

Neutrinos and Solar Metallicity

- ❑ The solar abundance problem and CN neutrinos
- ❑ Measurement opportunities



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INT

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The Standard Solar Model

- ❑ Origin of solar neutrino physics: desire to test a model of low-mass, main-sequence stellar evolution
 - **local hydrostatic equilibrium**: gas pressure gradient counteracting gravitational force
 - hydrogen burning: **pp chain, CN cycle**
 - energy transport by **radiation** (interior) and **convection** (envelope)
 - **boundary conditions**: today's mass, radius, luminosity
- ❑ The implementation of this physics requires
 - **electron gas EOS**
 - **low-energy nuclear cross sections**
 - **radiative opacity**
 - some means of fixing the **composition at ZAMS**, including the ratios $X:Y:Z$

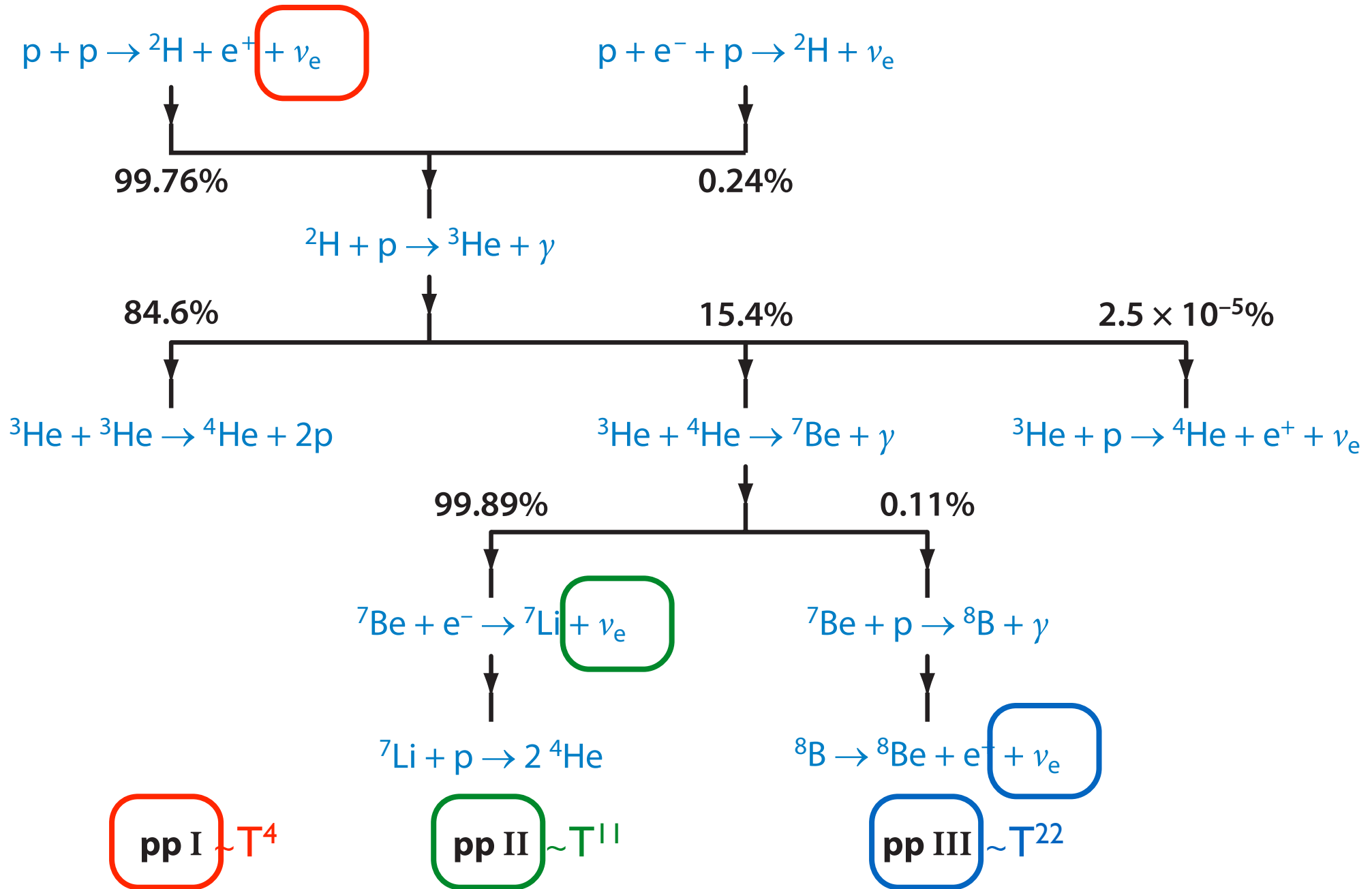
Composition/metallicity in the SSM:

- ❑ Standard picture of pre-solar contraction, evolution
 - Sun forms from a contracting primordial gas cloud
 - passes through the Hayashi phase: cool, highly opaque, large temperature gradients, slowly contracting \leftrightarrow convective (mixed)
 - radiative transport becomes more efficient at star's center: radiative core grows from the center outward
 - when dense and hot enough, nuclear burning starts...

- ❑ Because the Hayashi phase fully mixes the proto-Sun, a chemically homogeneous composition is traditionally assumed at ZAMS
 - $X_{\text{ini}} + Y_{\text{ini}} + Z_{\text{ini}} = 1$
 - relative metal abundances taken from a combination of photospheric (volatile) and meteoritic (refractory) abundances
 - Z_{ini} fixed by model's present-day Z_{\odot} , corrected for diffusion
 - Y_{ini} and α_{MLT} adjusted to produce present-day L_{\odot} and R_{\odot}

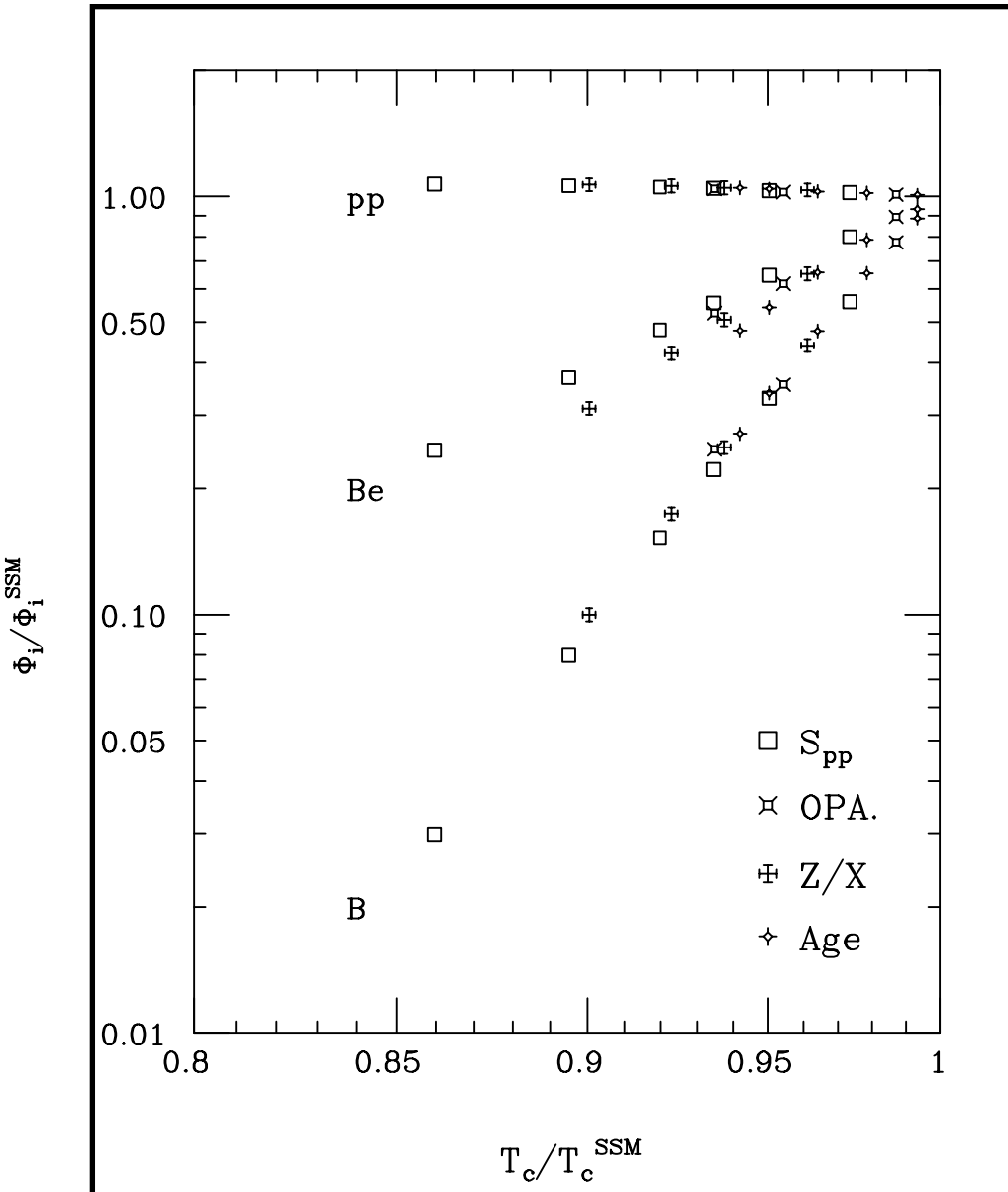
Model tests:

- ❑ **Solar neutrinos:** direct measure of core temperature to $\sim 0.5\%$
 - once the flavor physics has been sorted out
- ❑ **Helioseismology:** inversions map out the local sound speed, properties of the convective zone

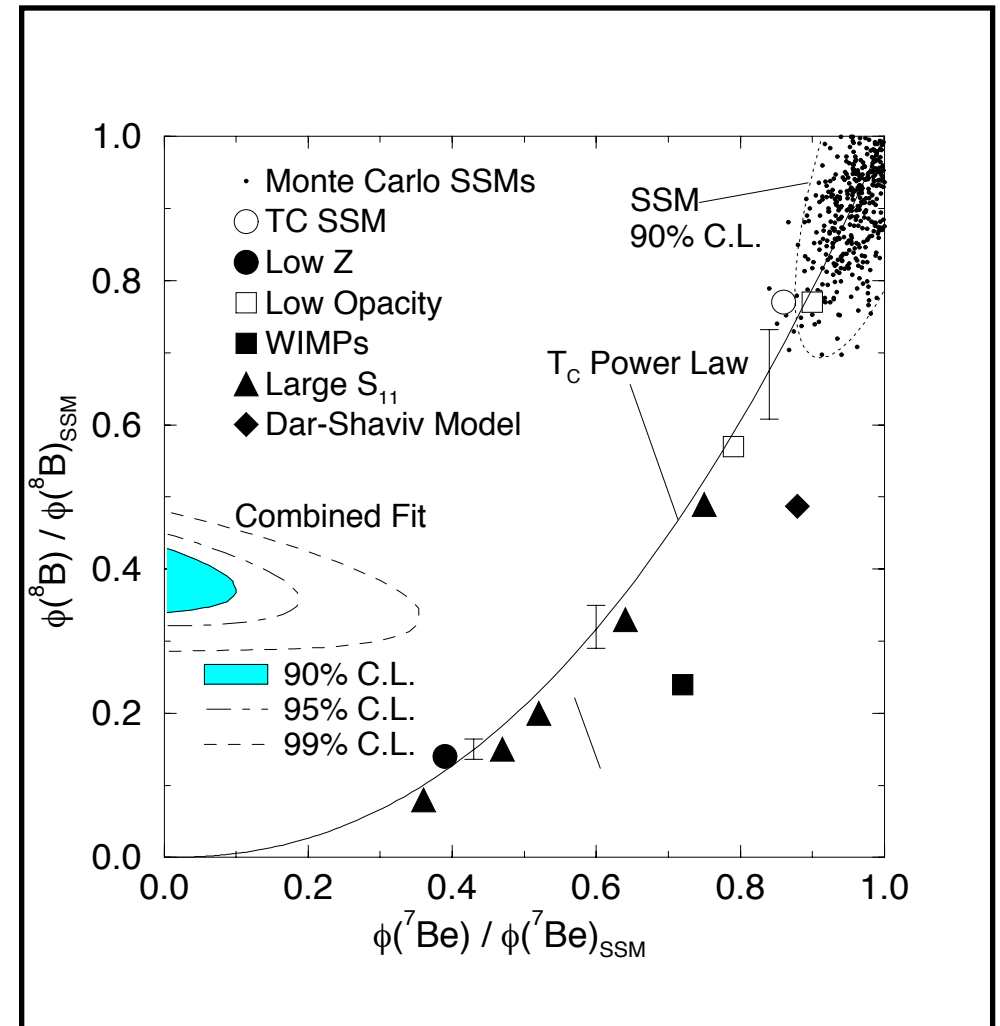




By mid-1990s model-independent arguments developed showing that no adjustment in the SSM could reproduce observed ν fluxes (Cl, Ga, water exps.)

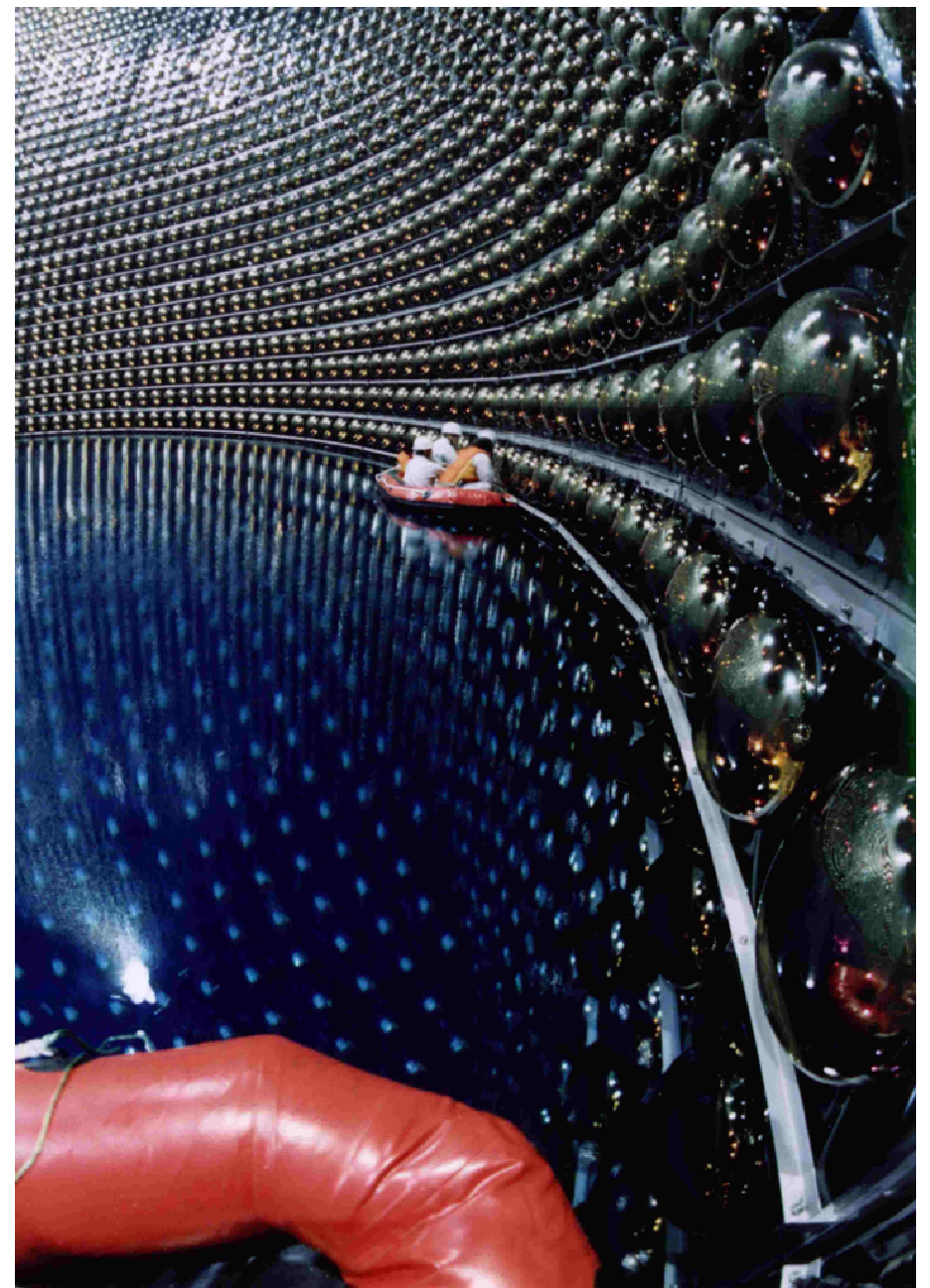
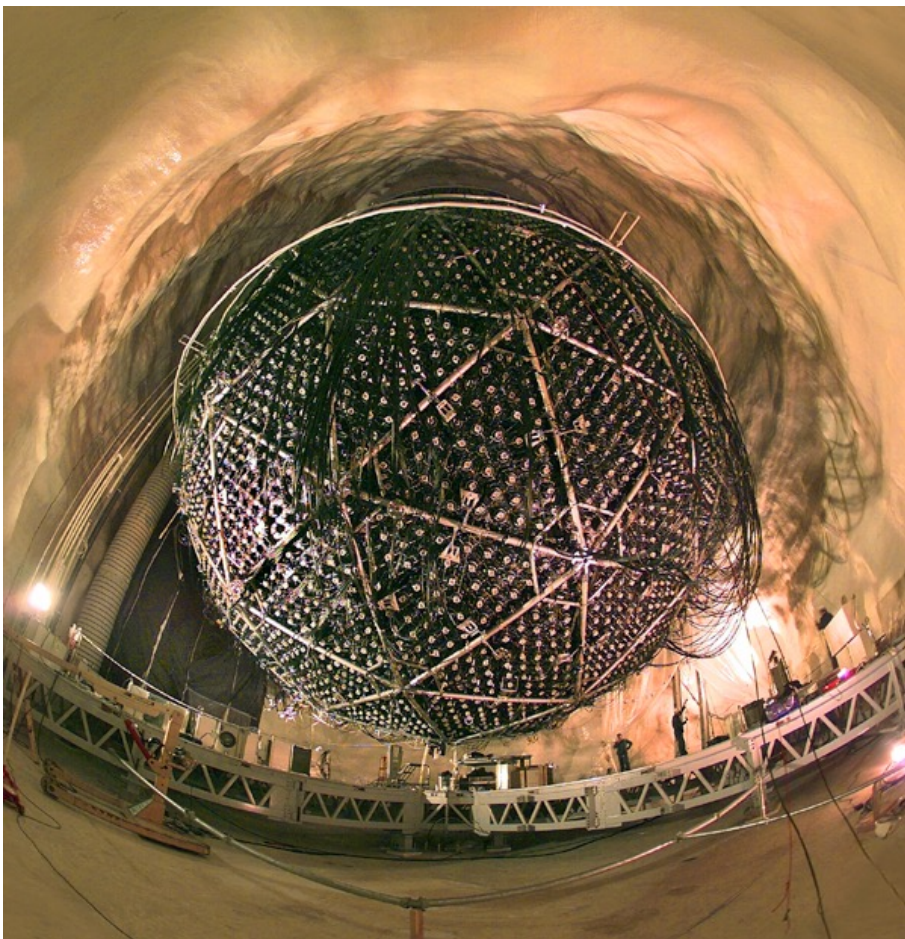


Castellani et al.



Hata et al.

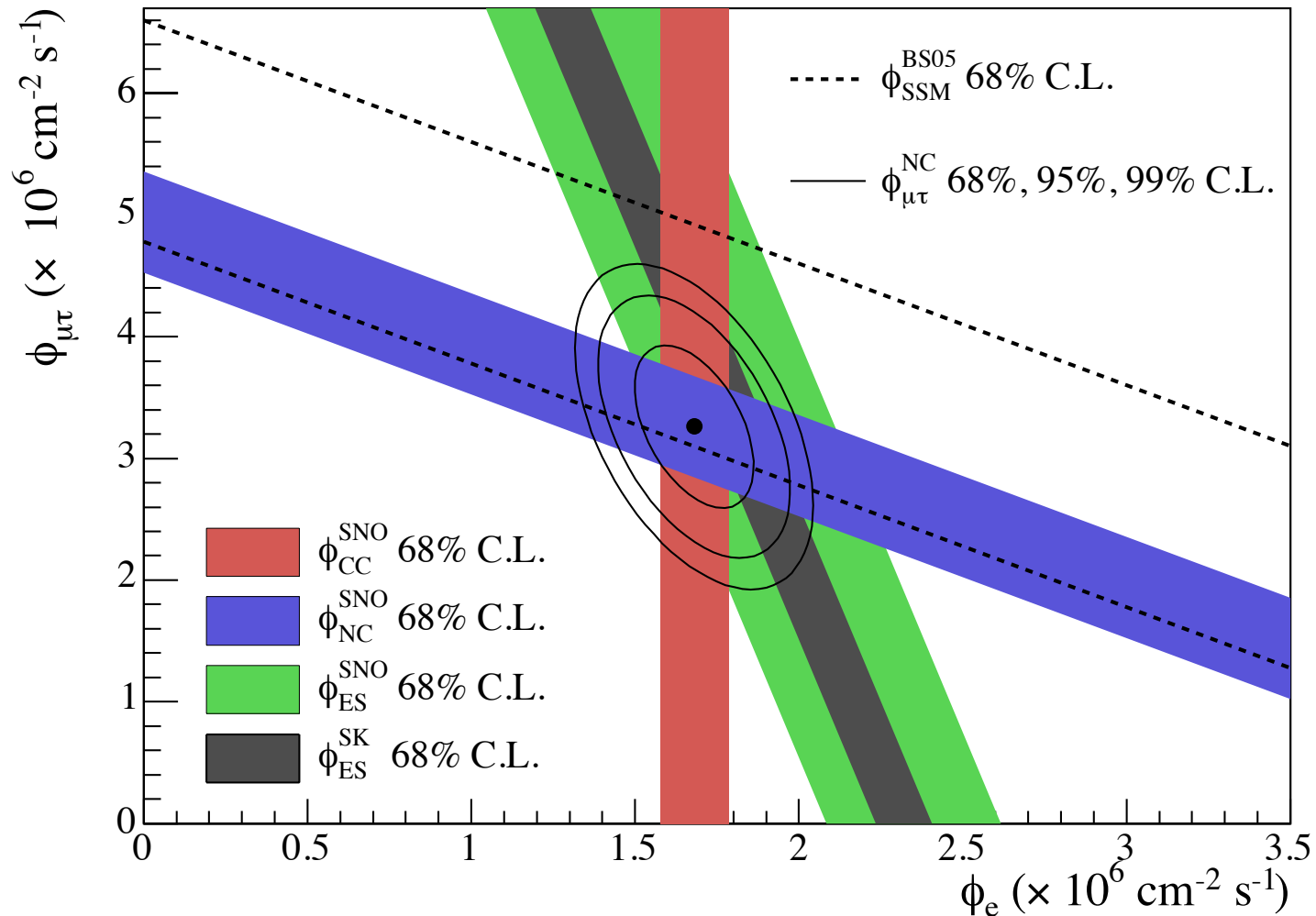
(and Heeger and Robertson)



SNO, Super-Kamiokande, Borexino

the “solar ν problem” was definitively traced to new physics by SNO

flavor conversion $\nu_e \rightarrow \nu_{\text{heavy}}$



requires an extension of the SM -- Majorana masses or ν_R

		high-Z SSM	low-Z SSM	luminosity constrained fit to data	
ν flux	E_ν^{\max} (MeV)	GS98-SFII	AGSS09-SFII	Solar	units
$p+p \rightarrow {}^2\text{H}+e^++\nu$	0.42	$5.98(1 \pm 0.006)$	$6.03(1 \pm 0.006)$	$6.05(1^{+0.003}_{-0.011})$	$10^{10}/\text{cm}^2\text{s}$
$p+e^-+p \rightarrow {}^2\text{H}+\nu$	1.44	$1.44(1 \pm 0.012)$	$1.47(1 \pm 0.012)$	$1.46(1^{+0.010}_{-0.014})$	$10^8/\text{cm}^2\text{s}$
${}^7\text{Be}+e^- \rightarrow {}^7\text{Li}+\nu$	0.86 (90%)	$5.00(1 \pm 0.07)$	$4.56(1 \pm 0.07)$	$4.82(1^{+0.05}_{-0.04})$	$10^9/\text{cm}^2\text{s}$
	0.38 (10%)				
${}^8\text{B} \rightarrow {}^8\text{Be}+e^++\nu$	~ 15	$5.58(1 \pm 0.14)$	$4.59(1 \pm 0.14)$	$5.00(1 \pm 0.03)$	$10^6/\text{cm}^2\text{s}$
${}^3\text{He}+p \rightarrow {}^4\text{He}+e^++\nu$	18.77	$8.04(1 \pm 0.30)$	$8.31(1 \pm 0.30)$	—	$10^3/\text{cm}^2\text{s}$
${}^{13}\text{N} \rightarrow {}^{13}\text{C}+e^++\nu$	1.20	$2.96(1 \pm 0.14)$	$2.17(1 \pm 0.14)$	≤ 6.7	$10^8/\text{cm}^2\text{s}$
${}^{15}\text{O} \rightarrow {}^{15}\text{N}+e^++\nu$	1.73	$2.23(1 \pm 0.15)$	$1.56(1 \pm 0.15)$	≤ 3.2	$10^8/\text{cm}^2\text{s}$
${}^{17}\text{F} \rightarrow {}^{17}\text{O}+e^++\nu$	1.74	$5.52(1 \pm 0.17)$	$3.40(1 \pm 0.16)$	$\leq 59.$	$10^6/\text{cm}^2\text{s}$
χ^2/P^{agr}		<u>$3.5/90\%$</u>	<u>$3.4/90\%$</u>		

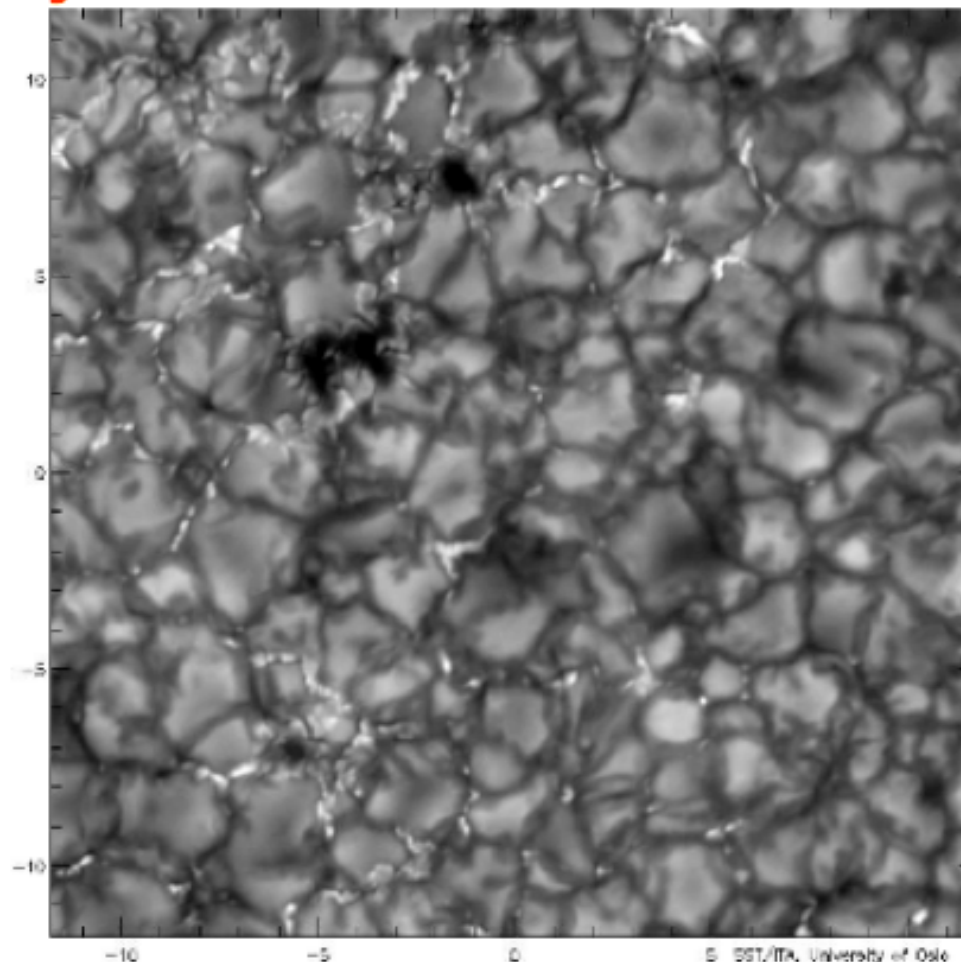
With the new ν physics added, theory and experiment seem to coincide

Recent Re-evaluations of Photospheric Abundances

- ❑ SSM requires as input an estimate of core metallicity at $t=0$, and assumes a homogeneous zero-age Sun
- ❑ The metals have an important influence on solar properties: free-bound transitions important to opacity, influencing local sound speed
- ❑ The once excellent agreement between SSM and helioseismology due in part to this input (Grevesse & Sauval 1998)

- ❑ The classic analyses modeled the photosphere in 1D, without explicit treatments of stratification, velocities, inhomogeneities
- ❑ New 3D, parameter-free methods were then introduced, significantly improving consistency of line analyses: MPI-Munich

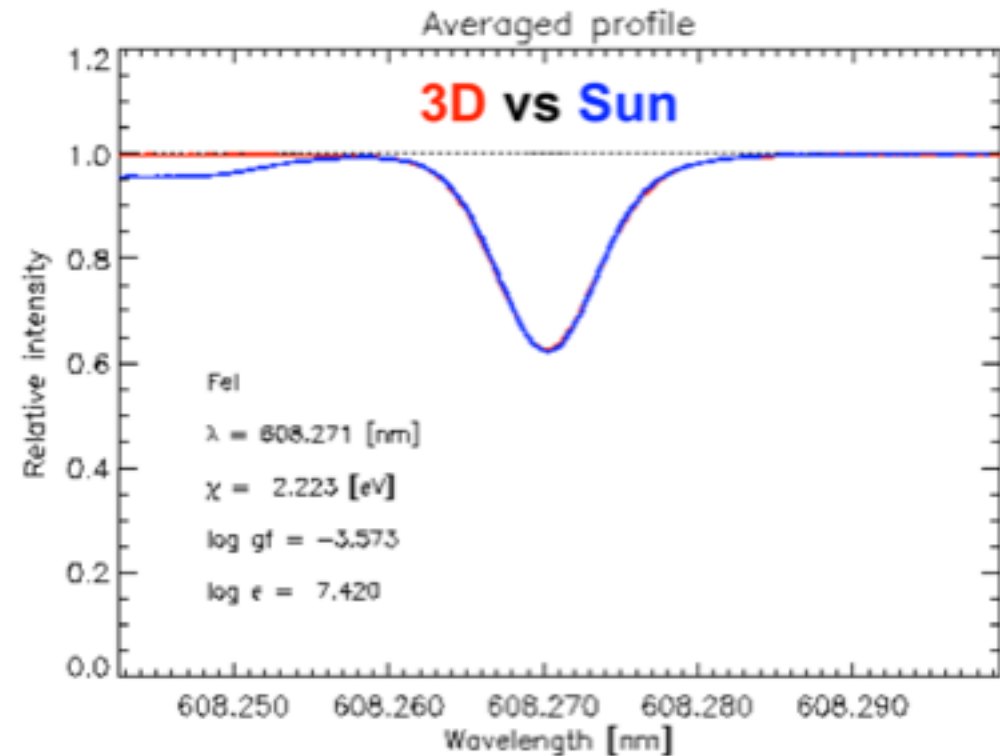
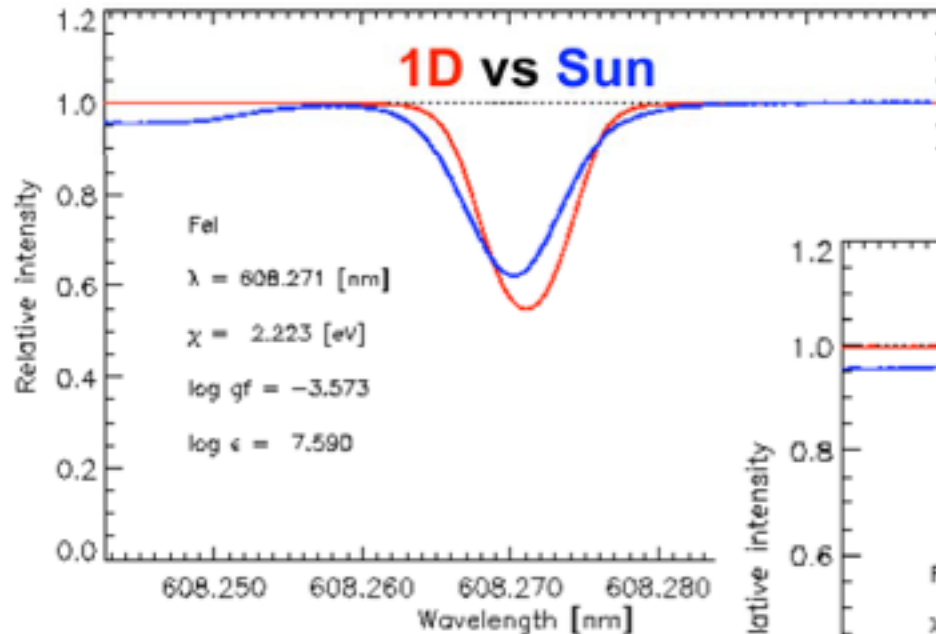
Dynamic and 3D due to convection



Mats Carlsson (Oslo)

Sun

Averaged line profiles (from Asplund 2007)



- ❑ Spread in abundances from different C, O lines sources reduced from $\sim 40\%$ to 10%
- ❑ But abundances significantly reduced Z: $0.0169 \Rightarrow 0.0122$
- ❑ Makes sun more consistent with similar stars in local neighborhood
- ❑ Lowers SSM ^8B flux by 20%

But adverse consequences for helioseismology

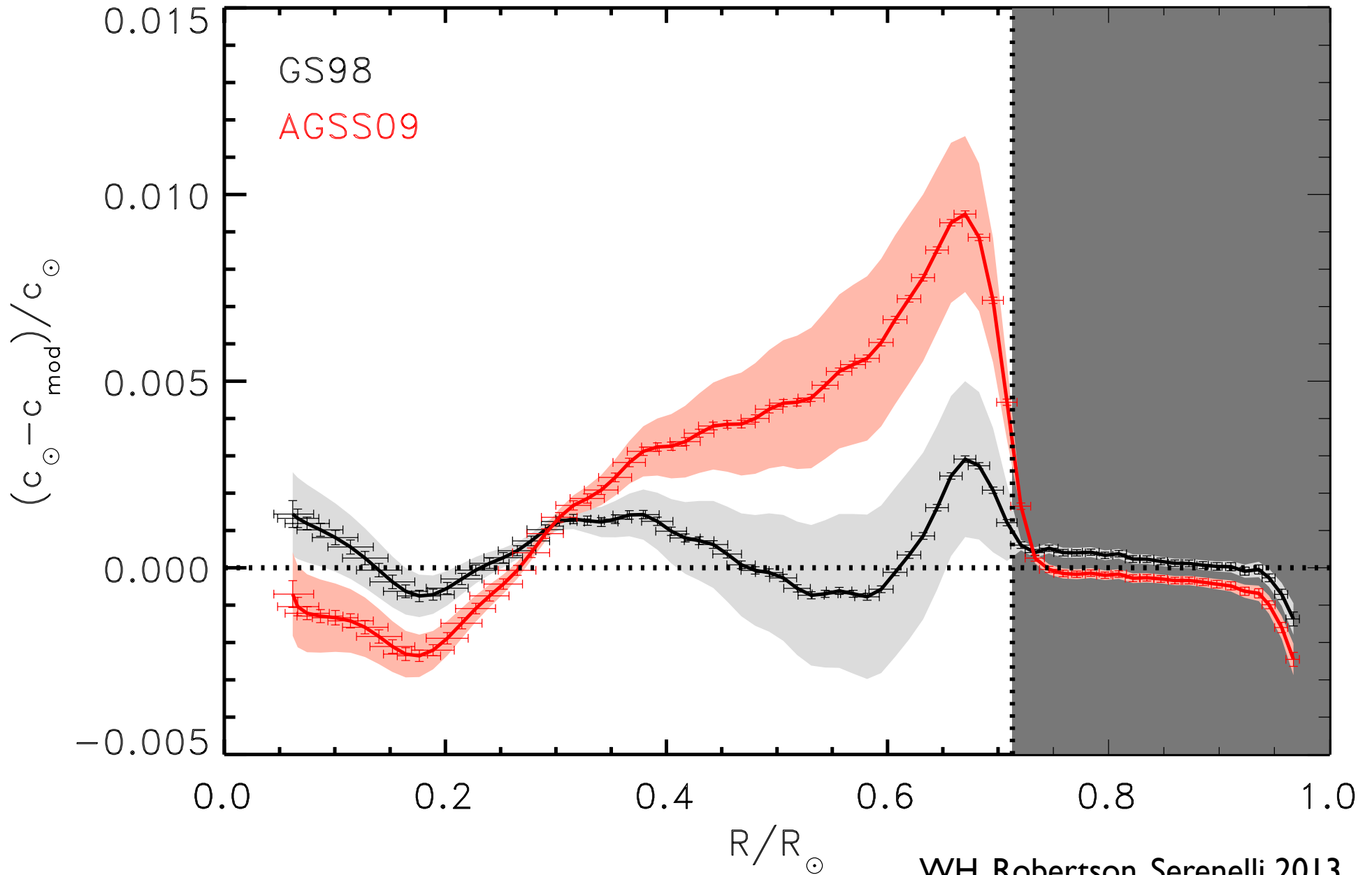


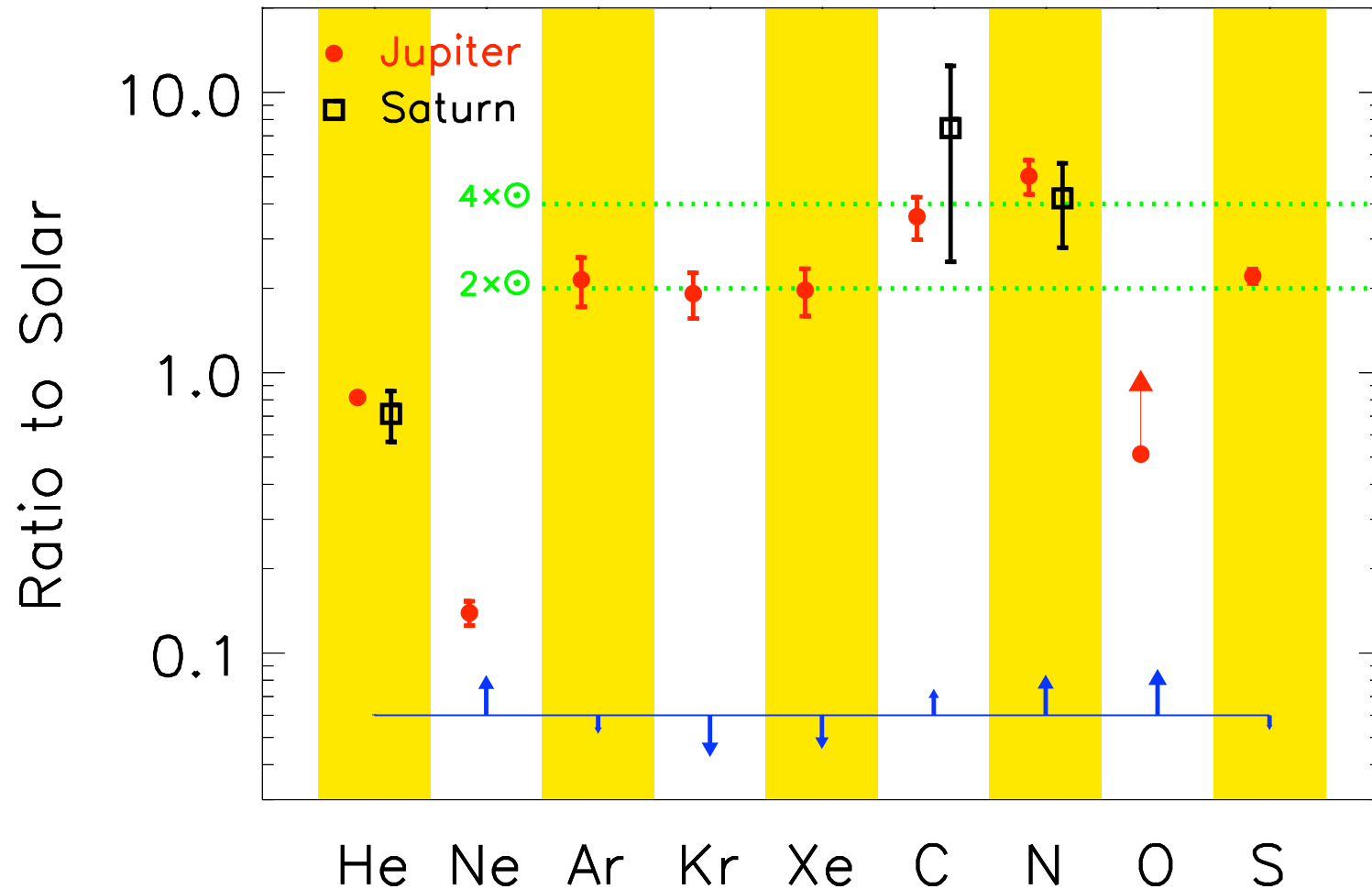
Table 1 Standard solar model characteristics are compared to helioseismic values, as determined by Basu & Antia (1997, 2004)

Property ^a	GS98-SFII	AGSS09-SFII	Solar
$(Z/X)_S$	0.0229	0.0178	–
Z_S	0.0170	0.0134	–
Y_S	0.2429	0.2319	0.2485 ± 0.0035
R_{CZ}/R_\odot	0.7124	0.7231	0.713 ± 0.001
$\langle \delta c/c \rangle$	0.0009	0.0037	0.0
Z_C	0.0200	0.0159	–
Y_C	0.6333	0.6222	–
Z_{ini}	0.0187	0.0149	–
Y_{ini}	0.2724	0.2620	–

Solar abundance problem: A disagreement between SSMs that are optimized to agree with interior properties deduced from our best analyses of helioseismology (high Z), and those optimized to agree with surface properties deduced from the most complete 3D analyses of photoabsorption lines (low Z).

Difference is $\sim 40 M_{\oplus}$ of metal, when integrated over the Sun's convective zone (which contains about 2.6% of the Sun's mass)

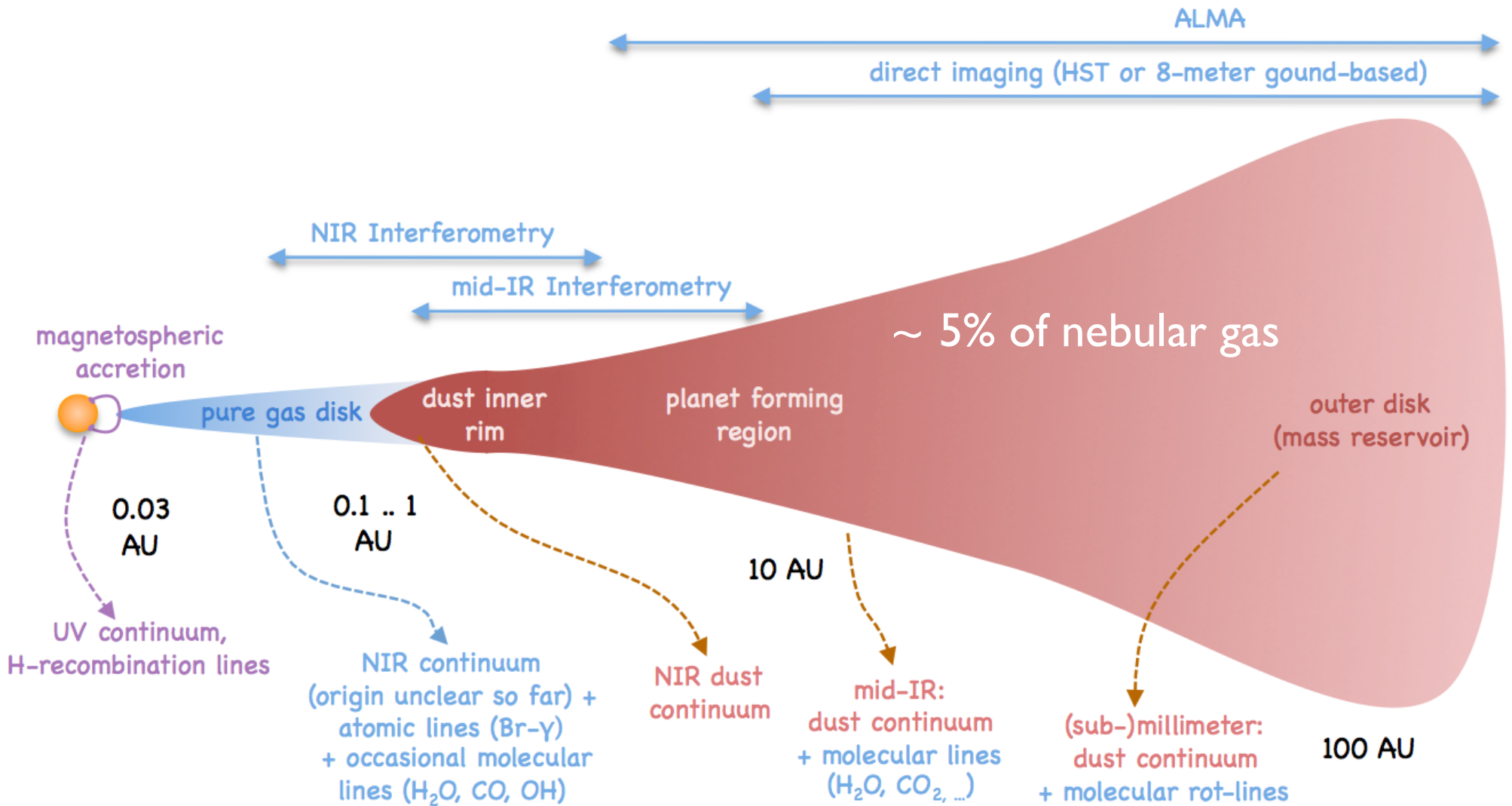
Did the Sun form from a homogeneous gas cloud?



Galileo data, from Guillot AREPS 2005

Standard interpretation: late-stage planetary formation in a chemically evolved disk over ~ 1 m.y. time scale

Contemporary picture of metal segregation, accretion



This (removal of ice, dust) from gas stream could alter Sun if

- ❑ processed gas - from which the elements we see concentrated in Jupiter were scrubbed - remains in the solar system, not expelled
- ❑ the Sun had a well-developed radiative core at the time of planetary formation (thus an isolated convective zone)

Numerically the mass of metals extracted by the protoplanetary disk is more than sufficient to account for the needed dilution of the convective zone (40-90 M_{\oplus})

Guzik, vol. 624, ESA (2006) 17

Castro, Vauclair, Richard A&A 463 (2007) 755

WH & Serenelli, Ap. J. 687 (2008) 678

Nordlund (2009) arXiv:0908.3479

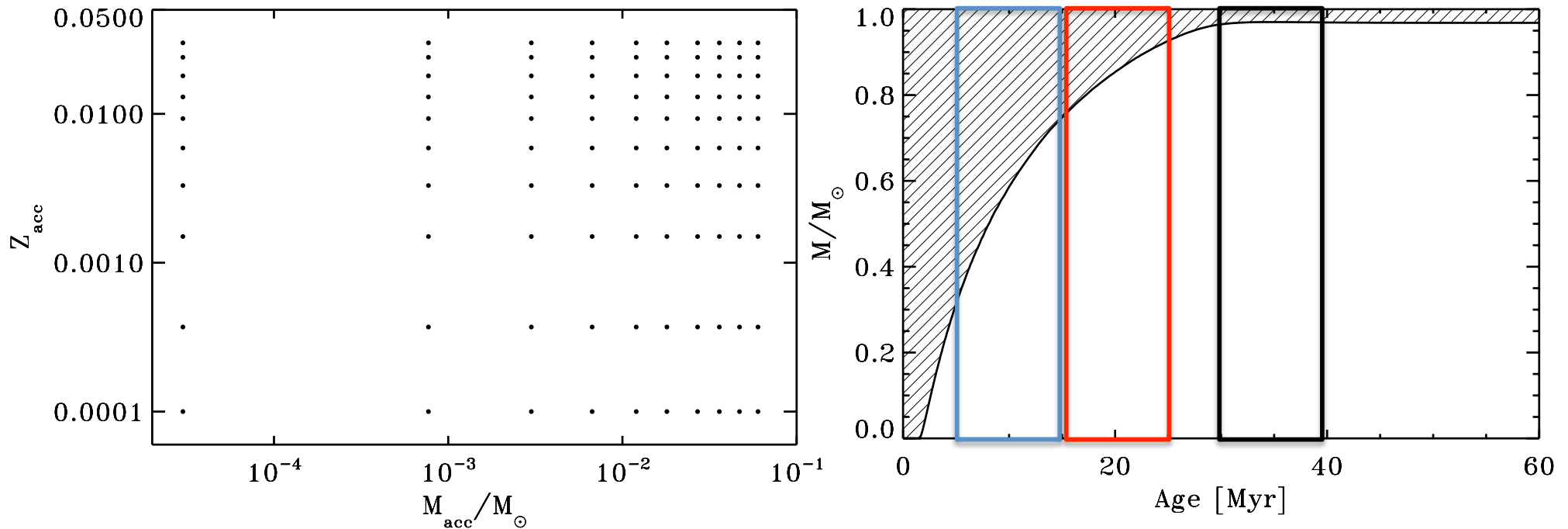
Guzik and Mussack, Ap. J. 713 (2010) 1108

Serenelli, WH, Pena-Garay, Ap. J. 743 (2011) 24

Self-consistent accreting nonstandard SMs

Evolve models with accretion in which the AGSS09 surface composition is taken as a constraint, Z is varied, but H/He is assumed fixed

Serenelli, Haxton, Peña-Garay 2011



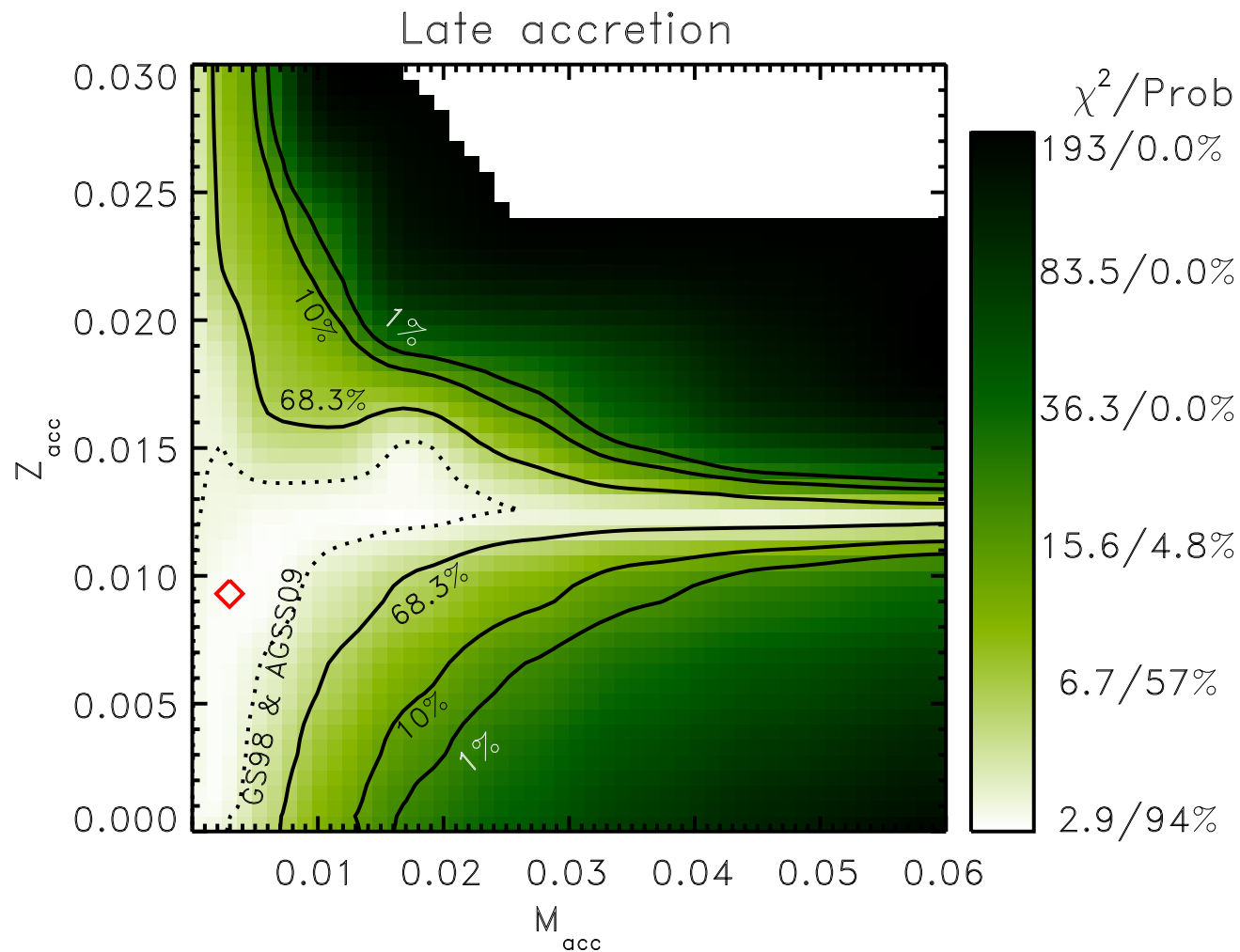
$$M_{\text{accr}} < 0.06 M_{\text{solar}}$$
$$0 < Z_{\text{accr}} < 0.03 (2 Z_{\text{solar}})$$

$$t_{\text{accr}} = 5, 15, 30 \text{ Myr}$$

($M_{\text{conv}}(t_{\text{accr}})$ determines dilution)

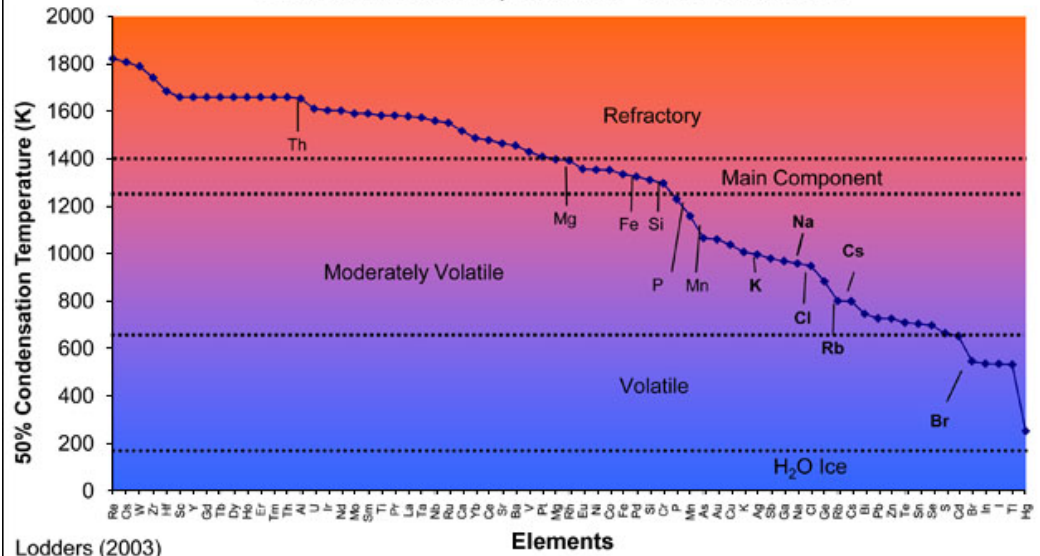
$$\Delta t_{\text{accr}} < 10 \text{ Myr}$$

neutrino constraints



For measured neutrino fluxes restrict accretion scenarios largely to those with modest masses of low- Z material

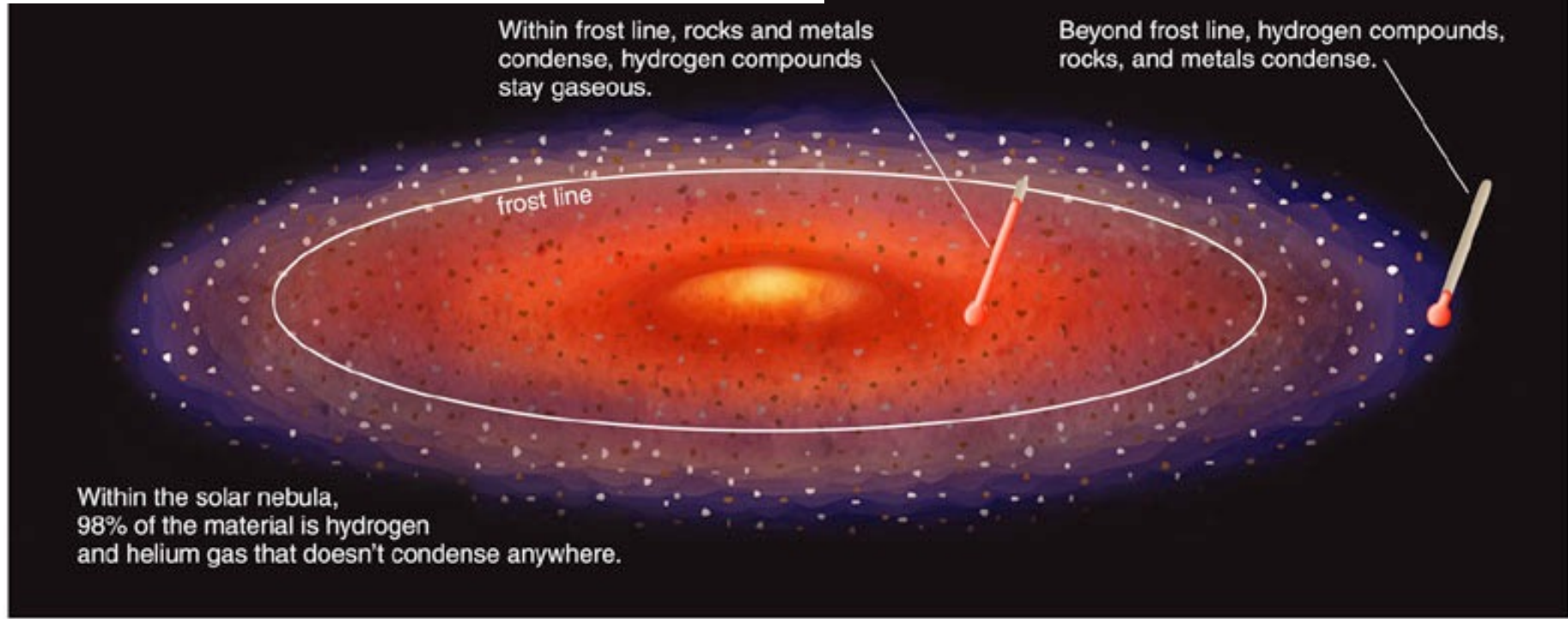
Condensation Temperatures of the Elements



Lodders (2003)
(PSRD graphic based on calculations done by Katarina Lodders, Washington University in St. Louis.)

modeling done to date is somewhat naive:
expect in condensation,
refractory > volatile > He

refractory elements condense



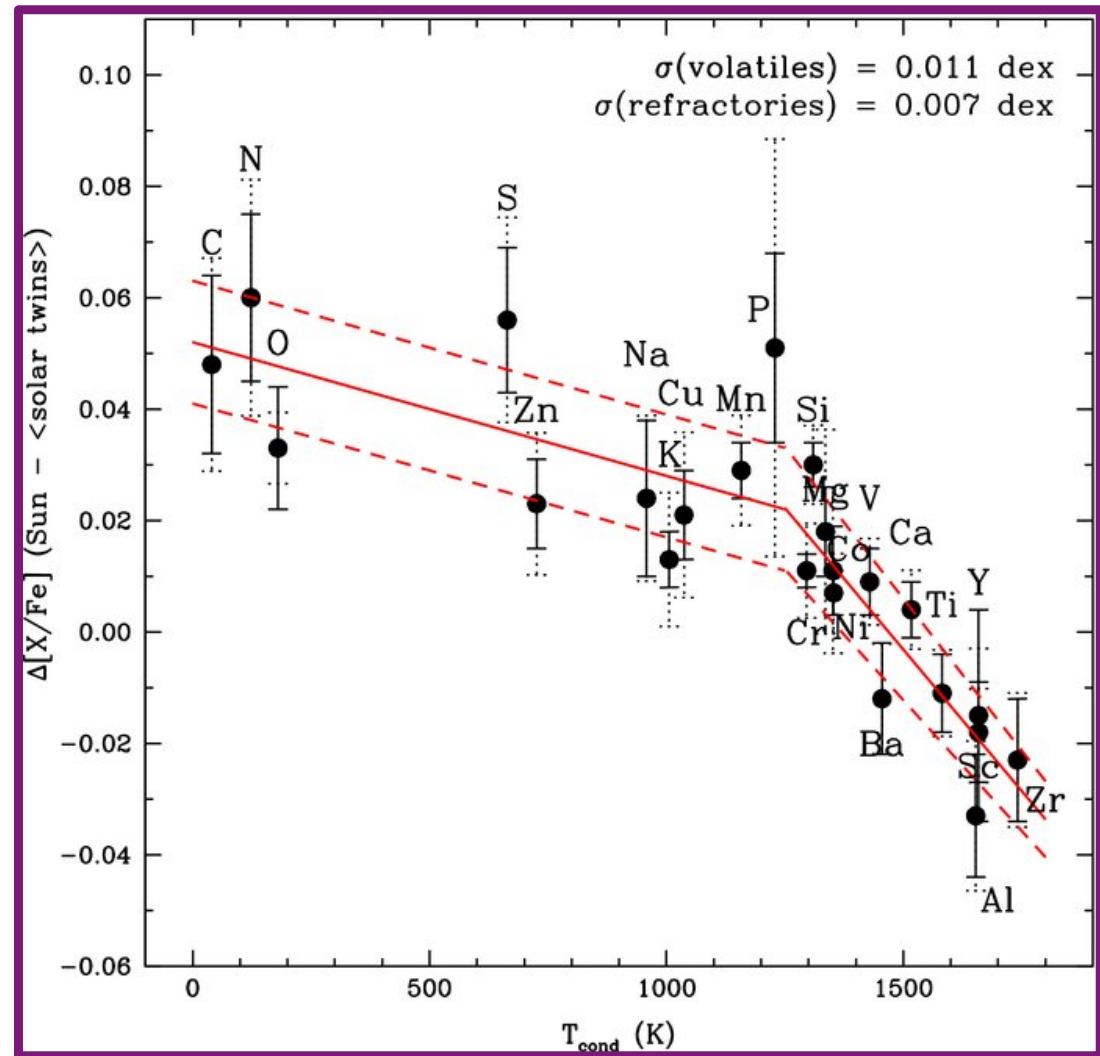
H₂O condenses

Abundances in solar twins

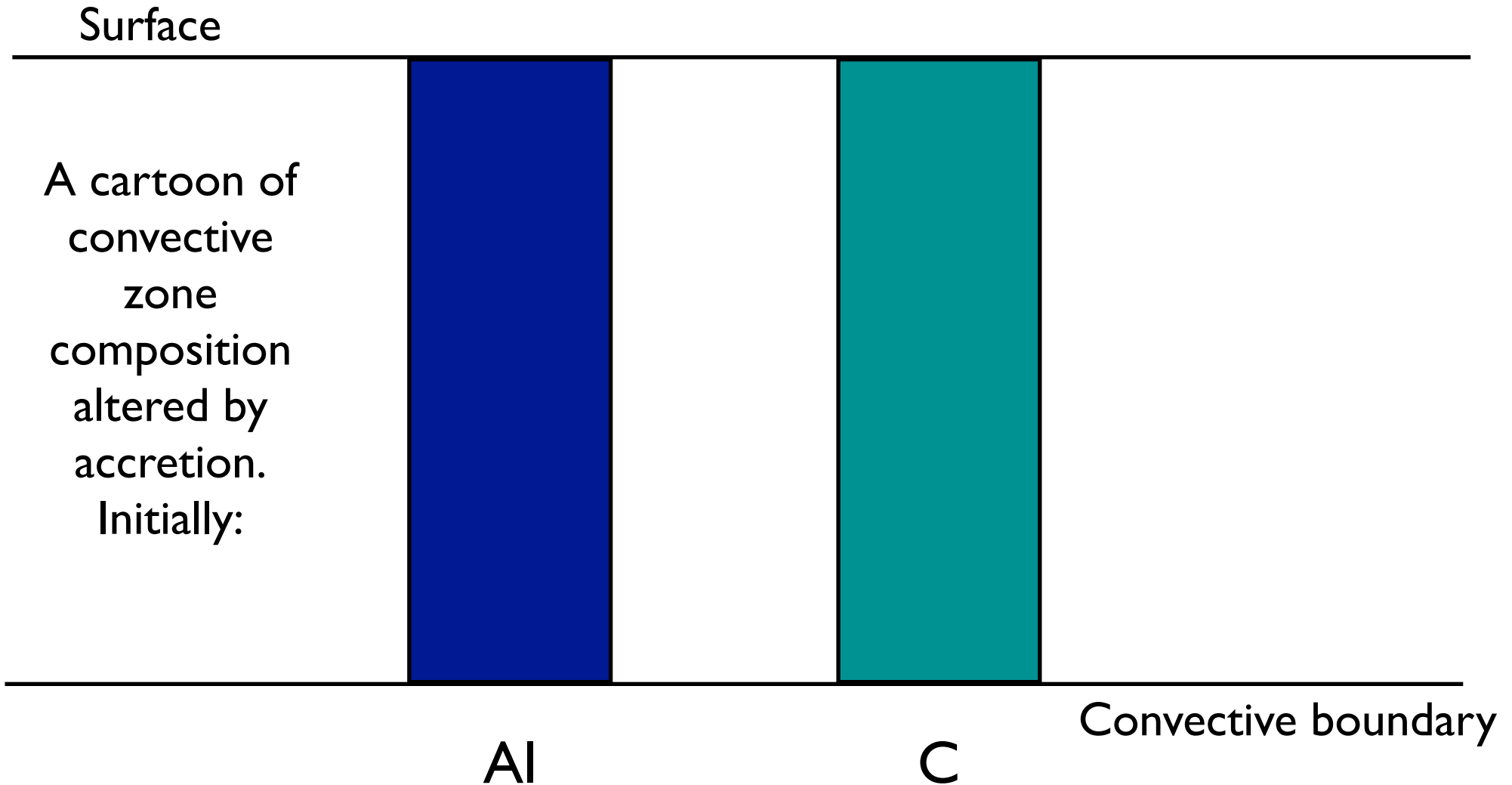
- Differential measurements of abundances in “solar twins” lacking Jupiters:
Melendez et al. 2009
Ramirez et al. 2010
- Claim: solar ratio of volatiles/refractories is higher than twin ratio by 0.05-0.10 dex
- Suggestive of disk chemistry; consistent with accretion where

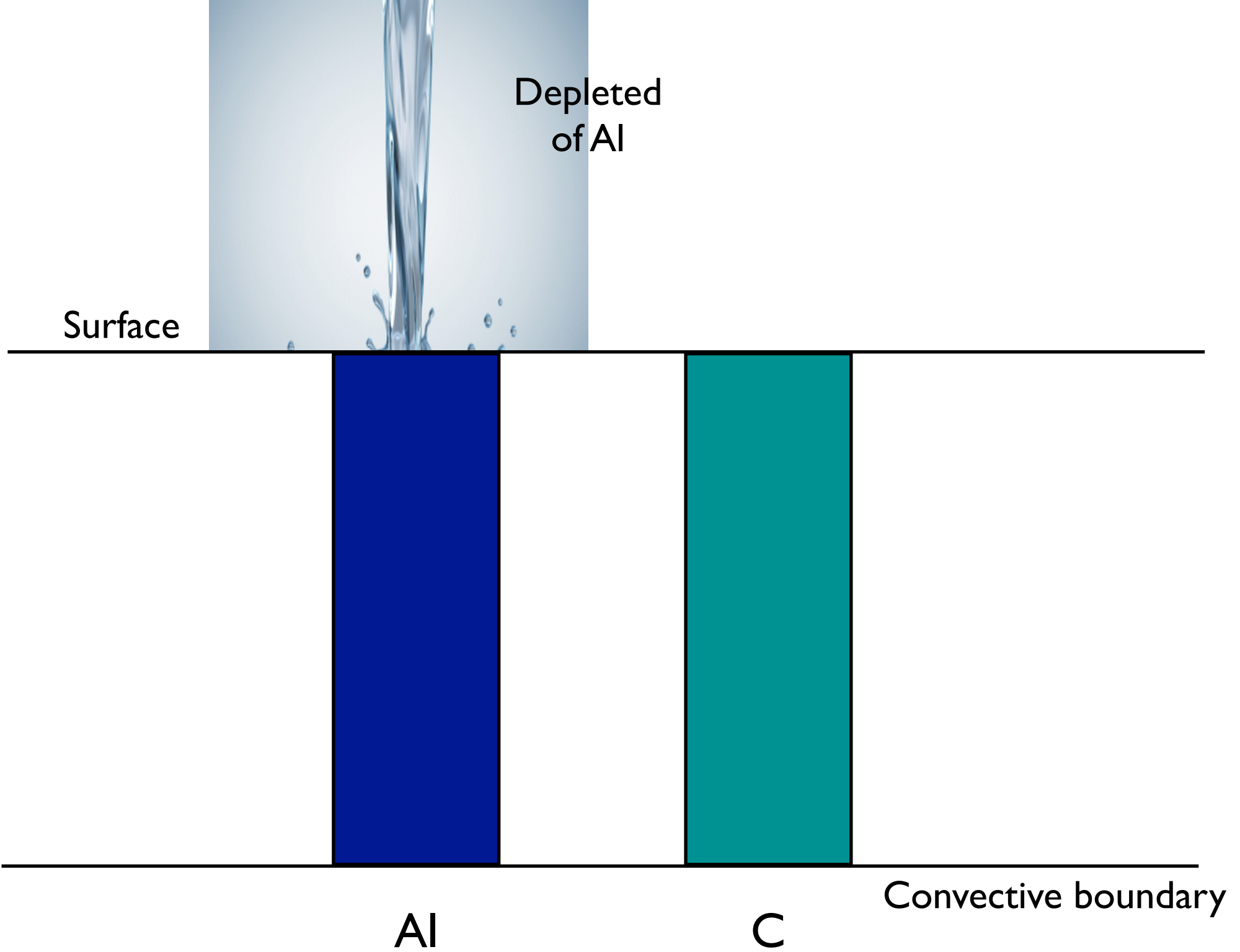
$$\tau_{\text{Al,Zr}}^{\text{freezeout}} < \tau_{\text{Fe}}^{\text{freezeout}} < \tau_{\text{CNP}}^{\text{freezeout}}$$

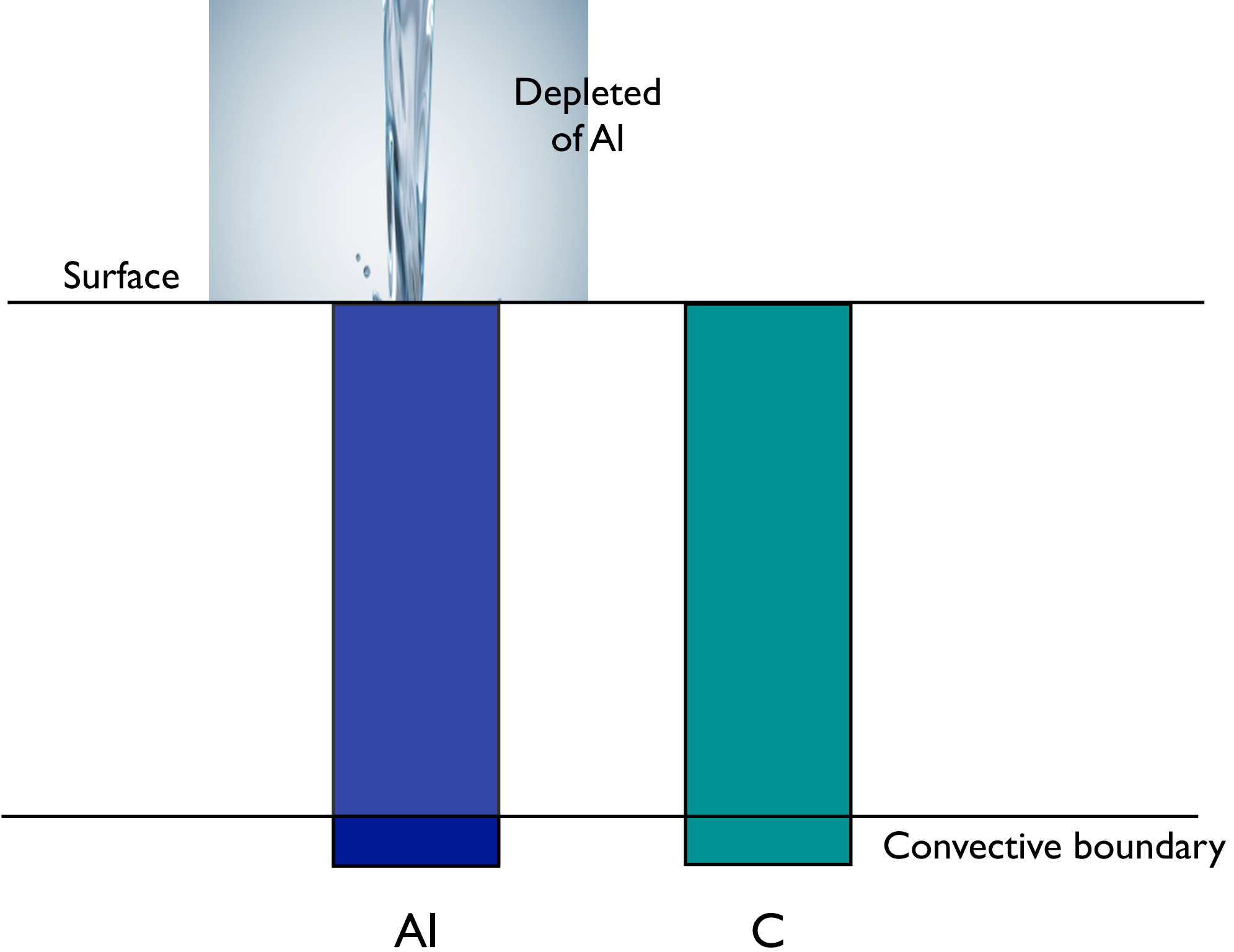
- Measurements at the limit of feasibility: debated...

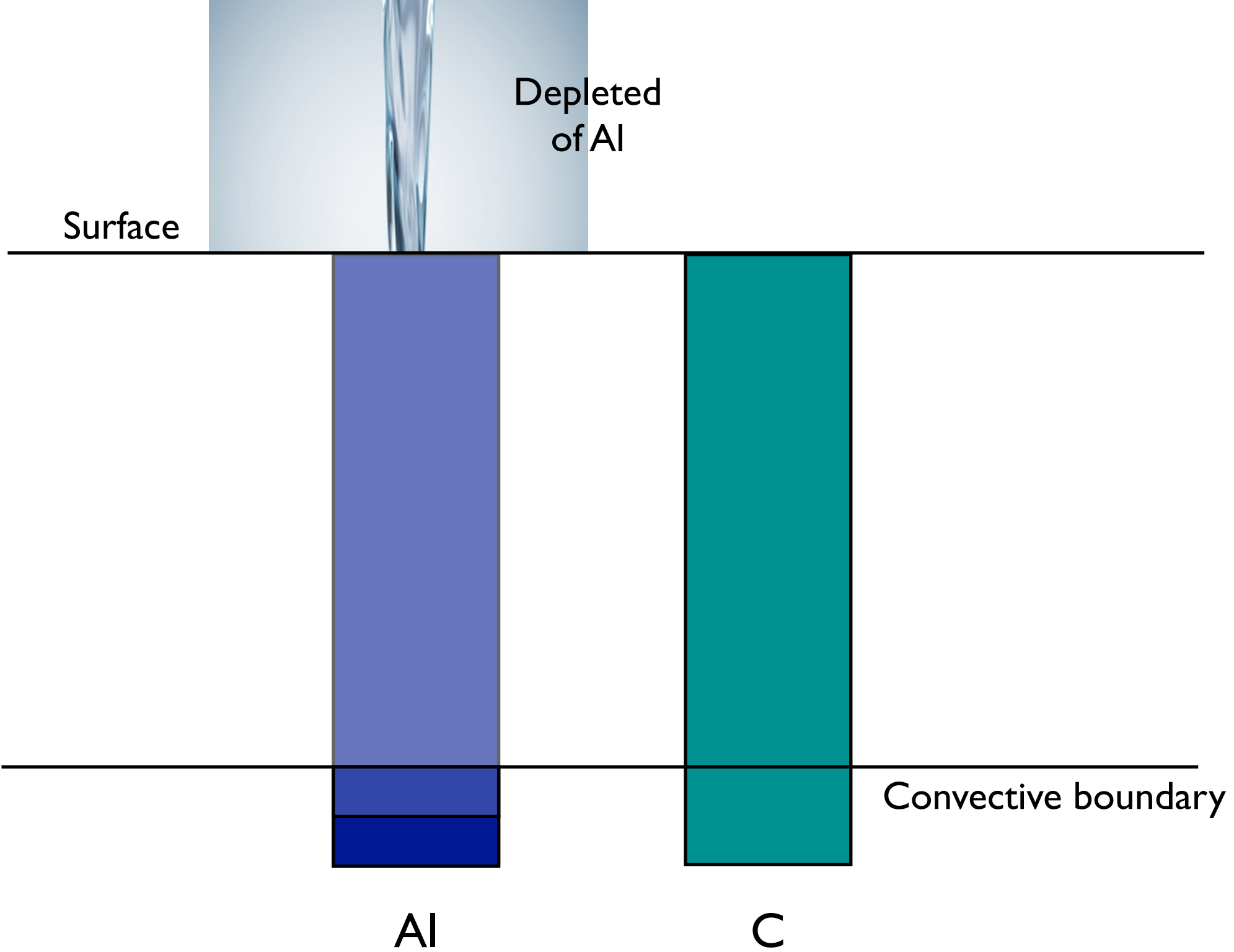


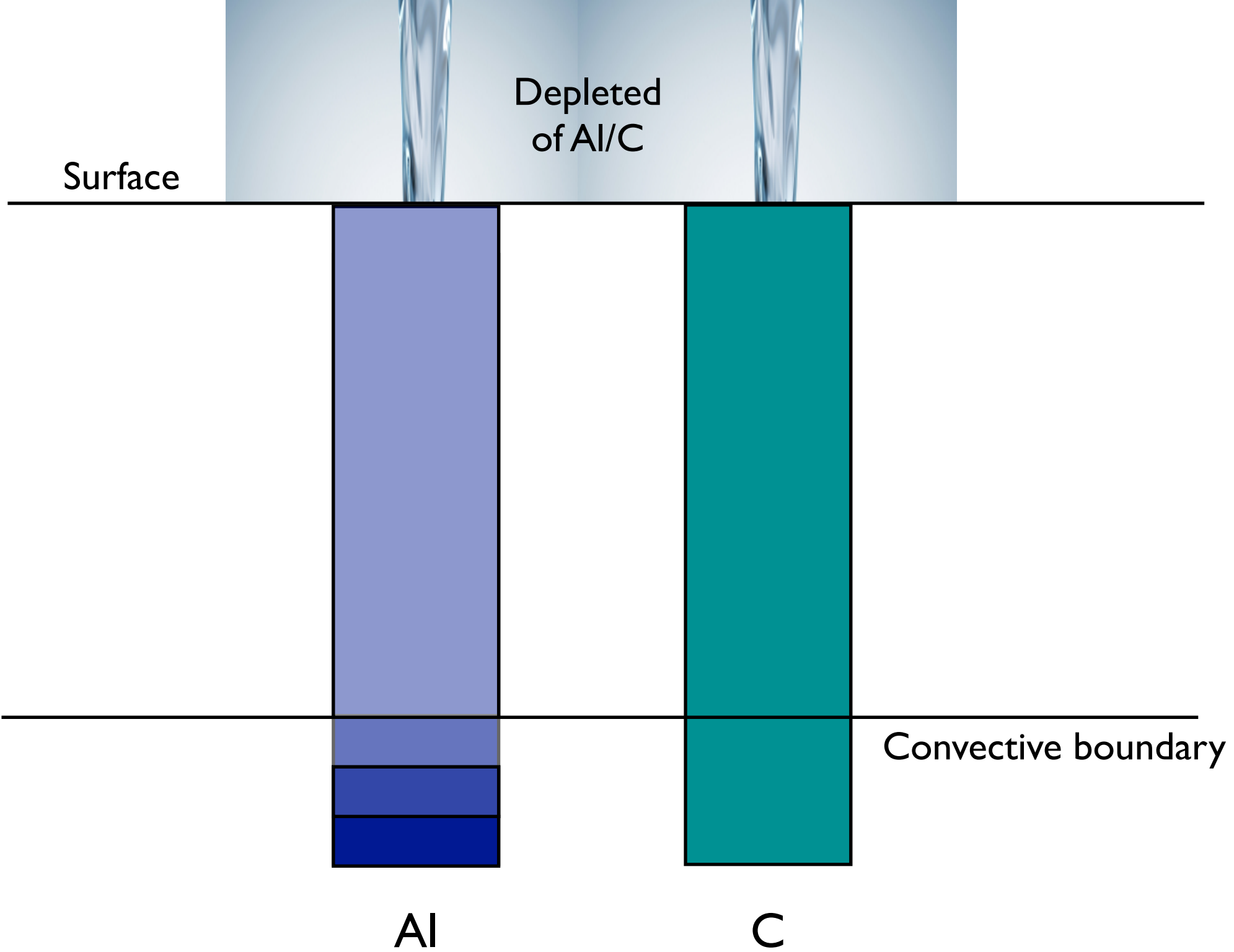
This is in accord with expectations ...

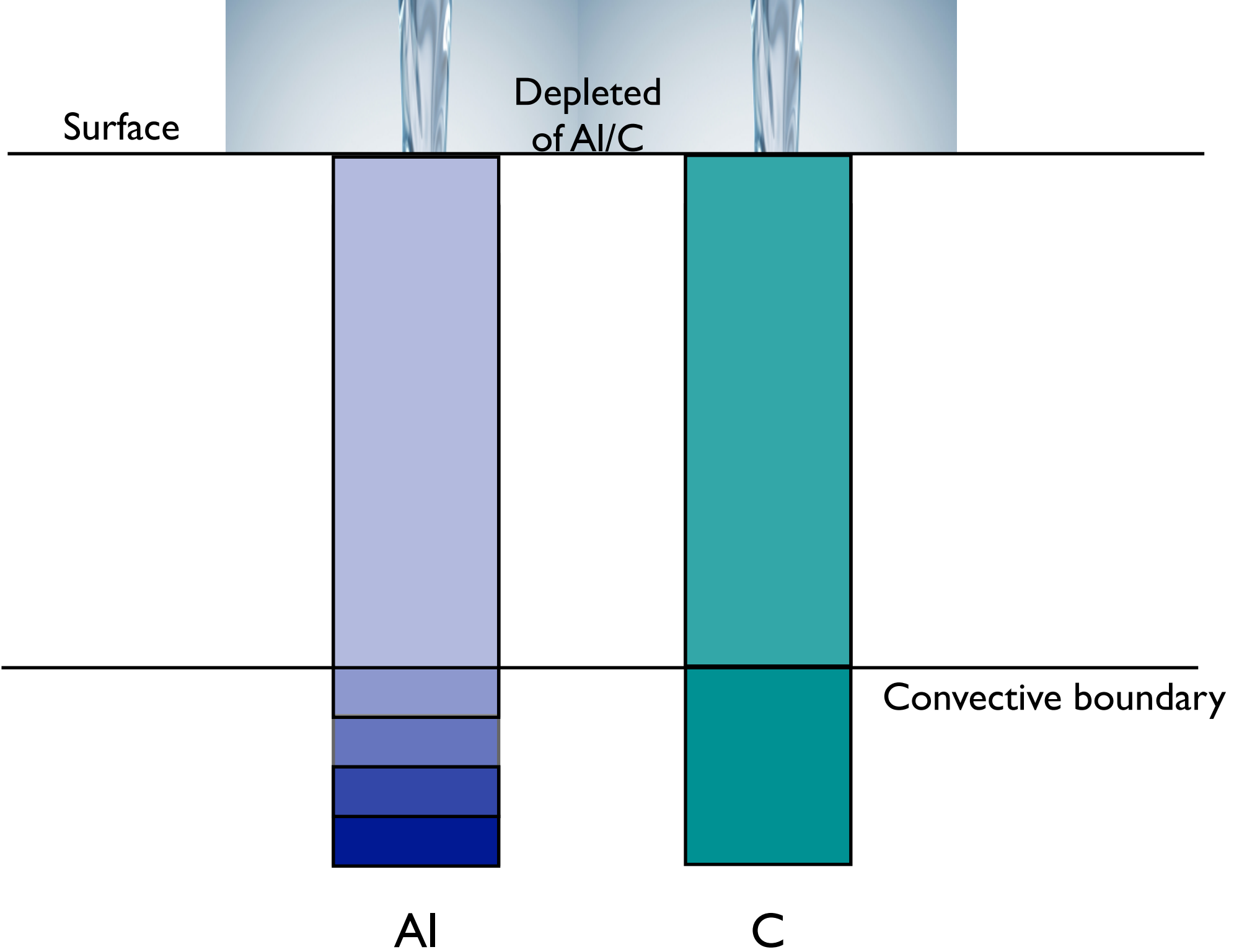






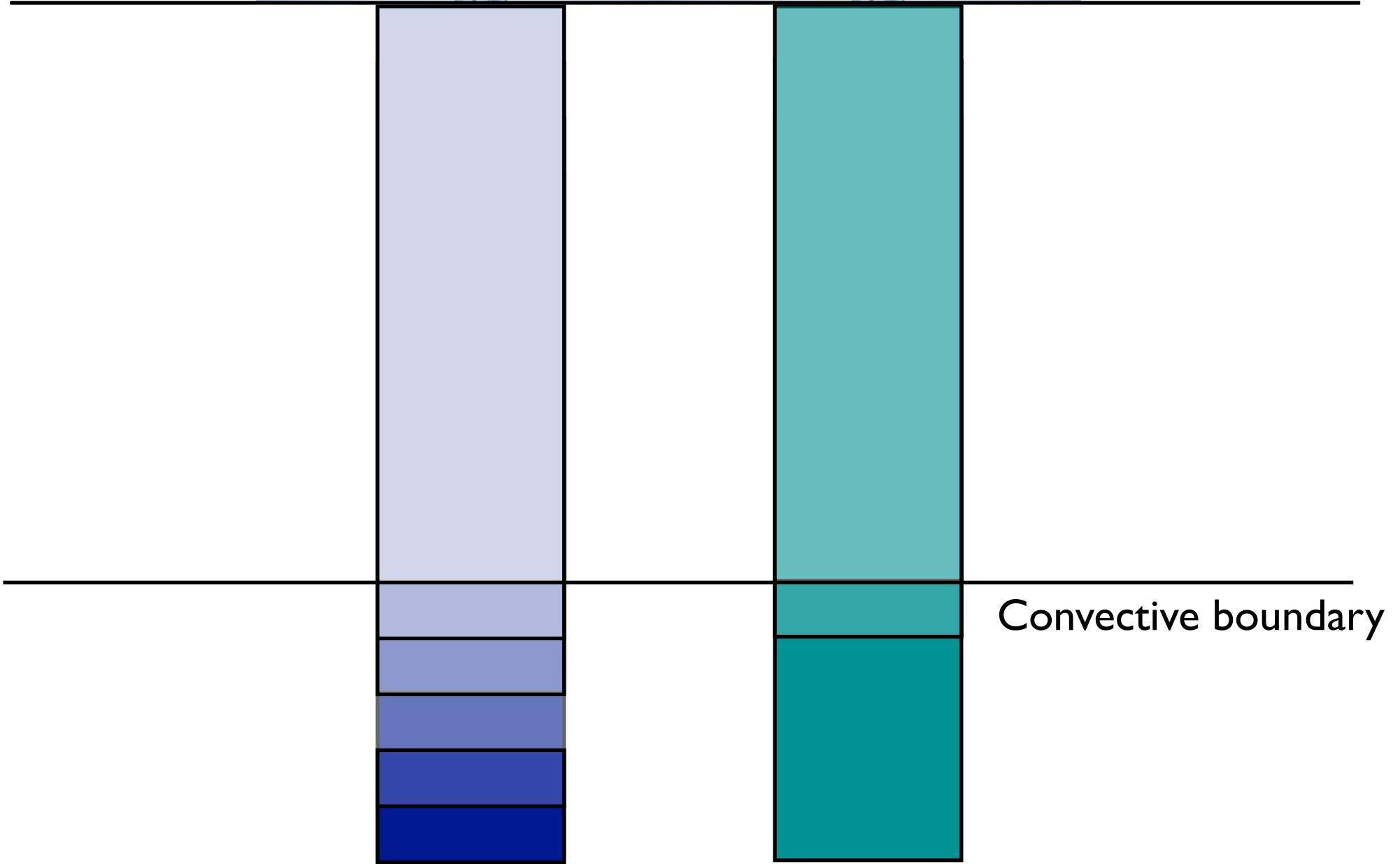






Surface

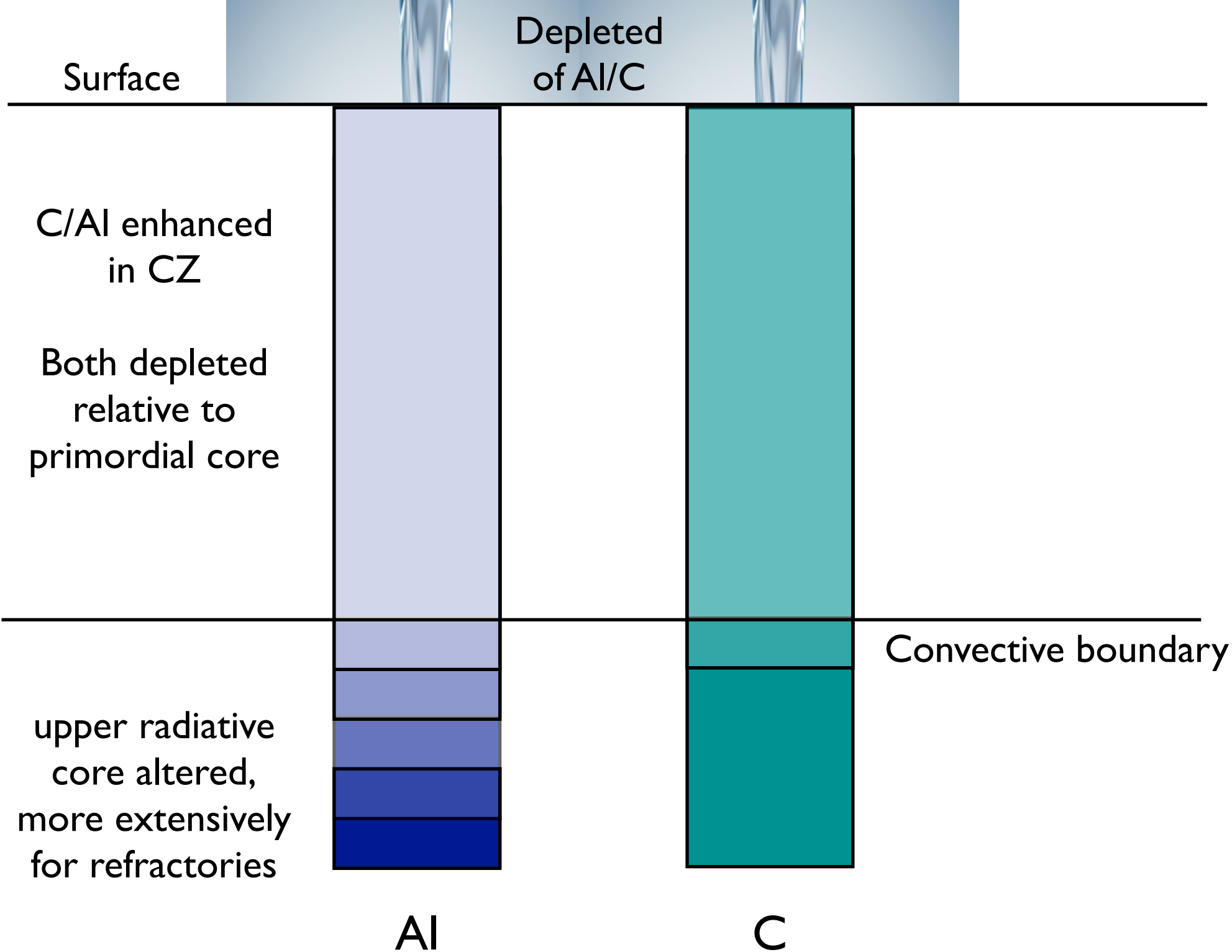
Depleted
of Al/C



Al

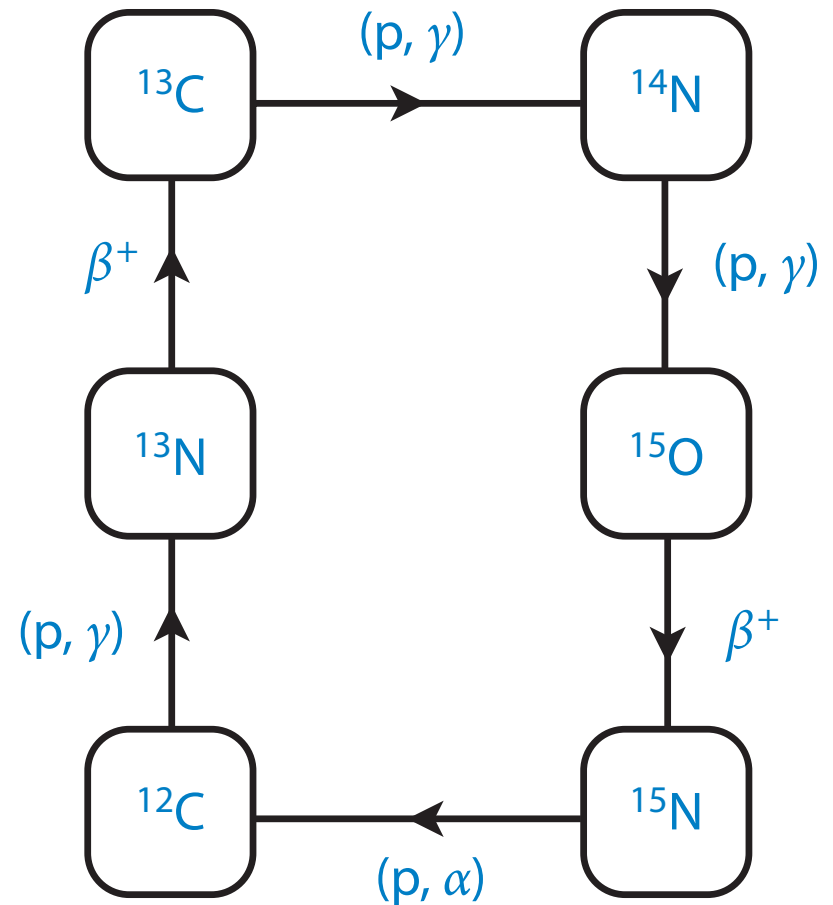
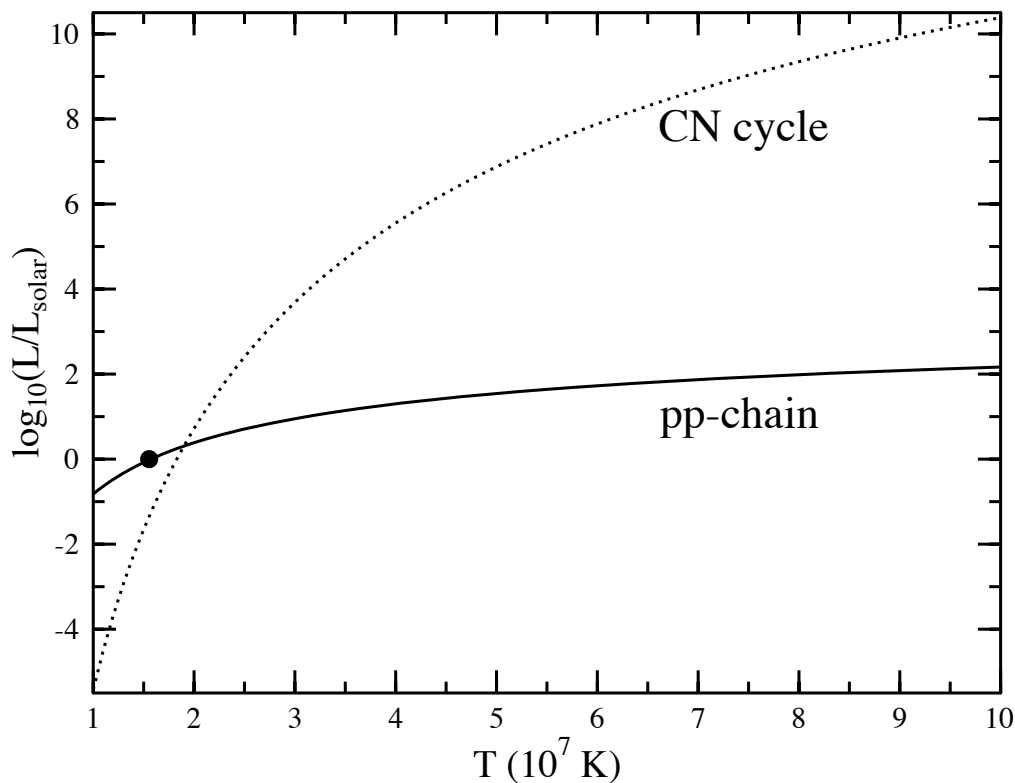
C

Convective boundary



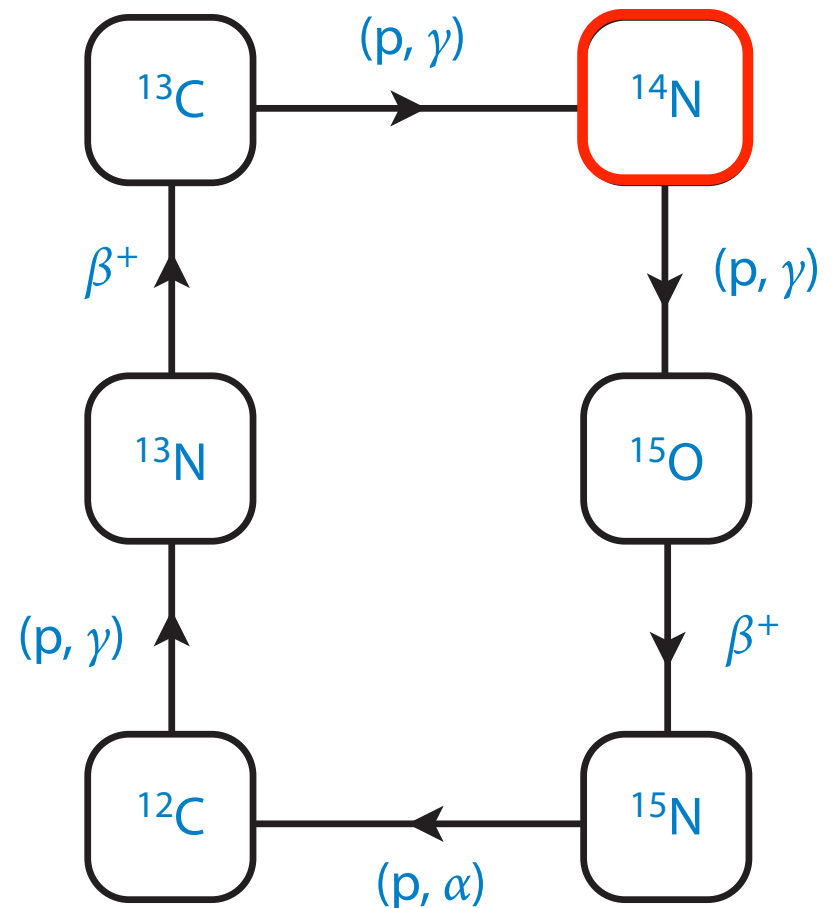
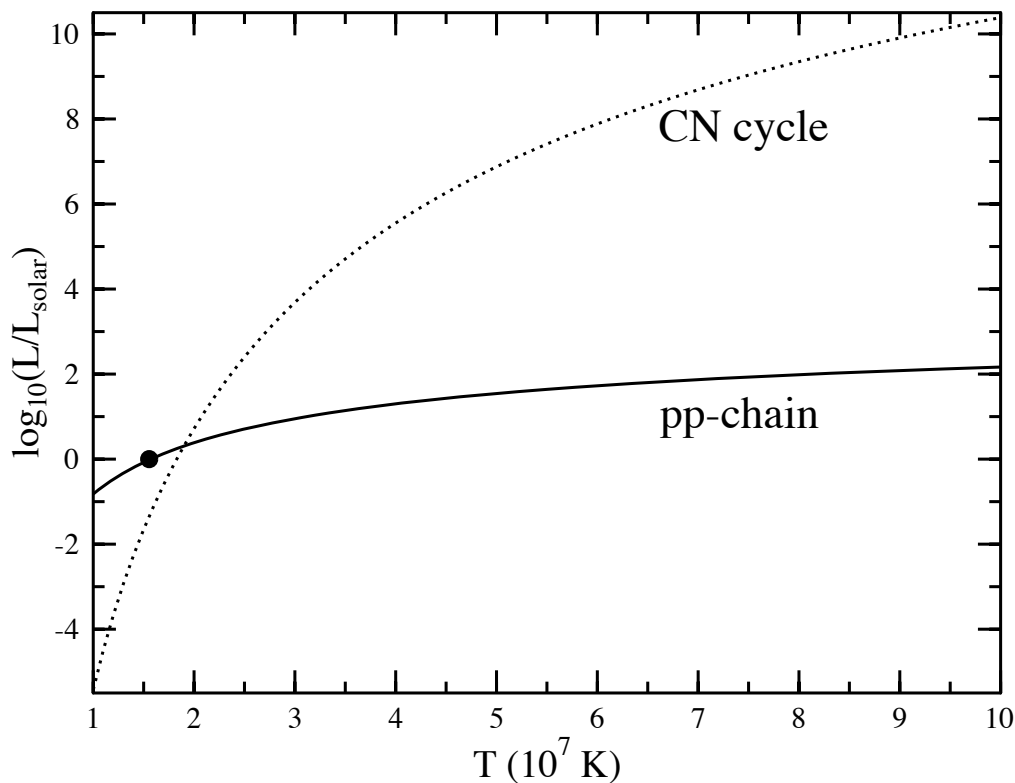
Using Vs to Probe Solar Core Composition Directly

- pp chain (primary) vs CN cycle (secondary): catalysts for CN cycle are pre-existing metals (except in the case of the first stars)



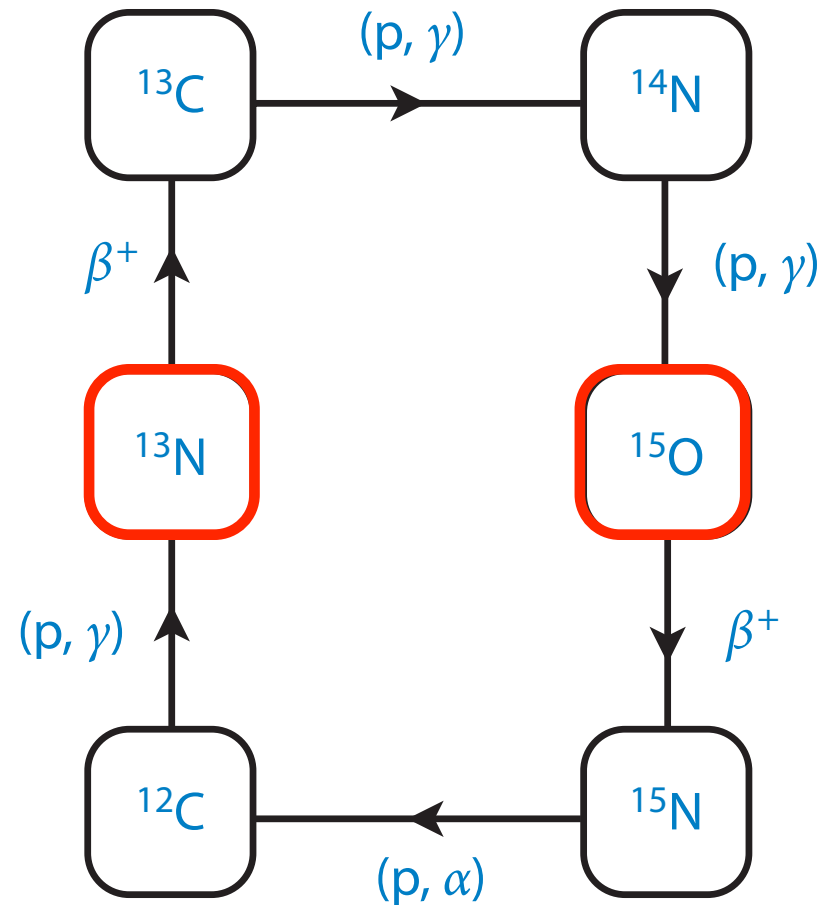
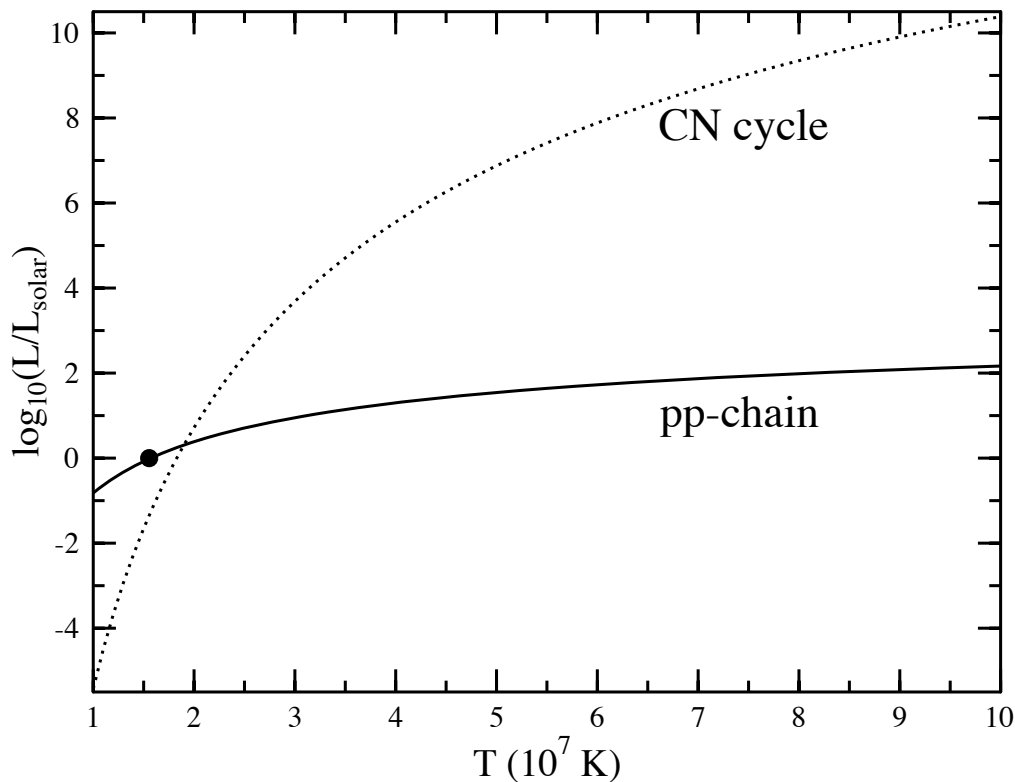
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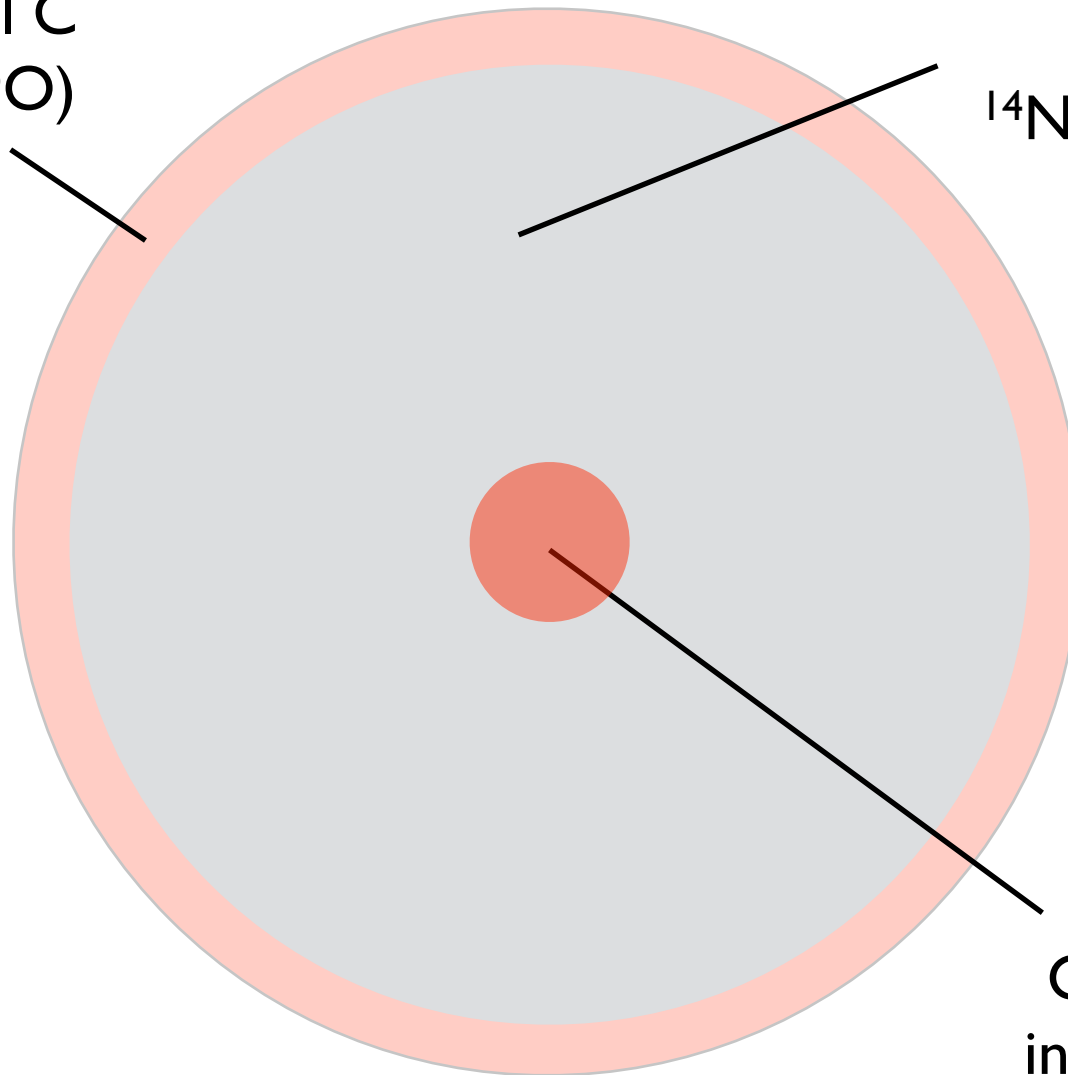
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present day burning
of primordial C
 $v(^{13}\text{N}) - v(^{15}\text{O})$

primordial C
burned:
 $^{14}\text{N}(p, \gamma)$ bottleneck



solar core

CN burning
in equilibrium
@ $T_7 \sim 1.5$
 $v(^{13}\text{N}) + v(^{15}\text{O})$

☐ measurable neutrino fluxes

$${}^{13}\text{N}(\beta^+){}^{13}\text{C} \quad E_\nu \lesssim 1.199 \text{ MeV} \quad \phi = (2.93_{-0.82}^{+0.91}) \times 10^8 / \text{cm}^2 \text{ s}$$

$${}^{15}\text{O}(\beta^+){}^{15}\text{N} \quad E_\nu \lesssim 1.732 \text{ MeV} \quad \phi = (2.20_{-0.63}^{+0.73}) \times 10^8 / \text{cm}^2 \text{ s}.$$

- ☐ these fluxes depend on the core temperature T (metal-dependent) but also have **an additional linear dependence** on the total core C+N
- ☐ absolute fluxes are uncertain, sensitive to small changes in many solar model uncertainties other than total metallicity
- ☐ but an appropriate ratio of the CN and ${}^8\text{B}$ ν flux is independent of these other uncertainties: the measured ${}^8\text{B}$ ν flux can be exploited as a solar thermometer

the bottom line

$$\frac{\phi(^{15}\text{O})}{\phi(^{15}\text{O})^{\text{SSM}}} = \left[\frac{\phi(^8\text{B})}{\phi(^8\text{B})^{\text{SSM}}} \right]^{0.729} x_{C+N}$$

$$\times [1 \pm 0.006(\text{solar}) \pm 0.027(\text{D}) \pm 0.099(\text{nucl}) \pm 0.032(\theta_{12})]$$


measured to 2% by SuperKamiokande
(the solar thermometer)



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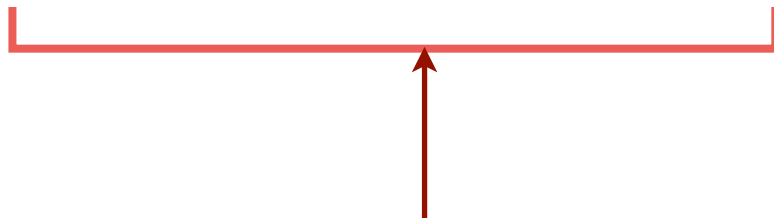
what we want to know: the primordial
core abundance of C + N (in units of SSM
best value)

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the entire solar model dependence: luminosity, metallicity, solar age, etc., eliminated -- except for small residual differential effects of heavy element diffusion (necessary to relate today's neutrino measurements to core abundance 4.7 b.y. ago)

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we have some work to do here: $^7\text{Be}(p, \gamma)$, $^{14}\text{N}(p, \gamma)$


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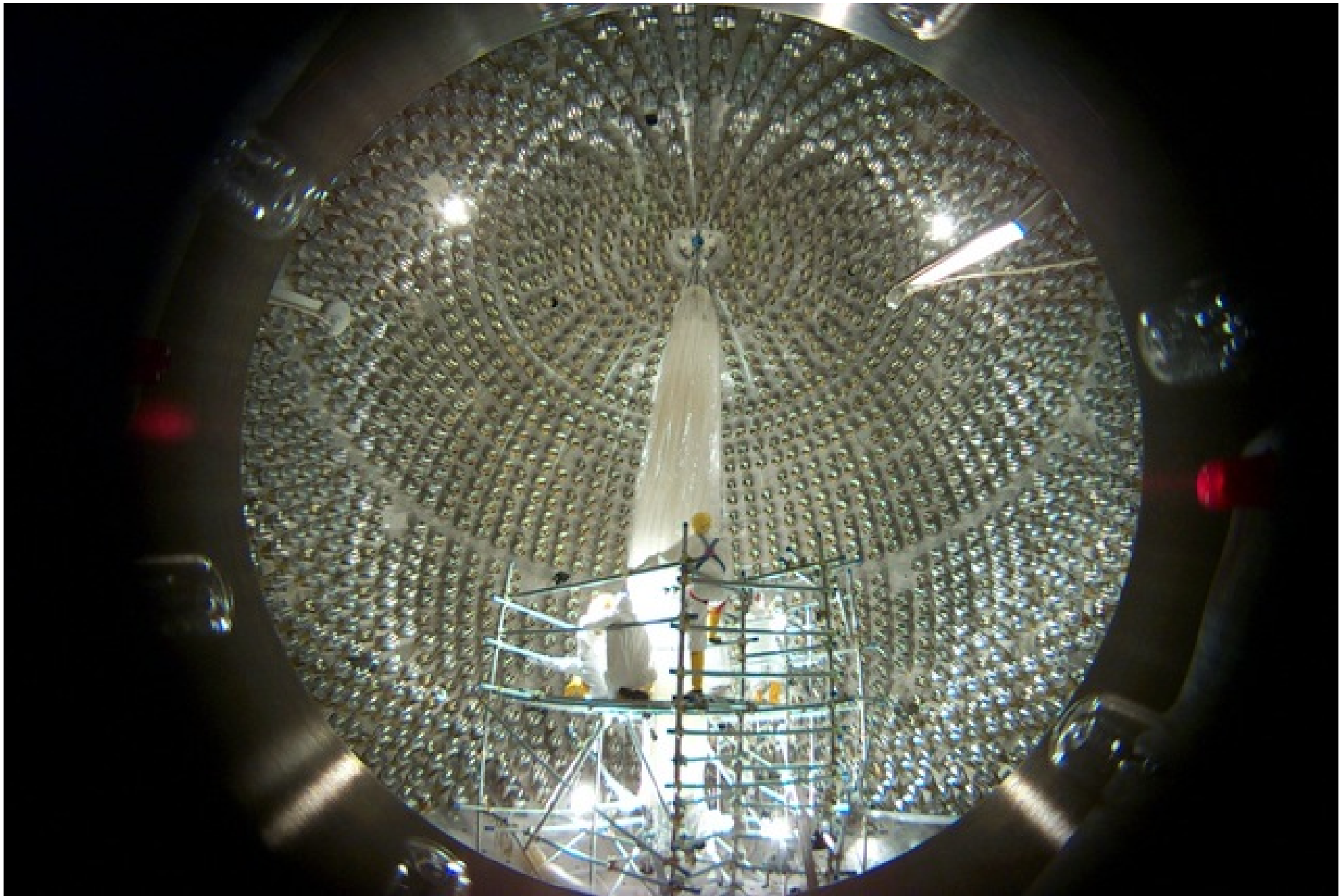


**SNO's marvelous measurement
of the weak mixing angle**

a future neutrino measurement: Borexino, SNO+, JinPing...?


$$\frac{\phi(^{15}\text{O})}{\phi(^{15}\text{O})^{\text{SSM}}} = \left[\frac{\phi(^8\text{B})}{\phi(^8\text{B})^{\text{SSM}}} \right]^{0.729} x_{C+N}$$

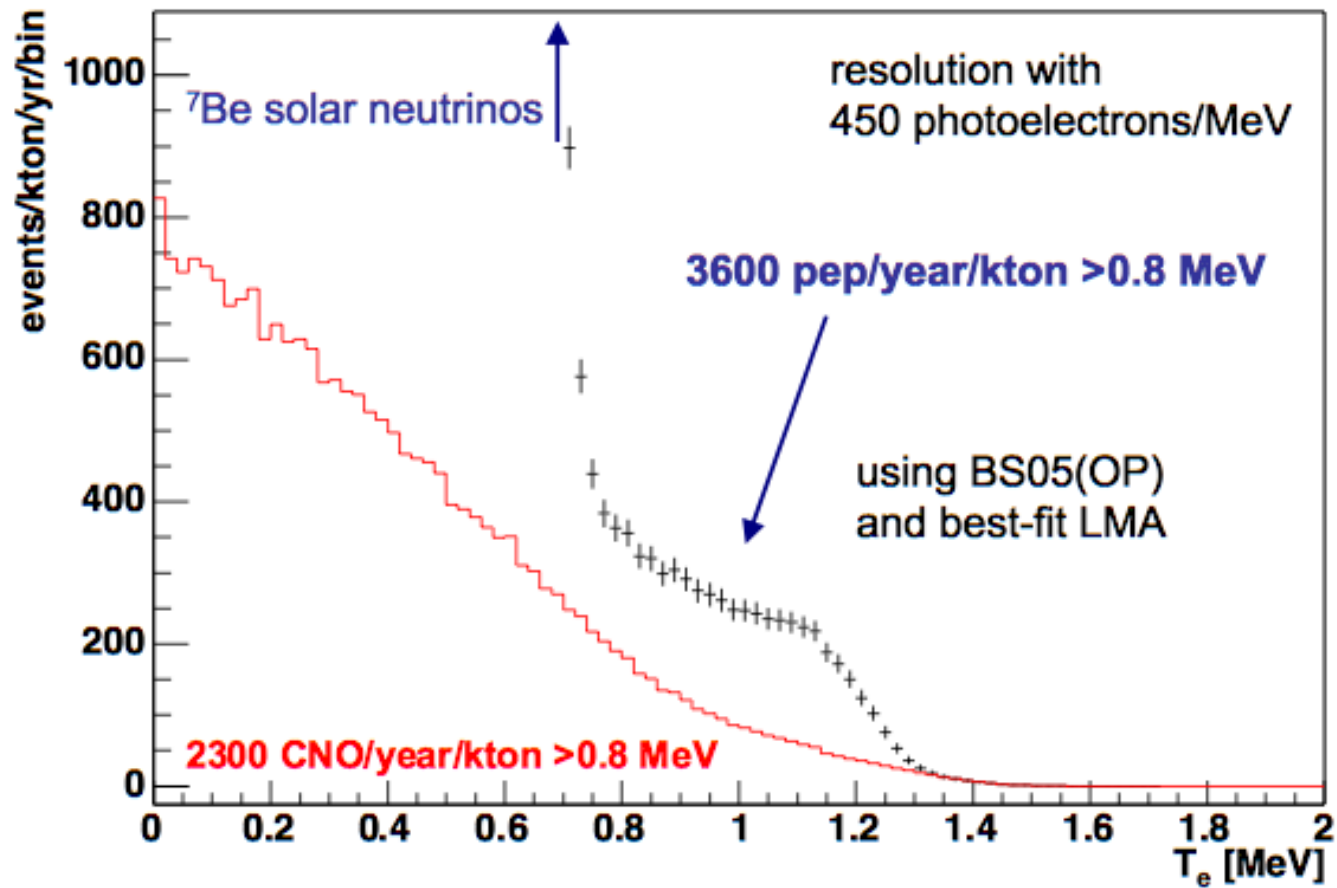
$$\times [1 \pm 0.006(\text{solar}) \pm 0.027(\text{D}) \pm 0.099(\text{nucl}) \pm 0.032(\theta_{12})]$$



Both SNO+ and Borexino have considered such a measurement
Depth crucial: SNO+/Borexino ^{11}C ratio is 1/70

an obvious candidate for exploiting JinPing's depth

^7Be , pep and CNO Recoil Electron Spectrum



(from Mark Chen)

this measurement is fundamental

- ❑ probes the primordial gas from which our solar system formed
- ❑ the first opportunity in astrophysics to directly compare surface and deep interior (primordial) compositions
- ❑ could help motivate “standard solar system models” that would link solar ν physics, solar system formation, planetary astrochemistry

summary

1960s

test the solar
model: precise
determination
of core
temperature



1990s

new neutrino
physics:
precise weak
interaction
parameters



2020

CN vs,
primordial
metallicity,
solar system
formation

Now that we have eliminated the weak interaction uncertainties that held us back for many years, we can finally use solar neutrinos as a precise probe of solar physics