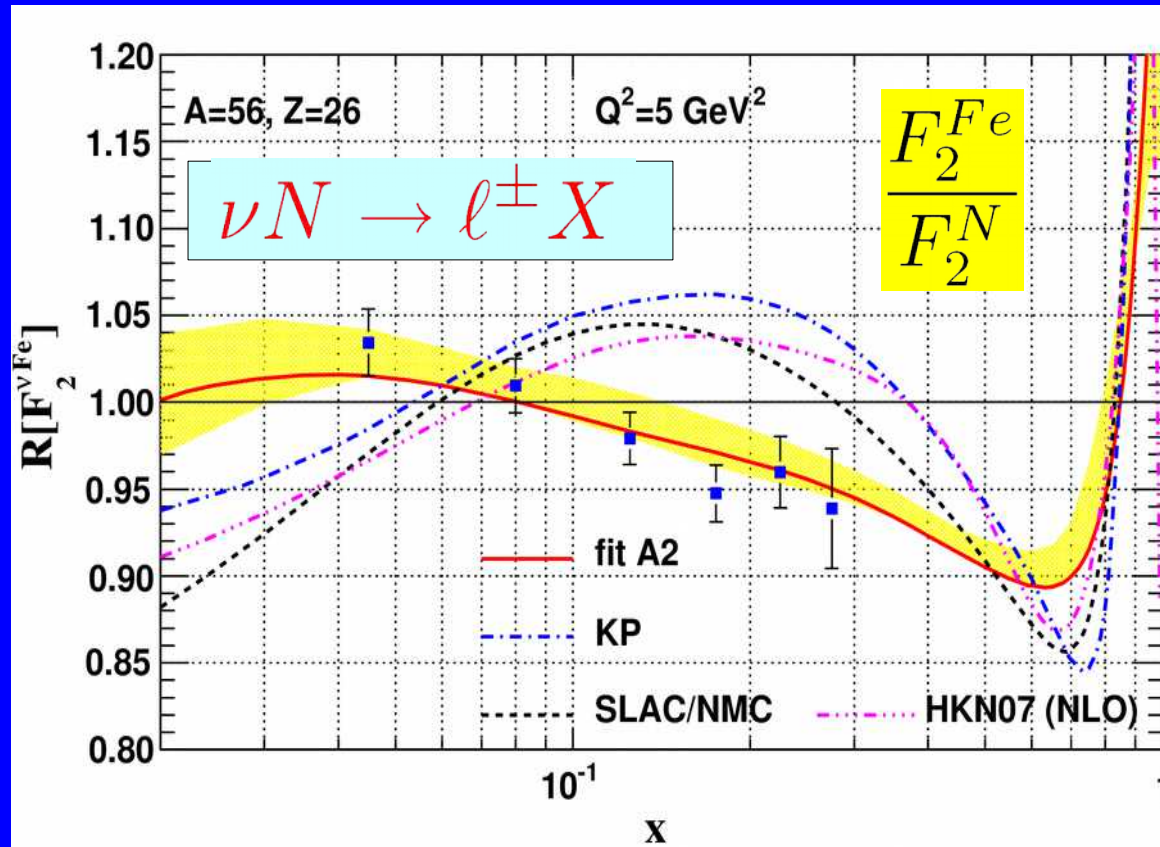
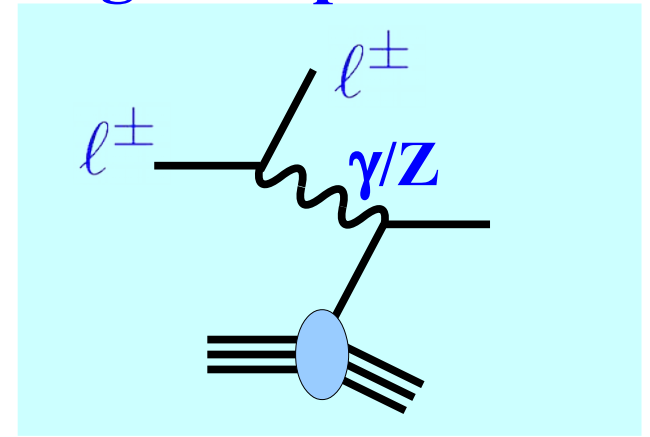


**Depends on
nuclear
corrections**

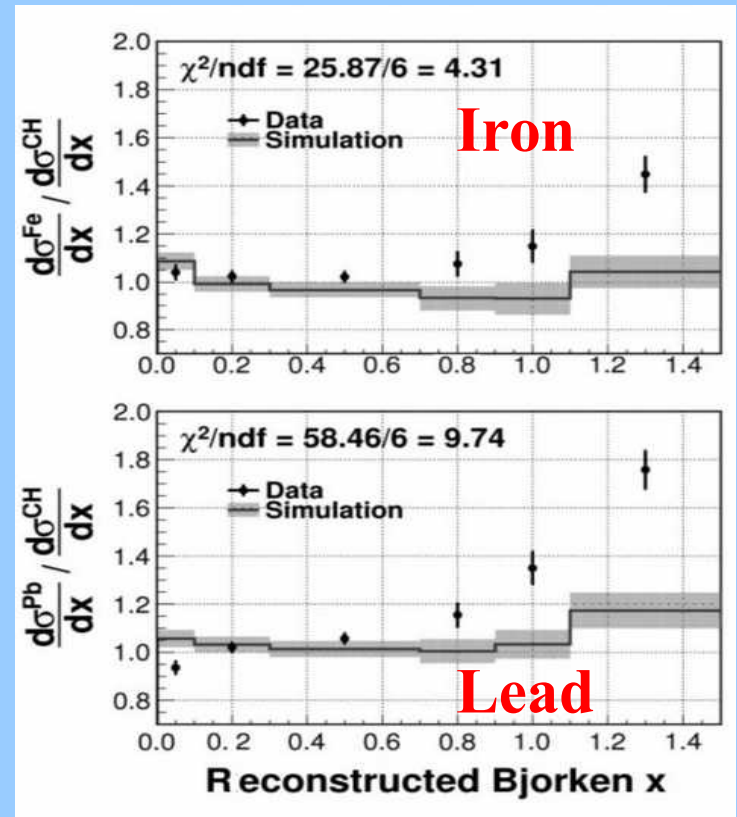
Can extract $s(x)$ and $\bar{s}(x)$ separately

Used in CTEQ Fits

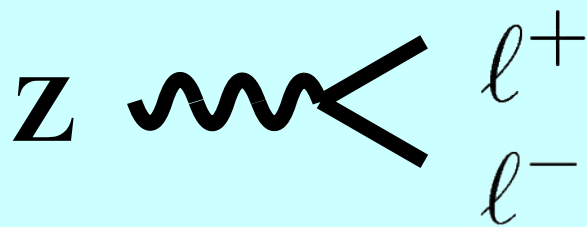
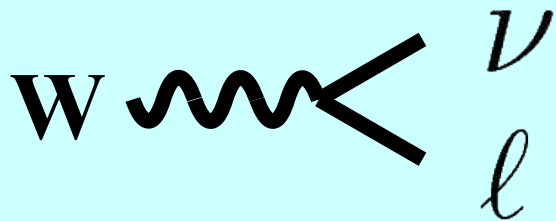
Charged Lepton DIS



Neutrino DIS

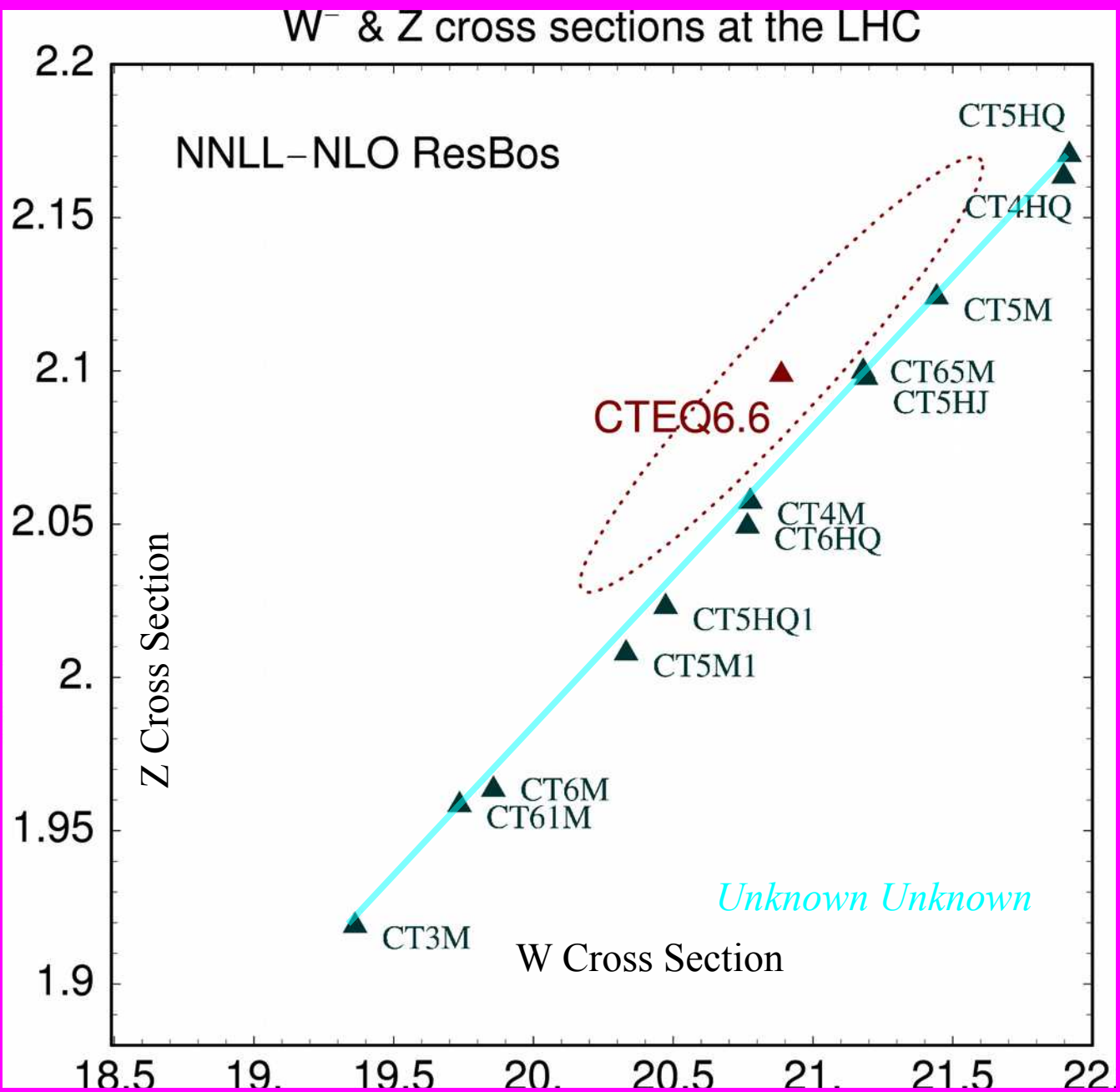


Strange Quark: Impact on LHC ... W/Z correlation \Rightarrow MW extraction¹⁴



The W-Z correlation is limited by the uncertainty coming from the strange quark distribution

Key for M_W determination



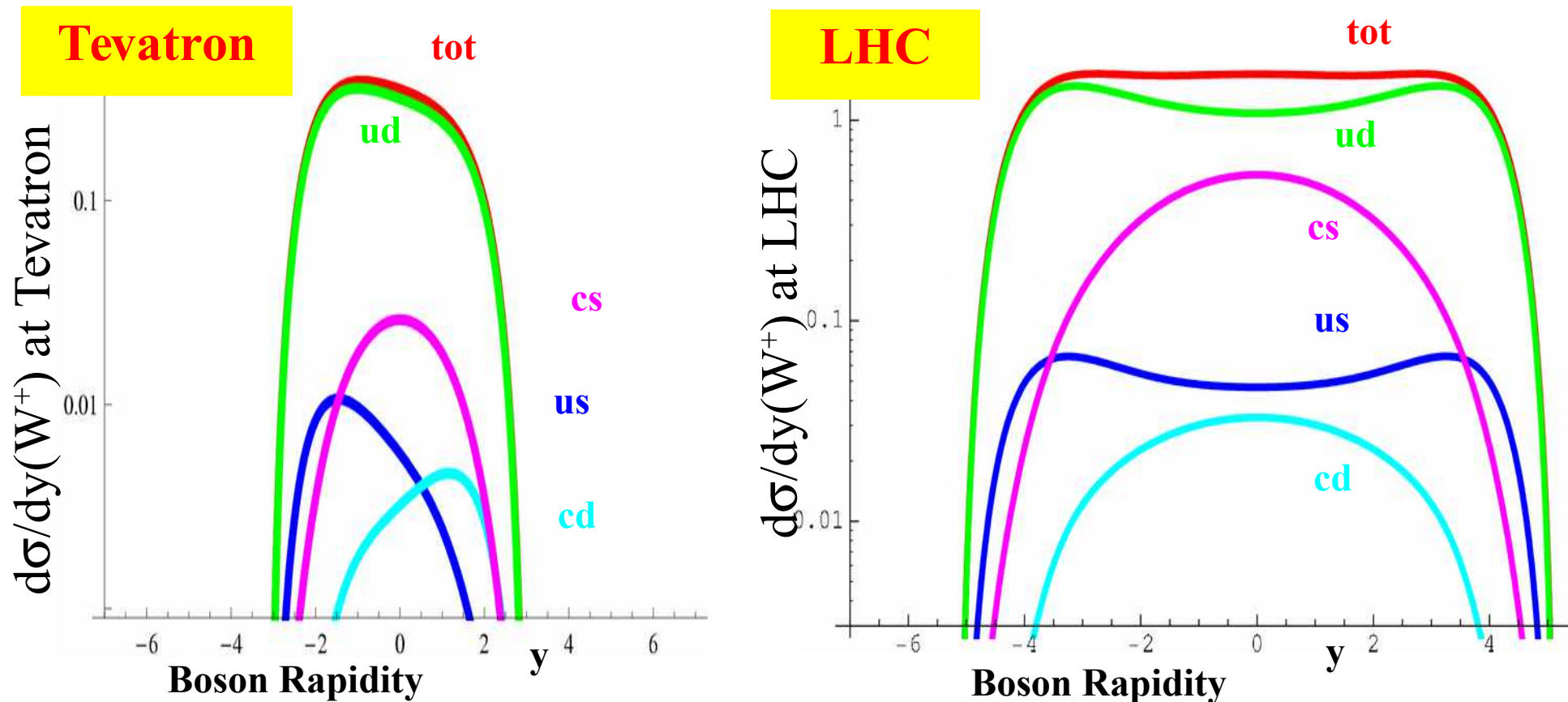
W/Z Production

“Benchmark Calculations”

... things are different at the LHC

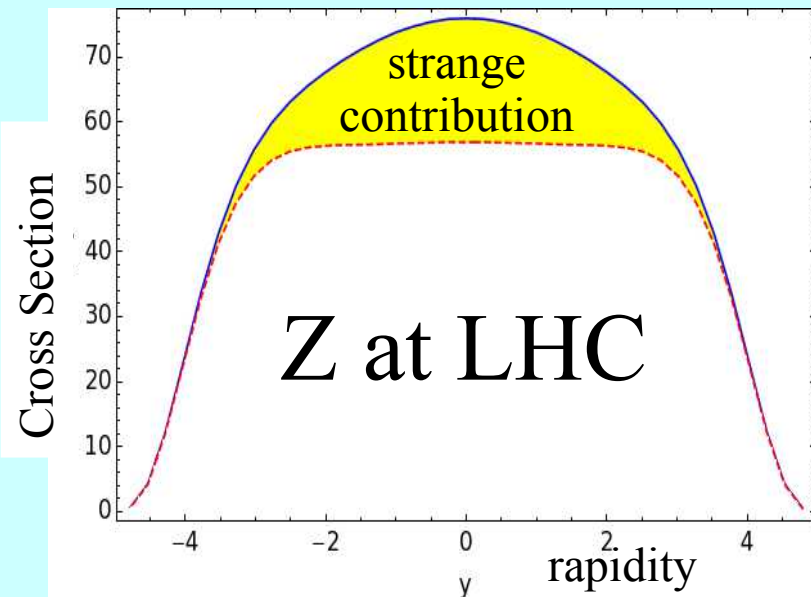
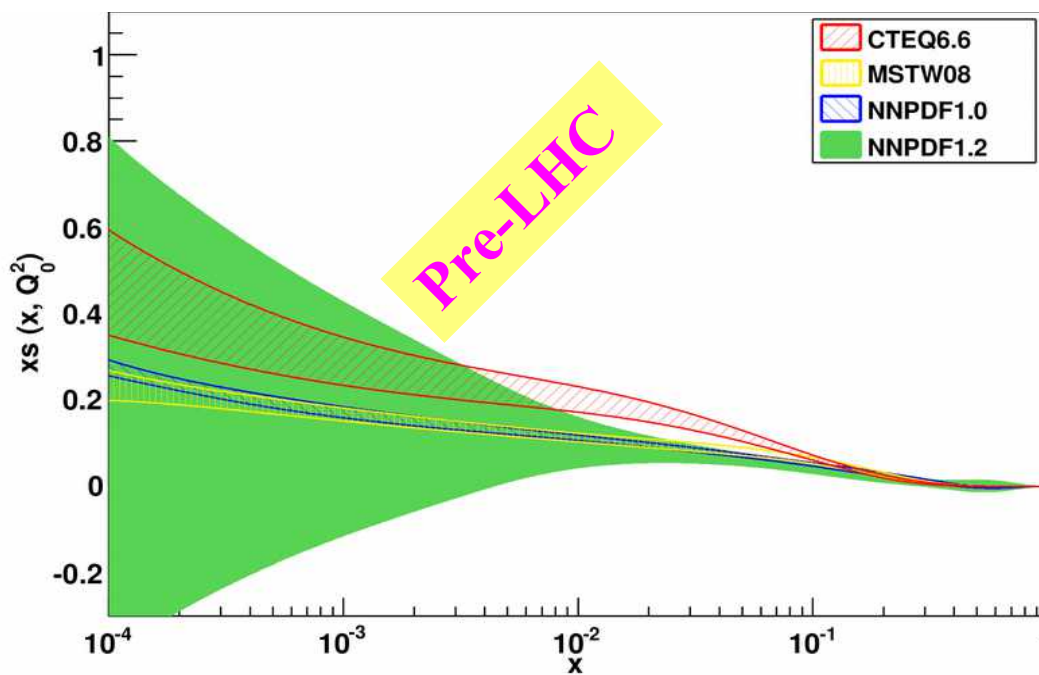
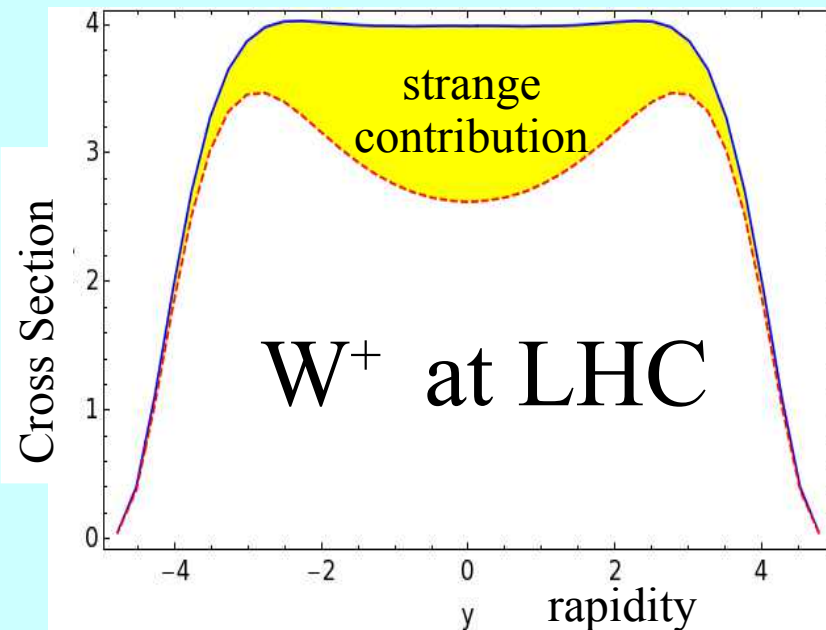
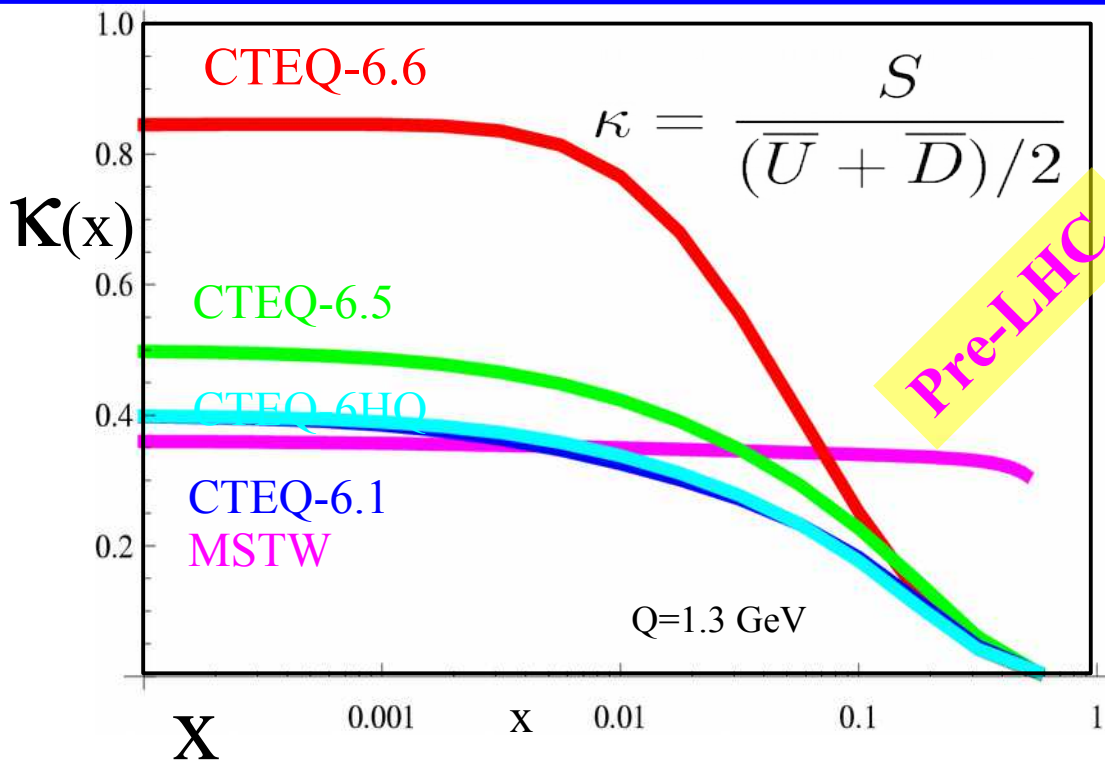
... the fine print:

Surprisingly, the LHC analysis depends on many other data sets



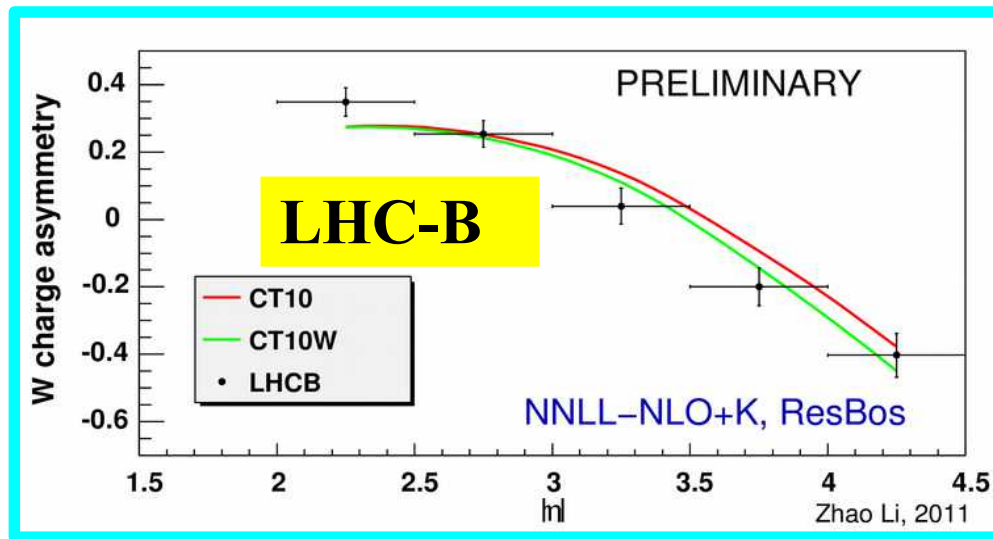
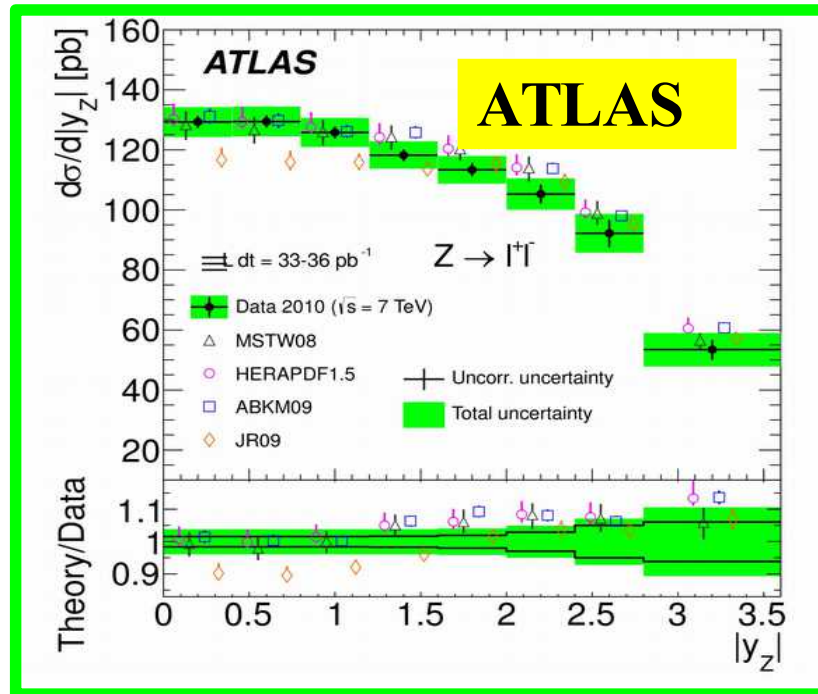
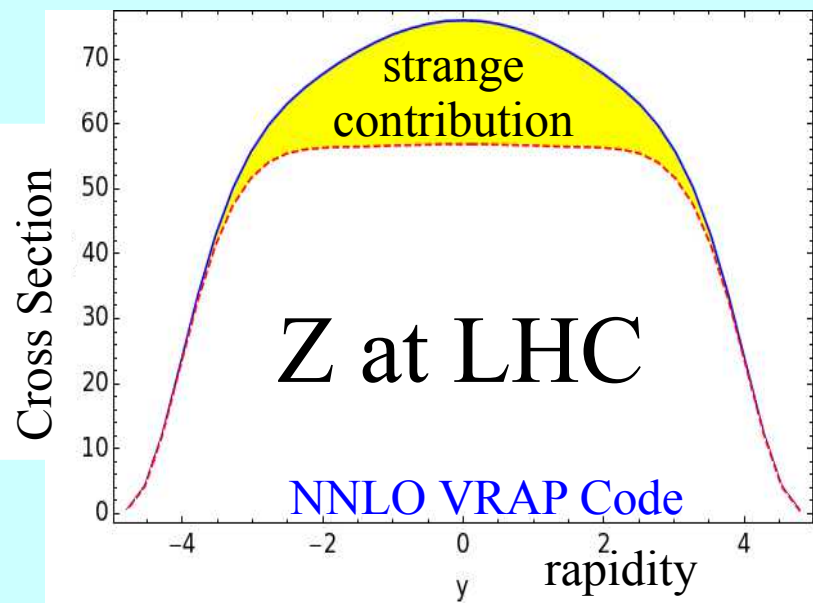
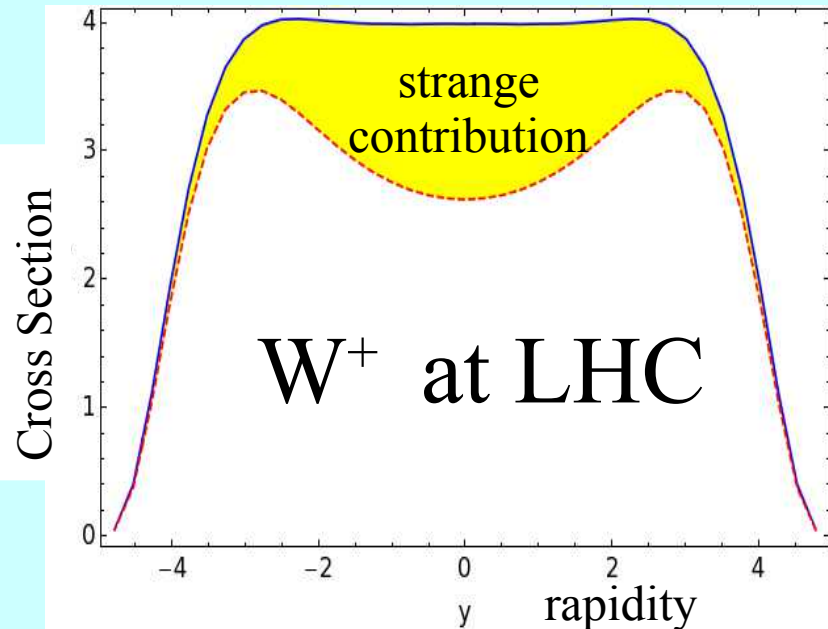
- Larger Energy \Rightarrow probes PDFs to small momentum fraction x
- Larger Rapidity (y) \Rightarrow probes PDFs to *really* small x
- Larger fraction of heavy quarks

Heavy Quark components play an increasingly important role at the LHC



VRAP
Code

Anastasiou, Dixon, Melnikov, Petriello,
Phys.Rev.D69:094008,2004.



NNLO VRAP Code
Anastasiou, Dixon, Melnikov, Petriello,
Phys.Rev.D69:094008,2004.

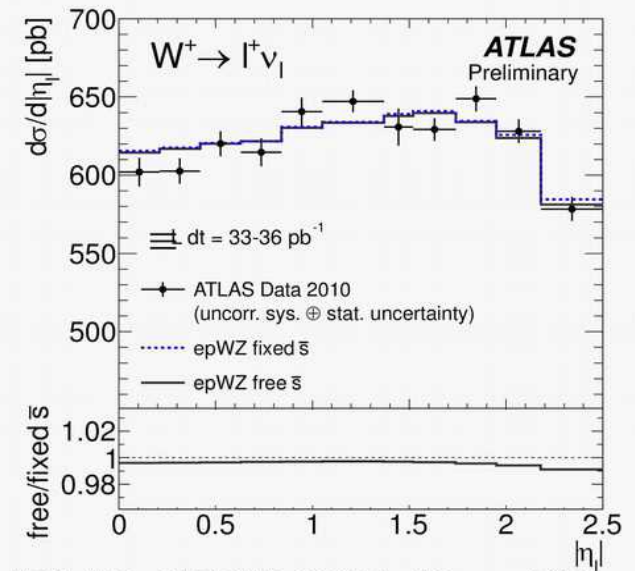
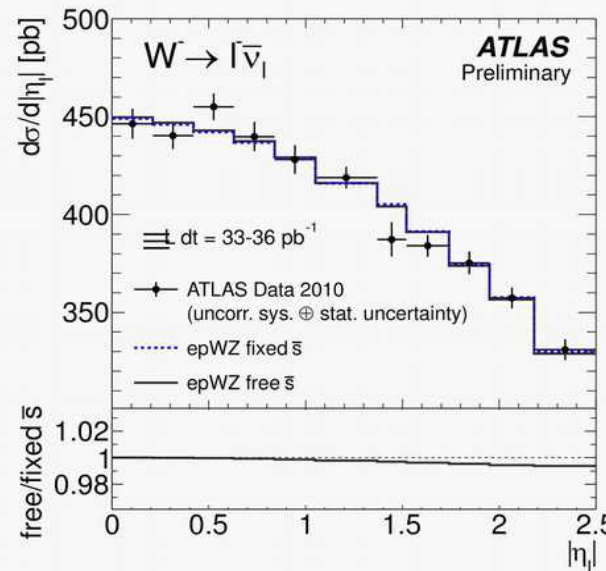
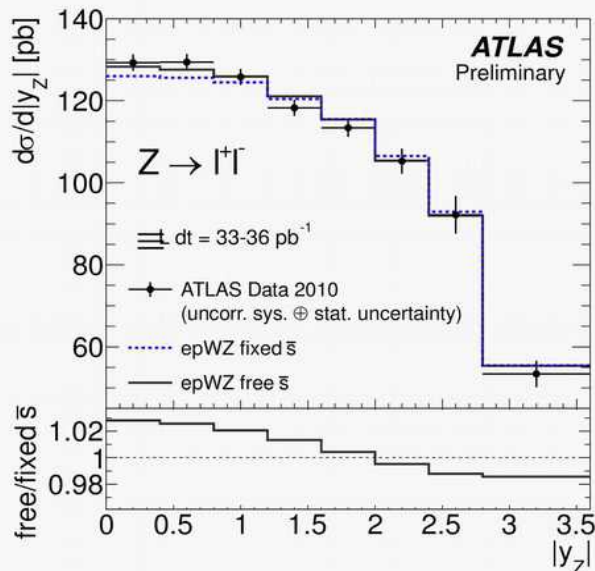
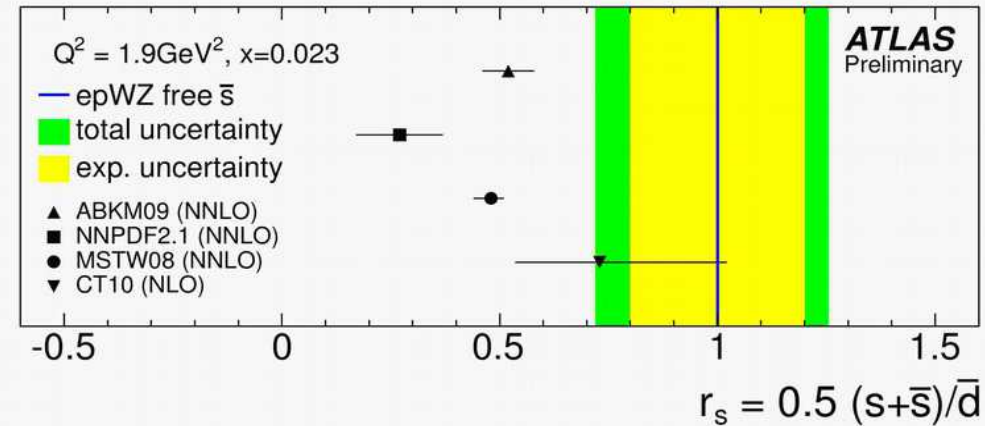
Kusina, Stavreva, Berge, Olness,
Schienbein, Kovarik, Jezo, Yu, Park
Phys.Rev. D85 (2012) 094028

**y distribution shape
can constrain s(x) PDF**

W, Z data sensitivity to strange sea

- ATLAS performed NNLO QCD fit to Z, W^+, W^- + HERA ep DIS cross sections: significant tension for Z observed when suppressing strange by 50% at low scale 1.9 GeV^2
- Fit with free strange sea gives no suppression

$$r_s = 1.00 \pm 0.20_{\text{exp}} \begin{matrix} +0.16 \\ -0.20 \text{ sys} \end{matrix}$$



CT14 strange quark PDF

- Conflicting results from experiments:

- **ATLAS** $r^s = \frac{\bar{s}(x, Q)}{\bar{d}(x, Q)} = 0.96^{+0.26}_{-0.30}$ at $x = 0.023$, $Q = 1.4$ GeV

$$r_{\text{CT14NNLO}}^s = 0.53 \pm 0.20$$

$$r_{\text{CT10NNLO}}^s = 0.76 \pm 0.17$$

- **CMS** $K^s = \frac{\int_0^1 x [s(x, Q) + \bar{s}(x, Q)] dx}{\int_0^1 x [\bar{u}(x, Q) + \bar{d}(x, Q)] dx} = 0.52^{+0.18}_{-0.15}$ at $Q^2 = 20$ GeV²

- **NOMAD** $K^s = 0.591 \pm 0.019$

$$K_{\text{CT14NNLO}}^s = 0.62 \pm 0.14$$

$$K_{\text{CT10NNLO}}^s = 0.73 \pm 0.11$$



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HERAFitter



Welcome to HERAFitter Project

HERAFitter is a QCD Fit Package used to determine HERAPDFs and it is part of the HERAPDF project <https://www.desy.de/h1zeus>.

Downloads of HERAFitter software package

New HERAFitter HERE upon registra

Registration

To register, please l
(firstnamelastname
<herafitter-help

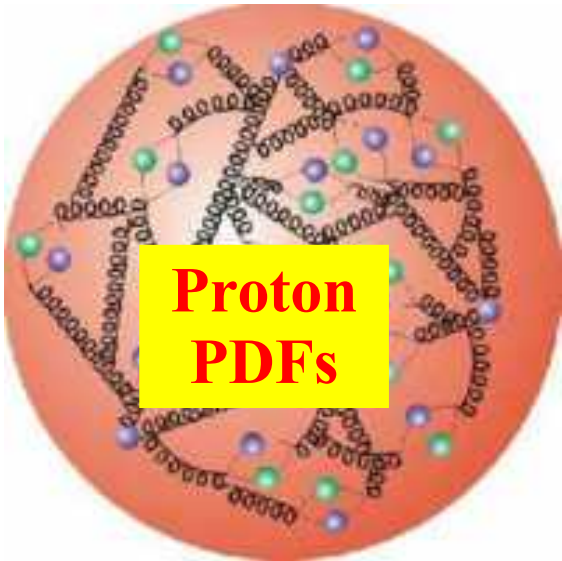
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- User's Meeti
and develop

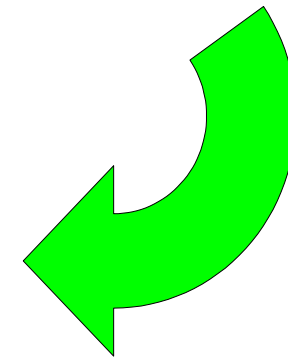
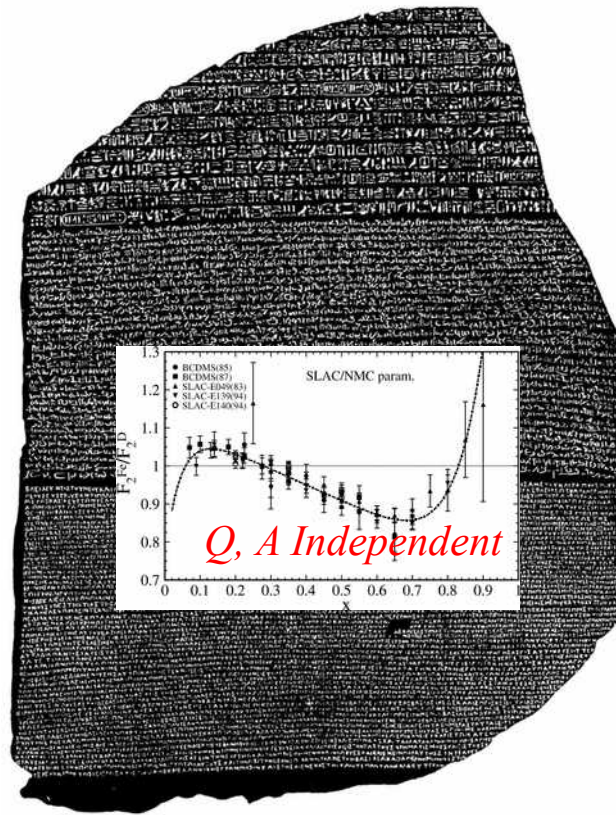
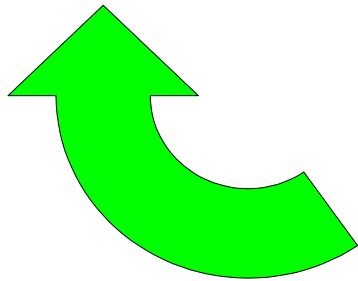
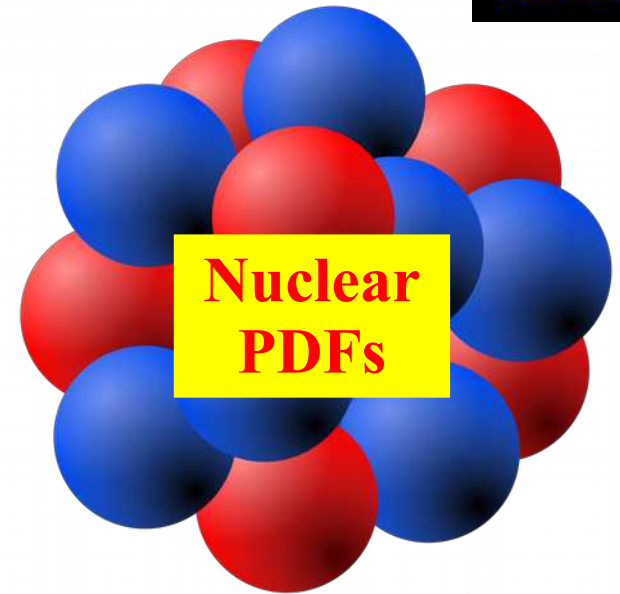


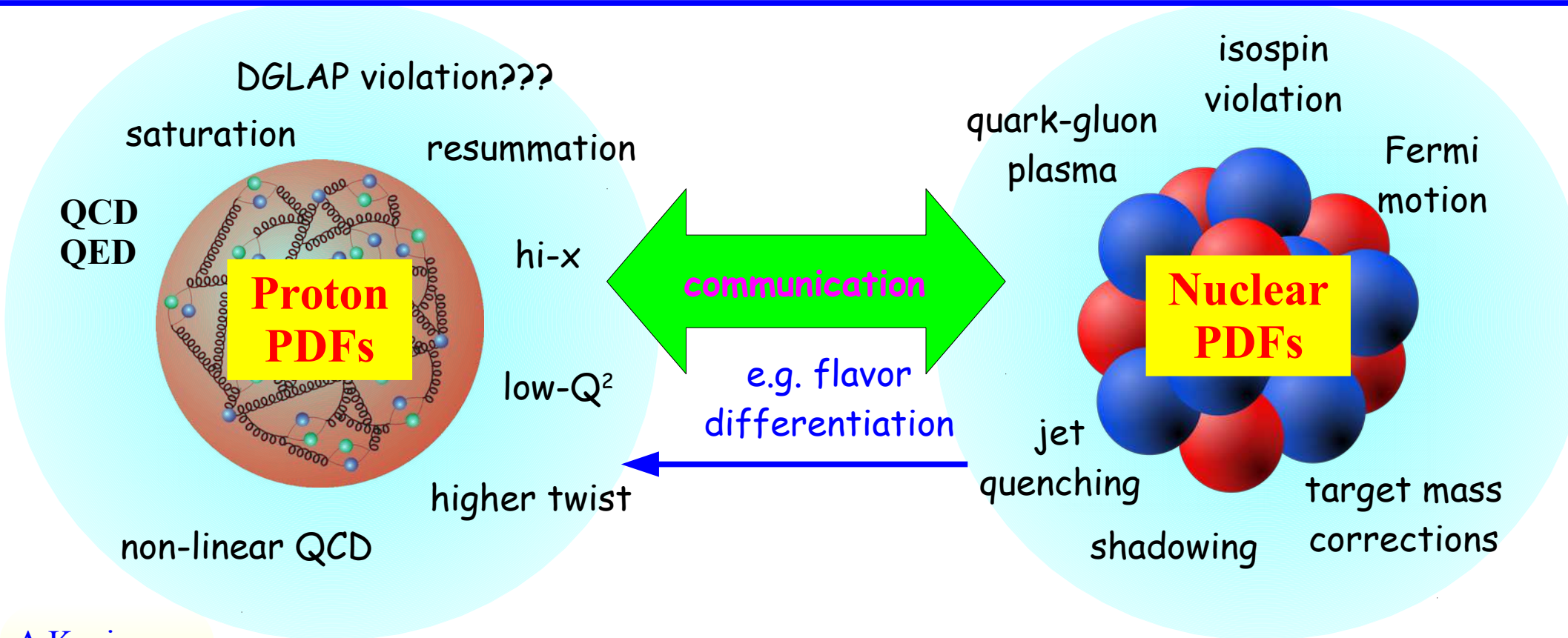
nCTEQ 15

PDFs



... there was a time when
nuclear corrections
were carved in stone ...



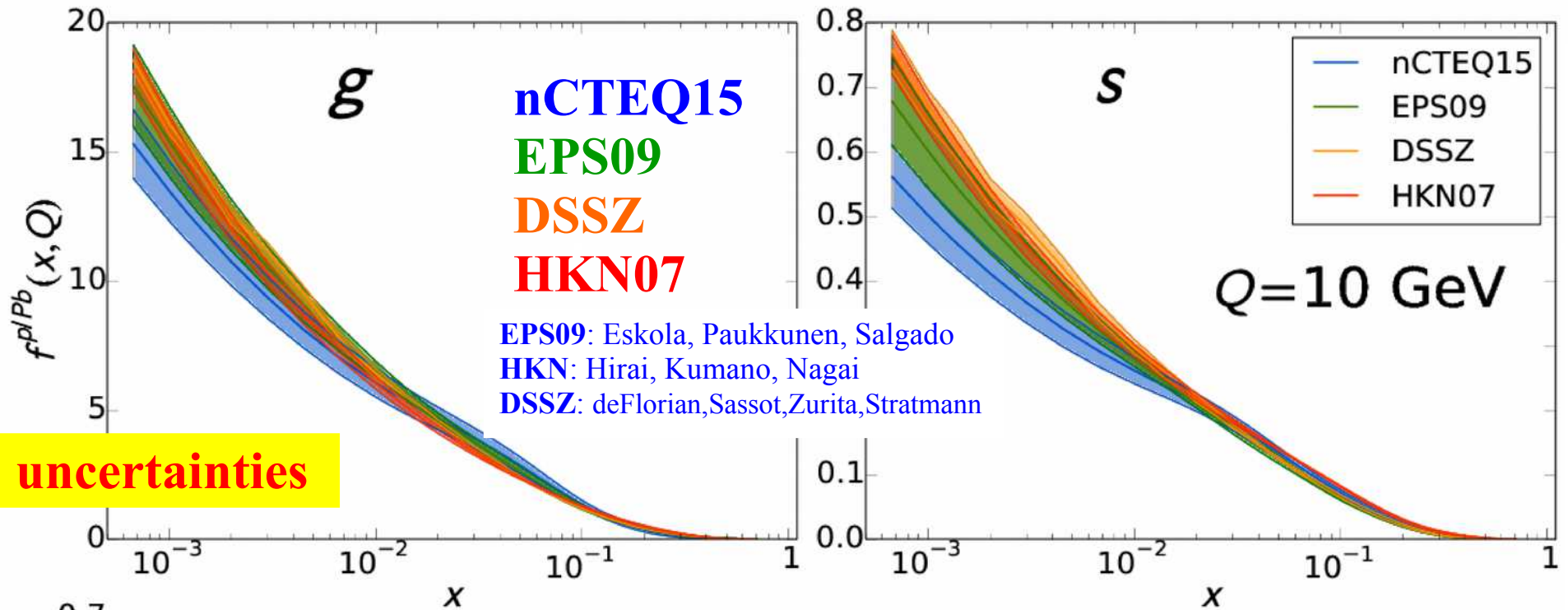
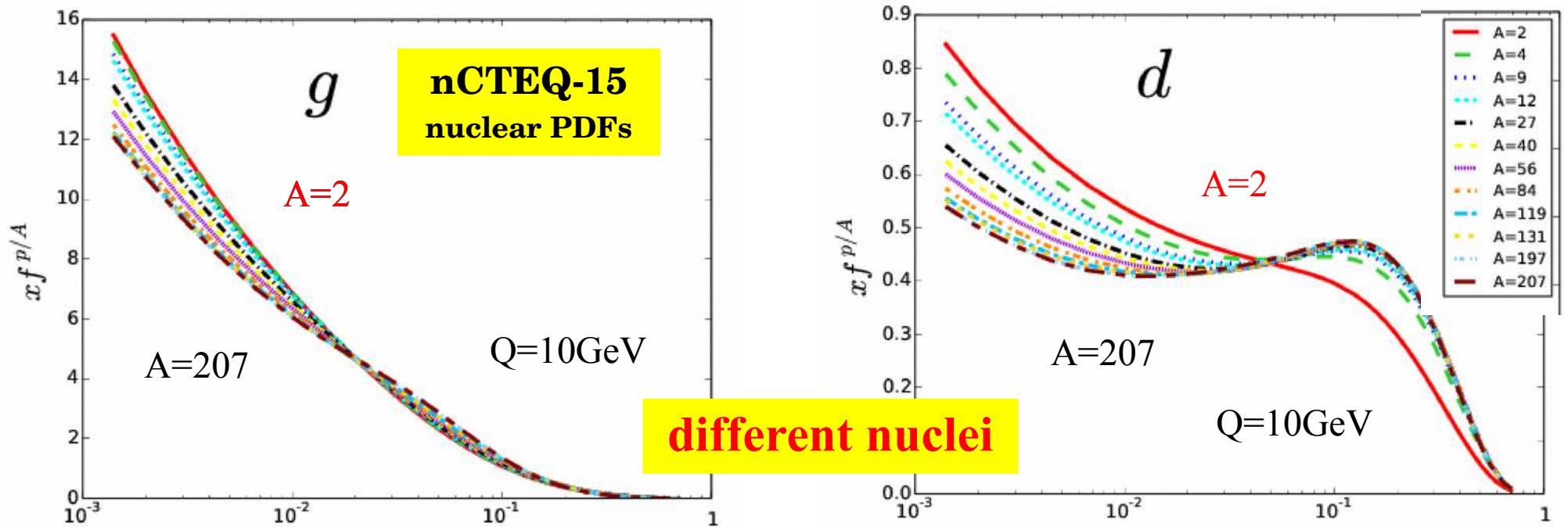


A Kusina,
K. Kovarik
T. Jezo,
D. Clark,
C. Keppel,
F. Lyonnet,
J. Morfin,
F. Olness
J. Owens,
I. Schienbein,
J. Yu
E. Godat

Data from nuclear targets is play a key role in the flavor differentiation

nCTEQ-15
nuclear parton distribution functions

... the original motivation for nCTEQ15



F_2^A/F_2^D : Observable	Experiment	ID	Ref.	# data	# data after cuts	χ^2
D	NMC-97	5160	47	292	201	247.73
He/D	Hermes	5156	48	182	17	18.02
	NMC-95,re	5124	49	18	12	10.64
	SLAC-E139	5141	50	18	3	1.04
Li/D	NMC-95	5115	51	24	11	3.94
Be/D	SLAC-E139	5138	50	17	3	0.44
C/D	FNAL-E665-95	5125	52	11	3	3.53
	SLAC-E139	5139	50	7	2	1.15
	EMC-88	5107	53	9	9	7.06
	EMC-90	5110	54	9	0	0.00
	NMC-95	5113	51	24	12	7.39
	NMC-95,re	5114	49	18	12	13.36
	N/D	Hermes	5157	48	175	19
Al/D	BCDMS-85	5103	55	9	9	4.66
	SLAC-E049	5134	56	18	0	0.00
Ca/D	SLAC-E139	5136	50	17	3	0.66
	NMC-95,re	5121	49	18	12	12.24
	FNAL-E665-95	5126	52	11	3	4.87
Fe/D	SLAC-E139	5140	50	7	2	1.43
	EMC-90	5109	54	9	0	0.00
	SLAC-E049	5131	57	14	2	0.67
	SLAC-E139	5132	50	23	6	8.20
	SLAC-E140	5133	58	10	0	0.00
	BCDMS-87	5101	59	10	10	6.47
	BCDMS-85	5102	55	6	6	2.83
Cu/D	EMC-93	5104	60	10	9	4.31
	EMC-93(chariot)	5105	60	9	9	5.72
	EMC-88	5106	53	9	9	3.97
Kr/D	Hermes	5158	48	167	12	9.68
Ag/D	SLAC-E139	5135	50	7	2	1.36
Sn/D	EMC-88	5108	53	8	8	17.88
Xe/D	FNAL-E665-92	5127	61	10	2	0.74
Au/D	SLAC-E139	5137	50	18	3	1.55
Pb/D	FNAL-E665-95	5129	52	11	3	5.91
Total:				1205	414	417.92

$F_2^A/F_2^{A'}$: Observable	Experiment	ID	Ref.	# data	# data after cuts	χ^2
C/Li	NMC-95,re	5123	49	25	7	5.22
Ca/Li	NMC-95,re	5122	49	25	7	1.49
Be/C	NMC-96	5112	62	15	14	7.25
Al/C	NMC-96	5111	62	15	14	4.98
	NMC-95,re	5120	49	25	7	3.31
Ca/C	NMC-96	5119	62	15	14	5.18
	NMC-96	5143	62	15	14	10.38
Fe/C	NMC-96	5159	63	146	111	62.95
Pb/C	NMC-96	5116	62	15	14	9.09
Total:				296	202	109.85

Table II: The DIS $F_2^A/F_2^{A'}$ data sets used in the nCTEQ15 fit. We list the same details for each data set as in Tab. [I](#).

$\sigma_{DY}^{pA}/\sigma_{DY}^{pA'}$: Observable	Experiment	ID	Ref.	# data	# data after cuts	χ^2
C/H2	FNAL-E772-90	5203	64	9	9	11.10
Ca/H2	FNAL-E772-90	5204	64	9	9	3.11
Fe/H2	FNAL-E772-90	5205	64	9	9	3.33
W/H2	FNAL-E772-90	5206	64	9	9	7.30
Fe/Be	FNAL-E886-99	5201	65	28	28	26.09
W/Be	FNAL-E886-99	5202	65	28	28	25.61
Total:				92	92	76.54

Table III: The Drell-Yan process data sets used in the nCTEQ15 fit. We list the same details for each data set as in Tab. [I](#).

R_{dAu}^π/R_{pp}^π : Observable	Experiment	ID	Ref.	# data	# data after cuts	χ^2
dAu/pp	PHENIX	PHENIX	66	21	20	5.07
	STAR-2010	STAR	67	13	12	1.30
Total:				34	32	6.37

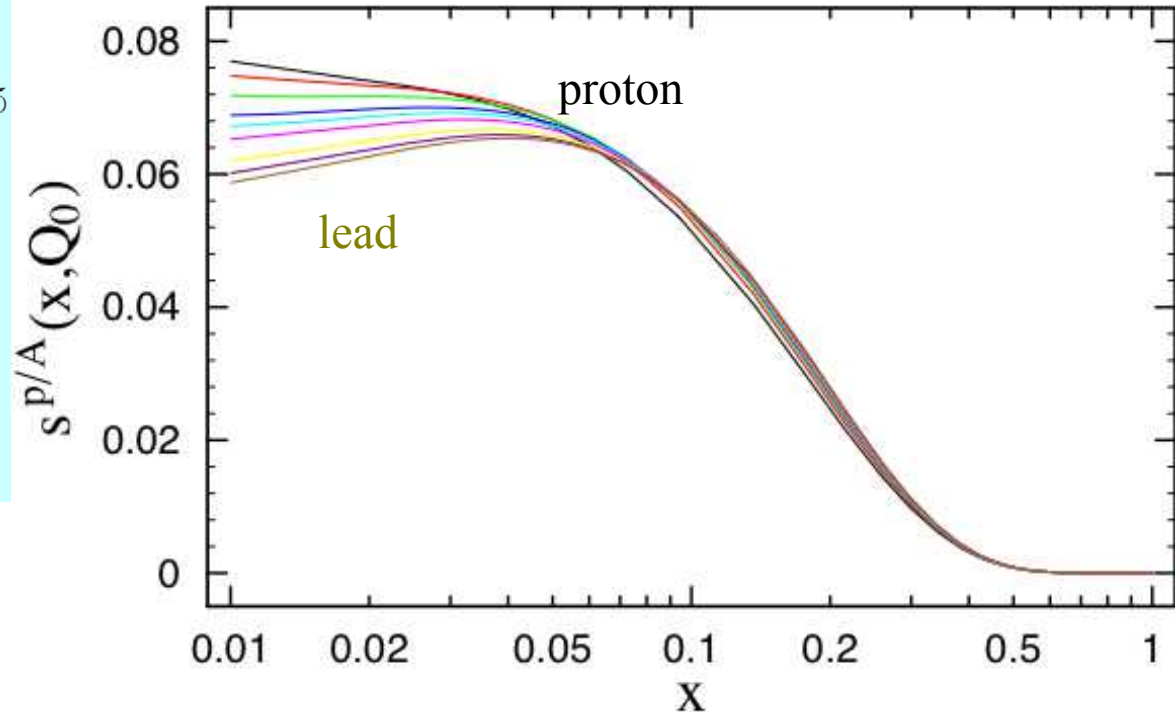
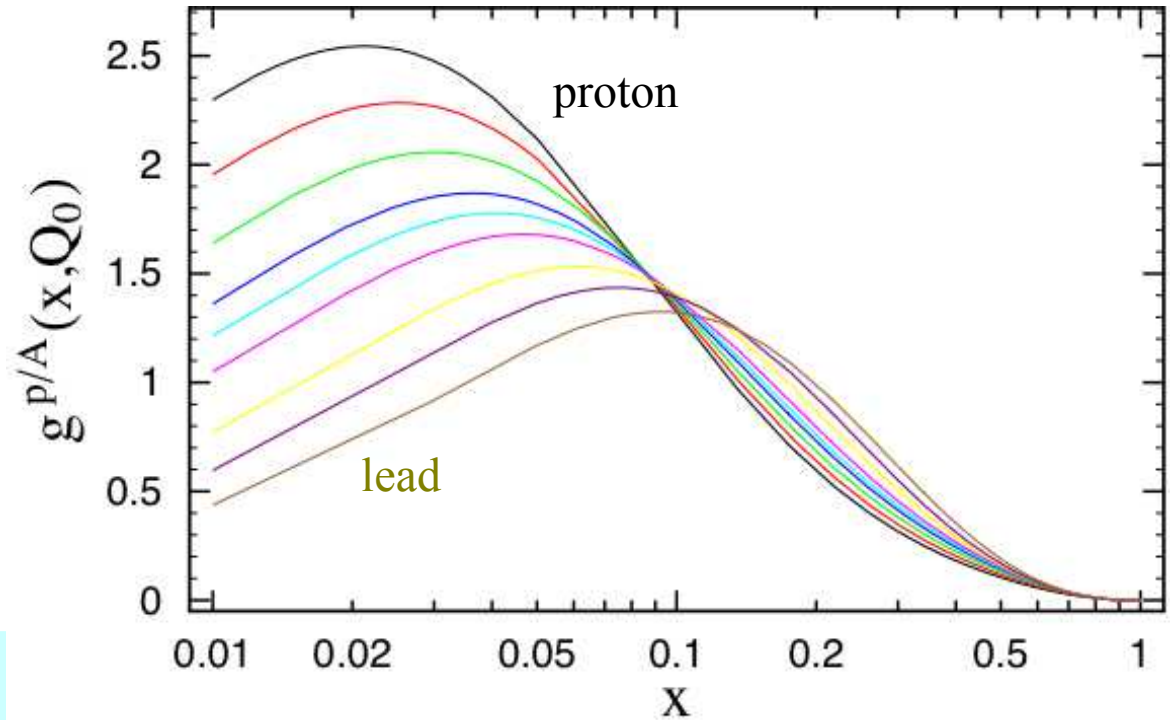
- ✓ CTEQ style global fit extended handle various nuclear targets
- ✓ CTEQ Data + nuclear DIS & DY [~ 15 targets; $\sim 2000+$ data]
- ✓ A-dependence modeled; NLO fits work well

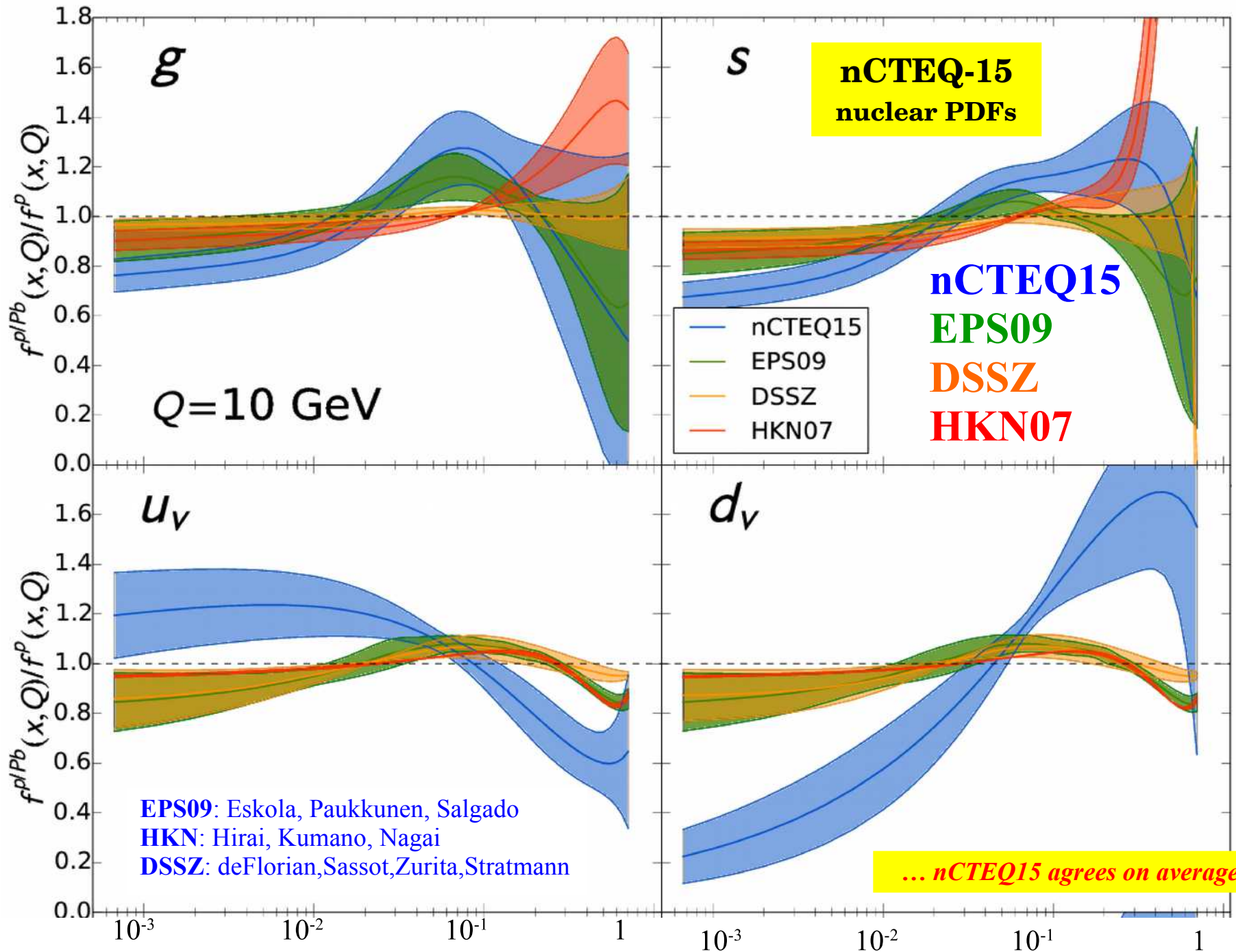
A-Dependent PDFs

$$xf(x) = x^{a_1}(1-x)^{a_2}e^{a_3x}(1+e^{a_4x})^{a_5}$$

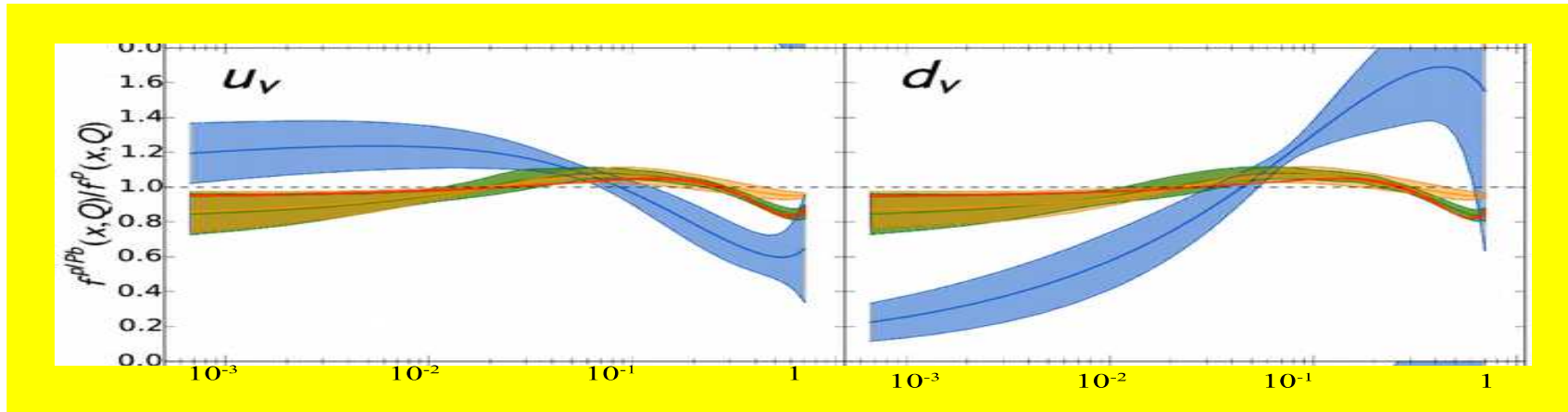
$$a_i \rightarrow a_i(A)$$

$$a_k = a_{k,0} + a_{k,1}(1 - A^{-a_{k,2}})$$

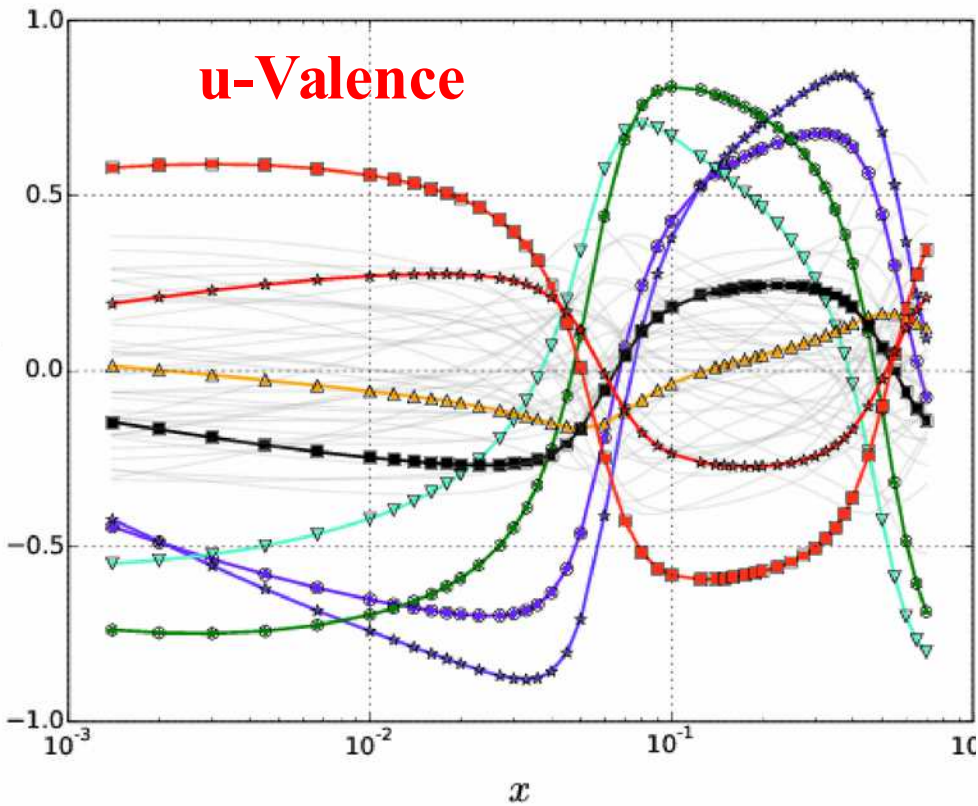




What data are influencing up & down



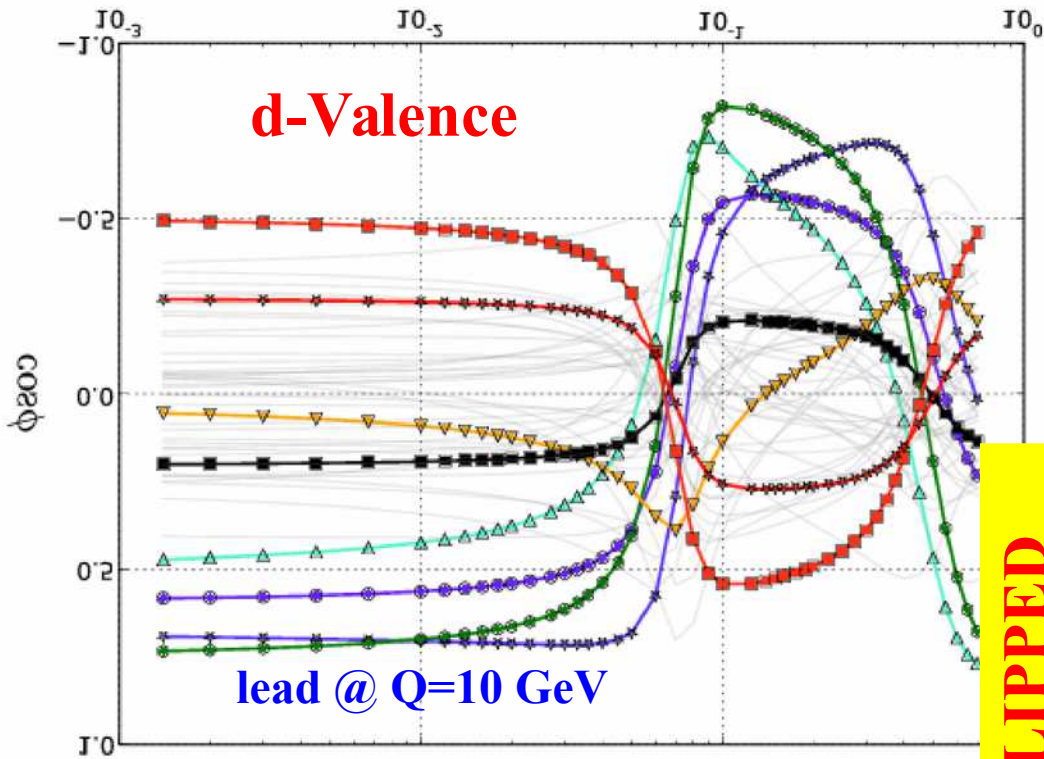
u-Valence



- DIS: Ca/Li (NMC-95,re)
- DIS: C/Li (NMC-95,re)
- DIS: He/D (NMC-95,re)
- DIS: He/D (Hermes)
- DIS: Sn/C (NMC-96)
- π^0 : DAu/pp (PHENIX)
- DIS: C/D (NMC-95,re)
- DIS: Pb/C (NMC-96)
- Other Experiments

- DIS: He/D (NMC-95,re)
- DIS: C/Li (NMC-95,re)
- DIS: C^e/Li (NMC-95,re)
- u_0 : D^0n^0/bb (БНЕНИХ)
- DIS: Sn/C (NMC-96)
- DIS: He/D (Hermes)
- DIS: Pb/C (NMC-96)
- DIS: C/D (NMC-95,re)
- Other Experiments

d-Valence



lead @ Q=10 GeV

FLIPPED

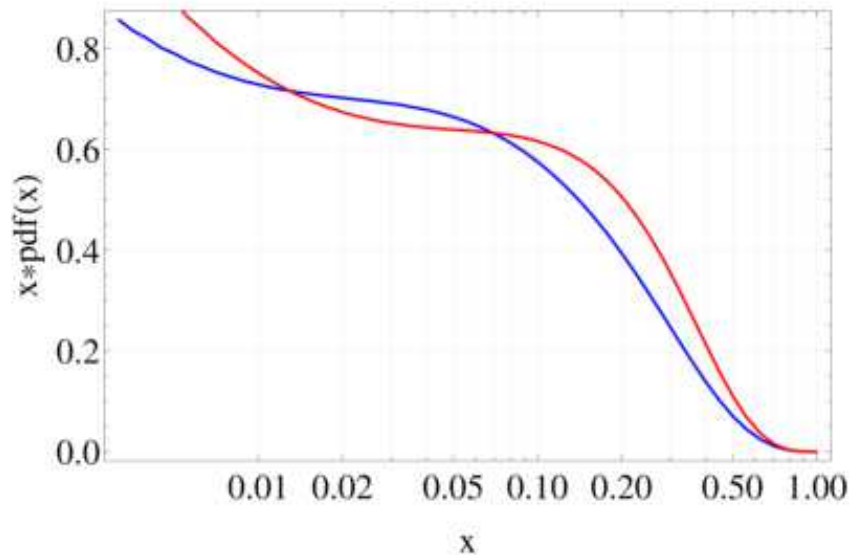
Heavy Ion *@* LHC

Nuclear Modifications

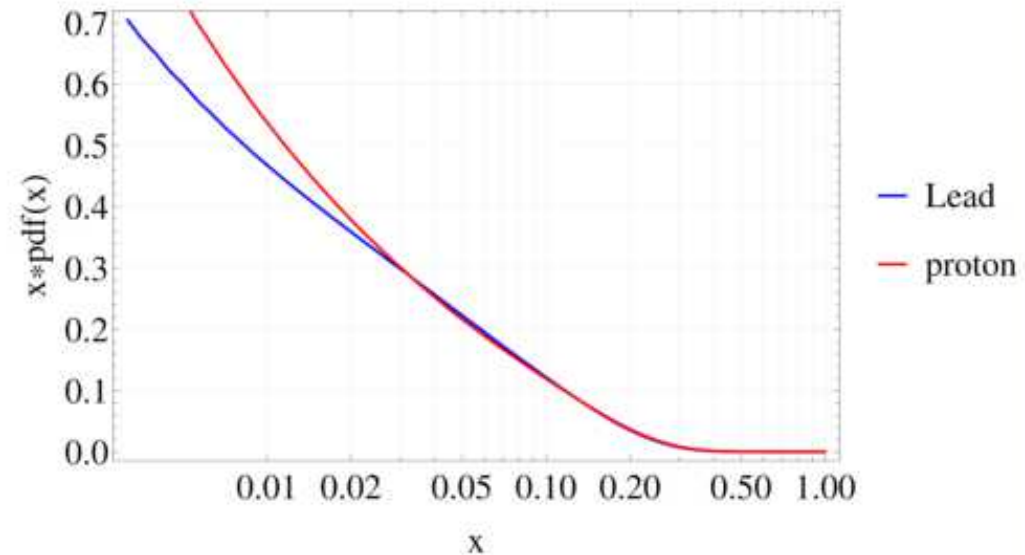
Slides stolen
from Ben Clark



up at 80 Gev



dbar at 80 Gev

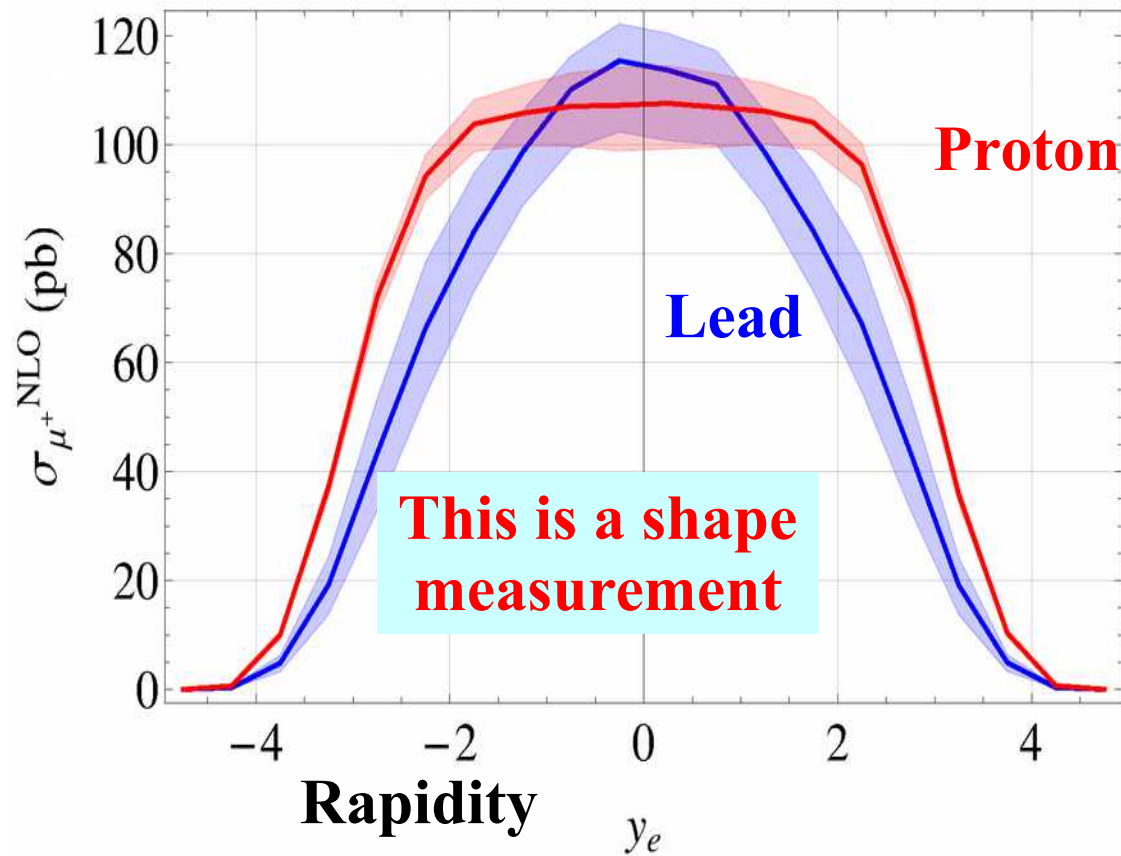


- The nuclear modifications are present in the PDFs and vary with A as well as x and Q .
- We expect modifications to any hadronic observable involving heavy nuclei.

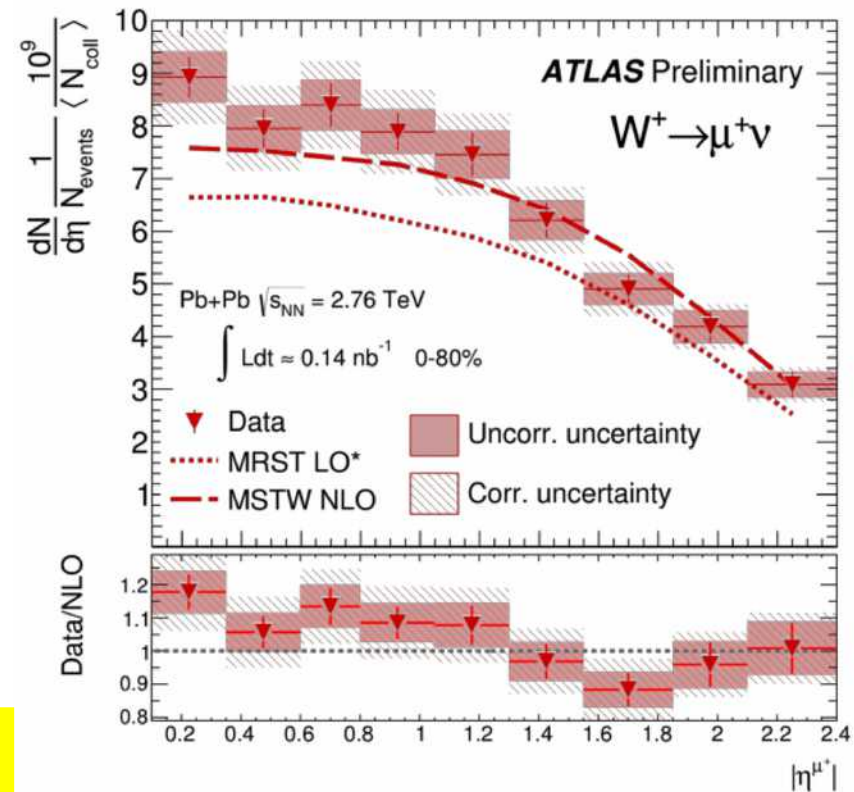
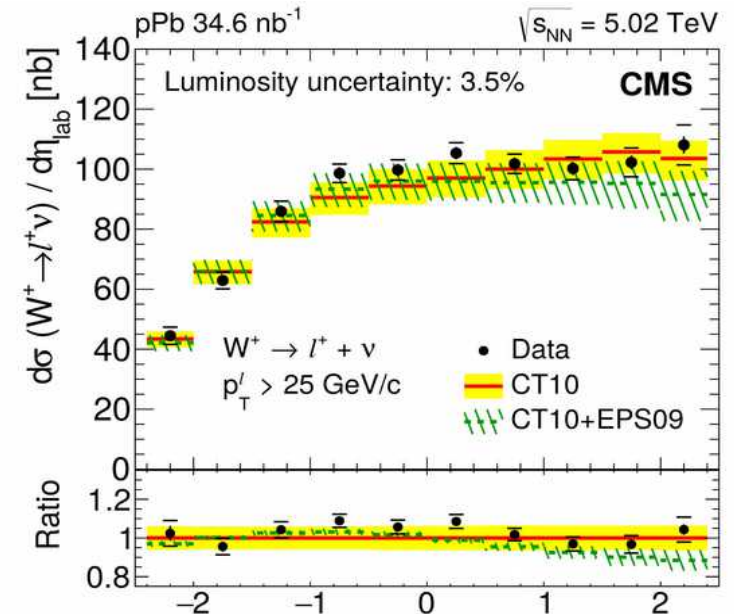


$$W^+ \rightarrow \mu^+ \nu$$

FEWZ $\mu^{+,NLO}$ at 2.76 TeV



Similar studies with Z:
ATLAS just released 2013 Z data for p-Pb at 5.02 TeV



... what about

Heavy Quarks

...

charm

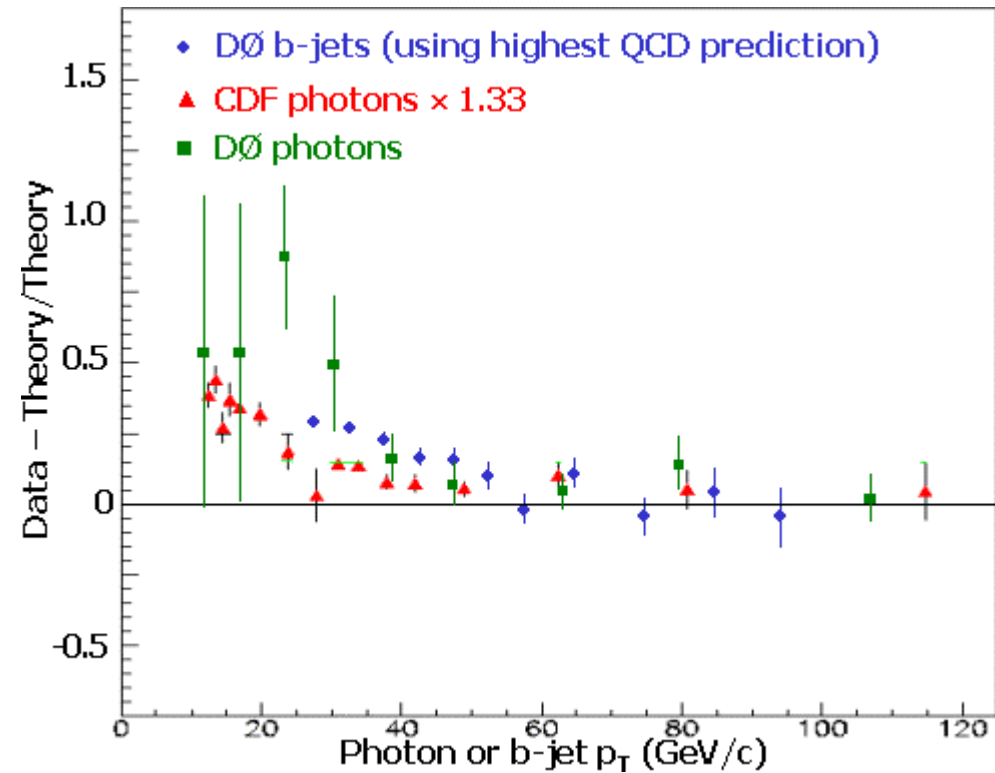
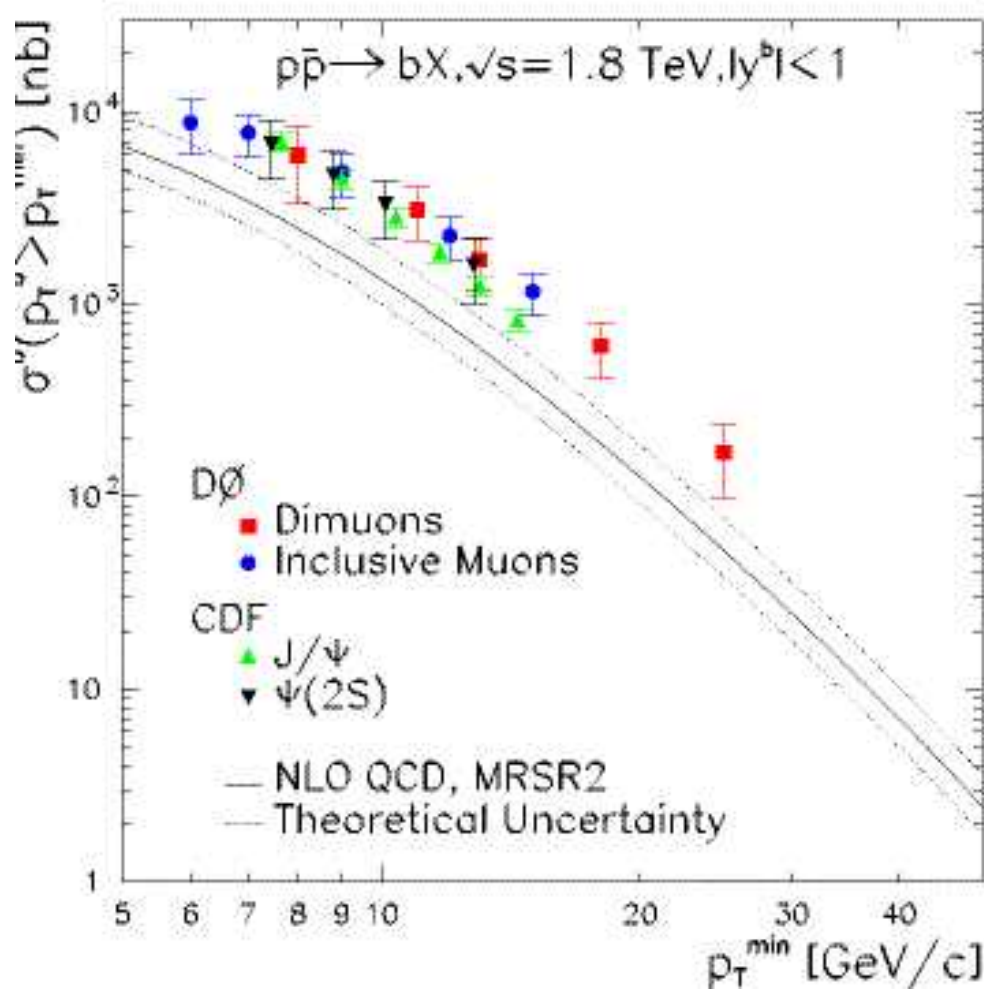
&

bottom

Heavy Quarks : ... past challenges

The CTEQ List of Challenges in Perturbative QCD

Calculating b-quark production cross sections at hadron-hadron colliders



~1995

Multi-Scale Problems are Challenging

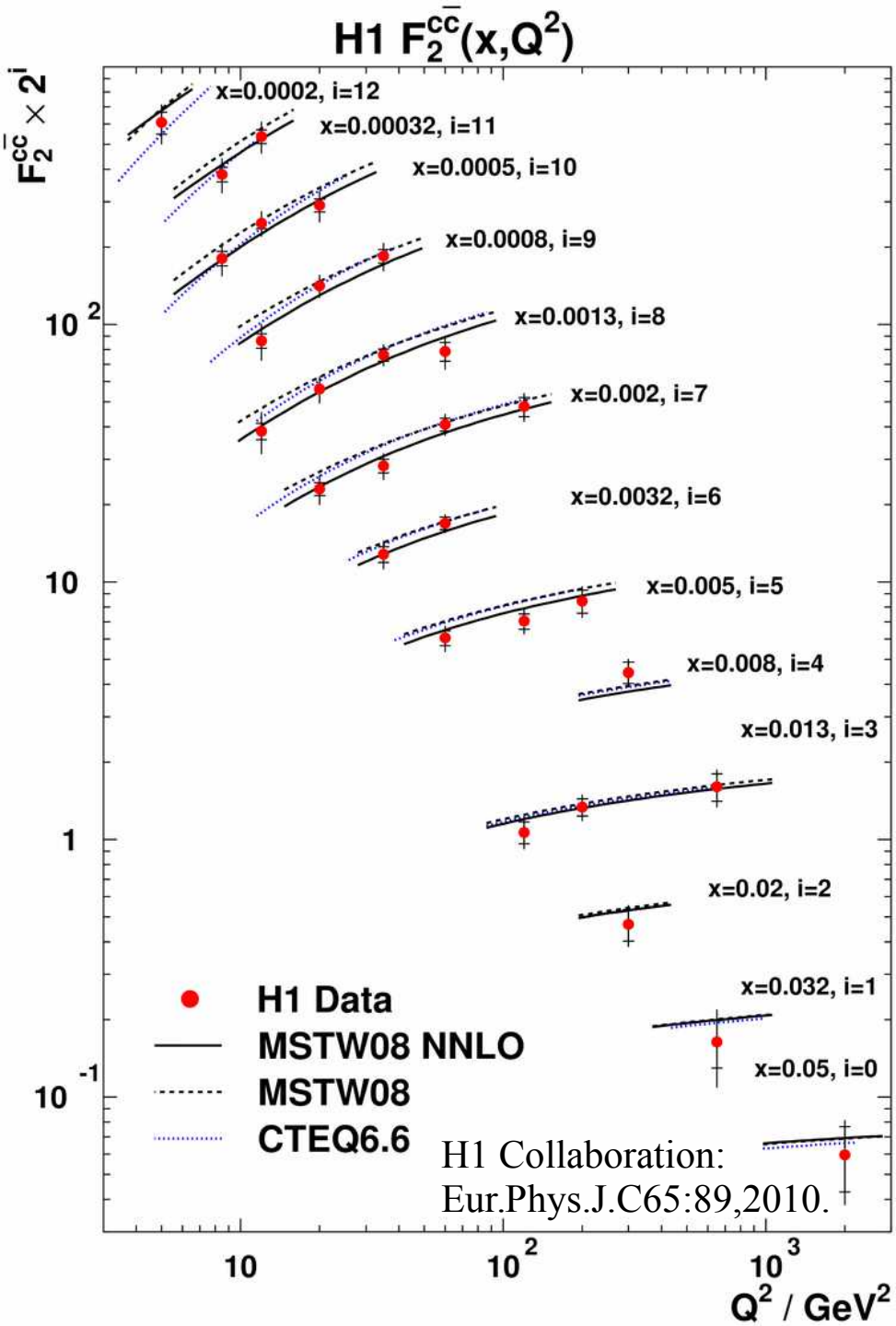
Two-Loop Total Cross Section: One Scale

$$\sigma(Q^2) = \sigma_0 \left\{ 1 + \frac{\alpha_s(Q^2)}{4\pi} (3C_F) + \left[\frac{\alpha_s(Q^2)}{4\pi} \right]^2 \left[-C_F^2 \left[\frac{3}{2} \right] + C_F C_A \left[\frac{123}{2} - 44\zeta(3) \right] + C_F T n_f (-22 + 16\zeta(3)) \right] \right\}$$

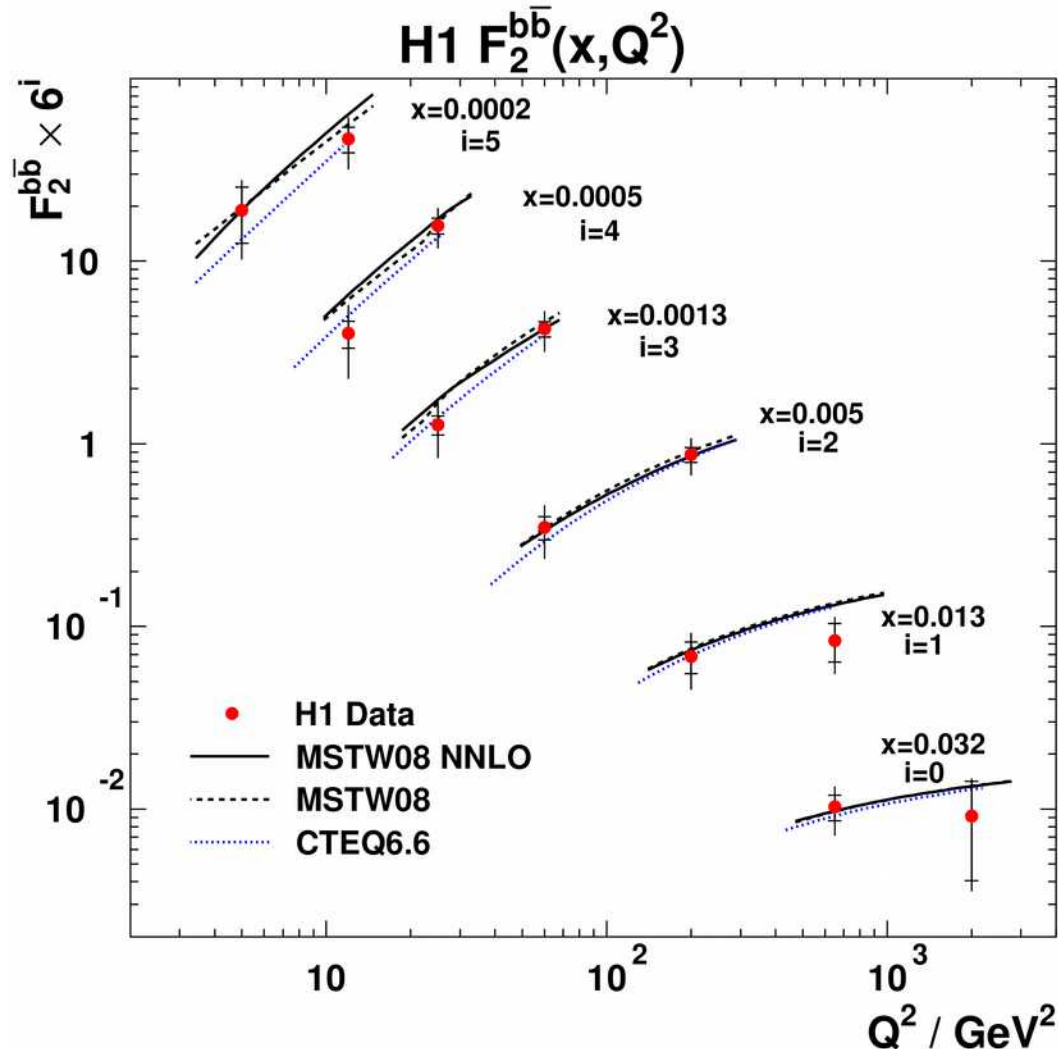
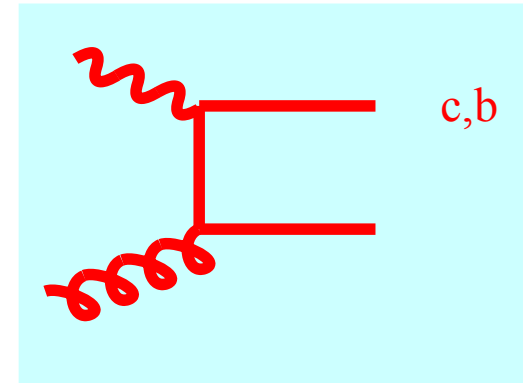
Two-Loop Drell-Yan Cross Section: Two Scales

$$\begin{aligned} H_{q\bar{q}}^{(2),S+V}(z) = & \left[\frac{\alpha_s}{4\pi} \right]^2 \delta(1-z) \left\{ C_A C_F \left[\left[\frac{193}{3} - 24\zeta(3) \right] \ln \left[\frac{Q^2}{M^2} \right] - 11 \ln^2 \left[\frac{Q^2}{M^2} \right] - \frac{12}{5} \zeta(2)^2 + \frac{592}{9} \zeta(2) + 28\zeta(3) - \frac{1535}{12} \right] \right. \\ & + C_F^2 \left[\left[18 - 32\zeta(2) \right] \ln^2 \left[\frac{Q^2}{M^2} \right] + \left[24\zeta(2) + 176\zeta(3) - 93 \right] \ln \left[\frac{Q^2}{M^2} \right] \right. \\ & \left. \left. + \frac{8}{3} \zeta(2)^2 - 70\zeta(2) - 60\zeta(3) + \frac{511}{4} \right] \right. \\ & \left. + n_f C_F \left[2 \ln^2 \left[\frac{Q^2}{M^2} \right] - \frac{34}{3} \ln \left[\frac{Q^2}{M^2} \right] + 8\zeta(3) - \frac{112}{9} \zeta(2) + \frac{127}{6} \right] \right\} \\ & + C_A C_F \left[-\frac{44}{3} \mathcal{D}_0(z) \ln^2 \left[\frac{Q^2}{M^2} \right] + \left\{ \left[\frac{536}{9} - 16\zeta(2) \right] \mathcal{D}_0(z) - \frac{176}{3} \mathcal{D}_1(z) \right\} \ln \left[\frac{Q^2}{M^2} \right] \right. \\ & \left. - \frac{176}{3} \mathcal{D}_2(z) + \left[\frac{1072}{9} - 32\zeta(2) \right] \mathcal{D}_1(z) + \left[56\zeta(3) + \frac{176}{3} \zeta(2) - \frac{1616}{27} \right] \mathcal{D}_0(z) \right] \\ & + C_F^2 \left[\left[64\mathcal{D}_1(z) + 48\mathcal{D}_0(z) \right] \ln^2 \left[\frac{Q^2}{M^2} \right] + \left\{ 192\mathcal{D}_2(z) + 96\mathcal{D}_1(z) - \left[128 + 64\zeta(2) \right] \mathcal{D}_0(z) \right\} \ln \left[\frac{Q^2}{M^2} \right] \right. \\ & \left. + 128\mathcal{D}_3(z) - \left(128\zeta(2) + 256 \right) \mathcal{D}_1(z) + 256\zeta(3) \mathcal{D}_0(z) \right] \\ & + n_f C_F \left[\frac{8}{3} \mathcal{D}_0(z) \ln^2 \left[\frac{Q^2}{M^2} \right] + \left[\frac{32}{3} \mathcal{D}_1(z) - \frac{80}{9} \mathcal{D}_0(z) \right] \ln \left[\frac{Q^2}{M^2} \right] + \frac{32}{3} \mathcal{D}_2(z) - \frac{160}{9} \mathcal{D}_1(z) + \left[\frac{224}{27} - \frac{32}{3} \zeta(2) \right] \mathcal{D}_0(z) \right] . \end{aligned}$$

Ref:
CTEQ
Handbook

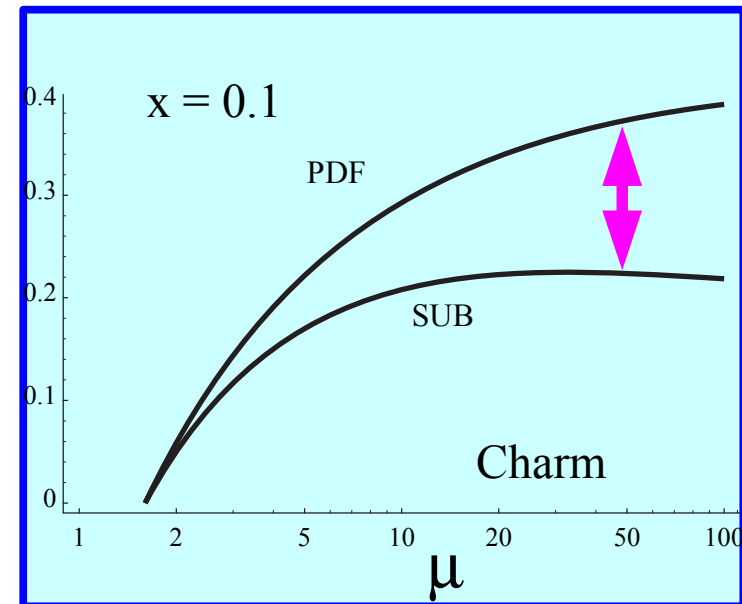
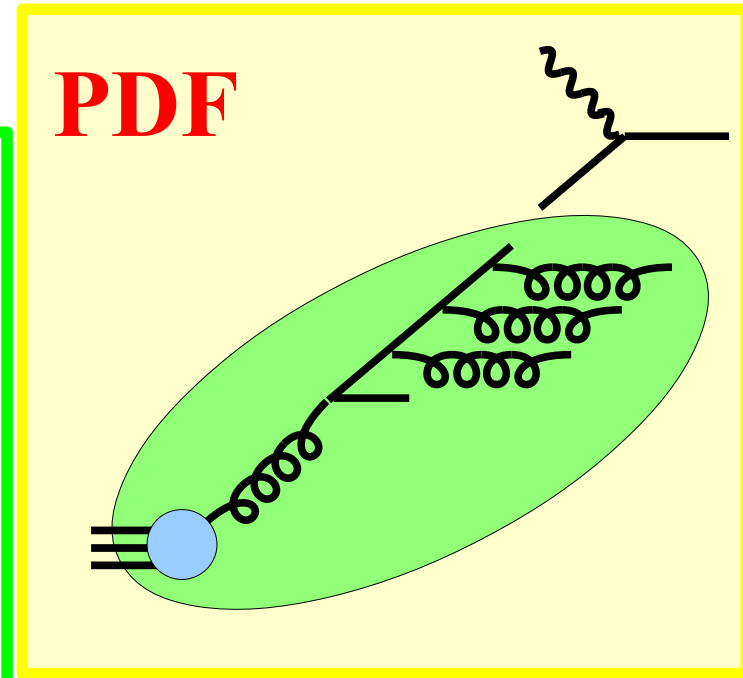
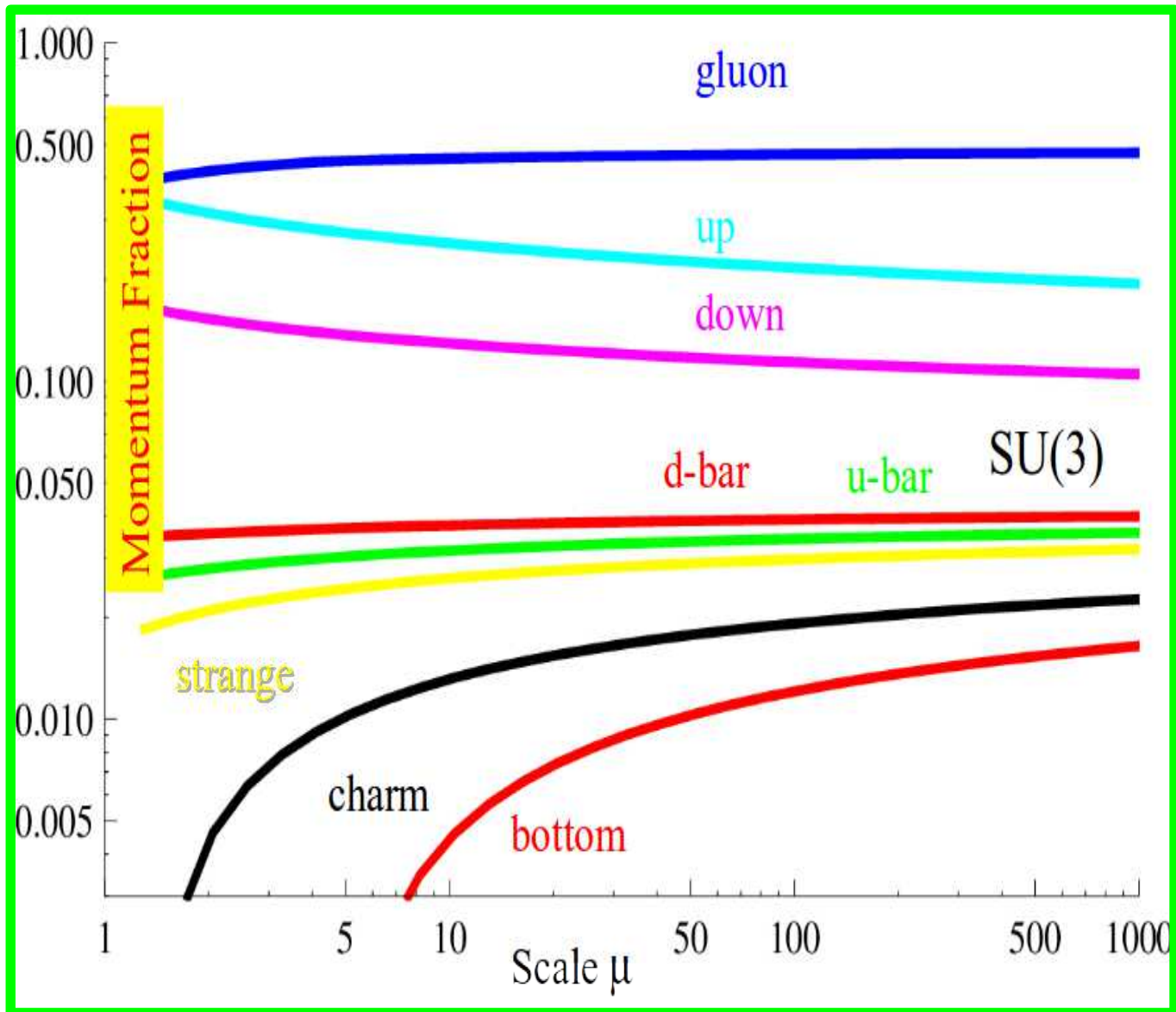


**c & b
tied to
gluon PDFs**



Charm & Bottom PDFs Resum Logs

Resum $\alpha_s \ln(m/Q)$



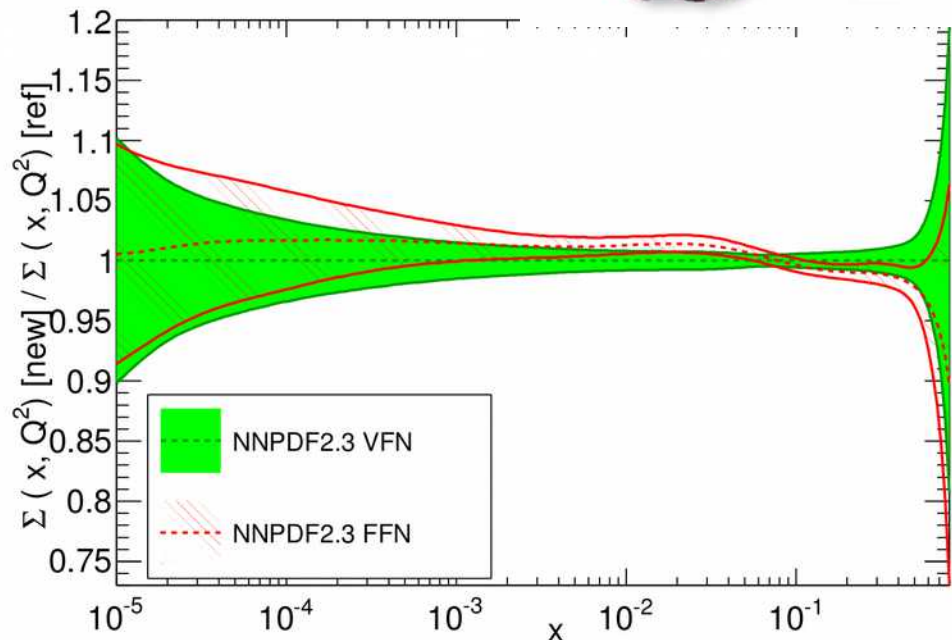
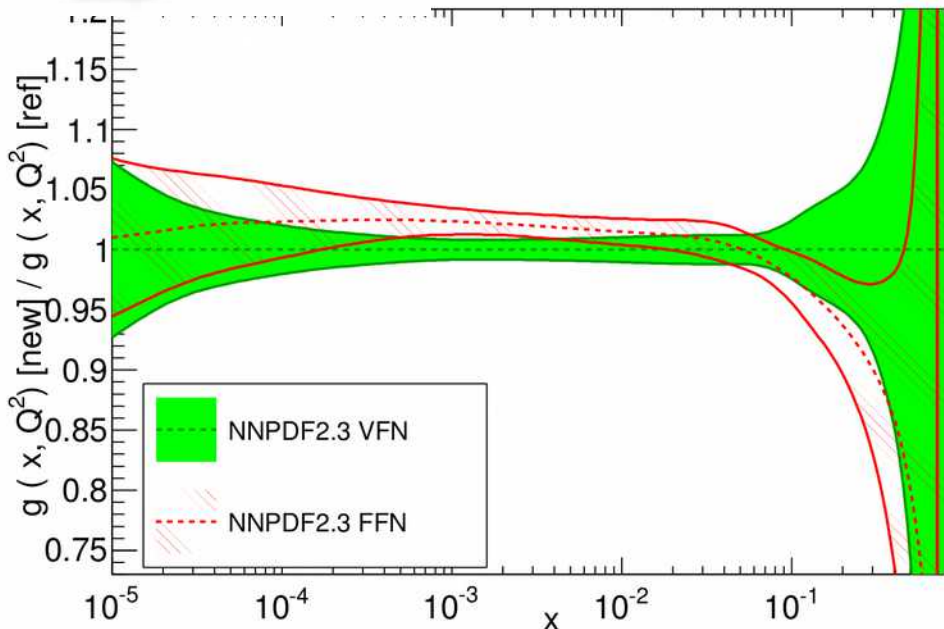
Compare VFN & FFN Schemes



Resum: $\alpha \ln(m/Q)$

NNLO, $\alpha_s = 0.119$, $Q^2 = 10^4 \text{ GeV}^2$

Ratio to NNPDF2.3 NNLC



$$\Delta\chi^2 \equiv \chi_{FFN}^2 - \chi_{VFN}^2 > 0$$

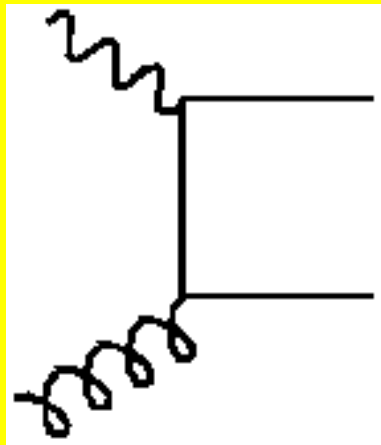
x_{\min}	x_{\max}	Q_{\min}^2 (GeV)	Q_{\max}^2 (GeV)	$\Delta\chi^2$ (DIS)	$N_{\text{dat}}^{\text{DIS}}$	$\Delta\chi^2$ (HERA-I)	$N_{\text{dat}}^{\text{hera-I}}$
$4 \cdot 10^{-5}$	1	3	10^6	72.2	2936	77.1	592
$4 \cdot 10^{-5}$	0.1	3	10^6	87.1	1055	67.8	405
$4 \cdot 10^{-5}$	0.01	3	10^6	40.9	422	17.8	202
$4 \cdot 10^{-5}$	1	10	10^6	53.6	2109	76.4	537
$4 \cdot 10^{-5}$	1	100	10^6	91.4	620	97.7	412
$4 \cdot 10^{-5}$	0.1	10	10^6	84.9	583	67.4	350
$4 \cdot 10^{-5}$	0.1	100	10^6	87.7	321	87.1	227

VFN Wins

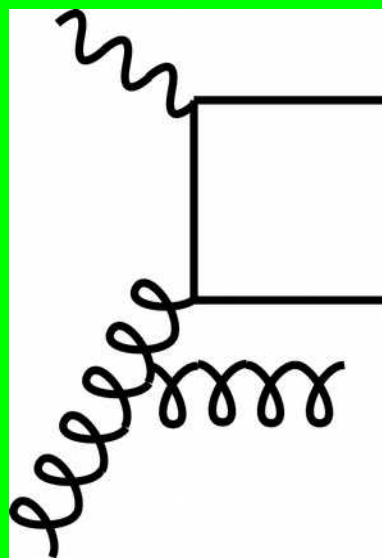
LO



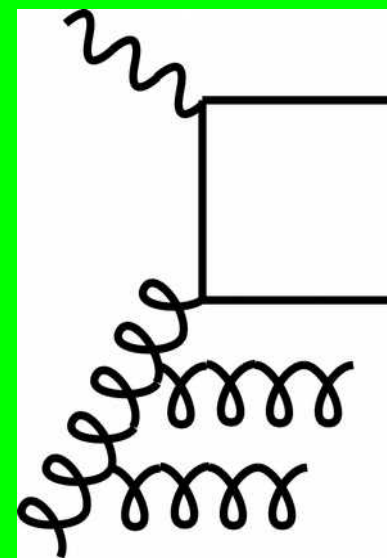
NLO



N2LO



N3LO



Full ACOT

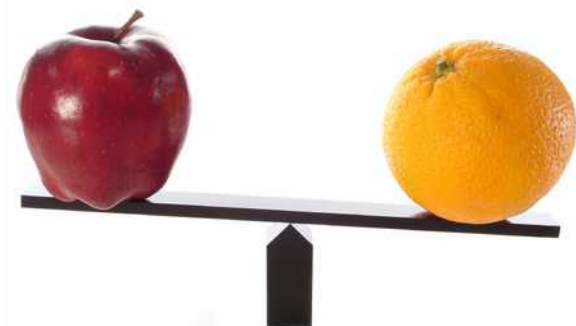
Based on the Collins-Wilczek-Zee (CWZ) Renormalization Scheme
... hence, extensible to all orders

DGLAP kernels & PDF evolution are pure MS-Bar
Subtractions are MS-Bar

ACOT: $m \rightarrow 0$ limit yields MS-Bar
with no finite renormalization

PDFs Discontinuous at N2LO

α_s Discontinuous at α_s^3

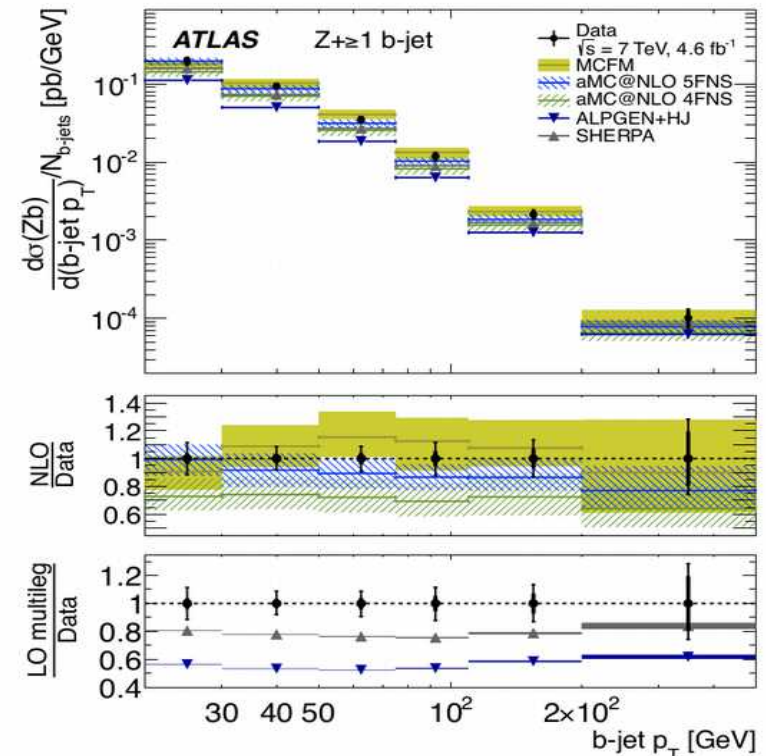
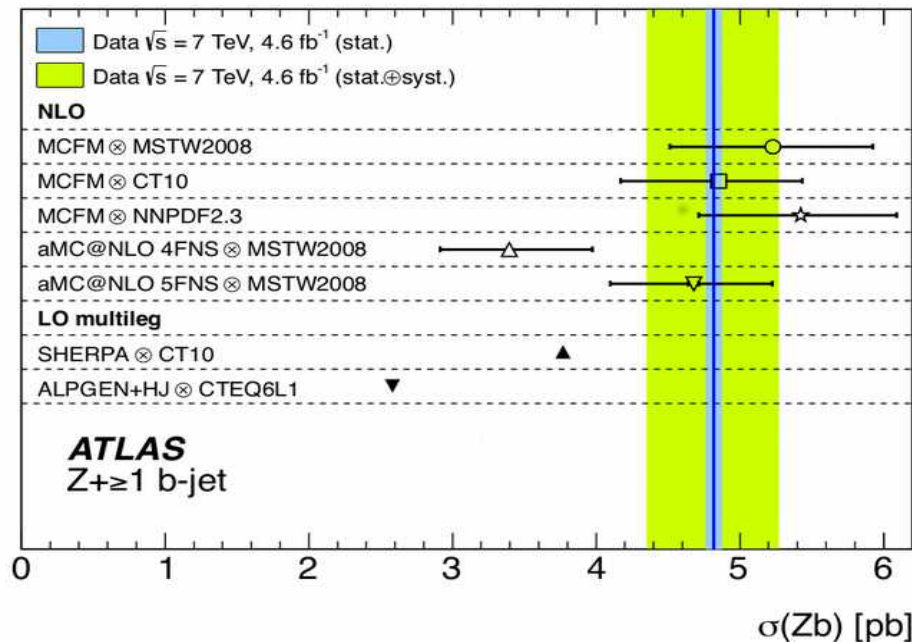


Heavy flavor: Z+b-jets

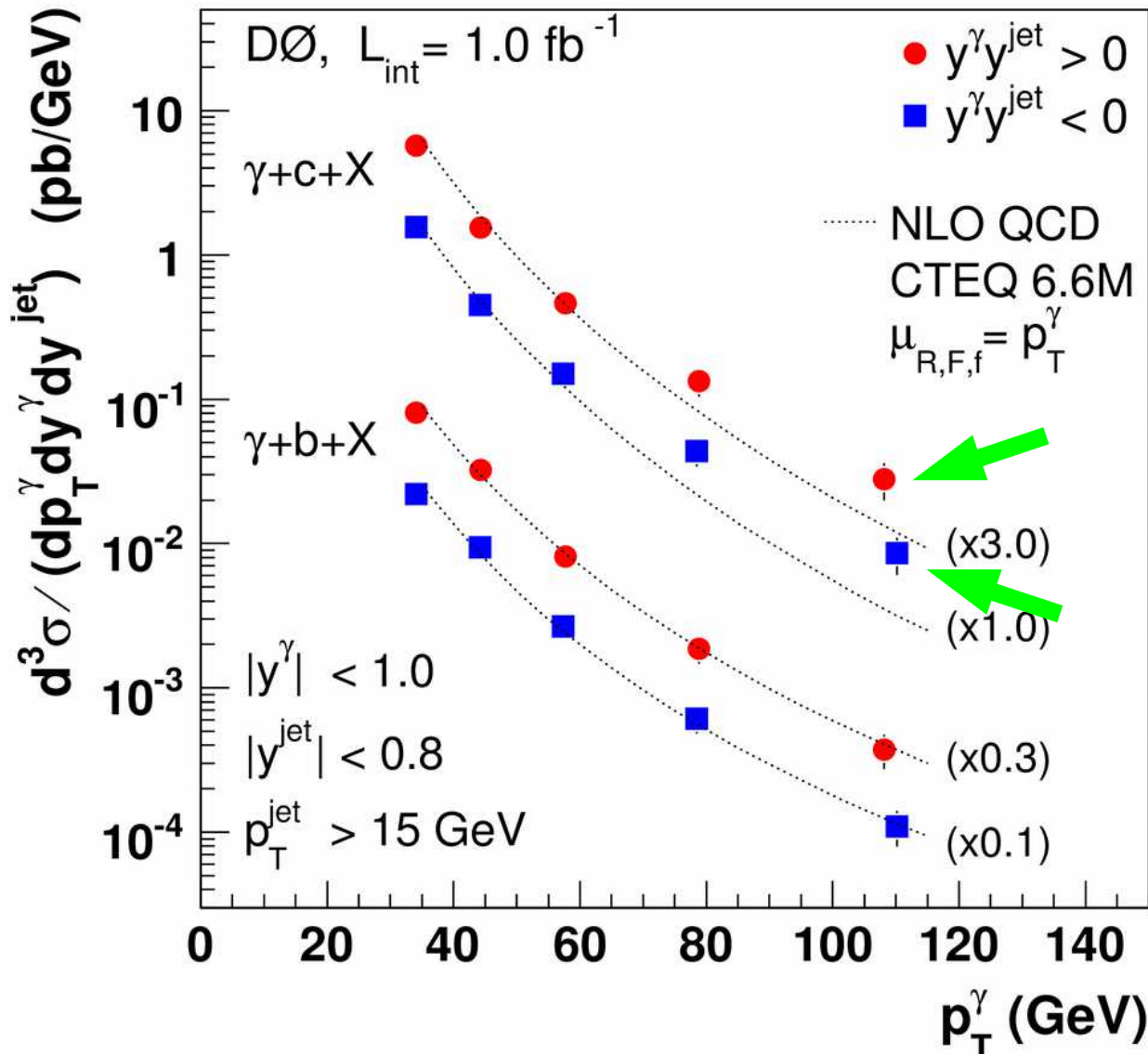
JHEP 10 (2014) 141

- + Good agreement with NLO MCFM and aMC@NLO
 - Seems to favor scheme where b-quark is taken from PDF (5 FNS)
 - LO+PS generators are underestimating the cross section
 - Can't constrain PDF yet due to too large uncertainty

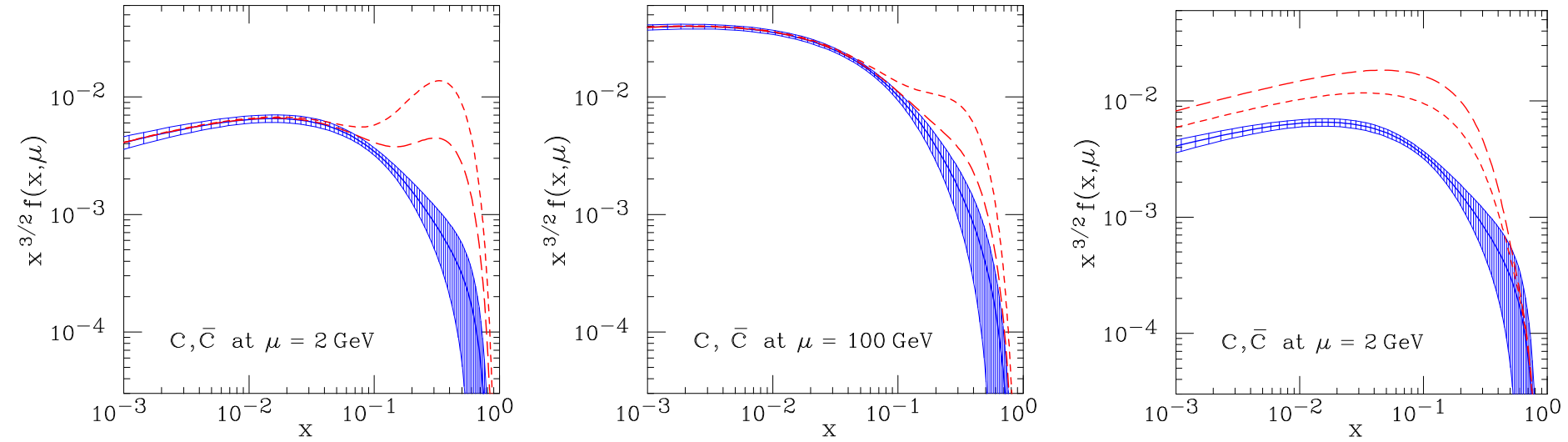
- + Good description of b-jet p_T shape
 - Normalization is off



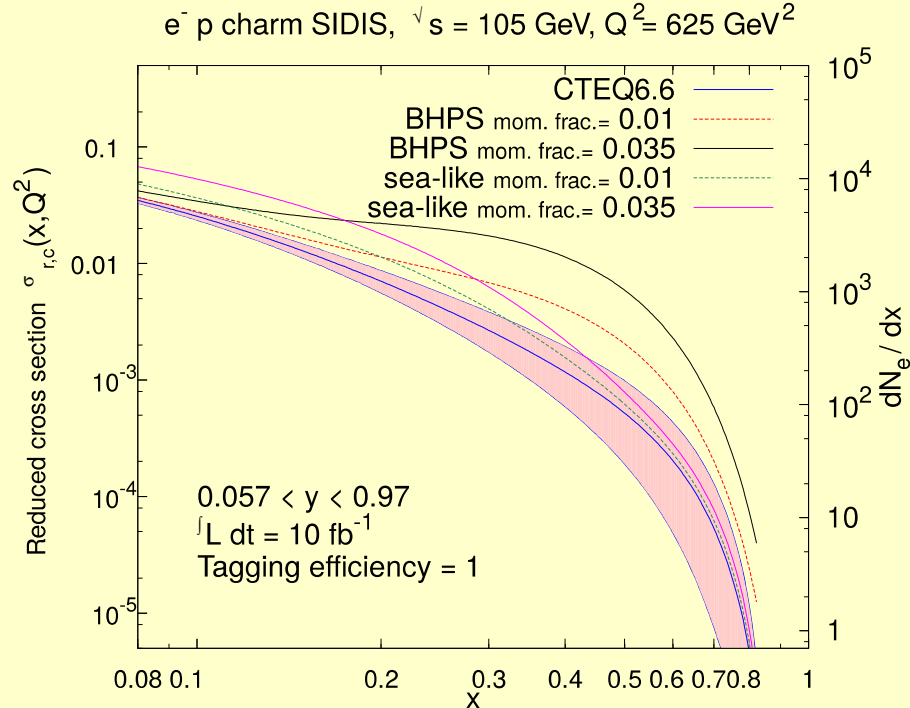
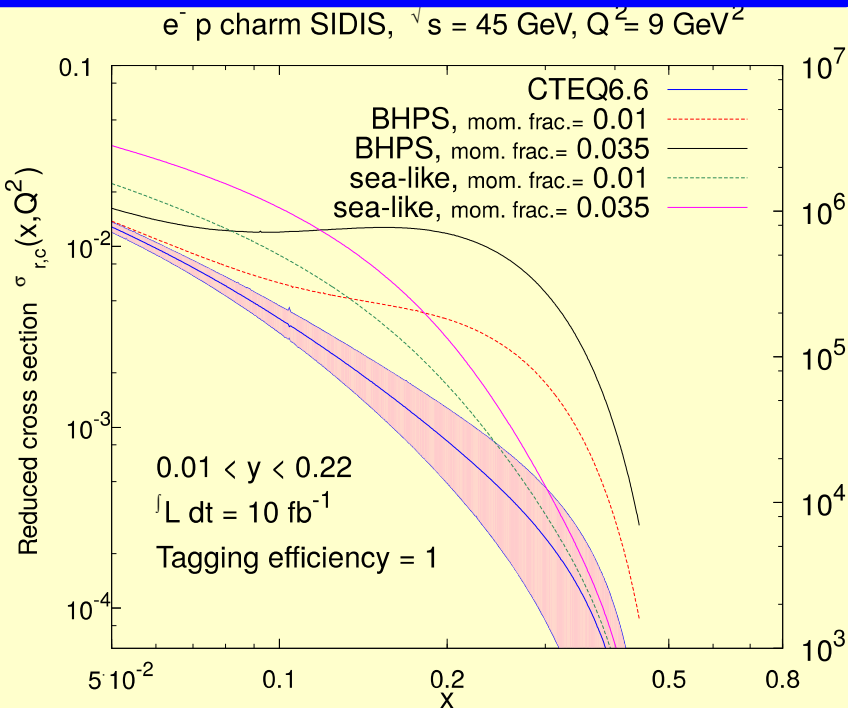
... what about the *Intrinsic* Heavy Quarks



Excess in Charm,
NOT Bottom
only at high PT



Gluons and the quark sea at high-energies
Institute for Nuclear Theory in Seattle in Fall 2010.



DGLAP Evolution equations ...

including **ordinary** Q_0 and **intrinsic** Q_1 heavy quark

$$\begin{aligned}\dot{g} &= P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q_0 + \cancel{P_{gQ} \otimes Q_1}, \\ \dot{q} &= P_{qq} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q_0 + \cancel{P_{qQ} \otimes Q_1}, \\ \dot{Q}_0 + \dot{Q}_1 &= P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q_0 + P_{QQ} \otimes Q_1.\end{aligned}$$

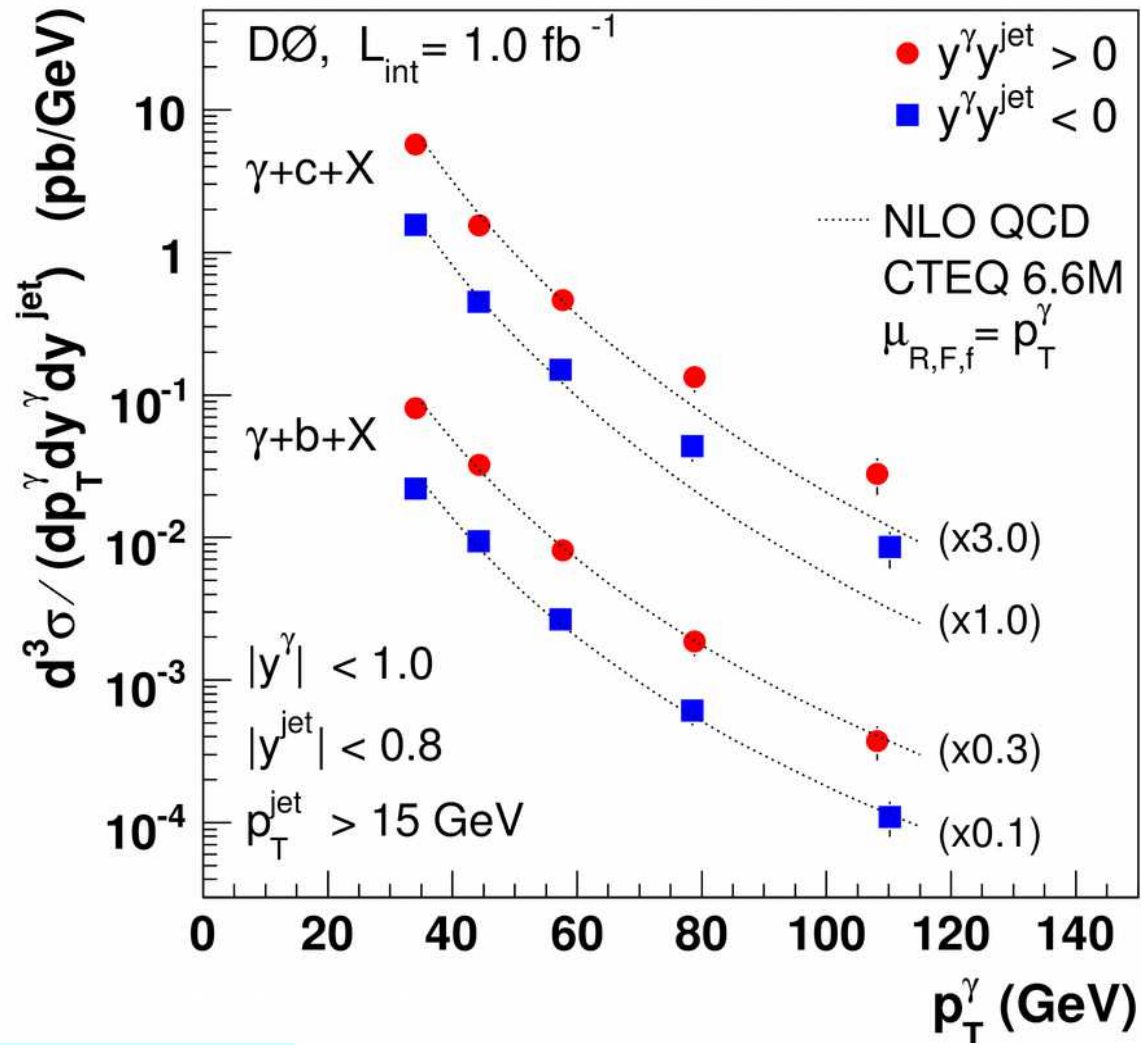
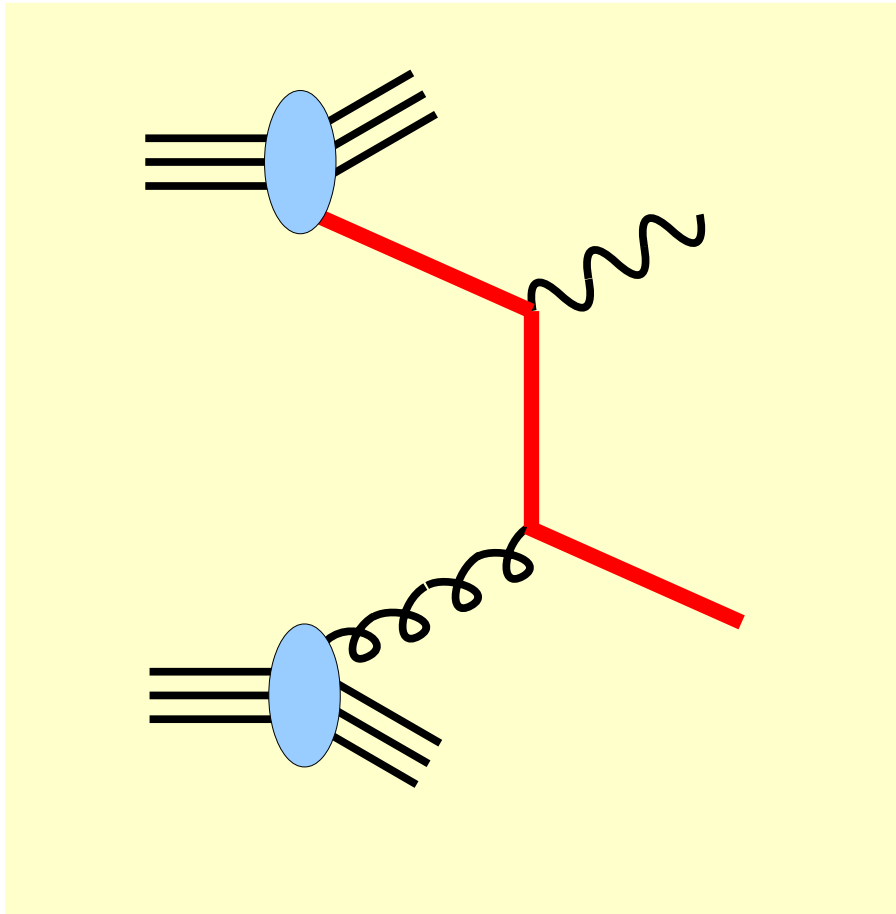
neglect

Equations decouple:

Intrinsic component evolves independently
Scale set by m_Q
Adjust normalization by simple rescaling

$$\dot{Q}_1 = P_{QQ} \otimes Q_1.$$

$$c_1(x) = \bar{c}_1(x) \propto x^2 [6x(1+x) \ln x + (1-x)(1+10x+x^2)]$$

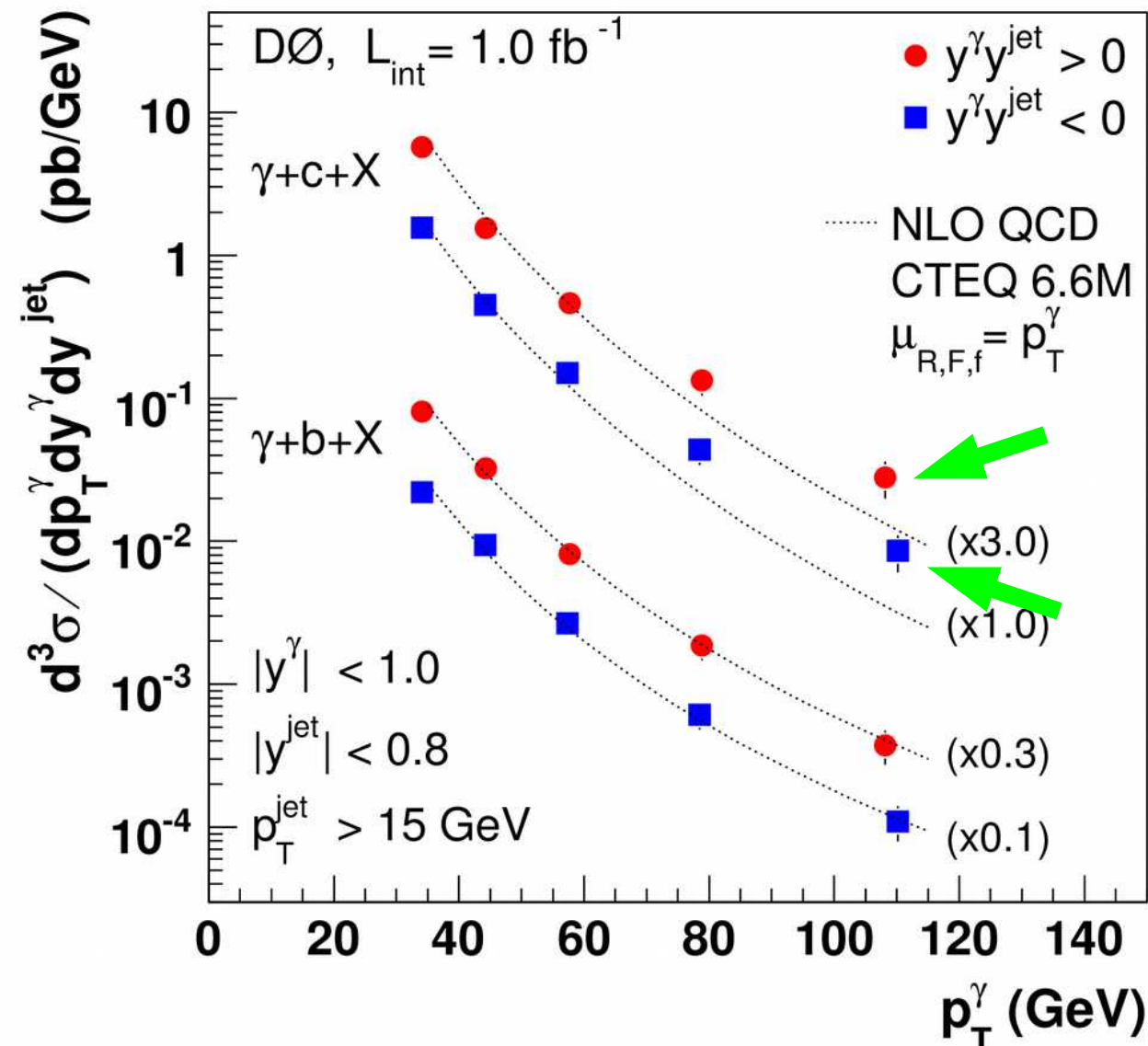


$$c \ g \rightarrow c \ \gamma$$

$$b \ g \rightarrow b \ \gamma$$

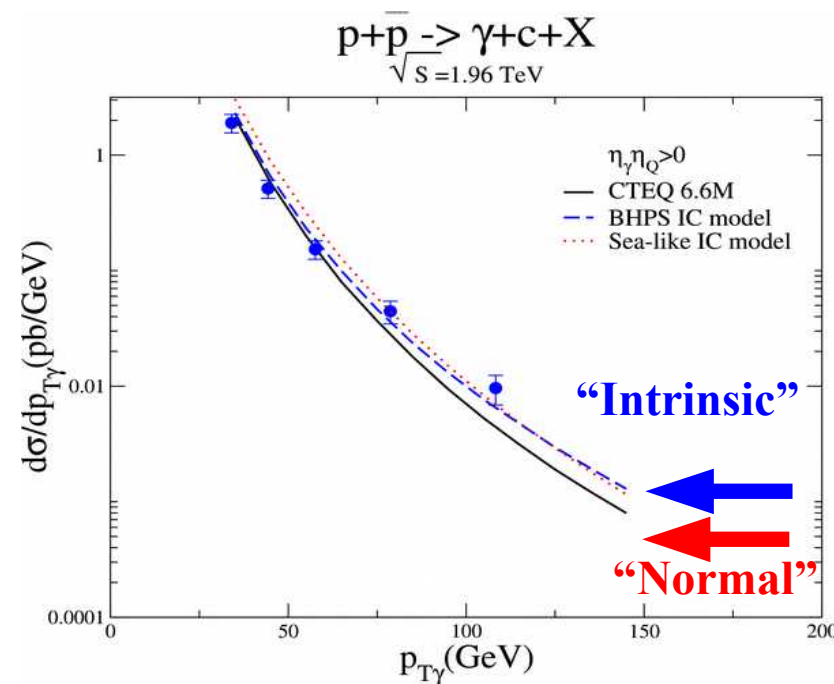
$$s \ g \rightarrow c \ W$$

$$c \ g \rightarrow b \ W$$



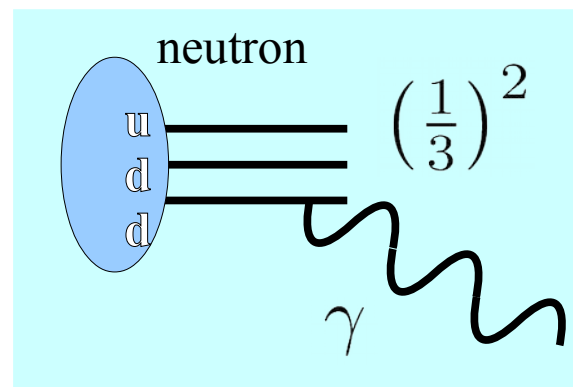
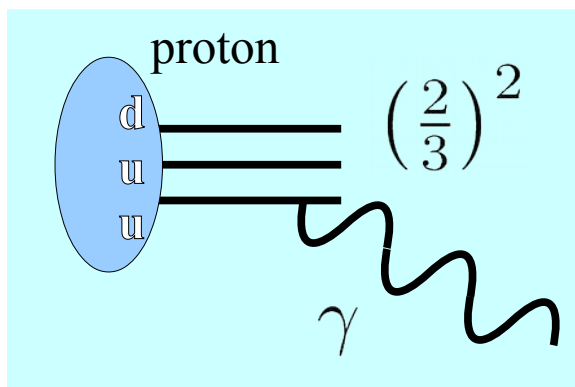
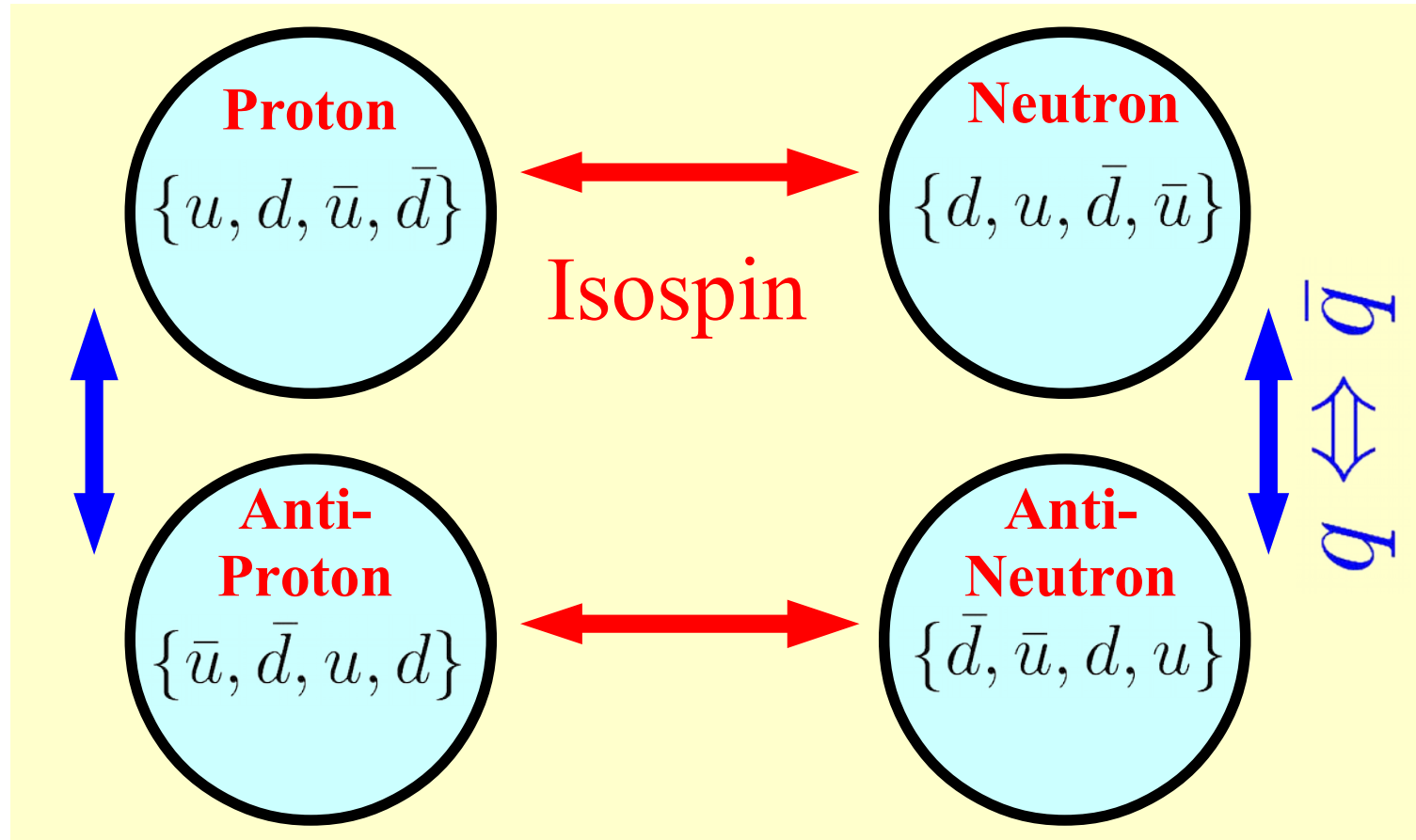
Excess in Charm,
NOT Bottom

only at high PT



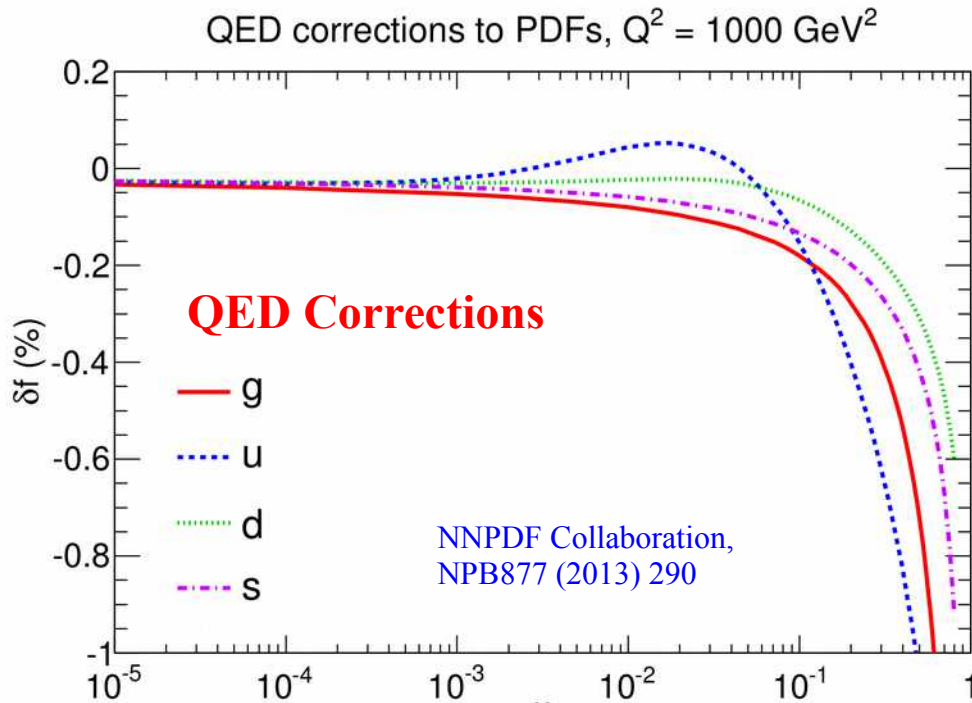
Things

I won't have time
to discuss

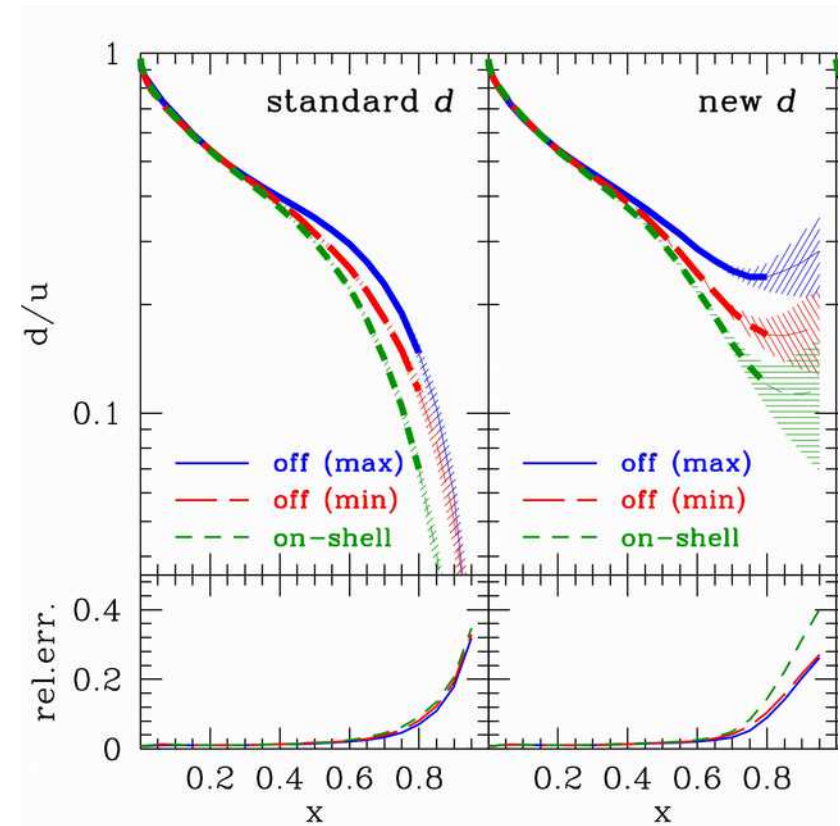


Isospin terms are comparable to NNLO QCD

QCD & EW Corrections do NOT factorize



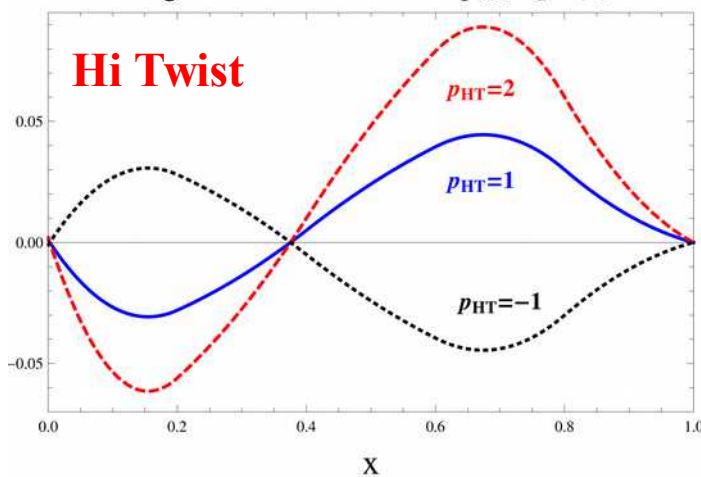
Hi-x is a "Gold Mine" for EIC



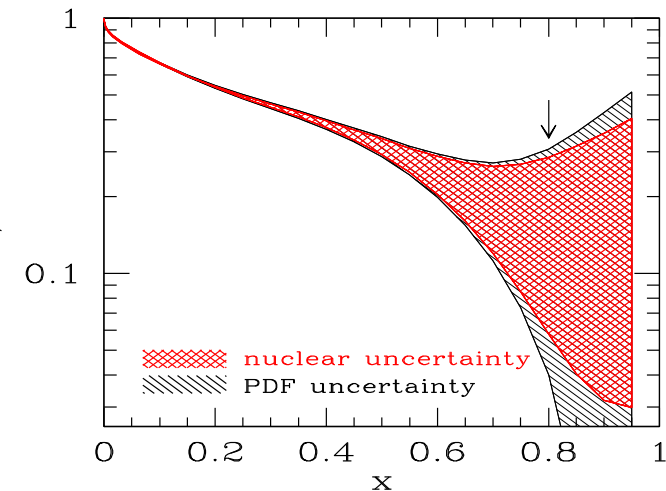
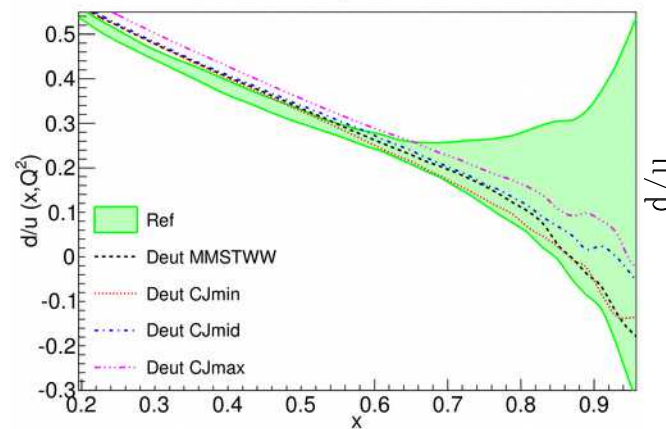
Nuclear Corrections or Parameterization???

Higher Twist Correction $p_{HT} H_2^{(4)}(x)$

Hi Twist



NNPDF2.3, $Q^2 = 2 \text{ GeV}^2$



previously discussed by: Rolf Ent & Michael Engelhardt

Kresimir Kumericki
Curse of dimensionality

Lattice Calculations

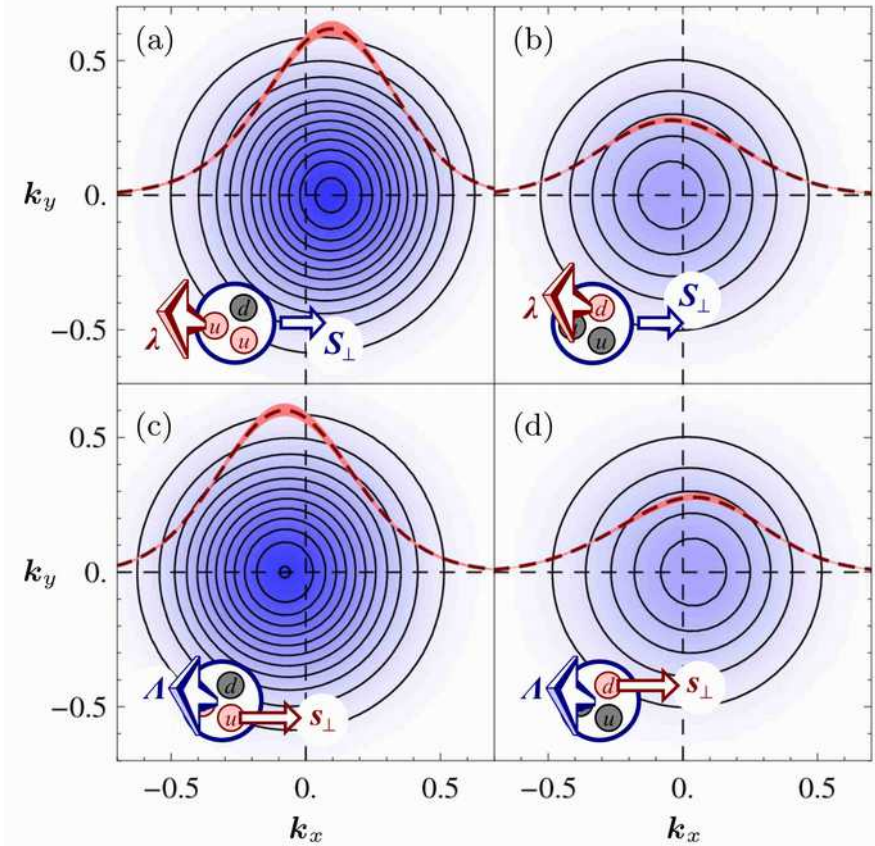
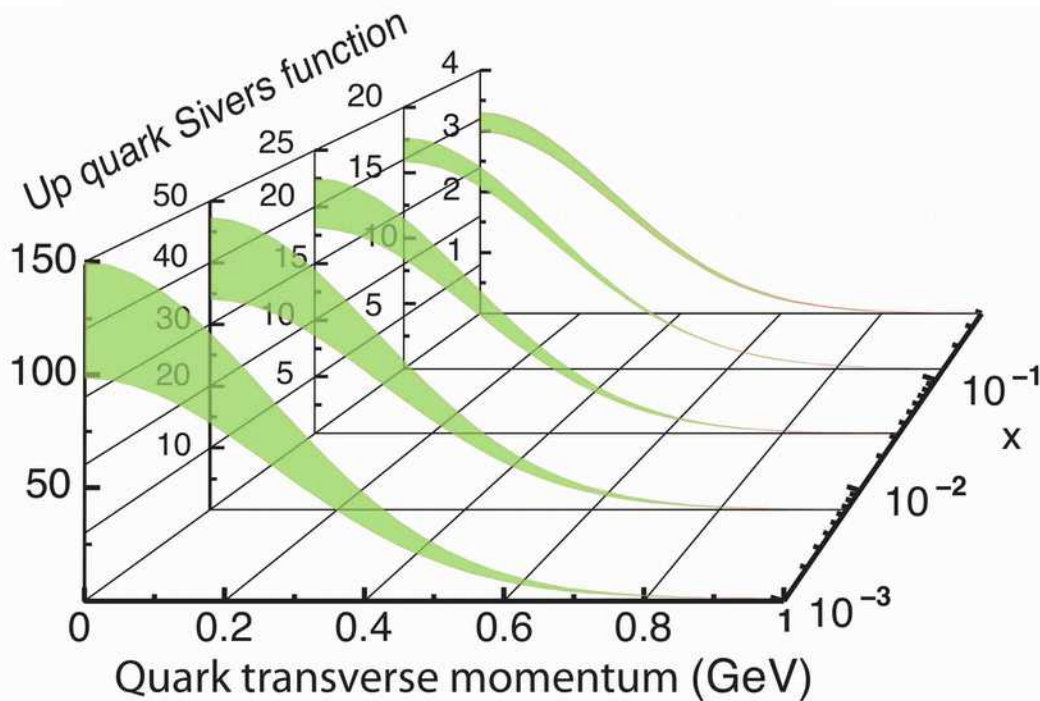
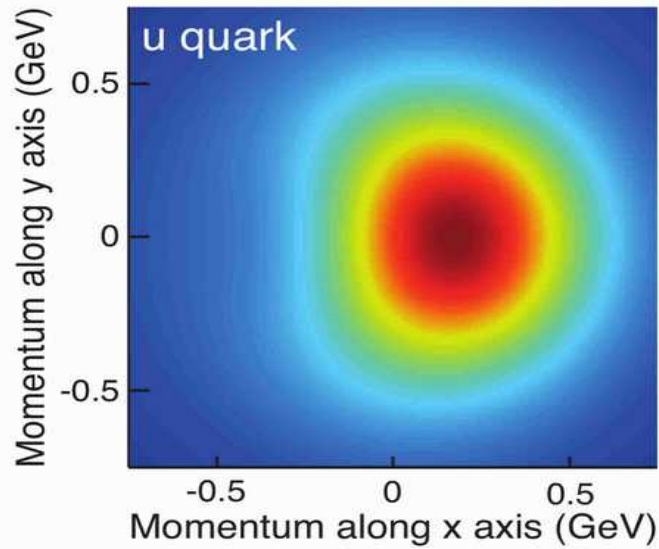
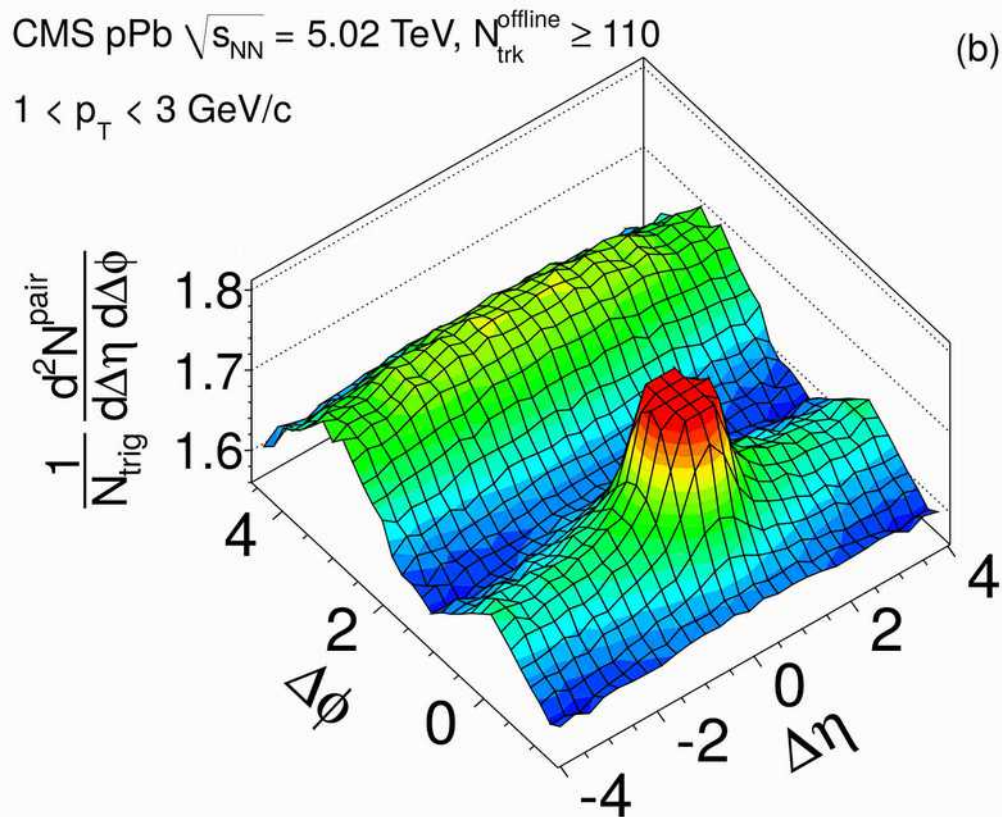
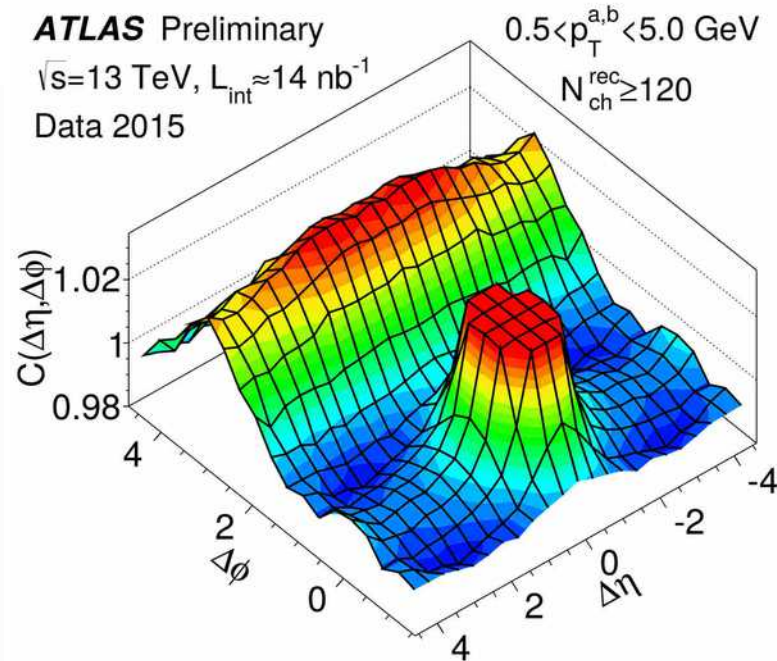


FIG. 3: Quark densities in the k_{\perp} -plane, for $m_{\pi} \approx 500$ MeV. (a) ρ_L for u-quarks and $\lambda = 1$, $S_{\perp} = (1, 0)$, (b) the same for d-quarks, (c) ρ_T for u-quarks and $\Lambda = 1$, $s_{\perp} = (1, 0)$, (d) the same for d-quarks. The error bands show the density profile at $k_y = 0$ as a function of k_x (scale not shown).



(b)

ATLAS Preliminary
 $\sqrt{s} = 13$ TeV, $L_{\text{int}} \approx 14$ nb $^{-1}$
 Data 2015



ALICE
 p-Pb $\sqrt{s_{NN}} = 5.02$ TeV
 V0S: (0-20%)-(60-100%)

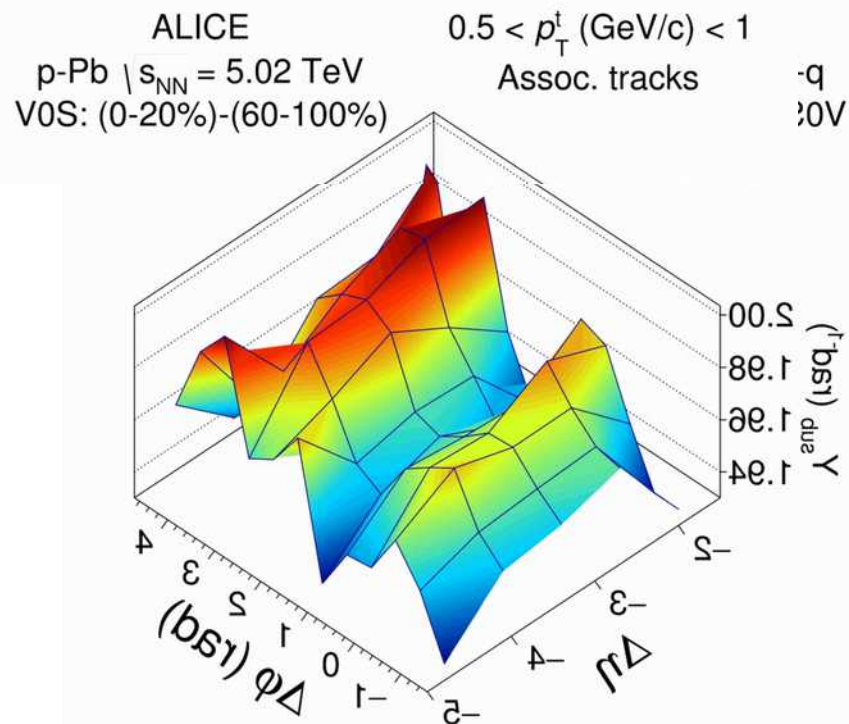
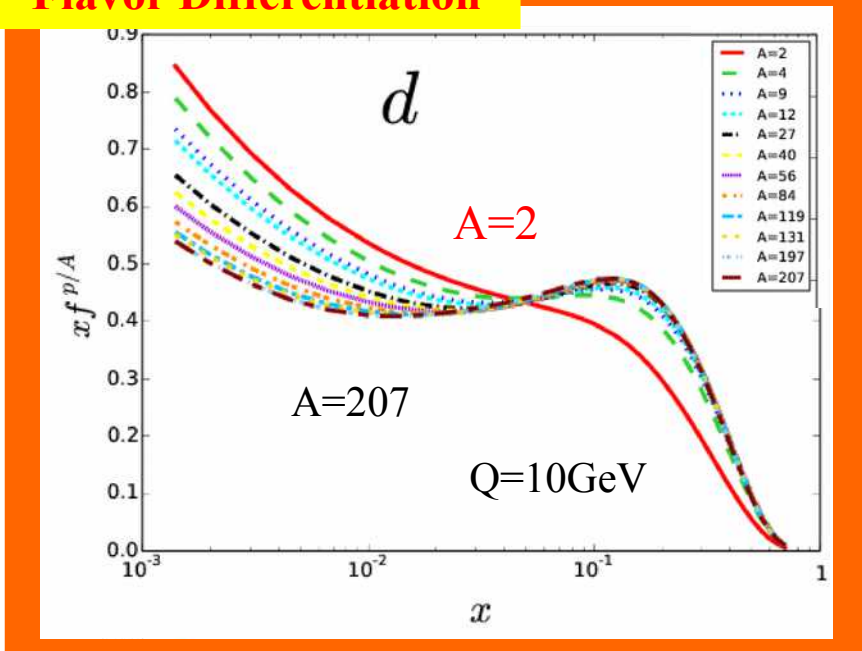


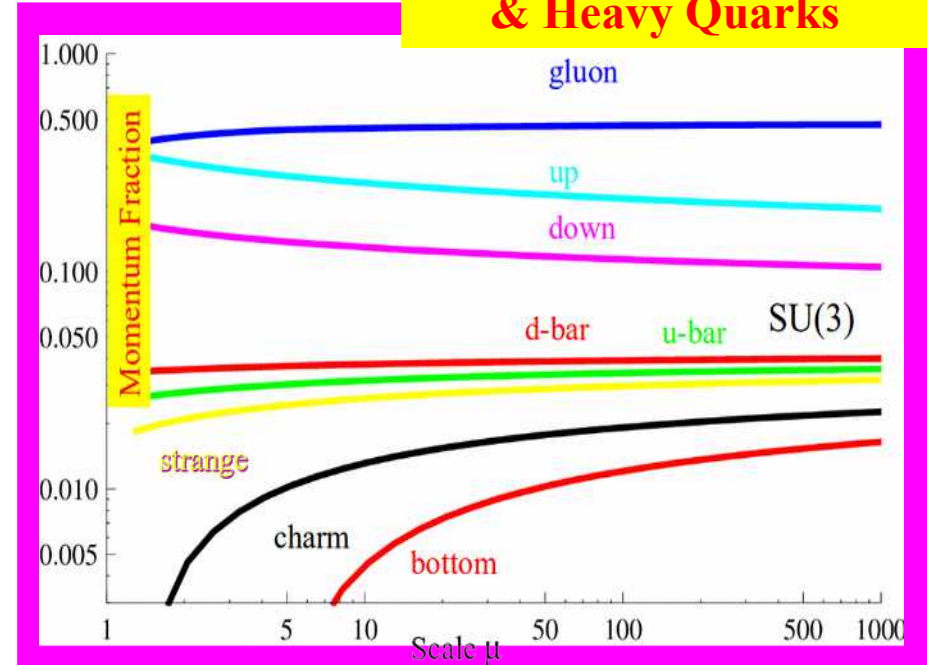
Figure 3.33: The two-particle correlation function in high-multiplicity p +Pb collisions as a function of $\Delta\phi$ and $\Delta\eta$ reported by the CMS collaboration [252]. The 'ridge' structure is seen as a correlation near $\Delta\phi = 0$ stretching over many units of rapidity $\Delta\eta$.

Conclusion

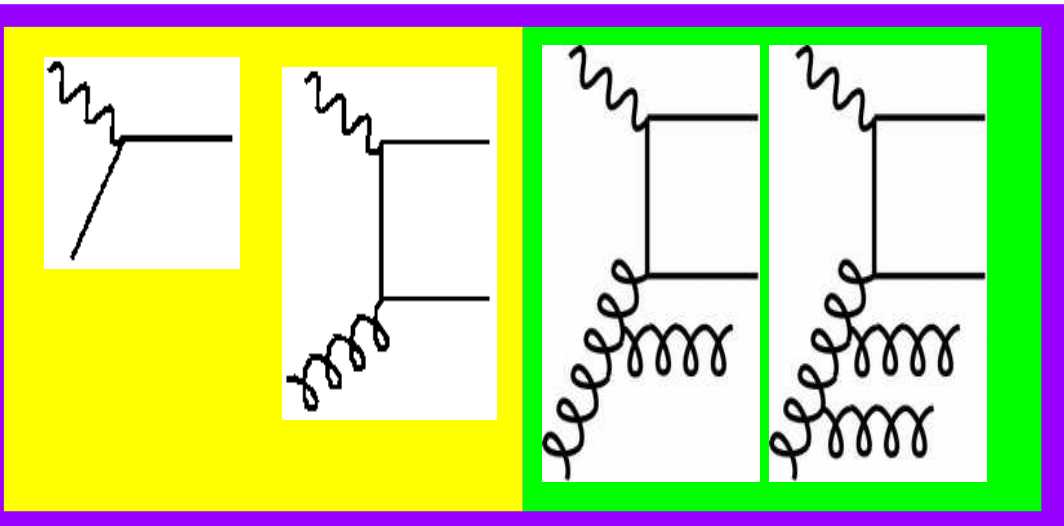
Nuclear Corrections & Flavor Differentiation



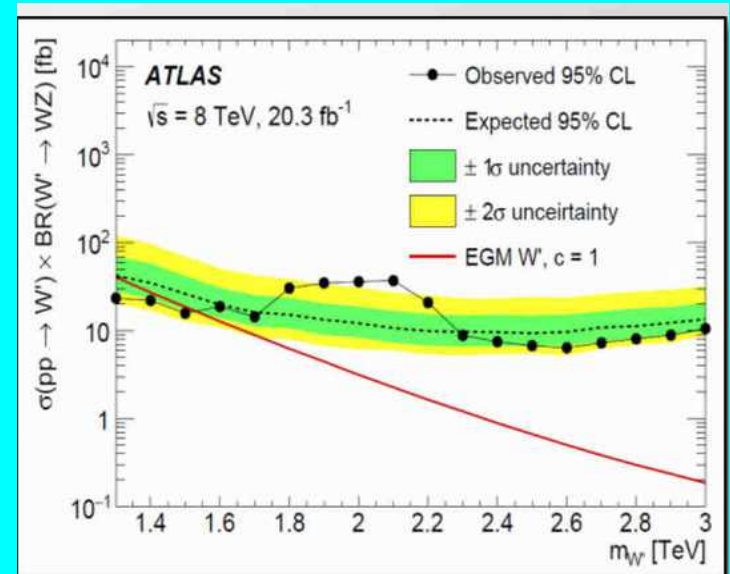
Multi-Scale Processes & Heavy Quarks



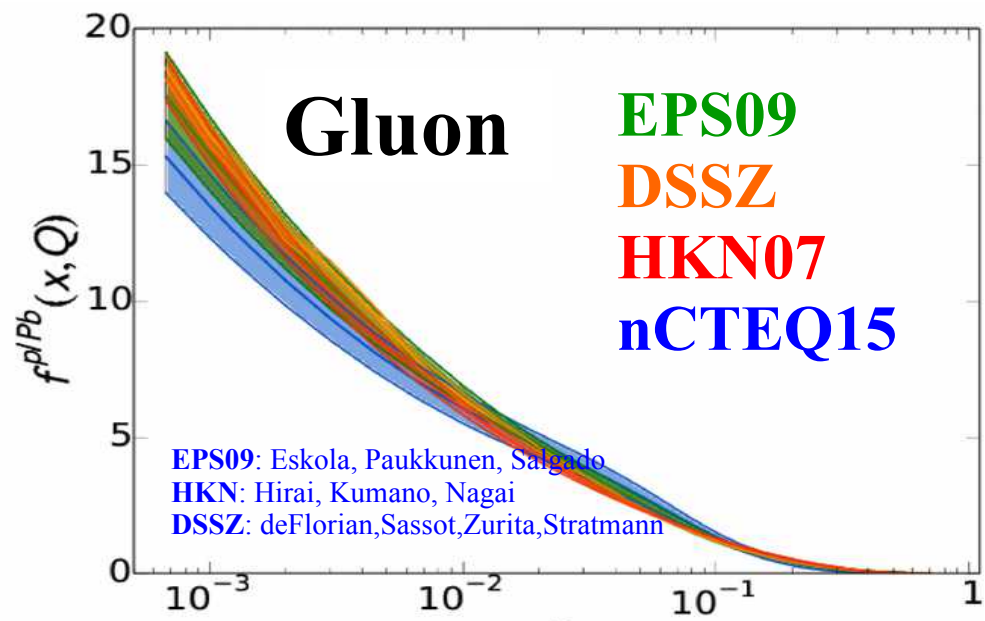
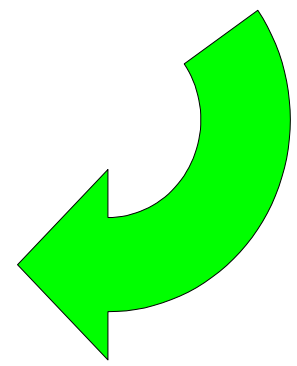
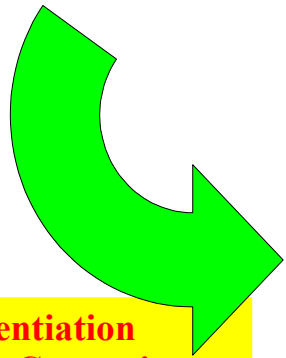
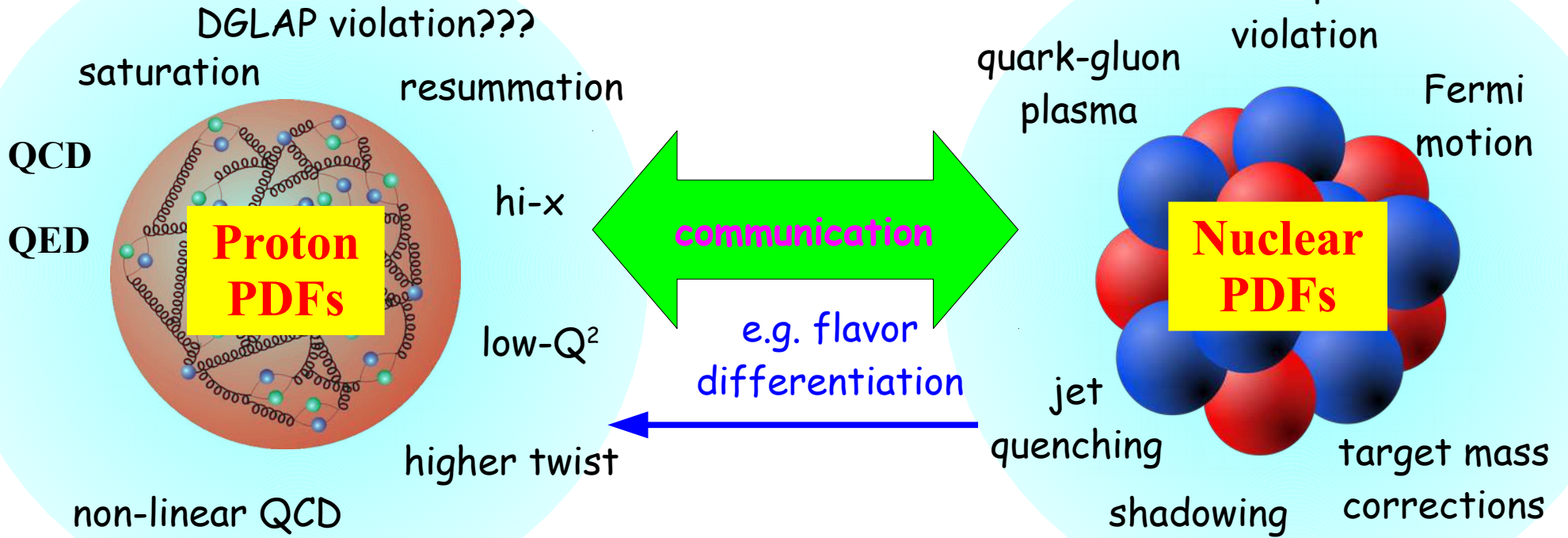
Higher Order Processes



Search for new physics



“QCD is our most perfect physical theory”



EPS09: Eskola, Paukkunen, Salgado
 HKN: Hirai, Kumano, Nagai
 DSSZ: deFlorian, Sassot, Zurita, Stratmann

- 1) Flavor Differentiation & Nuclear Corrections
- 2) Multi-scale problems: Heavy Quarks Resummation
- 3) Hi-Order Corrections

Lessons: The Nature of Nature ... alien, simple, beautiful, weird, & comprehensible