

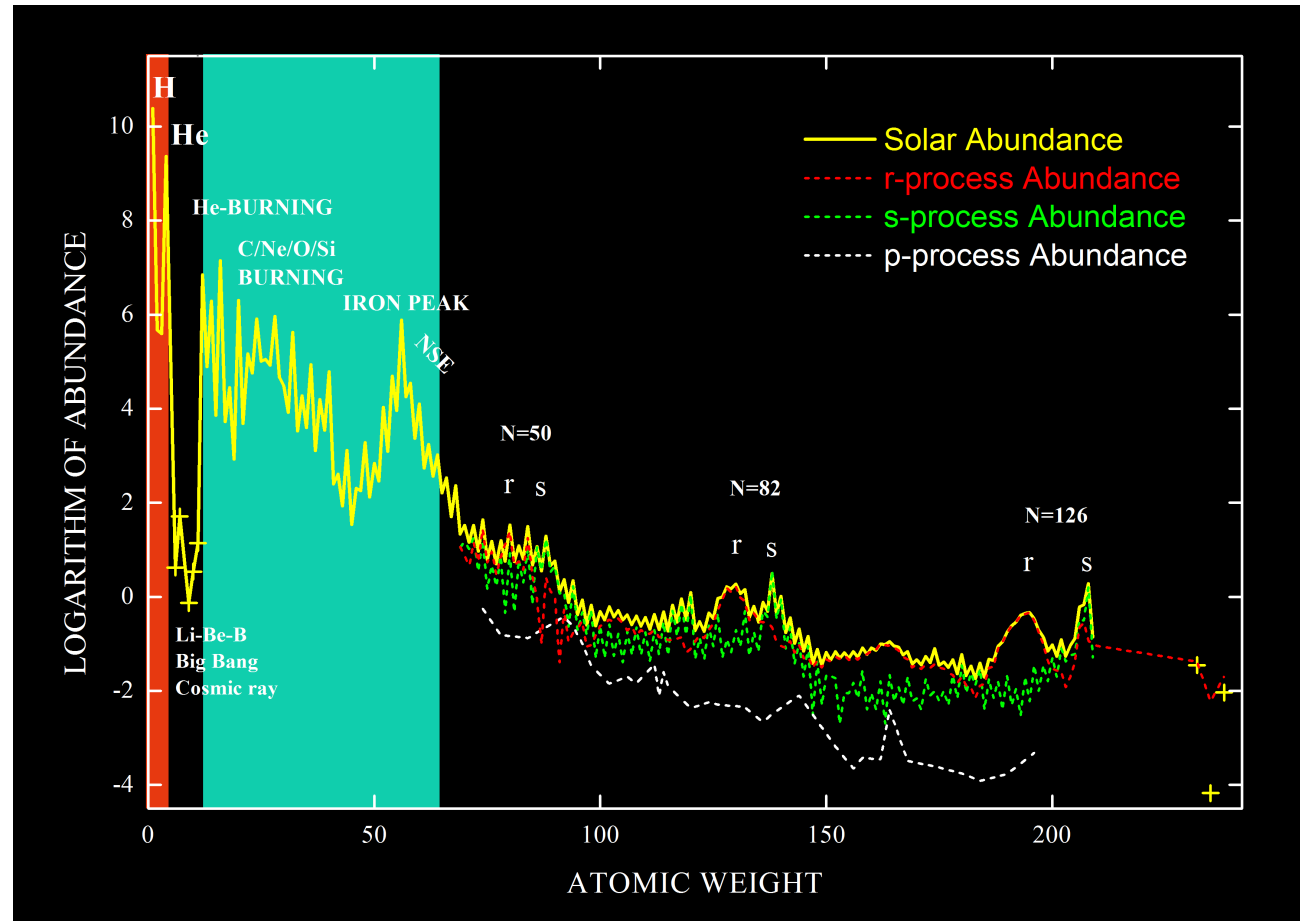
Parametric Study for Heavy Element Nucleosynthesis

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Heavy Elements in Universe

In solar system

- Hydrogen+Helium \sim 98% by mass
—> proton-rich environment
- “Metal” \sim 2% by mass
—> “neutron-rich” nuclei



Neutron is needed to produce the heavy nuclei.

Factories for (Neutron Rich) Heavy Elements

Supernovae:

- prompt bounce-back explosion; Hillebrandt 1978
- neutrino-driven wind; Qian & Woosley 1996
- shocked surface of O-Ne-Mg core; Ning et al. 2007
- neutrino-induced in He-shell; Banerjee et al. 2011
- jets; Winteler et al. 2012

Neutron Star Mergers:

- dynamical ejecta; Goriely et al. 2011, Korobkin et al. 2012
- evaporation disk; Fernandez & Metzger 2013

High initial temperature and fast adiabatic expansion.

Parametric Model

- Dynamical time scale $\tau_{\text{dyn.}}$ for expansion:

exponential form $T(t) = T_0 \exp(-t/\tau_{\text{dyn.}})$

power-law form $T(t) = T_0 / (1 + t/\tau_{\text{dyn.}})$

- Electron fraction $Y_e = Y_n / (Y_n + Y_p)$

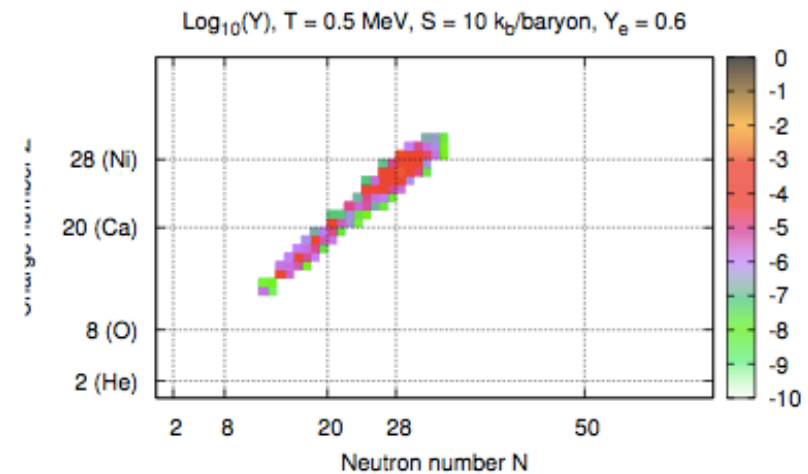
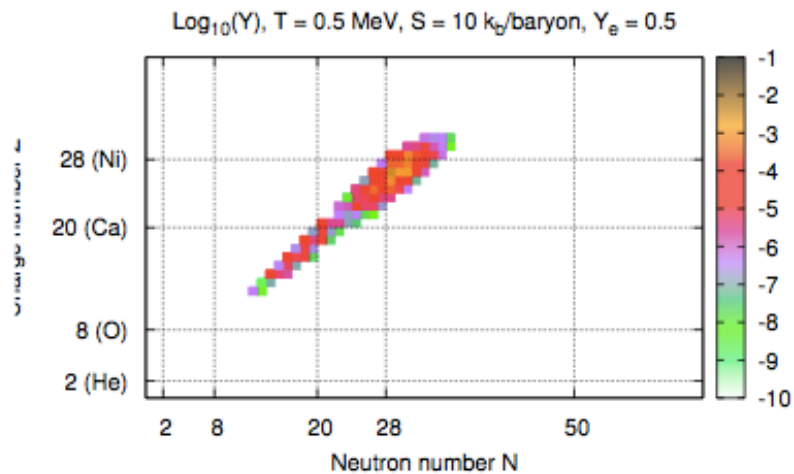
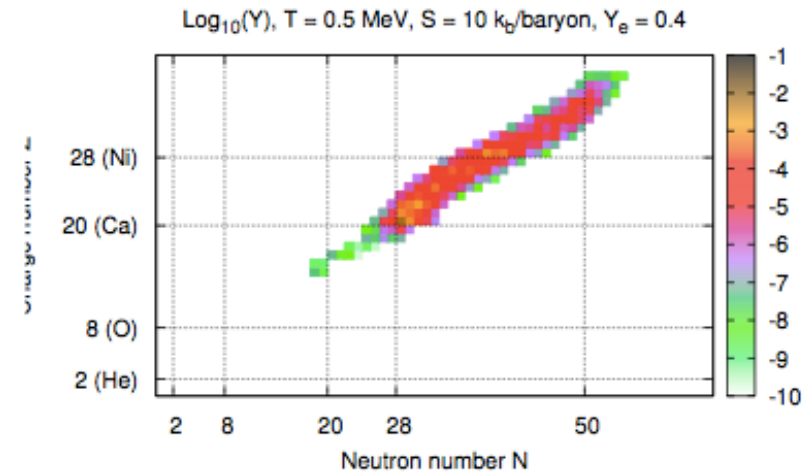
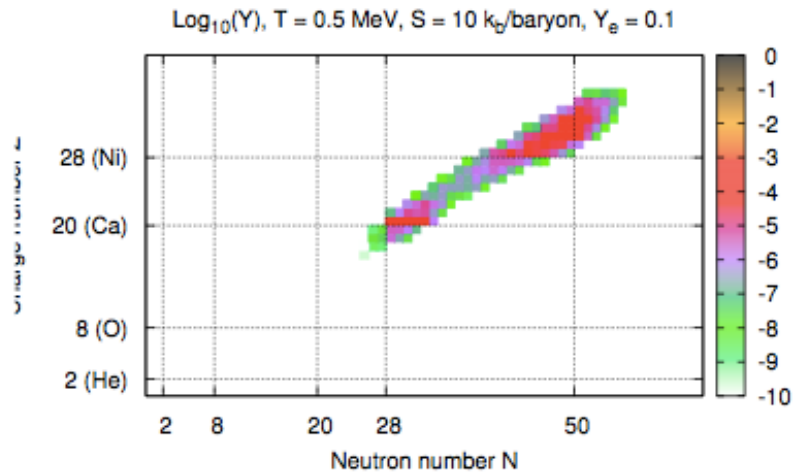
- Entropy stays constant

$$S(t) = S(T(t), \rho(t)) \equiv S_0$$

Any nucleosynthesis model is specified by a set of

$$(\tau_{\text{dyn.}}, T_0, S_0, Y_e)$$

NSE Abundances



$T=0.5 \text{ MeV}$, $S=10 \text{ k}_b/\text{baryon}$, $Y_e=0.1 / 0.4 / 0.5 / 0.6$

Equilibria in NSE: I

Various equilibria exist in NSE process, which favor specified nucleus:

$$(n/p, \gamma) \Leftrightarrow (\gamma, n/p)$$

$$S_{n,p}^* = T_9 \{1.052 + 0.198 \times [1.5 \log T_9 - \log(\rho_5 Y_{n,p})]\}$$

$$(\alpha, \gamma) \Leftrightarrow (\gamma, \alpha)$$

$$S_{\alpha}^* = T_9 \{1.29 + 0.198 \times [1.5 \log T_9 - \log(4\rho_5 Y_{\alpha})]\}$$

$$(n, p) \Leftrightarrow (p, n)$$

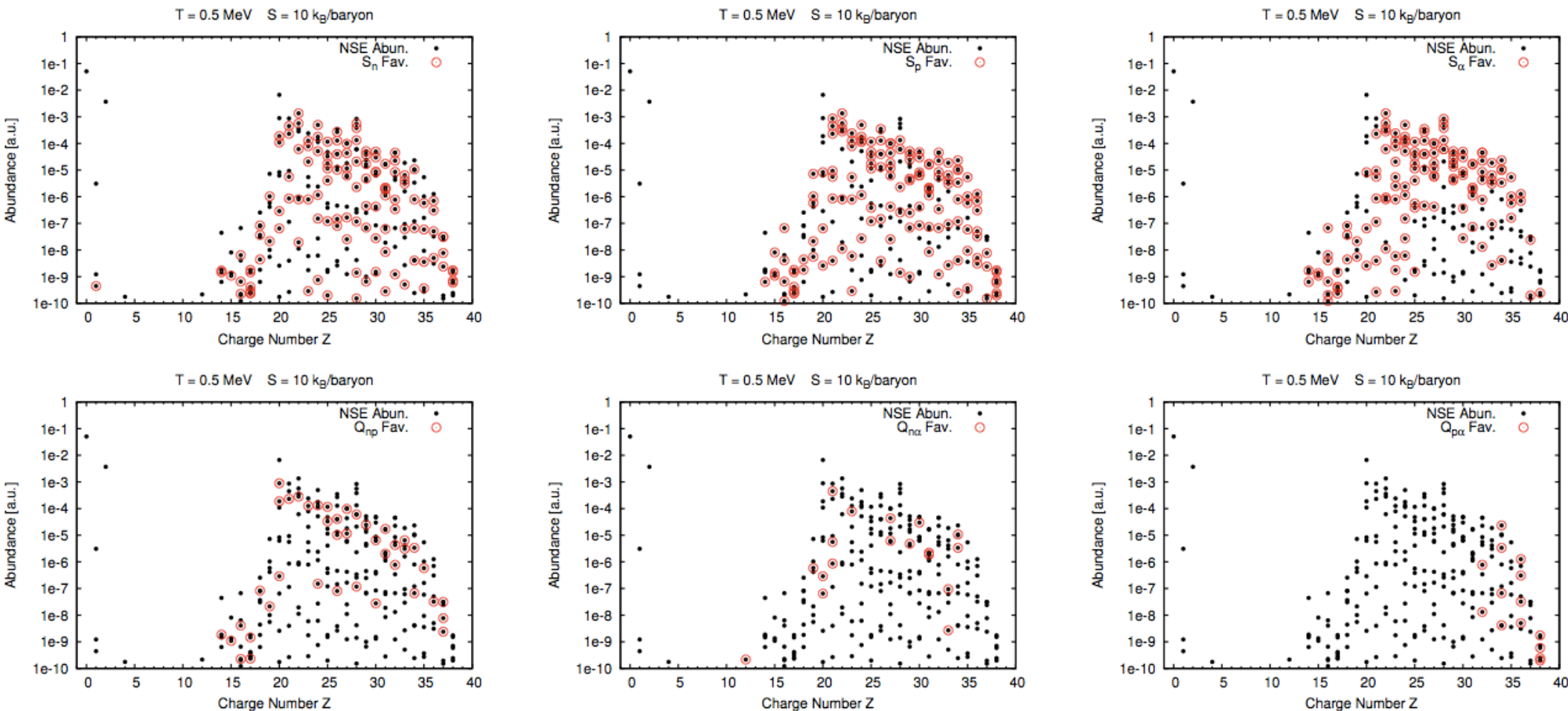
$$Q_{(n,p)}^* = 0.198 T_9 \log(Y_p/Y_n)$$

$$(n/p, \alpha) \Leftrightarrow (\alpha, n/p)$$

$$S_{(n/p,\alpha)}^* = 0.198 T_9 \log(Y_{\alpha}/4Y_{n,p})$$

Equilibria in NSE: II

$Y_e=0.4$

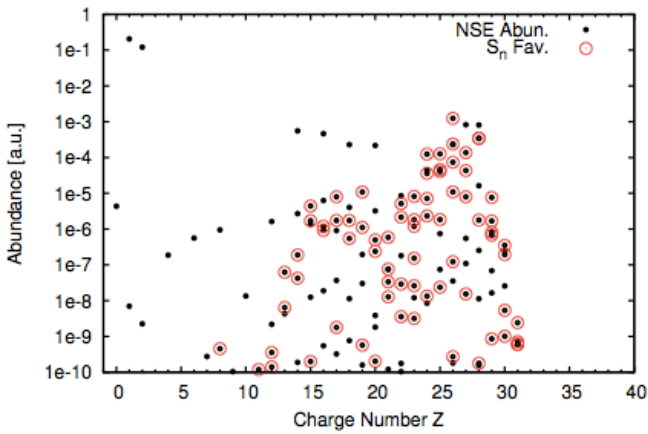


Equilibria between capture reactions and photo-disintegration dominate the NSE abundance

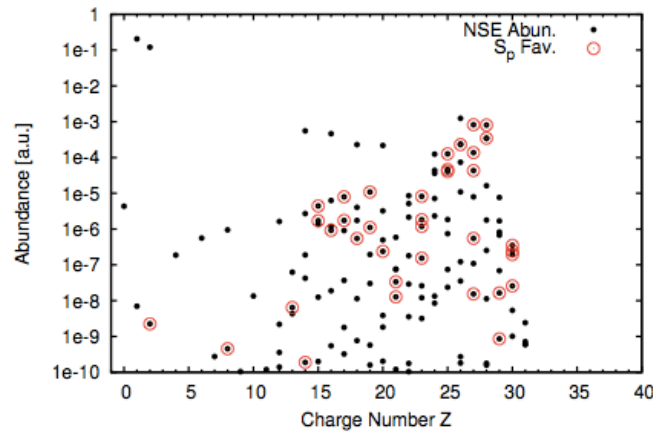
Equilibria in NSE: III

$Y_e=0.6$

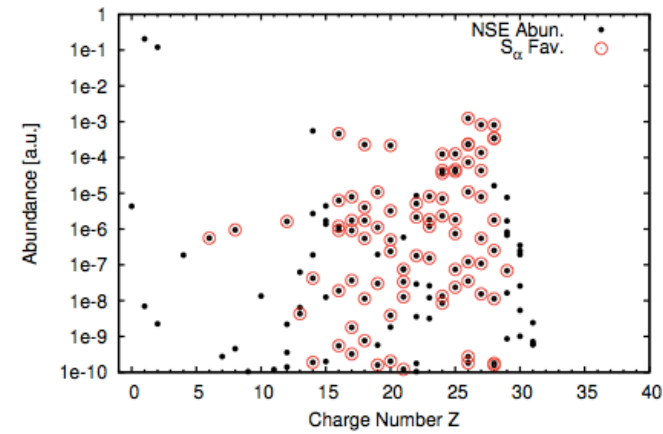
$T = 0.5 \text{ MeV}$ $S = 10 \text{ k}_B/\text{baryon}$



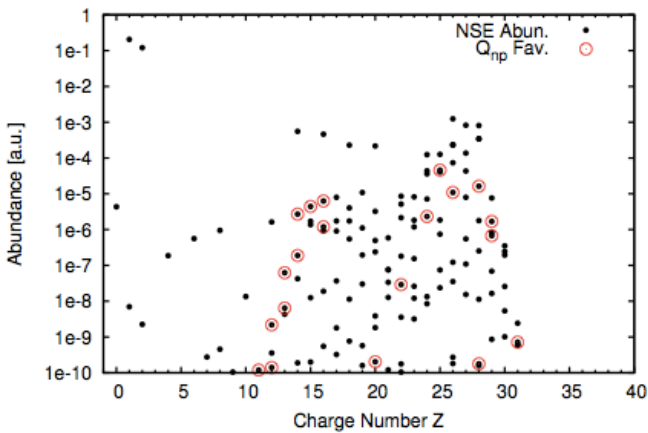
$T = 0.5 \text{ MeV}$ $S = 10 \text{ k}_B/\text{baryon}$



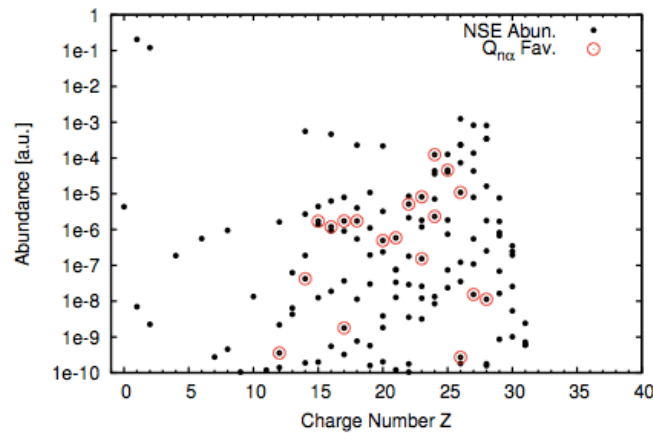
$T = 0.5 \text{ MeV}$ $S = 10 \text{ k}_B/\text{baryon}$



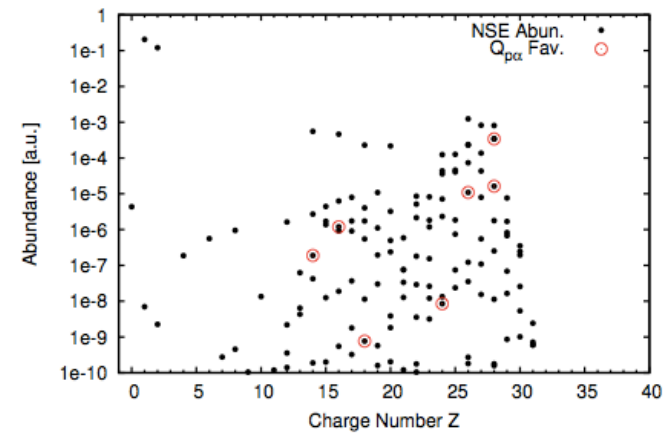
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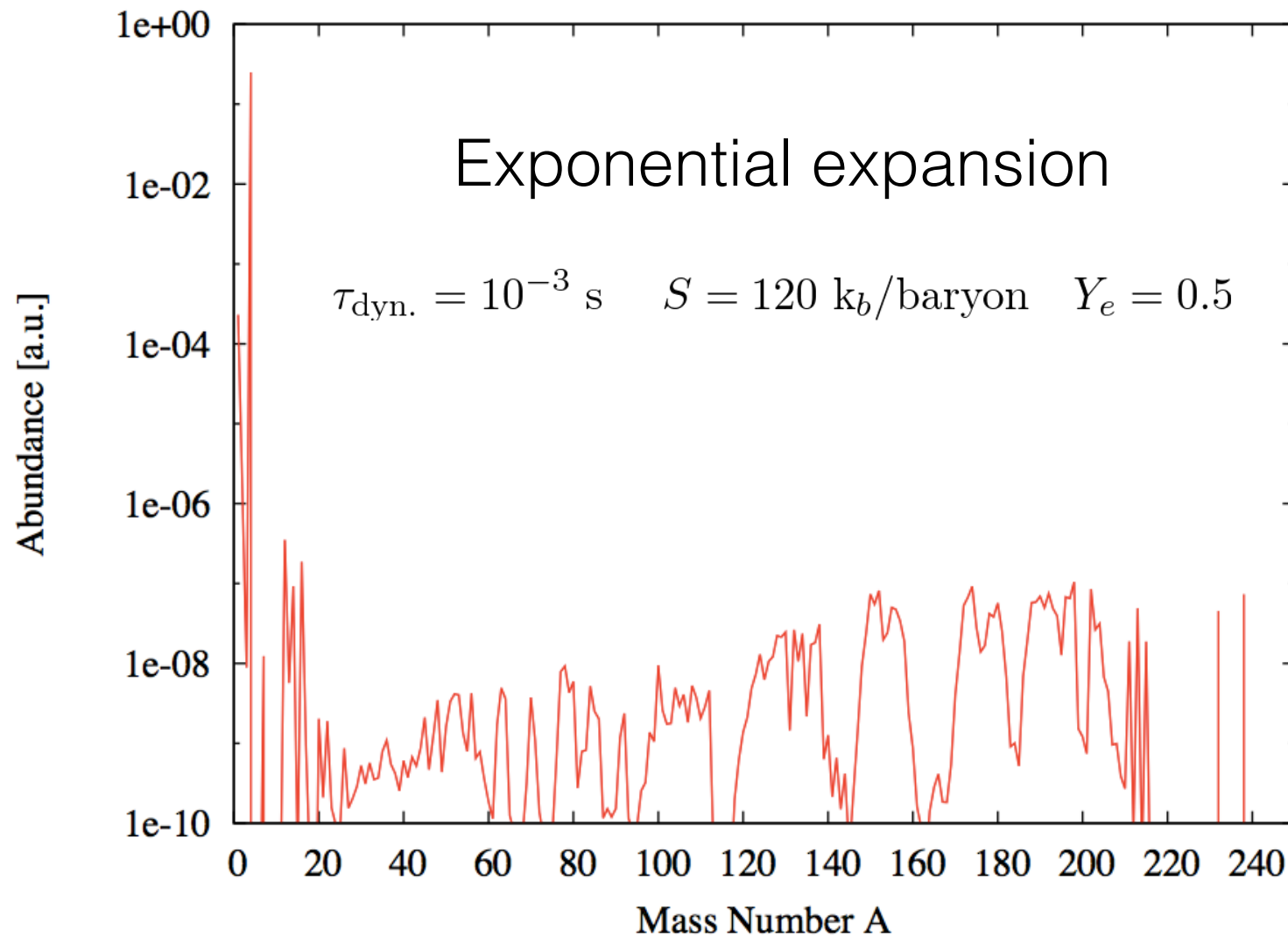


$T = 0.5 \text{ MeV}$ $S = 10 \text{ k}_B/\text{baryon}$

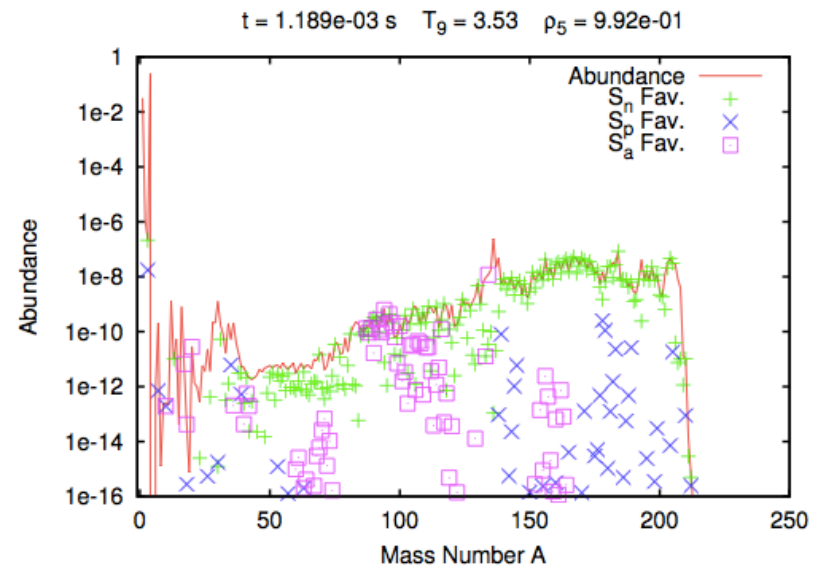
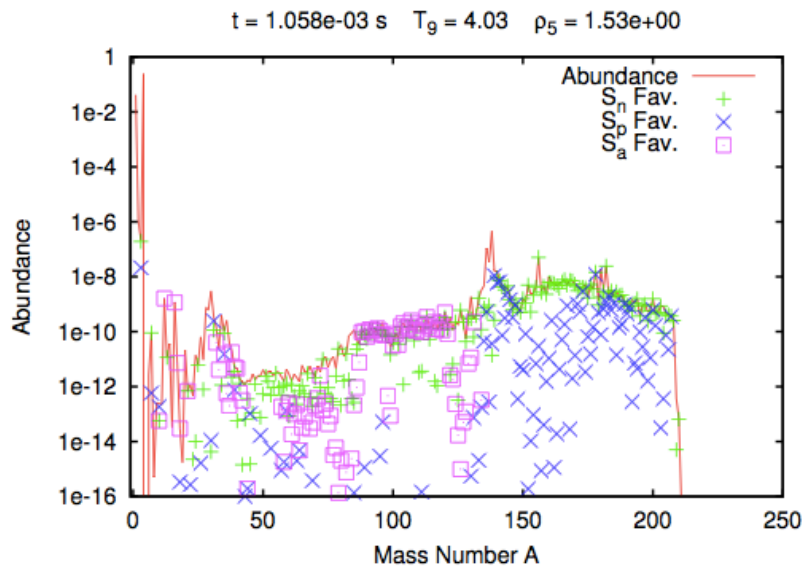
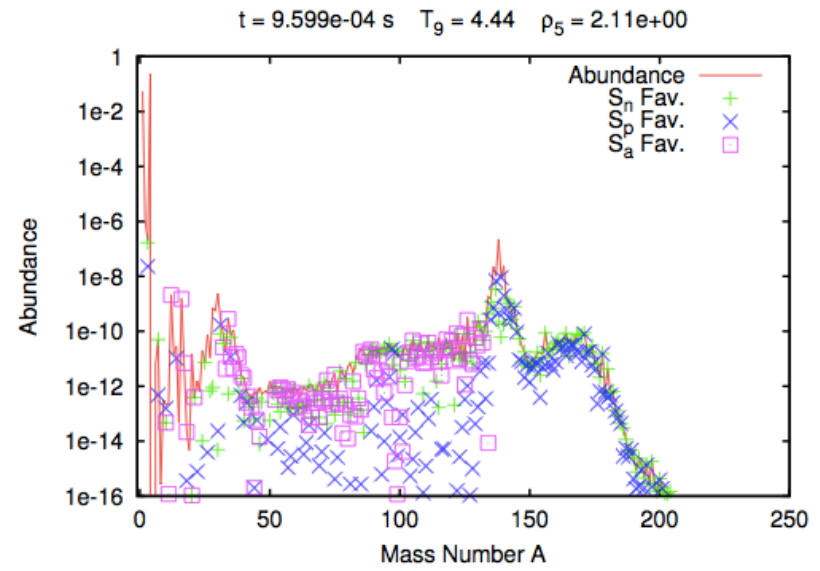
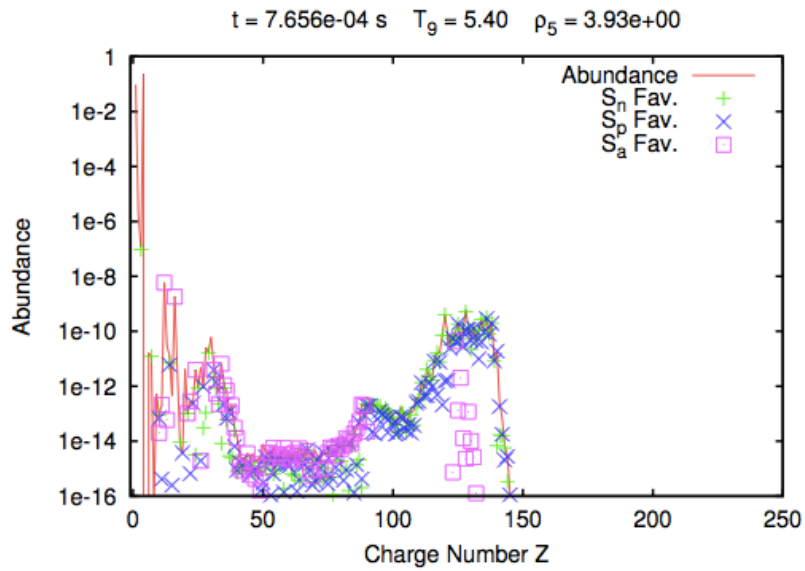


An Unsuccessful r -Process

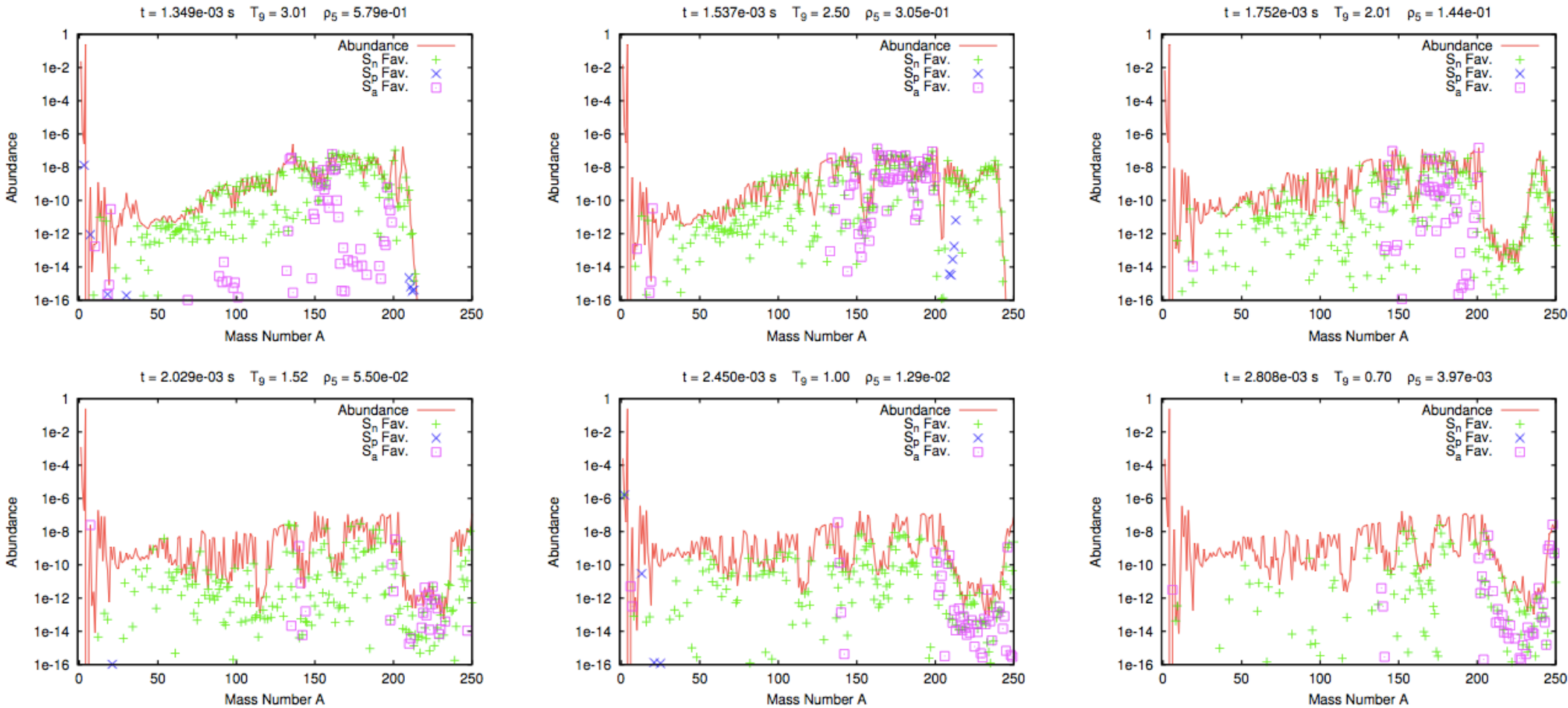
What can we learn from an UNSUCCESSFUL r -process?



Track the Evolution: I

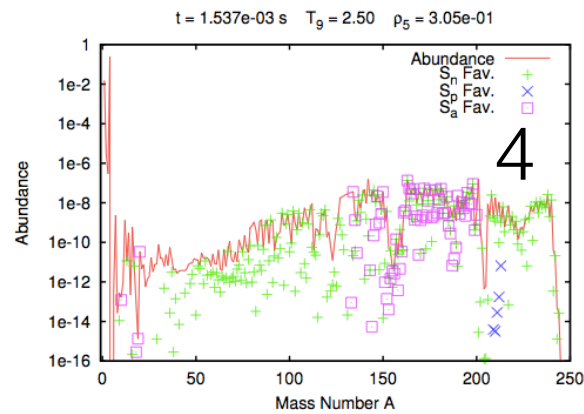
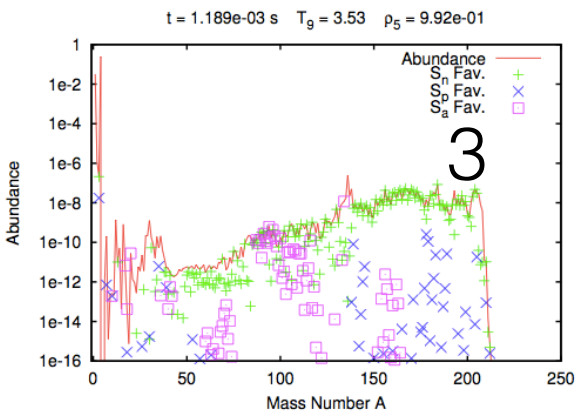
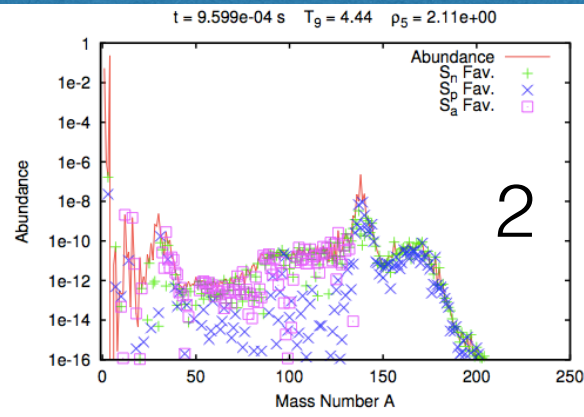
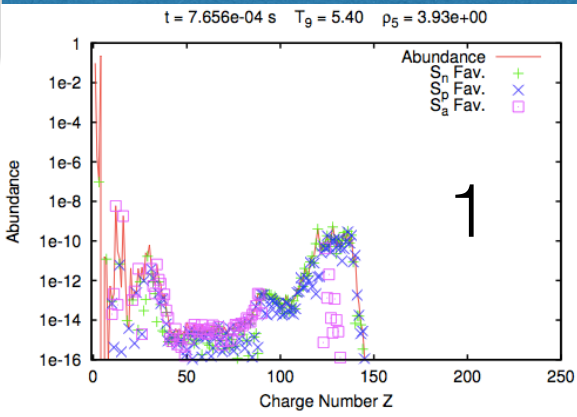


Track the Evolution: II



- Neutron reactions dominate the production of heavier nuclei.
- Alpha equilibria take over the nucleosynthesis but CANNOT make changes.

Reaction Rates



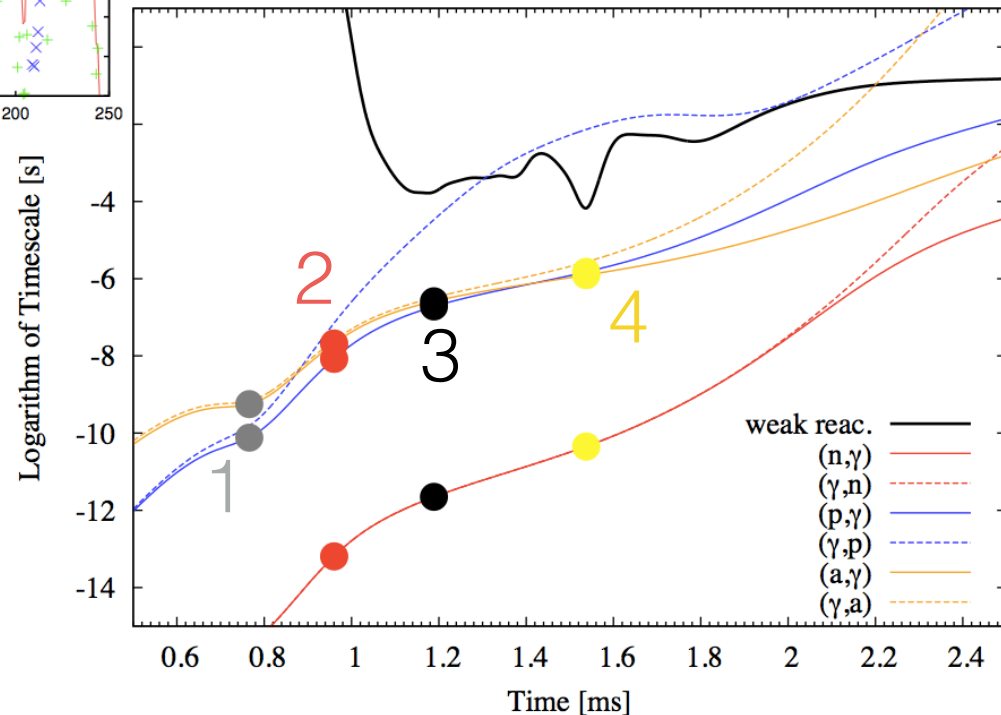
$$\tau_{\text{weak}} = \left[\frac{1}{Y_h} \sum_{Z>2,A} \lambda_w(Z,A) Y(Z,A) \right]^{-1}$$

$$\tau_{(i,\gamma)} = \left[\frac{\rho Y_i}{Y_h} N_A \sum_{Z>2,A} \langle \sigma v \rangle_{(i,\gamma)}(Z,A) Y(Z,A) \right]^{-1}$$

$$\tau_{(\gamma,i)} = \left[\frac{1}{Y_h} \sum_{Z>2,A} \lambda_{(\gamma,i)}(Z,A) Y(Z,A) \right]^{-1}$$

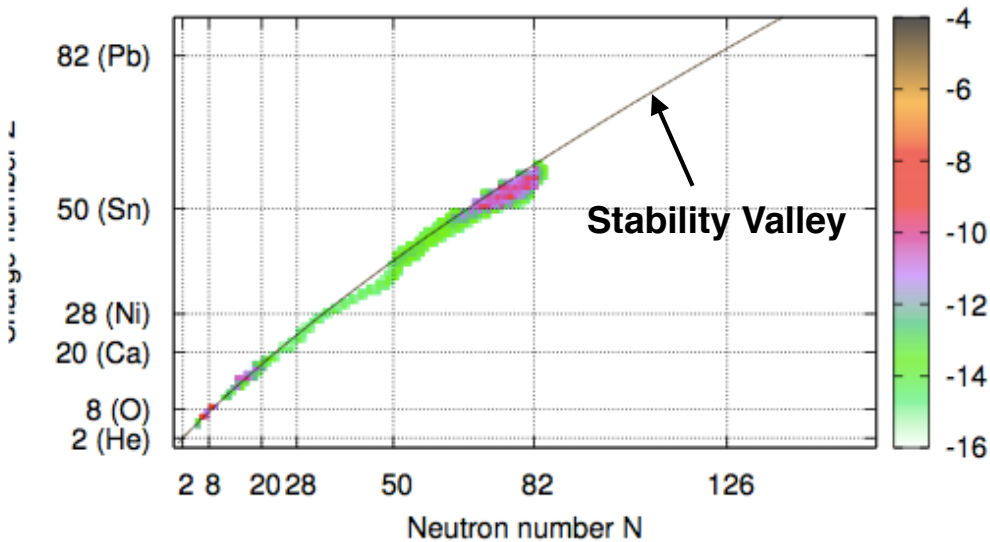
$$Y_n = \sum_{Z>2,A} Y(Z,A)$$

Neutron reactions are much faster !

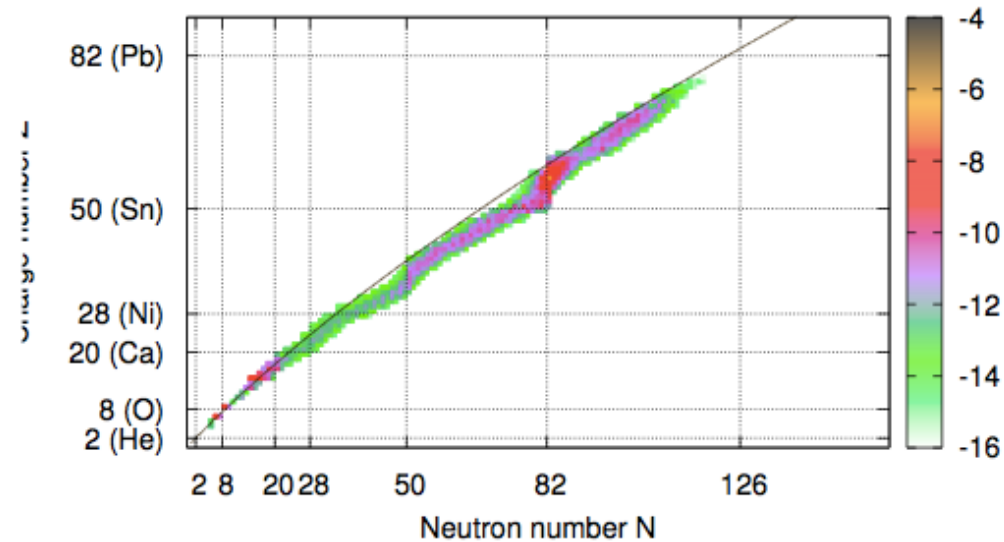


Neutrons Capture?

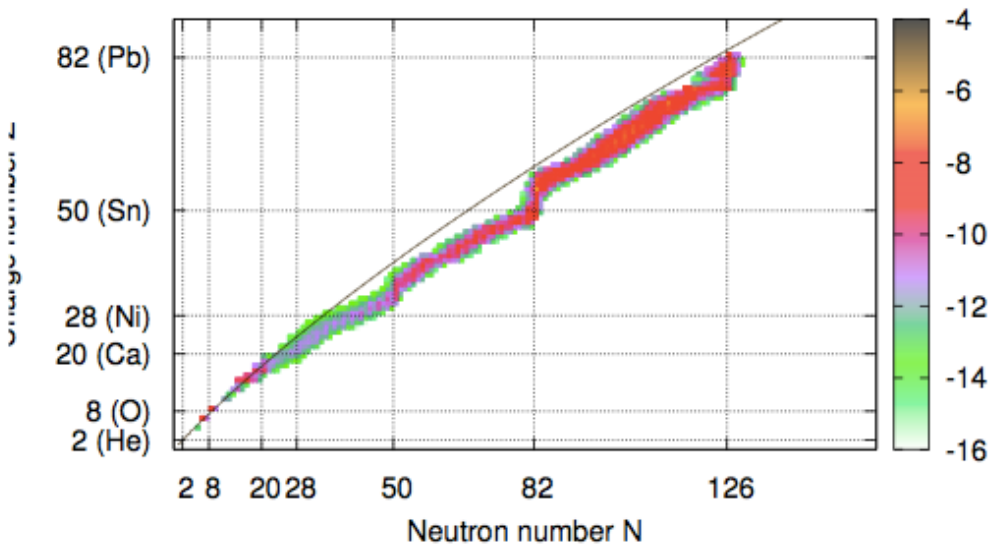
$T_g = 5.40$



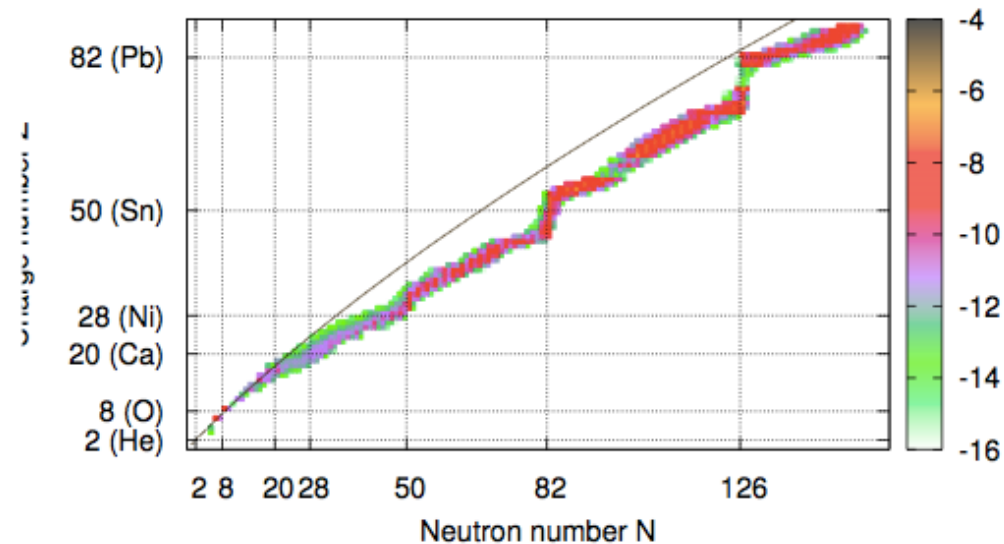
$T_g = 4.44$



$T_g = 3.53$

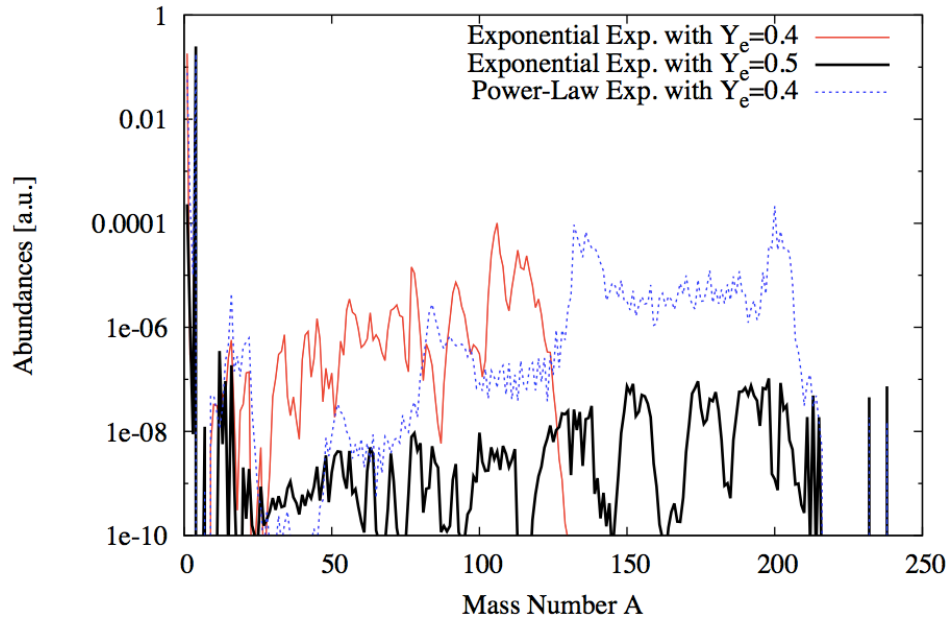


$T_g = 2.50$

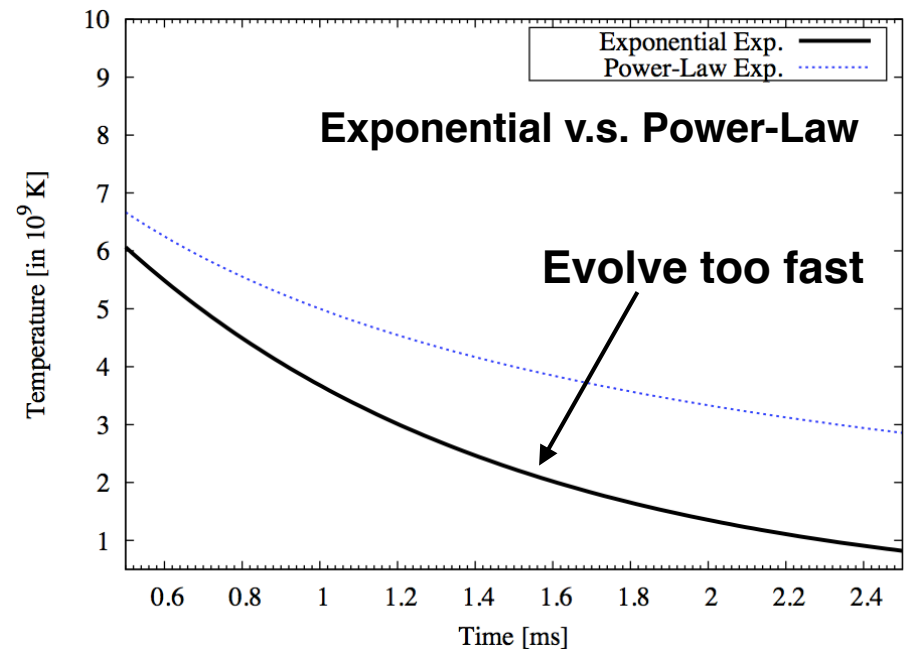
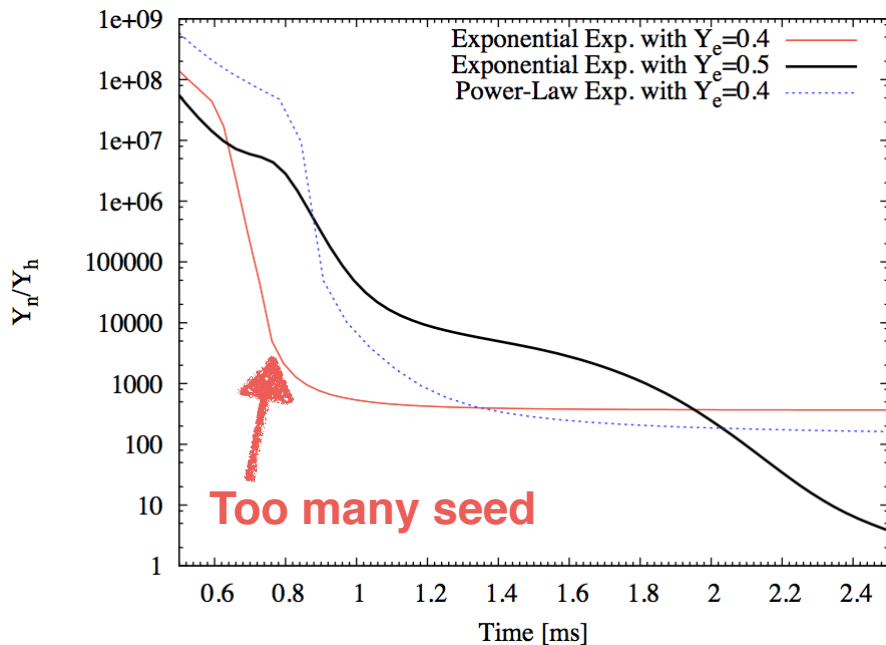
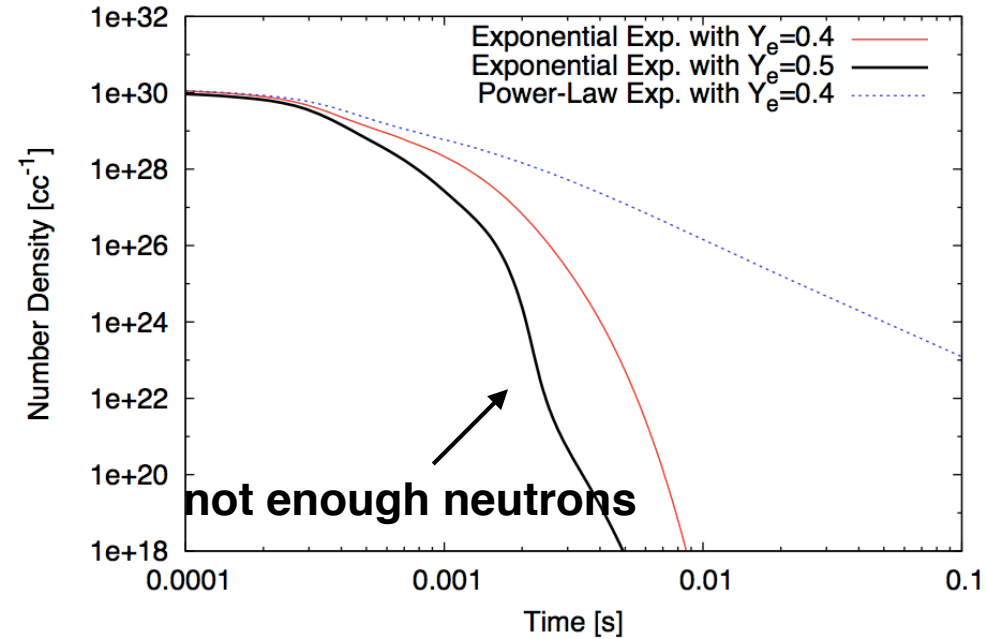


How to be successful?

Abundance with $S=120, \tau_{\text{dyn}}=10^{-3}$



Evolution of the neutron number density



Summary

- Neutrons dominate the production of heavy nuclei.
- To make a complete *r*-process:
 1. High neutron-to-seed ratio
 2. Enough time for neutron flux
- Power-Law expansion is a better parametric approximation for long time evolution.