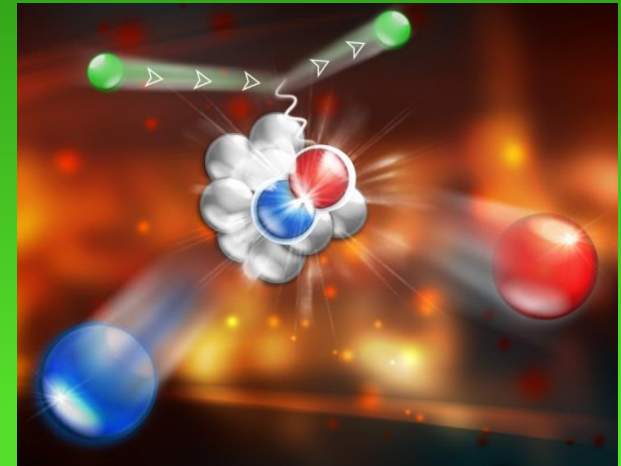
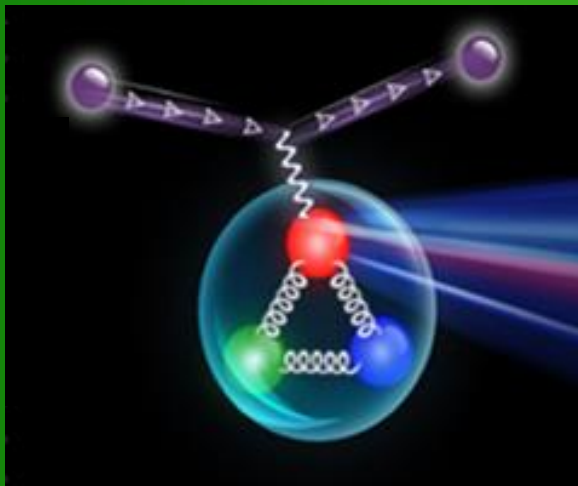


Unlocking what underlies the common nuclear dependence of EMC effect and Short Range Correlations



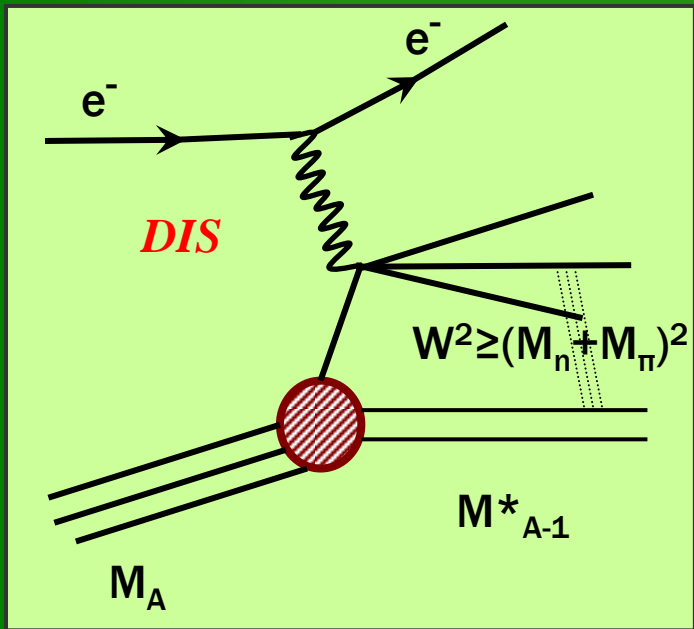
Nadia Fomin

Los Alamos National Laboratory

INT workshop on nuclear structure and dynamics

February 11th, 2013

The inclusive reaction

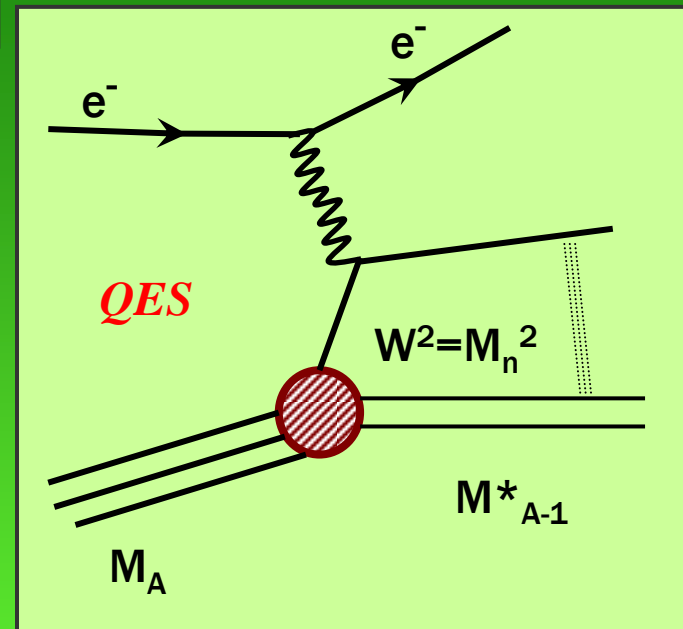


Same initial state
Different Q^2 behavior

$$\nu = E - E'$$

$$Q^2 = -q^2 = \vec{q}^2 - \nu^2$$

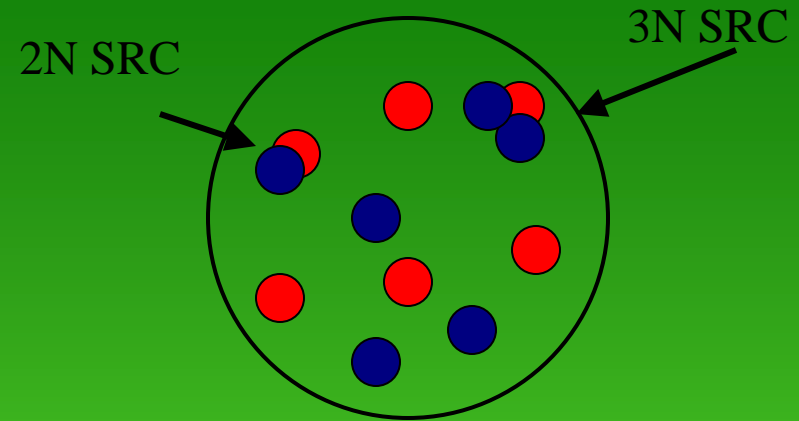
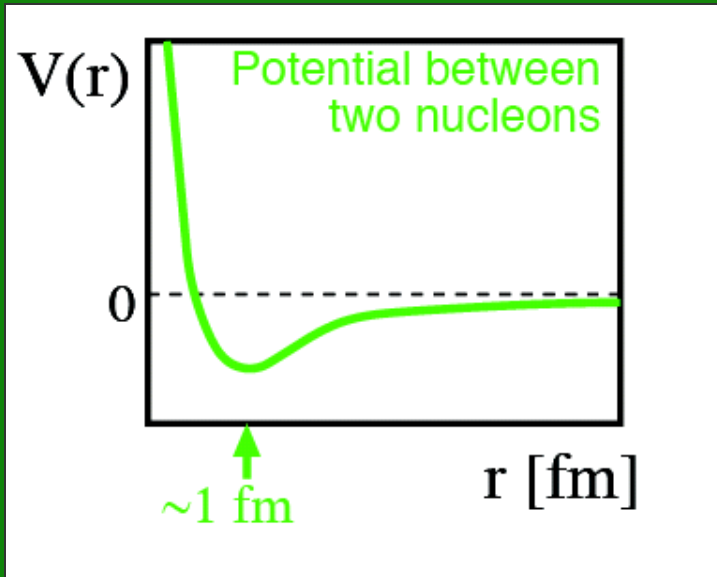
$$W^2 = 2M\nu + M^2 - Q^2$$

$$x = \frac{Q^2}{2M\nu}$$


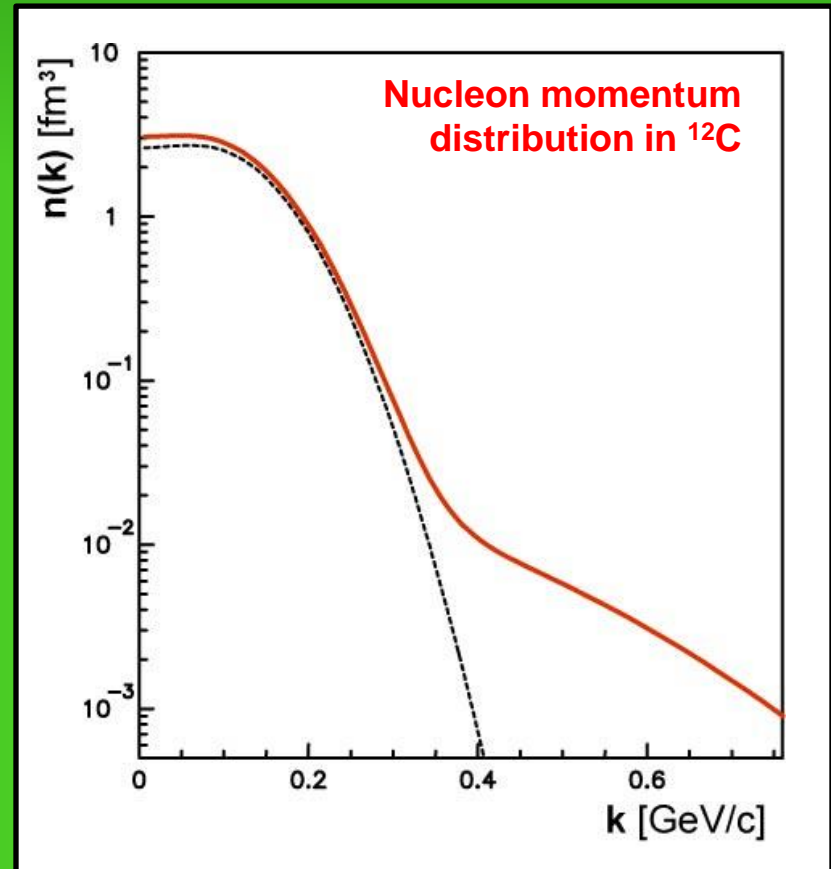
$$\frac{d\sigma}{d\Omega dE} \propto \int d\vec{k} \int dE W_{1,2}^{p,n} S(k, E)$$

$$\frac{d\sigma}{d\Omega dE} \propto \int d\vec{k} \int dE \sigma_{eN} S(k, E) \delta()$$

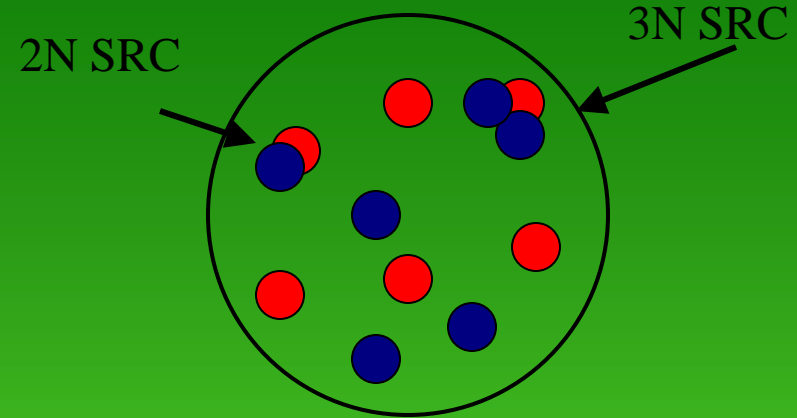
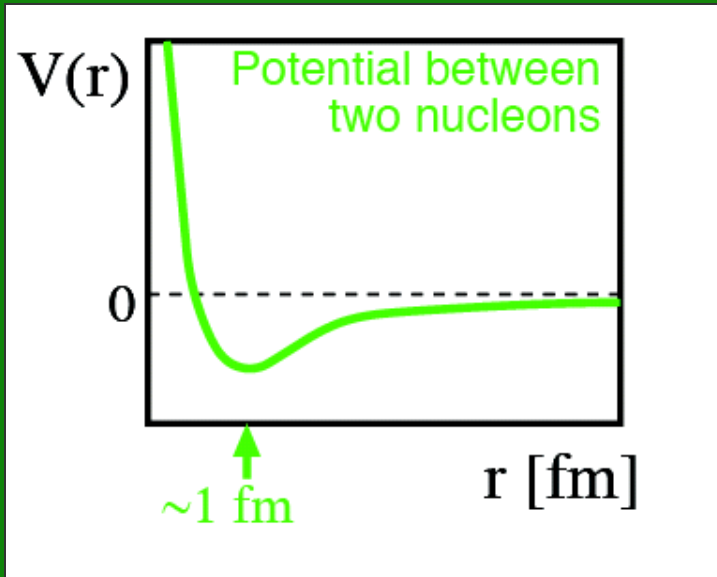
High momentum nucleons - Short Range Correlations



Cannot extract momentum distributions directly from inclusive data for $A > 2$



High momentum nucleons - Short Range Correlations

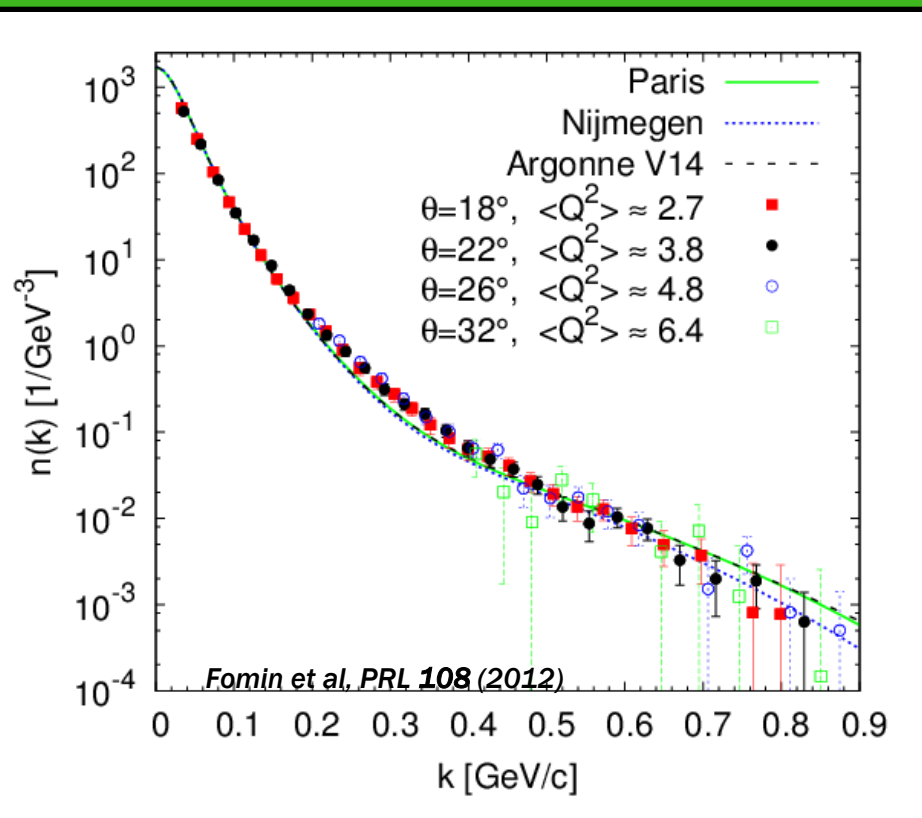


$$\frac{d\sigma^{QE}}{d\Omega dE'} \propto \int d\vec{k} \int dE \sigma_{ei} S_i(k, E) \delta(\text{Arg})$$

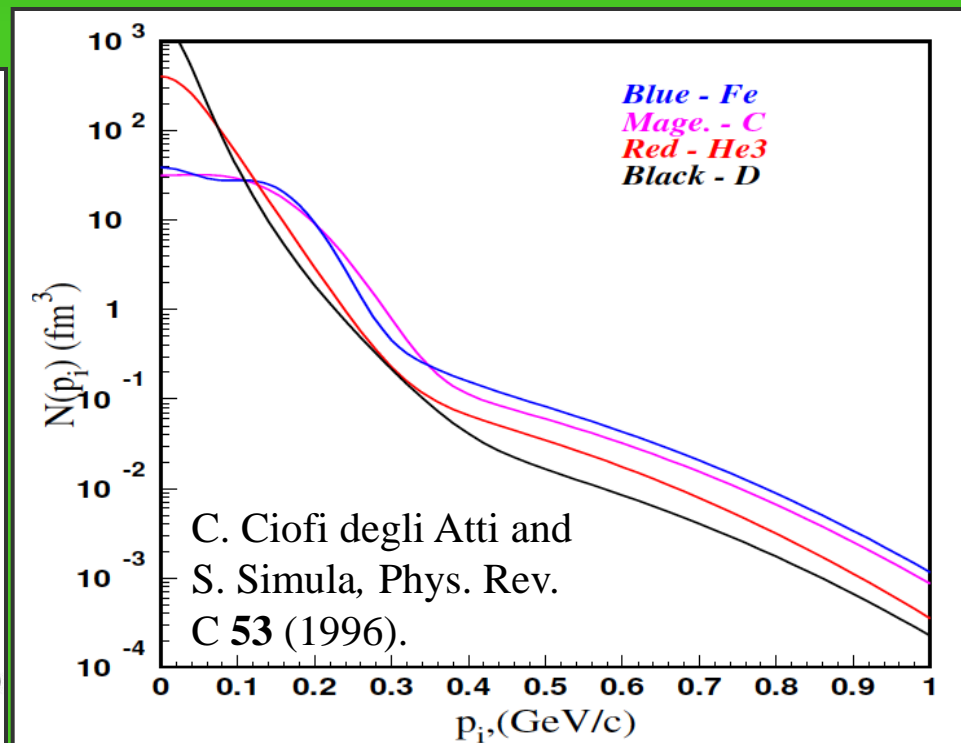
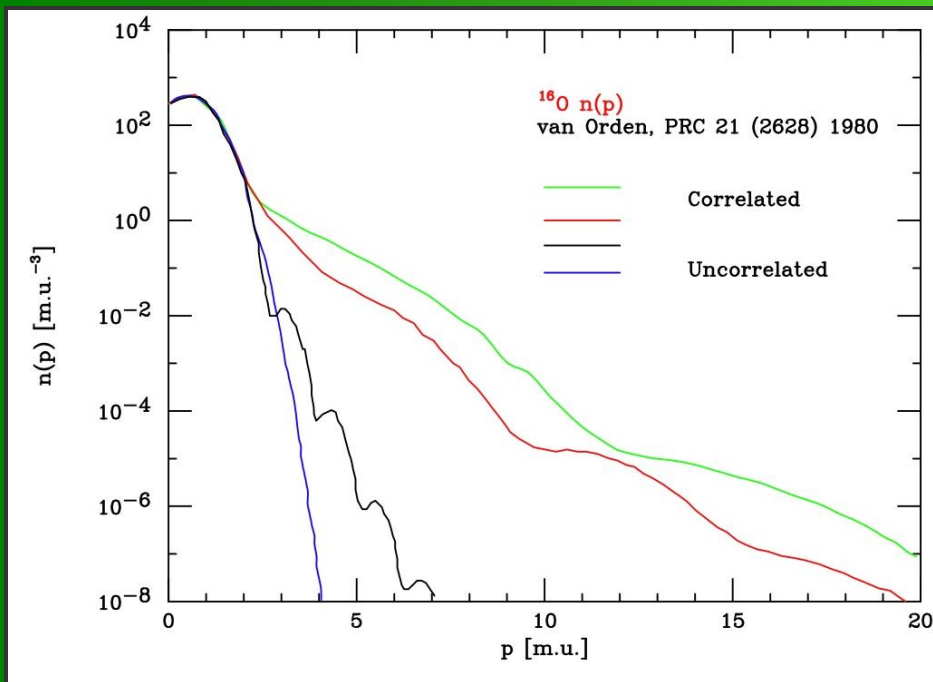
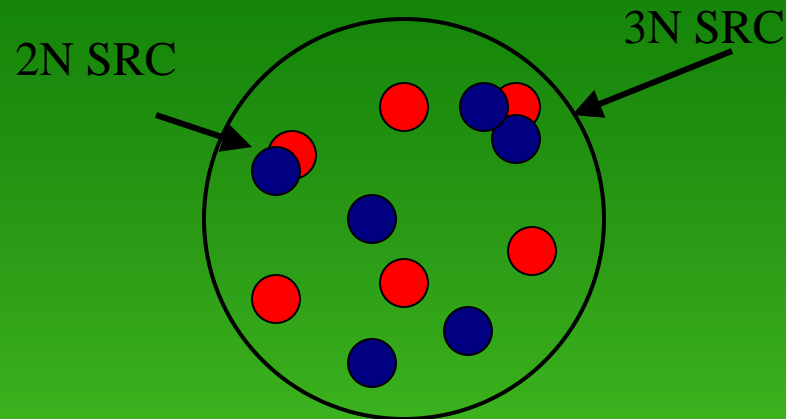
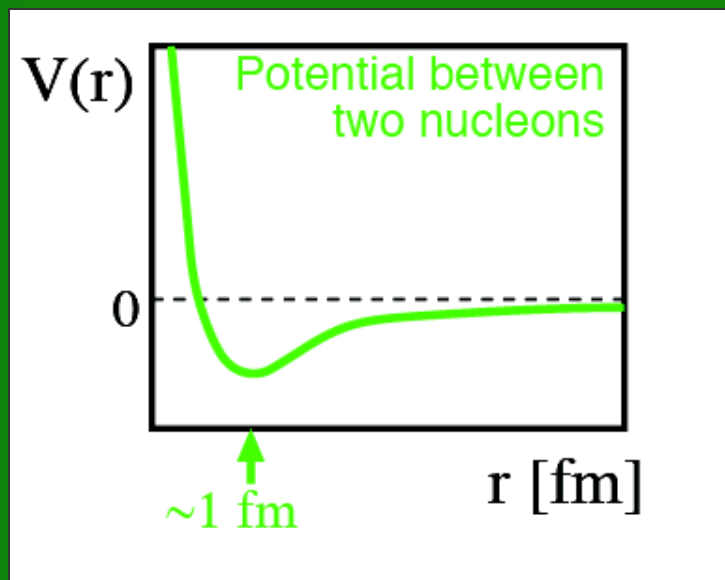
$$\text{Arg} = \nu + M_A - \sqrt{M^2 + p^2} - \sqrt{M_{A-1}^{*2} + k^2}$$

$$F(y, \mathbf{q}) = \frac{d^2\sigma}{d\Omega d\nu} \frac{1}{(Z\bar{\sigma}_p + N\bar{\sigma}_n)} \frac{\mathbf{q}}{\sqrt{M^2 + (y+q)^2}}$$

$$= 2\pi \int_{|y|}^{\infty} n(k) k dk \quad \text{Ok for A=2}$$



High momentum nucleons - Short Range Correlations



Short Range Correlations

- To experimentally probe SRCs, must be in the high-momentum region ($x > 1$)

• To measure the relative probability of finding a correlation, ratios of heavy to light nuclei are taken

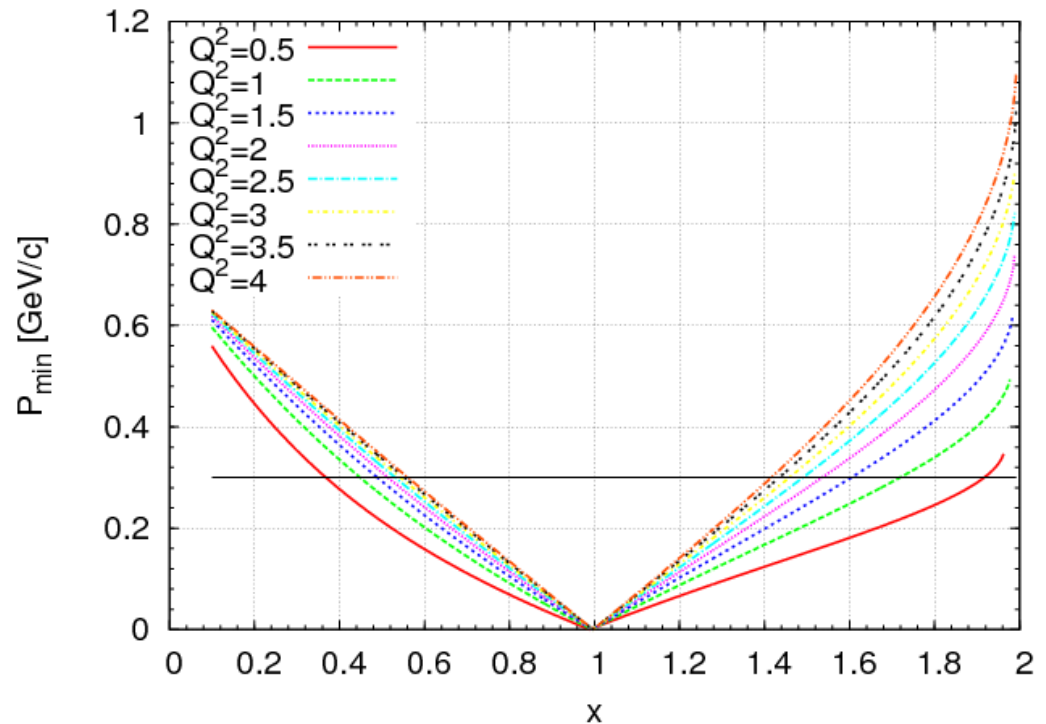
• In the high momentum region, FSIs are thought to be confined to the SRCs and therefore, cancel in the cross section ratios

$1.4 < x < 2 \Rightarrow$ 2 nucleon correlation

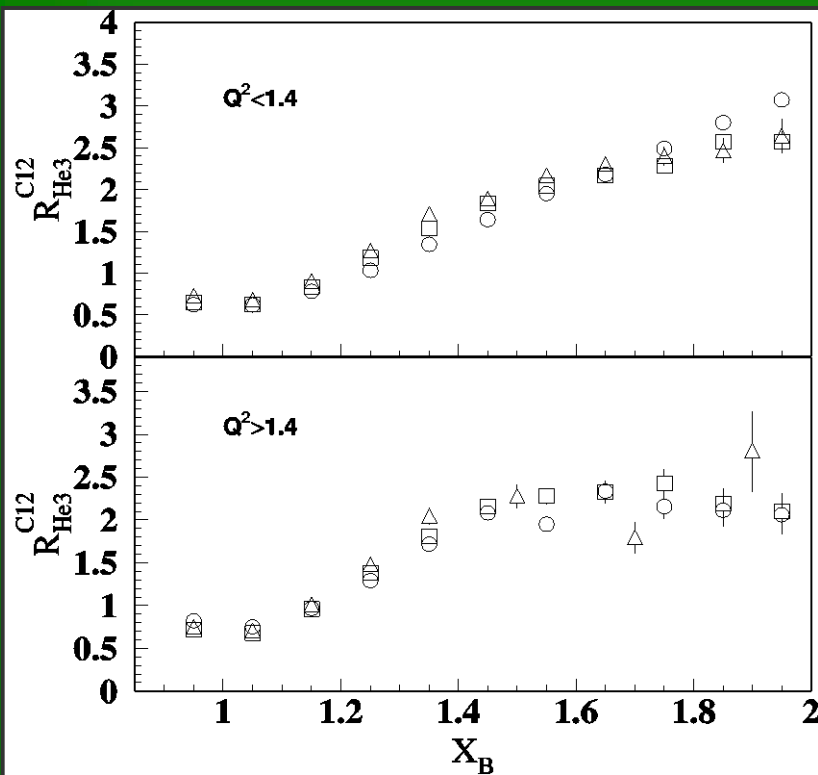
$2.4 < x < 3 \Rightarrow$ 3 nucleon correlation

- L. L. Frankfurt and M. I. Strikman, *Phys. Rept.* 76, 215(1981).
- J. Arrington, D. Higinbotham, G. Rosner, and M. Sargsian (2011), *arXiv:1104.1196*
- L. L. Frankfurt, M. I. Strikman, D. B. Day, and M. Sargsian, *Phys. Rev. C* 48, 2451 (1993).
- L. L. Frankfurt and M. I. Strikman, *Phys. Rept.* 160, 235 (1988).
- C. C. degli Atti and S. Simula, *Phys. Lett. B* 325, 276 (1994).
- C. C. degli Atti and S. Simula, *Phys. Rev. C* 53, 1689 (1996).

$$\frac{2}{A} \frac{\sigma_A}{\sigma_D} = a_2(A)$$



Previous measurements

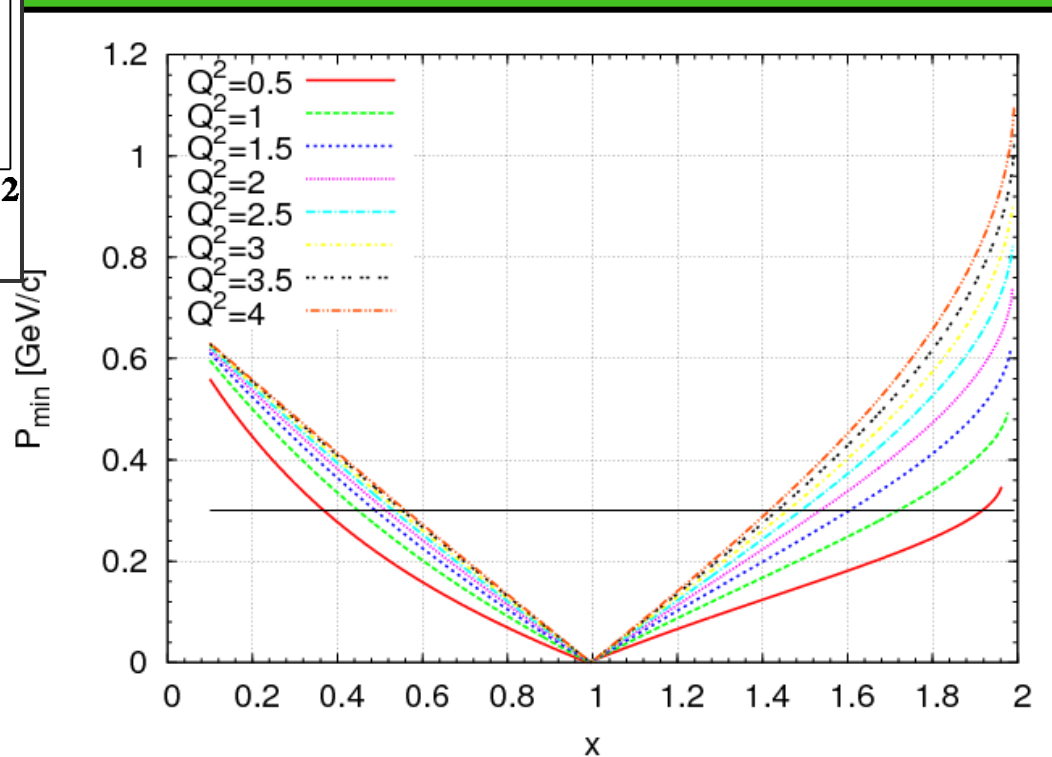


$1.4 < x < 2 \Rightarrow$ 2 nucleon correlation

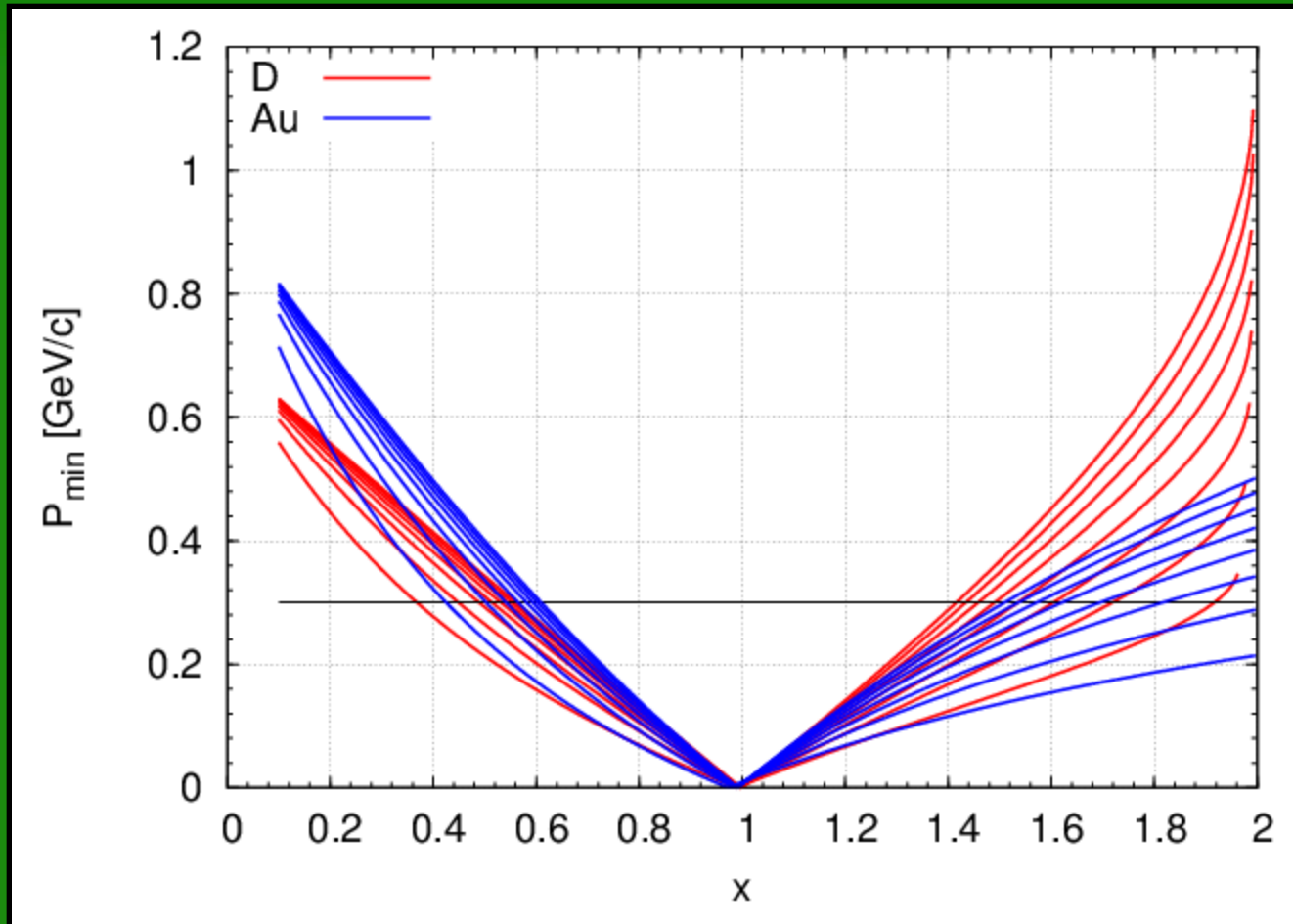
$2.4 < x < 3 \Rightarrow$ 3 nucleon correlation

Egiyan et al, Phys.Rev.C68, 2003

No observation of scaling for $Q^2 < 1.4 \text{ GeV}^2$

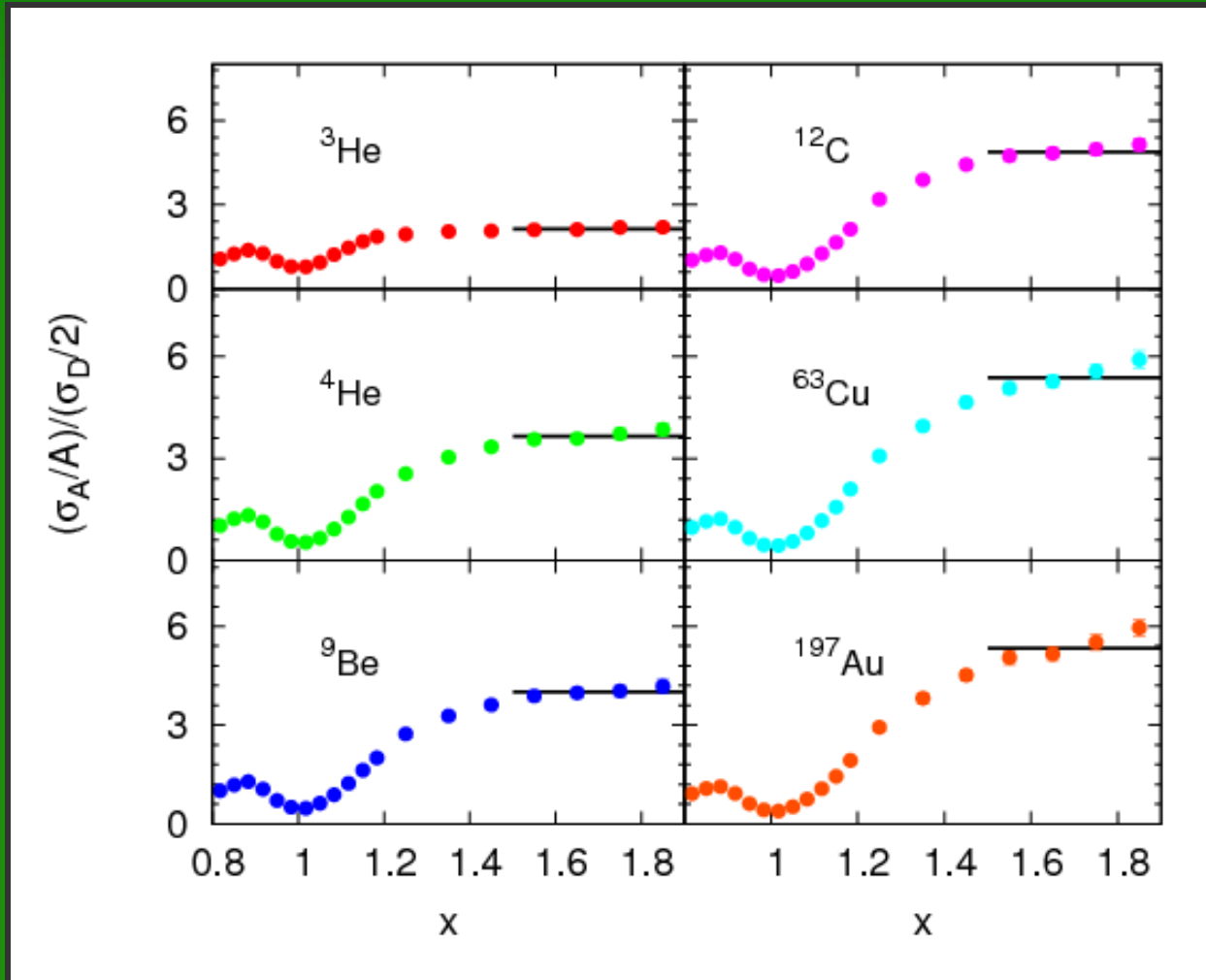


Kinematic cutoff is A-dependent



- For heavy nuclei, the minimum momentum changes \rightarrow heavier recoil system requires less kinetic energy to balance the momentum of the struck nucleon
- Larger fermi momenta for $A > 2$ \rightarrow MF contribution persists for longer

E02-019: 2N correlations in A/D ratios



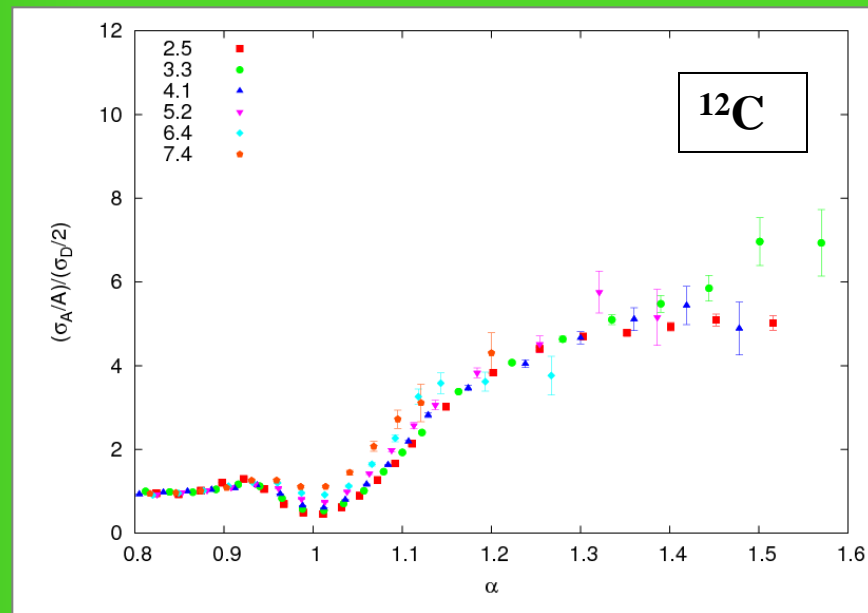
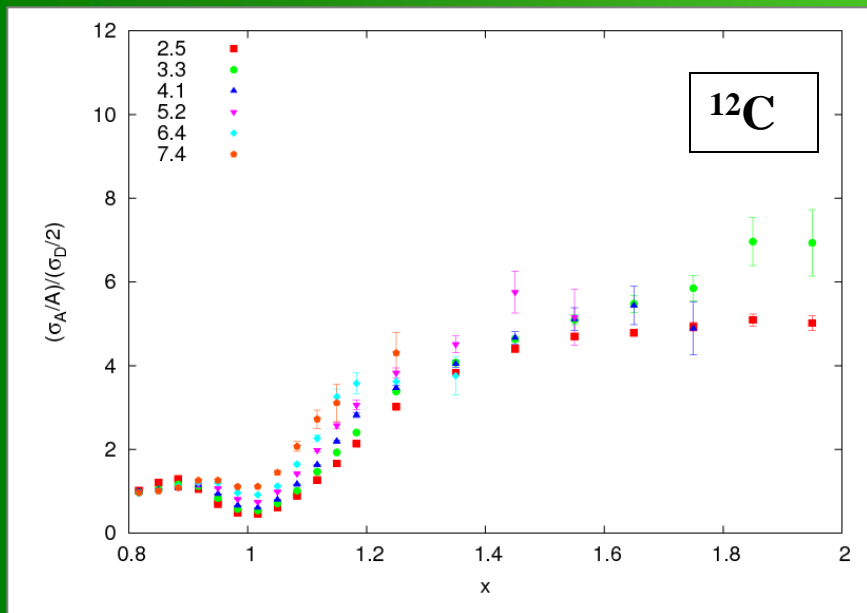
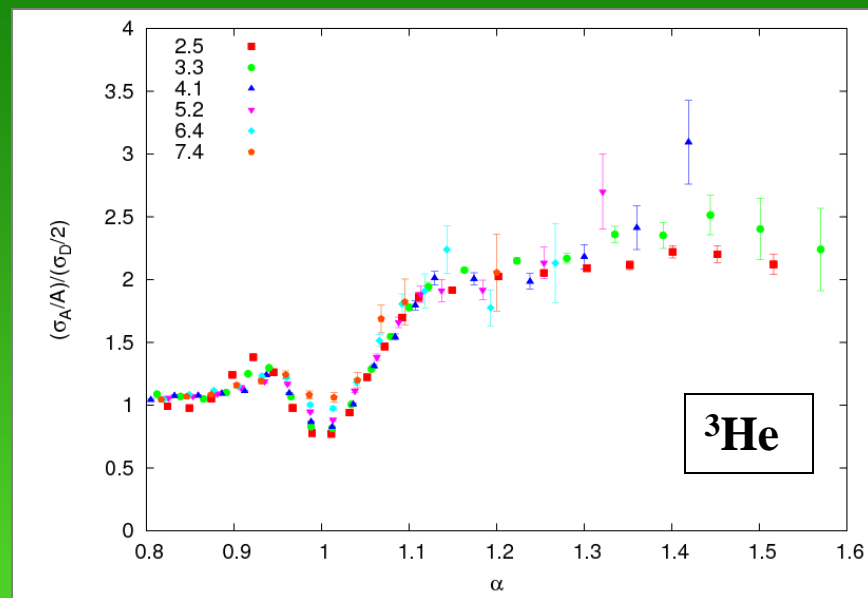
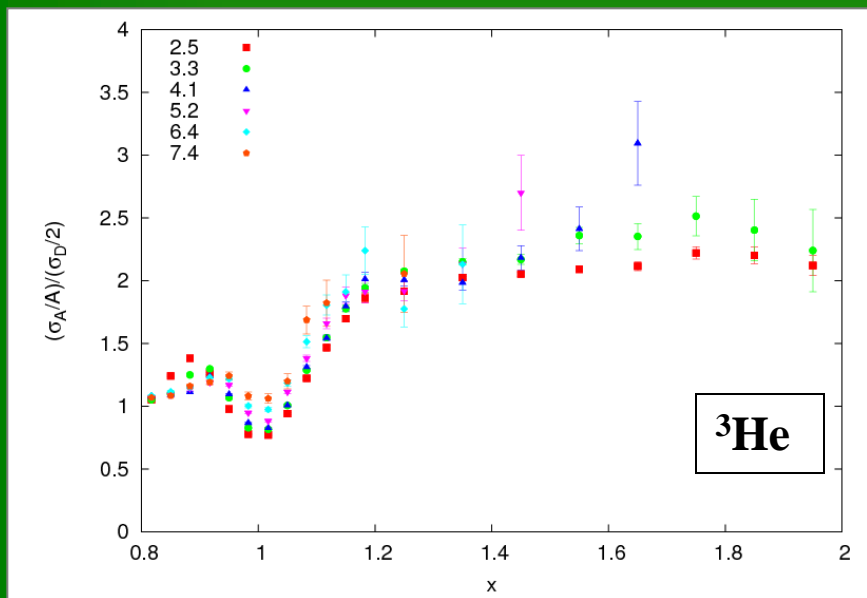
Fomin et al, PRL 108 (2012)

Jlab E02-019

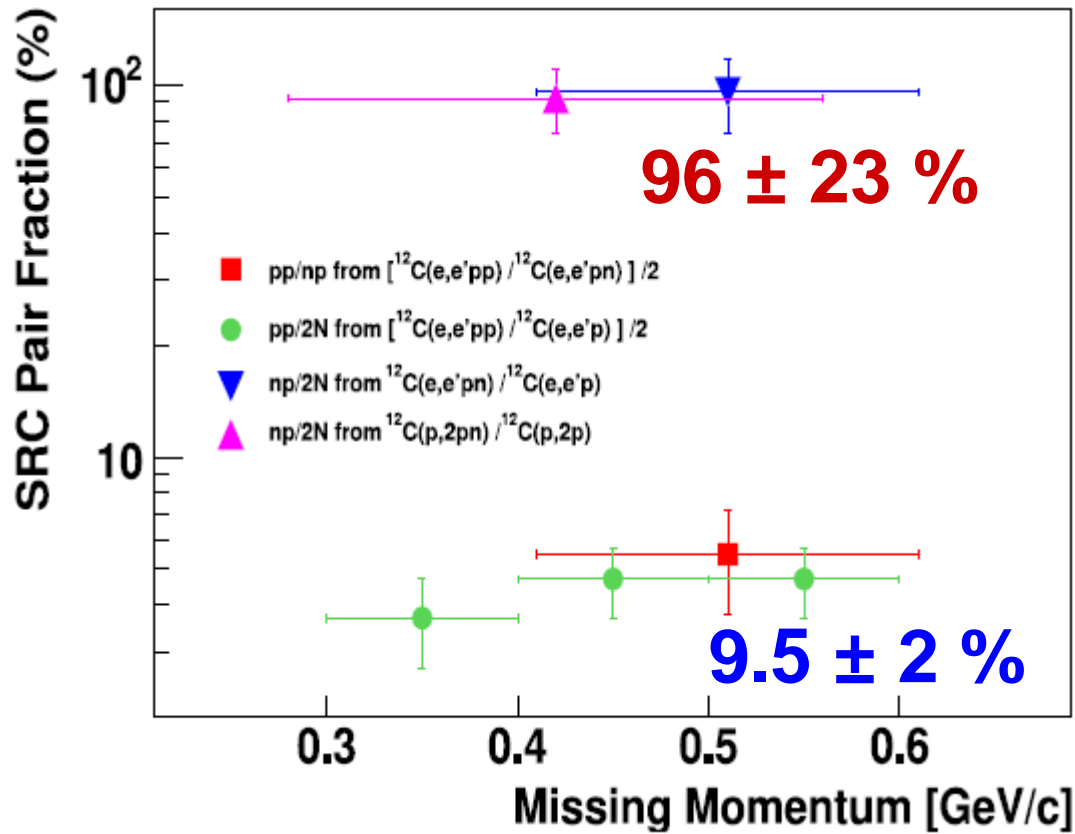
$$\langle Q^2 \rangle = 2.7 \text{ GeV}^2$$

Q^2 dependence features

$$\alpha = 2 - \frac{q^- + 2M}{2M} \left(1 + \frac{\sqrt{W^2 - 4M^2}}{W} \right)$$



NP dominance

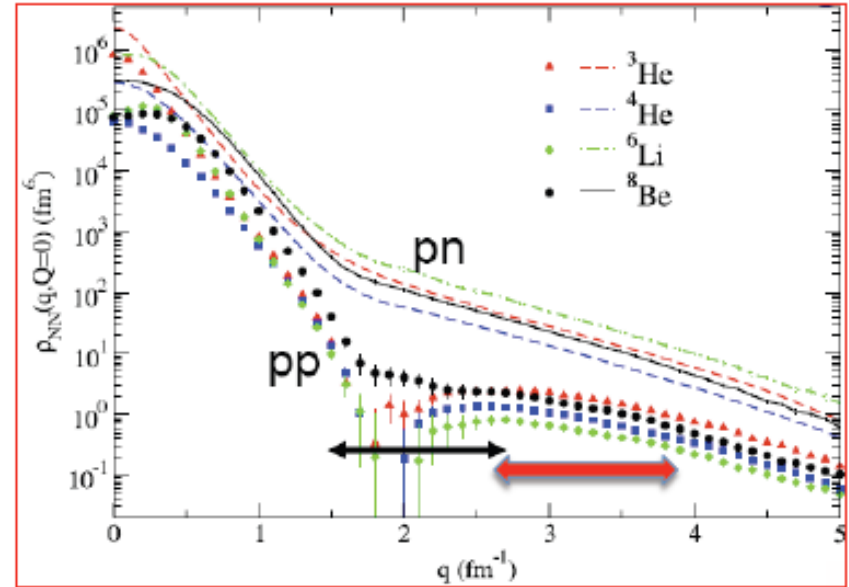
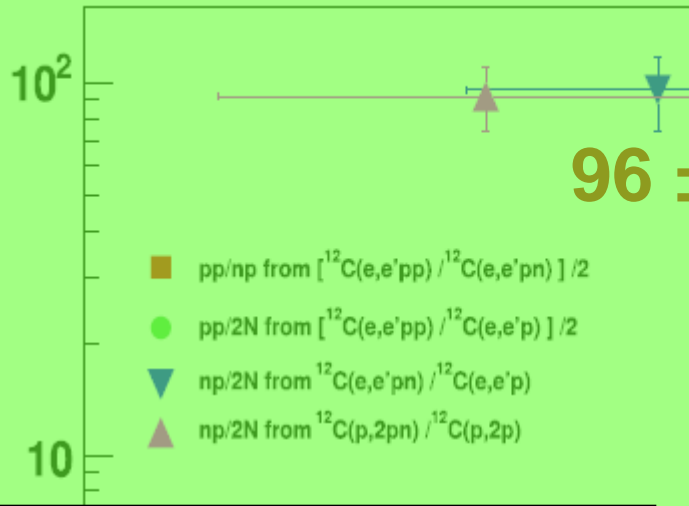


R. Subedi et al., *Science*
320, 1476 (2008)

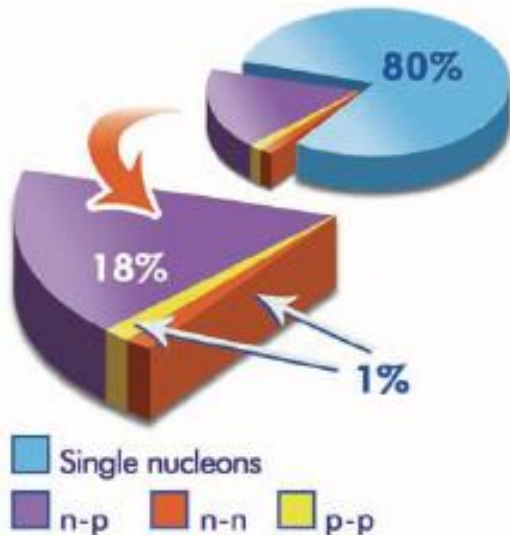
R. Shneor et al.,
PRL 99, 072501 (2007)

NP dominance

SRC Pair Fraction (%)



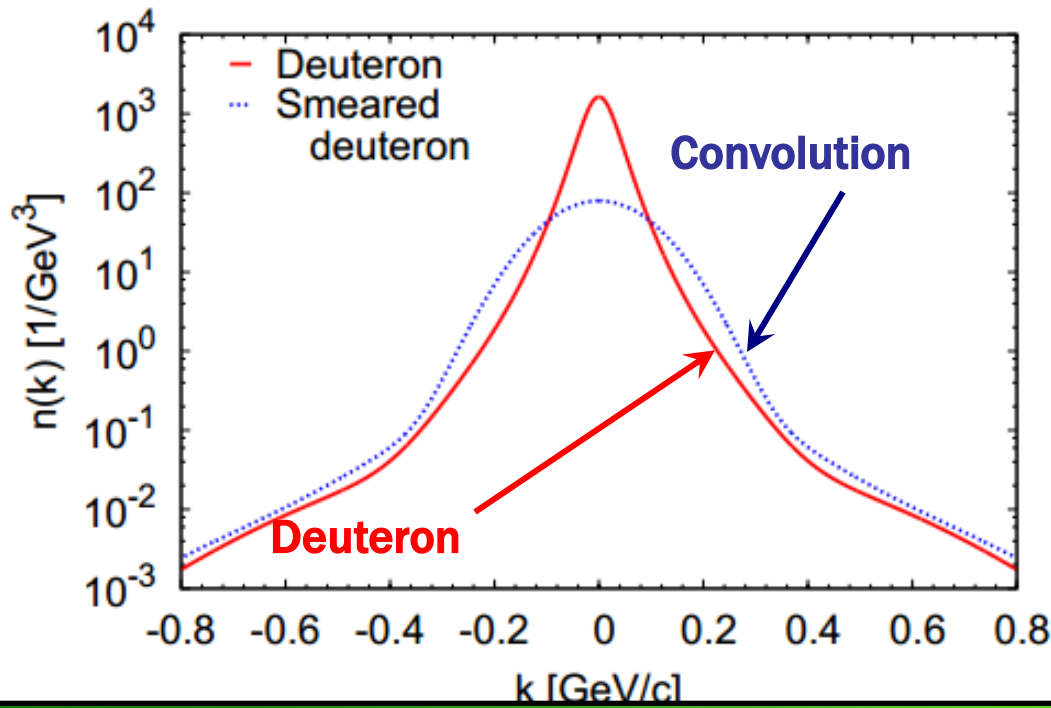
R. Schiavilla, R. B. Wiringa, S. C. Pieper, J. Carlson, Phys. Rev. Lett. **98** (2007) 132501



also

→ Ciofi and Alvioli PRL 100, 162503 (2008)
 → Sargsian, Abrahamyan, Strikman, Frankfurt PR C71 044615 (2005)

$(a_2 = \sigma_A / \sigma_D) \neq$ Relative # of SRCs



$n_D^{CONV}(k)$ is the convolution of $n_D(k)$ with the CM motion of correlated pairs in iron

Following prescription from C. Ciofi degli Atti and S. Simula, *Phys. Rev. C* 53 (1996)

	E02-019	SLAC	CLAS	R_{2N-ALL}	a_2-ALL
^3He	1.93 ± 0.10	1.8 ± 0.3	–	1.92 ± 0.09	2.13 ± 0.04
^4He	3.02 ± 0.17	2.8 ± 0.4	2.80 ± 0.28	2.94 ± 0.14	3.57 ± 0.09
Be	3.37 ± 0.17	–	–	3.37 ± 0.17	3.91 ± 0.12
C	4.00 ± 0.24	4.2 ± 0.5	3.50 ± 0.35	3.89 ± 0.18	4.65 ± 0.14
Al	–	4.4 ± 0.6	–	4.40 ± 0.60	5.30 ± 0.60
Fe	–	4.3 ± 0.8	3.90 ± 0.37	3.97 ± 0.34	4.75 ± 0.29
Cu	4.33 ± 0.28	–	–	4.33 ± 0.28	5.21 ± 0.20
Au	4.26 ± 0.29	4.0 ± 0.6	–	4.21 ± 0.26	5.13 ± 0.21

$a_2 = \sigma_A / \sigma_D \rightarrow$ relative measure of high momentum nucleons

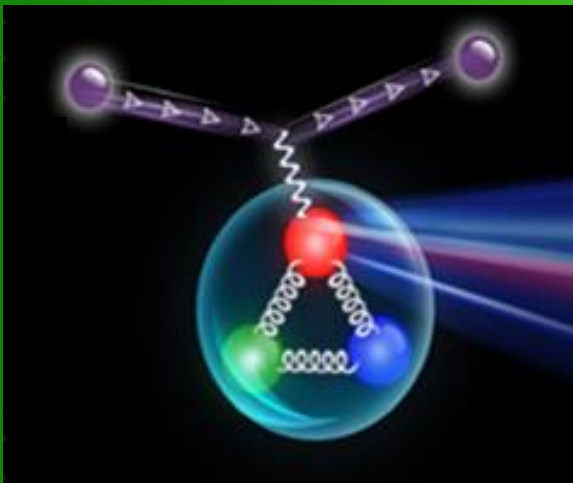
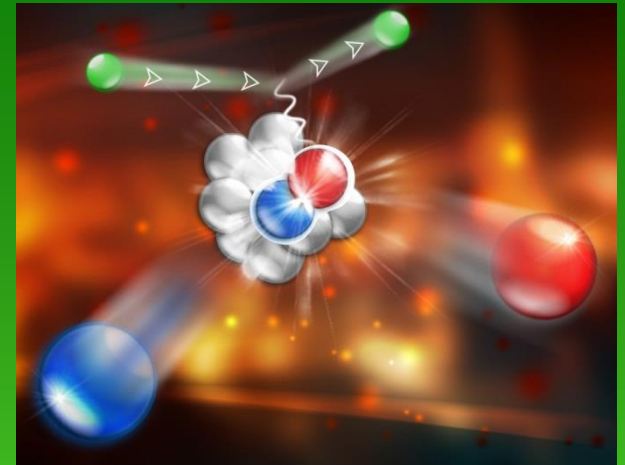
$R_{2n} \rightarrow$ relative measure of correlated pairs

FROM

Quasielastic Scattering at $x > 1$

to

DIS at $x < 1$



Where an unexpected connection is made

Discovery of the EMC effect

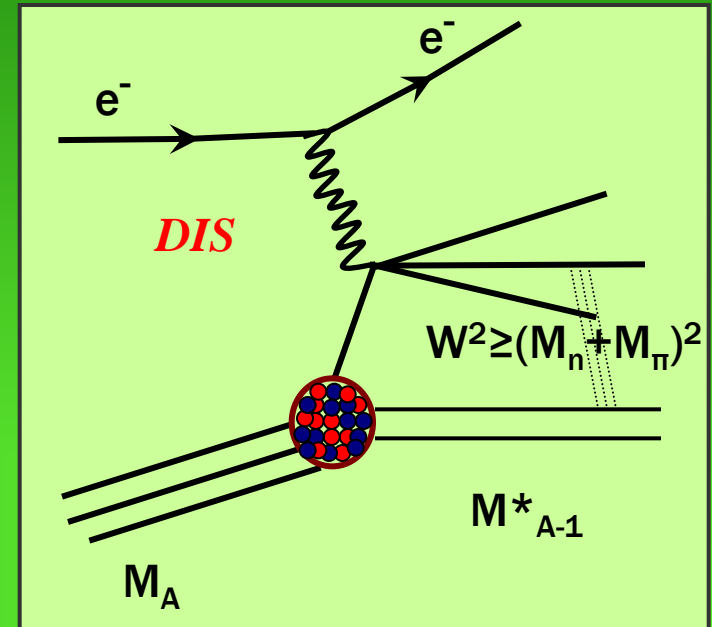
- Goal was a measurement of the lepton-nucleon cross section at high Q^2

- To achieve statistical precision in a reasonable amount of time, an iron target was used, on the assumption that

$$\frac{\sigma_A / A}{\sigma_D / 2} \approx 1$$

meaning

$$F_2^A(x) = ZF_2^p(x) + NF_2^n(x)$$

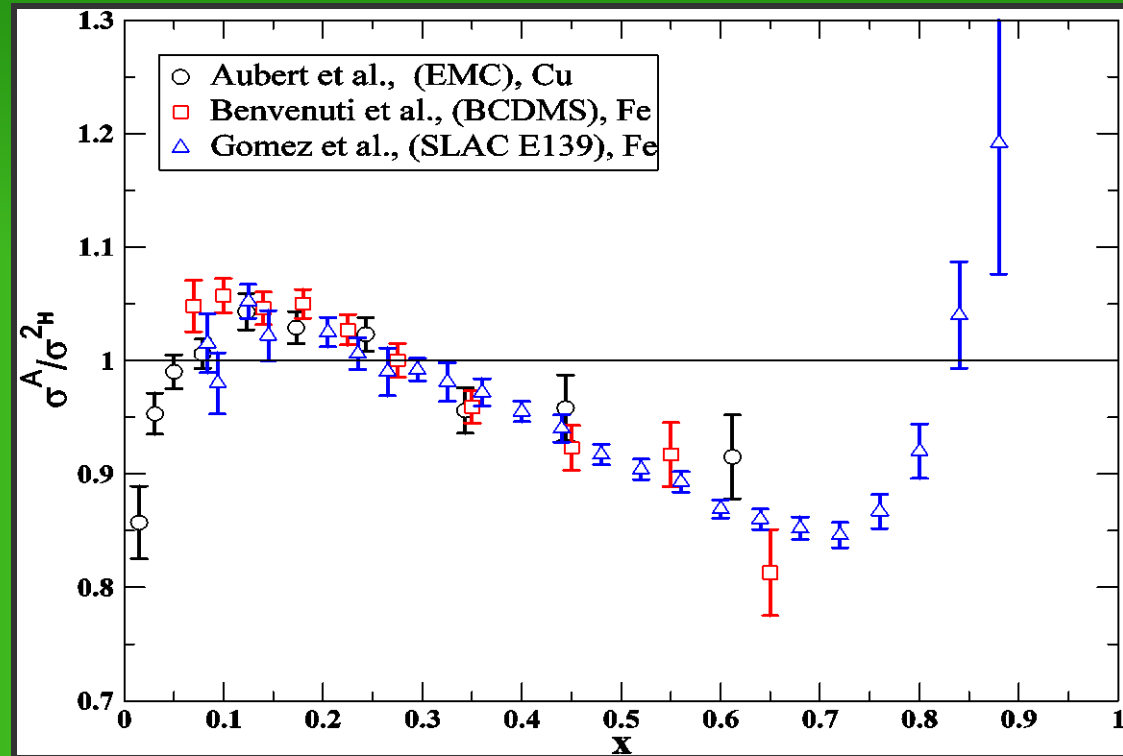
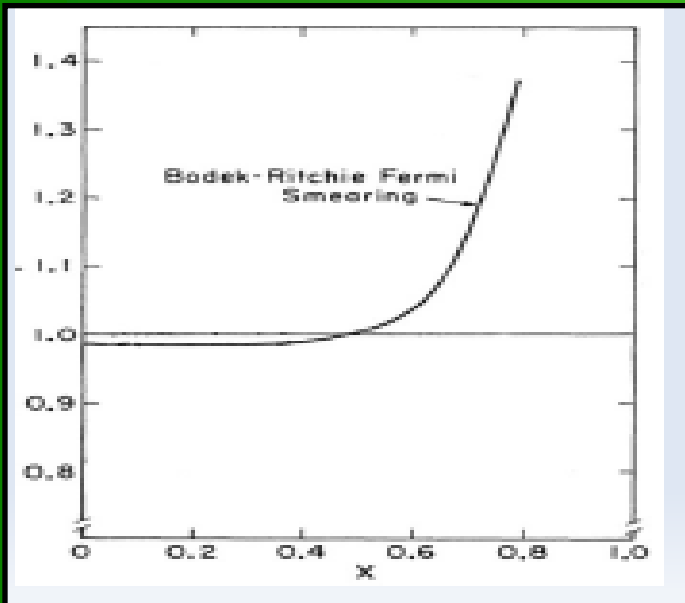


The EMC effect

$$F_2^A(x) \neq ZF_2^p(x) + NF_2^n(x)$$

Nuclear dependence of the structure functions discovered 30 years ago by the European Muon Collaboration (EMC effect)

Nucleon structure functions are modified by the nuclear medium



Shadowing

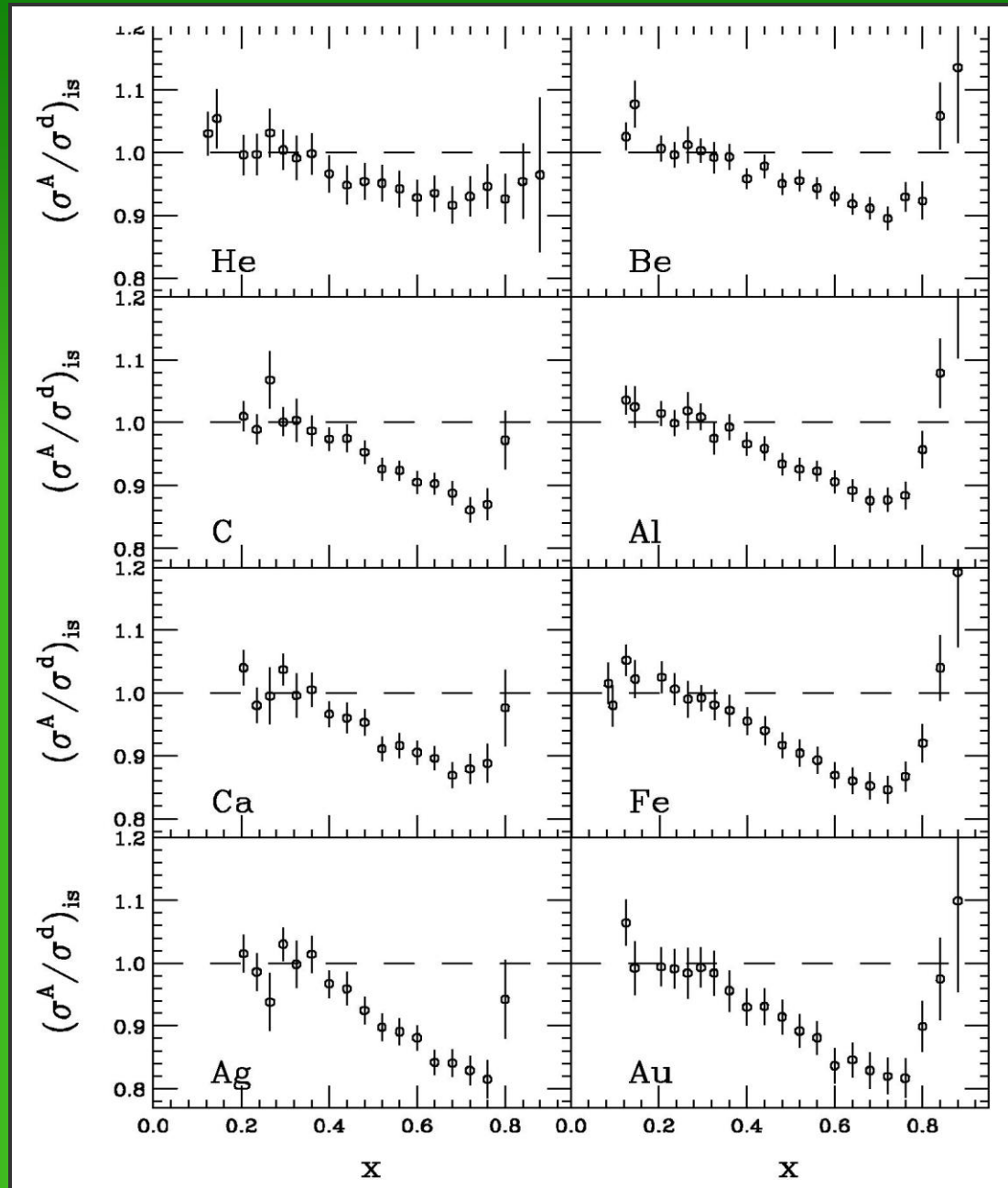
EMC region

Anti-Shadowing
(pion excess)

Fermi motion effects

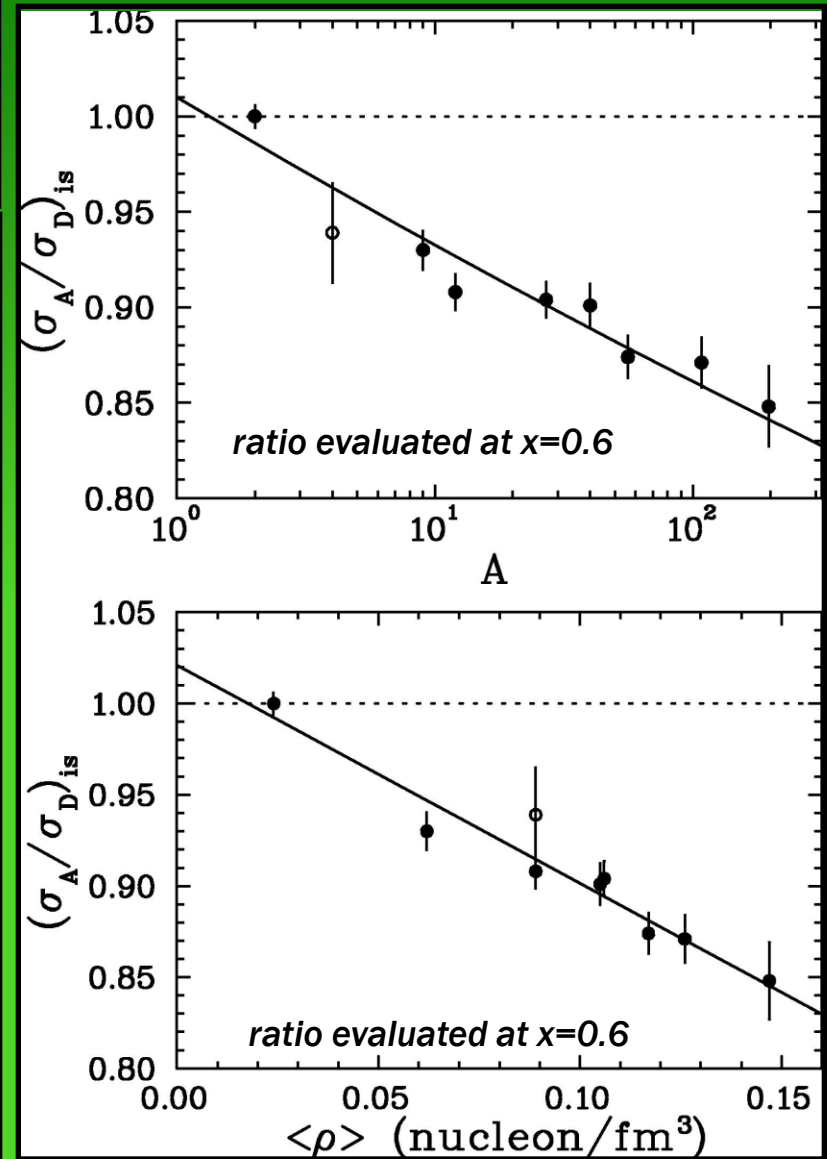
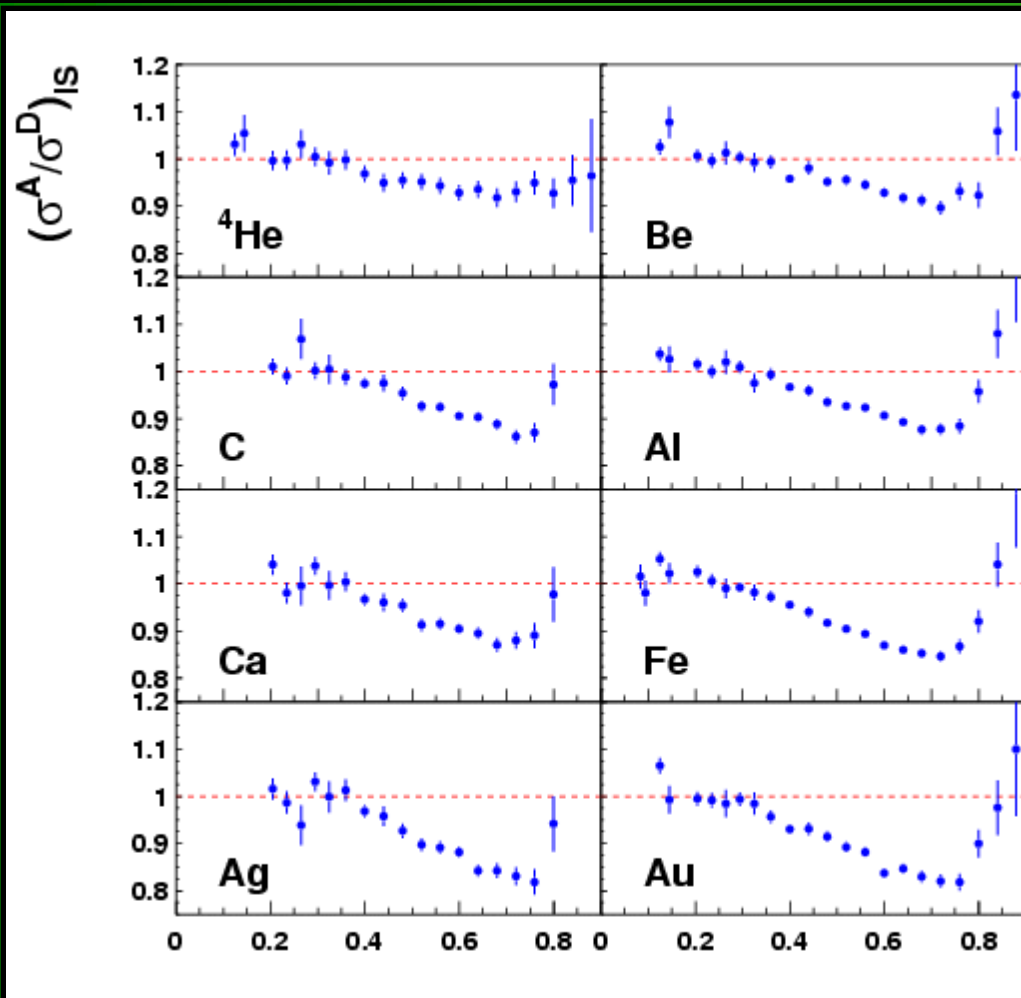
Measurements before 2004

- **NMC** – extraction of F_2^n/F_2^p
- **BCDMS** – $50 < Q^2 < 200$ (GeV²)
- **HERMES** – first measurement on ³He
- **SLAC E139** – most precise large x data
 - Q² independent
 - Universal shape
 - Magnitude approximately scales with density



Nuclear Dependence of the EMC effect

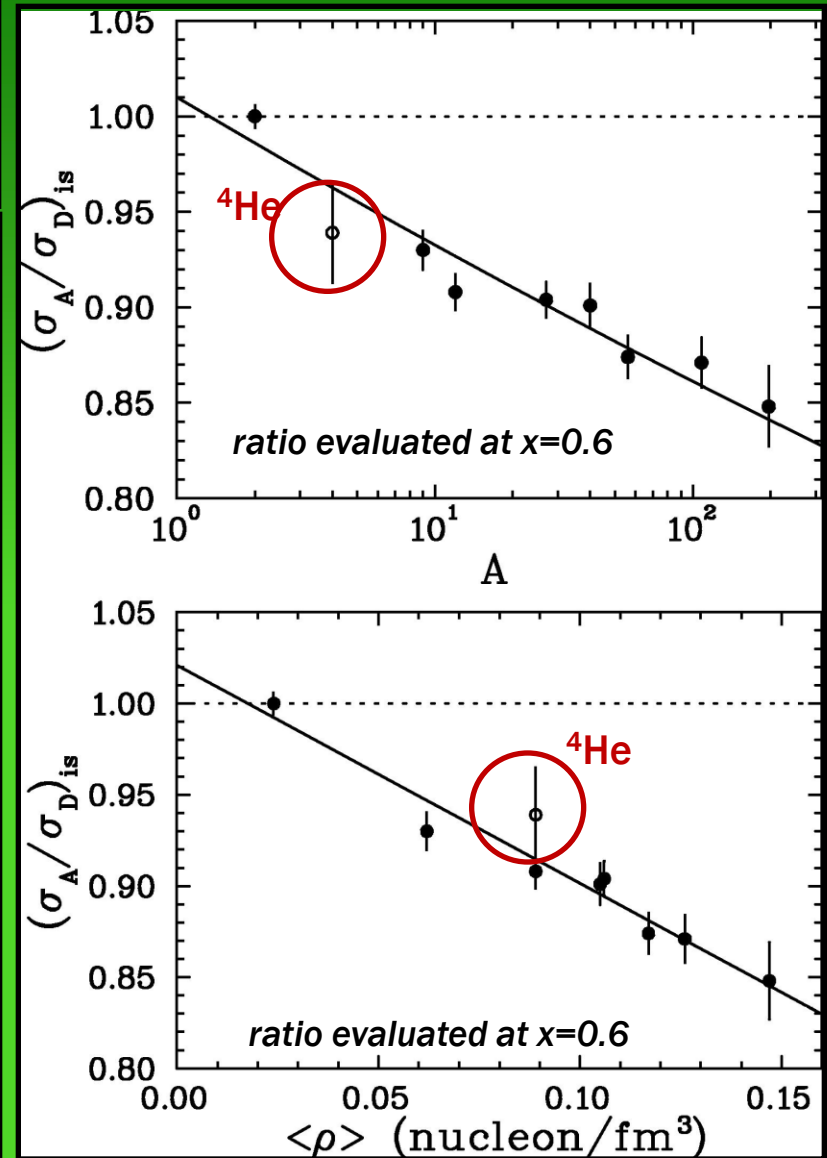
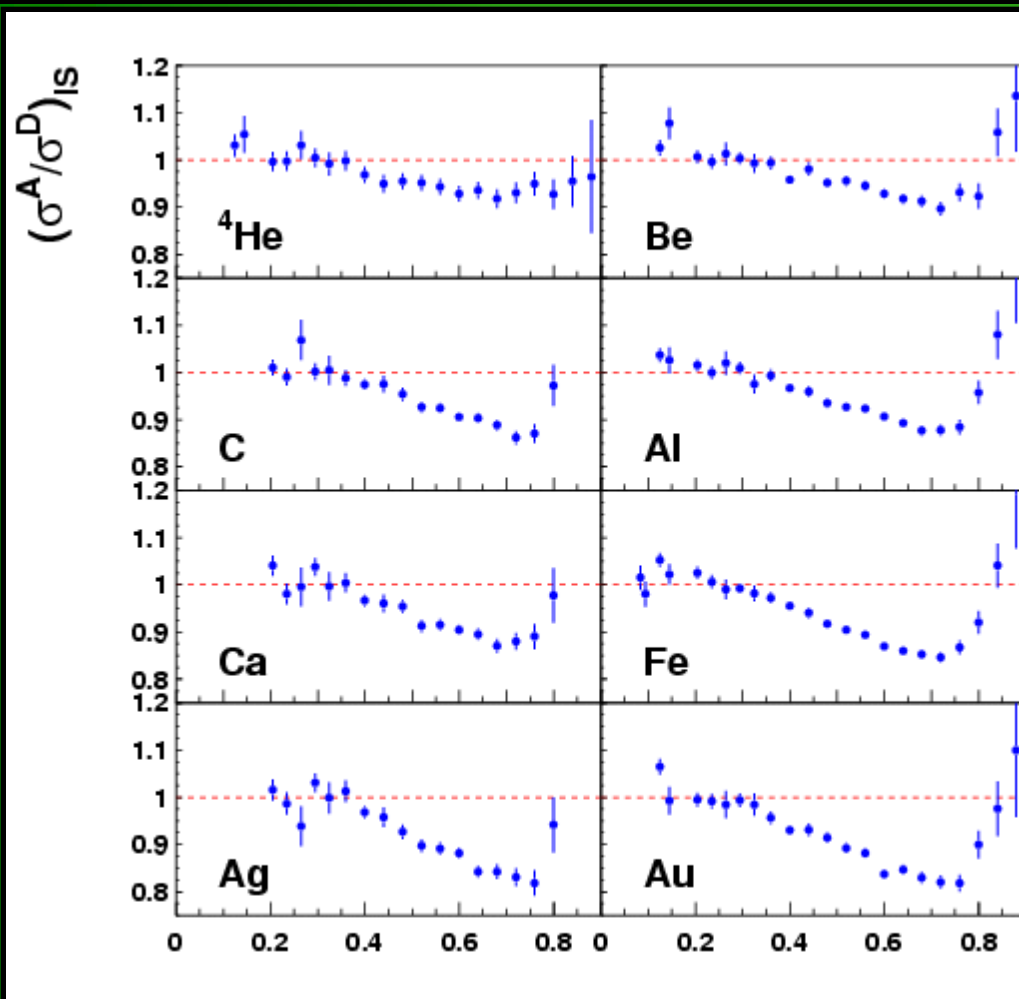
- Quark distributions are modified in nuclei
- Modification scales with A



Nuclear Dependence of the EMC effect

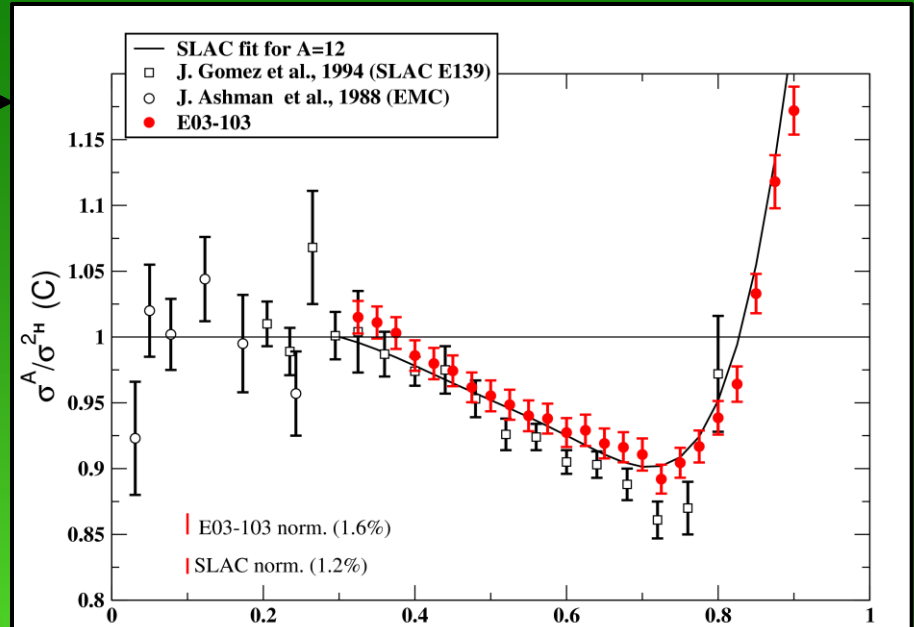
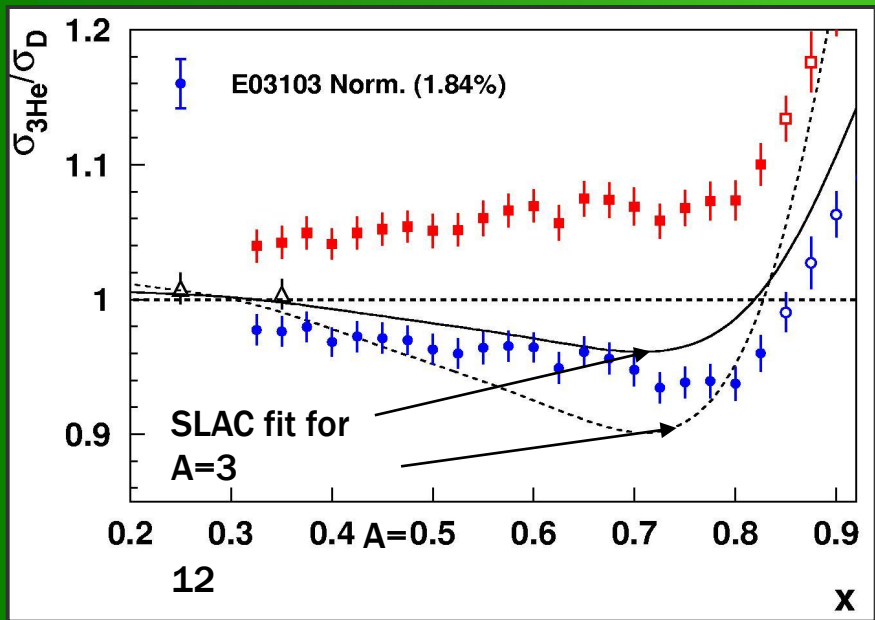
→ Quark distributions are modified in nuclei

→ Modification scales with A

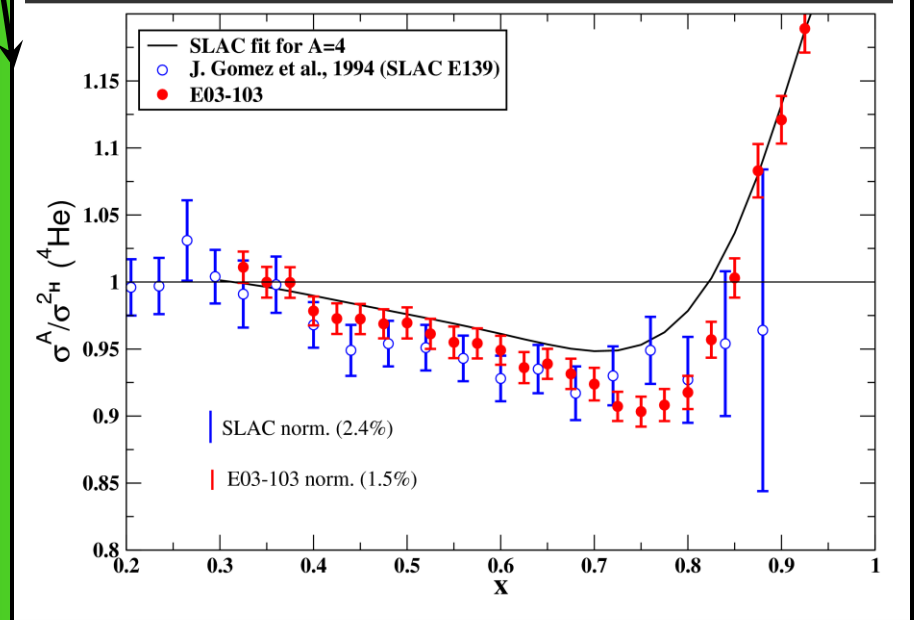


Precision results on light nuclei from JLab E03-103

- **C/D** and **⁴He/D** ratios – no isoscalar correction necessary
- Consistent with SLAC results, but much higher precision at high x



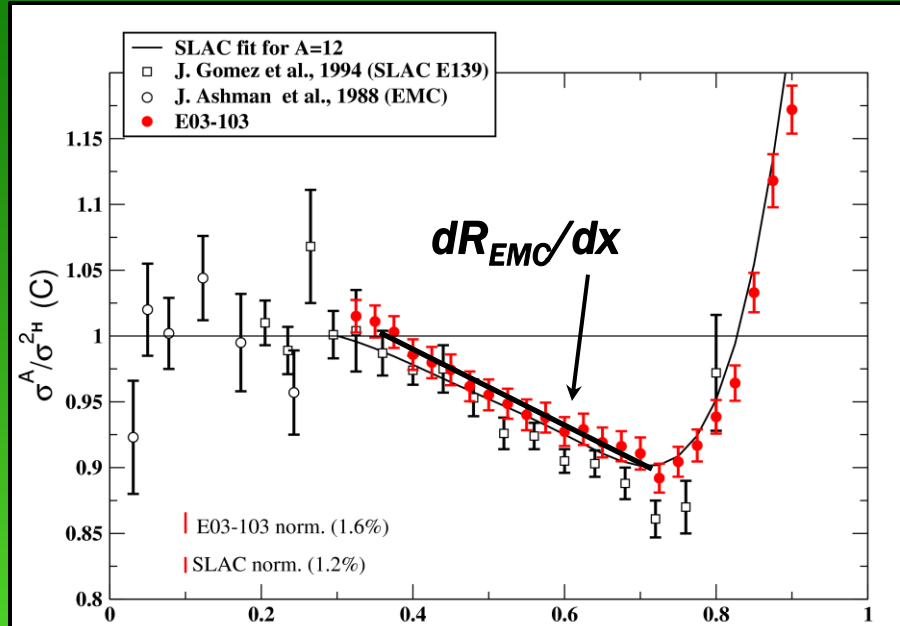
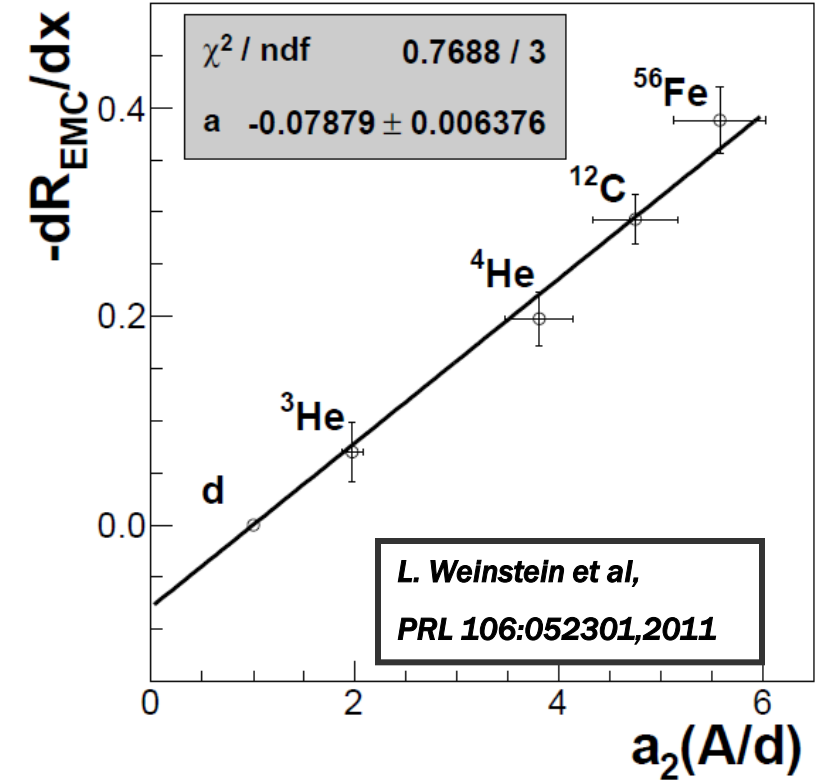
J.Seely, A. Daniel et al., PRL103, 202301 (2009)



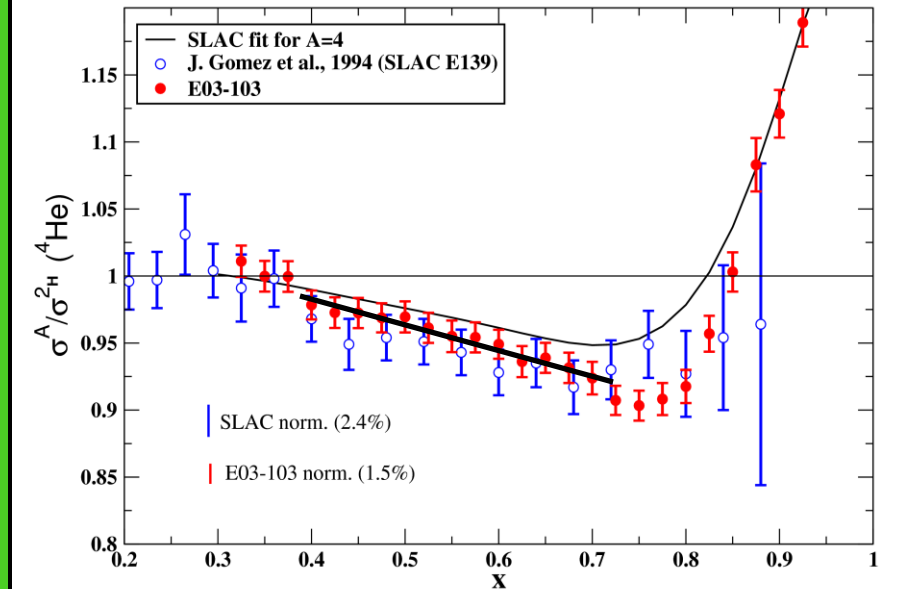
SRCs and EMC effect share the same nuclear dependence.

a_2 – relative measure of SRCs

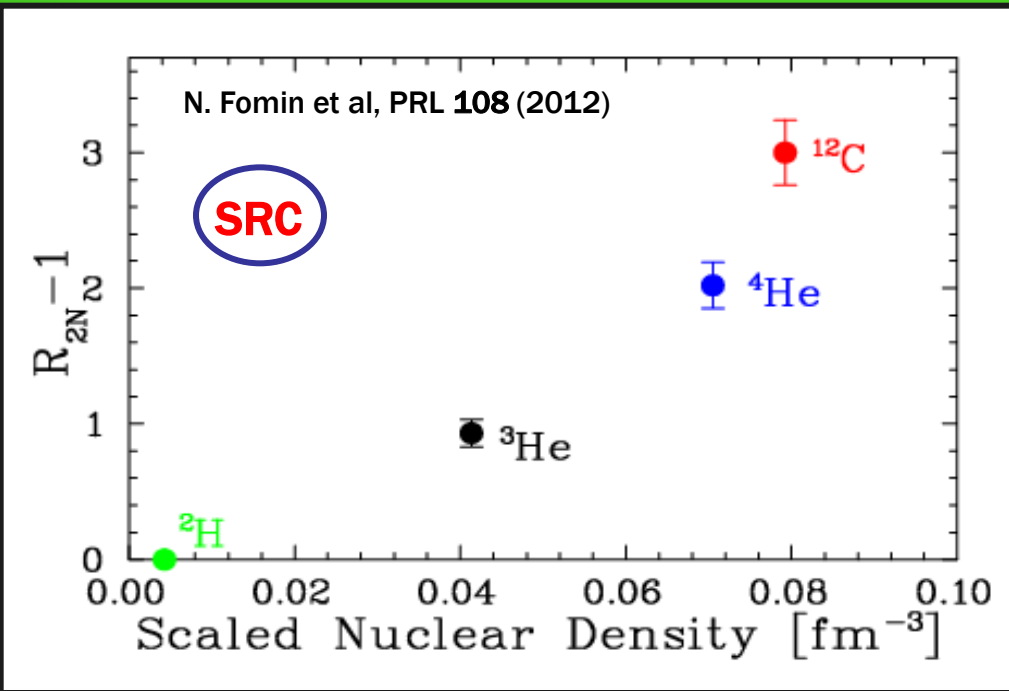
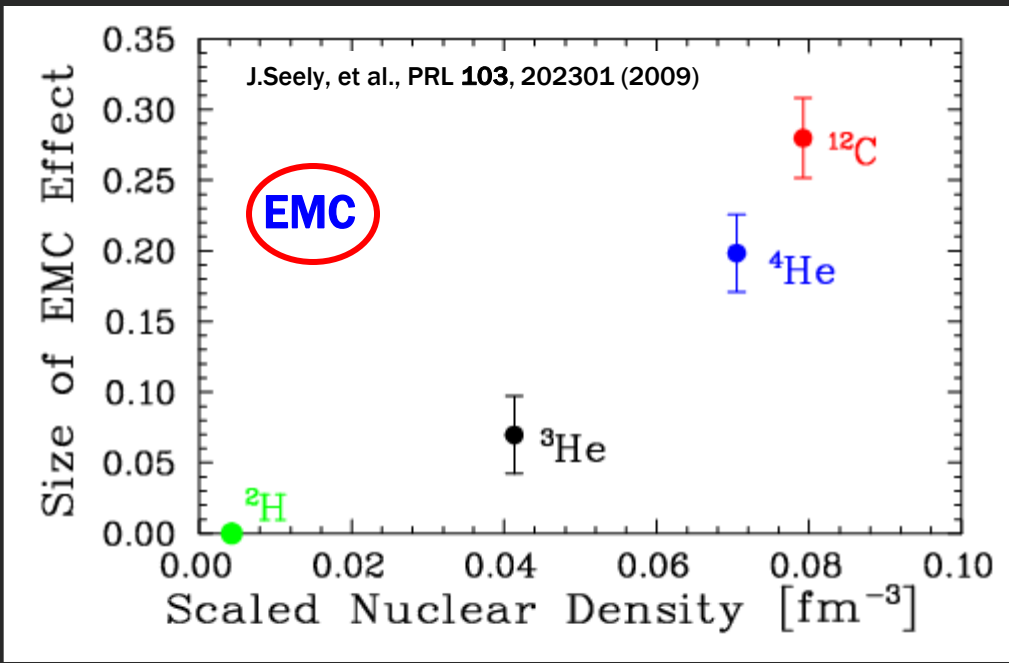
dR_{EMC}/dx – slope of the A/D cross section ratio in the $0.35 < x < 0.7$ region



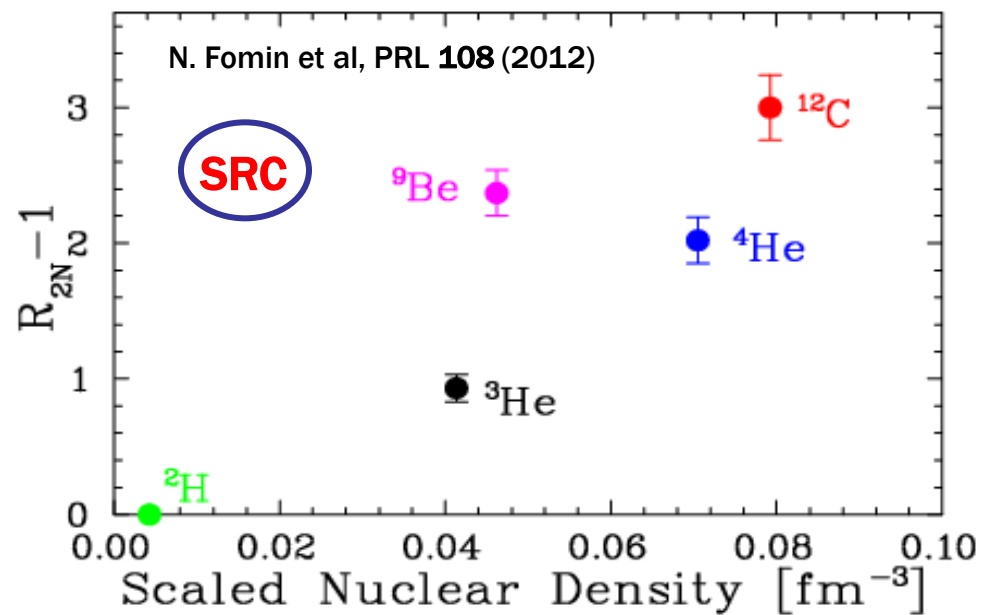
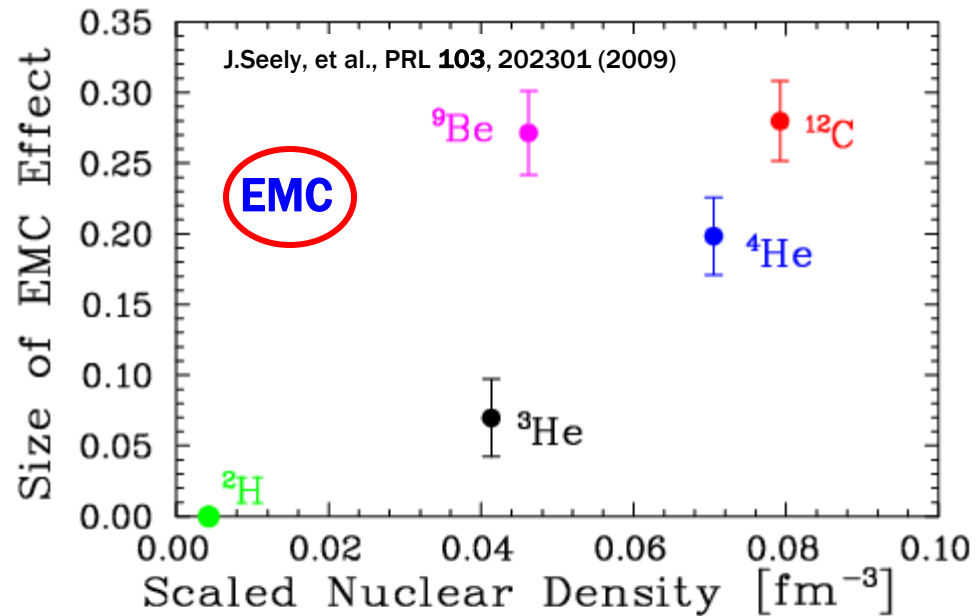
J. Seely, A. Daniel et al., PRL103, 202301 (2009)



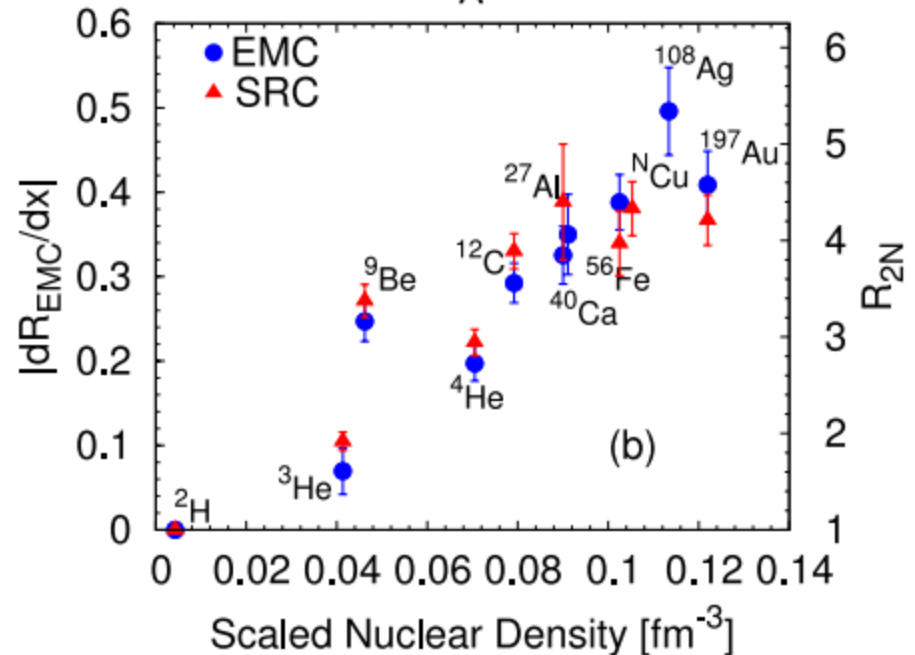
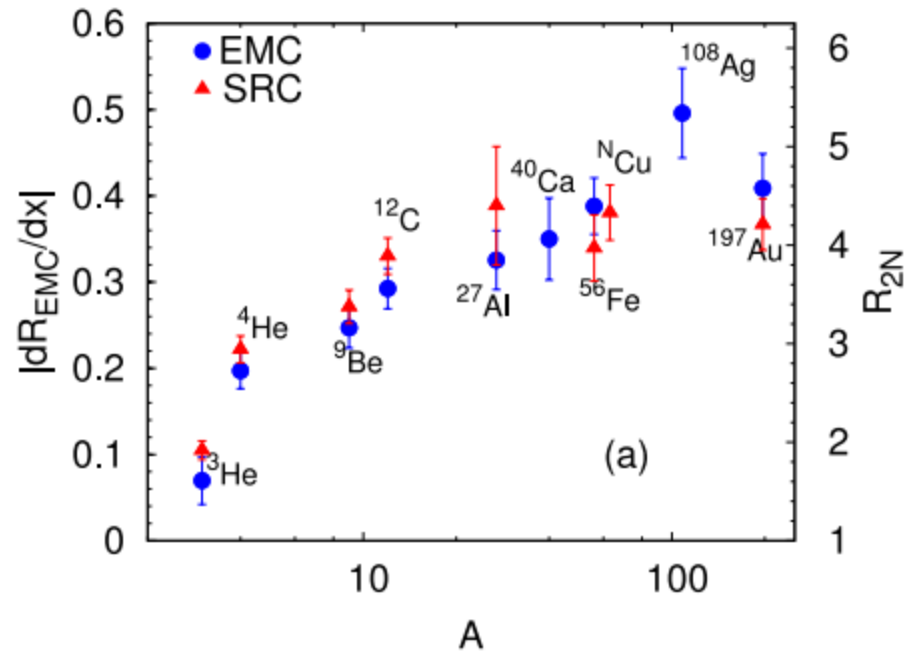
Common Density (or A)
dependence
→ linear correlation
makes sense



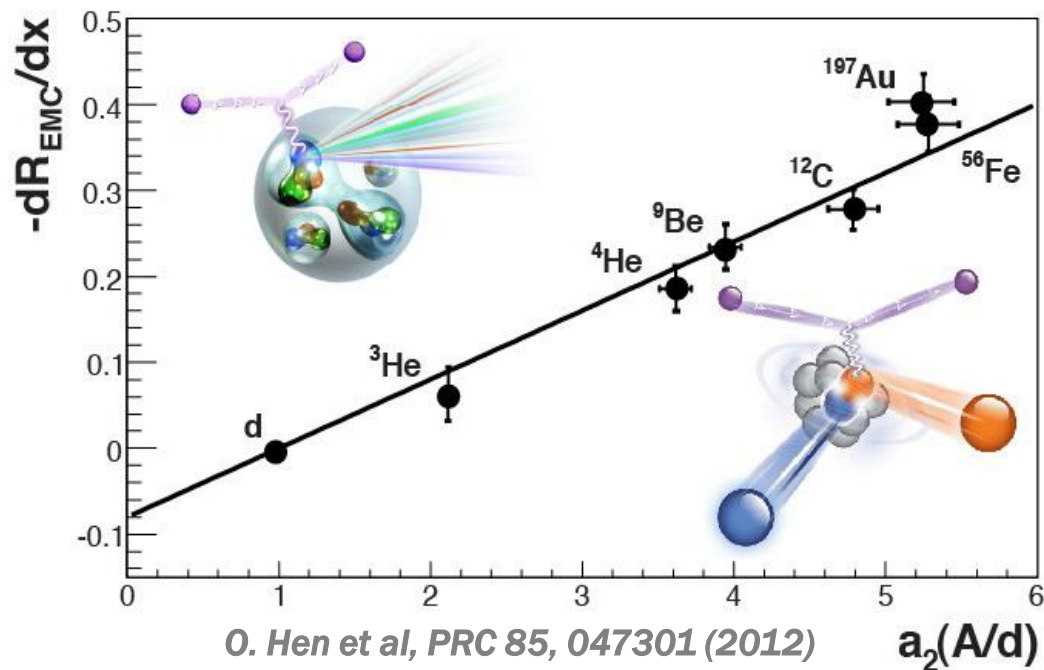
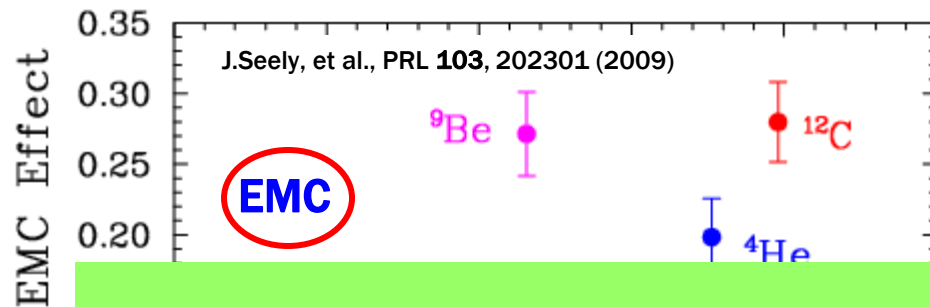
Enter ${}^9\text{Be}$



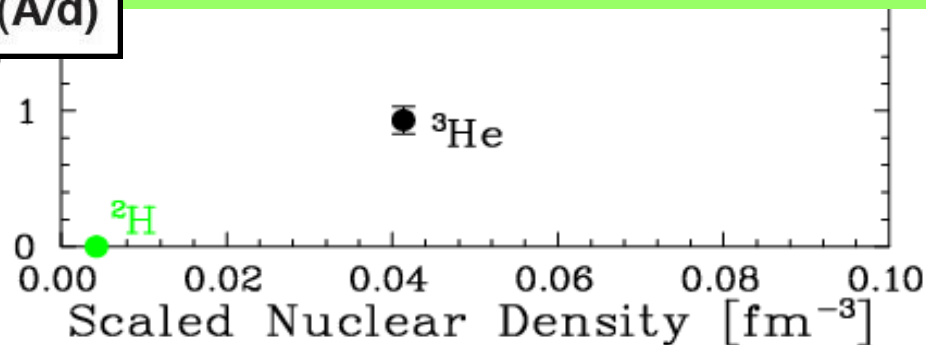
- Correlation between EMC effect and SRC data can no longer be explained by common density- or A -scaling
- However, the trends for both sets of data mirror each other as a function of A , or density



Enter ^9Be

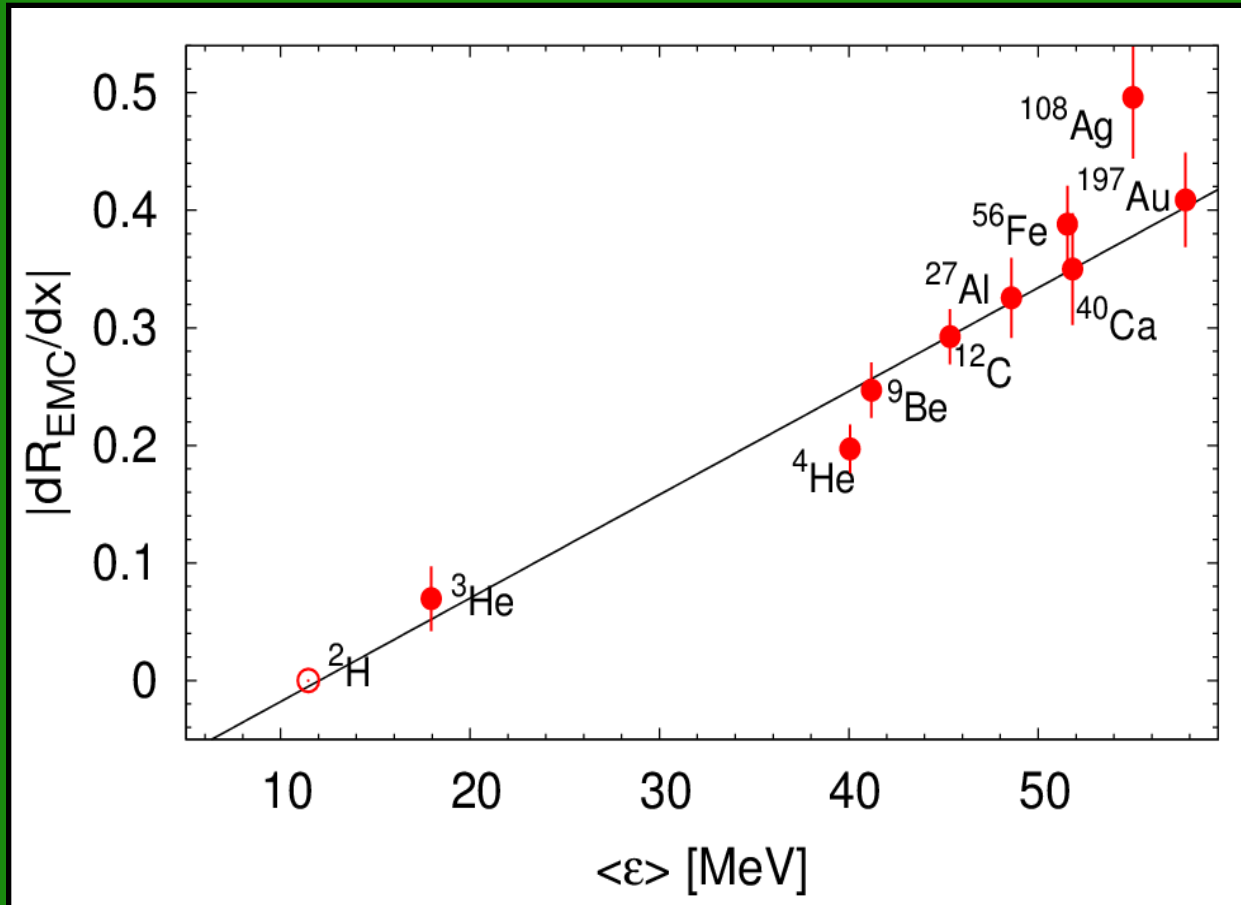


- Linear relationship still holds
- But, what does it *mean*?
 - Do the two effects share a common cause?
 - Is one sensitive to some dynamics that drive the other?



Both driven by a similar underlying cause?

Separation Energy

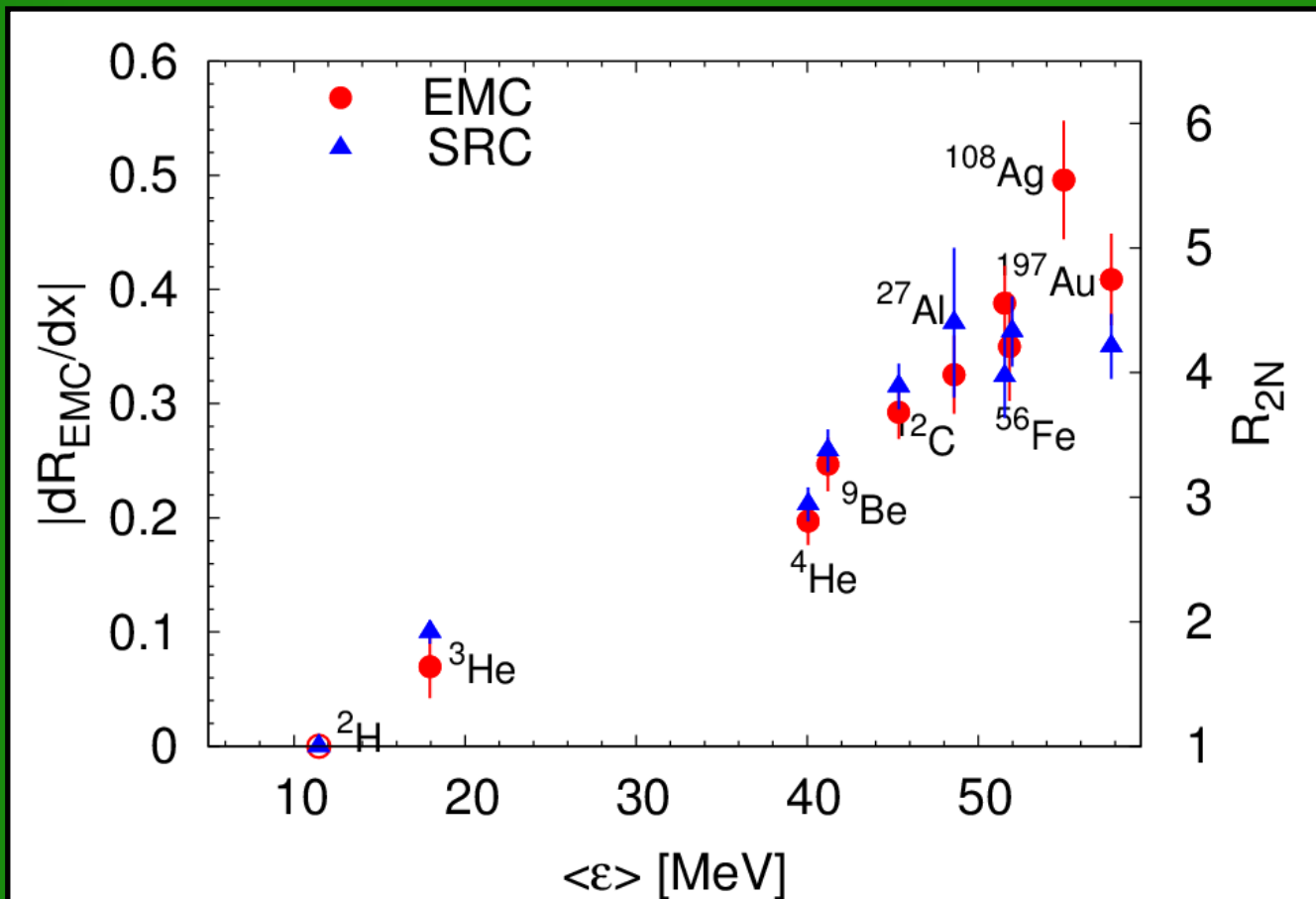


Separation energies were calculated from spectral functions, including MF and correlations

S.A. Kulagin and R. Petti, Nucl. Phys. A 176, 126 (2006)

Both driven by a similar underlying cause?

Separation Energy

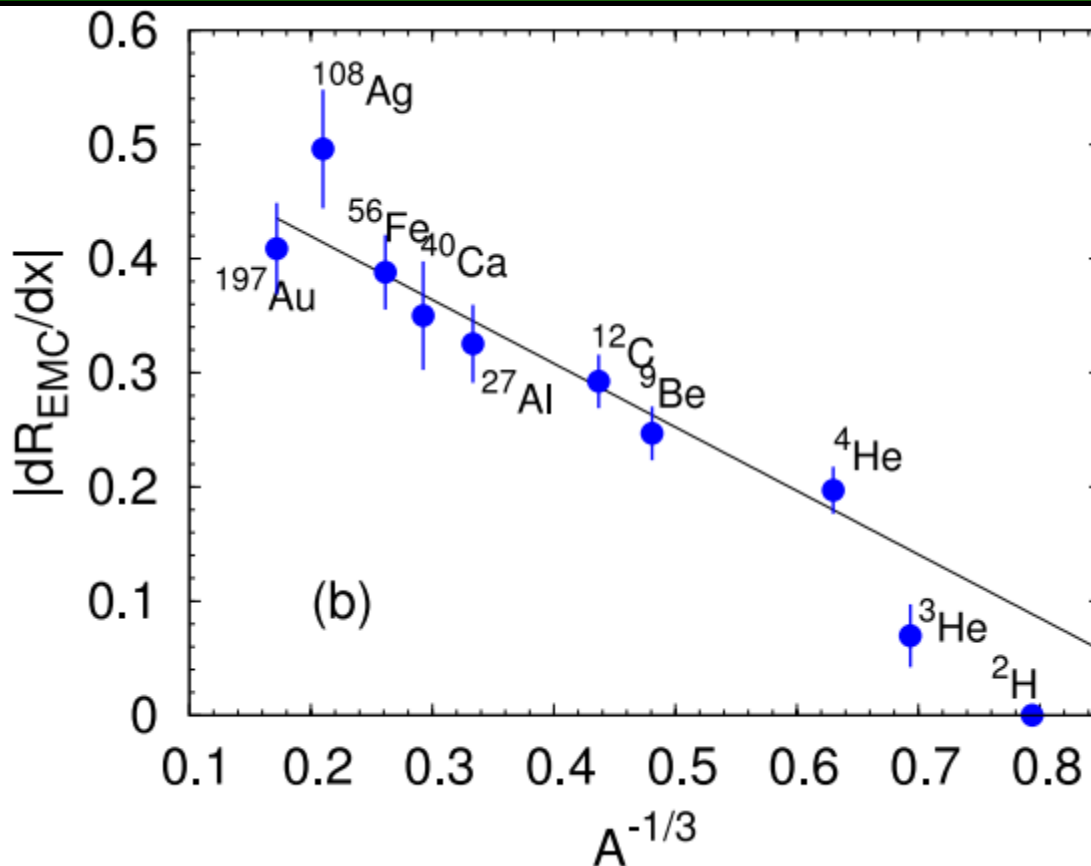


For SRCs, a linear relationship with $\langle \epsilon \rangle$ is less suggestive

S.A. Kulagin and R. Petti, Nucl. Phys. A 176, 126 (2006)

Both driven by a similar underlying cause?

$$A^{-1/3}$$



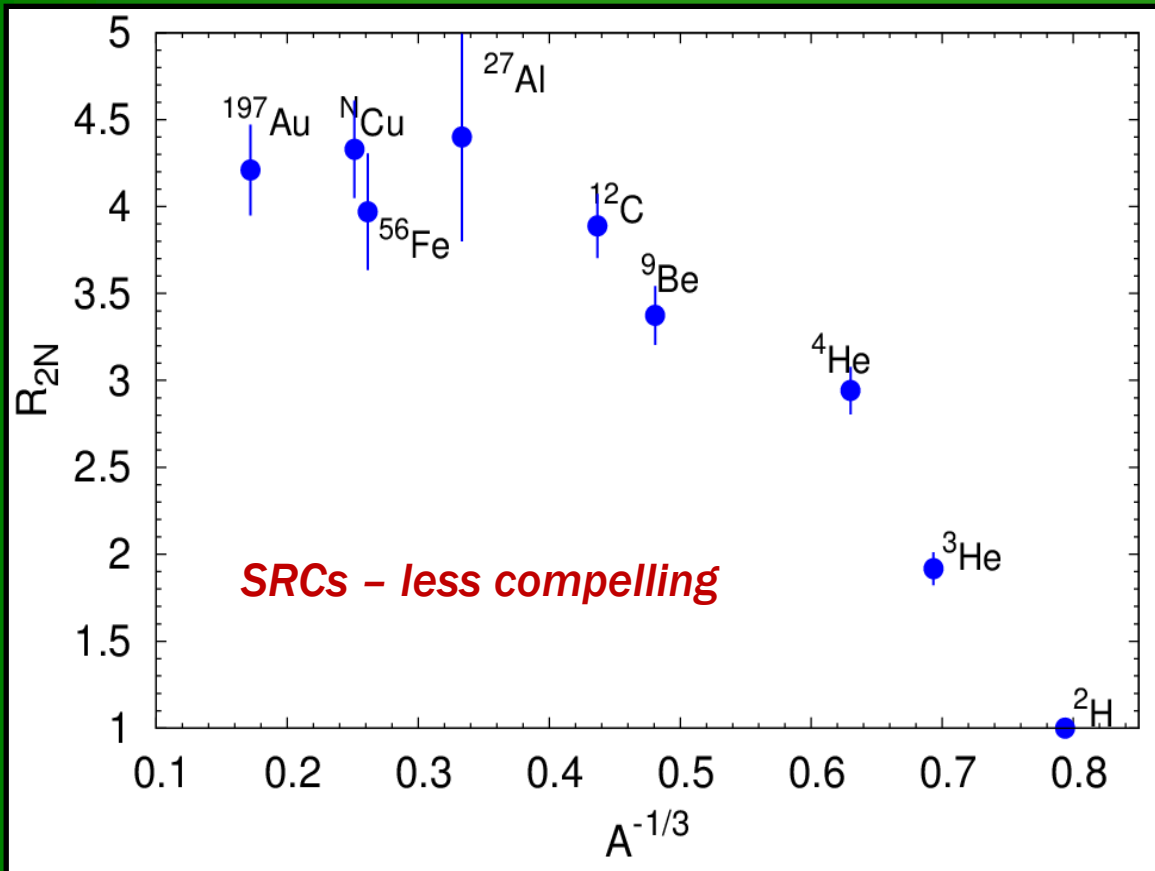
Apply exact NM calculations to finite nuclei via LDA

- (A. Antonov and I. Petkov, *Nuovo Cimento A* 94, 68 (1986))
- (I. Sick and D. Day, *Phys. Lett B* 274, 16 (1992))

- For $A > 12$, the nuclear density distribution has a common shape; constant in the nuclear interior (bulk)
→ **Scale with A**
- Nuclear surface contributions grow as $A^{2/3}$ (R^2)
- σ per nucleon would be constant with small deviations that go with $A^{-1/3}$

Both driven by a similar underlying cause?

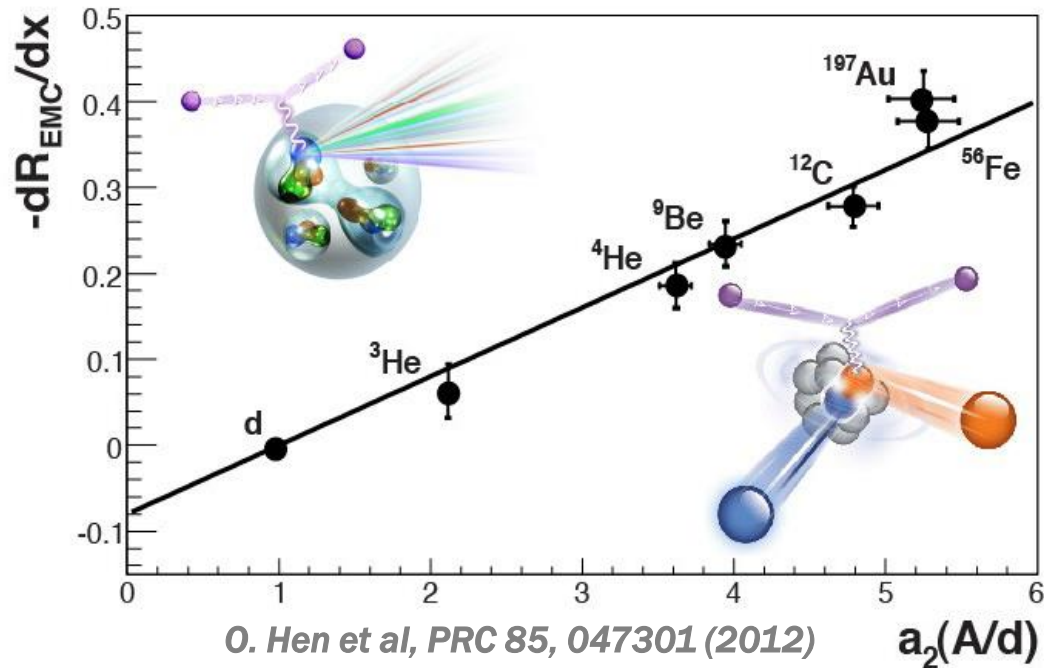
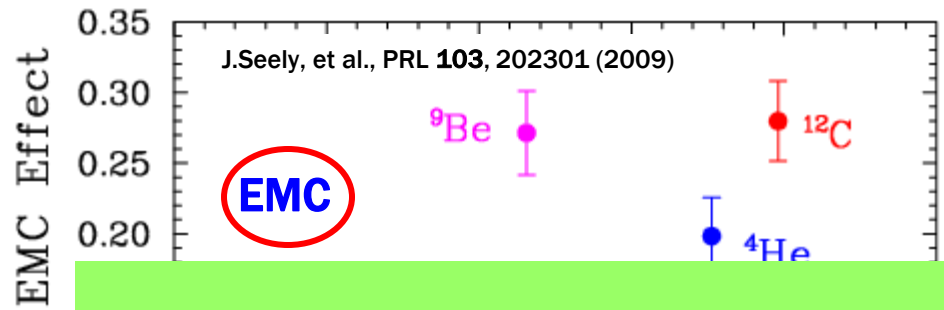
$$A^{-1/3}$$



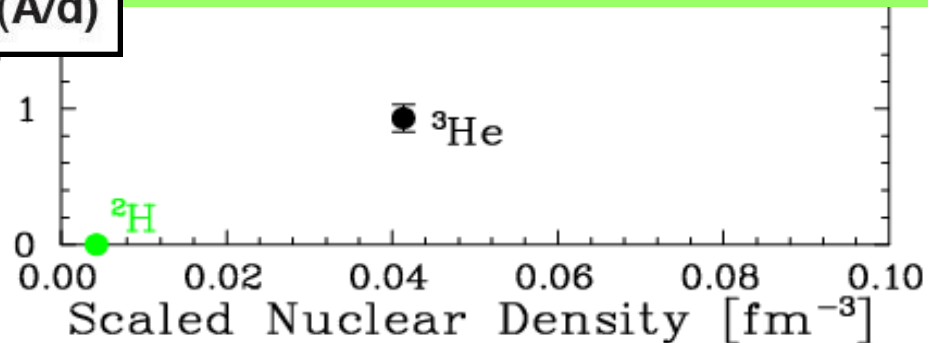
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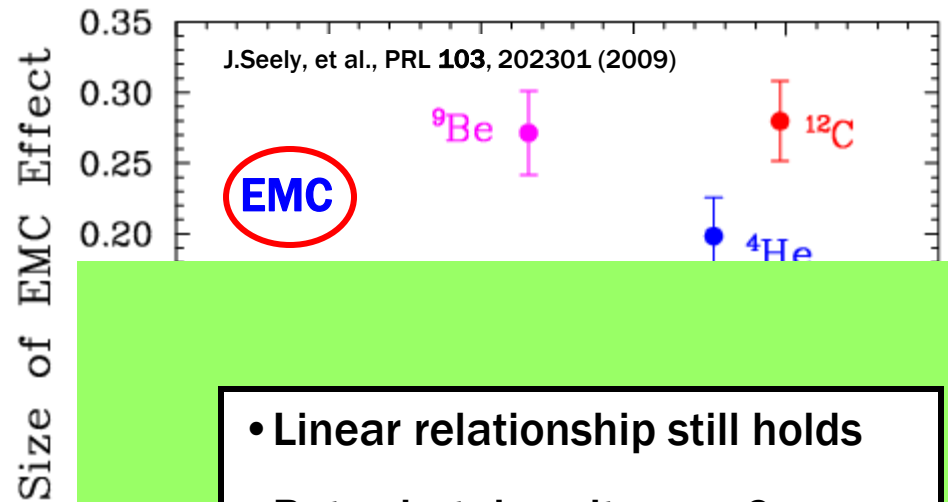
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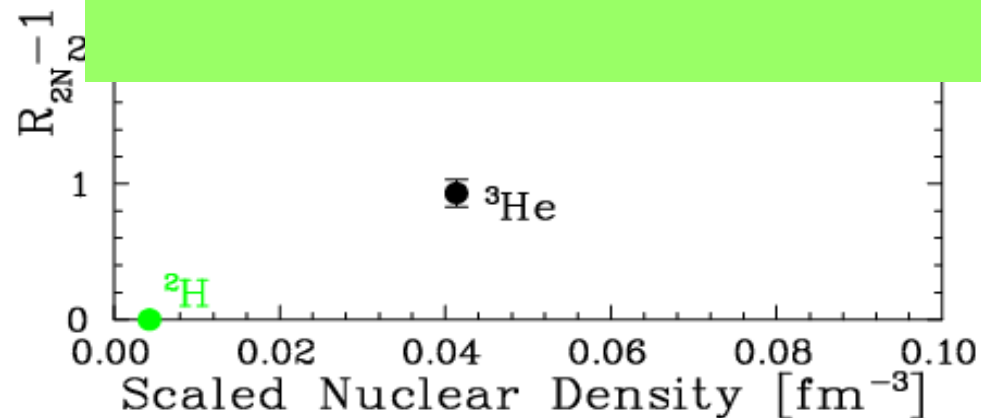
- Linear relationship still holds
- But, what does it *mean*?
 - Do the two effects share a common cause?
 - Is one sensitive to some dynamics that drive the other?



- All the usual (historical) suspects don't adequately describe the trends seen in both sets of data
- Perhaps, SRCs are an indirect (or not so indirect) measure of what drives medium modification



- Linear relationship still holds
- But, what does it *mean*?
 - *Do the two effects share a common cause?*
 - Is one sensitive to some dynamics that drive the other?



Two Hypotheses

1. Both quantities reflect **virtuality** of the nucleons (L. Weinstein et al, PRL 106:052301,2011)

- a_2 measures the relative high momentum tail – good for testing virtuality
- dR_{EMC}/dx – relevant quantity

2. EMC effect is driven by **“local density”**

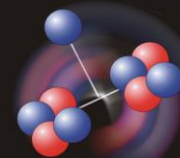
- SRCs are sensitive to high density configurations, but MUST remove the center of mass motion smearing to get R_{2N}
– *measure of correlated pairs relative to the deuteron*
- EMC effect samples *all* the nucleons, whereas R_{2N} is only sensitive to *np* pairs, a subset of all possible NN configurations
- If we’re going to use SRCs as a measure of local density, must scale R_{2N} by N_{total}/N_{iso} .

${}^4\text{He}$



Now that we have the relevant quantities, we can test the two hypotheses

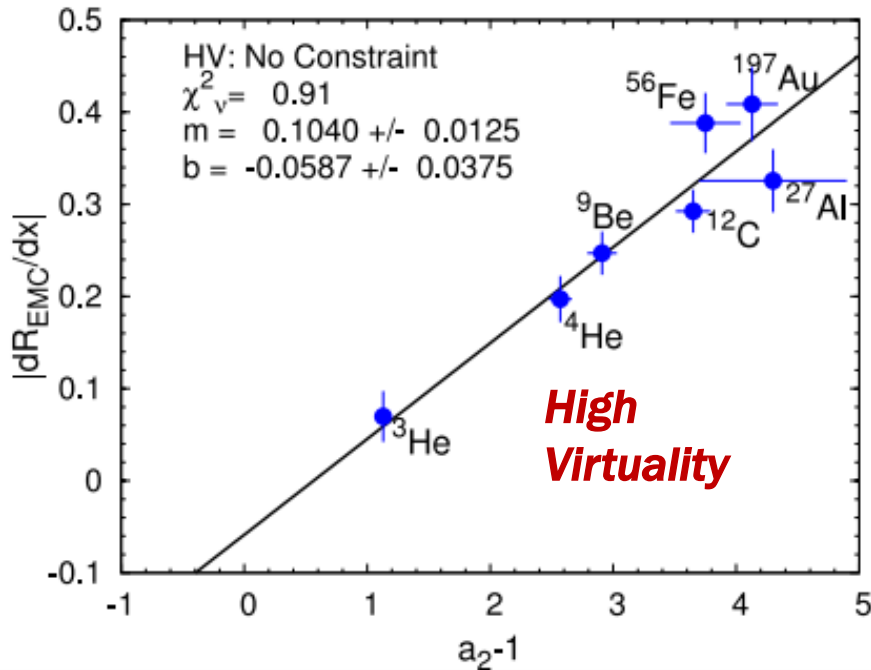
${}^9\text{Be}$



Two hypotheses

1. Both quantities reflect **virtuality** of the nucleons (L. Weinstein et al, *PRL* 106:052301,2011)

- a_2 is a measure of high momentum nucleons relative to the deuteron

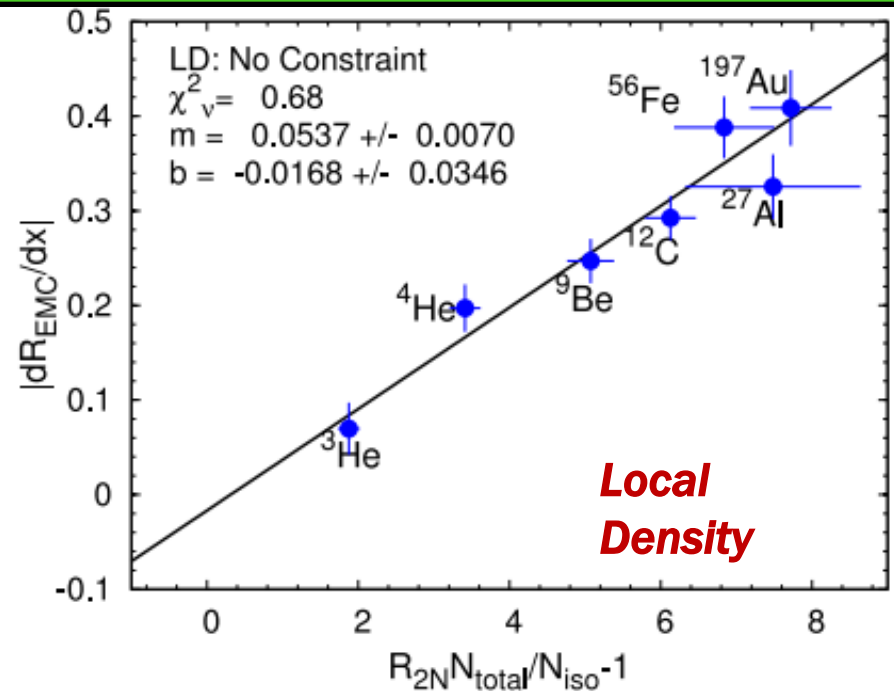


2. A measure of “**local density**”

$$R_{2N}$$

- measure of correlated pairs relative to the deuteron

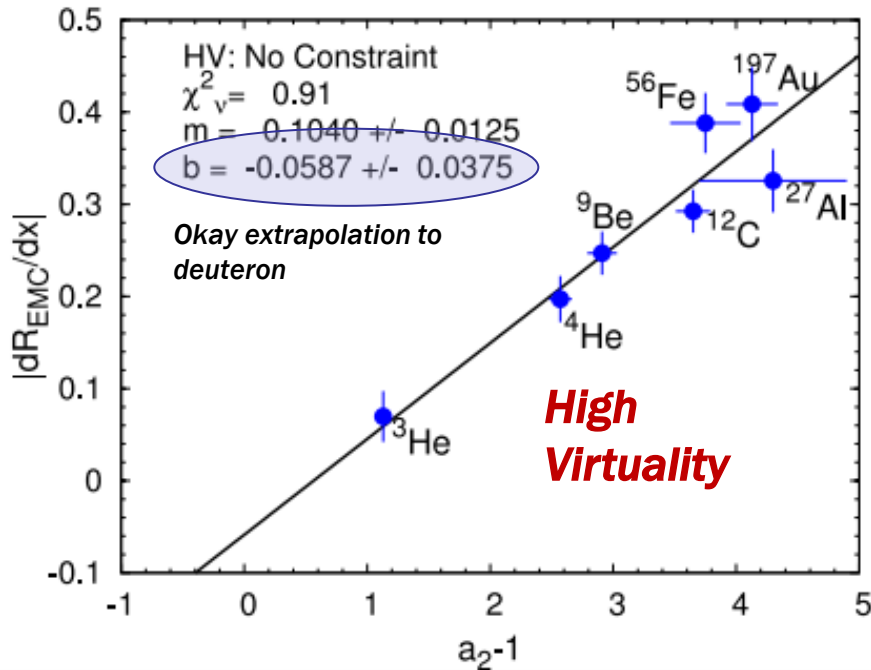
- Only sensitive to np pairs, scale by N_{total}/N_{iso}



Two hypotheses

1. Both quantities reflect **virtuality** of the nucleons (*L. Weinstein et al, PRL 106:052301,2011*)

- a_2 is a measure of high momentum nucleons relative to the deuteron

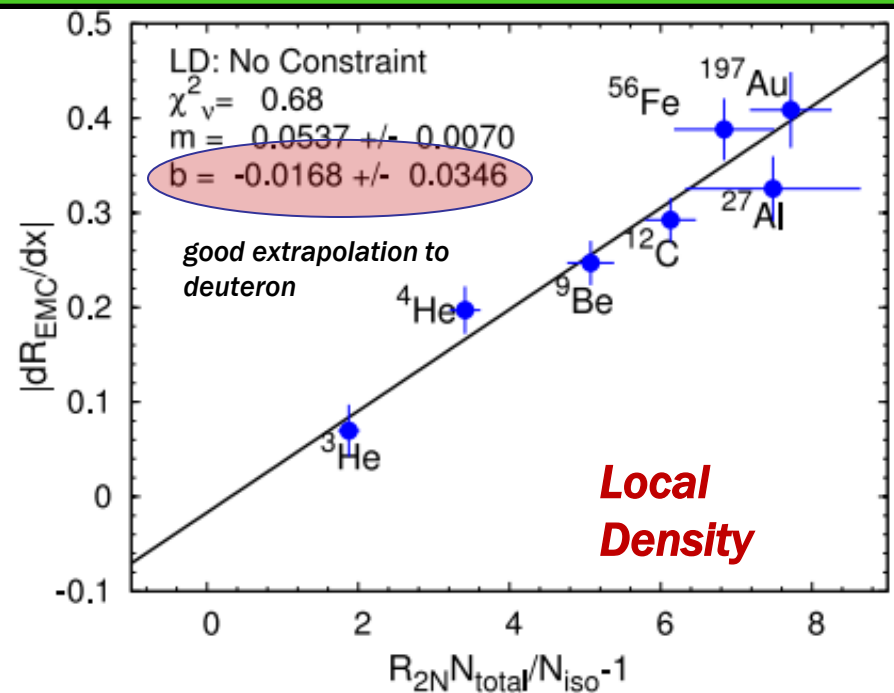


2. A measure of “**local density**”

$$R_{2N}$$

- measure of correlated pairs relative to the deuteron

- Only sensitive to np pairs, scale by N_{total}/N_{iso}



Hypothesis	Fit type	χ^2_v	EMC(D)	IMC(D)
High Virtuality	2-param No constraints	0.91	-0.0587±0.037	0.1040±0.012
High Virtuality	1-param	1.17	–	0.0856±0.004
High Virtuality	2-param D-constraint	1.14	-0.0041±0.010	0.0869±0.005
Local Density	2-param No constraints	0.68 (0.83)	-0.0168±0.035	0.0537±0.007
Local Density	1-param	0.61 (0.73)	–	0.0505±0.003
Local Density	2-param D-constraint	0.61 (0.73)	-0.0013 ±0.010	0.0508±0.003

Each hypothesis is tested with 3 types of fits:

- 1) 2-parameter linear fit, no deuteron constraint
- 2) 1-parameter fit, strict deuteron constraint
- 3) 2-parameter fit, deuteron constraint, partial accounting for correlated errors within a given experiment

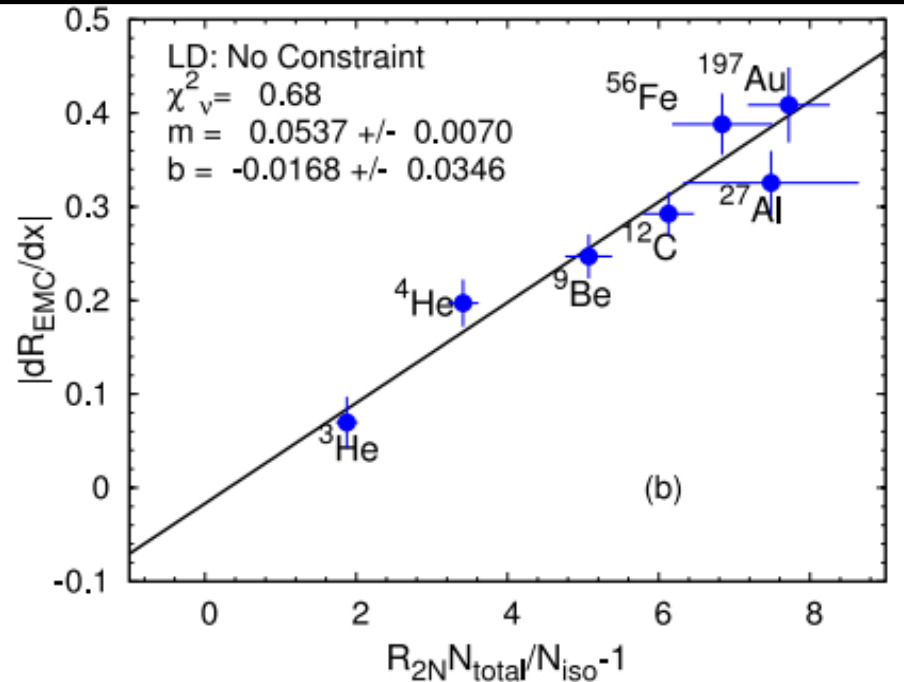
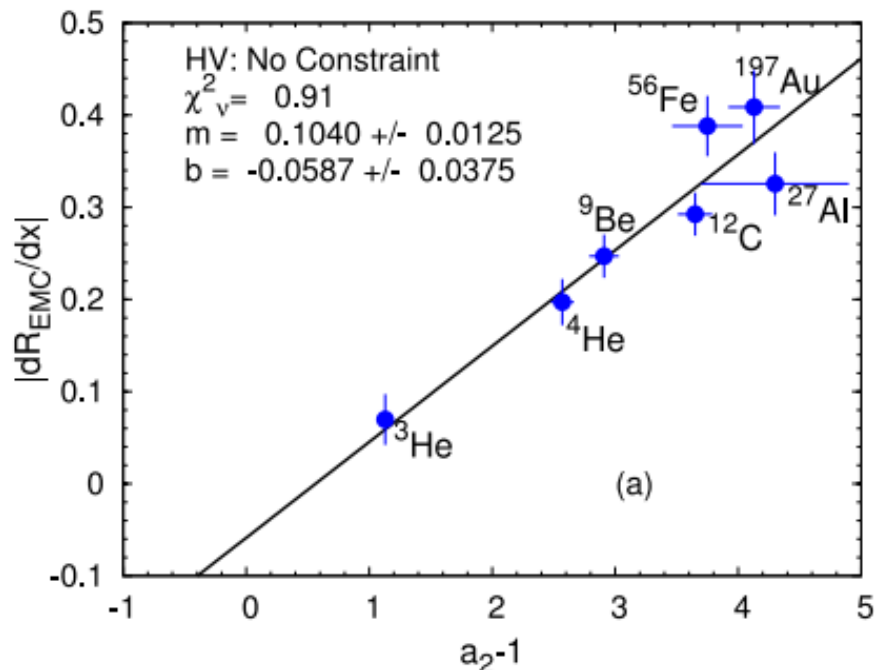
Hypothesis	Fit type	χ^2_{ν}	EMC(D)	IMC(D)
High Virtuality	2-param No constraints	0.91	-0.0587±0.037	0.1040±0.012
High Virtuality	1-param	1.17	–	0.0856±0.004
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Local Density	2-param No constraints	0.68 (0.88)	-0.0168±0.031	0.0537±0.007
Local Density	1-param	0.61 (0.73)	–	0.0505±0.003
Local Density	2-param D-constraint	0.61 (0.73)	-0.0013 ±0.010	0.0508±0.003

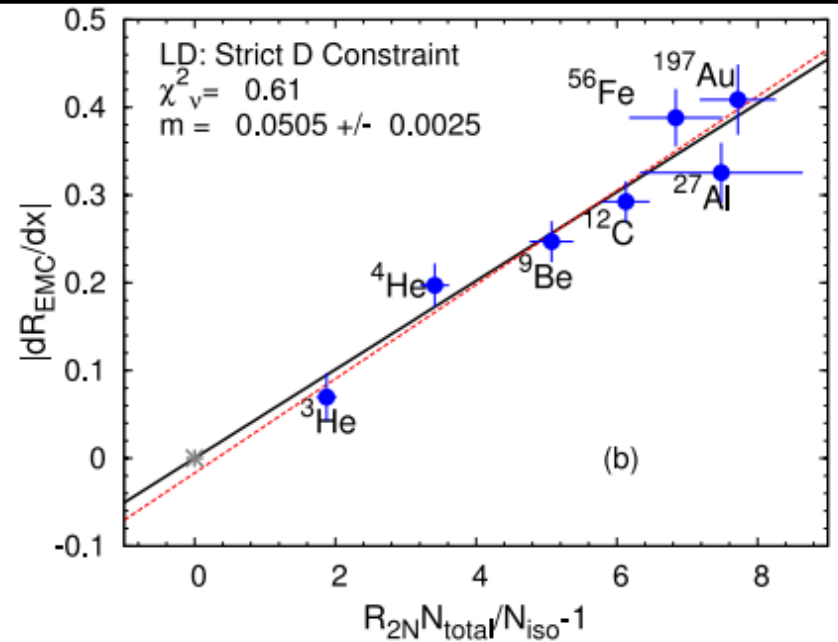
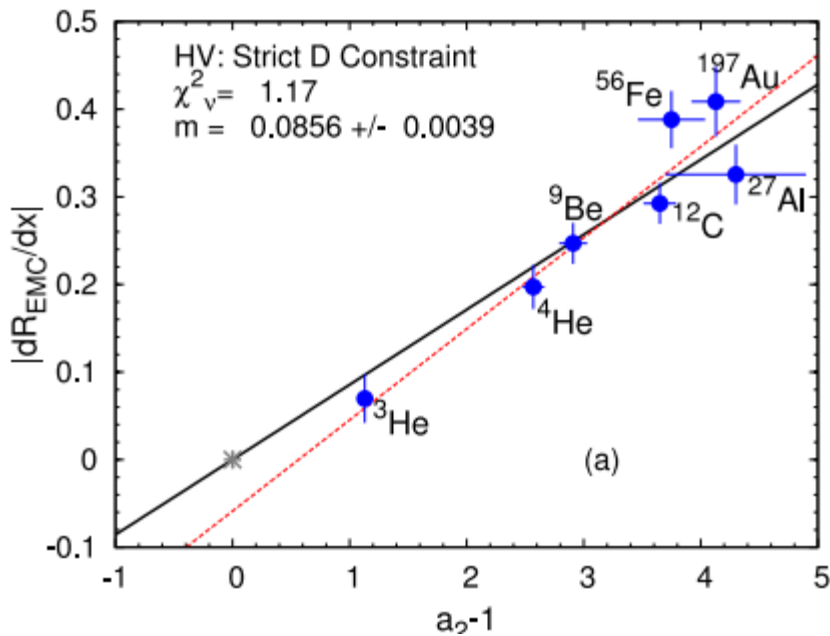
$$\left. \frac{dR_{IMC}}{dx} \right|_D = \left. \frac{dR_{EMC}}{dx} \right|_{a_2 = 0} - \left. \frac{dR_{EMC}}{dx} \right|_D$$

IMC effect → *in-medium correction effect, the ratio of the DIS cross section per nucleon bound in a nucleus relative to the free (unbound) pn pair cross section*

Hypothesis	Fit type	χ^2_v	EMC(D)	IMC(D)
High Virtuality	2-param No constraints	0.91	-0.0587 ± 0.037	0.1040 ± 0.012
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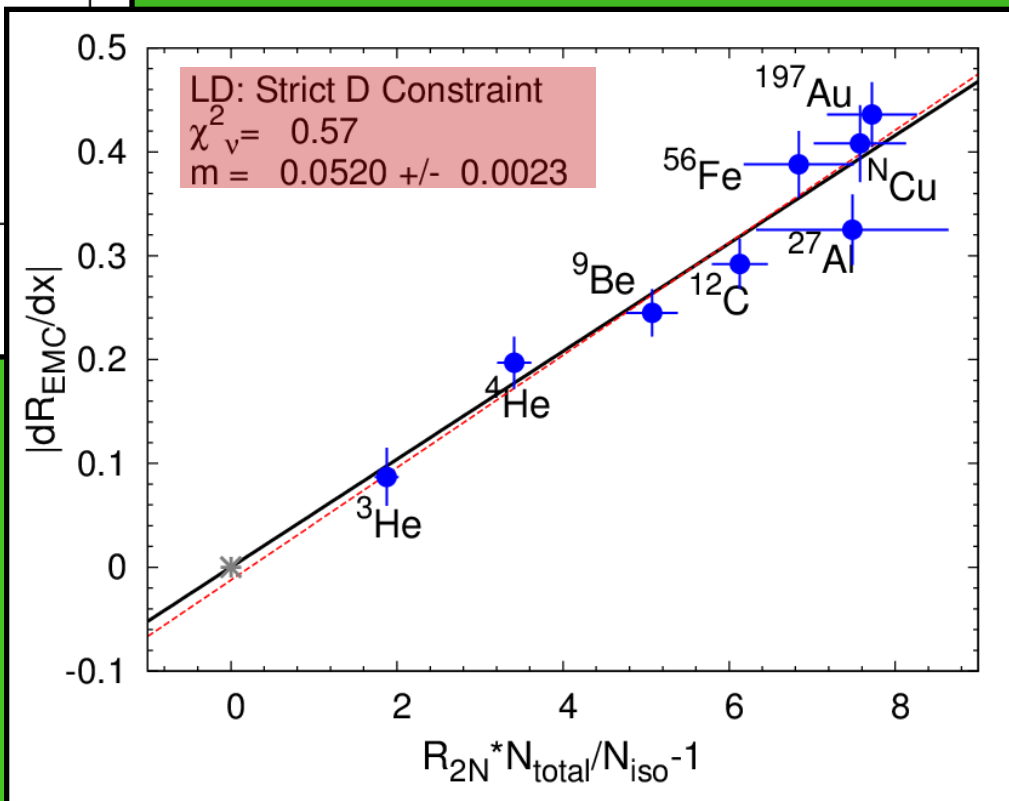
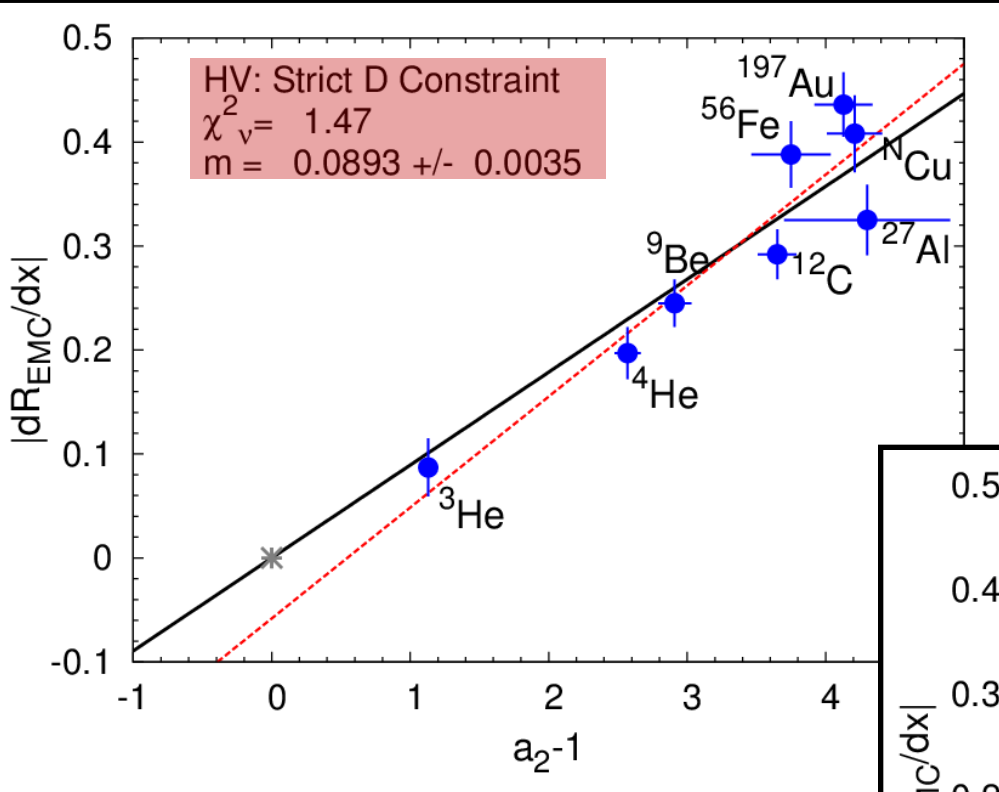


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<i>Local Density</i>	<i>1-param</i>	<i>0.61 (0.73)</i>	–	<i>0.0505 ± 0.003</i>
<i>Local Density</i>	<i>2-param</i>	<i>0.61 (0.73)</i>	<i>-0.0013 ± 0.010</i>	<i>0.0508 ± 0.003</i>



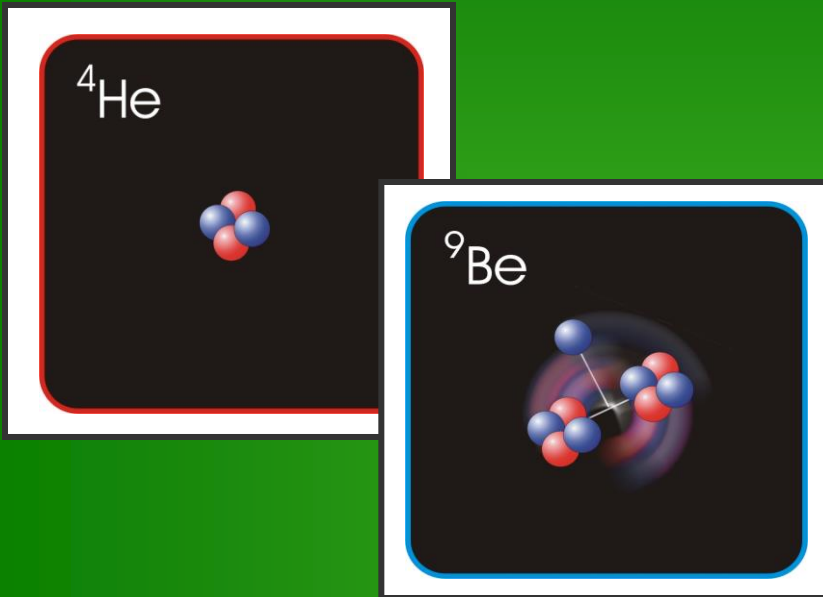
New Data are helping and more data will help even further

Heavy target data from Jlab
E03-103 (Cu, Au)

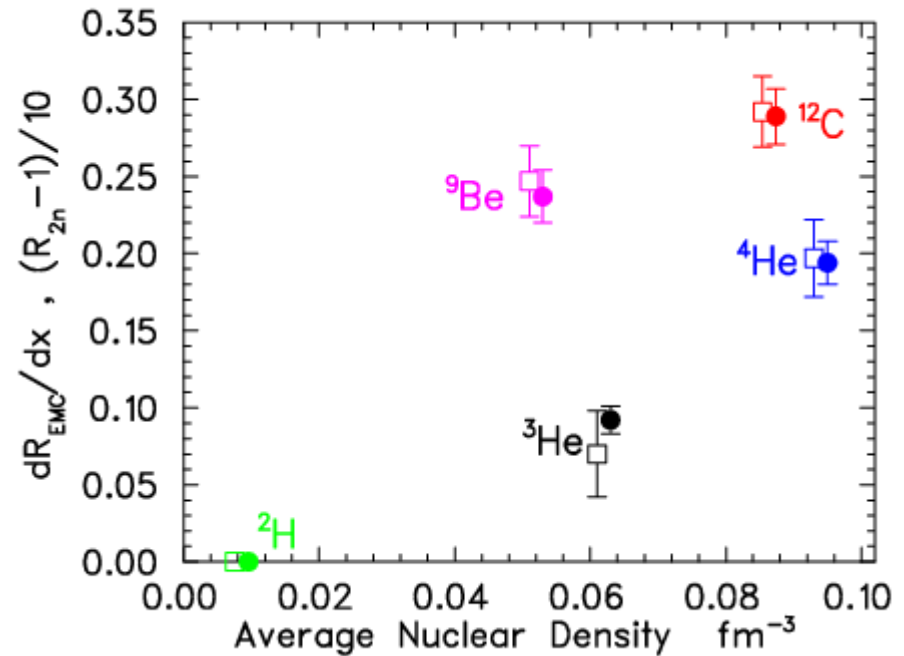


Compare χ^2 of **1.47** and **0.57**
 to χ^2 of **1.14** and **0.61**,
 respectively

Why local density?



- SRCs mirror same behavior

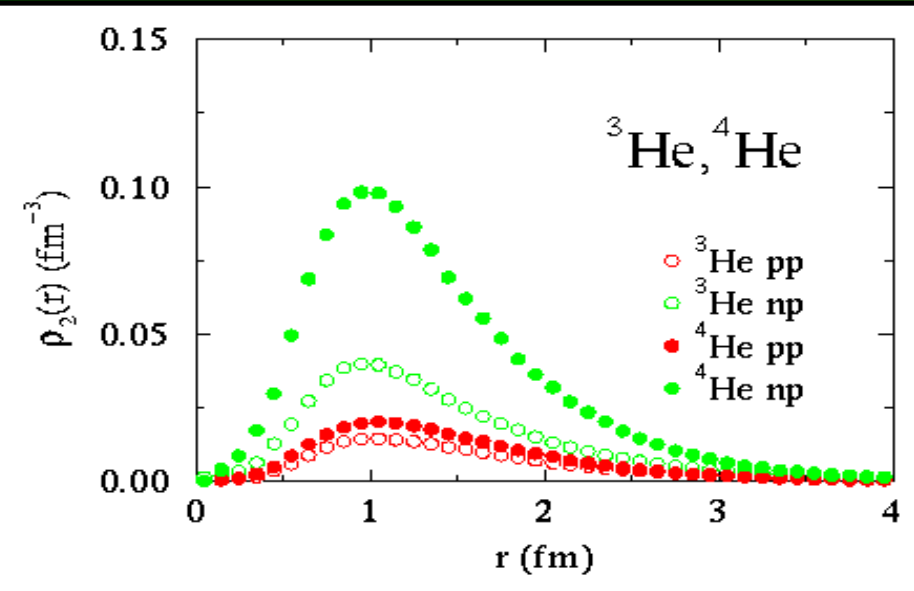
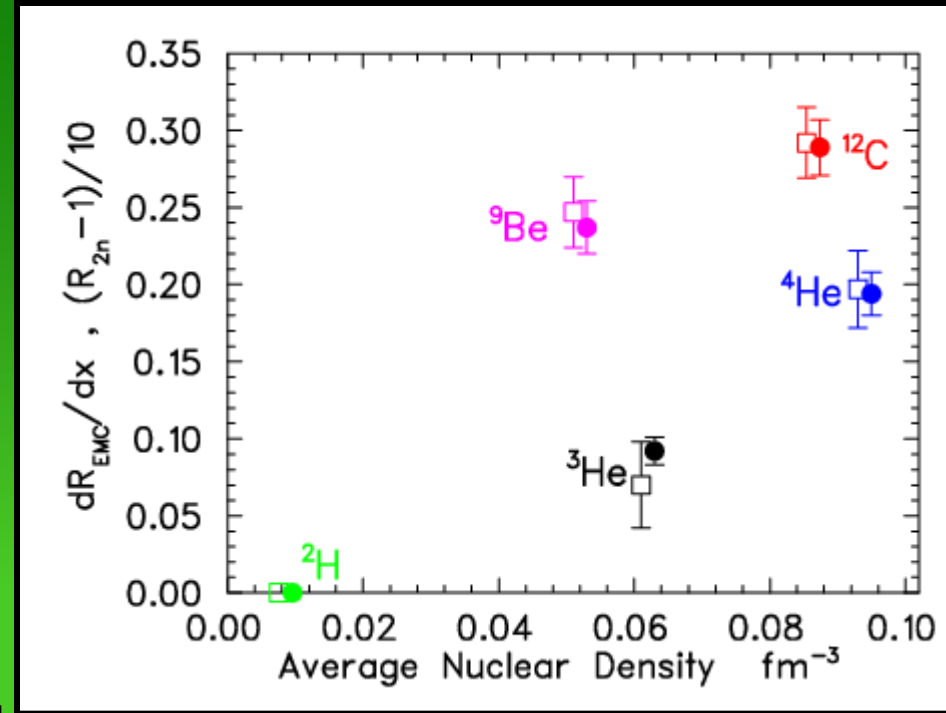
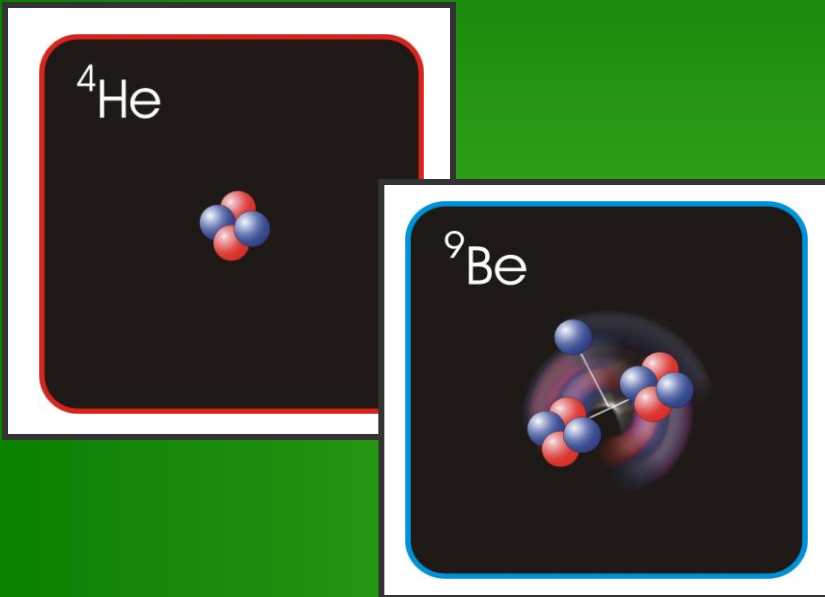


Nucleons can have significant overlap before feeling the repulsive force

We can calculate this overlap using 2-body density distributions via

$$\int_0^\infty W(r) \rho_2^{NN}(r) d^3r$$

Why local density?

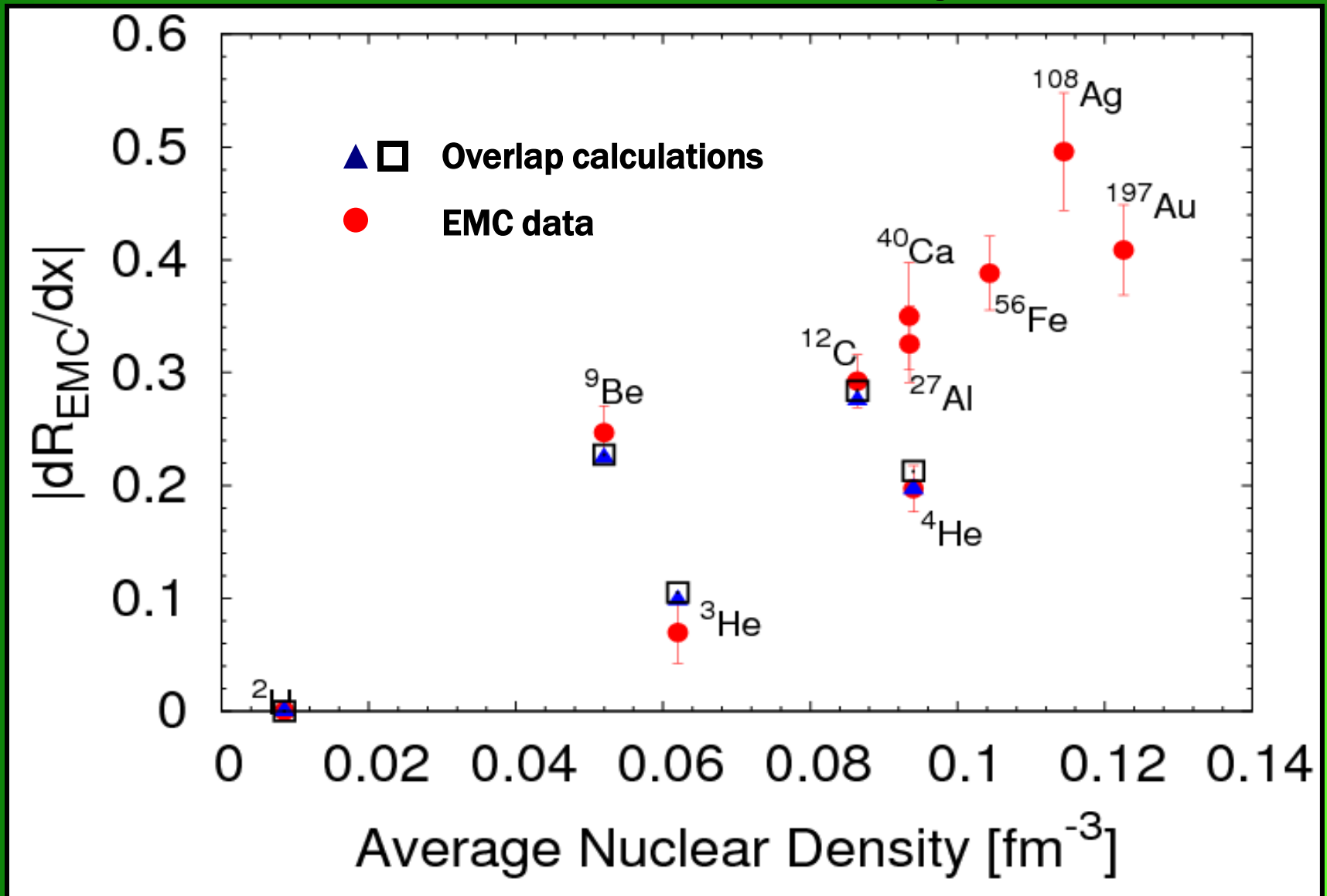


Nucleons can have significant overlap before feeling the repulsive force

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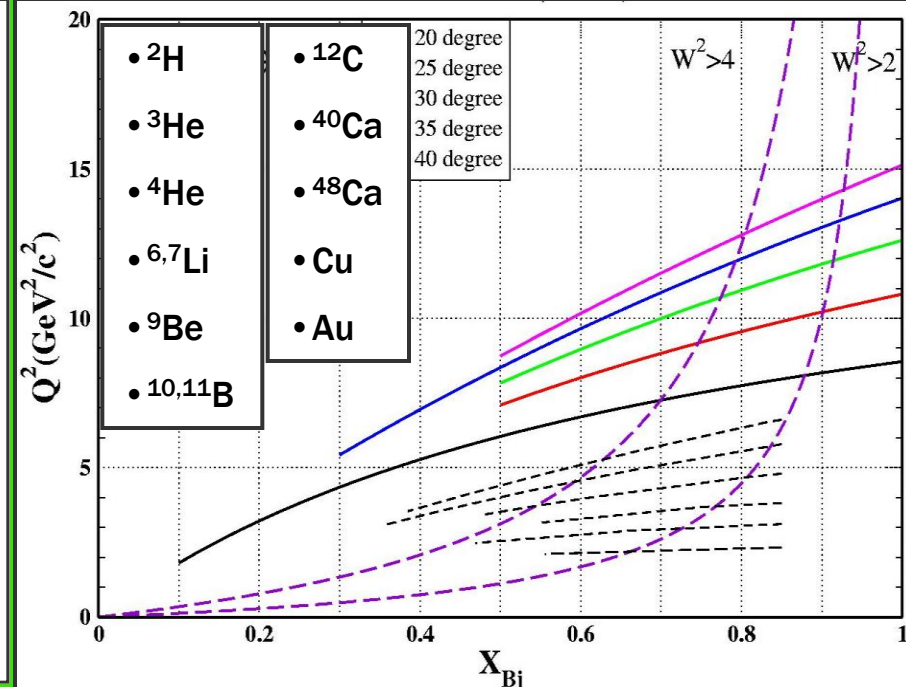
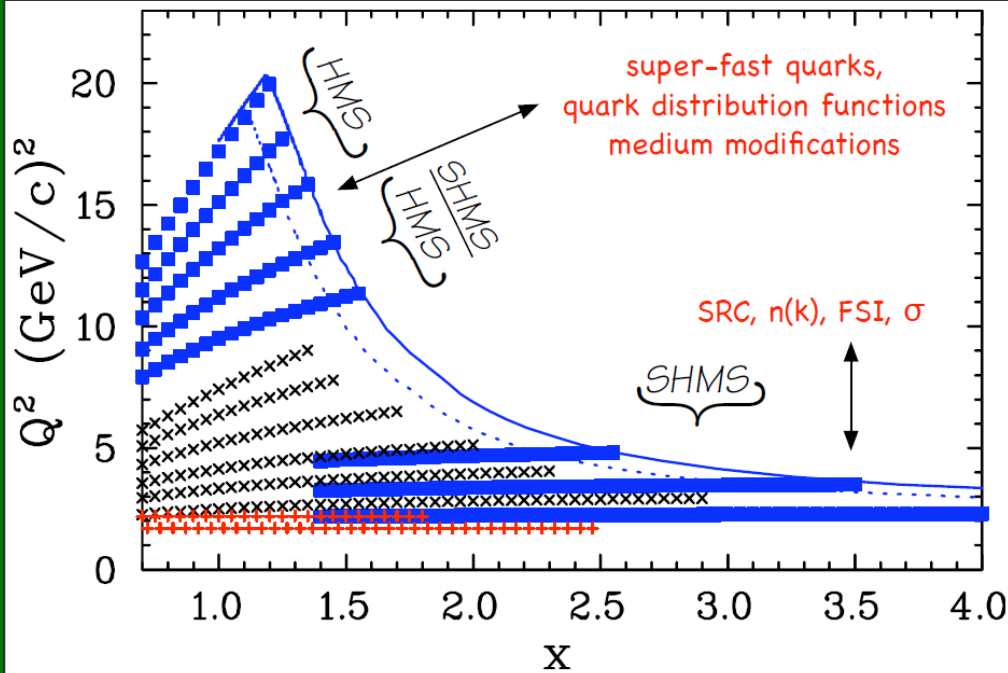
$$\int_0^\infty W(r) \rho_2^{NN}(r) d^3r$$

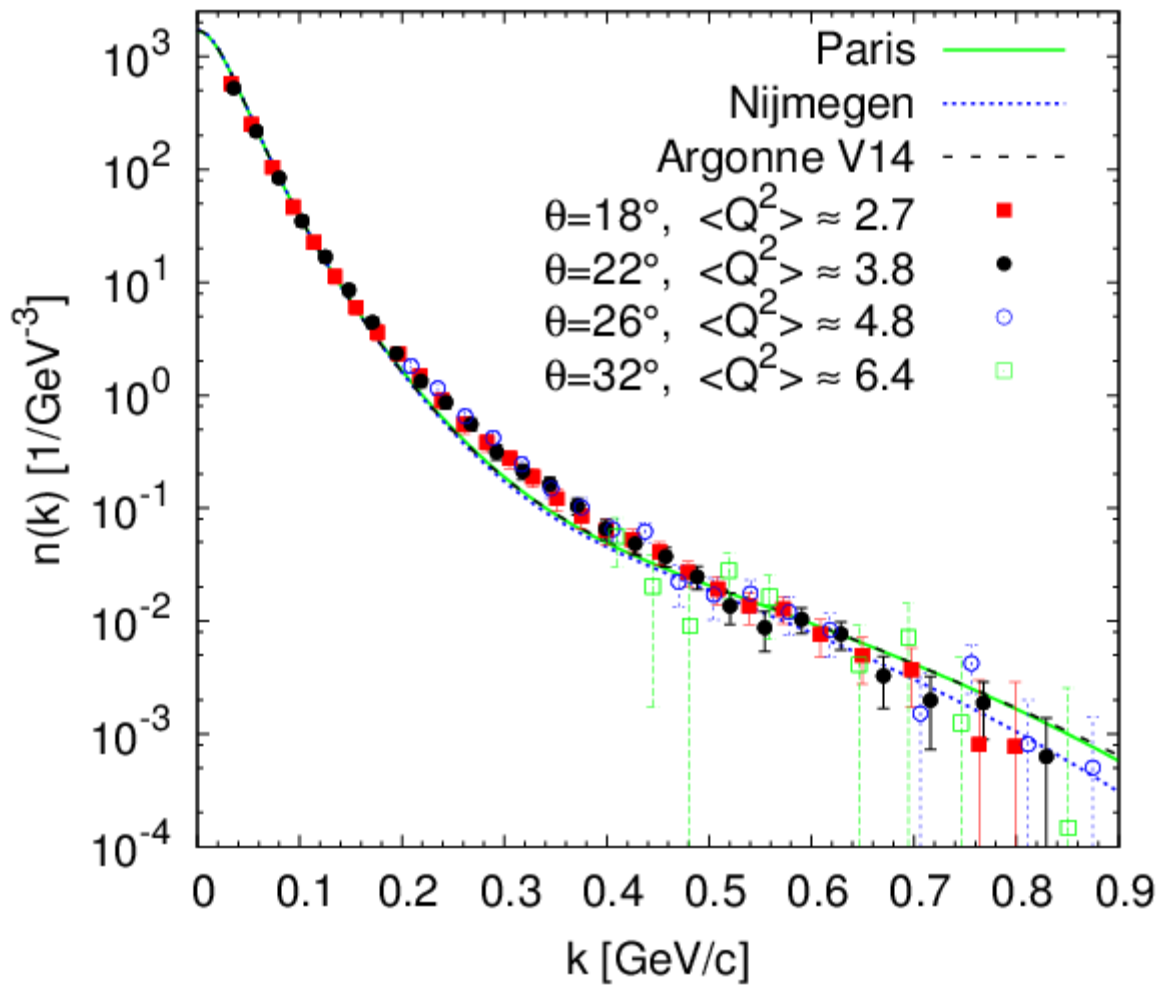
NN Overlap exhibits same density dependence



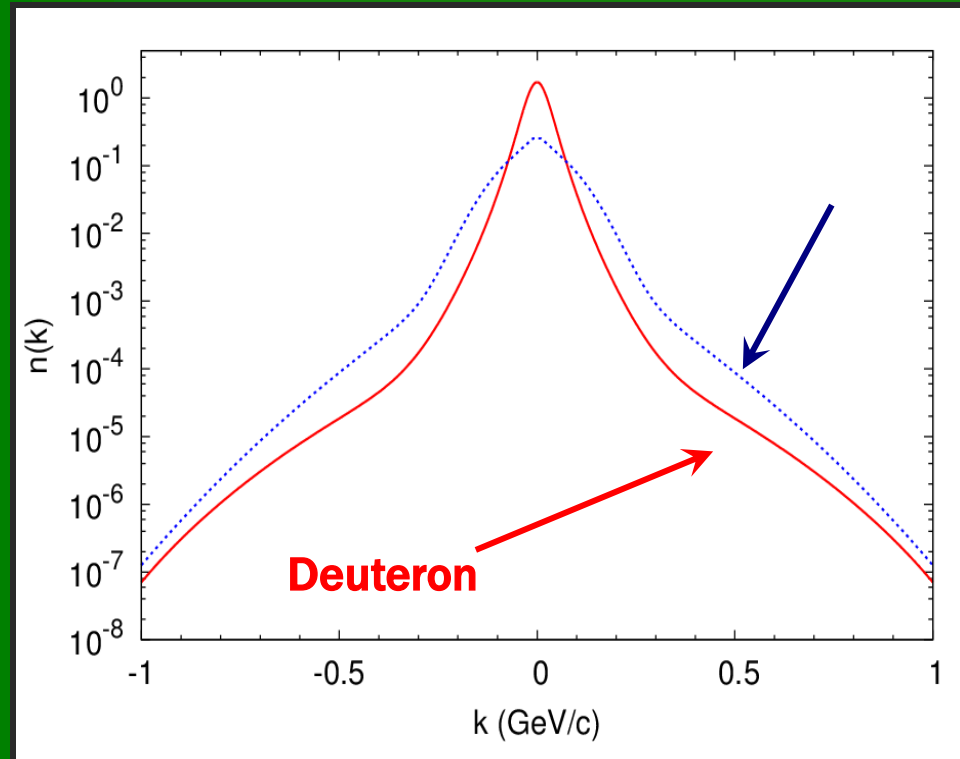
Summary

- New results suggest a local density dependence of the EMC effect as well as SRCs
- These hints and suggestions need to be further investigated with new experiments, focusing on light targets
 - E12-06-105 ($x > 1$) approved at Jlab
 - E12-10-008 (EMC effect) approved at Jlab

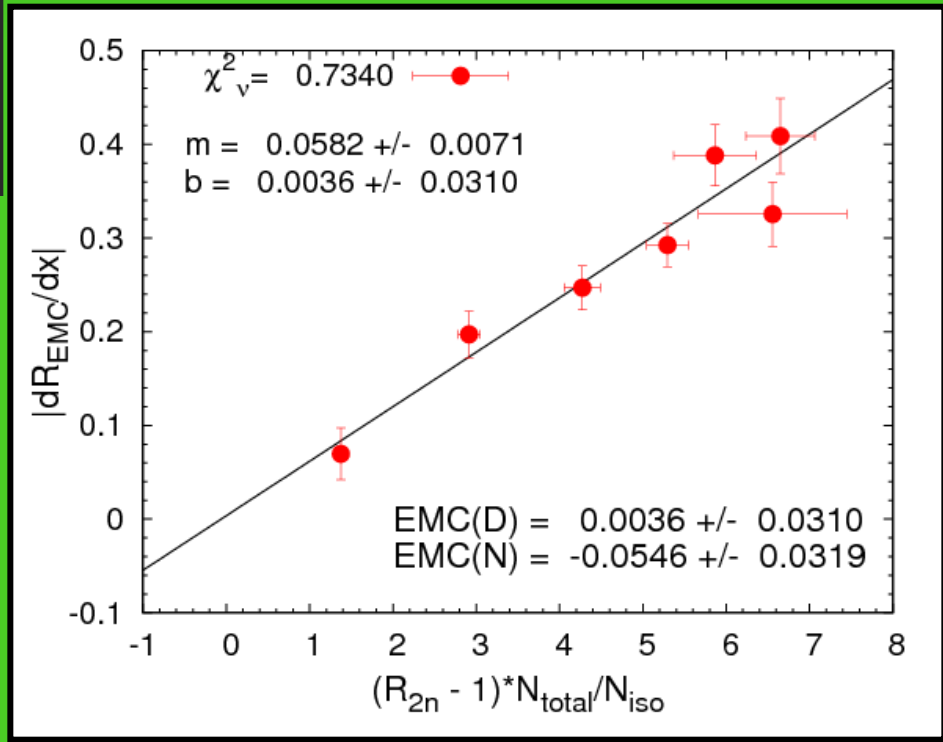




Two hypotheses



$$R_{2N} = a_2 / \frac{n_D^{CONV}(k)}{n_D(k)}$$

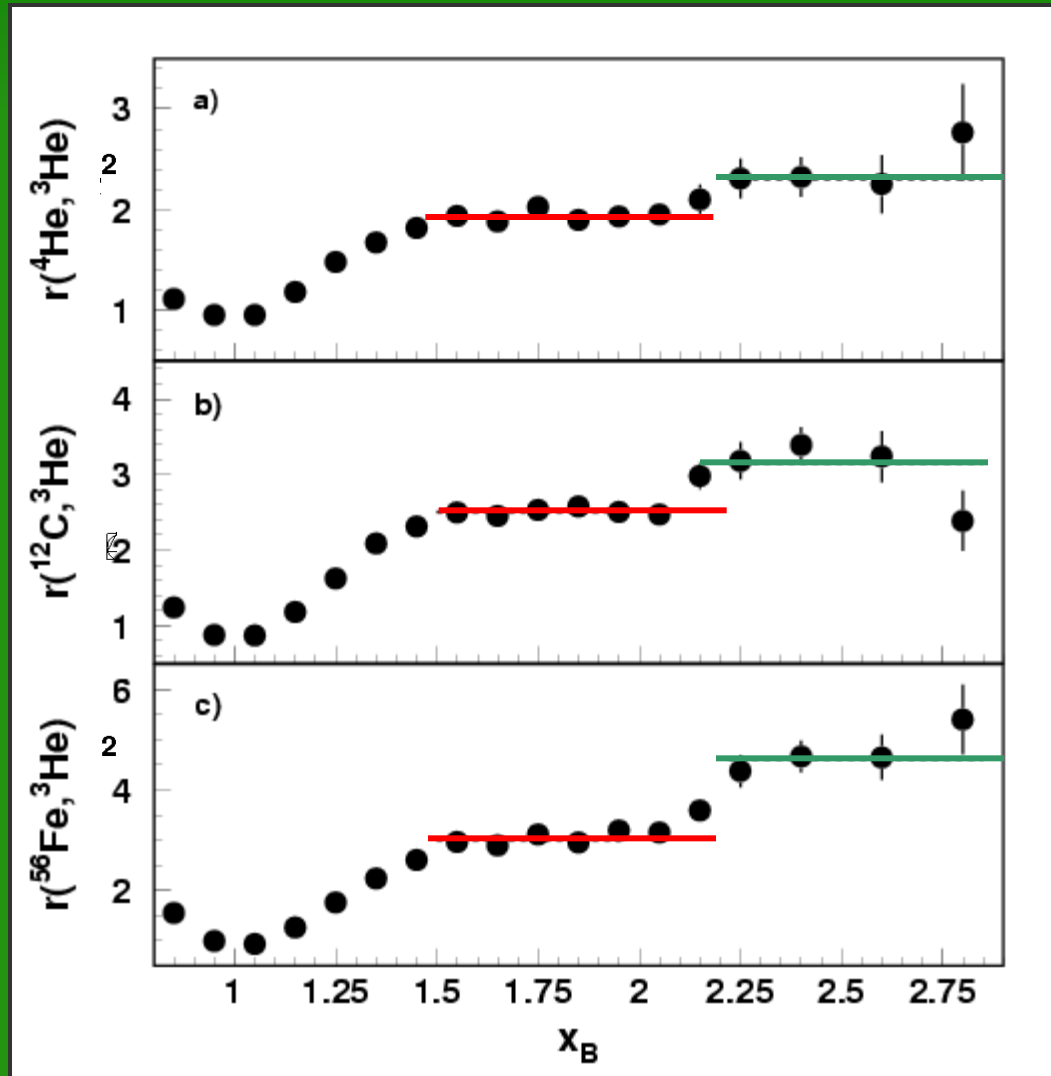


2. A measure of “local density”

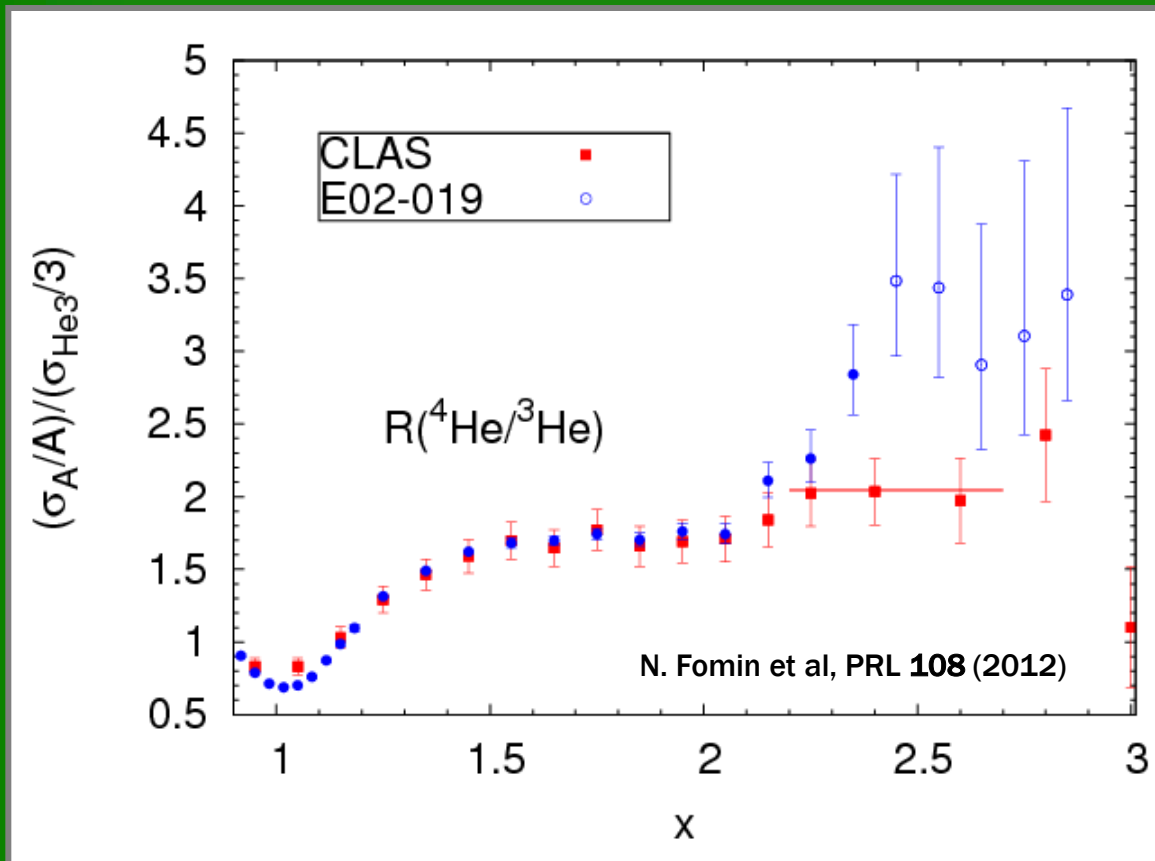
R_{2n}

- measure of correlated pairs relative to the deuteron
- Only sensitive to np pairs, scale by N_{total}/N_{iso}

Short Range Correlations – 3N



E02-019 Ratios



$\langle Q^2 \rangle$ (GeV²)

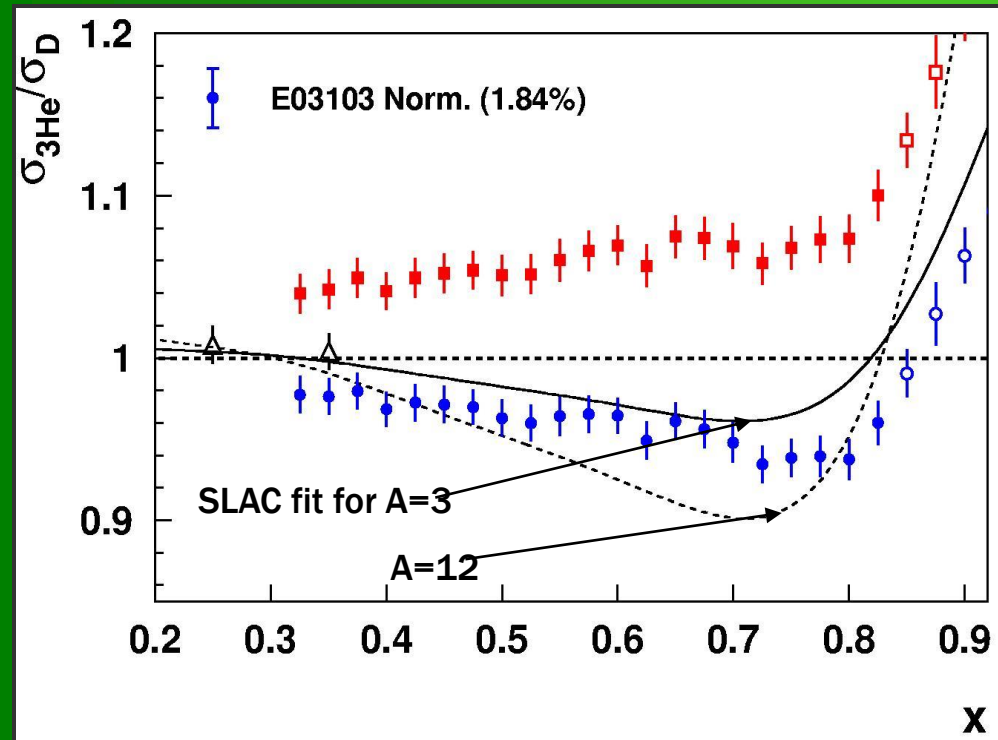
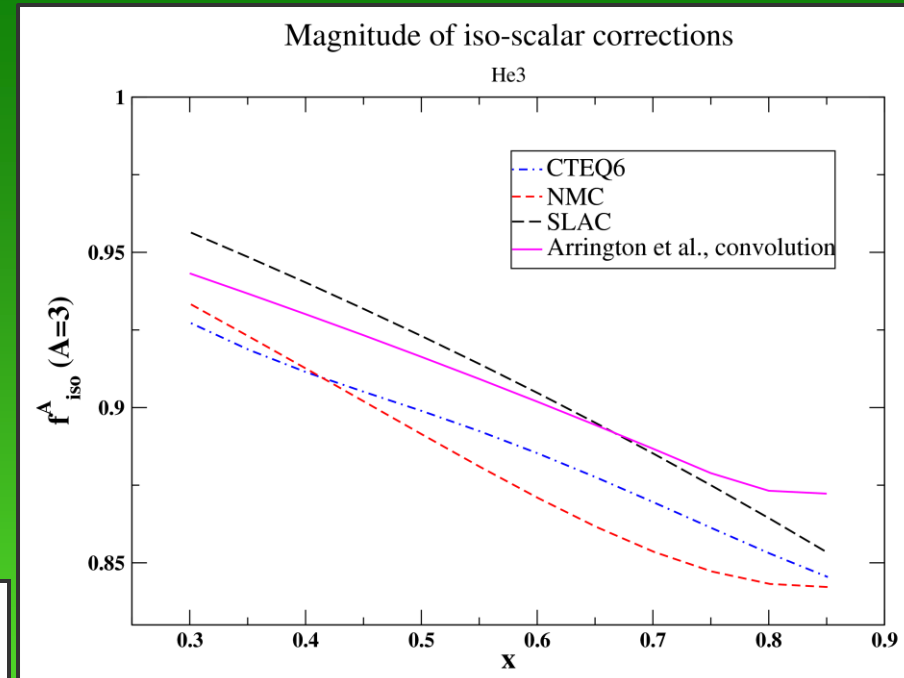
CLAS: 1.6

E02-019: 2.7

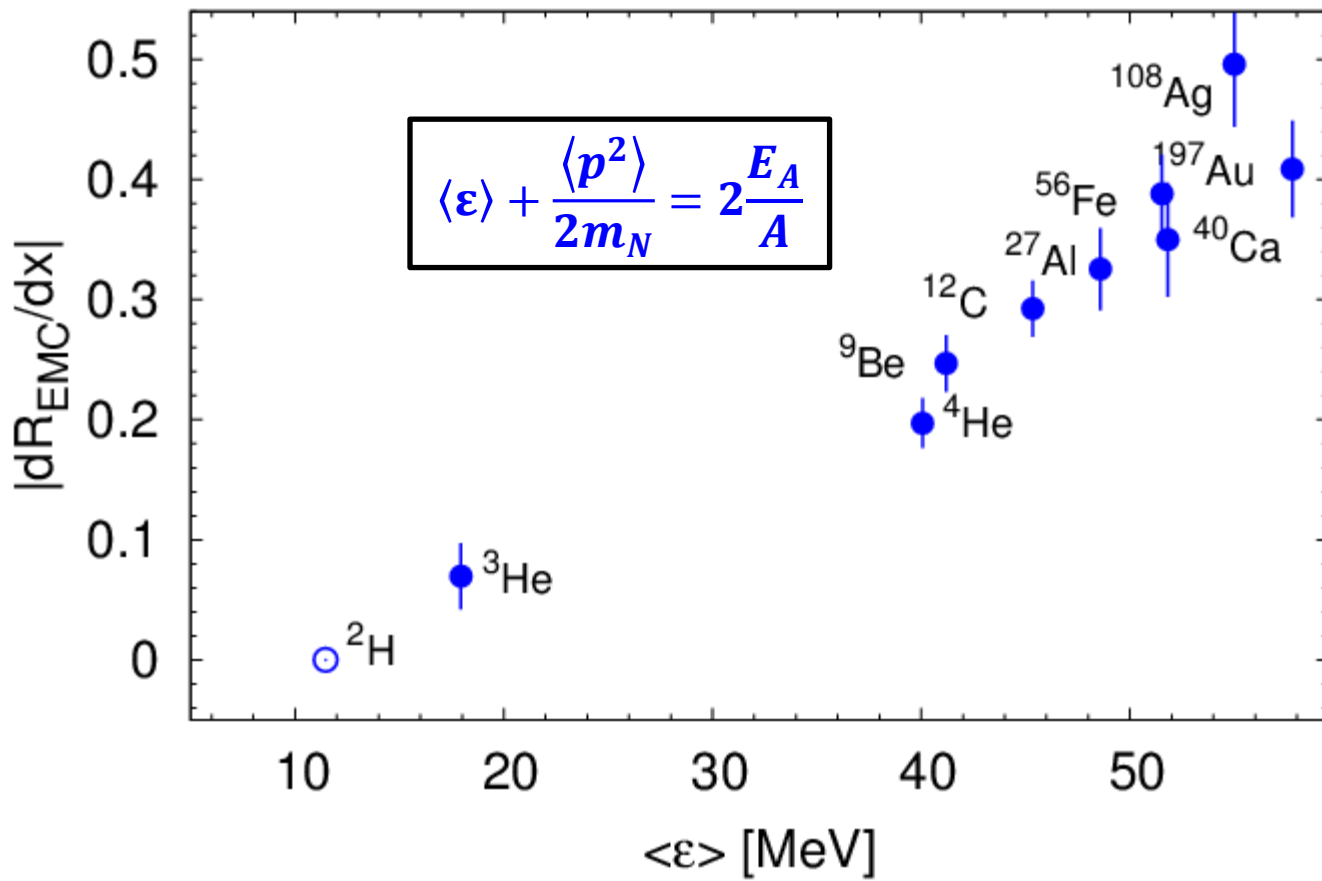
- Excellent agreement for $x \leq 2$
- Very different approaches to 3N plateau, later onset of scaling for E02-019
- Very similar behavior for heavier targets

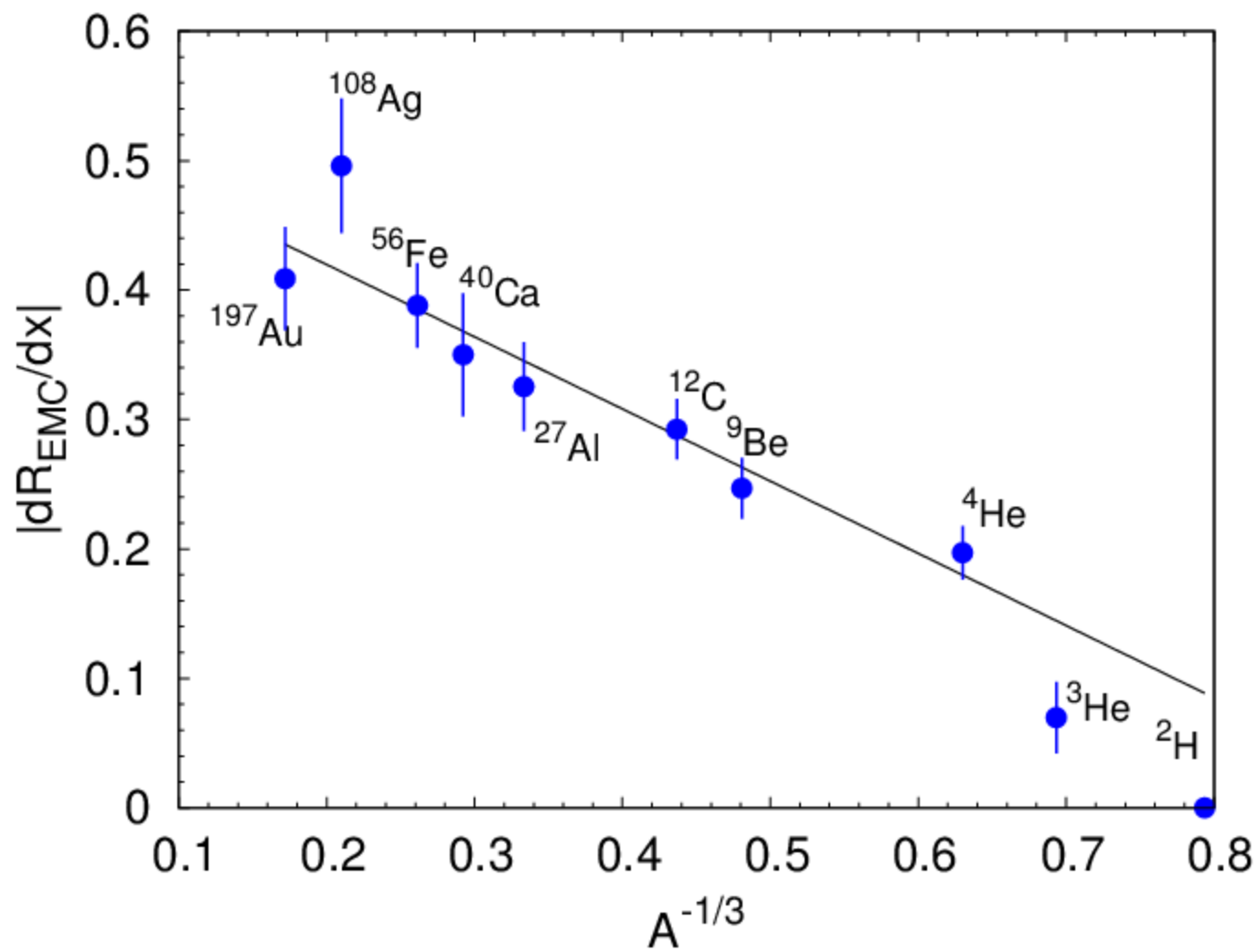
Isoscalar Correction if $Z \neq P$

$$Cor_{iso} = \frac{(Z\sigma_p + N\sigma_n)/A}{(\sigma_p + \sigma_n)/2}$$



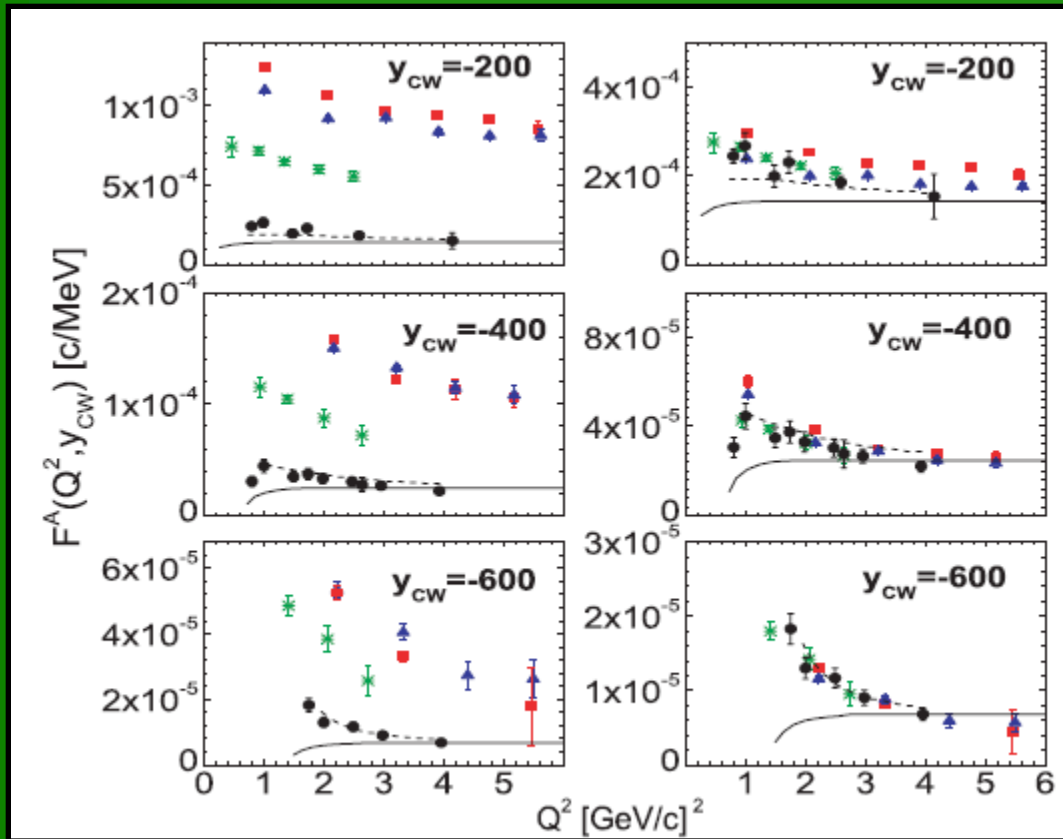
- No free neutron target \rightarrow extraction of F_2^n/F_2^p is model-dependent
- For E03-103, F_2^n/F_2^p for bound nucleons was used





Rescaling of the Deuteron

$$F_A(y) = C_n F_D(y)$$



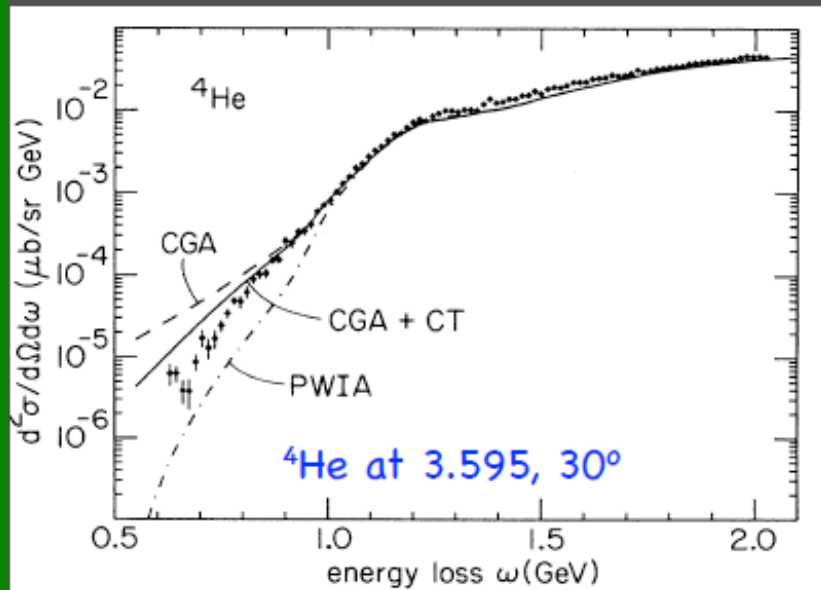
FSI in $A > 2$ are identical to those in the deuteron, and match calculations

Ciofi degli Atti, Mezzetti, PRC79

$F_A(y)$

$F_A(y)/C_n$

Overestimate of cross sections



Benhar et al. PRC 44, 2328

Benhar, Pandharipande, PRC 47, 2218

Benhar et al. PLB 3443, 47

