

# Role of short-range (and tensor) correlations in finite nuclei and nuclear matter

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WashU in St. Louis

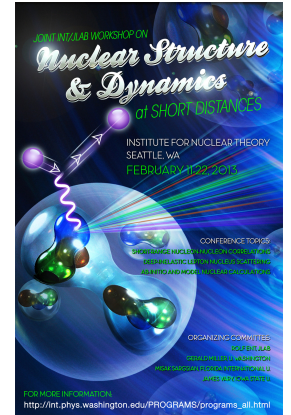
Hossein Mahzoon

Seth Waldecker

Helber Dussan

Bob Charity

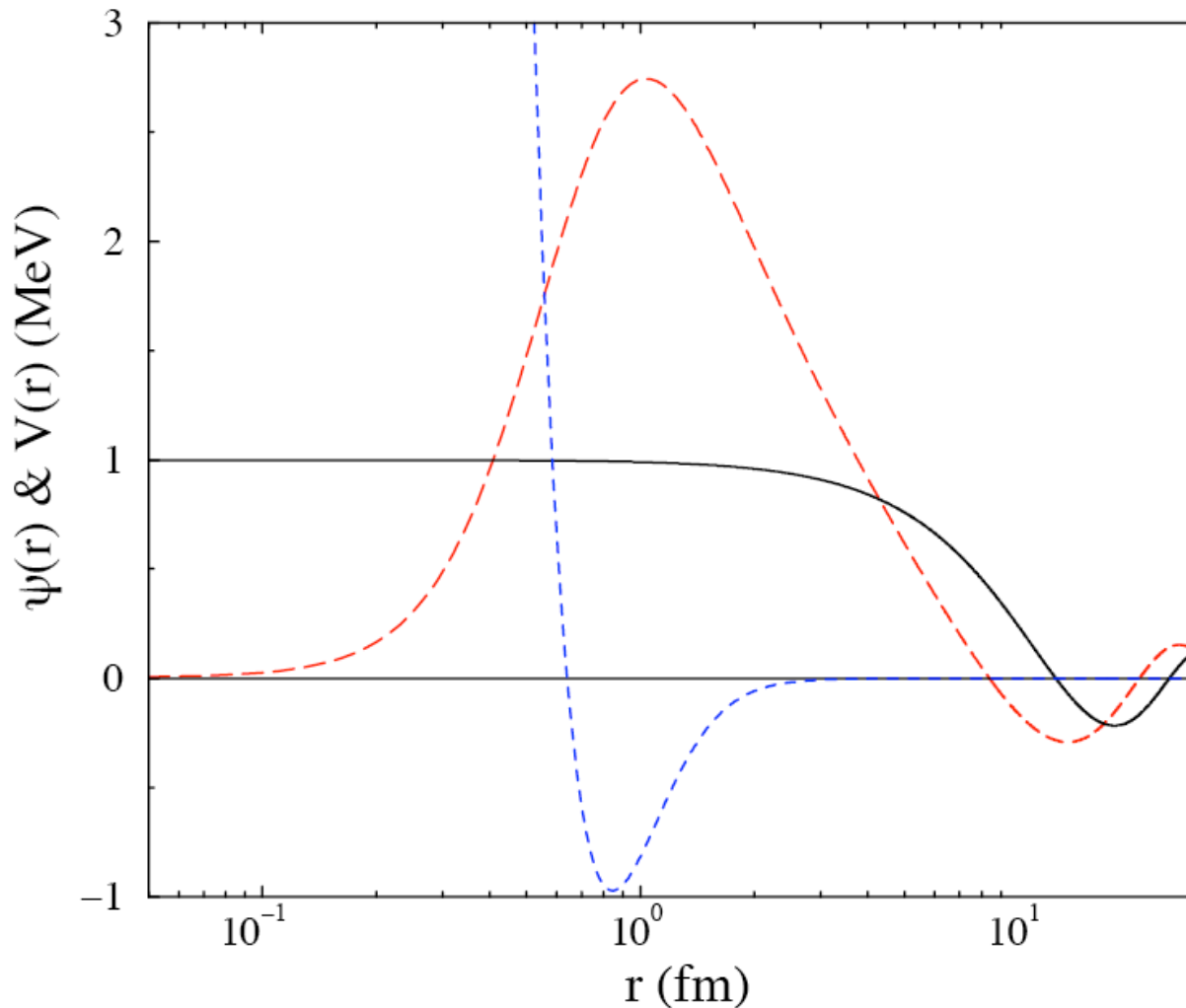
Wim Dickhoff



- SRC for two nucleons
- Review of older insights
- Recent self-consistent Green's functions calculations at finite T
  - Nuclear matter: symmetric and pure neutron matter
  - Asymmetric matter
- Finite nuclei with SRC from a Green's function calculation
  - Ab initio
- Dispersive Optical Model (Framework of Green's functions  $\leftrightarrow$  data)
- Conclusions and Outlook

Short-range and Tensor Correlations

# Repulsive core and wave function $\Rightarrow$ high-momenta



Reid  $^1S_0$   
 $k_0 = 0.25 \text{ fm}^{-1}$   
 $\sim \text{few MeV}$

$V(r)/100$

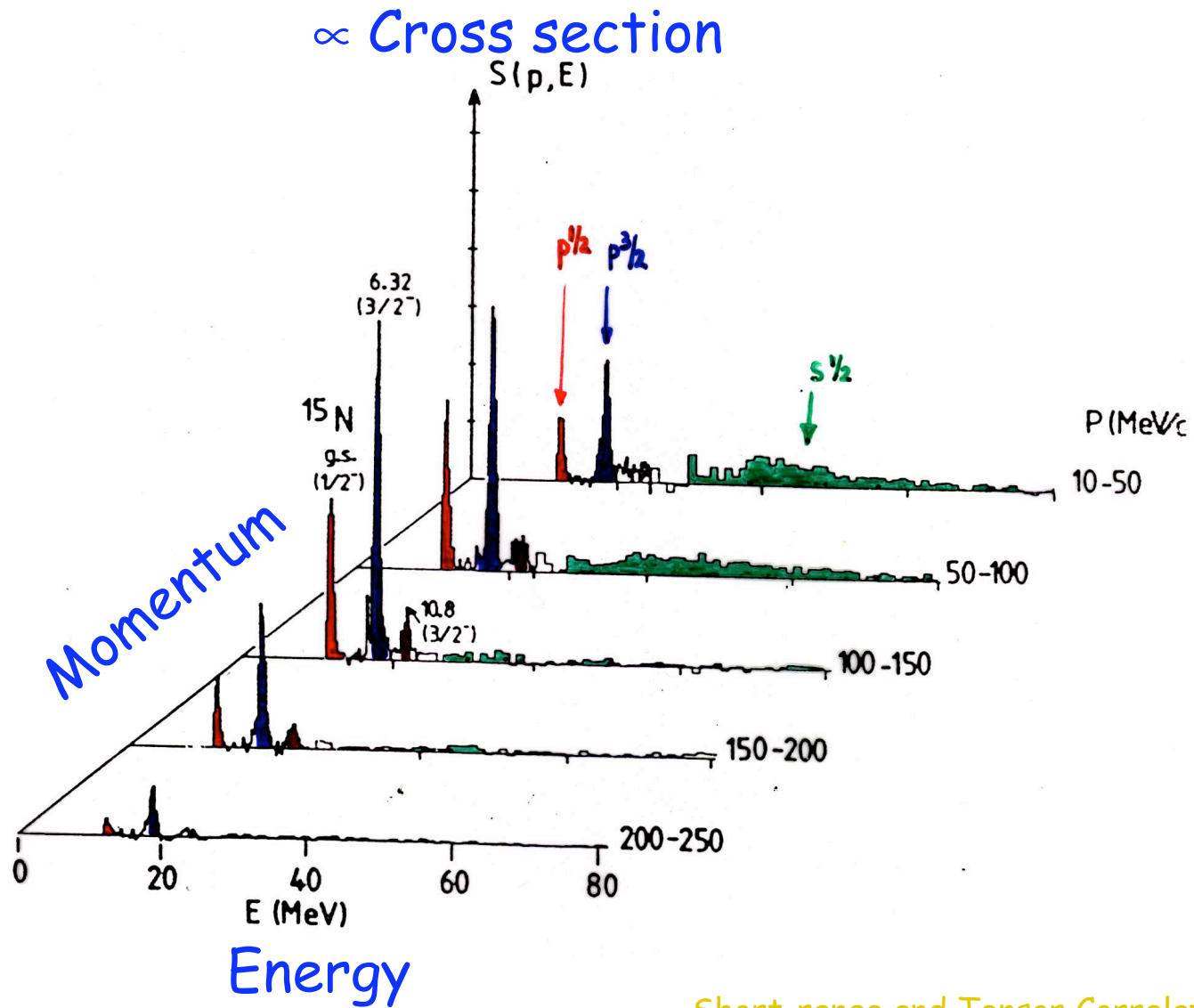
$\sin(k_0 r)/k_0 r$

correlated wf  
for a "hard"  
interaction

Short-range and Tensor Correlations

Mougey et al., Nucl. Phys. A335, 35 (1980)

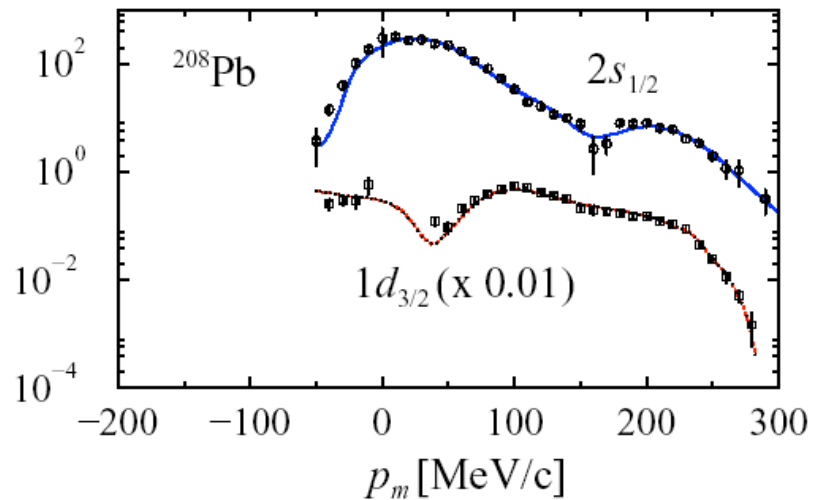
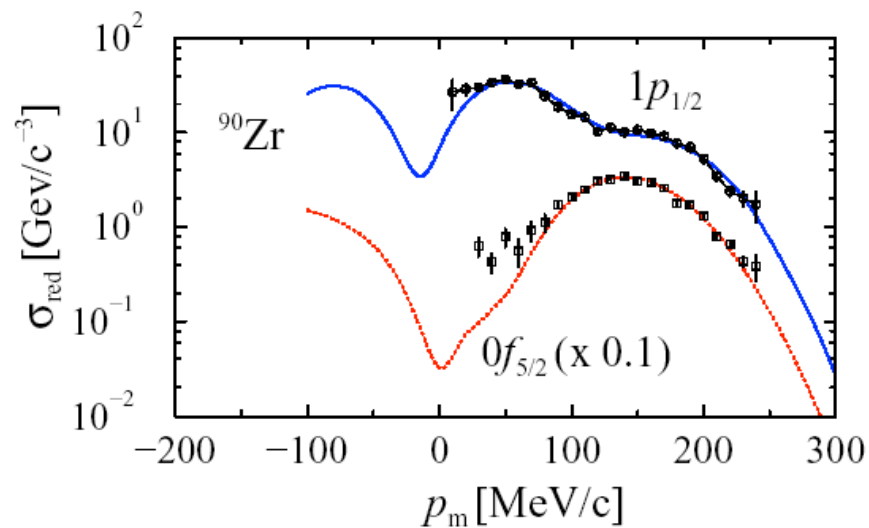
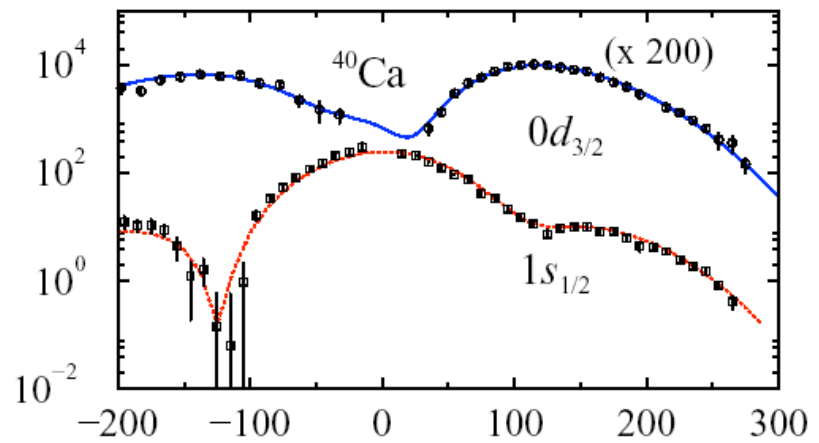
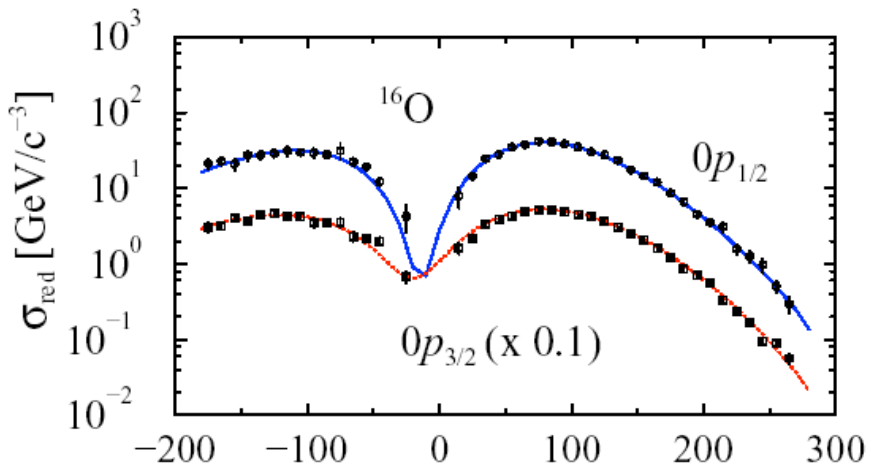
$^{16}\text{O}(e,e'p)$



Short-range and Tensor Correlations

# Nuclei (e,e'p) reaction

NIKHEF data, L. Lapikás, Nucl. Phys. A553, 297c (1993)



Wave functions as expected, except .... Short-range and Tensor Correlations

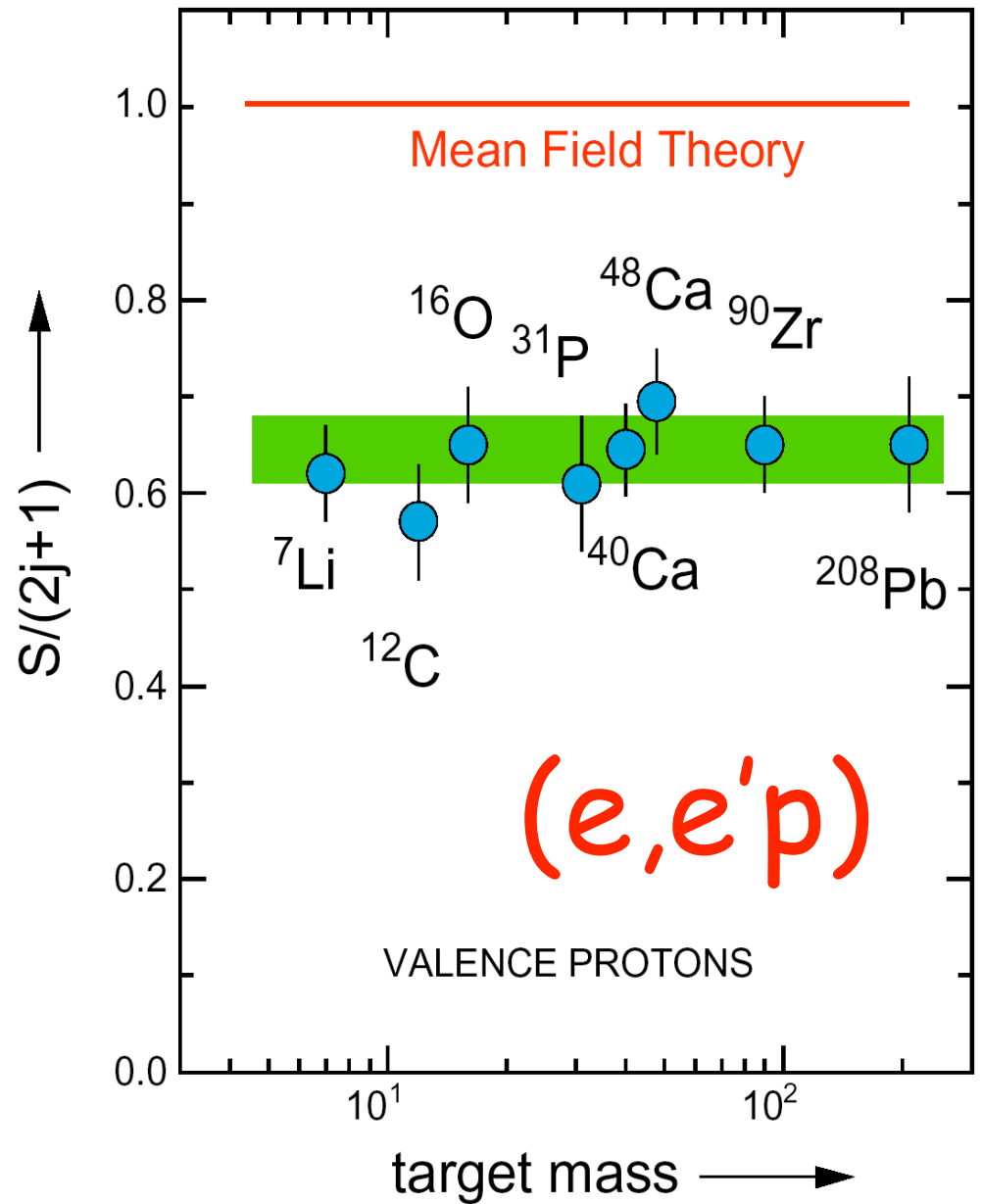
# Removal probability for valence protons from NIKHEF data

L. Lapikás, Nucl. Phys. A553,297c (1993)

$S \approx 0.65$  for valence protons  
Reduction  $\Rightarrow$  both SRC and LRC

Weak probe but propagation in the nucleus of removed proton using standard optical potentials to generate distorted wave  $\rightarrow$  associated uncertainty  $\sim 5-10\%$

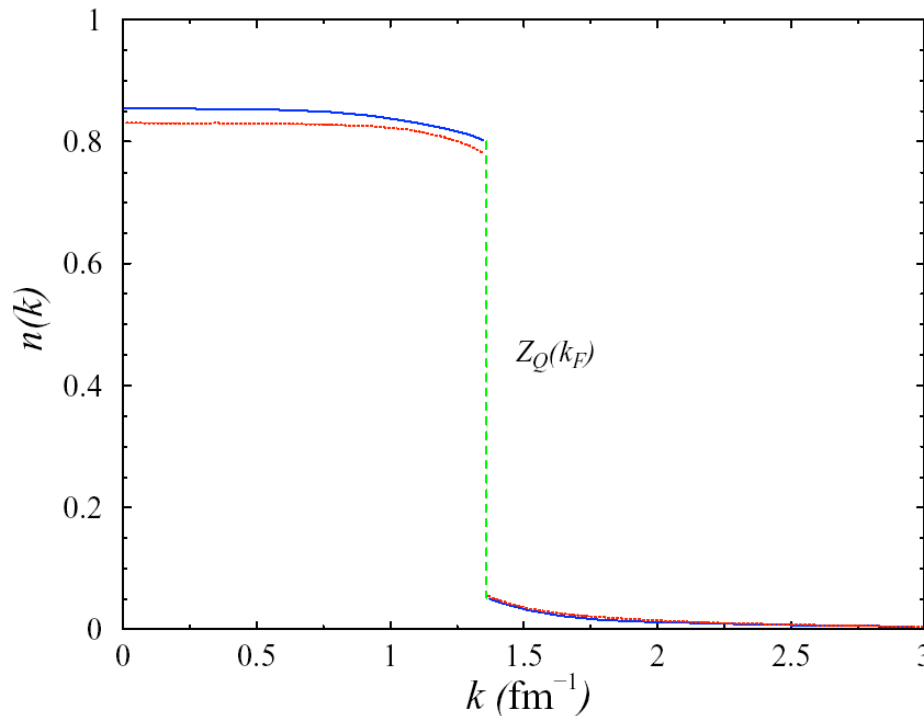
Why: details of the interior scattering wave function uncertain since non-locality is not constrained (so far)



Short-range and Tensor Correlations

# Short-range correlations in nuclear matter and $n(k)$

$n(k=0) = 0.83 / 0.85 \Rightarrow$  finite nuclei



$$n(k) = \int_{-\infty}^{\varepsilon_F} dE S_h(k; E)$$

Reid soft core  $k_F = 1.36 \text{ fm}^{-1}$

Old prediction!

Self-consistent result

$$Z_Q(k_F) = 0.72$$

$$Z_Q(k_F) = 0.75$$

$k < k_F$  : 17%  $> \varepsilon_F$  with 13% above 100 MeV (7% above 500 MeV)

Without tensor force only 10.5% above  $\varepsilon_F$

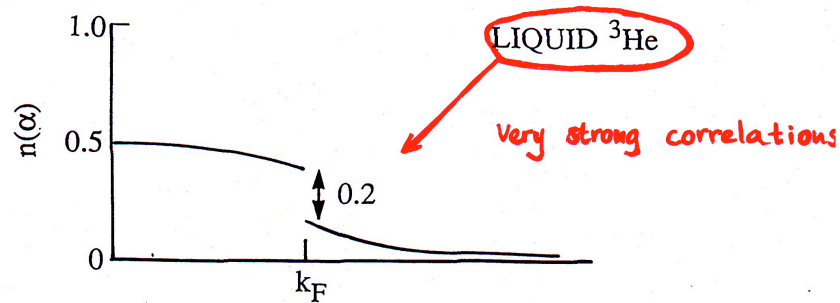
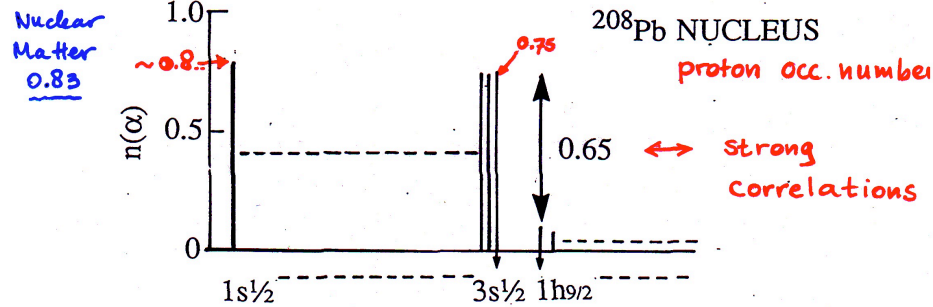
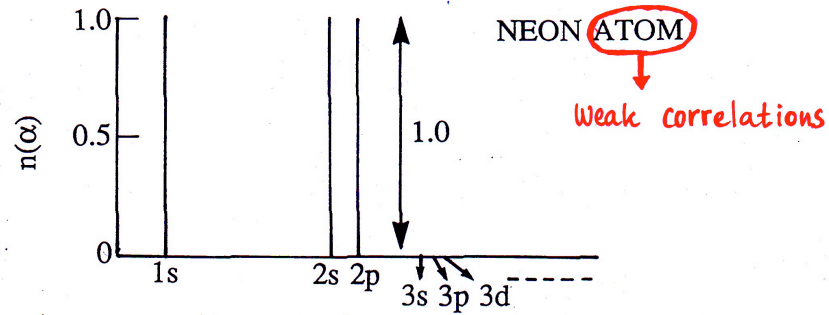
B.E.Vonderfecht et al. Nucl. Phys. A555, 1 (1993)

E.R.Stoddard, thesis WU 2000 (self-consistent ladders)

Short-range and Tensor Correlations

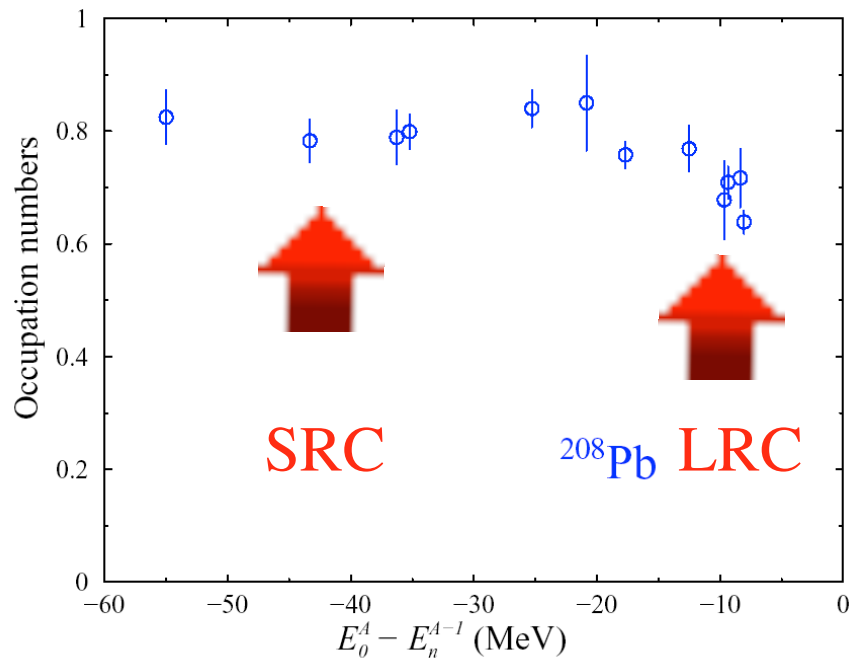
Occupation Numbers

slide from 20 years ago ...



M. van Batenburg & L. Lapikás from  $^{208}\text{Pb} (e,e' p) ^{207}\text{Tl}$   
 NIKHEF 2001 data (one of the last experiments)

## Occupation of deeply-bound proton levels from EXPERIMENT

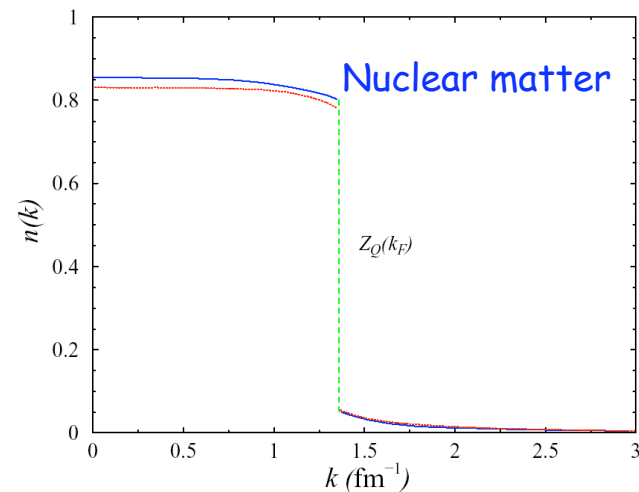


Up to 100 MeV missing energy and  
 270 MeV/c missing momentum

Covers the whole mean-field domain  
 for the FIRST time!!

Confirms predictions for depletion

$n(0) \Rightarrow$  0.85 Reid  
 0.87 Argonne V18  
 0.89 CDBonn/N3LO

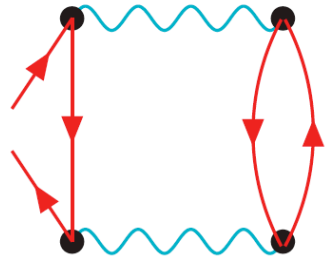


Short-range and Tensor Correlations



# Location of high-momentum components

*high momenta*



*require specific intermediate states*

External line  $\mathbf{k}$  (large).

Intermediate holes  $< k_F$ , say total momentum  $\sim 0$ .

Momentum conservation: intermediate particle  $-\mathbf{k}$

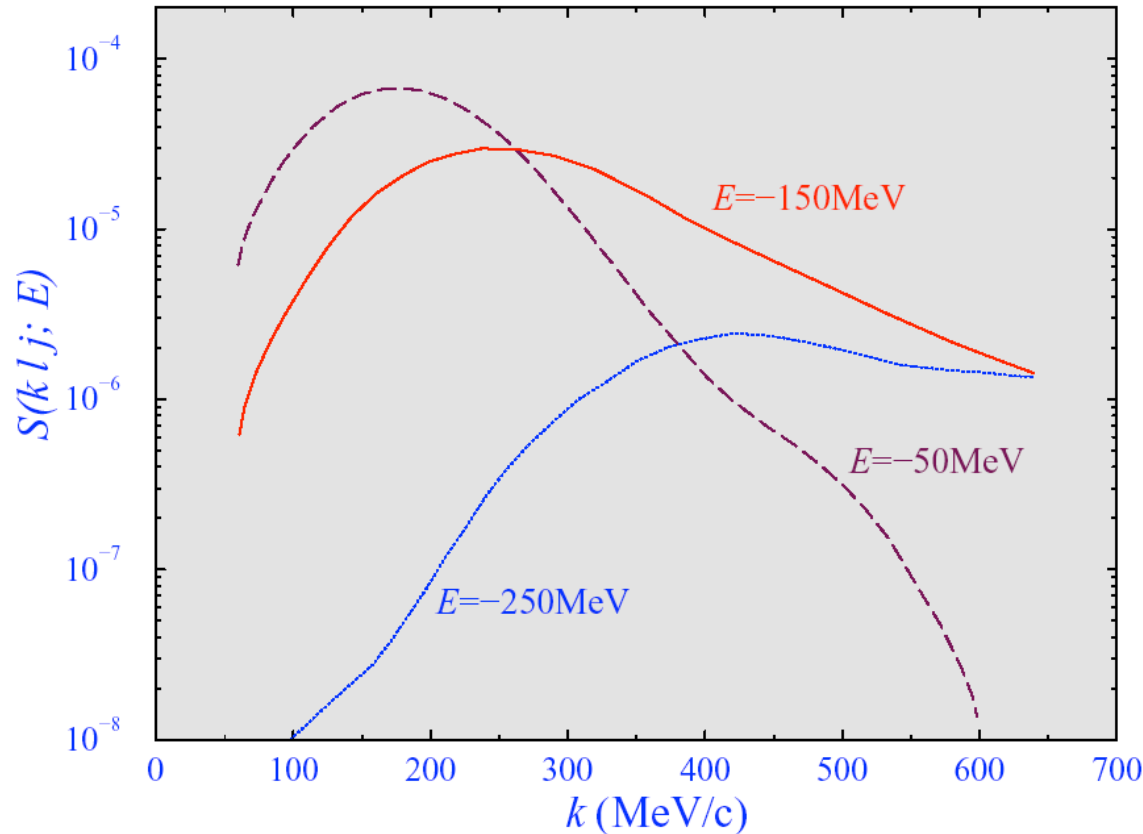
$\Rightarrow$  Energy intermediate state  $\sim \langle \epsilon_{2h} \rangle - \epsilon(\mathbf{k})$

$\Rightarrow$  the higher  $k$  the more negative the location of its strength

$\Rightarrow$  no high-momentum components near  $\epsilon_F$

Short-range and Tensor Correlations

## Prediction of high-momentum components calculated for $^{16}\text{O}$

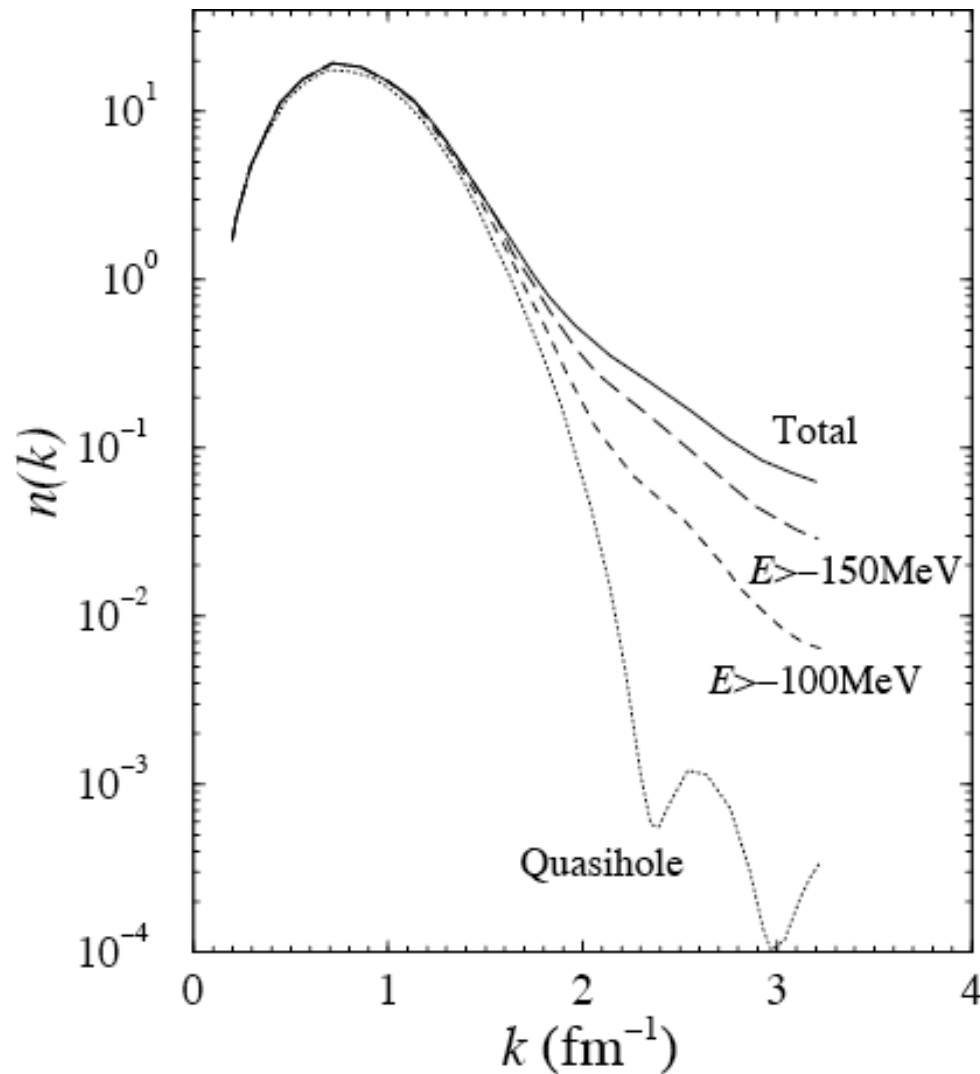


$p_{1/2}$  spectral function at fixed energies in  $^{16}\text{O}$

Phys. Rev. C49, R17 (1994)

Short-range and Tensor Correlations

# Momentum distribution $^{16}\text{O}$



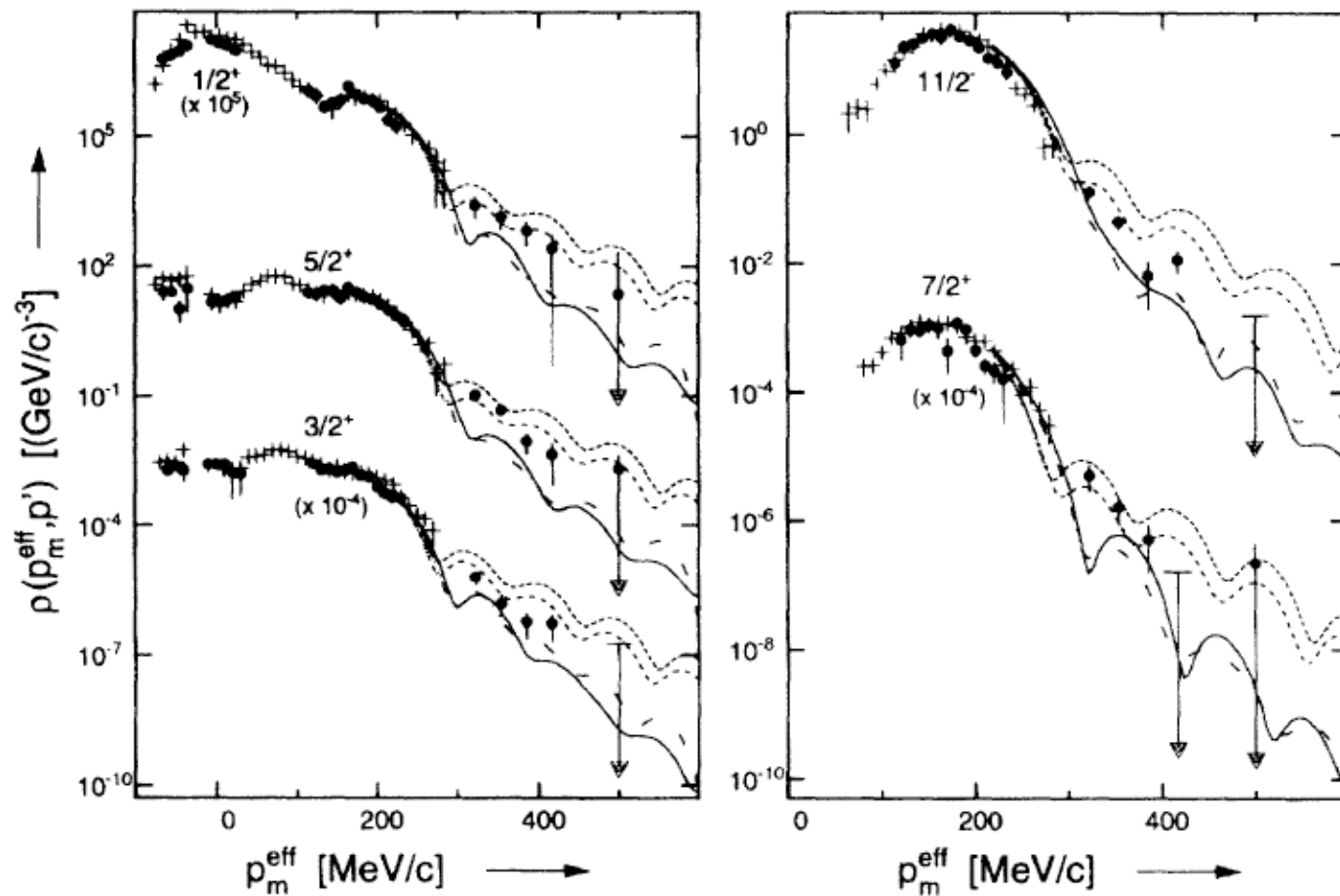
Confirms expectation:

High momentum nucleons  
can be found at large  
negative energies

Phys. Rev. C51, 3040 (1995)

Short-range and Tensor Correlations

# High-momenta near $\varepsilon_F$ ?



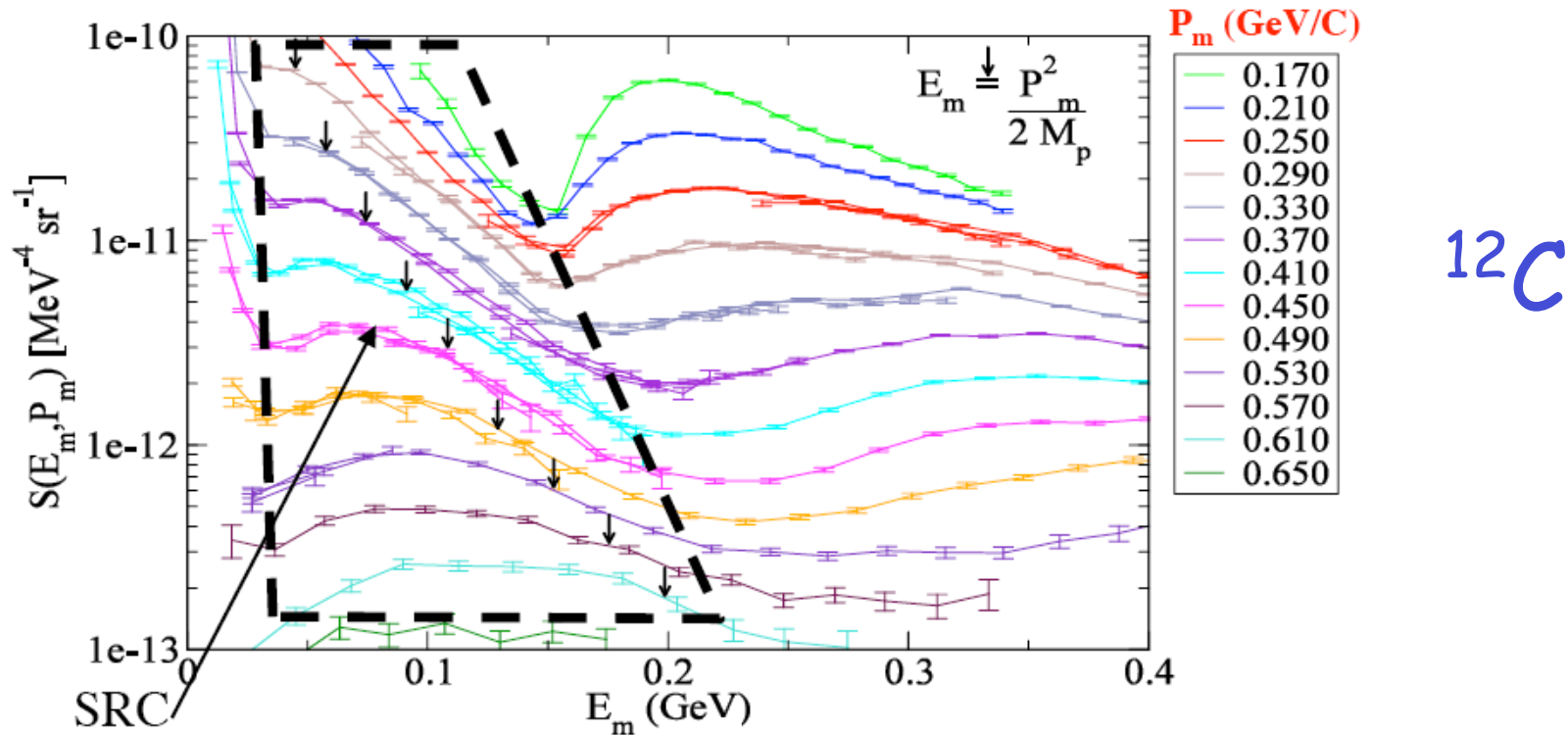
I. Bobeldijk et al., Phys. Rev. Lett. 73, 2684 (1994)

Short-range and Tensor Correlations

NO!

# High-momentum protons have been seen in nuclei!

Jlab E97-006 Phys. Rev. Lett. 93, 182501 (2004) D. Rohe et al.



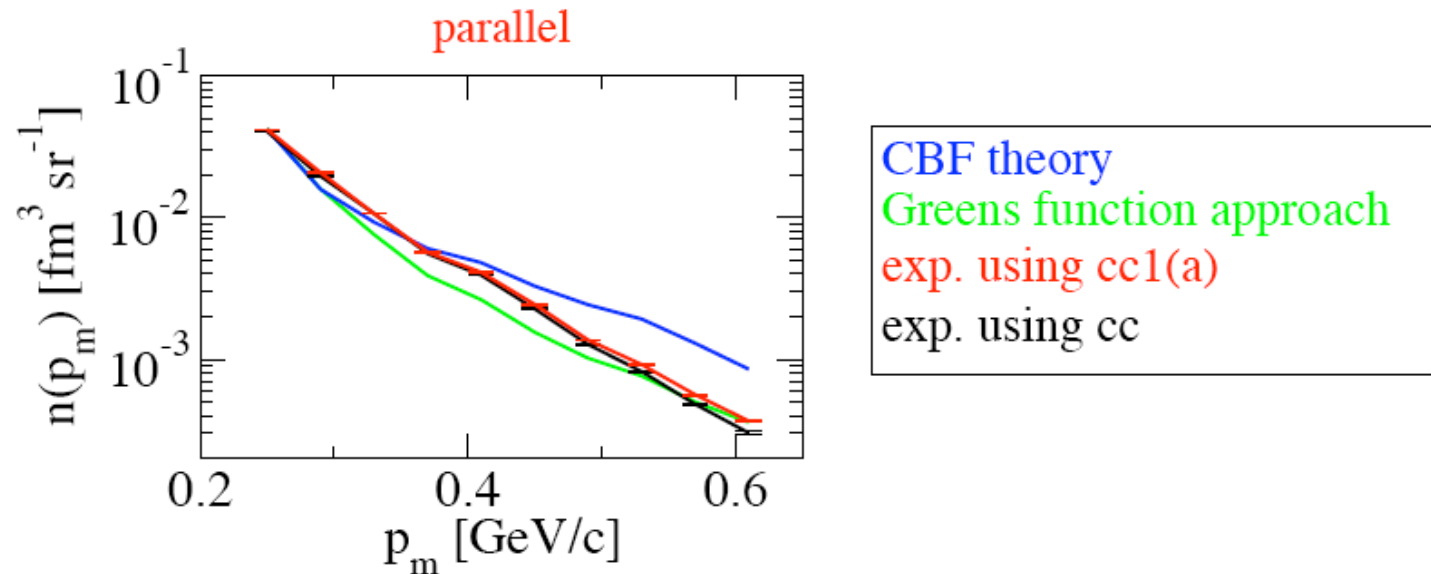
- Location of high-momentum components
- Integrated strength agrees with theoretical prediction Phys. Rev. C49, R17 (1994)

⇒ ~0.6 protons for  $^{12}\text{C}$  ⇒ **~10%**

Short-range and Tensor Correlations

# Integrated strength $\Rightarrow n(k)$

momentum dependence



$\rightarrow$  theory and experiment  $\pm$  agree

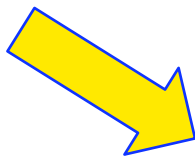
From: Sick, ECT\* workshop July 2007  
Daniela Rohe, Habilitation 2004, Basel

Short-range and Tensor Correlations

# Location of single-particle strength in closed-shell (stable) nuclei

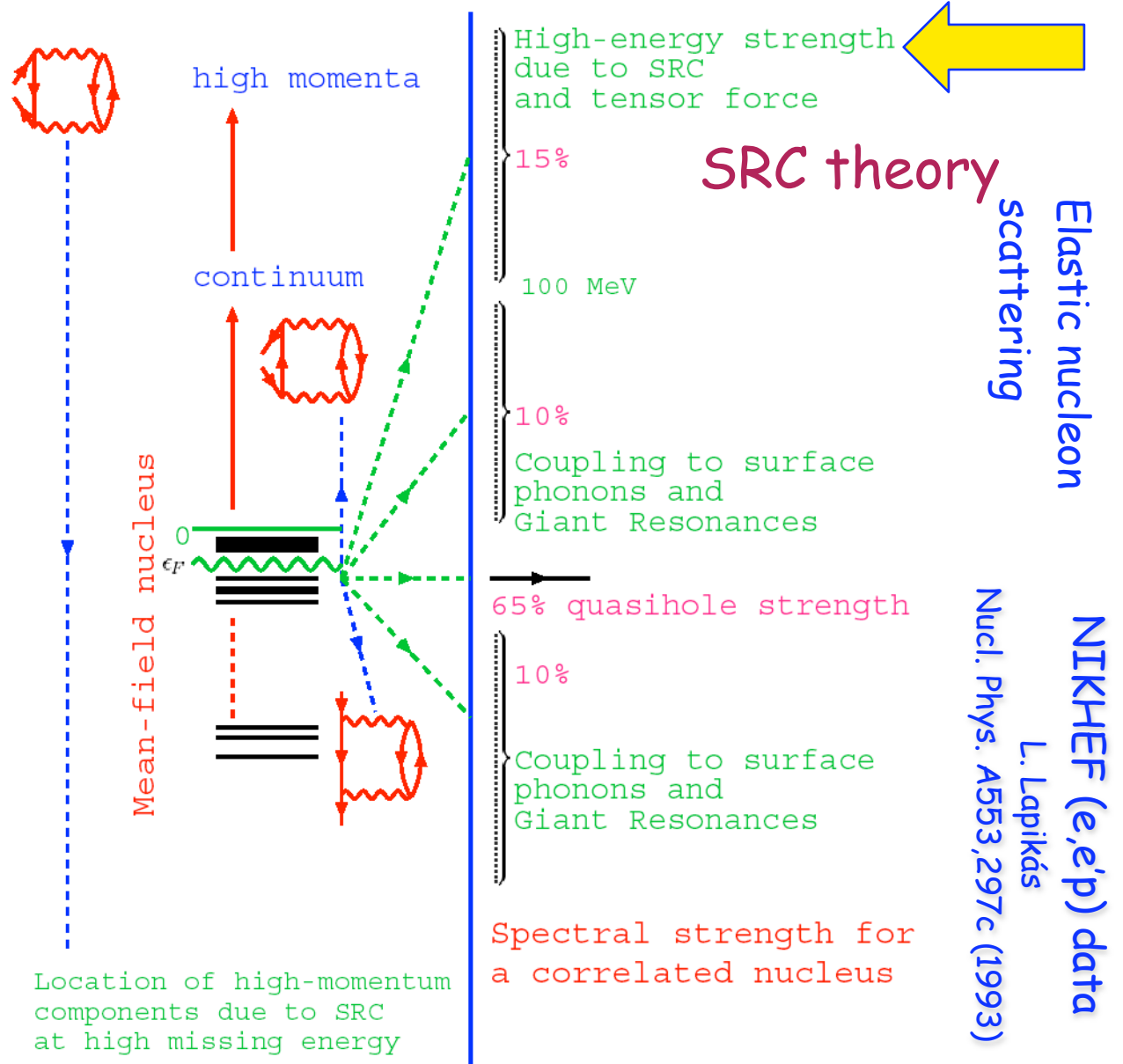
For example: protons in  $^{208}\text{Pb}$

SRC



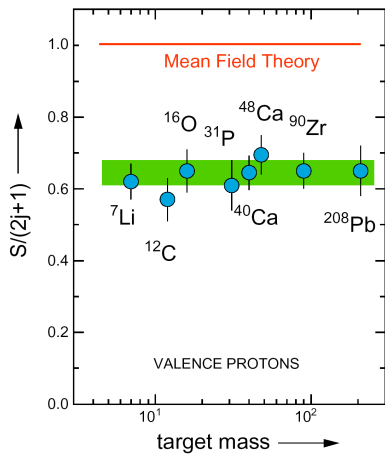
JLab E97-006

Phys. Rev. Lett. 93, 182501 (2004) D. Rohe et al.

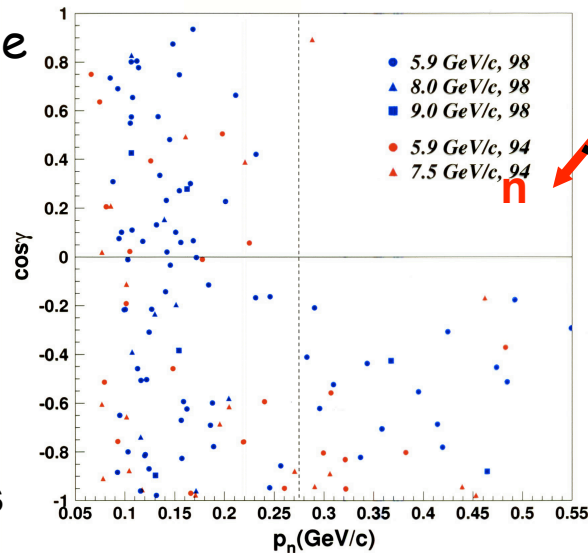


Short-range and Tensor Correlations

# Slide from John Watson, Kent State



NIKHEF  
A(e,e'p)



$^{12}\text{C}(p,2p n)$

Tang et al.  
PRL 042301 (2003)

Piassetzky, Sargsian,  
Frankfurt, Strikman,  
Watson  
PRL 162504(2006).

Long range (shell  
model) correlations

$^{12}\text{C}$

Single  
nucleons

60-70%

10-20%

20±5%

2N-SRC

2N-SRC

84-92 %

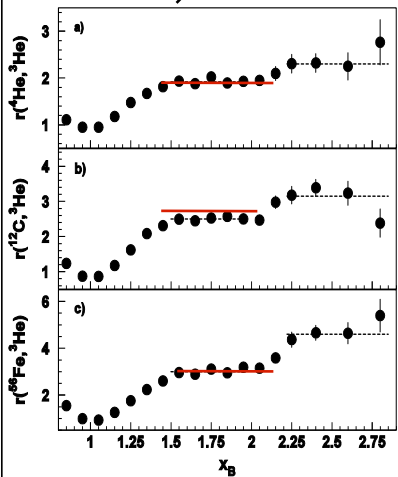
n-p pairs

5.5±1%

p-p pairs

5.5±1%

n-n pairs



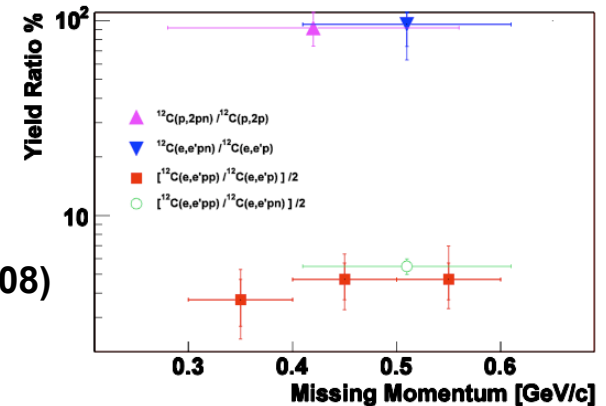
A(e,e')

Egiyan et al. PRC 68, 014313.

Egiyan et al. PRL. 96, 082501 (2006)

A(e,e'pN)

Subedi et al. Science 320, 1476 (2008)





# Full off-shell propagation in infinite matter

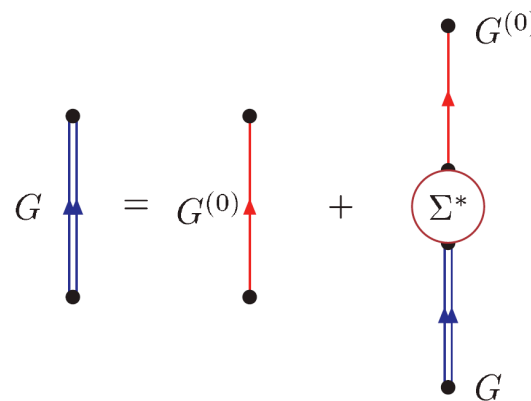
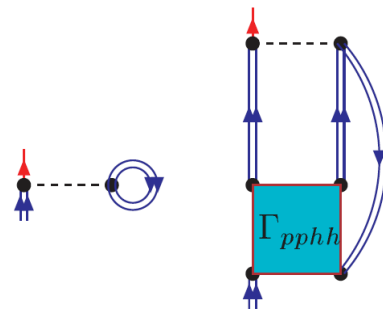
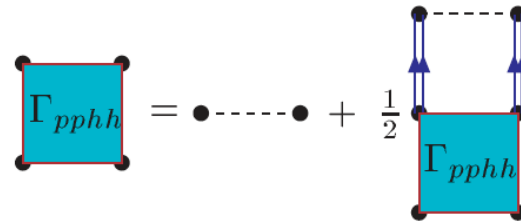
SCGF:  
self-consistent  
Green's functions  
for SRC and tensor  
effects

self-consistency  
=> thermodynamically consistent

Interaction in the  
medium properly  
treating short-range  
and tensor  
correlations

Self-energy =  
complex potential in  
nuclear matter

Dyson equation =>  
Schrödinger equation  
for dressed nucleons



Short-range and Tensor Correlations

Arnau Rios

Arturo Polls

W.D.

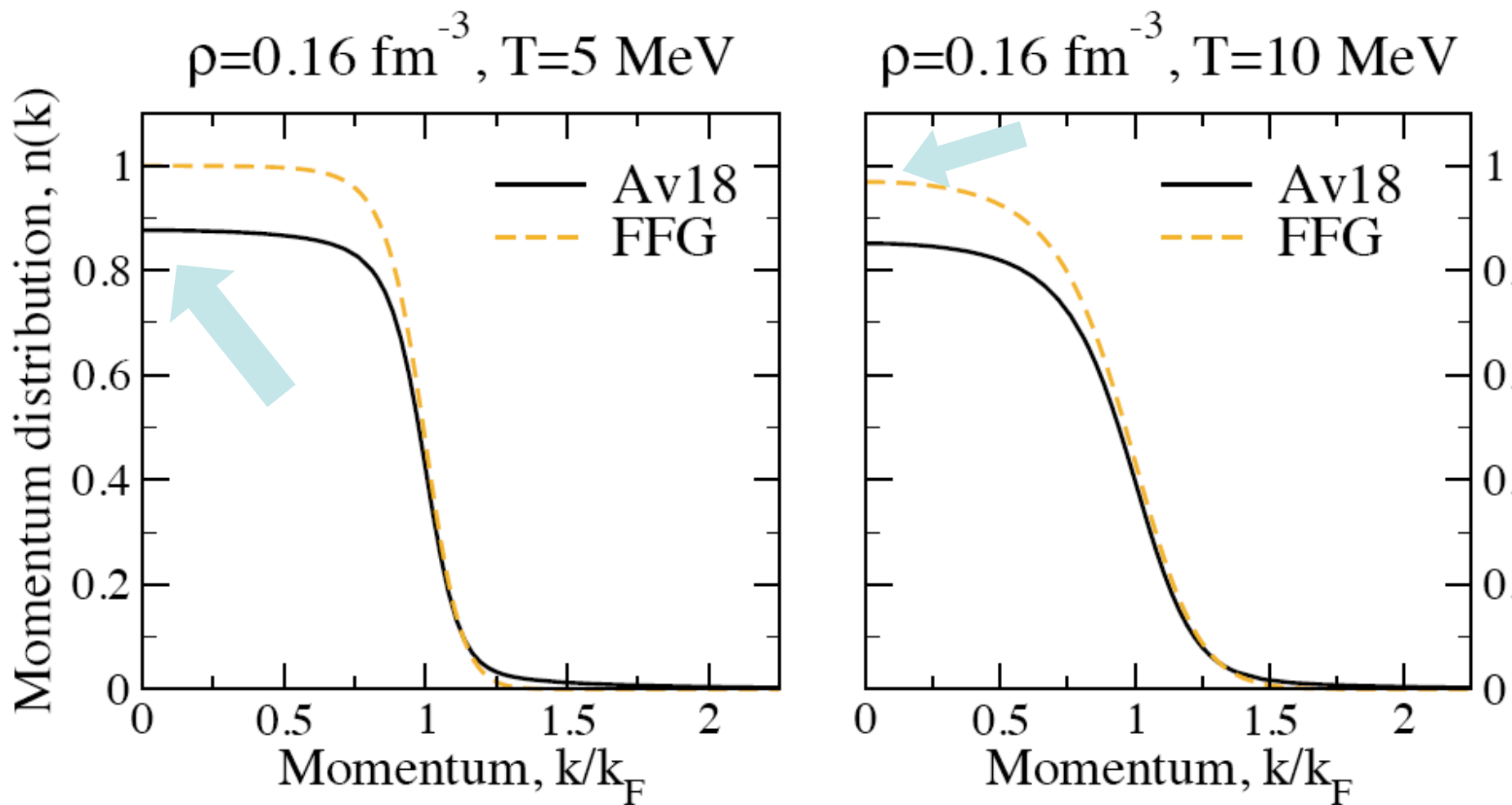
finite T avoids pairing

# Some results infinite matter

- Effect of temperature vs. SRC & tensor correlations
- Effect of density
- Choice of interaction: CDBonn & Argonne v18
- Symmetric nuclear matter vs. neutron matter
- Depletion vs. high-momentum components
- Asymmetric nuclear matter
- Temperature, Interaction
- Tensor, tensor, tensor  $\Rightarrow$  pion, pion, pion
- Recent results also for N3LO

A. Rios, A. Polls, and W. H. Dickhoff  
Depletion of the nuclear Fermi sea.  
[Phys. Rev. C79, 064308 \(2009\).](#)

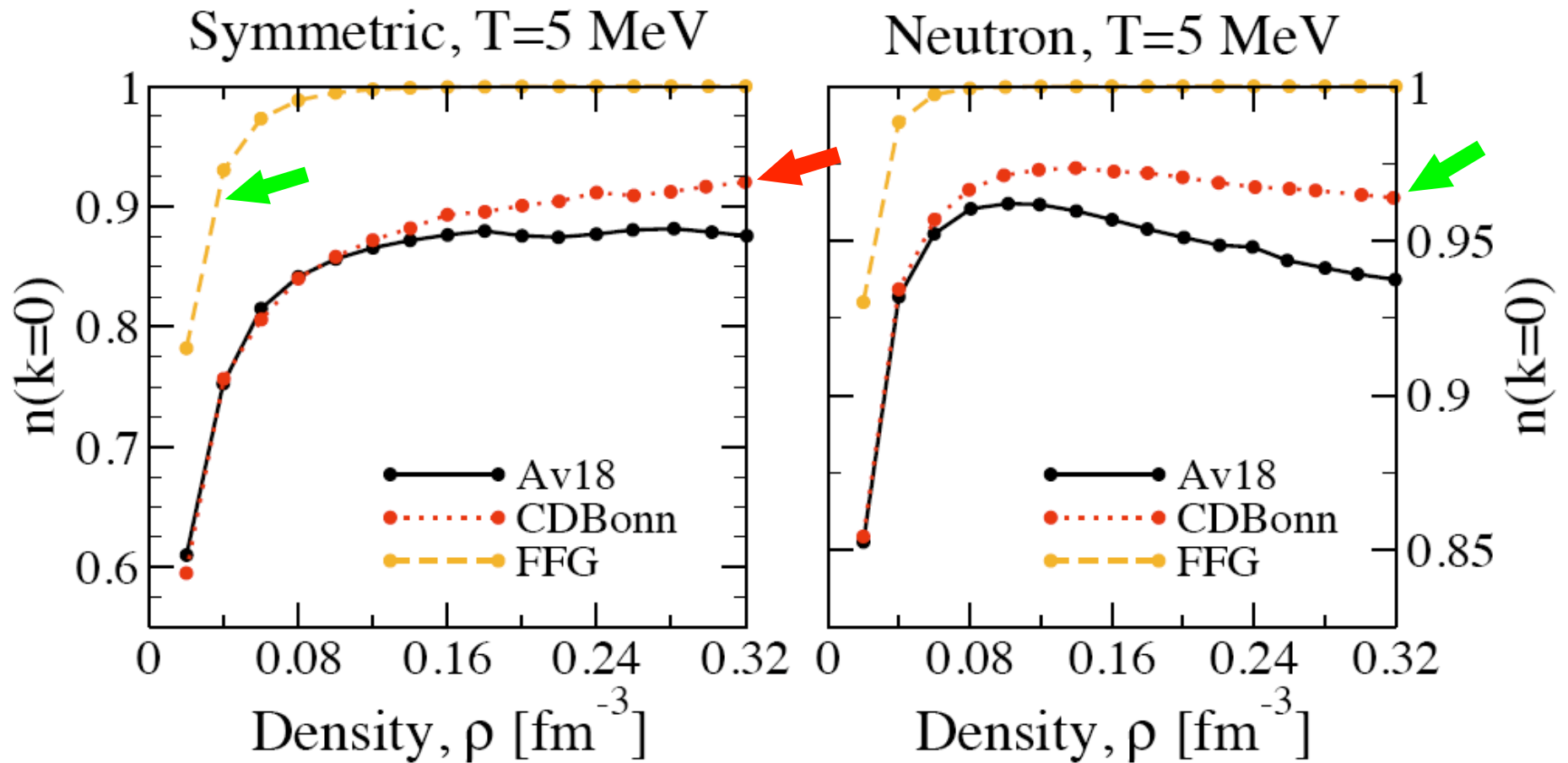
# Temperature vs. correlations



Symmetric nuclear matter

Short-range and Tensor Correlations

# Density dependence $n(0)$ for SNM & PNM

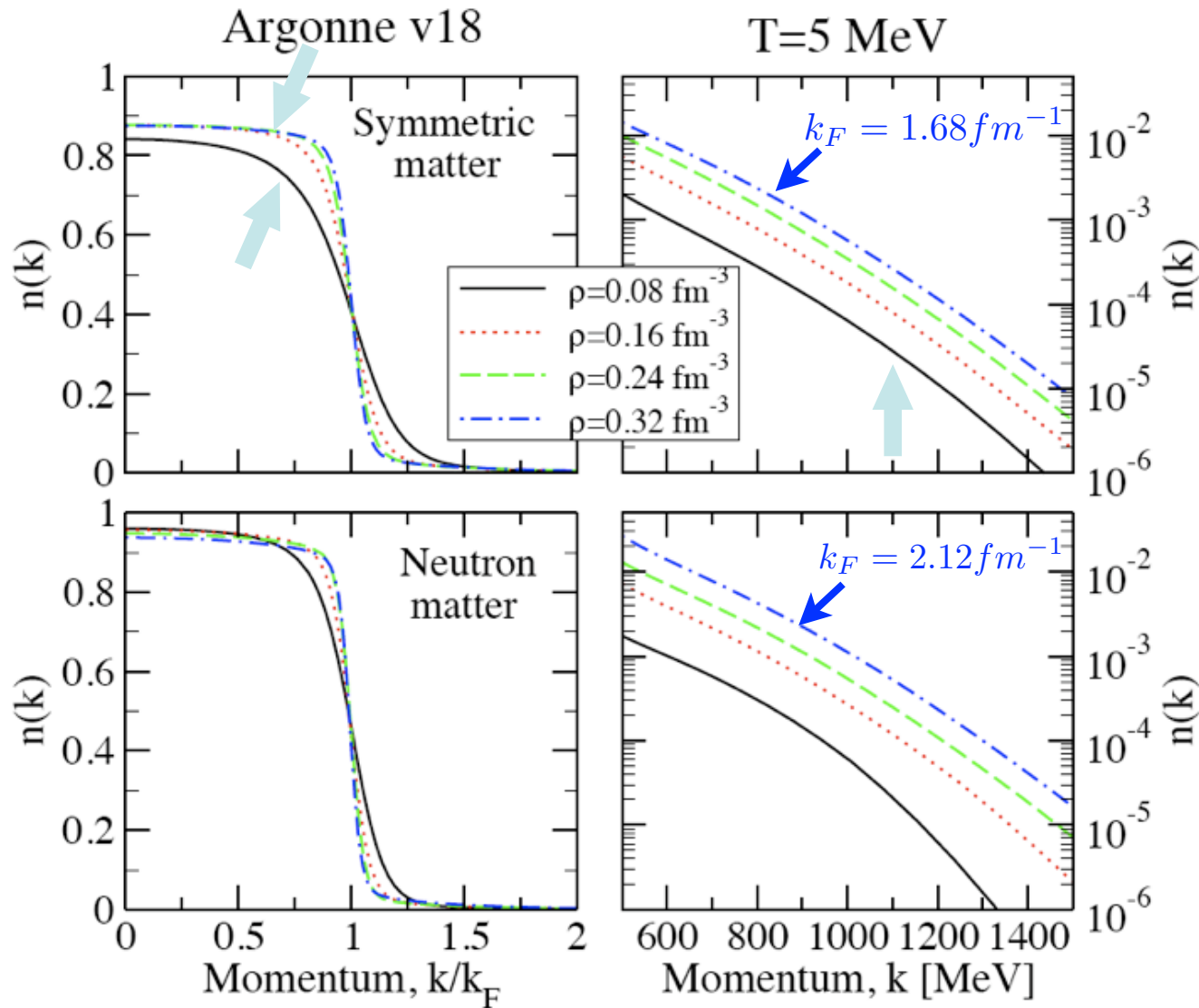


Different behavior for different interactions

Short-range and Tensor Correlations

# Momentum distribution & density

$$\rho = \frac{\nu}{6\pi^2} k_F^3$$

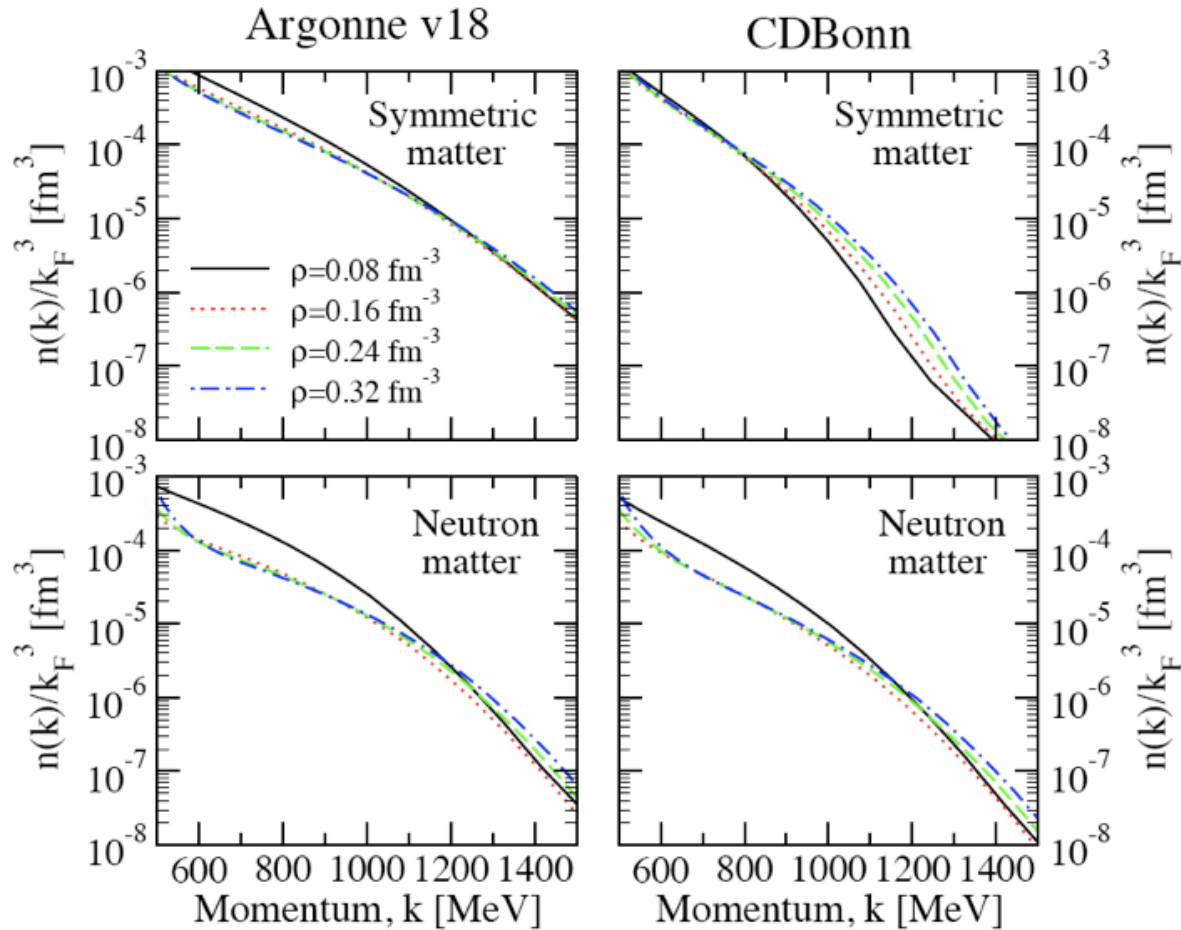


$$\nu = 4$$

$$\nu = 2$$

Short-range and Tensor Correlations

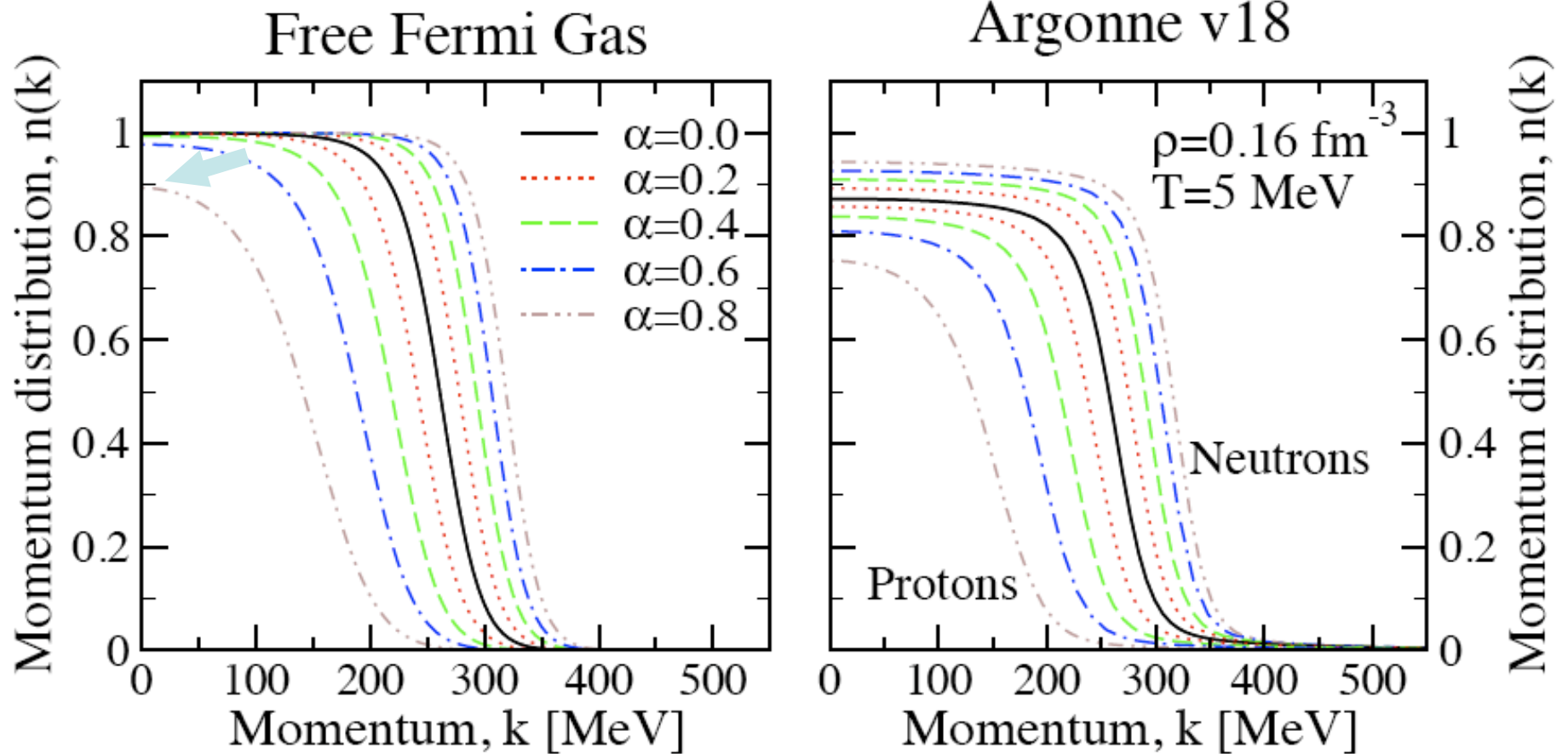
# High-momentum scaling $\sim (k_F)^3$



Harder interactions scale with  $(k_F)^5$

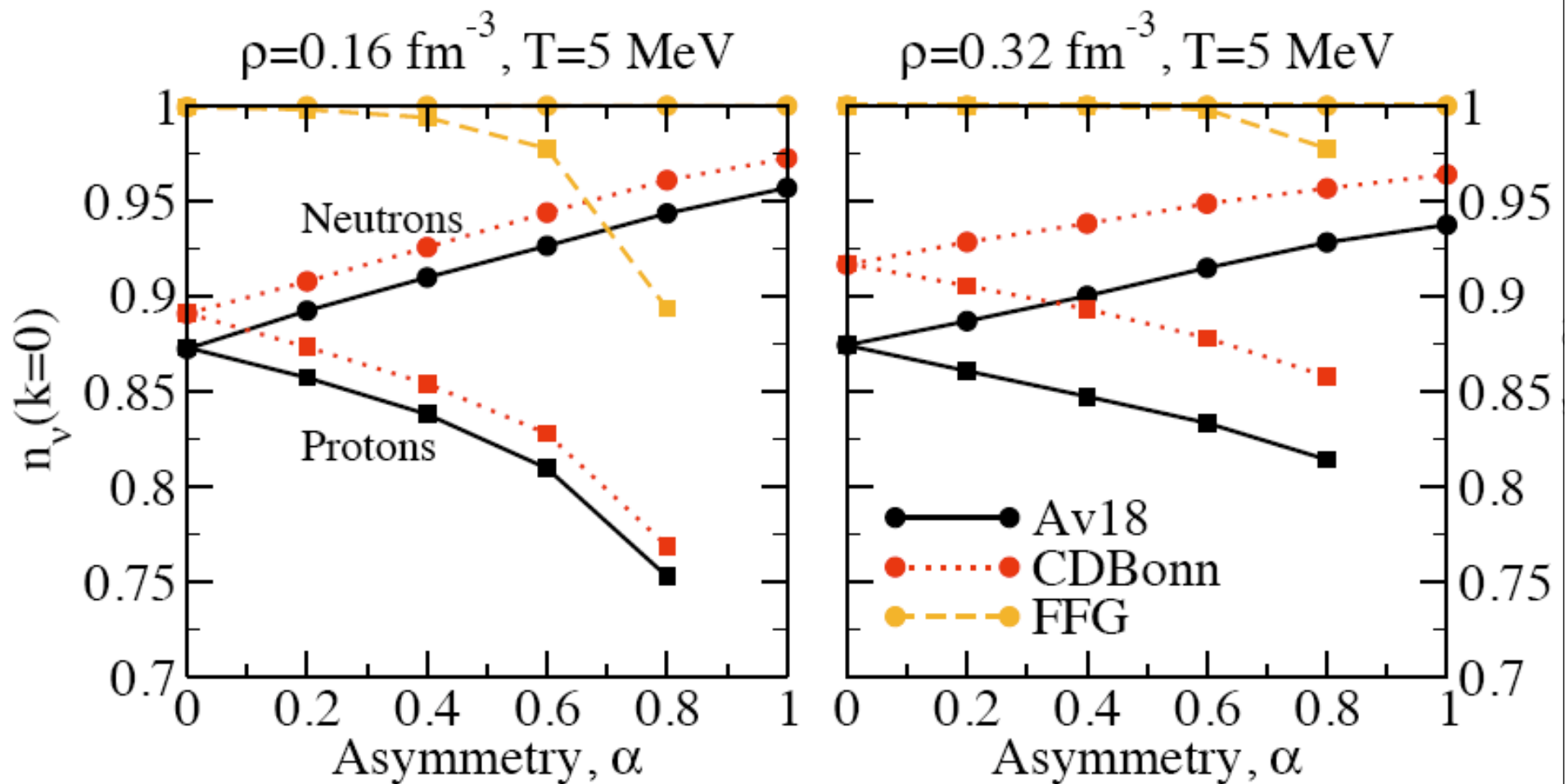
Short-range and Tensor Correlations

# Asymmetric nuclear matter



$$\alpha = \frac{N - Z}{N + Z} \quad \text{Short-range and Tensor Correlations}$$

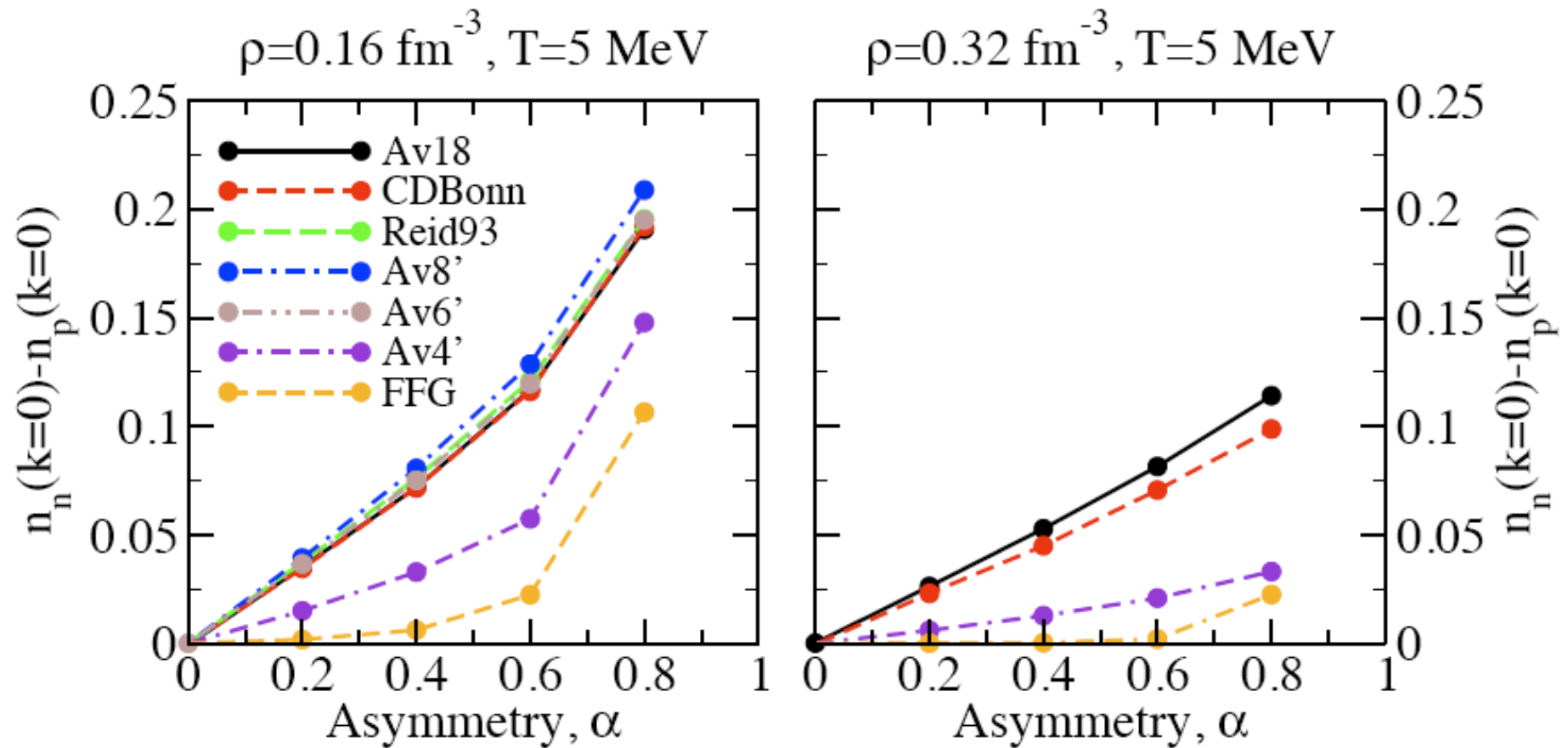
# Depletion as a function of asymmetry



Short-range and Tensor Correlations



# Difference $n_n(k=0)-n_p(k=0)$

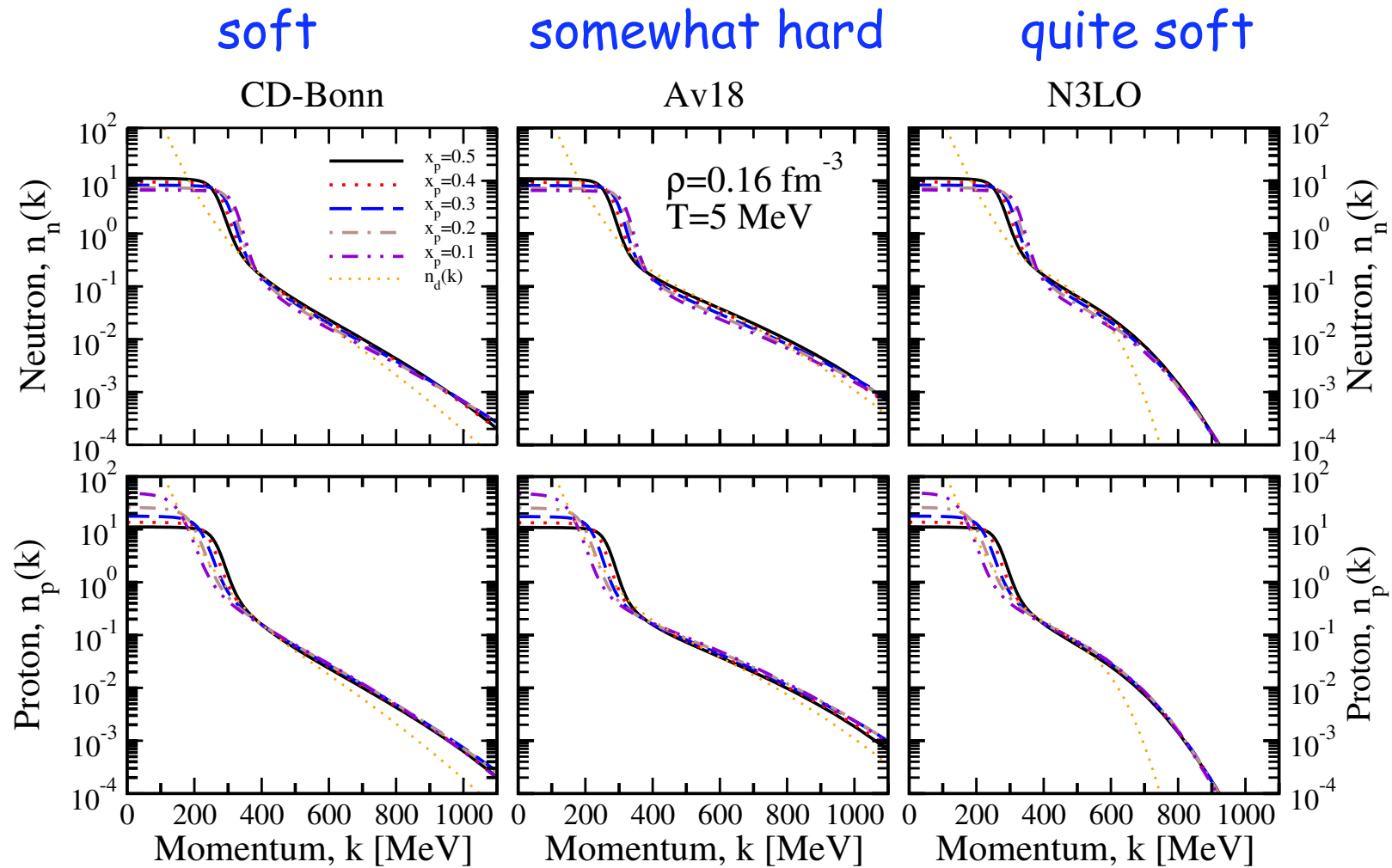


Apparently determined by phase shifts!

Tensor! Note Av4'

Short-range and Tensor Correlations

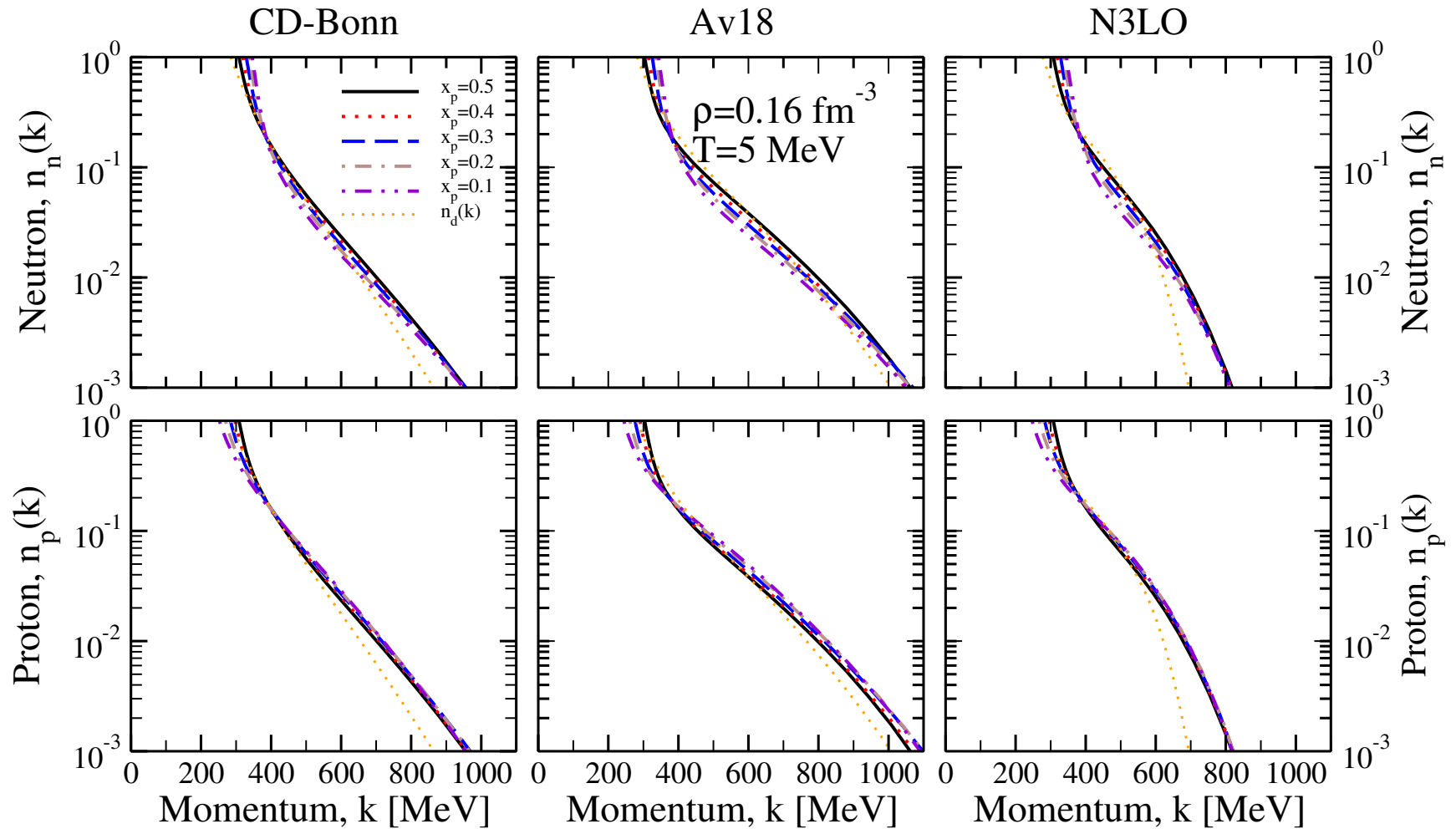
# Three different interactions (just calculated)



- Normalization of  $n(k) \rightarrow 1$  (not density)

# Focus on the tails in asymmetric matter

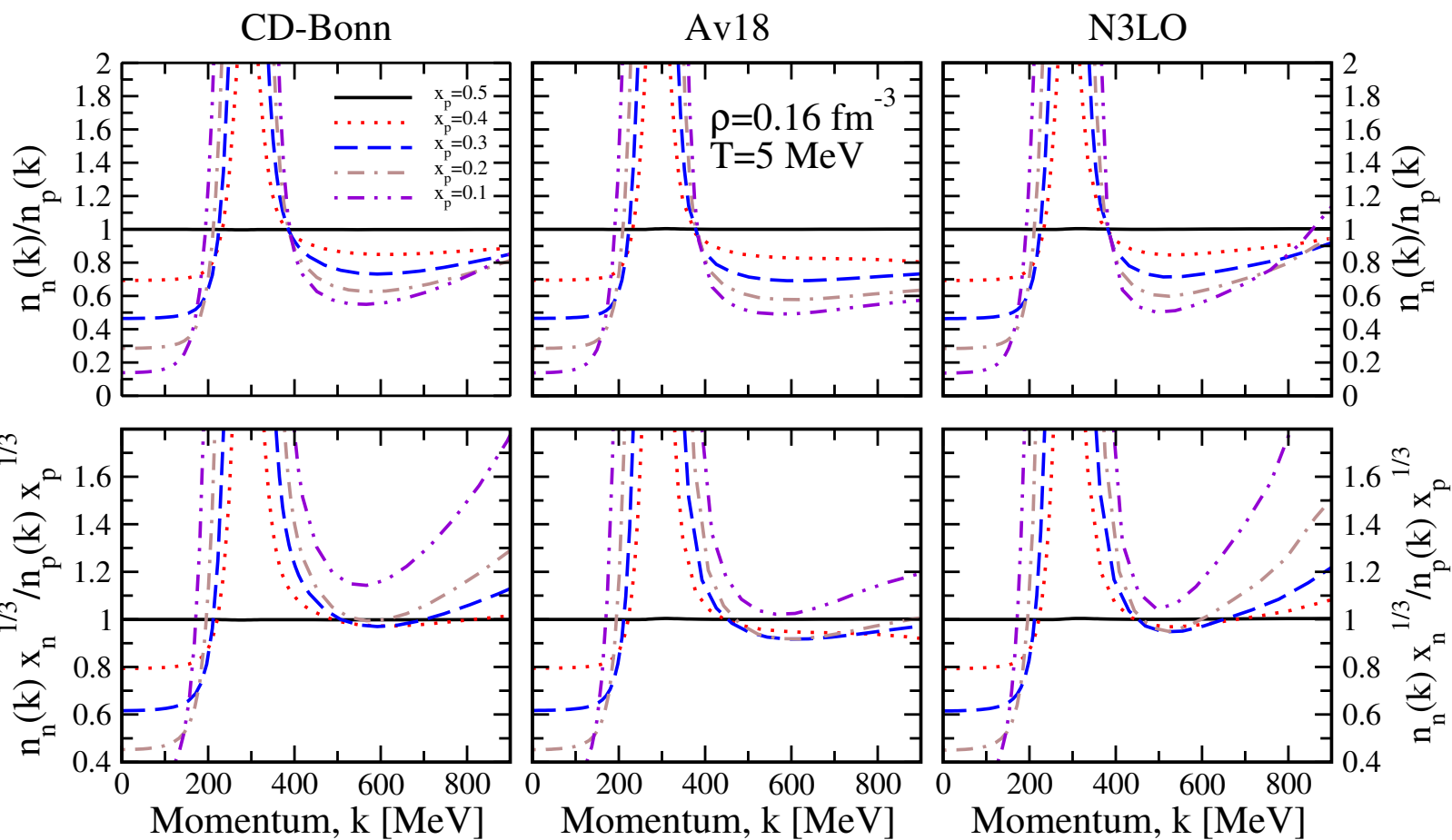
- Normalization of  $n(k) \rightarrow 1$



Short-range and Tensor Correlations

# Comparing neutrons and protons

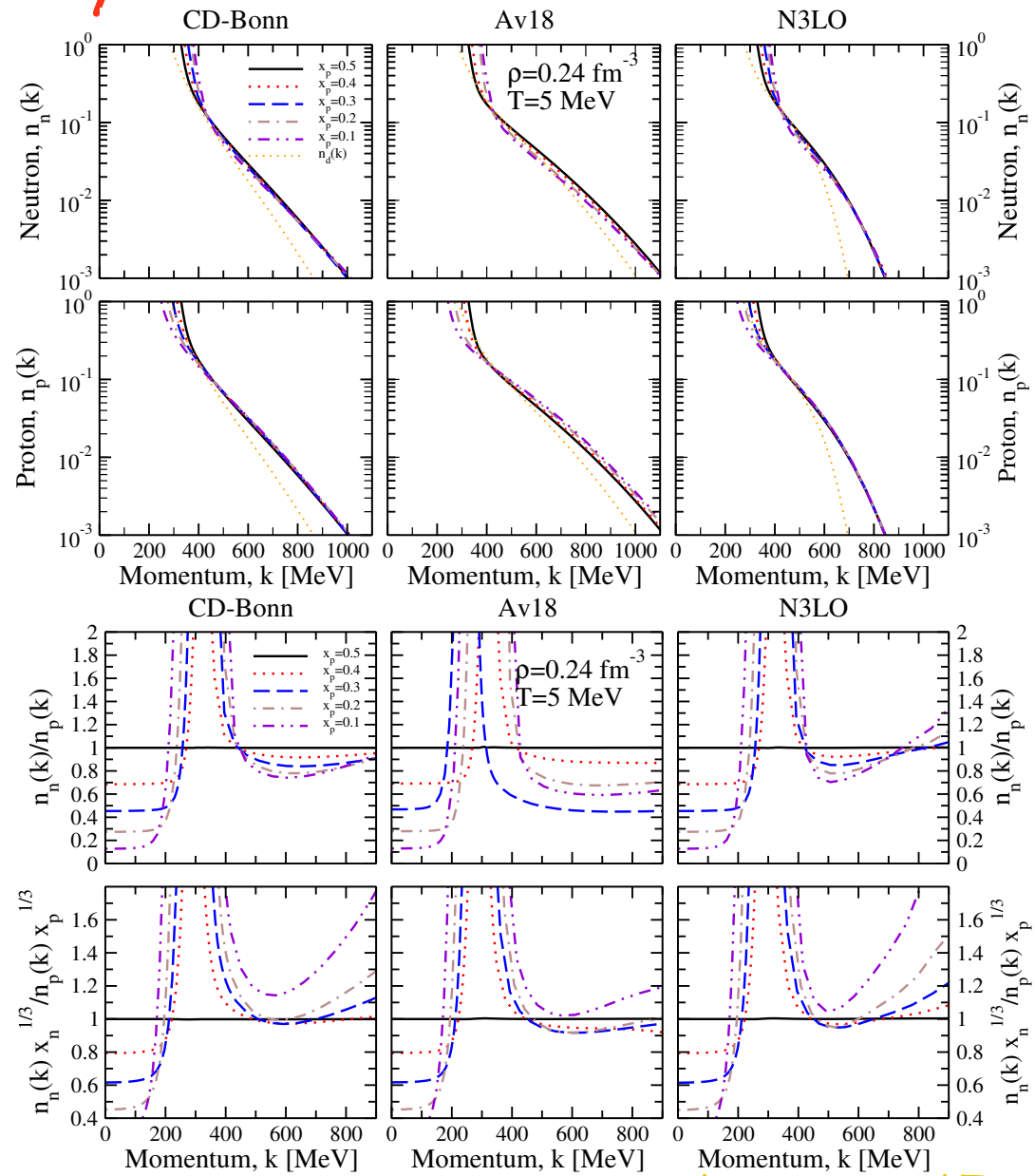
- Ratio



- Scaled

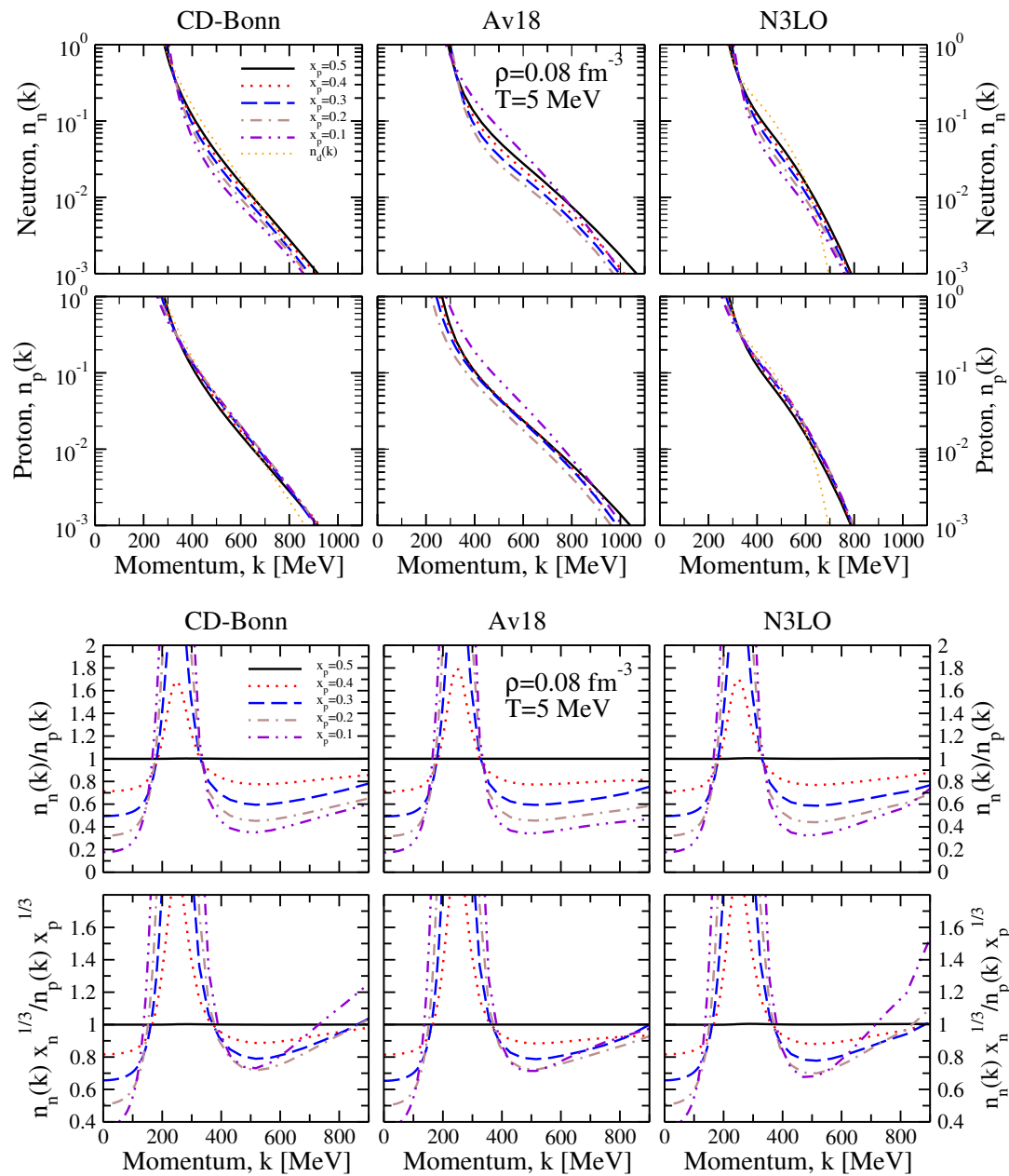
Short-range and Tensor Correlations

# Higher density



Short-range and Tensor Correlations

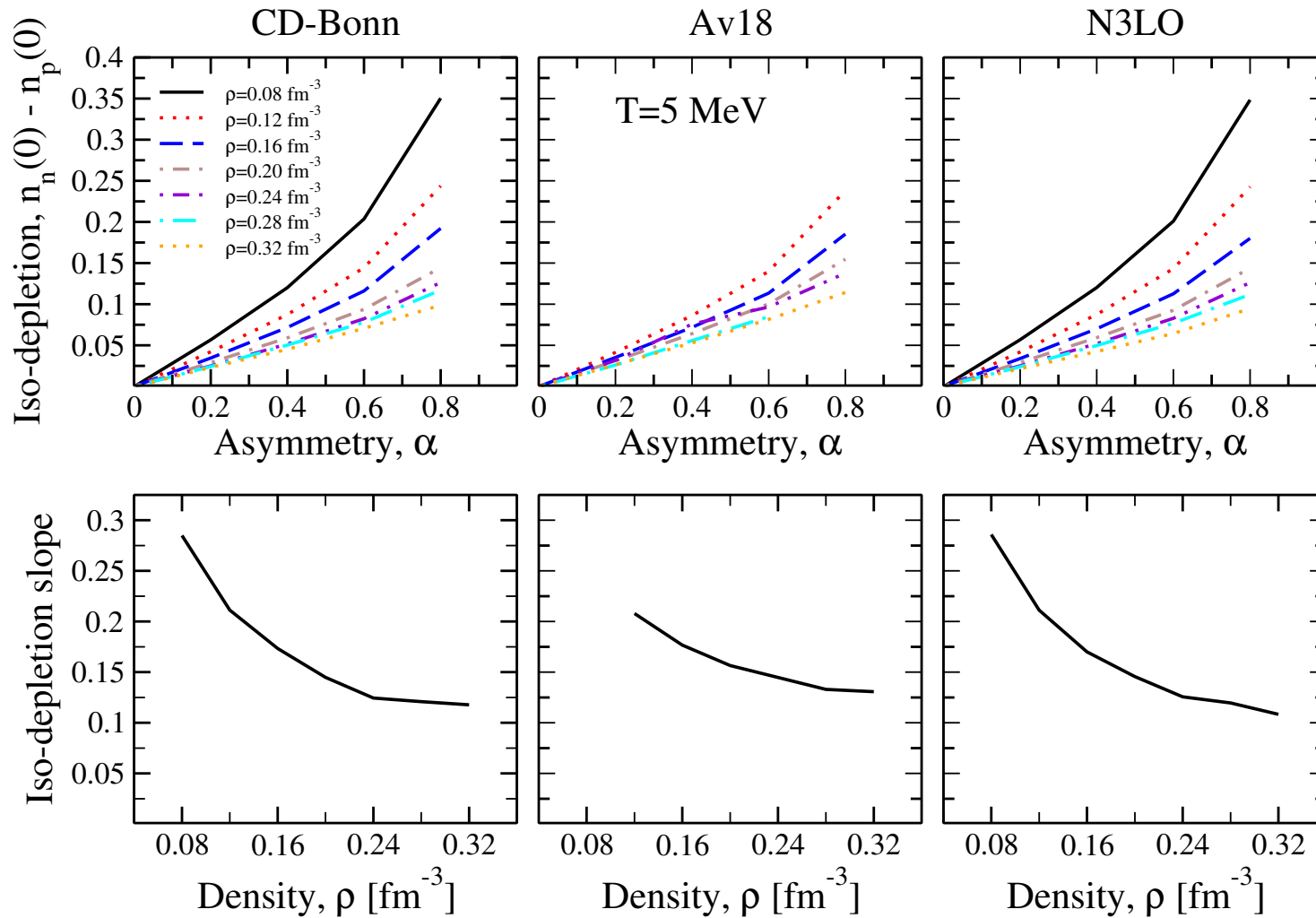
# Lower density



Short-range and Tensor Correlations

# "Iso-depletion"

- Constraint by data?!



Short-range and Tensor Correlations

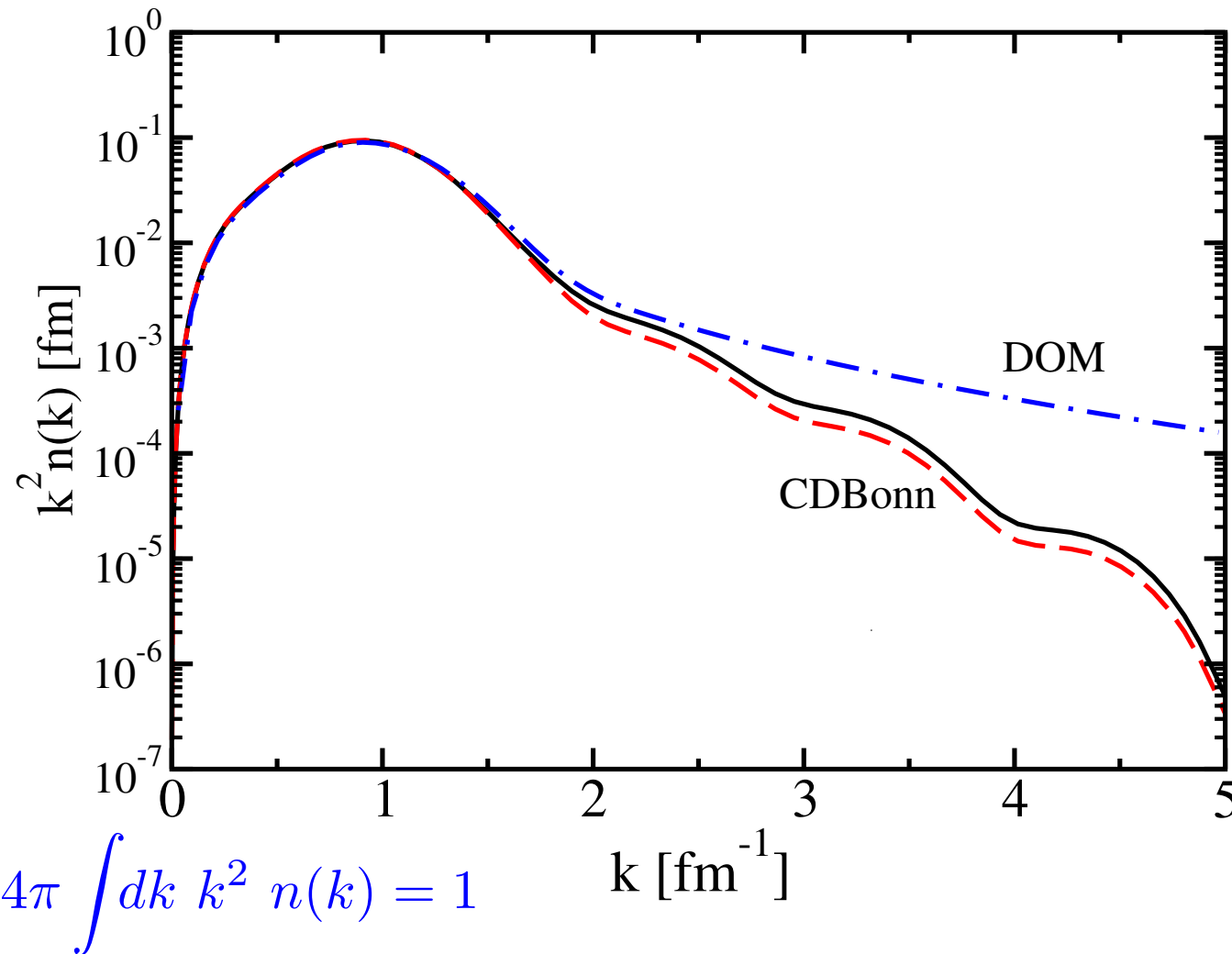
# High-momenta ab initio for heavier nuclei

- In the beginning stages of proper sophistication...
- But in progress!



# Ab initio with CDBonn for $^{40}\text{Ca}$

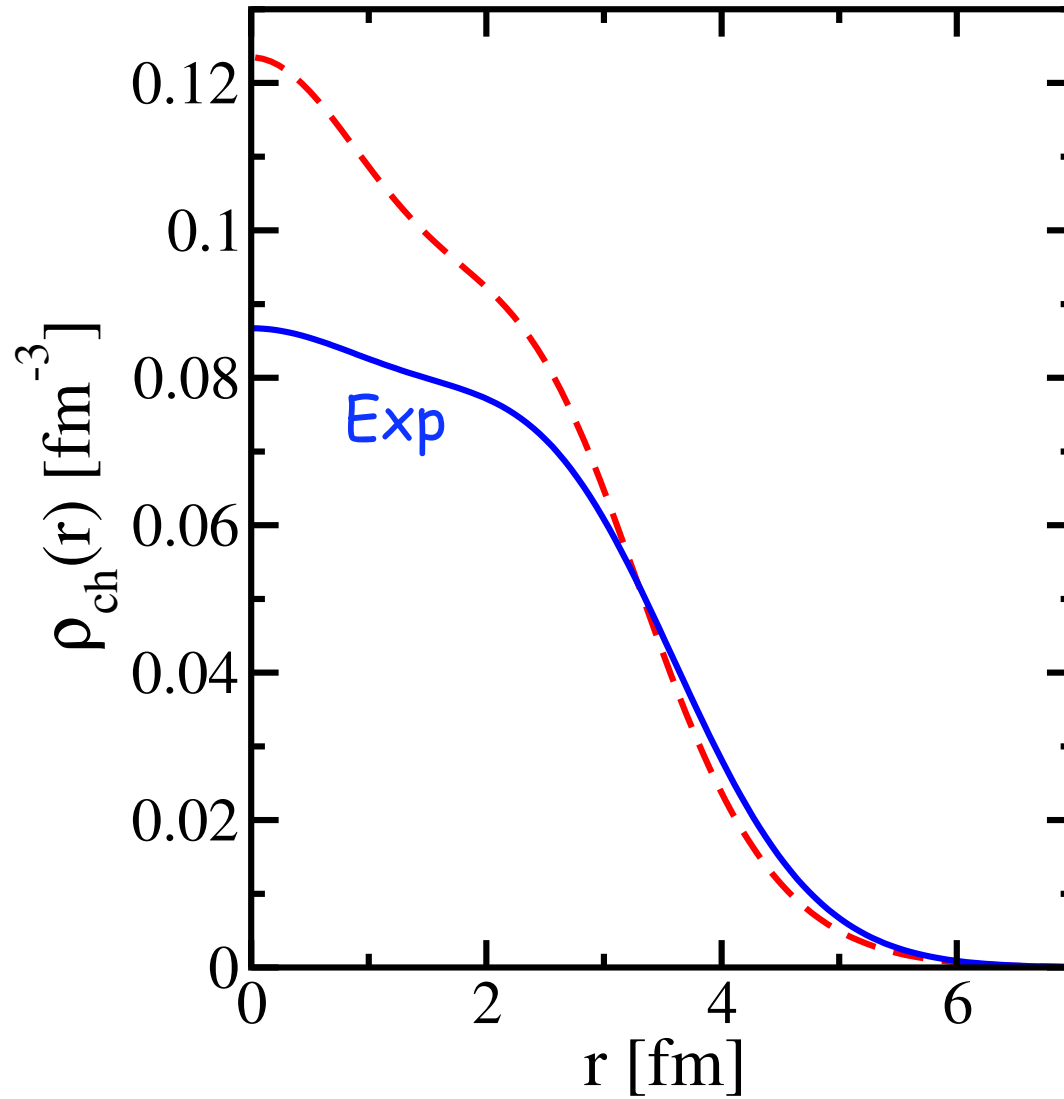
- Dussan et al. PRC84, 044319 (2011); spectral functions available



Short-range and Tensor Correlations

# CDBonn

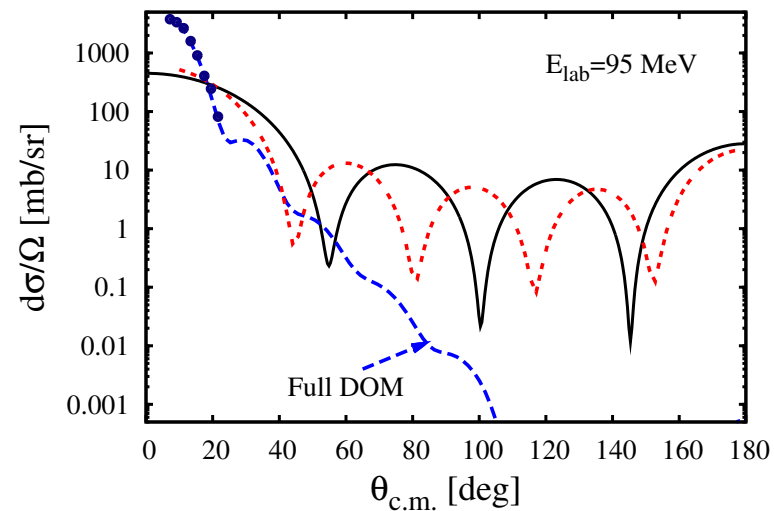
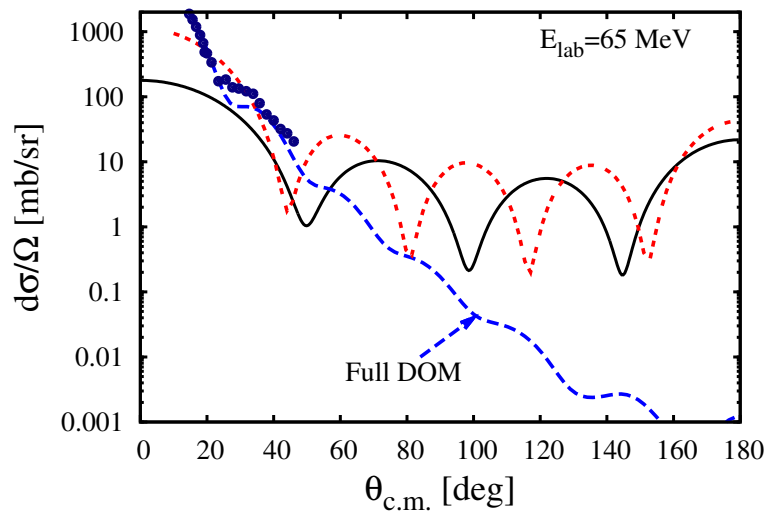
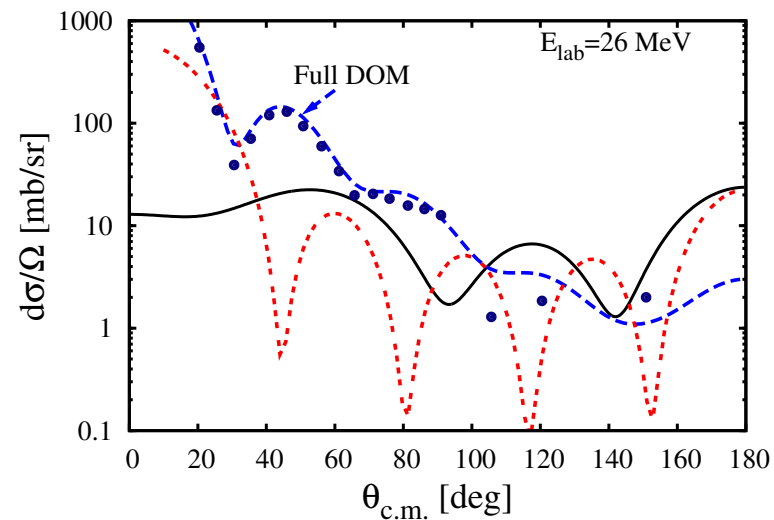
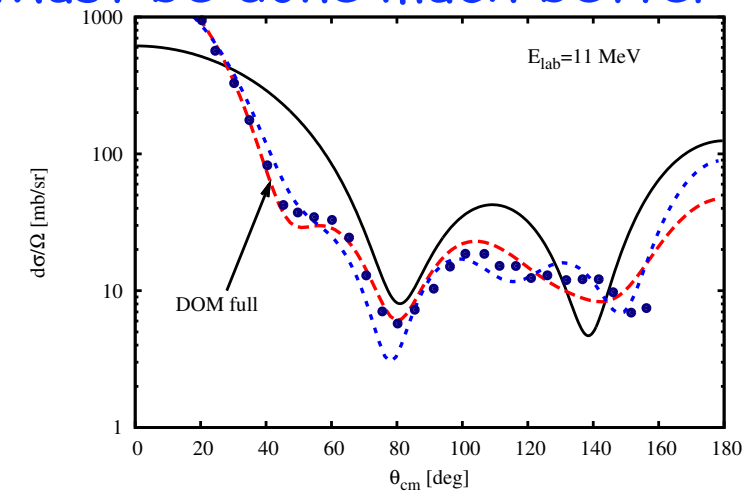
- Density ....



Short-range and Tensor Correlations

# Ab initio description of elastic scattering

- Must be done much better



Short-range and Tensor Correlations

# Drip-line nuclear physics

- Many reactions necessarily involve strongly interacting particles
  - (p,2p) perhaps (p,pn)
  - (d,p) or (p,d)
  - HI knock-out reactions
- Interactions of "projectiles" with "target" are not experimentally constrained at this time --> no unambiguous information
- Empirical Green's function project: Dispersive Optical Model (DOM)
  - intends to provide a frame work for such constraints
  - simultaneous treatment of negative (structure) and positive energies (reactions) for nucleons **PLUS** a reaction description
  - linking information below and above the Fermi energy such as **elastic scattering cross sections, level structure, charge densities, knock-out cross sections etc.** ----> **constrained description of p or n distorted waves**  
Short-range and Tensor Correlations

# DOM = Dispersive Optical Model

C. Mahaux and R. Sartor, *Adv. Nucl. Phys.* **20**, 1 (1991)

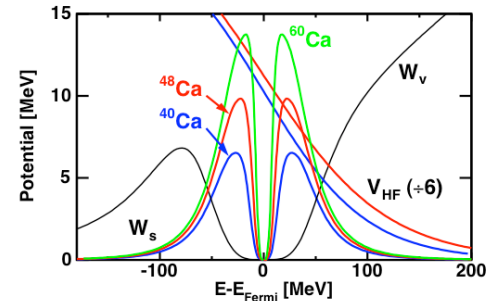
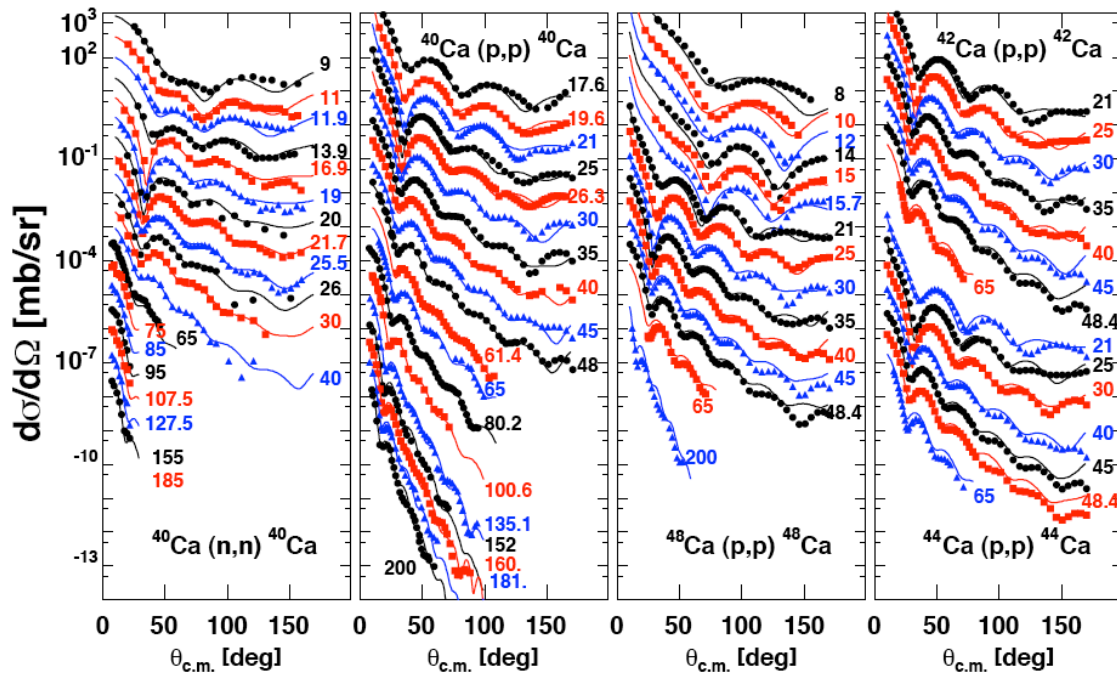
Goal: extract "propagator"/"self-energy" from data

Vehicle for data-driven extrapolations / predictions to the drip lines

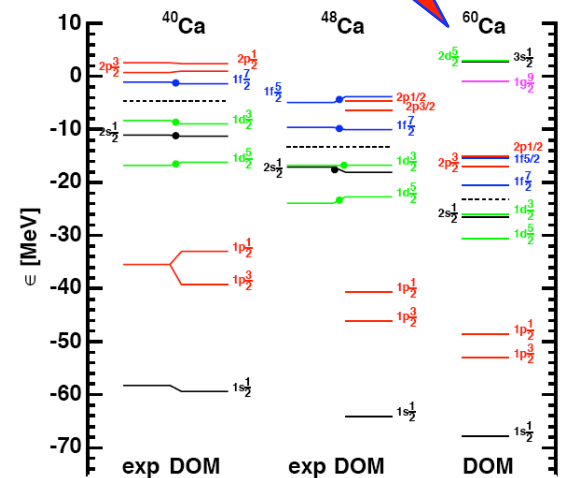
Combined analysis of protons/neutrons in  $^{40}\text{Ca}$  and  $^{48}\text{Ca}$

Charity, Sobotka, & WD, *PRL* **97**, 162503 (2006)

Charity, Mueller, Sobotka, & WD, *PRC* **76**, 044314 (2007)



Predict



Short-range and Tensor Correlations

# Flurry of recent DOM activity

W. H. Dickhoff, D. Van Neck, S. J. Waldecker, R. J. Charity, and L. G. Sobotka

Nonlocal extension of the dispersive-optical-model to describe data below the Fermi energy

[Phys. Rev. C82, 054306 \(2010\), 1-12.](#)

J. M. Mueller, R. J. Charity, R. Shane, L. G. Sobotka, S. J. Waldecker, W. H. Dickhoff, A. S. Crowell, J. H. Esterline, B. Fallin, C. R. Howell, C. Westerfeldt, M. Youngs, B. J. Crowe, III, and R. S. Pedroni

Asymmetry dependence of nucleon correlations in spherical nuclei extracted from a dispersive-optical-model analysis.

[Phys. Rev. C83, 064605 \(2011\), 1-32.](#)

S. J. Waldecker, C. Barbieri and W. H. Dickhoff

Microscopic self-energy calculations and dispersive-optical-model potentials.

[Phys. Rev. C84, 034616 \(2011\), 1-11.](#)

N. B. Nguyen, S. J. Waldecker, F. M. Nuñez, R. J. Charity, and W. H. Dickhoff

Transfer reactions and the dispersive optical-model.

[Phys. Rev. C84, 044611 \(2011\), 1-9.](#)

H. Dussan, S. J. Waldecker, W. H. Dickhoff, H. Müther, and A. Polls

Microscopic self-energy of  $^{40}\text{Ca}$  from the charge-dependent Bonn potential.

[Phys. Rev. C84, 044319 \(2011\), 1-16.](#)

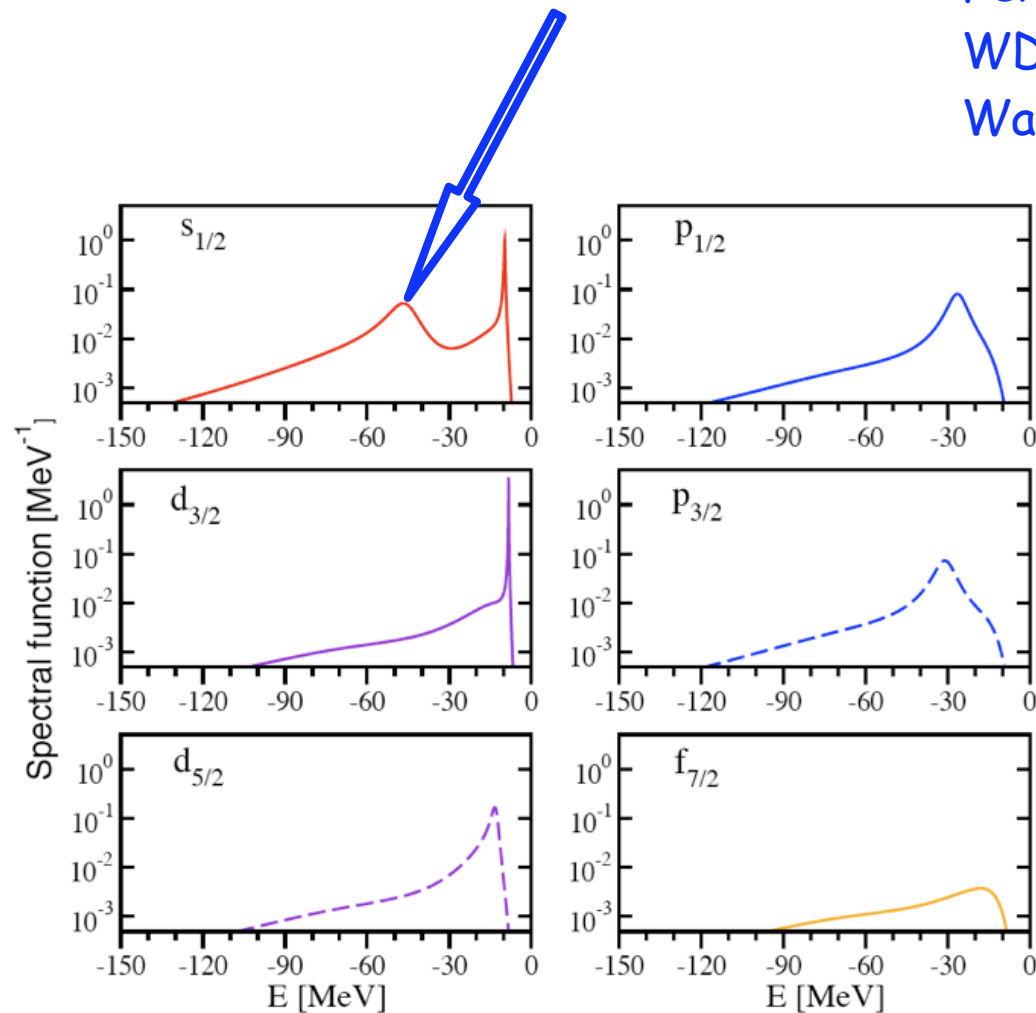
Short-range and Tensor Correlations

Below  $\epsilon_F$

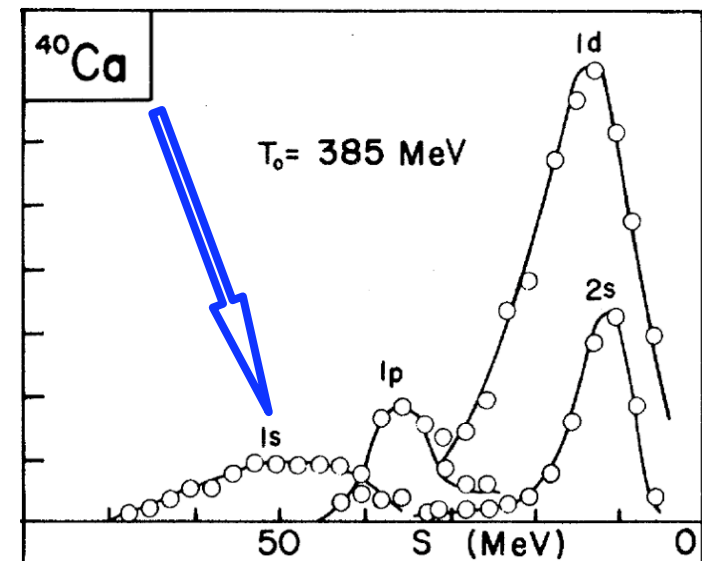
# $^{40}\text{Ca}$ spectral function

Recent theoretical development:  
nonlocal "HF" self-energy --> below the  
Fermi energy

WD, Van Neck, Charity, Sobotka,  
Waldecker, PRC82, 054306 (2010)



Old (p,2p) data from Liverpool

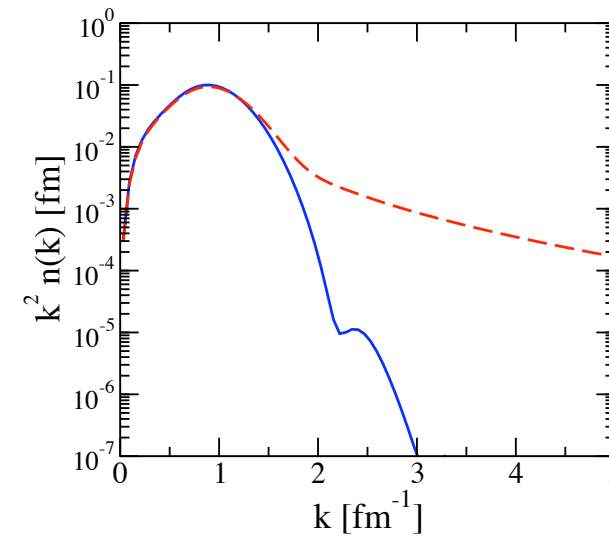
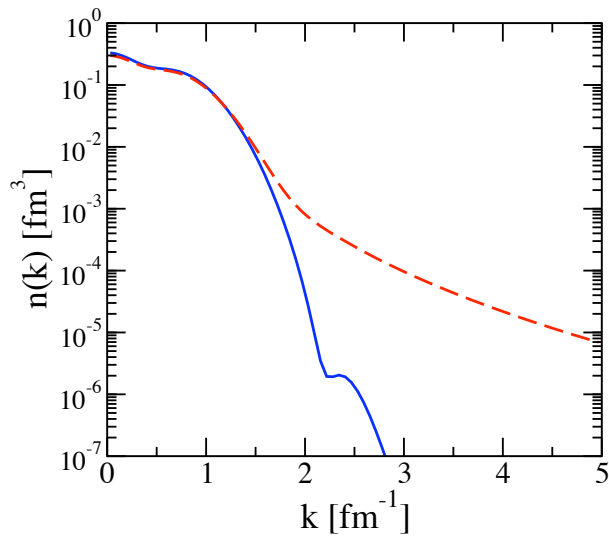
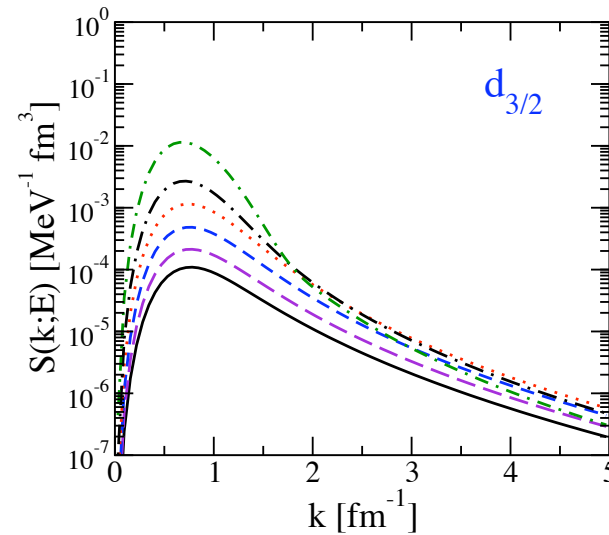
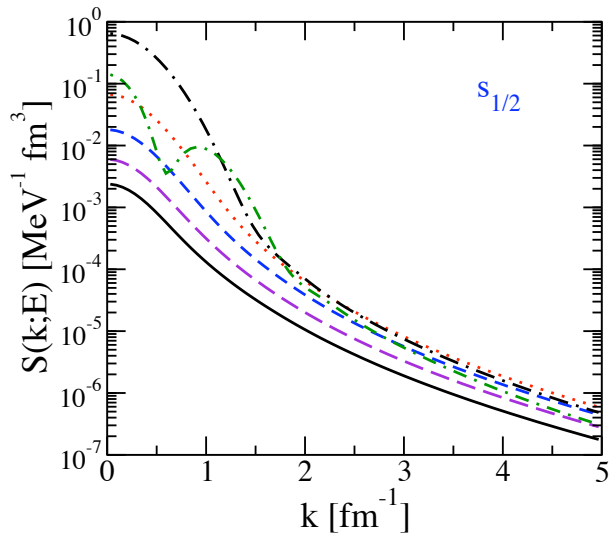


Short-range and Tensor Correlations

# Spectral functions and momentum distributions

•  $^{40}\text{Ca}$

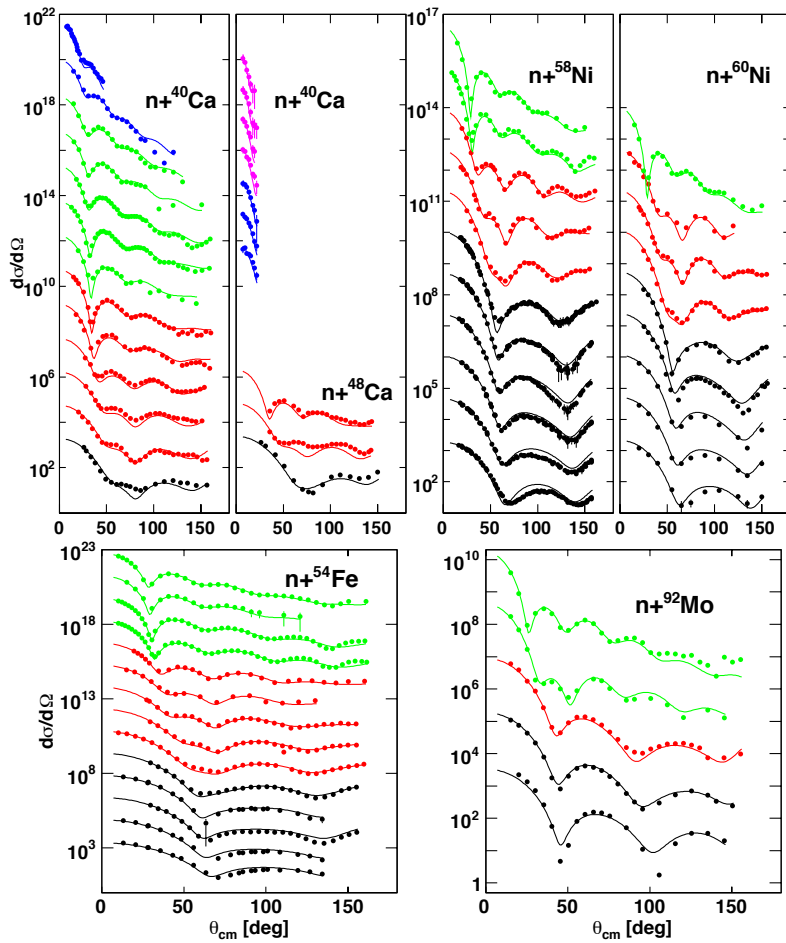
PRC 82, 054306 (2010)



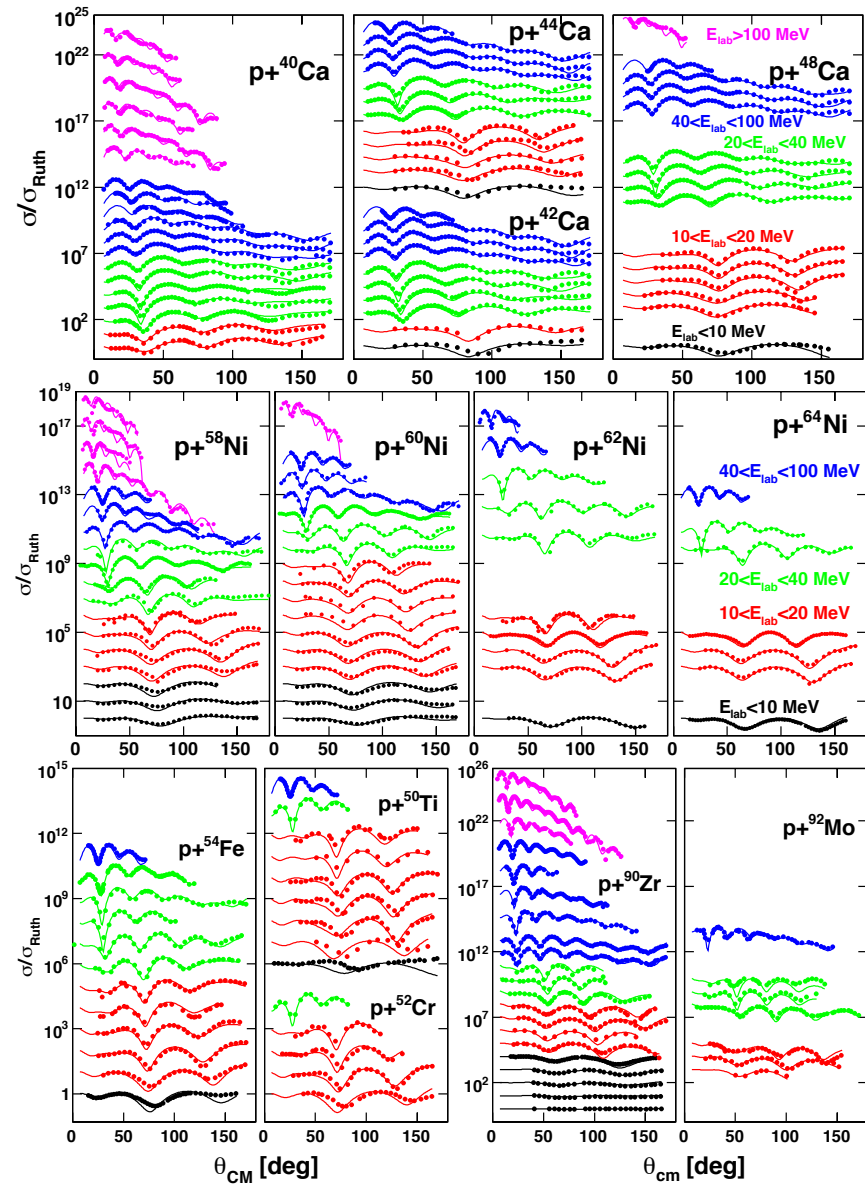


# Elastic scattering data for protons and neutrons

- Abundant for stable targets



[Phys. Rev. C83, 064605 \(2011\)](#)



Short-range and Tensor Correlations

# New DOM implementation in progress

- Particle number --> **nonlocal** imaginary part
- Microscopic FRPA & SRC --> different nonlocal properties above and below the Fermi energy
- Include charge density in fit
- Describe high-momentum nucleons <--> (e,e'p) data from JLab

## Implications

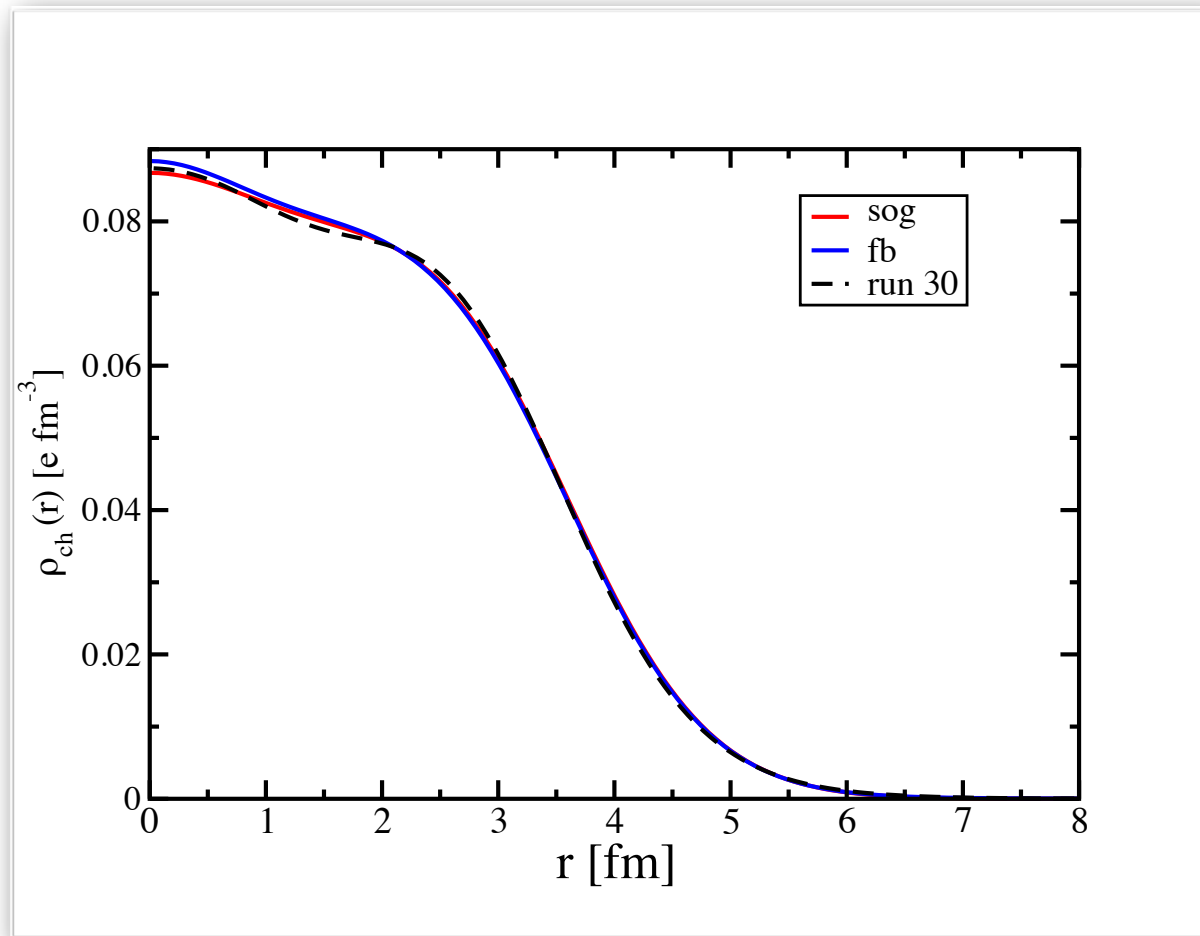
- Changes the description of hadronic reactions because interior nucleon wave functions depend on non-locality
- Consistency test of the interpretation of (e,e'p) possible
- Independent "experimental" statement on size of three-body contribution to the energy of the ground state--> two-body only:

$$E/A = \frac{1}{2A} \sum_{\ell_j} (2j+1) \int_0^\infty dk k^2 \frac{k^2}{2m} n_{\ell_j}(k) + \frac{1}{2A} \sum_{\ell_j} (2j+1) \int_0^\infty dk k^2 \int_{-\infty}^{\epsilon_F} dE E S_{\ell_j}(k; E)$$

Short-range and Tensor Correlations

# Critical experimental data

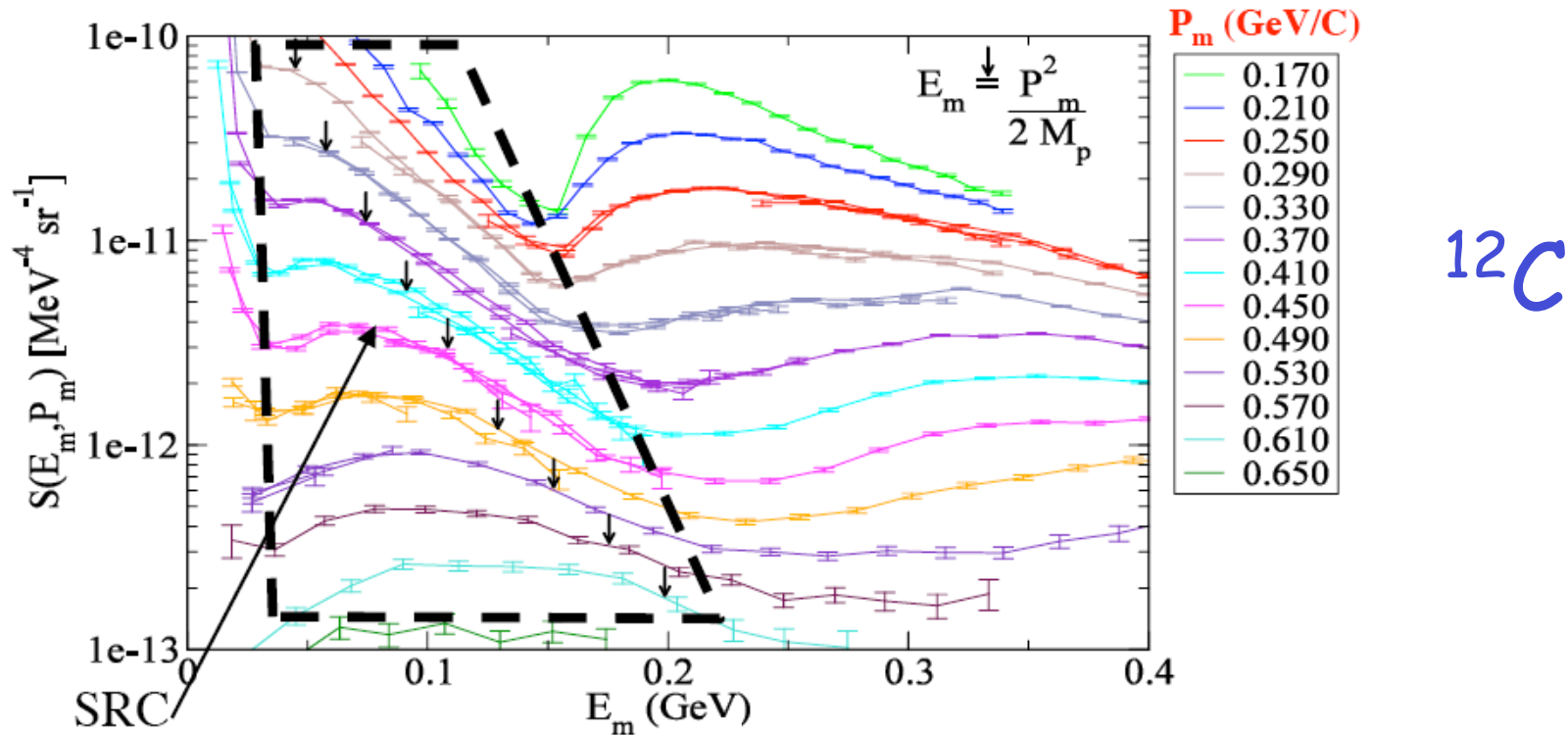
Charge density  $^{40}\text{Ca}$



Short-range and Tensor Correlations

# High-momentum protons have been seen in nuclei!

Jlab E97-006 Phys. Rev. Lett. 93, 182501 (2004) D. Rohe et al.



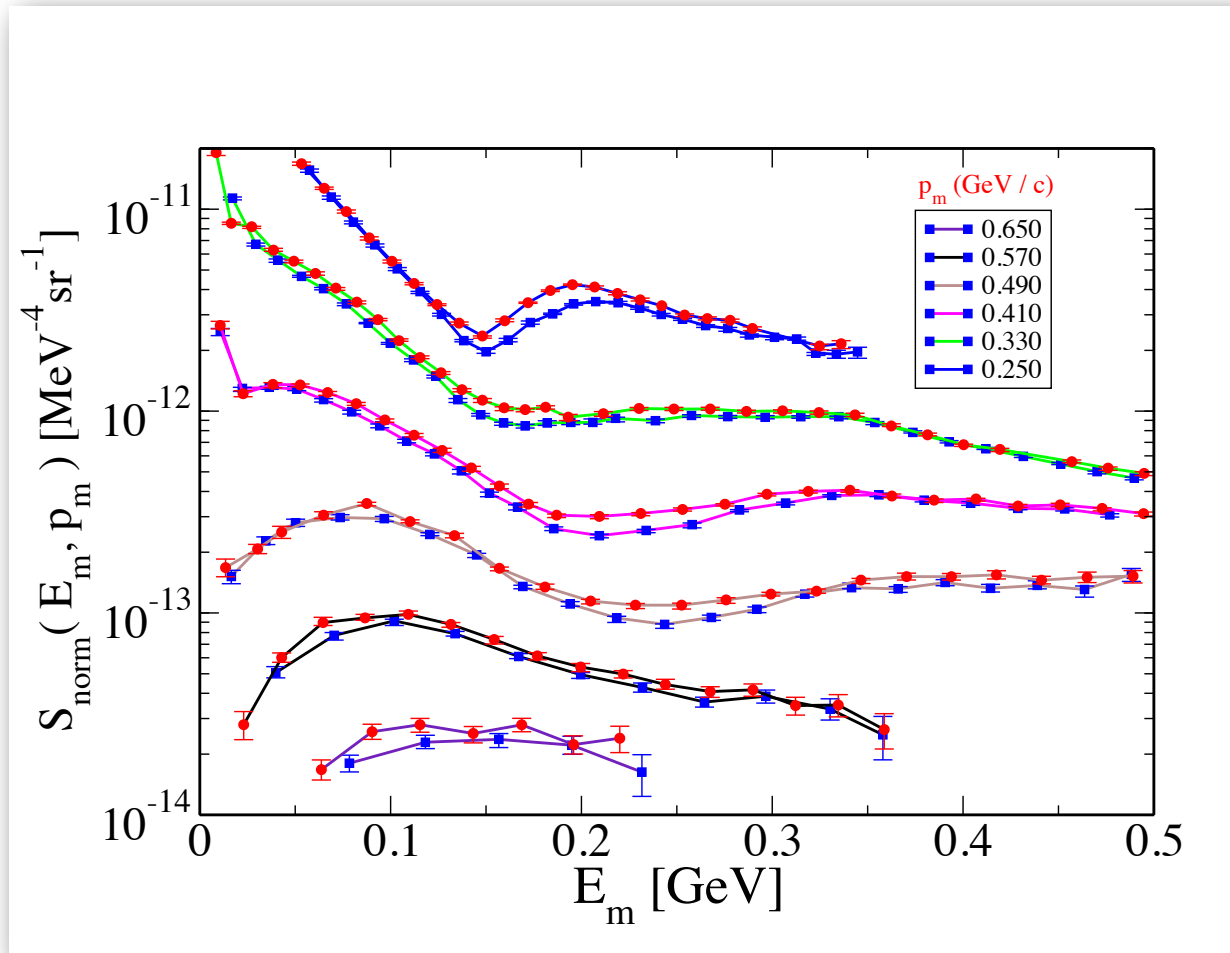
- Location of high-momentum components
- Integrated strength agrees with theoretical prediction Phys. Rev. C49, R17 (1994)

$\Rightarrow \sim 0.6$  protons for  $^{12}\text{C} \Rightarrow \sim 10\%$

Short-range and Tensor Correlations

# High-momentum components

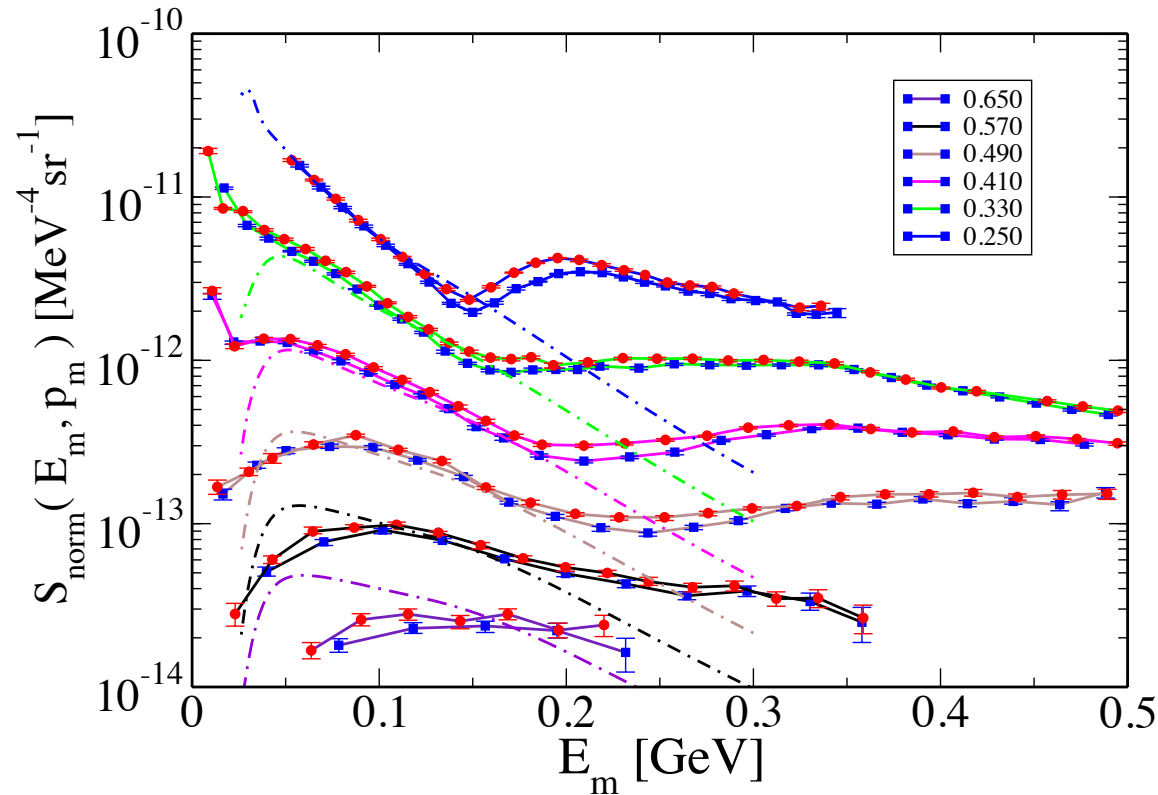
Rohe, Sick et al. Al and Fe (e,e'p) data per proton



Short-range and Tensor Correlations

# Preliminary results

- Mahzoon, Waldecker, Charity, Dussan, WD (2013)



Note: their location in energy yields an important contribution to the energy of the ground state

$$E/A = \frac{1}{2A} \sum_{\ell_j} (2j+1) \int_0^\infty dk k^2 \frac{k^2}{2m} n_{\ell_j}(k) + \frac{1}{2A} \sum_{\ell_j} (2j+1) \int_0^\infty dk k^2 \int_{-\infty}^{\varepsilon_F} dE E S_{\ell_j}(k; E)$$

Short-range and Tensor Correlations

# Conclusions and Outlook

- Given a realistic NN interaction, its implications for the role of short-range and tensor correlations can be calculated reliably for infinite matter of any nucleon asymmetry, density, and temperature
  - Two-body spectral function and momentum distributions this year
- For finite nuclei this is not the case but some efforts have been made
  - Is a difficult challenge but in progress right now...
- Alternative approach for finite nuclei: correlate a lot of data --> DOM --> drip line
  - Will be a tool for FRIB physics as well