

Striking observations in low-energy fission and what they tell us

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Program INT 13-3

Quantitative Large Amplitude Shape Dynamics: fission and heavy-ion fusion
September 23 – November 15, 2013

Work performed in collaboration with Beatriz Jurado.

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by the EFNUDAT (<http://www.efnudat.eu/>) and
by the ERINDA (<http://www.erinda.org/>) projects of the European Union.

Traditional knowledge

Recent experimental progress

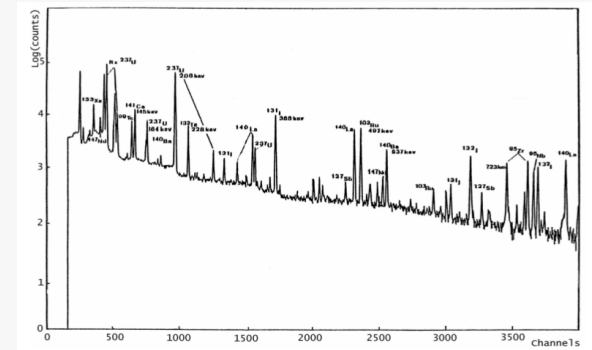
Specific results and interpretation

Conclusion and outlook

Conventional experimental techniques

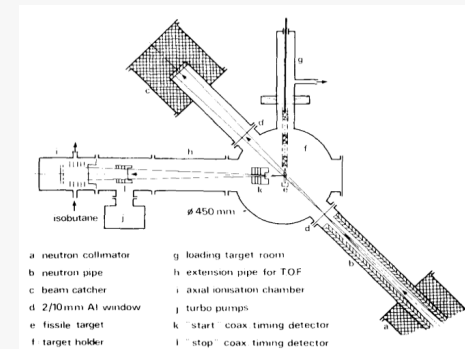
Off-line gamma spectroscopy

No short-lived fragments,
uncertainties from spectroscopic data.



Double ToF – double Energy

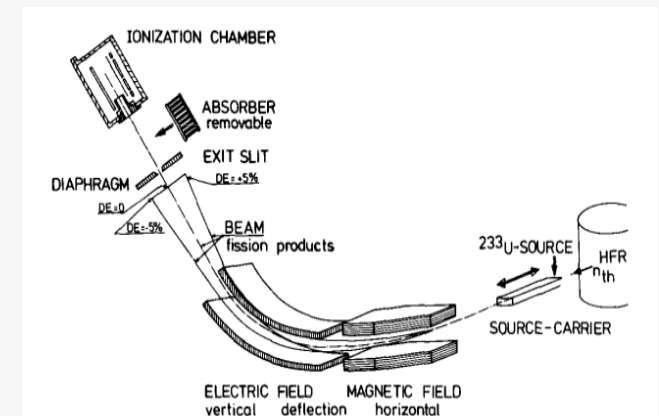
Pre- and post-neutron masses,
limited resolution.



Cosi
Fan
Tutte

Spectrograph LOHENGRIN

A of all fragments,
Z of light fragments
for thermal-neutron-induced fission.



Position of the heavy fragment

229Th

233U

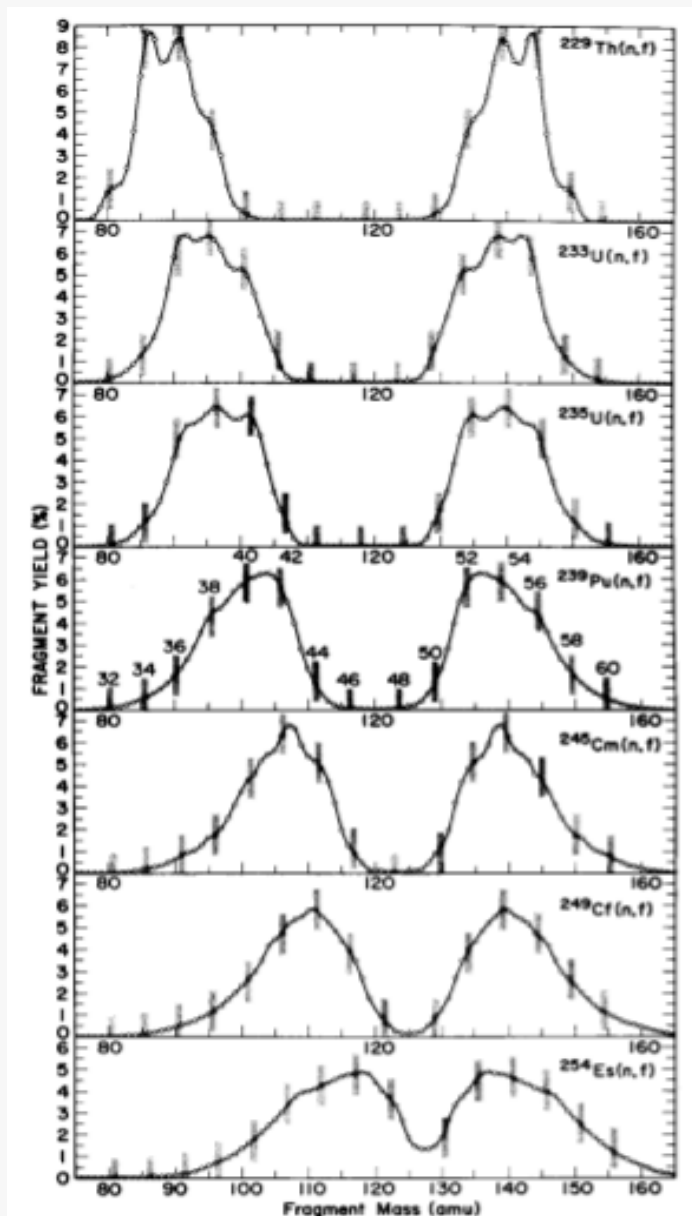
235U

239Pu

245Cm

249Cf

254Es

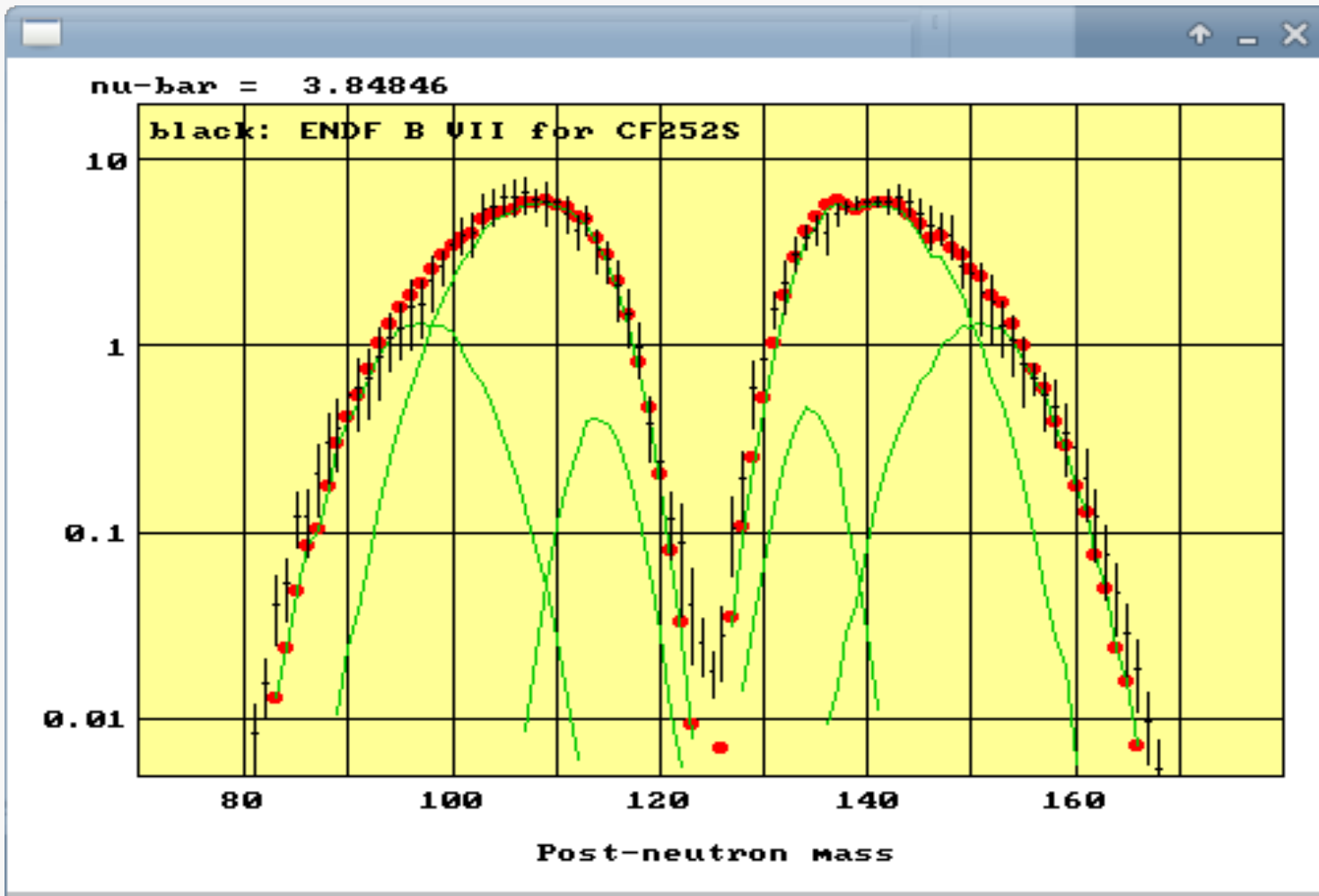


Unik et al., 1973

Fission-fragment mass distribution from $Z=90$ to $Z=99$.

The position of the heavy fragment is constant at $A \approx 140$.

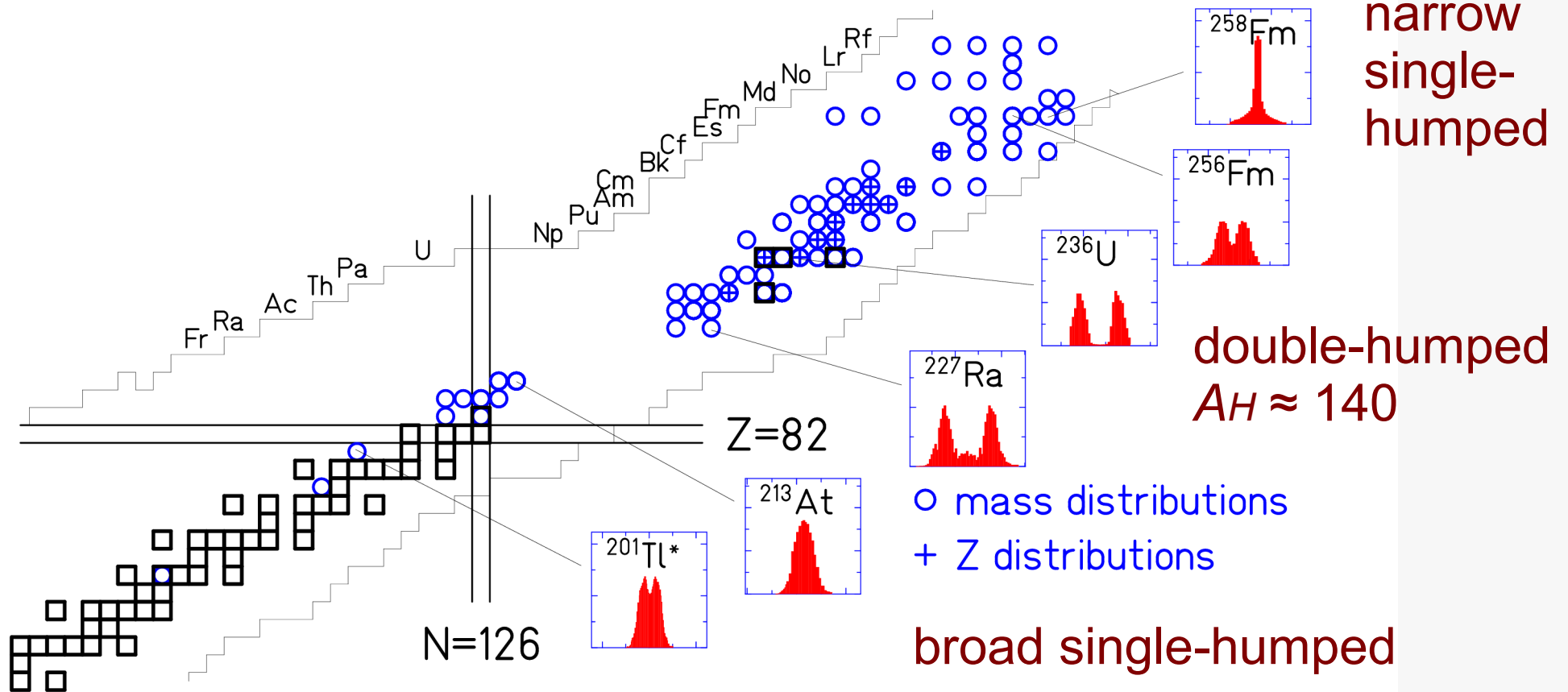
Fission modes



Mass
distribution
of
 $^{252}\text{Cf}(s,f)$

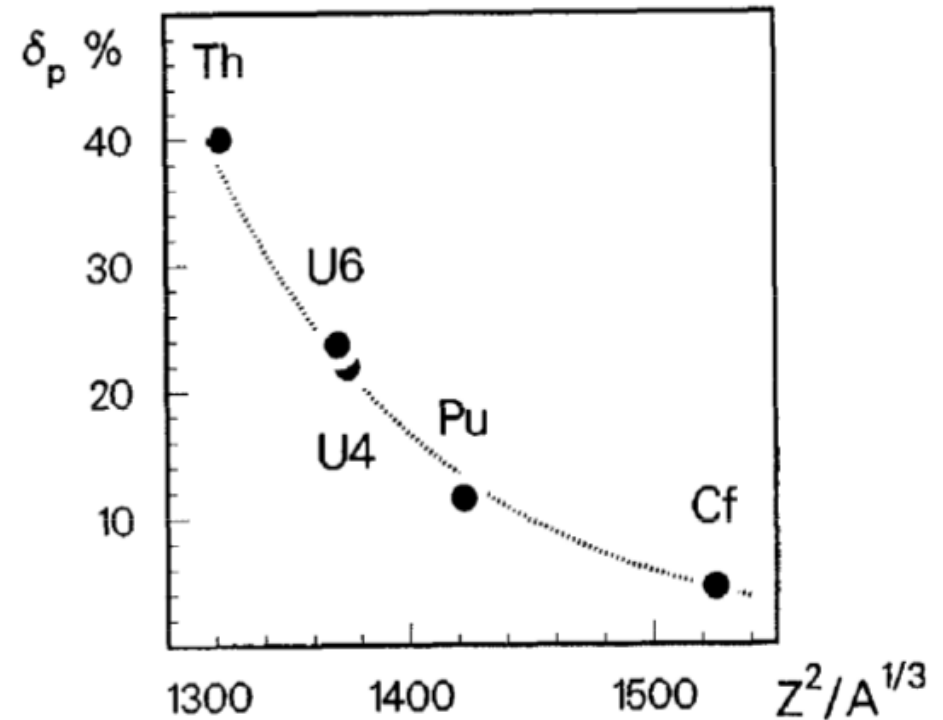
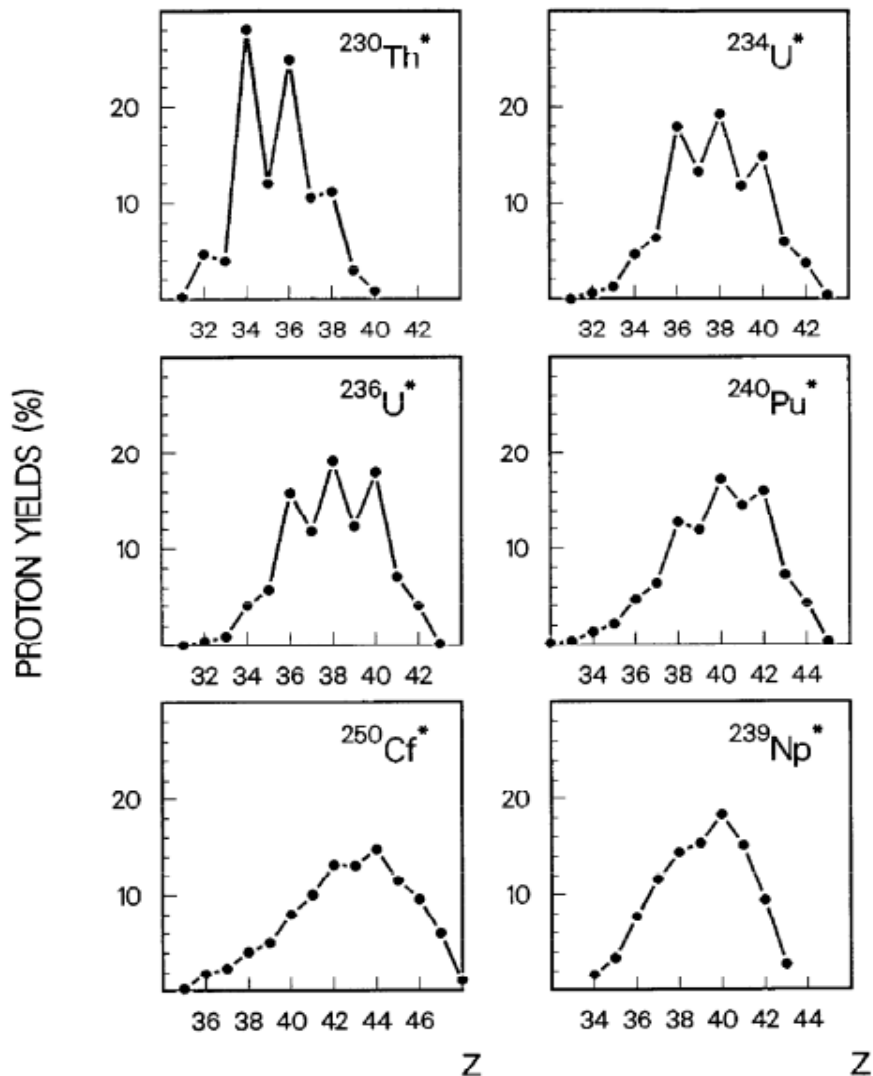
Fission-fragment distributions (A or A-TKE) can be described as the sum of fission modes, associated to valleys in the potential-energy surface.
GEF calculation (www.khs-erzhausen.de).

Global results of conventional experiments



^{201}Tl : Fine structure
 even at
 $E^* = 7 \text{ MeV}$
 above Bf! (Itkis et al., 1985-1991)

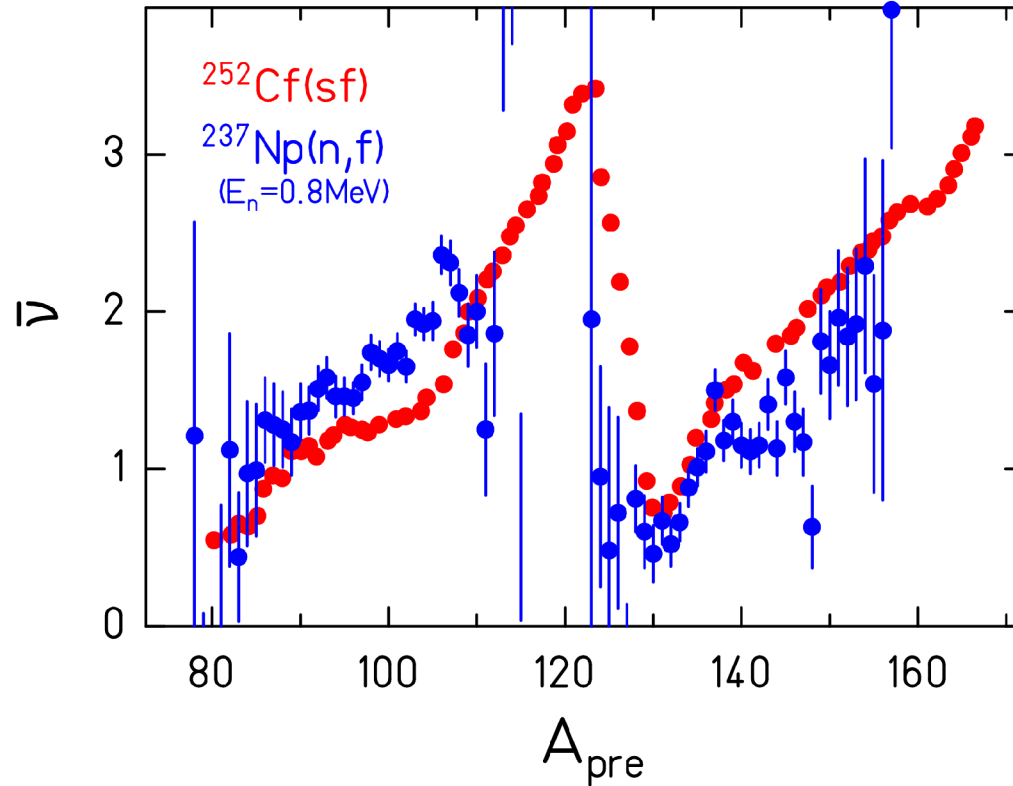
Global even-odd effect in fission-fragment Z distributions



Bocquet, Brissot, NPA 502
(1989) 213c

Systematic variation of
even-odd effect with the
Coulomb parameter.

Prompt-neutron multiplicities

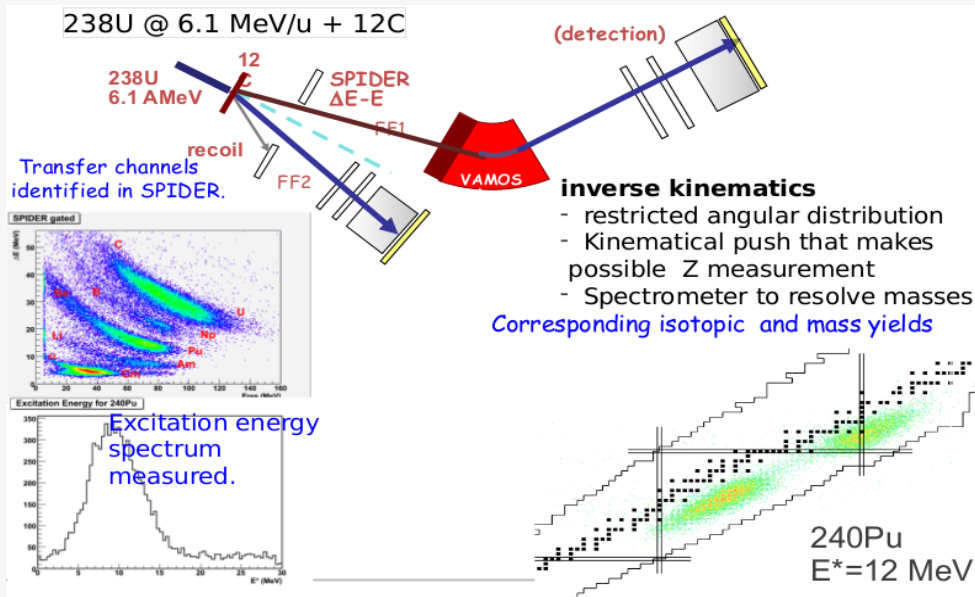


Zeynalov et al., 2012 /
Naqvi et al., PRC 34
(1986) 218

Sawtooth behaviour in the actinides

Recent experimental progress 1

Extended choice of fissioning systems

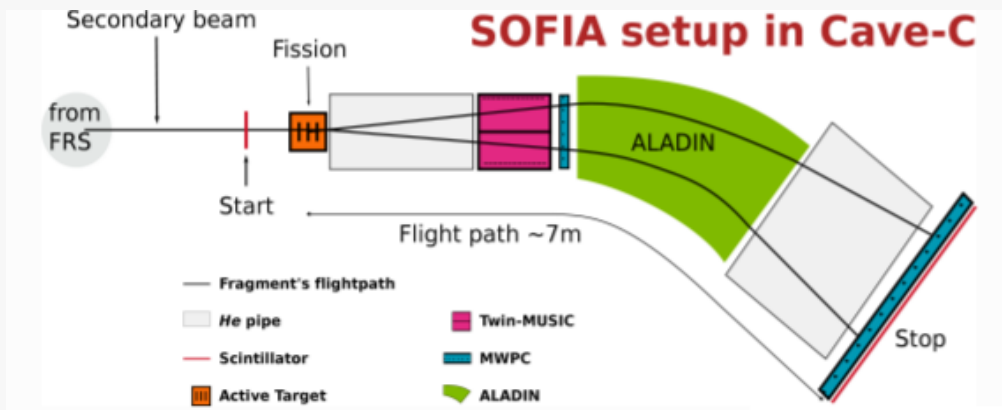


Beta-delayed fission
A. Andreyev et al.

Transfer-induced fission
K. Nishio et al.

←
Transfer-induced fission
(GANIL, F. Farget et al.)

←
Electromagnetic-induced fission
(GSI, J. Taieb et al.)



Recent experimental progress 2

Unambiguous identification of Z and A in experiments in inverse kinematics

Relativistic heavy beams ($\sim 1 A \text{ GeV}$):

Projectile fragments from fragmentation reactions

($A \leq A_{\text{proj}}$)

@ GSI Darmstadt, Germany

Fast heavy beams ($> 6 A \text{ MeV}$):

Transfer reactions, fusion reactions

(A in some distance to the projectiles, also $A > A_{\text{proj}}$)

@ GANIL Caen, France

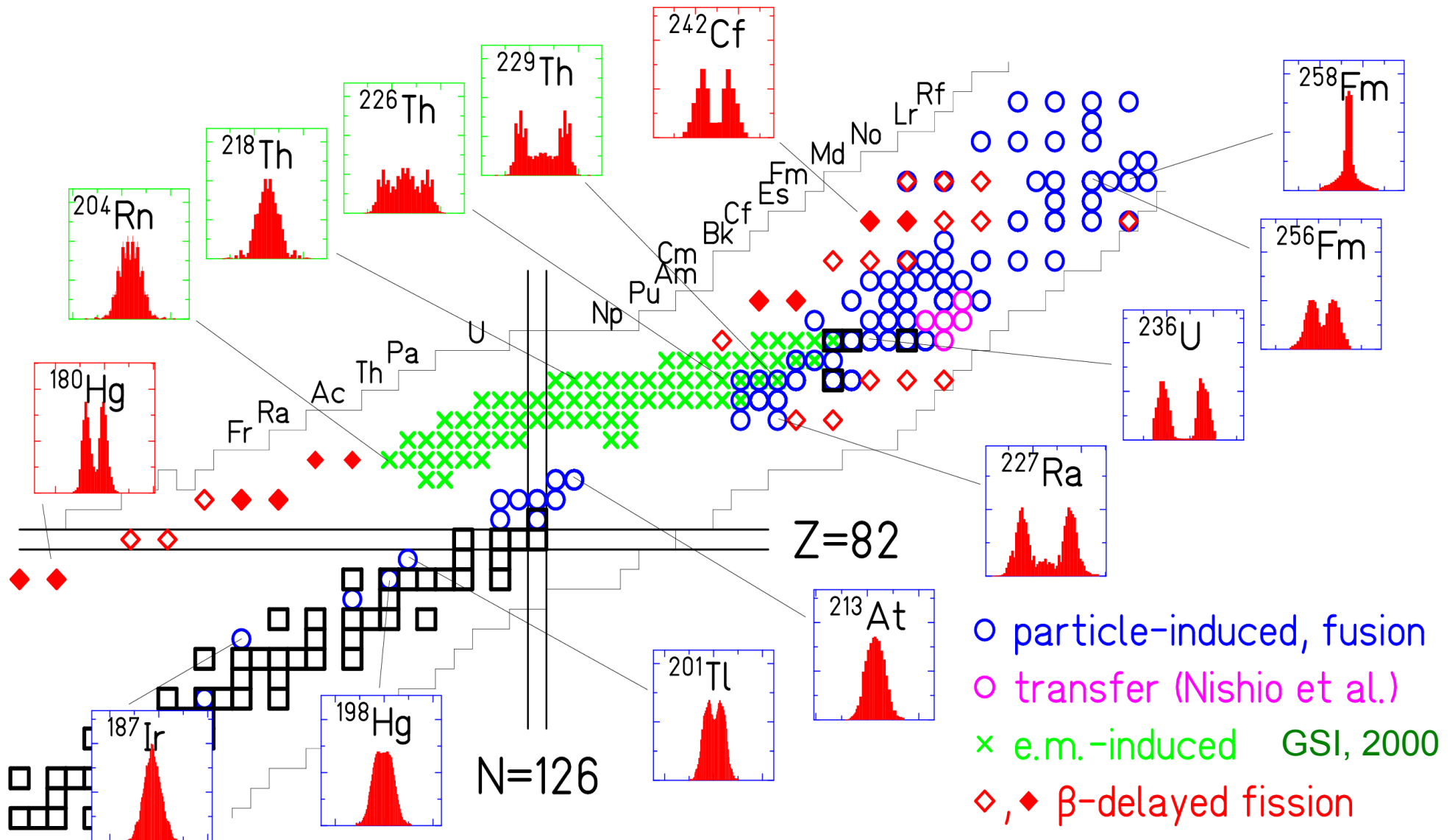
Specific results and interpretation

1. Fission-fragment mass distributions

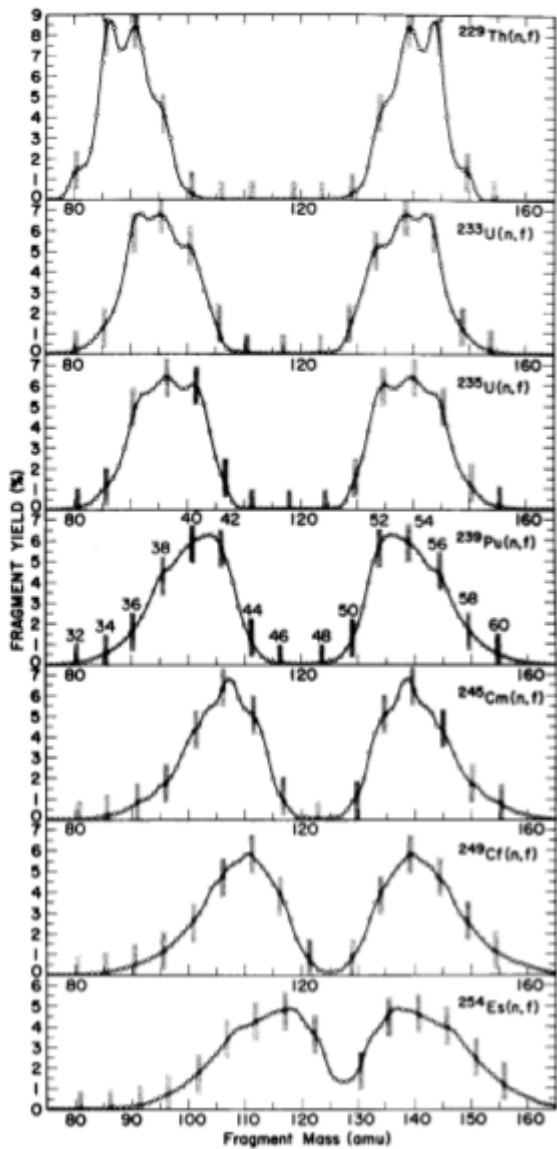
2. Energetics

3. Charge polarization / evaporation

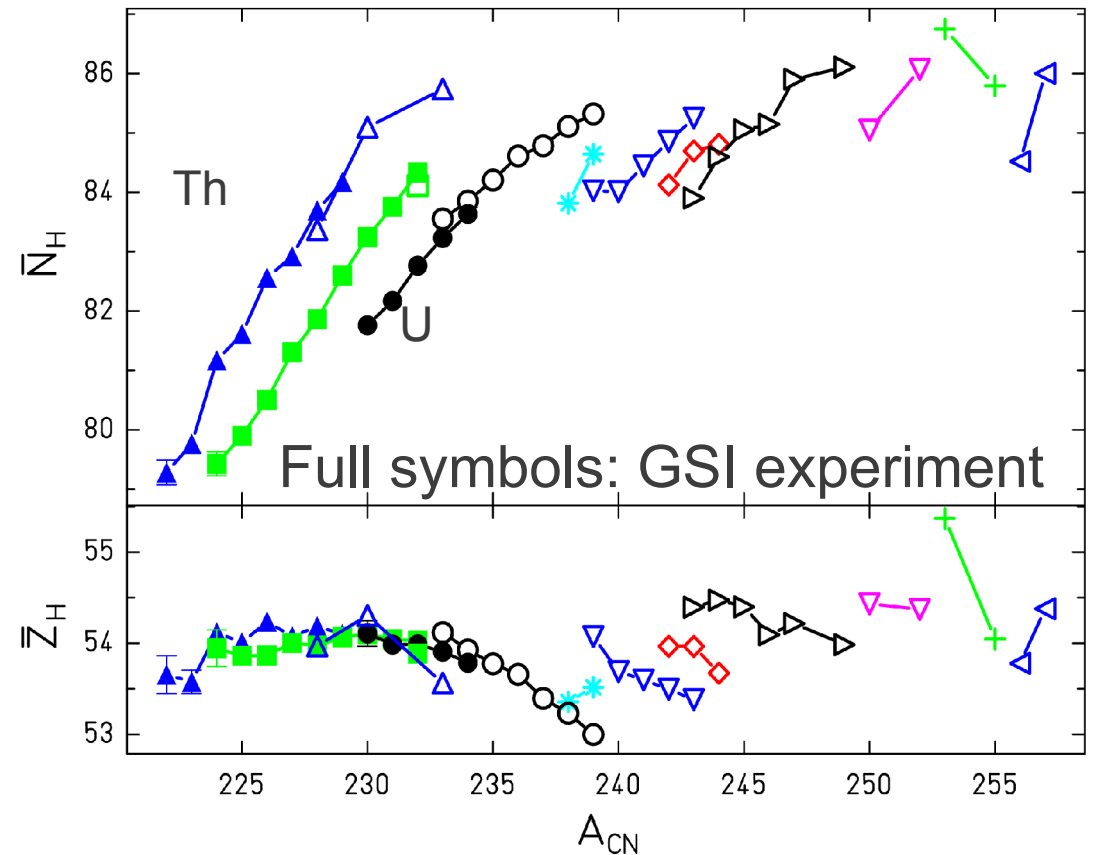
Extended systematics of fission-fragment distributions



Position of heavy fragment for the actinides



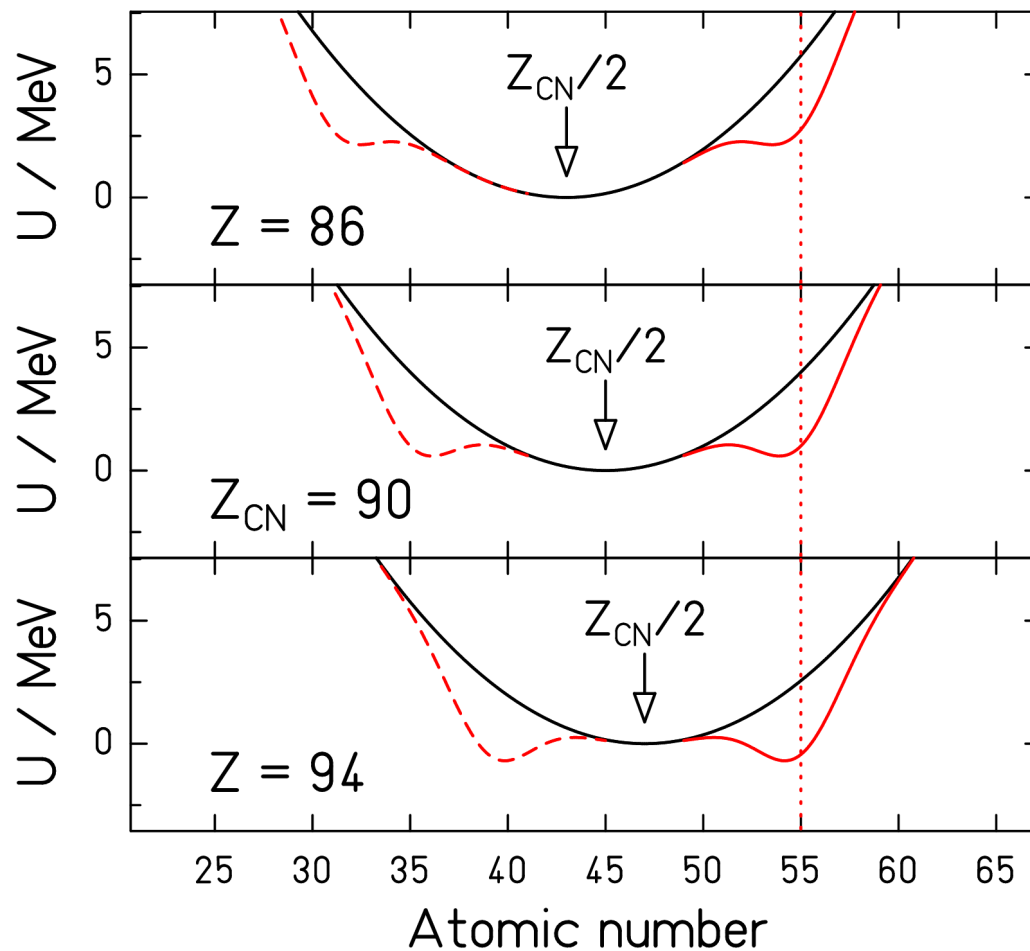
Unik et al., 1973
 $\langle A \rangle \approx 140$



Böckstiegel et al., NPA 802 (2008) 12

Position is constant at $Z \approx 54$ and varies strongly in A and N .
 → **General systematics of PES.**

Competition of mac. and mic. effects



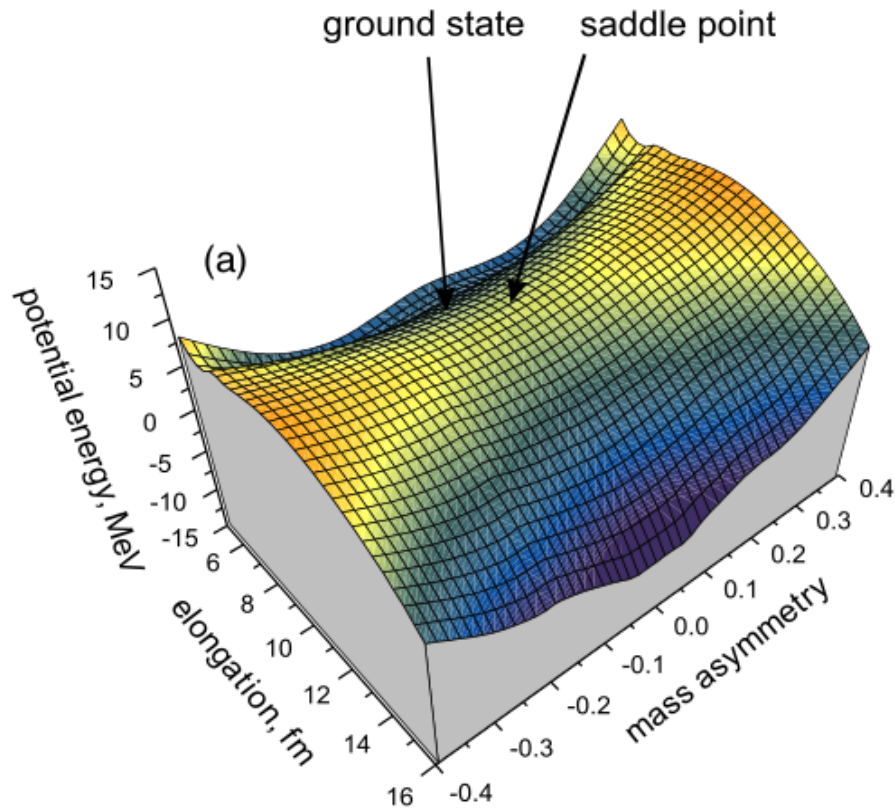
Asymmetric component is caused by shell effect in heavy fragment.

Explains transition from single-humped to double-humped distributions around $A=226$.

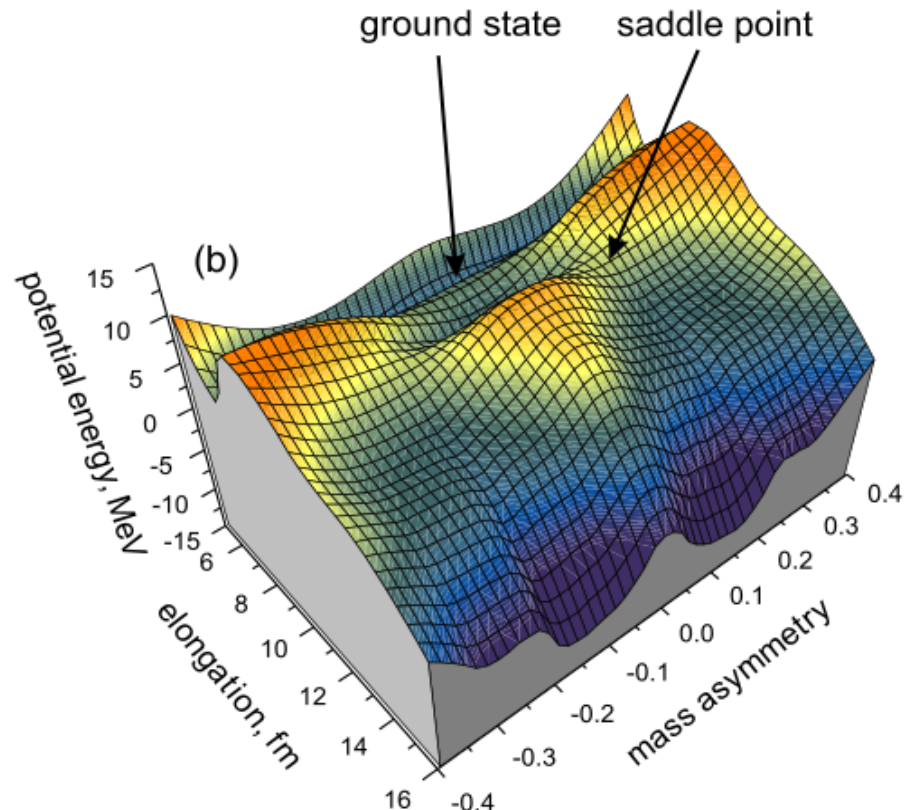
Qualitative idea of [M. Itkis et al. Z. Phys. A 320 \(1985\) 433](#)

Potential energy landscape

2-dim. calculation by A. Karpov, JPG 35 (2008) 035104



liquid-drop potential



With shell effects

Property of the CN

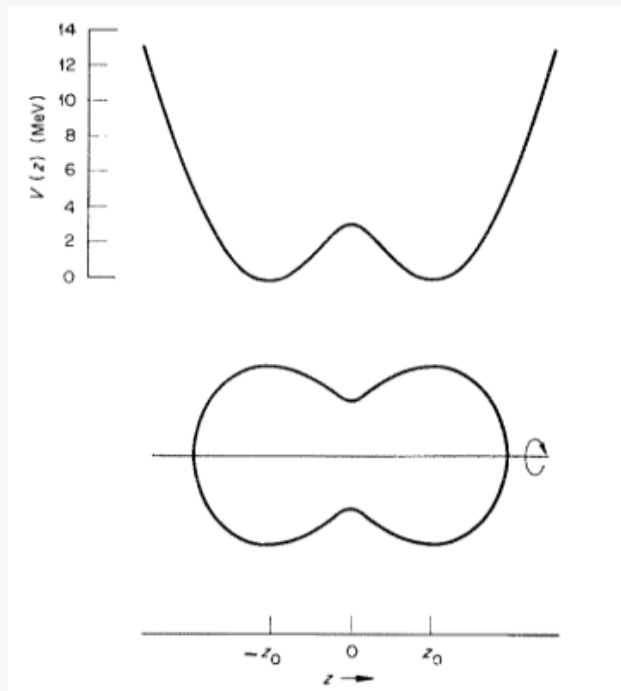
Shells behind outer saddle:
Property of the nascent fragments

→ **Separability principle**

Shells

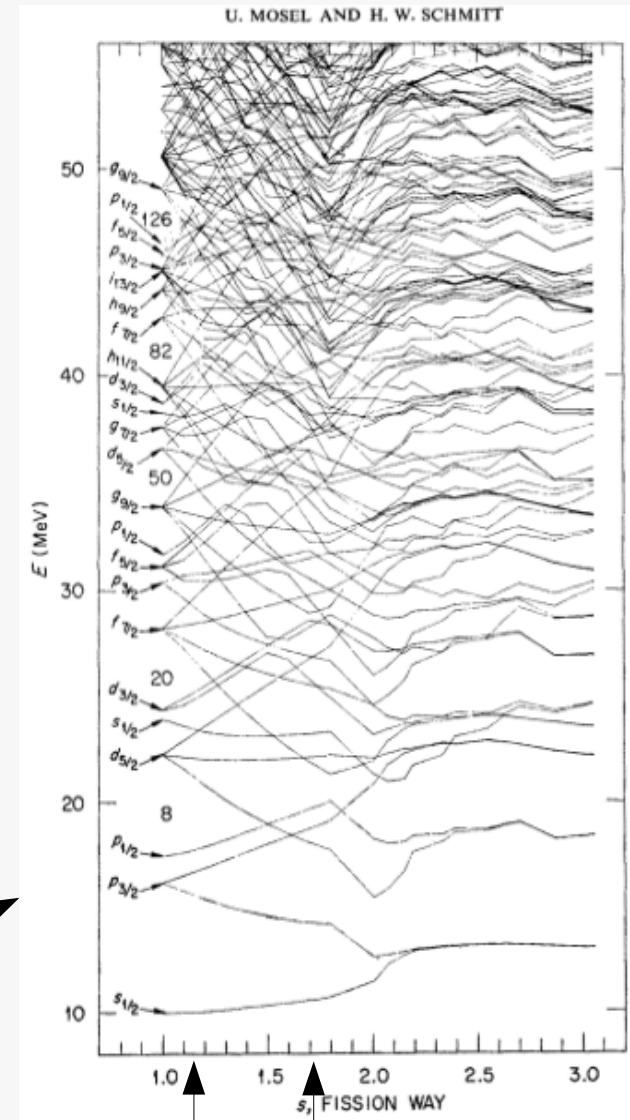
Two-centre shell model developed by:
Holzer, Mosel, Greiner (Nucl. Phys. A138 (1969) 241)

Continuous treatment from ground state to separated fragments.



U. Mosel, H. W. Schmitt
Nucl. Phys. A
165 (1971) 73

Single-particle levels
in a di-nuclear potential

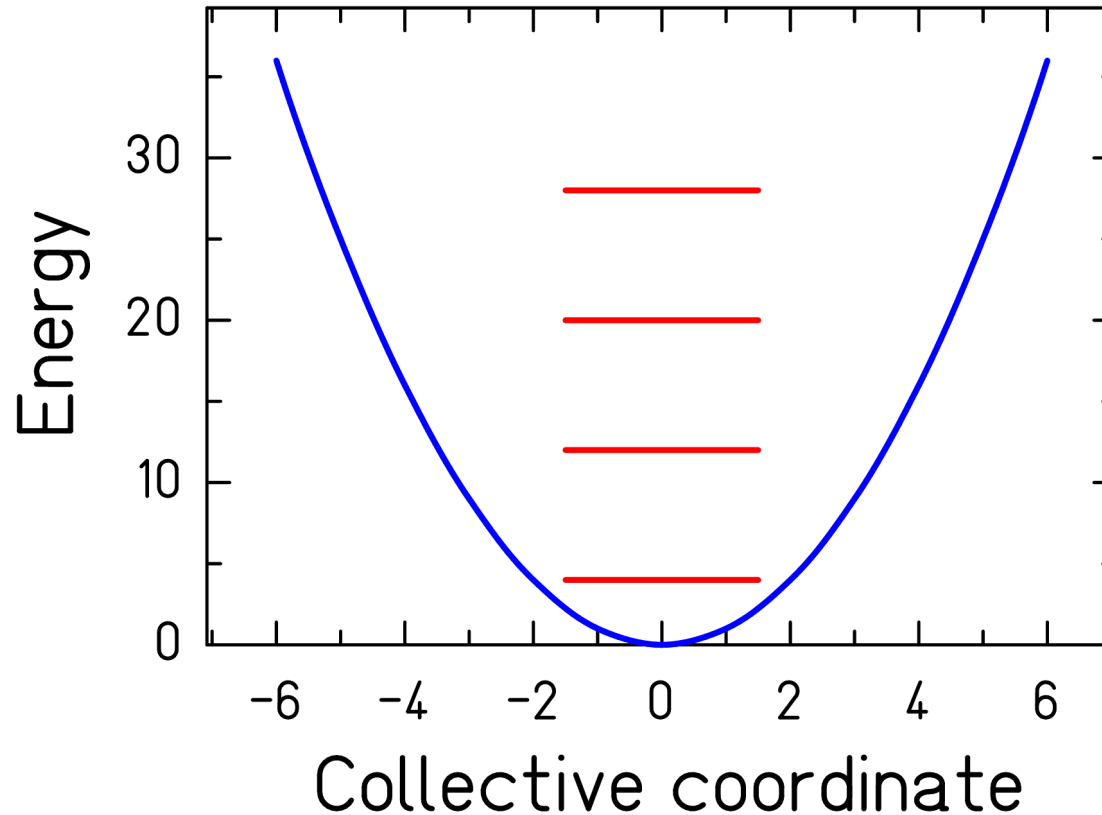


Ground state

Outer saddle

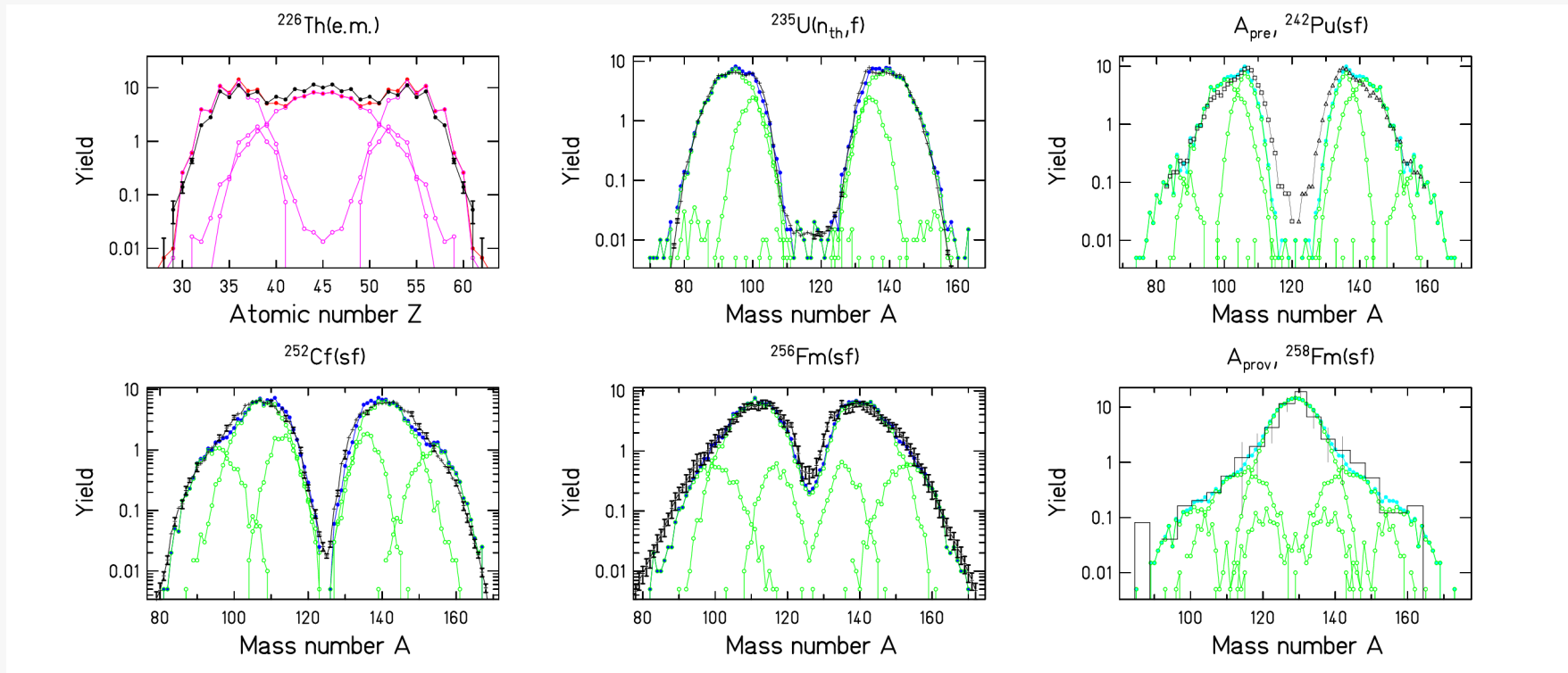
Early manifestation of fragment shells.

Quantum oscillators of normal modes



Assumption: Properties and populations of oscillator states (mass asymmetry, N/Z ratio etc.) in the nuclear heat bath determine the distributions of observables.

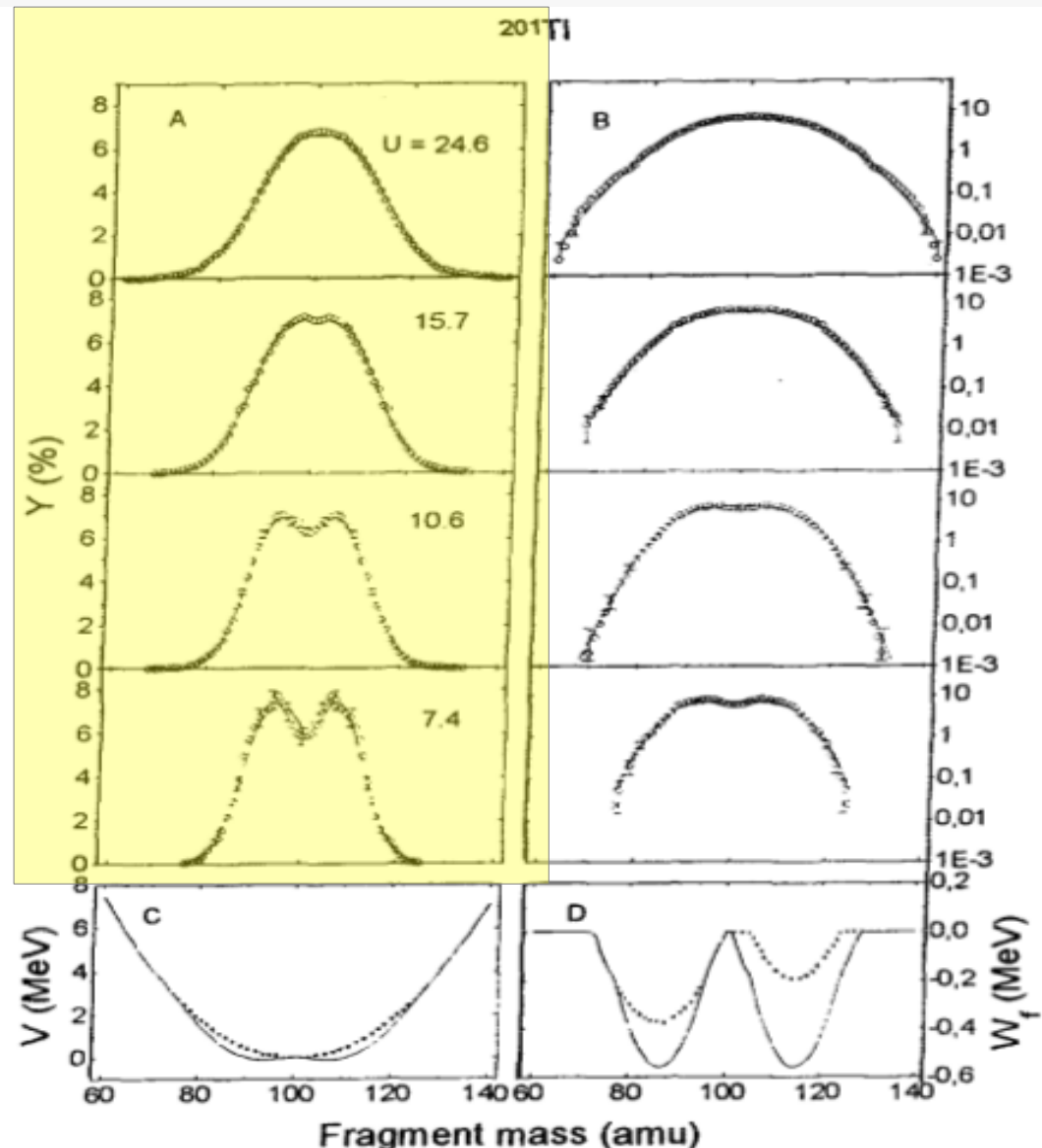
Hidden simplicity of fission !



Variety of mass (Z) distributions very well described with the same fragment shells ($Z \approx 51$, $Z \approx 55$, $Z \approx 59$, $Z \approx 42$)!
(All distributions obtained with the same parameter set: position, depth and width of shells.)

GEF code: www.khs-erzhausen.de or www.cenbg.in2p3.fr/GEF

Thermal washing out of shell effects



Low fission probability:
First-chance fission dominates in ^{201}Tl .

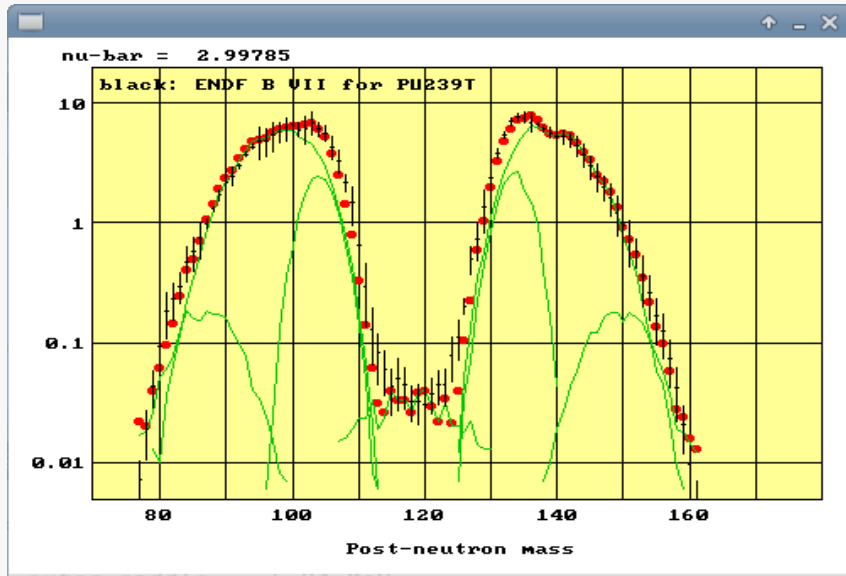
Direct information on thermal washing out of shell effects in fission-fragment mass distributions (PES).

U = energy above B_f

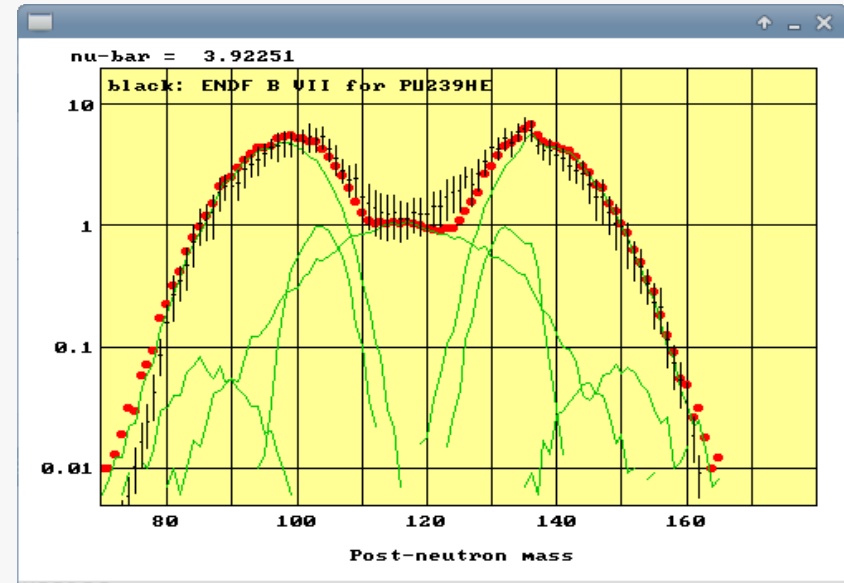
M. Itkis et al., SJNP 41 (1985) 544

Thermal shift of fission channels

$E_n = \text{thermal}$

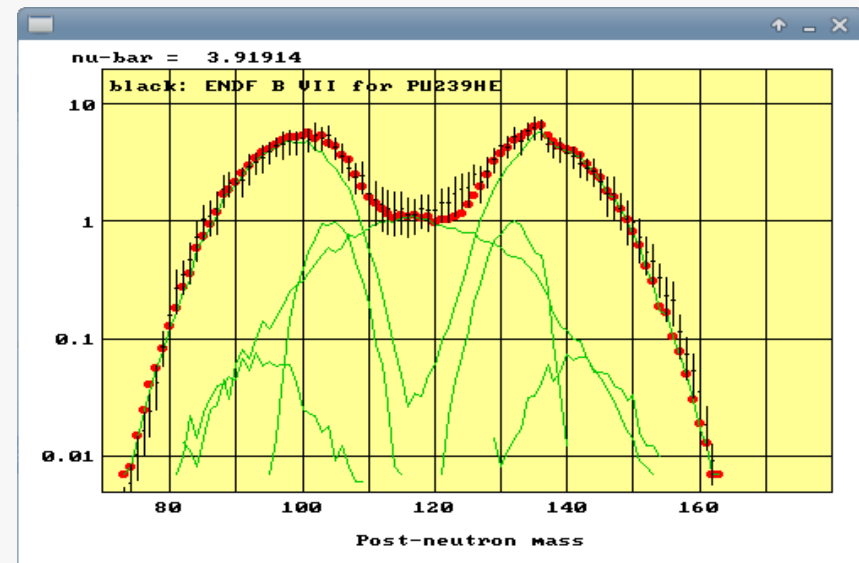


$E_n = 14 \text{ MeV}$



Increasing influence of
macroscopic potential with E^* :
Shift towards symmetry \rightarrow

Calculations with the GEF code
www.khs-erzhausen.de



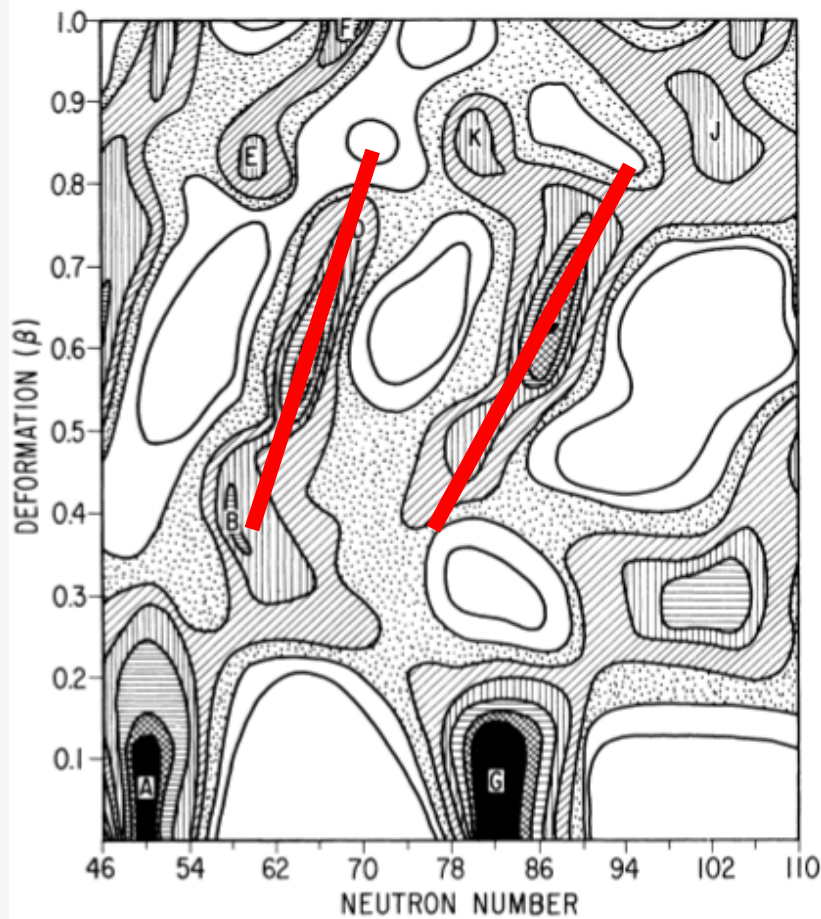
Specific results and interpretation

1. Fission-fragment mass distributions

2. Energetics

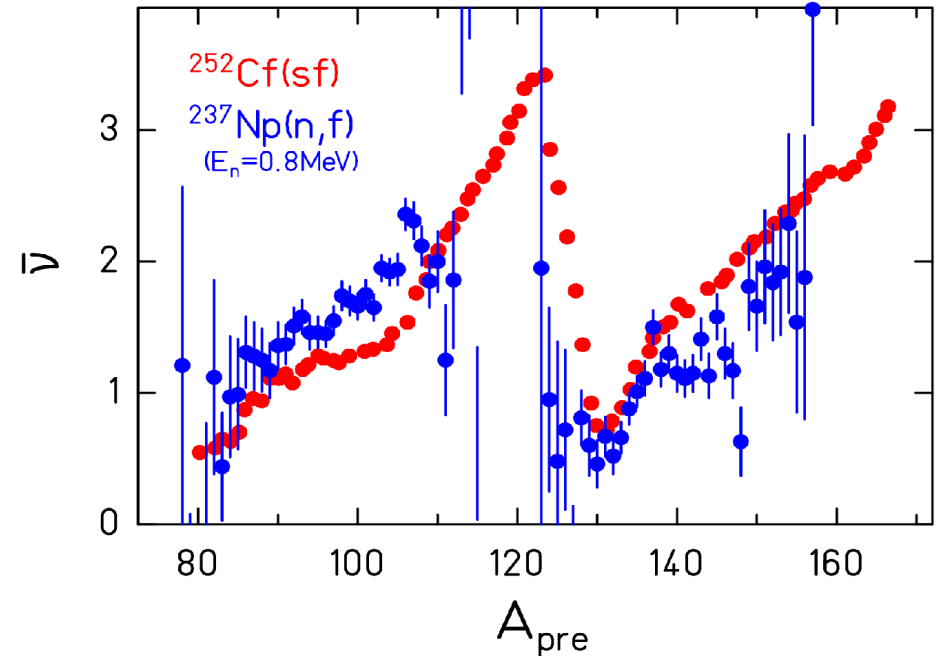
3. Charge polarization / evaporation

Fragment deformation \rightarrow prompt neutrons



Wilkins et al., Phys. Rev. C 14 (1976) 1832

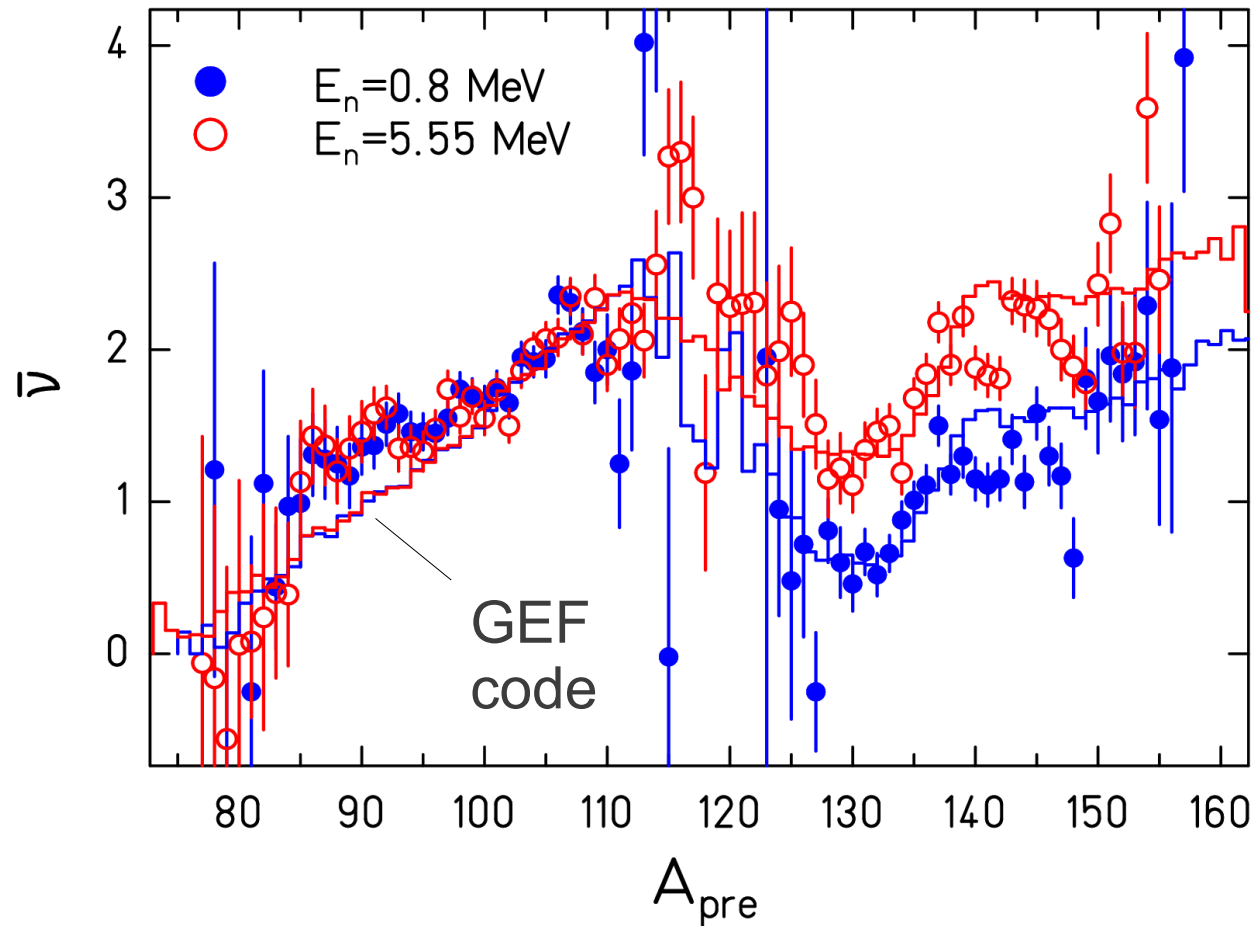
General systematics of deformed shells:
Correlation particle number \leftrightarrow deformation
(Additional influence of mac. potential.)



Naqvi et al, 1986 / Zeynalova et al., 2012

**Saw-tooth behaviour
reflects fragment
deformation at
scission.**

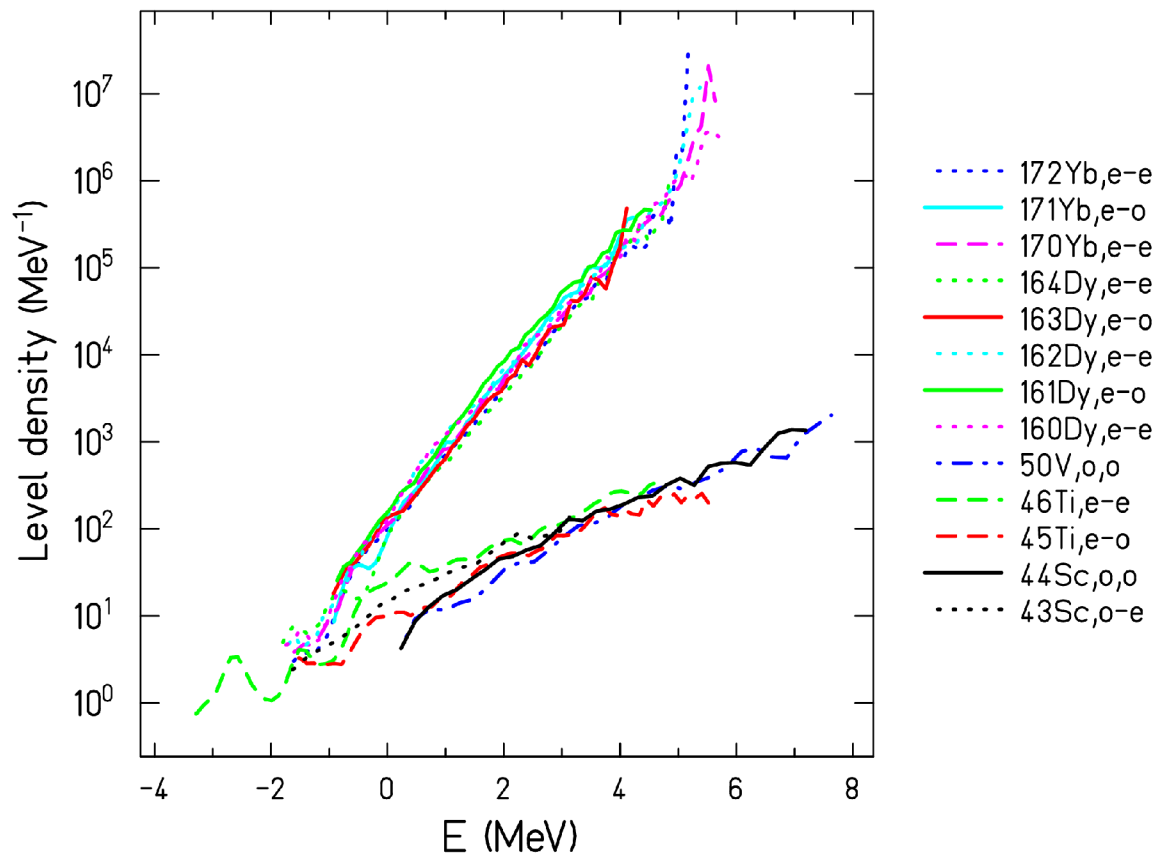
Prompt-neutron yields



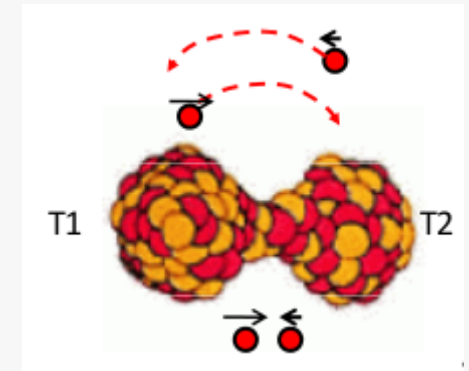
Experiment: Naqvi et al., 1986

All additional energy of the neutron ends up in the heavy fragment.

New results on level densities suggests energy sorting in fission



Guttormsen et al. 2012



Nascent fragments:

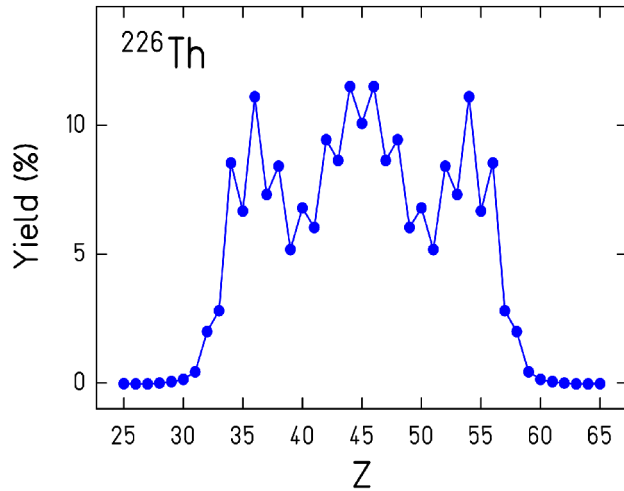
Two thermostats in contact.

→ Energy sorting

Schmidt, Jurado,
PRL 104 (2010) 212501

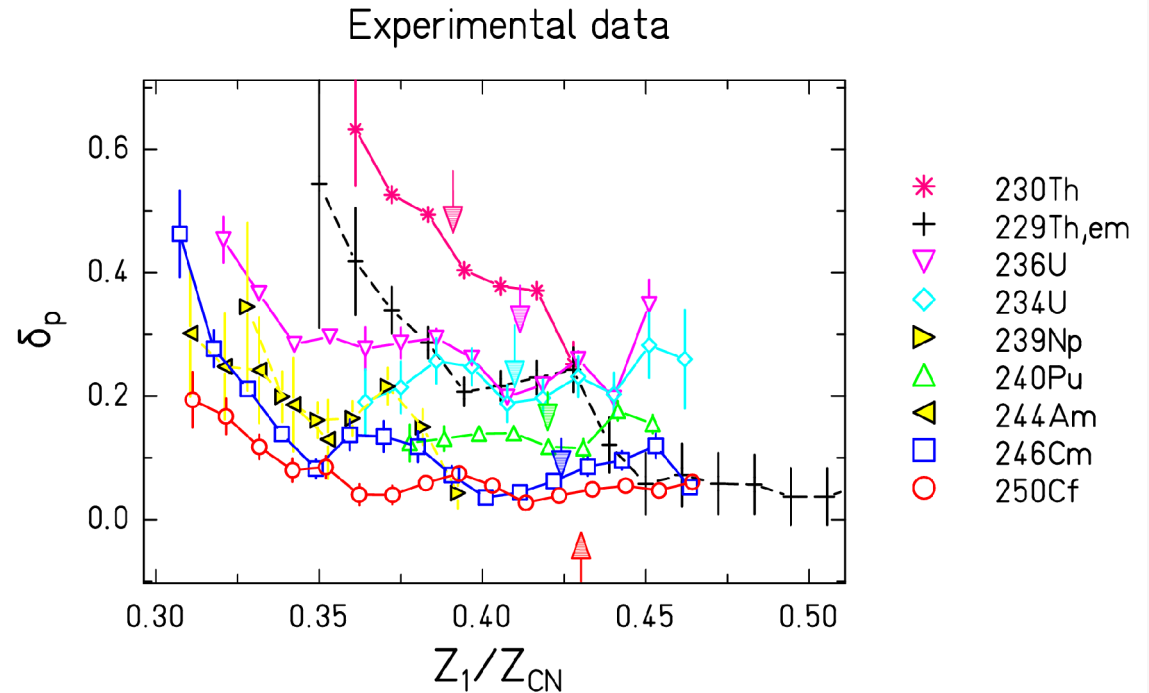
Constant nuclear temperature at low E^* .

Influence of asymmetry on even-odd effect



Schmidt et al., 2000

GSI-experiment:
Z distribution measured
over the whole range.



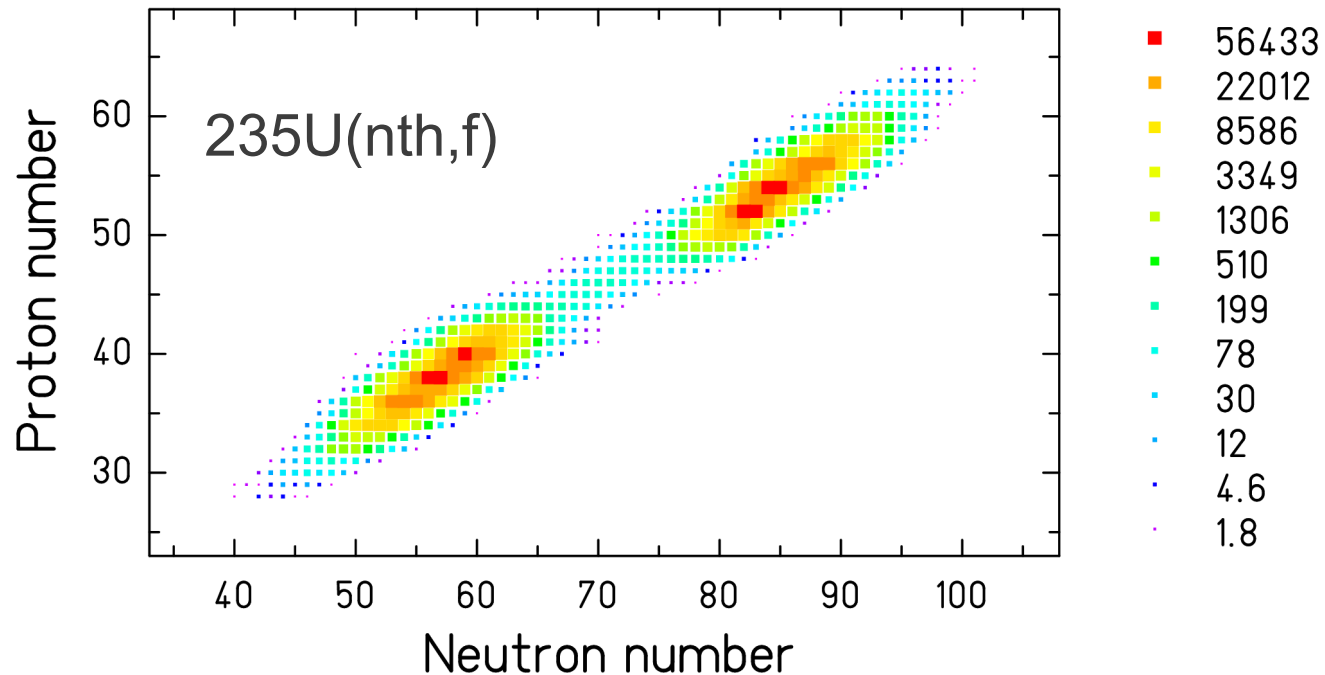
Caamano et al., 2011

Systematics:
Even-odd effect strongly enhanced
in asymmetric splits.
→ **even-even light fragments =
end products of energy sorting**

Specific results and interpretation

1. Fission-fragment mass distributions
2. Energetics
3. **Charge polarization / evaporation**

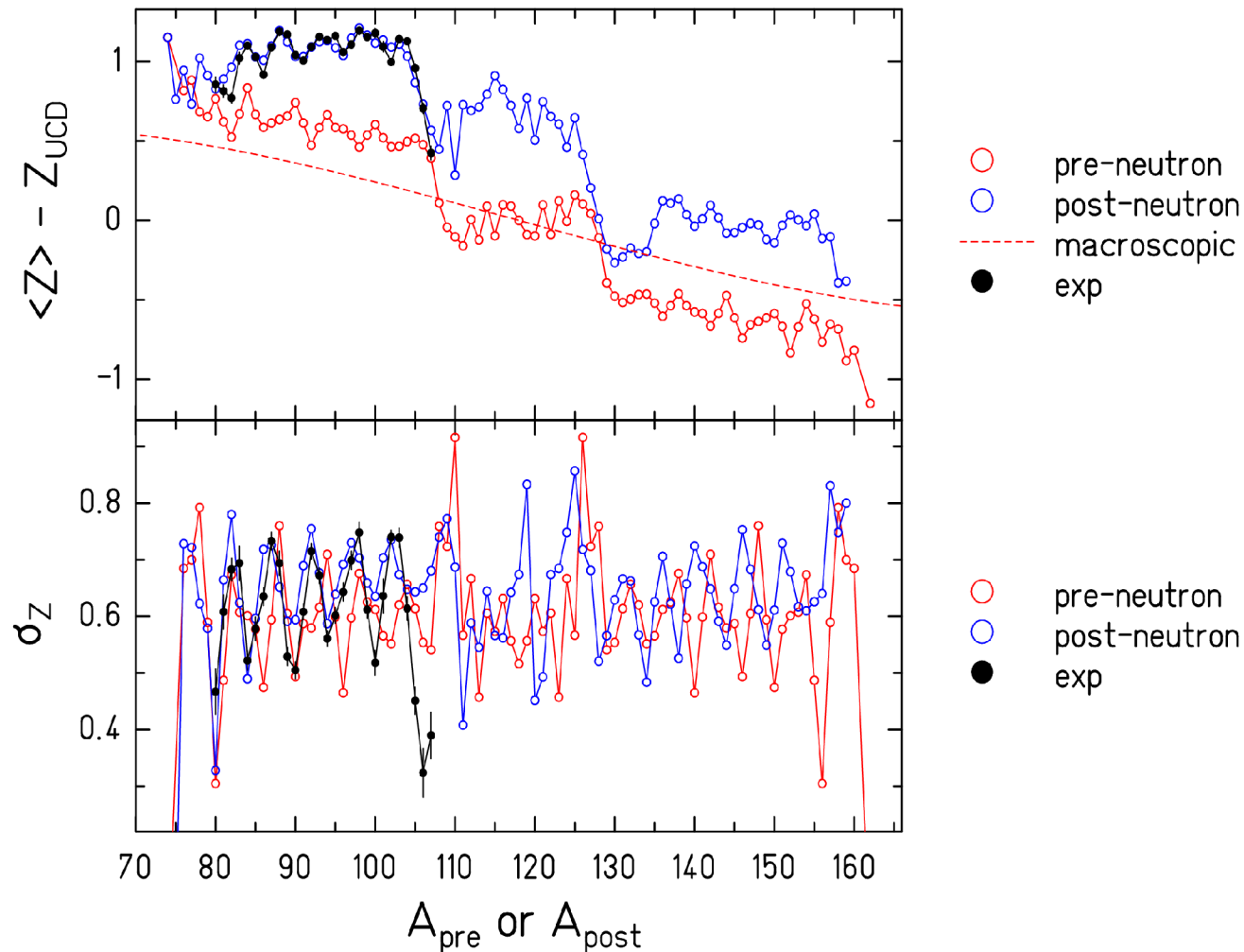
Nuclide distribution



GEF calculation

More than 500 nuclides produced.
Deviation from UCD: shift and fluctuations.

Information on charge polarization



$^{235}\text{U}(n\text{th},f)$

Moments of isobaric Z distributions.

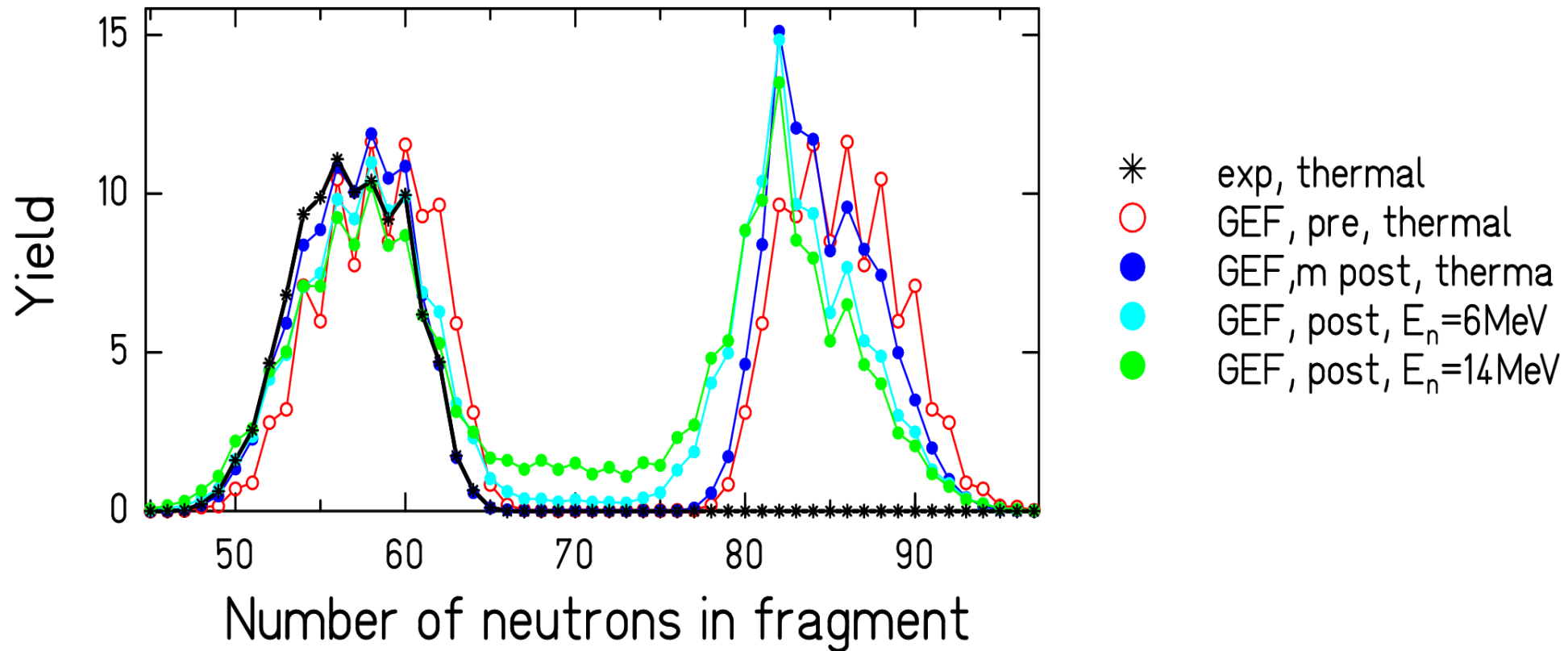


Influence of macroscopic potential, shell effects and evaporation.

GEF code and experiment.

→ Full resolution in A and Z required!

Even-odd effect in ff neutron number

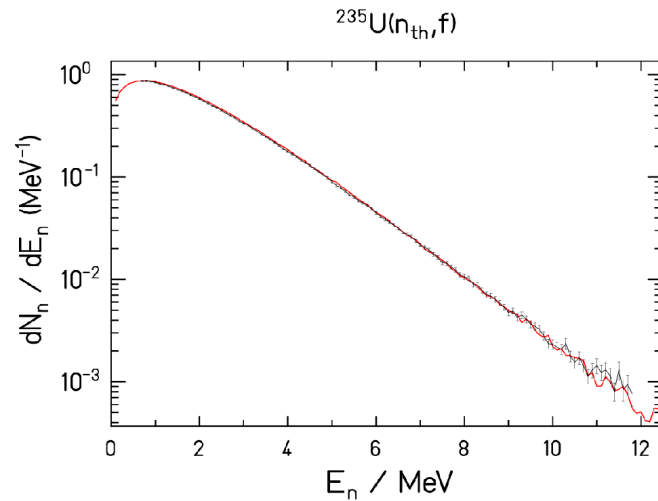


Even-odd effect in neutron number of fragments (post-neutron) is created by evaporation. (Does not depend on E^* !)

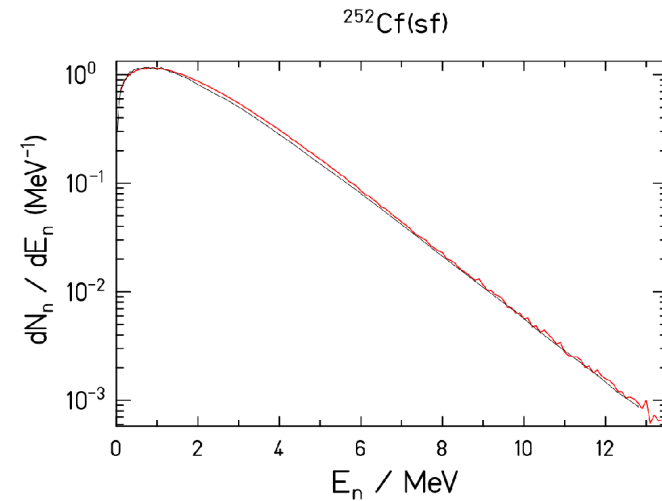
Influence of pairing on binding energies and level densities.

M. V. Ricciardi et al., Nucl. Phys. A 733 (2004) 299

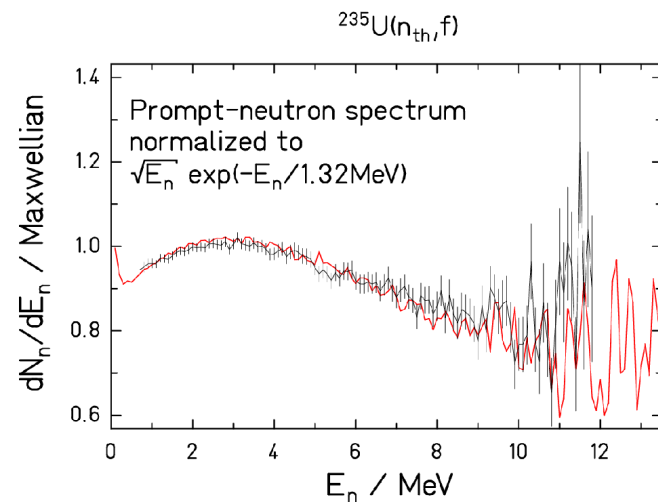
Energy spectra of prompt neutrons



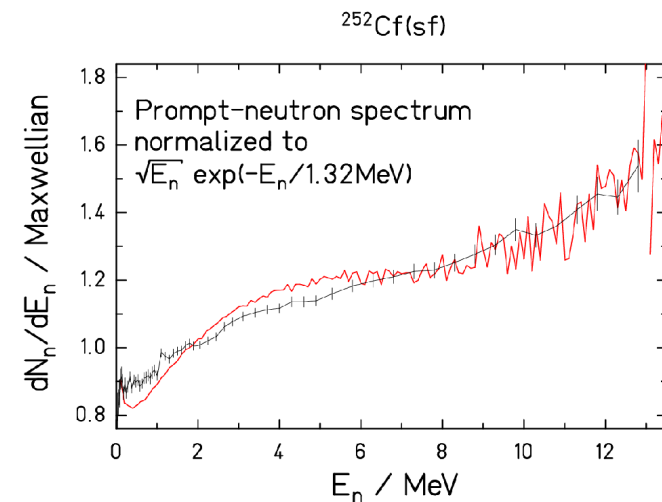
— GEF
— Kornilov



— GEF
— Mannhart



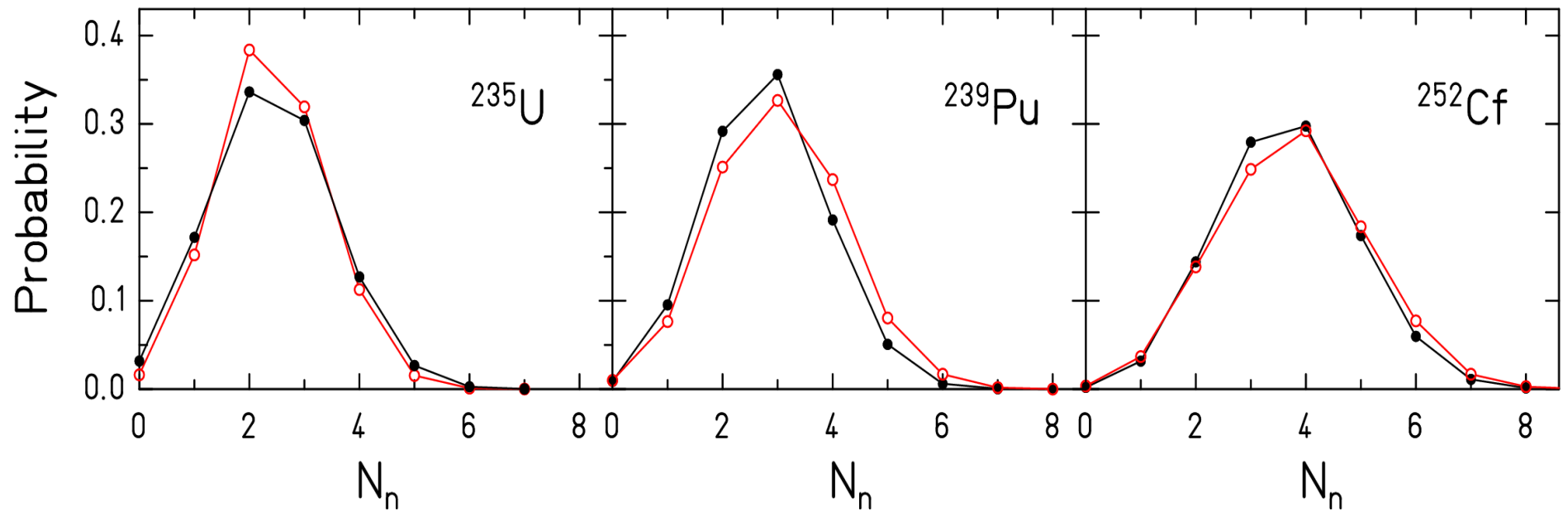
— GEF
— Kornilov



— GEF
— Mannhart

Clue: Modified composite Gilbert-Cameron nuclear level density.
(Increased condensation energy, collective enhancement)
K.-H. Schmidt, B. Jurado, Phys. Rev. C 86 (2012) 044322

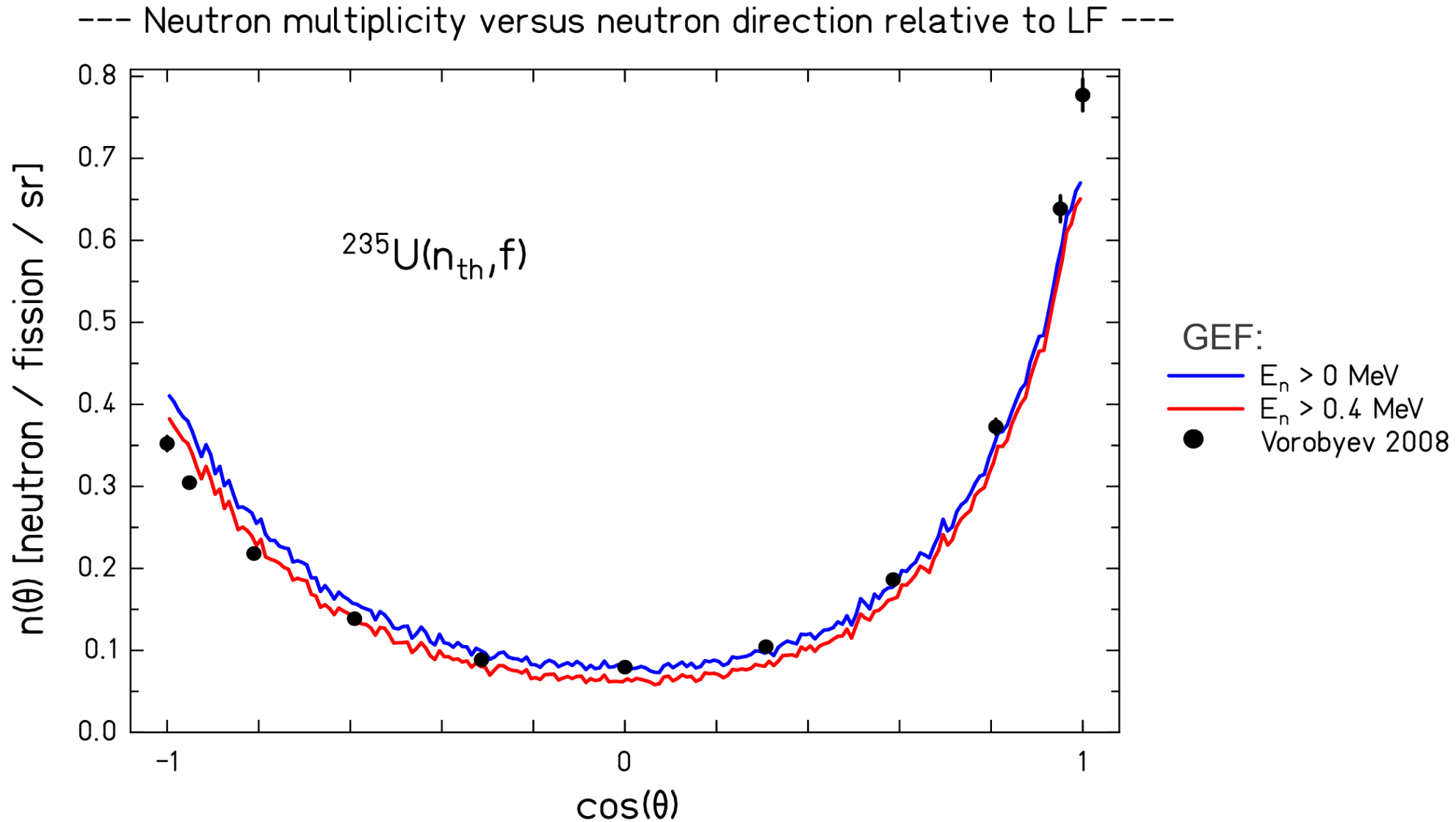
Multiplicities of prompt neutrons



--- experimental data
--- GEF code

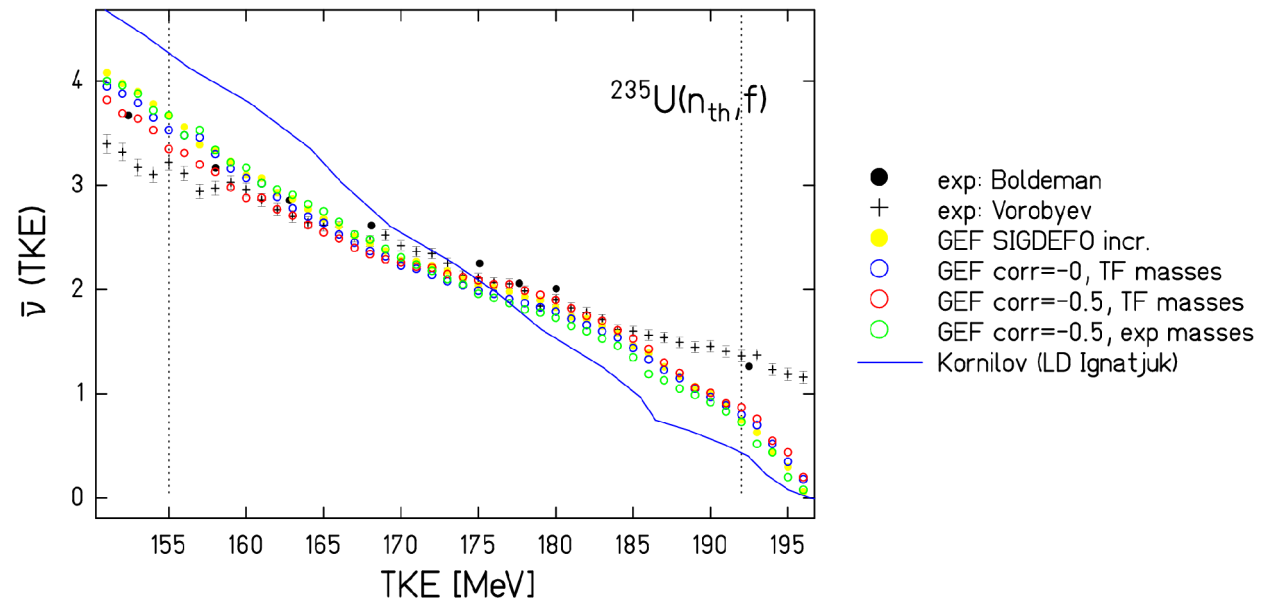
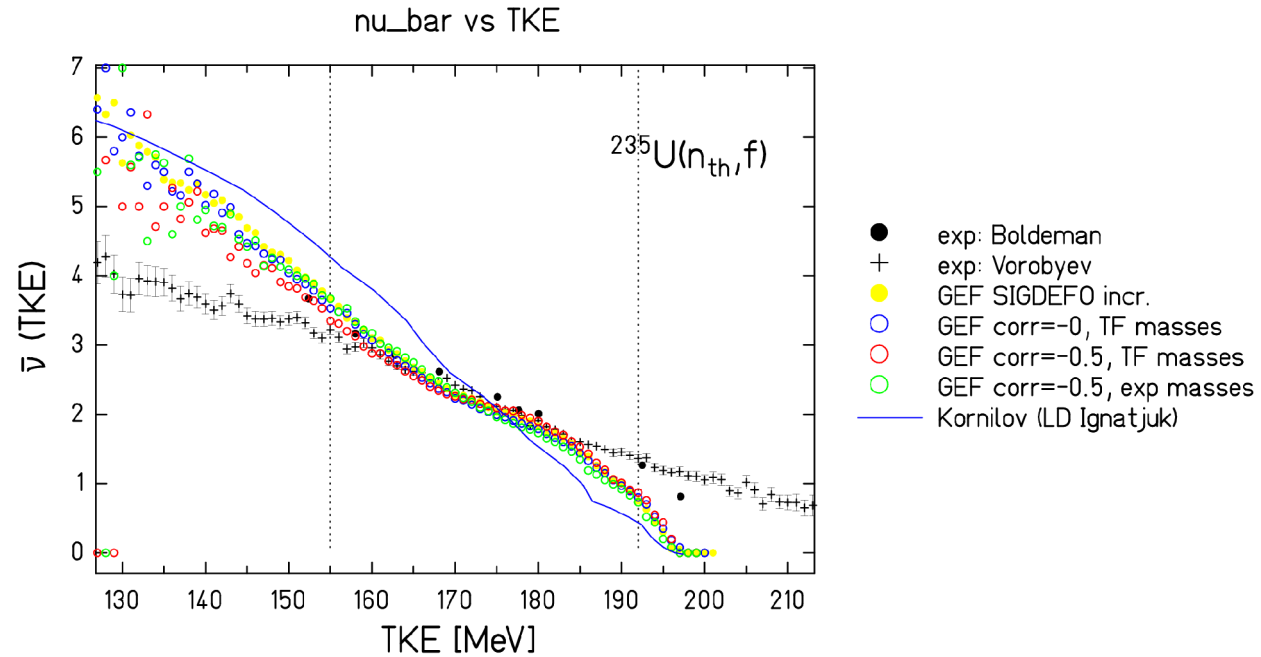
Multiplicity distribution mostly reflects the fluctuations in nuclear deformation at scission.

Correlations: nu-bar - angle



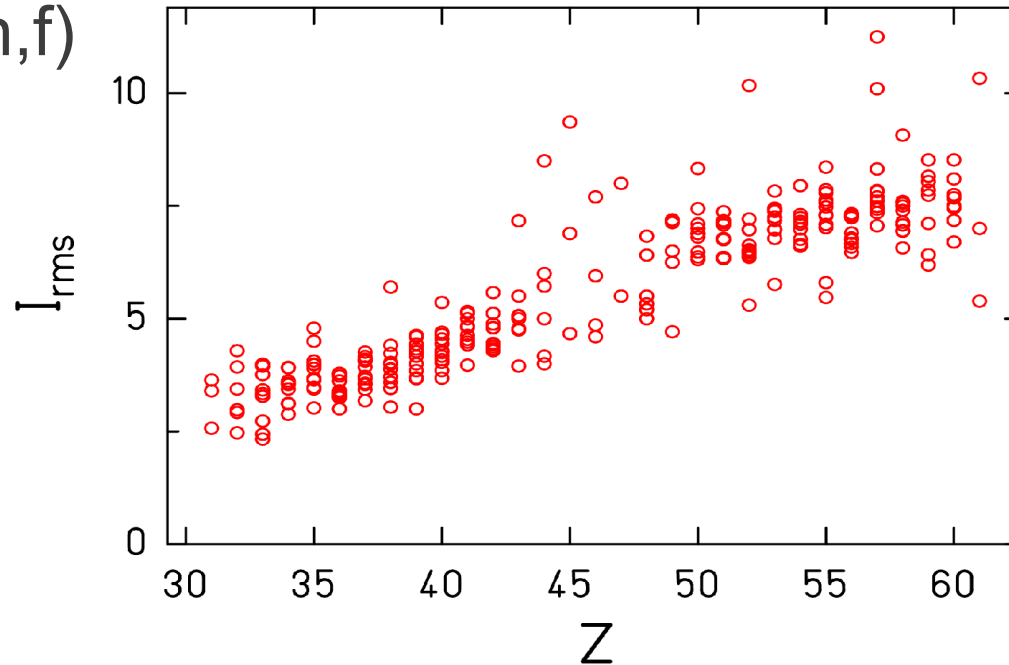
Searching for signatures of scission neutrons ...

Correlations: nu-bar - TKE



Fragment angular momentum

$^{235}\text{U}(\text{nth}, \text{f})$



GEF calculations

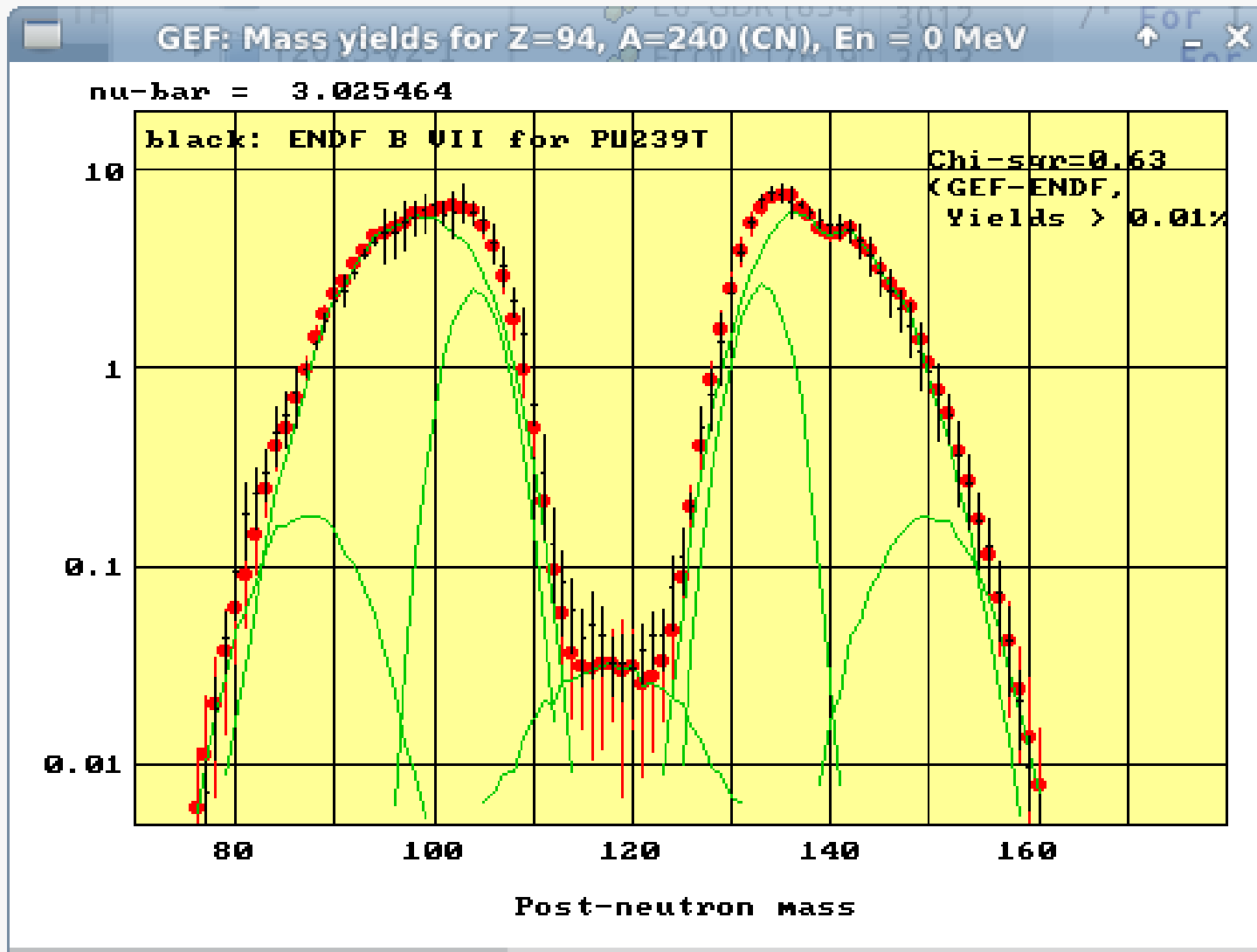
in good agreement with measured isomeric ratios

Theory: “Pumping” from q.m. uncertainty of orbital angular momentum (Kadmensky) + I of unpaired nucleons.

Fragment angular momentum

- stores collective energy at scission (less TKE)
- feeds contributions of rotational transitions to prompt gamma spectrum

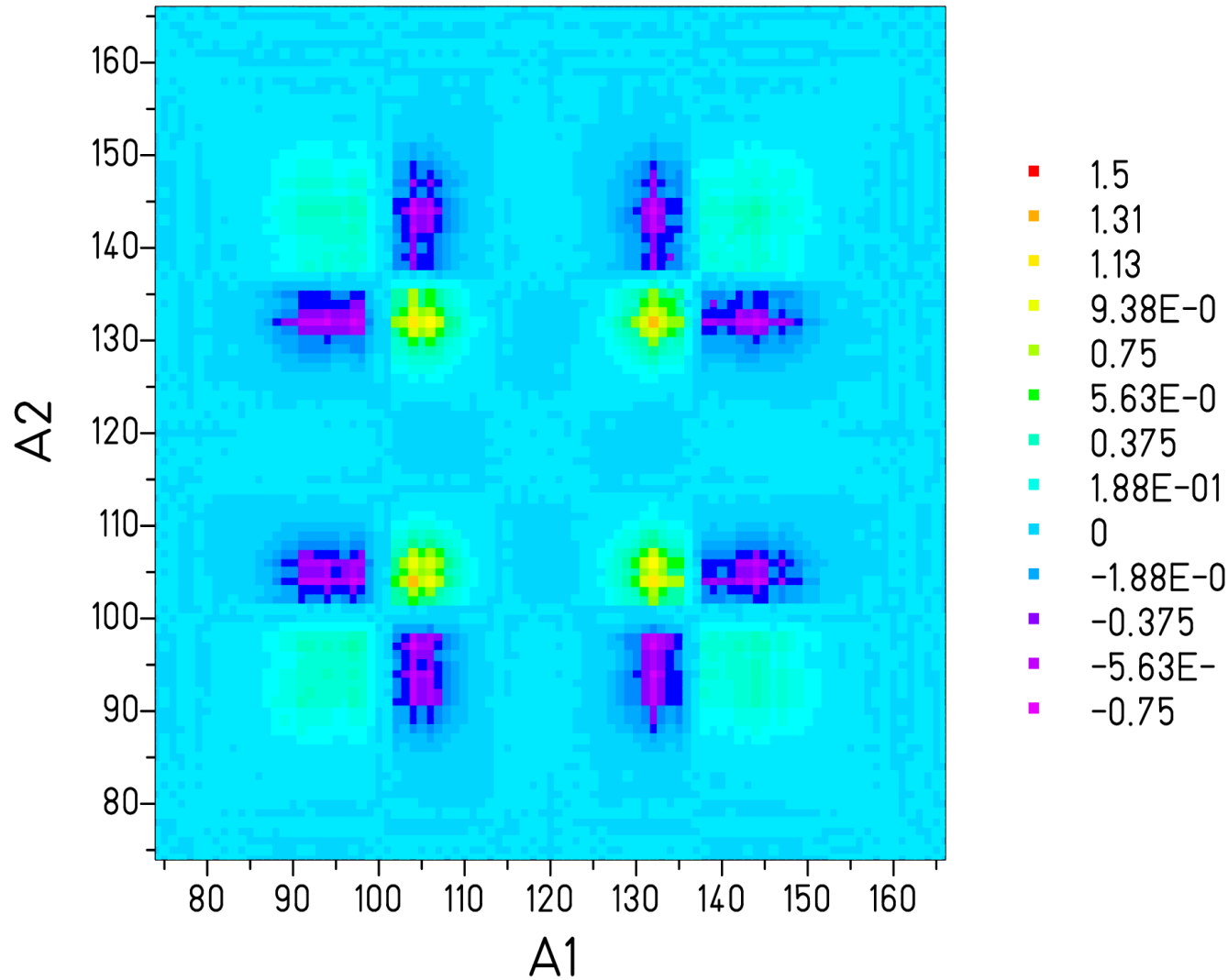
Uncertainties of the model



Mass yields from GEF with estimated uncertainties.

GEF calculations with perturbed parameters.

Covariance matrix



$^{240}\text{Pu}(\text{nth},f)$

Post-neutron masses.

Covariances defined by the model dependences.

A tool for improving evaluations.

Conclusion and outlook

- Fission is a large-amplitude shape evolution with a tremendous variety of final configurations.
- Fission experiments need to specify these configurations by as many observables with an as good resolution as possible.
- Inverse kinematics is a major clue for the revival of fission studies (→ variety of systems, isotopic resolution). Extending the data base considerably.
- A global view on experimental results reveals a surprising simplicity and systematics.
- Fission is governed to a great extent by general laws of quantum and statistical mechanics.

Further info: JEF/DOC 1423 (from www.khs-erzhausen.de)