

Applications of Neutron-Star
Universal Relations to
Gravitational Wave Observations

Kent Yagi

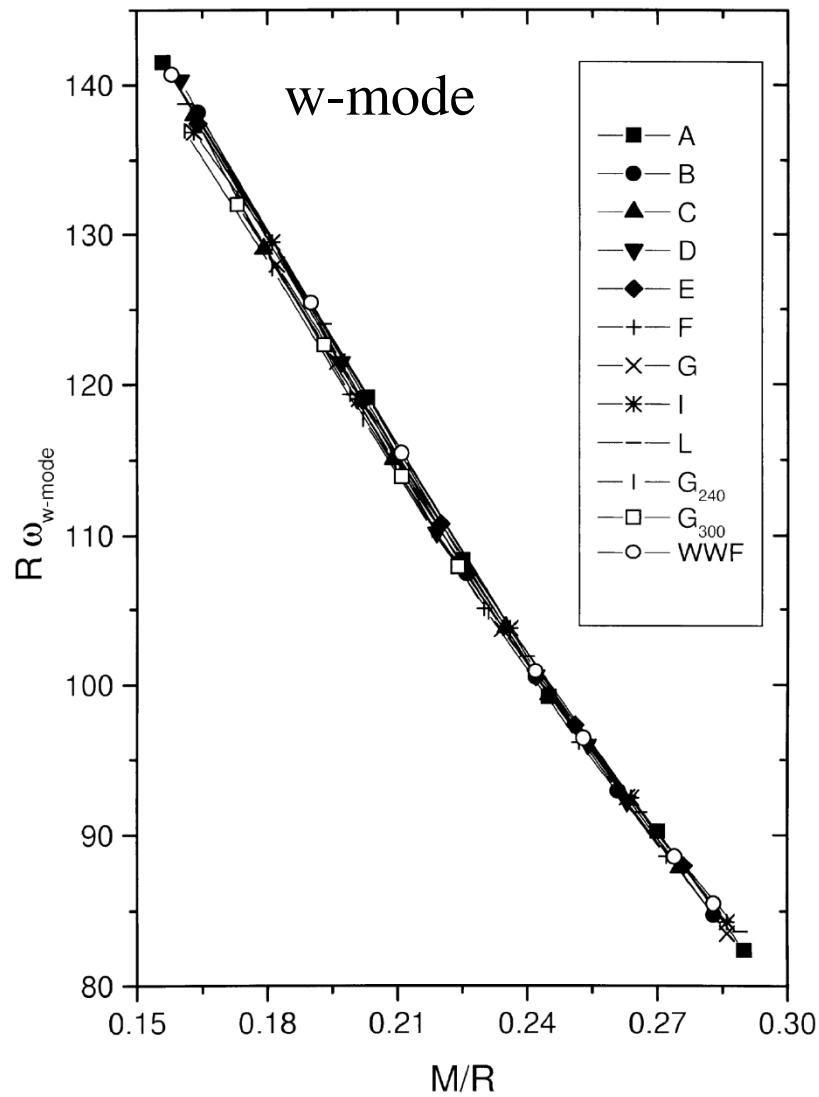
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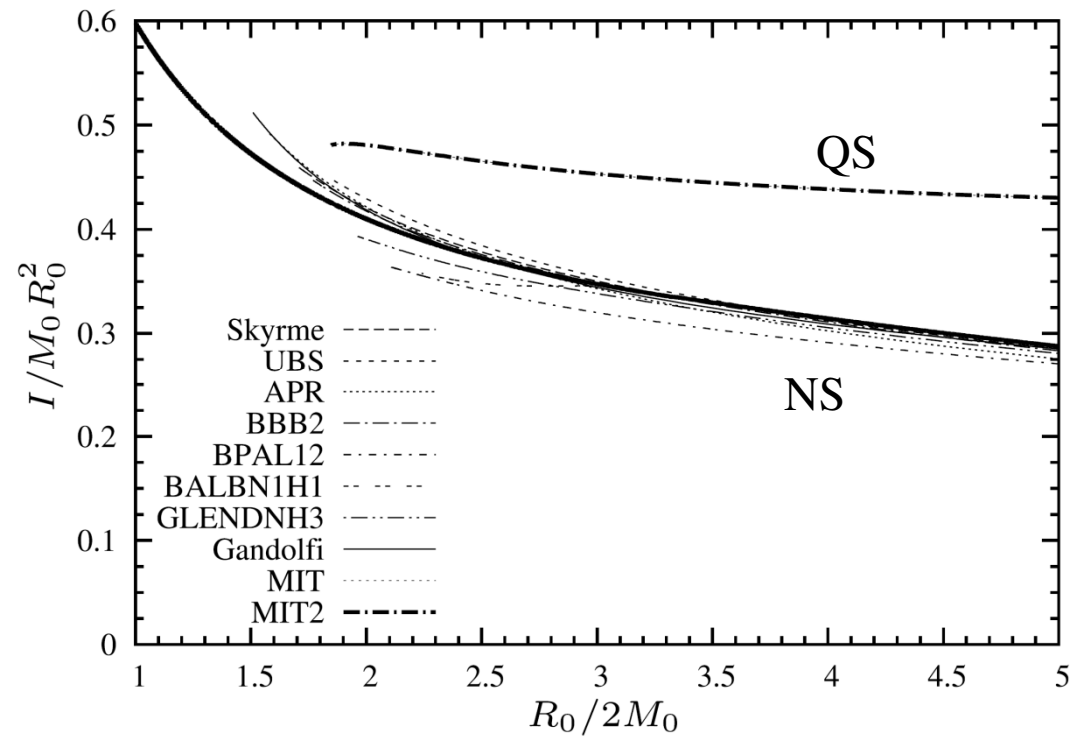
July 3rd 2014



Universal Relations: Isolated NSs



[Andersson & Kokkotas (1998)]



[Lattimer & Prakash (2001)]

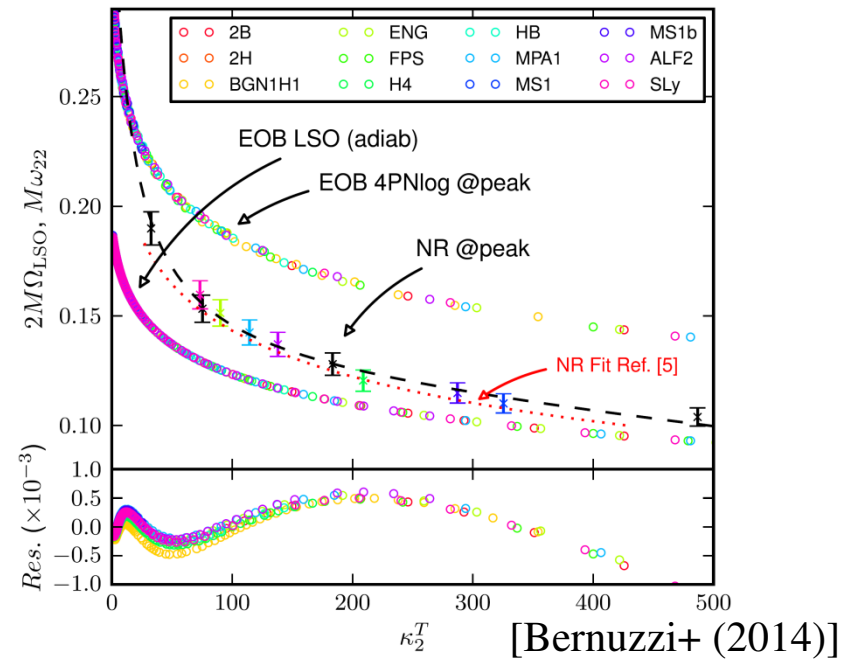
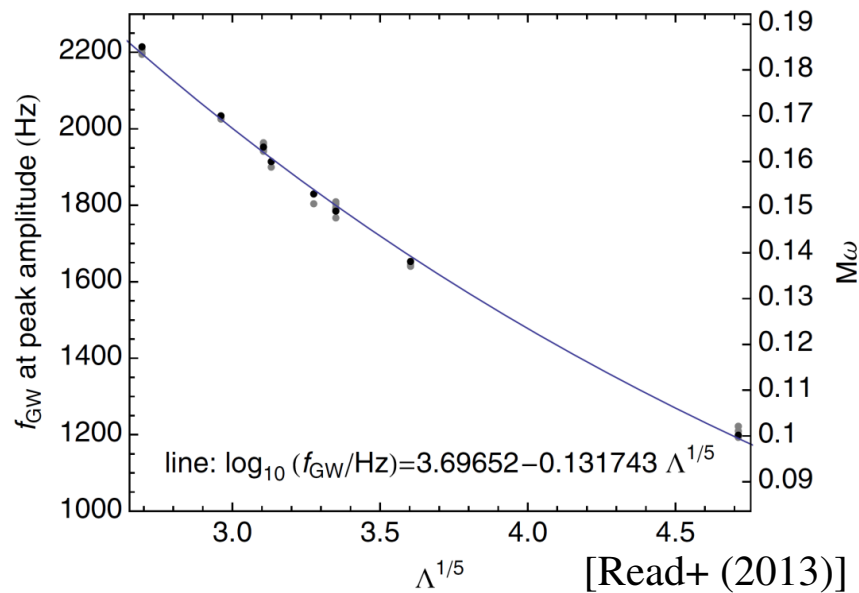
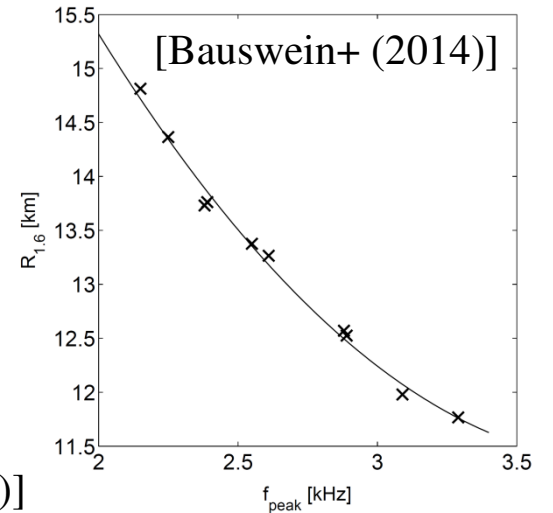
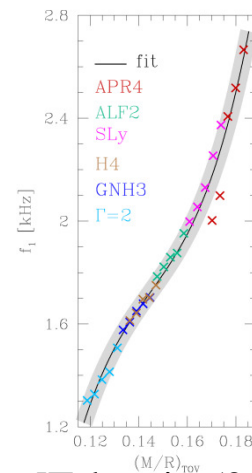
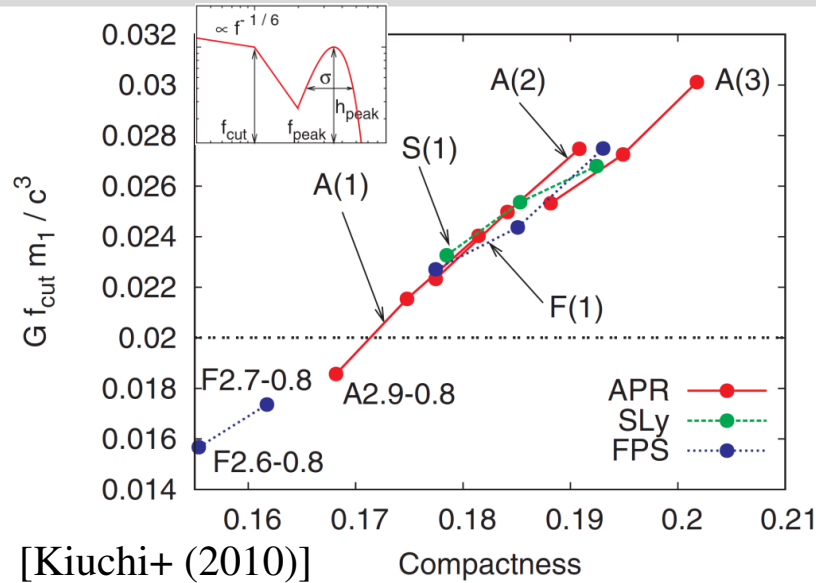
[Urbanec+ (2013)]

Many others

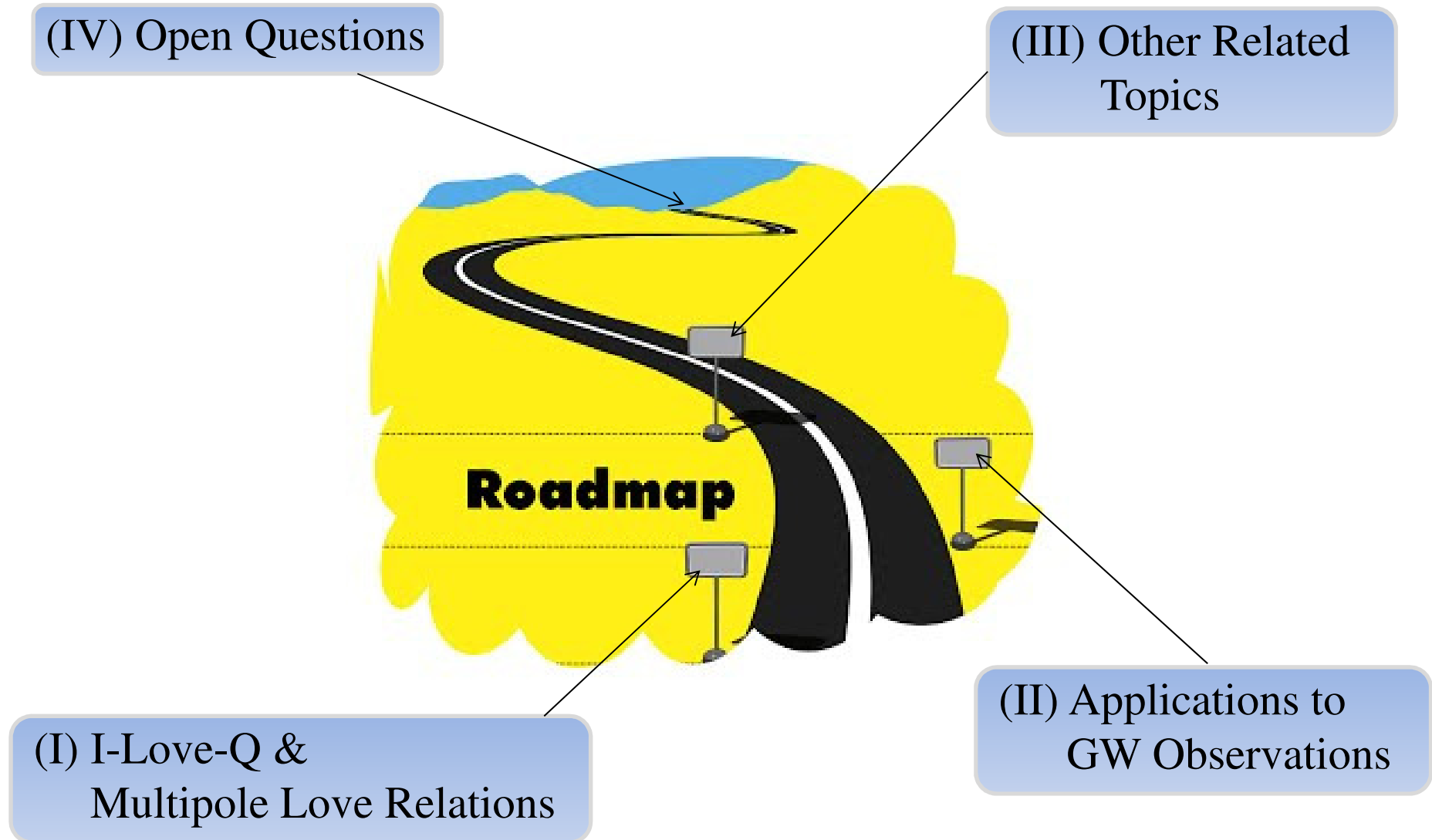
Universal Relations: Binary NSs

[Stergioulas' talk on Tuesday]

[Read's talk on Thursday]



Roadmap



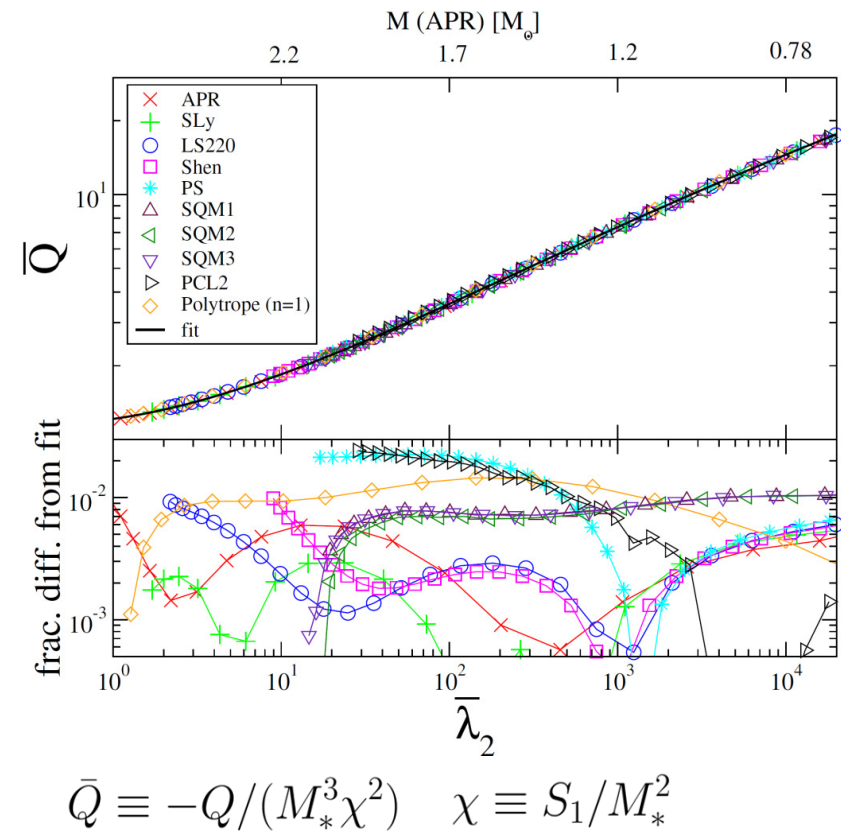
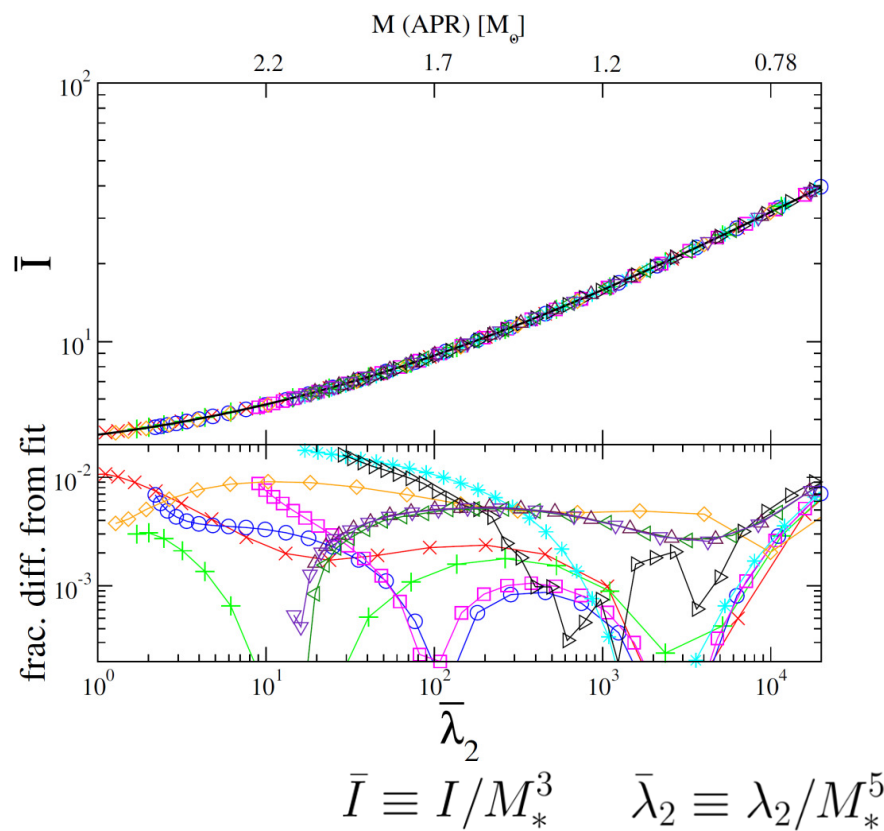


I-Love-Q &
Multipole Love Relations

I-Love-Q Relations

[KY & Yunes, Science, PRD (2013)]

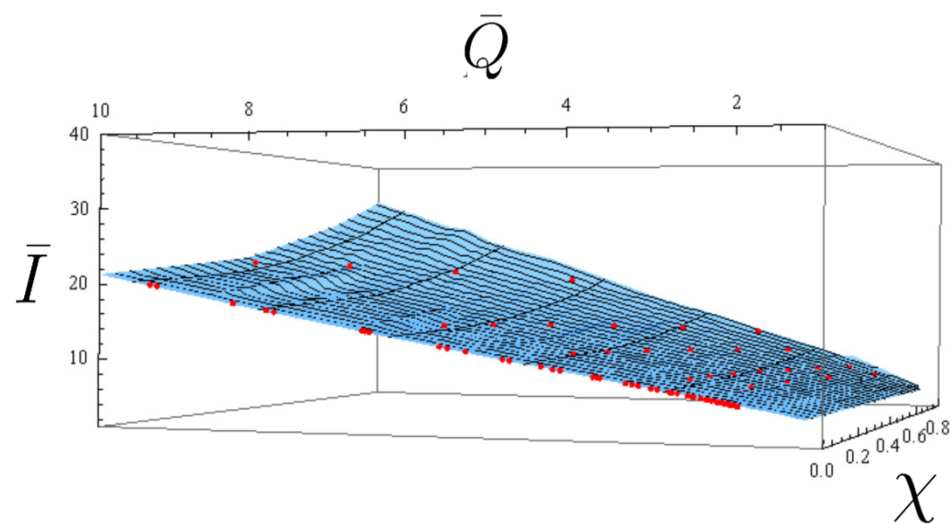
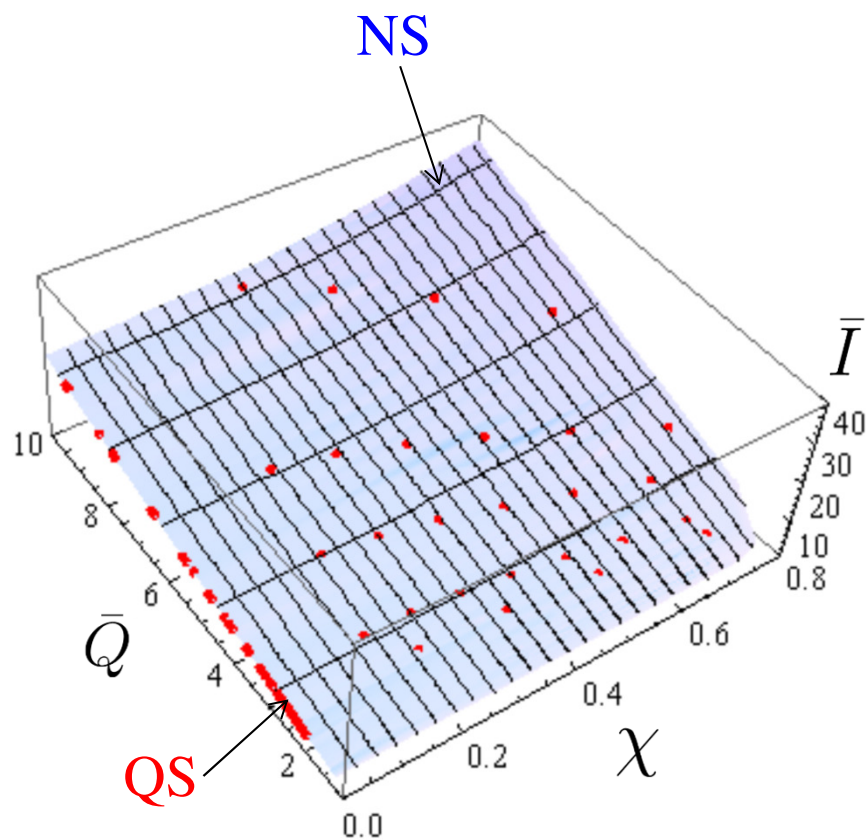
- (i) small/static tidal deformation → Maselli+ (2013)
- (ii) unmagnetized → Haskell+ (2014)
- (iii) uniform/slow-rotation → [Doneva+ (2013), Papps+ (2014),
Chakrabarti+ (2014), KY+ (2014)]
- (iv) barotropic → Martinon+ (2014)



Universal I-Q Plane

[Pappas & Apostolatos (2014)]
[KY+ (2014)]

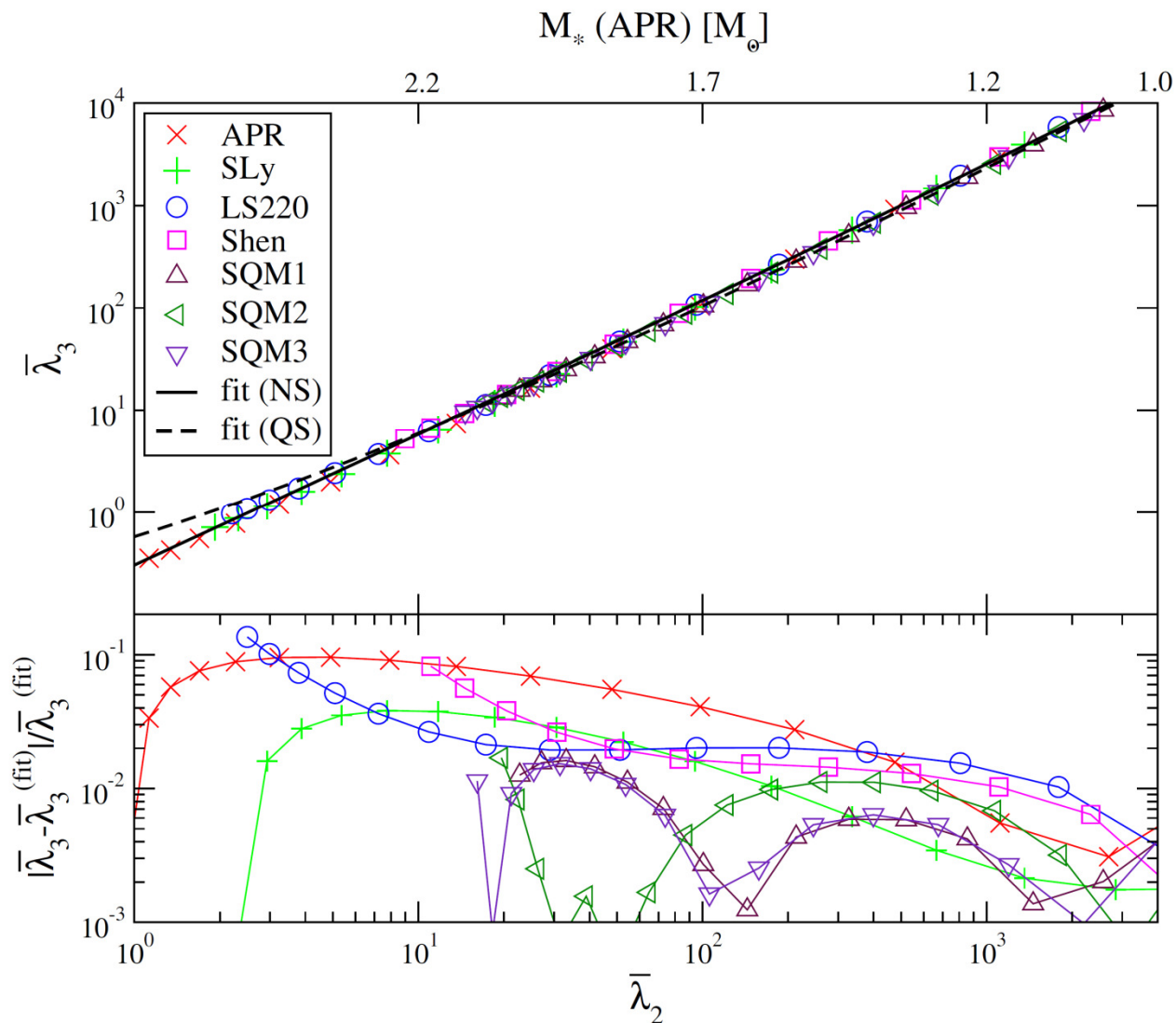
Universality still holds for a fixed $\chi (= S_1/M^2)$



QS plane is almost identical to the NS one

Multipole Love Relations

[KY (2014)]



multipole
moment

tidal tensor

$$M_L = -\lambda_l G_L$$

$$\bar{\lambda}_l \equiv \frac{\lambda_l}{m^{2l+1}}$$

Similar relation
holds for

$$\bar{\lambda}_4 - \bar{\lambda}_2$$

Applications to GW Observations

(I) GW Astrophysics

(II) Gravitational Physics

(III) Nuclear Physics

(I) GW Astrophysics

NS/NS gravitational waveform phase

$$\Psi(f) \approx \Psi_0 f^{-5/3} \left[1 + \dots + \Psi_3(\beta) f + \Psi_4(\sigma) f^{4/3} + \dots + \Psi_{10}(\lambda) f^{10/3} \right]$$

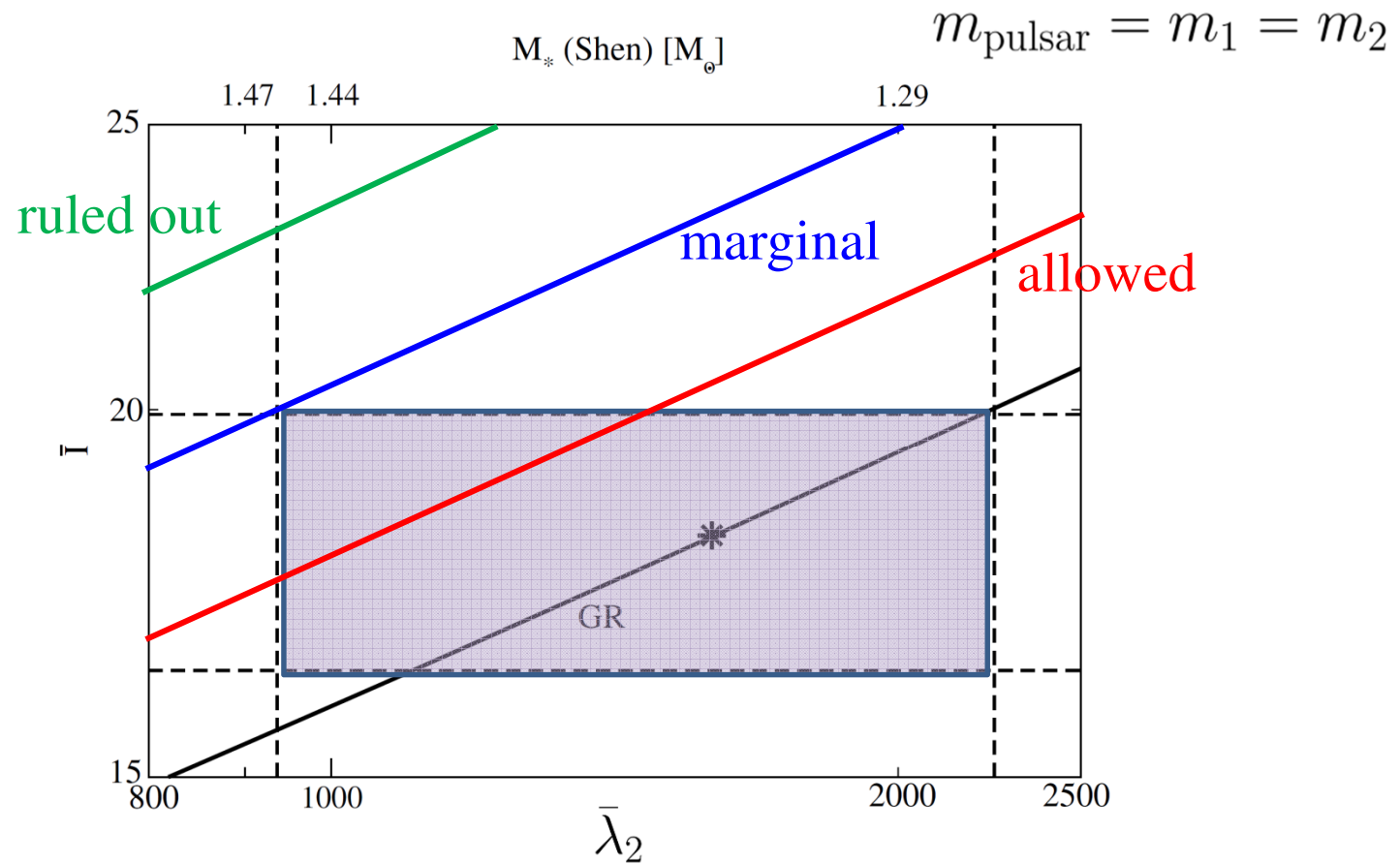
$$\sigma = \sigma_{SS} + \sigma_Q$$

Q-Love relation breaks the degeneracy between spins and Q

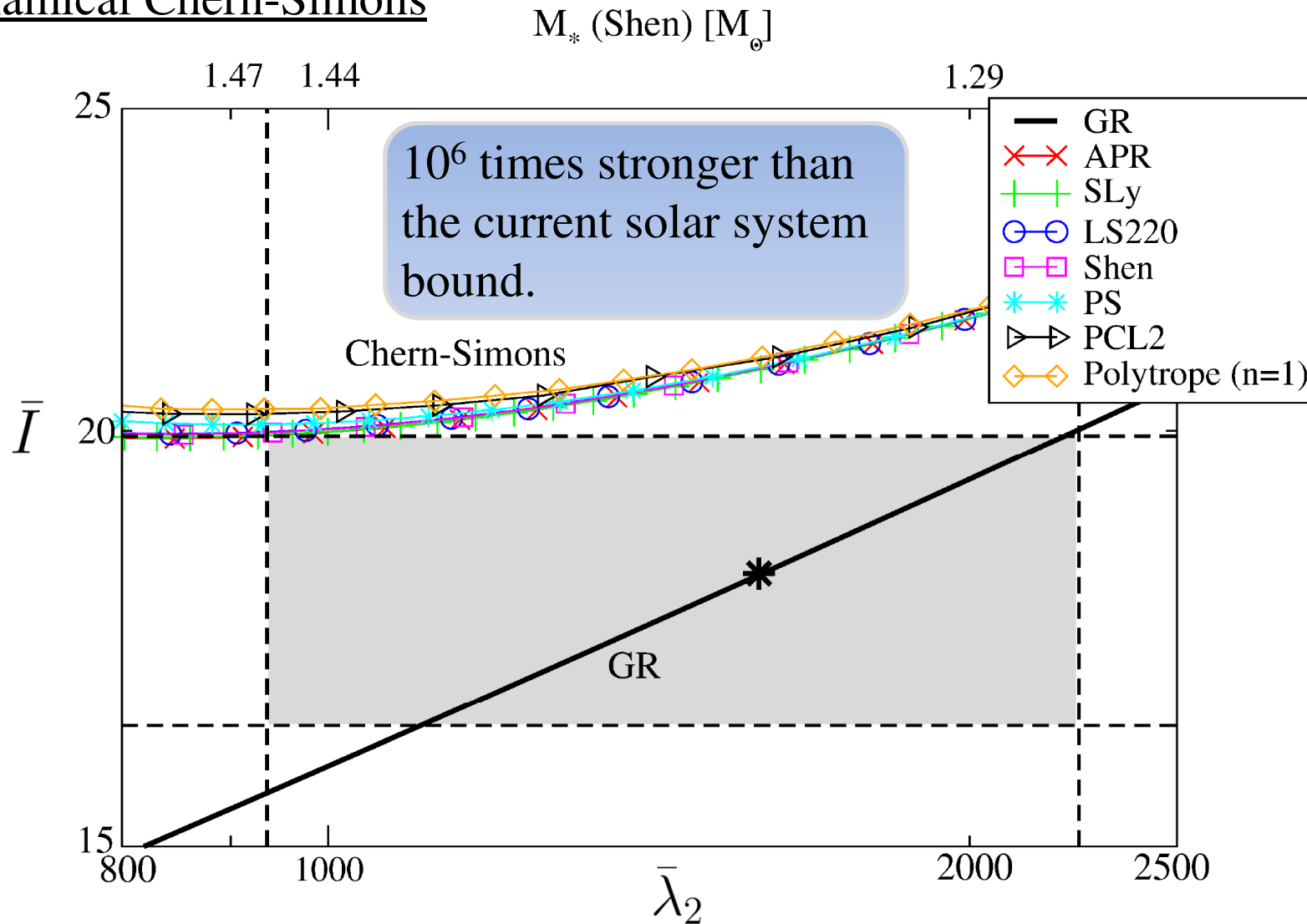
➔ Allows us, in principle, to measure independent spins

(II) Gravitational Physics

- double binary pulsar $\rightarrow \Delta \bar{I} / \bar{I} = 10\%$
- GWs $\rightarrow \Delta \bar{\lambda}_2 / \bar{\lambda}_2 = 60\%$



Dynamical Chern-Simons



(iii) Nuclear Physics

[KY (2014)]

$$\Psi_{\bar{\lambda}_\ell} \sim \bar{\lambda}_\ell^{(1)} X_1^{2\ell-1} x^{2\ell-3/2} + (1 \leftrightarrow 2)$$

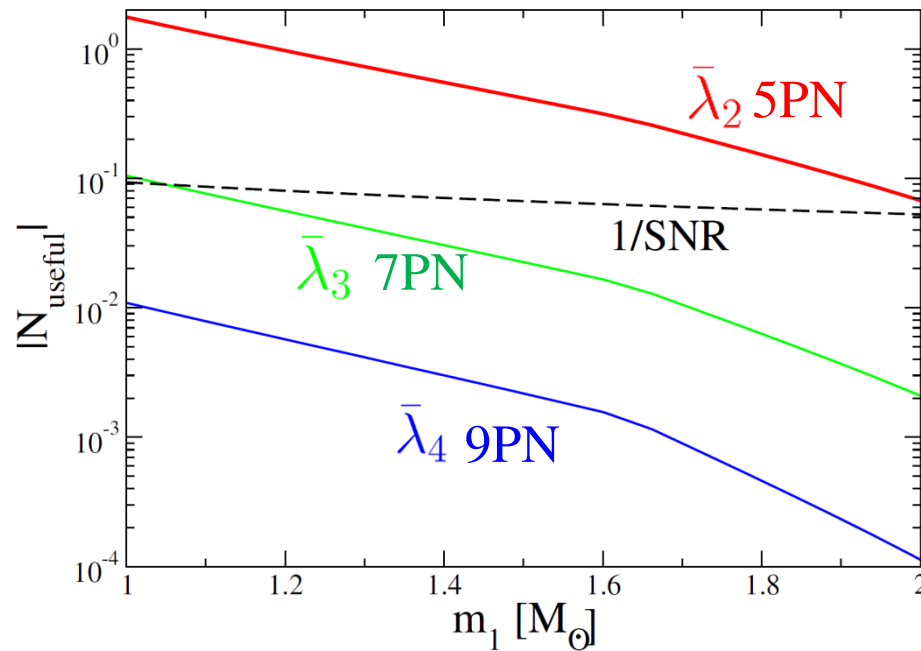
➔ $(2\ell + 1)$ PN

$$\left(\begin{array}{ll} \bar{\lambda}_\ell \equiv \frac{\lambda_\ell}{m^{2\ell+1}} & X_A \equiv \frac{m_A}{M} \\ x \equiv (\pi M f)^{2/3} & M \equiv m_1 + m_2 \end{array} \right)$$

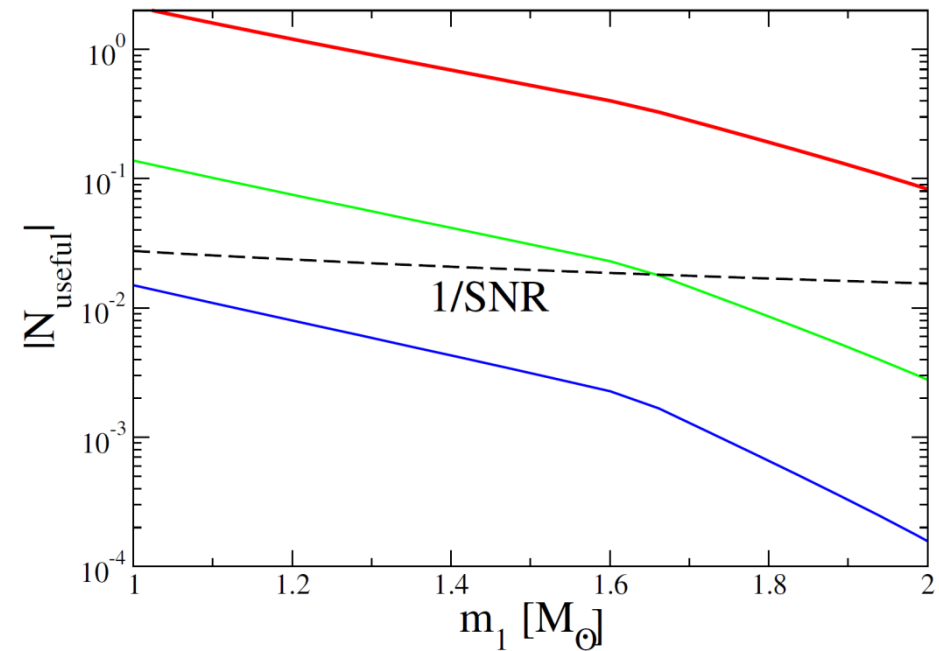
Useful number of cycles

$$D_L = 100 \text{Mpc} \quad m_1 = m_2$$

Adv. LIGO, Shen



LIGO III, Shen



Impact of Multipole Love Relations

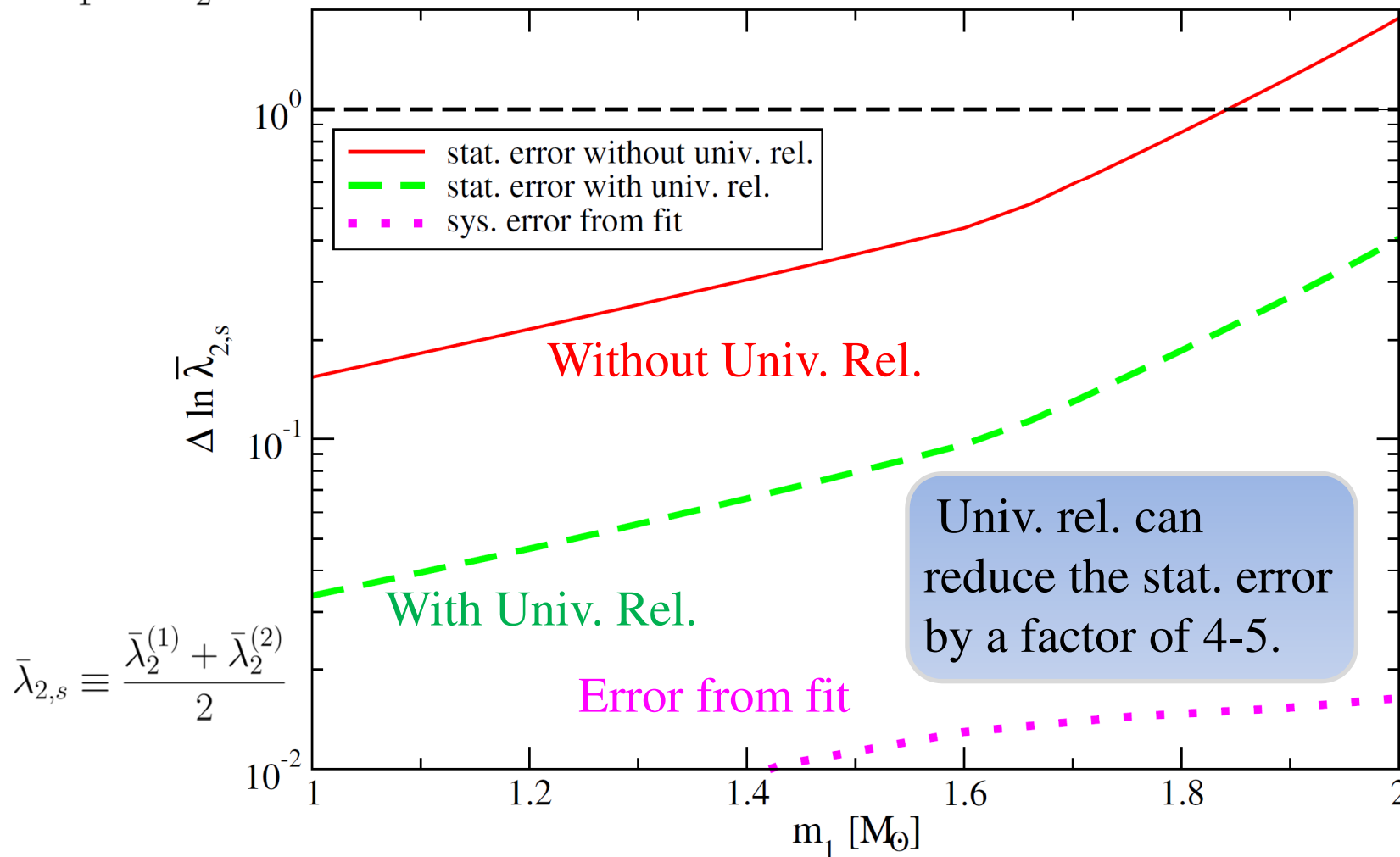
[KY (2014)]

$D_L = 100\text{Mpc}$

Shen EoS

LIGO III

$m_1 = m_2$



Other Related Topics

(I) Applications to X-ray Observations

(II) 3-Hair Relations for Newtonian Polytropes

(III) Why I-Love-Q

(I) Applications to X-ray Observations

Parameters:

(M, R, I, Q, \dots)

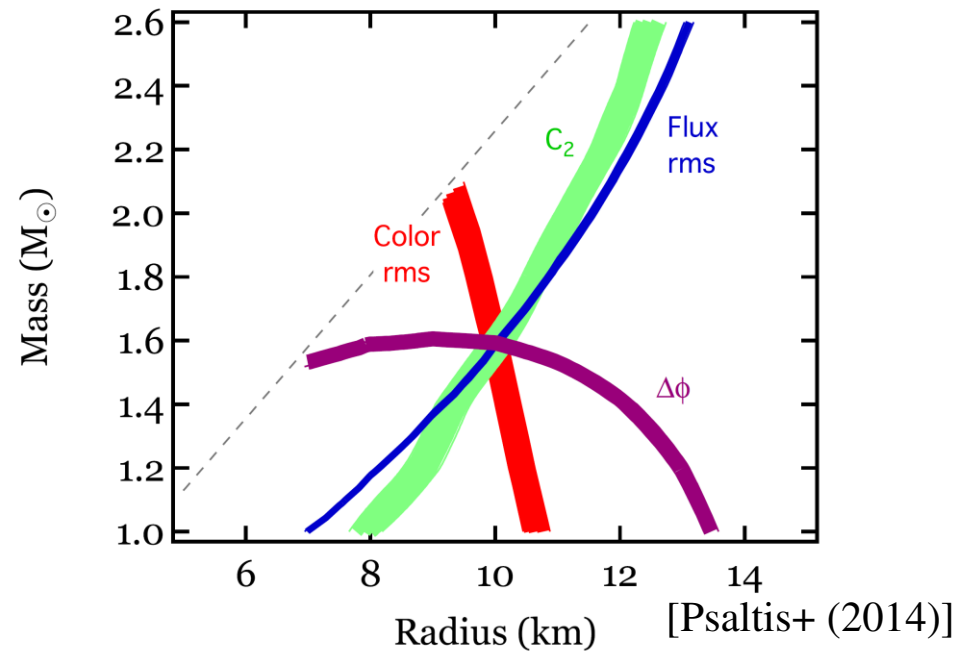
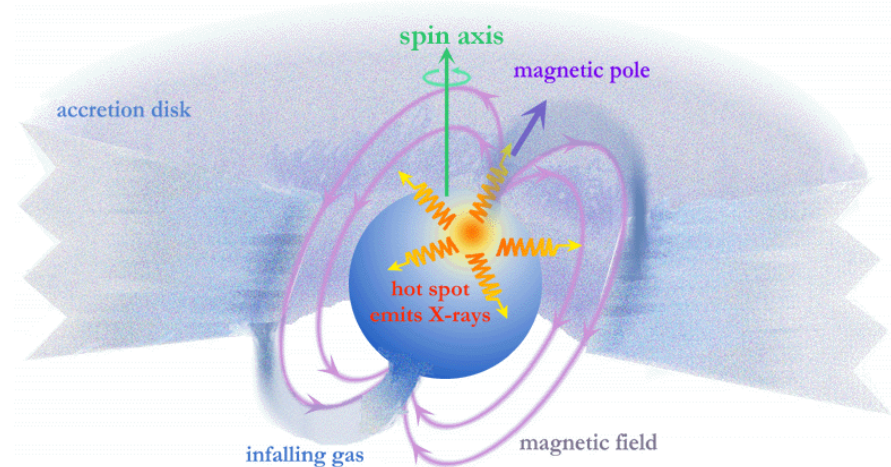
Strong degeneracies
among parameters

↓ universal
relations

Reduce the number of
parameters

↓

Allows one to measure mass
and radius accurately!



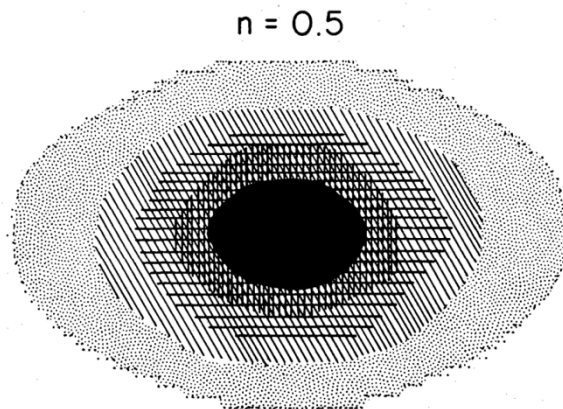
(II) Newtonian 3-Hair Relations

[Stein, KY & Yunes (2014)]

- Newtonian
- rigid rotation
- unmagnetized
- $p = K\rho^{1+1/n}$
- elliptical isodensity

$$M_\ell + i\frac{q}{a}S_\ell = \bar{B}_{n, \lfloor \frac{\ell-1}{2} \rfloor} M (iq)^\ell$$

$$\left[\begin{array}{ll} S_1 = aM & M_2 = -q^2 M \end{array} \right]$$



[Butterworth (1976)]

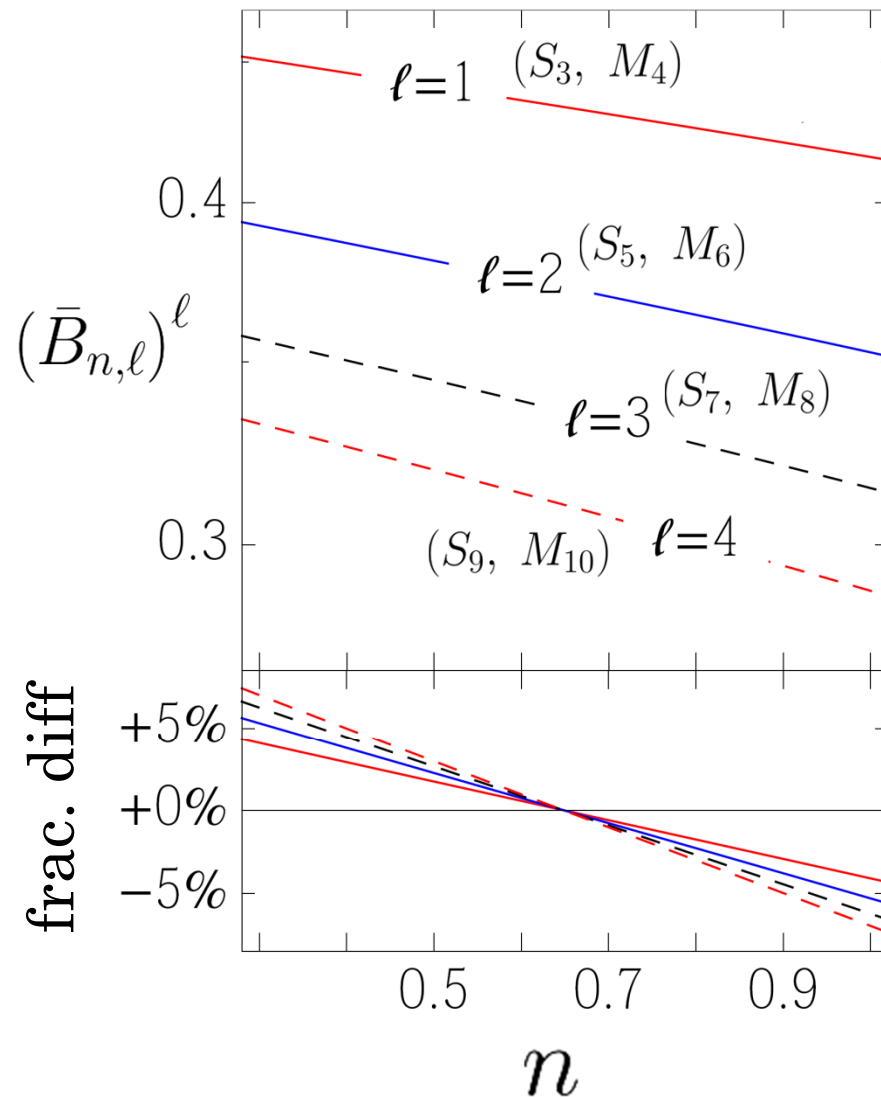
Black Hole No-hair Relation

[Hansen (1974)]

$$M_\ell + iS_\ell = M(ia)^\ell$$

Once the polytropic index n is specified, **all the higher moments** can be expressed in terms of **the first three**.

Equation of State Dependence



$$M_\ell + i\frac{q}{a}S_\ell = \bar{B}_{n, \lfloor \frac{\ell-1}{2} \rfloor} M(iq)^\ell$$

Coefficient is **equation of state insensitive** within ~5% for low- l modes

Effective NS No-hair Property

[KY+ (2014)]

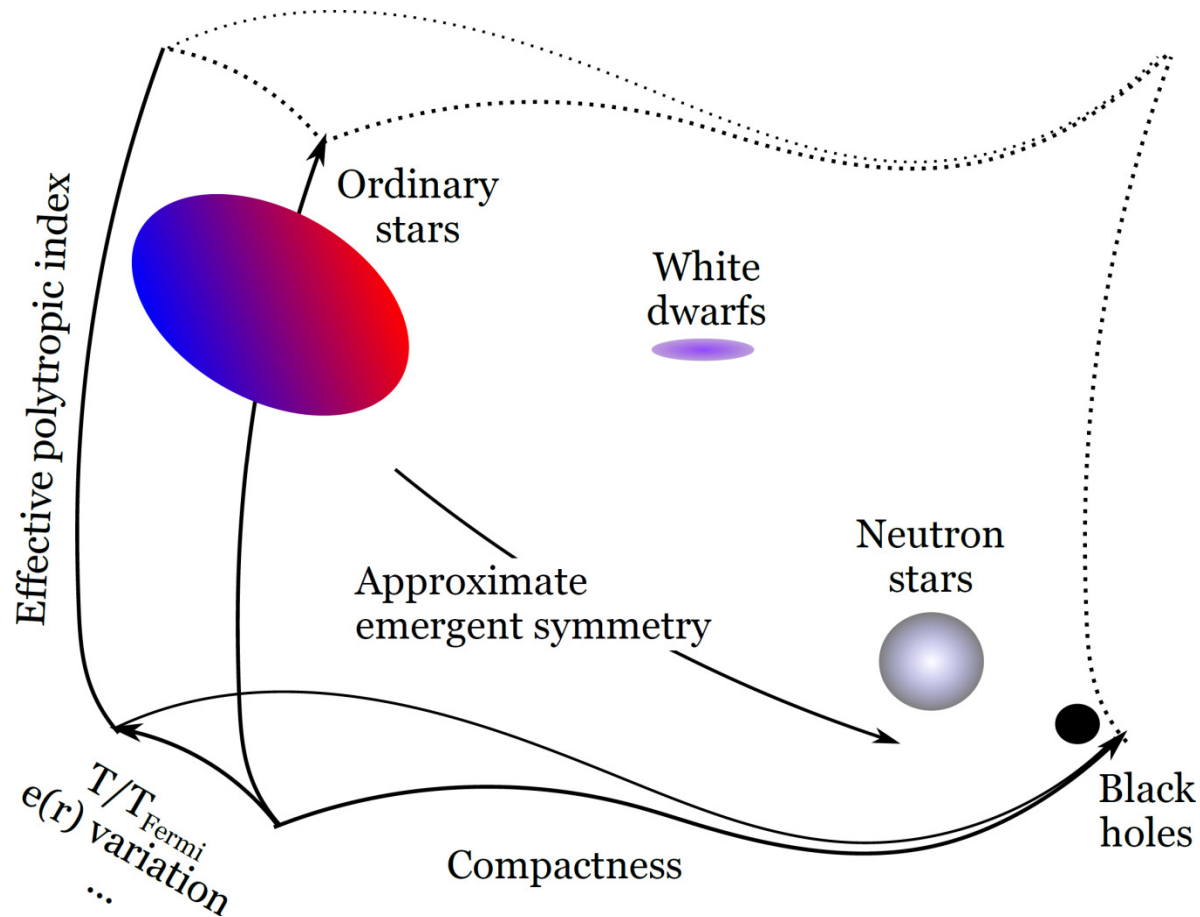
-NS lower multipole moments can be given in terms of the first three.

-confirmed up to M_4

(III) Why I-Love-Q

[KY+ (2014)]

Near self-similarity of isodensity contours plays a crucial role in the universality



Open Questions

Open Questions

(i) Improving parameter estimation:

-Fisher \rightarrow Bayesian

(ii) Universal relations & Tests of GR in other non-GR theories:

e.g. -Lorentz-violation in gravity
Einstein-Aether, Horava-Lifshitz
-curvature correction
Einstein-dilaton Gauss-Bonnet
 $f(R)$

(iii) Universal relations in differentially-rotating NSs

-Naturally breaks the isodensity self-similarity
-4-hair relation?

(iv) Newtonian analysis

-multipole Love relation
-NS oscillation modes?
Other universal relations?

(v) Love numbers for spinning NSs?

Discussion from Monday Afternoon + α

-Can we construct a **hybrid inspiral-merger-ringdown waveform** with just **one tidal parameter**?

Universal relations between the damping time and compactness?

Universal relations among other parameters and compactness?

-How much **post-merger oscillations** further help constrain the EoS on top of the inspiral?

Which is better?

(i) Rewrite Λ and f_2 into a single parameter (R ?) and constrain it strongly.

(ii) Treat Λ and f_2 independently and constrain different part of EoS.