

# MEASURING LOCAL SHEAR VISCOSITY IN FERMI GASES



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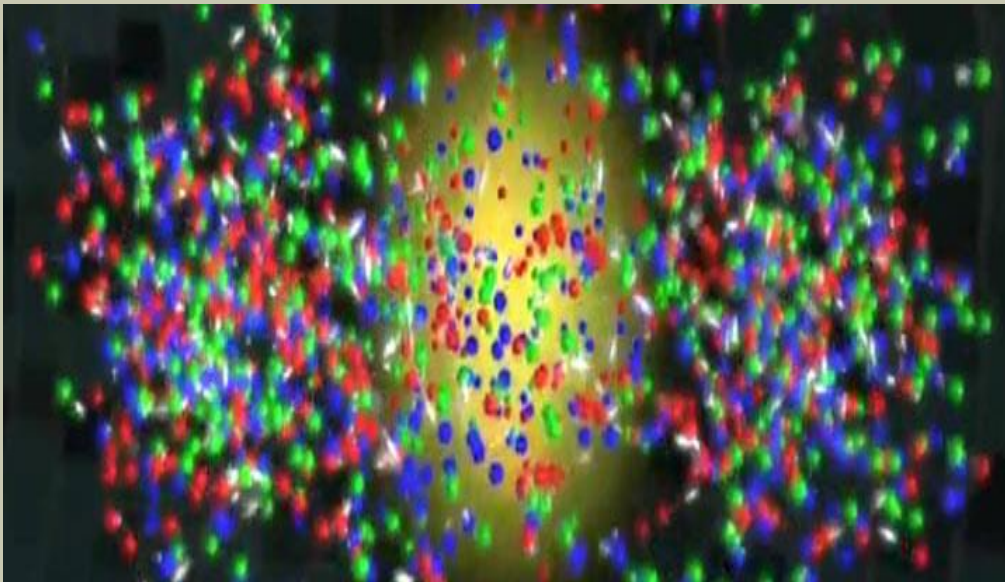
INT workshop  
Frontiers in  
quantum  
simulation with  
cold atoms

University of  
Washington

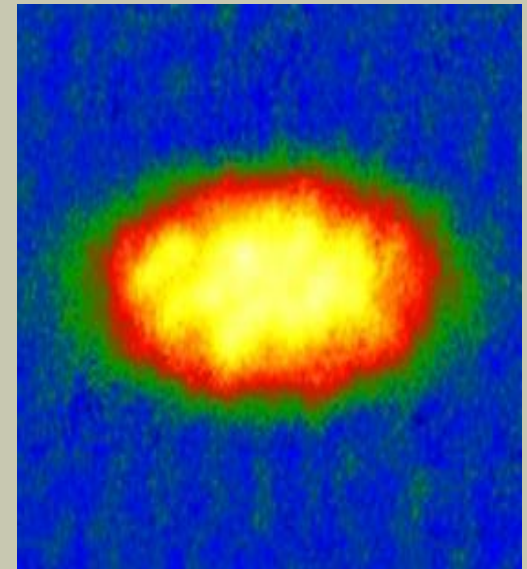
# WHY STUDY SHEAR VISCOSITY IN FERMION GASES?



## Strongly Interacting Hydrodynamic Systems



**Quark Gluon Plasma**



**Ultra-Cold Fermi Gas**

# OUTLINE

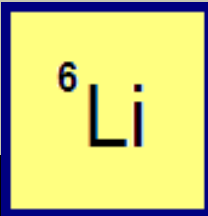


- **Creating a fluid out of a gas**
  - Optically trapped strongly interacting Fermi gas
- **Transport Measurements**
  - Measuring *cloud averaged* shear viscosity in expanding Fermi gases
  - Thermometry from the equation of state
- **Iterative Matrix Inversion**
  - Obtaining *local* shear viscosity from cloud averages using *image processing* methods
  - Discovering hidden features in the local shear viscosity and direct comparison to theory

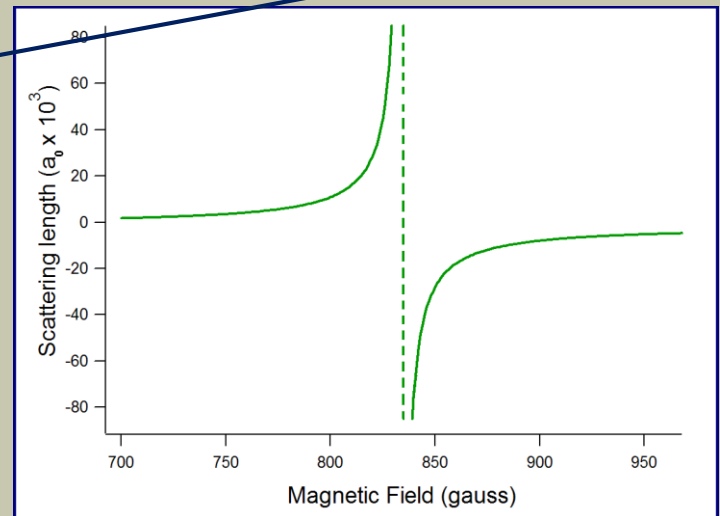
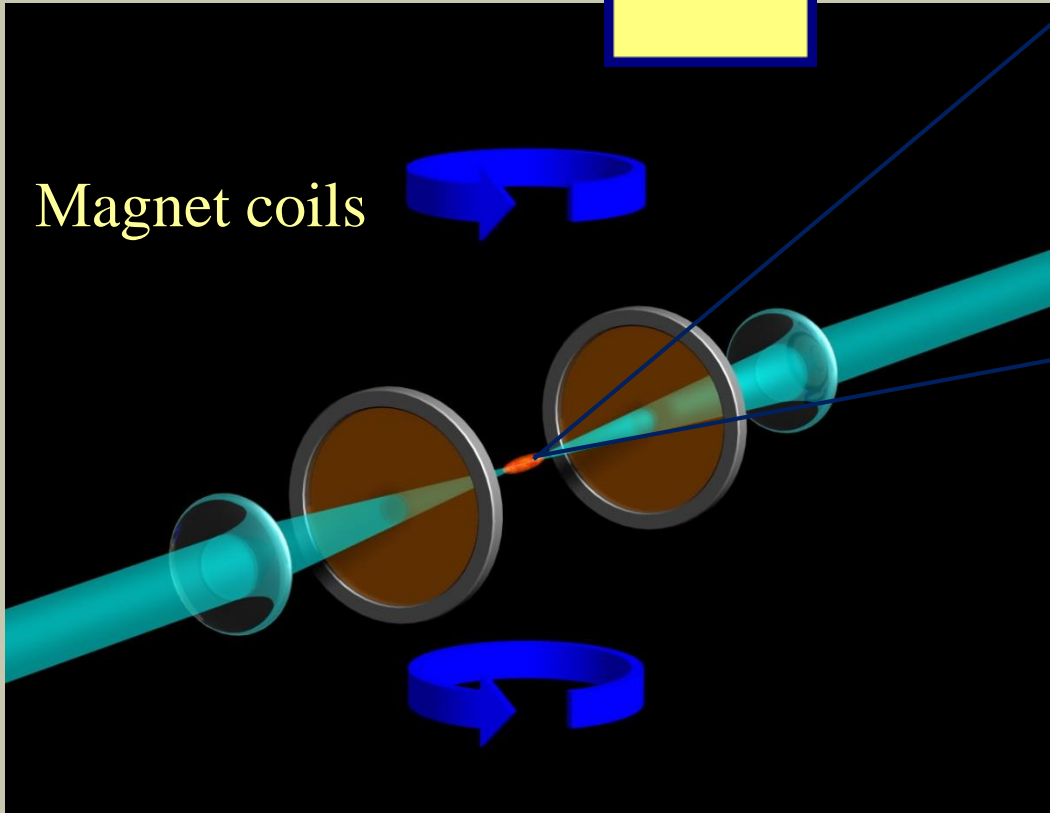
# OPTICALLY TRAPPED FERMI GAS



Our atom: Fermionic



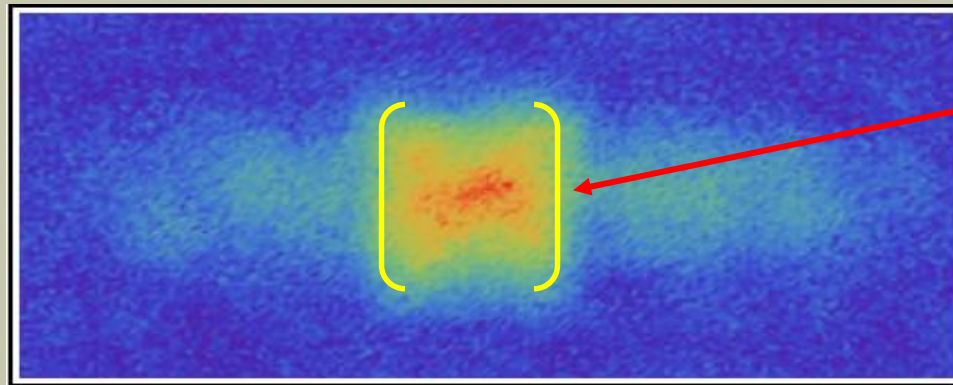
Magnet coils



# STRONG INTERACTIONS: SHOCK WAVES IN FERMI GASES



- Trapped gas is divided into **two** clouds with a repulsive optical potential.
- The repulsive potential is **extinguished**, the two clouds accelerate towards each other and collide.

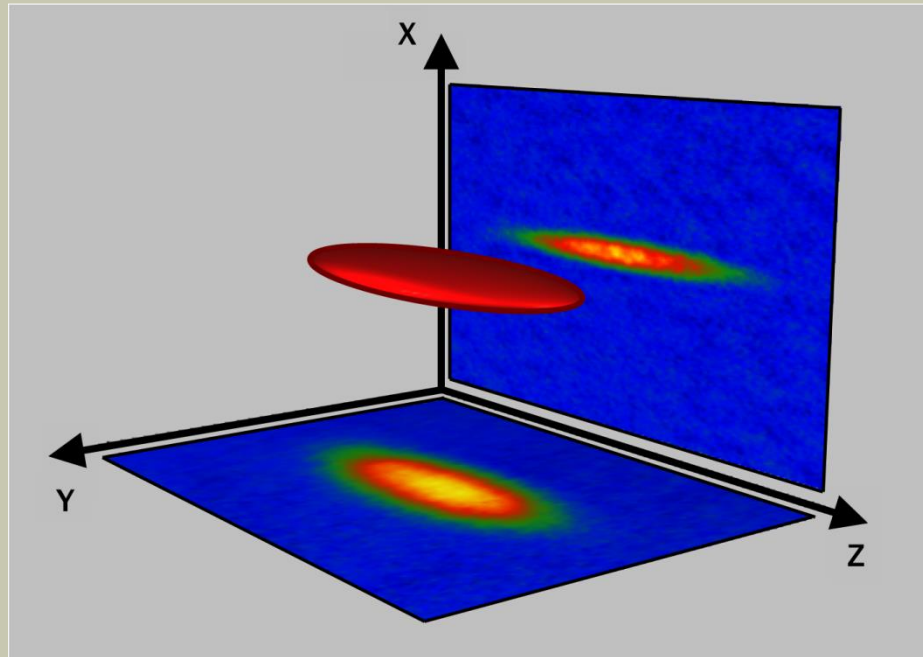


Shock  
Fronts

# SHEAR VISCOSITY FROM EXPANSION

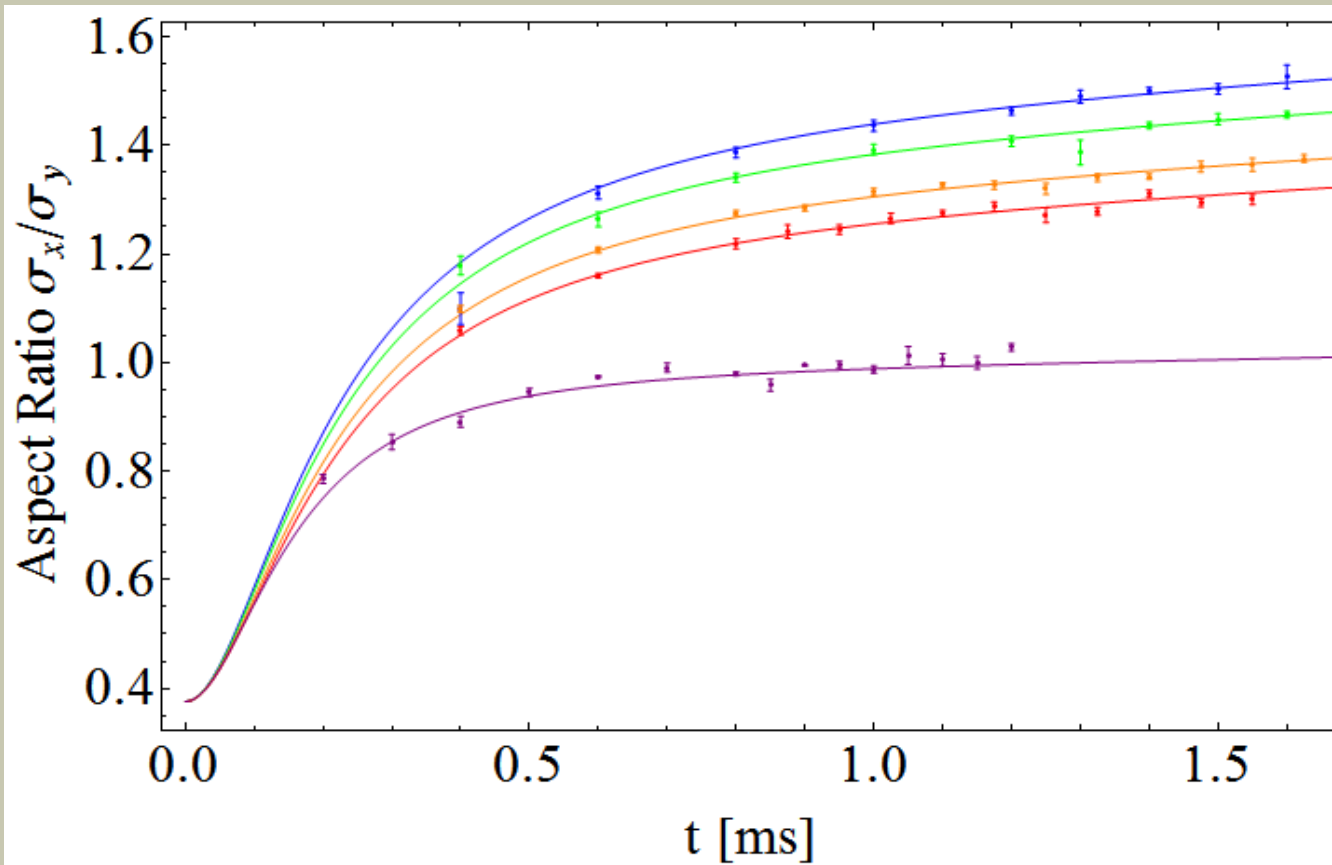


A gas trapped in a **3-wise** (1:3:30) elliptical trap is allowed to expand. Absorption images are taken in two planes.



Trap averaged viscosity determined from XY aspect ratio.

# ASPECT RATIO VS EXPANSION TIME



**832 G**

●  $E/E_F=0.52$

●  $E/E_F=0.75$

●  $E/E_F=1.22$

●  $E/E_F=1.69$

**527.5 G**

● Ballistic

# SCALING APPROXIMATION FOR HYDRODYNAMIC EXPANSION



$$n(x, y, z, t) = \frac{n_0(x/b_x, y/b_y, z/b_z)}{\Gamma}$$

$$\Gamma = b_x b_y b_z$$

Volume scale factor

$$\ddot{b}_i = \frac{\overline{\omega_i^2}}{\Gamma^{2/3} b_i} \left[ 1 + C_Q(b_{ijk}, \langle \alpha_s \rangle) \right] - \frac{\hbar \langle \alpha_s \rangle \sigma_{ii}}{m \langle x_i^2 \rangle_0 b_i}$$

$$\sigma_{ii} = 2 \frac{\dot{b}_i}{b_i} - \frac{2 \dot{\Gamma}}{3 \Gamma}$$

Viscous stress tensor

cloud-averaged shear viscosity coefficient

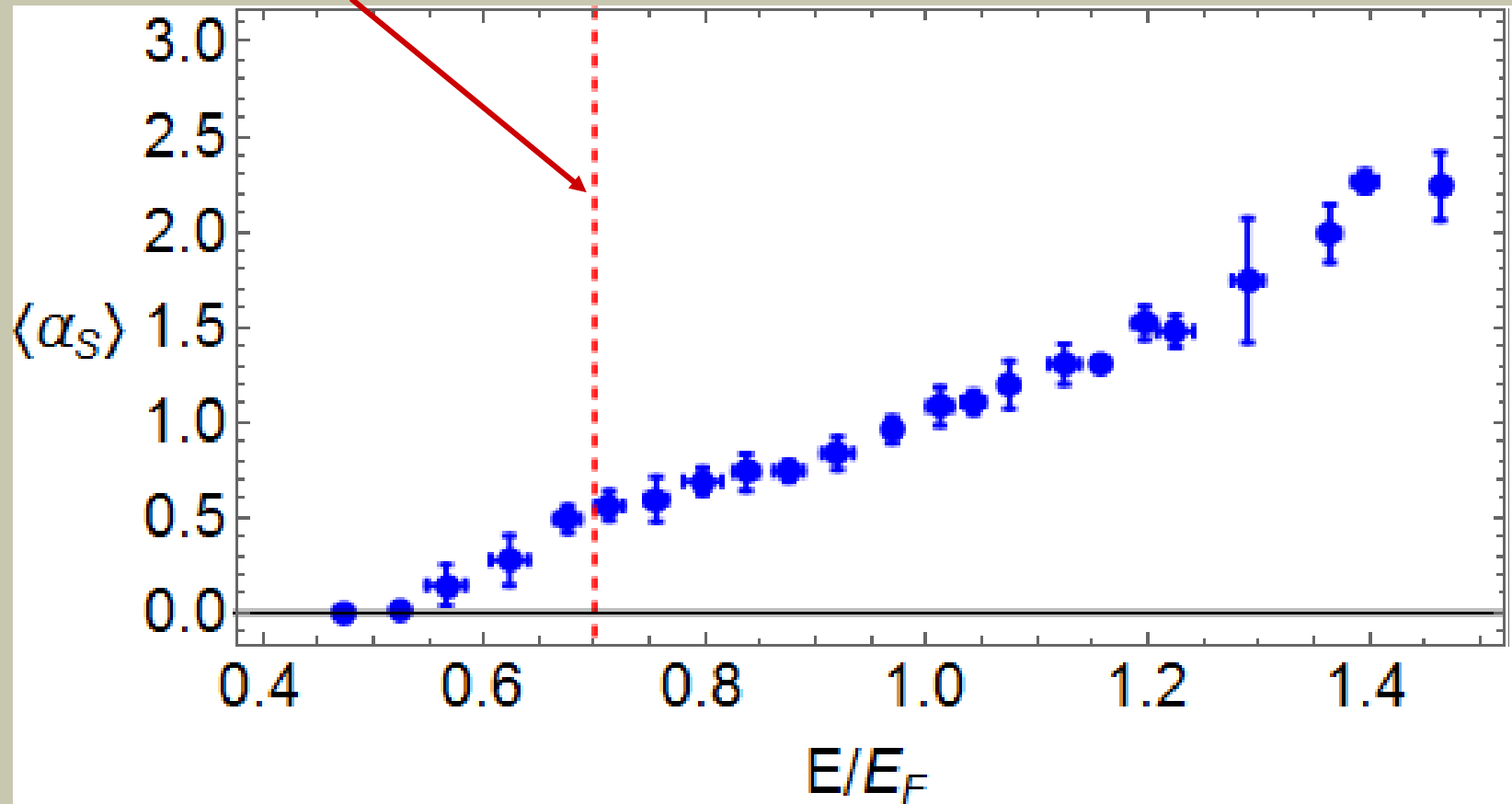
$$\eta = \hbar n \alpha \quad \langle \alpha_s \rangle = \frac{1}{N} \int d^3 r \alpha n$$



# CLOUD AVERAGE SHEAR VISCOSITY VS ENERGY



Transition to Superfluid



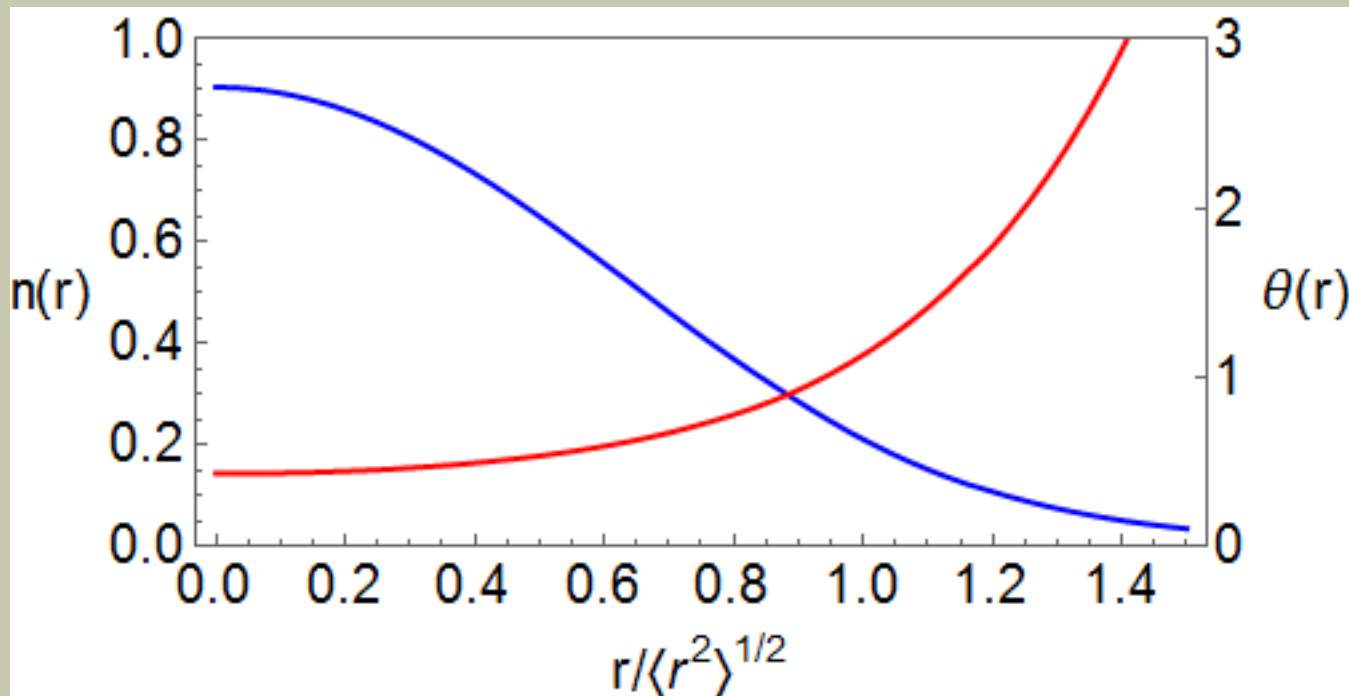
# REDUCED TEMPERATURE



The trapping potential and the equation of state determine the **density**  $n(r)$  as a function of position at a given **temperature**,  $T$ .

$$U(r) = U_0 \left[ 1 - \exp\left(\frac{-m\bar{\omega}^2 r^2}{2U_0}\right) \right]$$

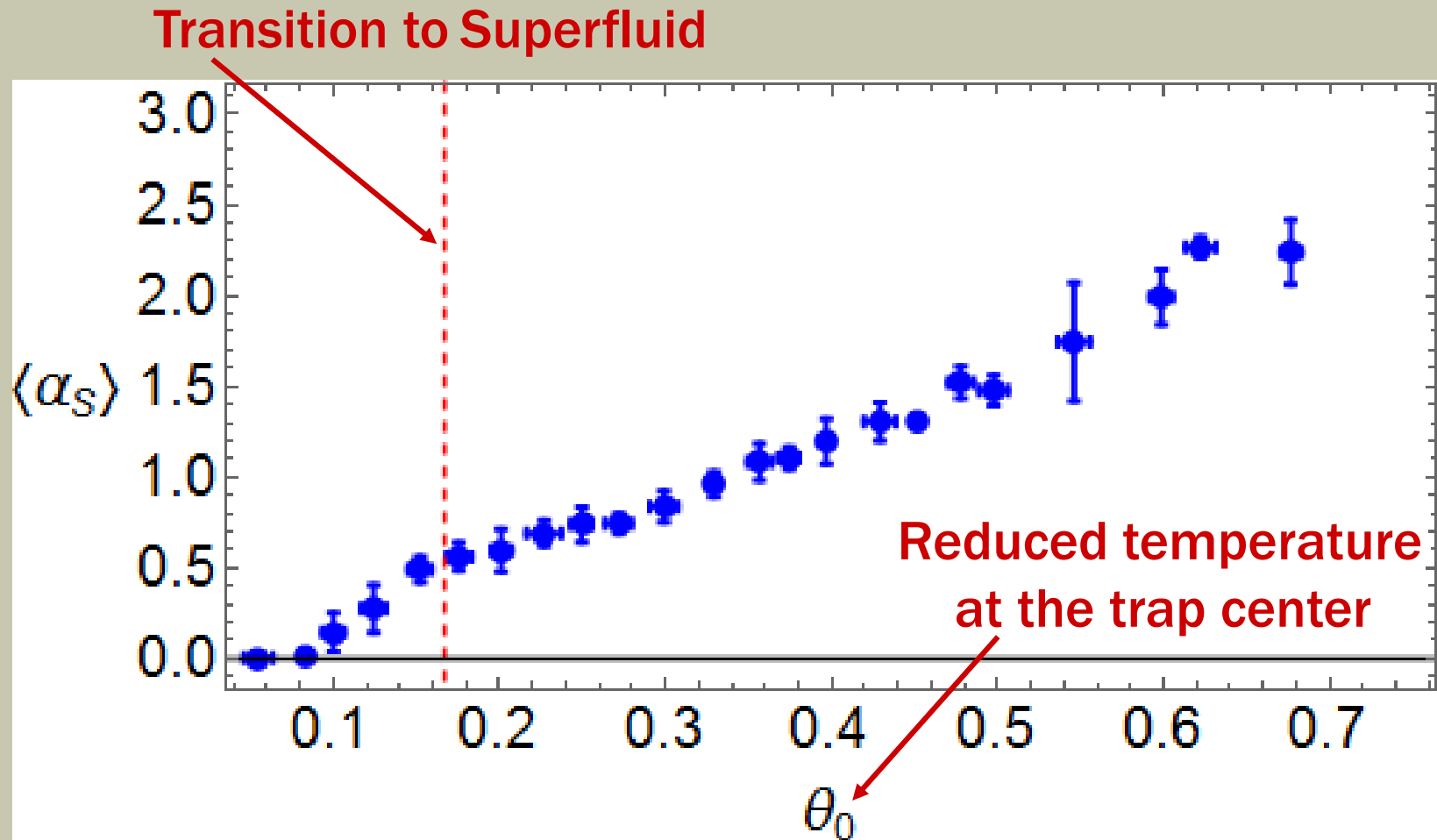
\*EoS from Ku et al., *Science*, 2012



Reduced Temperature

$$\theta(r) = \frac{T}{T_F(r)}$$
$$T_F(r) \propto n(r)^{2/3}$$

# CLOUD AVERAGED SHEAR VISCOSITY VERSUS REDUCED TEMPERATURE

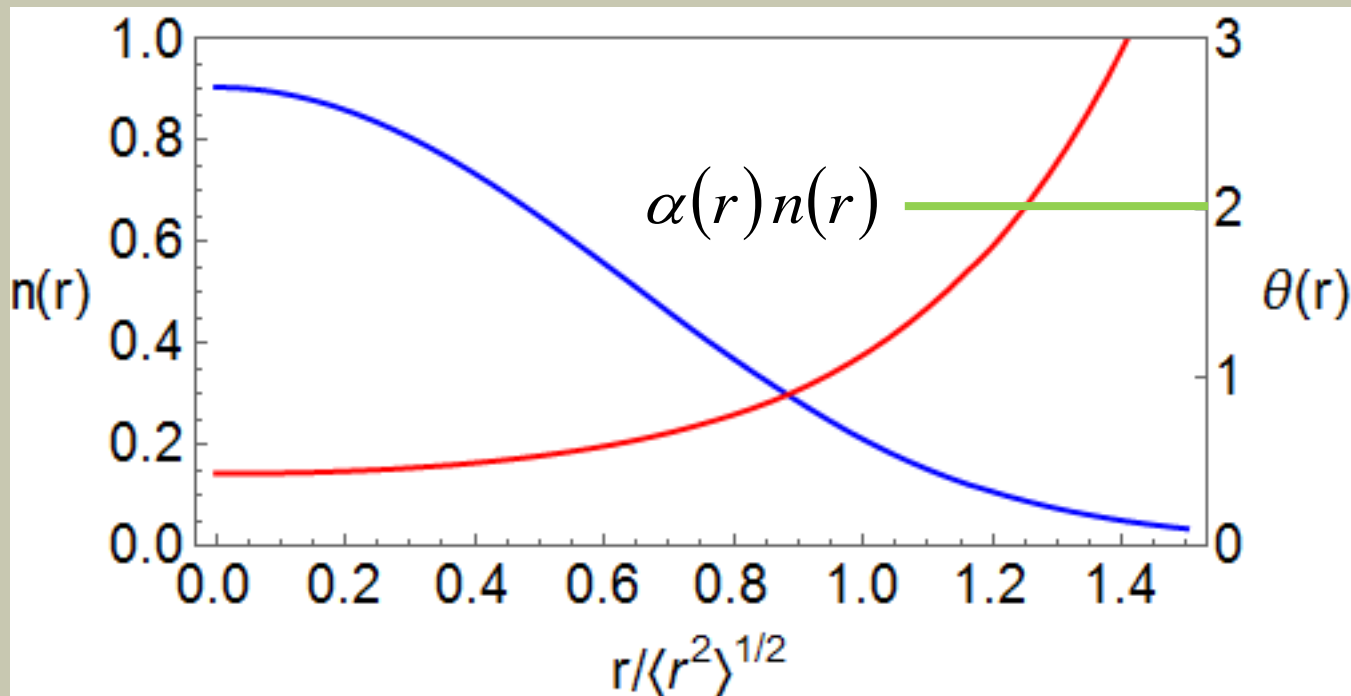


# LOCAL VISCOSITY VS POSITION (HIGH TEMPERATURE LIMIT)



$$\langle \alpha_s \rangle = \frac{1}{N} \int_0^\infty d^3r n(r) \alpha(r)$$

$$\eta = \hbar n(r) \alpha(r)$$



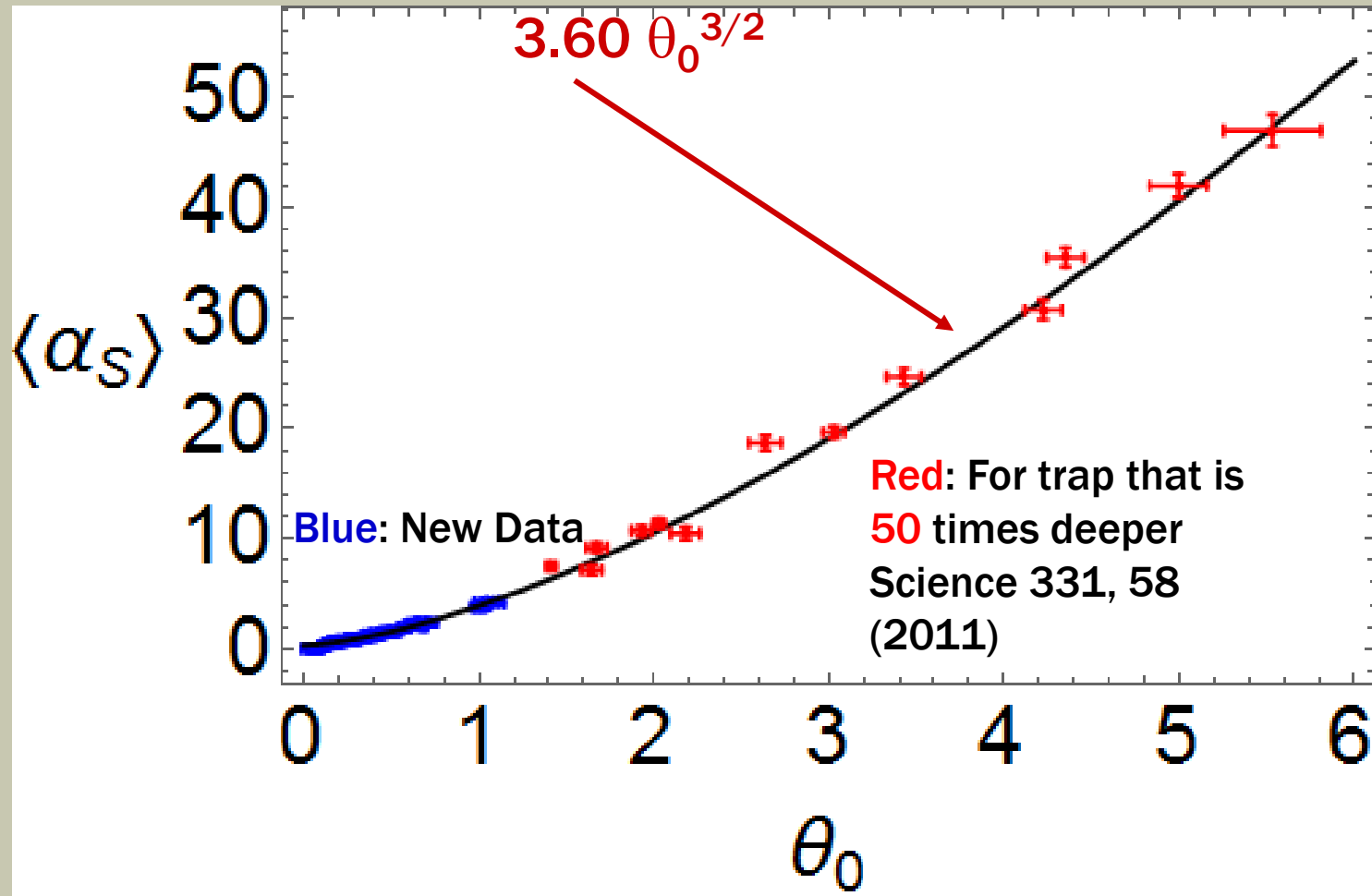
↓  
Constant in the trap

$$\eta \propto T^{3/2}$$

↓

$$\alpha(\theta) = \alpha_{3/2} \theta^{3/2}$$

# MEASURED CLOUD AVERAGED VISCOSITY (HIGH TEMPERATURE)



# FINITE VOLUME INTEGRAL



$$\langle \alpha_s \rangle = \frac{1}{N} \int_0^{R_C} d^3 r \alpha(r) n(r)$$



$$c_1 \theta_0^{3/2} = \frac{1}{N} \alpha_{3/2} \theta_0^{3/2} n_0 \frac{4\pi}{3} R_C^3$$

Volume

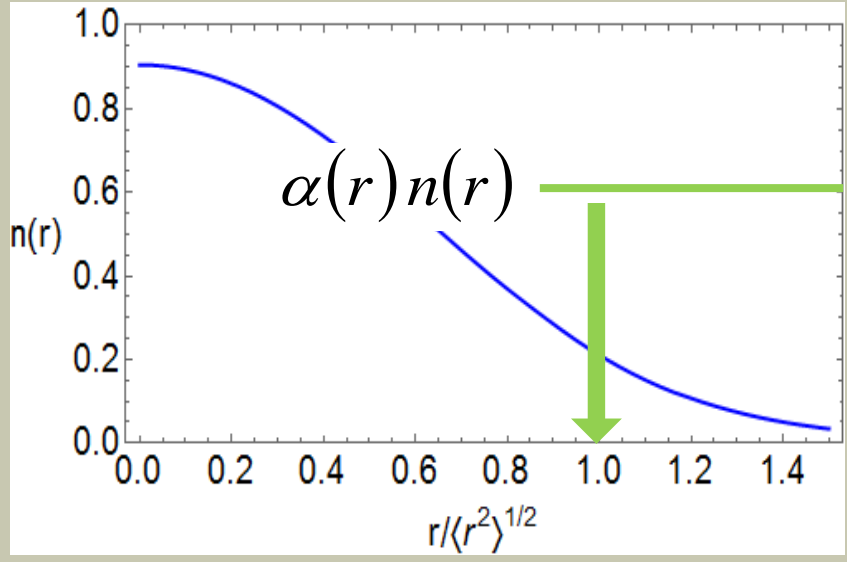
Fit from our data

$$c_1 = 3.60$$

from theory

$$\alpha_{3/2} = 2.77$$

G. M. Bruun and H. Smith, Phys. Rev. A 75, 043612 (2007).



$$n_0 = N \left( \pi \frac{2}{3} \langle r^2 \rangle \right)^{-3/2}$$

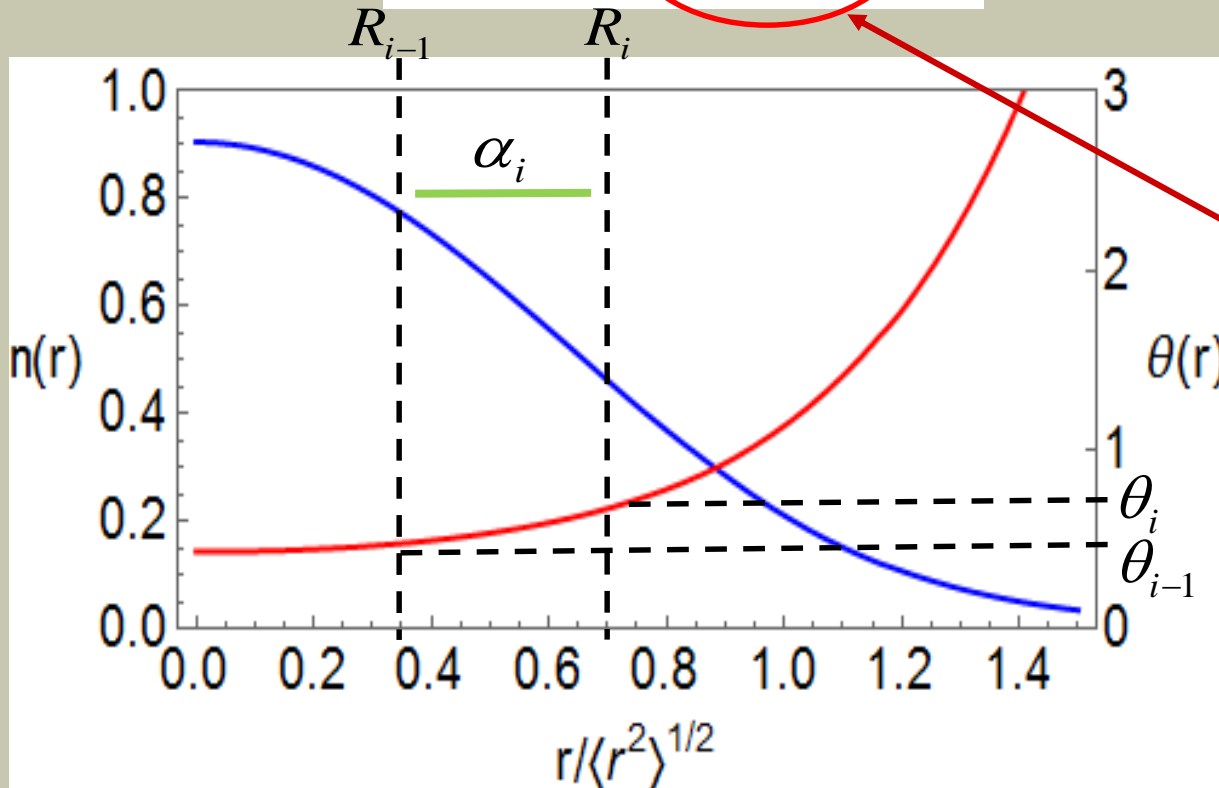
For a Gaussian density

$$R_C = 0.98 \langle r^2 \rangle^{1/2}$$



# LOCAL SHEAR VISCOSITY FROM TRAP AVERAGED MEASUREMENTS

$$\langle \alpha_S \rangle_j = \sum_i \frac{1}{N} \int_{R_{i-1}}^{R_i} d^3 r n(r) \alpha_i$$

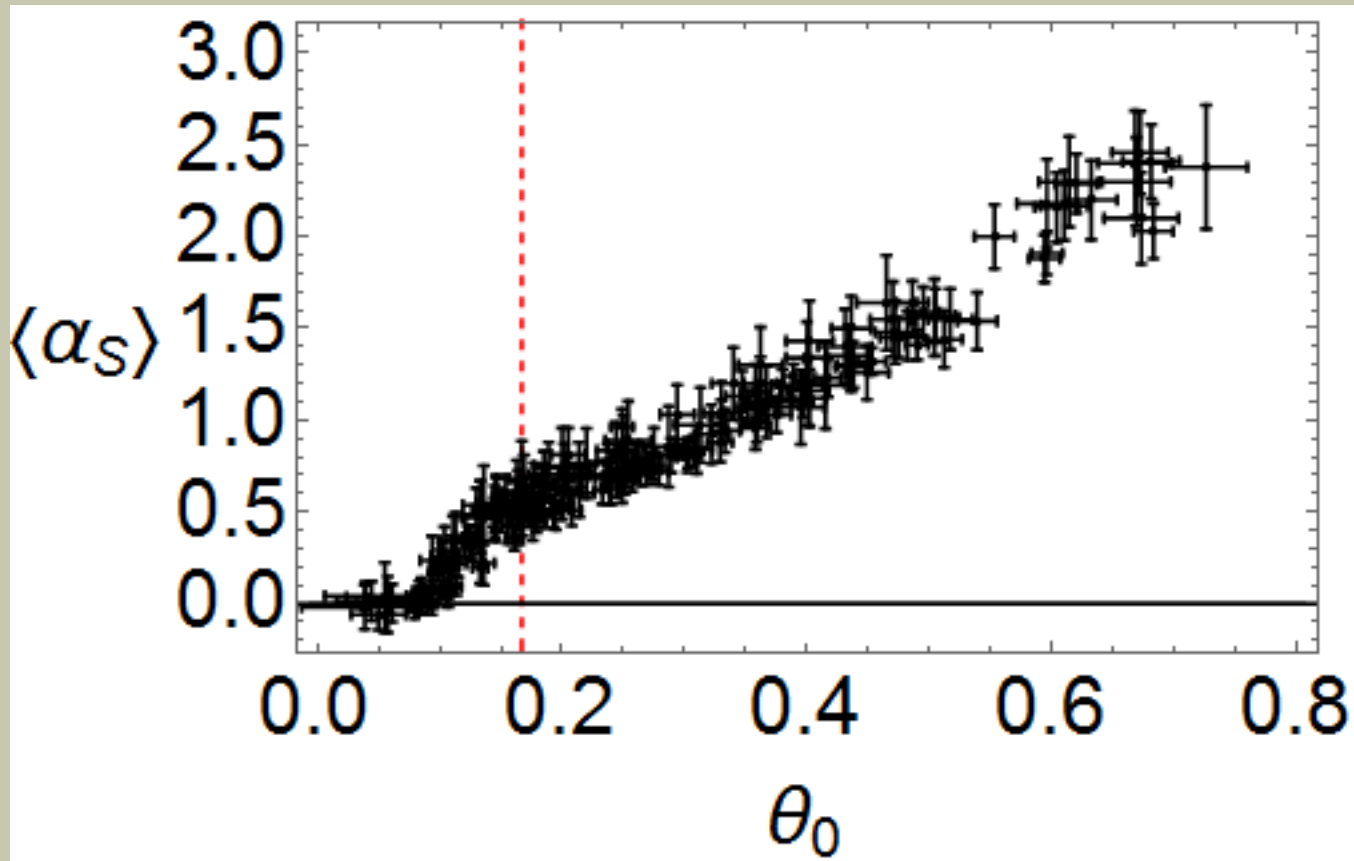


$$\alpha(\theta) = \begin{cases} \alpha_i : \theta_{i-1} < \theta < \theta_i \\ \alpha_{i+1} : \theta_i < \theta < \theta_{i+1} \\ \vdots \end{cases}$$

$C_{ji}$

$$\langle \mathbf{a}_S \rangle = \mathbf{C} \boldsymbol{\alpha}$$

# NOISY CLOUD-AVERAGED MEASUREMENTS (~200 POINTS)

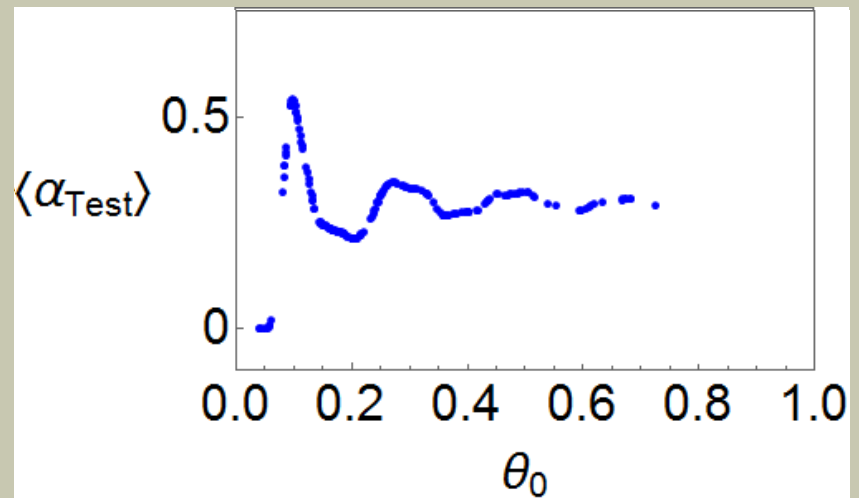
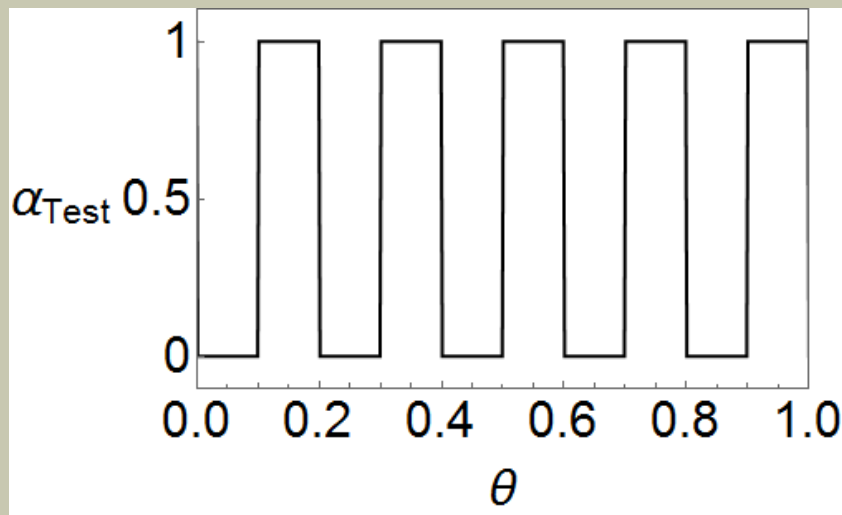




# IMAGE PROCESSING TECHNIQUE ITERATIVE MATRIX INVERSION



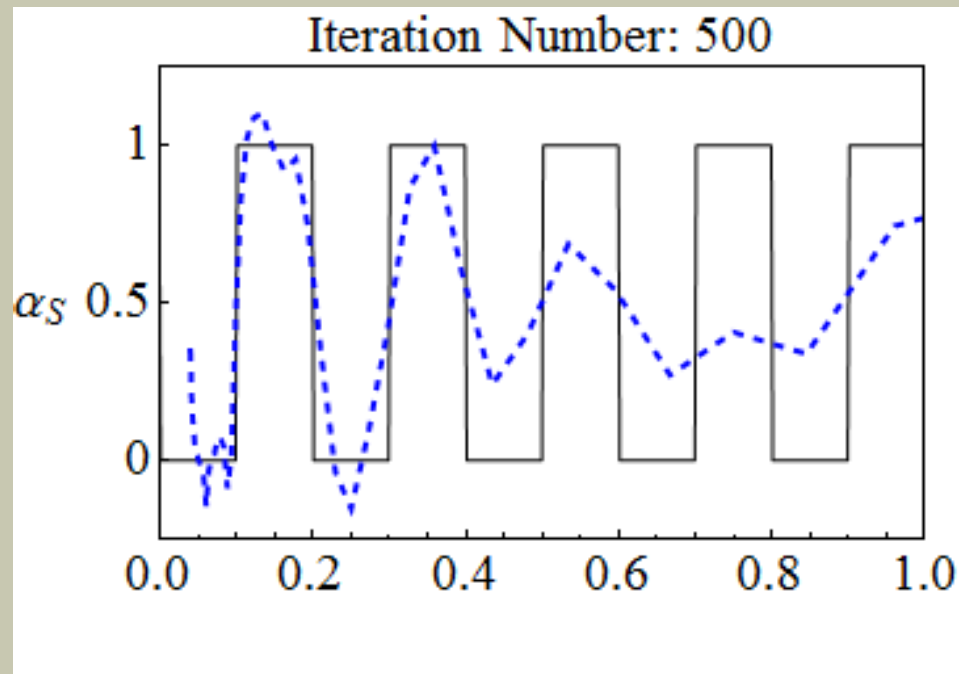
$$\mathbf{a}_{m+1} = (1 - \beta)\mathbf{a}_m + \beta \Psi \left[ \mathbf{a}_m + \mathbf{C}^T \left( \langle \mathbf{a}_S \rangle - \mathbf{C} \cdot \mathbf{a}_m \right) \right]$$



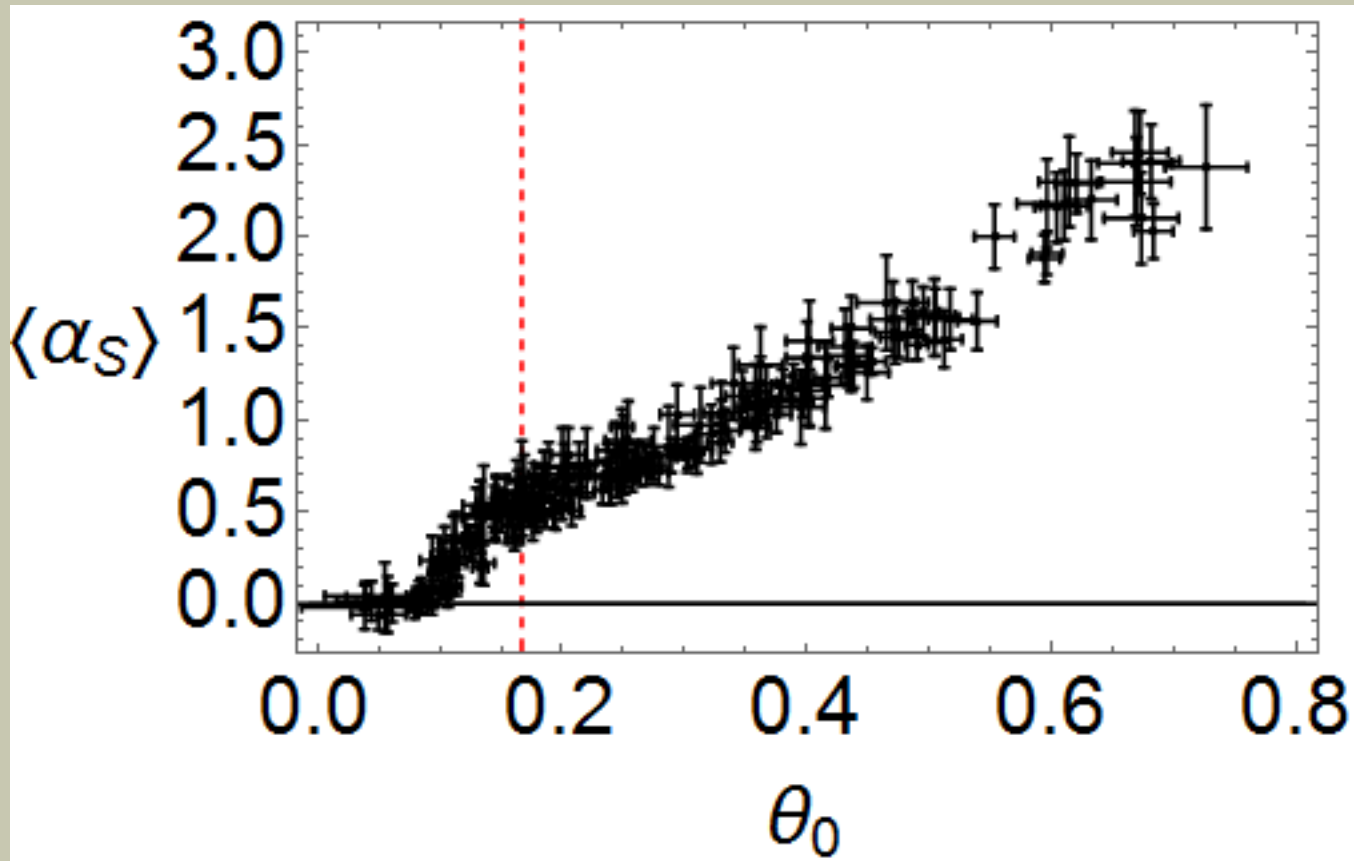
# ITERATIVE SOLUTION TEST FUNCTION



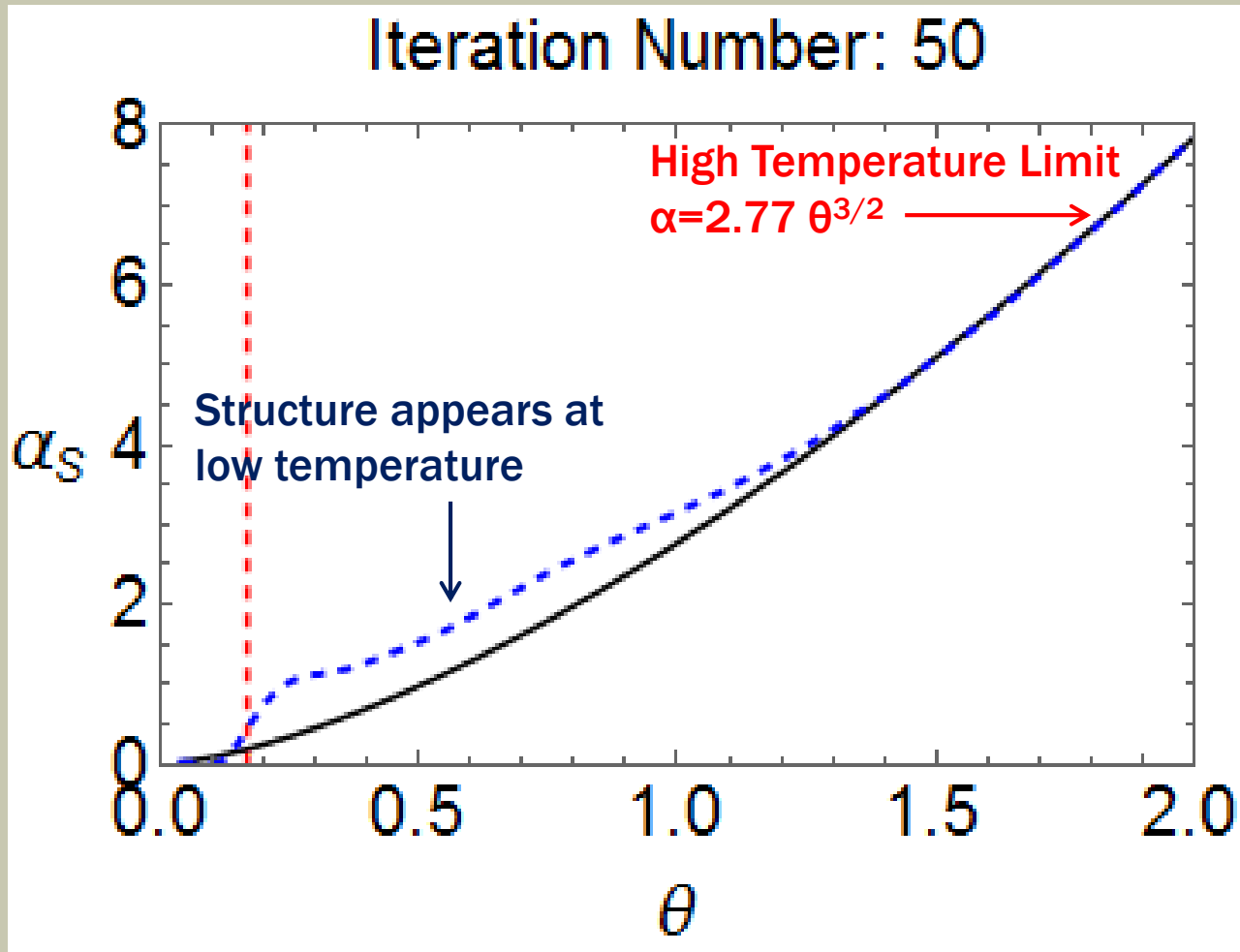
$$\mathbf{a}_{m+1} = (1 - \beta)\mathbf{a}_m + \beta \Psi \left[ \mathbf{a}_m + \mathbf{C}^T \left( \langle \mathbf{a}_S \rangle - \mathbf{C} \cdot \mathbf{a}_m \right) \right]$$



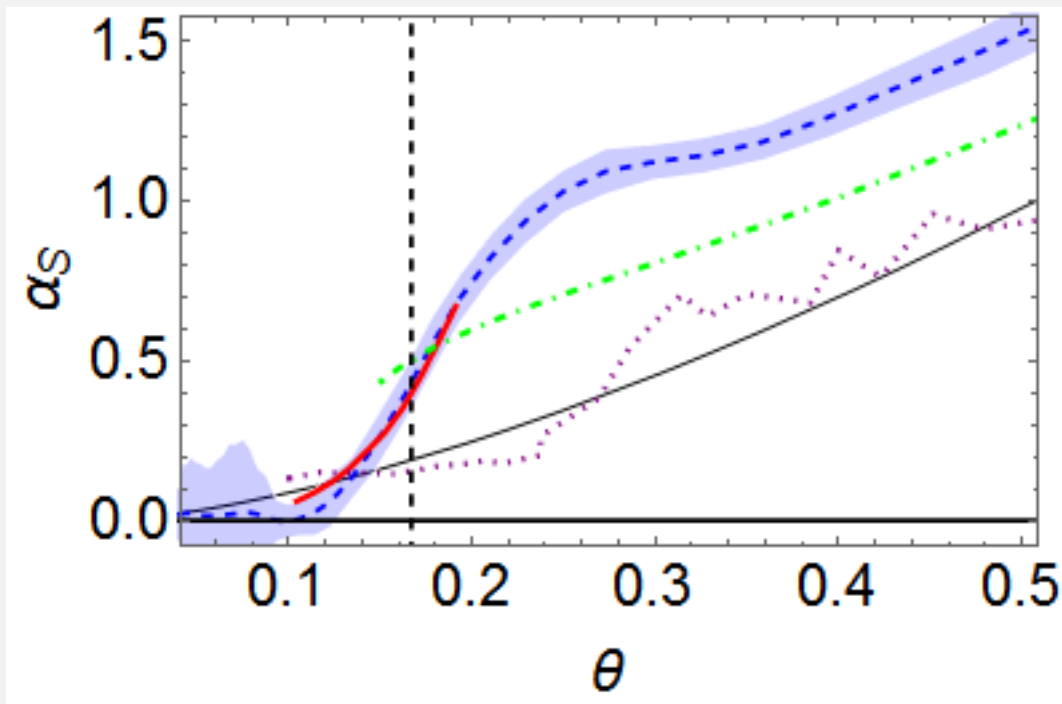
# NOISY CLOUD-AVERAGED MEASUREMENTS (~200 POINTS)



# LOCAL SHEAR VISCOSITY VERSUS TEMPERATURE



# LOCAL SHEAR VISCOSITY (COMPARISON TO THEORY)



--- measured

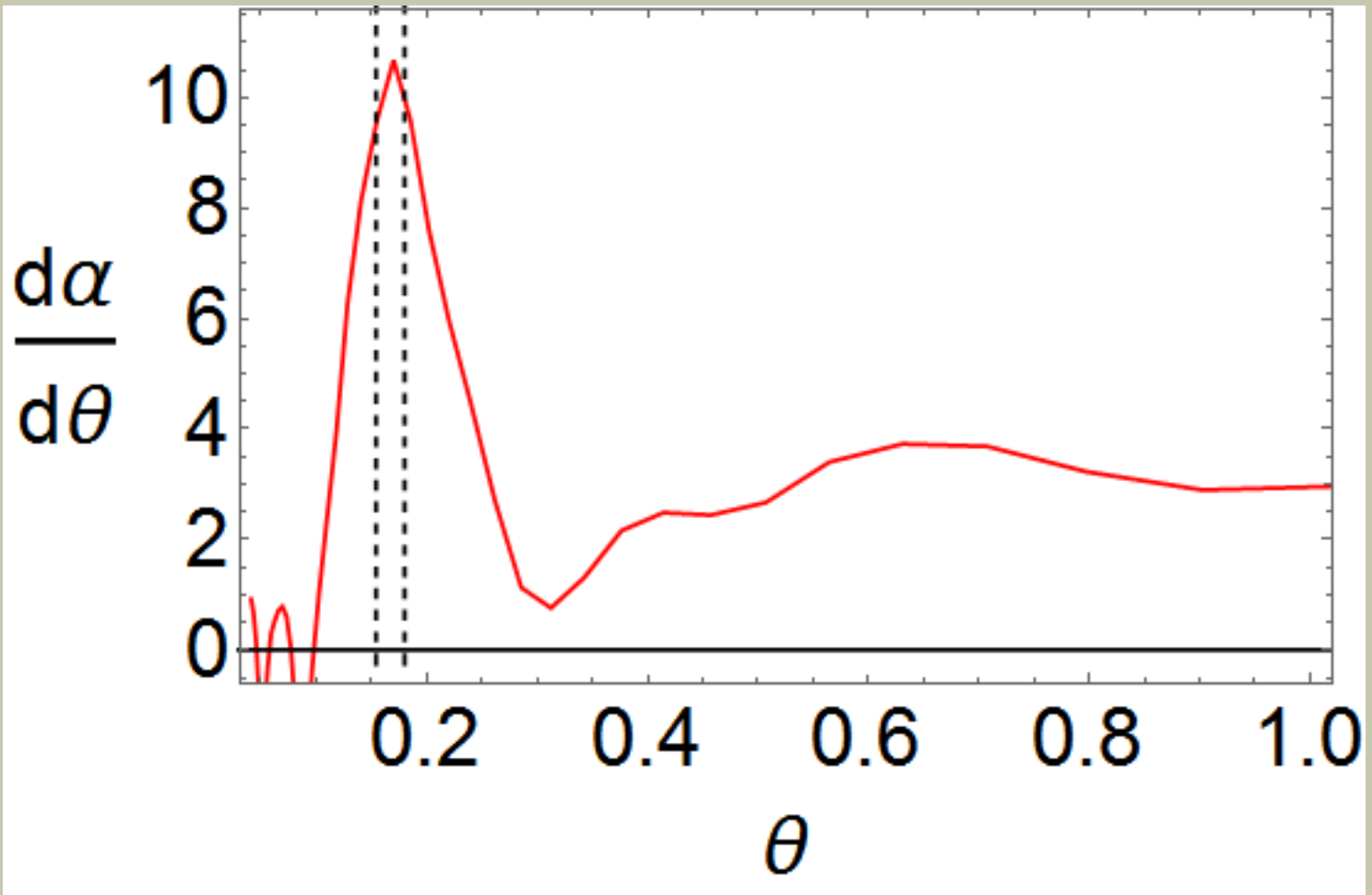
— kinetic theory  
 $\alpha = 2.77 \theta^{3/2}$

— Guo et al., PRL 2011  
(absent bosonic modes)

- · - Enss et al., Annals 2011  
(Diagrammatic Kubo  
formula)

····· Wlazowski et al., PRL  
2012 (Monte Carlo)

# DERIVATIVE OF LOCAL SHEAR VISCOSITY VERSUS TEMPERATURE



# SUMMARY



- **Hydrodynamic Strongly Interacting Fermi Gas**
- **Measuring Cloud Averaged Shear**
  - Scaling approximation used to measure energy per particle and cloud averaged shear viscosity self consistently
- **Determining Local Shear Viscosity**
  - From image processing techniques
  - Comparison to theory

# THANK YOU



Graduate Student:  
**Ethan Elliot**

PI:  
**John Thomas**

Support:  
ARO  
NSF  
DOE  
AFOSR

