

# Heavy-quarkonium theory in the LHC era

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In collaboration with Mathias Butenschön

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# Outline

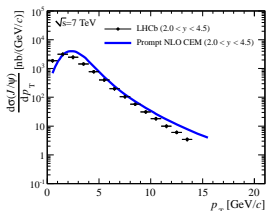
- 1 **Introduction:** CEM, CSM, NRQCD factorization
- 2 **NLO NRQCD:** General concept, singularities
- 3 **Global fit:** Unpolarized  $J/\psi$  yield
- 4 **Further tests:** ATLAS, FTPS, ZEUS
- 5 **Polarization:** HERA, Tevatron, LHC
- 6 **Summary:** NRQCD at the crossroads

# Introduction: CEM, CSM, NRQCD factorization

## Color evaporation model [Fritzsch 77; Halzen 77; Glück Owens Reya 78]

$$\sigma_{J/\psi} \approx \frac{1}{9} \rho_{J/\psi} \int_{2m_c}^{2m_D} ds_{c\bar{c}} \frac{d\sigma_{c\bar{c}}}{ds_{c\bar{c}}}$$

- $1/9$ : statistical probability that  $3 \times \bar{3}$   $c\bar{c}$  pair is asymptotically in color-single state
- $\rho_{J/\psi}$ : fraction of charmonia that materialize as  $J/\psi$
- Based **local parton-hadron duality**
- Assumes soft-gluon exchange with underlying event
- $2S+1 L_J^{[c]}$  quantum numbers do not enter
- Useful qualitative picture, rather than rigorous theory



[Schuler Vogt 96; Vogt 99; Frawley Ullrich Vogt 08]

# Color-singlet model vs. NRQCD factorization

## Color-singlet model [Berger Jones 81; Baier Rückl 81]

- $c\bar{c}$  pair in physical **color-singlet** state, e.g.  $c\bar{c}[{}^3S_1^{[1]}]$  for  $J/\psi$ .
- Nonperturbative information in  $J/\psi$  wave function at origin.
- Leftover IR divergences for P-wave quarkonia  $\rightsquigarrow$  **inconsistent!**
- Predicted cross section factor  $10^1$ – $10^2$  below Tevatron data.

## NRQCD factorization [Bodwin Braaten Lepage 95]

- Rigorous effective field theory
- Based on **factorization of soft and hard scales**  
(Scale hierarchy:  $Mv^2 \lesssim \Lambda_{\text{QCD}} \ll Mv \ll M$ )
- Theoretically consistent: no leftover singularities.
- NNLO proof of factorization [Nayak Qiu Sterman 05]
- Can explain hadroproduction at Tevatron.

# NRQCD factorization in a nutshell

**Factorization theorem**  $\sigma_{J/\psi} = \sum_n \sigma_{c\bar{c}[n]} \cdot \langle O^{J/\psi}[n] \rangle$

- $n$ : every possible Fock state, including **color-octet** states.
- $\sigma_{c\bar{c}[n]}$ : production rate of  $c\bar{c}[n]$ , calculated in perturbative QCD.
- $\langle O^{J/\psi}[n] \rangle$ : long-distance matrix elements (LDMEs), nonperturbative, extracted from experiment, universal?

**Scaling rules** [Lepage Magnea<sup>2</sup> Nakhleh Hornbostel 92]

LDMEs scale with relative velocity  $v$  ( $v^2 \approx 0.2$ ).

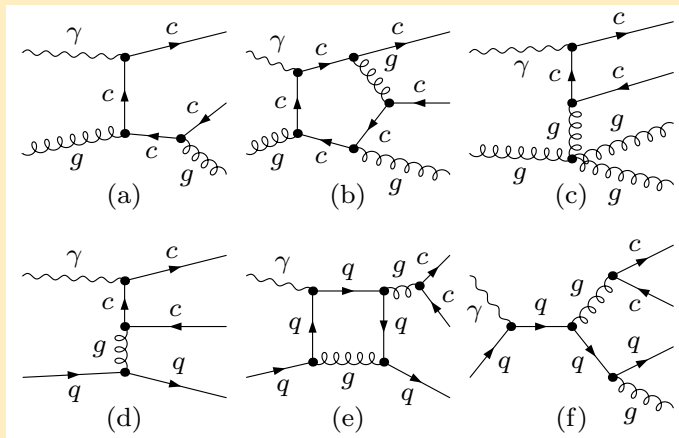
| scaling | $v^3$ (CS state) | $v^7$ (CO states)                                   | $v^{11}$ |
|---------|------------------|---|----------|
| $n$     | ${}^3S_1^{[1]}$  | ${}^1S_0^{[8]}, {}^3S_1^{[8]}, {}^3P_{0/1/2}^{[8]}$ | ...      |

- **Double expansion** in  $v$  and  $\alpha_s$ .
- Leading term in  $v$  ( $n = {}^3S_1^{[1]}$ ) corresponds to **color-singlet model**.

# NLO NRQCD calculations

- **Petrelli Cacciari Greco Maltoni Mangano 98:**  
Photo- and hadroproduction (only  $2 \rightarrow 1$  processes)
- **Klasen BK Mihaila Steinhauser 05:**  
Two-photon scattering (w/o resolved photons)
- **Butenschön BK 09:**  
Photoproduction (w/o resolved photons)
- **Zhang Ma Wang Chao 10:**  
 $e^+e^-$  annihilation
- **Ma Wang Chao 10, Butenschön BK 10:**  
Hadroproduction
- **Butenschön BK 11:**  
 $\gamma p$  and  $\gamma\gamma$  (resolved photons)  $\rightsquigarrow$  global fit of CO LDMEs
- **Butenschön BK 11:**  
Polarization in photoproduction
- **Butenschön BK 12, Chao Ma K. Wang Y.-J. Zhang 12, Gong, Wan, J.-X. Wang, H.-F. Zhang 12, Shao, Ma, K. Wang, Chao 14:**  
Polarization in hadroproduction

# Sample diagrams for $J/\psi$ photoproduction in NRQCD





# Color and spin projection

## Amplitudes for $c\bar{c}[n]$ production by projector application:

$$A_{c\bar{c}[1S_0^{[8]}]} = \text{Tr} [C_8 \Pi_0 A_{c\bar{c}}] |_{q=0}$$

$$A_{c\bar{c}[3S_1^{[1/8]}]} = \varepsilon_\alpha \text{Tr} [C_{1/8} \Pi^\alpha A_{c\bar{c}}] |_{q=0}$$

$$A_{c\bar{c}[3P_J^{[8]}]} = \varepsilon_{\alpha\beta} \frac{d}{dq_\beta} \text{Tr} [C_8 \Pi^\alpha A_{c\bar{c}}] |_{q=0}$$

- $A_{c\bar{c}}$ : amputated pQCD amplitude for open  $c\bar{c}$  production.
- $q$ : relative momentum between  $c$  and  $\bar{c}$ .
- $C_{1/8}$ : color projectors
- $\Pi_{0/1}$ : spin projectors
- $\varepsilon$ : polarization vectors and tensors

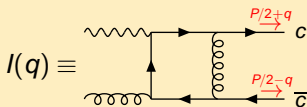
# Main Difference to Previous Calculations

## Virtual corrections: Two different approaches:

- First loop integration, then projectors: (Previous publications)
  - Loop integrals **Coulomb divergent**.
- First projectors, then loop integration: (Our method)
  - + **No Coulomb singularities**.
  - + One scale less in loop integration.
  - Loop integrals not standard form.

## Where do Coulomb divergences come from?

- Projectors: Relative momentum  $q \rightarrow 0$ .
- Scalar diagrams with gluon between external  $c$  and  $\bar{c}$ , e.g.:



$$\lim_{q \rightarrow 0} I(q) = \frac{A}{q^2} + \frac{B}{\epsilon} + C$$

$$\text{But: } I(0) = \frac{B}{\epsilon} + C$$

- $\implies$  **No Coulomb singularities in dimensional regularization!**

# Cancellation of divergences

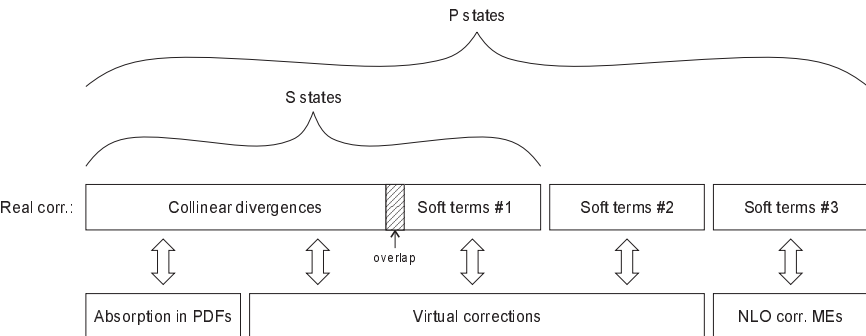
**UV divergences:** Cancellation within virtual corrections:

- Loop integrals
- Charm mass renormalization
- Strong coupling constant renormalization
- Wave function renormalization of external particles

**IR divergences:** Cancellation between:

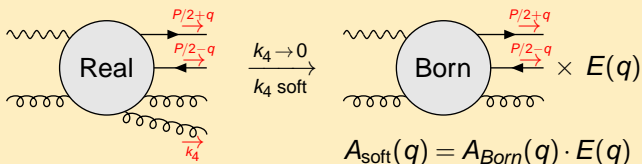
- **Virtual corrections** (loop integrals + wave function renormal.)
- Soft and collinear parts of **real corrections**
- Universal part absorbed into **proton** and **photon PDFs**
- Radiative corrections to **long distance matrix elements**

# Overview of IR singularity structure



# Structure of Soft Singularities

## Soft limits of the real corrections:



## S and P states: Soft #1 + Soft #2 + Soft #3 terms:

$$A_{\text{soft},s} = A_{\text{soft}}(0) = A_{\text{Born},s} \cdot E(0)$$

$$A_{\text{soft},p} = A'_{\text{soft}}(0) = A_{\text{Born},p} \cdot E(0) + A_{\text{Born},s} \cdot E'(0)$$

$$|A_{\text{soft},s}|^2 = |A_{\text{Born},s}|^2 \cdot E(0)^2$$

$$|A_{\text{soft},p}|^2 = |A_{\text{Born},p}|^2 \cdot E(0)^2 + 2 \operatorname{Re} A_{\text{Born},s}^* A_{\text{Born},p} \cdot E(0) E'(0) + |A_{\text{Born},s}|^2 \cdot E'(0)^2$$

# Radiative Corrections to Long Distance MEs

In NRQCD: Long distance MEs =  $c\bar{c}$  scattering amplitudes:

$$\langle O^{J/\psi}[n] \rangle =$$

$$O[n] = \text{4-fermion operators}$$

$$(n = {}^3S_1^{[1]}, {}^1S_0^{[8]}, {}^3S_1^{[8]}, {}^3P_{0/1/2}^{[8]}, \dots)$$

Corrections to  $\langle O^{J/\psi}[{}^3S_1^{[1/8]}] \rangle$  with NRQCD Feynman rules:

$$+ \text{similar diagrams} \propto \frac{4\alpha_s}{3\pi m_c^2} \left( \frac{1}{\epsilon_{UV}} - \frac{1}{\epsilon_{IR}} \right) \cdot$$

- **UV singularity** cancelled by renormalization of 4-fermion operat.
- **IR singularity** cancels soft #3 terms of  $p$  states!

# Global fit at NLO in NRQCD

Fit CO LDMEs to all available world data on  $J/\psi$  inclusive production:

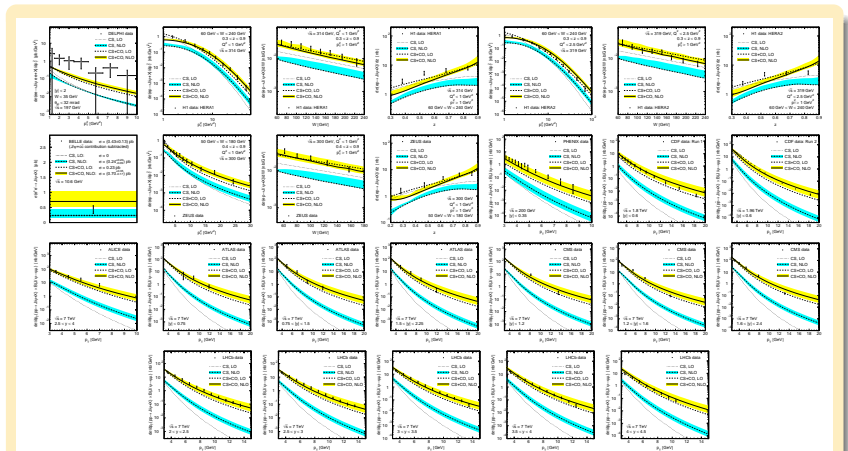
| type           | $\sqrt{s}$ | collider    | collaboration | reference                  |
|----------------|------------|-------------|---------------|----------------------------|
| $pp$           | 200 GeV    | RHIC        | PHENIX        | PRD82(2010)012001          |
| $p\bar{p}$     | 1.8 TeV    | Tevatron I  | CDF           | PRL97(1997)572; 578        |
| $p\bar{p}$     | 1.96 TeV   | Tevatron II | CDF           | PRD71(2005)032001          |
| $pp$           | 7 TeV      | LHC         | ALICE         | NPB(PS)214(2011)56         |
|                |            |             | ATLAS         | PoS(ICHEP 2010)013         |
|                |            |             | CMS           | EPJC71(2011)1575           |
|                |            |             | LHCb          | EPJC71(2011)1645           |
| $\gamma p$     | 300 GeV    | HERA I      | H1, ZEUS      | EPJ25(2002)25; 27(2003)173 |
| $\gamma p$     | 319 GeV    | HERA II     | H1            | EPJ68(2010)401             |
| $\gamma\gamma$ | 197 GeV    | LEP II      | DELPHI        | PLB565(2003)76             |
| $e^+e^-$       | 10.6 GeV   | KEKB        | Belle         | PRD79(2009)071101          |

Fit values for CO LDMEs:

| $10^{-2} \text{ GeV}^{3+2L}$               | feed-down included | feed-down subtracted |
|--|--------------------|----------------------|
| $\langle \mathcal{O}[^1S_0^{[8]}] \rangle$ | $4.97 \pm 0.44$    | $3.04 \pm 0.35$      |
| $\langle \mathcal{O}[^3S_1^{[8]}] \rangle$ | $0.224 \pm 0.059$  | $0.168 \pm 0.046$    |
| $\langle \mathcal{O}[^3P_0^{[8]}] \rangle$ | $-1.61 \pm 0.20$   | $-0.908 \pm 0.161$   |
| $\chi^2/\text{d.o.f.}$                     | $857/194 = 4.42$   | $725/194 = 3.74$     |

Note: CO LDMEs  $\propto v^4 \times \langle \mathcal{O}[^3S_1^{[1]}] \rangle \rightsquigarrow$  NRQCD **velocity scaling rules** ✓

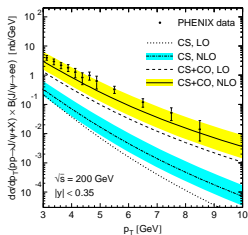
# Comparison with world data



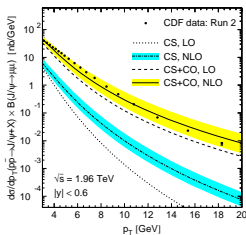


# Comparison with RHIC and Tevatron

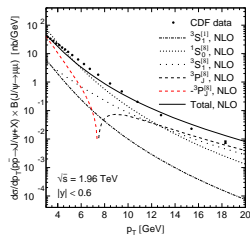
## RHIC PHENIX



## Tevatron II CDF

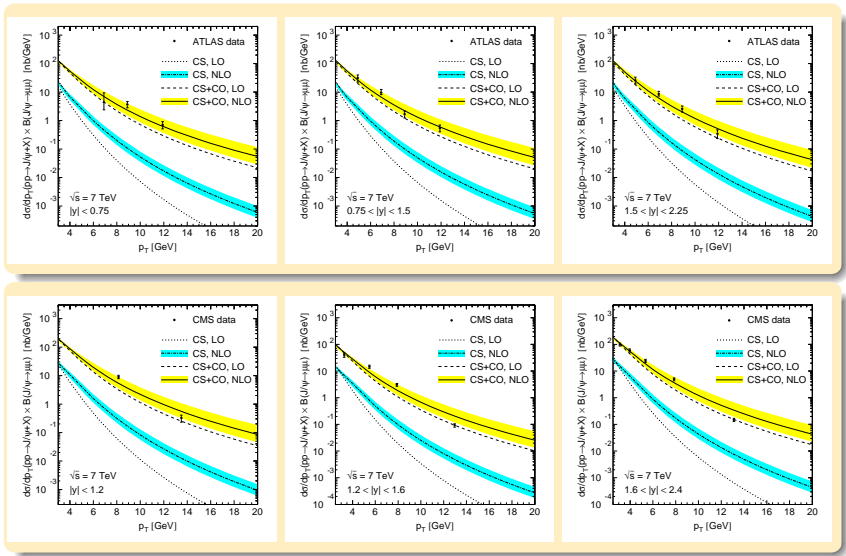


## Decomposition of NLO NRQCD

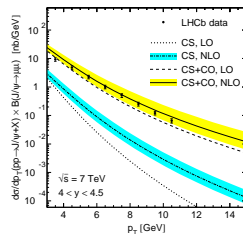
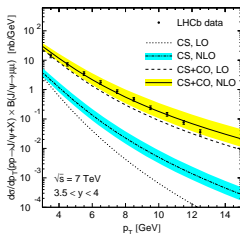
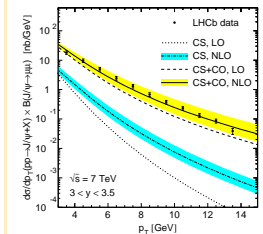
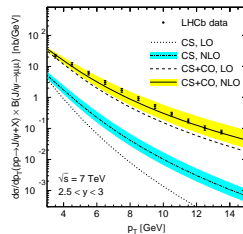
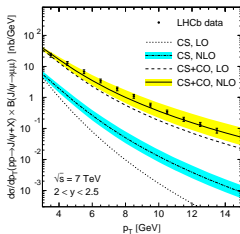
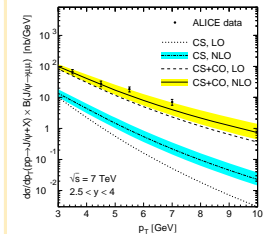


- Data **well described** by CS+CO at NLO.
- **CS** orders of magnitudes **below** data.
- **Sizeable NLO corrections**, especially in the  $3P_J^{[8]}$  channels.

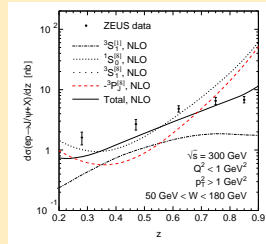
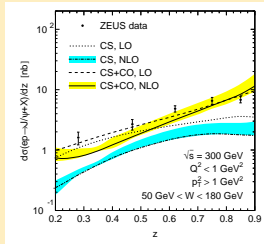
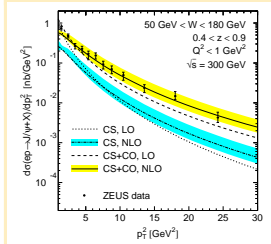
# Comparison with ATLAS and CMS at LHC



# Comparison with ALICE and LHCb at LHC

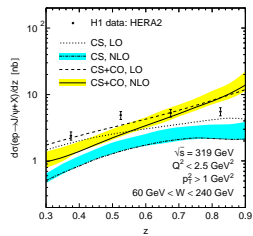
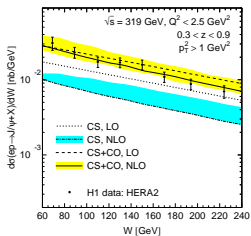
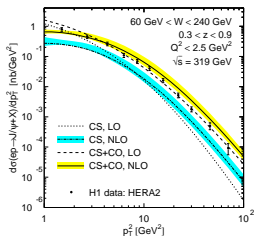
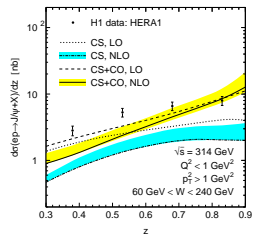
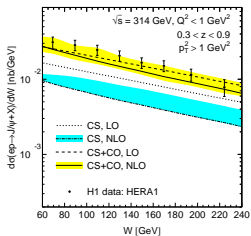
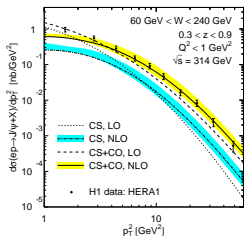


# Comparison with ZEUS at HERA I

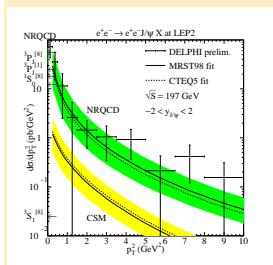


- $W = \gamma p$  CM energy.
- $z =$  fraction of  $\gamma$  energy going to  $J/\psi$  in  $p$  rest frame.
- Compensation of  $^1S_0^{[8]}$  vs.  $^3P_J^{[8]} \rightsquigarrow$  regular  $z \rightarrow 1$  behavior.
- Data **well described** by CS+CO at NLO.
- **CS** factor of 3–5 **below** the data.

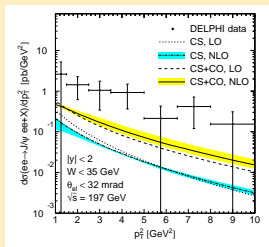
# Comparison with H1 at HERA I and II



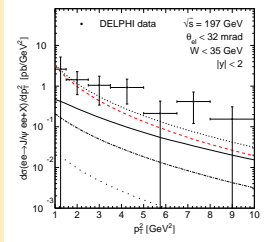
# Comparison with DELPHI at LEP II



[Klasen BK Mihaila  
Steinhauser 02]



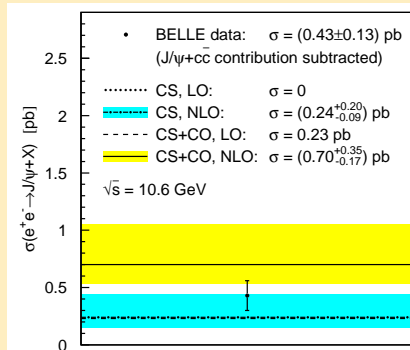
NLO NRQCD



Decomposition of  
NLO NRQCD

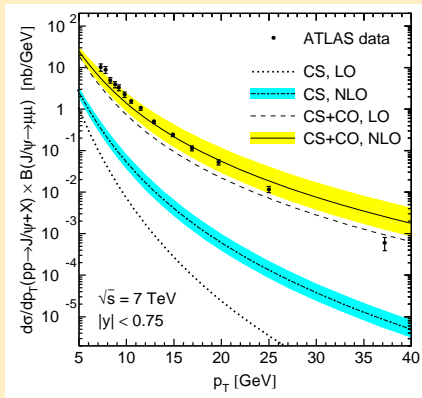
- Agreement with NRQCD at NLO worse than in 2002 at LO.
- Just 16 DELPHI events with  $p_T > 1$  GeV.
- No results from ALEPH, L3, OPAL.
- Data exhausted by single-resolved contribution.

# Comparison with Belle at KEKB



- At NLO, both CSM and NRQCD agree with data.
- # of charged tracks  $> 4$ , missing events **not corrected** for.  
 $\rightsquigarrow$  Belle point likely **higher**.

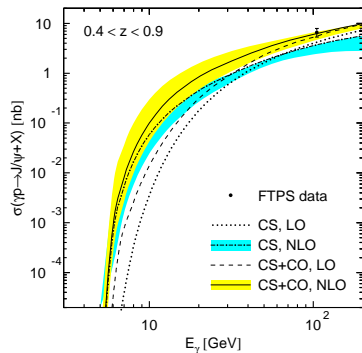
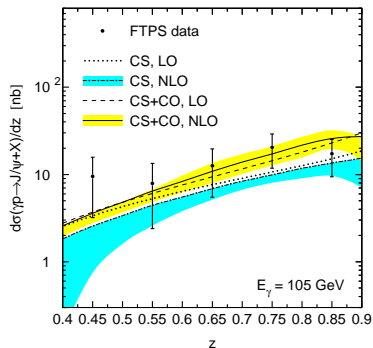
# Comparison with ATLAS (after fit) [NPB850(2011)387]



- Resummation of large logs  $\ln(p_T^2/M^2)$  necessary at large  $p_T$ .
- New formalism to include non-leading powers in  $p_T^2/M^2$  [Kang Qiu Sterman 2012].

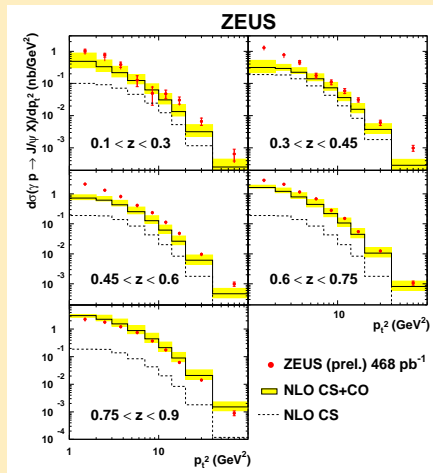


# Comparison with Fermilab Tagged-Photon Spectrometer data (excluded from fit) [PRL52(1984)795]



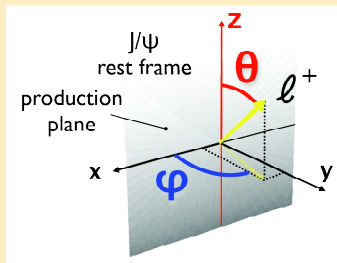
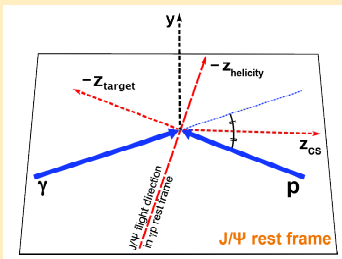
- Inelastic scattering of 105 GeV photons on hydrogen target.
- Data **remarkably well described** by CS+CO at NLO.

# Comparison with ZEUS (after fit) [JHEP1302(2013)071]



- Notorious NRQCD overshoot at **large z** overcome.

# Polarized $J/\psi$ photo- and hadroproduction



Decay angular distribution:

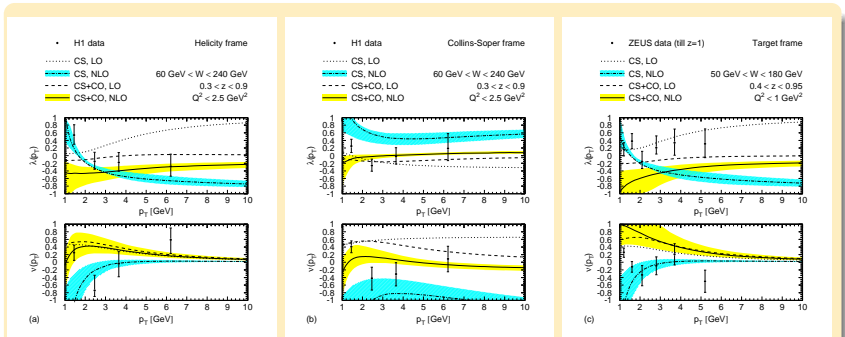
$$\frac{d\Gamma(J/\psi \rightarrow l^+l^-)}{d\cos\theta d\phi} \propto 1 + \lambda_\theta \cos^2\theta + \lambda_\phi \sin^2\theta \cos(2\phi) + \lambda_{\theta\phi} \sin(2\theta) \cos\phi$$

Polarization observables in spin density matrix formalism:

$$\lambda_\theta = \frac{d\sigma_{11} - d\sigma_{00}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_\phi = \frac{d\sigma_{1,-1}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_{\theta\phi} = \frac{\sqrt{2}\text{Re} d\sigma_{10}}{d\sigma_{11} + d\sigma_{00}}$$

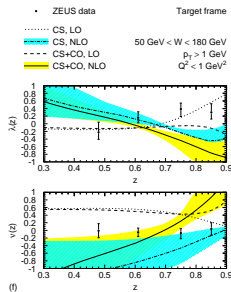
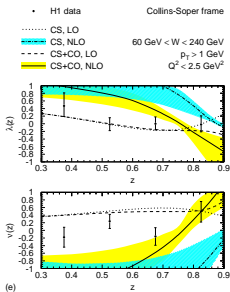
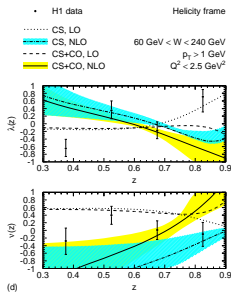
$\lambda = 0, +1, -1$ : unpolarized, transversely and longitudinally polarized.

# Comparison with H1 and ZEUS



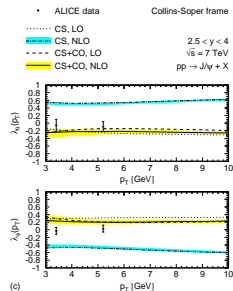
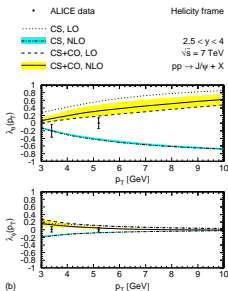
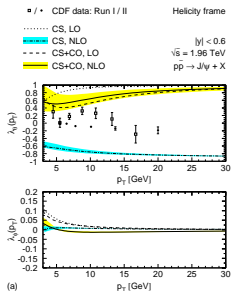
- No z cut on ZEUS data  $\rightsquigarrow$  diffractive production included.
- Perturbative stability in NRQCD higher than in CSM.
- $J/\psi$  preferably unpolarized at large  $p_T$ .

# Comparison with H1 and ZEUS (cont.)



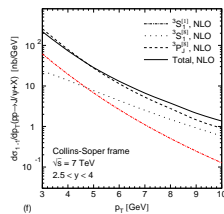
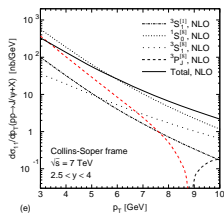
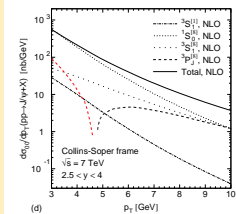
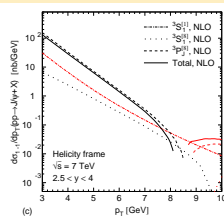
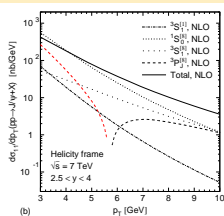
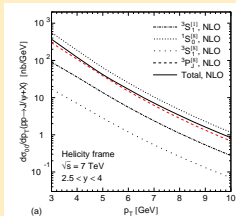
- Large scale uncertainties due to low cut  $p_T > 1$ .
- Overall  $\chi^2$  w.r.t. default prediction more than halved by going from CSM to NRQCD.

# Comparison with CDF and ALICE



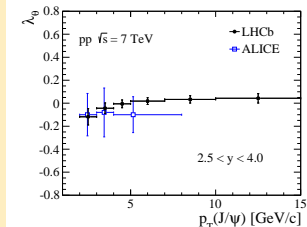
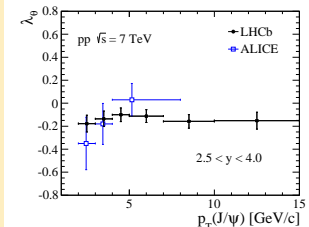
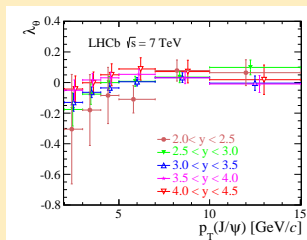
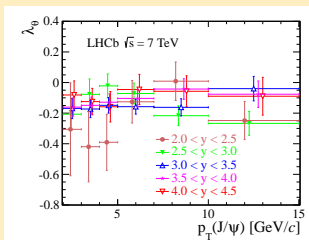
- CDF I and II data mutually inconsistent for  $p_T < 12$  GeV.
- CDF  $J/\psi$  polarization anomaly persists at NLO.
- 4/8 ALICE points agree w/ NLO NRQCD within errors, others  $< 2\sigma$  away.

# Decomposition for ALICE



- $d\sigma_{\text{unpol}} = d\sigma_{00} + 2d\sigma_{11}$ ;  $d\sigma_{1,-1}$  auxiliary.
- Previously unknown  ${}^3P_J^{[8]}$  NLO correction significant.

# LHCb data on prompt $J/\psi$ polarization [EPJC73(2013)2631]

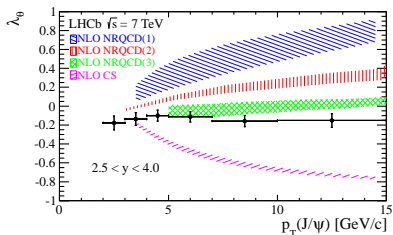


helicity frame

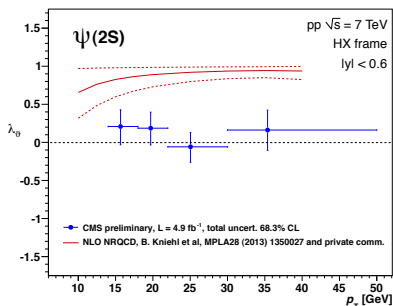
Collins-Soper frame



# Comparison with LHCb and CMS polarization data



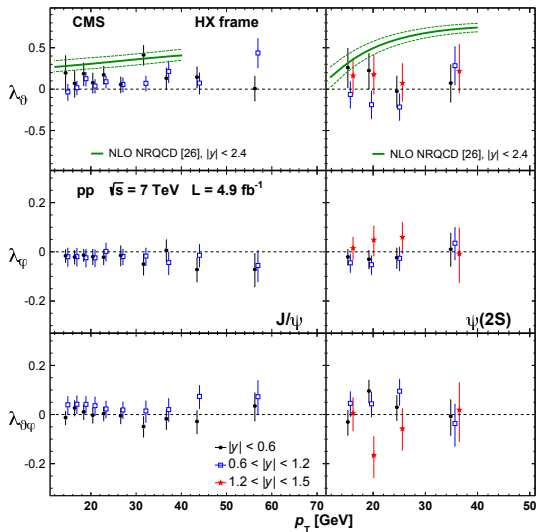
prompt  $J/\psi$  polarization  
LHCb, EPJC73(2013)2631



$\psi'$  polarization  
CMS, PLB727(2013)381

- (1): Global NLO NRQCD fit to  $J/\psi$  yield [PRD84(2011)051501(R)]
- New NLO NRQCD fit to  $\psi'$  yield from HERA, Tevatron, and LHC

# CMS data on $J/\psi$ and $\psi'$ polarization [PLB727(2013)381]

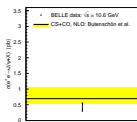


# Comparison with Gong et al. and Chao et al.

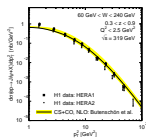
BK, MB

PRL108(2012)172002

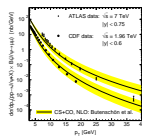
$e^+e^-$  yield



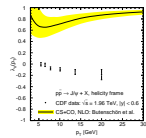
$\gamma p$  yield



$p\bar{p}/pp$  yield

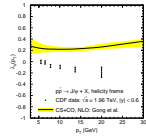
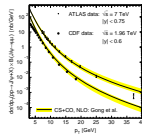
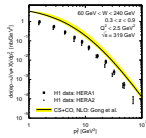
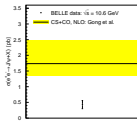


CDF polariz.



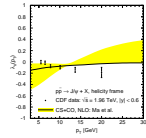
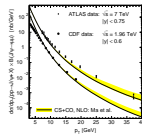
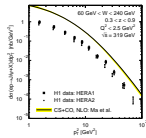
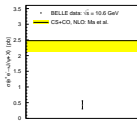
Gong et al.

PRL110(2013)042002



Chao et al.

PRL108(2012)242004



# Summary

- NRQCD provides rigorous **factorization theorem** for production and decay of heavy quarkonia; predicts:
  - existence of CO states;
  - universality of LDMEs.
- Previous LO tests not conclusive.
- Here: first global analysis of unpolarized  $J/\psi$  world data at NLO.
- Hadro- and photoproduction: striking evidence for NRQCD.
- CSM greatly undershoots data, except for  $e^+e^-$  annihilation.
- $\gamma\gamma$  scattering not conclusive yet.
- Contributions from feed-down and  $B$  decays throughout small against theoretical uncertainties  $\rightsquigarrow$  subtracted in fit.
- Hadroproduction data alone cannot reliably fix all 3 CO LDMEs.

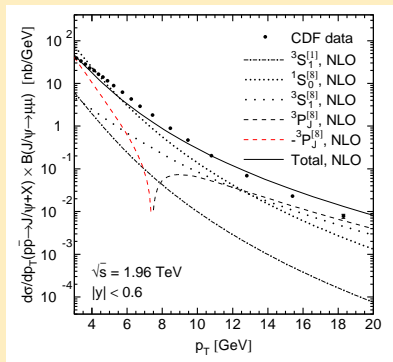
## Summary (cont.)

- Case for NRQCD less strong in polarized  $J/\psi$  photoproduction at HERA.
- NLO NRQCD predictions for polarized  $J/\psi$  hadroproduction based on global analysis of  $J/\psi$  yield agrees with ALICE, but disagrees with CDF, CMS, and LHCb.
- NRQCD factorization remains among the hottest topics of QCD @ LHC.

# Backup Slides

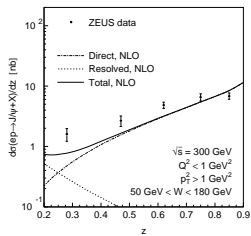
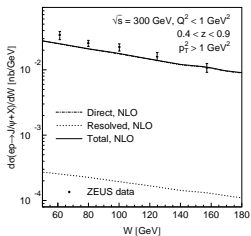
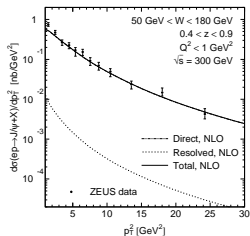
# Comparison with Tevatron (cont.)

## Relative importance of CO processes:



- Short-distance  $\sigma(c\bar{c}[^3P_J^{[8]}]) < 0$  for  $p_T \gtrsim 7$  GeV.
- But: Short-distance cross sections and LDMEs **unphysical** (NRQCD scale and scheme dependence)  $\rightsquigarrow$  No problem!

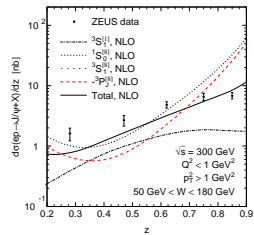
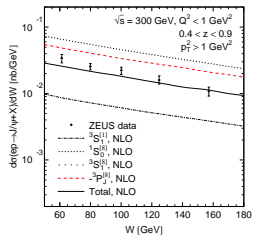
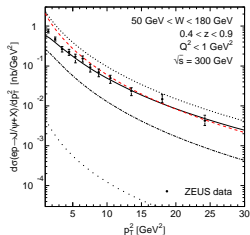
# Comparison with ZEUS at HERA I (cont.)



- Data for  $0.4 < z < 0.9$  exhausted by direct photoproduction.
- Resolved photoproduction only relevant for  $z \lesssim 0.4$ .



# Comparison with ZEUS at HERA I (cont.)



- $\langle \mathcal{O}[^3P_0^{[8]}] \rangle < 0 \rightsquigarrow ^3P_0^{[8]}$  contribution negative.
- Negative interference with  $^1S_0^{[8]}$  contribution beneficial.
- $^3S_1^{[8]}$  contribution negligible here.

# Dependence on low- $p_T$ cut: Global fit

Vary low- $p_T$  cut on  $pp$  and  $p\bar{p}$  data:

| Data left                                      | $p_T > 1$ GeV<br>148 points | $p_T > 2$ GeV<br>134 points | $p_T > 3$ GeV<br>119 points | $p_T > 5$ GeV<br>86 points | $p_T > 7$ GeV<br>60 points |
|--|-----------------------------|-----------------------------|-----------------------------|----------------------------|----------------------------|
| $\langle \sigma^{J/\psi}[^1S_0^{[8]}] \rangle$ | $5.68 \pm 0.37$             | $4.25 \pm 0.43$             | $4.97 \pm 0.44$             | $4.92 \pm 0.49$            | $3.91 \pm 0.51$            |
| $\langle \sigma^{J/\psi}[^3S_1^{[8]}] \rangle$ | $0.90 \pm 0.50$             | $2.94 \pm 0.58$             | $2.24 \pm 0.59$             | $2.23 \pm 0.62$            | $2.96 \pm 0.64$            |
| $\langle \sigma^{J/\psi}[^3P_0^{[8]}] \rangle$ | $-2.23 \pm 0.17$            | $-1.38 \pm 0.20$            | $-1.61 \pm 0.20$            | $-1.59 \pm 0.22$           | $-1.16 \pm 0.23$           |

↪ Global fit insensitive to low- $p_T$  cut on  $pp$  and  $p\bar{p}$  data as long as  $\gamma p$ ,  $\gamma\gamma$  (74 points with  $p_T > 1$  GeV), and  $e^+e^-$  data (1 point) are retained.

Vary low- $p_T$  cut on  $\gamma p$  and  $\gamma\gamma$  data:

| Data left                                      | $p_T > 1$ GeV<br>74 points | $p_T > 2$ GeV<br>30 points | $p_T > 3$ GeV<br>15 points | $p_T > 5$ GeV<br>5 points | $p_T > 7$ GeV<br>1 points |
|--|----------------------------|----------------------------|----------------------------|---------------------------|---------------------------|
| $\langle \sigma^{J/\psi}[^1S_0^{[8]}] \rangle$ | $4.97 \pm 0.44$            | $5.10 \pm 0.92$            | $4.05 \pm 1.17$            | $5.44 \pm 1.27$           | $9.56 \pm 1.59$           |
| $\langle \sigma^{J/\psi}[^3S_1^{[8]}] \rangle$ | $2.24 \pm 0.59$            | $2.11 \pm 1.22$            | $3.52 \pm 1.56$            | $1.73 \pm 1.68$           | $-3.66 \pm 2.09$          |
| $\langle \sigma^{J/\psi}[^3P_0^{[8]}] \rangle$ | $-1.61 \pm 0.20$           | $-1.58 \pm 0.48$           | $-0.97 \pm 0.63$           | $-1.63 \pm 0.68$          | $-3.73 \pm 0.83$          |

↪ Global fit insensitive to **moderate** low- $p_T$  cut on  $\gamma p$  and  $\gamma\gamma$  data as long as  $pp$  and  $p\bar{p}$  data (119 points with  $p_T > 3$  GeV), and  $e^+e^-$  data (1 point) are retained.

# Dependence on low- $p_T$ cut: Fit to $pp$ and $p\bar{p}$ data only

Vary low- $p_T$  cut:

| Data left                                      | $p_T > 1$ GeV<br>148 points | $p_T > 2$ GeV<br>134 points | $p_T > 3$ GeV<br>119 points | $p_T > 5$ GeV<br>86 points | $p_T > 7$ GeV<br>60 points |
|--|-----------------------------|-----------------------------|-----------------------------|----------------------------|----------------------------|
| $\langle \sigma^{J/\psi}[^1S_0^{[8]}] \rangle$ | $8.54 \pm 0.52$             | $16.85 \pm 1.23$            | $11.02 \pm 1.67$            | $1.68 \pm 2.20$            | $2.18 \pm 2.56$            |
| $\langle \sigma^{J/\psi}[^3S_1^{[8]}] \rangle$ | $-2.66 \pm 0.69$            | $-13.36 \pm 1.60$           | $-5.56 \pm 2.19$            | $8.75 \pm 2.98$            | $10.34 \pm 3.55$           |
| $\langle \sigma^{J/\psi}[^3P_0^{[8]}] \rangle$ | $-3.63 \pm 0.23$            | $-7.70 \pm 0.61$            | $-4.46 \pm 0.87$            | $2.20 \pm 1.23$            | $3.50 \pm 1.50$            |
| $M_0$  | $2.25 \pm 0.12$             | $3.51 \pm 0.19$             | $3.29 \pm 0.20$             | $5.50 \pm 0.29$            | $8.24 \pm 0.58$            |
| $M_1$  | $6.37 \pm 0.19$             | $5.80 \pm 0.19$             | $5.54 \pm 0.20$             | $3.27 \pm 0.29$            | $1.63 \pm 0.43$            |

↪ Fit highly sensitive to low- $p_T$  cut.

Comparison with fit to unpolarized, direct CDF II data with  $p_T > 7$  GeV  
 Y.-Q. Ma, K. Wang, and K.-T. Chao, Phys. Rev. D **84**, 114001 (2011):

$$M_0 = (8.54 \pm 1.02) \times 10^{-2} \text{ GeV}^3$$

$$M_1 = (1.67 \pm 1.05) \times 10^{-3} \text{ GeV}^3$$