

The EOS of neutron matter, symmetry energy, and the effect of Λ hyperons to neutron star structure

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Binary Neutron Star Coalescence as a Fundamental Physics Laboratory,
June 30 - August 1 2014, INT, University of Washington, Seattle.

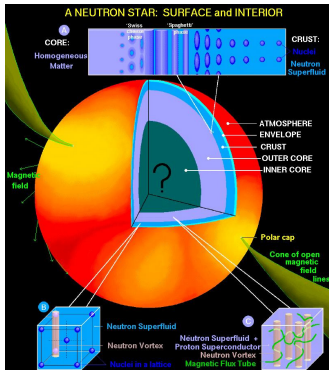


www.computingnuclei.org



Neutron stars

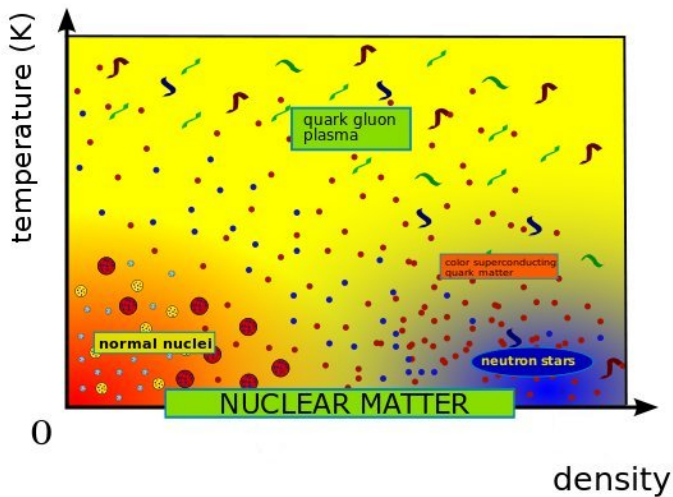
Neutron star is a wonderful natural laboratory



D. Page

- Atmosphere: atomic and plasma physics
- Crust: physics of superfluids (neutrons, vortex), solid state physics (nuclei)
- Inner crust: deformed nuclei, pasta phase
- Outer core: nuclear matter
- Inner core: hyperons? quark matter? π or K condensates?

Homogeneous neutron matter



- The model and the method
- Equation of state of neutron matter, role of three-neutron force
- Symmetry energy
- Neutron star structure
- Λ -neutron matter
- Conclusions

Nuclear Hamiltonian

Model: non-relativistic nucleons interacting with an effective nucleon-nucleon force (NN) and three-nucleon interaction (TNI).

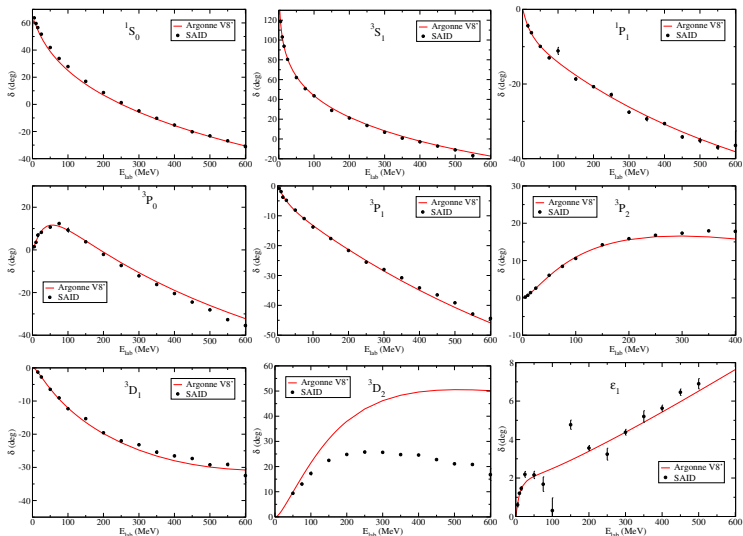
$$H = -\frac{\hbar^2}{2m} \sum_{i=1}^A \nabla_i^2 + \sum_{i<j} v_{ij} + \sum_{i<j<k} V_{ijk}$$

v_{ij} NN fitted on scattering data. Sum of operators:

$$v_{ij} = \sum O_{ij}^{p=1,8} v^p(r_{ij}), \quad O_{ij}^p = (1, \vec{\sigma}_i \cdot \vec{\sigma}_j, S_{ij}, \vec{L}_{ij} \cdot \vec{S}_{ij}) \times (1, \vec{\tau}_i \cdot \vec{\tau}_j)$$

NN interaction - Argonne AV8'.

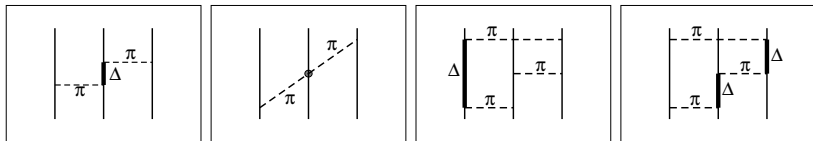
Phase shifts, AV8'



At $\rho = \rho_0$, $k_F \simeq 330$ MeV. Two neutrons have $E_{CM} \simeq 120$ MeV,
 $E_{LAB} \simeq 240$ MeV. \rightarrow Argonne NN accurate up to (at least) $2-3\rho_0$.

Three-body forces

Urbana–Illinois V_{ijk} models processes like



+ short-range correlations (spin/isospin independent).

$$H\psi(\vec{r}_1 \dots \vec{r}_N) = E\psi(\vec{r}_1 \dots \vec{r}_N) \quad \psi(t) = e^{-(H-E_T)t}\psi(0)$$

Ground-state extracted in the limit of $t \rightarrow \infty$.

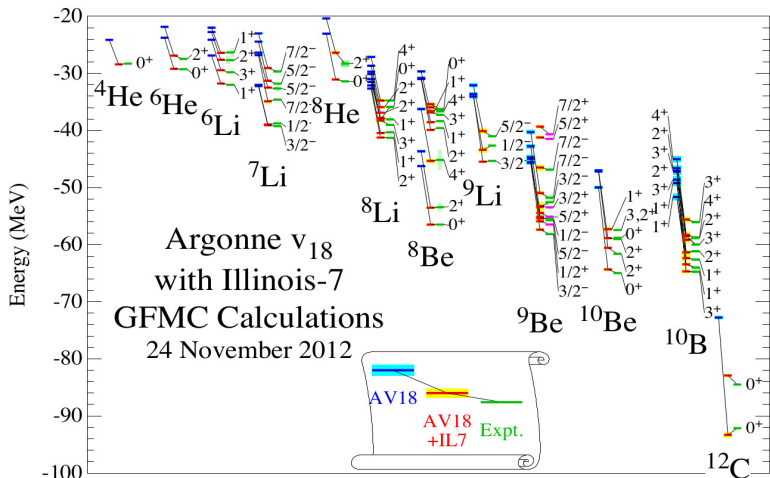
Propagation performed by

$$\psi(R, t) = \langle R|\psi(t)\rangle = \int dR' G(R, R', t)\psi(R', 0)$$

- Importance sampling: $G(R, R', t) \rightarrow G(R, R', t) \Psi_I(R')/\Psi_I(R)$
- Constrained-path approximation to control the sign problem.

Ground-state obtained in a **non-perturbative way**. Systematic uncertainties within 1-2 %.

Light nuclei spectrum computed with GFMC



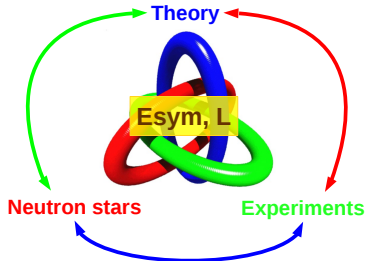
Carlson, Pieper, Wiringa, many papers

Neutron matter equation of state

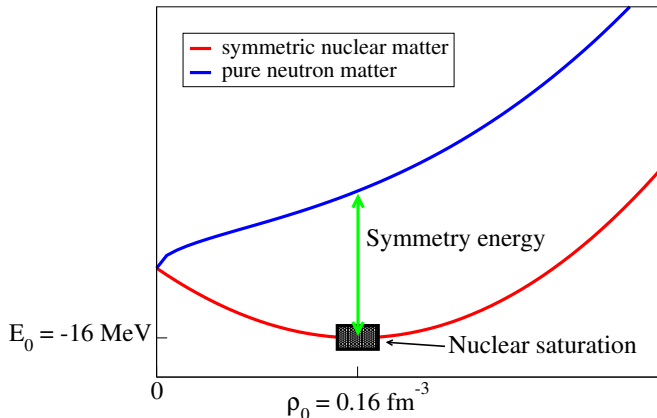
Why to study neutron matter at nuclear densities?

- EOS of neutron matter gives the symmetry energy and its slope.
- The three-neutron force ($T = 3/2$) very weak in light nuclei, while $T = 1/2$ is the dominant part. No direct $T = 3/2$ experiments available.

Why to study symmetry energy?



What is the Symmetry energy?



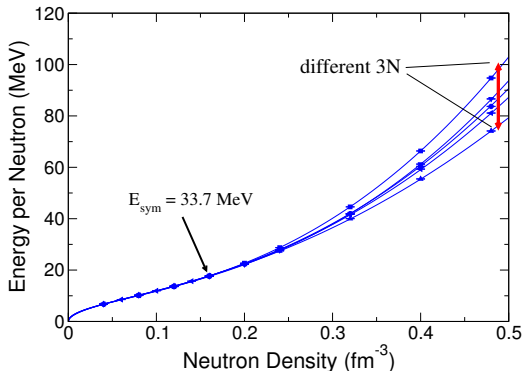
Assumption from experiments:

$$E_{SNM}(\rho_0) = -16 \text{ MeV}, \quad \rho_0 = 0.16 \text{ fm}^{-3}, \quad E_{sym} = E_{PNM}(\rho_0) + 16$$

At ρ_0 we access E_{sym} by studying PNM.

Neutron matter

We consider different forms of three-neutron interaction by only requiring a particular value of E_{sym} at saturation.

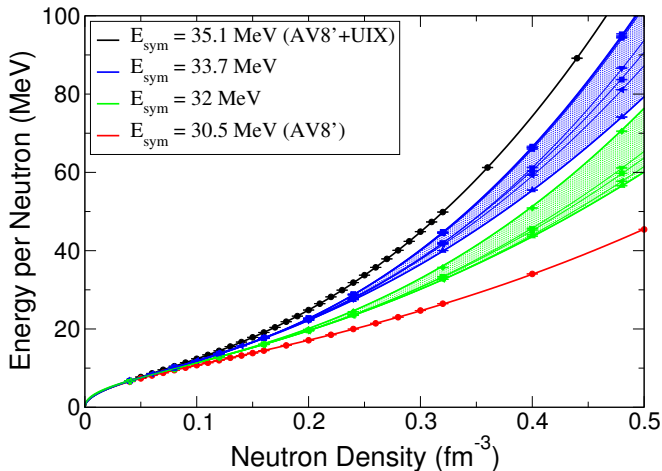


different 3N:

- $V_{2\pi} + \alpha V_R$
- $V_{2\pi} + \alpha V_R^\mu$
(several μ)
- $V_{2\pi} + \alpha \tilde{V}_R$
- $V_{3\pi} + \alpha V_R$

Neutron matter

Equation of state of neutron matter using Argonne forces:

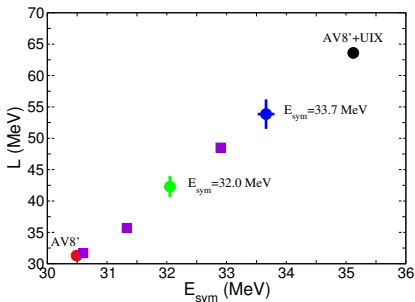


Gandolfi, Carlson, Reddy, PRC (2012)

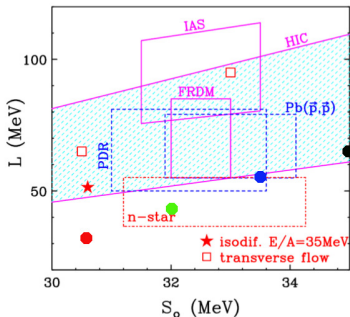
Neutron matter and symmetry energy

From the EOS, we can fit the symmetry energy around ρ_0 using

$$E_{\text{sym}}(\rho) = E_{\text{sym}} + \frac{L}{3} \frac{\rho - 0.16}{0.16} + \dots$$



Gandolfi *et al.*, EPJ (2014)

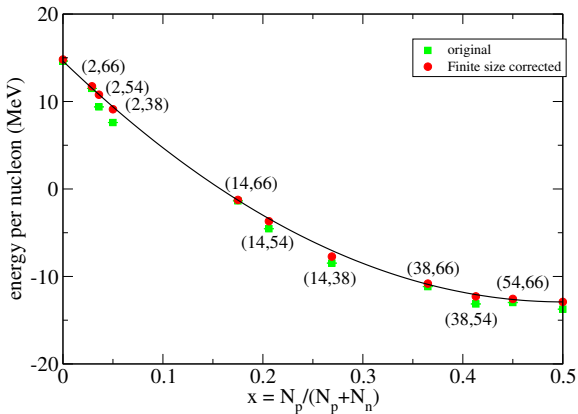


Tsang *et al.*, PRC (2012)

Very weak dependence to the model of 3N force for a given E_{sym} .
Chiral Hamiltonians give compatible results.

Nuclear matter

Asymmetric nuclear matter $E(\rho, x) = E_{SNM}(\rho) + E_{sym}^{(2)}(\rho)(1 - 2x)^2 + \dots$



Gandolfi, Lovato, Carlson, Schmidt, arXiv:1406.3388

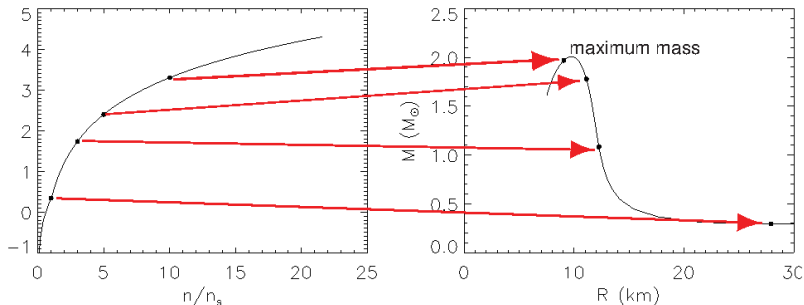
Quadratic dependence to isospin-asymmetry look fine.

Neutron matter and neutron star structure

TOV equations:

$$\frac{dP}{dr} = -\frac{G[m(r) + 4\pi r^3 P/c^2][\epsilon + P/c^2]}{r[r - 2Gm(r)/c^2]},$$

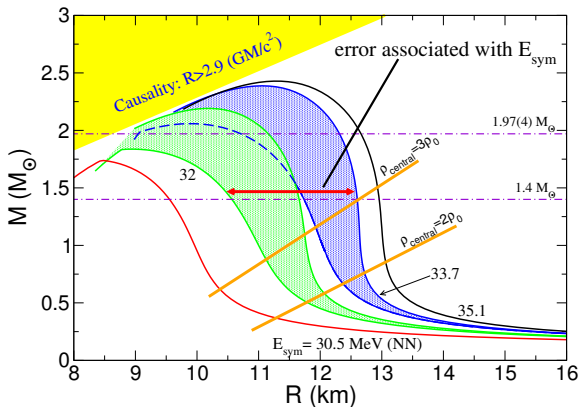
$$\frac{dm(r)}{dr} = 4\pi\epsilon r^2,$$



J. Lattimer

Neutron star structure

EOS used to solve the TOV equations.

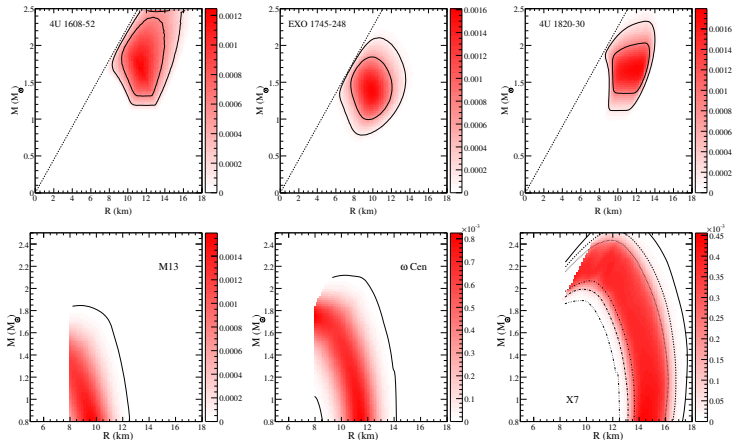


Gandolfi, Carlson, Reddy, PRC (2012).

Accurate measurement of E_{sym} put a constraint to the radius of neutron stars, **OR** observation of M and R would constrain E_{sym} !

Neutron stars

Observations of the mass-radius relation are becoming available:



Steiner, Lattimer, Brown, ApJ (2010)

Neutron star observations can be used to 'measure' the EOS and constrain E_{sym} and L .

Neutron star matter

Neutron star matter model:

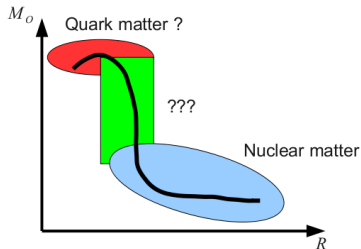
$$E_{NSM} = a \left(\frac{\rho}{\rho_0} \right)^\alpha + b \left(\frac{\rho}{\rho_0} \right)^\beta, \quad \rho < \rho_t$$

(form suggested by QMC simulations),

and a high density model for $\rho > \rho_t$

i) two polytropes

ii) polytrope+quark matter model



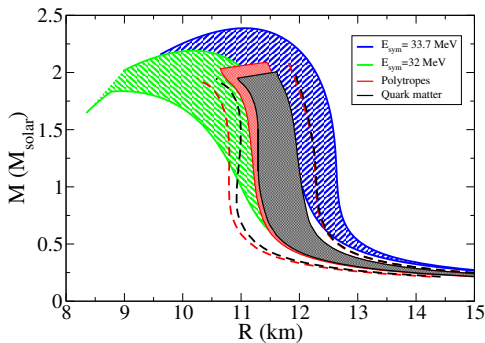
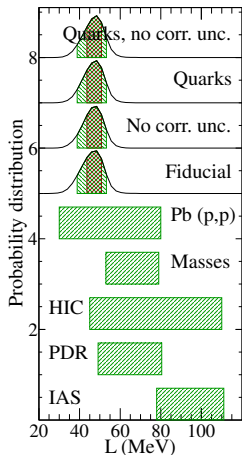
Neutron star radius sensitive to the EOS at nuclear densities!

Direct way to extract E_{sym} and L from neutron stars observations:

$$E_{sym} = a + b + 16, \quad L = 3(a\alpha + b\beta)$$

Neutron star matter really matters!

Here an 'astrophysical measurement'



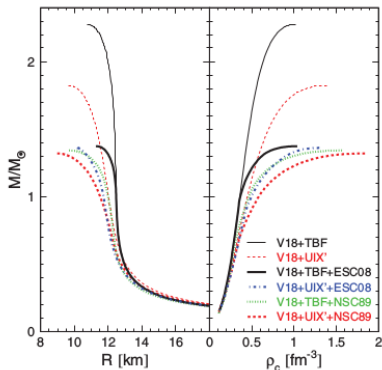
$$32 < E_{\text{sym}} < 34 \text{ MeV}, \quad 43 < L < 52 \text{ MeV}$$

Steiner, Gandolfi, PRL (2012).

High density neutron matter

If chemical potential large enough, heavier particles form, i.e. Λ , Σ , ...

Non-relativistic BHF calculations suggest that **none** of the available hyperon-nucleon Hamiltonians support an EOS with $M > 2M_{\odot}$:

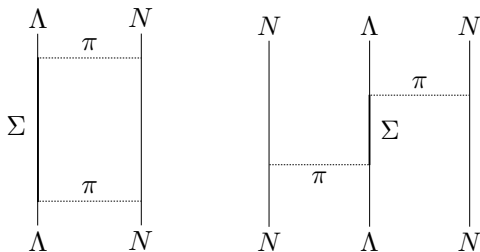


Schulze and Rijken PRC (2011).

(Some) other relativistic model support $2M_{\odot}$ neutron stars.

ΛN and ΛNN interactions

ΛNN has the same range of ΛN



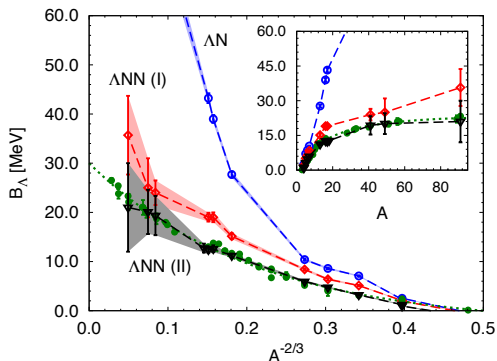
But, three-body interactions are not included in non-relativistic calculations!

Hypernuclei and hypermatter:

$$H = H_N + \frac{\hbar^2}{2m_\Lambda} \sum_{i=1}^A \nabla_i^2 + \sum_{i < j} v_{ij}^{\Lambda N} + \sum_{i < j < k} V_{ijk}^{\Lambda NN}$$

Λ hypernuclei

$v^{\Lambda N}$ and $V^{\Lambda NN}$ are phenomenological (Usmani).



Lonardonì, Pederiva, SG, PRC (2013) and PRC (2014).

$V^{\Lambda NN}$ (II) is a new form where the parameters have been fine tuned.
As expected, the role of ΛNN is crucial.

Hyper-neutron matter

Neutrons and Λ particles:

$$\rho = \rho_n + \rho_\Lambda, \quad x = \frac{\rho_\Lambda}{\rho}$$

$$E_{\text{HNM}}(\rho, x) = \left[E_{\text{PNM}}((1-x)\rho) + m_n \right] (1-x) + \left[E_{\text{P}\Lambda\text{M}}(x\rho) + m_\Lambda \right] x + f(\rho, x)$$

where $E_{\text{P}\Lambda\text{M}}$ is the non-interacting energy (no $v_{\Lambda\Lambda}$ interaction),

$$E_{\text{PNM}}(\rho) = a \left(\frac{\rho}{\rho_0} \right)^\alpha + b \left(\frac{\rho}{\rho_0} \right)^\beta$$

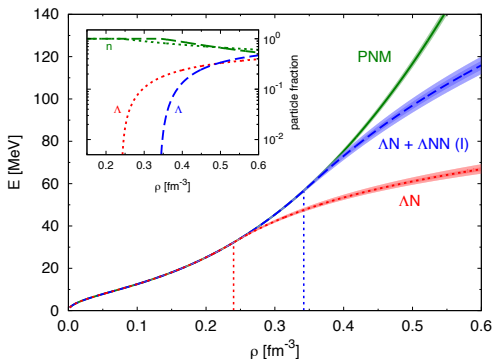
and

$$f(\rho, x) = c_1 \frac{x(1-x)\rho}{\rho_0} + c_2 \frac{x(1-x)^2 \rho^2}{\rho_0^2}$$

All the parameters are fit to AFDMC results.

Λ -neutron matter

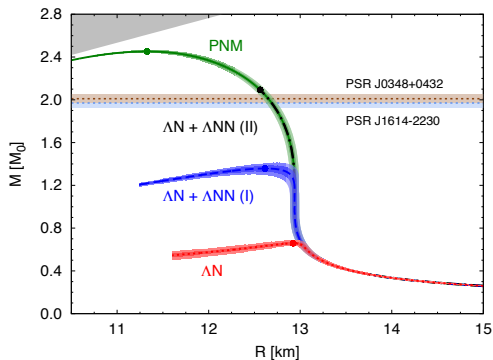
EOS obtained by solving for $\mu_\Lambda(\rho, x) = \mu_n(\rho, x)$



Lonardoni, Lovato, Gandolfi, Pederiva, arXiv:1407.4448 (2014)

No hyperons for ΛNN (II) up to $\rho = 0.5 \text{ fm}^{-3}$!

Λ -neutron matter



Lonardoni, Lovato, Gandolfi, Pederiva, arXiv:1407.4448 (2014)

Drastic role played by ΛNN . Calculations compatible with neutron star observations.

Note: no $v_{\Lambda\Lambda}$, no protons, and no other hyperons included

QMC methods useful to study nuclear systems in a coherent framework:

- Three-neutron force is the bridge between E_{sym} and neutron star structure.
- Neutron star observations becoming competitive with experiments.
Can we use observations with current uncertainties to constrain nuclear interactions?
- Λ -nucleon data very limited. Role of Λ in neutron stars far to be understood. Input from Lattice QCD?
Conclusion? We cannot conclude anything with present models...

Acknowledgments

- J. Carlson, J. Lynn (LANL)
- D. Lonardoni, A. Lovato, R. Wiringa (ANL)
- F. Pederiva (Trento)
- A. Steiner (INT)
- K. Schmidt (ASU)