

# Test Fundamental Symmetries via Precision Measurements of $\pi^0$ , $\eta$ , $\eta'$ Decays

Liping Gan

University of North Carolina Wilmington

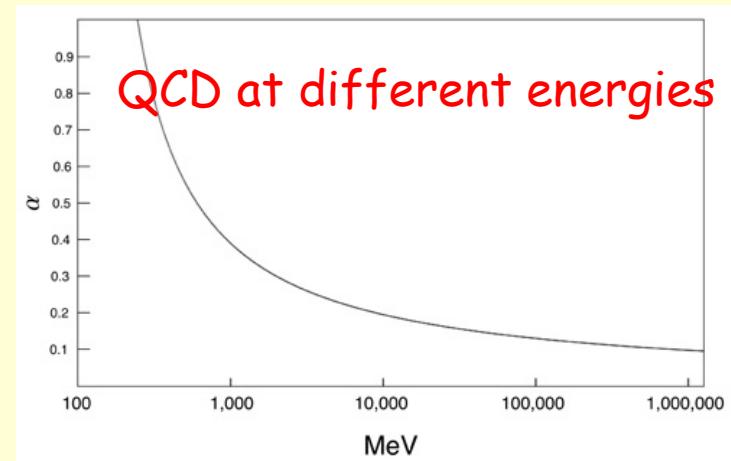
## Outline

1. Introduction
  - challenges in physics
2. PrimEx experiments on  $\pi^0$ ,  $\eta$ ,  $\eta'$ 
  - precision tests confinement QCD symmetries
3. Jlab Eta Factory (JEF) Program for SM forbidden or allowed  $\eta$  decays
  - search for BSM new physics and improve light quark mass ratio
4. Summary

# Challenges in Physics

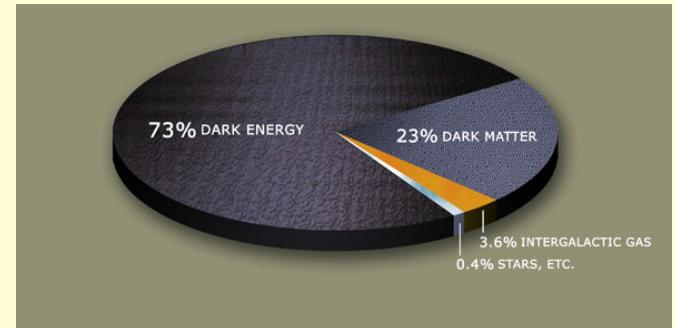
## ➤ Confinement QCD

- QCD confinement and its relationship to the dynamical chiral symmetry breaking



## ➤ New physics beyond the Standard Model (SM)

- Dark matter and dark energy
- New sources of CP violation



"As far as I see, all priori statements in physics have their origin in symmetry". By H. Weyl

# QCD Symmetries and Light Mesons

- QCD Lagrangian in Chiral limit ( $m_q \rightarrow 0$ ) is invariant under:

$$SU_L(3) \times SU_R(3) \times U_A(1) \times U_B(1)$$

- Chiral symmetry  $SU_L(3) \times SU_R(3)$  spontaneously breaks to  $SU(3)$

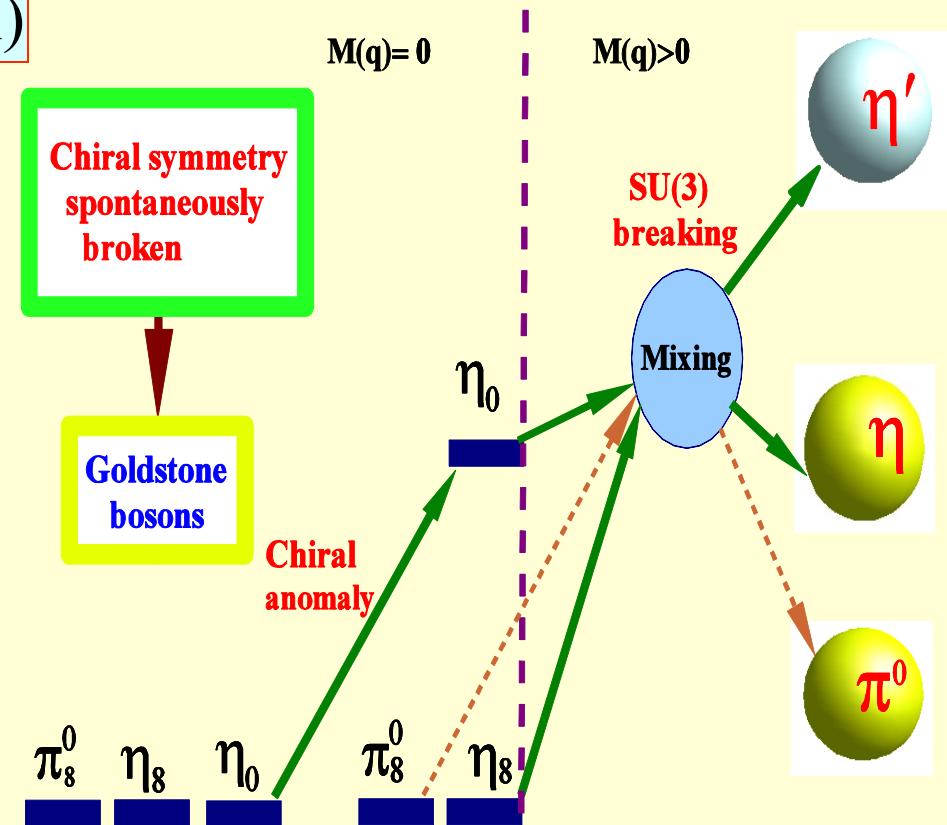
- 8 Goldstone Bosons (GB)

- $U_A(1)$  is explicitly broken:  
(Chiral anomalies)

- $\Gamma(\pi^0 \rightarrow \gamma\gamma)$ ,  $\Gamma(\eta \rightarrow \gamma\gamma)$ ,  $\Gamma(\eta' \rightarrow \gamma\gamma)$
- Mass of  $\eta_0$

- $SU_L(3) \times SU_R(3)$  and  $SU(3)$  are explicitly broken:

- GB are massive
- Mixing of  $\pi^0$ ,  $\eta$ ,  $\eta'$



The  $\pi^0$ ,  $\eta$ ,  $\eta'$  system provides a rich laboratory to study the symmetry structure of QCD at low energies.

# Primakoff Program at Jlab 6 & 12 GeV

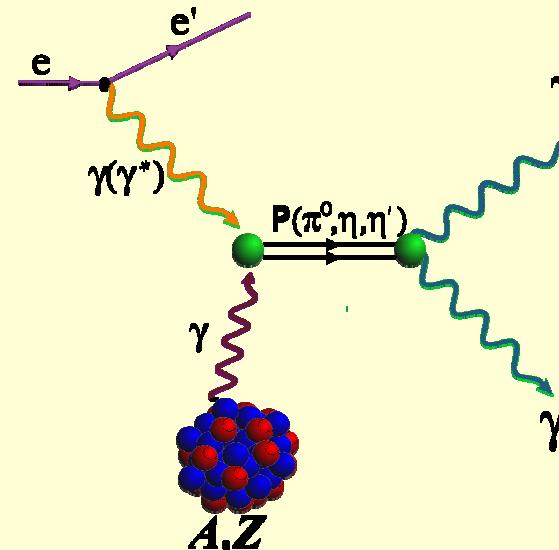
Precision measurements of electromagnetic properties of  $\pi^0$ ,  $\eta$ ,  $\eta'$  via Primakoff effect.

## a) Two-Photon Decay Widths:

- 1)  $\Gamma(\pi^0 \rightarrow \gamma\gamma)$  @ 6 GeV
- 2)  $\Gamma(\eta \rightarrow \gamma\gamma)$
- 3)  $\Gamma(\eta' \rightarrow \gamma\gamma)$

### Input to Physics:

- precision tests of Chiral symmetry and anomalies
- determination of light quark mass ratio
- $\eta$ - $\eta'$  mixing angle



## b) Transition Form Factors at low

$Q^2$  (0.001-0.5  $\text{GeV}^2/c^2$ ):  
 $F(\gamma\gamma^* \rightarrow \pi^0)$ ,  $F(\gamma\gamma^* \rightarrow \eta)$ ,  $F(\gamma\gamma^* \rightarrow \eta')$

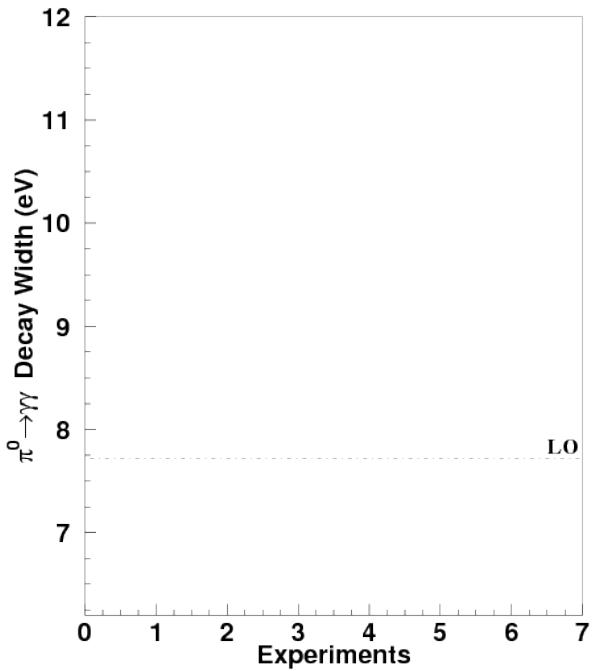
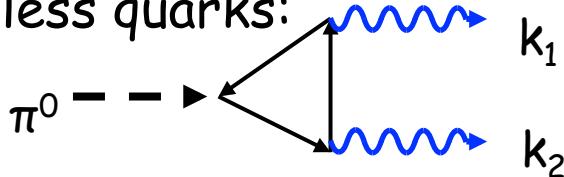
### Input to Physics:

- $\pi^0, \eta$  and  $\eta'$  electromagnetic interaction radii
- is the  $\eta'$  an approximate Goldstone boson?
- inputs to  $a_\mu$ (HLbL) calculations

# Axial Anomaly Determines $\pi^0$ Lifetime

- ◆  $\pi^0 \rightarrow \gamma\gamma$  decay proceeds primarily via the **chiral anomaly** in QCD.
- ◆ The chiral anomaly prediction is **exact** for massless quarks:

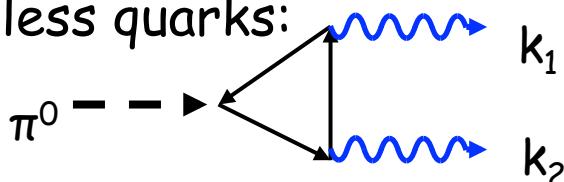
$$\Gamma(\pi^0 \rightarrow \gamma\gamma) = \frac{\alpha^2 N_c^2 m_\pi^3}{576\pi^3 F_\pi^2} = 7.725 \text{ eV}$$



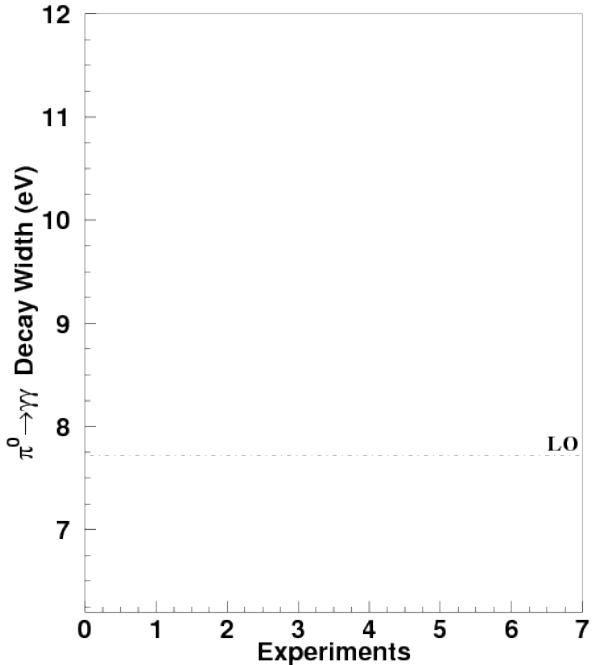
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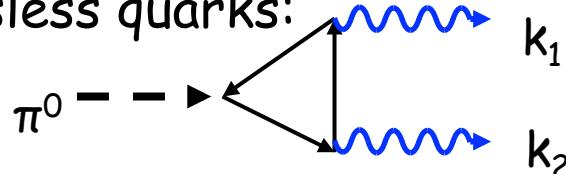


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- Corrections to the chiral anomaly prediction:

**Calculations in NLO ChPT:**

◻  $\Gamma(\pi^0 \rightarrow \gamma\gamma) = 8.10 \text{ eV} \pm 1.0\%$

(J. Góity, et al. Phys. Rev. D66:076014, 2002)

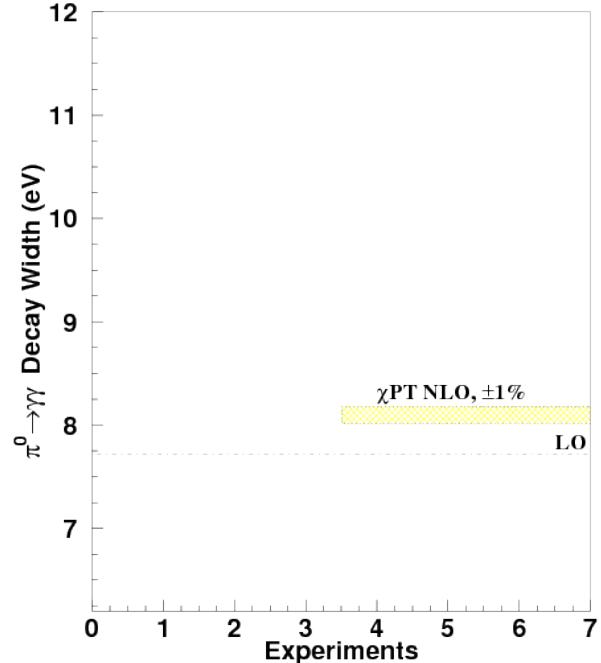
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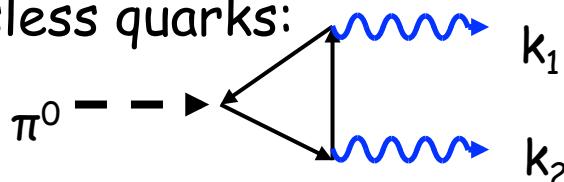
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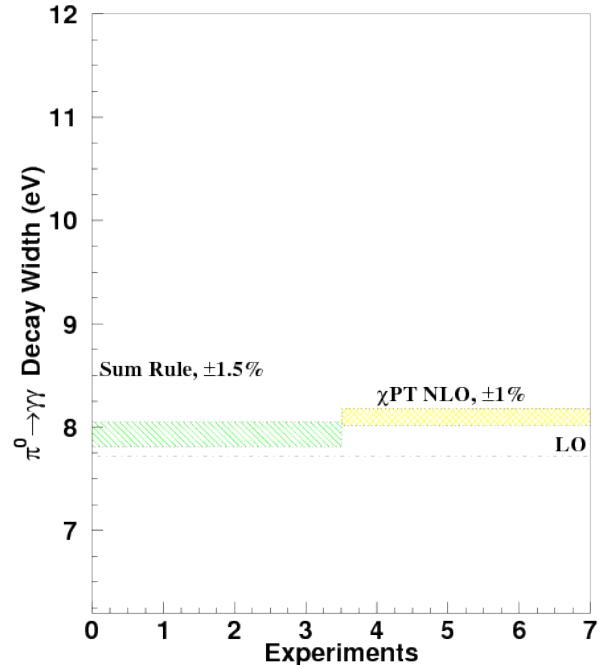
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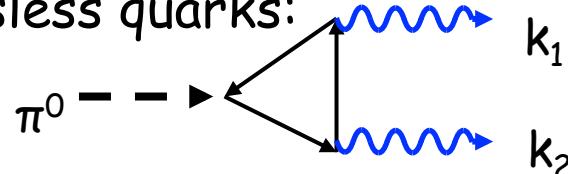


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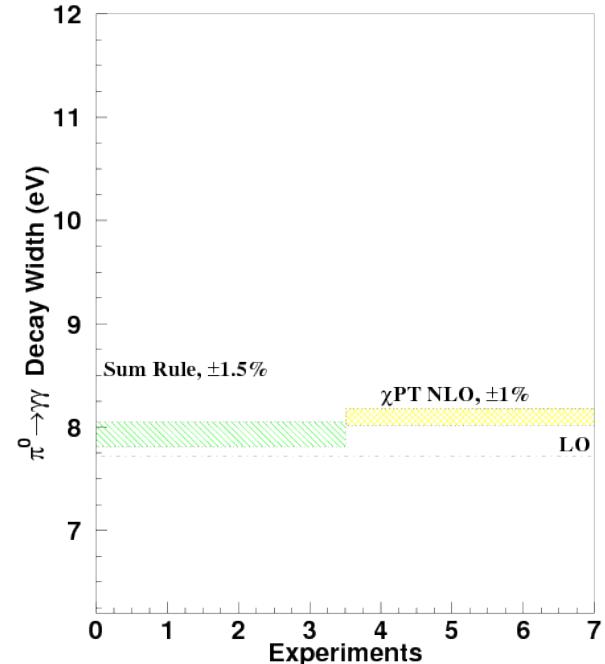
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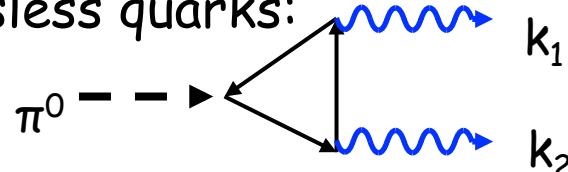


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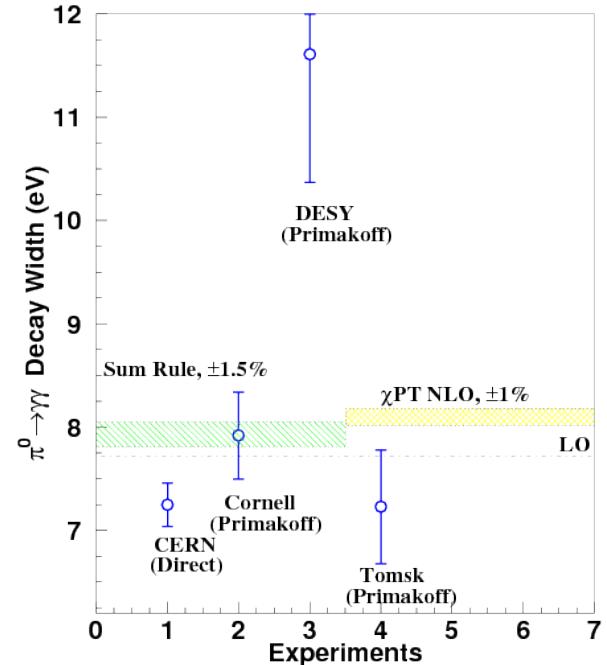
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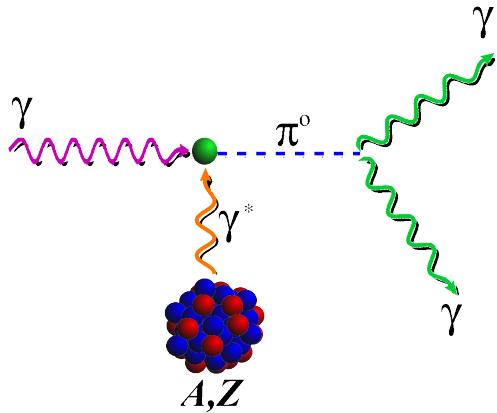
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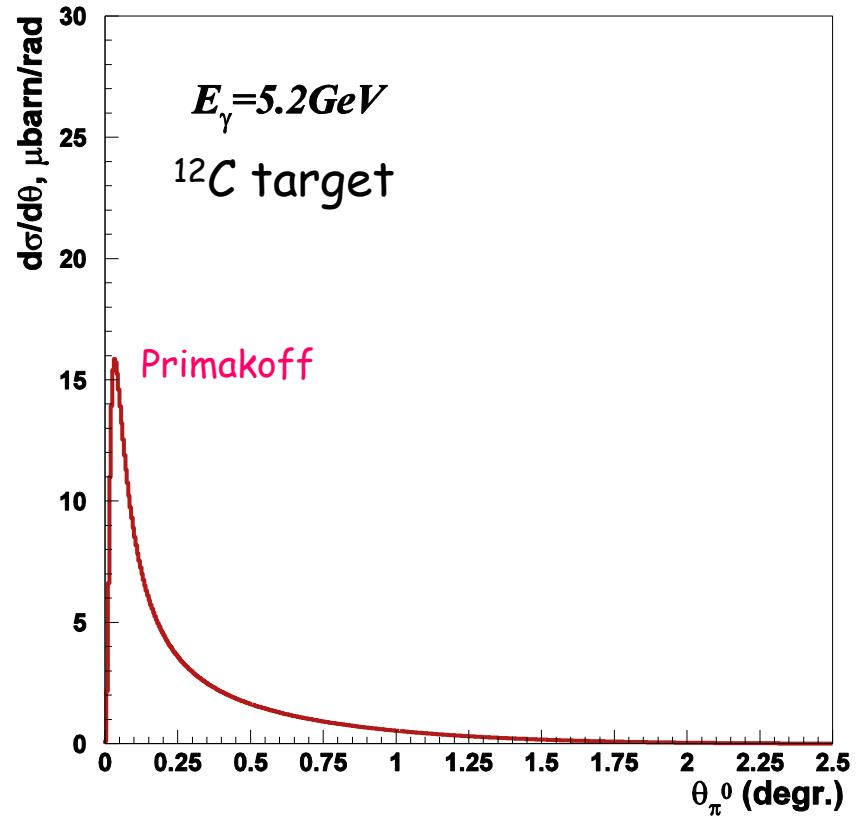
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# Primakoff Method



$$\frac{d\sigma_{\text{Pr}}}{d\Omega} = \boxed{\Gamma_{\pi\pi}} \frac{8\alpha Z^2}{m_\pi^3} \frac{\beta^3 E^4}{Q^4} |F_{e.m.}(Q)|^2 \sin^2 \theta_\pi$$



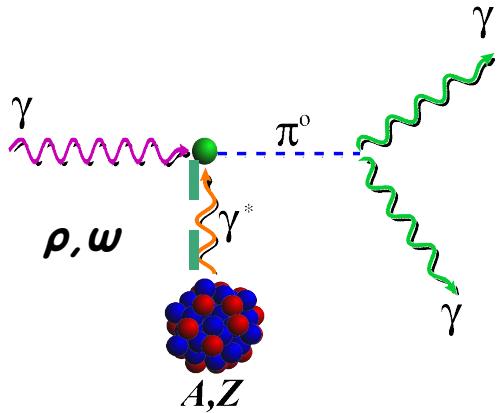
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- Peaked at very small forward angle:  

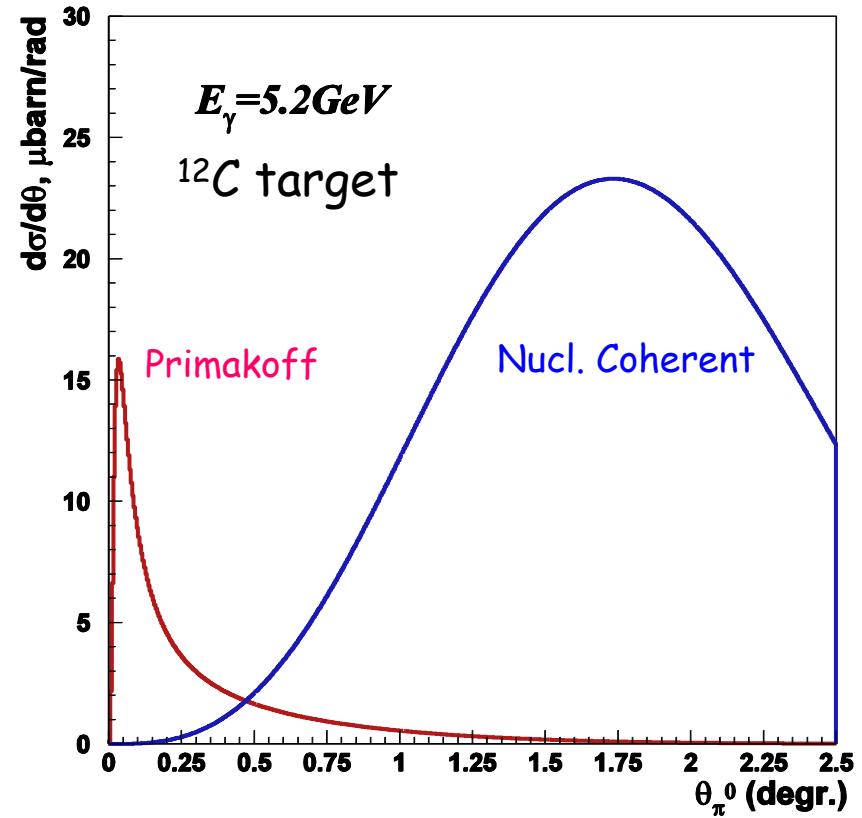
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- Beam energy sensitive:  

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- Coherent process

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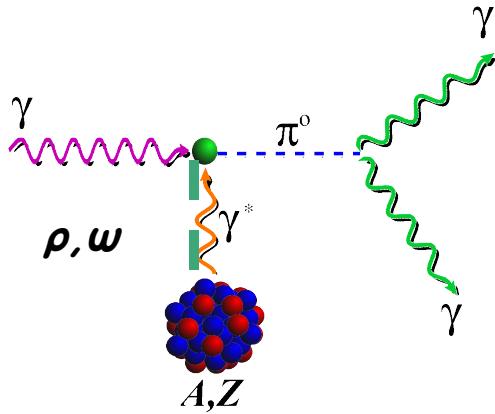
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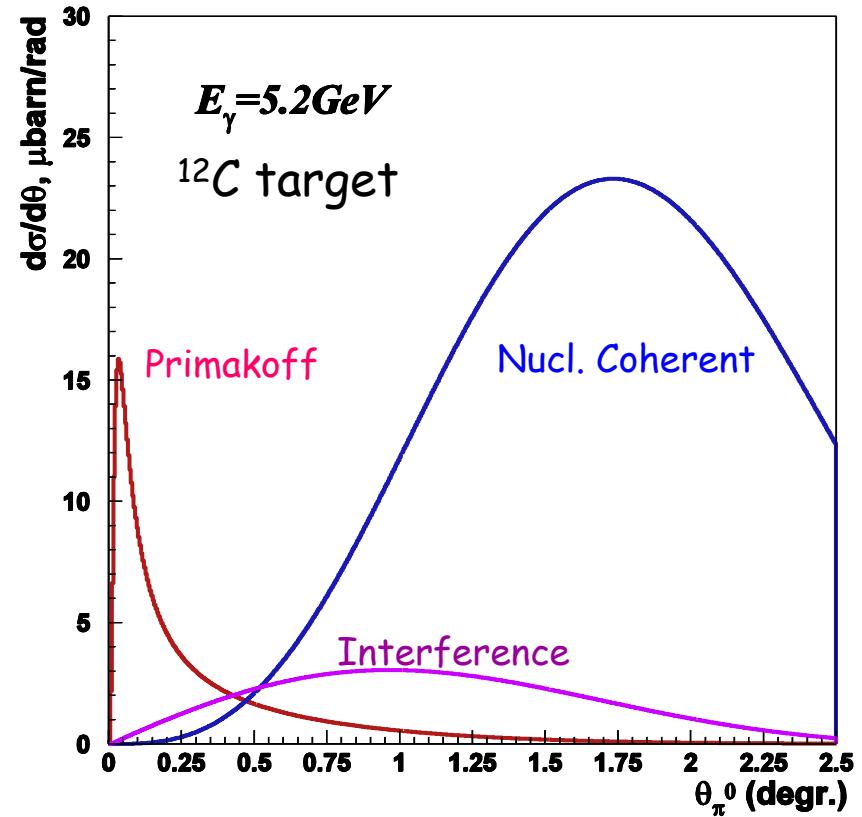
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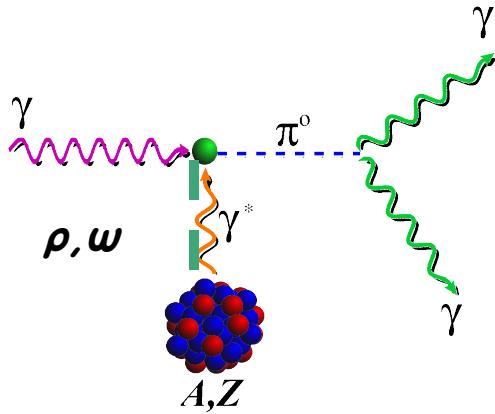
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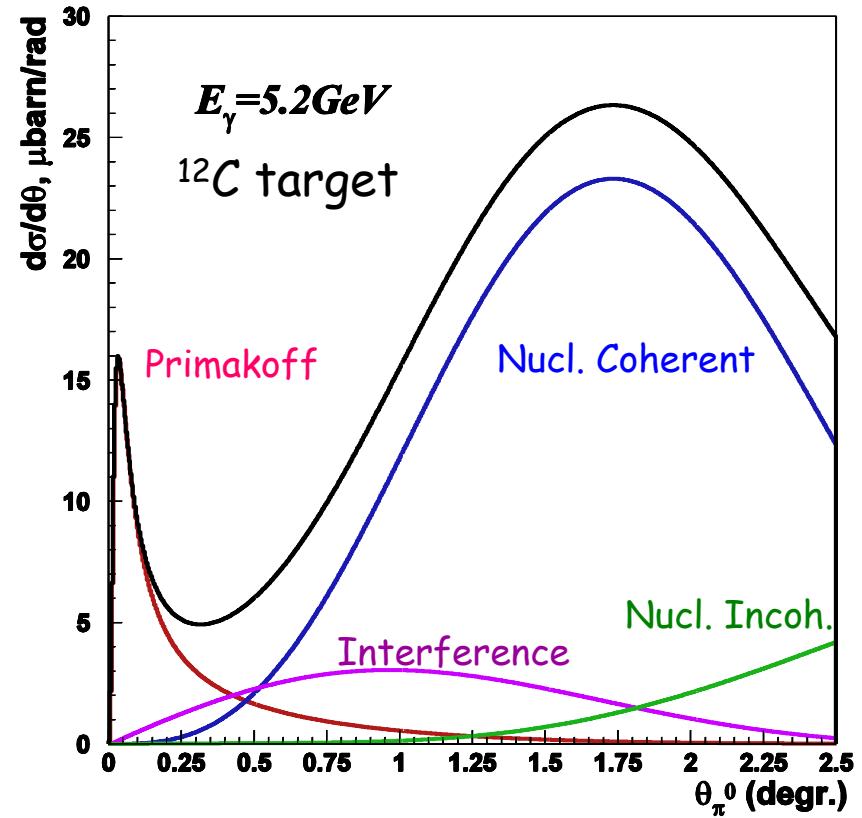
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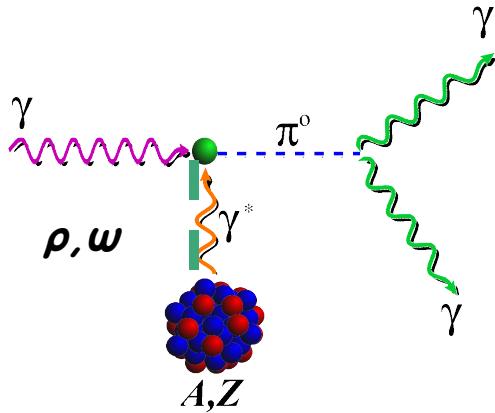
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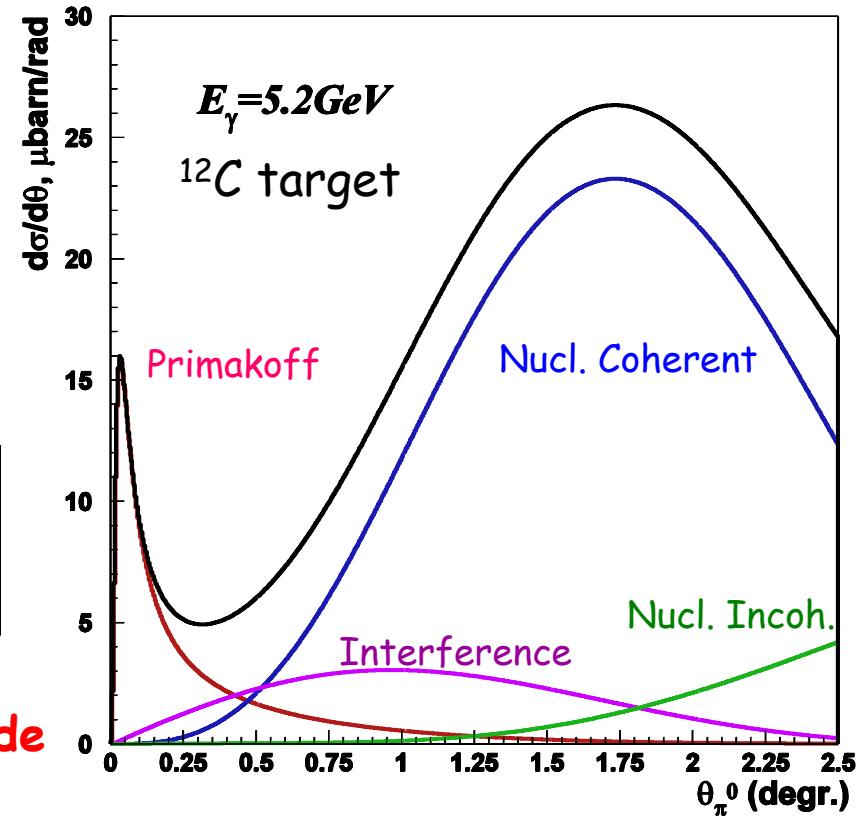
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Challenge: Extract the Primakoff amplitude

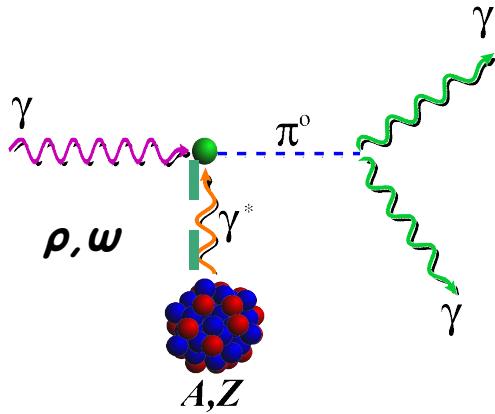
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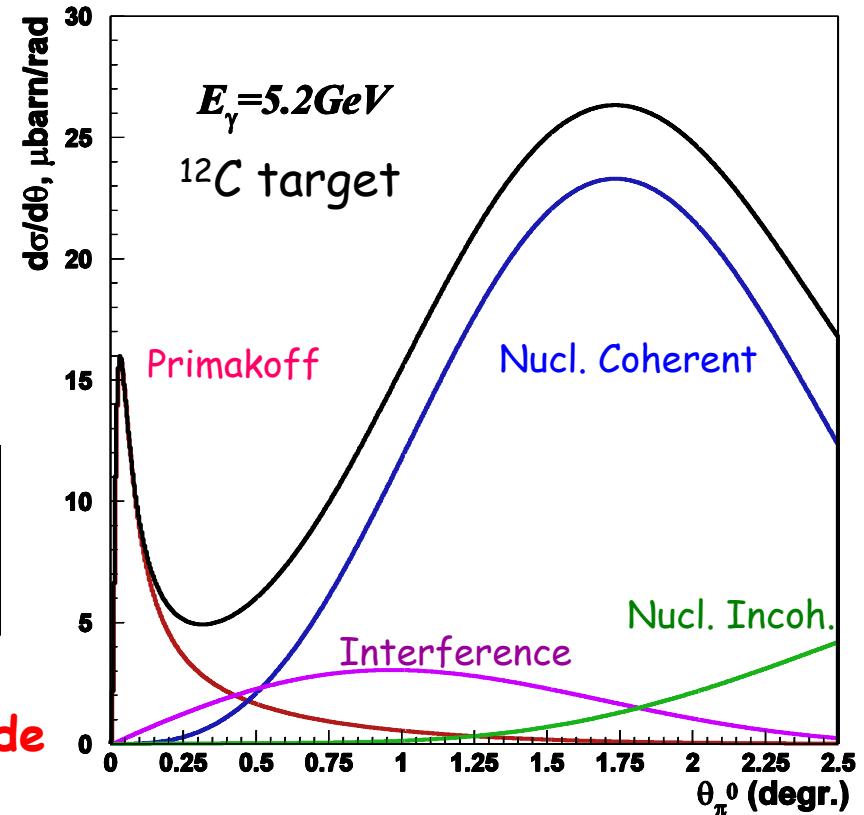


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**Challenge:** Extract the Primakoff amplitude

## Requirement:

- Photon flux
- Beam energy
- $\pi^0$  production angle resolution
- Compact nuclear target



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# PrimEx Experimental Setup

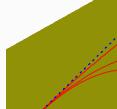
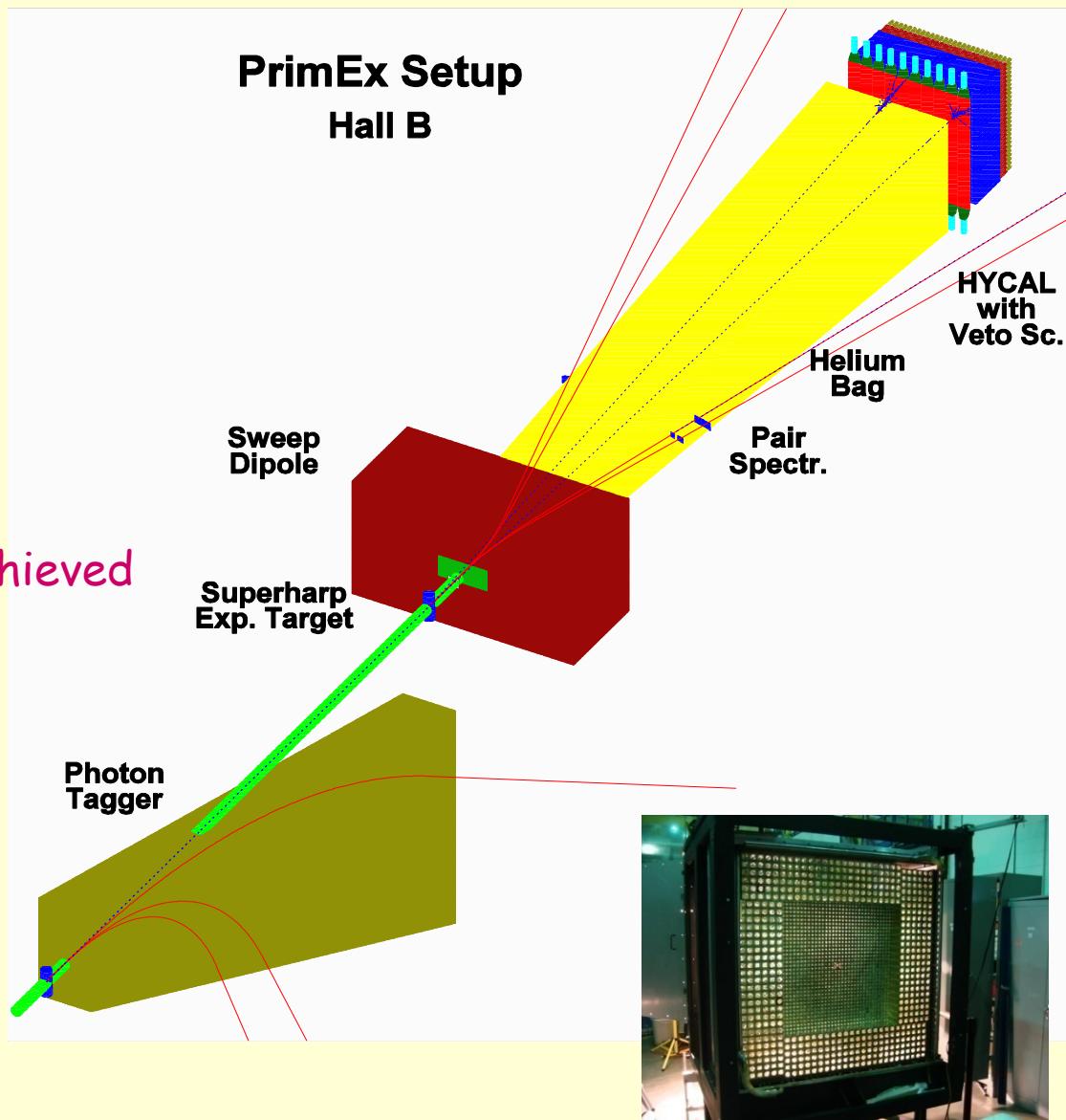
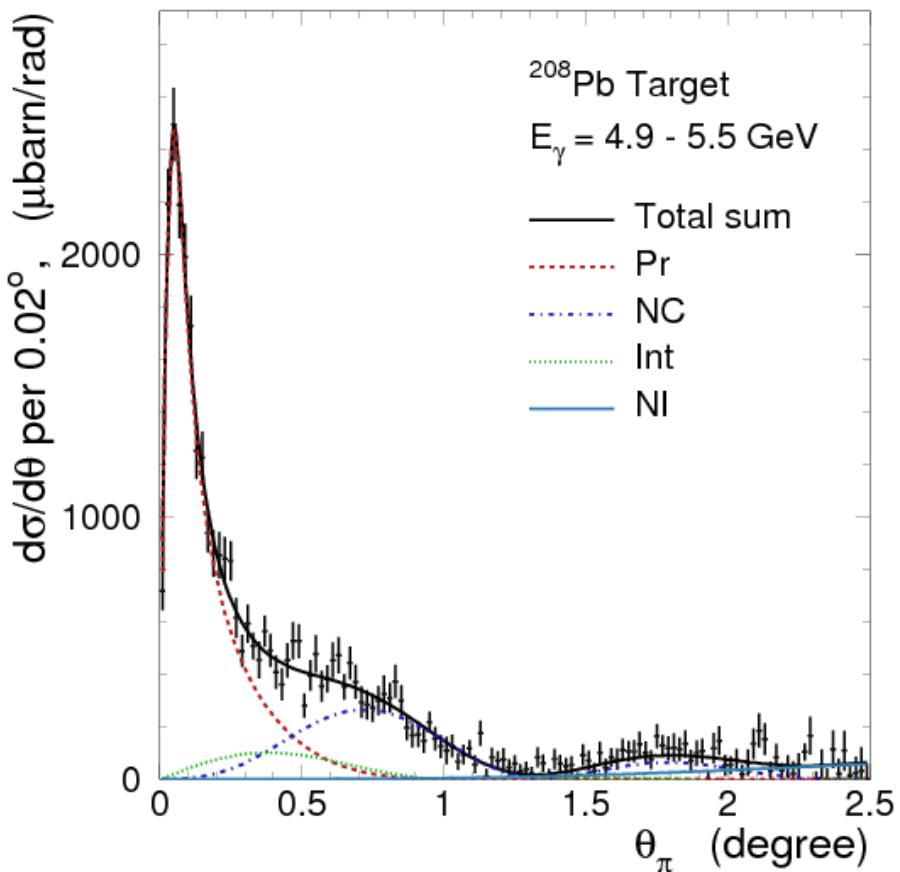
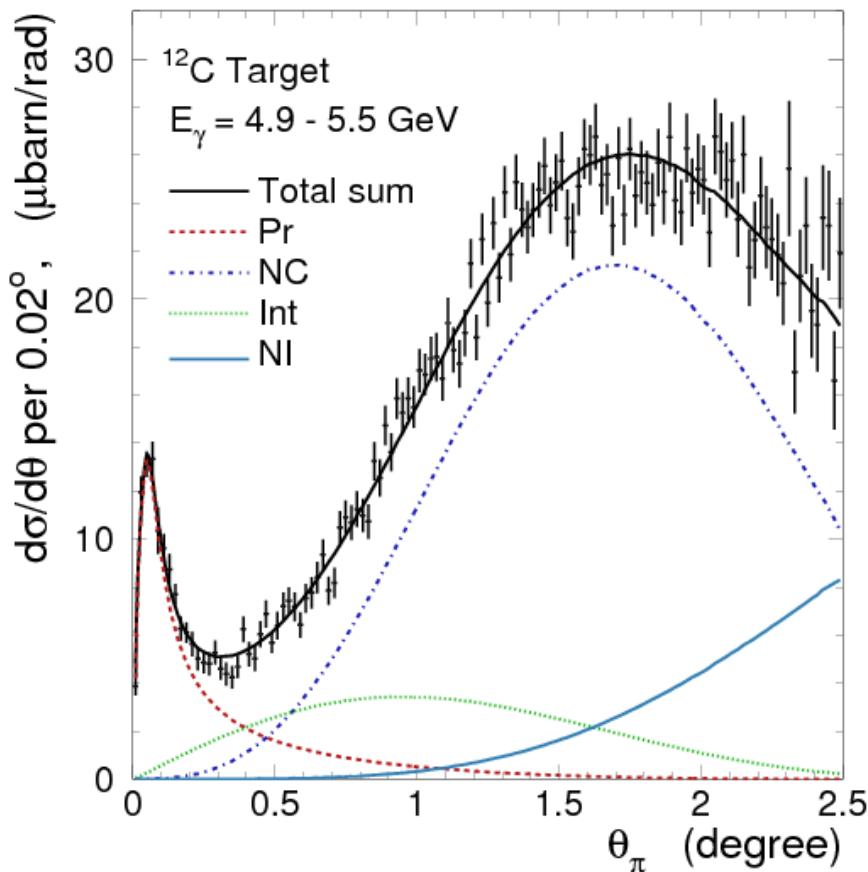
- ❑ JLab Hall B high resolution, high intensity photon tagging facility
  - ❑ New pair spectrometer for photon flux control at high beam intensities
    - 1% accuracy has been achieved
  - ❑ New high resolution hybrid multi-channel calorimeter (HyCal)

Photo Tagge



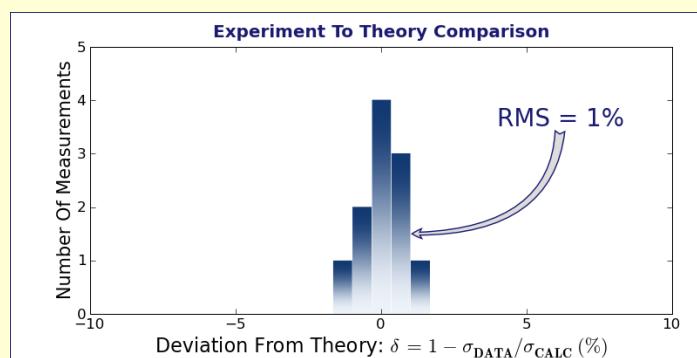
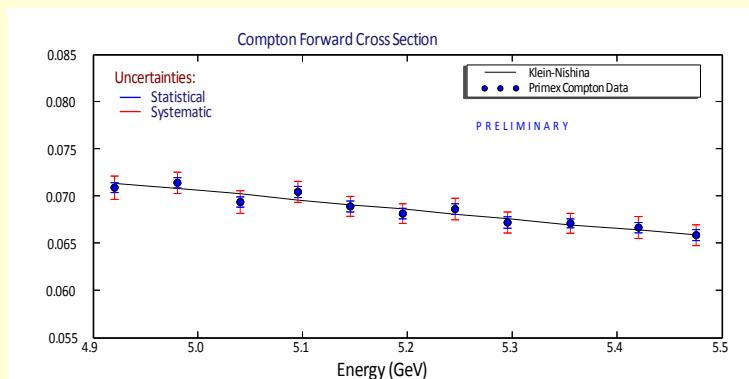
# The First Experiment: PrimEx-I (2004)

Theoretical angular distributions smeared with experimental resolutions are fit to the data on two nuclear targets to extract  $\Gamma(\pi^0 \rightarrow \gamma\gamma)$

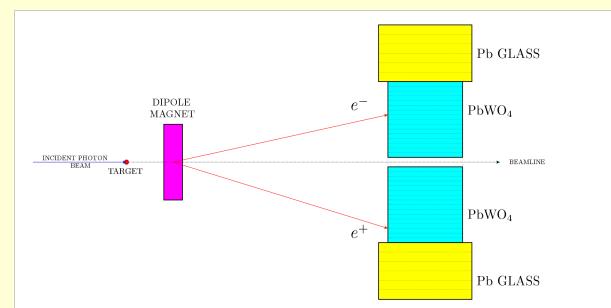
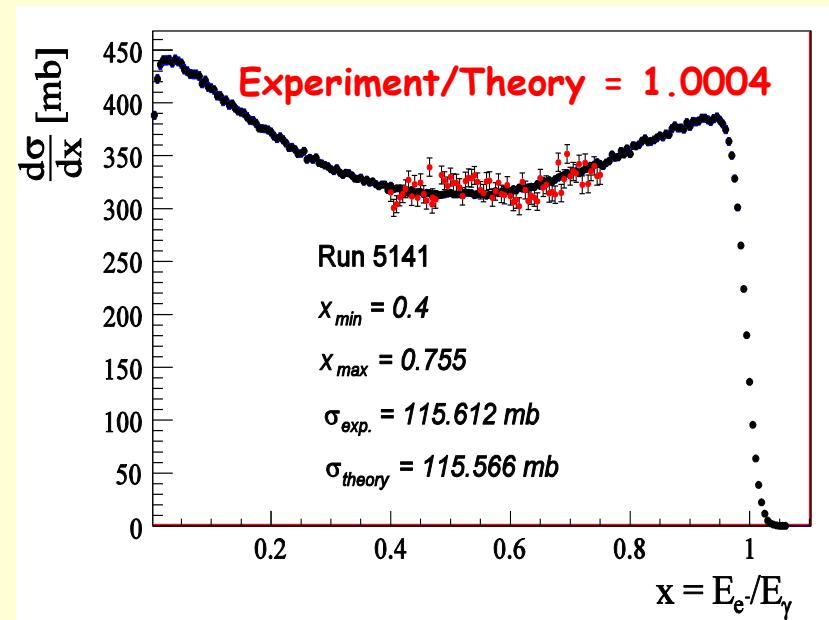


# Verification of Overall Systematical Uncertainties

- $\gamma + e \rightarrow \gamma + e$  Compton cross section measurement

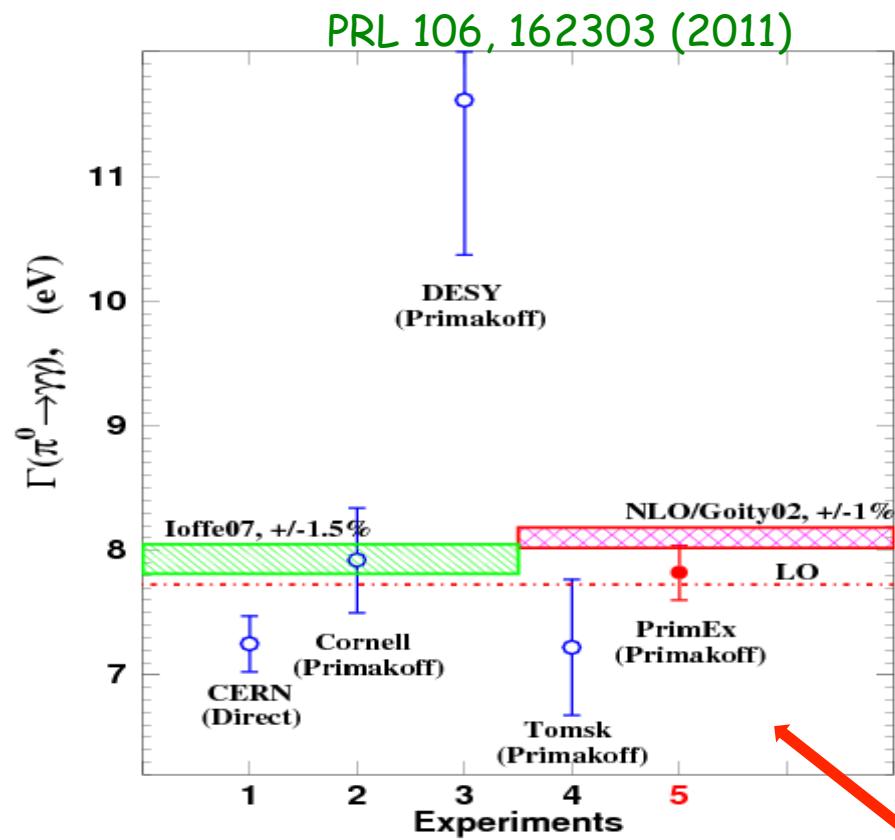


- $e^+e^-$  pair-production cross section measurement:



Systematic uncertainties on cross section are controlled under 1.3%

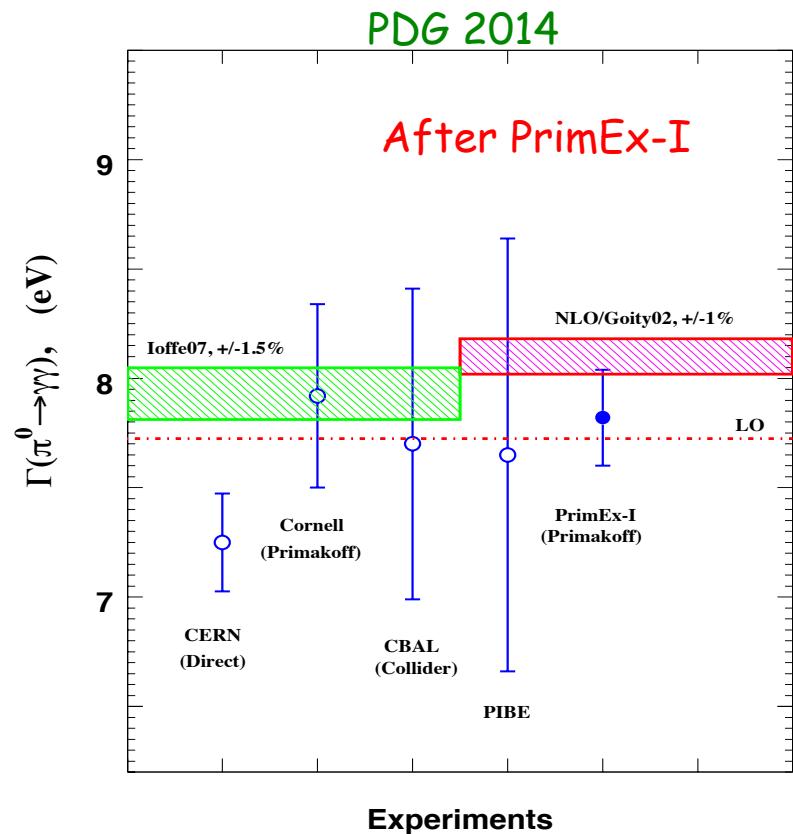
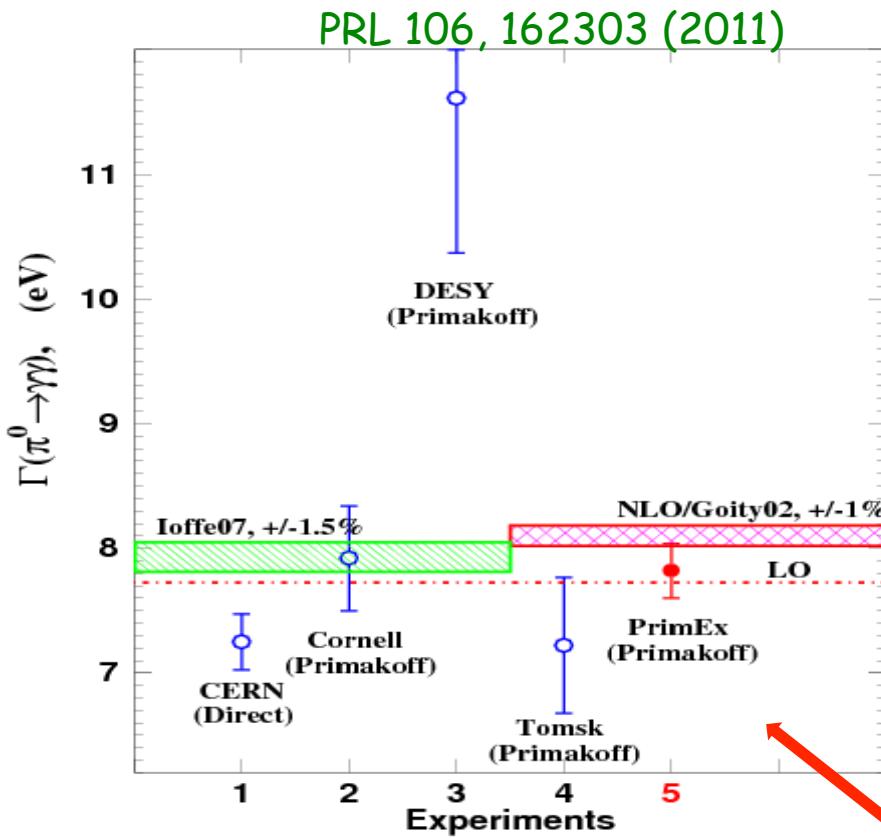
# The first experiment: PrimEx-I Result



$$\Gamma(\pi^0 \rightarrow \gamma\gamma) = 7.82 \pm 0.14(\text{stat}) \pm 0.17(\text{syst}) \text{ eV}$$

2.8% total uncertainty

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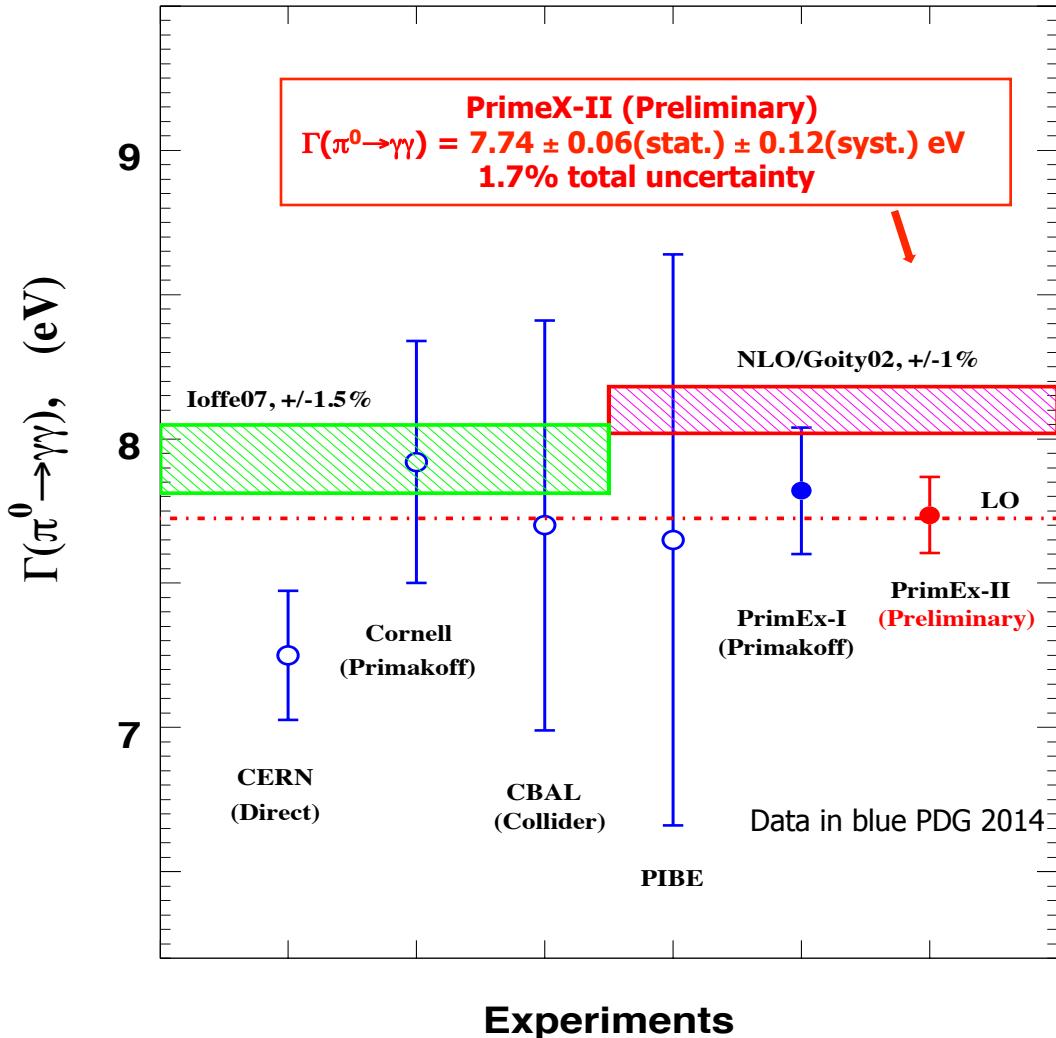
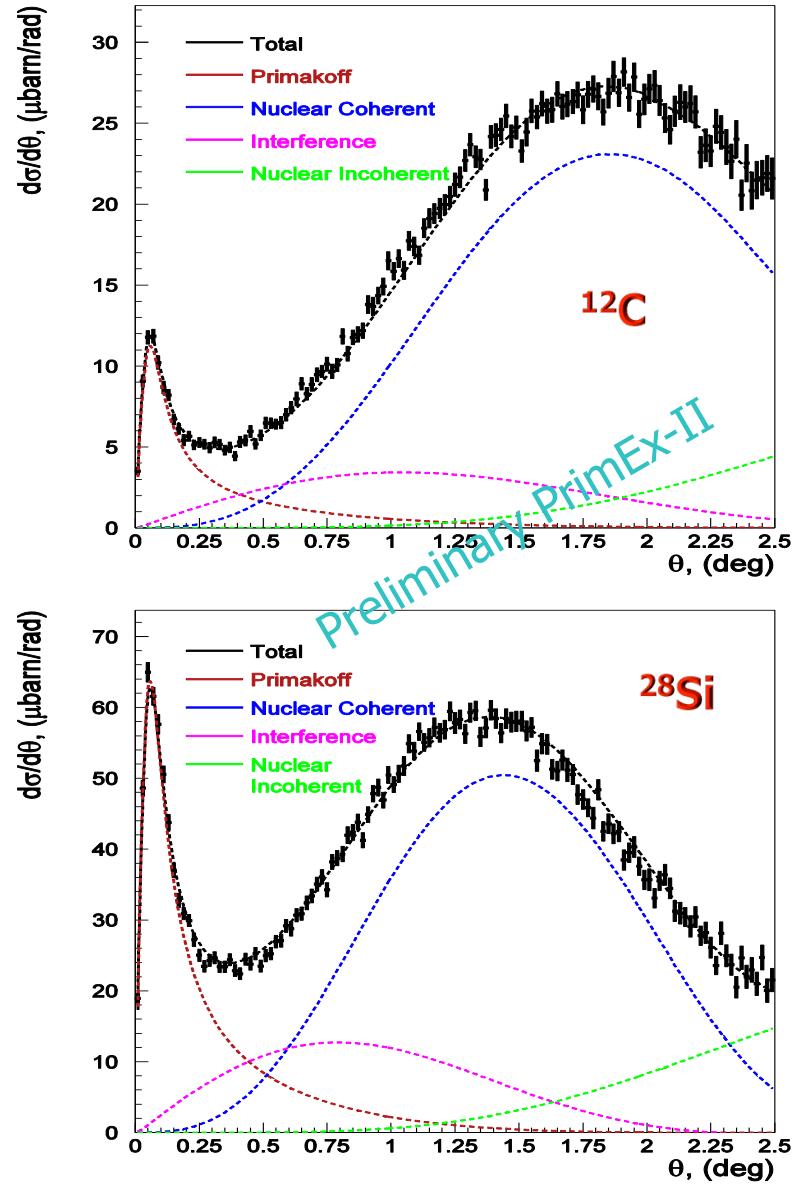


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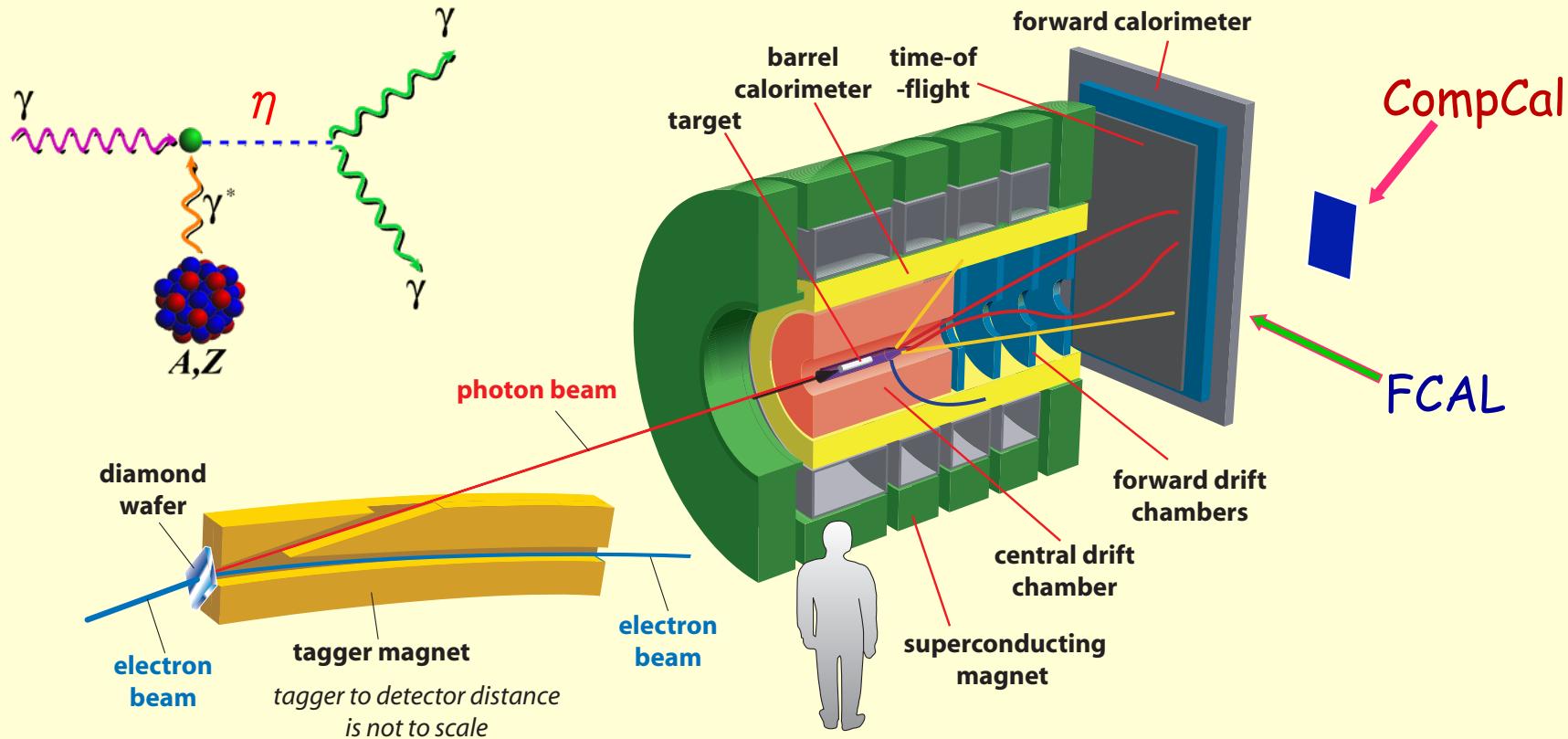
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PrimEx-I improved the precision of PDG average by more than a factor of two

# The Second Experiment: PrimEx-II (two analysis groups)



# Measurement of $\Gamma(\eta \rightarrow \gamma\gamma)$ in Hall D at 12 GeV



- Incoherent tagged photon beam ( $\sim 10.5\text{-}11.5$  GeV)
- Pair spectrometer and a TAC detector for the photon flux control
- 30 cm liquid Hydrogen and  ${}^4\text{He}$  targets ( $\sim 3.6\%$  r.l.)
- Forward Calorimeter (FCAL) for  $\eta \rightarrow \gamma\gamma$  decay photons
- CompCal and FCAL to measure well-known Compton scattering for control of overall systematic uncertainties.
- Solenoid detectors and forward tracking detectors (for background rejection)

# Challenges in the $\eta \rightarrow \gamma\gamma$ Primakoff Experiment

Compared to  $\pi^0$ :

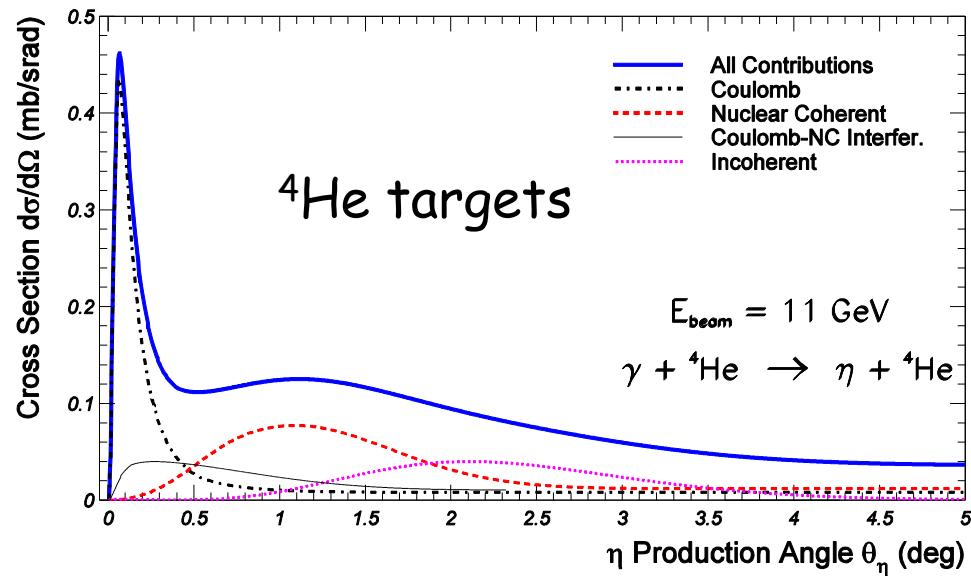
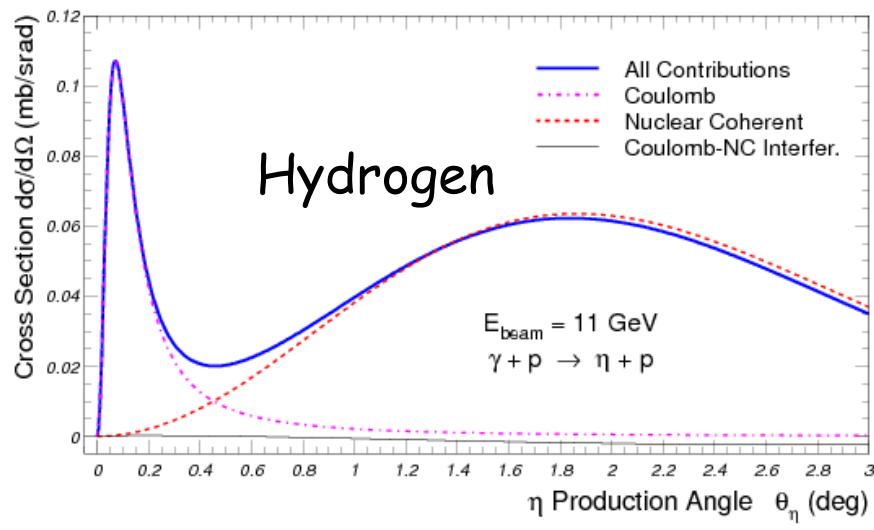
- $\eta$  mass is a factor of 4 larger than  $\pi^0$  and has a smaller cross section

$$\left( \frac{d\sigma_{\text{Pr}}}{d\Omega} \right)_{\text{peak}} \propto \frac{E^4}{m^3}$$

- larger overlap between Primakoff and hadronic processes;

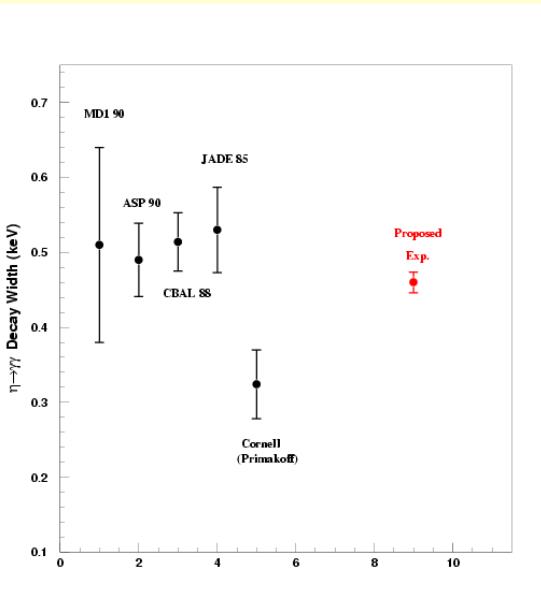
$$\langle \theta_{\text{Pr}} \rangle_{\text{peak}} \propto \frac{m^2}{2E^2} \quad \theta_{NC} \propto \frac{2}{E \cdot A^{1/3}}$$

- larger momentum transfer (coherency, form factors, FSI,...)

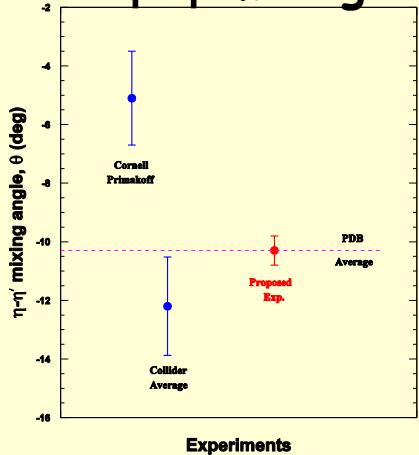


# $\Gamma(\eta \rightarrow \gamma\gamma)$ Experiment @ 12 GeV

1. Resolve long standing discrepancy between collider and Primakoff measurements:

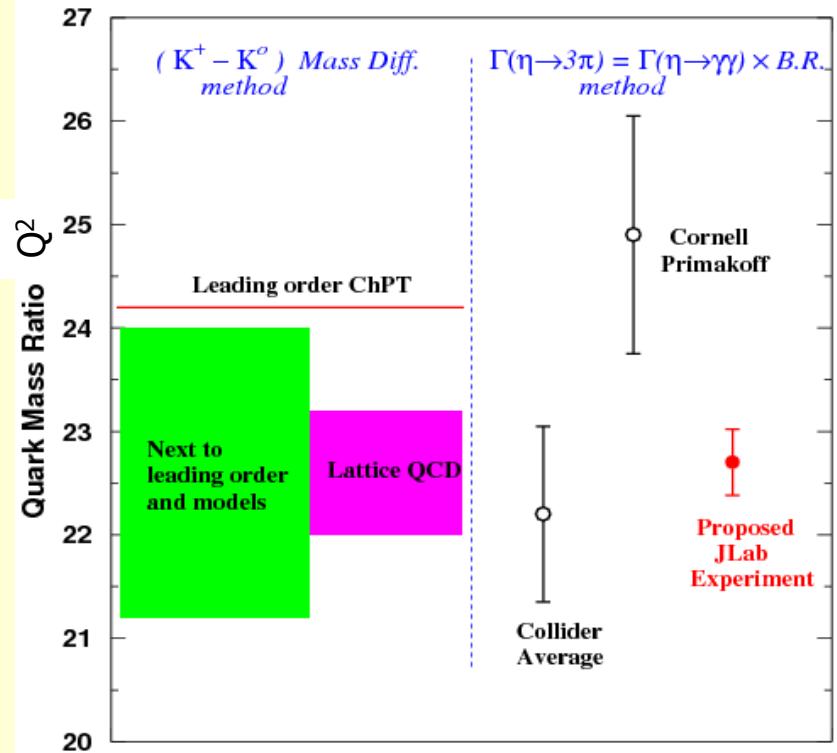


2. Extract  $\eta$ - $\eta'$  mixing angle:



3. Determine Light quark mass ratio:

$$Q^2 = \frac{m_s^2 - \hat{m}^2}{m_d^2 - m_u^2}, \quad \text{where } \hat{m} = \frac{1}{2}(m_u + m_d)$$

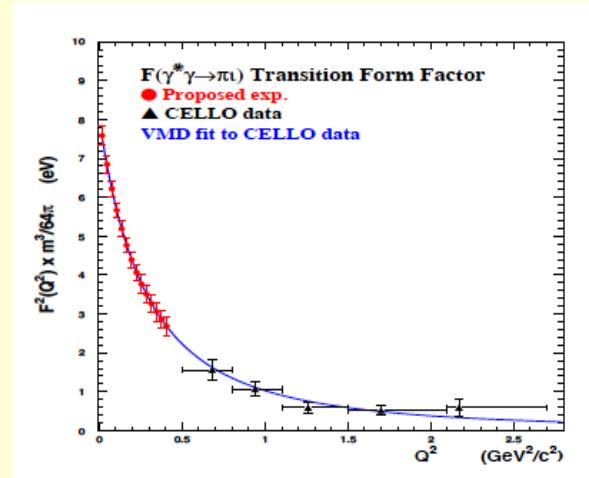


H. Leutwyler Phys. Lett., B378, 313 (1996)

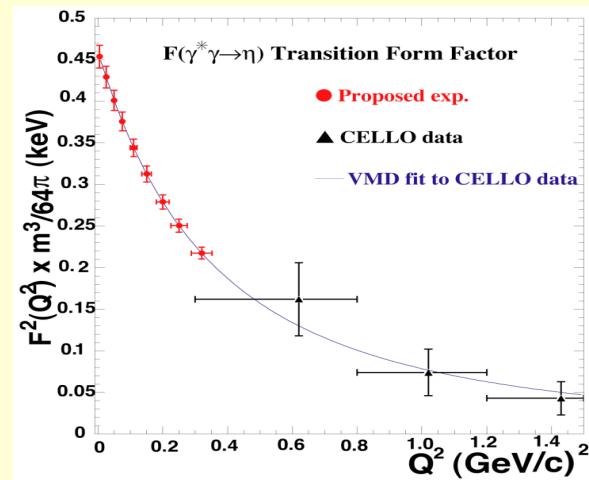
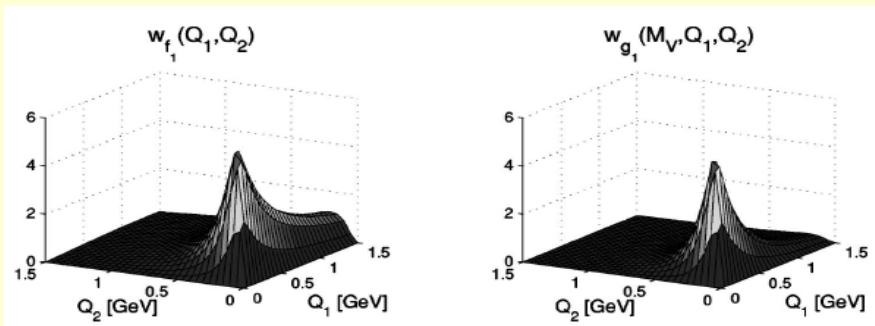
# Transition Form Factors $F(\gamma\gamma^*\rightarrow p)$ (at low $Q^2$ : 0.001-0.5 GeV $^2/c^2$ )

- Direct measurement of slopes

- Interaction radii:  
 $F_{\gamma\gamma^*p}(Q^2) \approx 1 - 1/6 \cdot \langle r^2 \rangle_p Q^2$
- ChPT for large  $N_c$  predicts relation between the three slopes. Extraction of  $O(p^6)$  low-energy constant in the chiral Lagrangian



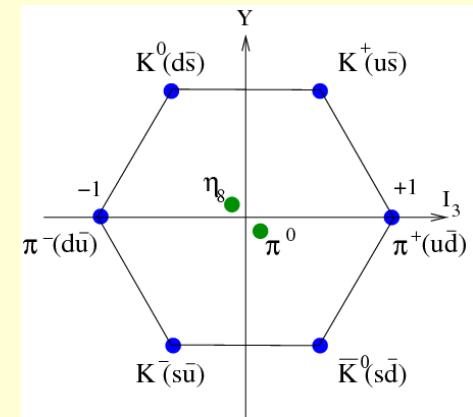
- Input for hadronic light-by-light calculations in muon ( $g-2$ )



M. Knecht and A. Nyffeler, Phys.Rev.D65,073034

# $\eta$ is a unique probe for fundamental symmetries

- ◆ The most massive member in the octet of pseudoscalar Goldstone mesons ( $547.9 \text{ MeV}/c^2$ )
  - ➡ Many open decay channels
  - ➡ Sensitive to symmetry breakings



- ◆  $\eta$  decay width  $\Gamma_\eta = 1.3 \text{ KeV}$  is **narrow** (relative to  $\Gamma_\omega = 8.5 \text{ MeV}$ )
  - ➡ The lowest orders of  $\eta$  decays are filtered out, enhancing the contributions from higher orders (by a factor of  $\sim 7000$  compared to  $\omega$  decays).
- ◆ Eigenstate of P, **C**, CP, and G:  $I^G J^{PC} = 0^+ 0^{--}$ 
  - ➡ Study violations of **discrete symmetries**
- ◆ The  $\eta$  decays are **flavor-conserving** reactions effectively free of SM backgrounds for new physics search.

# Overview of the Jlab Eta Factory (JEF) Project

Mode	Branching Ratio	Physics Highlight	Photons
priority:			
$\pi^0 2\gamma$	$(2.7 \pm 0.5) \times 10^{-4}$	$\chi$ PTh at $\mathcal{O}(p^6)$	4
$\gamma + B$	beyond SM	leptophobic dark boson	4
$3\pi^0$	$(32.6 \pm 0.2)\%$	$m_u - m_d$	6
$\pi^+ \pi^- \pi^0$	$(22.7 \pm 0.3)\%$	$m_u - m_d$ , CV	2
$3\gamma$	$< 1.6 \times 10^{-5}$	CV, CPV	3
ancillary:			
$4\gamma$	$< 2.8 \times 10^{-4}$	$< 10^{-11}$ [112]	4
$2\pi^0$	$< 3.5 \times 10^{-4}$	CPV, PV	4
$2\pi^0 \gamma$	$< 5 \times 10^{-4}$	CV, CPV	5
$3\pi^0 \gamma$	$< 6 \times 10^{-5}$	CV, CPV	6
$4\pi^0$	$< 6.9 \times 10^{-7}$	CPV, PV	8
$\pi^0 \gamma$	$< 9 \times 10^{-5}$	CV, Ang. Mom. viol.	3
normalization:			
$2\gamma$	$(39.3 \pm 0.2)\%$	anomaly, $\eta-\eta'$ mixing PR12-10-011	2

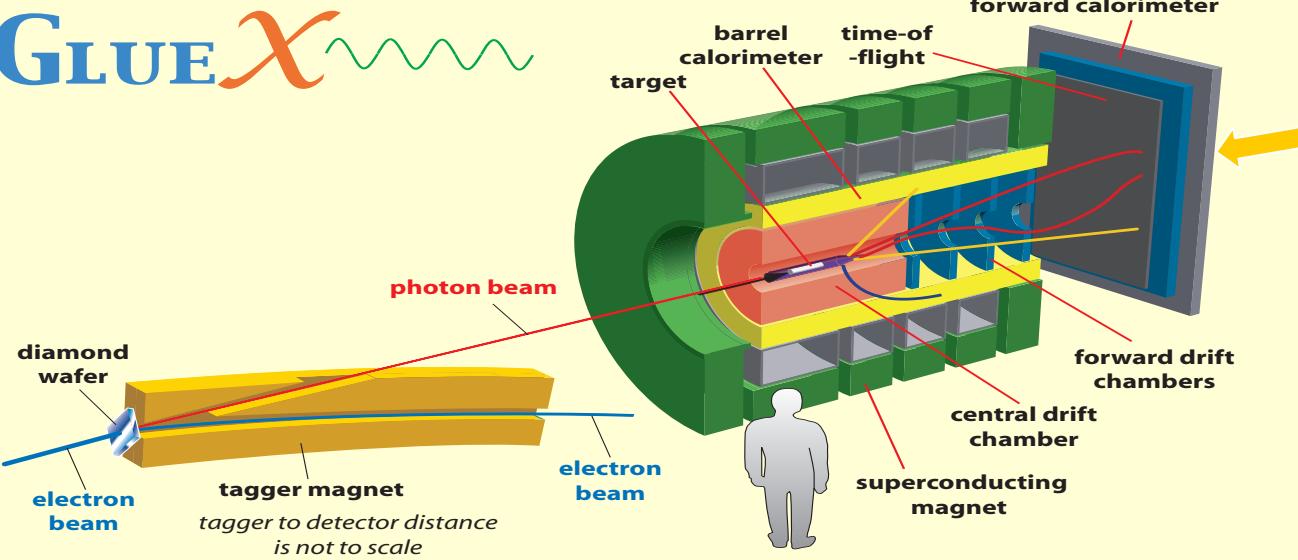
Main physics goals:

1. Search for a leptophobic dark boson (B).
2. Directly constrain CVPC new physics
3. Improve the light quark mass ratio
4. Probe interplay of VMD & scalar resonances in ChPT.

FCAL-II is required for the rare decays

# Jlab Eta Factory (JEF) Experiment

GlueX



Simultaneously measure  $\eta$  decays:  $\eta \rightarrow \pi^0 \gamma\gamma$ ,  $\eta \rightarrow 3\gamma$ , and ...

- ◆  $\eta$  produced on LH<sub>2</sub> target with **9-11.7 GeV tagged photon beam**:  
 $\gamma + p \rightarrow \eta + p$
- ◆ Reduce non-coplanar backgrounds by **detecting recoil p's** with GlueX detector ( $\epsilon \sim 75\%$ )
- ◆ Upgraded Forward Calorimeter with **High resolution, high granularity PbWO<sub>4</sub>** insertion (**FCAL-II**) to detect multi-photons from rare  $\eta$  decays

# World competition in $\eta$ decays

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$e^+e^-$   
Collider

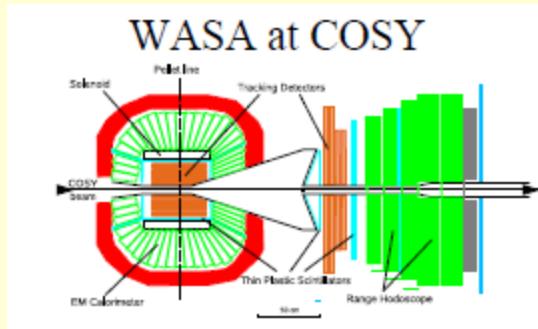


# World competition in $\eta$ decays

$e^+e^-$   
Collider

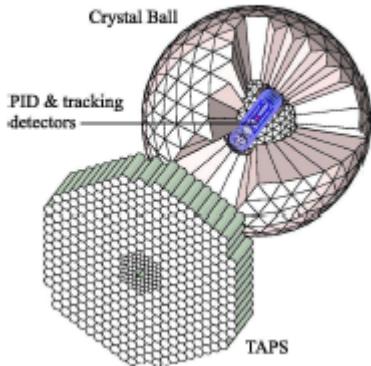


Fixed-target

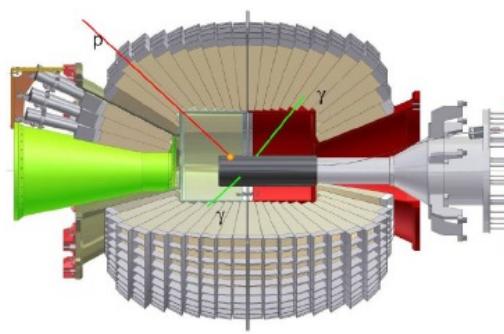


hadroproduction

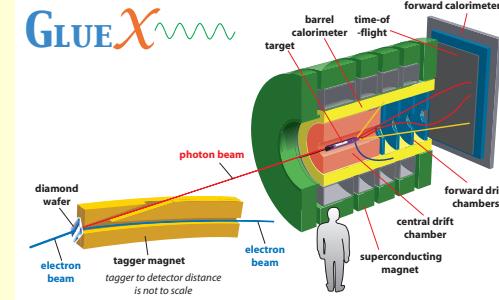
Crystall Ball at MAMI



CBELSA/TAPS at ELSA



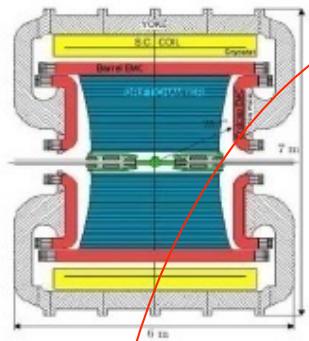
JEF at Jlab



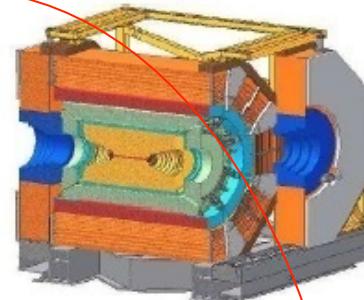
# World competition in $\eta$ decays

e<sup>+</sup>e<sup>-</sup>  
Collider

KLOE-2 at DAΦNE



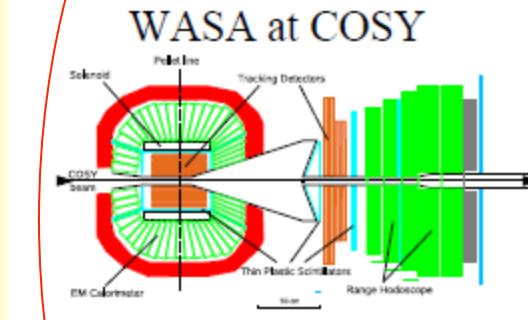
BESIII at BEPCII



Low energy  
 $\eta$ -facilities

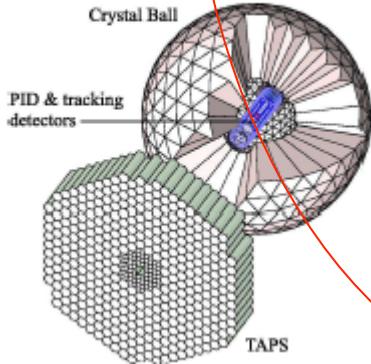
Fixed-target

WASA at COSY



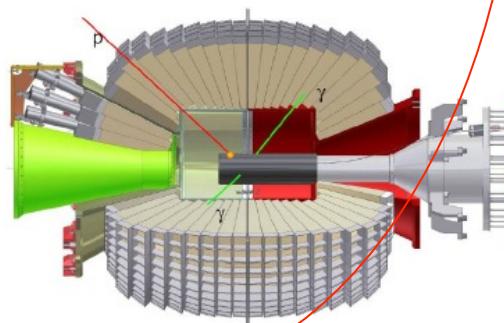
hadroproduction

Crystall Ball at MAMI



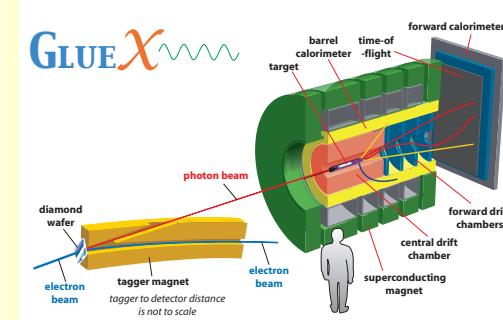
photoproduction

CBELSA/TAPS at ELSA



JEF at Jlab

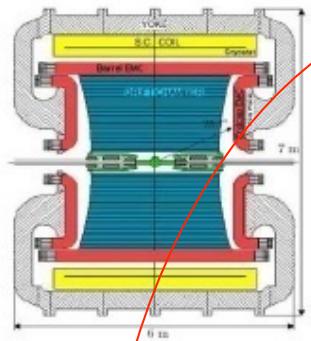
GLUE X



# World Competition in $\eta$ Decays

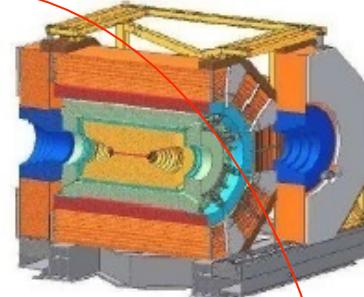
e<sup>+</sup>e<sup>-</sup>  
Collider

KLOE-2 at DAΦNE



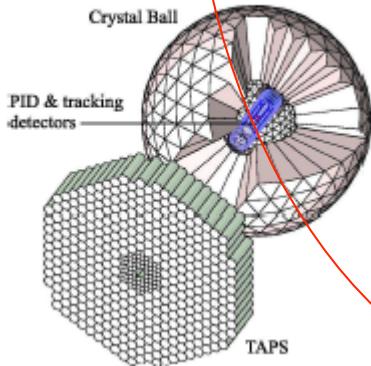
Fixed-target

BESIII at BEPCII



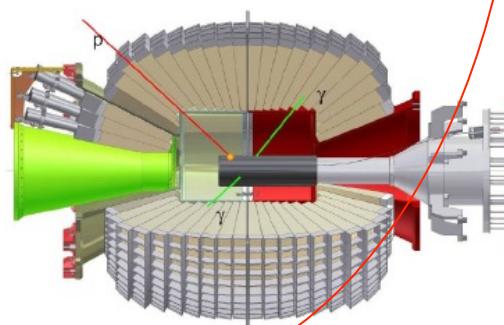
Low energy  
 $\eta$ -facilities

Crystall Ball at MAMI



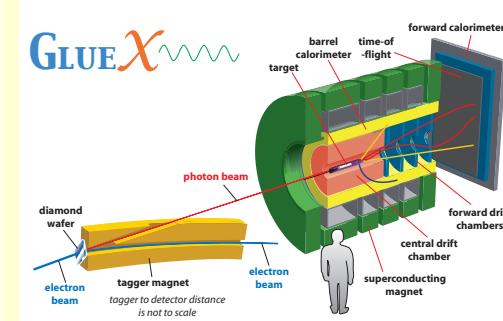
photoproduction

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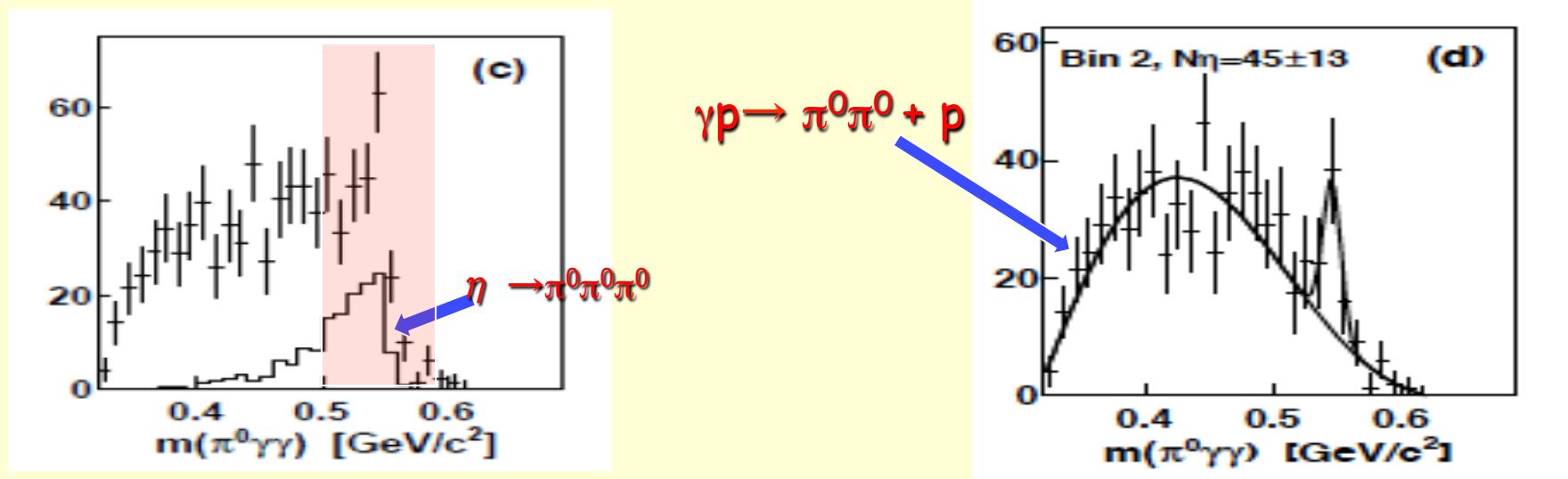
JEF at Jlab

GLUE 



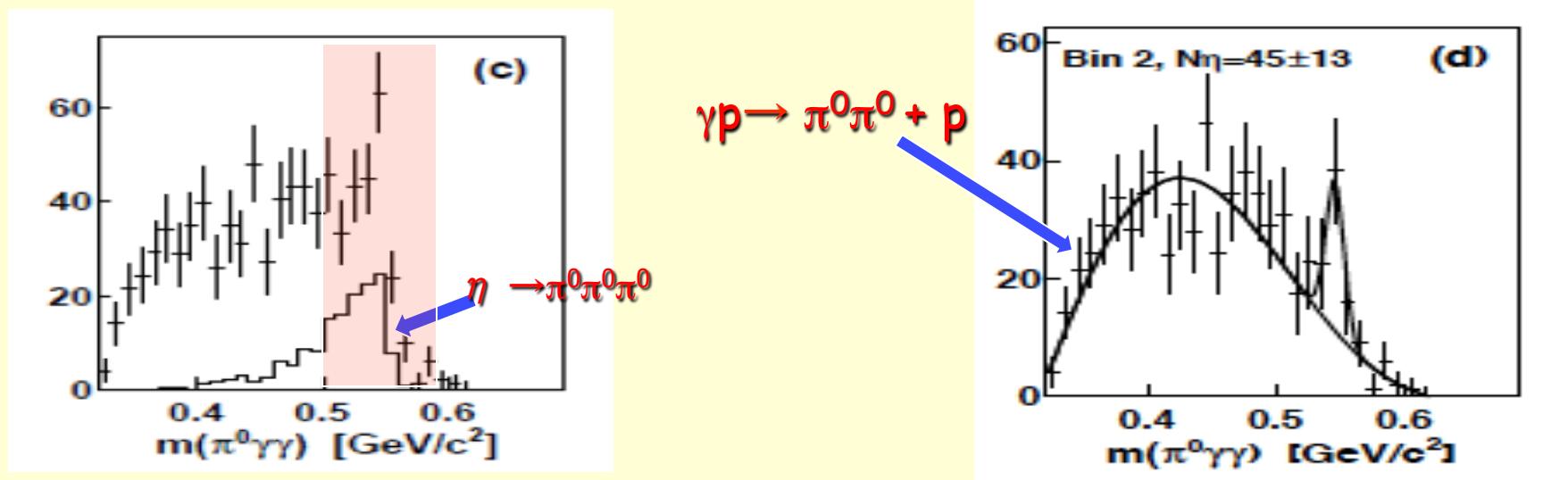
# Filter Background with $\eta$ Energy Boost ( $\eta \rightarrow \pi^0\gamma\gamma$ )

A2 at MAMI (Phys.Rev. C90 (2014) 025206):  $\gamma p \rightarrow np$  ( $E_\gamma = 1.5 \text{ GeV}$ )

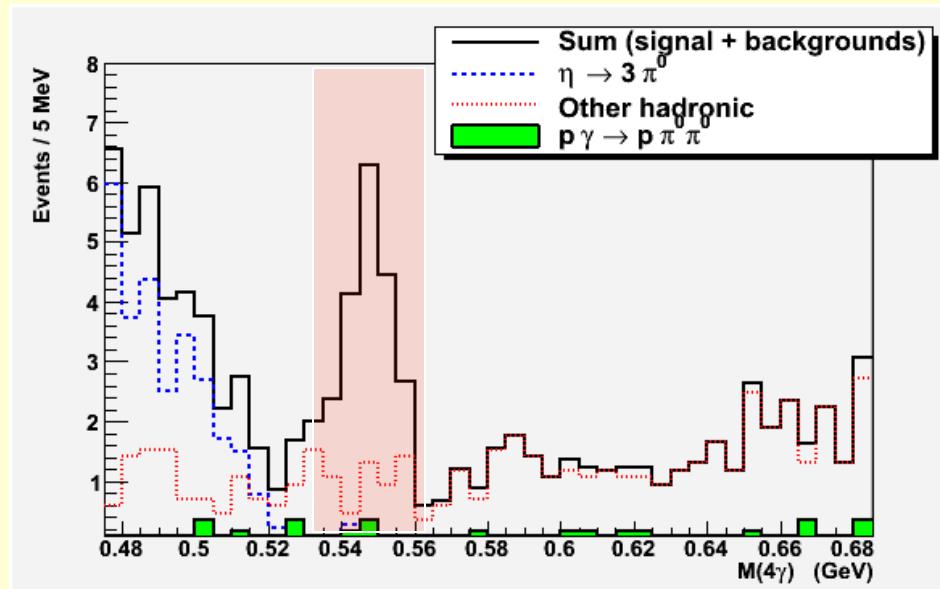


# Filter Background with $\eta$ Energy Boost ( $\eta \rightarrow \pi^0\gamma\gamma$ )

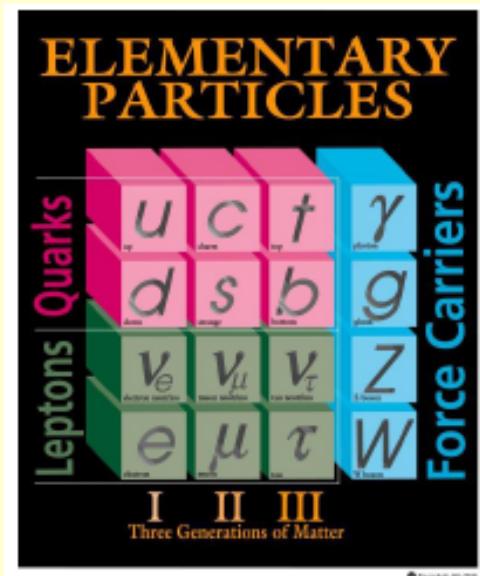
A2 at MAMI (Phys.Rev. C90 (2014) 025206):  $\gamma p \rightarrow np$  ( $E_\gamma = 1.5 \text{ GeV}$ )



Jlab:  
 $\gamma p \rightarrow np$  ( $E_\gamma = 9-11.7 \text{ GeV}$ )



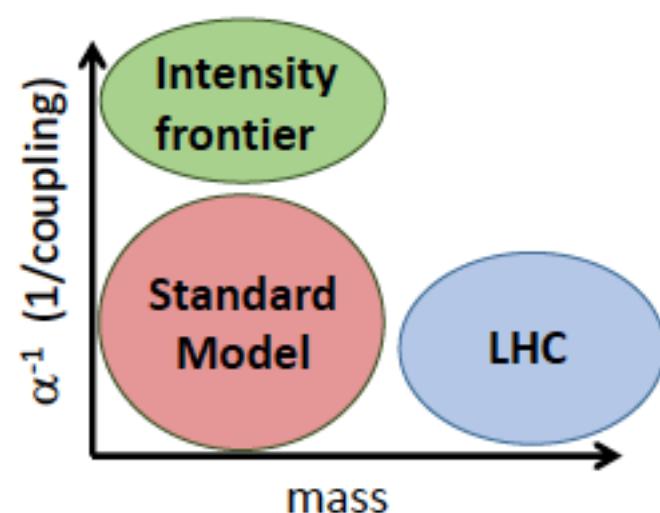
# Search for Dark Forces



SM based on  $SU(3)_C \times SU(2)_L \times U(1)_Y$  gauge symmetry. Are there any additional gauge symmetries? Look for new gauge bosons.

## Motivations:

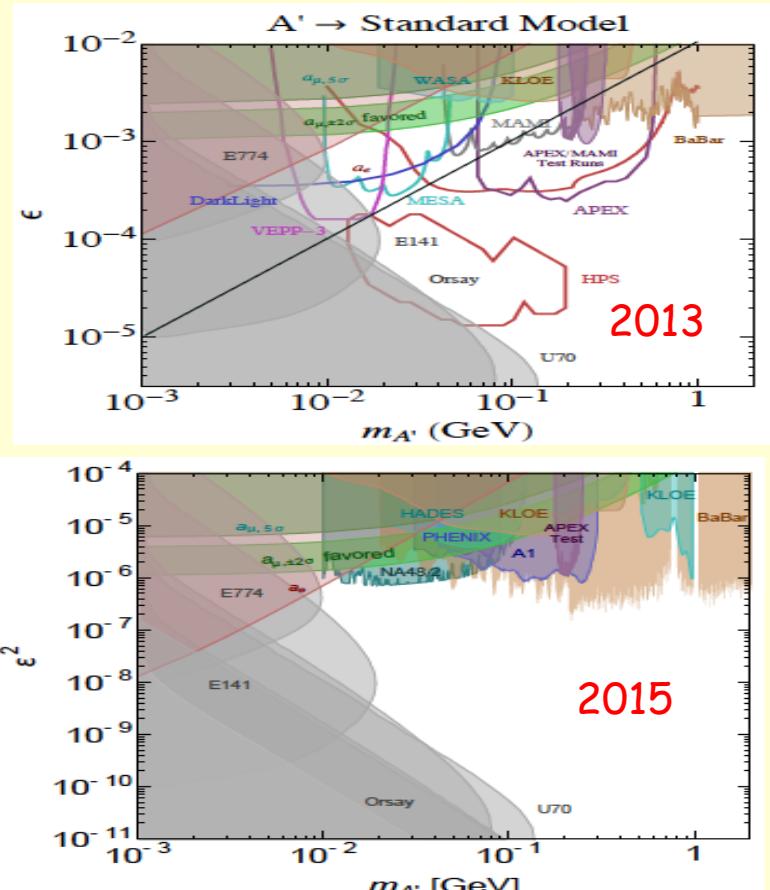
- Grand unified theories:** Generically have additional gauge bosons, but typically very heavy ( $10^{16}$  GeV).
- Dark matter:** Stability of dark matter related to new gauge symmetry?  
Can also give the right relic density.



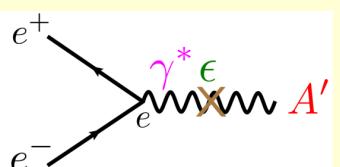
# "Vector Portal" to Dark Sector

## 1. Dark photon $A'$

$$-\frac{1}{2}\epsilon F^{\mu\nu}F_{\mu\nu}' \text{ Kinetic mixing and U(1)'} \\$$



Most  $A'$  searches look for  $A' \rightarrow l^+l^-$ , relying on the leptonic coupling of new force



## 2. Dark leptophobic B-boson (dark $\omega$ , $\gamma_B$ , or $Z'$ ):

$$\frac{1}{3}g_B \bar{q}\gamma^\mu q B_\mu$$

Gauged baryon symmetry  $U(1)_B$

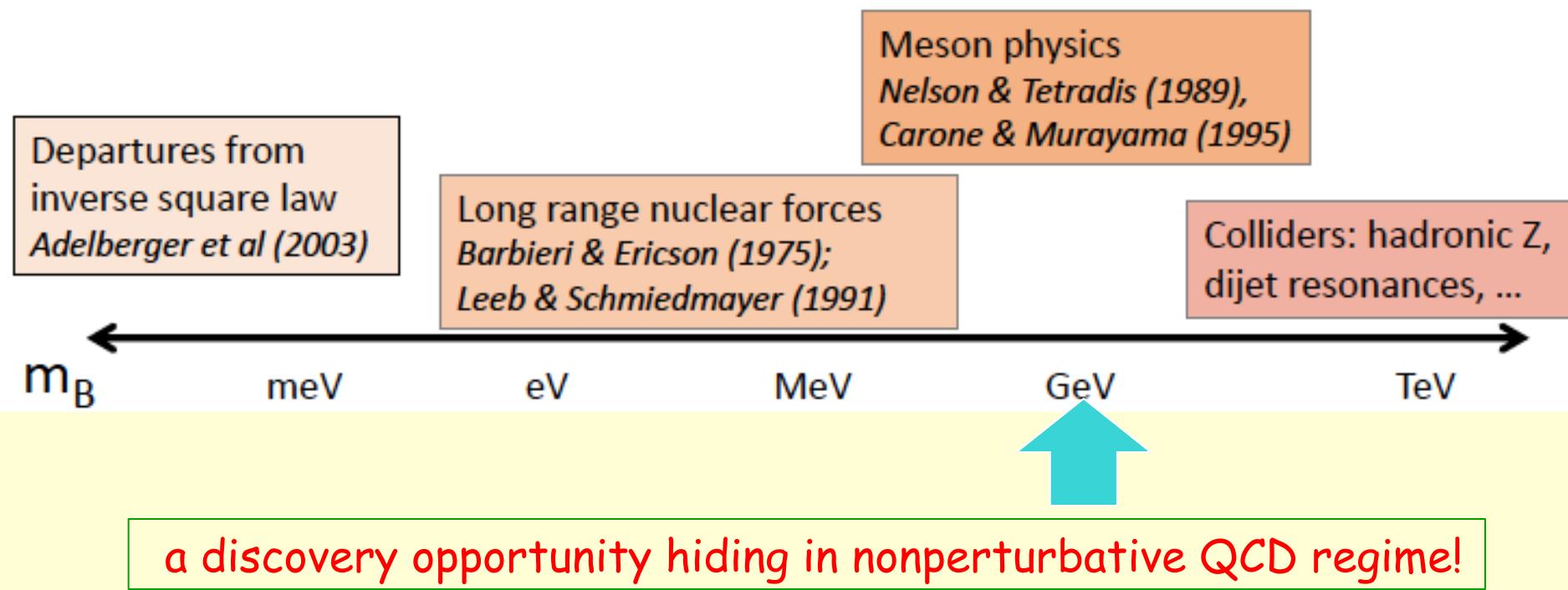
T.D. Lee and C.N. Yang, Phys.Rev., 98, 1501 (1955)

- ◆ the stability of baryonic and dark matter
- ◆ a unified genesis of baryonic and dark matter      M.Graesser, I. Shoemaker and L. Vecchi, arXiv:1107.2666
- ◆ a natural framework for resolving "Strong CP problem" in QCD

# Experimental Probes for B-boson

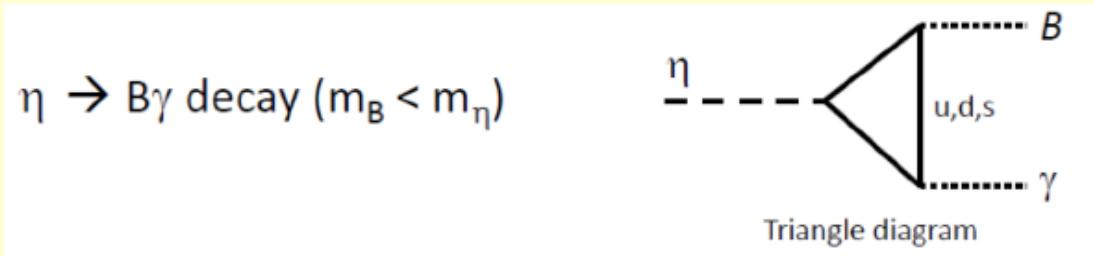
Discovery signals depend on the B mass:

- ◆ the  $m_B < m_\pi$  region is strongly constrained by long-range forces search and nuclear scattering experiments.
- ◆ the  $m_B > 50\text{GeV}$  region has been investigated by the collider experiments.
- ◆ **GeV-scale domain is nearly untouched.**

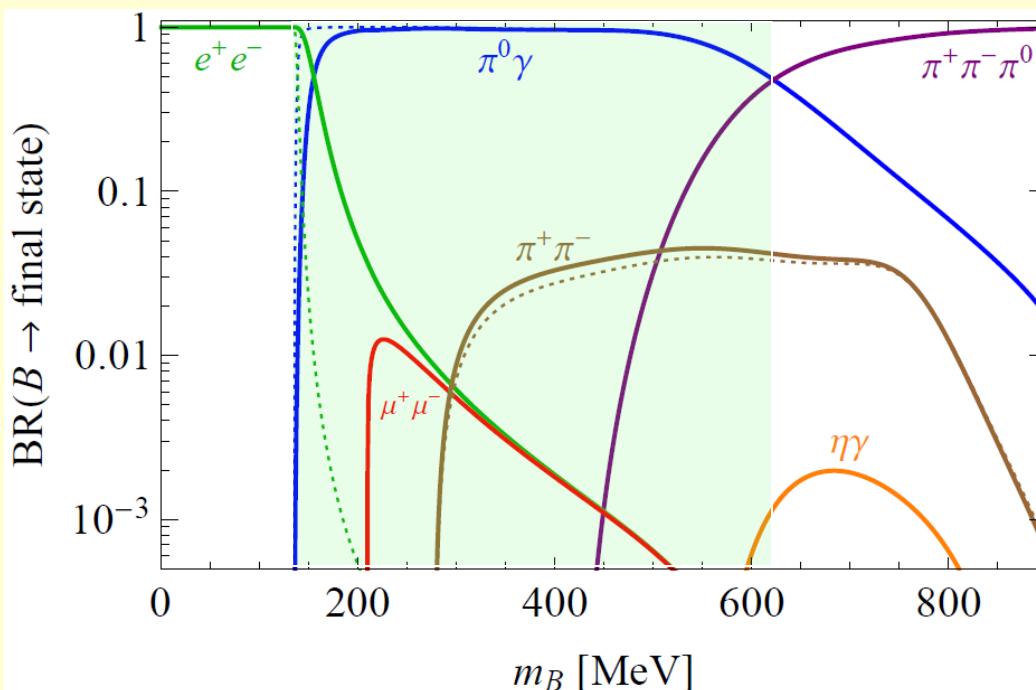


# Striking Signature for B-boson in $\eta \rightarrow \pi^0 \gamma\gamma$

- ◆ B production: A.E. Nelson, N. Tetradis, Phys. Lett., B221, 80 (1989)



- ◆ B decays:  $B \rightarrow \pi^0 \gamma$  in 140-620 MeV mass range



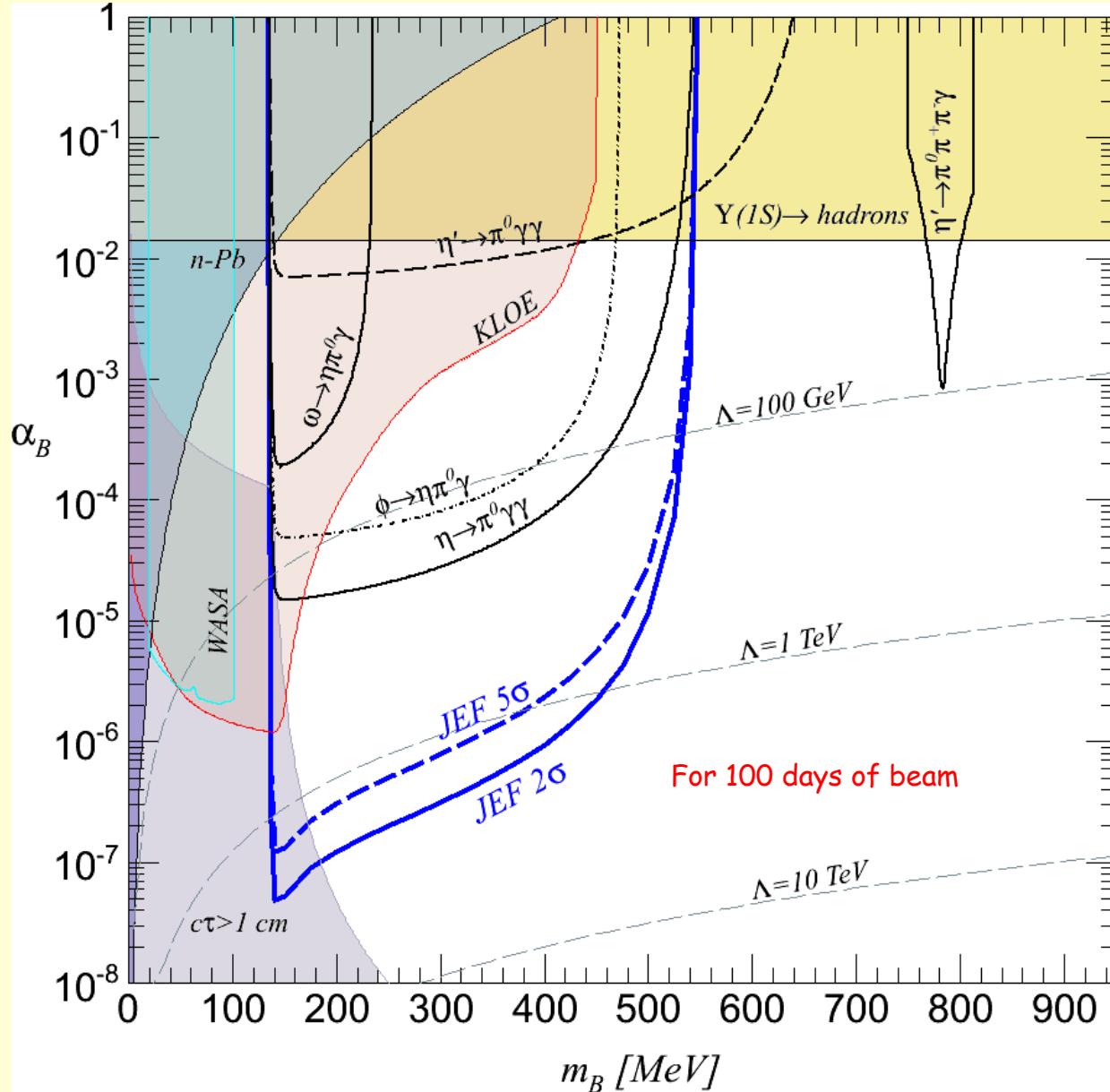
$$\eta \rightarrow \gamma B \rightarrow \gamma + \pi^0 \gamma$$

Search for a resonance peak of  $\pi^0 \gamma$  for  $m_B \sim 140-550$  MeV

S. Tulin, Phys.Rev., D89, 14008 (2014)

- ◆  $\Gamma(\eta \rightarrow \pi^0 \gamma\gamma) \sim 0.3 eV \longrightarrow$  highly suppressed SM background

# JEF Experimental Reach ( $\eta \rightarrow B\gamma \rightarrow \pi^0\gamma\gamma$ )



- ◆ A stringent constraint on the leptophobic B-boson in 140-550 MeV range.
- ◆ A positive signal of B in JEF will **imply a new fermion with a mass up to a few TeV due to electro-weak anomaly cancellation.**
- ◆ Future  $\eta'$  experiment will extend the experimental reach up to 1 GeV

Constraints from  $A'$  search (KLOE and WASA) assumed:  
 $\varepsilon \sim 0.1 \times eg_B / (4\pi)^2$

# The Four Classes of $C$ , $P$ , and $T$ Violations Assuming CPT Invariance

B. Nefkens and J. Price, Phys. Scrip., T99, 114 (2002)

Class	Violated	Valid
1	$C, P, CT, PT$	$T, CP$
2	$C, P, T, CP, CT, PT$	
3	$P, T, CP, CT$	$C, PT$
4	$C, T, CP, PT$	$P, CT$

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EDM,  $\eta \rightarrow$ even  $\pi$ 's

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P-violating exp.,  
 $\beta$ -decays,  
K-, B-, D-meson decays  
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P-violating exp.,  
 $\beta$ -decays,  
 $K$ -,  $B$ -,  $D$ -meson decays

**EDM**,  $\eta \rightarrow$ even  $\pi$ 's

17 C-tests involving  
 $\eta, \eta', \pi, \omega, J/\psi$  decays

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## Experimental tests

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P-violating exp.,  
 $\beta$ -decays,  
K-, B-, D-meson decays  
EDM,  $\eta \rightarrow$ even  $\pi$ 's  
17 C-tests involving  $\eta$ ,  
 $\eta'$ ,  $\pi$ ,  $\omega$ ,  $J/\psi$  decays

### For class 4:

- ❖ a few tests available
- ❖ not well tested experimentally in EM and strong interactions
- ❖ less constrained by nEDM and parity-violating experiments.
- ❖ offer a golden opportunity for new physics search.

# C Invariance

- ◆ Maximally violated in the weak force and is well tested.
- ◆ Assumed in SM for electromagnetic and strong forces, but **it is not experimentally well tested** (The current constraint:  $\Lambda \geq 1 \text{ GeV}$ )
- ◆ EDMs place no constraint on CVPC in the presence of a conspiracy or new symmetry; **only the direct searches are unambiguous.**

(M. Ramsey-Musolf, phys. Rev., D63, 076007 (2001); [talk at the AFCI workshop](#))

## C Violating n neutral decays

Final State	Branching Ratio (upper limit)	Gammas in Final State
$3\gamma$	$< 1.6 \cdot 10^{-5}$	3
$\pi^0\gamma$	$< 9 \cdot 10^{-5}$	
$2\pi^0\gamma$	$< 5 \cdot 10^{-4}$	5
$3\gamma\pi^0$	Nothing published	
$3\pi^0\gamma$	$< 6 \cdot 10^{-5}$	7
$3\gamma 2\pi^0$	Nothing published	

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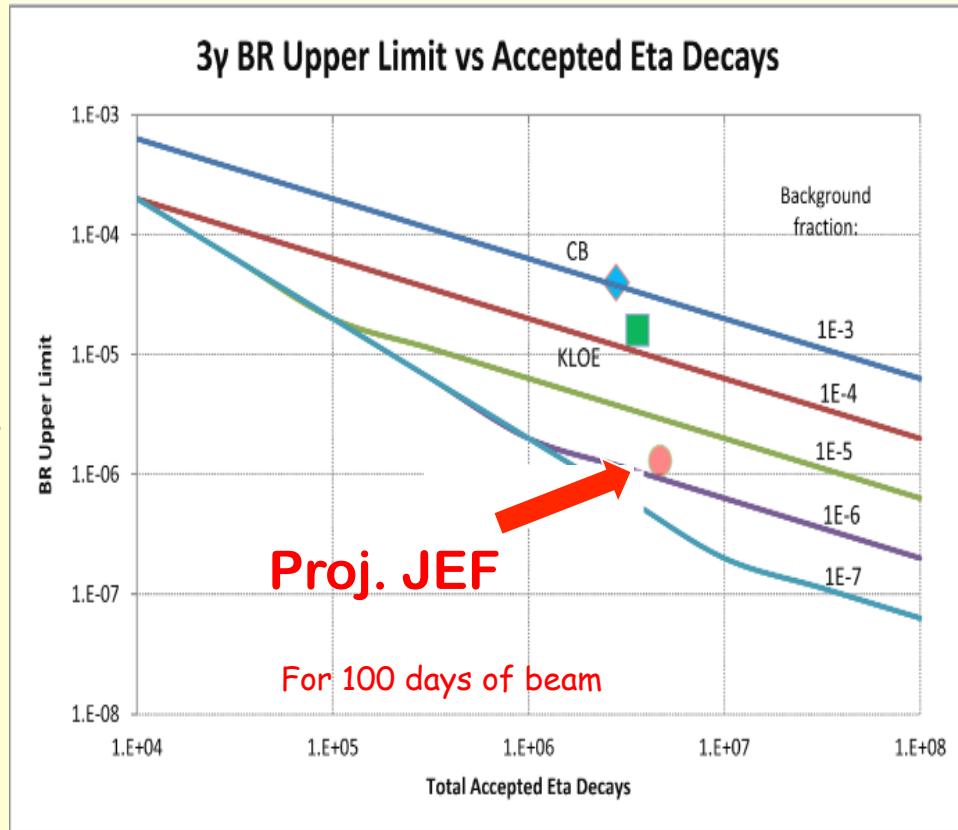
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$3\gamma 2\pi^0$	Nothing published	

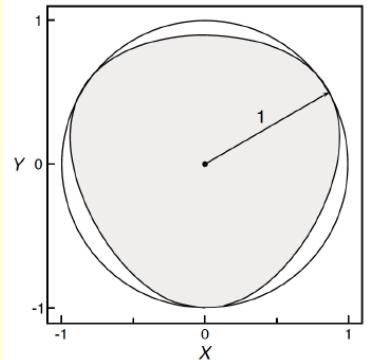
# Experimental Improvement in $\eta \rightarrow 3\gamma$

- ◆ SM contribution:  
 $\text{BR}(\eta \rightarrow 3\gamma) < 10^{-19}$  via P-violating weak interaction.
- ◆ A new C- and T-violating, and P-conserving interaction was proposed by Bernstein, Feinberg and Lee Phys. Rev., 139, B1965 (1965)
- ◆ A calculation due to such new physics by Tarasov suggests:  
 $\text{BR}(\eta \rightarrow 3\gamma) < 10^{-2}$   
Sov. J. Nucl. Phys., 5, 445 (1967)
- ◆ A new investigation by M. Ramsey-Musolf and two Ph.D. students is in progress



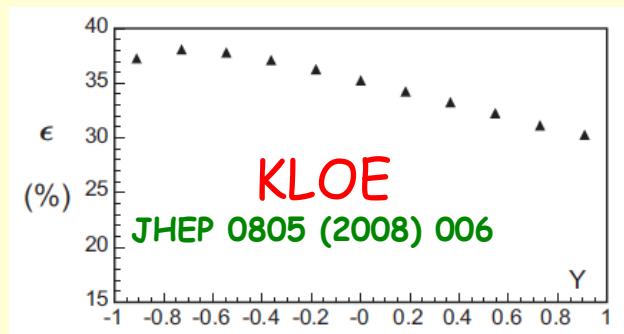
Improve BR upper limit by one order of magnitude to directly tighten the constraint on CVPC new physics

# Experimental Measurements of $\eta \rightarrow 3\pi$



$$X = \frac{\sqrt{3}}{2M_\eta Q_c} (u - t)$$

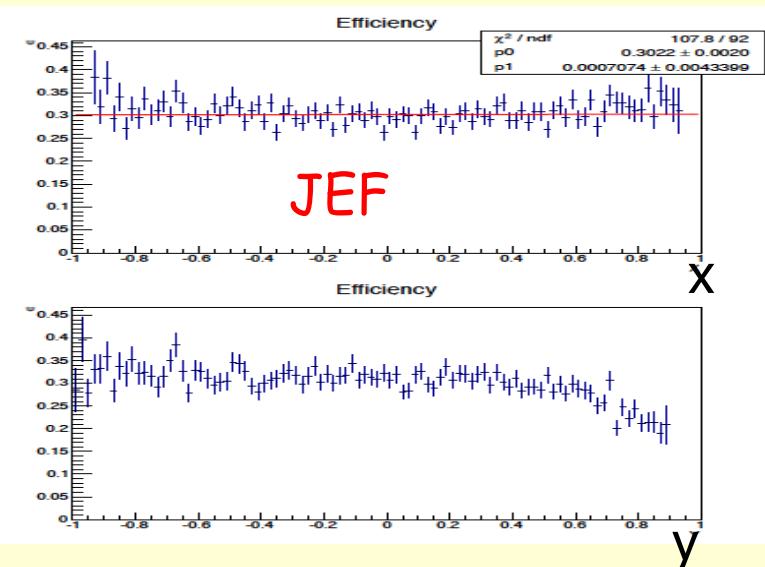
$$Q_c \equiv M_\eta - 2M_{\pi^+} - M_{\pi^0}$$



$$Y = \frac{3}{2M_\eta Q_c} \left( (M_\eta - M_{\pi^0})^2 - s \right) - 1$$

$$Z = X^2 + Y^2$$

Exp.	$3\pi^0$ Events ( $10^6$ )	$\pi^+ \pi^- \pi^0$ Events ( $10^6$ )
Total world data (include prel. WASA and prel. KLOE)	6.5	6.0
GlueX+PrimEx- $\eta$ +JEF	20	19.6



- ◆ Existing data from the **low energy** facilities are sensitive to the detection threshold effects
- ◆ JEF at **high energy** has uniform detection efficiency over Dalitz phase space
- ◆ JEF will offer large statistics and improved systematics

# Determine Light Quark Mass Ratio via $\eta \rightarrow 3\pi$

◆ A clean probe for quark mass ratio:

$$Q^2 = \frac{m_s^2 - \hat{m}^2}{m_d^2 - m_u^2} \quad \hat{m} = \frac{m_u + m_d}{2}$$

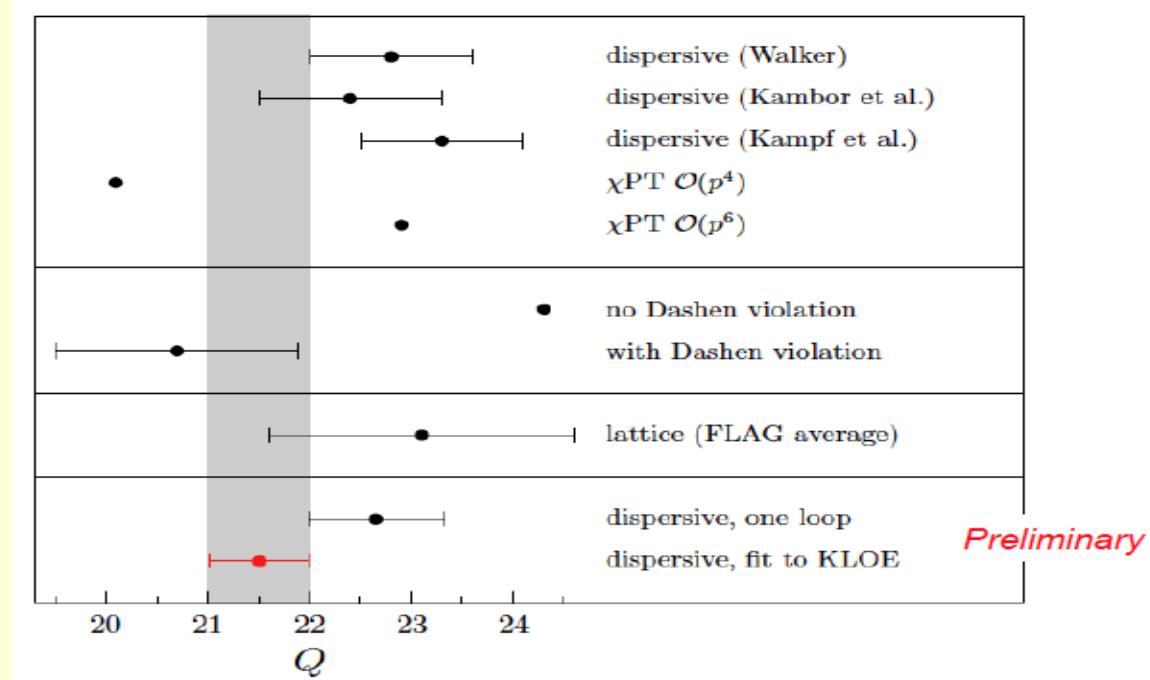
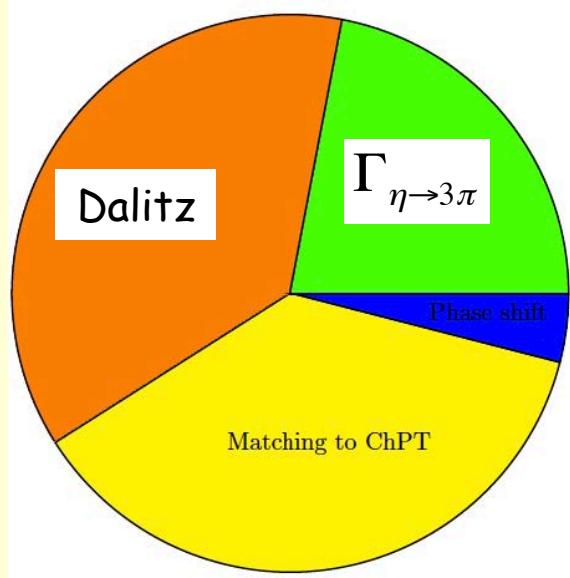
➤ decays through isospin violation:  $A = (m_u - m_d)A_1 + \alpha_{em}A_2$

➤  $\alpha_{em}$  is small

➤ Amplitude:

$$A(s, t, u) = \frac{1}{Q^2} \frac{m_K^2}{m_\pi^2} (m_\pi^2 - m_K^2) \frac{\mathcal{M}(s, t, u)}{3\sqrt{3}F_\pi^2},$$

◆ Uncertainties in quark mass ratio (E. Passemar, [talk at AFCI workshop](#))



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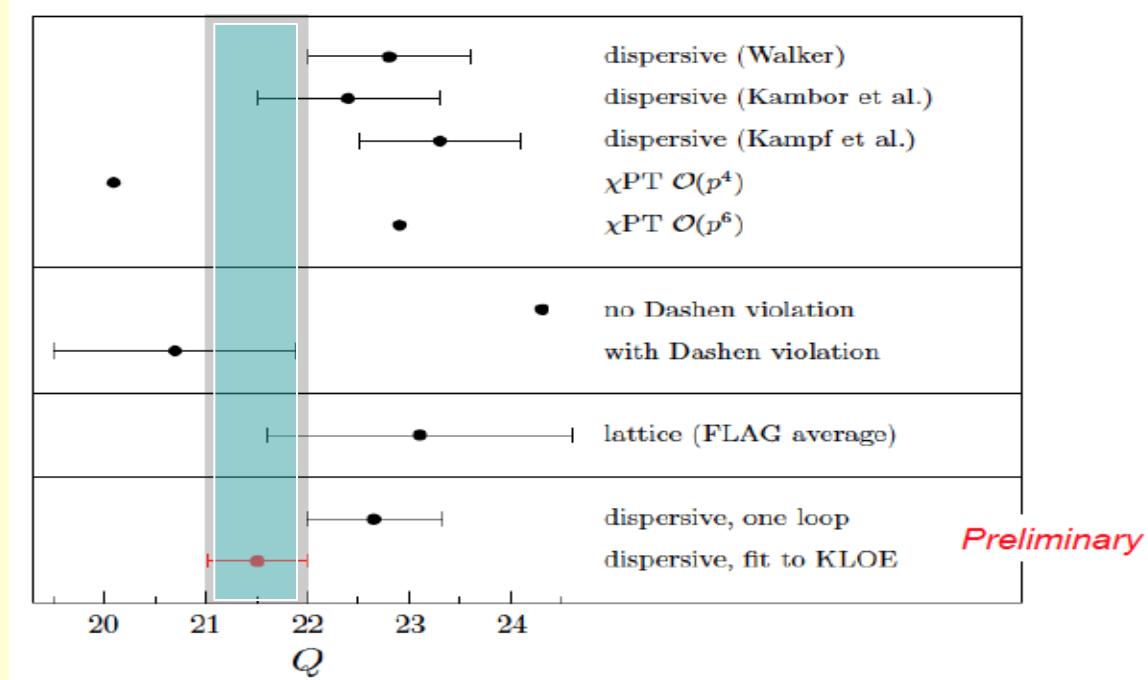
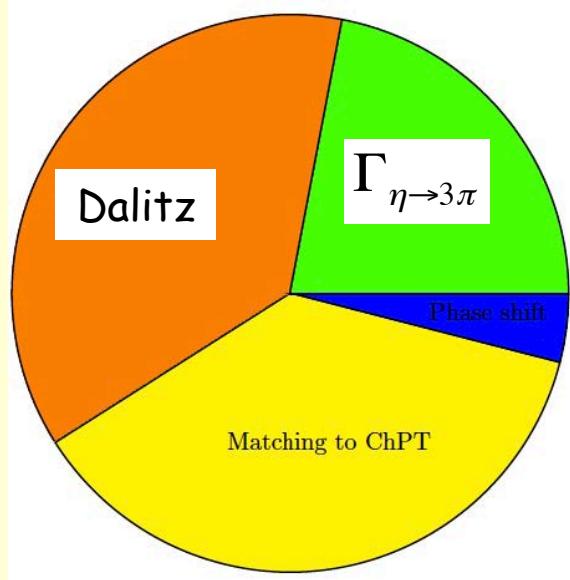
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## Anatomy of CP Violation in $\Gamma(M_{C=+} \rightarrow \pi^+\pi^-\pi^0)$

C-odd, P-even

This can be generated by  $s - p$  interference of  
 $|\pi^+(\mathbf{p})\pi^-(-\mathbf{p})]_I\pi^0(\mathbf{p}')_I\rangle$  final states of  $0^-$  meson decay.

It is linear in a CP-violating parameter.

This contribution **cannot** be generated by  $\bar{\theta}_{\text{QCD}}$ !

“C violation” [Lee and Wolfenstein, 1965; Lee, 1965; Nauenberg, 1965; Bernstein, Feinberg, and Lee, 1965]

C-even, P-odd

This can be generated by the interference of amplitudes which distinguish  $|\pi^-(\mathbf{p})\pi^0(-\mathbf{p})]_I\pi^+(\mathbf{p}')_I\rangle$  from  $|\pi^+(\mathbf{p})\pi^0(-\mathbf{p})]_I\pi^-(\mathbf{p}')_I\rangle$  as in, e.g.,  $B \rightarrow \rho^+\pi^-$  vs.  $B \rightarrow \rho^-\pi^+$ . “CP-enantiomers” [SG, 2003]

This possibility is not accessible in  $\eta \rightarrow \pi^+\pi^-\pi^0$  decay (but in  $\eta'$  decay, yes). Thus a “left-right” asymmetry in  $\eta \rightarrow \pi^+\pi^-\pi^0$  decay tests C-invariance, too.

## SM Allowed $\eta \rightarrow \pi^0 \gamma\gamma$

→ A rare window to probe interplay of VMD & scalar resonances in ChPT to calculate  $O(p^6)$  LEC's in the chiral Lagrangian  
 (J. Bijnens, [talk at AFCI workshop](#))

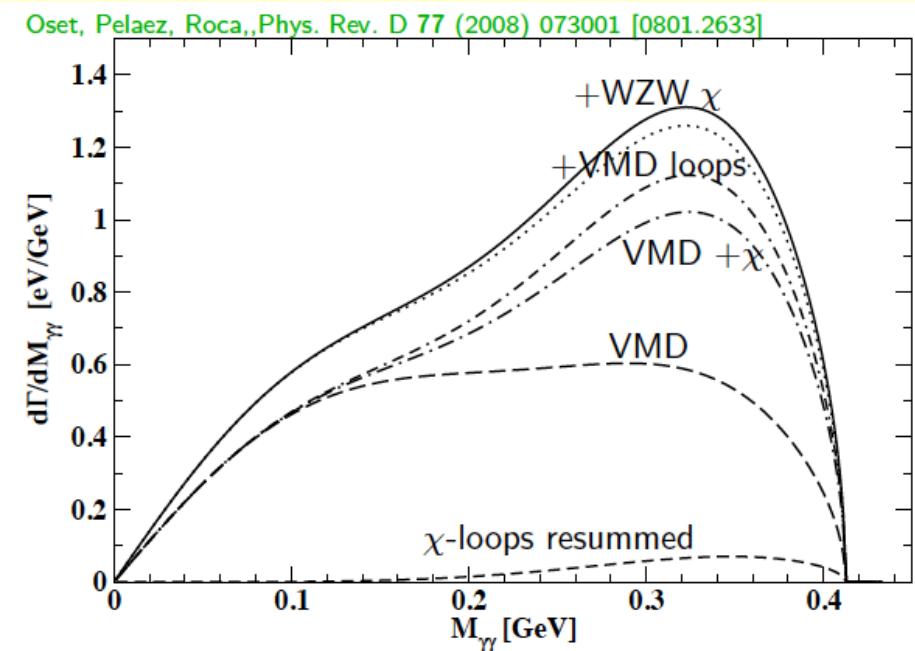
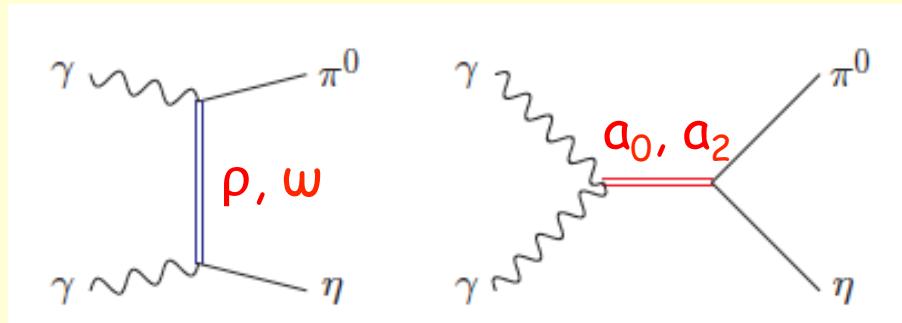
- ◆ The major contributions to  $\eta \rightarrow \pi^0 \gamma\gamma$  are two  $O(p^6)$  counter-terms in the chiral Lagrangian → an unique probe for the high order ChPT.

L. Ametller, J. Bijnens, and F. Cornet, Phys. Lett., B276, 185 (1992)

- ◆ Shape of Dalitz distribution is sensitive to the role of scalar resonances.

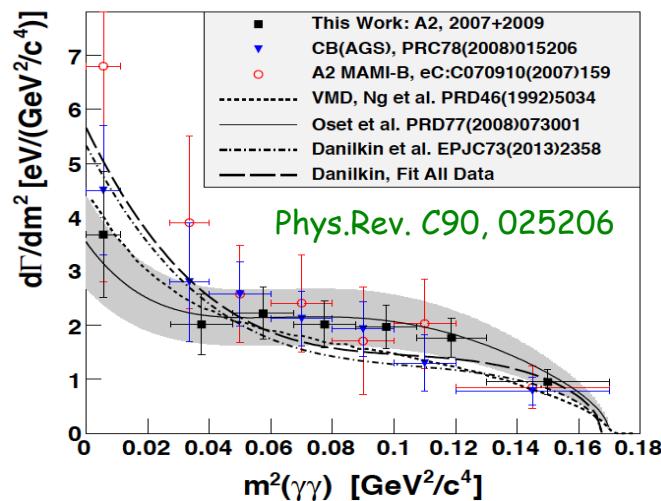
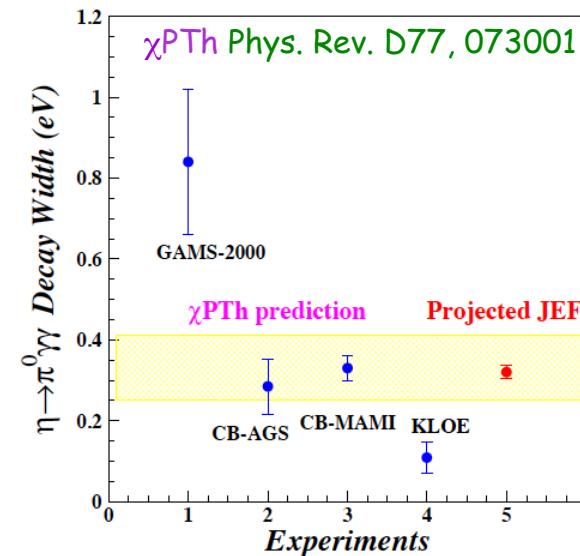
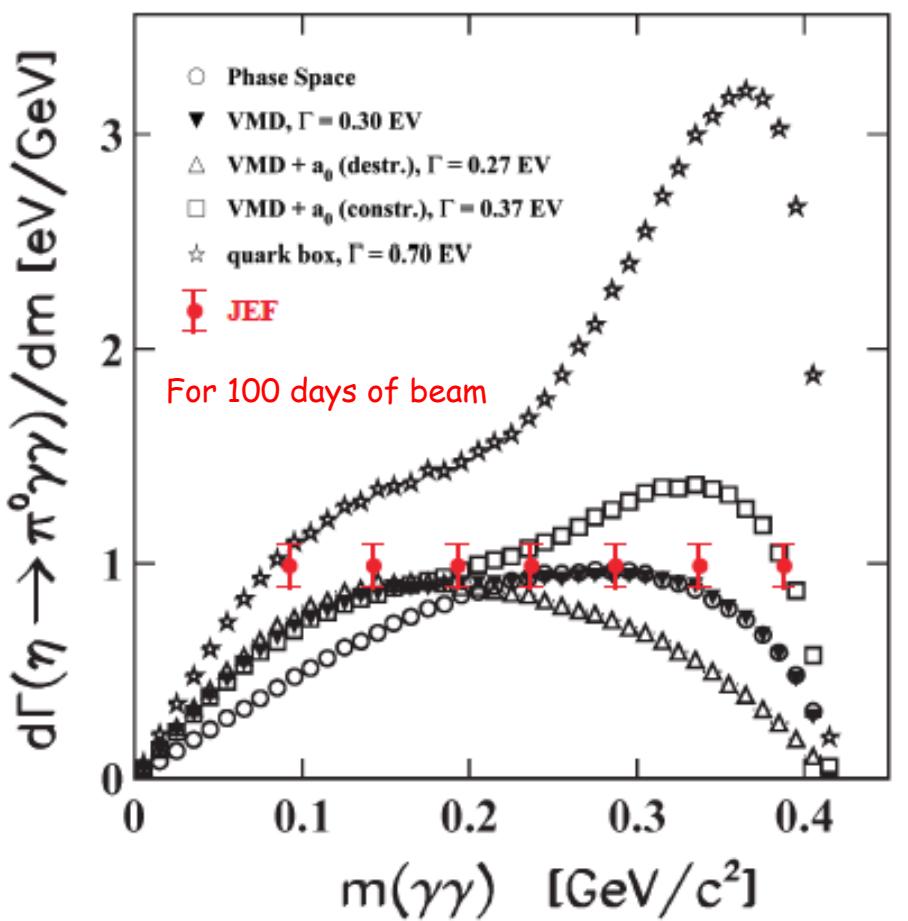
LEC's are dominated by meson resonances

Gasser, Leutwyler 84; Ecker, Gasser, Pich, de Rafael 1989; Donoghue, Ramirez, Valencia 1989



# Projected JEF Results on $\eta \rightarrow \pi^0 \gamma\gamma$

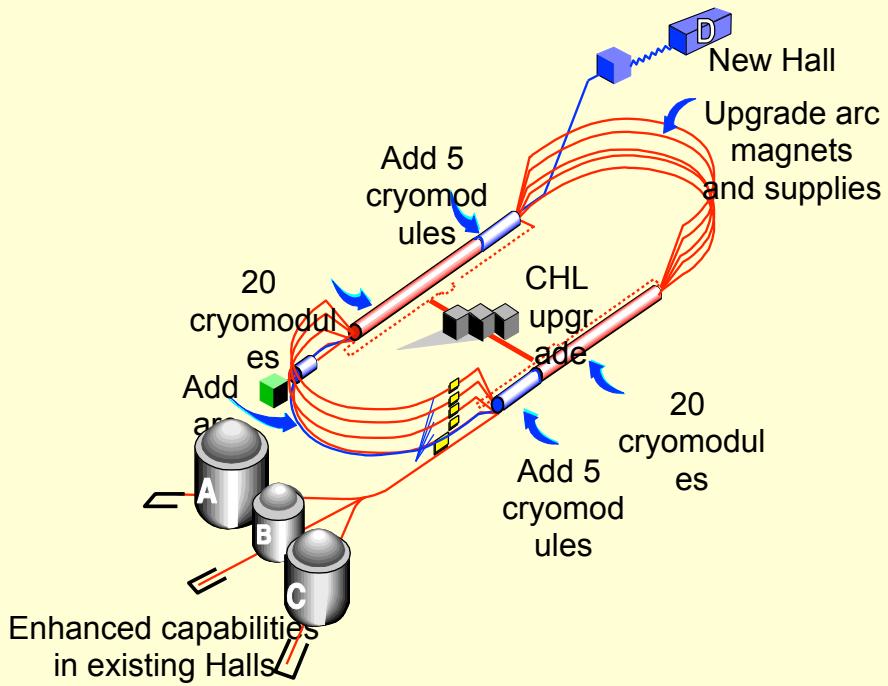
J.N. Ng and D.J. Peters, Phys. Rev. D47, 4939



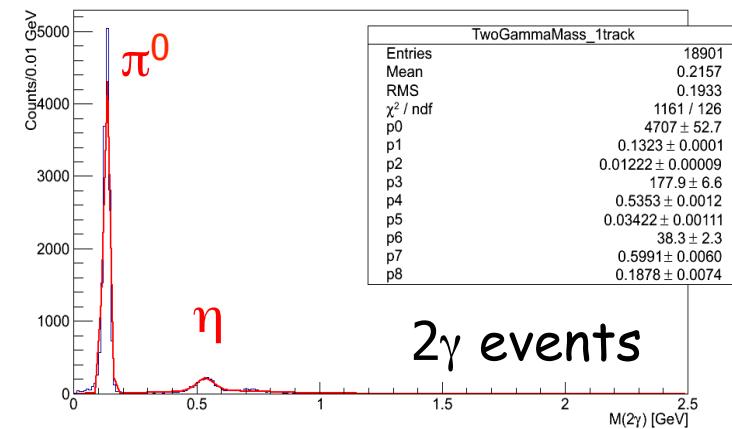
We measure both BR and Dalitz distribution

- ◆ model-independent determination of two LEC's of the  $O(p^6)$  counter- terms
- ◆ probe the role of scalar resonances to calculate other unknown  $O(p^6)$  LEC's

# 12 GeV Jlab and GlueX



Preliminary result from commissioning runs  
 $M(2\gamma)$



## Summary

- A comprehensive Primakoff program has been developed at Jlab to measure  $\Gamma(p \rightarrow \gamma\gamma)$  and  $F(\gamma\gamma^* \rightarrow p)$  of  $\pi^0$ ,  $\eta$  and  $\eta'$ . These results will provide rich data sets to test the fundamental symmetries of QCD at low energy.
  - tests of chiral symmetry and anomalies
  - light quark mass ratio
  - $\eta$ - $\eta'$  mixing angle
  - $\pi^0, \eta$  and  $\eta'$  electromagnetic interaction radii
  - inputs for  $a_\mu$ (HLbL) calculations
- 12 GeV tagged photon beam with GlueX setup offers a unique  $\eta$  facility with two orders of magnitude in background reduction in the neutral rare  $\eta$  decays compared to other facilities in the world.
  - Probe a leptophobic dark B-boson in 140-550 MeV range via  $\eta \rightarrow B\gamma \rightarrow \pi^0\gamma\gamma$
  - Directly constrain CVPC new physics via  $\eta \rightarrow 3\gamma$  and other C-violating channels
  - A clean determination of the light quark mass ratio via  $\eta \rightarrow 3\pi$
  - Test the role of scalar dynamics in ChPT through  $\eta \rightarrow \pi^0\gamma\gamma$

# $\eta$ Production Rate Estimation

LH2 target length L=30cm,  $\rho=0.0708 \text{ g/cm}^3$

$$N_p = \frac{\rho L}{A} N_A = \frac{0.0708 \times 30}{1} \times 6.022 \times 10^{23} = 1.28 \times 10^{24} \text{ p/cm}^2$$

The  $\gamma + p \rightarrow \eta/\eta' + p$  cross section: ~70 nb for  $\eta$ ; ~57 nb for  $\eta'$

J.M. Laget, Phys.Rev., C72, 022202 (2005) and A. Sibirtsev et al. Eur.Phys.J., A44, 169 (2010)

Photon beam intensity  $N_\gamma \sim 5 \times 10^7 \text{ Hz}$  (for  $E_\gamma \sim 9\text{-}11.7 \text{ GeV}$ )

$$N_\eta = N_\gamma N_p \sigma = 5 \times 10^7 \times 1.28 \times 10^{24} \times 70 \times 10^{-33}$$

$$= 4.5 \text{ Hz}$$

$$\approx 3.9 \times 10^5 \text{ } (\eta \text{'s/day})$$

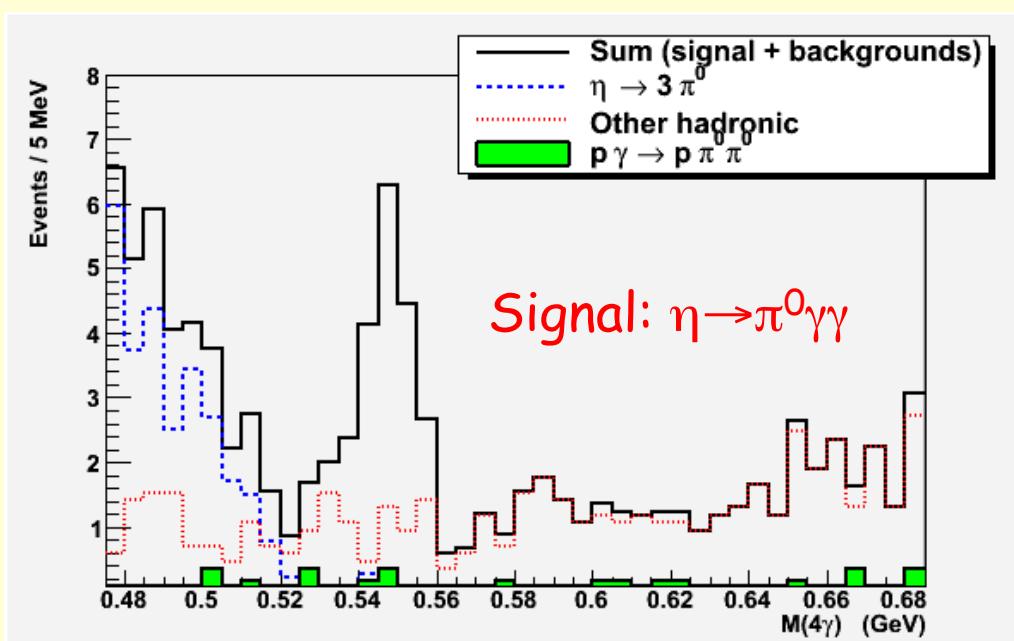
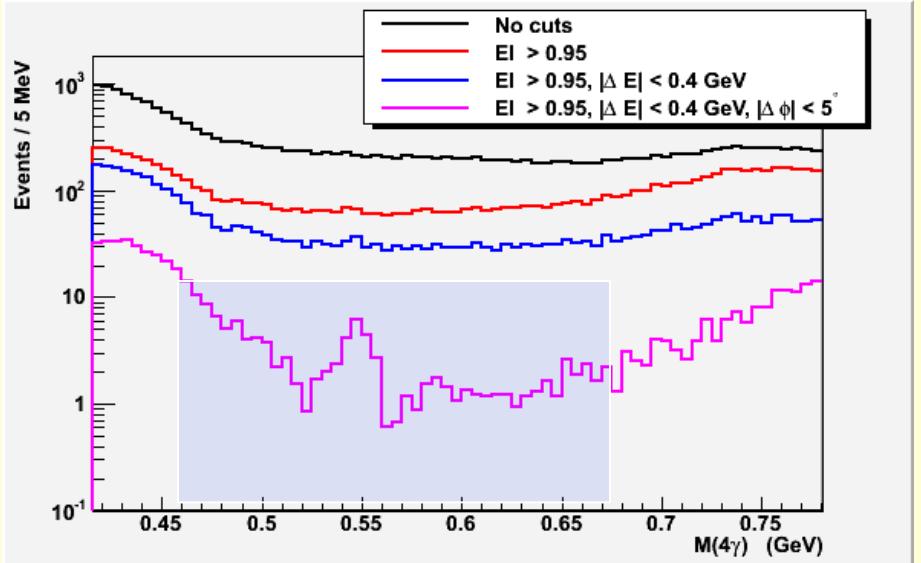
Jlab Eta Factory (JEF)

$$N_{\eta'} \approx 3.2 \times 10^5 \text{ } (\eta' \text{/day})$$

# Estimated Systematic Uncertainties PrimEx-II (Preliminary)

Contributions	Uncertainty (%)
Photon flux	0.7
Beam parameters	0.4
Accidentals	0.1
Target parameters	0.2 $^{12}\text{C}$ ; 0.4 $^{28}\text{Si}$
Yield extraction	1.0
Acceptance	0.3
Trigger efficiency	0.3
Detector resolution	0.28
Model errors (theory)	0.5
Physics background	0.3
Branching ratio (PDG)	0.03
<b>Total</b>	<b>1.6</b>

# Hadronic Backgrounds Reduction in $4\gamma$ States



## Event Selection

- Elasticity is  $EL = \sum E_\gamma / E_{\text{tagged-}\gamma}$
- Energy conservation for  $\gamma + p \rightarrow \eta + p$  reaction:  $\Delta E = E(\eta) + E(p) - E(\text{beam}) - M(p)$
- Co-planarity  $\Delta\phi = \phi(\eta) - \phi(p)$

### Note:

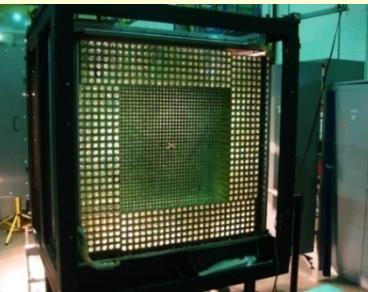
- Statistics is normalized to 1 beam day.
- BG will be further reduced by requiring that only one pair of  $\gamma$ 's have the  $\pi^0$  invariant mass.

# New Equipment: FCAL-II

FCAL



HyCal

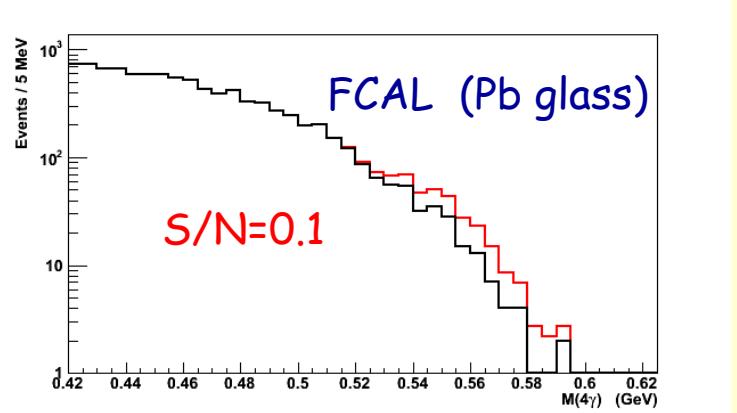


FCAL with PWO insertion:

- $118 \times 118 \text{ cm}^2$  in Size ( $3445 \text{ PbWO}_4$ )
- $2\text{cm} \times 2\text{cm} \times 18\text{cm}$  per module

**S/N Ratio vs. Calorimeter Types**

**signal:**  $\eta \rightarrow \pi^0 \gamma\gamma$ , **background:**  $\eta \rightarrow 3\pi^0$



**FCAL-II ( $\text{PbWO}_4$ ) vs. FCAL ( $\text{Pb glass}$ )**

Property	Improvement factor
Energy $\sigma$	2
Position $\sigma$	2
Granularity	4
Radiation-resistance	10

