

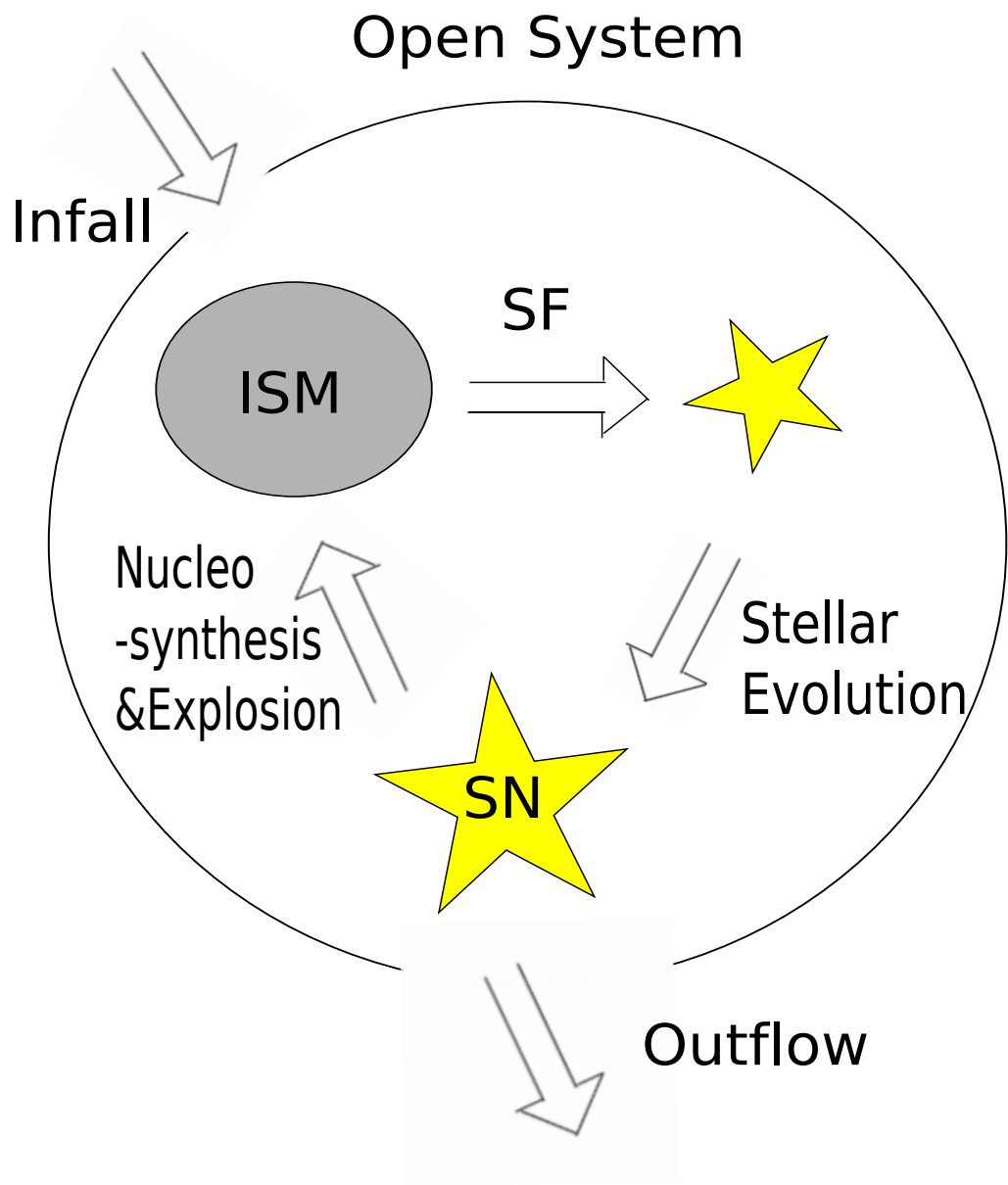
Chemical Evolution Model  
of  
Fornax Dwarf Spheroidal Galaxy

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# Outline

- Halo model and Gas Dynamics of Fornax dSph
- Analytic Chemical Evolution Model  
(homogeneous mixing)
- Numerical Chemical Evolution Model  
(inhomogeneous mixing)



$$\psi = \lambda_* M_g^{1.5}$$

$$\psi \approx \frac{M_g}{\tau}$$

$$\tau \approx \frac{1}{\sqrt{G\rho}}$$

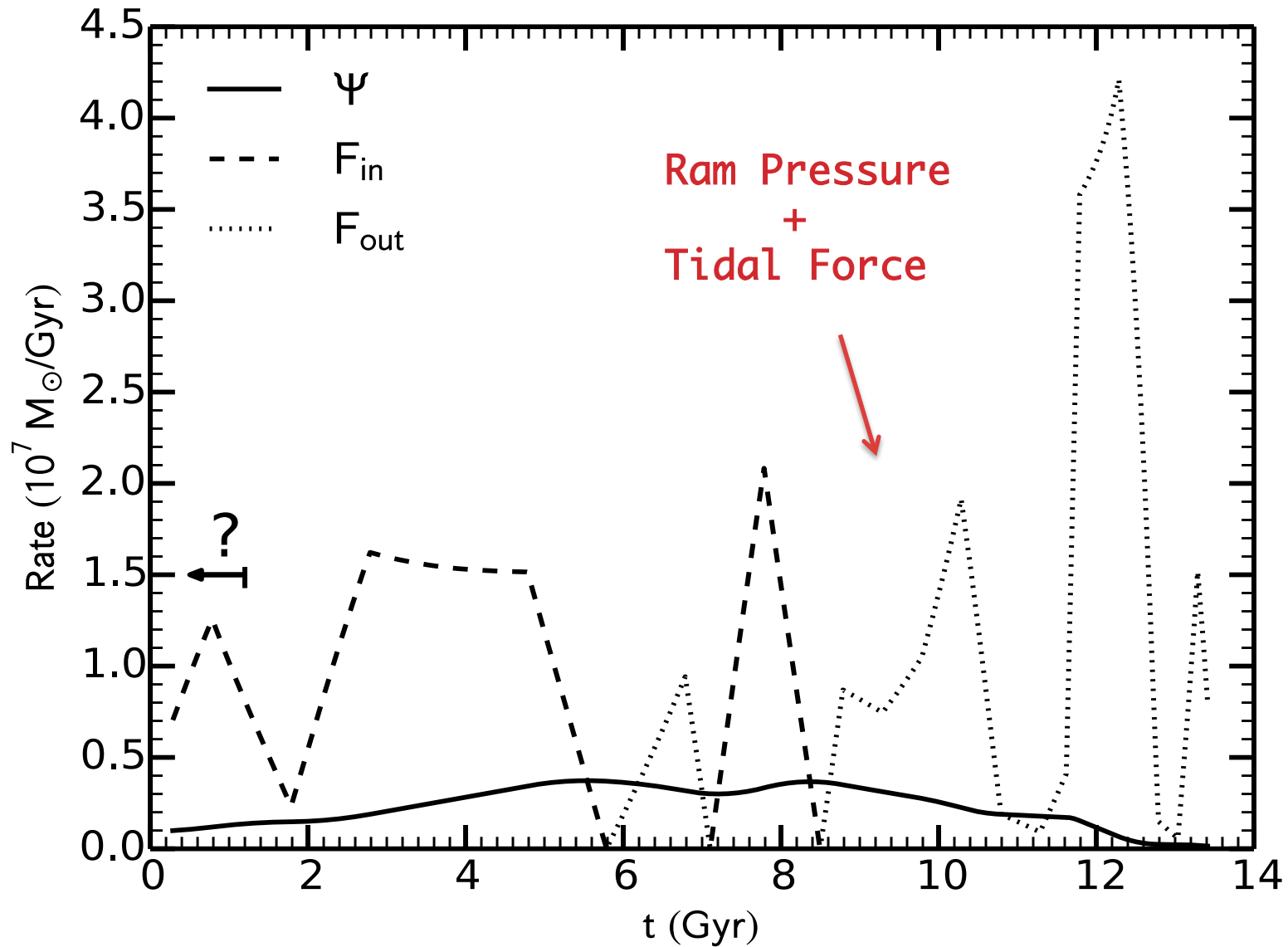
$$\frac{dM_g}{dt} = F_{in} - \psi - F_{out}$$

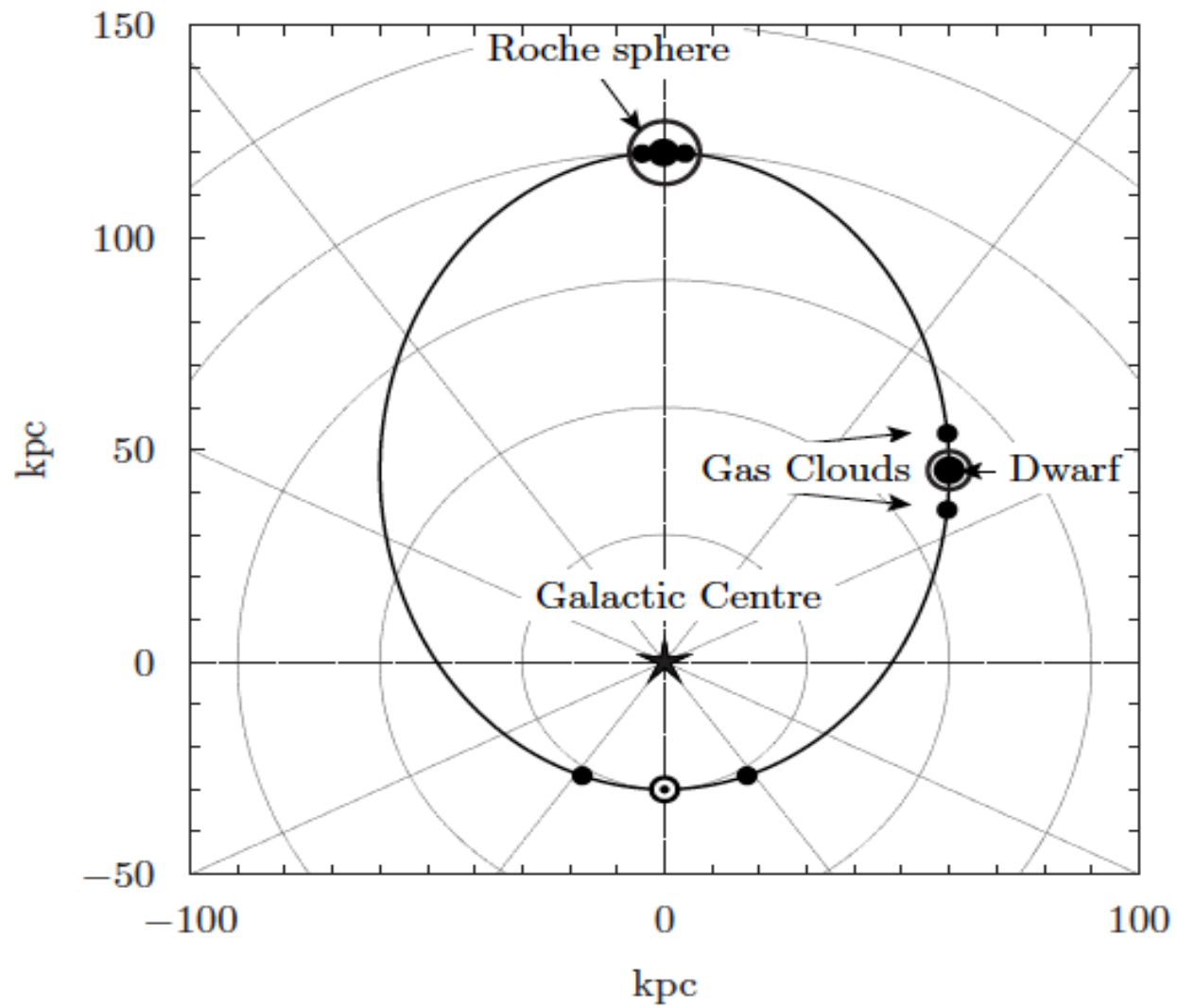
$$\frac{dM_g}{dt} + \psi = F_{in} - F_{out}$$

$$F_{out} = 0 \Rightarrow F_{in} = \psi + \frac{dM_g}{dt}$$

$$F_{in} = 0 \Rightarrow F_{out} = -\psi - \frac{dM_g}{dt}$$

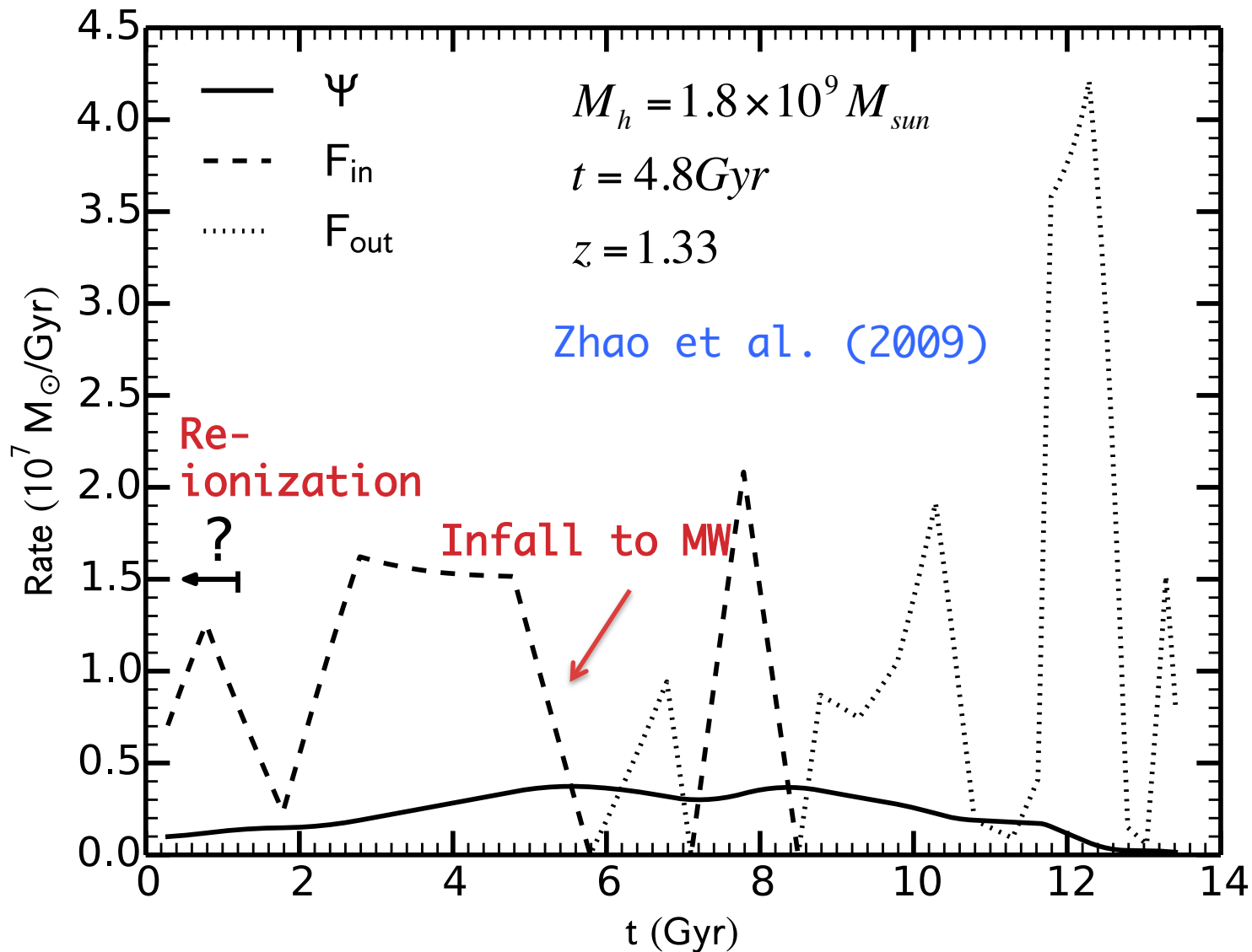
# Gas Dynamics based on SFH



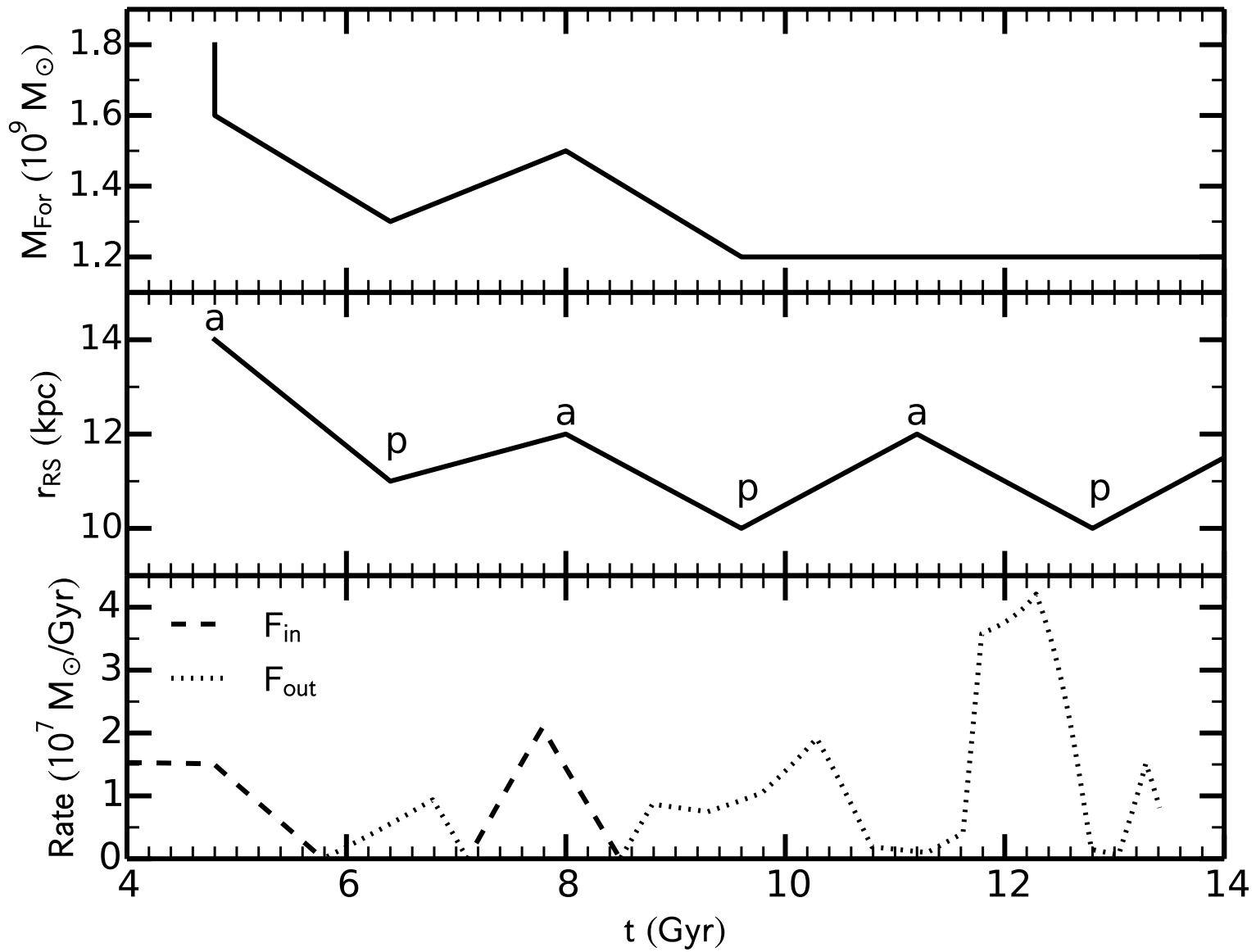


Nichols, M., Lin, D. et al (2012)

# Gas Dynamics based on SFH



Yuan, Qian, Jing (2014 submitted)



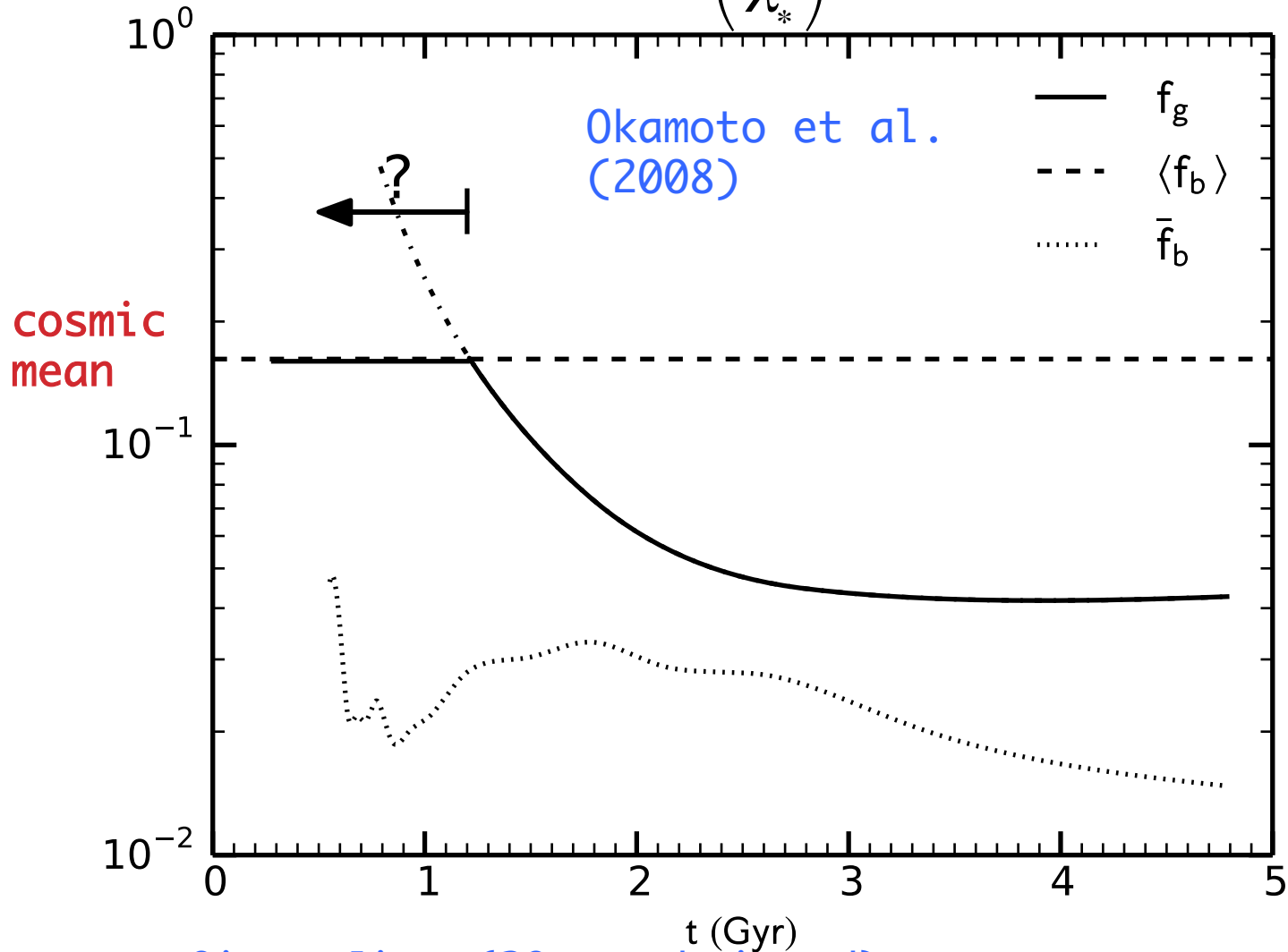
Yuan, Qian, Jing (2014 submitted)



$$f_b = \frac{M_g}{M_h}$$

$$M_g = f_{b,\text{cosmic}} M_h \quad t < 1.2 \text{ Gyr}$$

$$M_g = \left( \frac{\psi}{\lambda_*} \right)^{2/3} \quad t > 1.2 \text{ Gyr}$$



Yuan, Qian, Jing (2014 submitted)

# Analytic Model

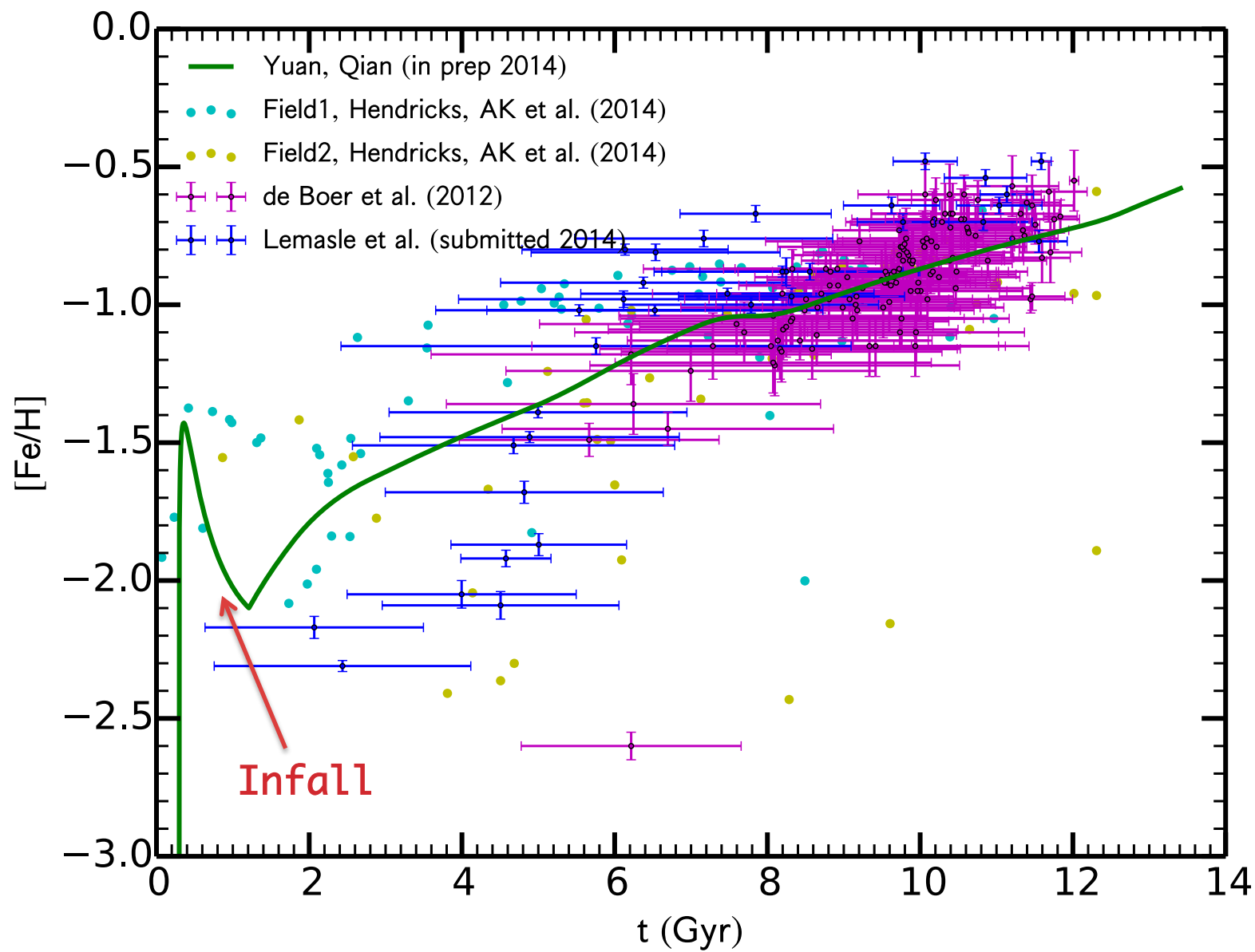
## --- homogeneous Mixing

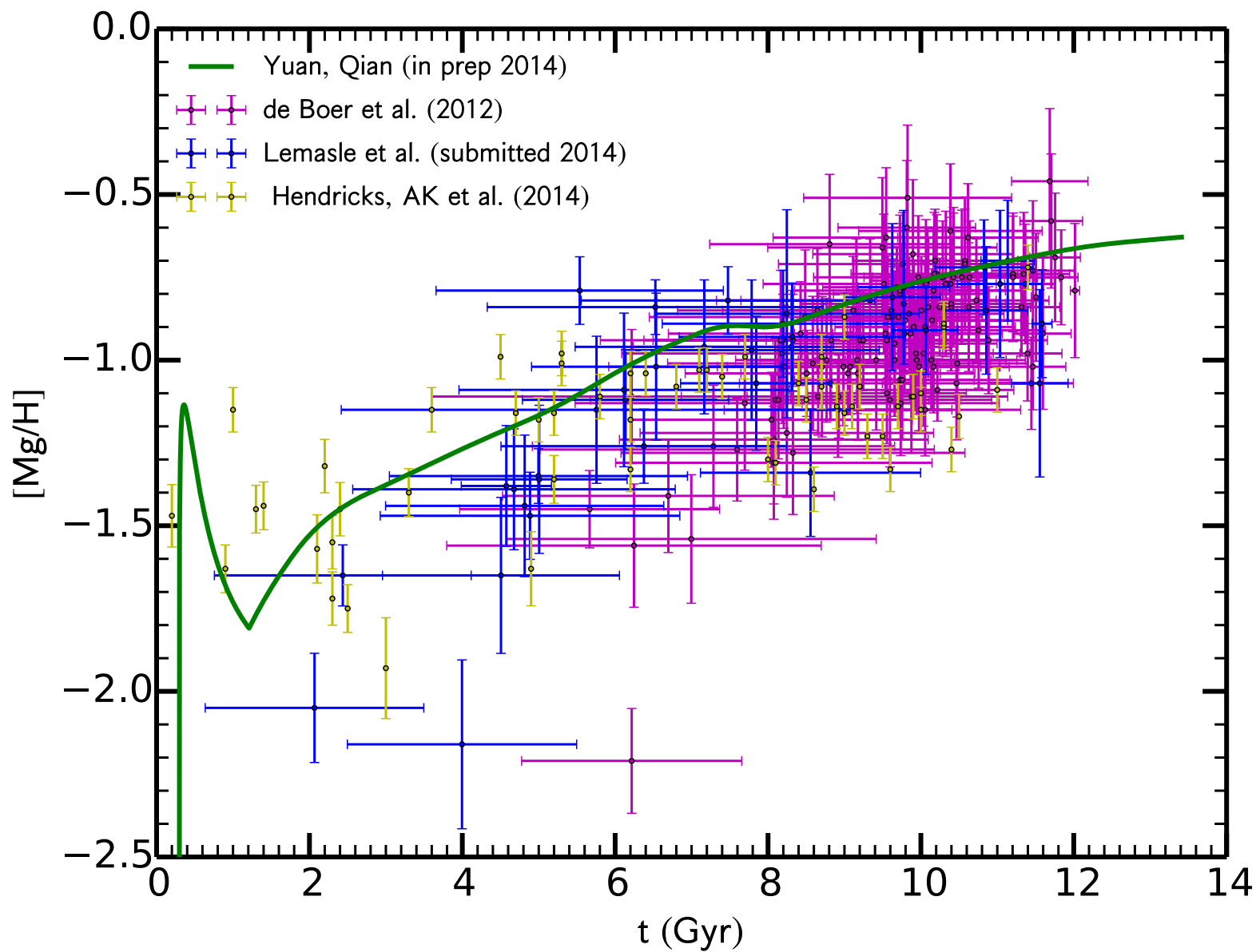
$$\frac{d(Z_{Fe}M_g)}{dt} = P_{Fe}(\psi) - F_{out}Z_{Fe} + F_{in}Z_{Fe,in}$$

$$P_{Fe} = \eta_{Fe}^{cc}\psi + \eta_{Fe}^{Ia} \int_{\tau_{Ia}}^t \psi(t - \tau)D(\tau)d\tau$$

Yields from Heger & Woosley (2008)

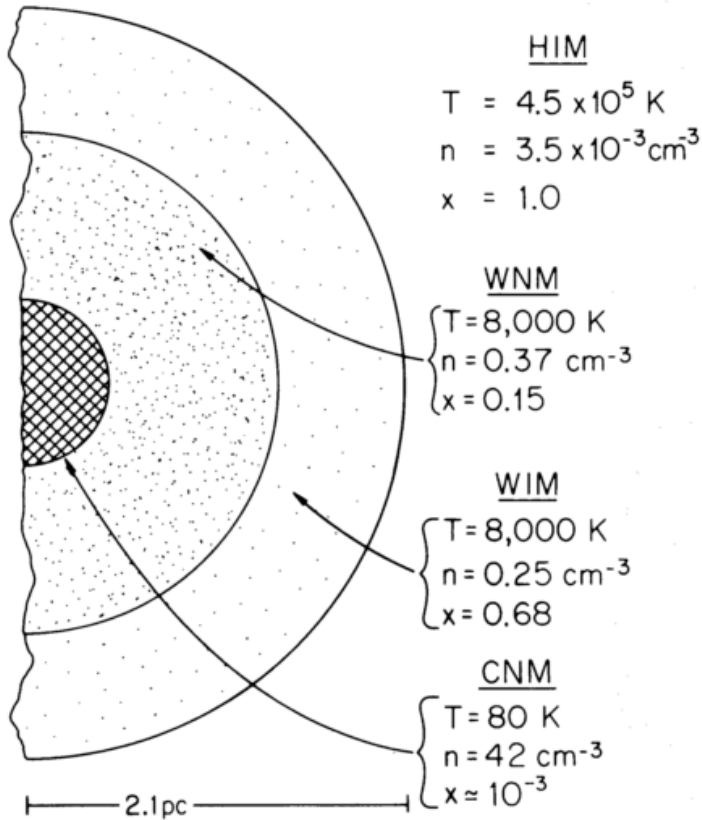
Standard Mixing, E=1.2 B, S=4 Piston



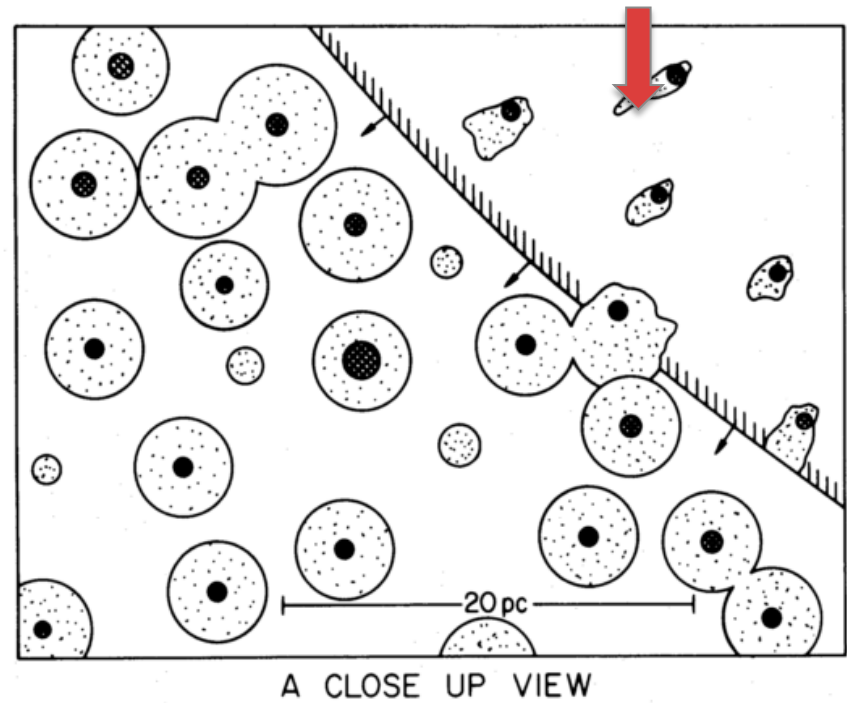


# Structure of ISM

## A SMALL CLOUD



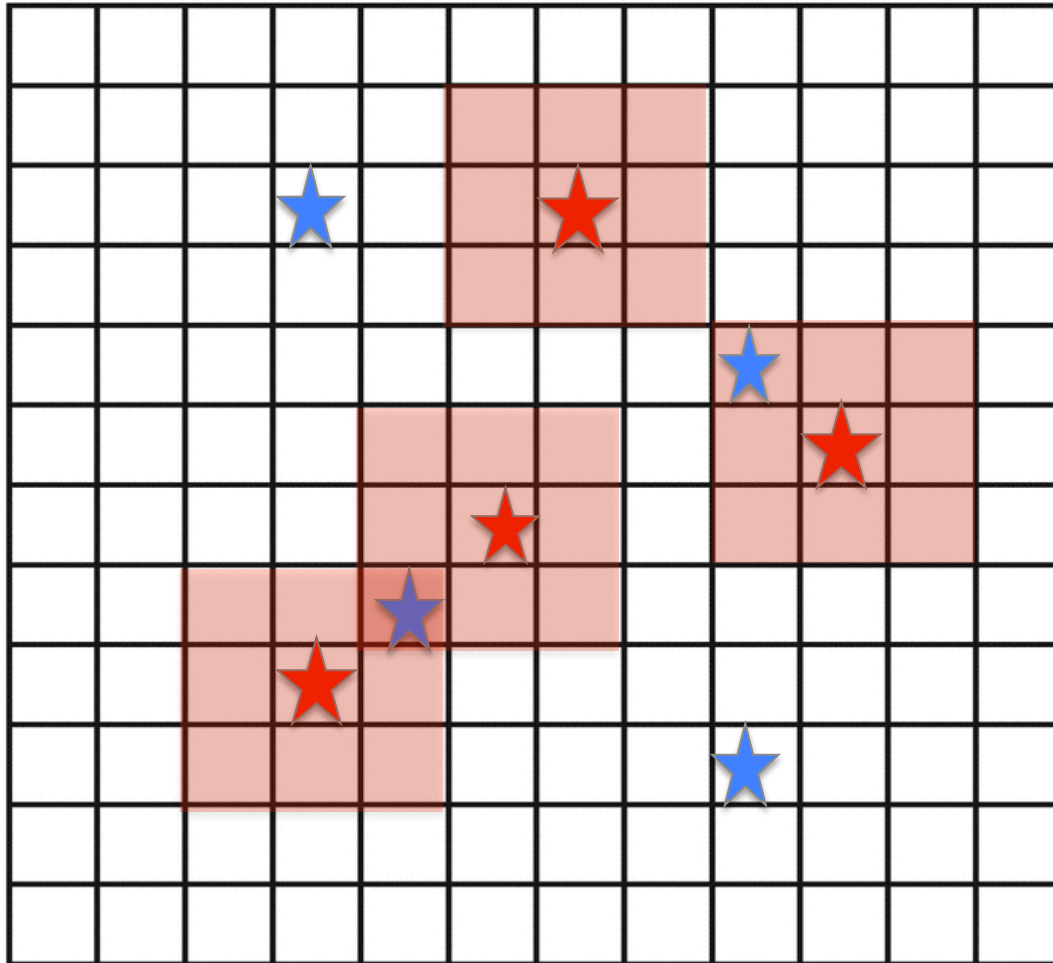
SN hot bubble



McKee & Ostriker (1977)

# Numerical Model

## --- Inhomogeneous Mixing



$$N = 2000^2$$

$$\Delta t = 0.25 \text{Gyr}$$

$$m_{0,i} = \frac{M_{g,i}}{N}$$

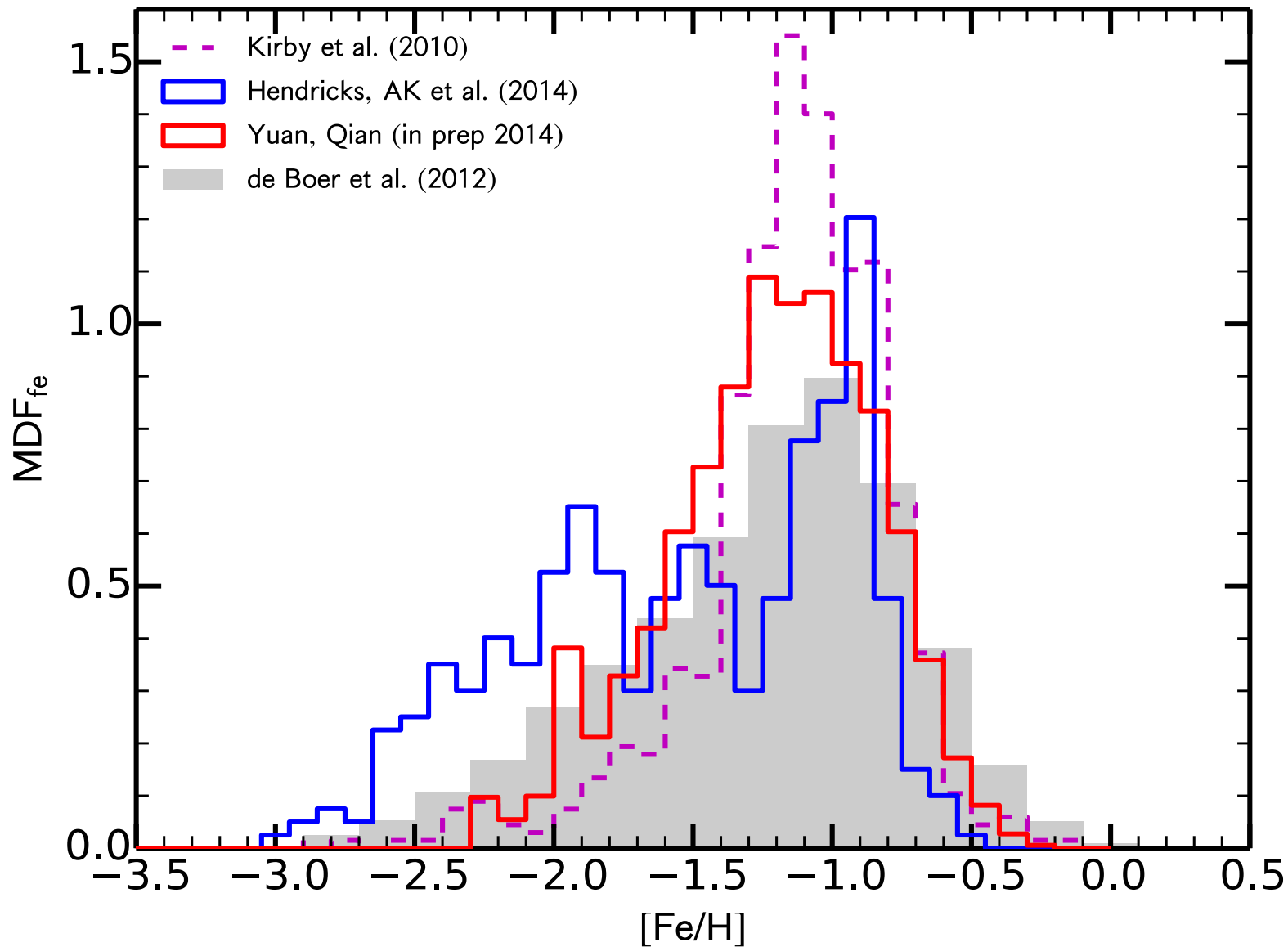
$$Z_{Fe,i,(x,y)} m_{0,i} = m_{0,i-1} Z_{Fe,i-1,(x,y)}$$

$Z_{Fe,0,1}$	$Z_{Fe,0,2}$	$Z_{Fe,0,2}$
$Z_{Fe,1,0}$	$Z_{Fe,1,1}$	$Z_{Fe,1,2}$
$Z_{Fe,2,0}$	$Z_{Fe,2,1}$	$Z_{Fe,2,2}$

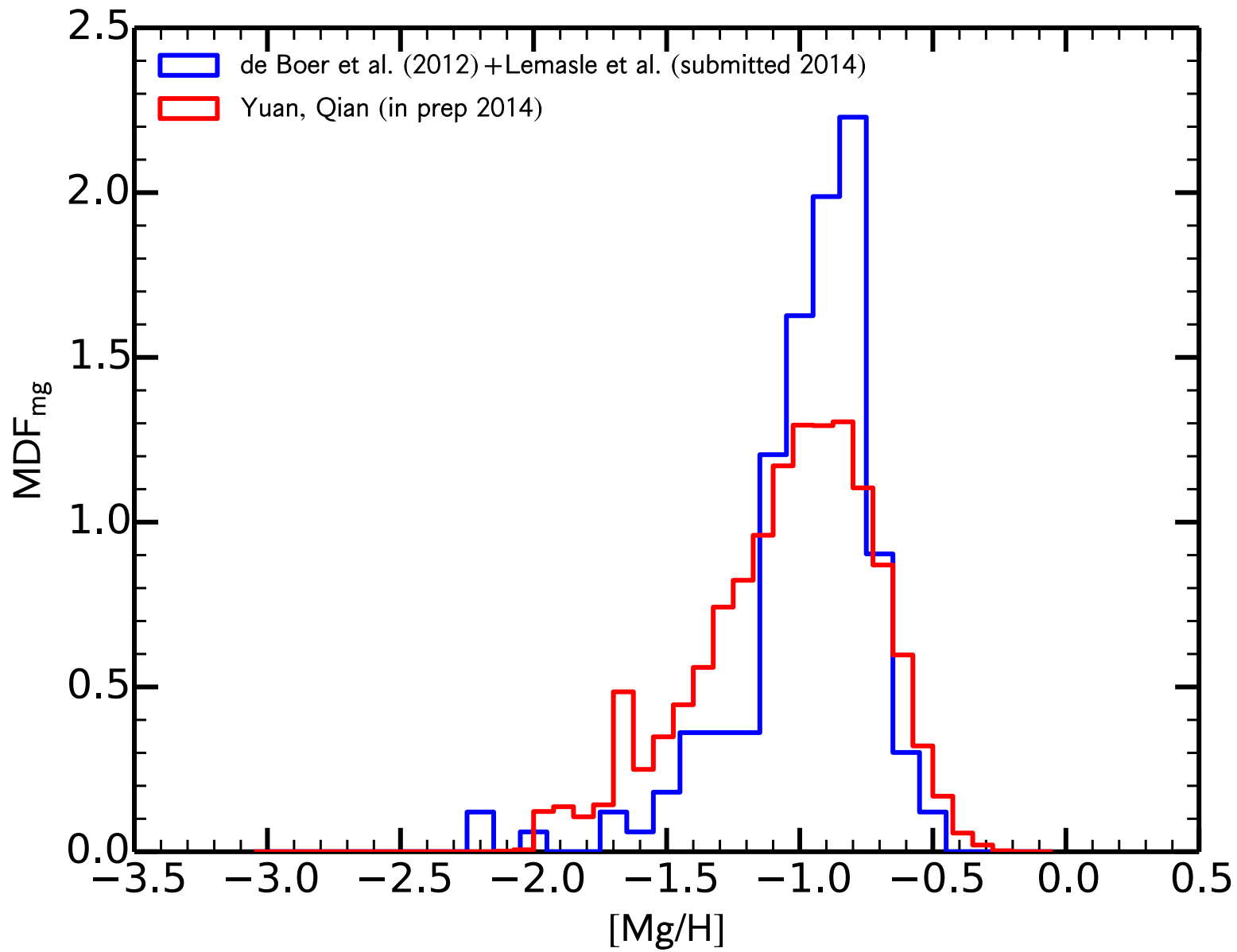
$$n_{mix,i} = \frac{M_{mix}}{m_{0,i}} \quad \delta Y_{Fe,i} = \frac{Y_{Fe}}{n_{mix,i}}$$

$$Z_{Fe,i,(x,y)} = Z_{Fe,i-1,(x,y)} + \delta Y_{Fe,i}$$

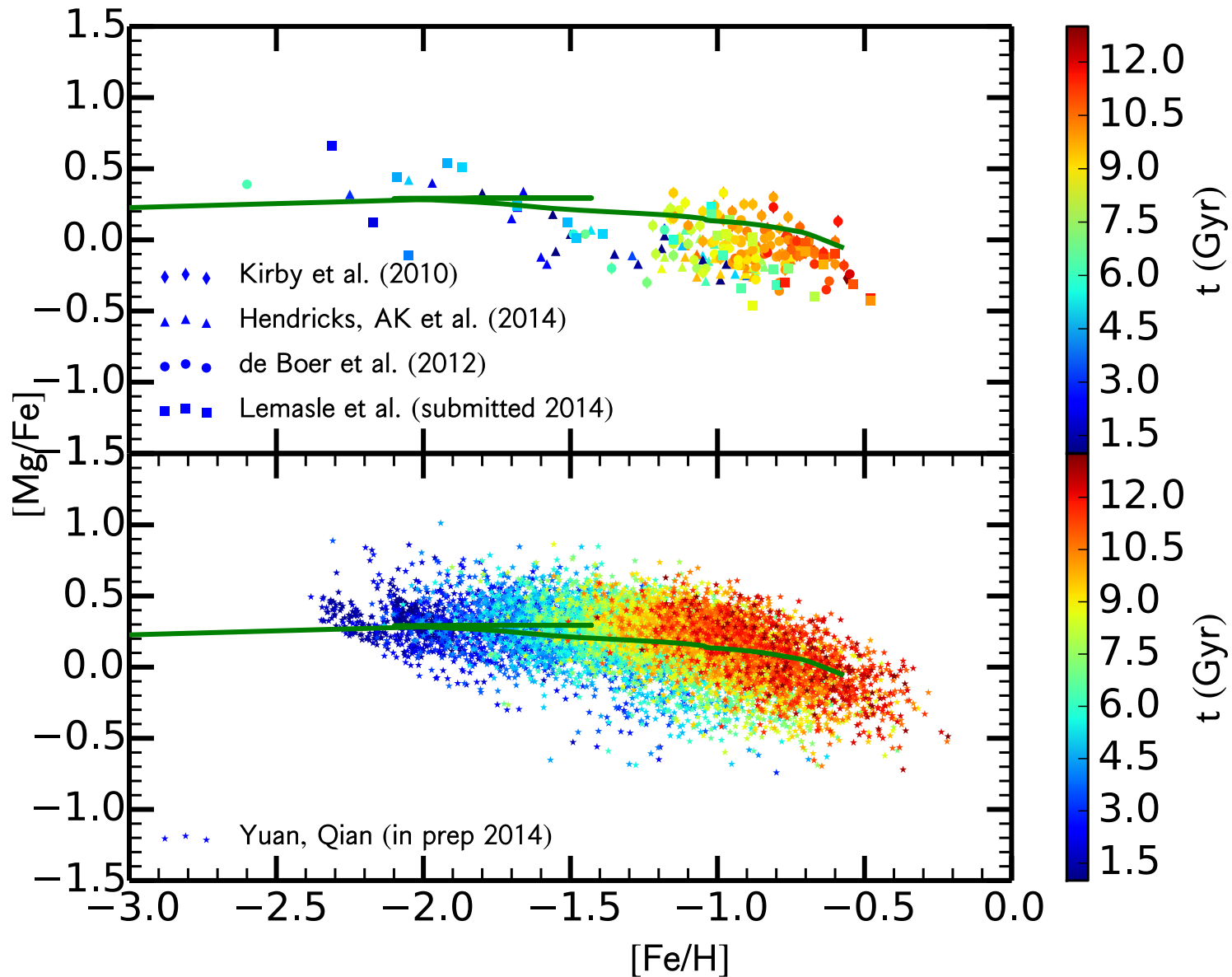
# Comparison with Observation

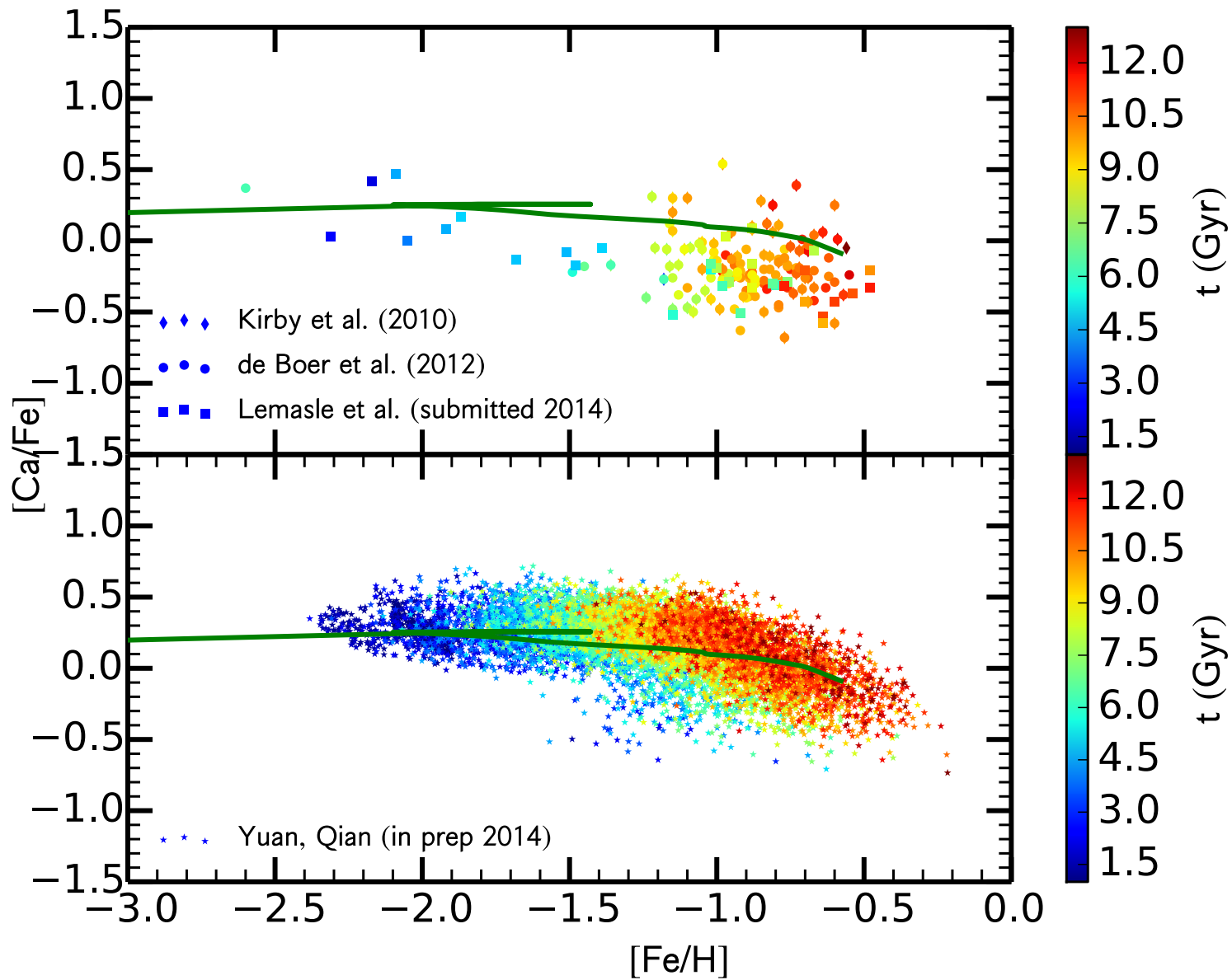


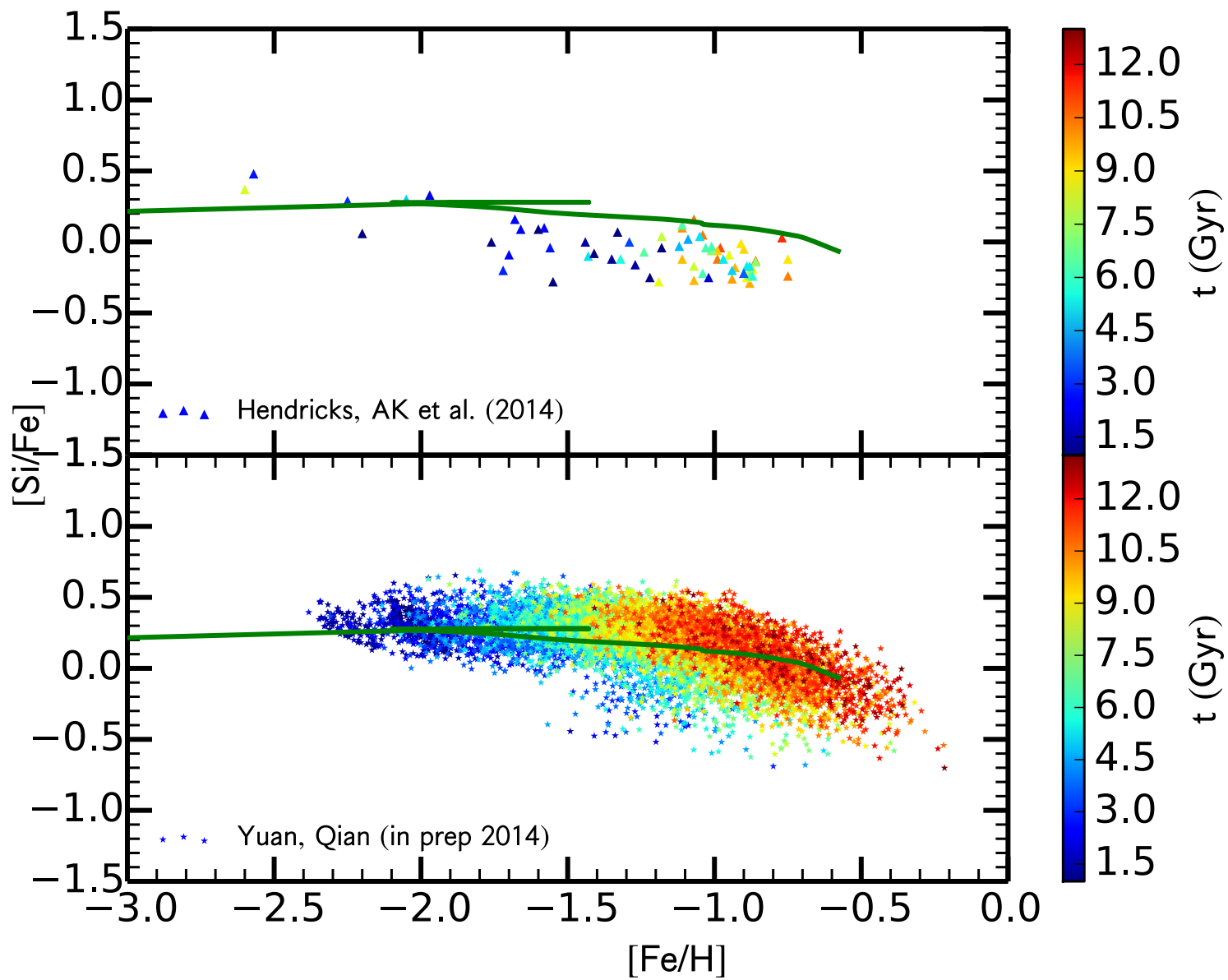


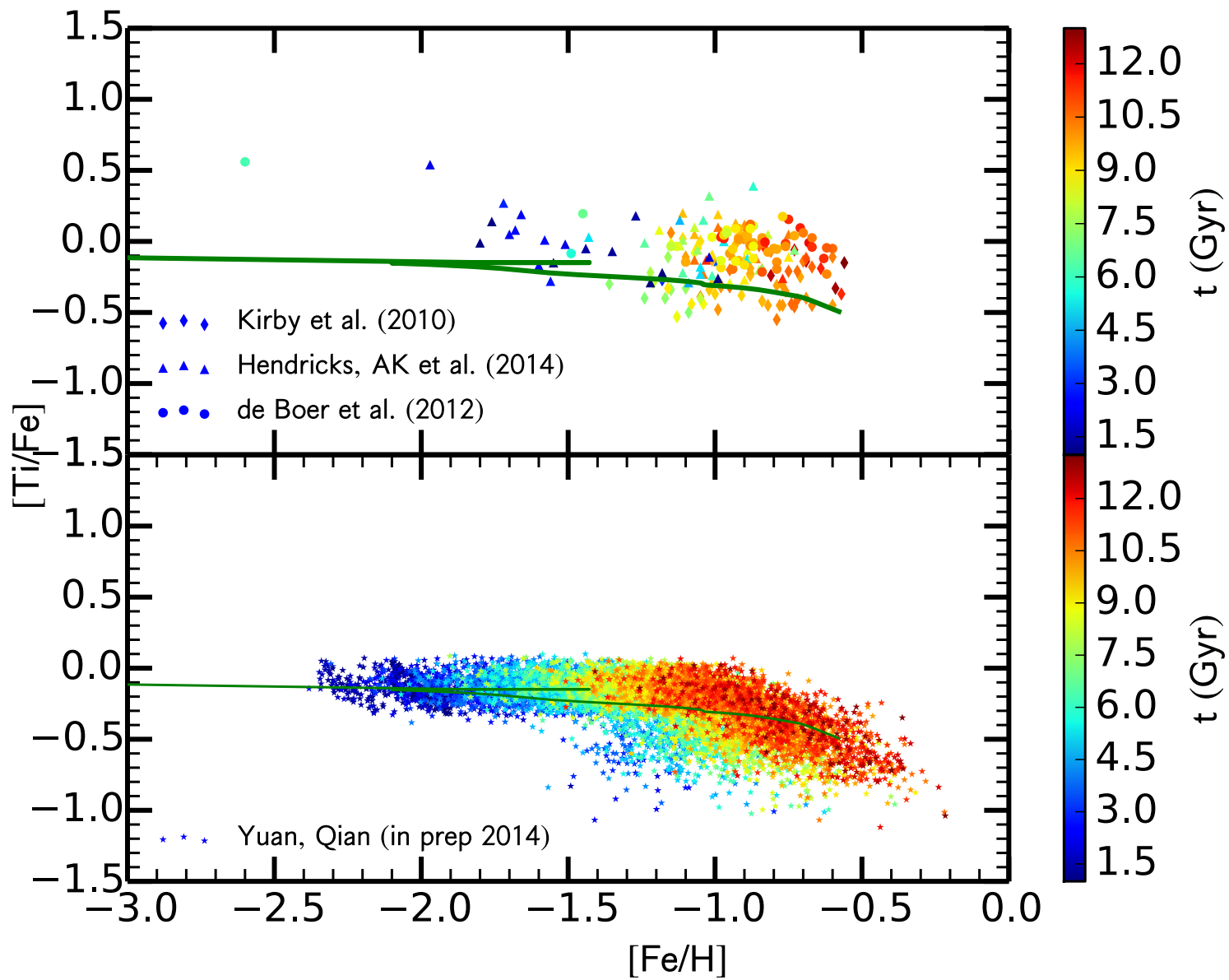


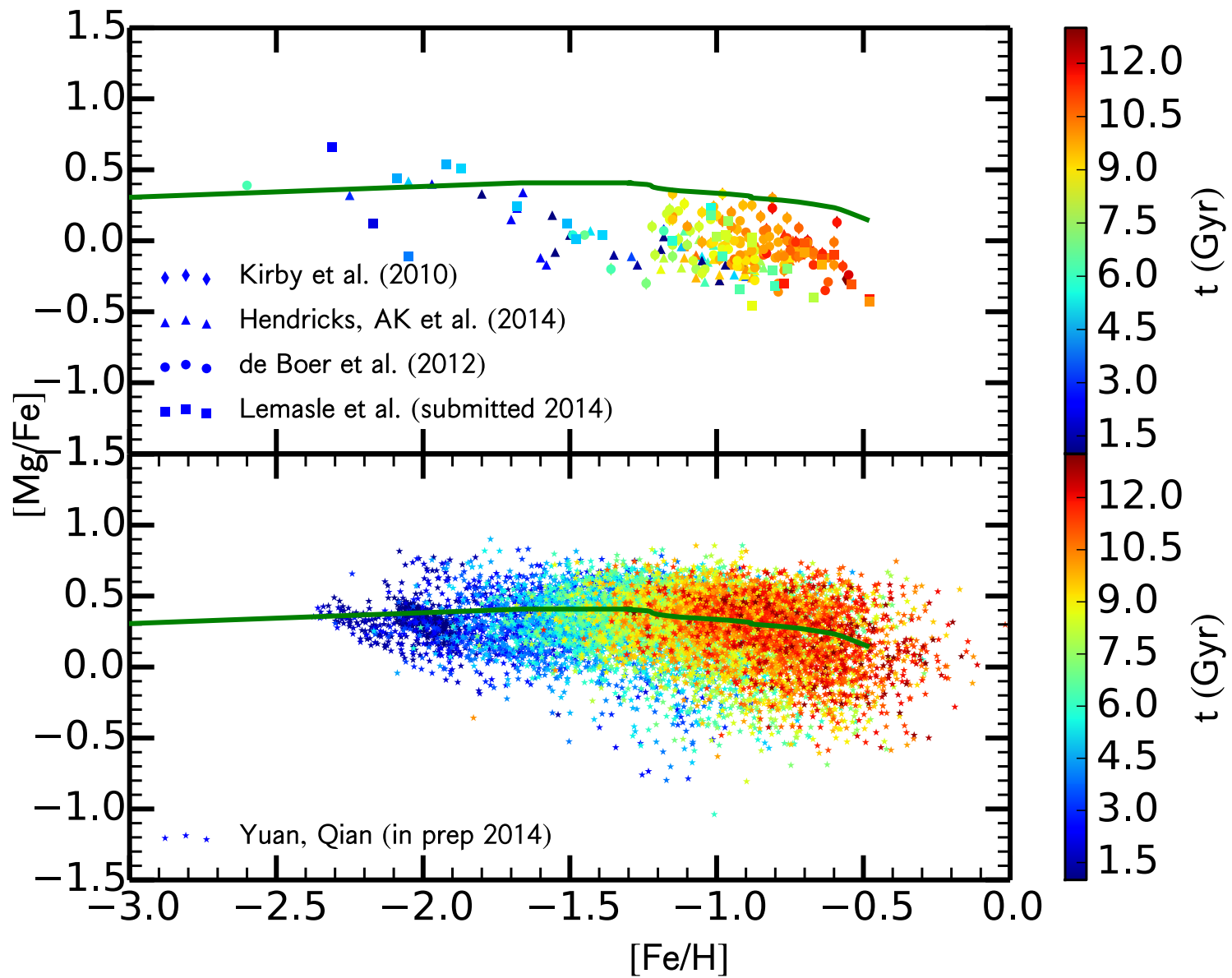
# Scatter comes from astrophysical sites !





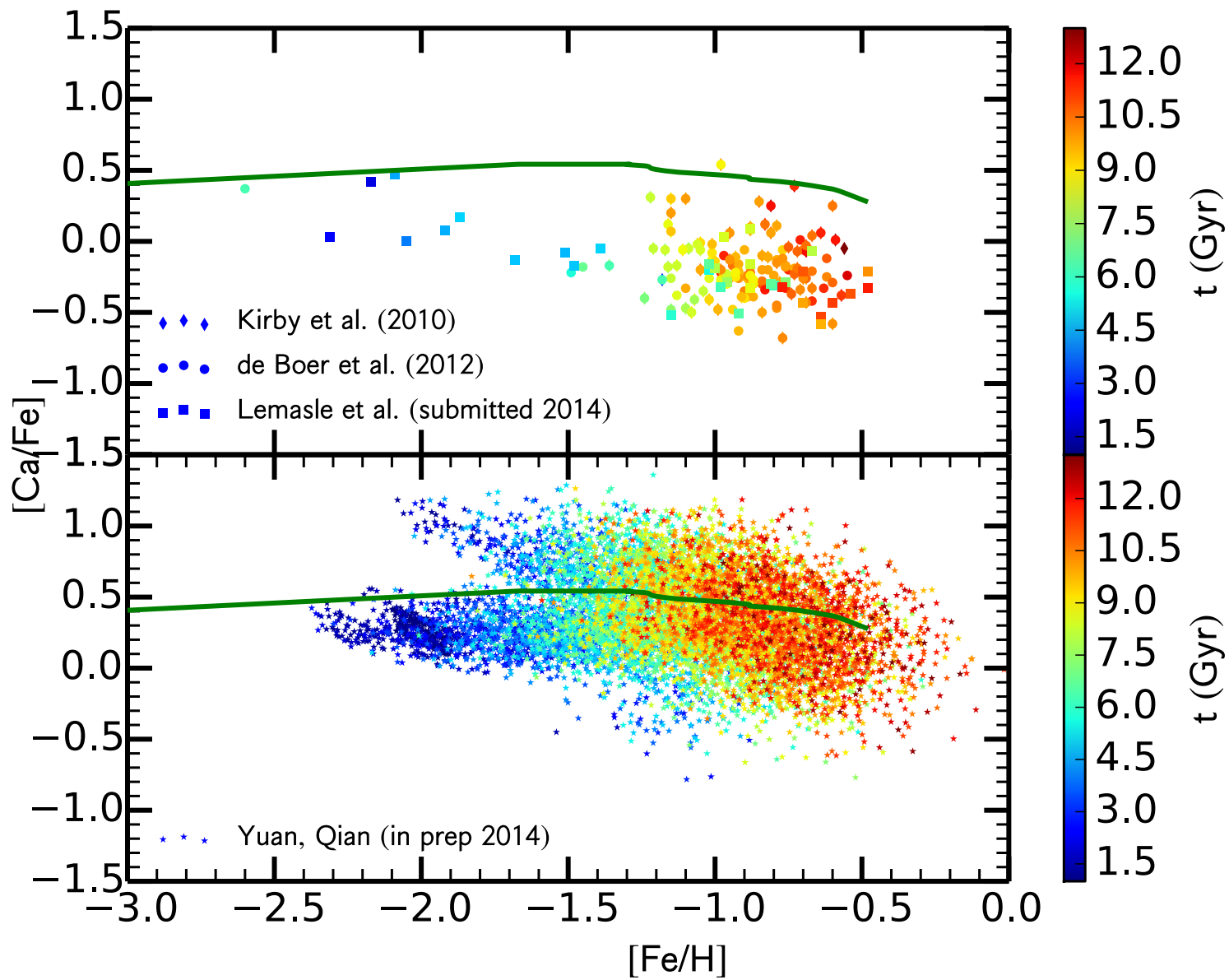


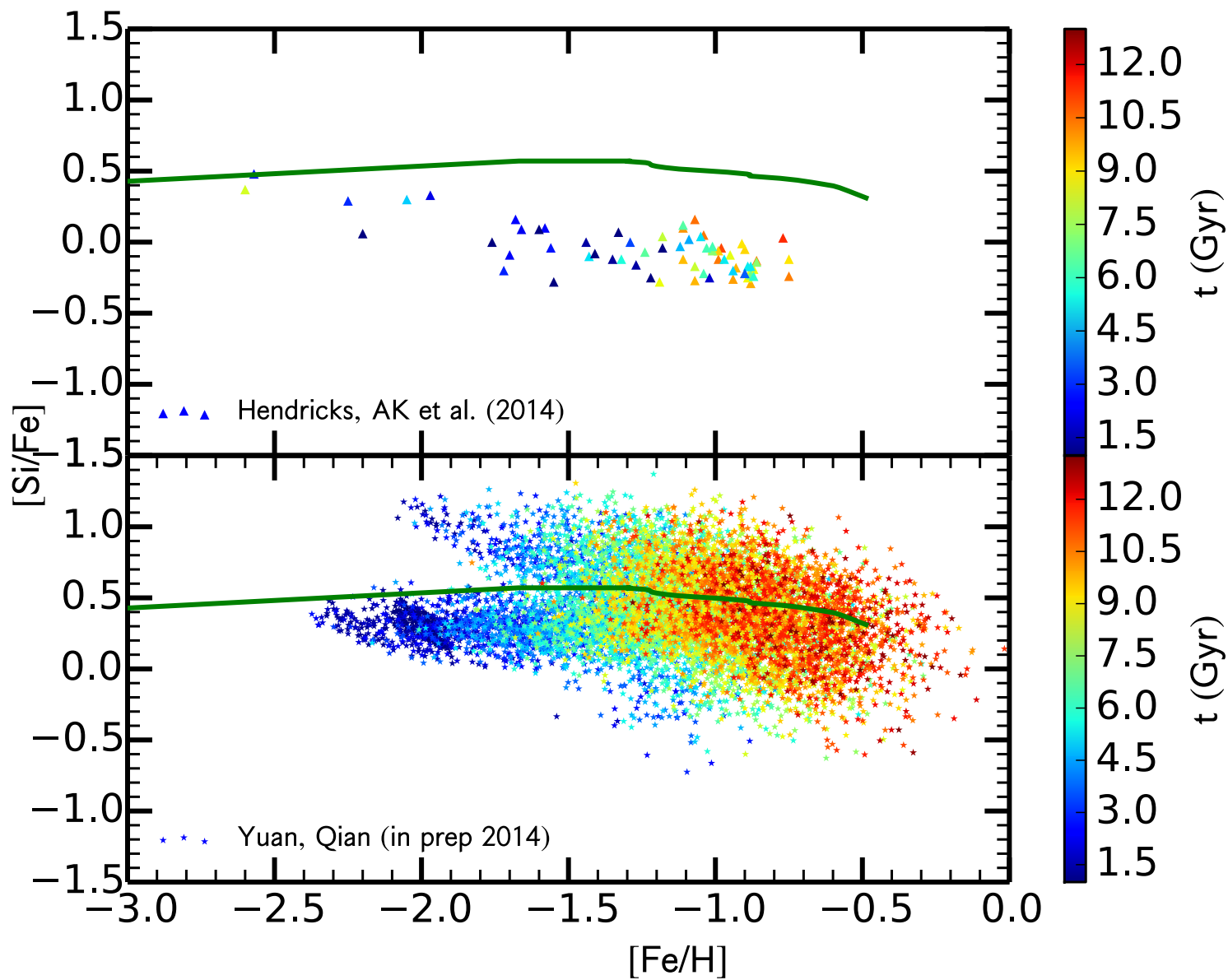




Yields from Heger & Woosley (2008)

80 Msun – 100 Msun, Standard Mixing,  $E=5.0$  B,  $S=4$  Piston







# Future work

- SN Model with different E, mixing ?
- 1D, 2D, 3D?
- Motivation from Observations?
- Other dSph: Sculptor, Carina, etc
- r-process/s-process elements
  
- Hydro-simulation of gas dynamics and chemical evolution in dSph
- Dark Matter Halo Model for Fornax