

Axion / Axino Dark Matter

BBN constraints and LHC phenomenology

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Vistas in Axion Physics
INT Seattle, April 25, 2012

Outline

- Axion DM
 - Lee-Weinberg curve
 - decoupling temperature T_D
- Axino DM scenarios with long-lived staus
 - BBN constraints: new f_{PQ} limits
 - LHC phenomenology: probing f_{PQ}

Extremely Weakly Interacting Particles (EWIPs)

Extensions of the Standard Model

Peccei-Quinn Symmetry & Supersymmetry

	Axions $f_a > 10^9 \text{ GeV}$	Axinos $f_a > 10^9 \text{ GeV}$	Gravitinos $M_{\text{Pl}} = 2.4 \times 10^{18} \text{ GeV}$
spin	0	1/2	3/2
mass	$< 10 \text{ meV}$?	eV-TeV
int.	$\propto (p/f_a)^n$	$\propto (p/f_a)^n$	$\propto (p/M_{\text{Pl}})^n$

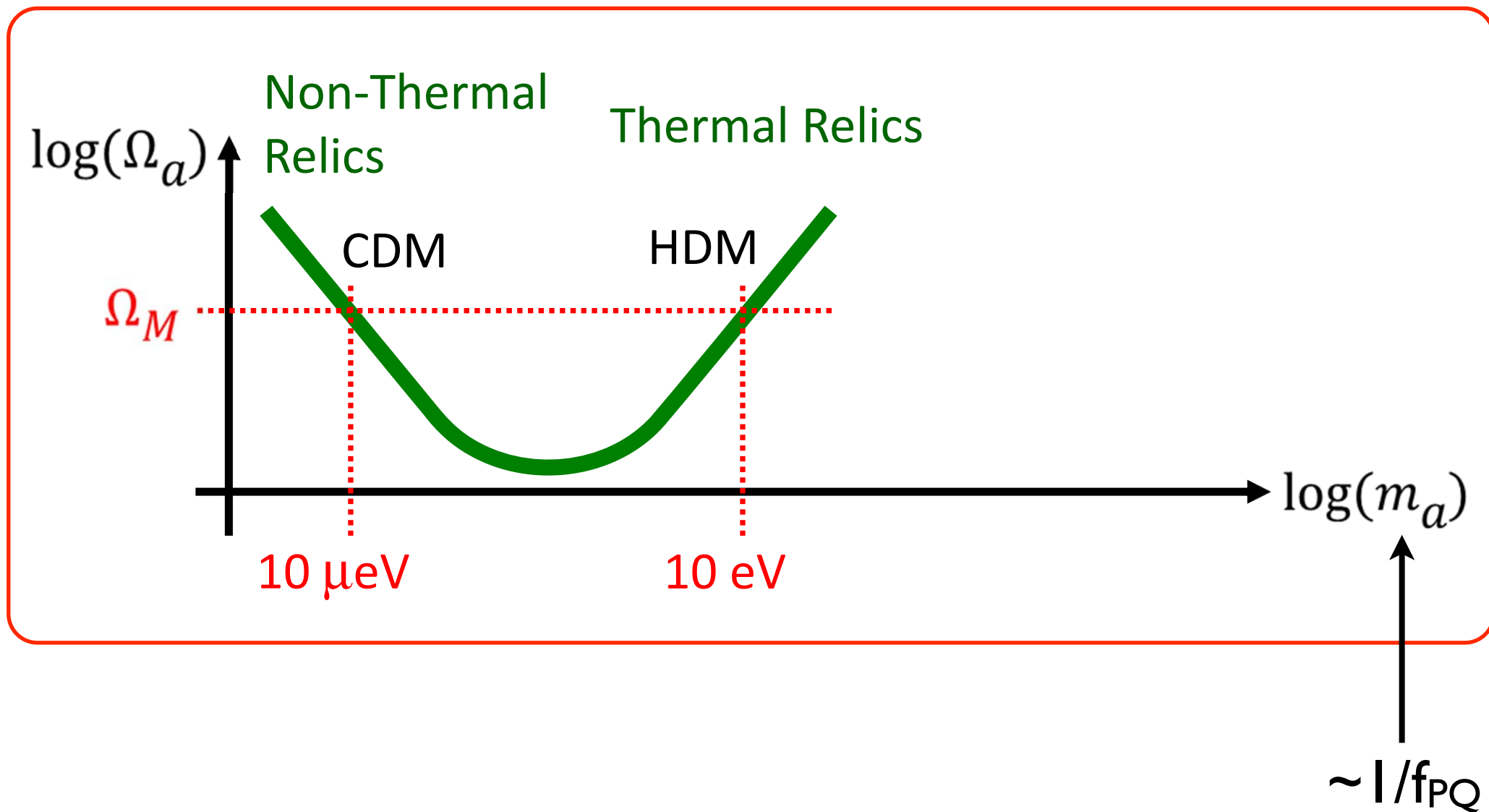
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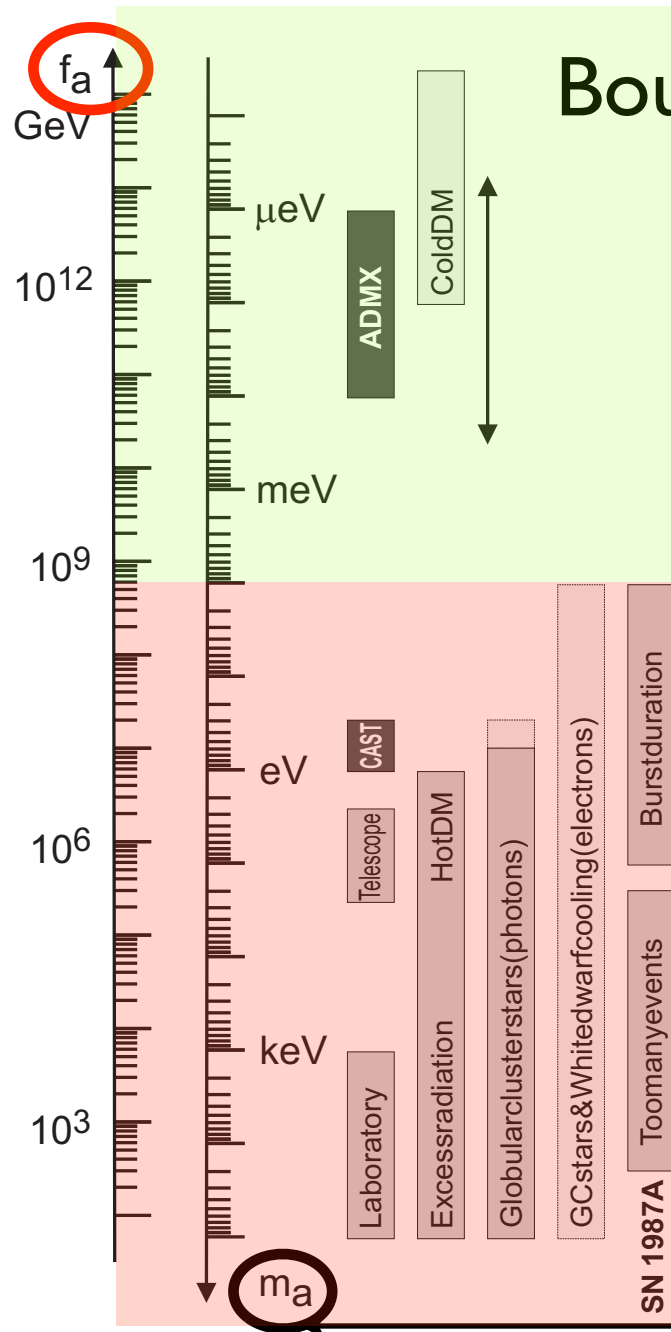
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Lee-Weinberg Curve for Axions



Bounds on the Peccei-Quinn Scale



Bounds from Axion Searches

Cosmological Axion Bounds

Astrophysical Axion Bounds

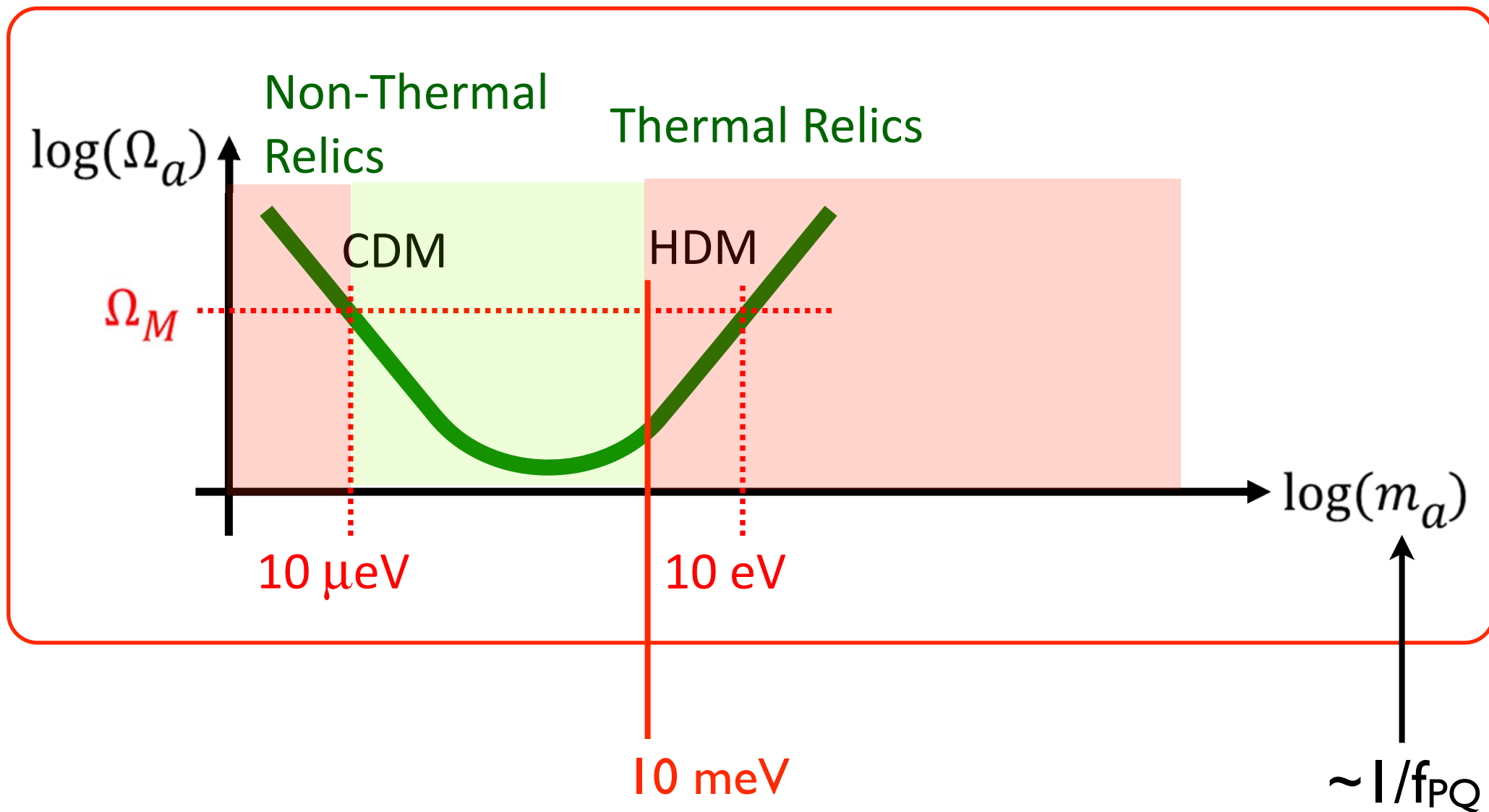
Peccei-Quinn Scale

$$f_a \gtrsim 6 \times 10^8 \text{ GeV}$$

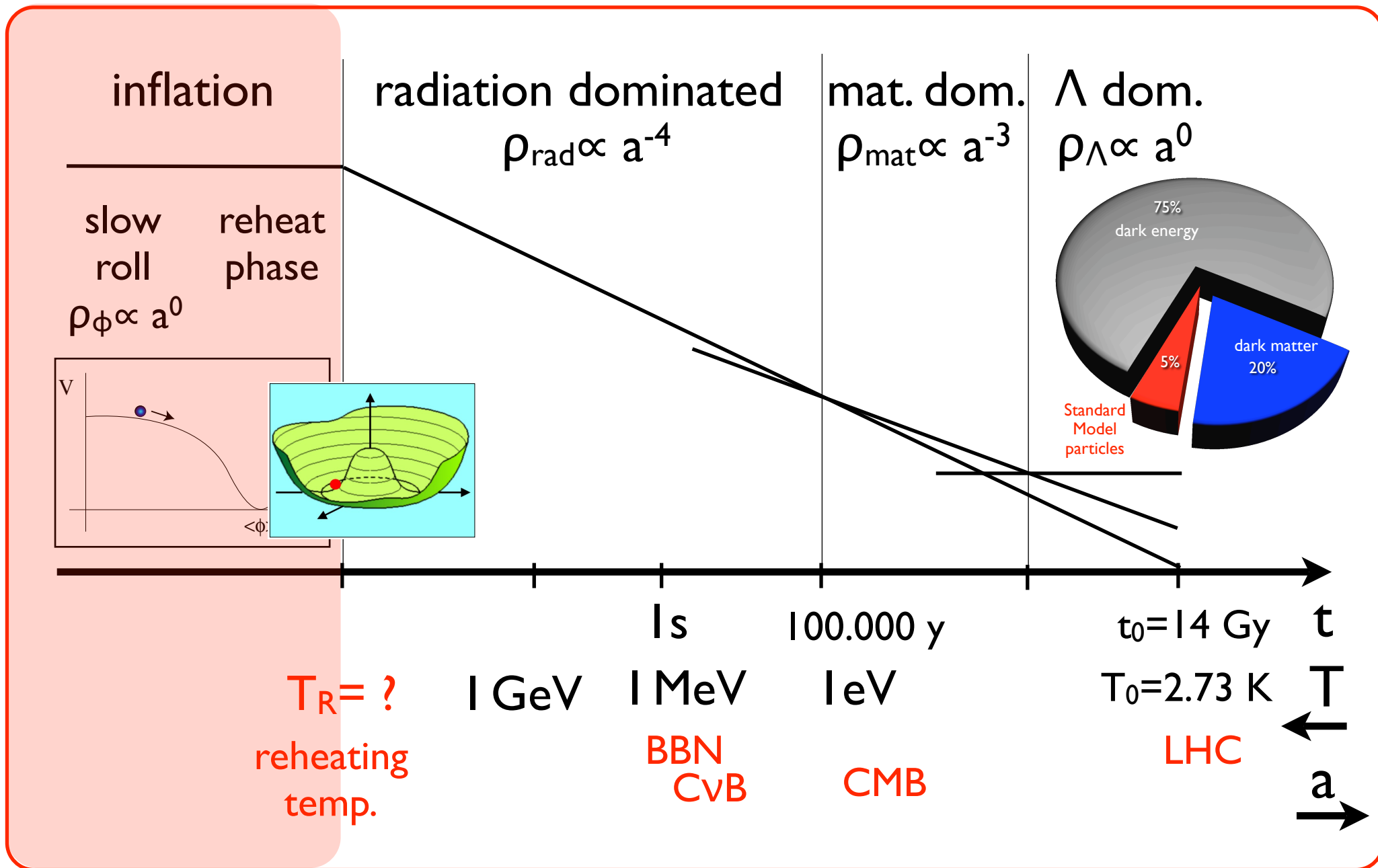
Axion Mass

$$m_a \simeq 0.6 \text{ meV} (10^{10} \text{ GeV} / f_{\text{PQ}})$$

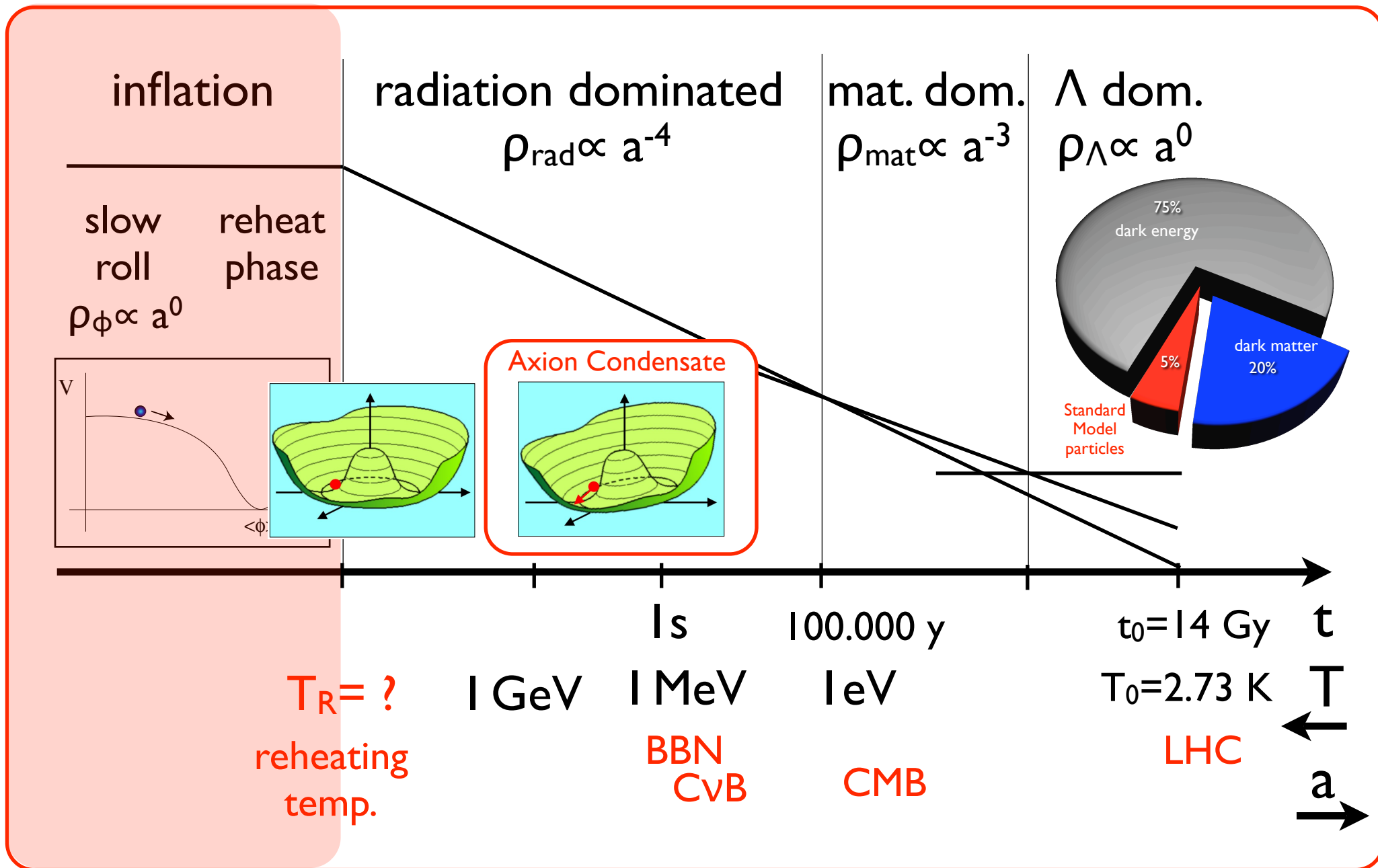
Lee-Weinberg Curve for Axions



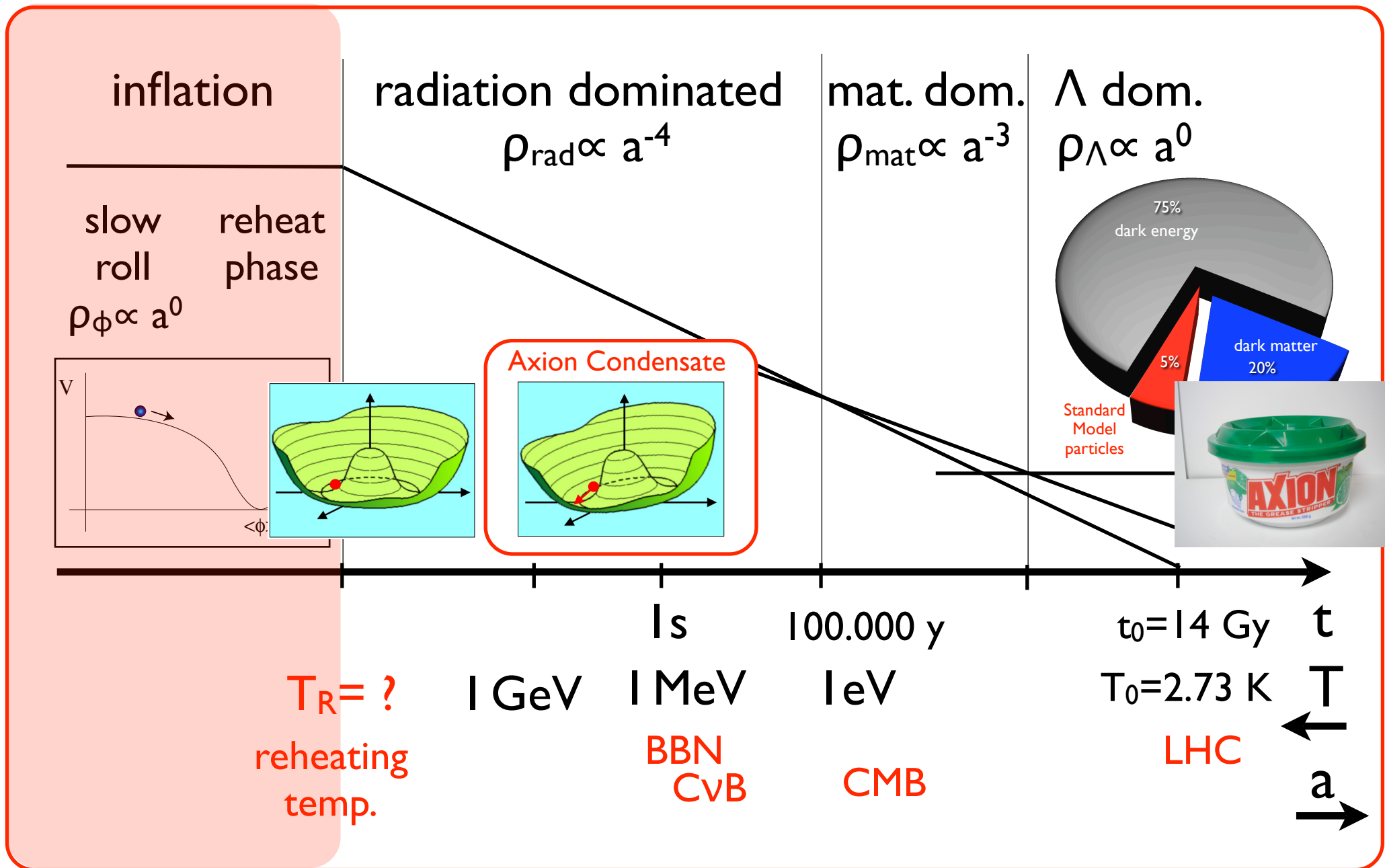
Axion Dark Matter



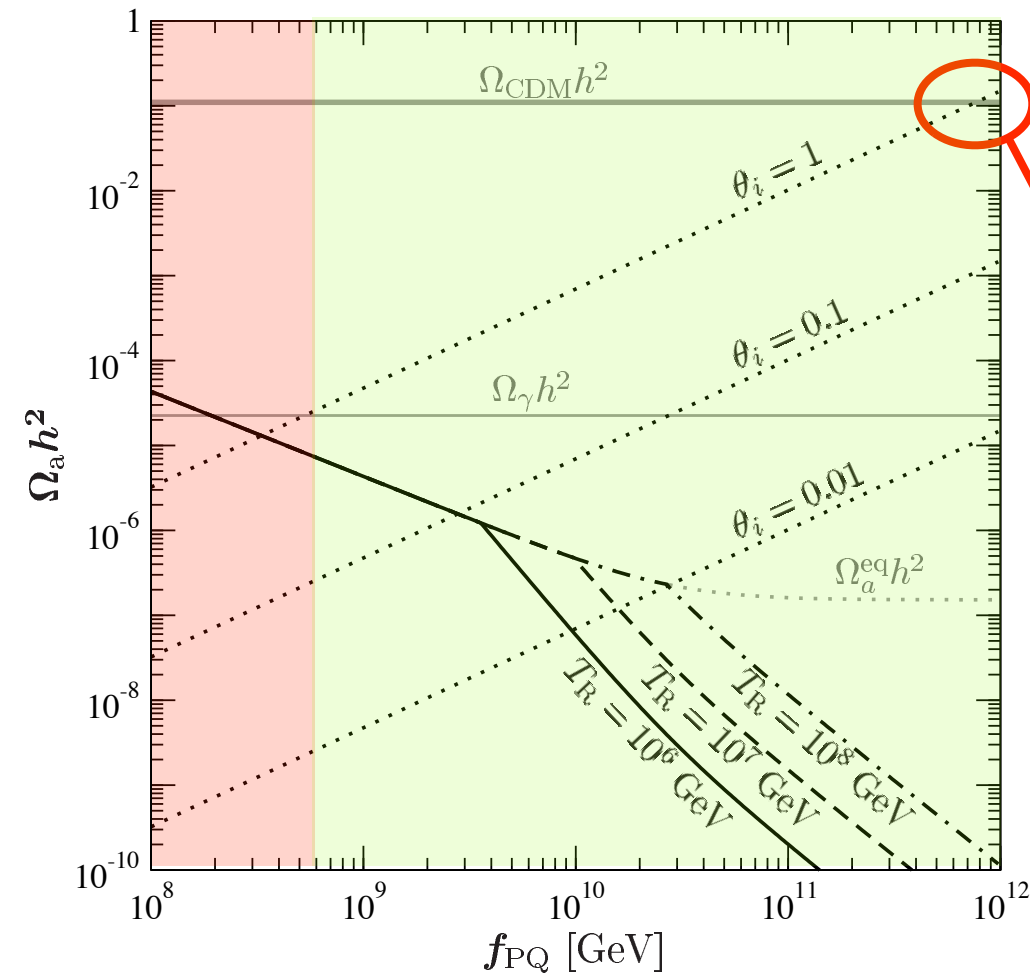
Axion Dark Matter



Axion Dark Matter



Lee-Weinberg Curve for Axions



Axion Condensate: CDM

$$\Omega_a^{\text{MIS}} h^2 \sim 0.15 \theta_i^2 (f_{\text{PQ}}/10^{12} \text{ GeV})^{7/6}$$

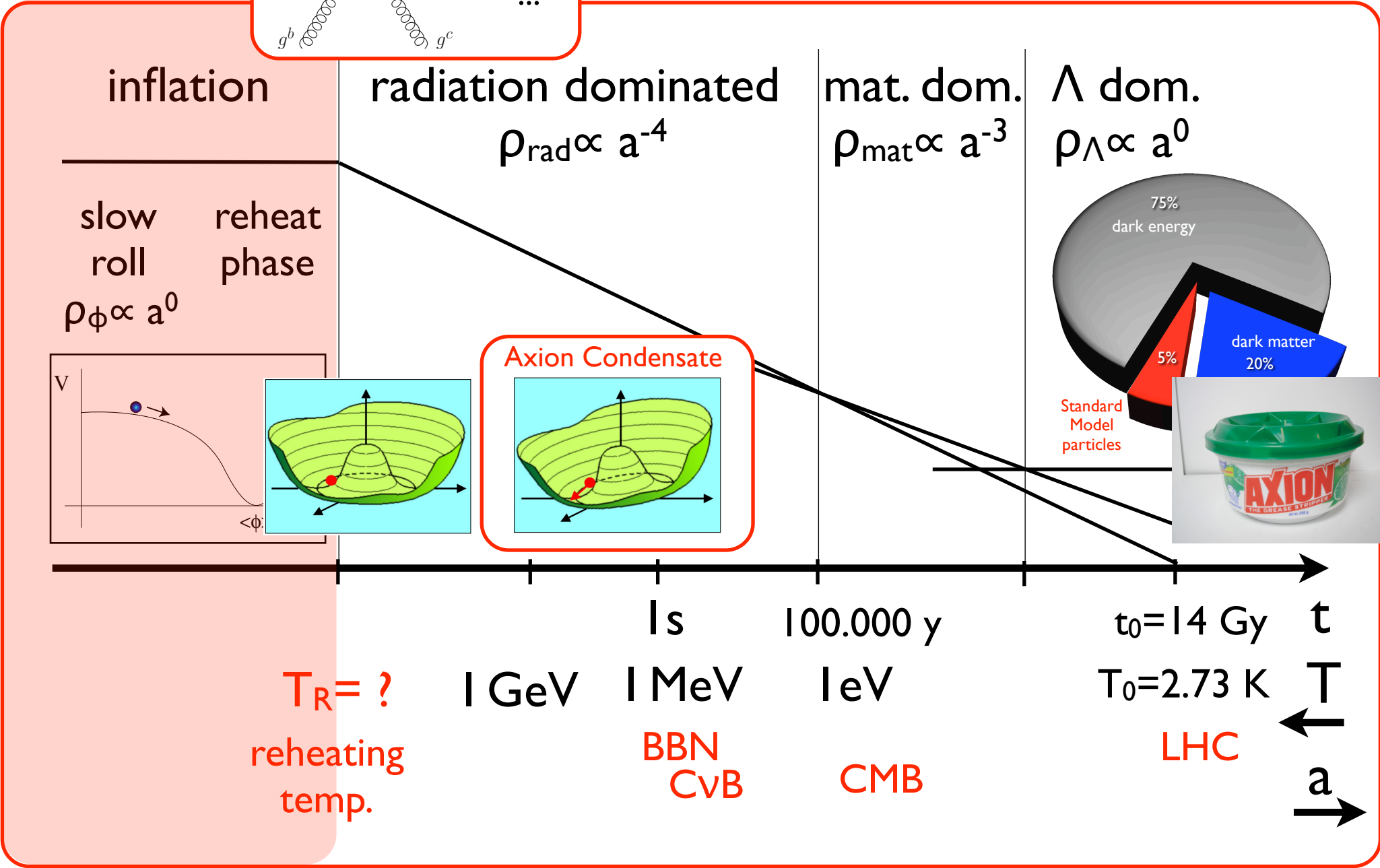
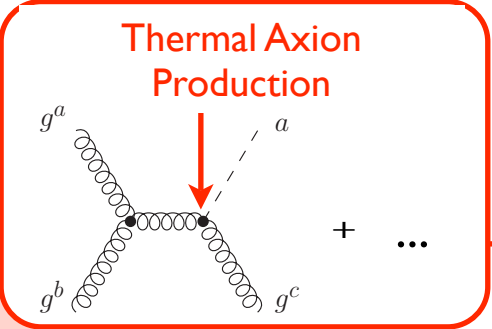
[...; Sikivie, '08; Kim, Carosi, '08; ...]

Axions can provide CDM

Axion Mass

$$m_a \simeq 0.6 \text{ meV} (10^{10} \text{ GeV}/f_{\text{PQ}})$$

Axion Dark Matter



Axion Interactions

- with gluons
model independent

$$\mathcal{L}_{agg} = \frac{g_s^2}{32\pi^2 f_a} a G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

- with photons
model dependent

$$\mathcal{L}_{a\gamma\gamma} = \frac{e^2 C_{a\gamma\gamma}}{32\pi^2 f_a} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

(or $\mathcal{L}_{a\gamma\gamma} = \frac{g_{a\gamma\gamma}}{4} a F_{\mu\nu} \tilde{F}^{\mu\nu}$)



but crucial for axion searches

and governs the axion lifetime $\tau_a = \Gamma_{a \rightarrow \gamma\gamma}^{-1} = \frac{64\pi}{g_{a\gamma\gamma}^2 m_a^3}$

Axion Decoupling Temperature

reheating temp.



decoupling temp.



- $T_R > T_D: 1+2 \rightleftharpoons 3+\text{axion}$

$T > T_D$: axion in thermal eq. with the primordial plasma

$T \sim T_D$: axion decouples as a **hot thermal relic**

- $T_R > T_D: 1+2 \rightarrow 3+\text{axion}$

$T_D \gg T$: axion is never in th. eq. with the prim. plasma

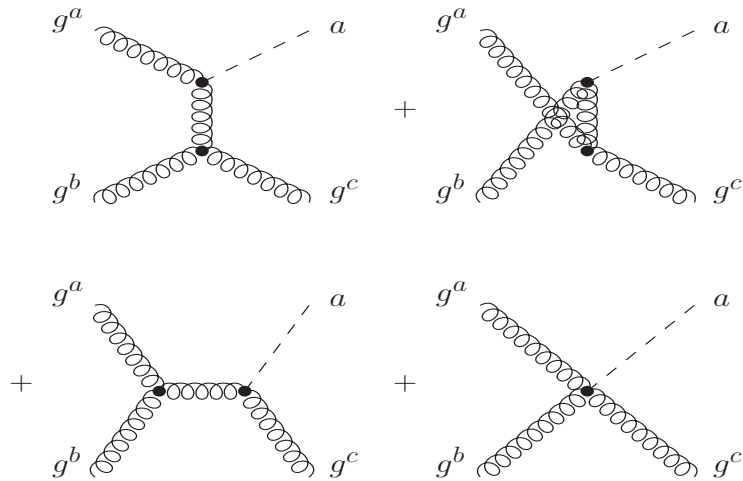
but **thermally produced** \rightarrow Boltzmann eq.



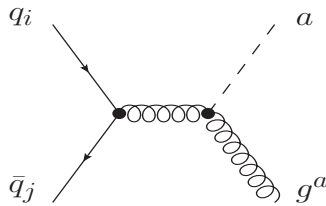
collision term

Thermal Axion Production in the Hot QGP

Process A: $g^a + g^b \rightarrow g^c + a$



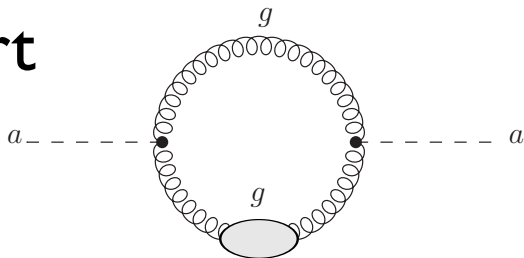
Process B: $q_i + \bar{q}_j \rightarrow g^a + a$



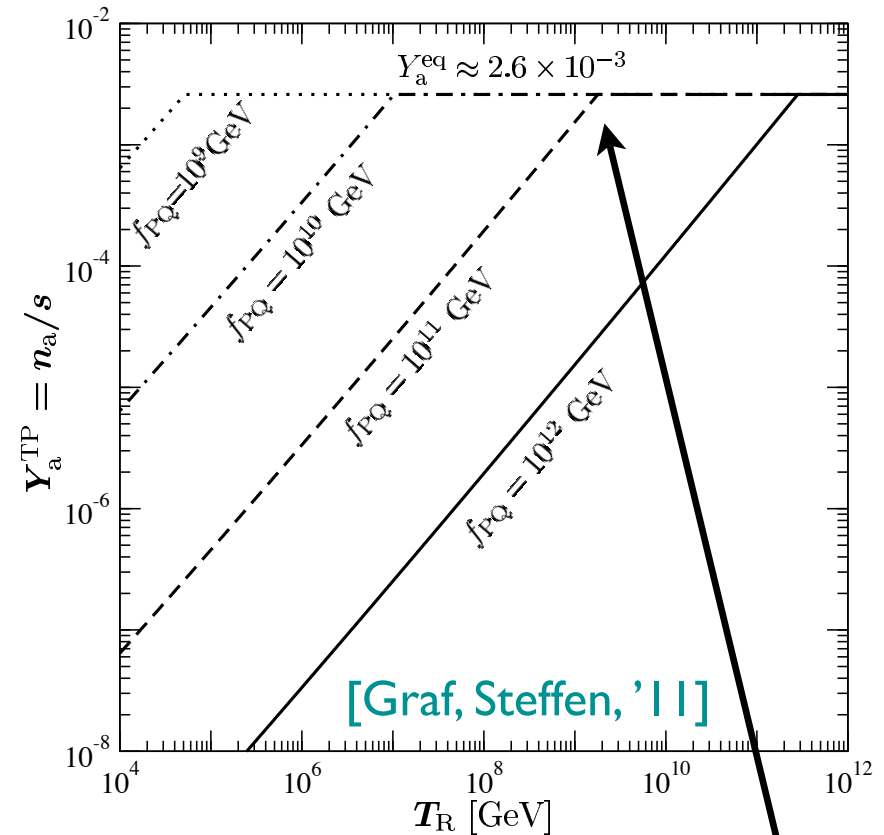
Process C: $q_i + g^a \rightarrow q_j + a$ (crossing of B)

Hard Part

Soft Part



Axion Yield

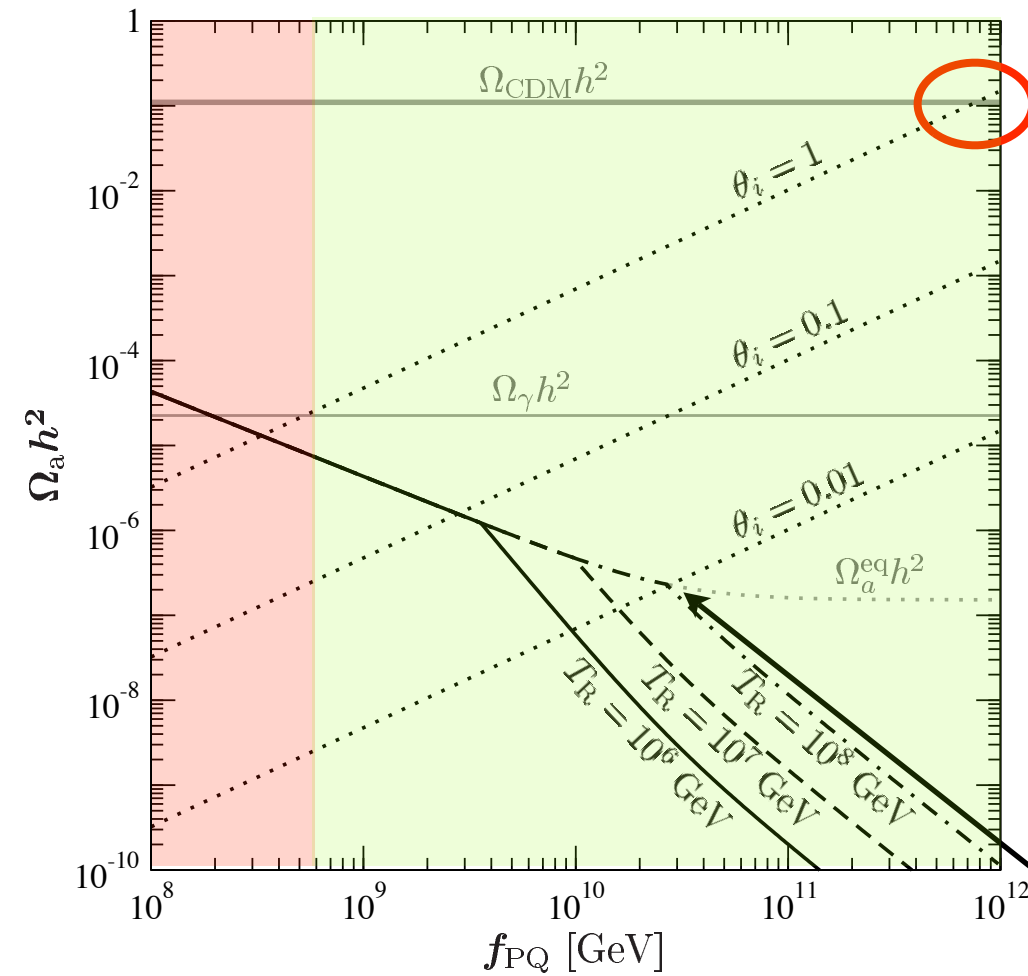


Axion Decoupling Temperature

$$T_D \approx 9.6 \times 10^6 \text{ GeV} \left(\frac{f_{\text{PQ}}}{10^{10} \text{ GeV}} \right)^{2.246}$$

[Masso et al., '02; Sikivie, '08; Graf, Steffen, '11]

Lee-Weinberg Curve for Axions



Axion Condensate: CDM

$$\Omega_a^{\text{MIS}} h^2 \sim 0.15 \theta_i^2 (f_{\text{PQ}}/10^{12} \text{ GeV})^{7/6}$$

[...; Sikivie, '08; Kim, Carosi, '08; ...]

Thermal Axions: WDM/HDM

$$\Omega_a^{\text{TP/eq}} h^2 \simeq \sqrt{\langle p_{a,0} \rangle^2 + m_a^2} Y_a^{\text{TP/eq}} s(T_0) h^2 / \rho_c$$

$$18.6 g_s^6 \ln\left(\frac{1.501}{g_s}\right) \left(\frac{10^{10} \text{ GeV}}{f_{\text{PQ}}}\right)^2 \left(\frac{T_{\text{R}}}{10^{10} \text{ GeV}}\right)$$

Axion Decoupling Temperature

$$T_{\text{D}} \approx 9.6 \times 10^6 \text{ GeV} \left(\frac{f_{\text{PQ}}}{10^{10} \text{ GeV}}\right)^{2.246}$$

Axion Mass

$$m_a \simeq 0.6 \text{ meV} (10^{10} \text{ GeV} / f_{\text{PQ}})$$

Conclusions - Part I

- Lee-Weinberg curve for axions
- two guaranteed axion populations
- axions from the misalignm. mech. may provide all or only a fraction of Ω_{dm} - depending on f_{PQ} & θ_i
- thermal relic or thermally produced axions will be present as a HDM with $(\Omega_a)^{\text{th}} < \Omega_\gamma \ll \Omega_{\text{dm}}$

↑
extremely challenging
to detect experimentally

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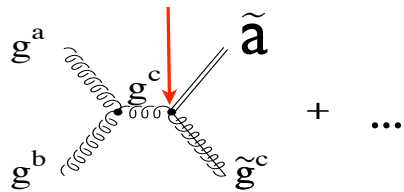
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[see also talk by Howard Baer]

Thermal Axino Production



inflation

radiation dominated

mat. dom.

Λ dom.

$$\rho_{\text{rad}} \propto a^{-4}$$

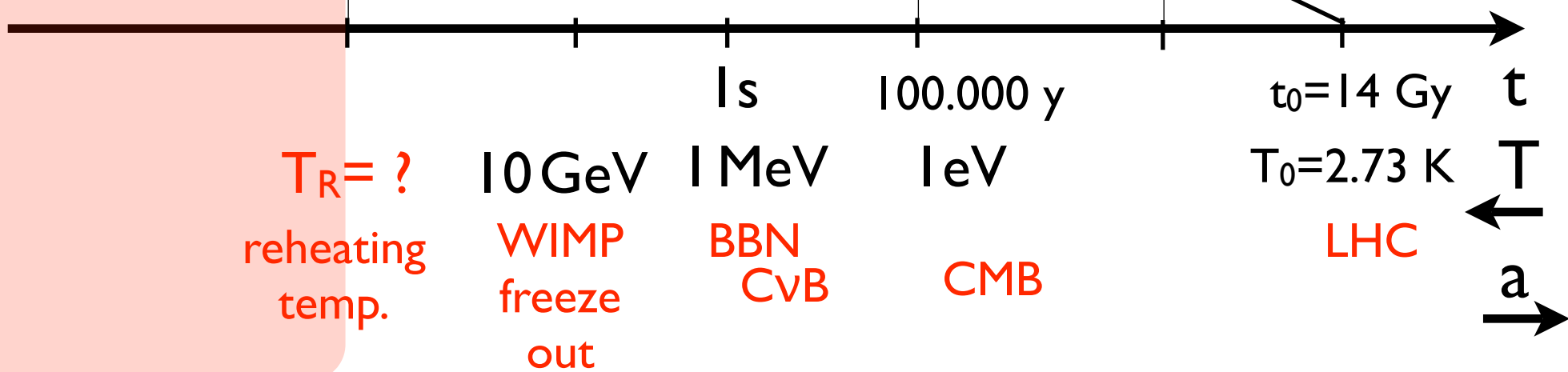
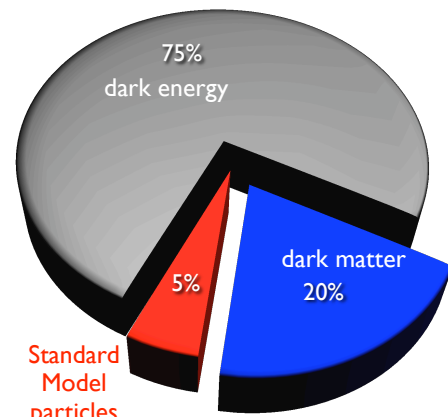
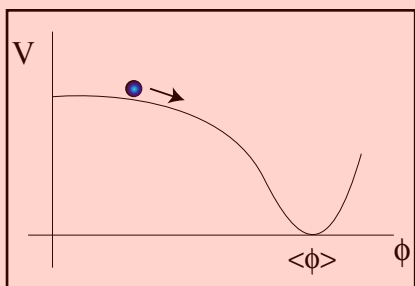
$$\rho_{\text{mat}} \propto a^{-3}$$

$$\rho_{\Lambda} \propto a^0$$

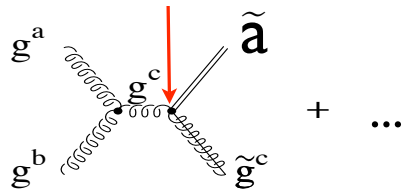
slow roll

reheat phase

$$\rho_{\phi} \propto a^0$$



Thermal Axino Production



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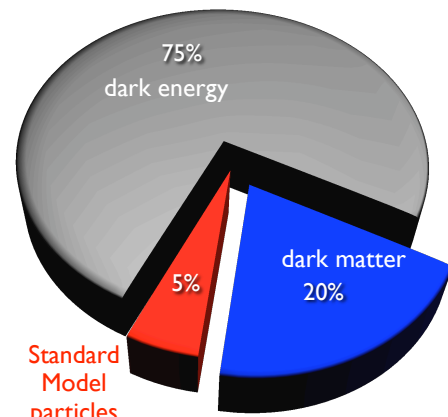
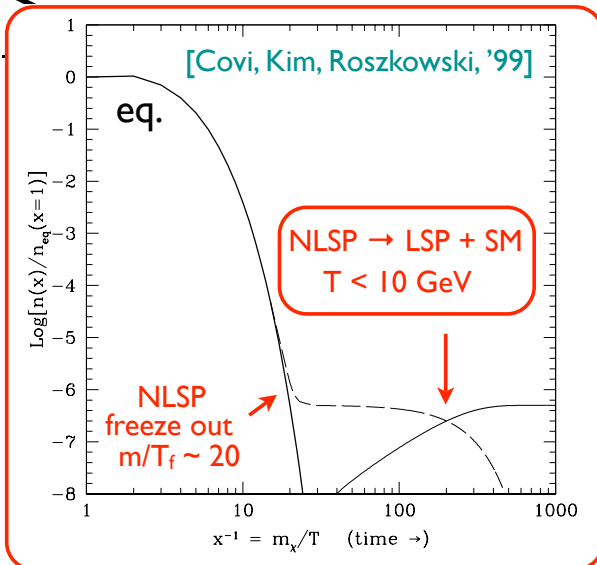
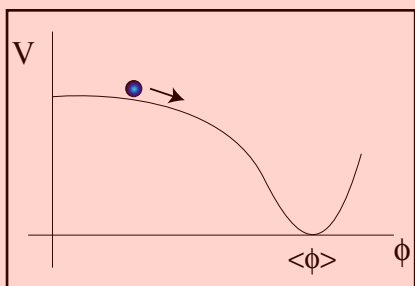
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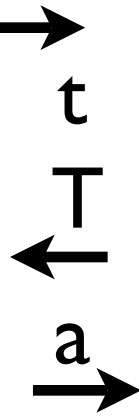
$T_R = ?$
reheating temp.

10 GeV
WIMP freeze out

1 MeV
BBN
CvB

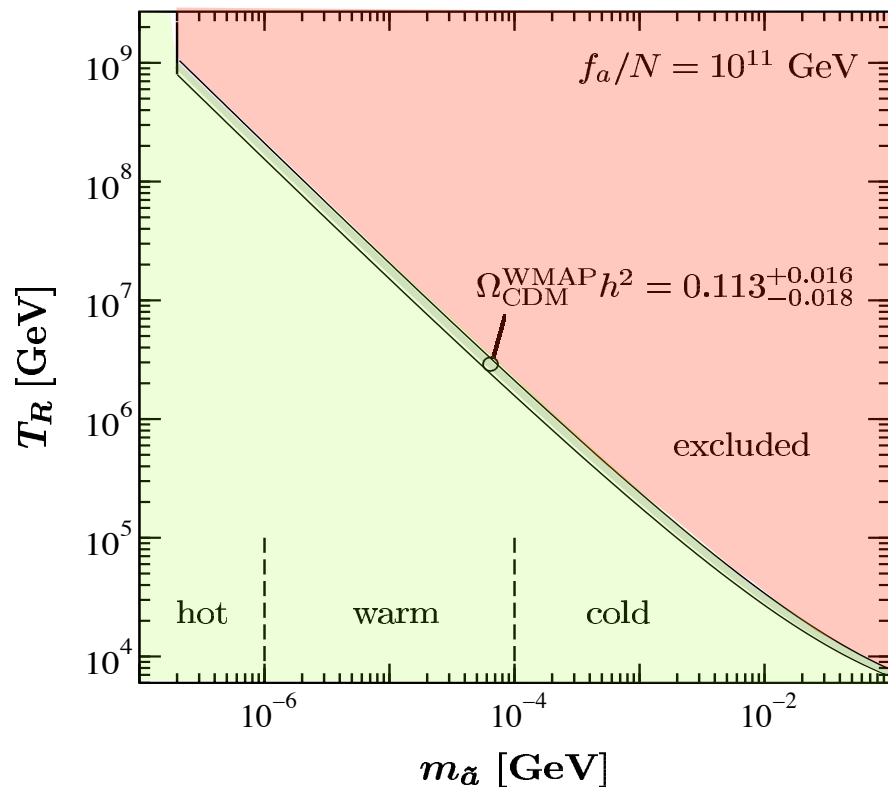
1 eV
CMB

$t_0 = 14 \text{ Gy}$
 $T_0 = 2.73 \text{ K}$
LHC



Axino LSP Case

Thermal \tilde{a} Production

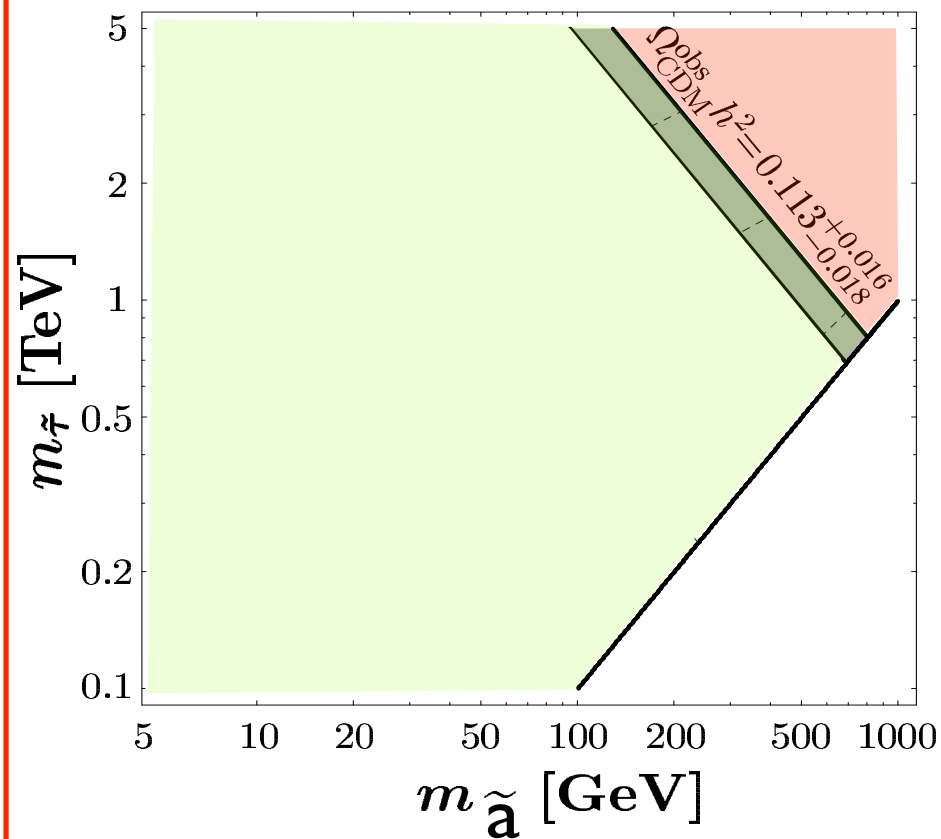


[Brandenburg, FDS, '04]

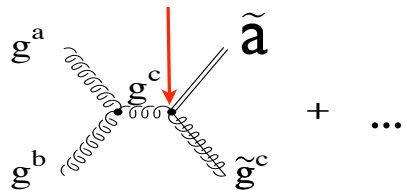
see also [Covi et al., '01]

and [Strumia, '10]

$\tilde{\tau}$ NLSP $\rightarrow \tilde{a} + \tau$



Thermal Axino Production



inflation

radiation dominated

mat. dom.

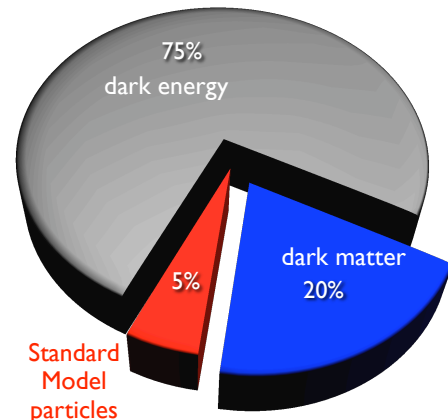
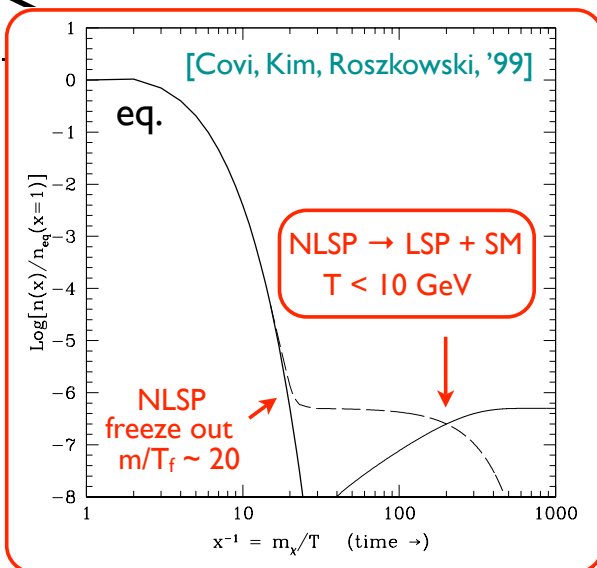
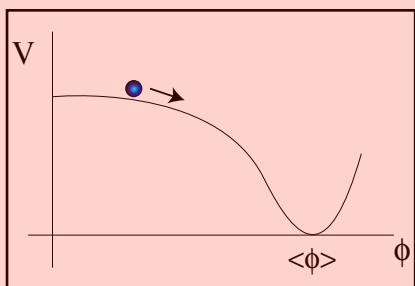
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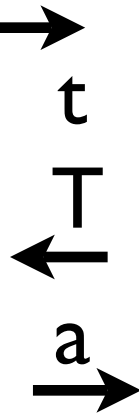
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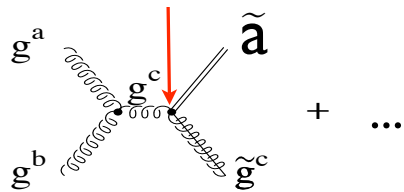
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Thermal Axino Production



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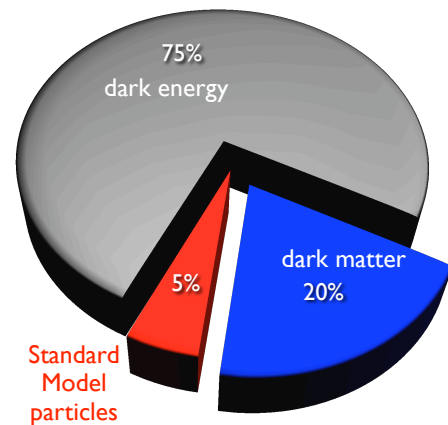
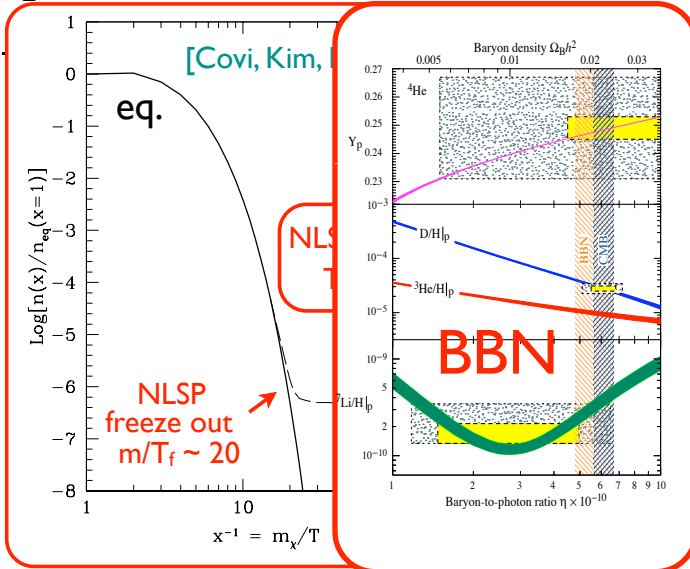
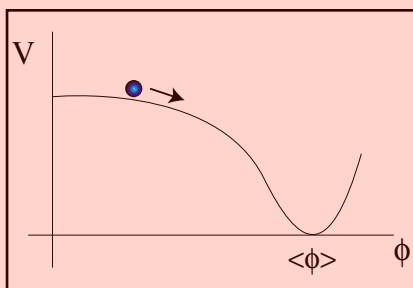
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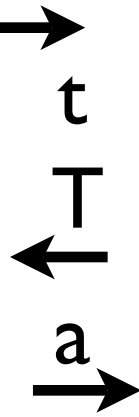
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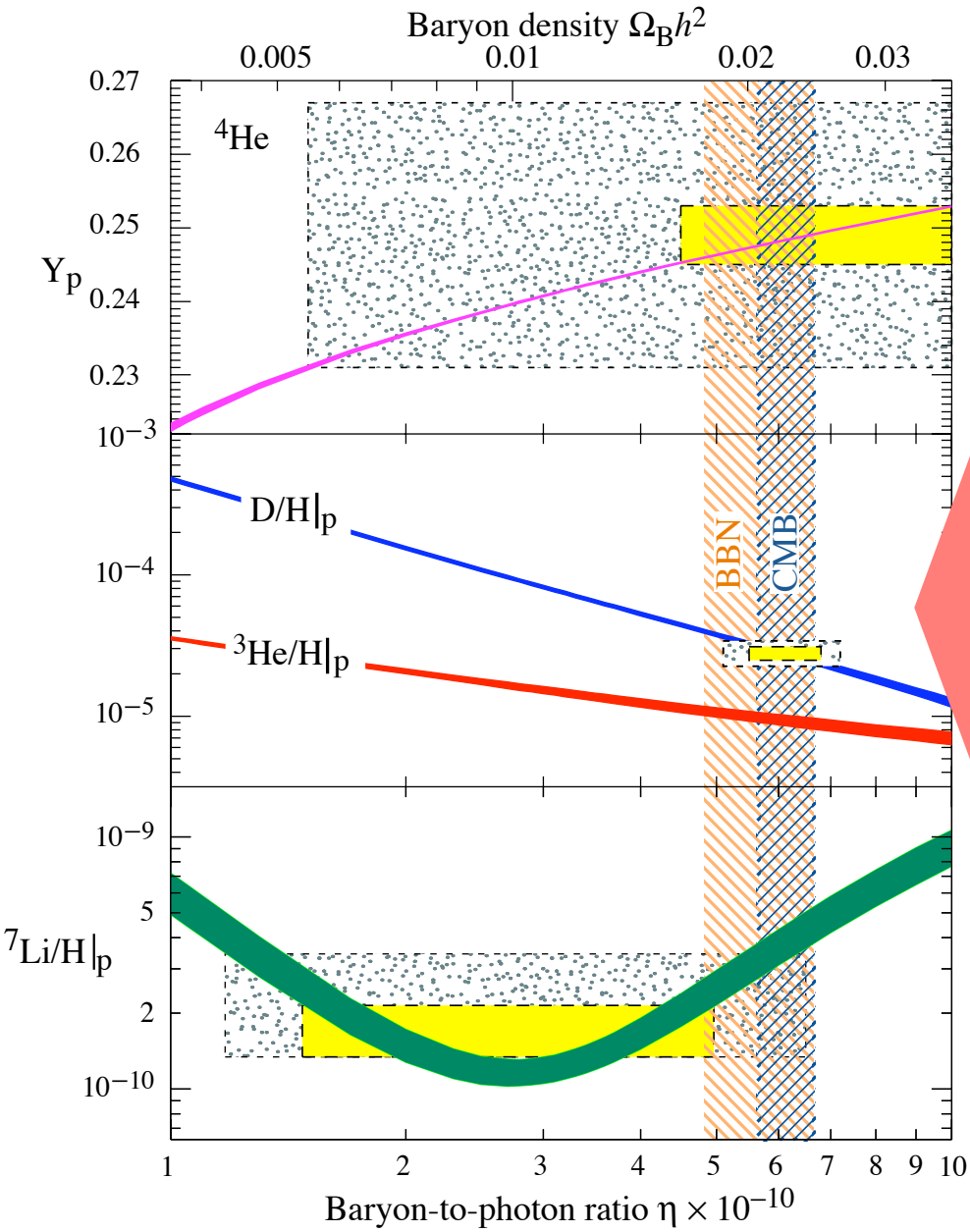
1 MeV
BBN
CMB

1 eV
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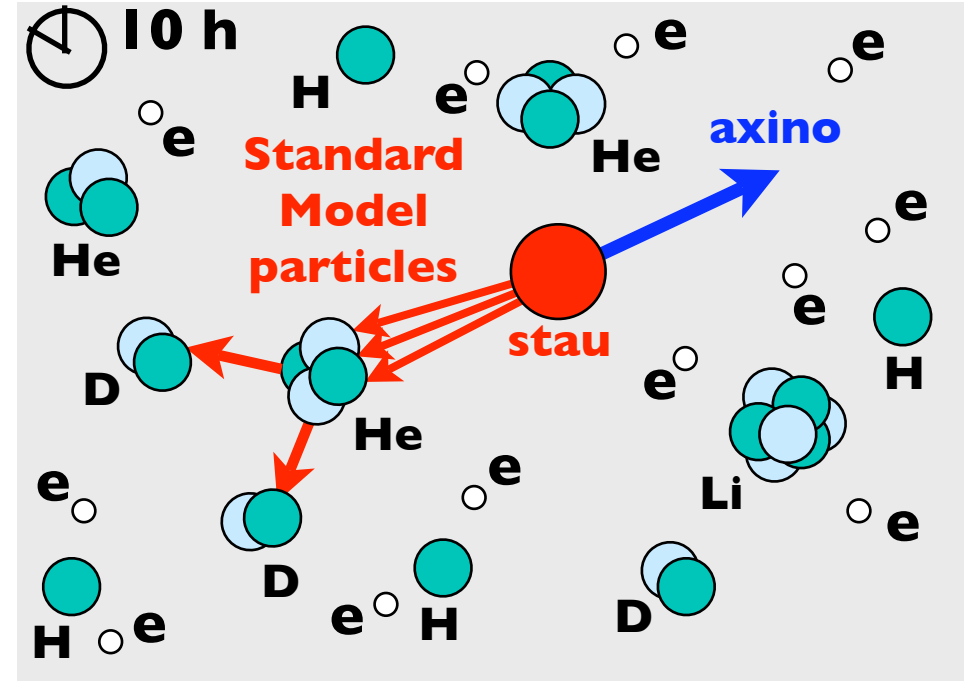
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LHC



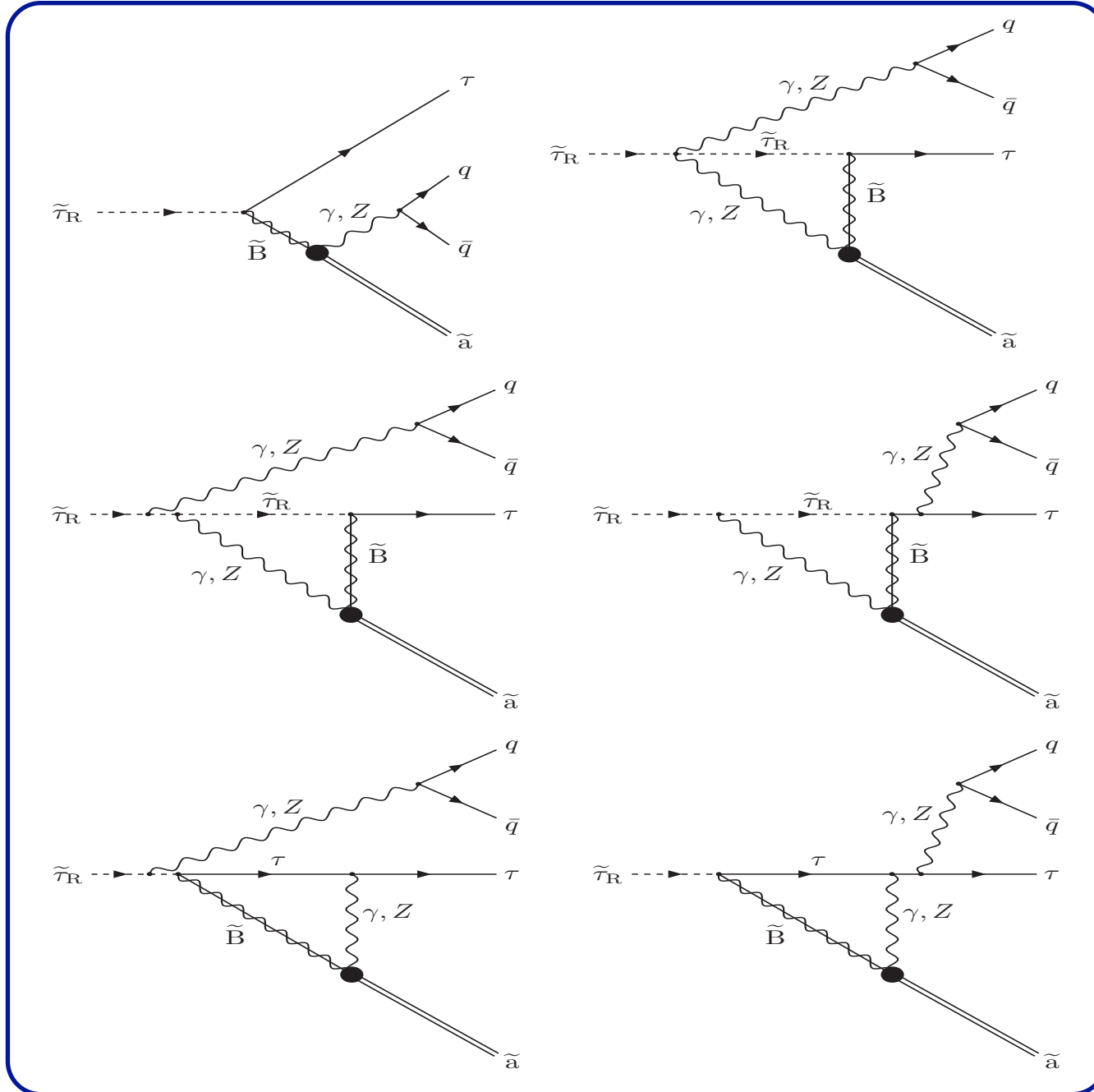
Big-Bang Nucleosynthesis



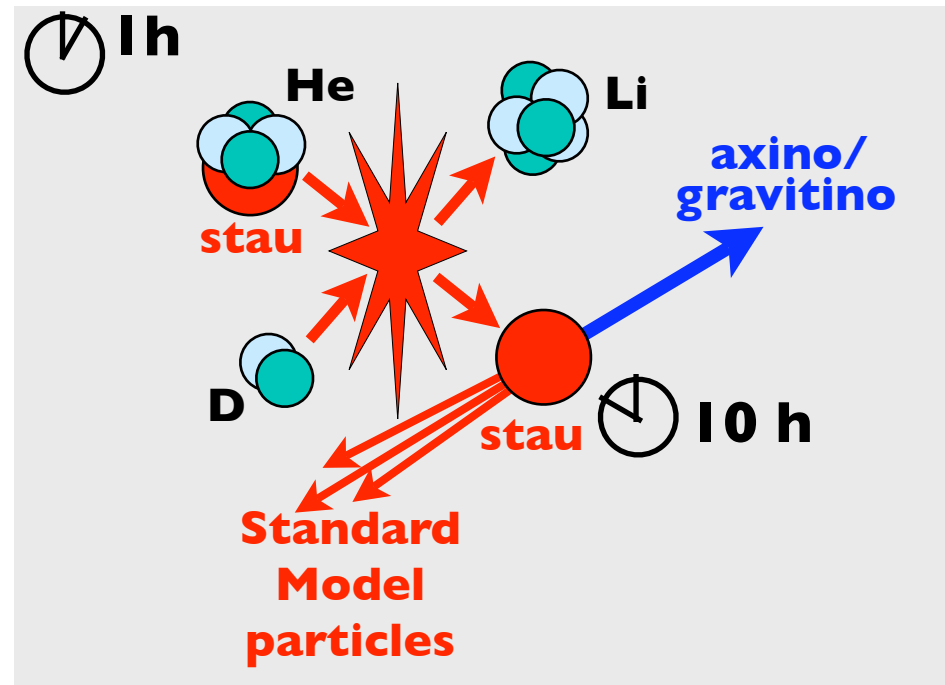
[Particle Data Book 2006]



Late Hadronic Energy Injection



Catalyzed BBN [Pospelov, '06]

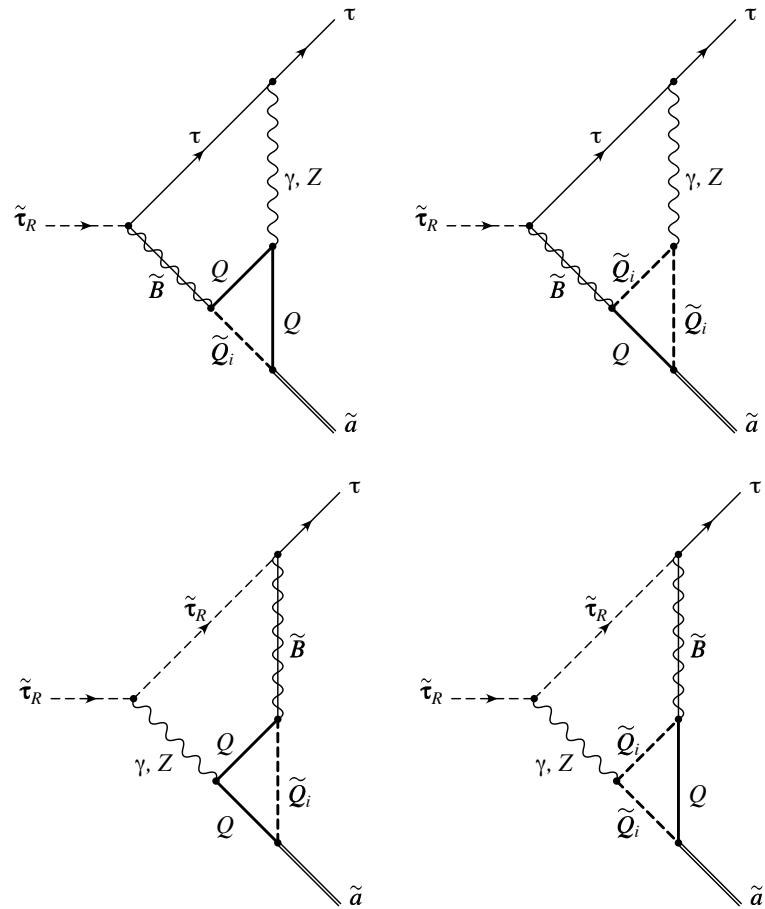


[Cyburt et al., '06; FDS, '06; Pradler, FDS, '07; Hamaguchi et al., '07; Kawasaki, Kohri, Moroi, '07; Takayama, '07; Jedamzik, '07; Pradler, FDS, '08]

CBBN of ${}^9\text{Be}$: [Pospelov, '07; Pospelov, Pradler, FDS, '08]

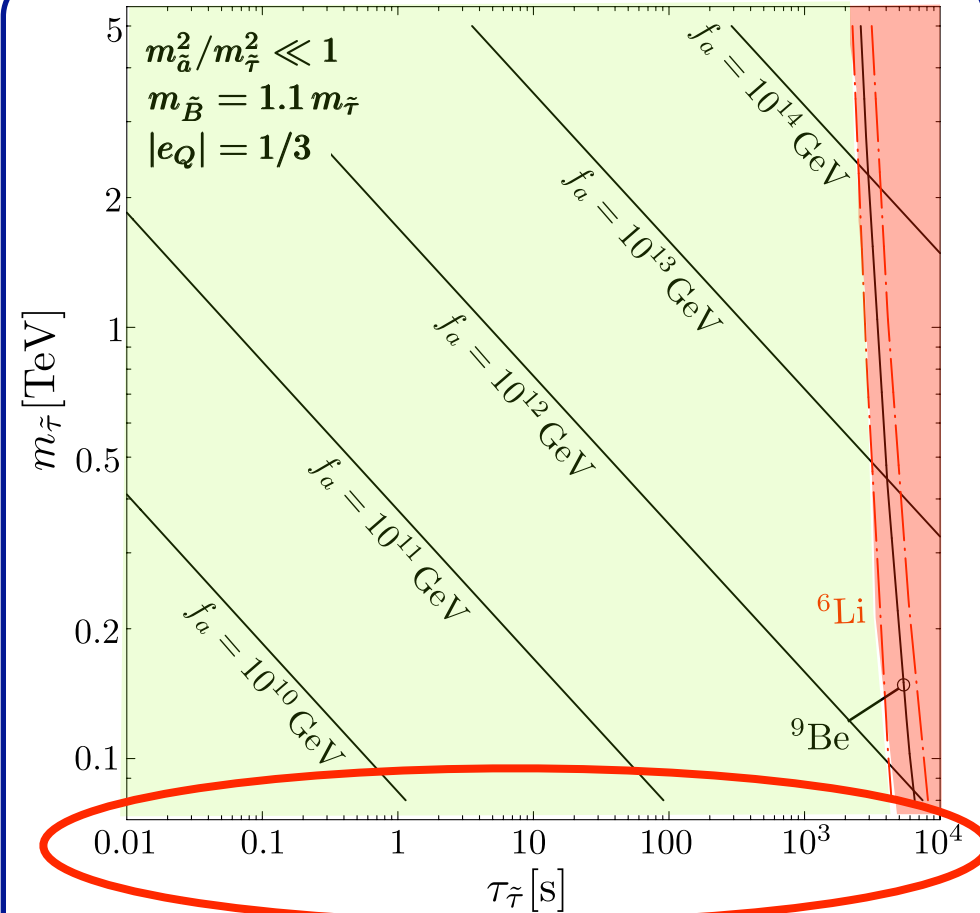
Stau Decays into Axinos

BBN



$$W_{PQ} = y\Phi Q_1 Q_2 \quad M_{\tilde{Q}_{1,2}} = M_Q = y\langle\phi\rangle = yf_a/\sqrt{2}$$

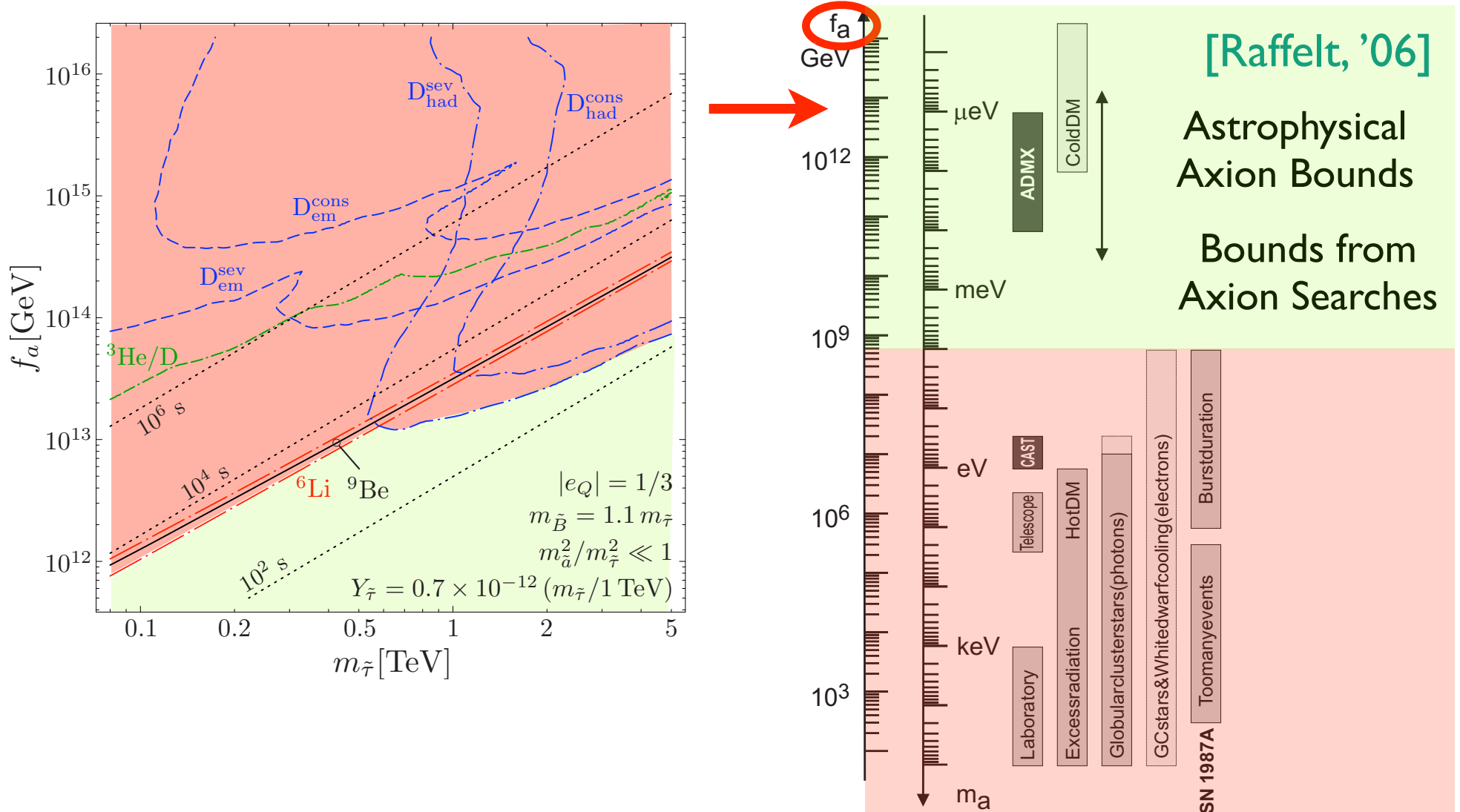
Chiral multiplet	$U(1)_{PQ}$	$(SU(3)_c, SU(2)_L)_Y$
$\Phi = \phi + \sqrt{2}\chi\theta + F_\phi\theta\theta$	+1	$(\mathbf{1}, \mathbf{1})_0$
$Q_1 = \tilde{Q}_1 + \sqrt{2}q_1\theta + F_1\theta\theta$	-1/2	$(\mathbf{3}, \mathbf{1})_{+e_Q}$
$Q_2 = \tilde{Q}_2 + \sqrt{2}q_2\theta + F_2\theta\theta$	-1/2	$(\mathbf{3}^*, \mathbf{1})_{-e_Q}$



$$\Gamma_{\text{tot}}^{\tilde{\tau}_R} \approx \Gamma(\tilde{\tau}_R \rightarrow \tau \tilde{a})_{\text{LL}}$$

$$= \frac{81\alpha^4 e_Q^4}{128\pi^5 \cos^8 \theta_W} \frac{m_{\tilde{\tau}} m_{\tilde{B}}^2}{f_a^2} \left(1 - \frac{m_{\tilde{a}}^2}{m_{\tilde{\tau}}^2}\right)^2 \ln^2\left(\frac{yf_a}{\sqrt{2}m_{\tilde{\tau}}}\right)$$

Axino LSP Case with a Charged Slepton NLSP

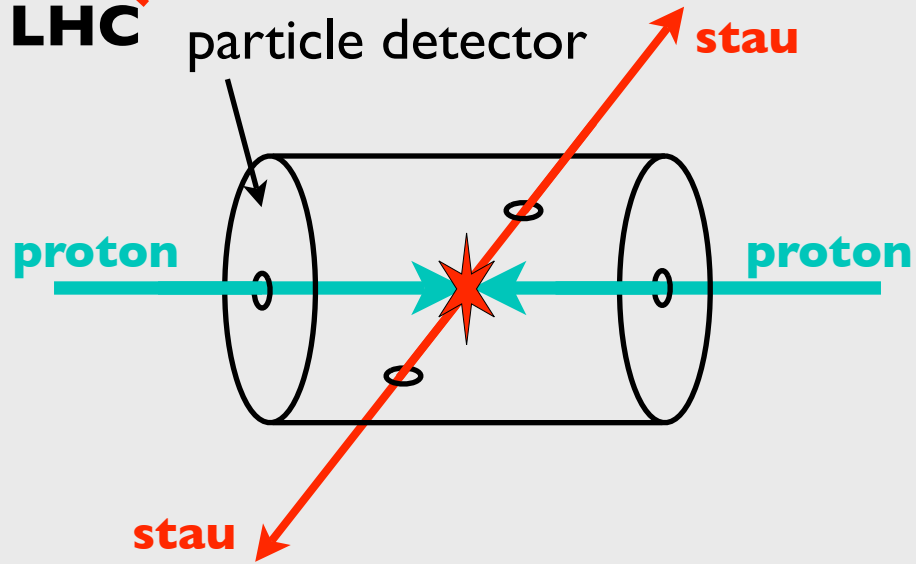


Upper Limits on the Peccei-Quinn Scale

Axino DM @ LHC

← **Stau NLSP**

~~2009~~ 12
LHC

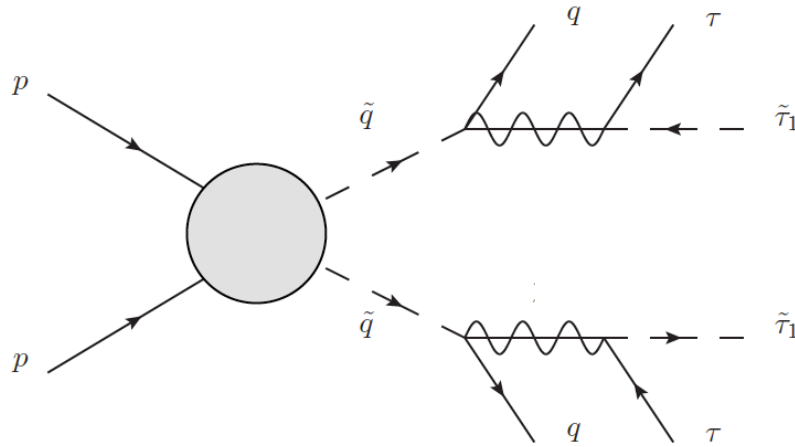


The signal:
jets + leptons
+ 2 “stable”
charged particles

Very different from the large E_T^{miss} signal of Neutralino DM

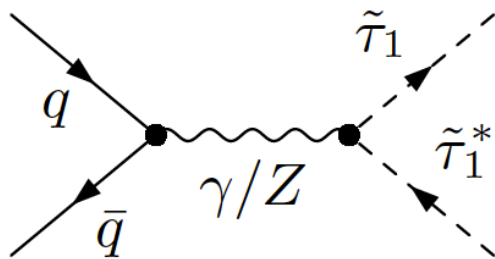
Stau Production @ LHC

- Production in cascade decays



determined by
squark + gluino production
(& BRs)

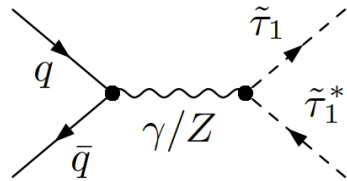
- Direct production



Drell-Yan
(known @ NLO (S)QCD
[Benakker, Klasen, Krämer, Plehn, Spira; '99]
and @ NLL [Bozzi, Fuks, Klasen; '06])

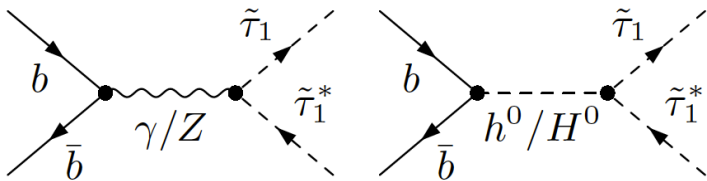
Direct Stau Production at Hadron Colliders

Drell-Yan production



$O(\alpha^2)$ & NLO (S)QCD $O(\alpha_s^2 \alpha^2)$

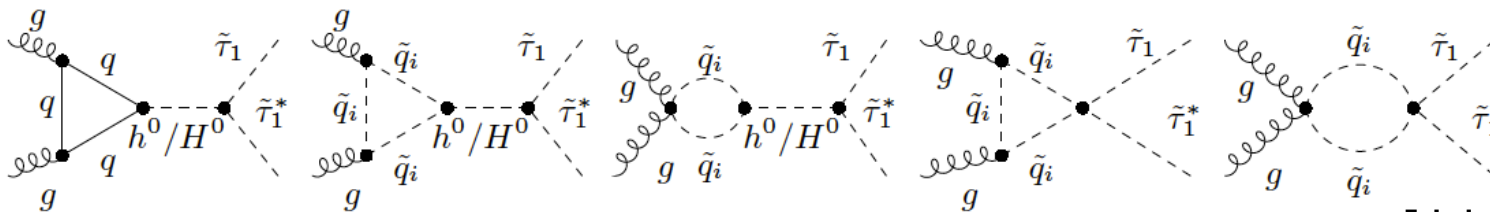
$b\bar{b}$ annihilation



$O(\alpha^2)$ + bottom PDFs

[del Aguila, Ametller; '91; Bisset, Raychaudhuri; '96]

gluon fusion

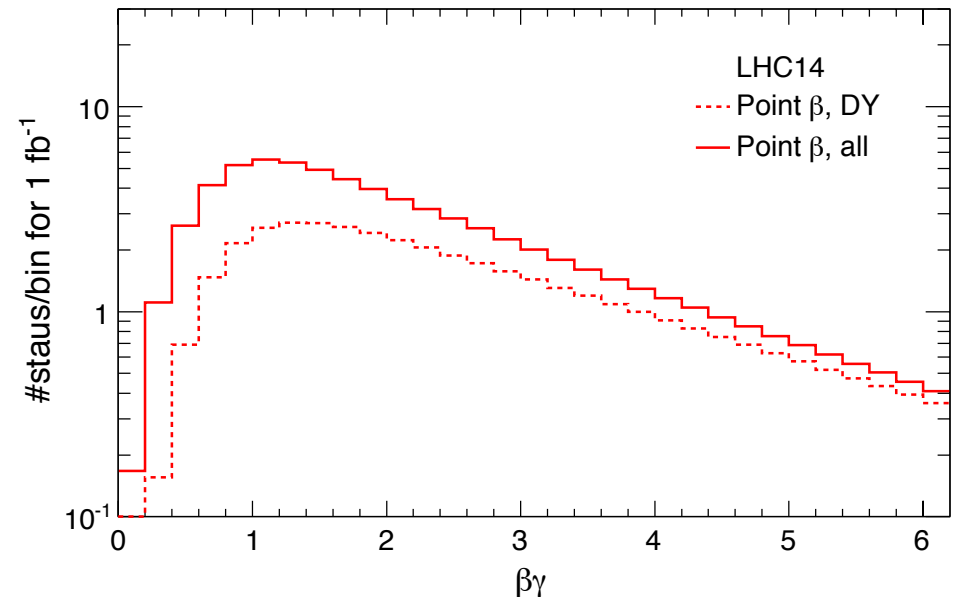
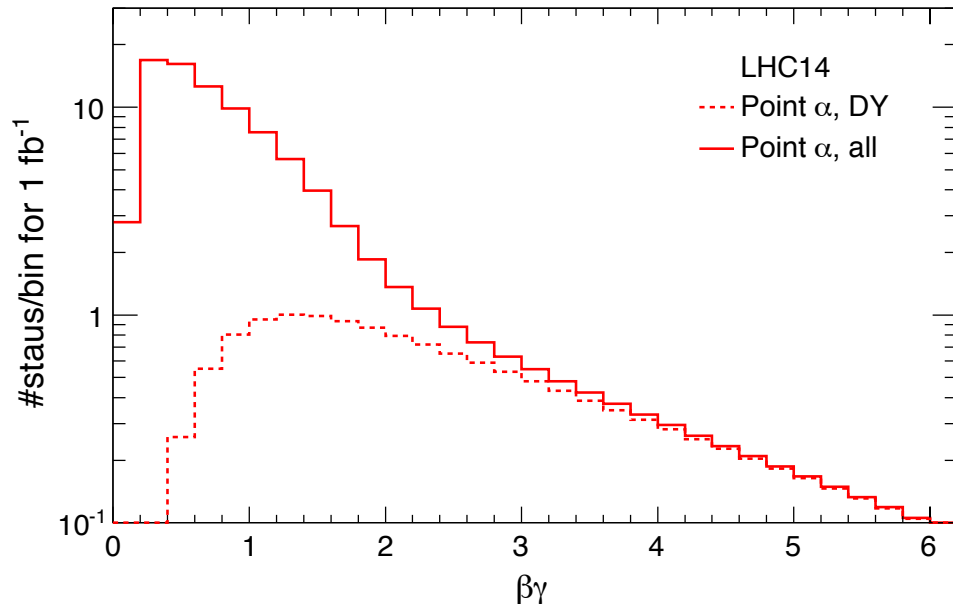


$O(\alpha_s^2 \alpha^2)$

[del Aguila, Ametller; '91; Borzumati, Hagiwara; '09]

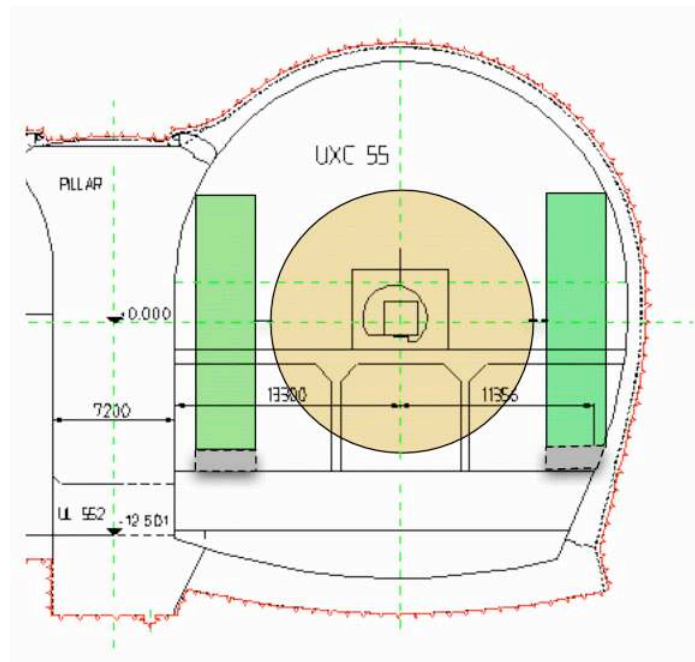
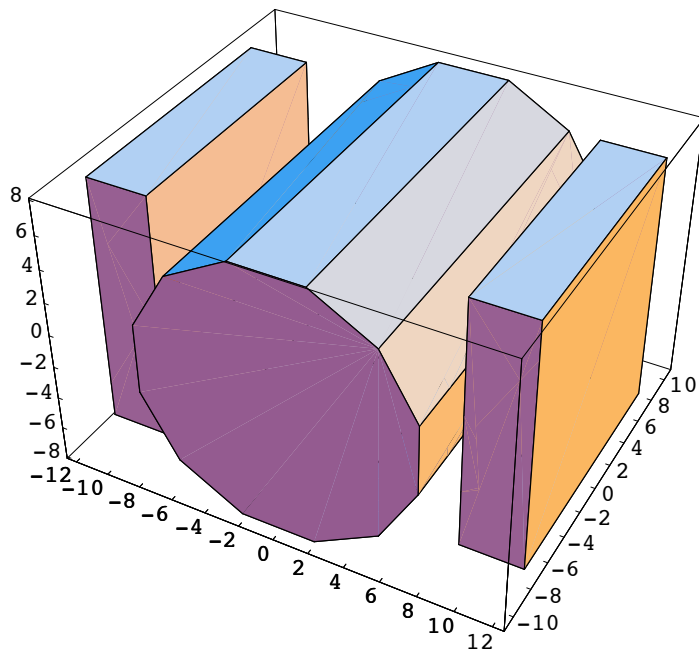
on-shell: $\frac{1}{p^2 - m_{H^0}^2} \rightarrow \frac{1}{p^2 - m_{H^0}^2 + im_{H^0}\Gamma_{H^0}}$

Stopping of long-lived staus



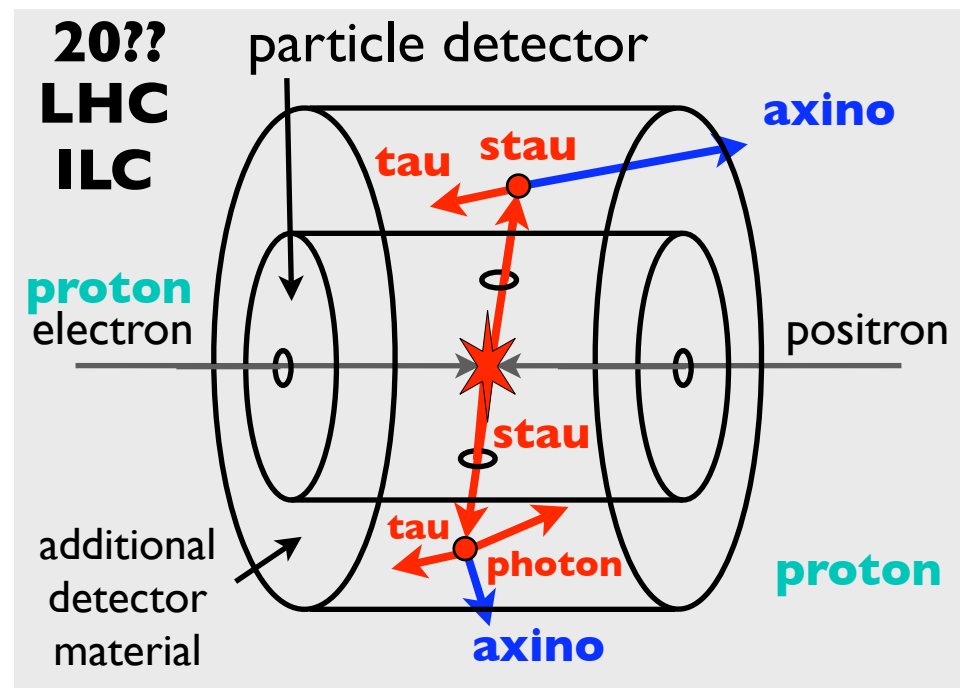
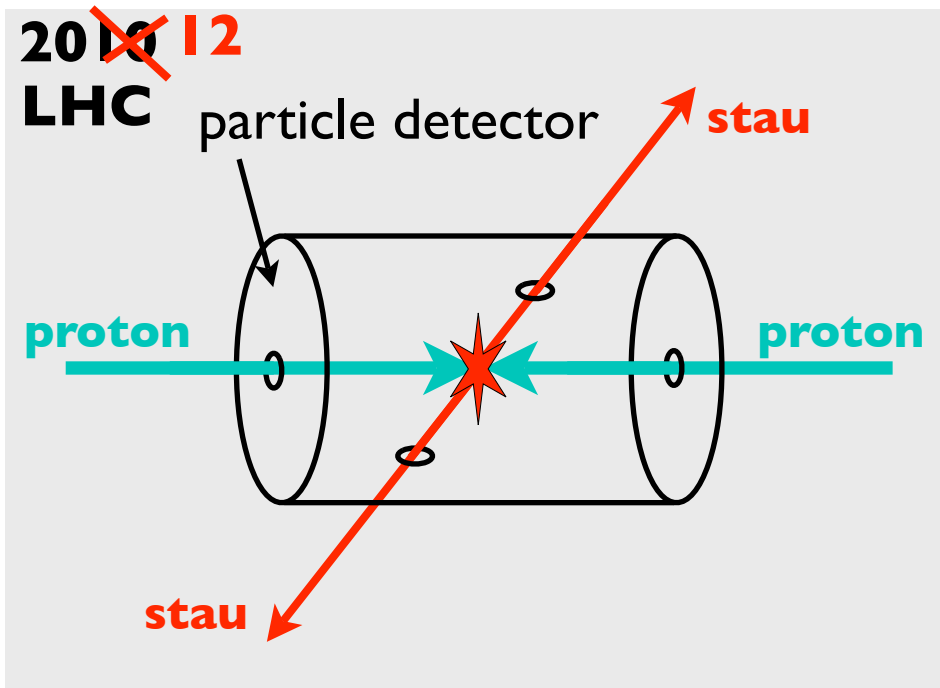
$\tilde{\tau}_1$ are stopped for: $\beta\gamma \lesssim 0.45$

Stopping of long-lived staus @ CMS



[Hamaguchi, Nojiri, de Roeck, '07]

Stopping of long-lived staus



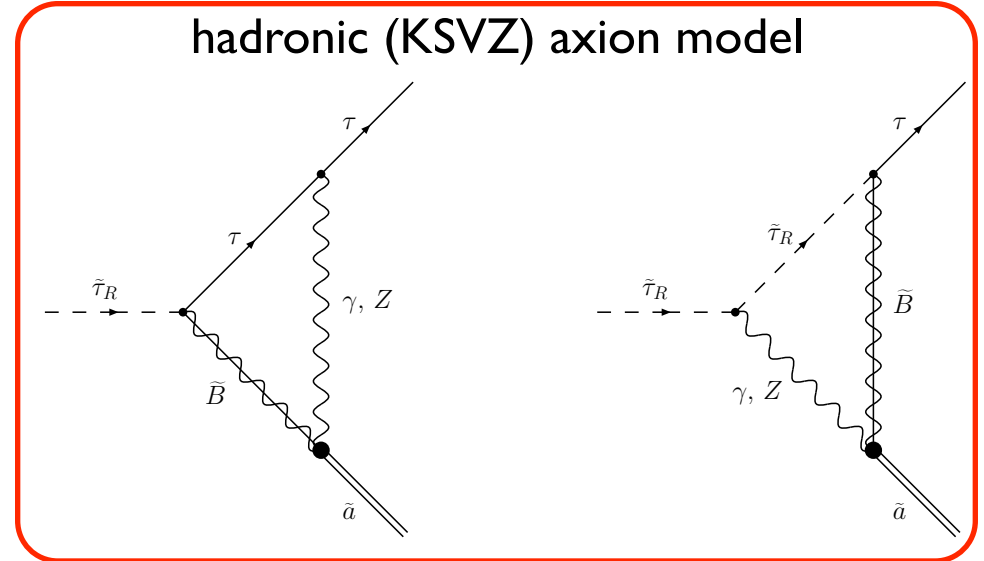
Probing f_a @ Colliders

[Brandenburg et al., '05]

\tilde{a} LSP \rightarrow Peccei–Quinn Scale f_a & Axino Mass $m_{\tilde{a}}$

□ Assumption: $\tilde{\tau}_R$ NLSP & $\tilde{\chi}^0 \simeq \tilde{B}$

- 2-Body Decay $\tilde{\tau}_R \rightarrow \tau + \tilde{a}$



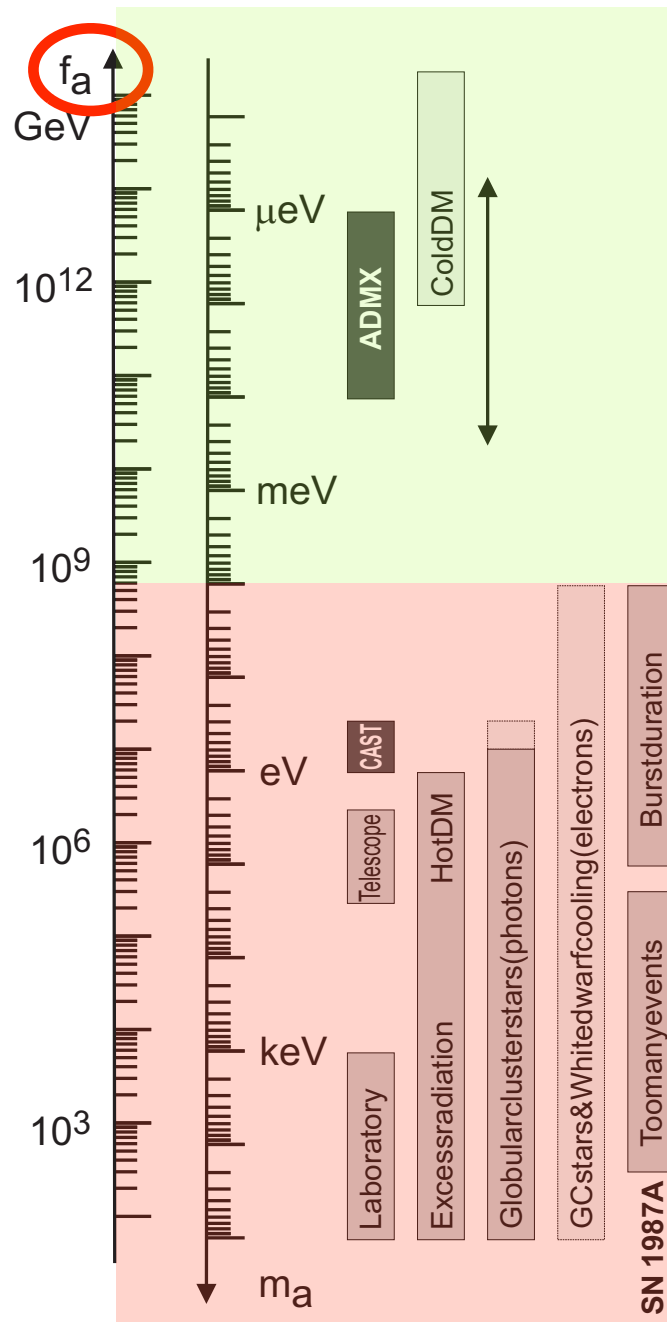
$$\Gamma(\tilde{\tau}_R \rightarrow \tau \tilde{a}) \simeq \xi^2 (25 \text{ sec})^{-1} C_{aYY}^2 \left(1 - \frac{m_{\tilde{a}}^2}{m_{\tilde{\tau}}^2}\right) \left(\frac{m_{\tilde{\tau}}}{100 \text{ GeV}}\right) \left(\frac{10^{11} \text{ GeV}}{f_a}\right)^2 \left(\frac{m_{\tilde{B}}}{100 \text{ GeV}}\right)^2$$

- Peccei–Quinn Scale f_a \longleftarrow NLSP Lifetime $\tau_{\tilde{\tau}} \approx 1/\Gamma(\tilde{\tau}_R \rightarrow \tau \tilde{a})$

$$f_a^2 \simeq \left(\frac{\tau_{\tilde{\tau}}}{25 \text{ sec}}\right) \xi^2 C_{aYY}^2 \left(1 - \frac{m_{\tilde{a}}^2}{m_{\tilde{\tau}}^2}\right) \left(\frac{m_{\tilde{\tau}}}{100 \text{ GeV}}\right) \left(\frac{m_{\tilde{B}}}{100 \text{ GeV}}\right)^2 (10^{11} \text{ GeV})^2$$

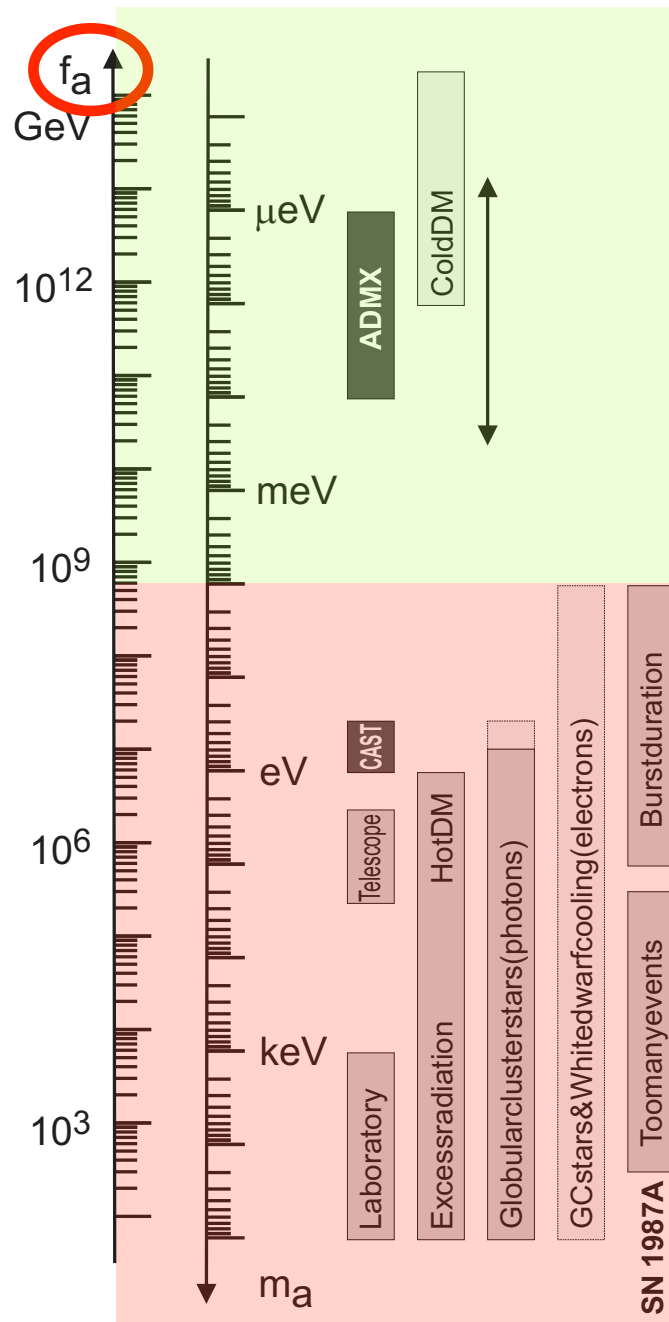
- Axino Mass $m_{\tilde{a}} = \sqrt{m_{\tilde{\tau}}^2 + m_{\tau}^2 - 2m_{\tilde{\tau}}E_{\tau}}$ \longleftarrow Kinematics

Bounds on the Peccei-Quinn Scale



Is the value of the Peccei-Quinn scale inferred from axino searches consistent with astrophysical axion bounds and results from axion searches?

Bounds on the Peccei-Quinn Scale

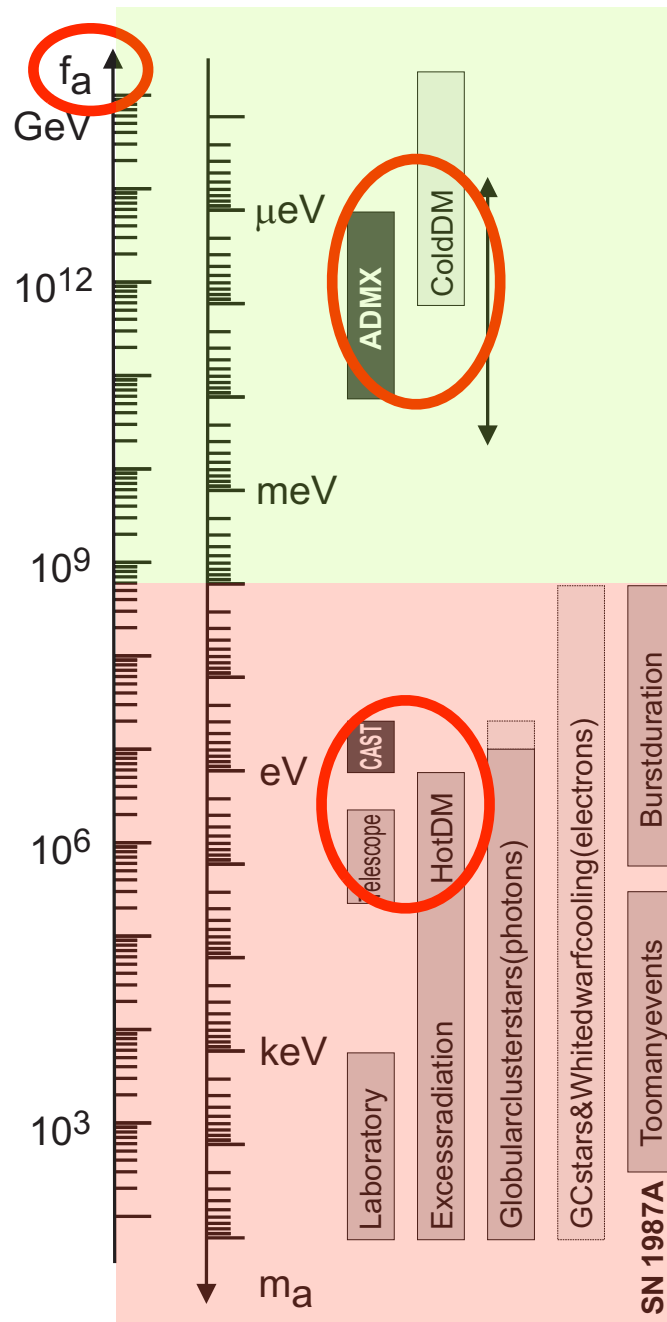


**Agreement between
Axion & Axino Searches**



**Strong Hint for the
Axino LSP**

Bounds on the Peccei-Quinn Scale



**Agreement between
Axion & Axino Searches**

↓

**Strong Hint for the
Axino LSP**

**Axion DM & Axino DM
might coexist!**

Conclusions - Part II

- axino LSP is possible if PQ mech. & SUSY exist
- axinos from therm. prod. and NLSP decays may provide (a fraction of) Ω_{dm} - dep. on $f_{\text{PQ}}, T_{\text{R}}, m_{\text{stau}}$
- stau NLSP is possible - CHAMP signal @ LHC
- BBN constraints - new m_{stau} -dep. upper limits on f_{PQ}
- LHC pheno - prod. & stopping of staus - probing f_{PQ}



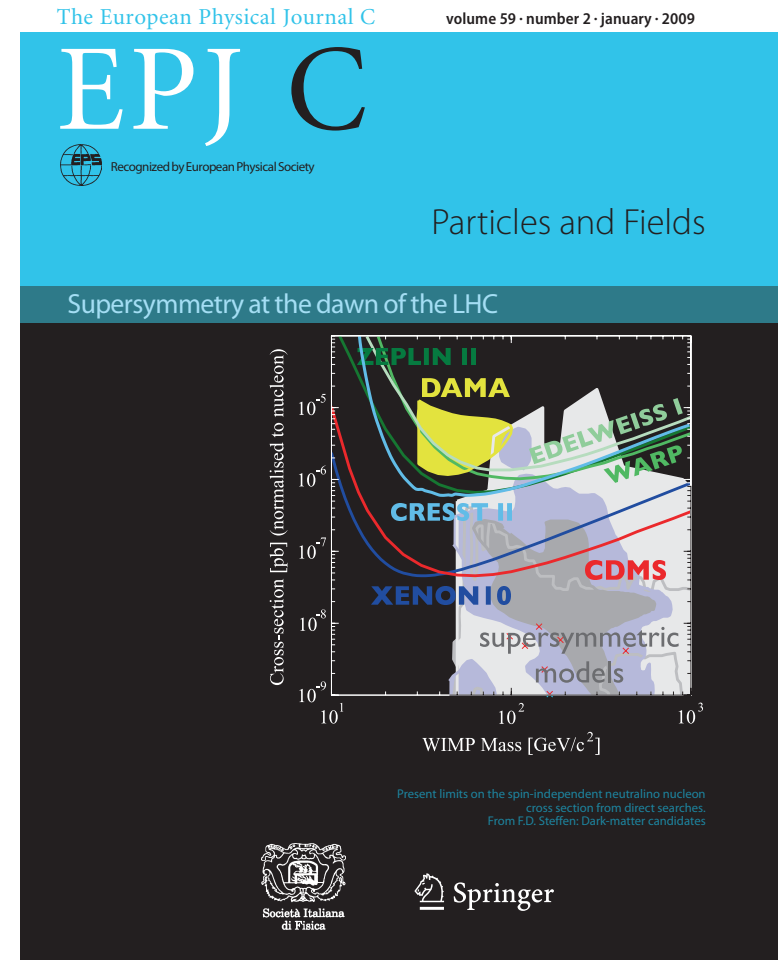
complementary to f_{PQ} determ. in axion searches

For a review (including an extensive list of references),

see

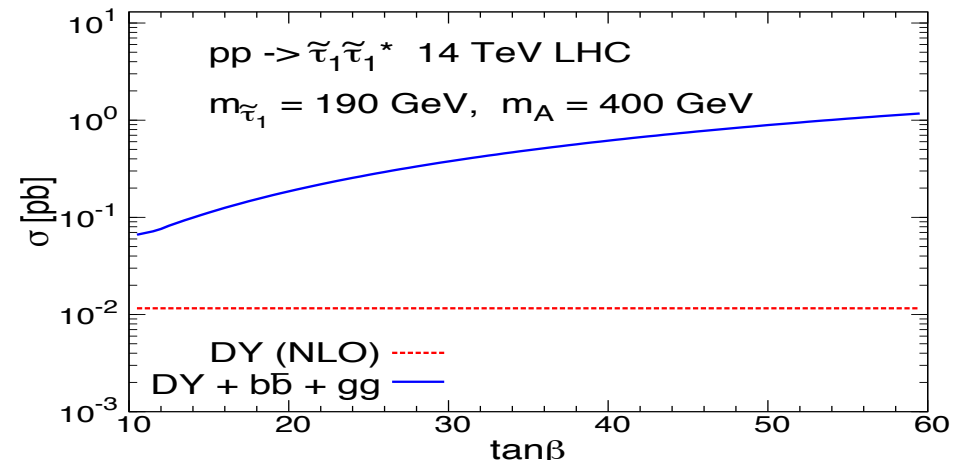
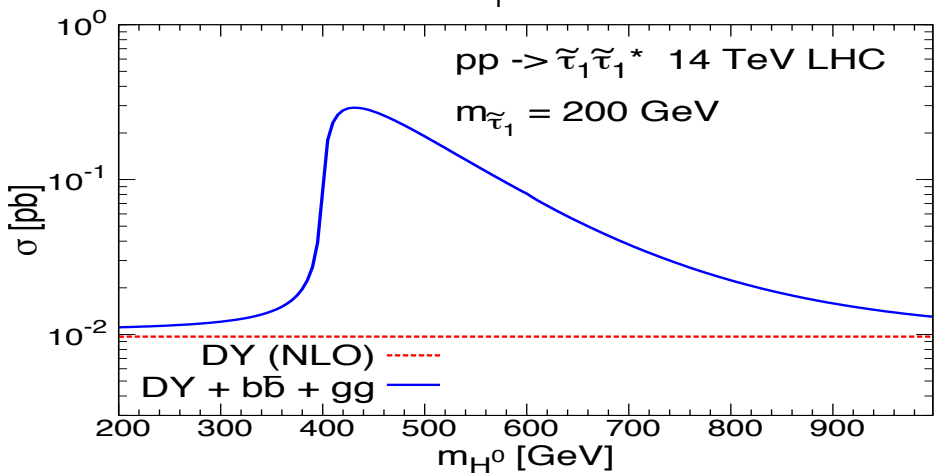
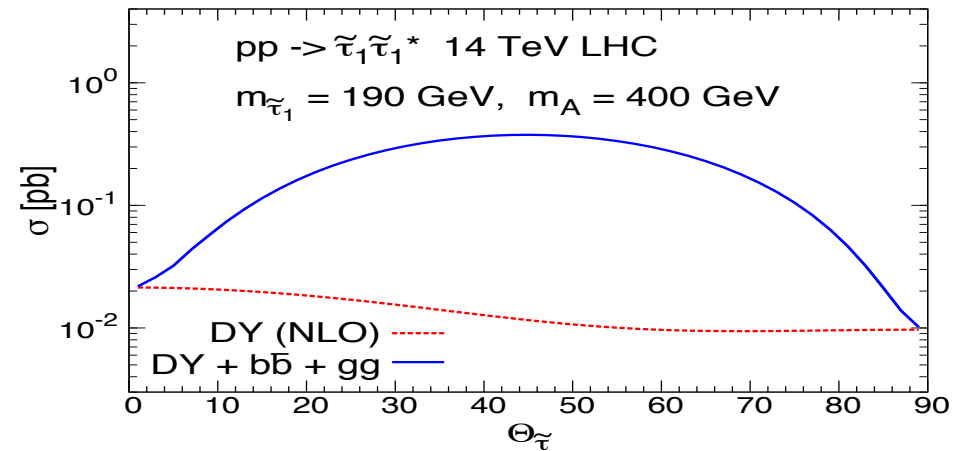
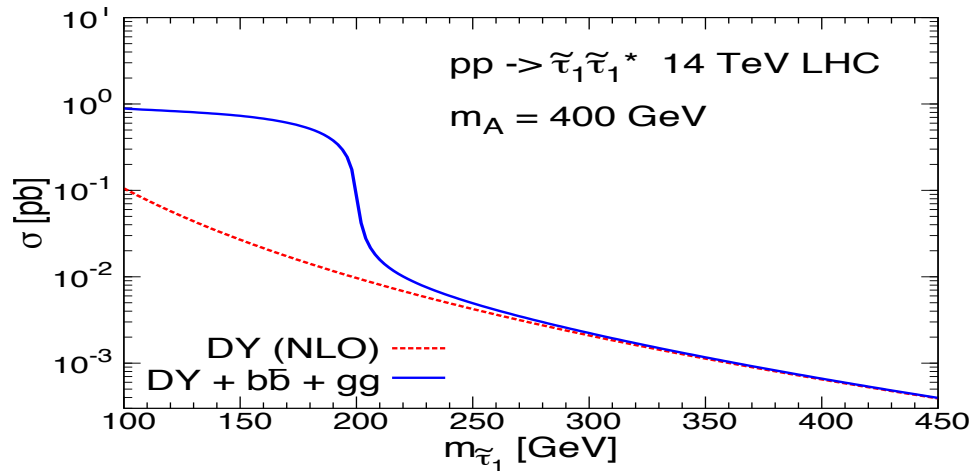
**[FDS, *Dark Matter Candidates*,
Eur. Phys. J. C59 (2009) 557,
arXiv:0811.3347]**

in



Bonus slides

Direct Stau Production @ LHC



$$\theta_{\tilde{\tau}} = 45^\circ, \quad m_{\tilde{\tau}_1} = 200 \text{ GeV},$$

$$\tan \beta = 30, \quad \mu = 500 \text{ GeV}, \quad m_A = 400 \text{ GeV}.$$

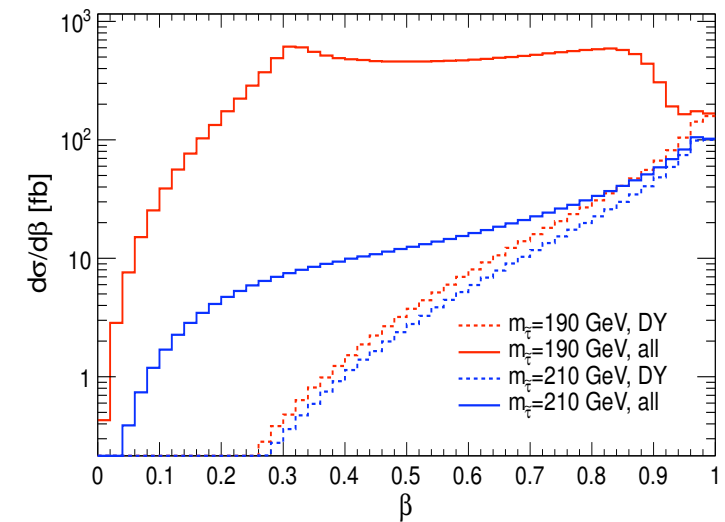
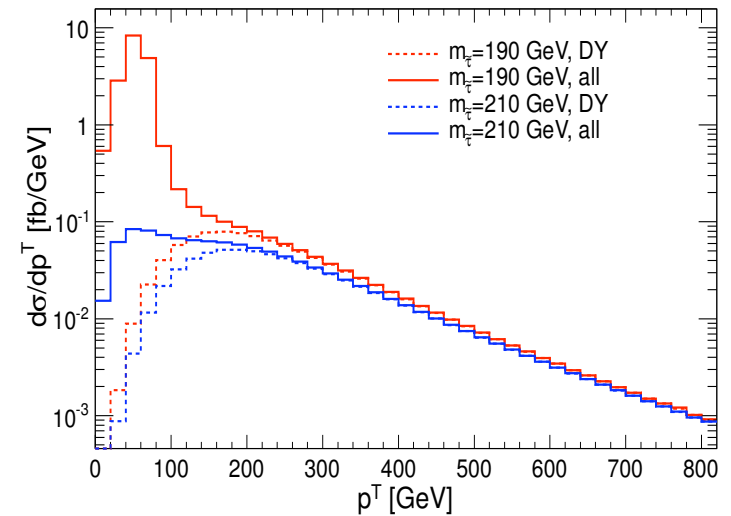
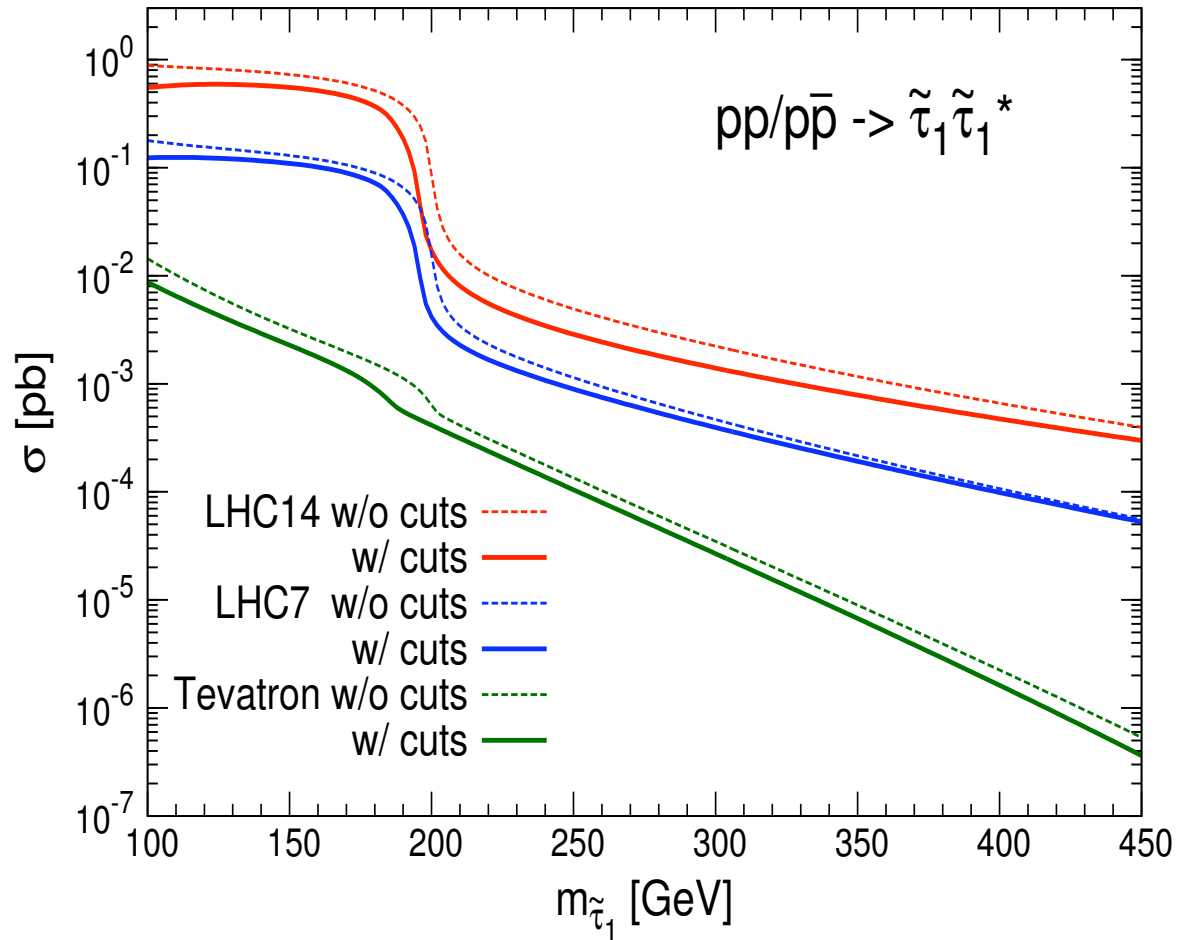
$$M_1 = M_2 = M_3 = 1.2 \text{ TeV}, \quad A_t = A_b = A_\tau = 600 \text{ GeV},$$

$$m_{\tilde{Q}_i} = m_{\tilde{U}_i} = m_{\tilde{D}_i} = 1 \text{ TeV}, \quad m_{\tilde{L}_{1/2}} = m_{\tilde{E}_{1/2}} = 500 \text{ GeV}$$

Kinematical Cuts

$$p^T > 40 \text{ GeV}, \quad 0.4 < \beta < 0.9,$$

$$|\eta| < 0.7 \text{ (Tevatron)} \quad |\eta| < 2.4 \text{ (LHC)}$$



Direct Production vs. Cascade Decays

Benchmark point	α	β	γ	ϵ
LHC 7 TeV				
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{\text{DY}}$	[fb] 3.2 (2.3)	12.5 (7.3)	9.0 (5.6)	7.95 (5.00)
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{b\bar{b}}$	[fb] 9.8 (5.1)	0.03 (0.02)	19.2 (16.5)	0.07 (0.06)
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{\text{gg}}$	[fb] 0.1 (0.1)	3.3 (2.4)	0.32 (0.25)	0.01 (0.01)
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{\text{all}}$	[fb] 13.1 (7.5)	15.8 (9.7)	28.5 (22.4)	8.03 (5.07)
$\sigma(\tilde{g}\tilde{g})$	[fb] 0.05	10^{-6}	0.06	2.57
$\sigma(\tilde{g}\tilde{q})$	[fb] 0.63	4×10^{-4}	0.99	37.36
$\sigma(\tilde{q}\tilde{q})$	[fb] 1.18	0.006	2.41	77.25
$\sigma(\tilde{\chi}\tilde{q})+\sigma(\tilde{\chi}\tilde{g})$	[fb] 0.481	0.007	0.72	12.77
$\sigma(\tilde{\chi}\tilde{\chi})$	[fb] 20.4	0.29	19.8	91.78
LHC 14 TeV				
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{\text{DY}}$	[fb] 11.2 (5.64)	37.5 (15.9)	28.0 (12.4)	24.7 (11.2)
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{b\bar{b}}$	[fb] 58.4 (27.0)	0.7 (0.2)	113.3 (87.1)	0.5 (0.4)
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{\text{gg}}$	[fb] 0.7 (0.4)	17.4 (11.1)	1.8 (1.3)	0.07 (0.05)
$\sigma(\tilde{\tau}_1 \tilde{\tau}_1^*)_{\text{all}}$	[fb] 70.3 (33.1)	55.6 (27.2)	143.1 (100.8)	25.3 (11.6)
$\sigma(\tilde{g}\tilde{g})$	[fb] 20.2	0.12	20.8	232.19
$\sigma(\tilde{g}\tilde{q})$	[fb] 104.4	2.46	133.2	1328.4
$\sigma(\tilde{q}\tilde{q})$	[fb] 92.5	6.46	139.0	1301.1
$\sigma(\tilde{\chi}\tilde{q})+\sigma(\tilde{\chi}\tilde{g})$	[fb] 16.9	1.08	22.4	175.12
$\sigma(\tilde{\chi}\tilde{\chi})$	[fb] 134.5	6.40	131.1	422.2

Benchmark point	α	β	γ	ϵ
$m_{1/2}$	[GeV] 600	1050	600	440
m_0	[GeV] 800	30	600	20
$\tan\beta$		55	55	15
A_0	[GeV] 1600	60	1200	-250
$m_{\tilde{\tau}_1}$	[GeV] 193	136	148	153
$\theta_{\tilde{\tau}}$		81°	73°	77°
m_{H^0}	[GeV] 402	763	413	613
Γ_{H^0}	[GeV] 15	26	16	2.2
$m_{\tilde{g}}$	[GeV] 1397	2276	1385	1028
avg. $m_{\tilde{q}}$	[GeV] 1370	1943	1287	894
μ	[GeV] 667	1166	648	562
A_τ	[GeV] 515	-143	351	-275
$\text{BR}(b \rightarrow s\gamma)$	$[10^{-4}]$ 3.08	3.03	2.94	3.00
$\text{BR}(B_s^0 \rightarrow \mu^+\mu^-)$	$[10^{-8}]$ 1.65	1.04	2.44	0.30
a_μ	$[10^{-10}]$ 13.2	11.5	16.8	18.7
CCB [108]		✓	—	✓
$Y_{\tilde{\tau}_1}$	$[10^{-15}]$ 3.5	2.5	37.7	164

$m_{\text{axino}}, m_{\text{gravitino}} < m_{\text{stau}}$

