

$a < 0$

Seattle, 13 May 2014

$a > 0$



$1/a$

Efimov and beyond:

new twists in
few-body physics
with ultracold bosons
and fermions

Rudi Grimm,

Innsbruck





V. Efimov, Yad. Fiz.
12, 1080 (1970)

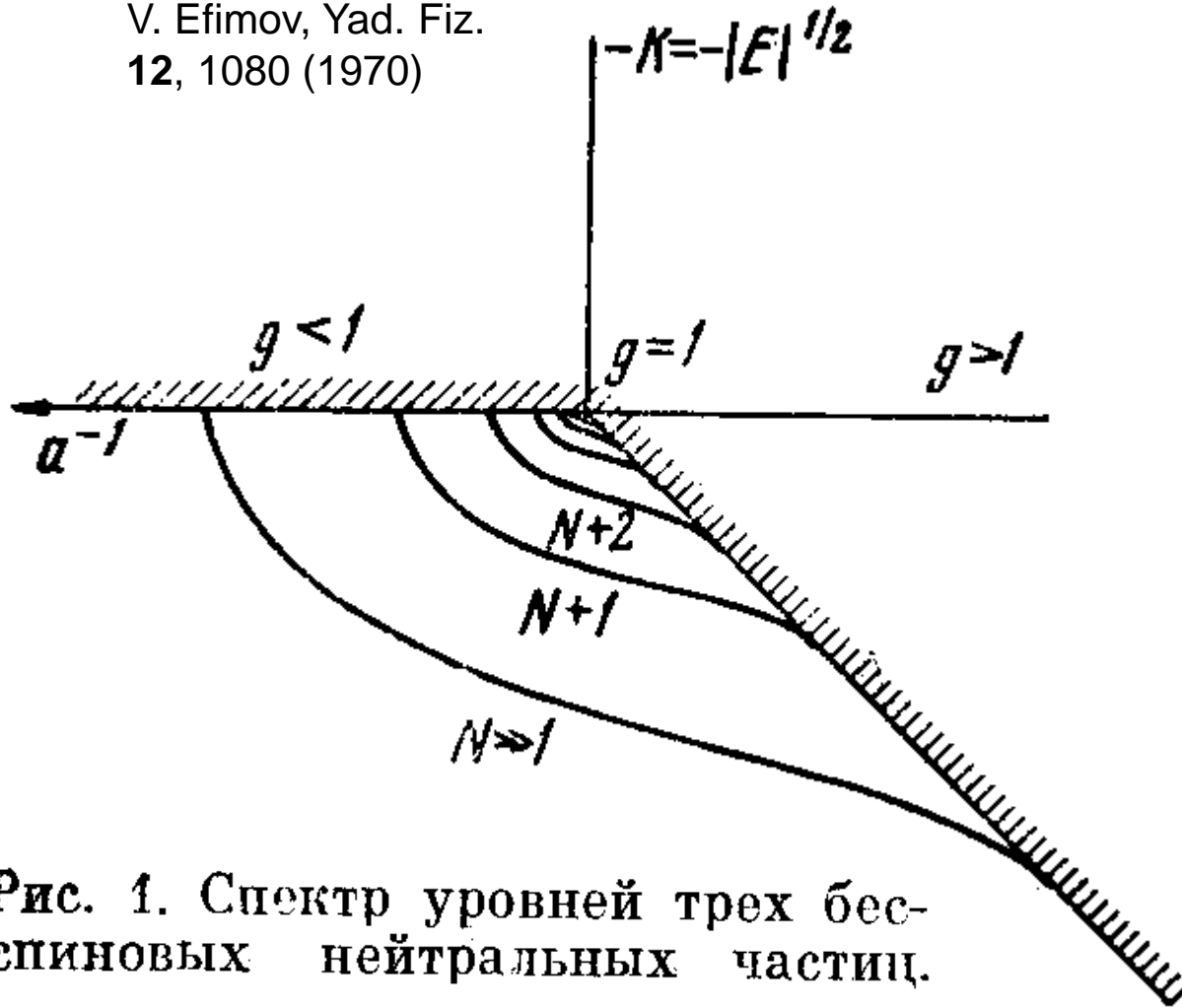


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

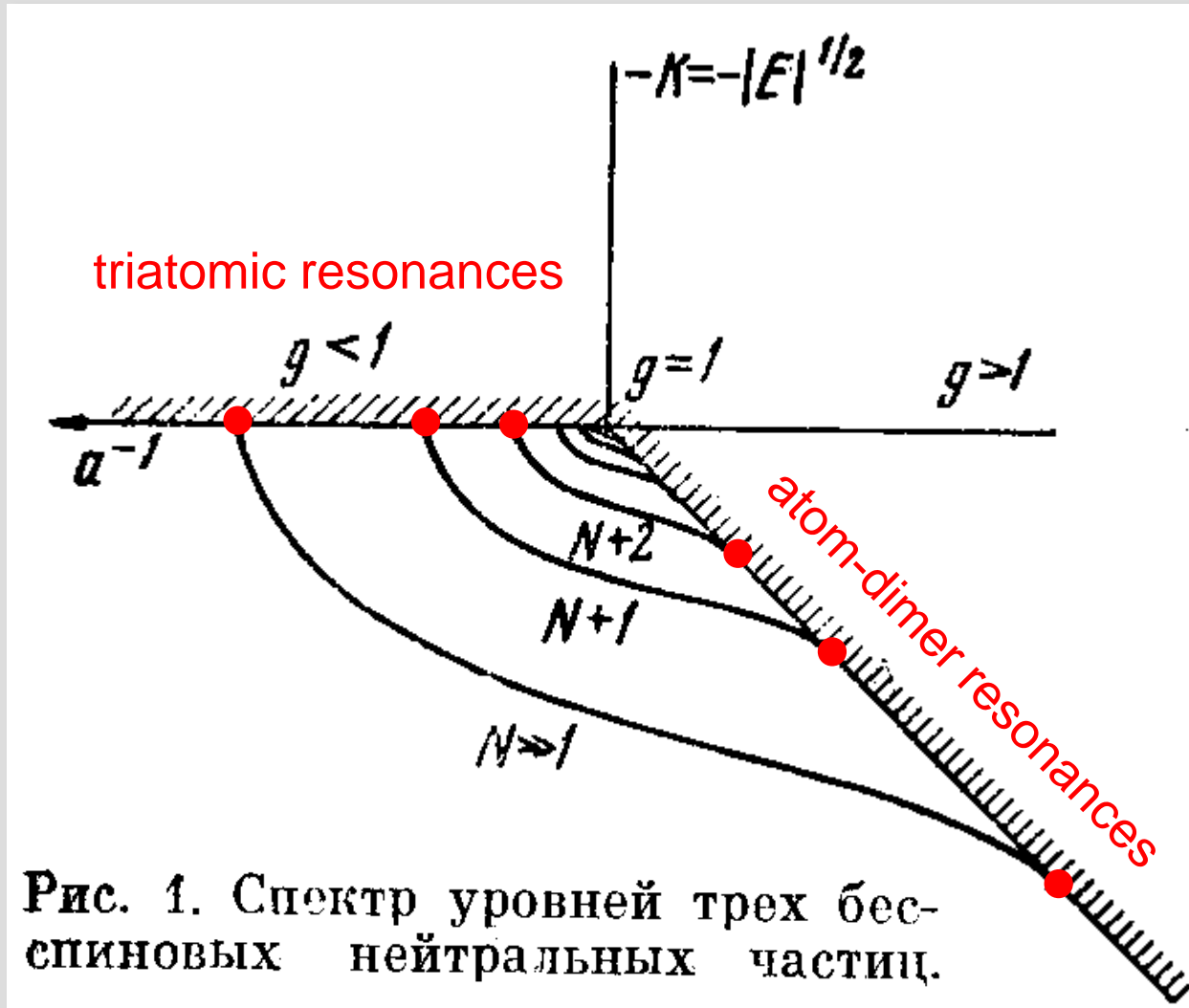


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

$$a_{-}^{(n+1)} / a_{-}^{(n)} = 22.7$$

$$a_{*}^{(n+1)} / a_{-}^{(n)} = 1.06$$

unknown $a_{-}^{(0)}$
(three-body parameter)

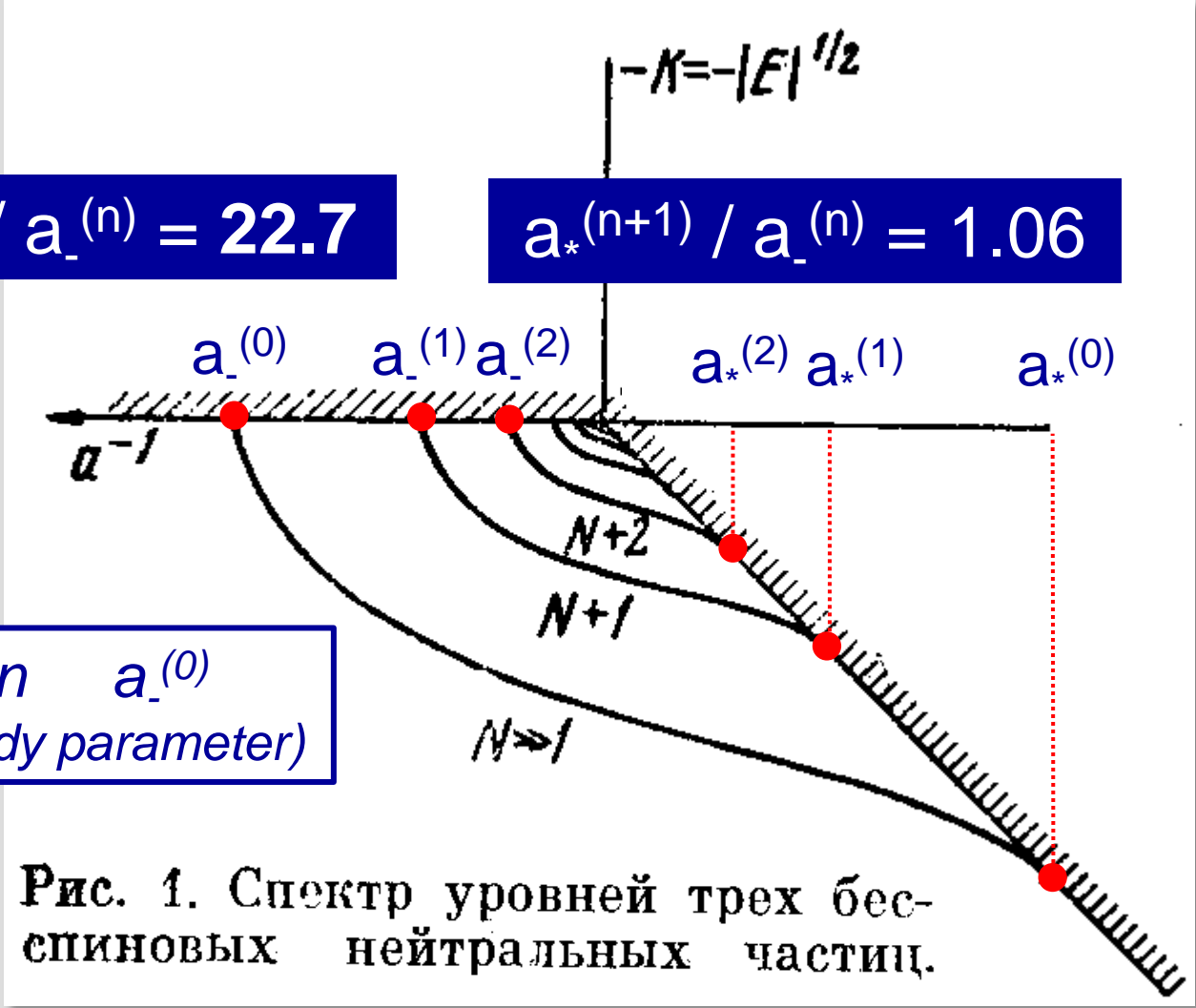
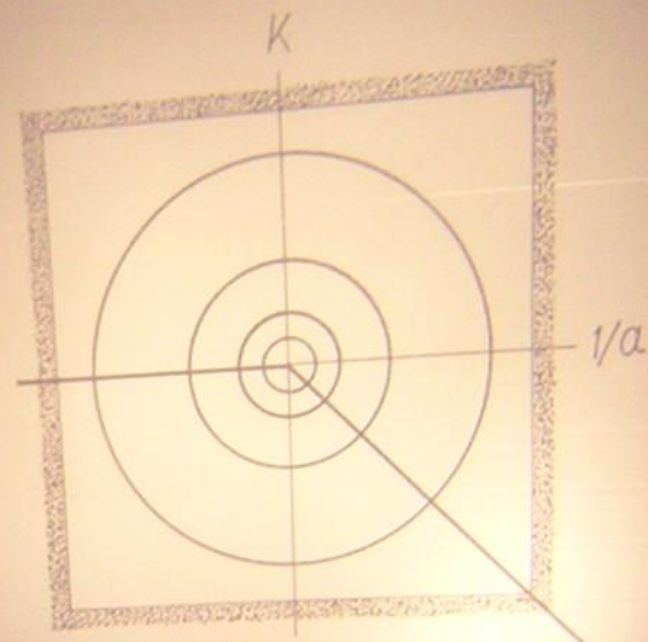


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

INSIDE THE WINDOW OF UNIVERSALITY



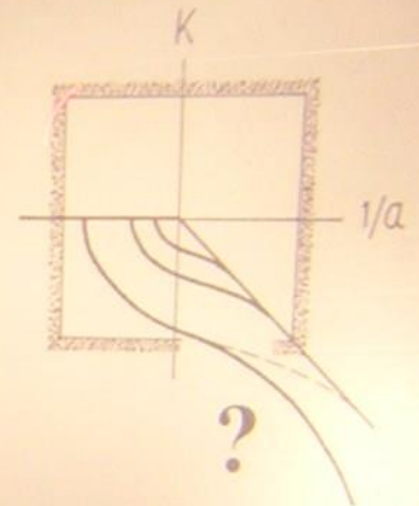
$$K < 1/r_0,$$

$$1/a < 1/r_0$$



FB 18, Santos, Brazil
26 Aug 2006

MISCONCEPTION 1



FB 18, Santos, Brazil
26 Aug 2006

van der
Waals
length

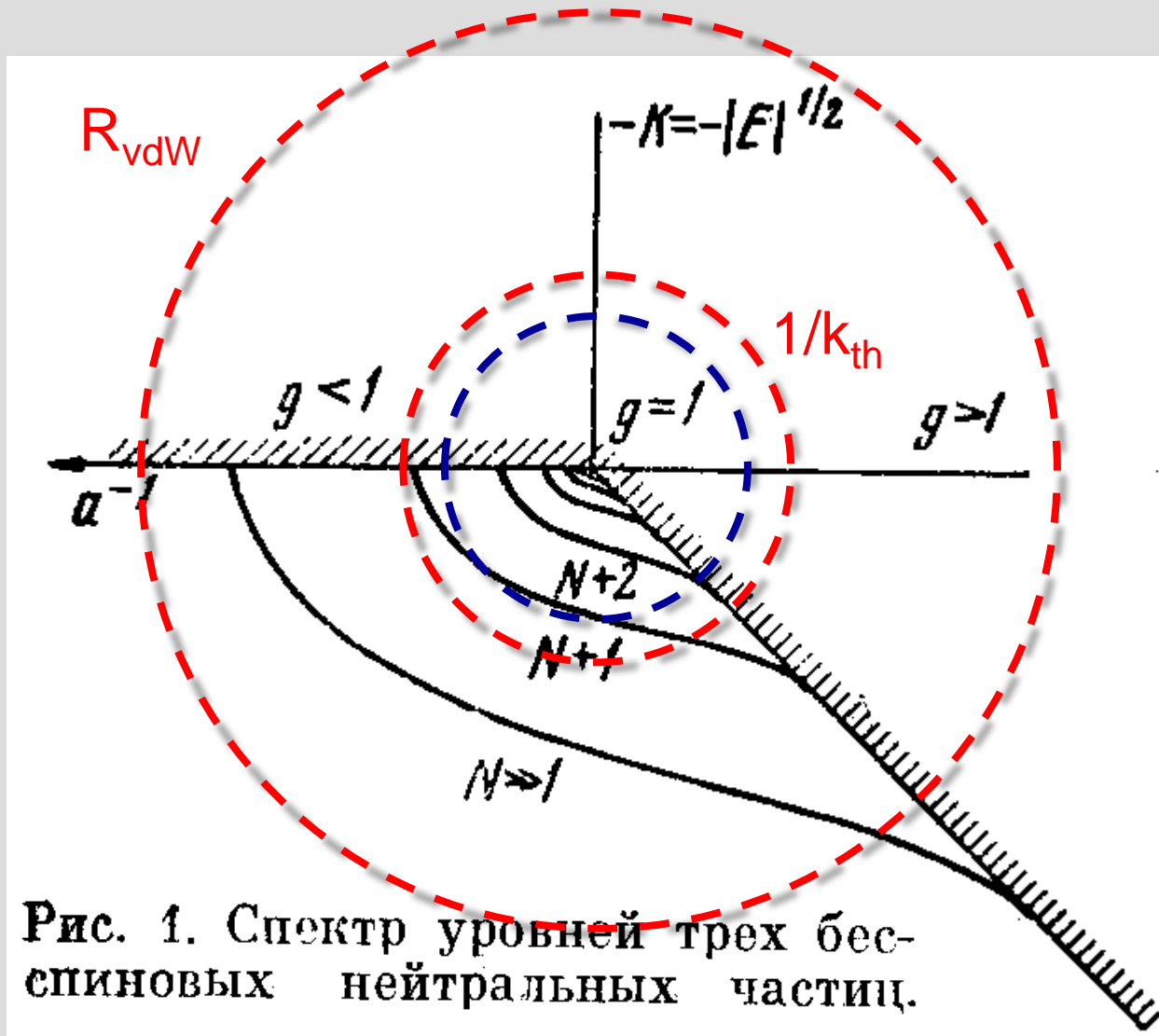


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

thermal
de Broglie
wavelength

mean
interparticle
distance
 $n^{-1/3}$

$\approx 1/k_{\text{th}}$
near-deg. gas

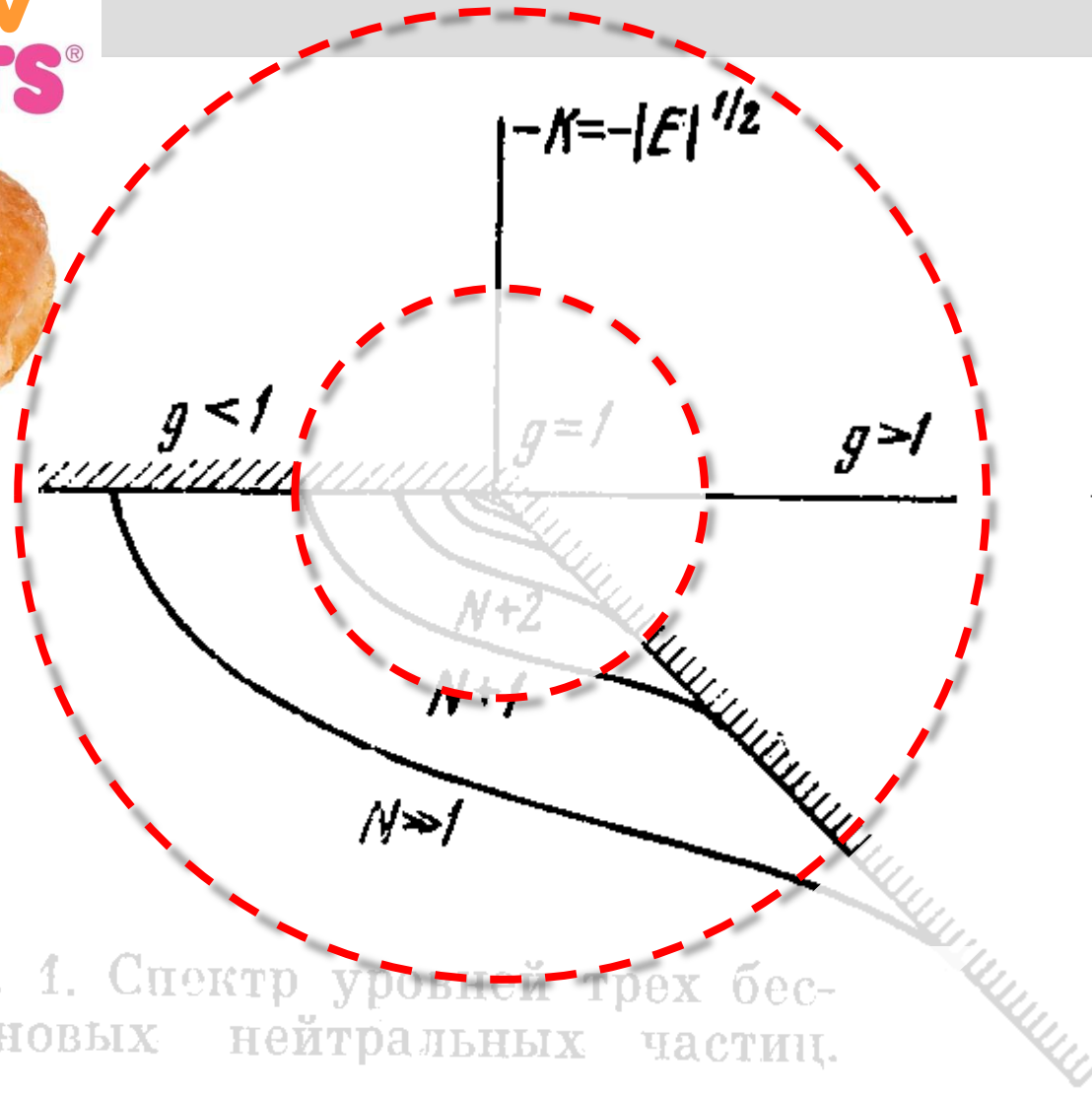


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

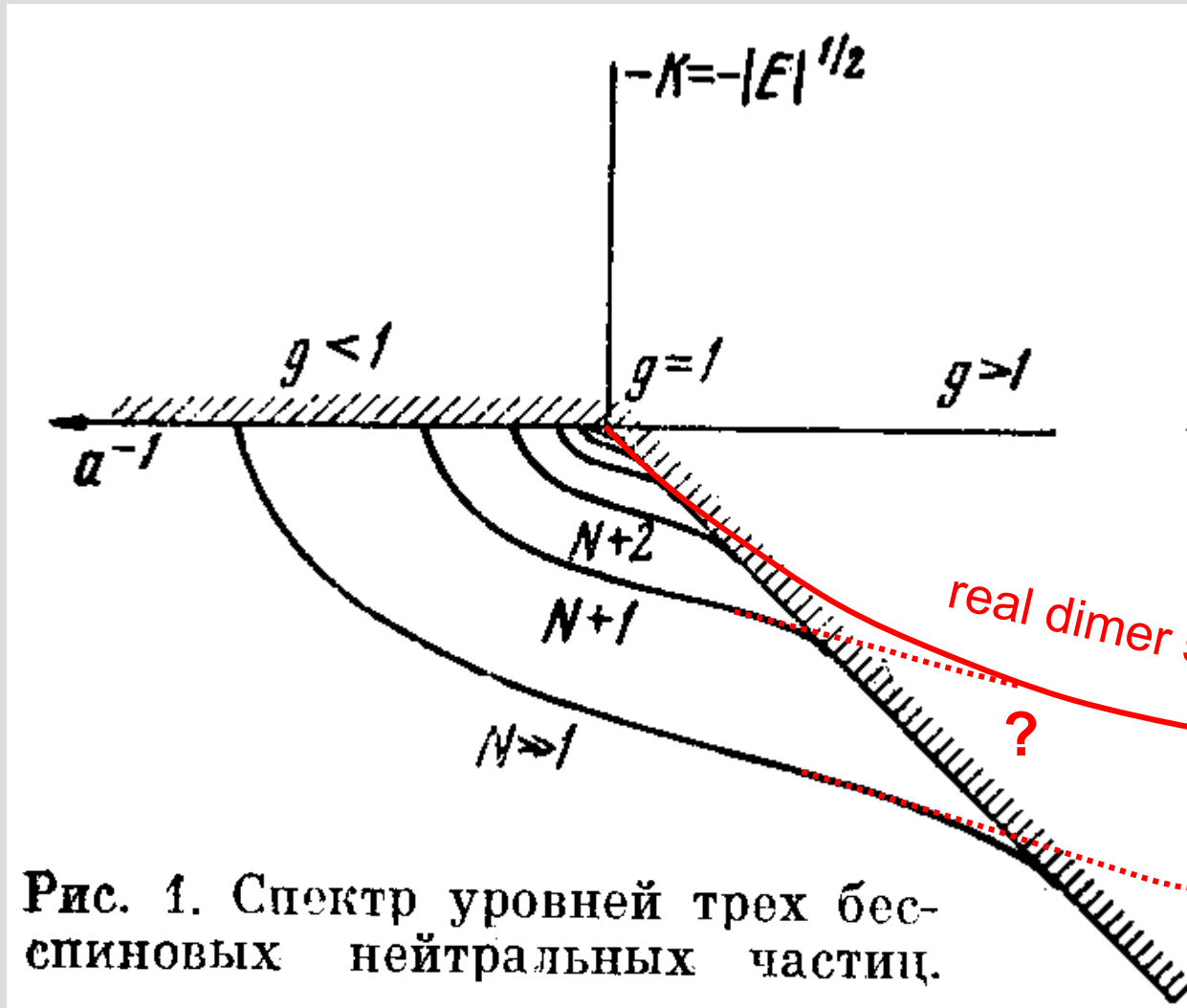
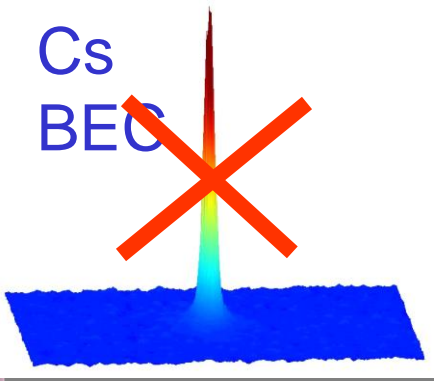
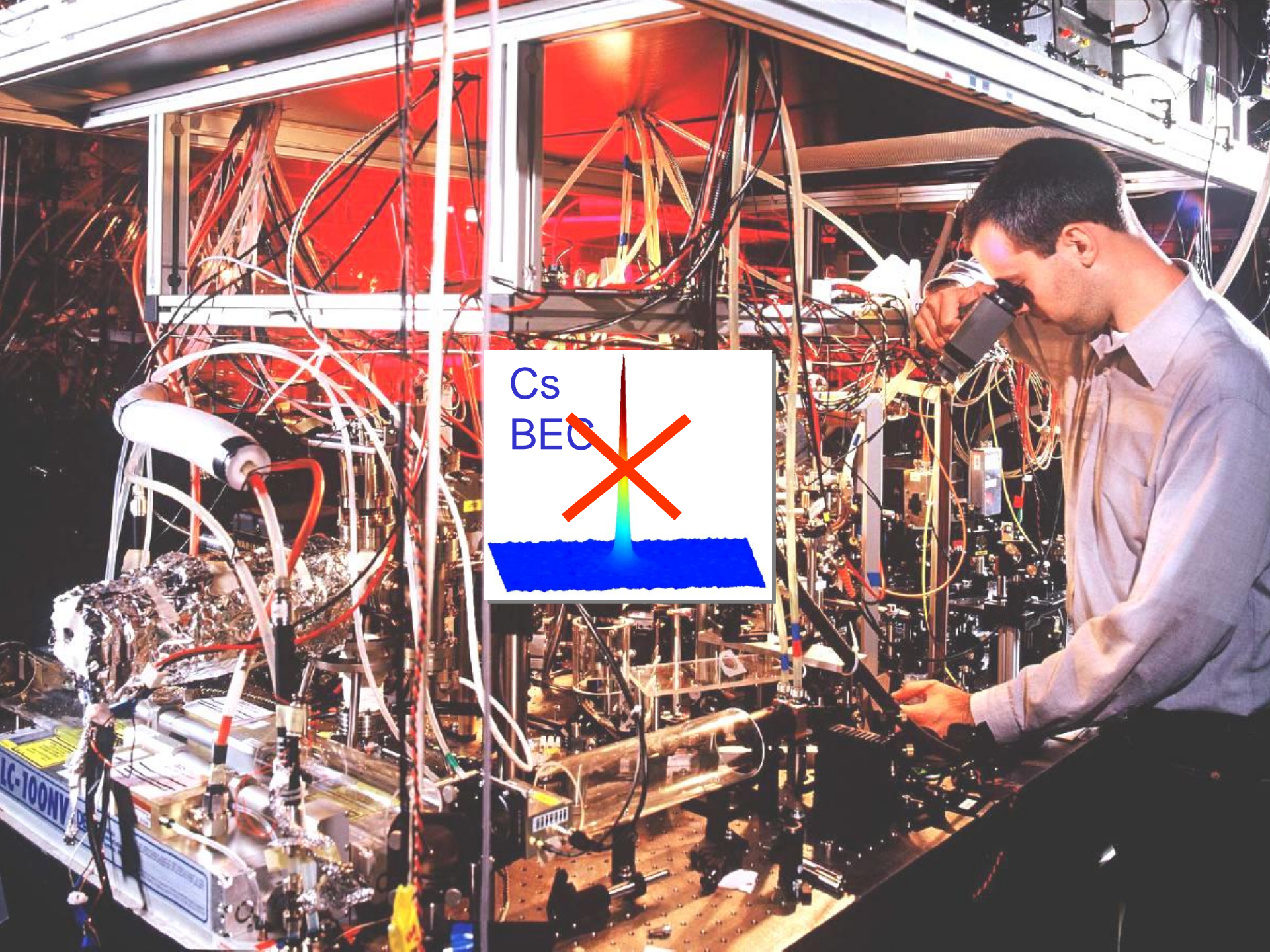
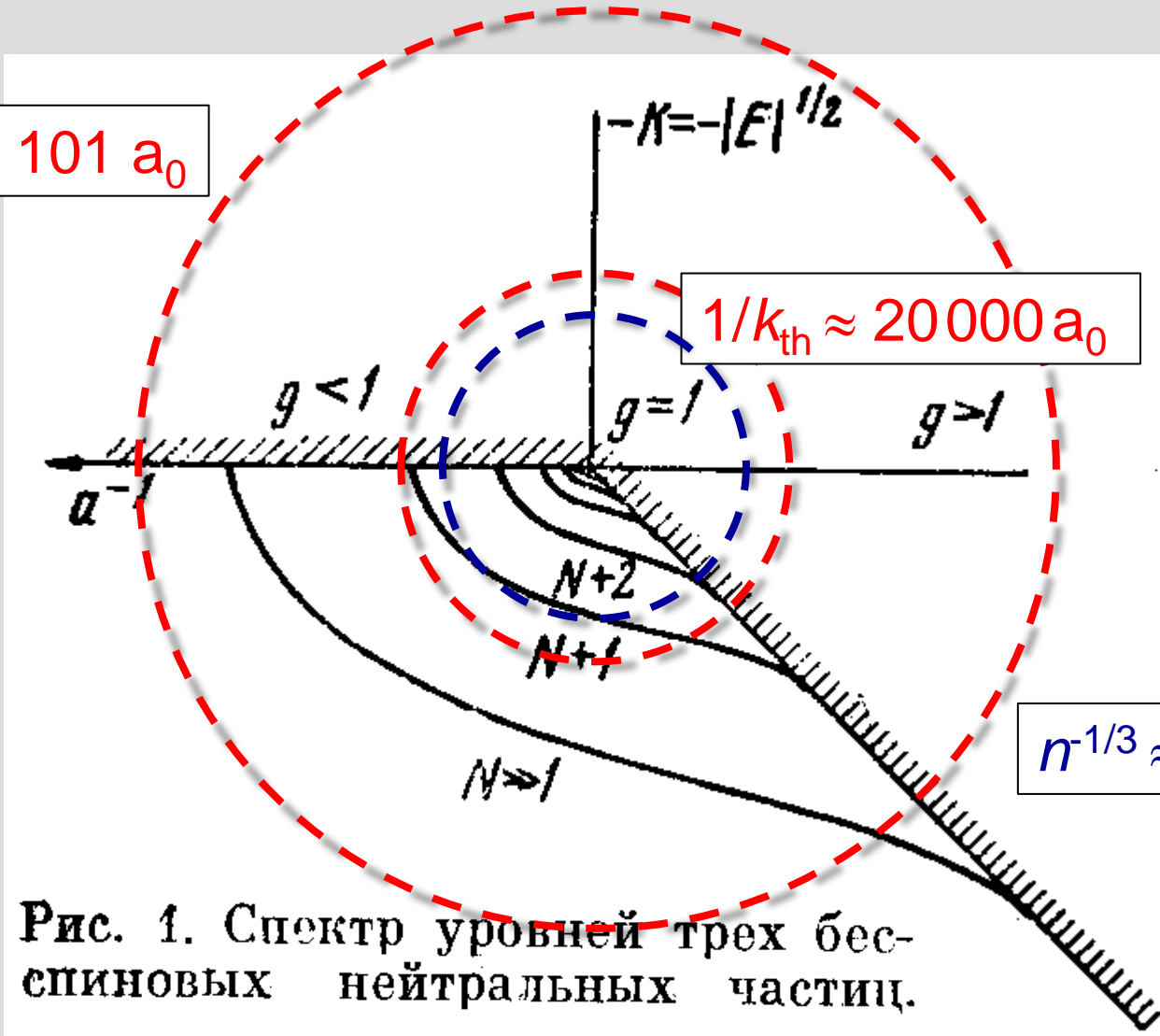


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.



$$R_{\text{vdW}} = 101 a_0$$



$T = 8\text{nK}$

$$n^{1/3} \approx 70\,000 a_0$$

$$n = 2 \times 10^{10} \text{cm}^{-3}$$

Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

magnetic tunability of Cs

ultracold.atoms

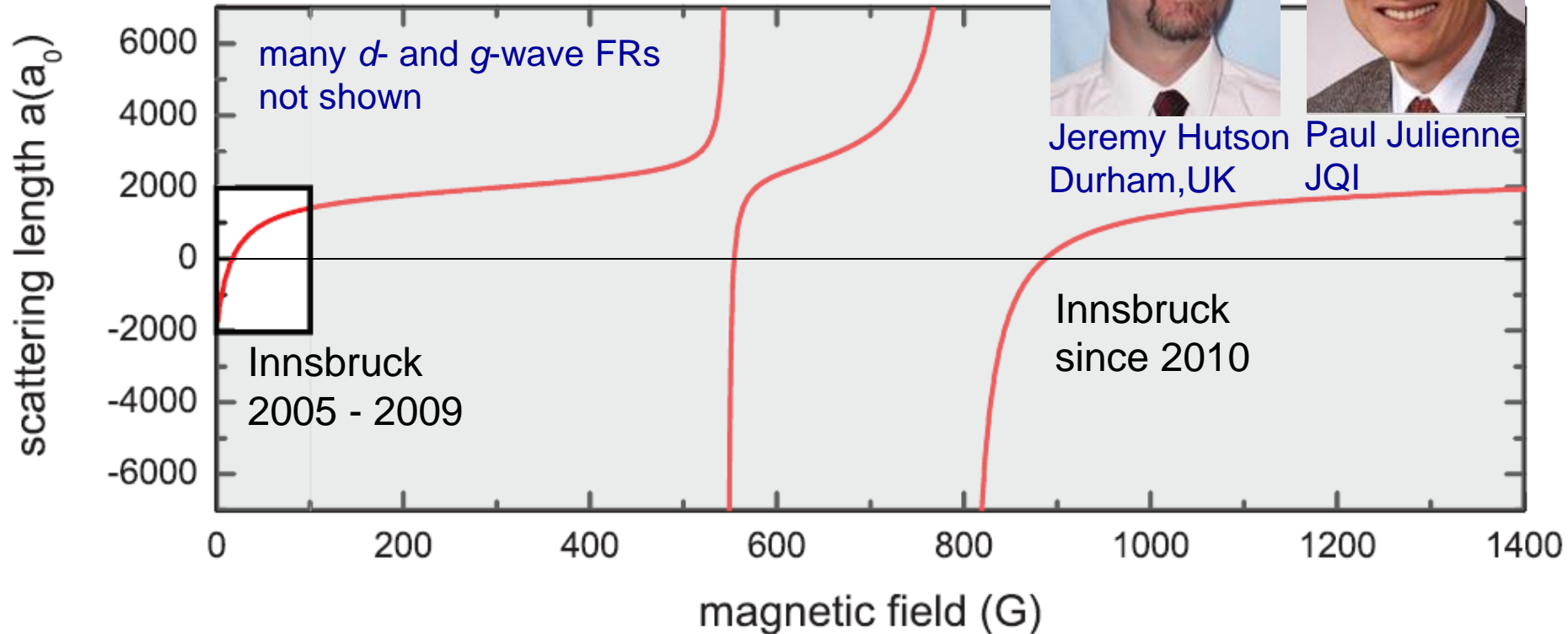
many more details and most accurate $a(B)$ mapping
Berninger et al., PRA 87, 032517 (2013)



Jeremy Hutson
Durham, UK



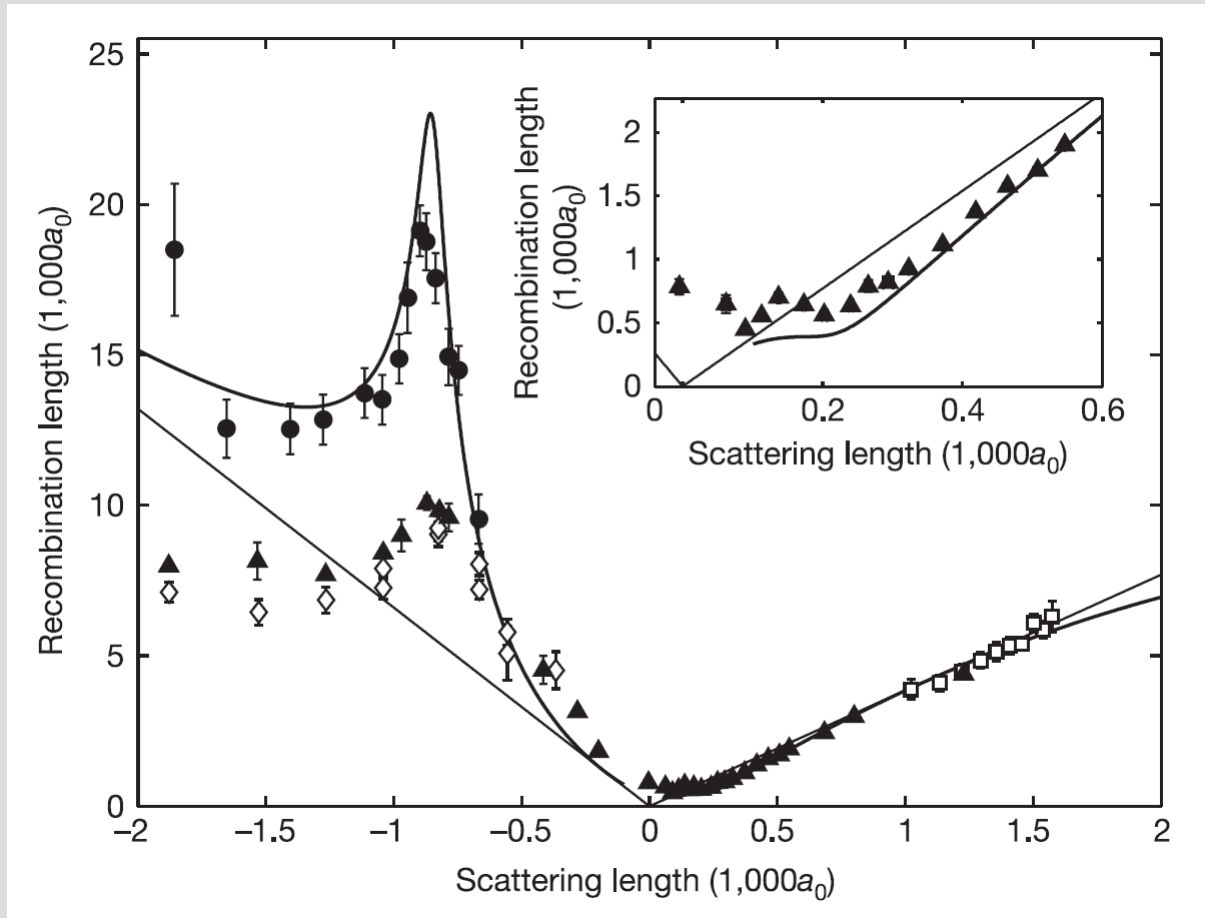
Paul Julienne
JQI



cesium ($F=3$, $m_F=3$, region of low B-fields)

$T=10\text{nK}$

250nK



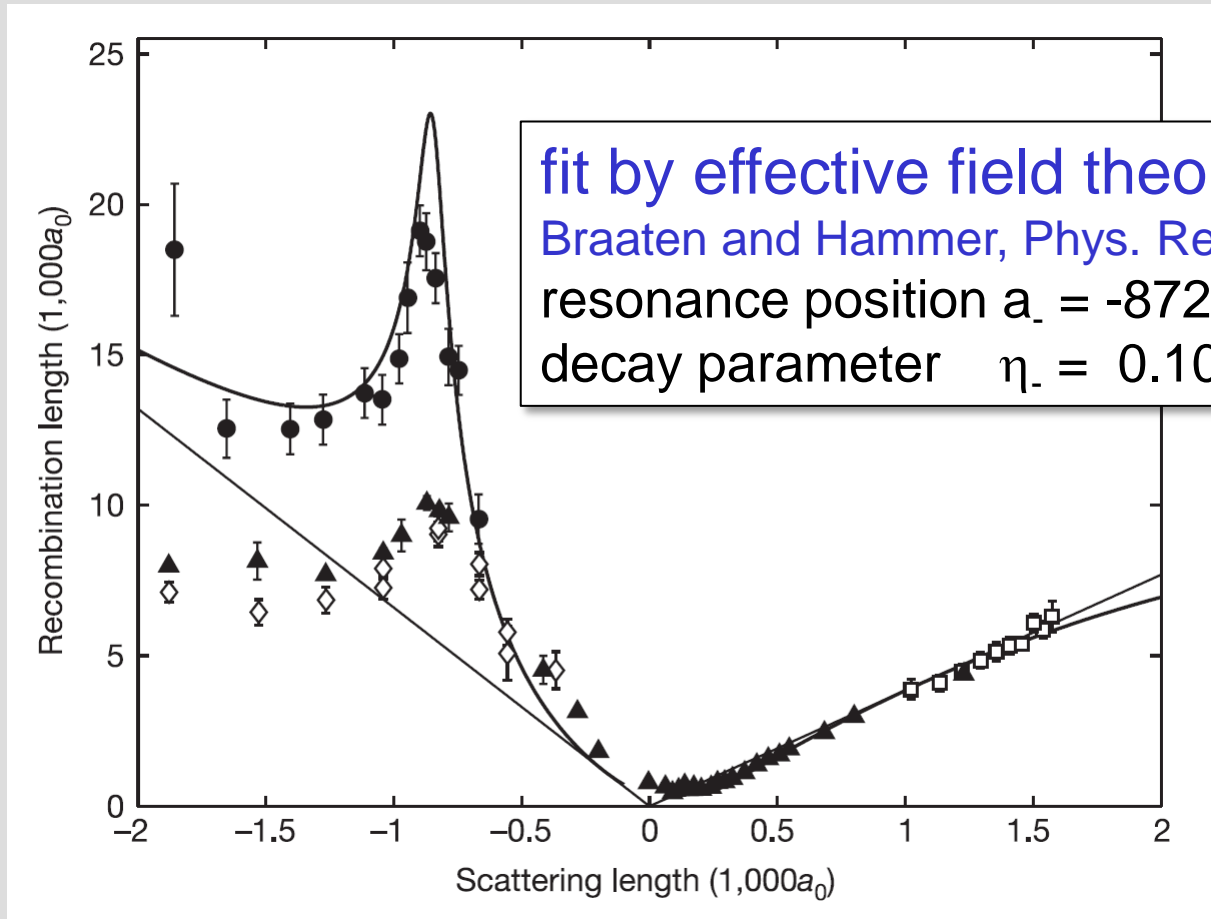
original results: Kraemer et al. Nature **440**, 315 (2006)
updated analysis: Berninger et al., PRL **107**, 120401 (2011)

first observations in Cs (2006)

cesium ($F=3$, $m_F=3$, region of low B-fields)

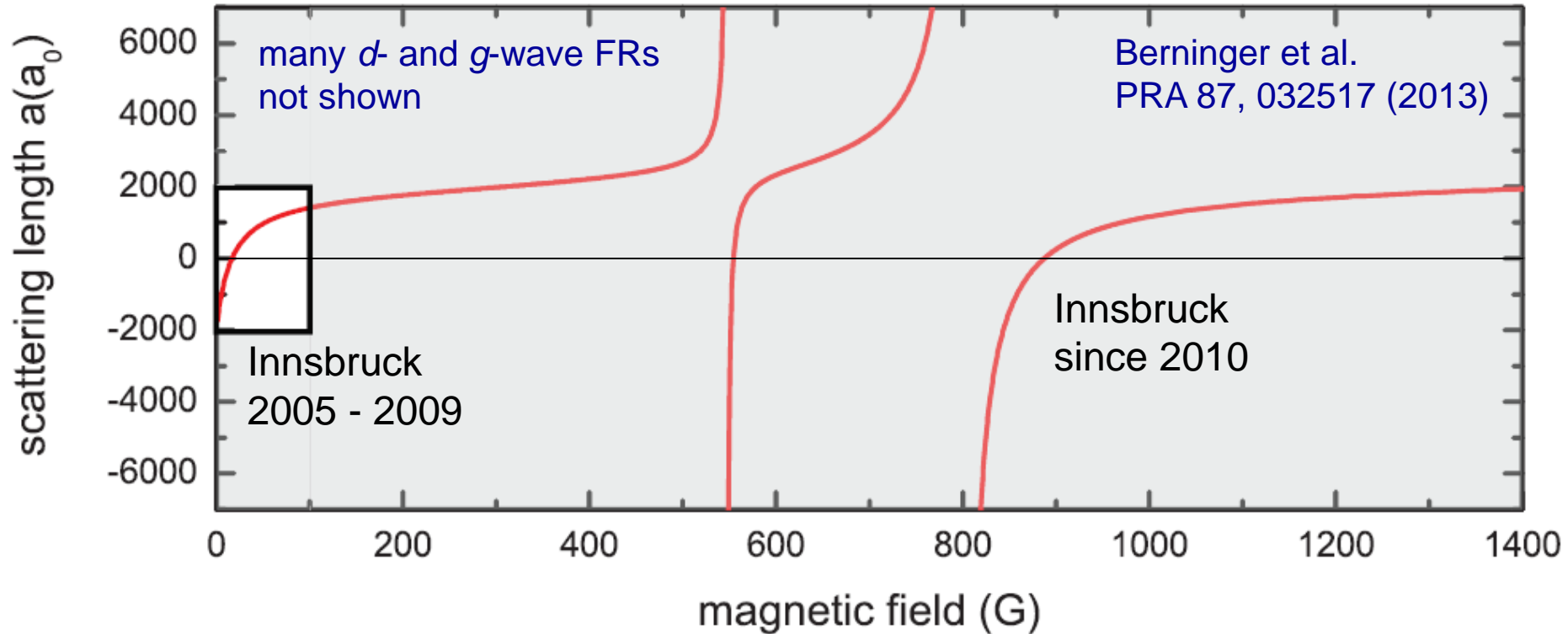
$T=10\text{nK}$

250nK



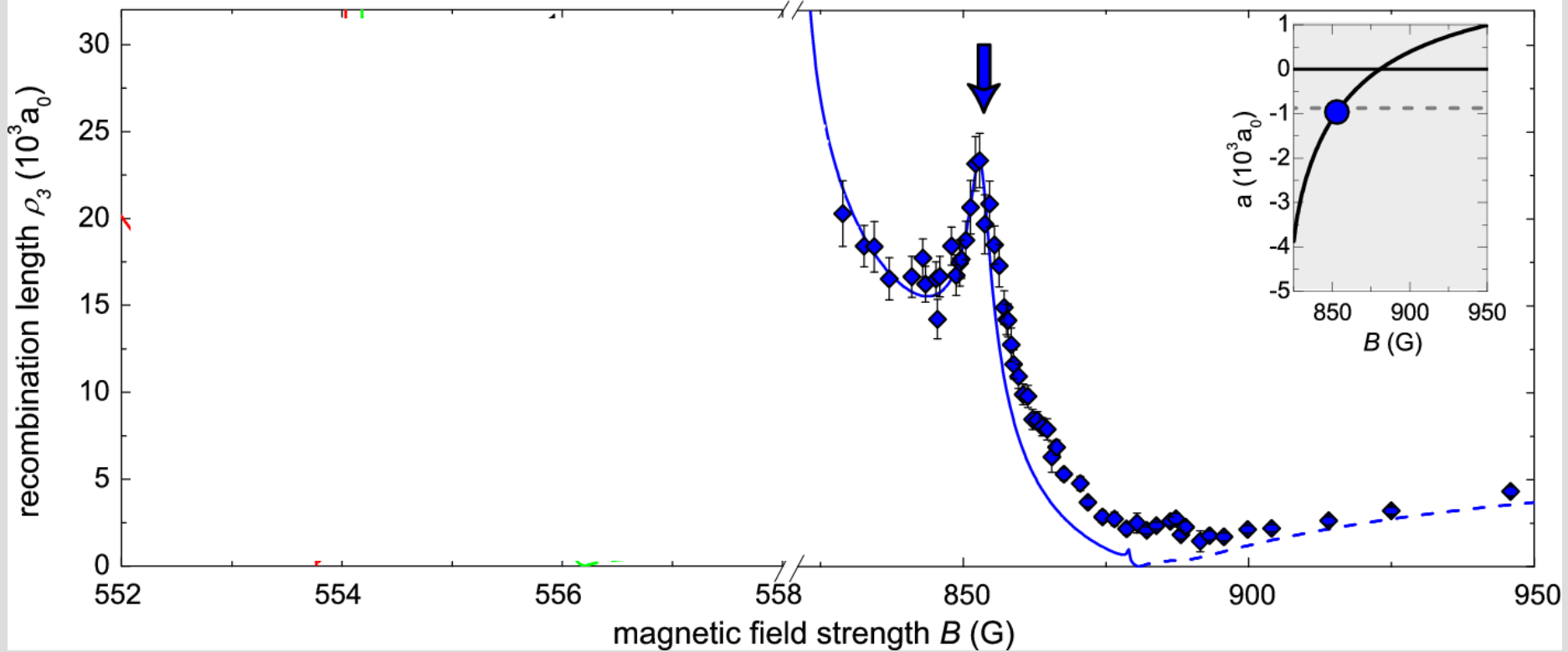
original results: Kraemer et al. Nature **440**, 315 (2006)

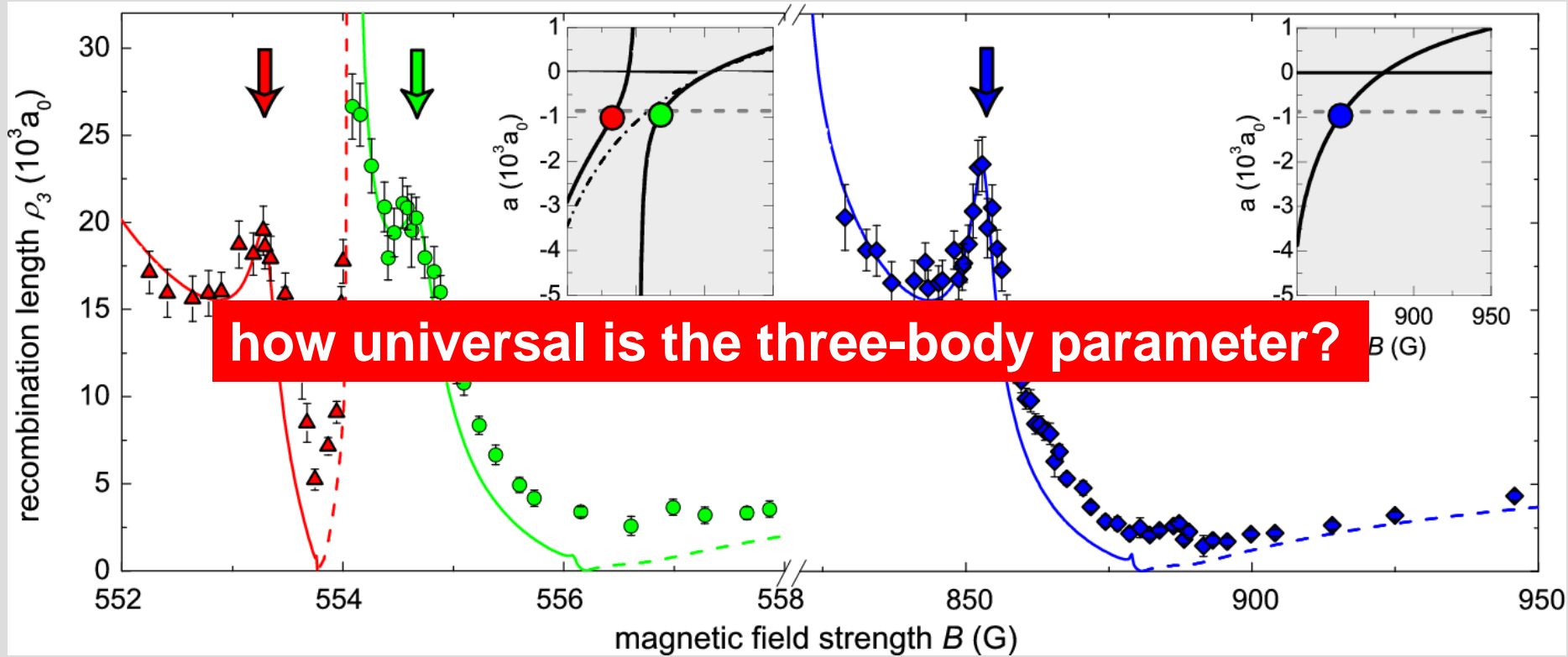
updated analysis: Berninger et al., PRL **107**, 120401 (2011)



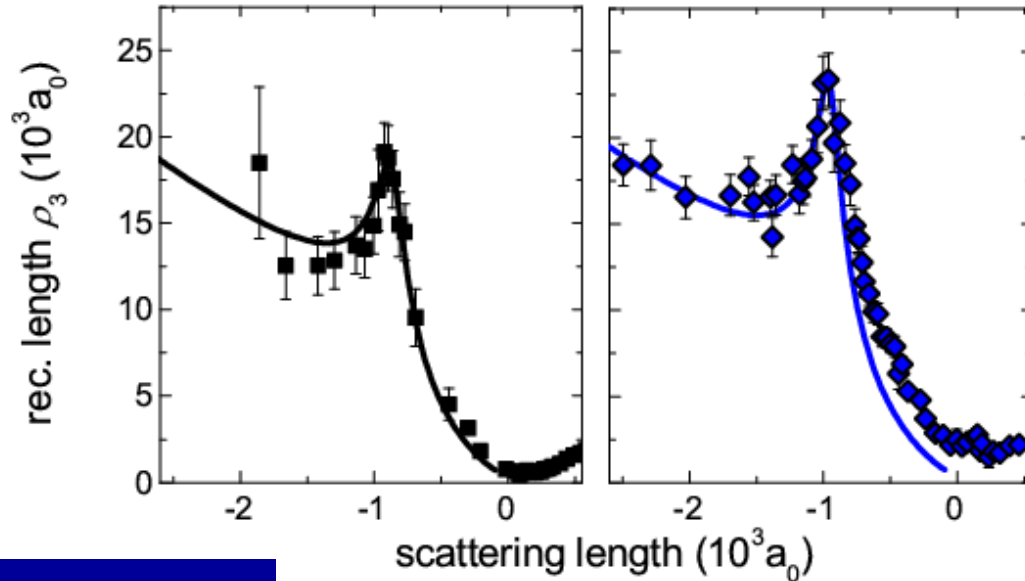
observation of new Efimov resonances in Cs

ultracold.atoms

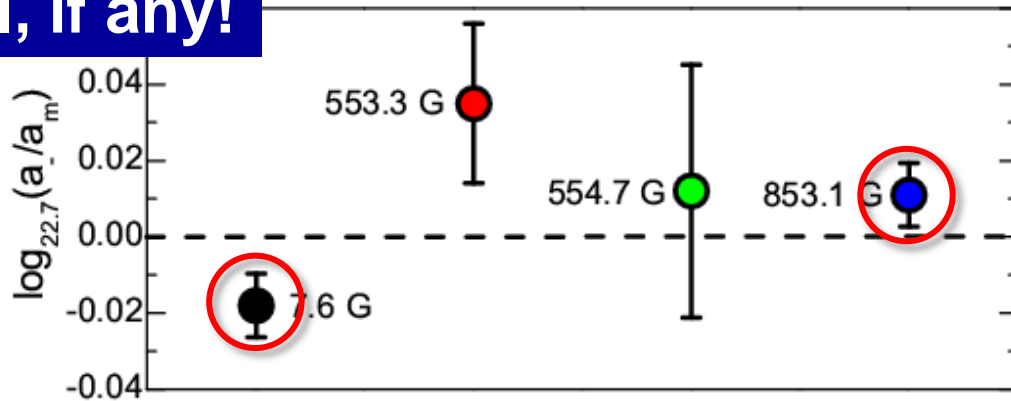




variations of the three-body parameter?



very small, if any!



strongly entrance-channel dominated FRs

same message from other species

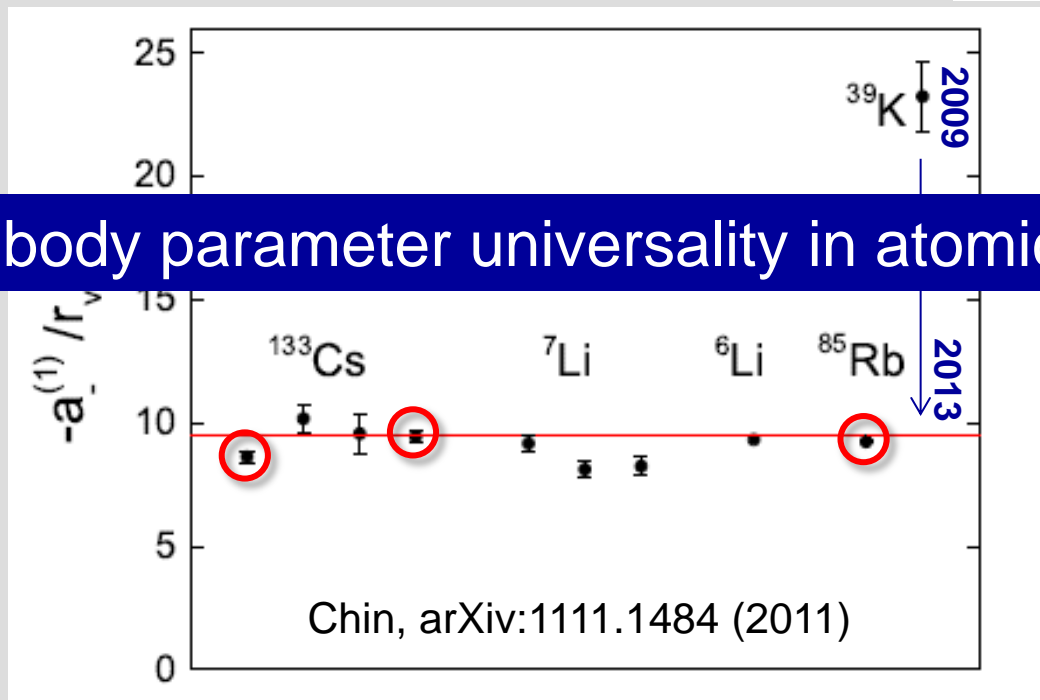
experiments on ${}^6\text{Li}$, ${}^7\text{Li}$, ${}^{39}\text{K}$, ${}^{85}\text{Rb}$, ${}^{133}\text{Cs}$ show

$$a_- \approx -9.5 R_{\text{vdW}}$$

$$R_{\text{vdW}} = \frac{1}{2} \left(\frac{2\mu C_6}{\hbar^2} \right)^{1/4}$$

van der Waals length

three-body parameter universality in atomic systems



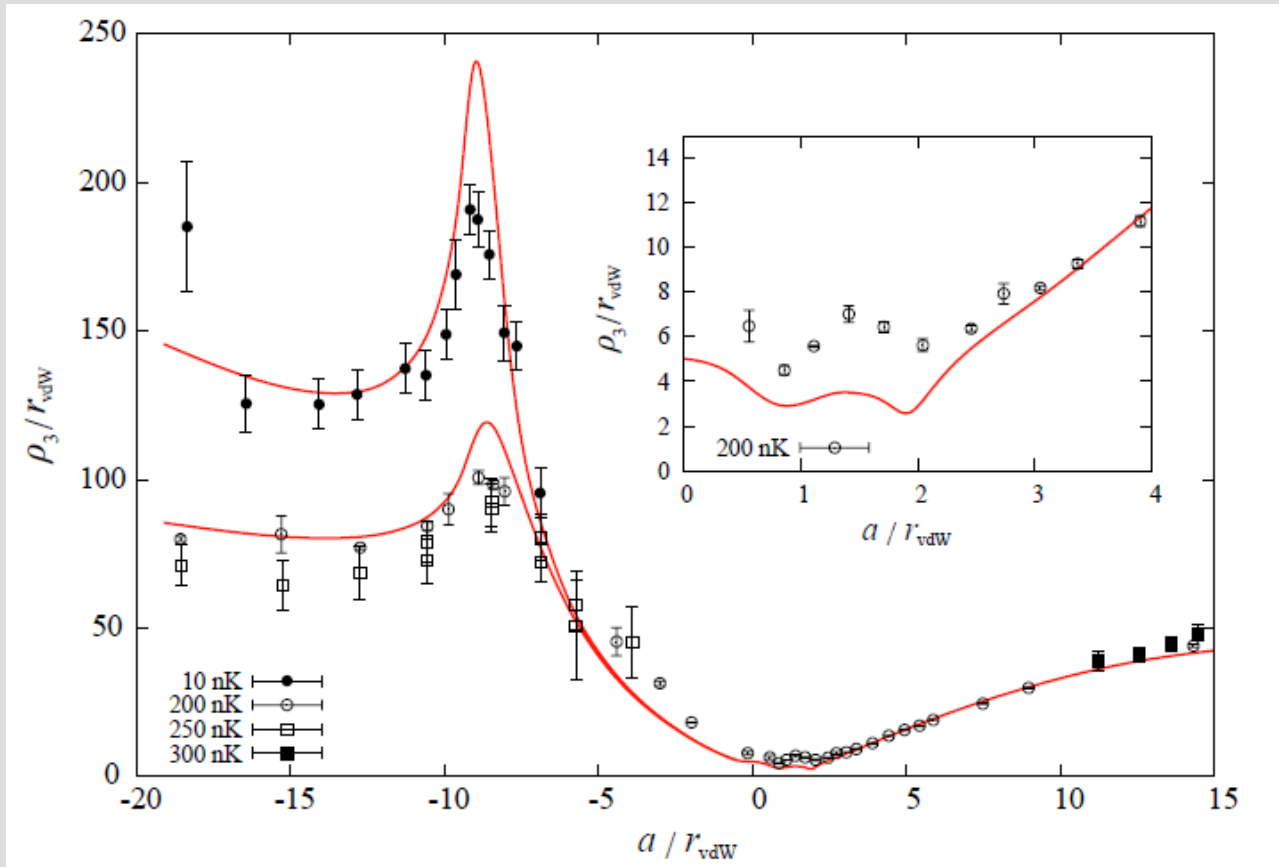
Wang et al., PRL **106**, 263001 (2012)

Schmidt et al., EPJB **85**, 386 (2012)

Naidon et al., PRL **112**, 105301 (2014)

Y. Wang and P. Julienne
arXiv:1404.0483

two dimensionless parameters to describe
particular Feshbach resonance: s_{res} and r_{bg}

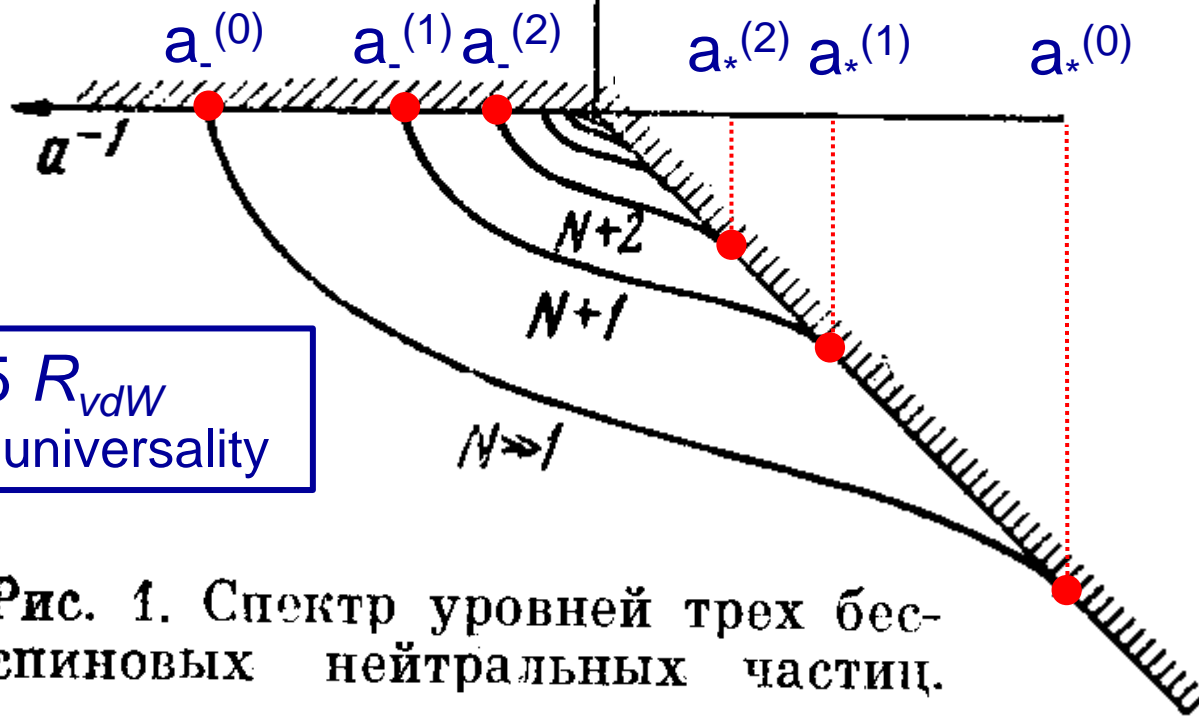


can we test these relations?

$$-K = -|E|^{1/2}$$

$$a_{-}^{(n+1)} / a_{-}^{(n)} = 22.7$$

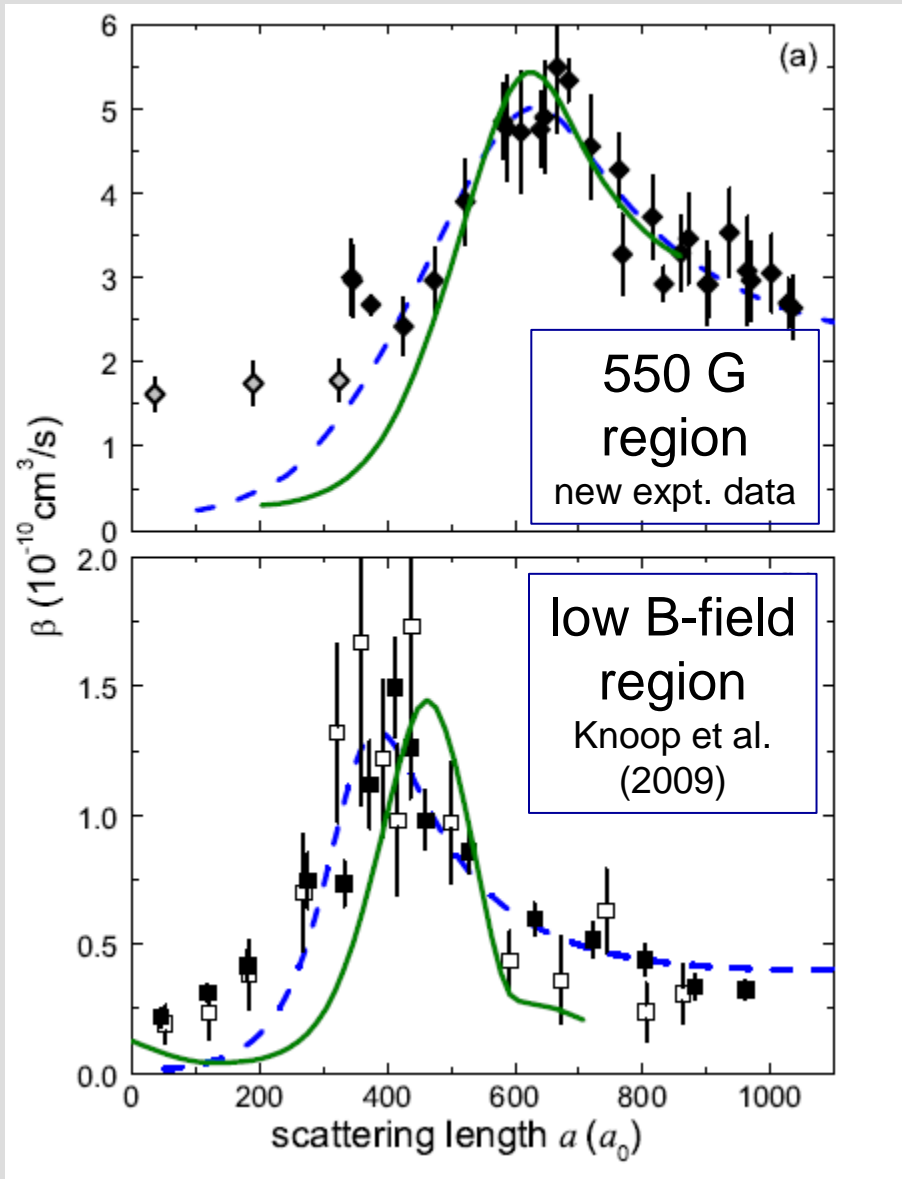
$$a_{*}^{(n+1)} / a_{-}^{(n)} = 1.06$$



$$a_{-}^{(0)} \approx -9.5 R_{vdW}$$

vdW universality

Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.



Zenesini et al., soon on arXiv

EFT fit \rightarrow

$$a_*^{(1)} / a_-^{(0)} = 0.48(2)$$

$\neq 1.06$

$$a_*^{(1)} / a_-^{(0)} = 0.68(6)$$

vdW universal model
gets positions essentially
right !

Y. Wang and P. Julienne

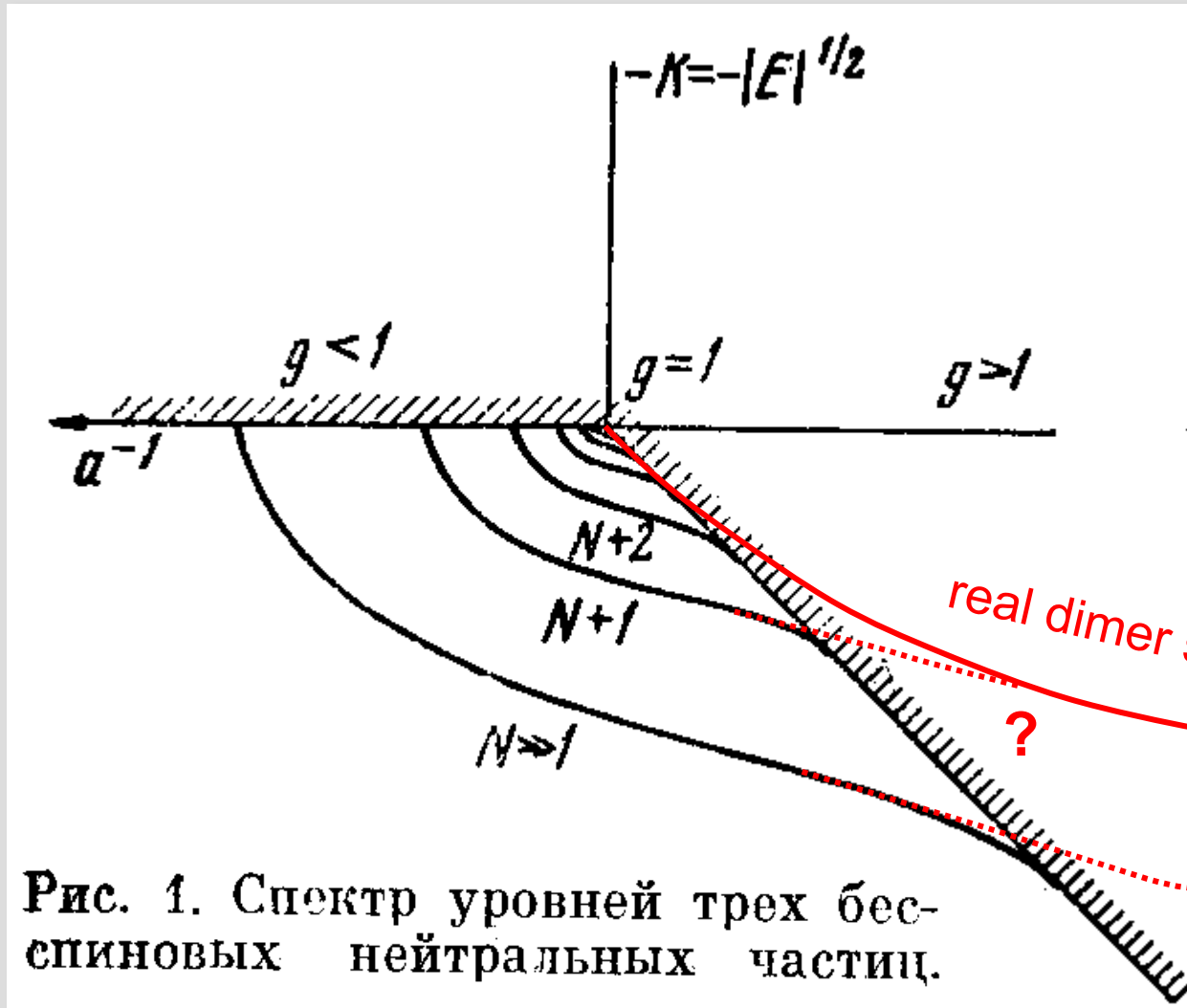


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

test of Efimov period?

$$a_{-}^{(n+1)} / a_{-}^{(n)} = 22.7$$

$$a_{*}^{(n+1)} / a_{-}^{(n)} = 1.06$$

problematic
in real atomic
systems
(but vdW univ.
works)

$$a_{-}^{(0)} \approx -9.5 R_{vdW}$$

vdW universality

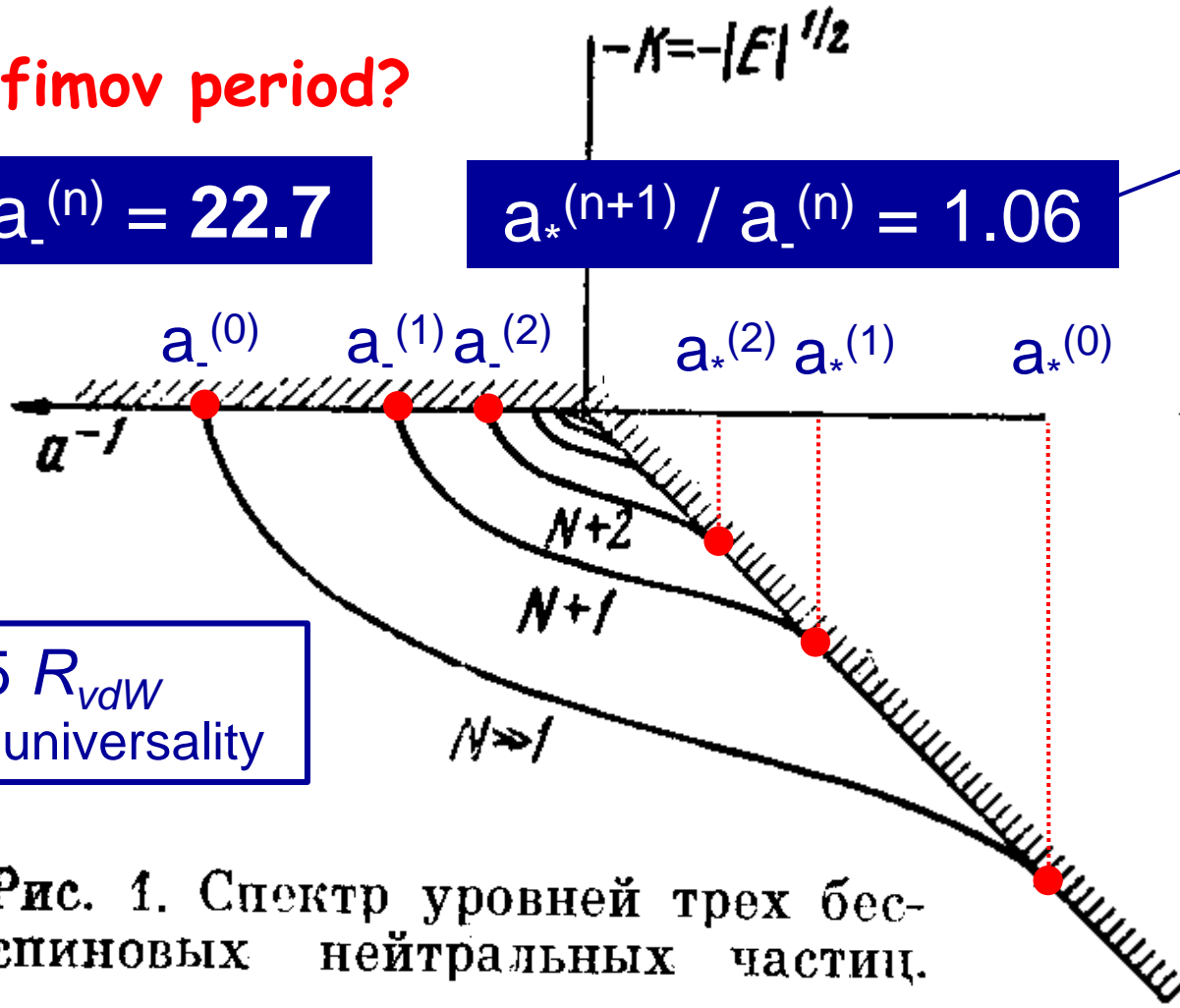
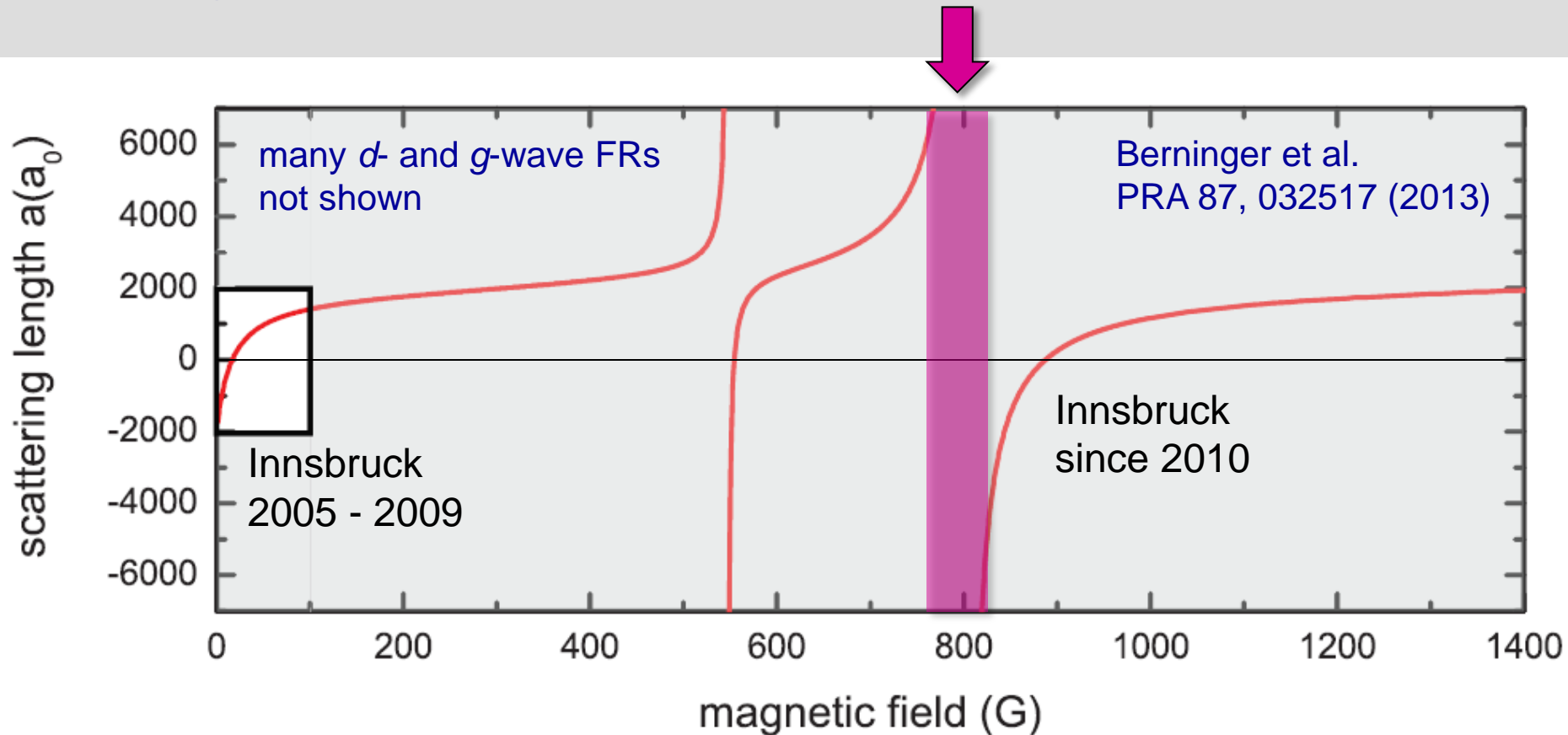


Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц.

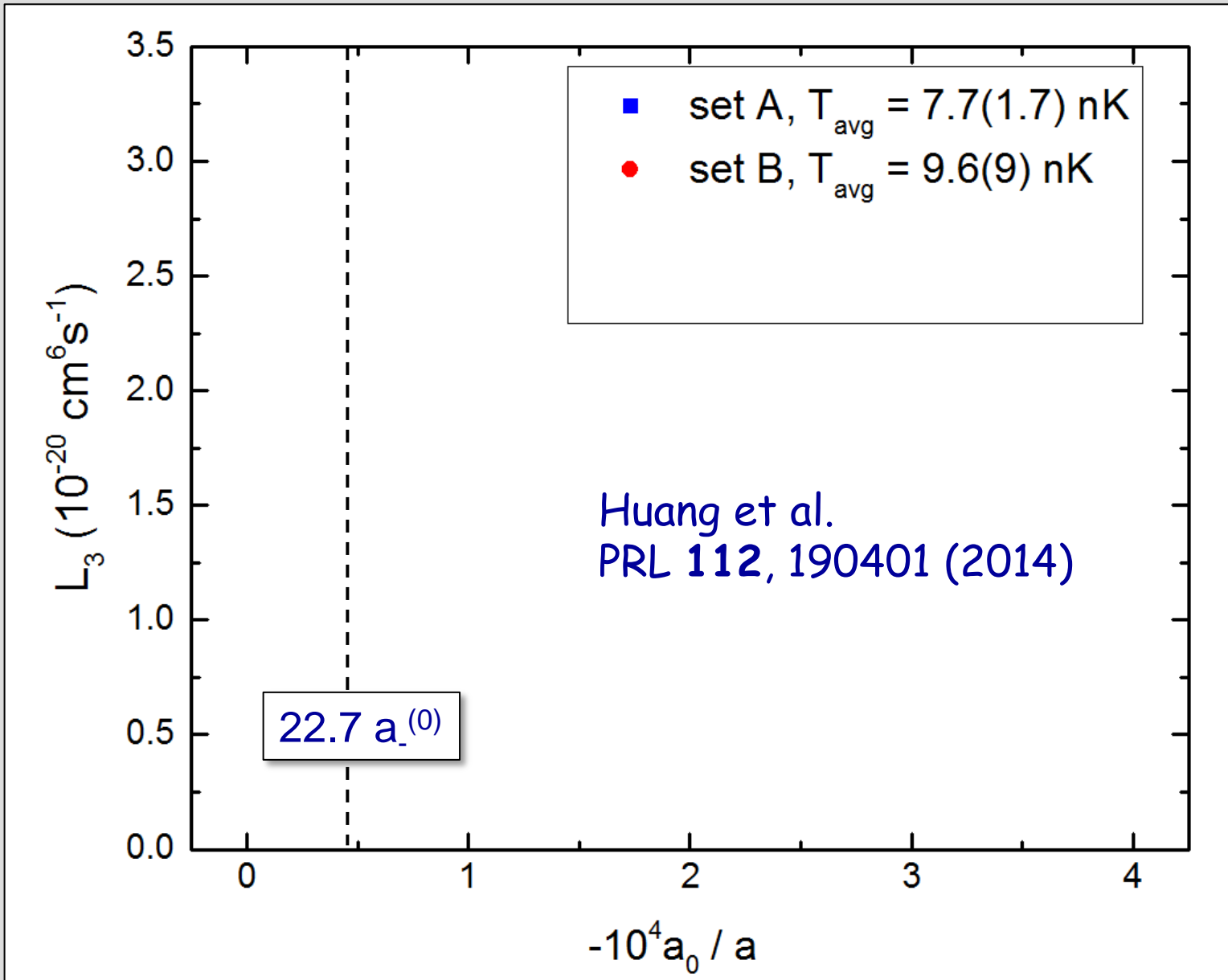
amazing 800-G Feshbach resonance

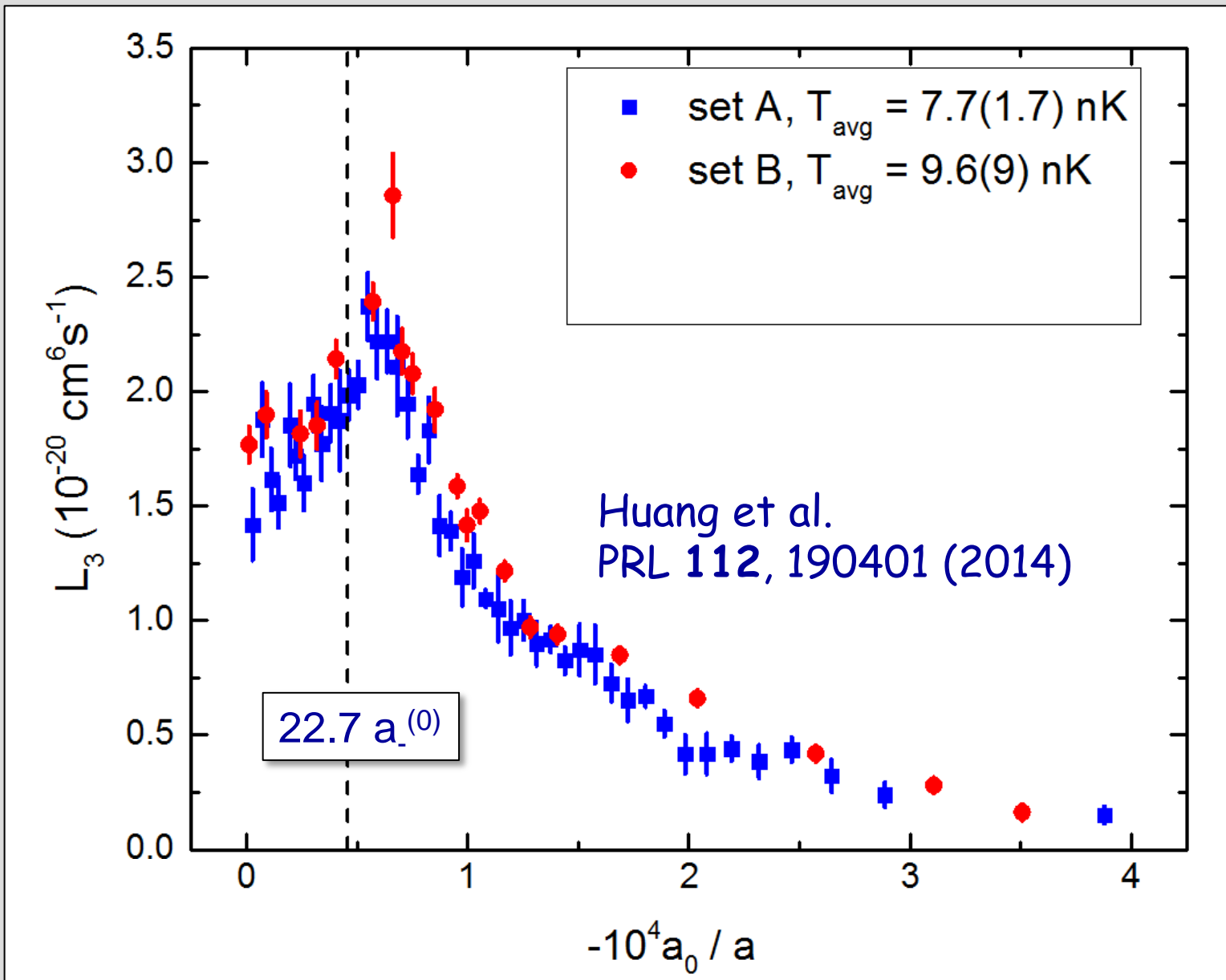
$$s_{\text{res}} \approx 15,000$$

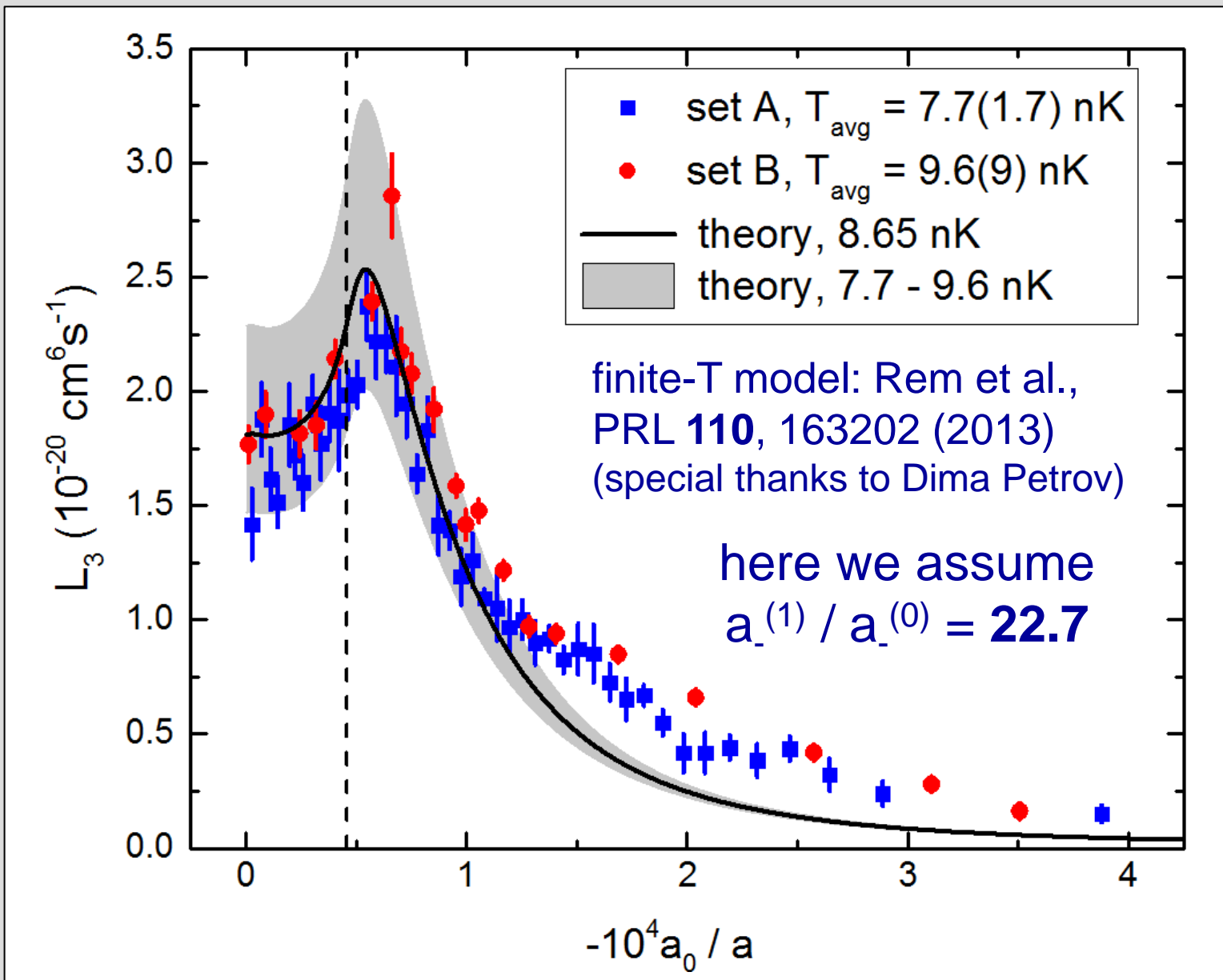


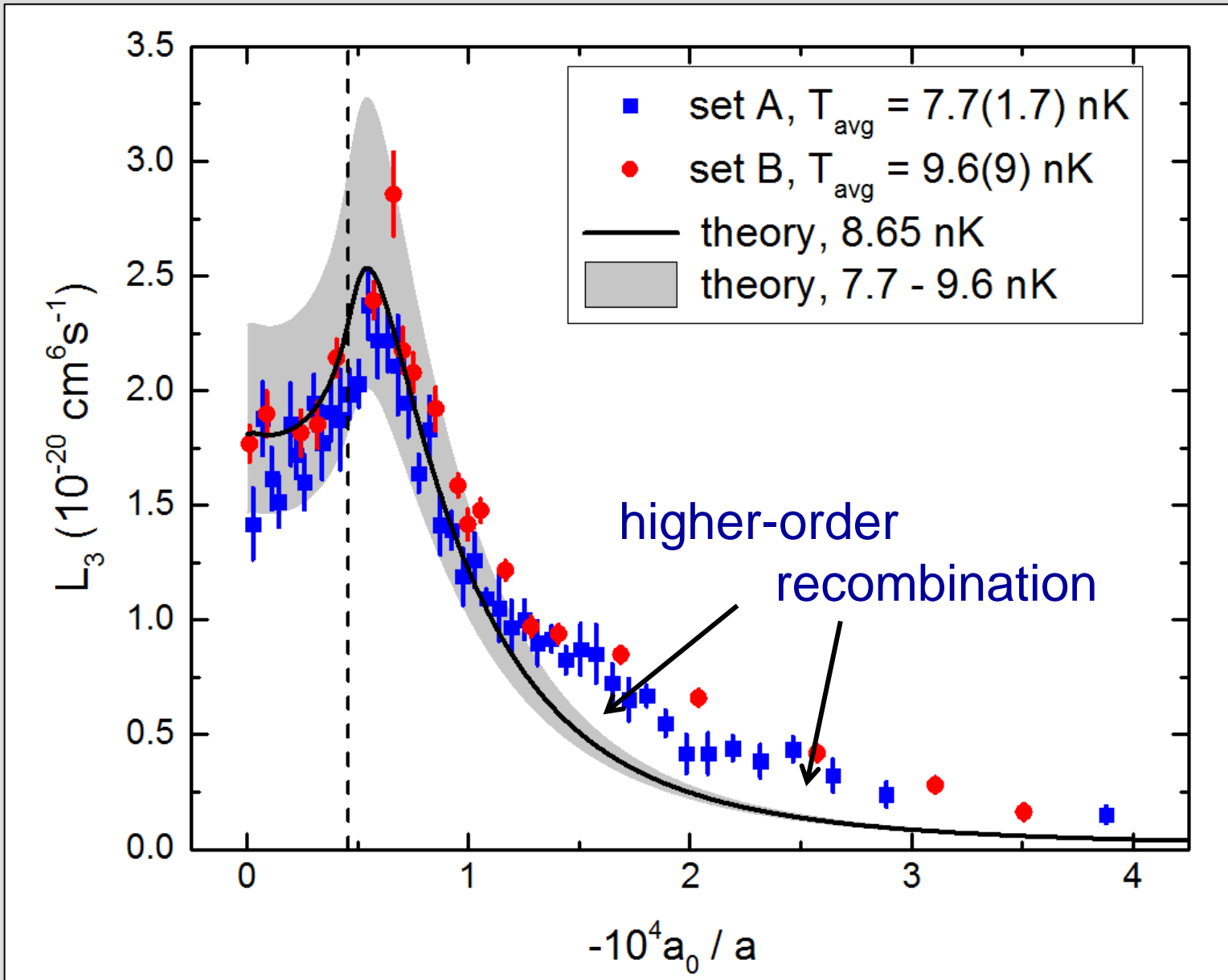
accurate control of a on the few **10,000 a_0** level !

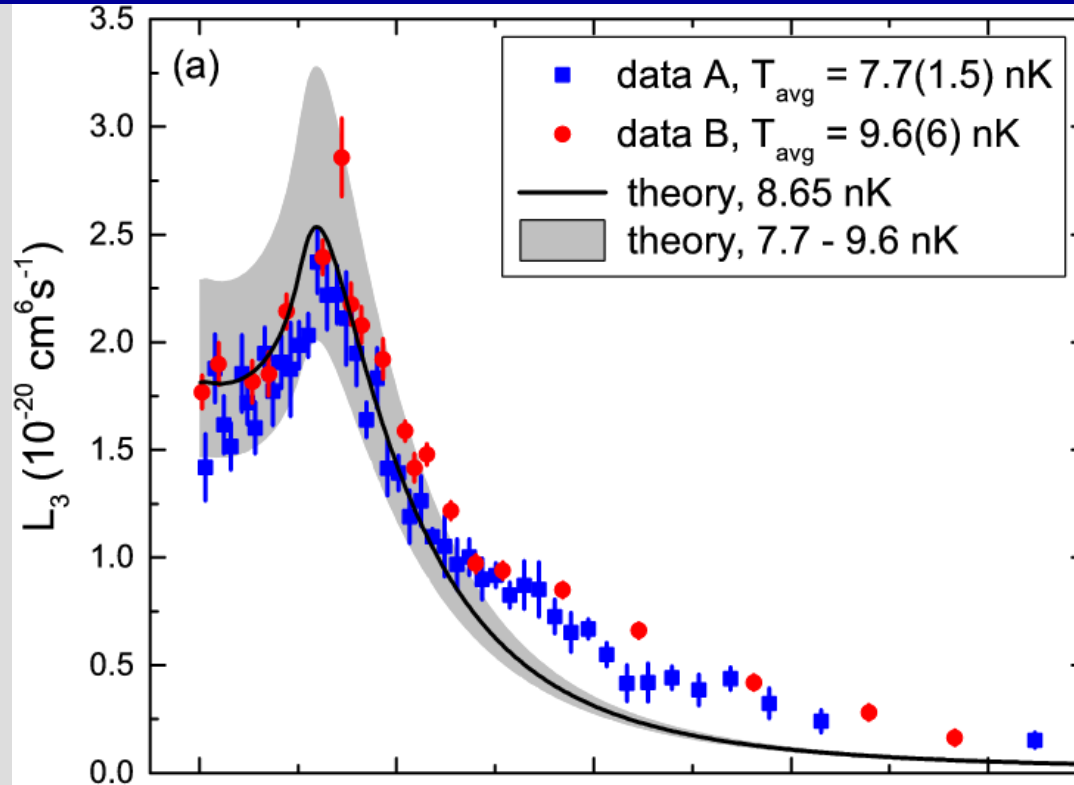
uncertainty of pole ± 0.3 G corresponds to $\pm 500,000 a_0$





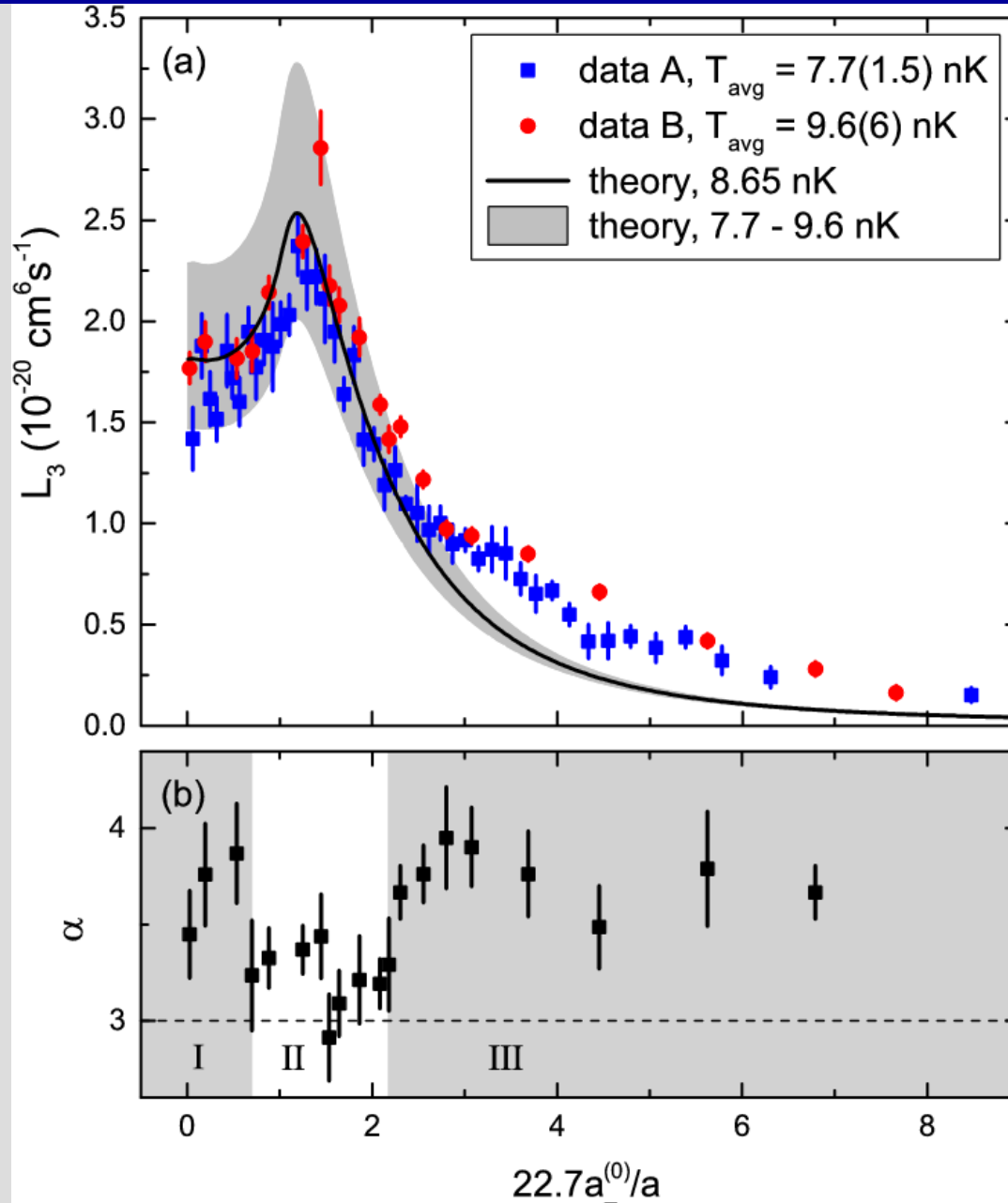




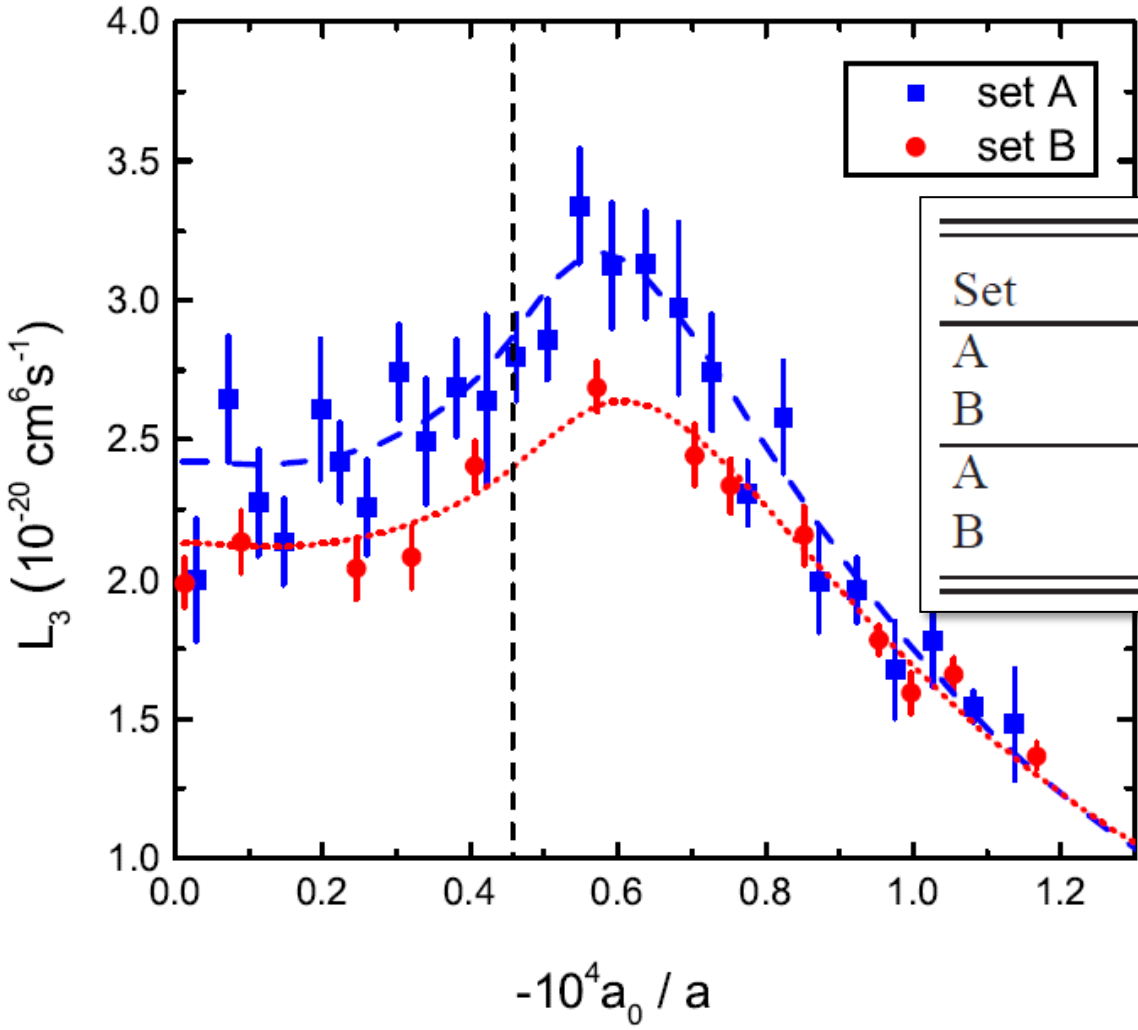


$$\dot{n} = -L_{\alpha} n^{\alpha}$$

α -body loss



let's get more accurate - let's fit



Set	T/nK	$a_{-}^{(1)}/a_0$
A	8.7(2)	-20790(390)
B	10.0(2)	-19740(430)
A	7.7*	-20580(390)
B	9.6*	-19650(430)

2nd Efimov resonance: $a_{-}^{(1)} = -20190(1200) a_0$

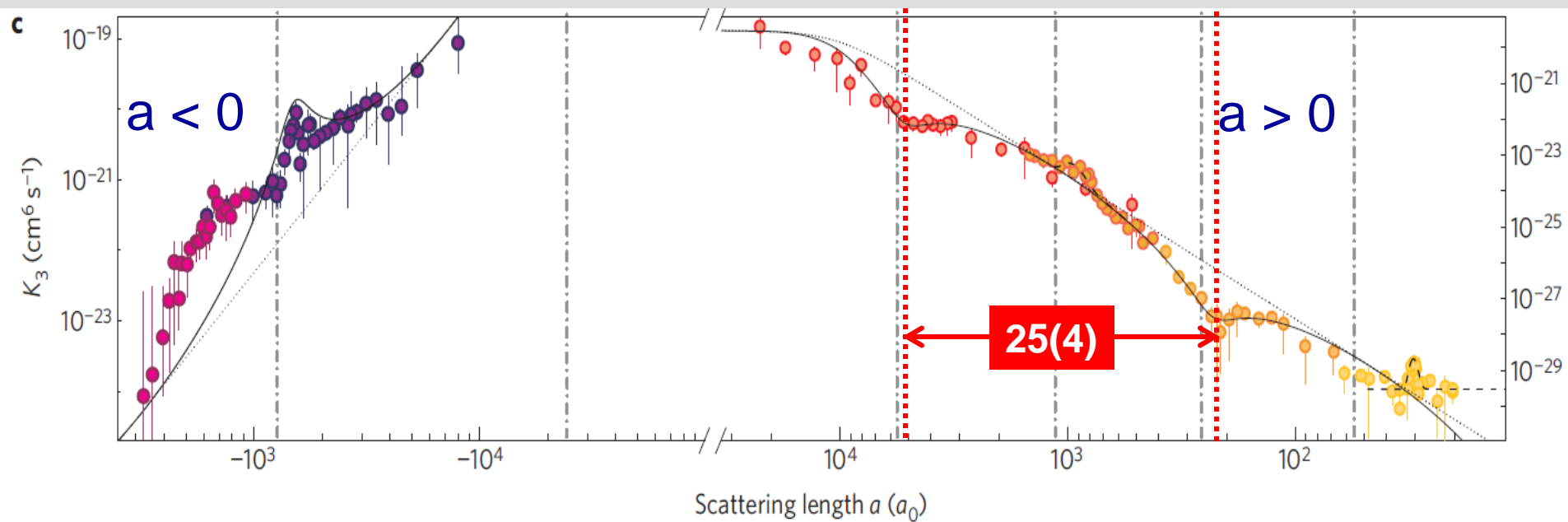
1st Efimov resonance: $a_{-}^{(0)} = -933(16) a_0$

21.0(1.3)

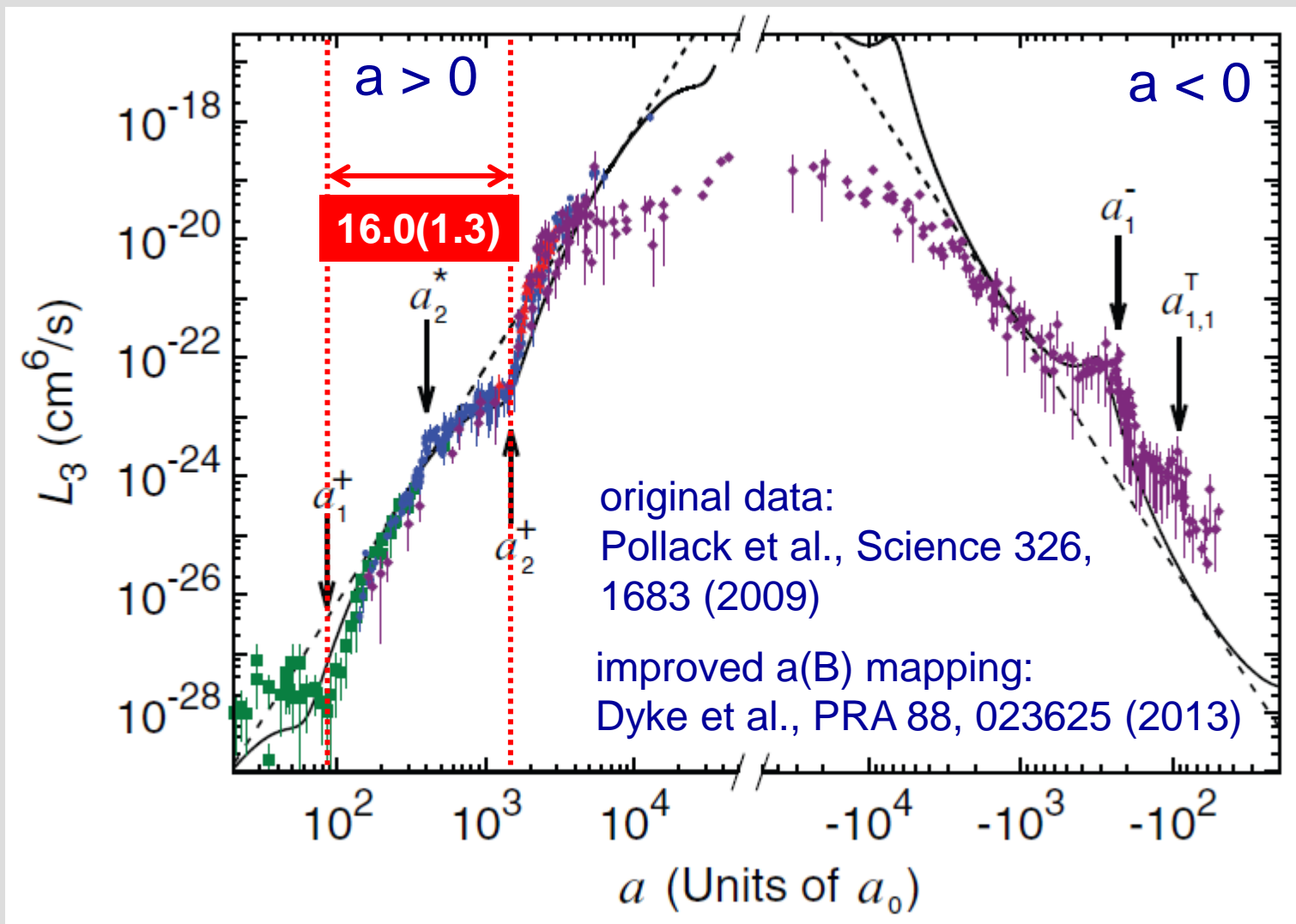
1.2 σ away from 22.7

universal vdW theory (Wang, Julienne) predicts
20.5 ... 21.5 for our particular case

observables:
recombination minima



Zaccanti et al., Nature Phys. **5**, 586 (2009)



experiments on ^{39}K , ^7Li

lowest reference points
(minima) at $\sim 3 R_{\text{vdW}}$

phenomena at $a > 0$ generally
sensitive to non-universal
corrections (weakly bound mol. state)

Feshbach resonances of
intermediate character

^{133}Cs

1st triatomic resonance
at $-9.5 R_{\text{vdW}}$

$a < 0$: situation
quite robust

extremely broad
Feshbach resonances
available

*much closer to ideal
conditions*

second Efimov
peak
(Glungezer)

first Efimov
peak
(Patscherkofel)

Леонид
Сидоренков

黄博

the team & our collaborators

ultracold.atoms



Paul
Julienne



Jeremy
Hutson

Javier von Stecher
Chris Greene
José D'Incao

Francesca
Ferlaino



Hanns-
Christoph
Nägerl

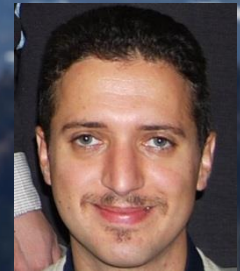


Леонид
Сидоренков

黄博



Martin
Berninger



Alessandro
Zenesini

Steven Knoop
Walter Harm
Harald Schöbel

Few-body physics with ultracold atoms

is this (only) the physics of losses?

Few-body physics with ultracold atoms

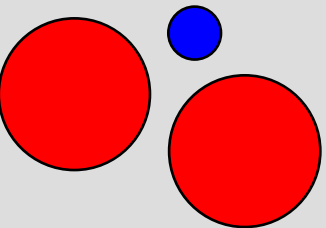
is this (only) the physics of losses?

no !

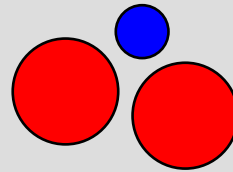
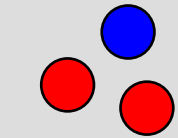
Jag et al., PRL **112**, 075302 (2014)

J. Phys. B: At. Mol. Opt.
Phys. 40, 1429 (2007)

**Kartavtsev-Malykh
trimer**



Efimov states



1

6.7

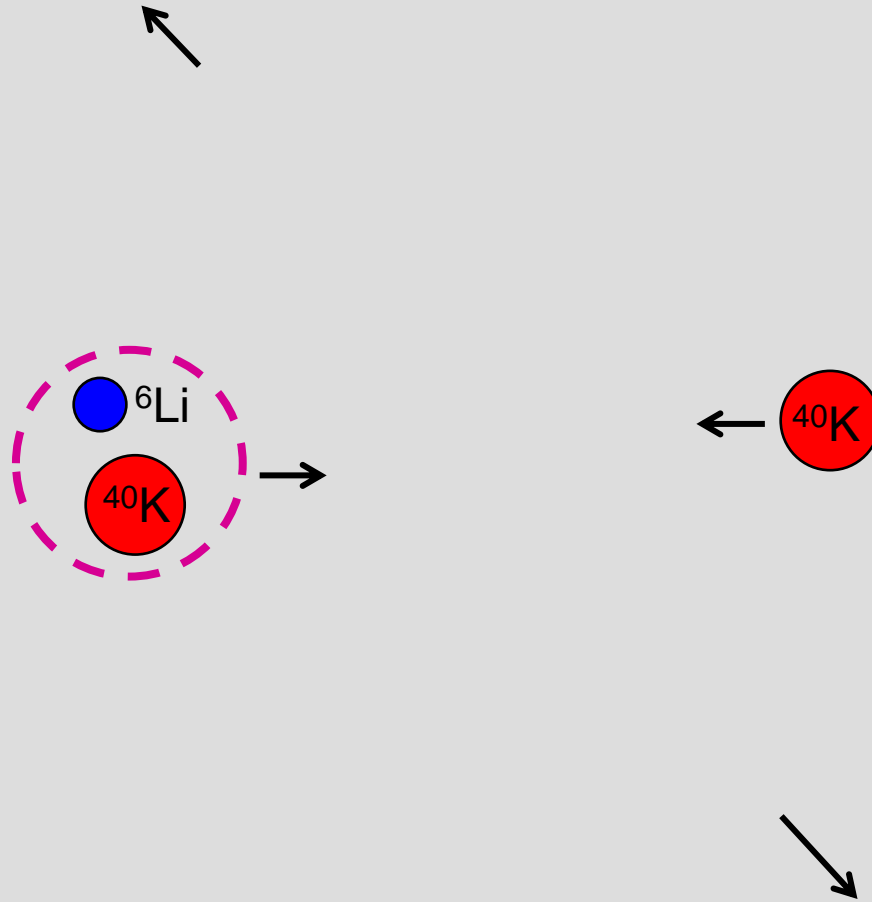
8.2

13.6

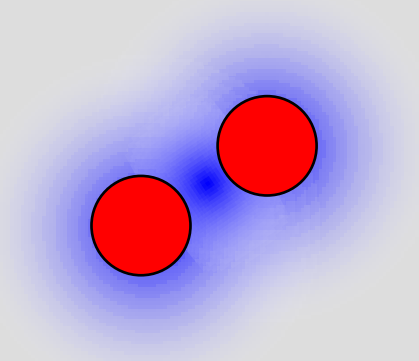
M/m



we are here !
 $^{40}\text{K} - ^6\text{Li}$



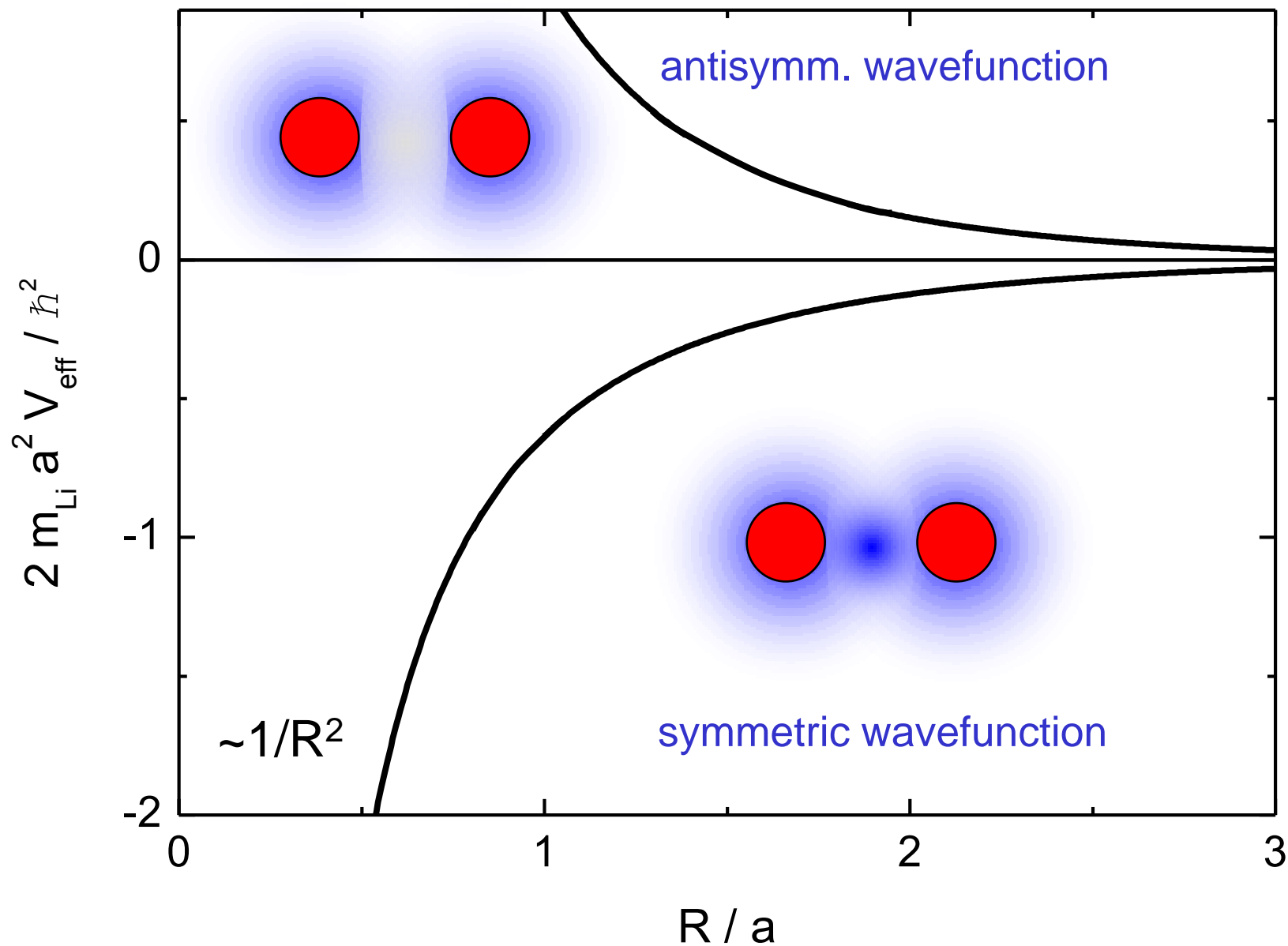


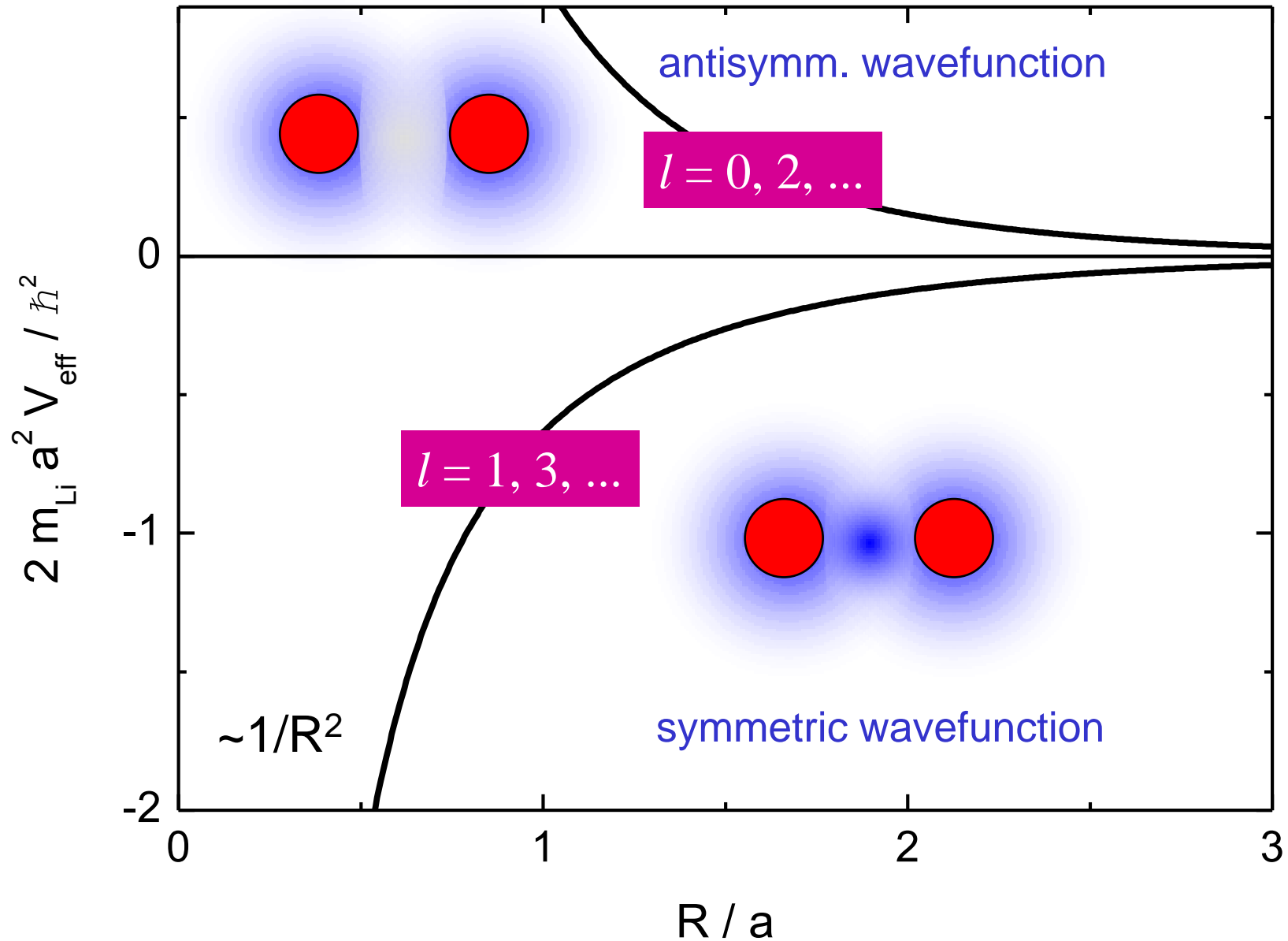


Levinsen, Tiecke, Walraven, Petrov, PRL **103**, 153202 (2009)

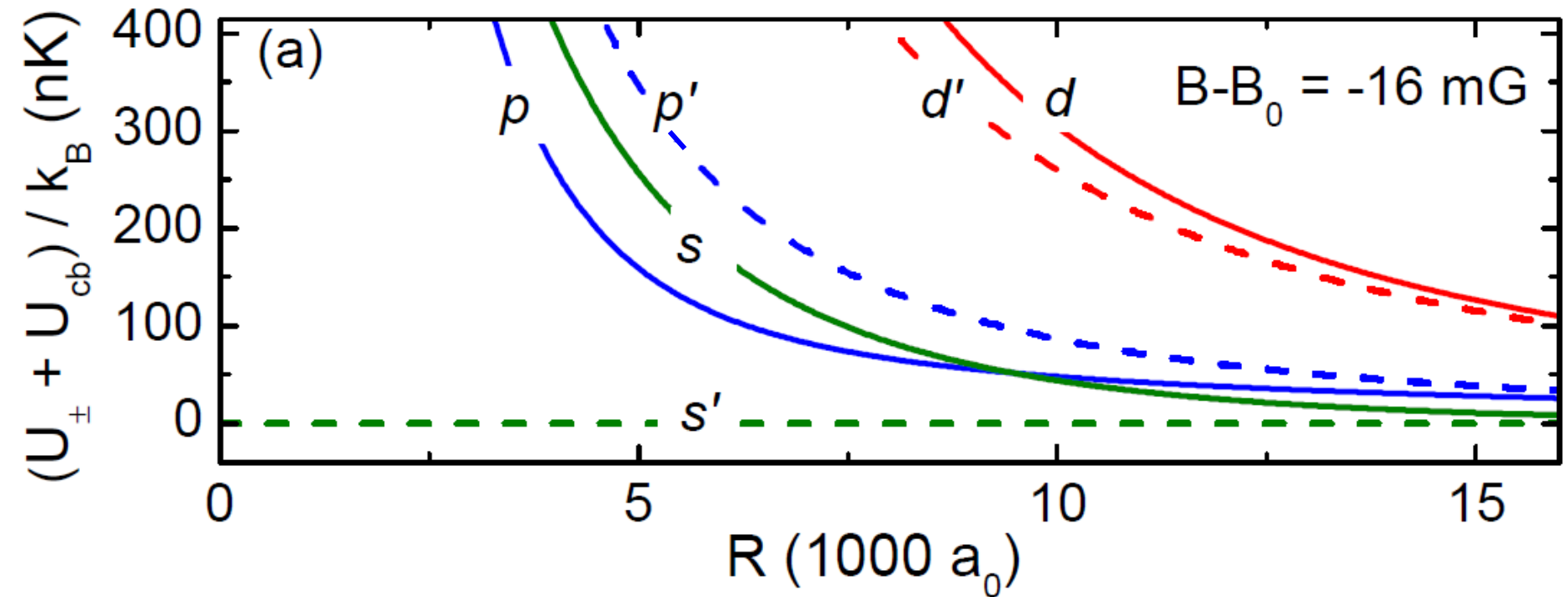
Levinsen, Petrov, EPJD **65**, 67 (2011)

see also Alzetta, Combescot, Leyronas, PRA **86**, 062708 (2012)



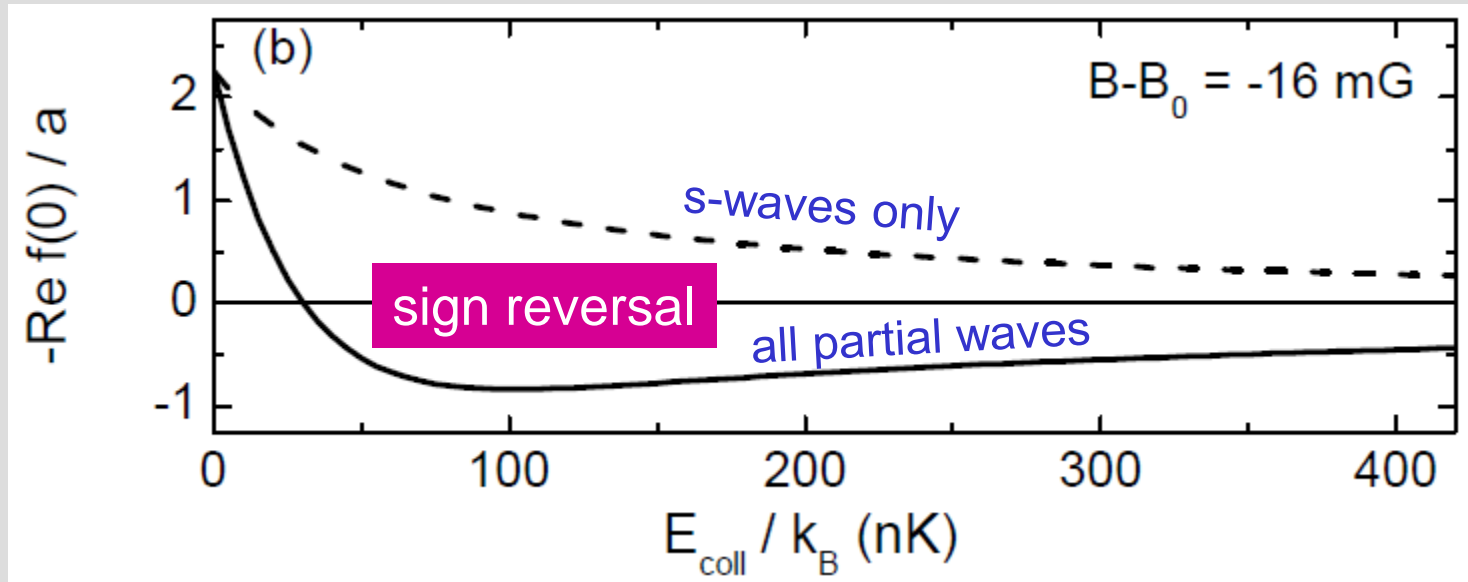


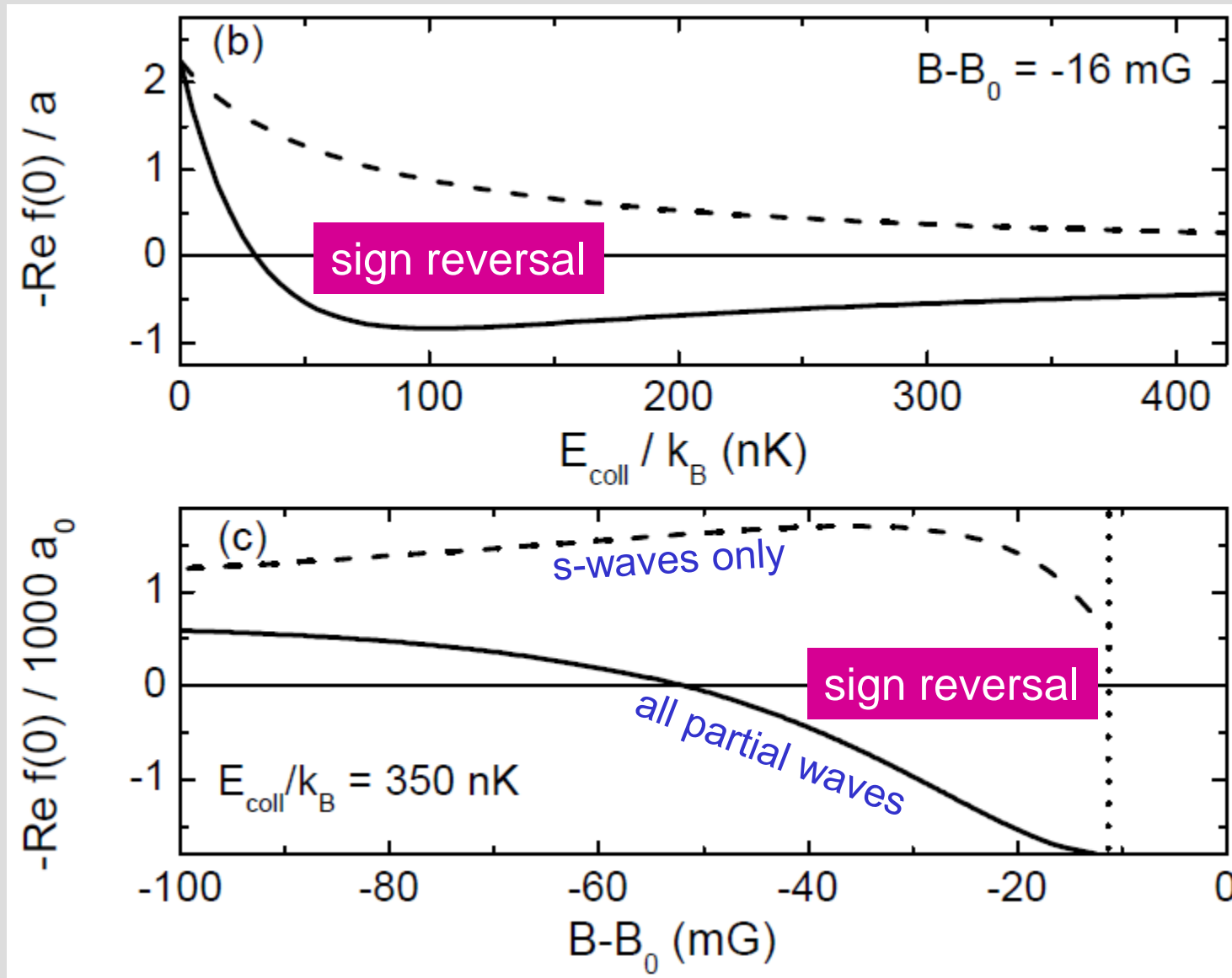
for 155G Li-K Feshbach resonance (880mG wide)



strong effect on p -wave barrier

strong atom-dimer attraction!







Univ.
Aarhus,
DK



Jesper
Levinsen



Dima
Petrov

LPTMS,
Orsay,
France



Rianne
Lous

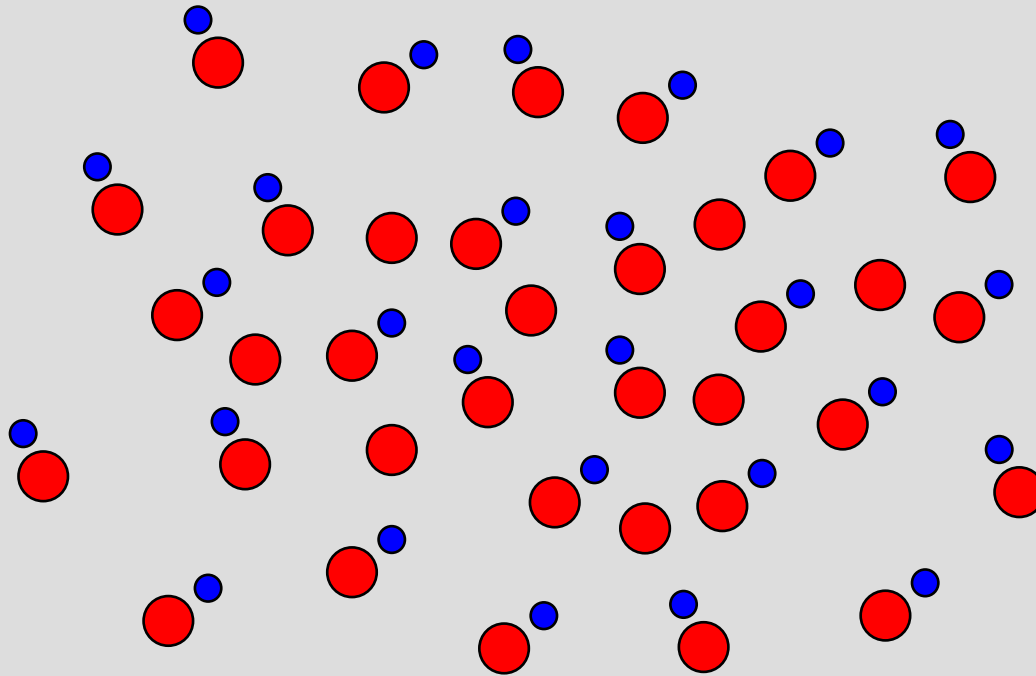
Michael
Jag

Florian
Schreck

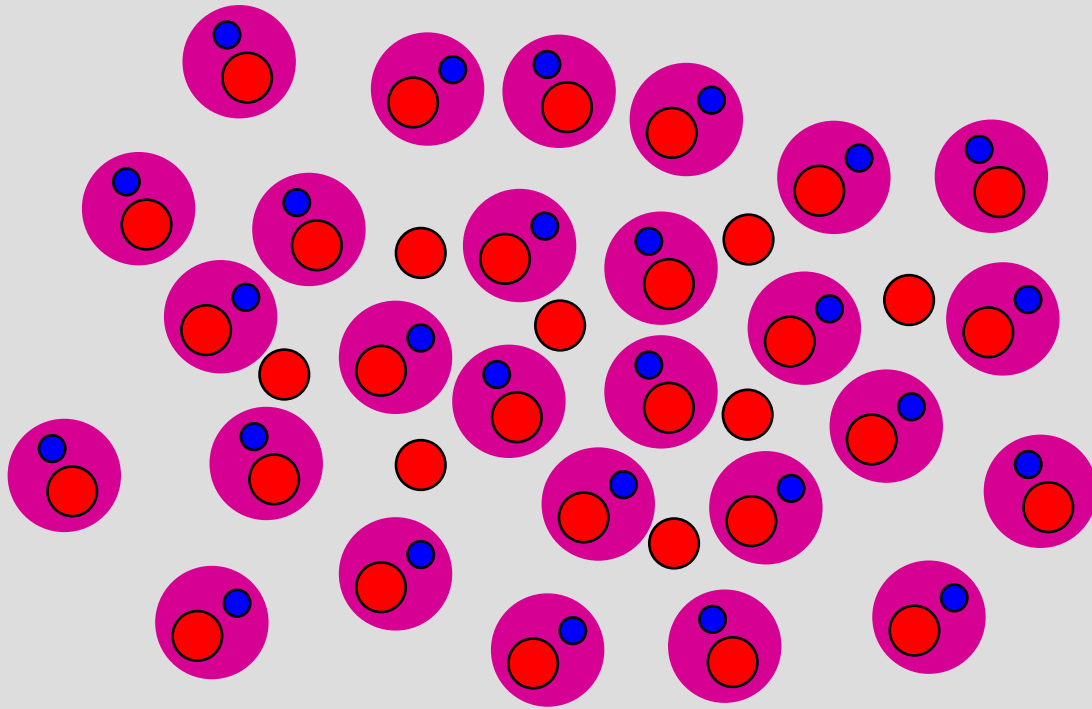
Matteo
Zaccanti
(LENS)


Marko
Cetina

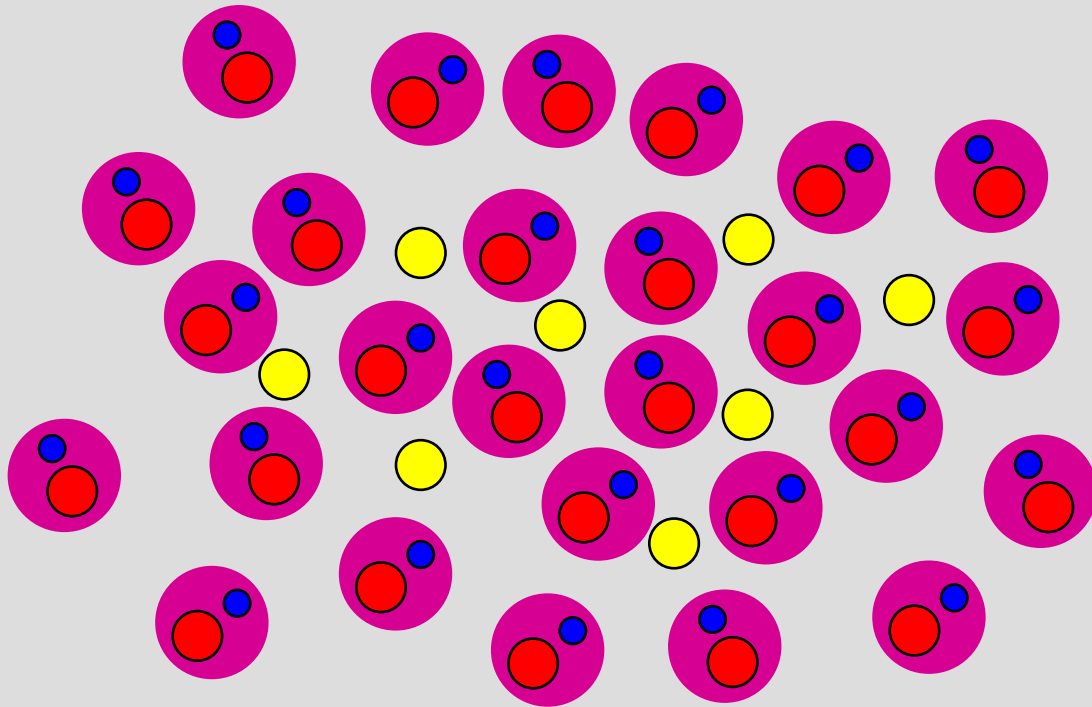
Rudi
Grimm





making weakly bound dimers ($a > 0$)

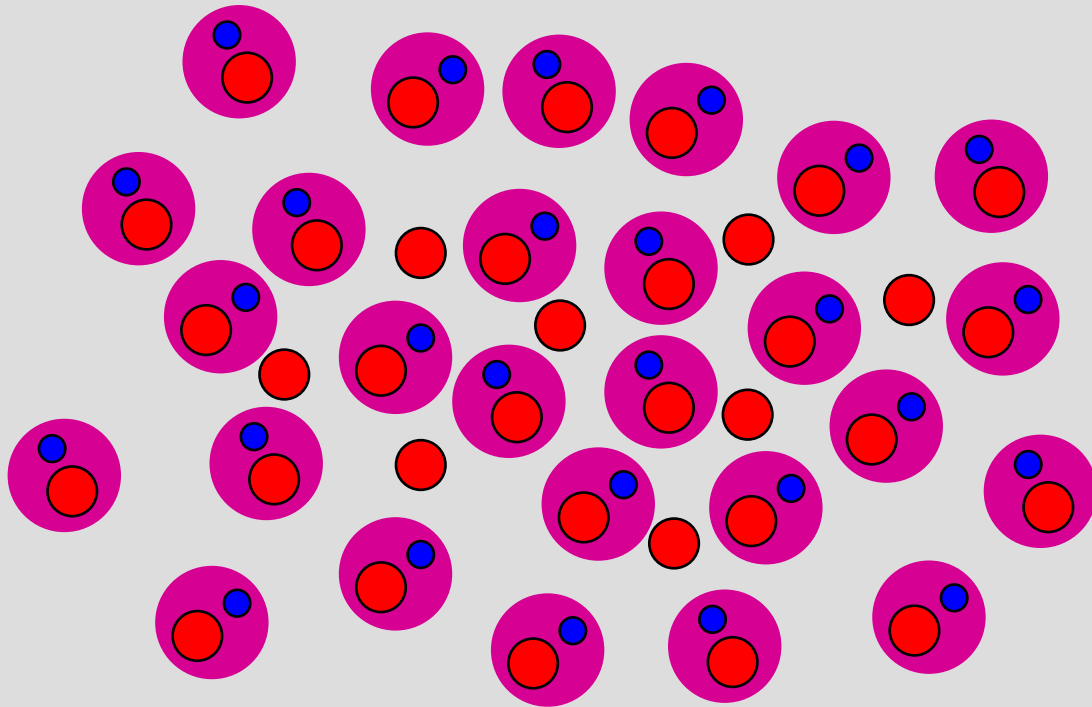


^{40}K  interacting spin state } *rf* coupling
 non-interacting spin state




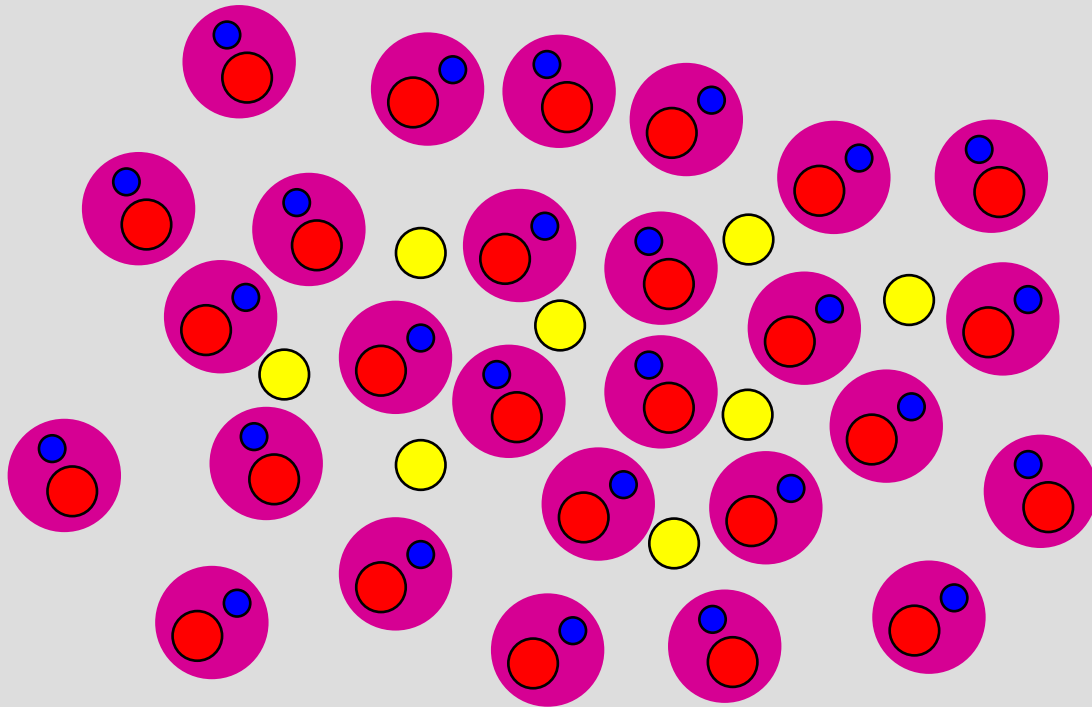
flipping the spin state of the free atoms

^{40}K  interacting spin state } *rf* coupling
 non-interacting spin state



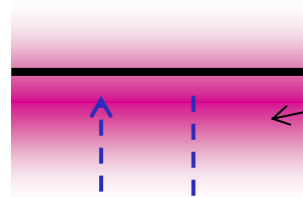
flipping the spin state of the free atoms

^{40}K  interacting spin state } *rf* coupling
 non-interacting spin state }



interacting
spin state

^{40}K

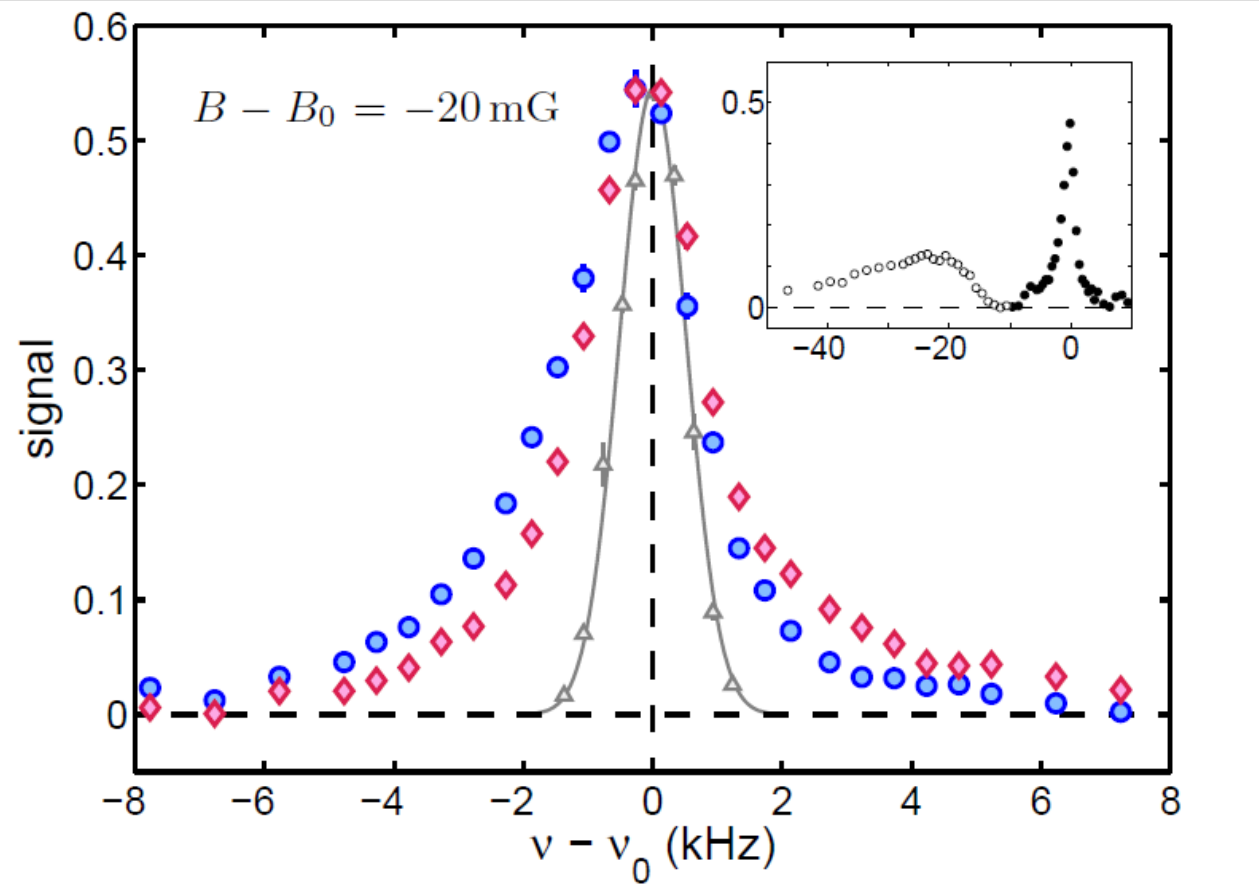


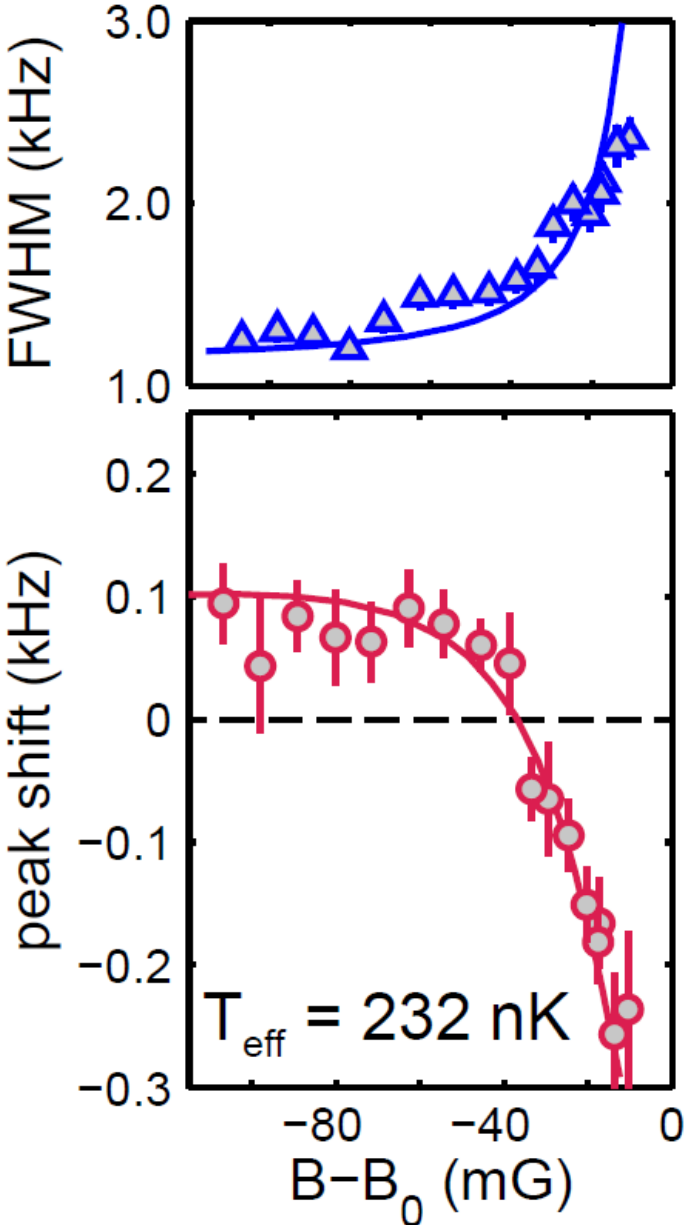
interaction with
 $^6\text{Li}^{40}\text{K}$ dimers

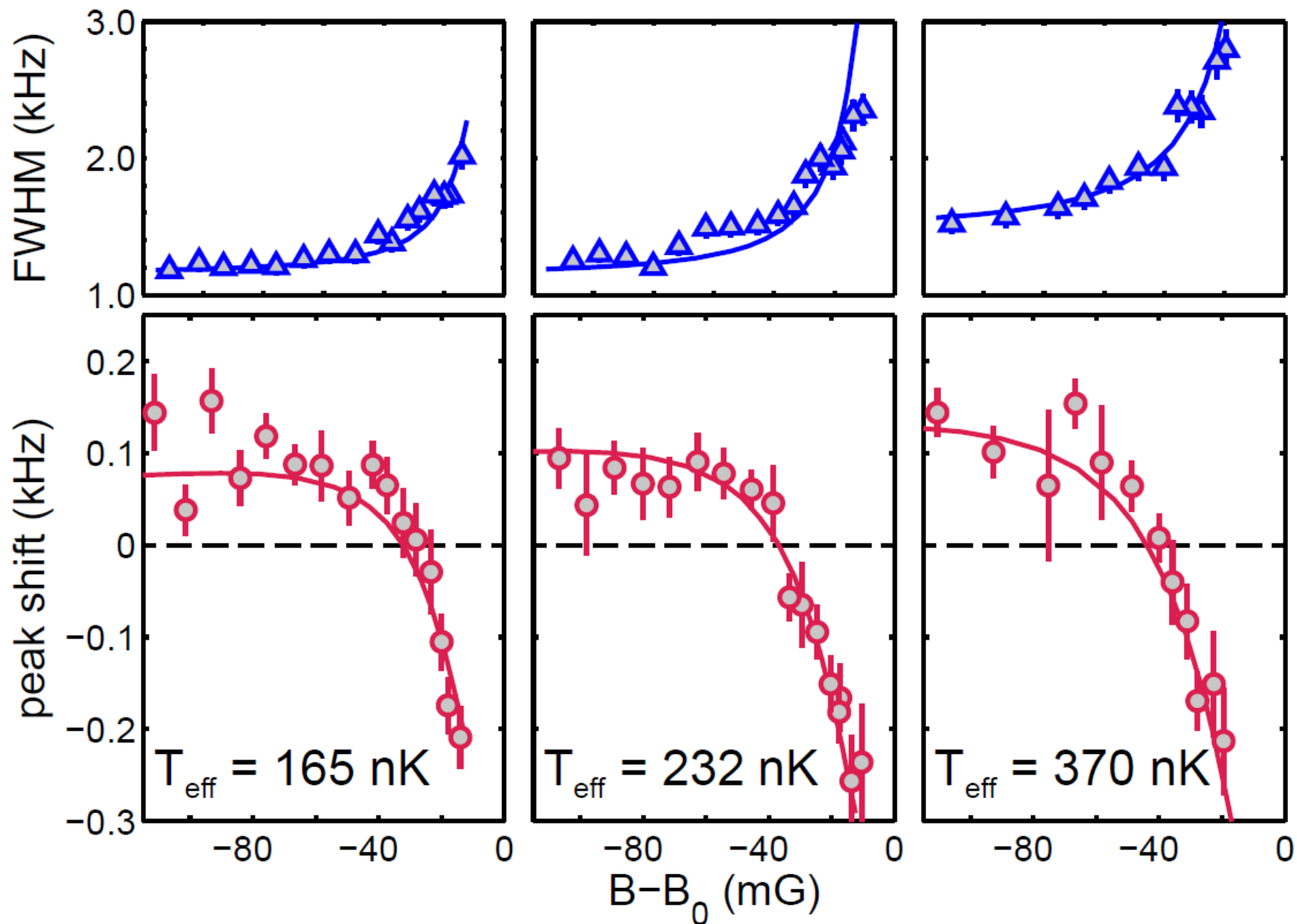
non-interacting
spin state



**excellent tool to
probe interaction
shifts !!!**

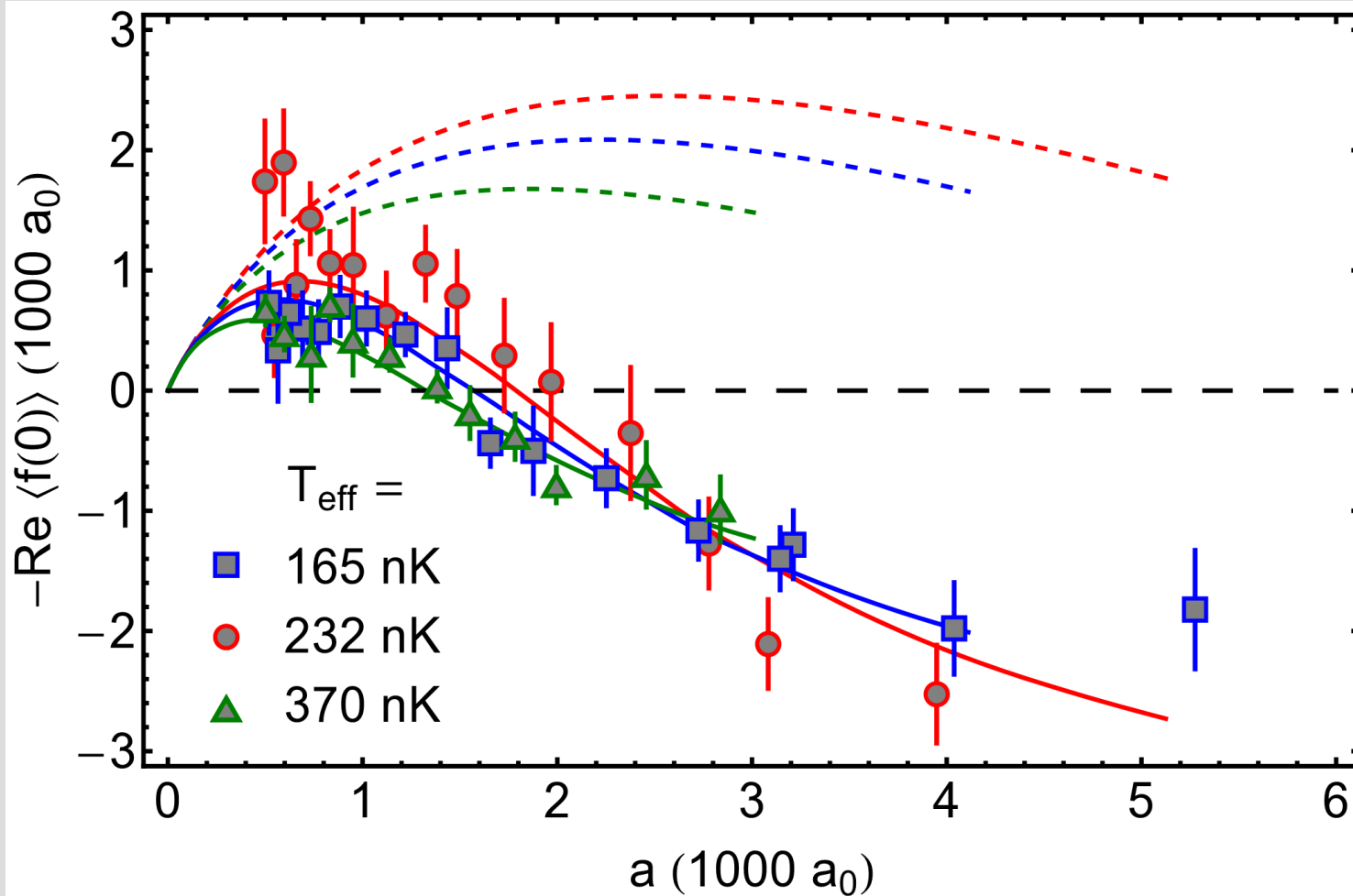






$$\delta\nu = \hbar \bar{n}_D a_{\text{eff}} / \mu_3$$

shift in terms of eff. sc. length



why we are so excited!

ultracold.atoms

mass imbalance: qualitatively new interaction properties

no-loss few-body effect

ultracold paradigm shift:
physics beyond s-waves

potentially
strong impact on
many-body physics !!!



Periodic Table of the Elements

1	IA	1	H	I	IIA	2	He	O																													
2		3	Li	4	Be	5	B	6	C	7	N	8	O	9	F	10	Ne																				
3		11	Na	12	Mg	13	Al	14	Si	15	P	16	S	17	Cl	18	Ar																				
4		19	K	20	Ca	21	Sc	22	Ti	23	V	24	Cr	25	Mn	26	Fe	27	Co	28	Ni	29	Cu	30	Zn	31	Ga	32	Ge	33	As	34	Se	35	Br	36	Kr
5		37	Rb	38	Sr	39	Y	40	Zr	41	Nb	42	Mo	43	Tc	44	Ru	45	Rh	46	Pd	47	Ag	48	Cd	49	In	50	Sn	51	Sb	52	Te	53	I	54	Xe
6		55	Cs	56	Ba	57	*La	72	Hf	73	Ta	74	W	75	Re	76	Os	77	Ir	78	Pt	79	Au	80	Hg	81	Tl	82	Pb	83	Bi	84	Po	85	At	86	Rn
7		87	Fr	88	Ra	89	+Ac	104	Rf	105	Ha	106	Sg	107	Ns	108	Hs	109	Mt	110	Ds	111	112	113													

new project
in Innsbruck
Dy-K mixtures

alkali-lanthanoid mixtures

* Lanthanide Series

+ Actinide Series

58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
90	91	92	93	94	95	96	97	98	99	100	101	102	103
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

thank you for your
attention

FWF

Der Wissenschaftsfonds.



Foundations and
Applications of
Quantum Science