

Flow analysis methods in small multiplicity events

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INT Program INT-15-2b: Correlations and Fluctuations in p+A and A+A Collisions

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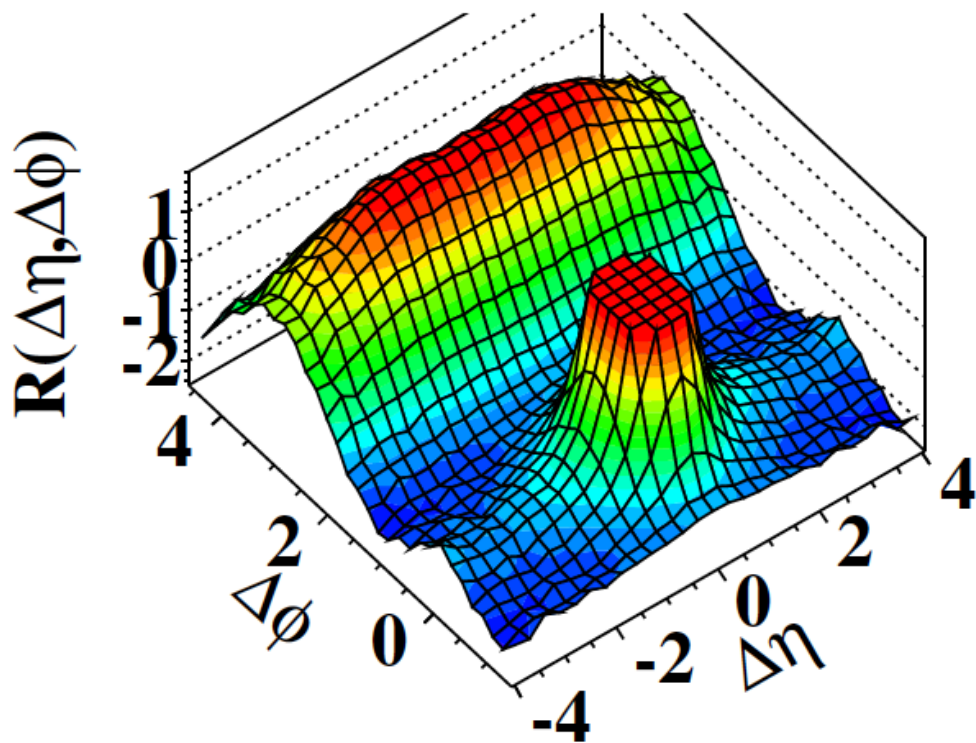
Outline

- Motivations
- Toy model and Analysis methods
- Similar studies using AMPT
- Summary

Ridge in high multiplicity pp and pPb

pp 7 TeV in 2010

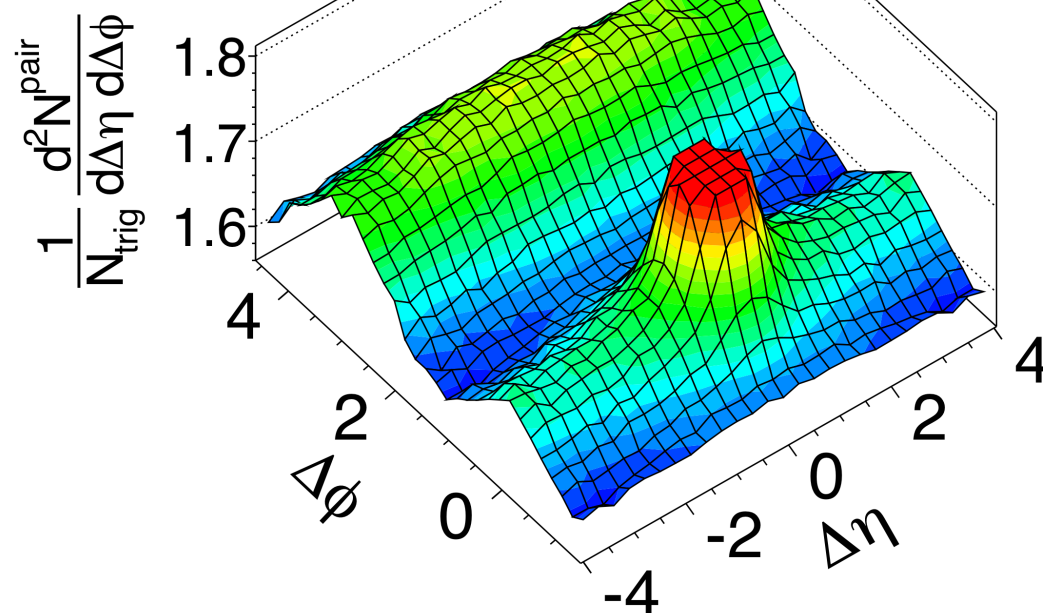
(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



$N \geq 110$

CMS pPb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$, $N_{\text{trk}}^{\text{offline}} \geq 110$ pPb in 2012 (b)

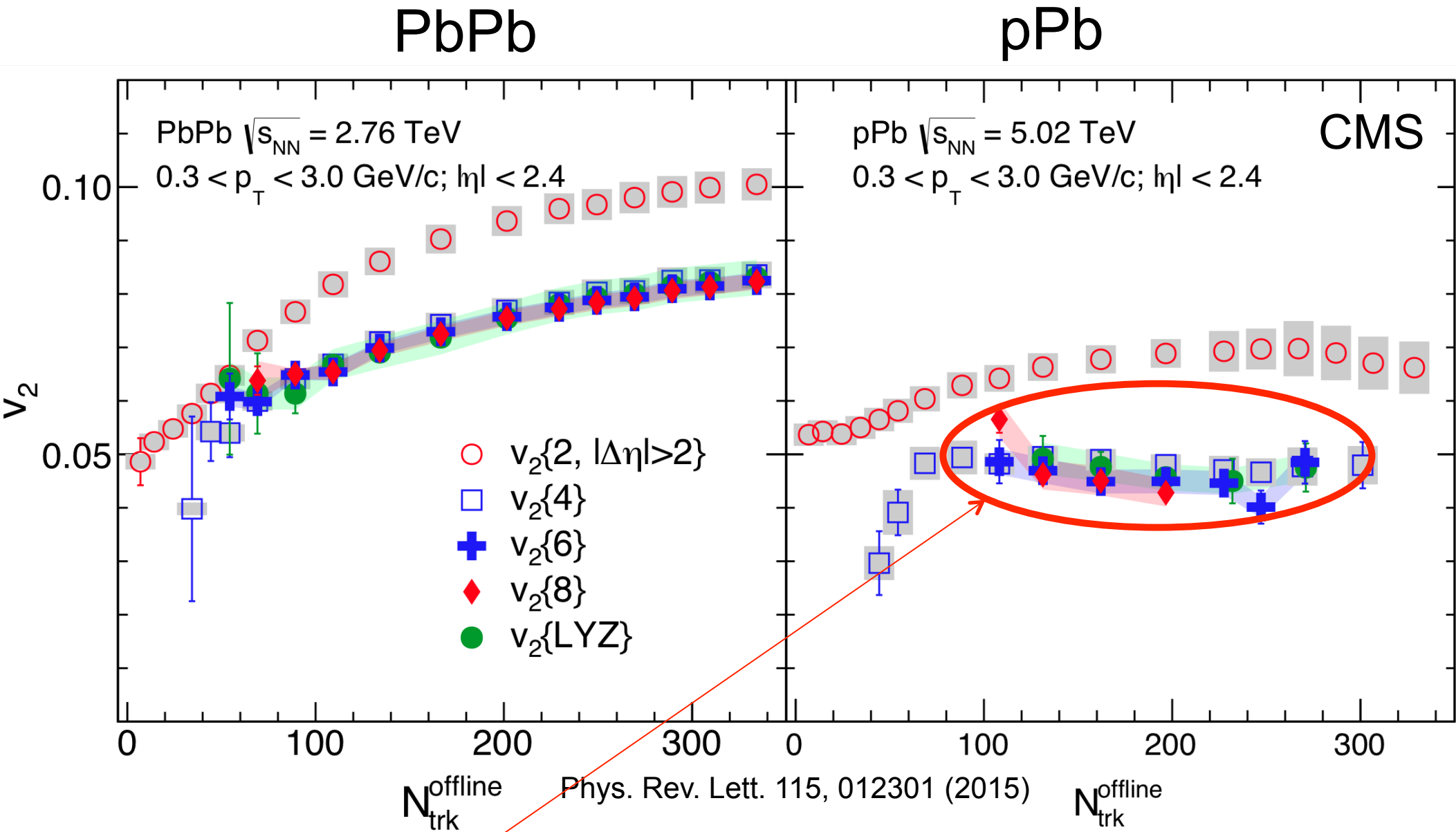
$1 < p_T < 3 \text{ GeV}/c$



$N \geq 110$

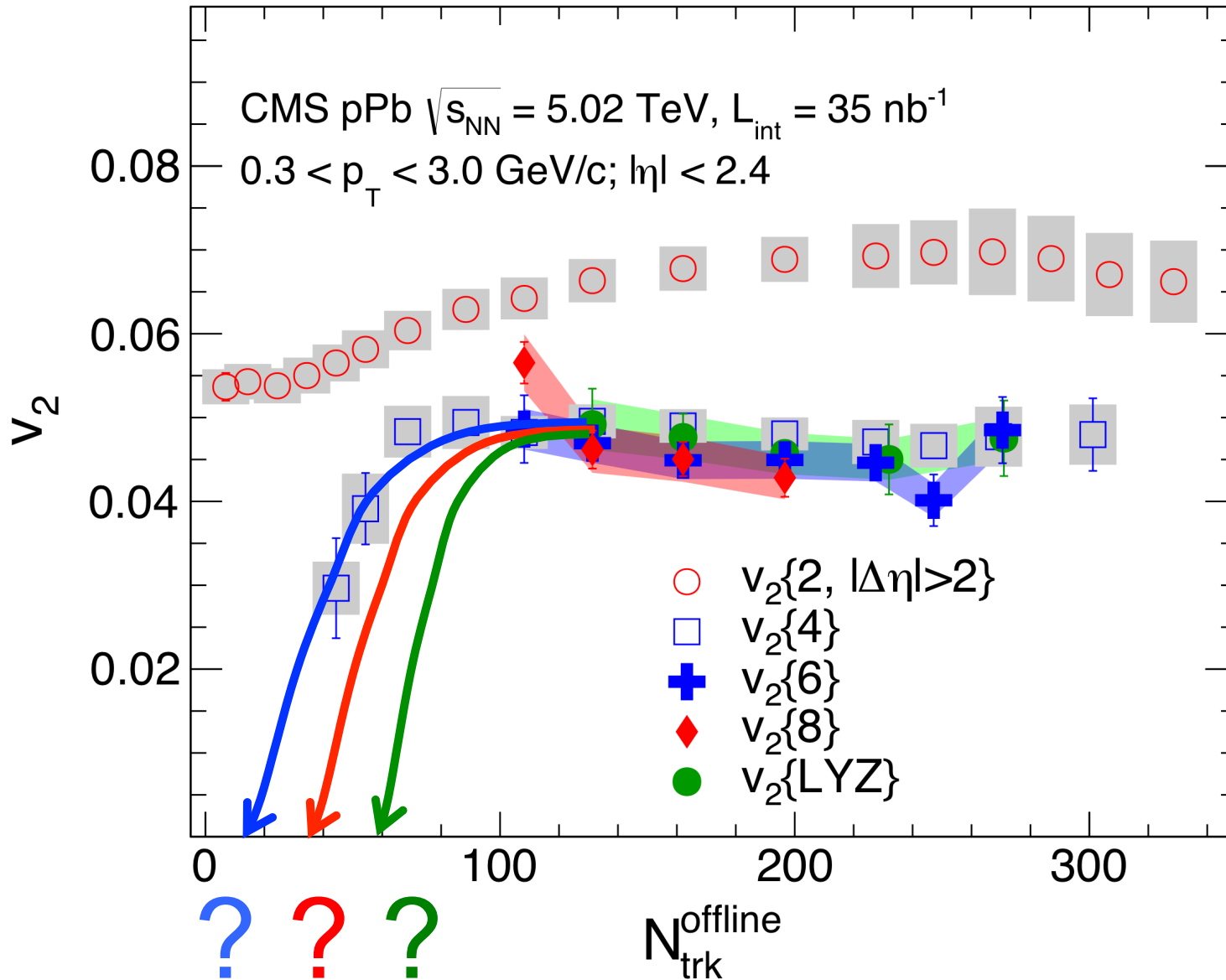
Require high multiplicity

Multiparticle correlation analysis



$N \geq 100$ for $v_2\{6\}$, $v_2\{8\}$ and $v_2\{\text{LYZ}\}$ in pPb₄

Low multiplicity ?



How low can we go ?

Flow Turn-On ?

Smallest droplet?

The Hot QCD White Paper:

arXiv:1502.02730

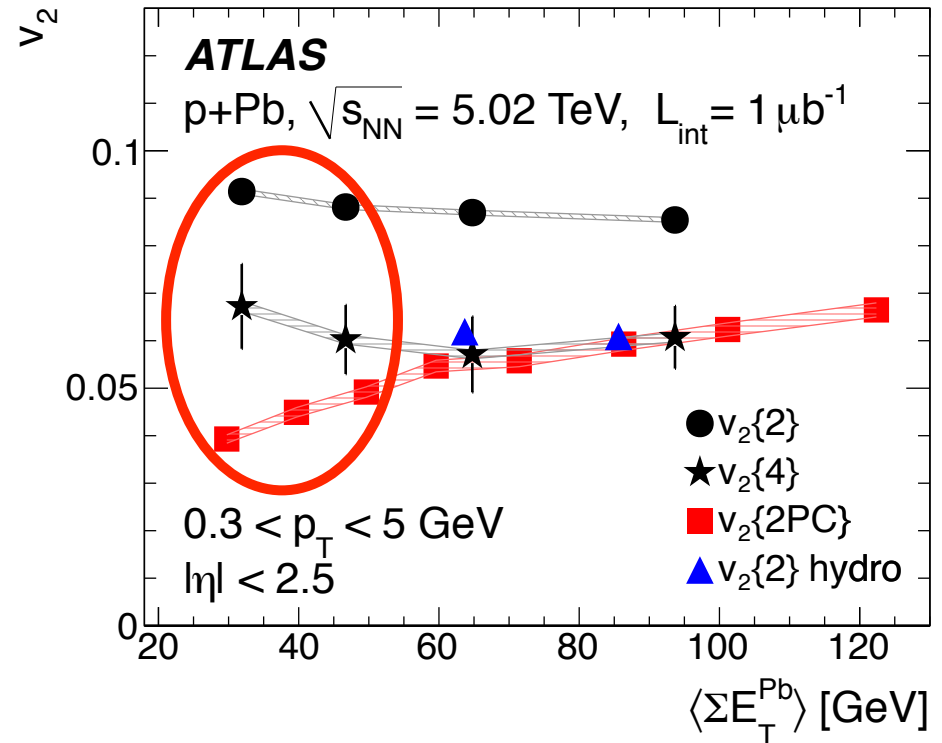
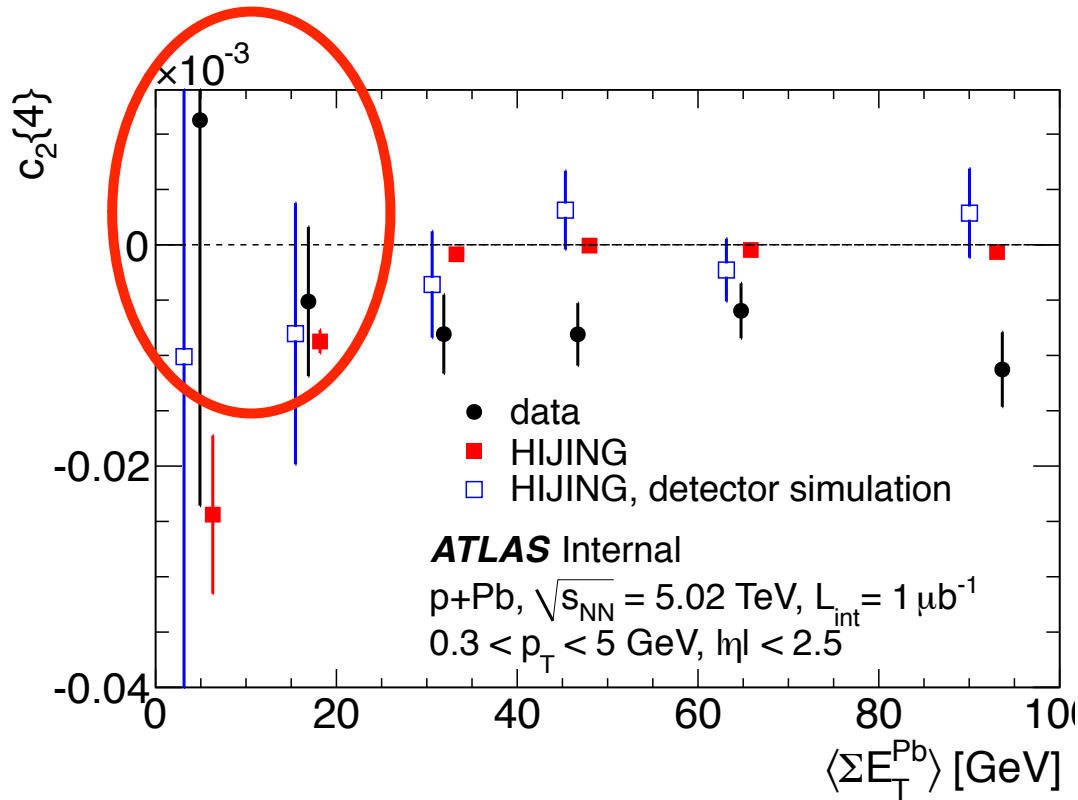
At the same time, the discovery of strongly coupled QGP poses many questions. How do its properties vary over a broad range of temperature and chemical potential? Is there a critical point in the QCD phase diagram where the hadron gas to QGP phase transition becomes first-order? What is the smallest droplet of hot QCD matter whose behavior is liquid-like? What are the initial

What is the smallest droplet of hot QCD matter whose behavior is liquid-like ?

Status from ATLAS

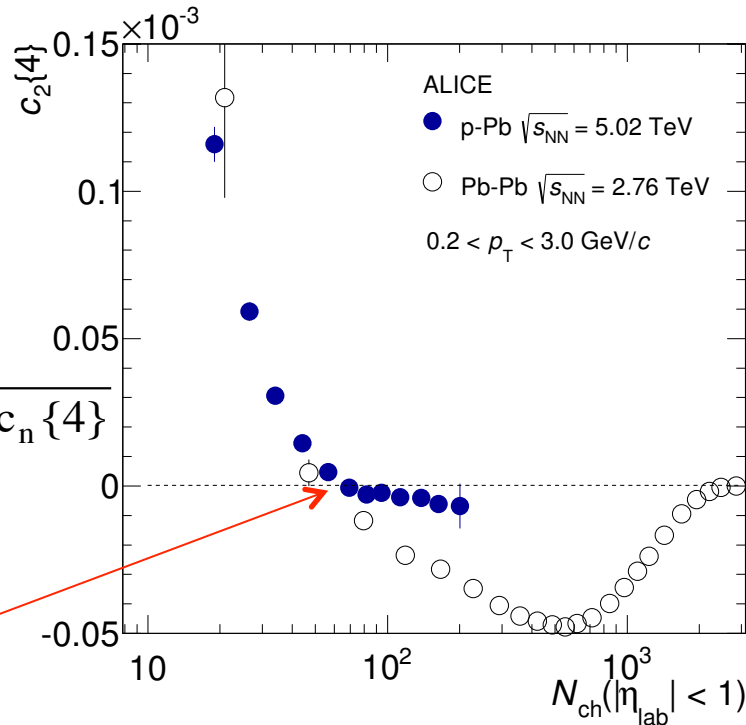
Phys. Lett. B 725 (2013) 60-78

$$v_n \{4\} = \sqrt[4]{-c_n \{4\}}$$



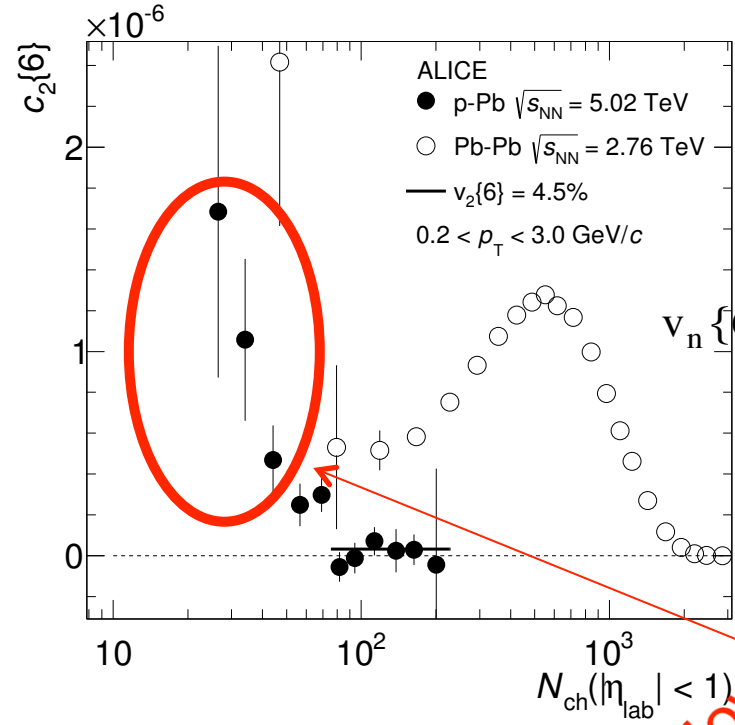
- Studied vs. forward calorimeter energy
- Signal exists at low E_T (~ 30 GeV)

Status from ALICE



$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}$$

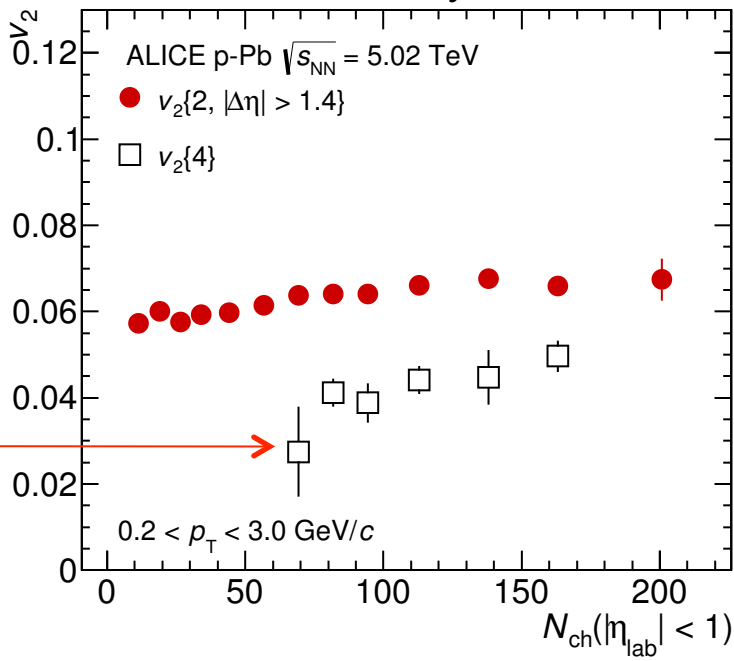
Turn-on ?



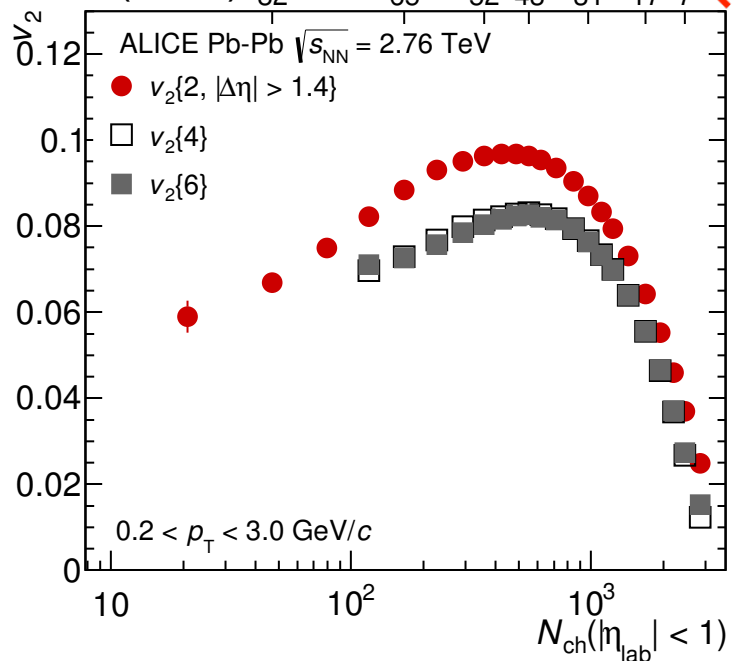
$$v_n\{6\} = \sqrt[6]{\frac{1}{4} c_n\{6\}}$$

How to understand ?

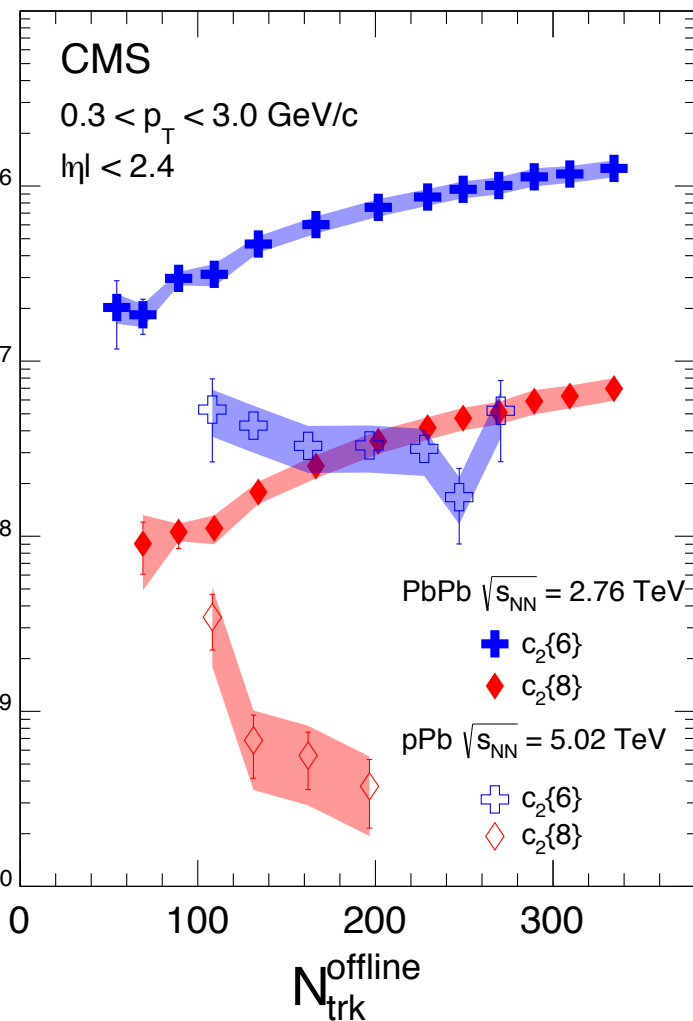
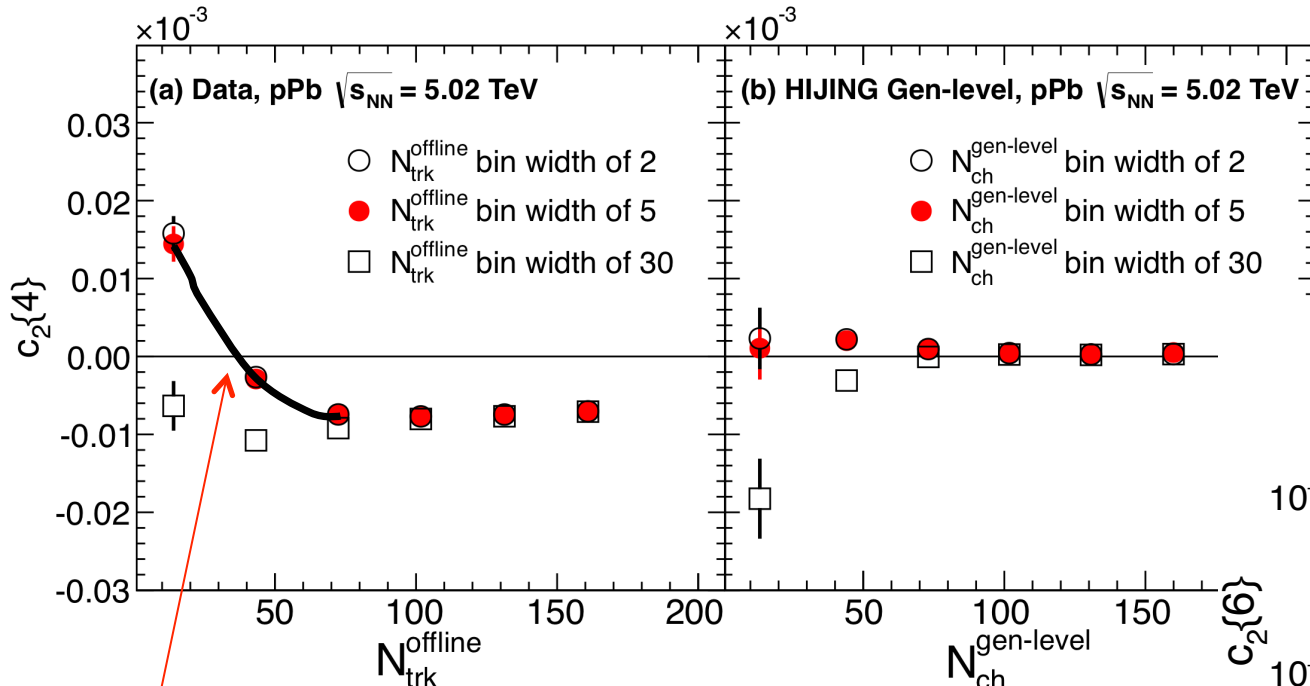
Phys. Rev. C 90, 054901 (2014)



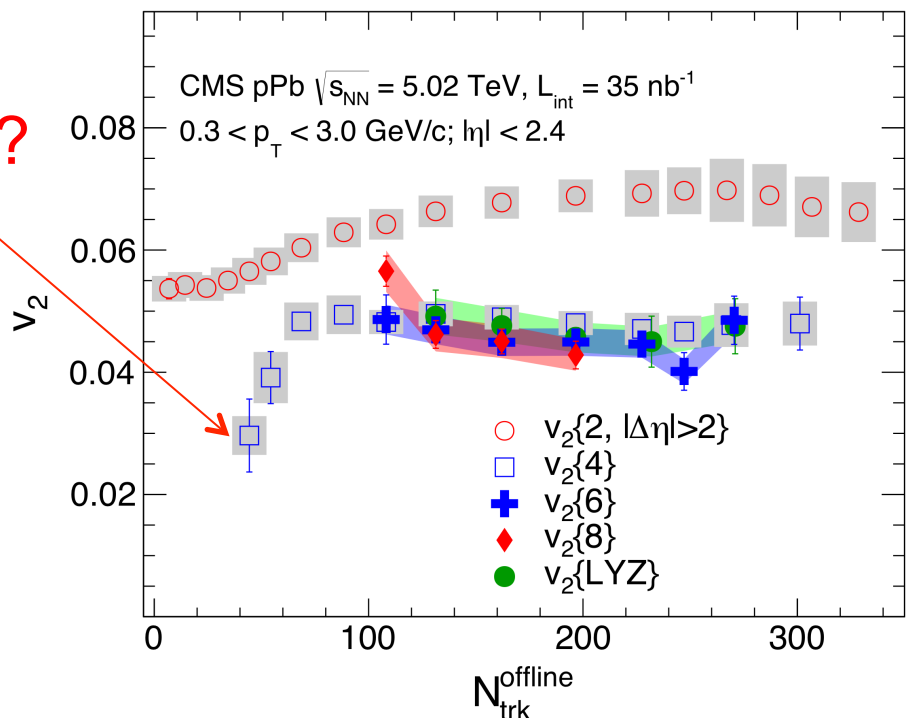
Similar to CMS $v_2\{4\}$



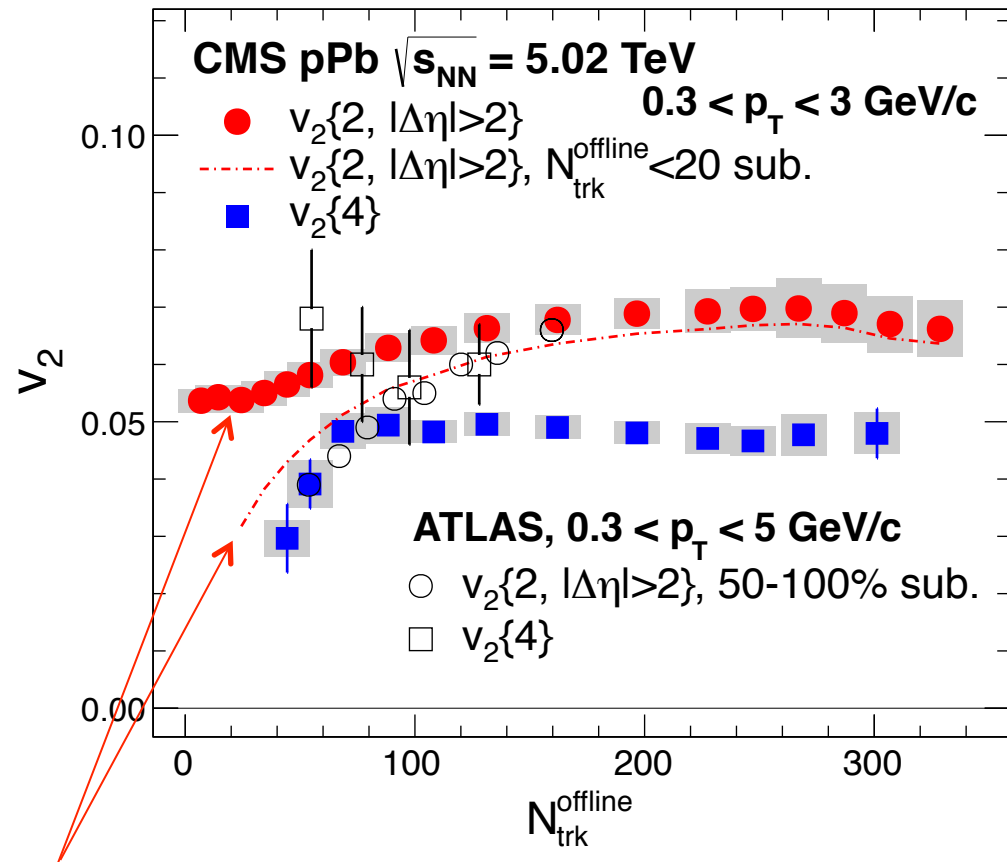
Status from CMS



Turn-on ?

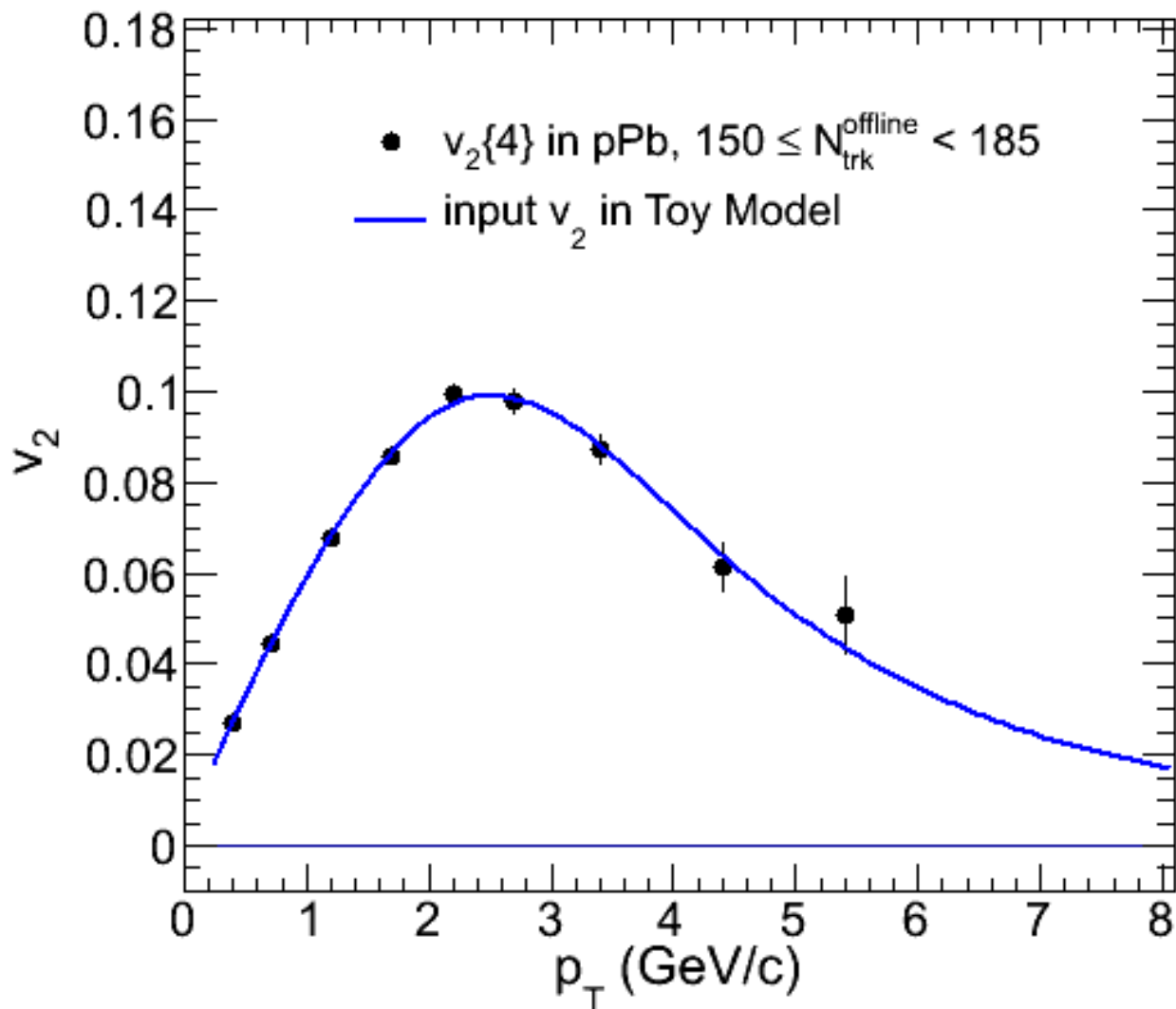


Analysis methods in small multiplicity



- Large difference between with and without peripheral subtraction in long-range two-particle correlation method
- Non-flow is important in this range
- Need multi-particle correlation methods

Toy model with input flow



- Change event multiplicity in Toy model
- Study the behavior of different methods in low multiplicity range
- The Toy model does not include flow fluctuation and non-flow

Q-cumulant method

Six- and eight-particle correlations, averaged over all events:

$$\langle\langle 6 \rangle\rangle \equiv \langle\langle e^{in(\phi_1+\phi_2+\phi_3-\phi_4-\phi_5-\phi_6)} \rangle\rangle,$$

$$\langle\langle 8 \rangle\rangle \equiv \langle\langle e^{in(\phi_1+\phi_2+\phi_3+\phi_4-\phi_5-\phi_6-\phi_7-\phi_8)} \rangle\rangle.$$

Six- and eight-particle cumulants:

$$c_n\{6\} = \langle\langle 6 \rangle\rangle - 9 \cdot \langle\langle 4 \rangle\rangle \langle\langle 2 \rangle\rangle + 12 \cdot \langle\langle 2 \rangle\rangle^3,$$

$$c_n\{8\} = \langle\langle 8 \rangle\rangle - 16 \cdot \langle\langle 6 \rangle\rangle \langle\langle 2 \rangle\rangle - 18 \cdot \langle\langle 4 \rangle\rangle^2 + 144 \cdot \langle\langle 4 \rangle\rangle \langle\langle 2 \rangle\rangle^2 - 144 \langle\langle 2 \rangle\rangle^4,$$

Six- and eight-particle v_2 :

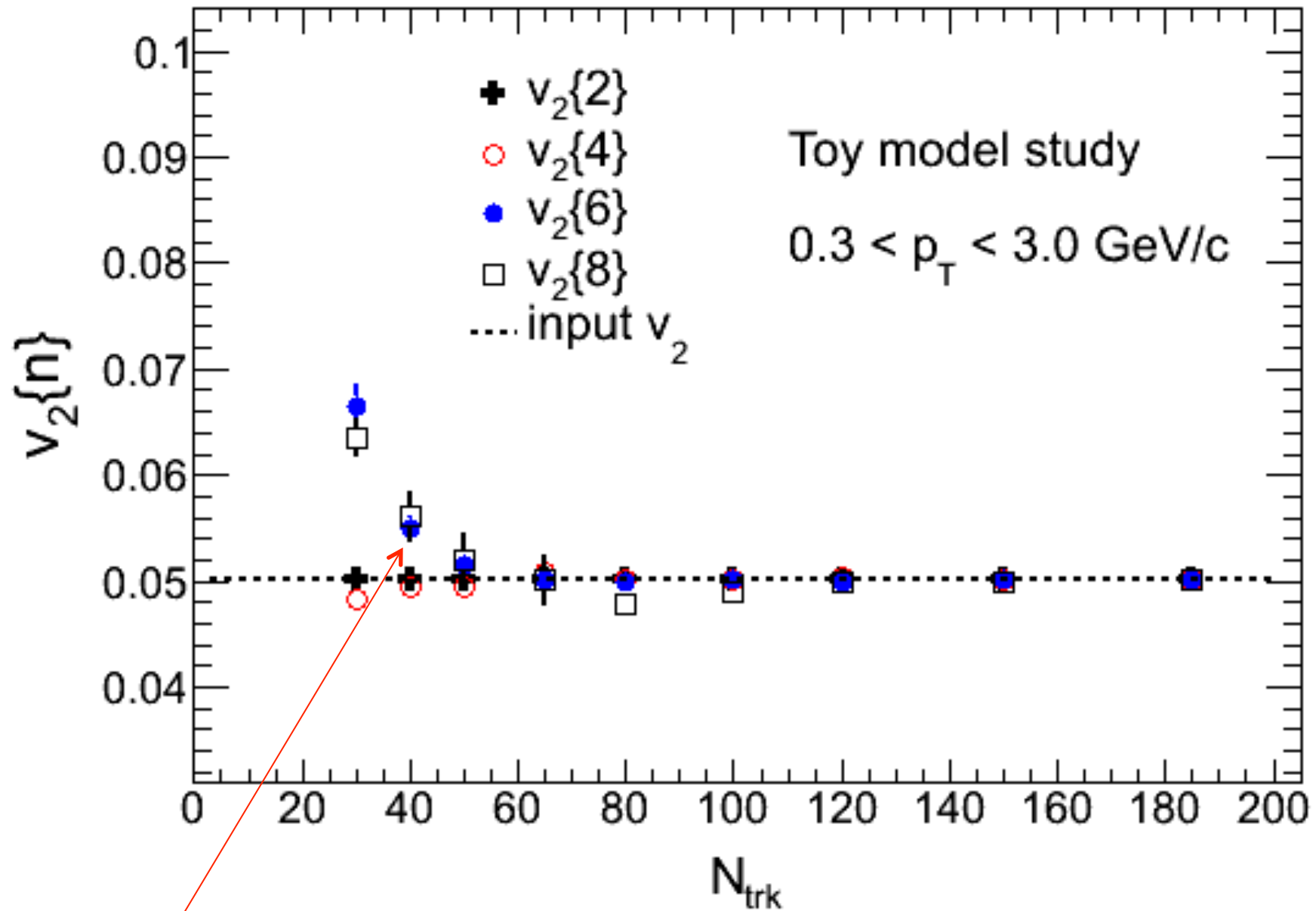
$$v_n\{6\} = \sqrt[6]{\frac{1}{4} c_n\{6\}},$$

$$v_n\{8\} = \sqrt[8]{-\frac{1}{33} c_n\{8\}}.$$

Correlations and cumulants are expressed in terms of moments of Q-vector

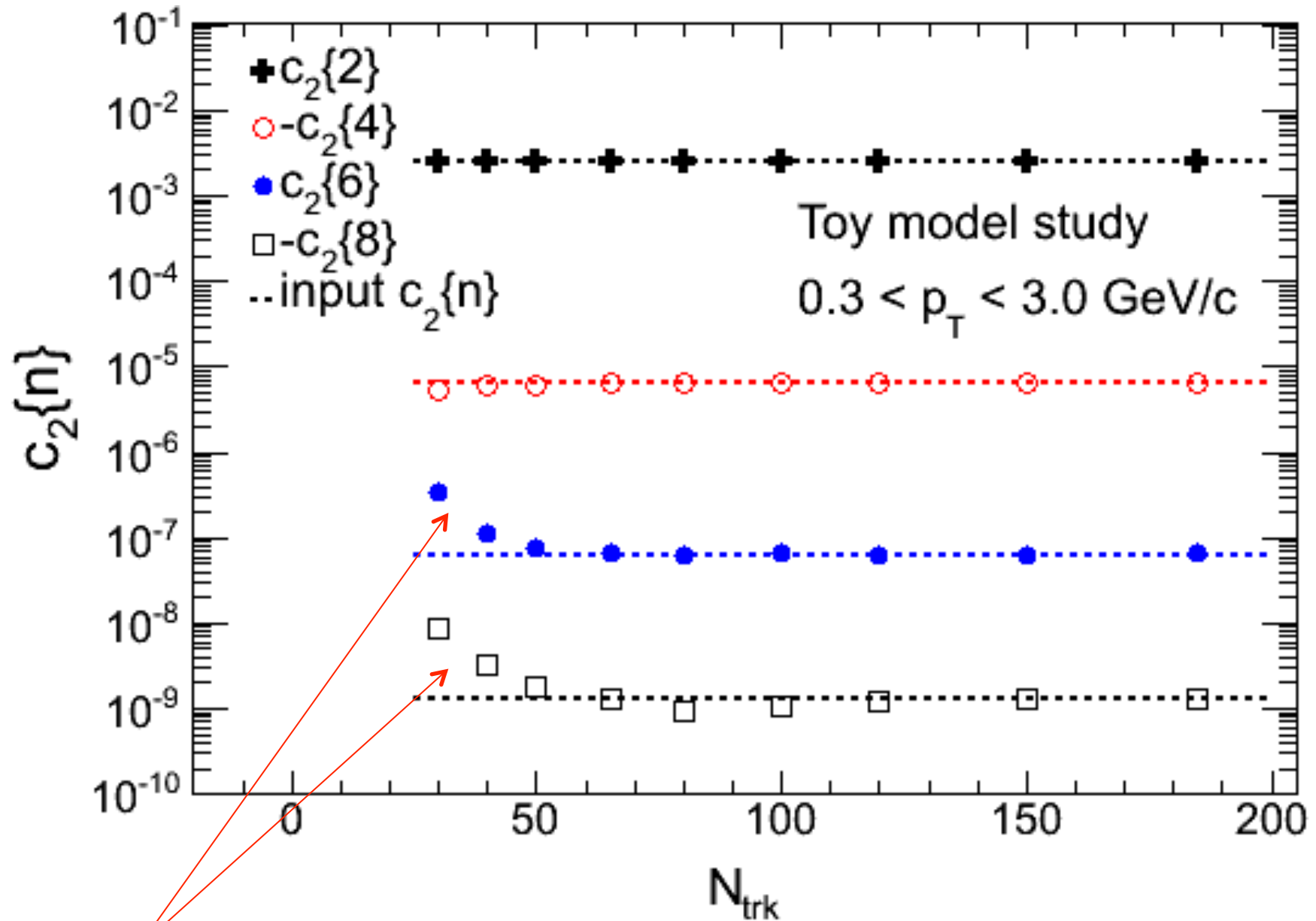
$$Q_n \equiv \sum_{i=1}^M e^{in\phi_i}$$

$v_2\{n\}$ in Toy model



- $v_2\{6\}$ and $v_2\{8\}$ over estimate the signal in low multiplicity events

Cumulants in Toy model



- $c_2\{6\}$ and $-c_2\{8\}$ over estimate the signal in low multiplicity events

Lee-Yang Zeros method

All-particle correlations, per event:

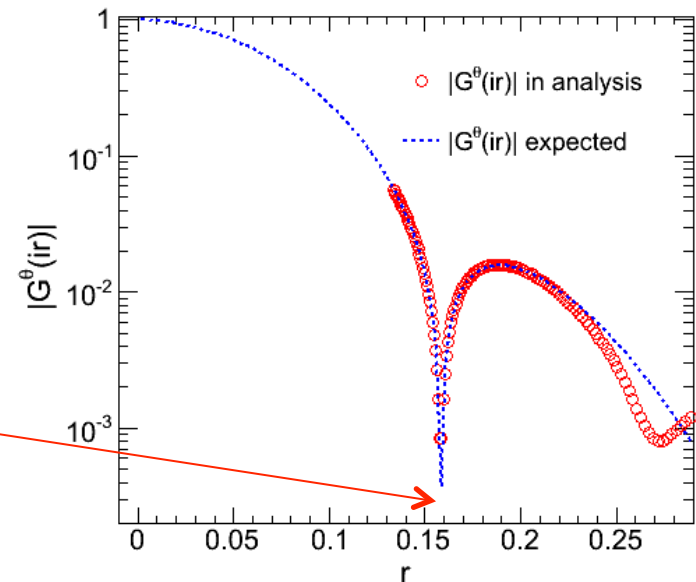
$$g^\theta(ir) \equiv \prod_{j=1}^M [1 + ir w_j \cos(n(\phi_j - \theta))]$$

Generating function, all events:

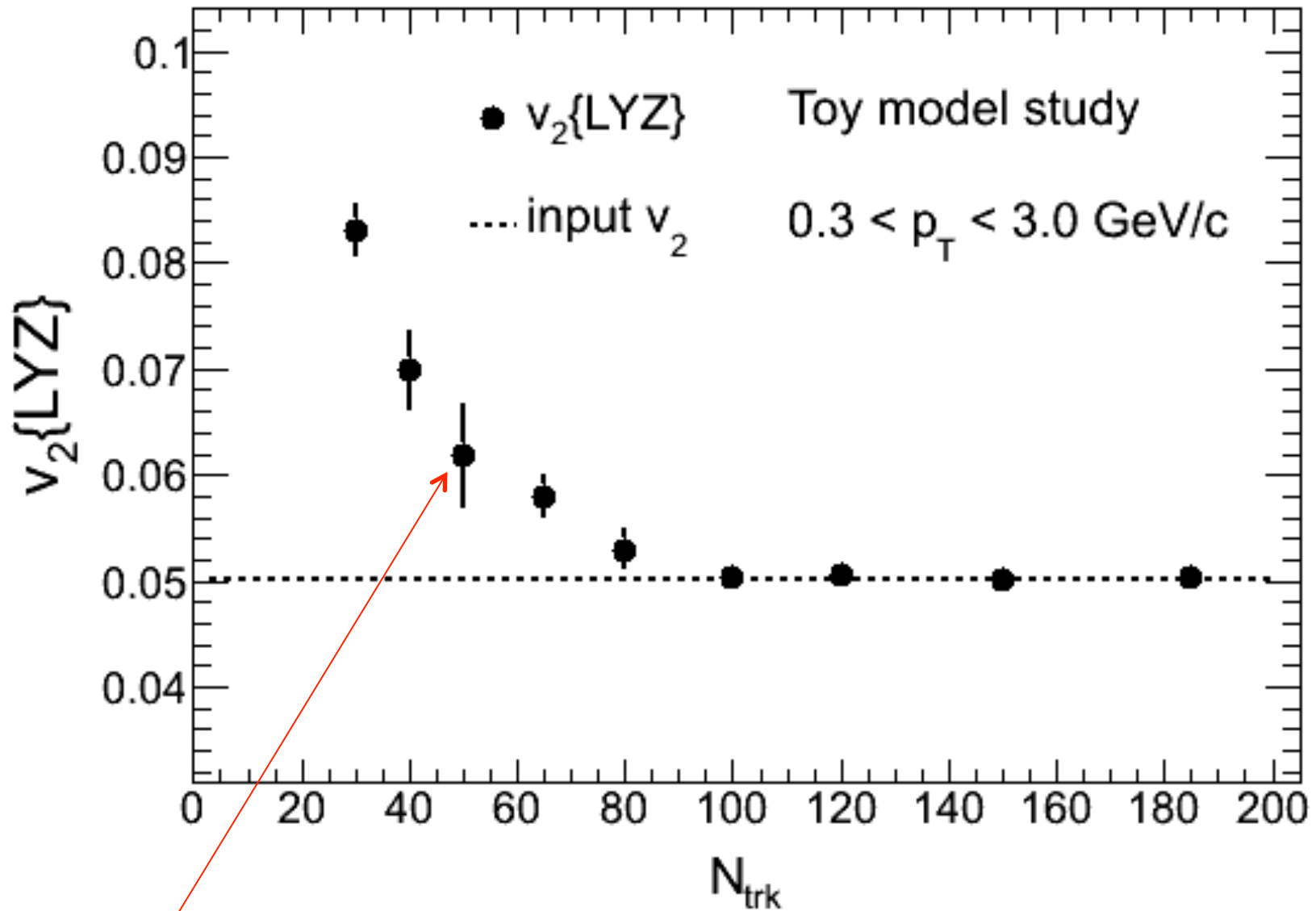
$$G^\theta(ir) \equiv \langle g^\theta(ir) \rangle_{\text{evts}} \equiv \frac{1}{N_{\text{evts}}} \sum_{\text{events}} g^\theta(ir)$$

Integrated flow, $V_n\{\text{LYZ}\}$:

$$V_n^\theta\{\text{LYZ}\} \equiv \frac{j_{01}}{r_0^\theta}$$

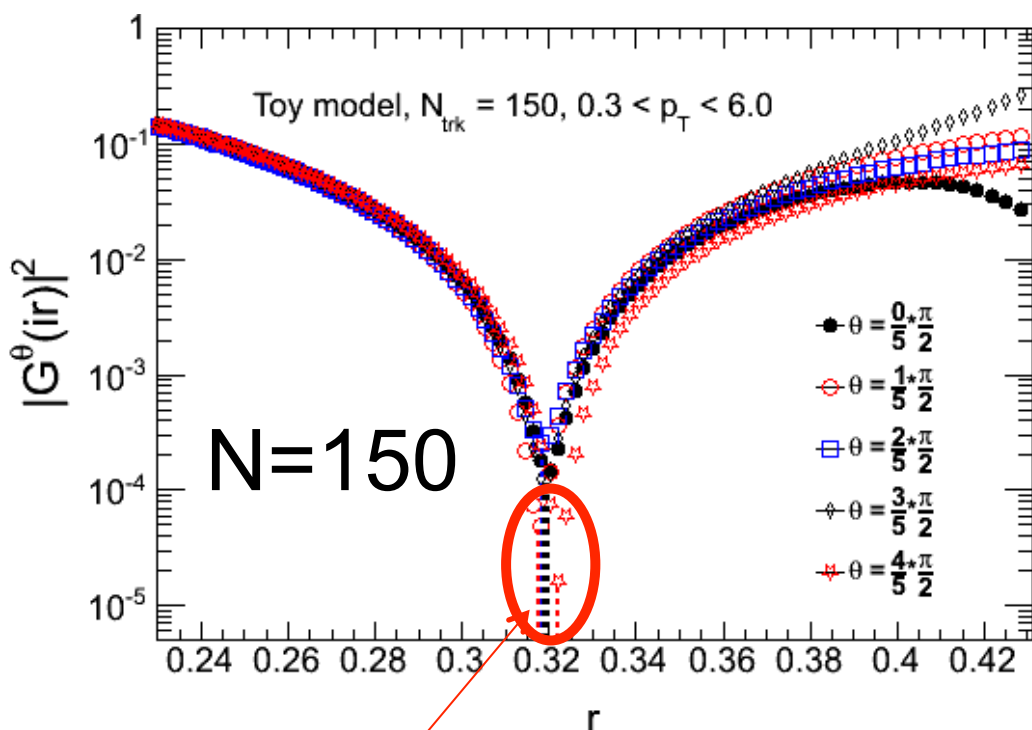


$v_2\{\text{LYZ}\}$ in Toy model



- $v_2\{\text{LYZ}\}$ over estimates the signal in low multiplicity events

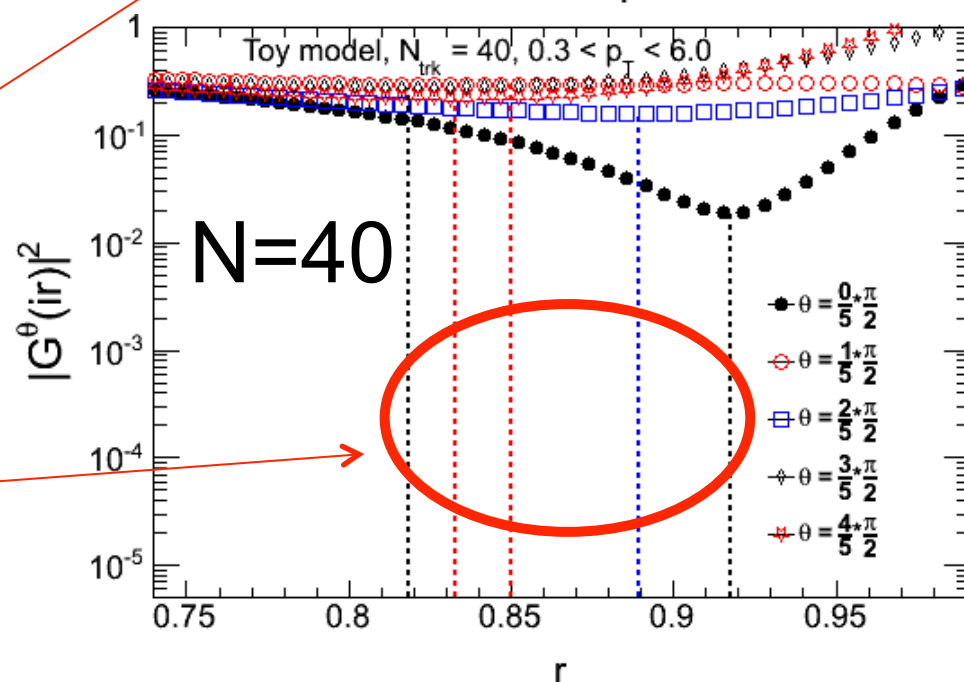
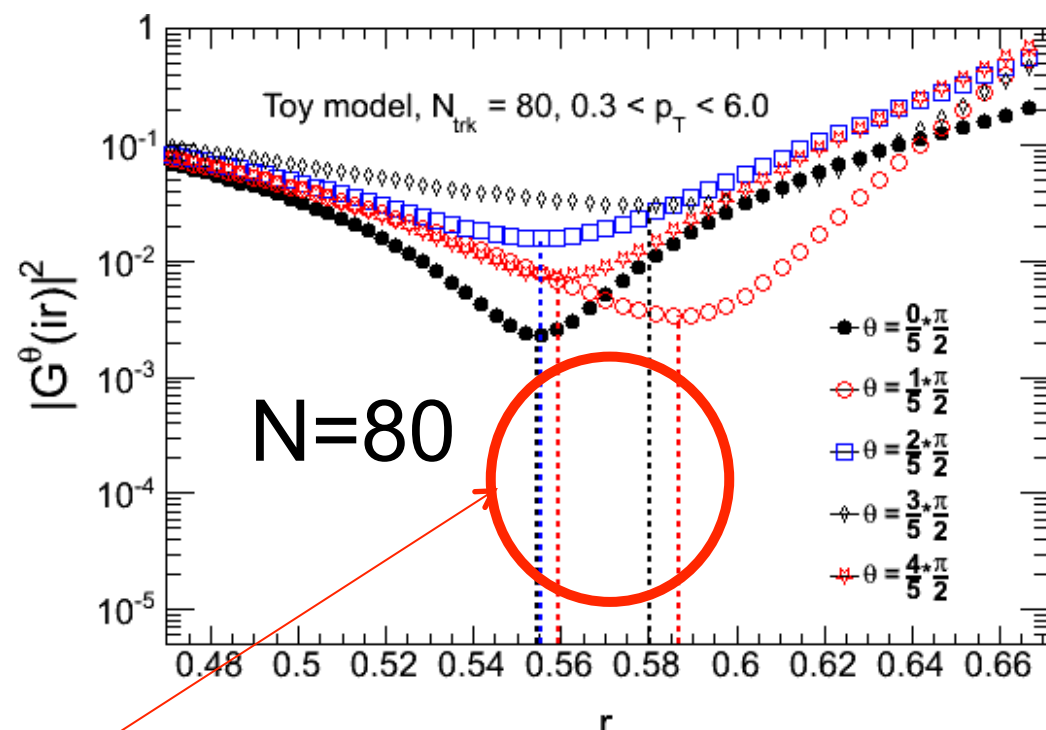
The first minimum of the generating function



Good !

So wide !

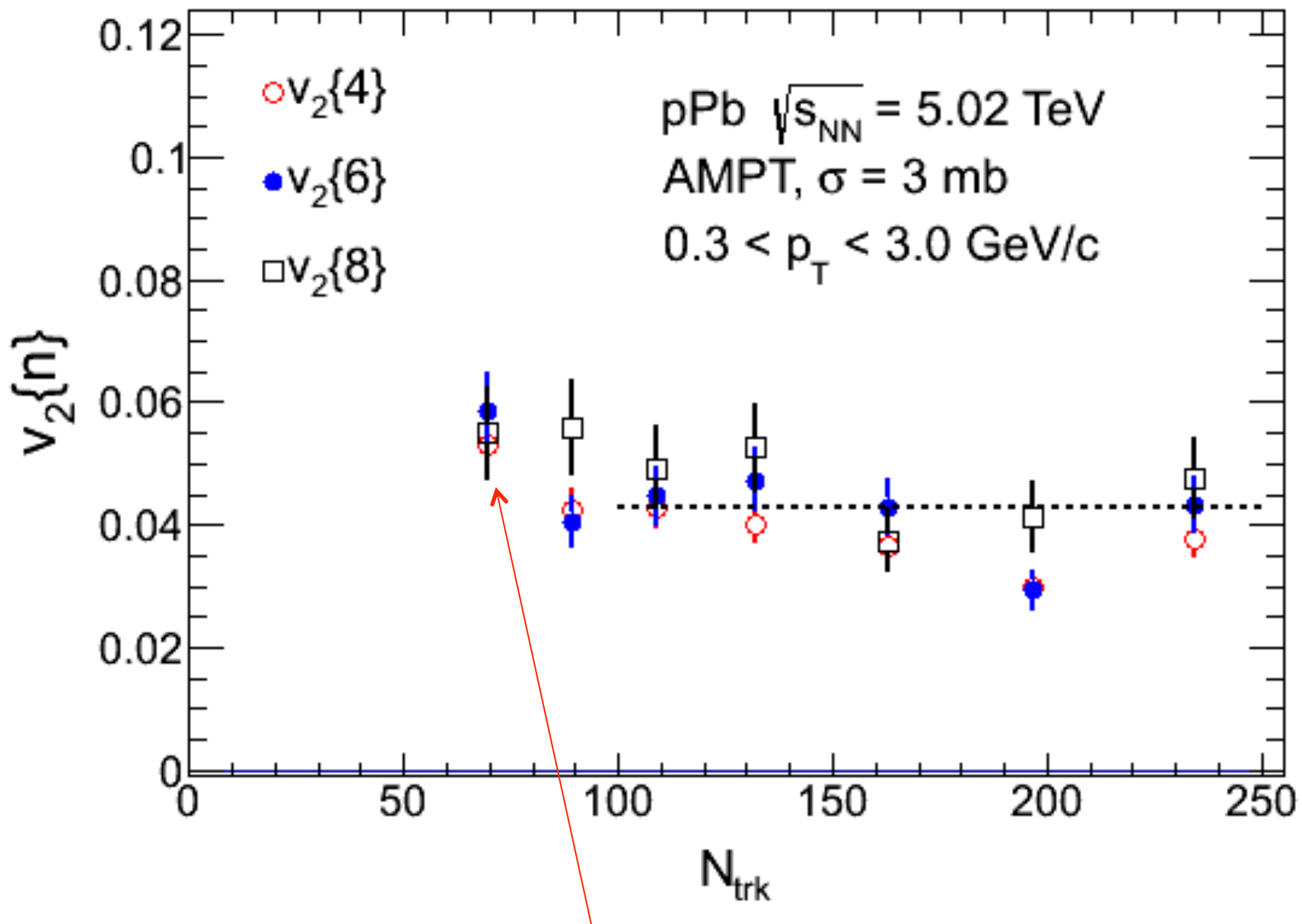
Not acceptable !



Some similar studies using AMPT

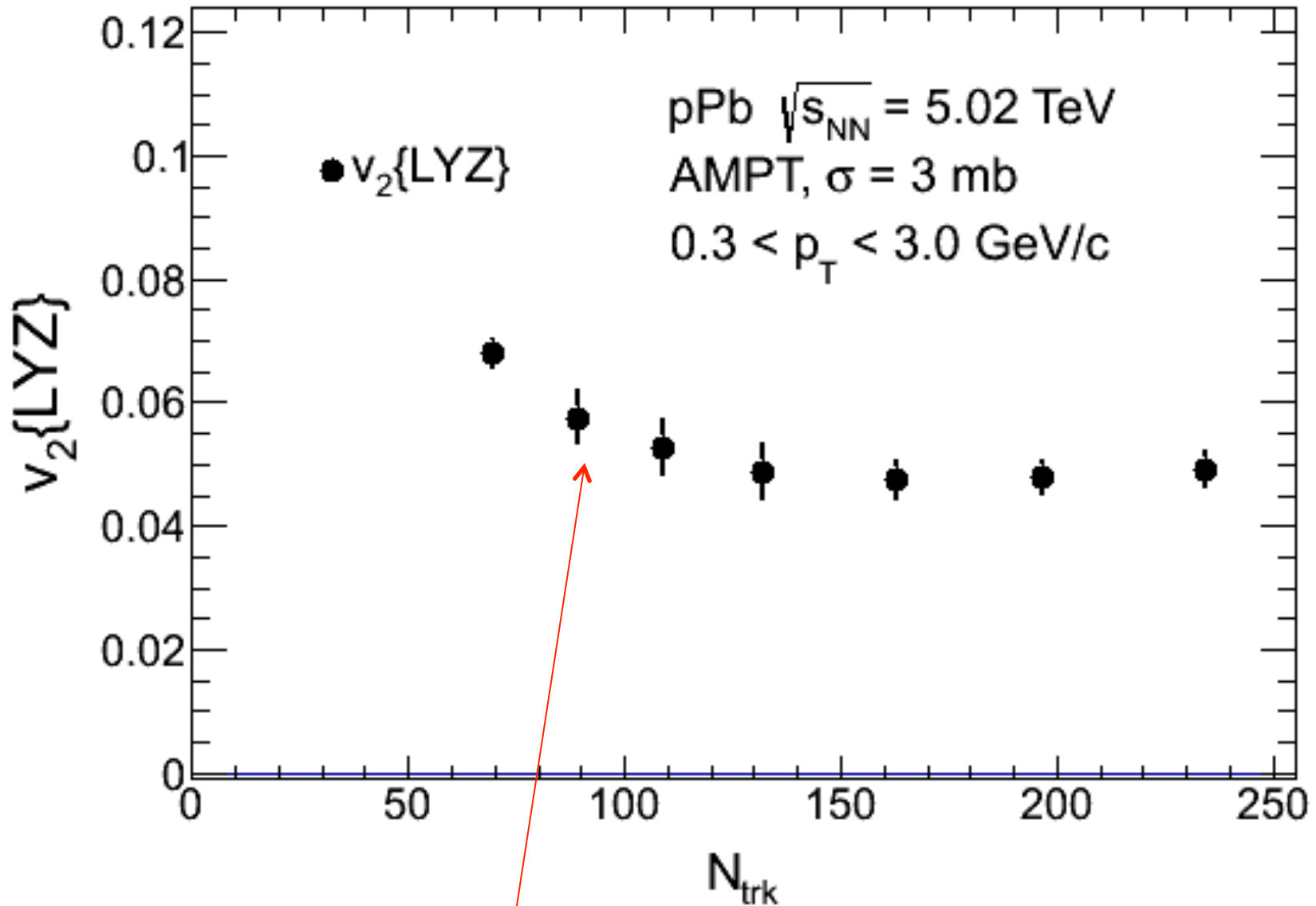
- Using the latest version of AMPT
<http://myweb.ecu.edu/linz/ampt/>
(ampt-v1.26t5-v2.26t5.zip)
- The input parameters (input.ampt) are the same as Adam and Guo-Liang's PRL paper (Phys. Rev. Lett. 113, 252301 (2014)) in pPb and PbPb
- The parton-parton cross section $\sigma = 3 \text{ mb}$
- Results are very preliminary !

$v_2\{n\}$ in AMPT



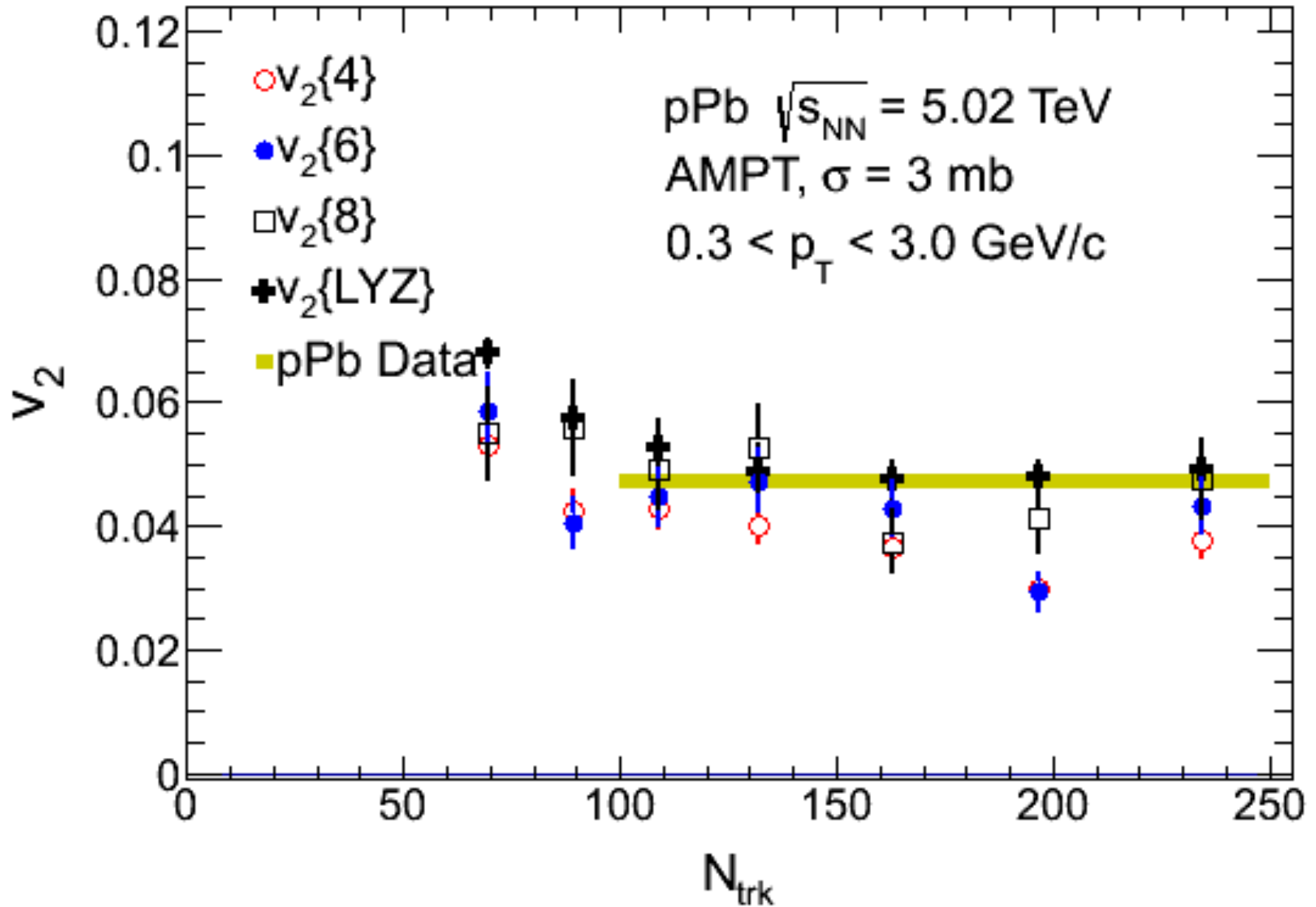
- Already showing the overestimate at $N_{\text{trk}} \sim 70$

$V_2\{\text{LYZ}\}$ in AMPT



- Over estimate, not the true signal !

$v_2\{n\}$ and $v_2\{\text{LYZ}\}$ in AMPT



- Results are very close to pPb data

Summary

- Studying flow in low multiplicity events can tell us the size of the smallest droplet of hot QCD matter with liquid-like behavior
- Toy model studies show that current multi-particle correlation methods tend to fail in low multiplicity, giving fake signals
- The low multiplicity fake signals also appear in AMPT
- With parton-parton cross section $\sigma = 3$ mb in AMPT, the multi-particle correlation results are comparable with real pPb data in high multiplicity

Backup