

# Extracting $\eta/s$ in the presence of bulk viscosity in heavy ion collisions

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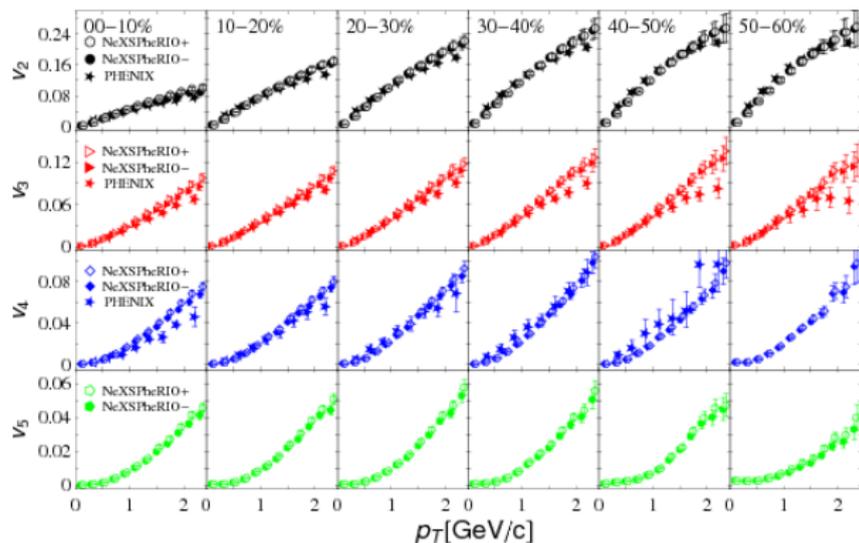
# Outline

- 1 Heavy-Ion Collisions
- 2 Effects of Viscosity
- 3 Viscous Rel. Hydro Event by Event
- 4 Results
  - Qualitative Effects of Bulk+Shear Viscosity (direct  $\pi^+$  only)
  - Extracting  $\eta/s$  when bulk viscosity is used, comparing to data
  - Keep in mind
- 5 Conclusions



# Ideal hydrodynamics and Collective Flow

- Event-by-event NeXus initial conditions and 3+1 ideal relativistic hydrodynamics fit the flow harmonics well

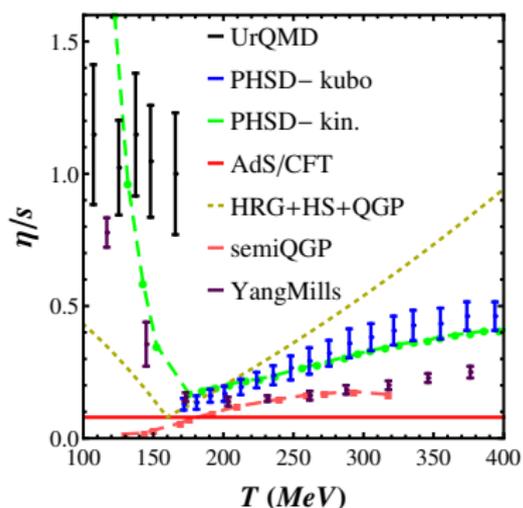


Gardim, Grassi, Luzum, Ollitrault, Phys.Rev.Lett. 109 (2012) 202302

# Shear Viscosity in Heavy-Ion Collisions

- Resistance against the deformation of a fluid

$$\Pi_{\text{Navier-Stokes}}^{\mu\nu} \sim \eta \partial^{\langle\mu} u^{\nu\rangle}$$

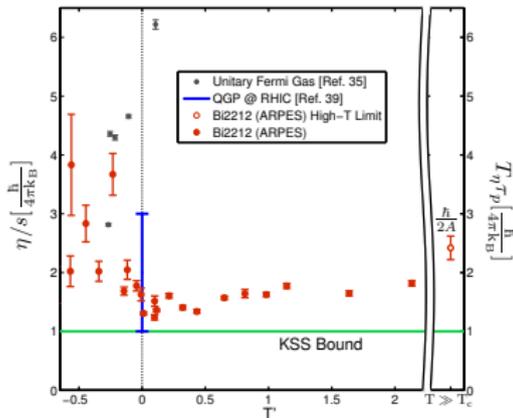


- Dyson-Schwinger Yang-Mills (arXiv:1411.7986 )

- HRG+HS+QGP (JNH et al PRL103(2009)172302, Niemi et al PRL106(2011)212302 )
- PHSD (PRC87(2013)064903)
- AdS/CFT -KSS limit (Kovtun, Son, Stairnets PRL94(2005)111601)
- UrQMD (Demir, Bass PRL(2009)102 )
- semi-QGP-  $\kappa = 32$  ( Hidaka, Pisarski PRD81(2010)076002 )
- Also, Csernai, Kapusta, McLerran PRL 97, 152303 (2006) (not shown)

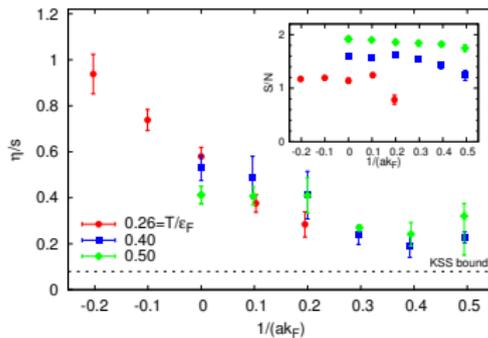
# $\eta/s(T)$ in other nearly perfect fluids

## High Temperature Superconductor



PRB 90, 134509 (2014)

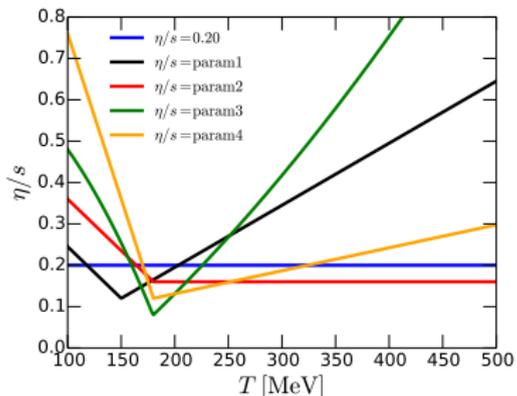
## Dilute Fermi Gas



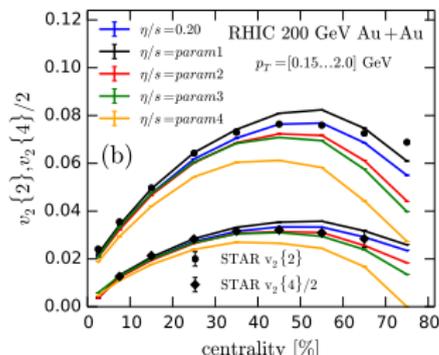
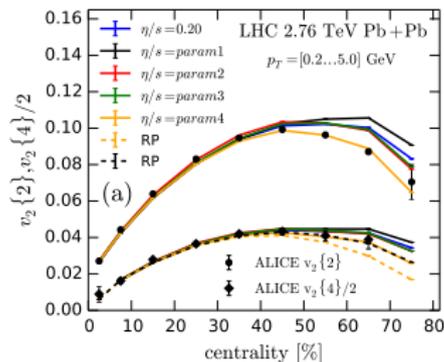
Wlazlowski, Quan, Bulgac arXiv:1504.02560

# Shear Viscosity in Heavy-Ion Collisions

Varying  $\eta/s$ : Niemi et al. arXiv:1505.02677

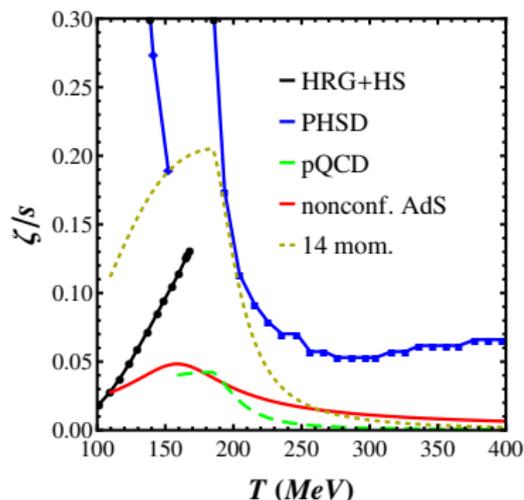


- RHIC probes lower temperatures,  $\eta/s = 0.2$  (for EKRT), LHC prefers  $\eta/s(T)$  that is small in the hadron gas phase



# Bulk Viscosity in Heavy-Ion Collisions

- Resistance against the radial expansion or compression of a fluid  $\Pi_{Navier-Stokes} \sim -\zeta(\partial_\mu U^\mu)$



- HRG+HS(Kadam and Mishra arXiv:1408.6329 )
- PHSD (PRC 87, 064903 (2013) )
- non-conformal holographic model (Finazzo et al - JHEP 1502 (2015) 051 )
- pQCD (Arnold, Dogan, Moore Phys.Rev. D74 (2006) 085021)
- 14 mom. (Denicol et al, PRC90(2014)024912)

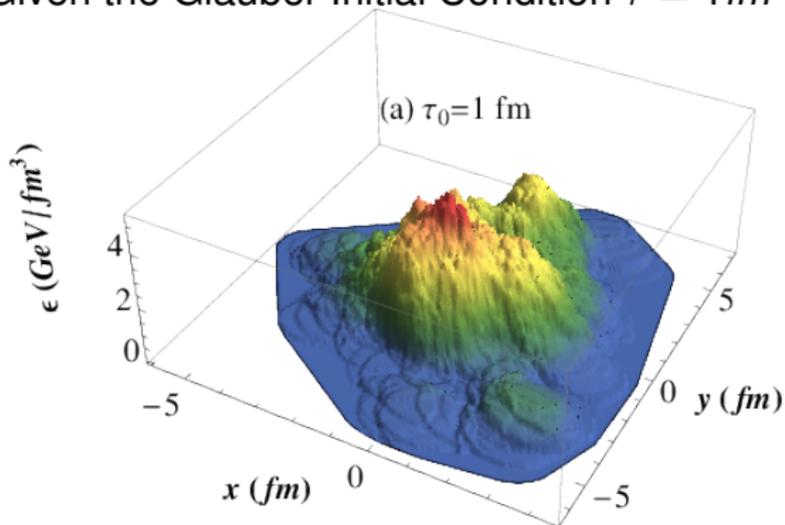
Peak also seen in:

JNH, PRL 103 (2009) 172302,  
 Kharzeev JHEP 0809 (2008) 093

# Viscosity in Heavy-Ion Collisions

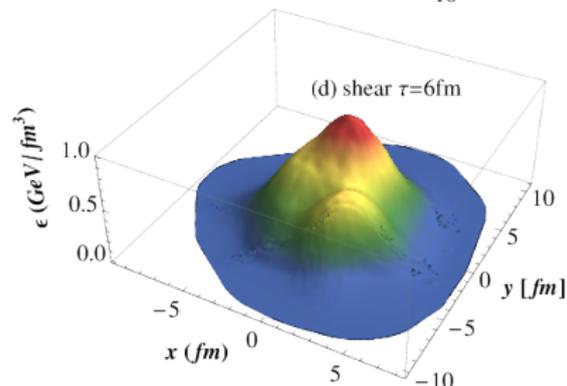
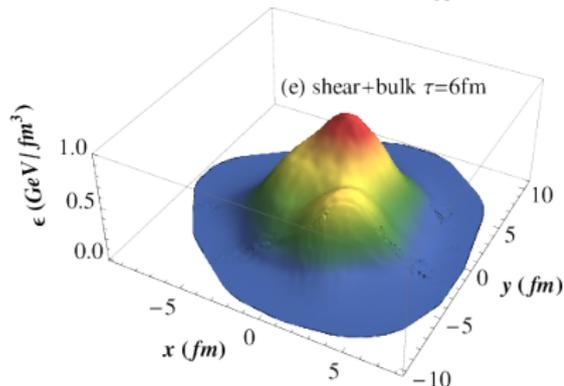
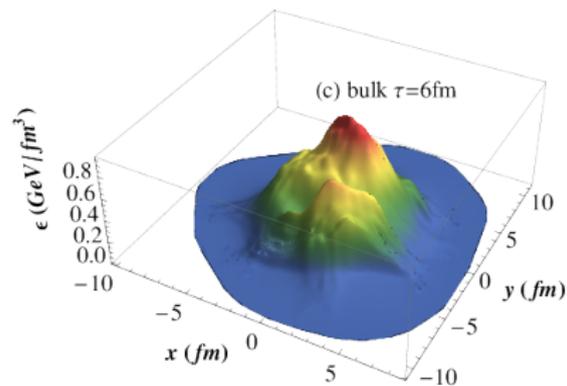
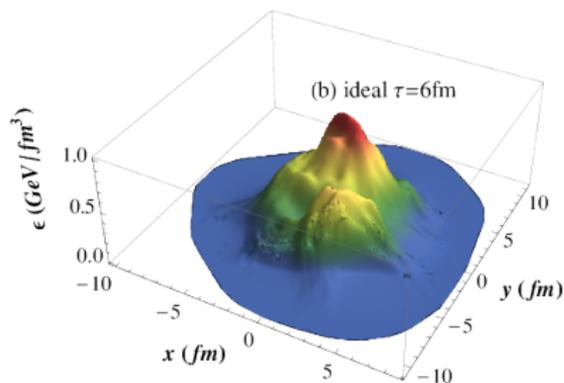
JNH et al, Phys.Rev. C90 (2014) 3, 034907

Given the Glauber Initial Condition  $\tau = 1 \text{ fm}$



# Viscosity in Heavy-Ion Collisions

JNH et al, Phys.Rev. C90 (2014) 3, 034907



# Initializing the Energy-Momentum Tensor

Hydrodynamics boils down to:

$$\partial_\mu T^{\mu\nu} = 0 \quad (1)$$

$$T^{\mu\nu} = \varepsilon u^\nu u^\nu - (p + \Pi) \Delta^{\mu\nu} + \pi^{\mu\nu} \quad (2)$$

$$(3)$$

where we obtain an initial  $T^{\mu\nu}$  from NEXUS/IP-Glasma or  $\varepsilon(\mathbf{r})$  from Glauber/MCKLN/EKRT/URQMD etc.

From  $T^{\mu\nu}$  we get:

$$\varepsilon(\mathbf{r}), u^\mu, \pi^{\mu\nu}, \Pi$$

but we only use  $\varepsilon(\mathbf{r}), u^\mu$ !!!

Precision hydrodynamics necessitates the entire  $T^{\mu\nu}$ , so BOTH bulk and shear are needed!

# Effects of viscosity with hydrodynamics (hydro only)

JNH et al, Phys.Rev. C90 (2014) 3, 034907

Compare percentage change of mean and variance in the presence of shear+bulk vs. bulk only (or shear only)

## Effects of shear on $\Pi$

- The mean has almost no variation
- Shear increases the variation in bulk (at late times)
- Variation decreases significantly at early times

## Effects of bulk on $\pi^{00}$ and $\pi^{12}$

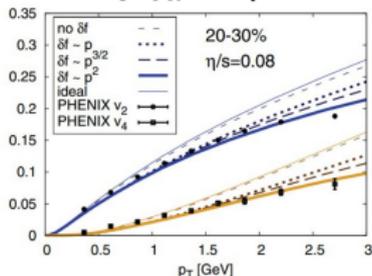
- Bulk suppresses the  $\pi^{\mu\nu}$
- Largest effect at late times.
- Variation decreases across the board

# Cooper-Frye Freeze-out

$$\text{Hydro into Particles: } \left( E_p \frac{dN}{d^3p} \right)_i = g_i \int_{\Sigma} d\Sigma_{\mu} p^{\mu} f_i$$

## Shear Viscosity

$$\delta f_{shear} \propto p^2$$

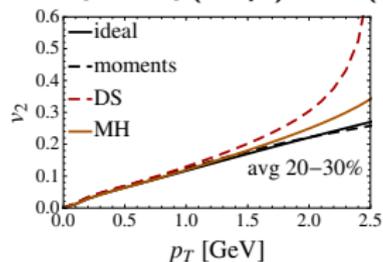


Schenke, Jeon, Gale, PRC85(2012)024901

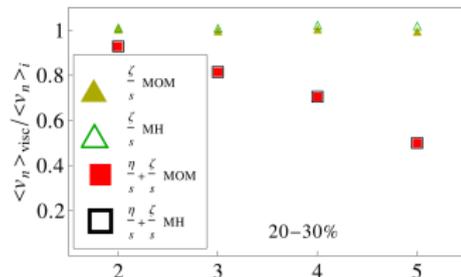
- Shear  $\uparrow$  flow, bulk  $\downarrow$  flow
- Bulk is highly model dependent for higher  $p_T$

## Bulk Viscosity

$$\delta f_{bulk} \propto B_0 + D_0(u \cdot p) + E(u \cdot p)^2$$



JNH et al, Phys.Rev. C88 (2013) 044916



- Integrated  $v_n$ 's not affected by  $\delta f$

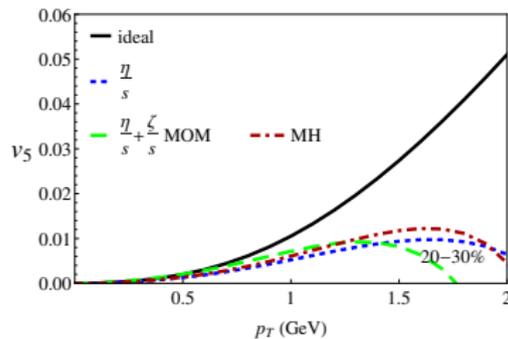
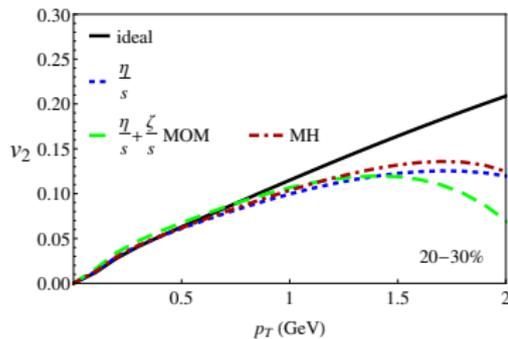
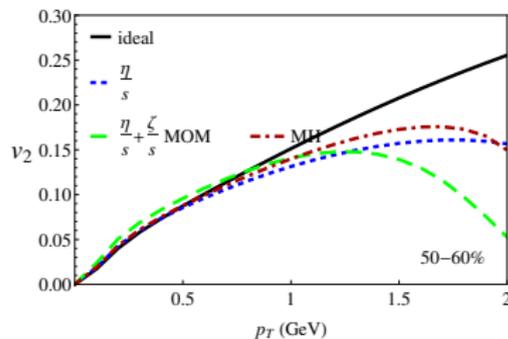
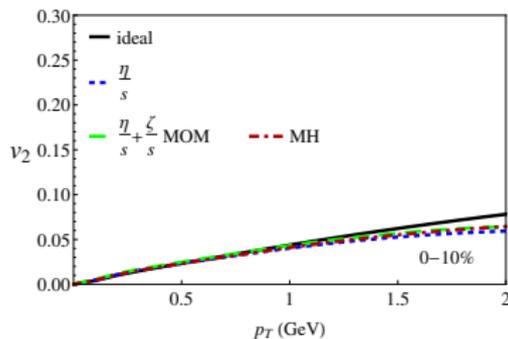
	$E_0$ [ $fm^4$ ]	$D_0$	$\frac{fm^4}{GeV}$	$B_0$	$\frac{fm^4}{GeV^2}$	
mo	-65.85	171.27		-63.05		PRC88(2013)044916
DS	-71.96	121.50		0		PRC85(2012)044909
MH	-0.69	-38.96		49.69		PRC80(2009)054906

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# Event-by-Event $v_2$ at RHIC in $v$ -USPhydro

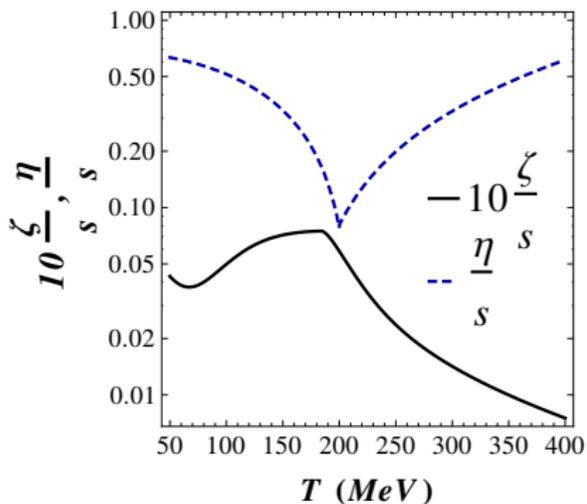
JNH, Noronha, Grassi, PRC90(2014)034907



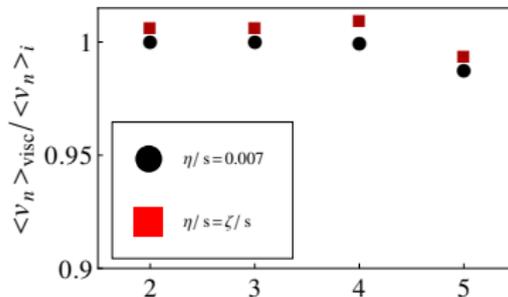
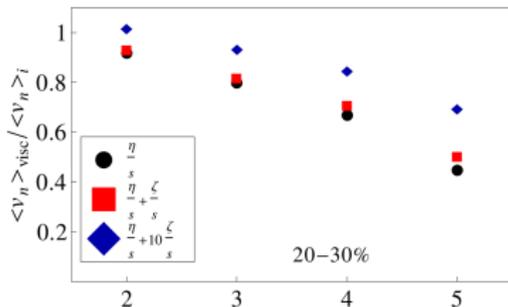
# Integrated $v_n$ 's at RHIC in v-USPhydro - Comparing

## $\zeta/s$

JNH, Noronha, Grassi, PRC90(2014)034907



- $\zeta/s$  increases the integrated  $v_n$ 's

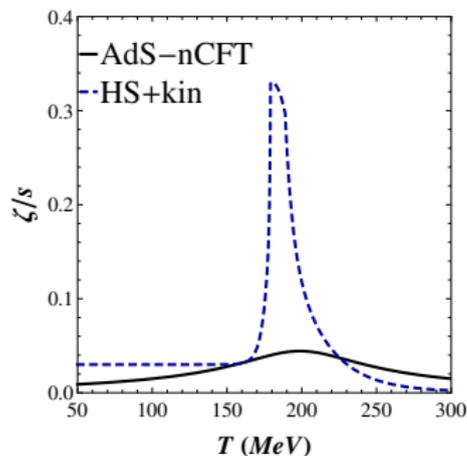


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# $\zeta/s$ Description

- $\zeta/s^1$  Hagedorn States  
(JNH et al, PRL103(2009)172302)  
+kinetic theory  
(Denicol et al, PR90(2014)no.2,024912)
- $\zeta/s^2$  non-conformal AdS  
(Finazzo et al, JHEP1502(2015)051)

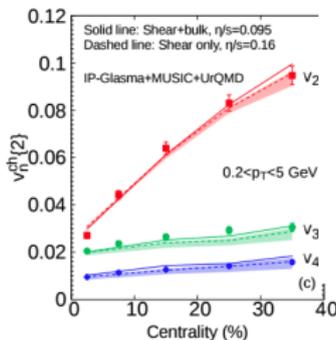
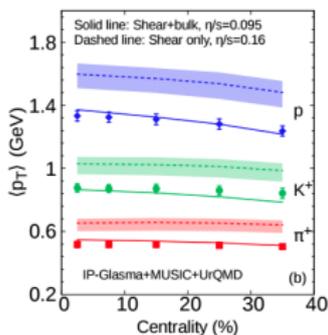


$$\bullet \tau_{\pi}^1 = 5 \frac{\zeta}{(1-c_s)^2(\epsilon+p)}$$

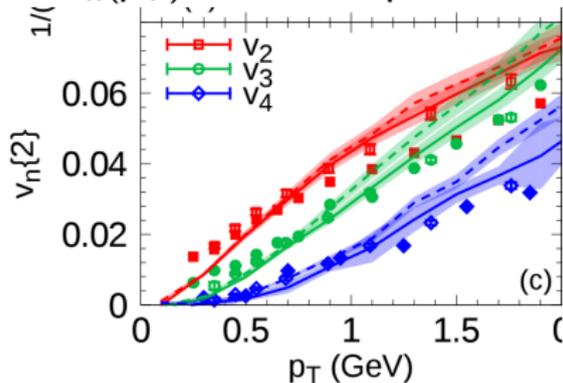
$$\bullet \tau_{\pi}^2 = 9 \left( -0.0506 \frac{T_c}{T^2} + \frac{10.453}{T \sqrt{0.156658 + (T/T_c - 1.131)^2}} \right)$$

# Bulk viscosity at LHC in IP-Glasma+MUSIC

- Bulk decreases  $\langle p_T \rangle$  at LHC
- Fits integrated  $v_n$  well



- $v_n(p_T)$  has a steeper slope



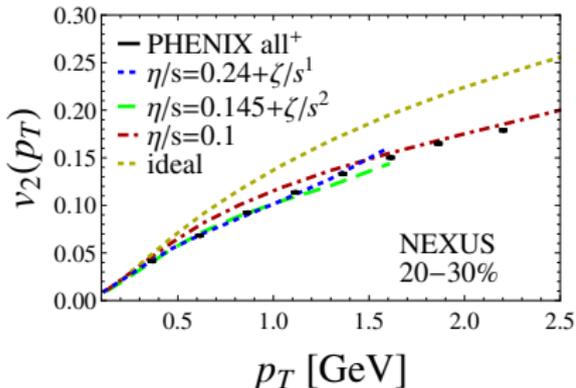
Ryu et al, arXiv:1502.01675

Ryu et al, arXiv:1502.01675

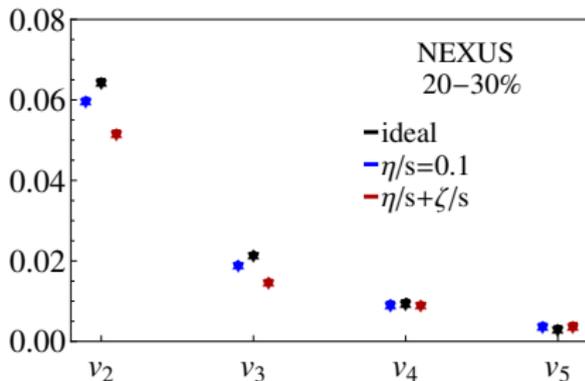
Here bulk viscosity  $\Downarrow \eta/s$  to fit the  $v_n$ 's (for IP-Glasma+MUSIC)

# Bulk viscosity at RHIC in NEXUS+v-USPhydro-preliminary!!

- Bulk viscosity has smaller model dependencies for  $\delta f$  below  $p_T = 1.5$  GeV
- Bulk require twice as large  $\eta/s$



- Bulk contributes little to  $v_n$ 's
- Same  $\zeta/s$  as in IP-Glasma arXiv:1502.01675



Here bulk  $\uparrow \eta/s$  to fit  $v_n$ 's (NEXUS-v-USPhydro) - differences in 2<sup>nd</sup> order transport coef.? UrQMD? RHIC vs. LHC?  $\delta f$ ? NEXUS vs. IP-Glasma?

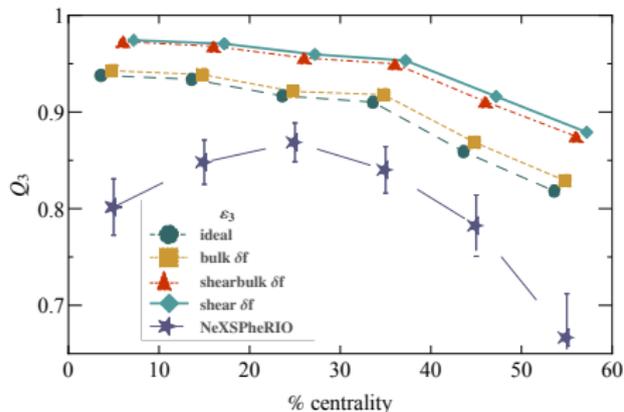
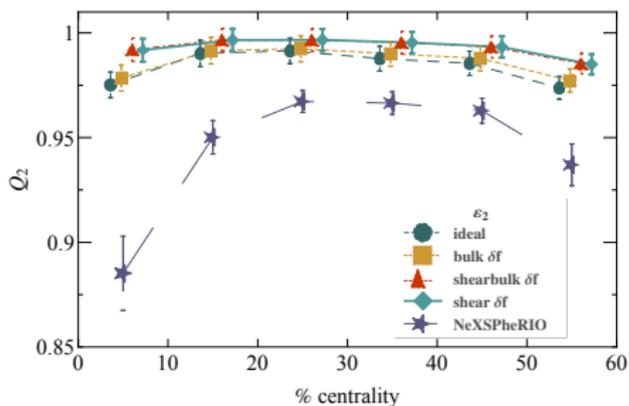
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# Shear and bulk effects on the mapping of eccentricities

Gardim, JNH, Luzum, Grassi, arXiv:1411.2574

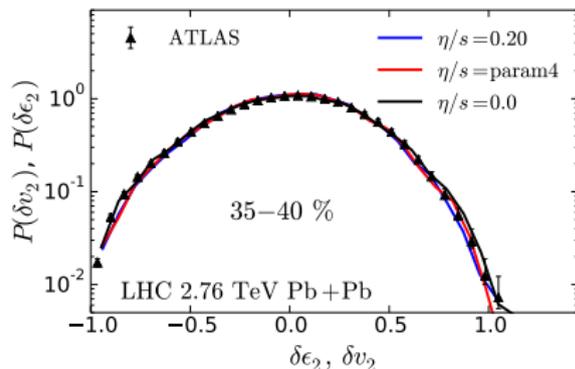
- **But in the end, the eccentricities are vital!**
- If the initial eccentricities are wrong, there is only so much that shear/bulk can do
- Shear and bulk increase the mapping between initial eccentricities and  $v_n$ 's



# Where do we go from here?

- $\langle p_T \rangle$  with different initial states
- $\delta f$  improvements- current models don't converge!
- Effects of bulk viscosity in hard probes?
- $pA$  (see Niemi and Denicol arXiv:1404.7327)
- Non-zero initial shear stress tensor/bulk pressure (free streaming checked Liu et al arXiv:1504.02160 but need QCD inspired initializations)
- Effects of granularity

- Shear viscosity doesn't affect  $P(v_2)$ , what about bulk?



Niemi et al. arXiv:1505.02677

# Conclusions

- Bulk viscosity and shear viscosity have a non-trivial interplay for the flow harmonics
- Depending on the initial conditions/RHIC vs. LHC etc bulk viscosity either increases or decreases  $\eta/s$ !
- You can't escape the initial eccentricities- viscosity just strengthens that relationship
- So much more work to be done...