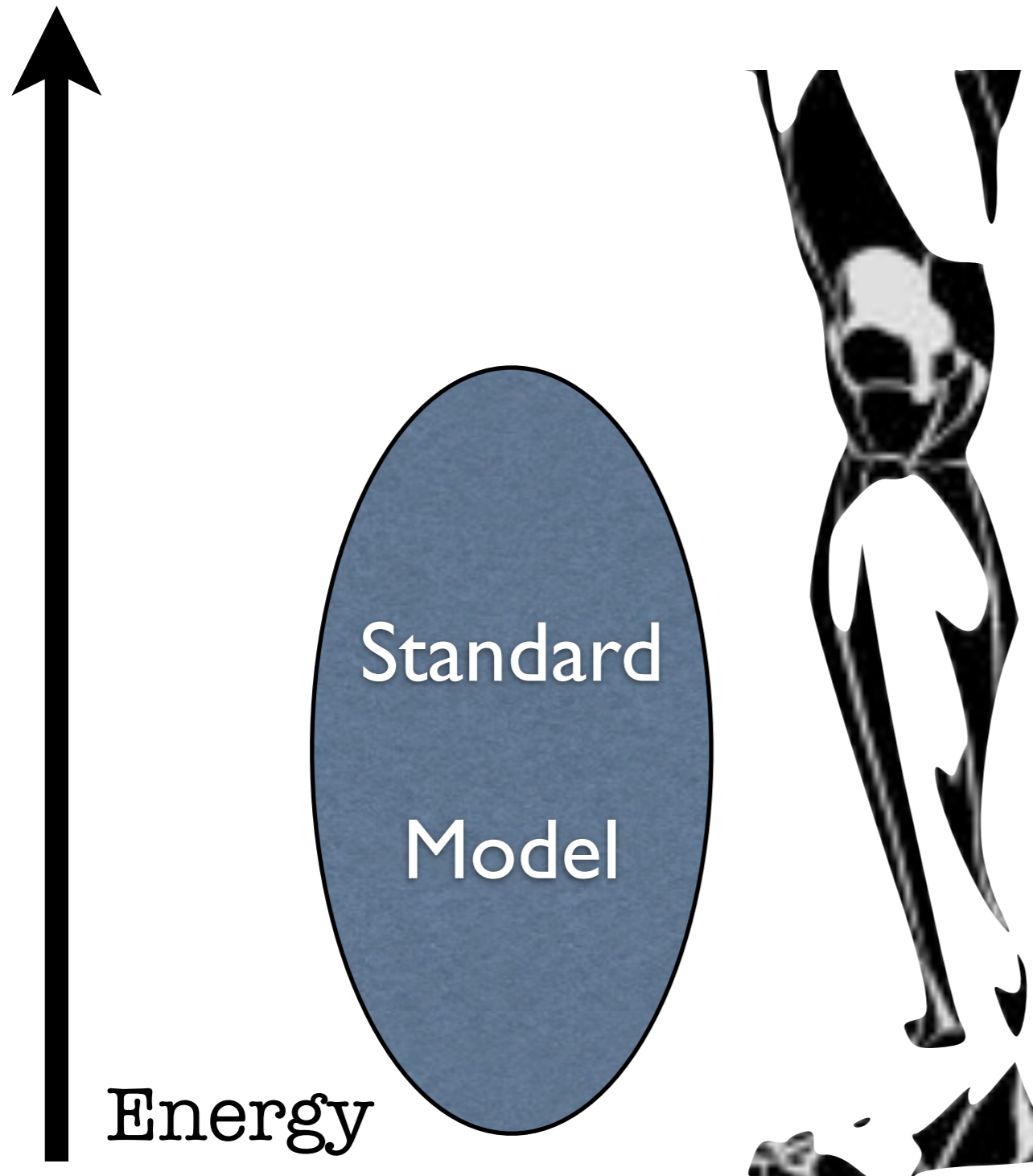




WISPy Cold Dark Matter

Heretic contribution to Vistas in axions:
A Roadmap for Theoretical and Experimental Axions Physics through 2025

Javier Redondo, MPP München



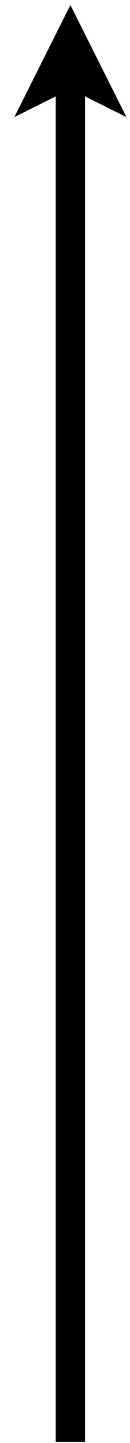
Describes
extremely well
fundamental physics
(at low energies)

but feels certainly

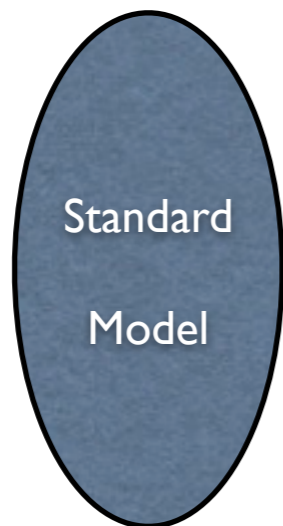
INCOMPLETE

Beyond the SM

... at low energies



Energy



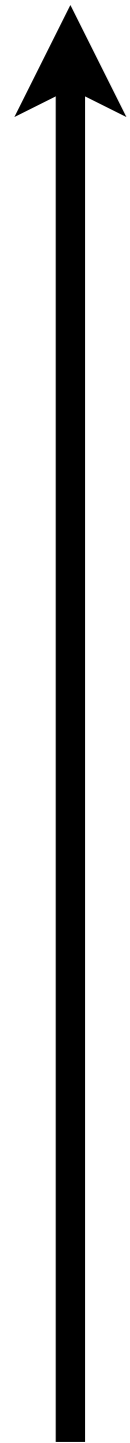
Standard
Model



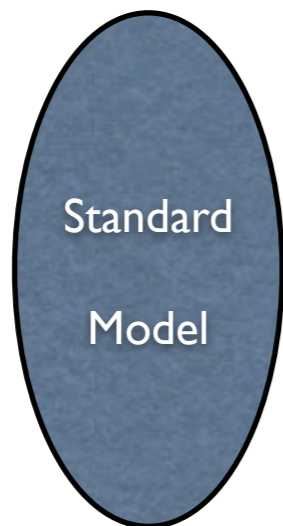
Answers are
awaiting in the
high energy frontier
where more symmetric
beautiful theories arise

Beyond the SM

... at low energies



Energy



Standard
Model



Answers are
awaiting in the
high energy frontier
where more symmetric
beautiful theories arise

... and often
imply physics at low
energies



Energy

Standard
Model



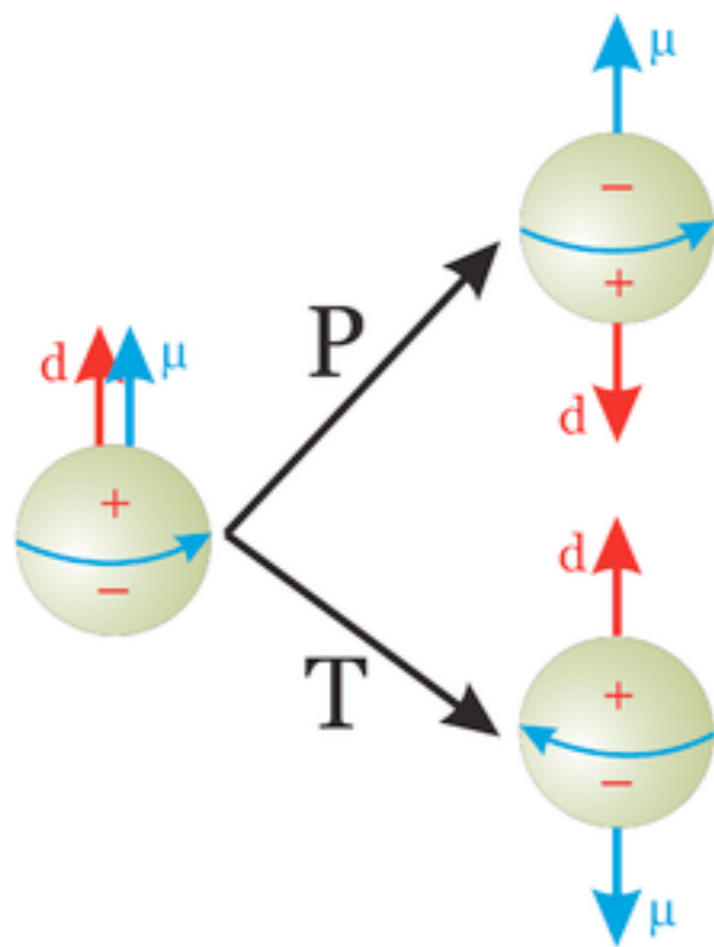
Weakly Interacting
Slim Particles
WISPs

The paradigmatic example: Strong CP problem

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \theta$$

Violates P and T

neutron EDM



$\theta_{\text{QCD}} \in (-\pi, \pi)$
 $\arg \det \mathcal{M}_q \sim \mathcal{O}(1)?$

Prediction:

$$d_n \sim 10^{-15} \theta \text{ ecm}$$

The paradigmatic example: Strong CP problem

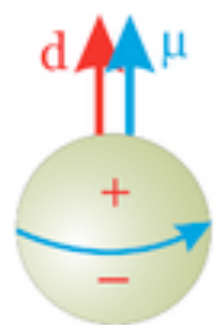
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Violates P and T

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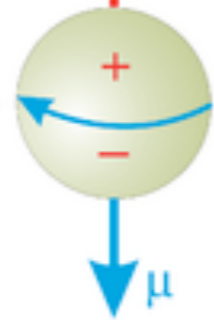
$\theta_{\text{QCD}} \in (-\pi, \pi)$
 $\arg \det M_q \sim \mathcal{O}(1)?$

Non Observation:
 $d_n < 2.6 \times 10^{-26} \text{ ecm}$
 $\theta \lesssim 10^{-11}$ Why ??????



P

T



Prediction:

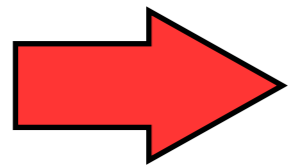
$$d_n \sim 10^{-15} \theta \text{ ecm}$$

Peccei-Quinn symmetry and the axion

Introduce a new axial global color-anomalous symmetry, which is spontaneously broken at a high energy scale, $\gg \text{TeV}$

Peccei-Quinn symmetry and the axion

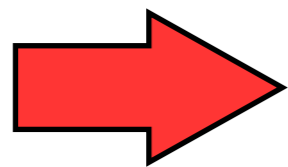
Introduce a new axial global color-anomalous symmetry, which is spontaneously broken at a high energy scale, $\gg \text{TeV}$



Massless Goldstone Boson: the axion

Peccei-Quinn symmetry and the axion

Introduce a new axial global color-anomalous symmetry, which is spontaneously broken at a high energy scale, $\gg \text{TeV}$



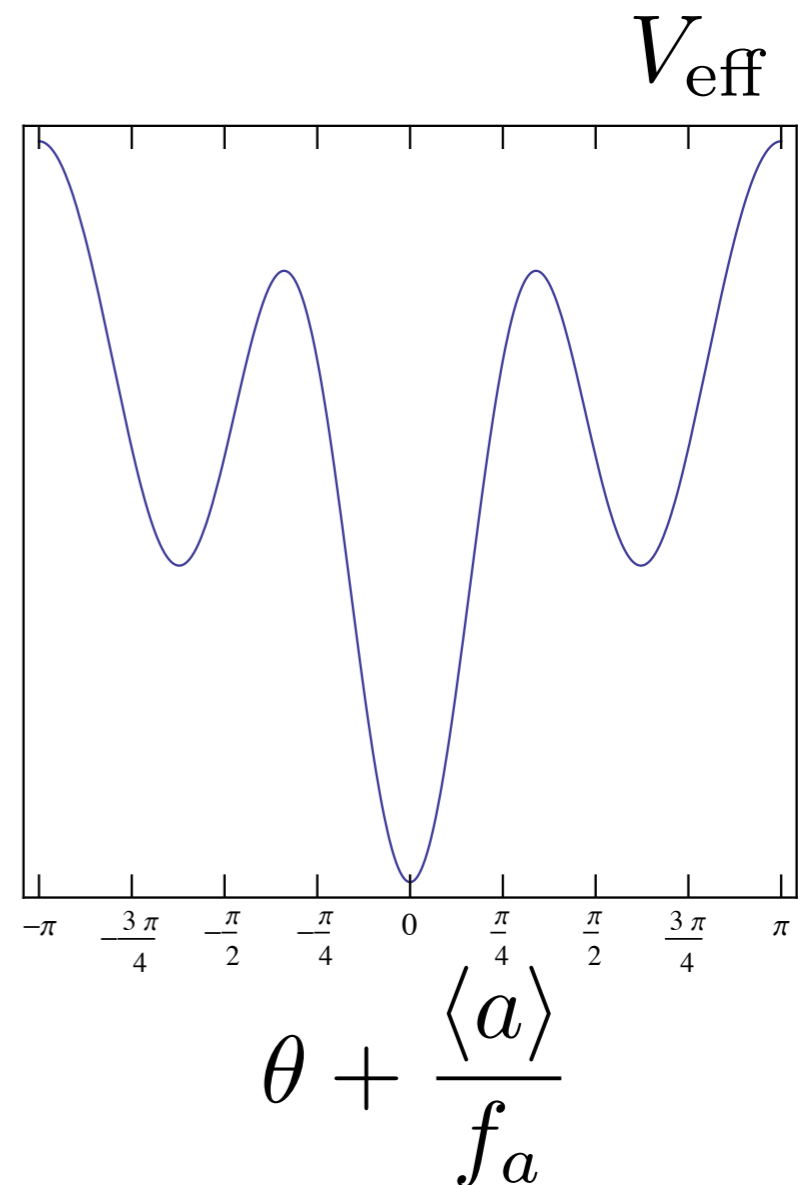
Massless Goldstone Boson: the axion

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \left(\theta + \frac{a}{f_a} \right)$$

Free parameter

The QCD induced potential is minimized for ...

$$\theta_{\text{eff}} = \theta + \frac{\langle a \rangle}{f_a} = 0$$



Peccei-Quinn symmetry and the axion

Introduce a new axial global color-anomalous symmetry, which is spontaneously broken at a high energy scale.

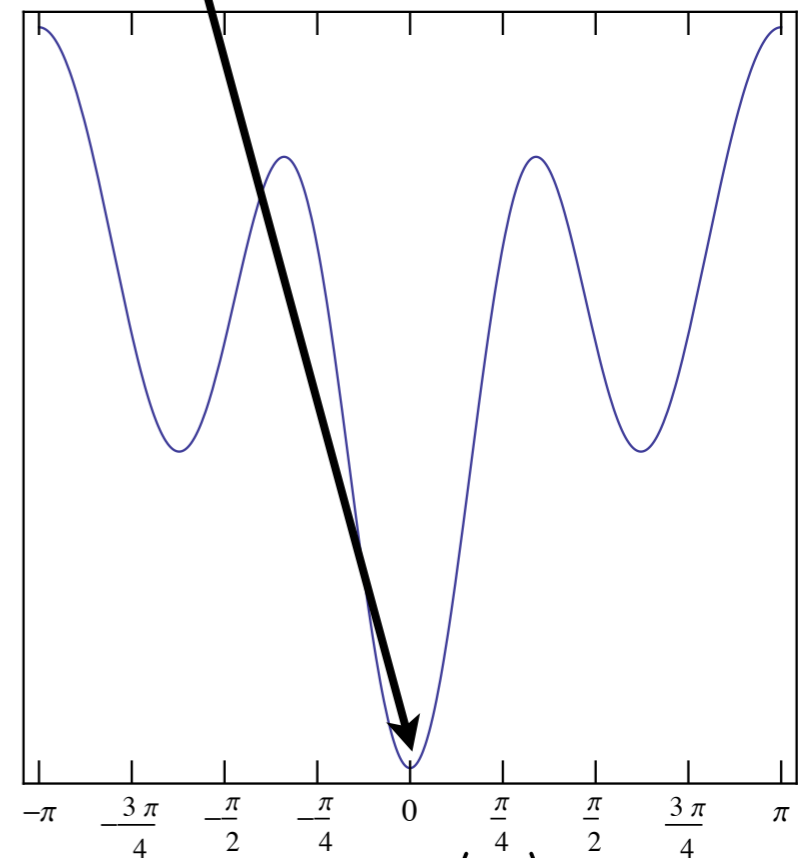
The axions adjust its v.e.v. to cancel the effects of any theta!

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \left(\theta + \frac{a}{f_a} \right)$$

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$$\theta_{\text{eff}} = \theta + \frac{\langle a \rangle}{f_a} = 0$$



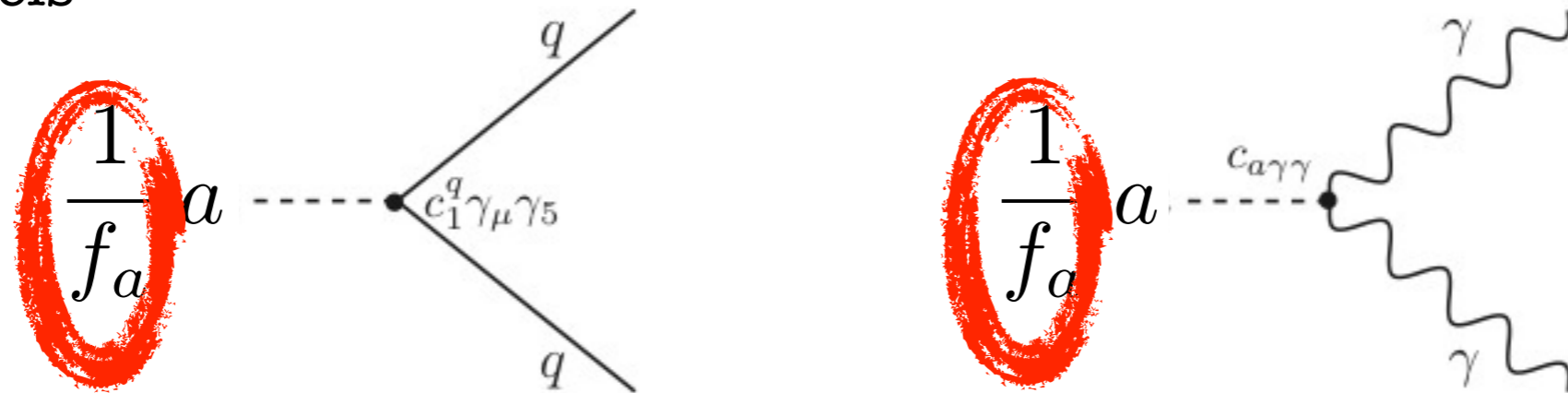
$$\theta + \frac{\langle a \rangle}{f_a}$$

Axion mixes with QCD mesons and gets mass and couplings

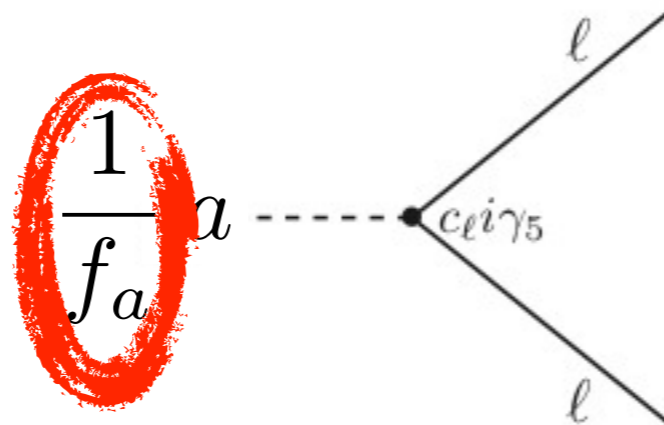
Mass

$$m_a \simeq m_\pi \frac{f_\pi}{f_a} \simeq 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$$

Bare models



Extended models also feature couplings to leptons



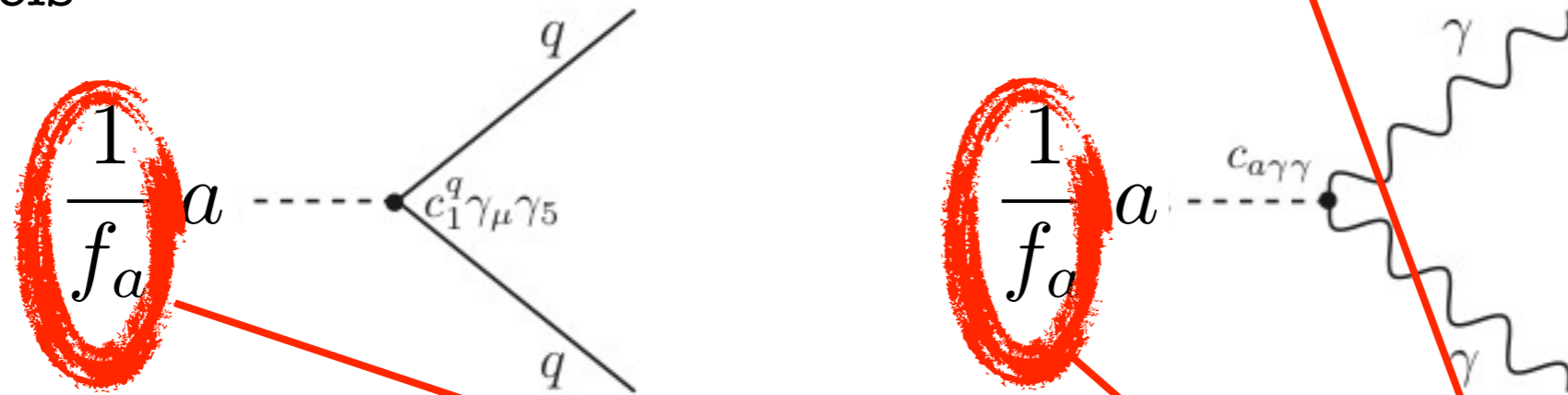
Axion mixes with QCD mesons and gets mass and couplings

Typical from Nambu-Goldstone Bosons

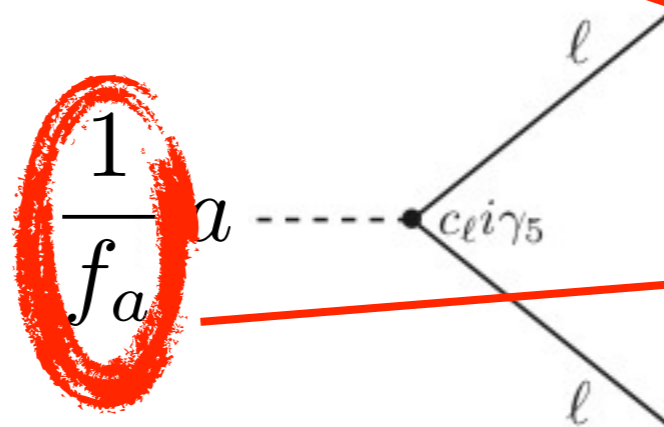
Mass

$$m_a \simeq m_\pi \frac{f_\pi}{f_a} \simeq 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$$

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Extended models also feature couplings to leptons

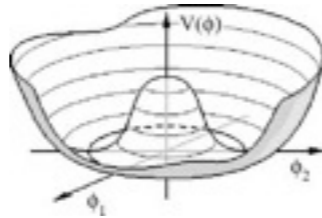


Axion-like particles (ALPs)

0-

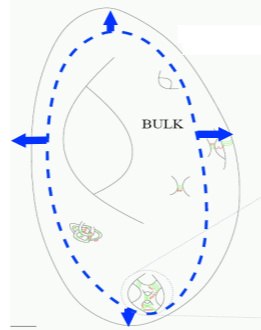
pseudo Goldstone bosons

Global continuous symmetry spontaneously broken at high energy scale M



String 'axions'

Sizes and deformations of extra dimensions, gauge couplings



Reference model (this talk)

$$\mathcal{L} = \mathcal{L}_{\text{free}} + \frac{g}{4} F_{\mu\nu} \tilde{F}^{\mu\nu} \phi$$

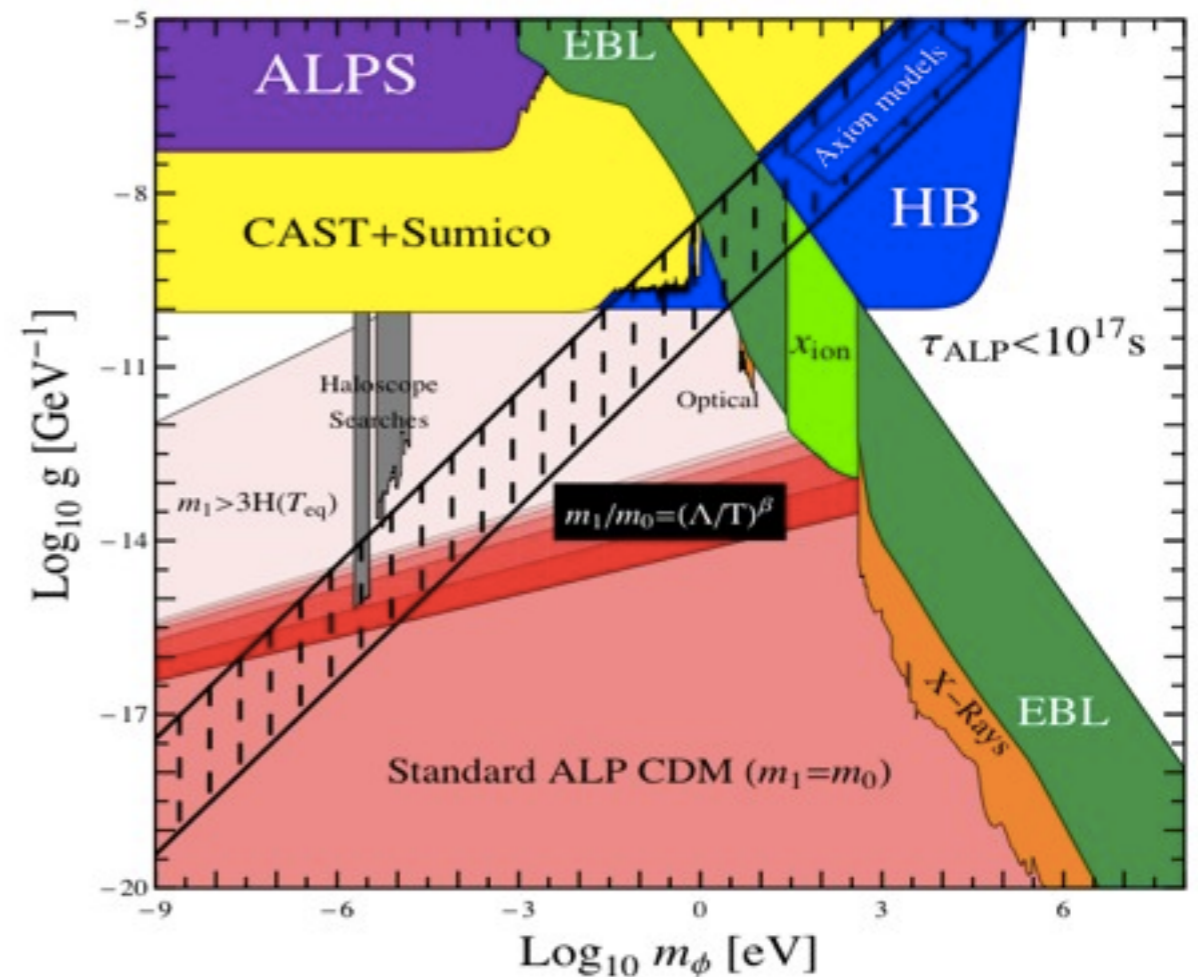
$$g \sim \alpha / 2\pi M$$

independent

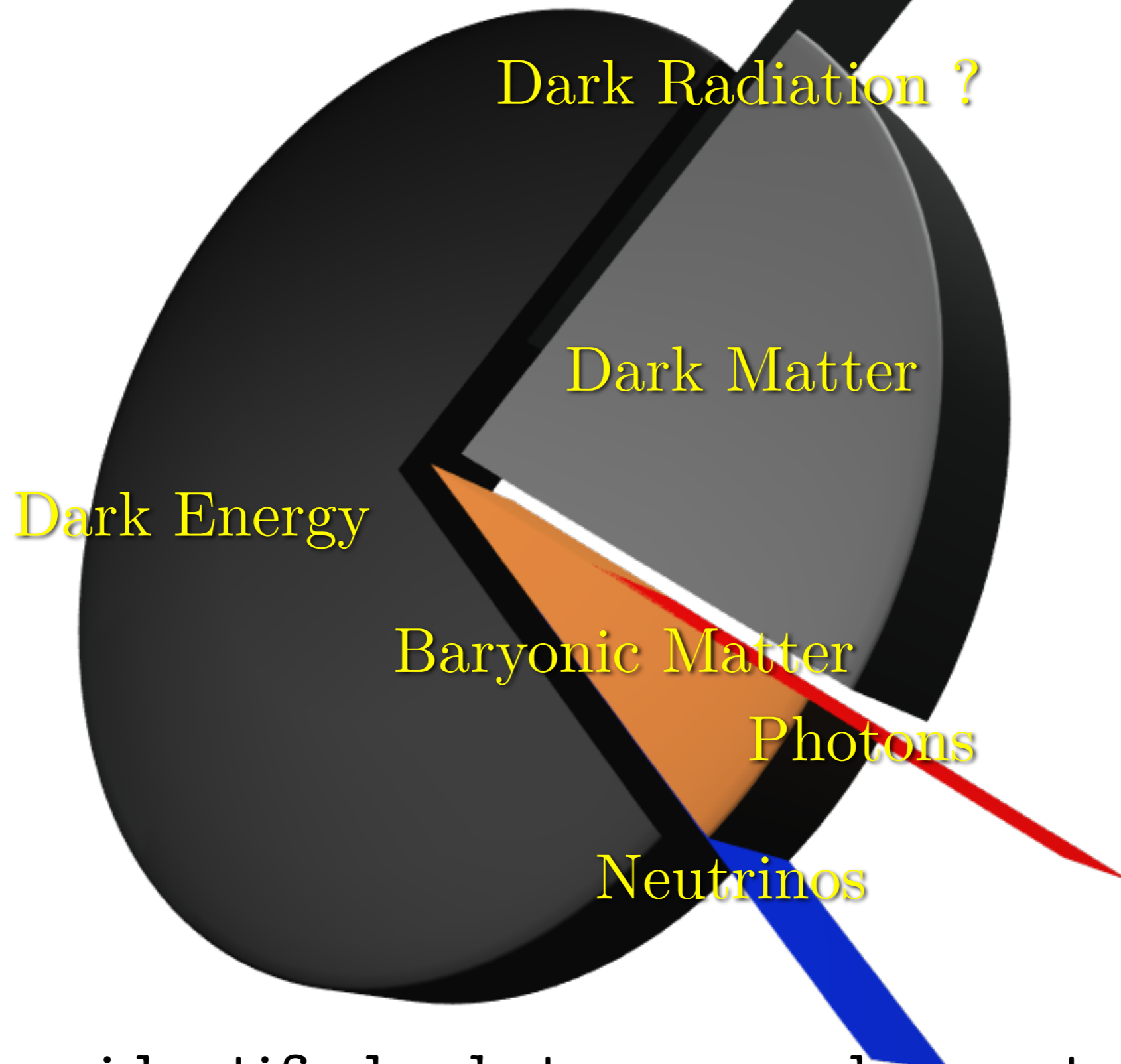
mass m_ϕ

π^0 MAJORONS
 η R-AXION FAMILONS
 η'
 a

DILATONS
 MODULI
 RADION



Energy content of the Universe today



Three unidentified substances make most of it!

Energy content of the Universe today

Dark Radiation ?

Can they be made out of WISPs?

Dark Matter

Dark Energy

... Indeed!

Three unidentified substances make most of it!

Energy content of the Universe today



Three unidentified substances make most of it!

What do we know about Dark Matter particles?

Basically only what the name suggests:

- Dark -
in the sense that they
interact very weakly
with SM particles.
(and among themselves)



Dark Matter

- Matter -
in the sense that are
non-relativistic
(most of them)

What do we know about Dark Matter particles?

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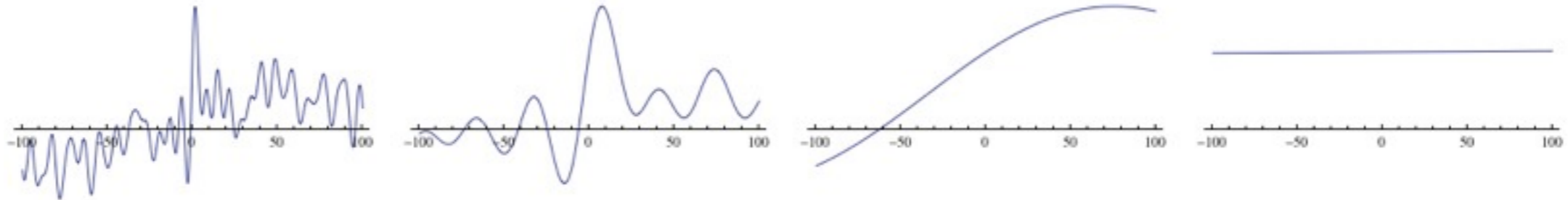
- Dark -
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Dark Matter

- Matter -
in the sense that are
non-relativistic
(most of them)

WISPy Dark matter is generically COLD!

During Inflation inhomogeneities in bosonic fields are stretched out.
Fields become ultra-homogeneous (ultra COLD!)



Afterwards:

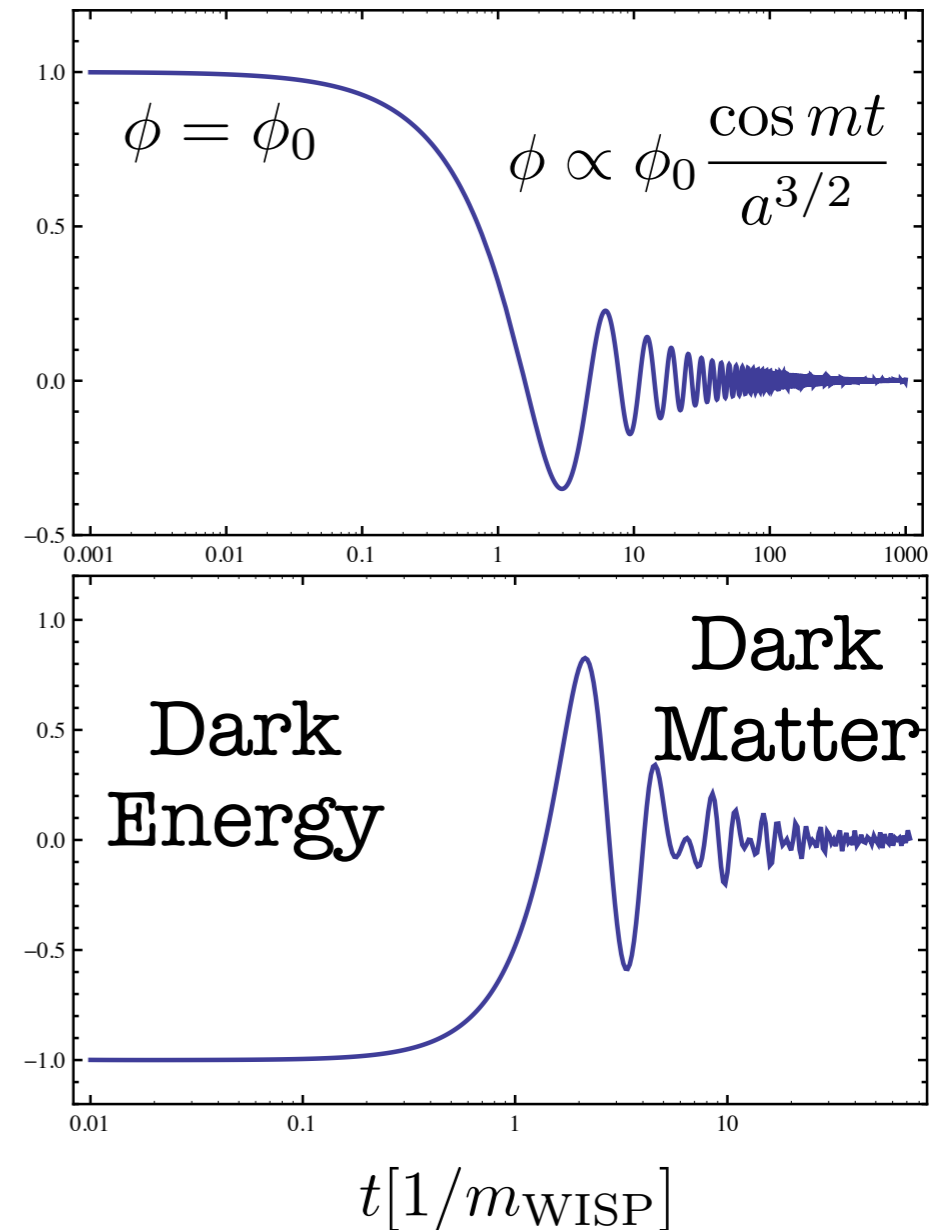
$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = (\text{very weak interactions})$$

Evolution of homogeneous WISP field
in expanding universe

Equation of state

$$\frac{\phi(t)}{\phi_0}$$

$$\frac{p}{\rho}$$



Right amount of WISPy Dark matter

In the simplest ALP/HP models:

$$\rho_{\phi,0} \simeq 1.17 \frac{\text{keV}}{\text{cm}^3} \times \sqrt{\frac{m_\phi}{\text{eV}}} \left(\frac{\phi_0}{4.8 \times 10^{11} \text{ GeV}} \right)^2 \mathcal{F},$$

$$\text{recall } \rho_{\text{CDM}} = 1.17(6) \frac{\text{keV}}{\text{cm}^3}$$

The most important factor is the initial amplitude
it requires physics at very high energies at play

(Detecting WISPy DM opens a window to HEP!!!)
in a sense...

But this model only testable if BECs and forms
caustic rings (See P. Sikivie's talk)

One more level of complication

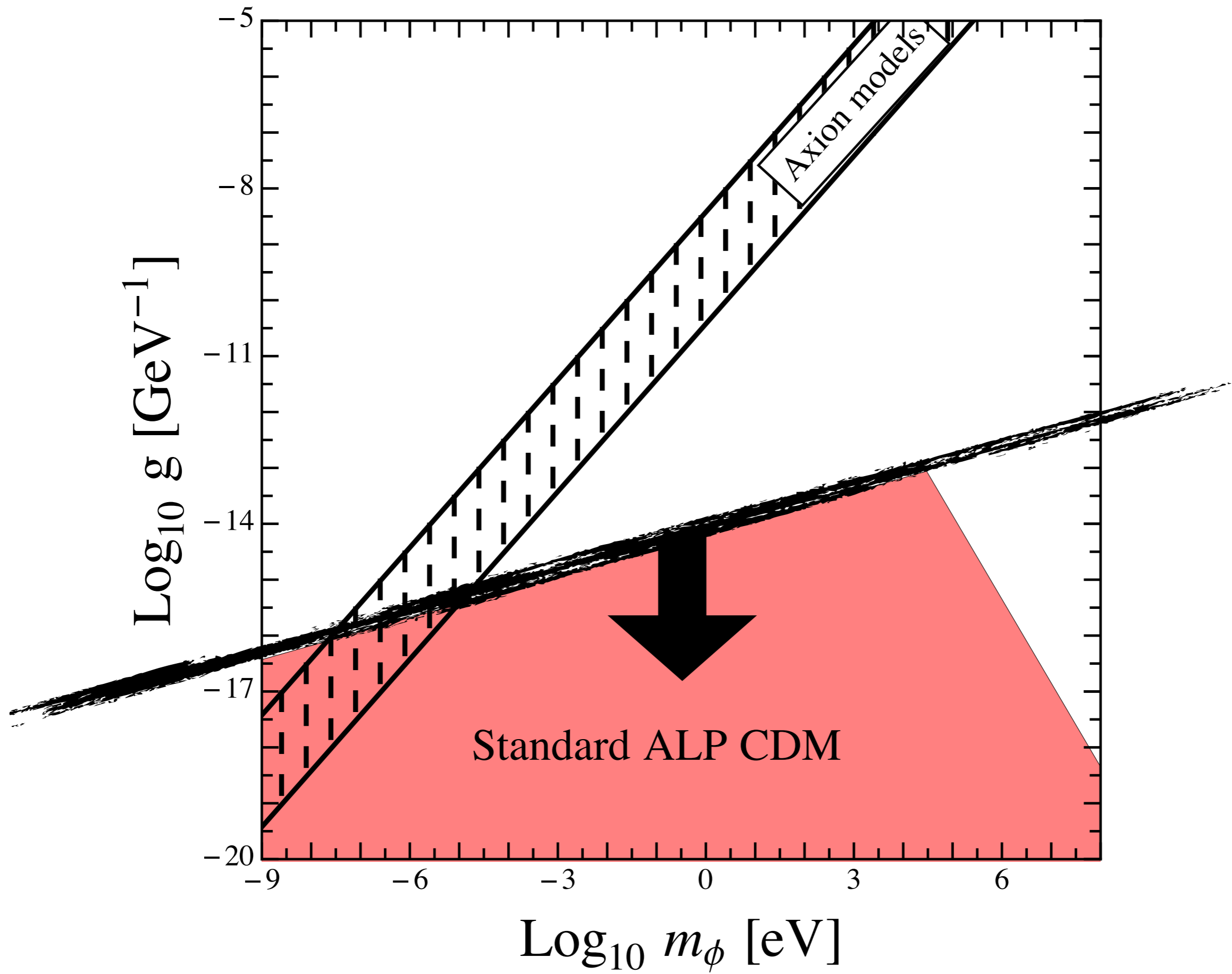
Consider an ALP with a two photon coupling

$$\mathcal{L} = \mathcal{L}_{\text{free}} + \frac{g}{4} F_{\mu\nu} \tilde{F}^{\mu\nu} \phi \quad g \equiv \frac{\alpha}{2\pi} \frac{1}{f_\phi} \mathcal{N} \quad \mathcal{N} \sim \mathcal{O}(1)$$

Since the coupling is $1/f$ and the v.e.v. is $\mathcal{O}(f)$
we can relate the DM abundance with coupling

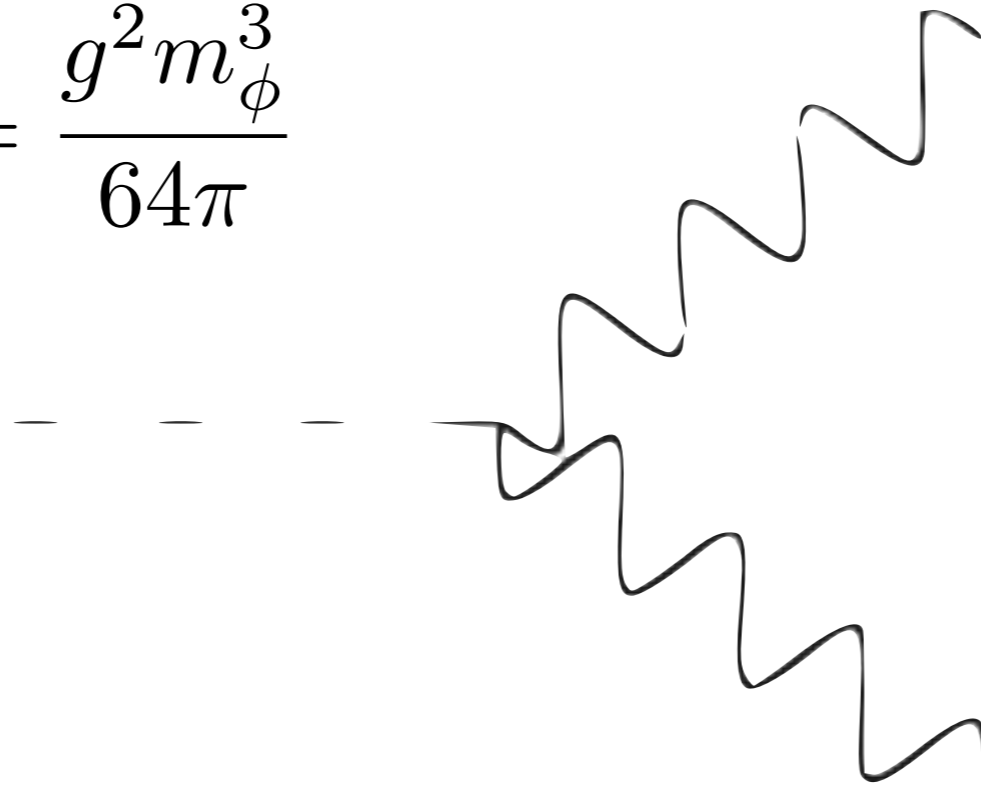
$$\phi_0 \in (-\pi f_\phi, \pi f_\phi) \quad \phi_0 < \frac{\alpha \mathcal{N}}{2} \frac{1}{g}$$

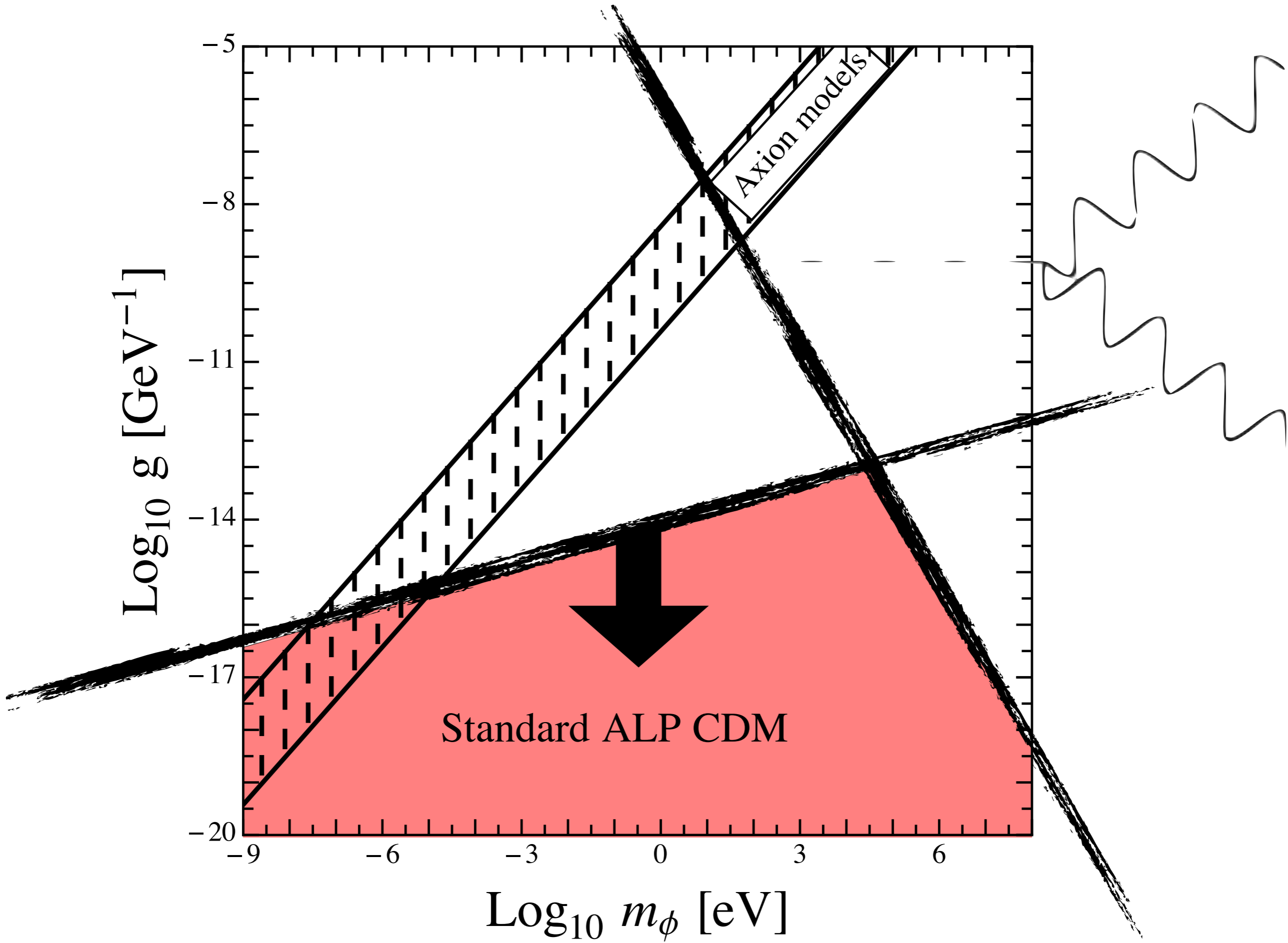
$$\rho_{\phi,0} \lesssim 1.17 \frac{\text{keV}}{\text{cm}^3} \times \sqrt{\frac{m_\phi}{\text{eV}}} \left(\frac{0.8 \times 10^{-14} \text{ GeV}^{-1}}{g} \right)^2 \mathcal{F} \mathcal{N}^2,$$



But ALPs decay

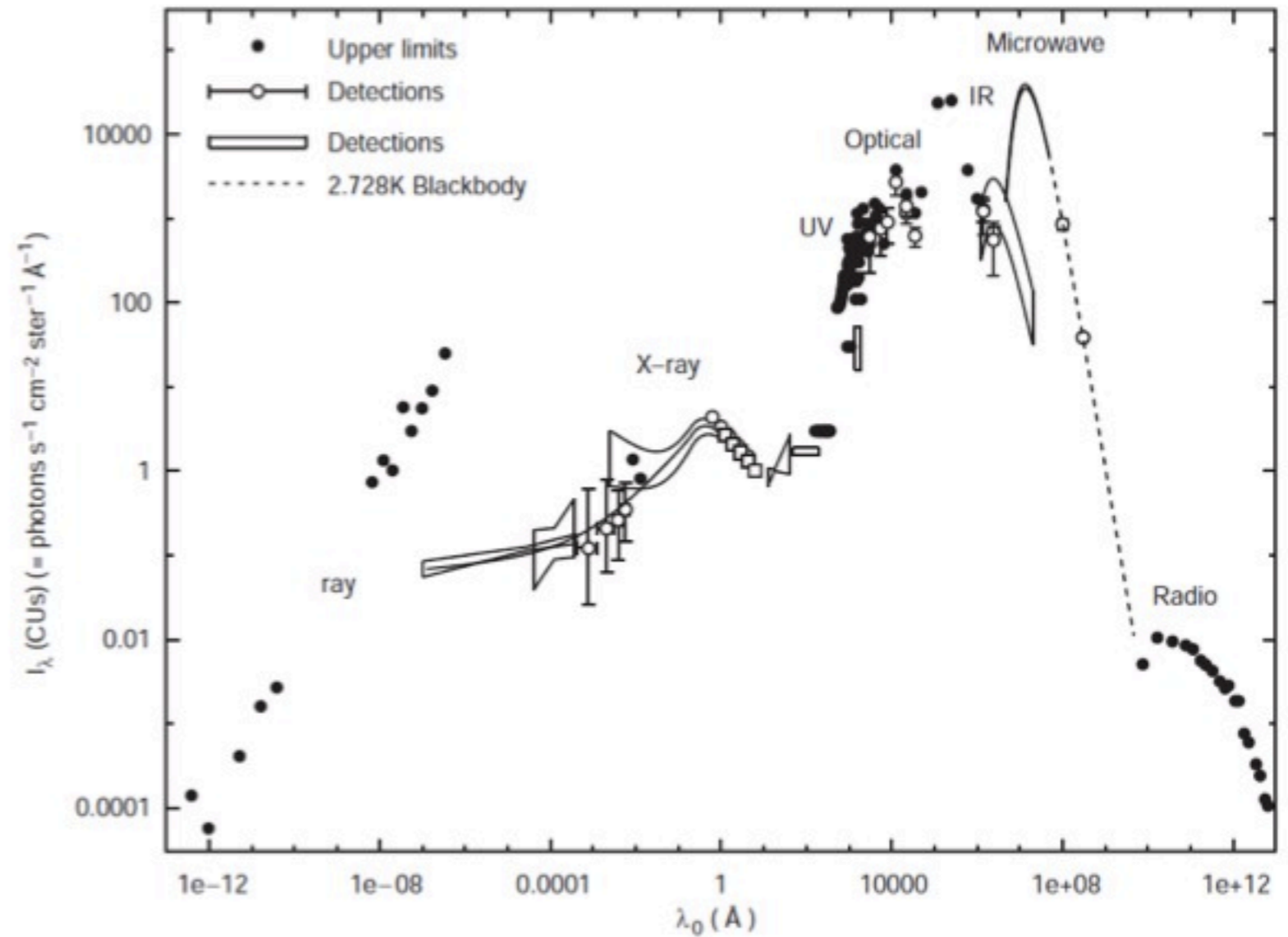
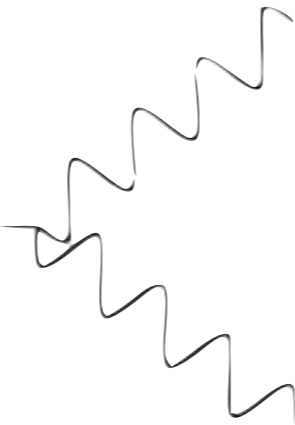
$$\Gamma = \frac{g^2 m_\phi^3}{64\pi}$$

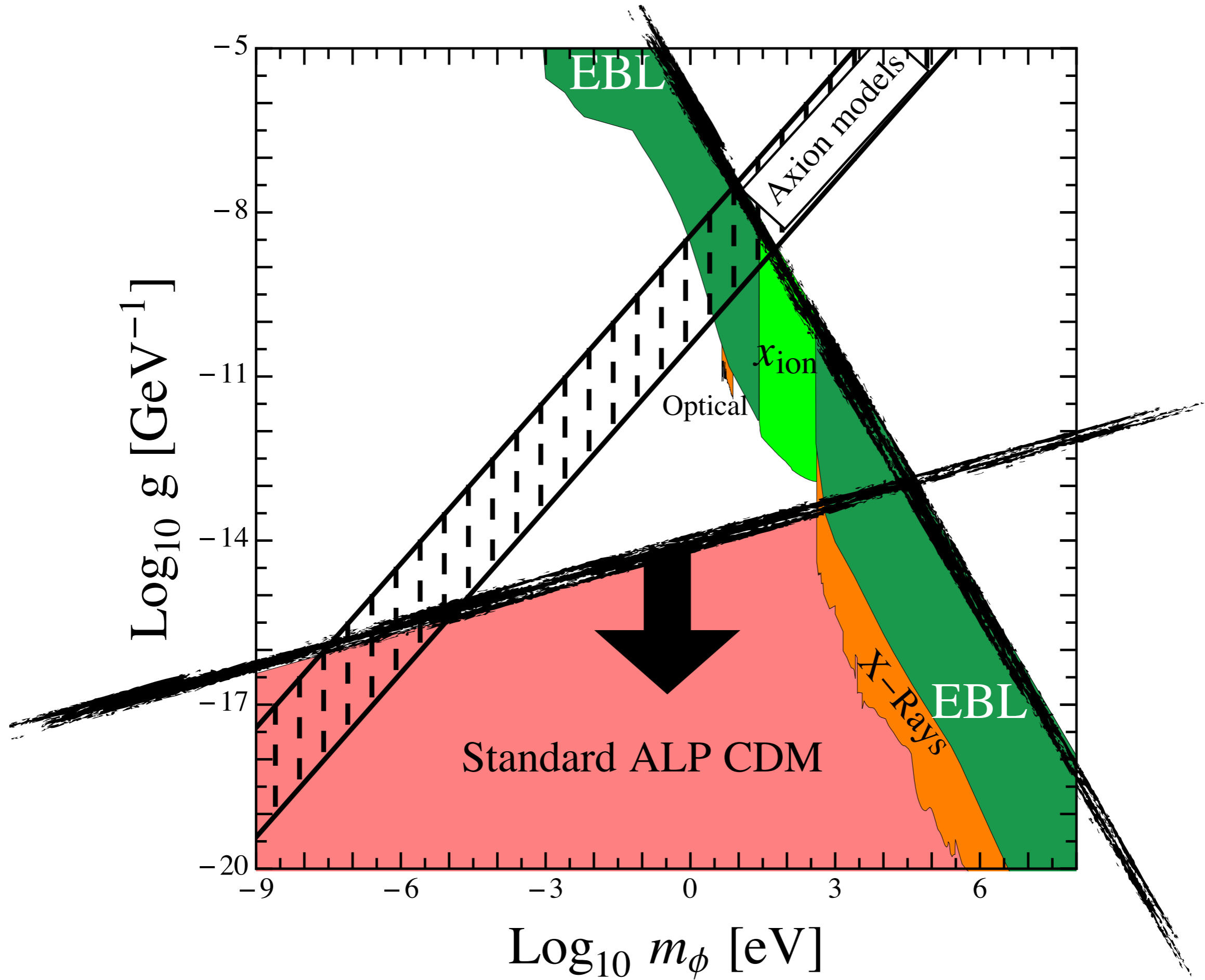




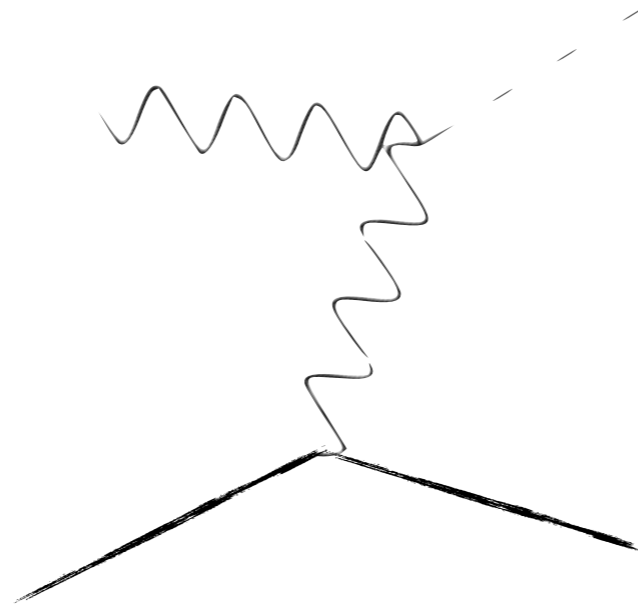
But ALPs decay and we don't see the photons...

$$\Gamma = \frac{g^2 m_\phi^3}{64\pi}$$

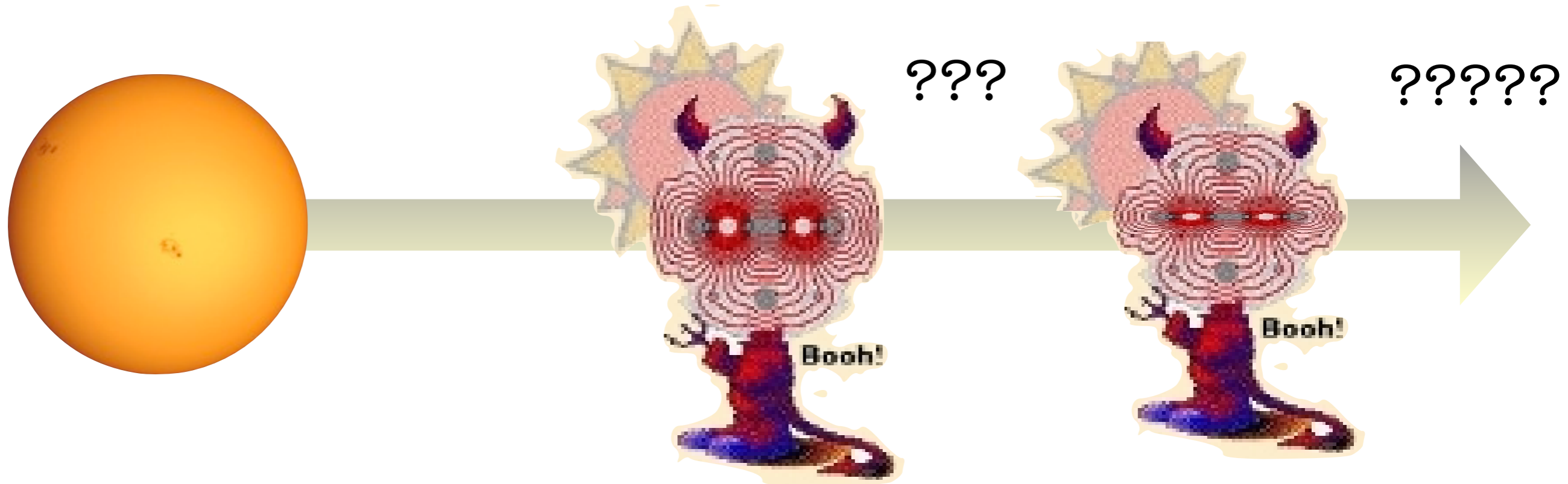


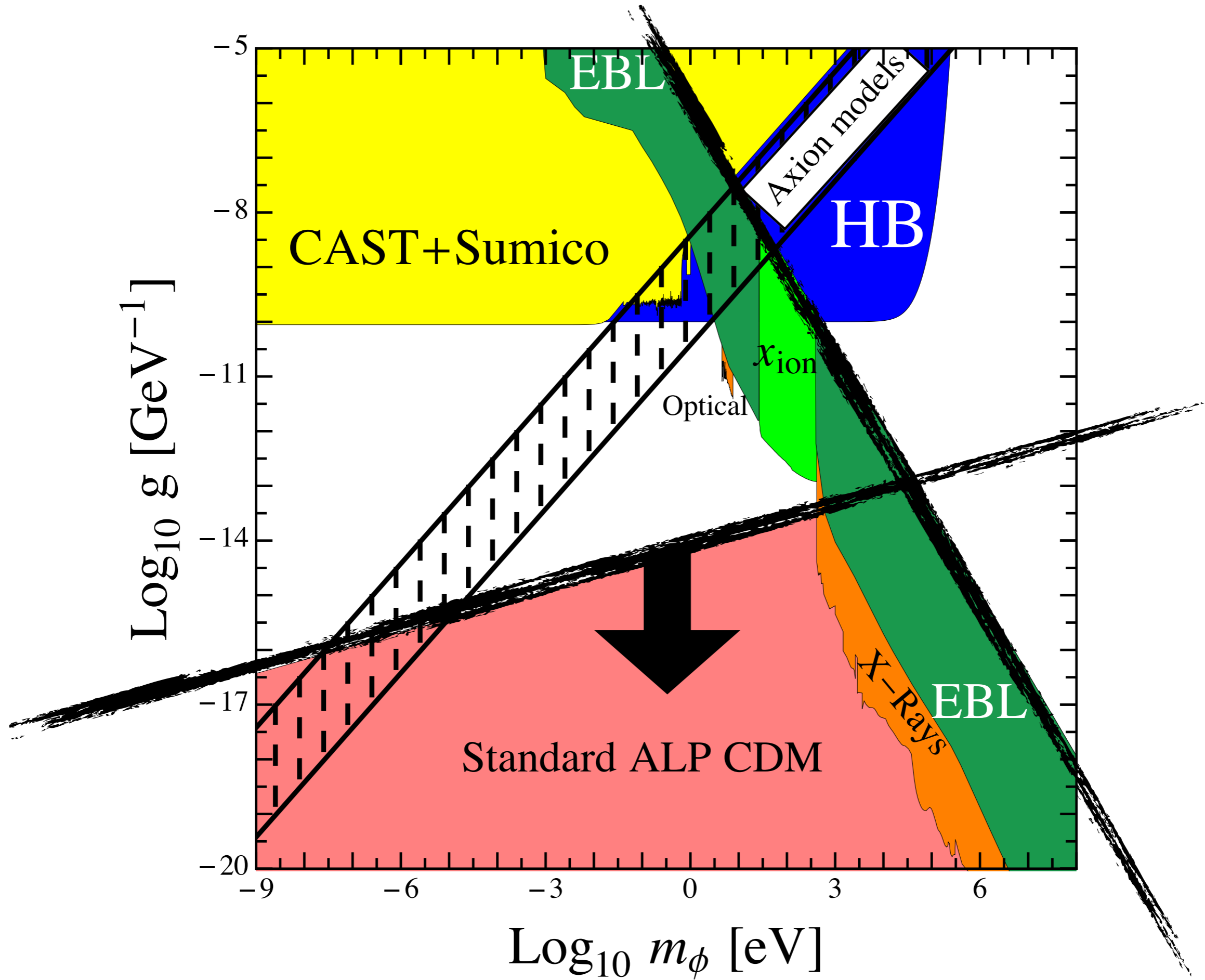


And they are radiated from stars

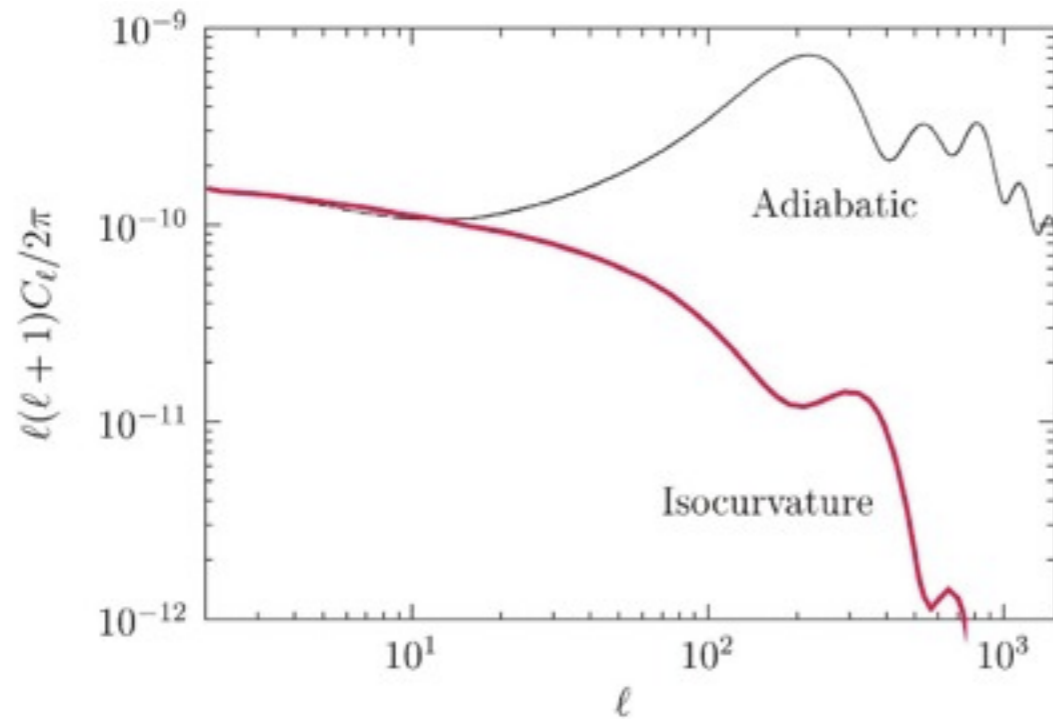


And CAST and SUMICO do not see them

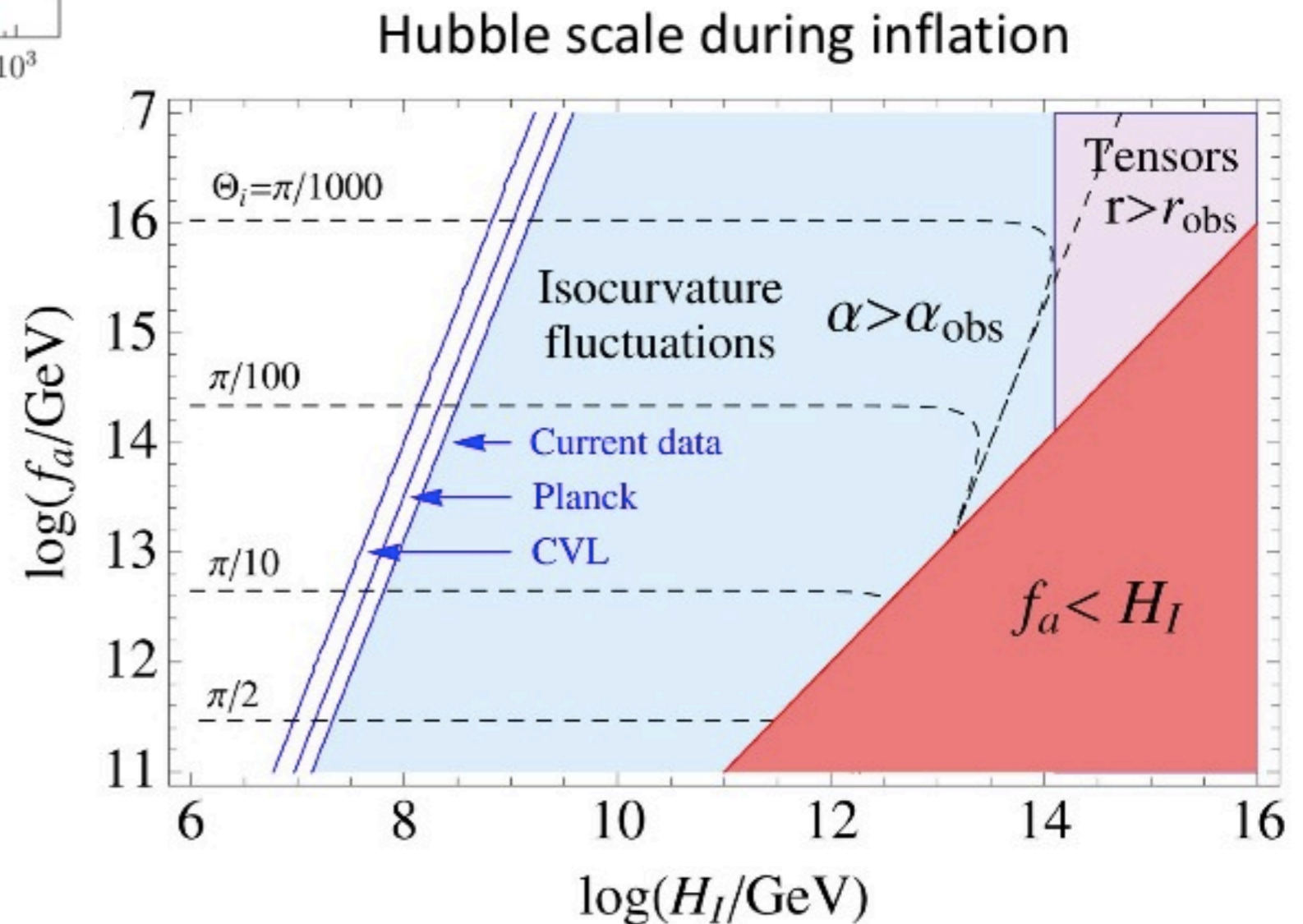




AND they imprint ISOCURVATURE perturbations



but this depends on H during inflation...

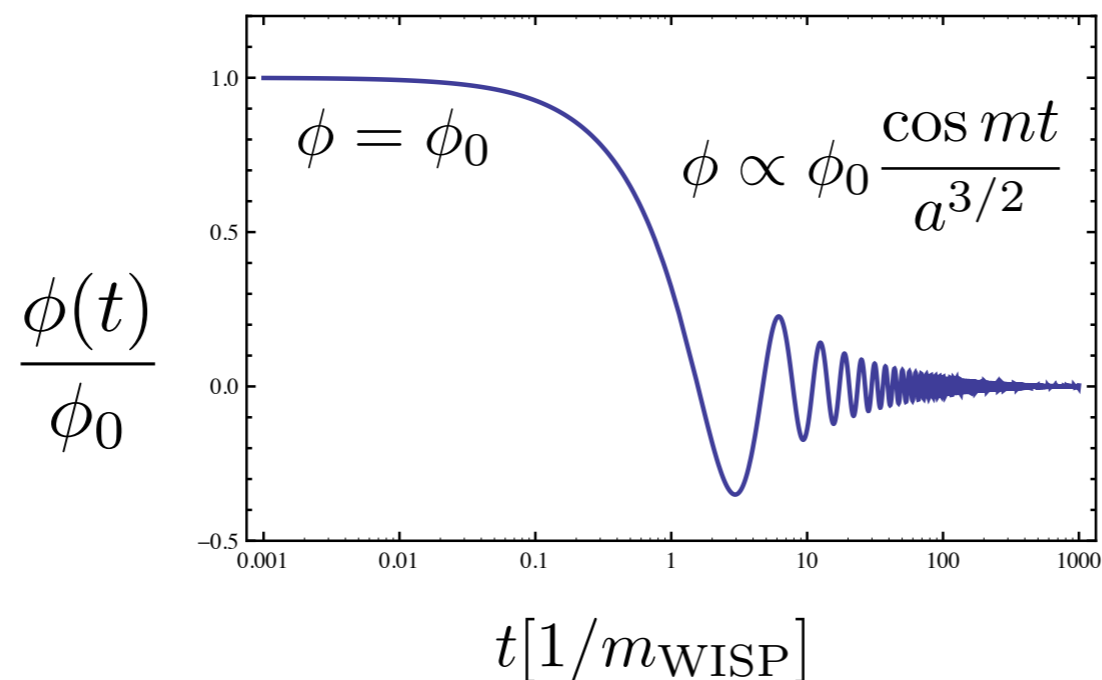


Standard ALP CDM not soooo promising for det.

Situation can change much if thermal mass

$$m = m(T)$$

Damping of the oscillations starts when $m_1 \sim 3H$

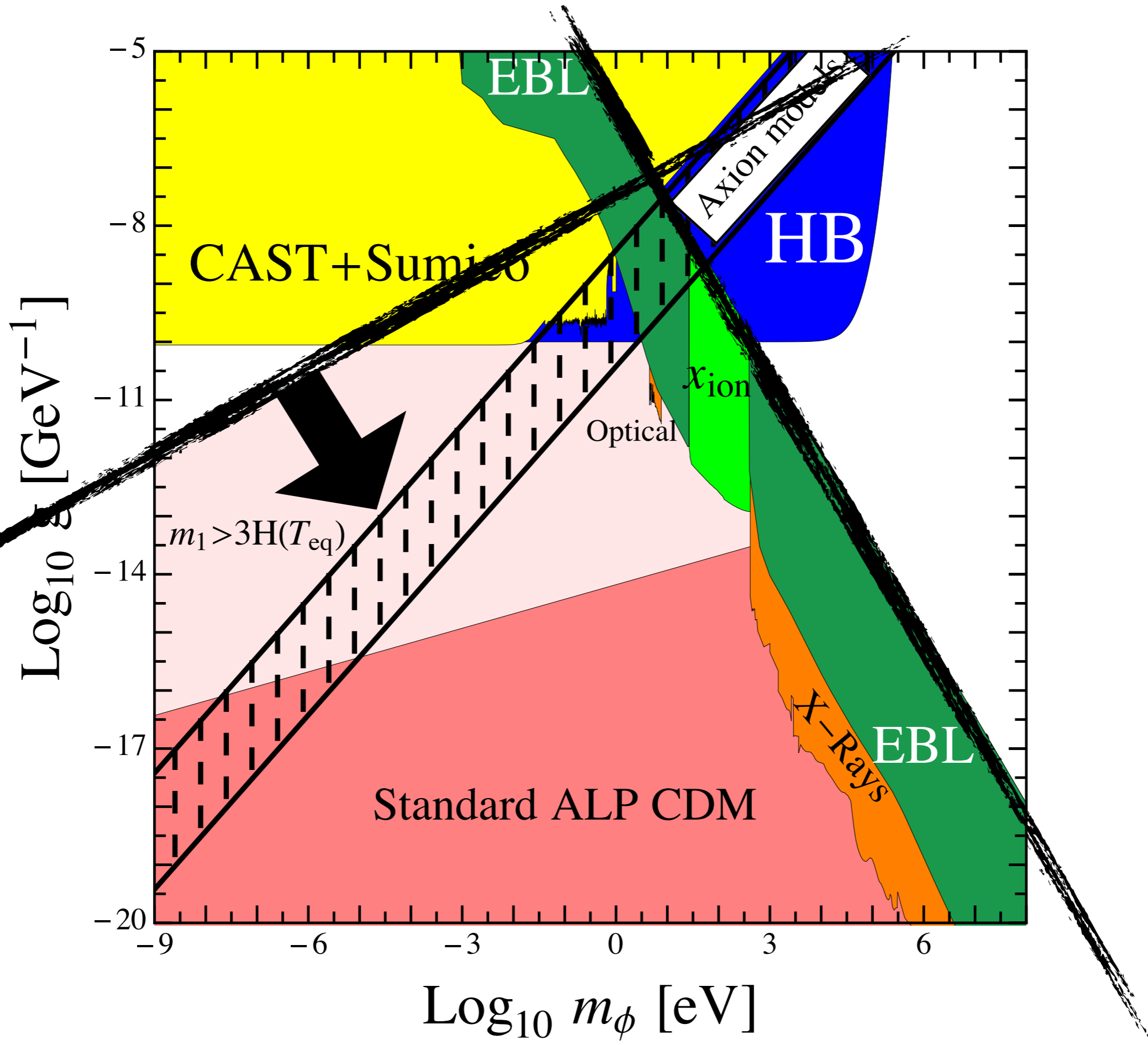


$$\rho_{\phi,0} \simeq 1.17 \frac{\text{keV}}{\text{cm}^3} \times \sqrt{\frac{m_0}{\text{eV}}} \sqrt{\frac{m_0}{m_1}} \left(\frac{\phi_0}{4.8 \times 10^{11} \text{ GeV}} \right)^2 \mathcal{F},$$

How small can be m_1 ??

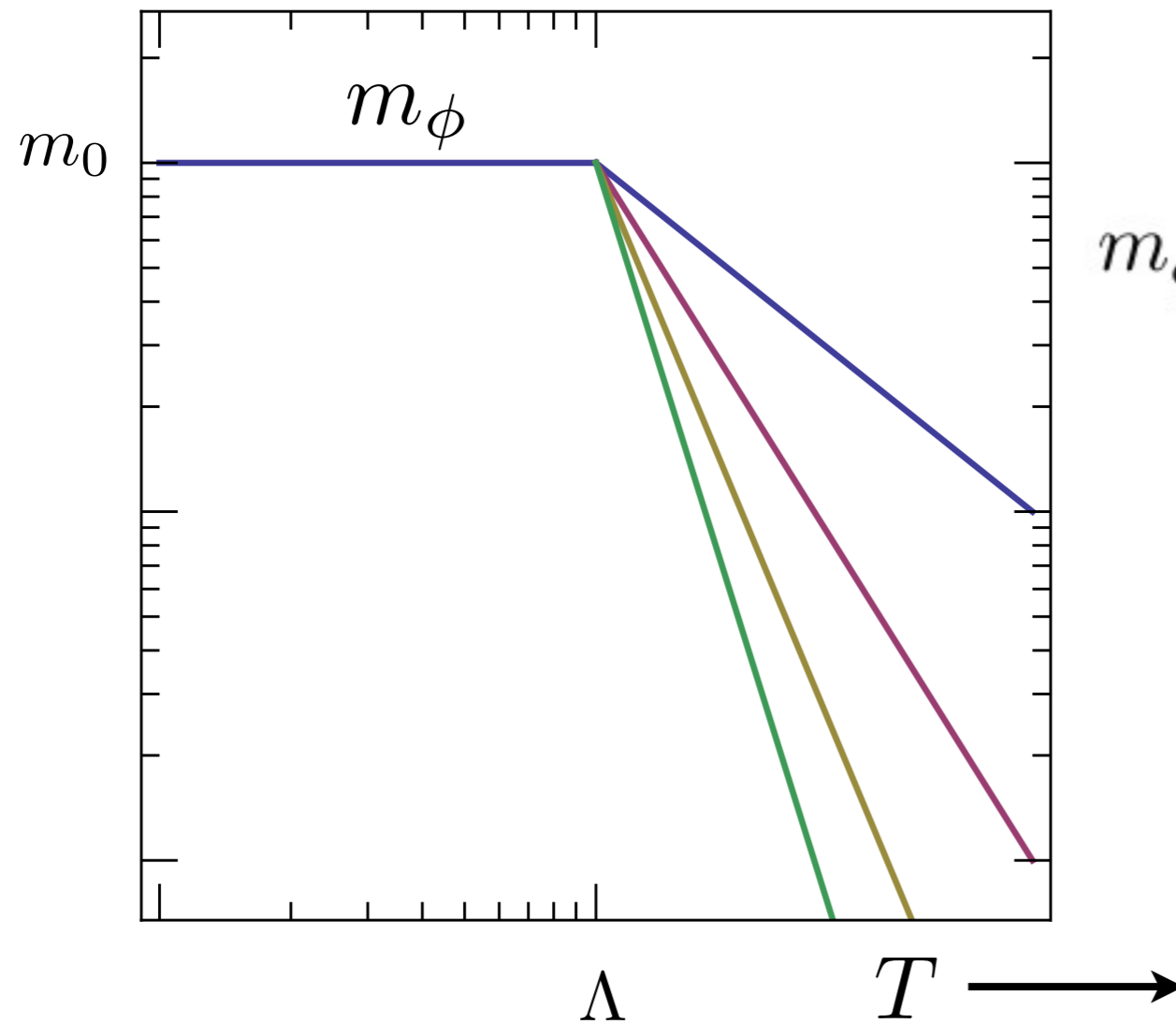
If we want the ALP to behave as CDM after standard Matter-Radiation equality $T_{\text{eq}} \sim 1.3 \text{ eV}$

$$m_0 > m_1 > 3H_{\text{eq}} = 1.8 \times 10^{-27} \text{ eV}$$

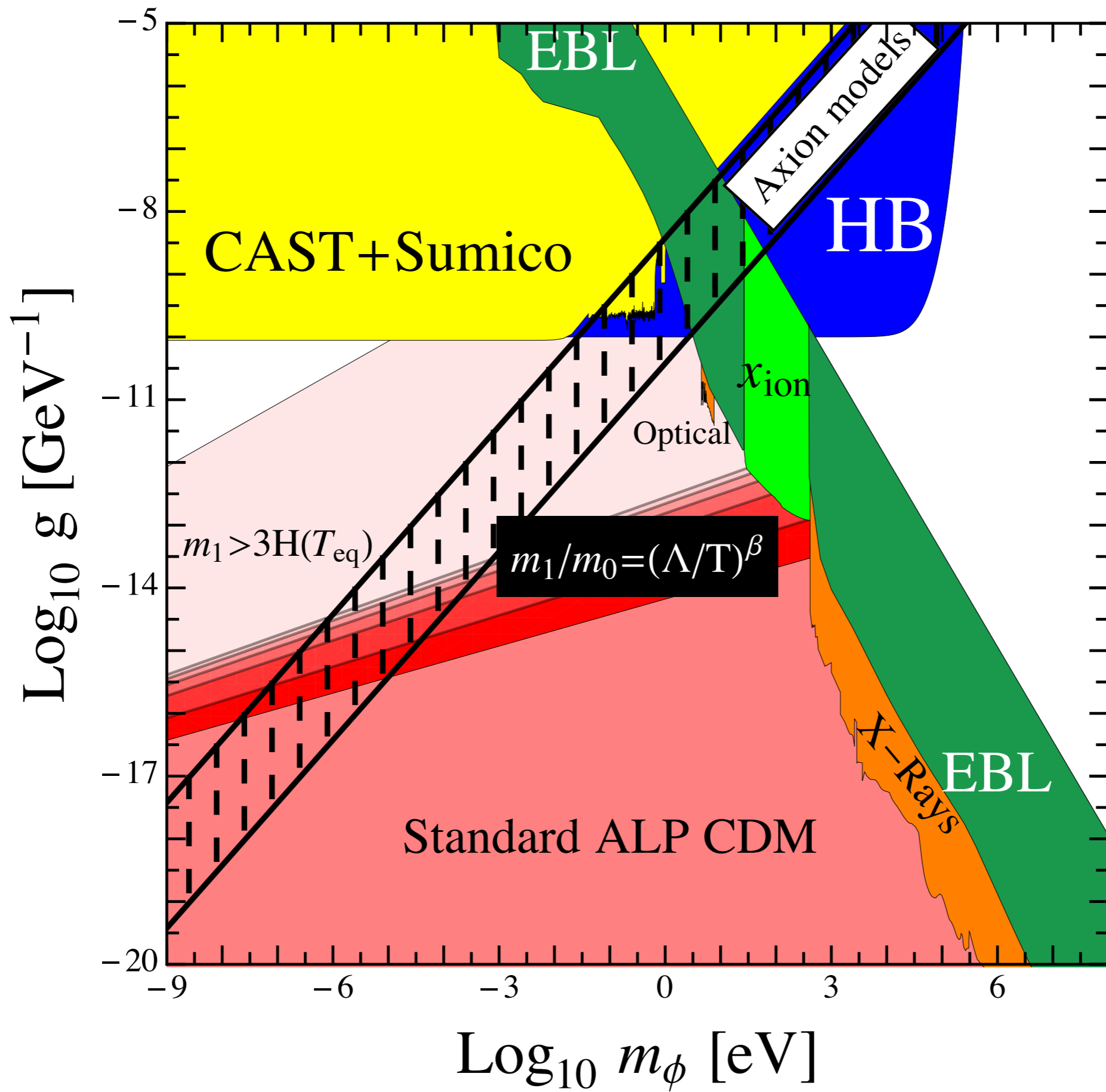


It is however kind of difficult to build such models

Instantonic-like potentials (like for the axion)

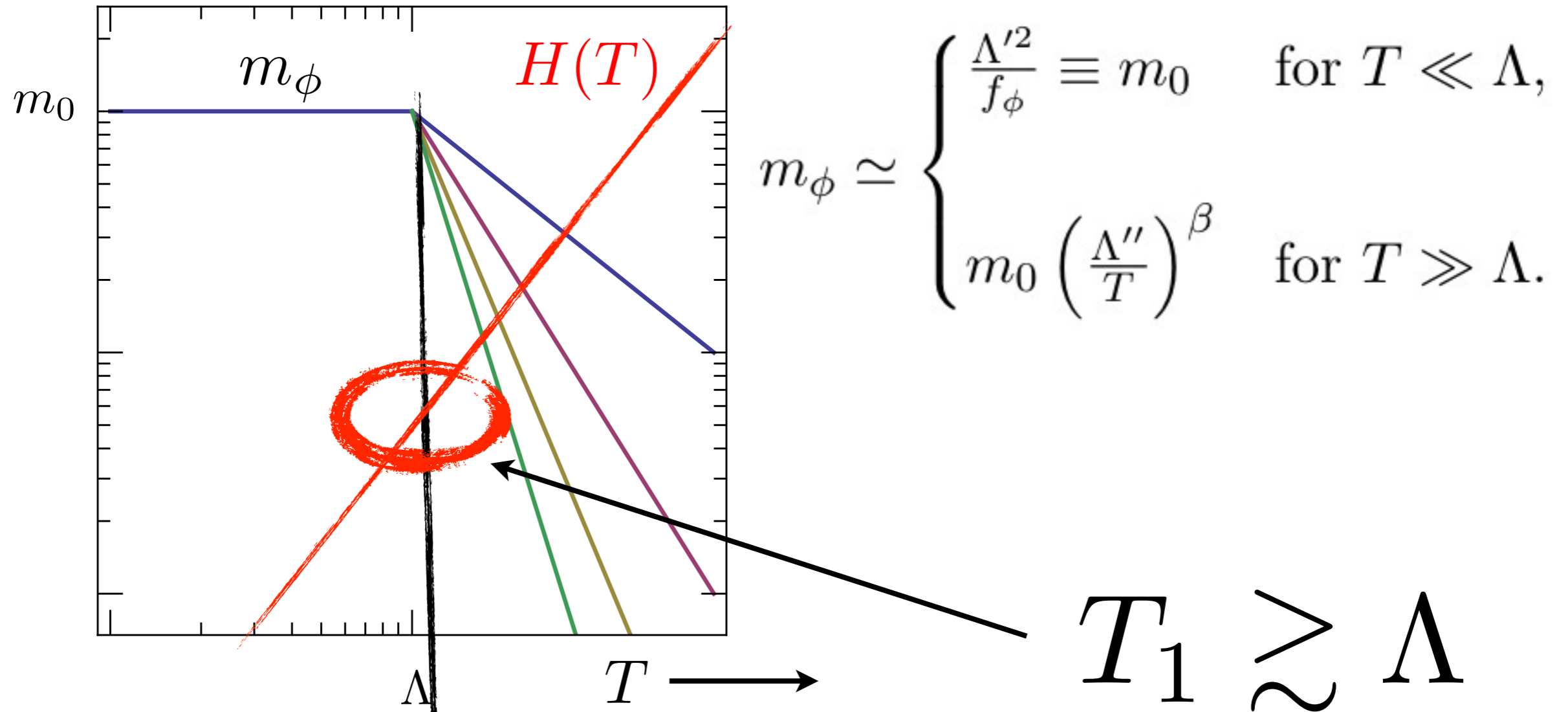


$$m_\phi \simeq \begin{cases} \frac{\Lambda'^2}{f_\phi} \equiv m_0 & \text{for } T \ll \Lambda, \\ m_0 \left(\frac{\Lambda''}{T} \right)^\beta & \text{for } T \gg \Lambda. \end{cases}$$

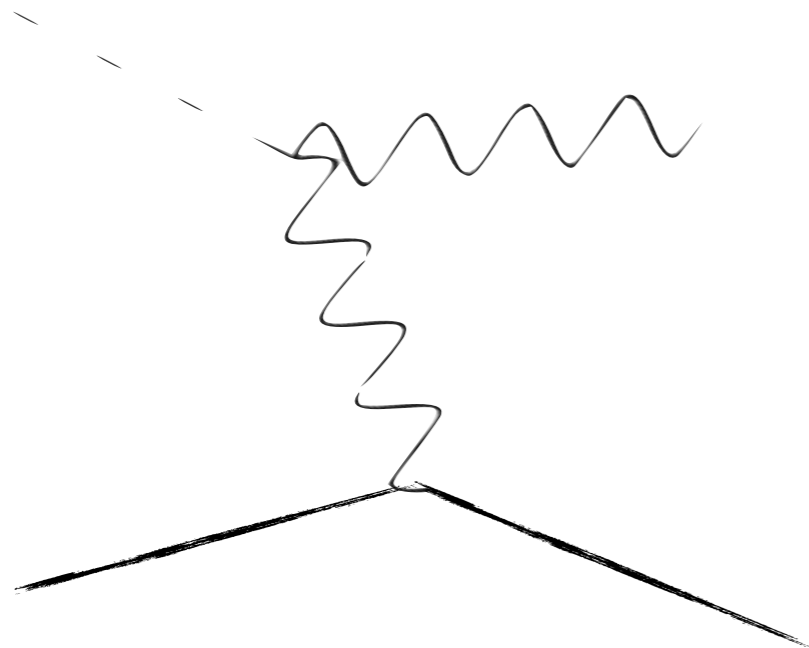


It is however kind of difficult to build such models

Instantonic-like potentials (like for the axion)



Thermalization of ALP CDM I



Primakoff process very effective at high T ...

$$\frac{\Gamma}{H} \propto g^2 m_{\text{Pl}} T$$

If ALP energy $E_a \sim T$

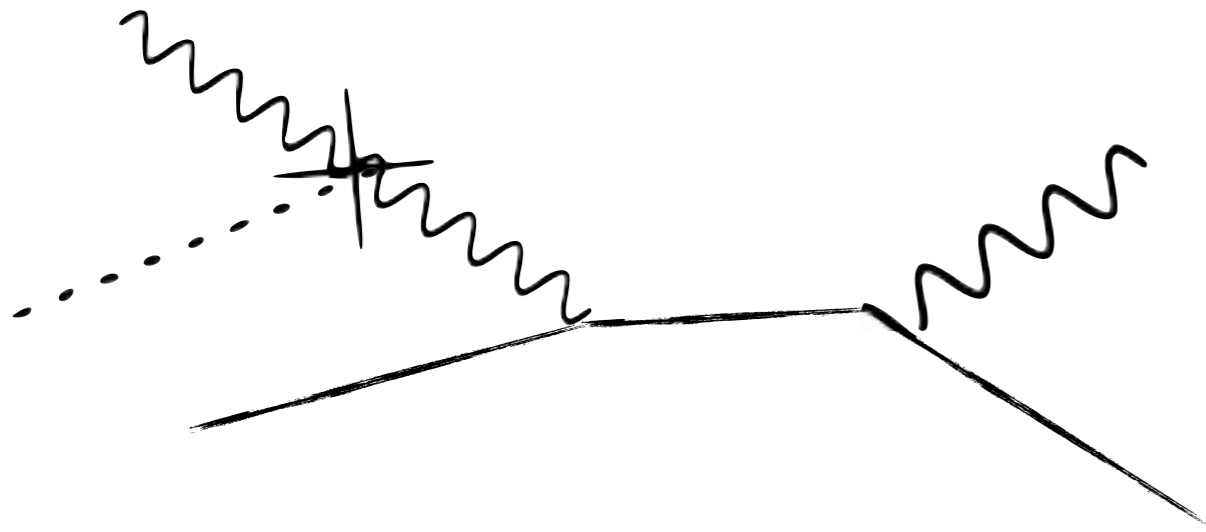
When ALP energies $E_a = m_a \ll T$
the COM energy is not sufficient to produce a plasmon!

$$s = m_e^2 + m_a^2 + 2E_e m_a > (m_e + m_\gamma)^2$$

$$E_e > \frac{2m_e m_\gamma + m_\gamma^2}{2m_a} \gg T$$

Exponentially suppressed!

Thermalization of ALP CDM II



Add other photon in the initial state ...

$$\begin{aligned}
 d\Gamma_{\phi C} &= \frac{1}{2m_\phi} \Gamma_C(\omega) |\mathcal{M}(\gamma\phi \rightarrow \gamma^*)|^2 \frac{1}{(2\omega m_\phi)^2 + (\omega\Gamma_C(\omega))^2} dn_\gamma(\omega) \\
 &= g^2 m_\phi \beta^2 \frac{\omega^2 \Gamma_C(\omega)}{(2\omega m_\phi)^2 + (\omega\Gamma_C(\omega))^2} dn_\gamma(\omega)
 \end{aligned}$$

$$\Gamma_{\phi C} \sim g^2 T^3 \frac{m_\phi}{\langle \Gamma_C \rangle} \quad \text{To still find a suppression} \quad \sim \frac{m_a}{T}$$

which makes it irrelevant in the region shown :-)

$$\phi F \tilde{F} \sim (\partial_\mu \phi) K^\mu = m_\phi K_0$$

Thermalization of ALP CDM III

Primordial Magnetic fields trigger $\phi \leftrightarrow \vec{E}$

And Electric fields are amazingly damped, due to the huge conductivity of the primordial plasma

$$\sigma \sim \frac{T}{\alpha}$$

However, the conductivity also enters into the mixing matrix... and highly suppresses mixing

Eff. mixing...
$$\frac{(2gB\omega)^2}{(m_\phi^2 - \omega_P^2)^2 + (\omega\sigma)^2}$$

Thermalization of ALP CDM III

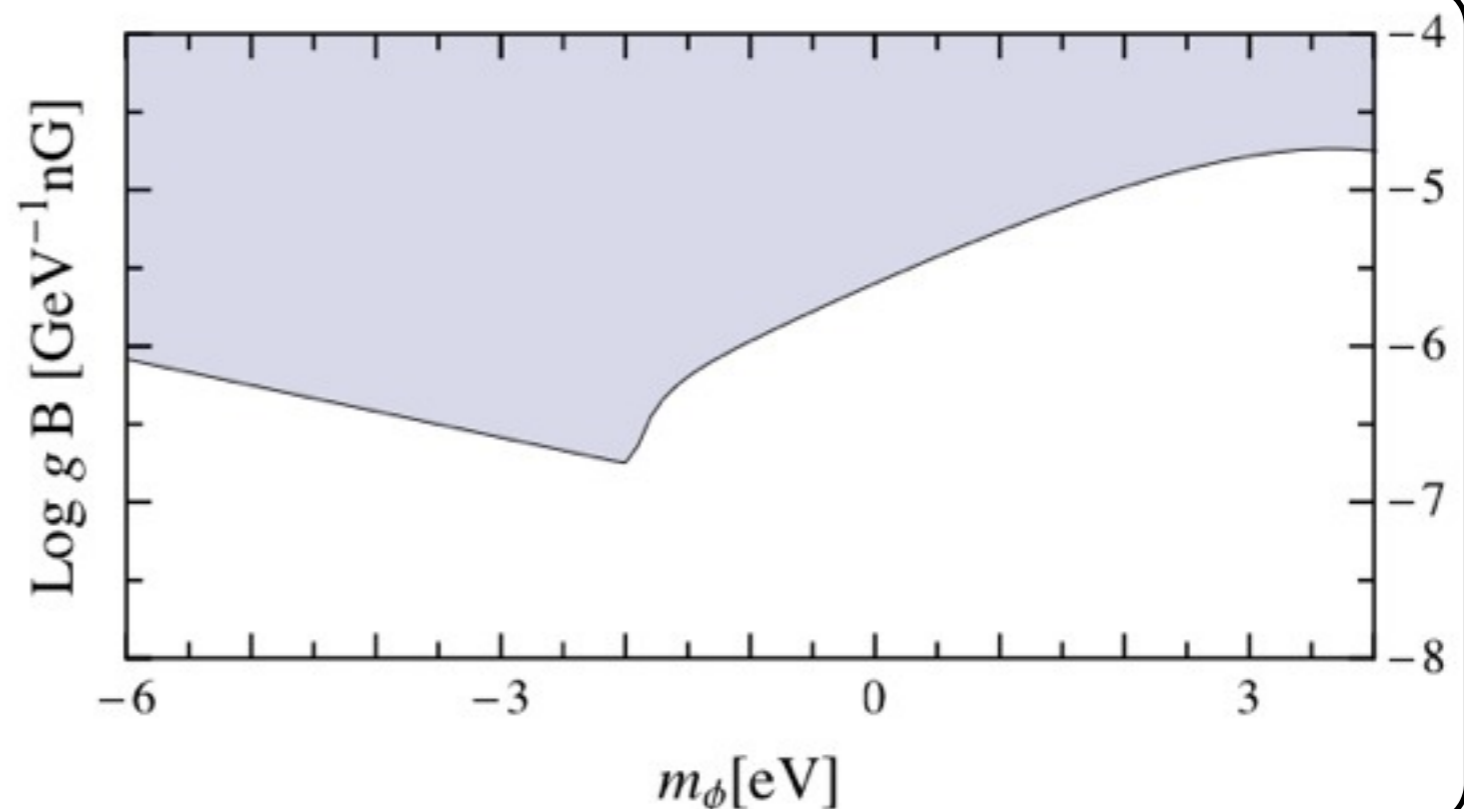
Primordial Magnetic fields trigger $\phi \leftrightarrow \vec{E}$

but very big fields (or very primordial) required

high T constraint
(if $B \propto T^2$)

$$\left(\frac{g}{10^{-10} \text{ GeV}^{-1}} \right)^2 \left(\frac{B_0}{3 \text{ nG}} \right)^2 \frac{T_B}{10^9 \text{ GeV}} \lesssim 1$$

res. oscillations



And what if $T_R > f_\phi$??

Different causally connected regions diff.

$$\phi_0 \in (-\pi f_\phi, \pi f_\phi)$$

As long as $m_\phi \ll H(T_R)$ the ALP does not know where its minimum is ... (we don't need $m_\phi(T_R) = 0$)

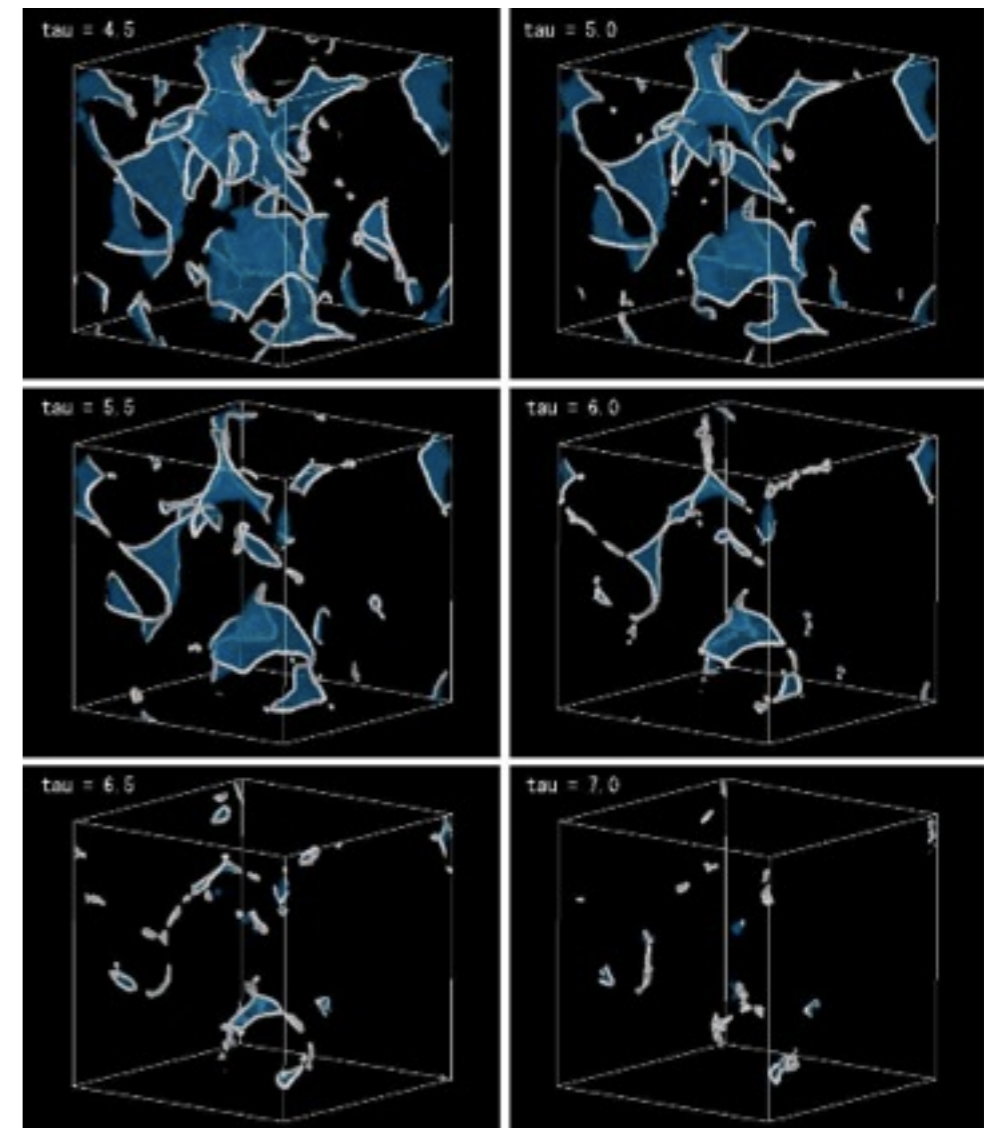
Leads to **Cosmic Strings**

(decay into ALP DM)

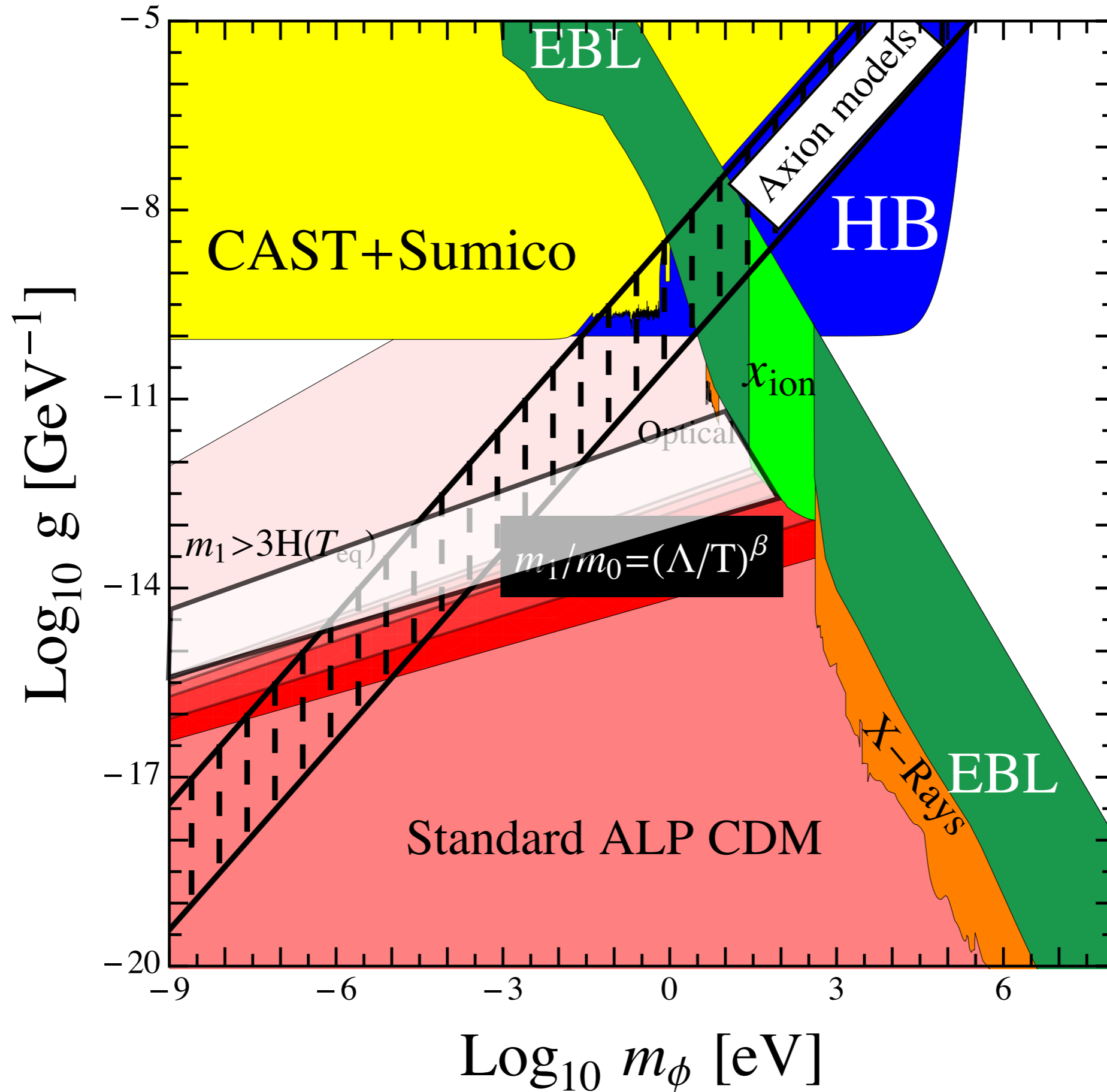
and plausibly **Domain Walls!**

decay if SYM is exp. Broken
(remind about axions...)

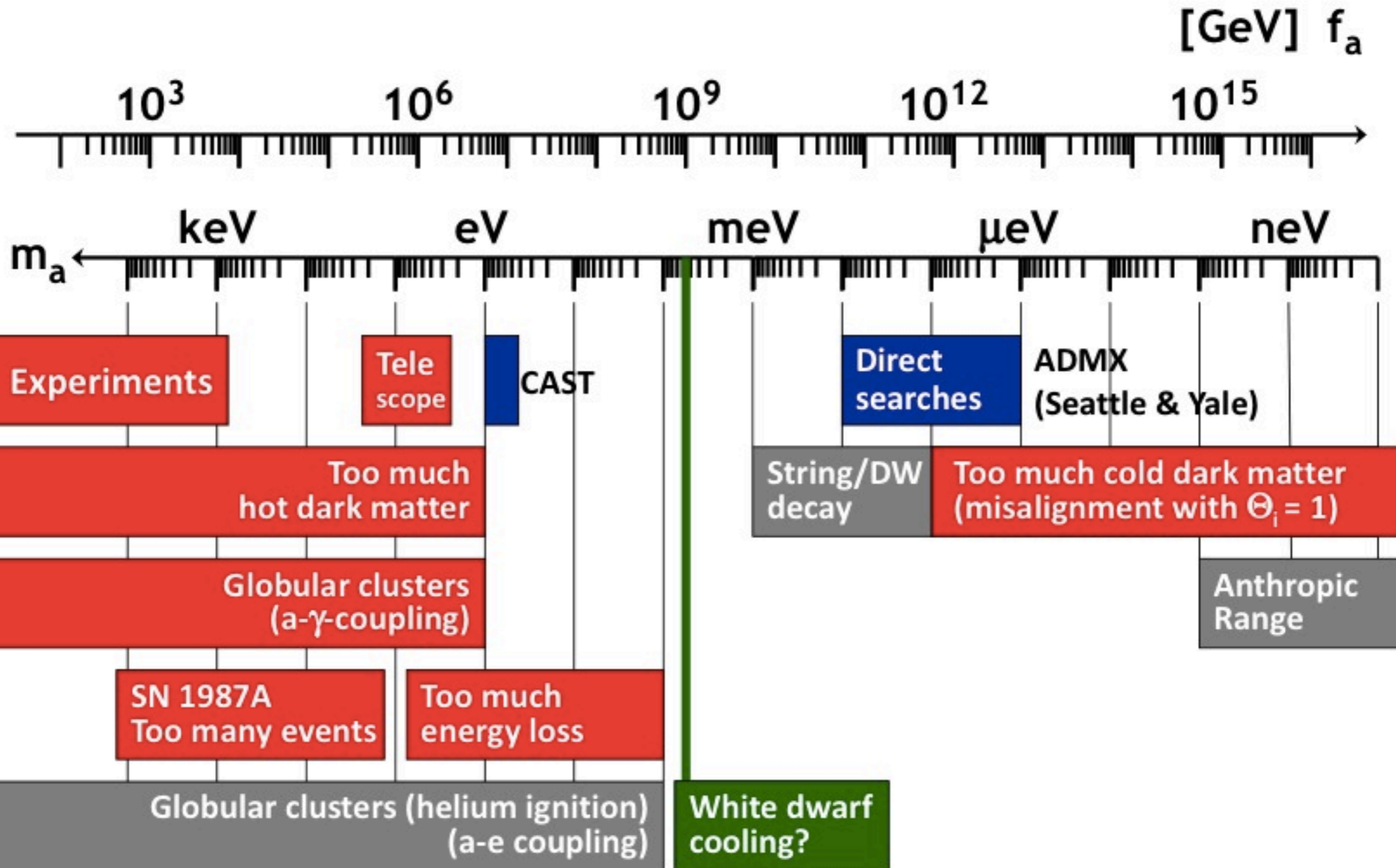
dominant contribution to DM?



Smaller f_ϕ are preferred \rightarrow stronger couplings

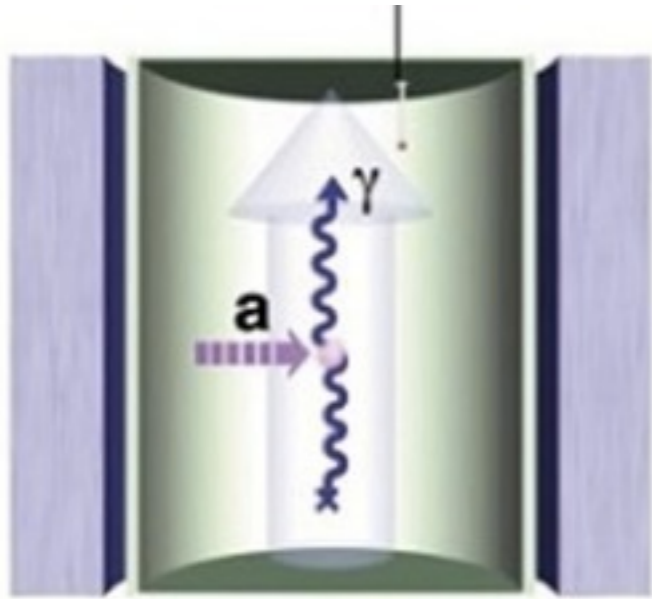


Axion Bounds and Searches



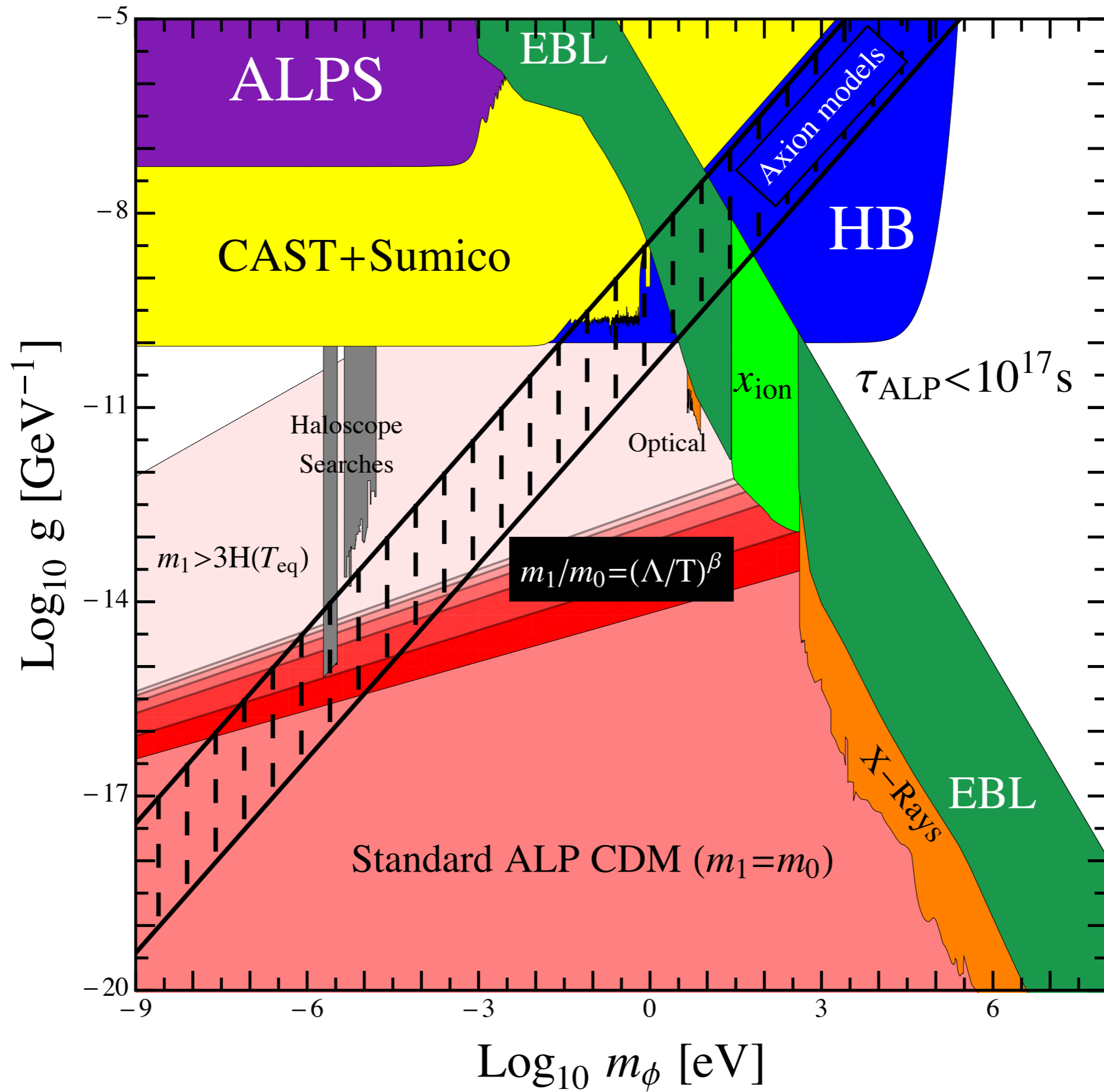
Cavity experiments

(are sensible in a wider range than previously expected)



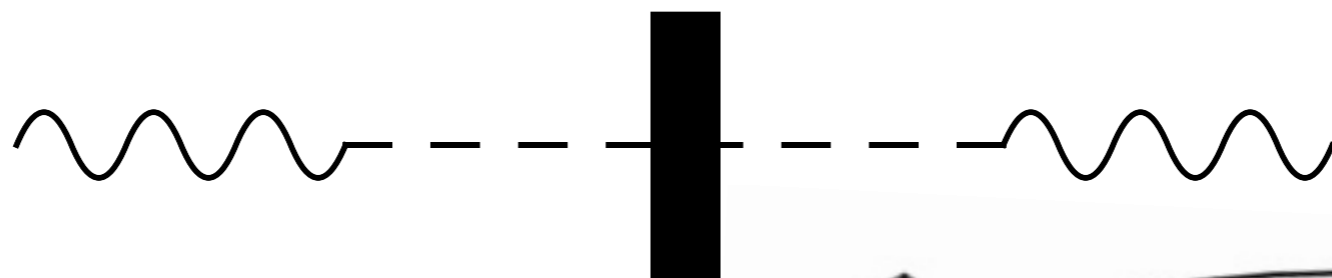
- ADMX, ADMX-II, and HF (Yale)
- Proposed at DESY, CERN
- IAXO
- UWA

They seem too few for such a
wealth of possibilities !!!!!!!!!!!!!

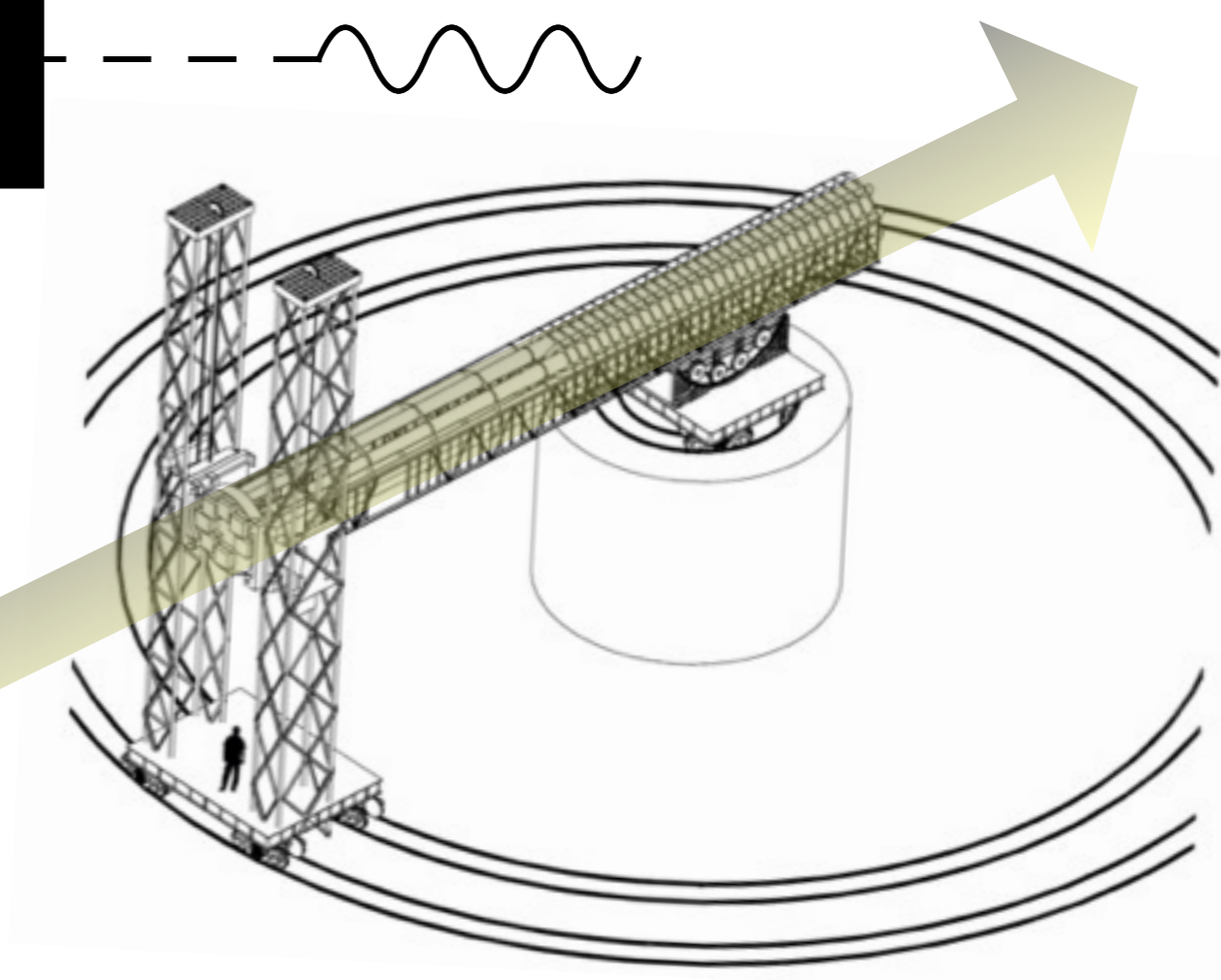
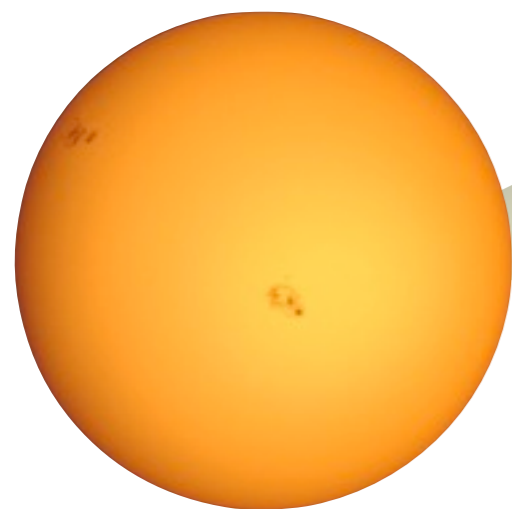


Other experiments are sensible to WISPy ALP DM

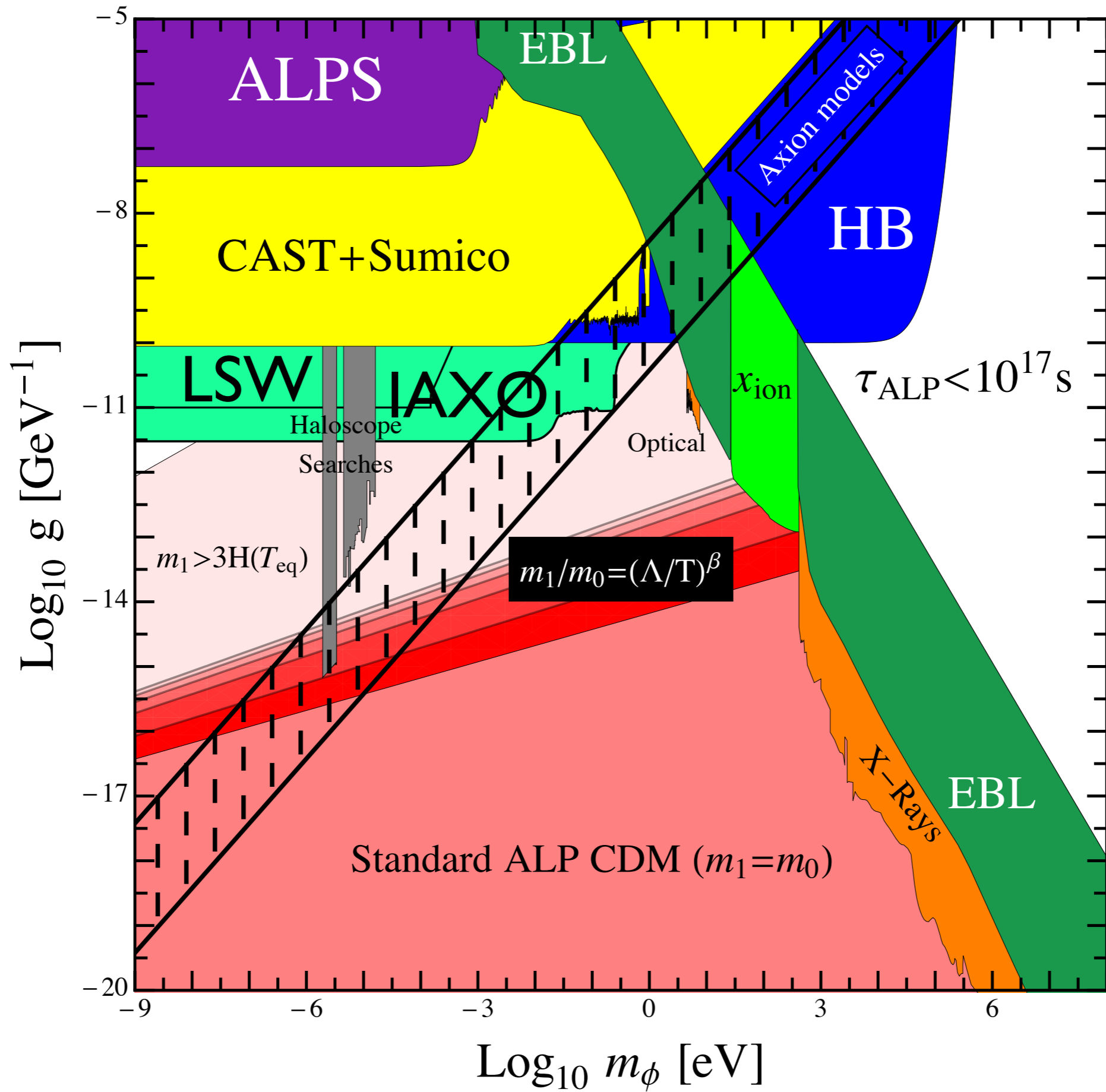
- Light Shinning through walls (REAPR, ALPS II)



- IAXO



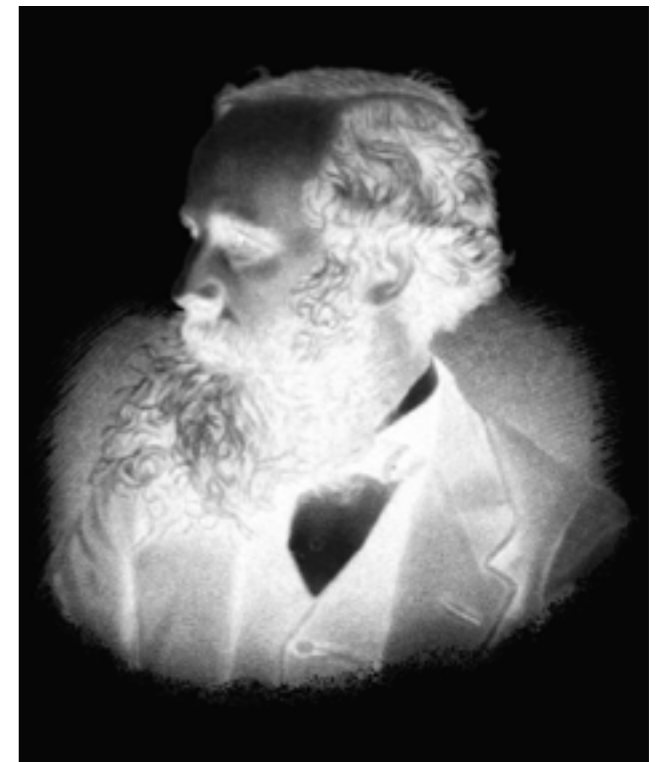
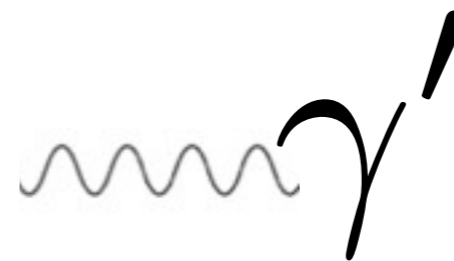
- 5th forces ? (still don't know...)



Local U(1)'s: Hidden Photons & kinetic mixing

Extra U(1) symmetries are ubiquitous BSM (for instance in String Theory)

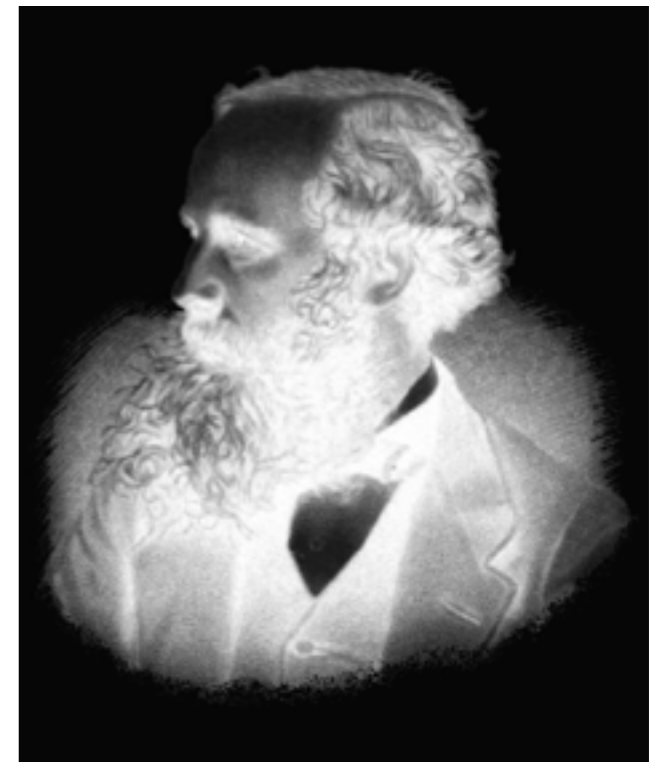
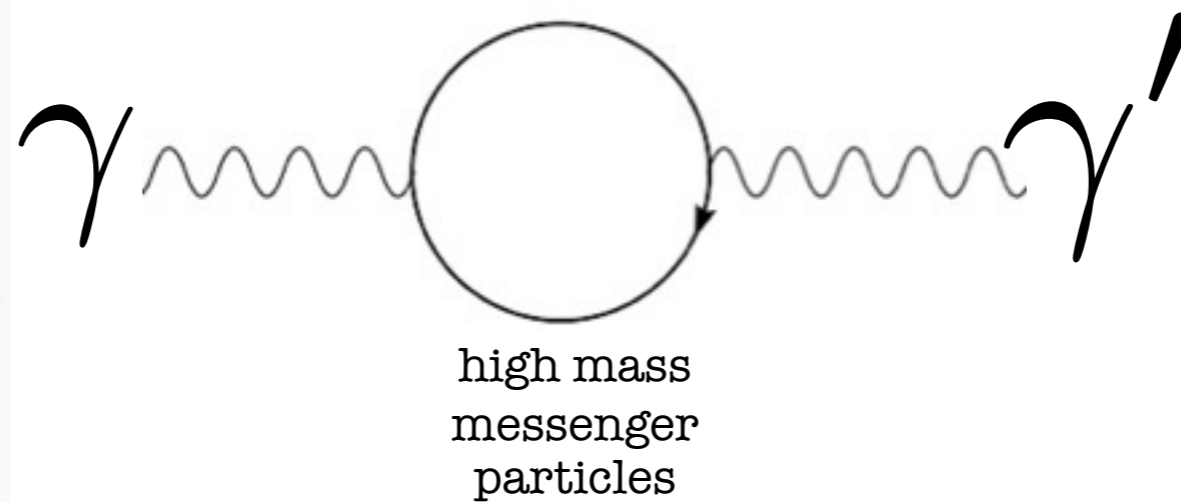
If the corresponding Hidden photon does not couple to SM particles ->
HIDDEN PHOTON



Local U(1)'s: Hidden Photons & kinetic mixing

Extra U(1) symmetries are ubiquitous BSM (for instance in String Theory)

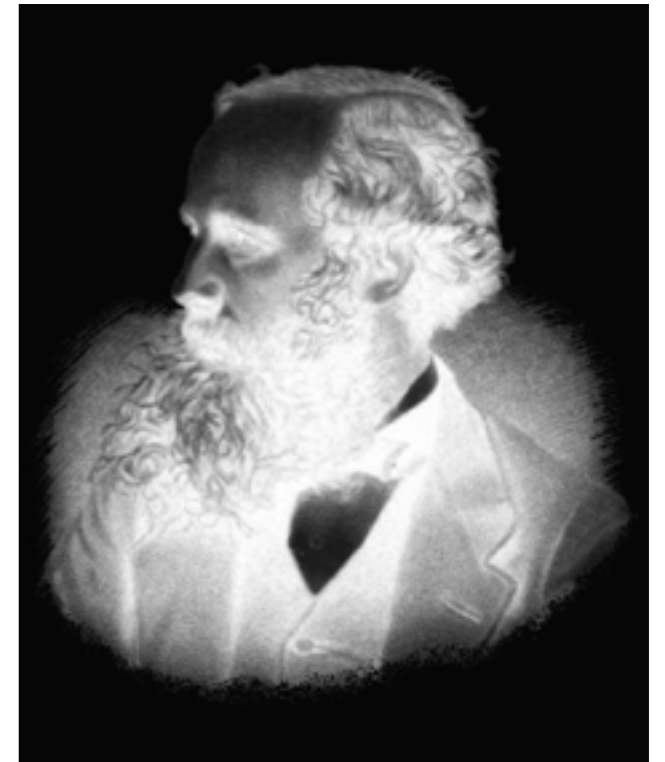
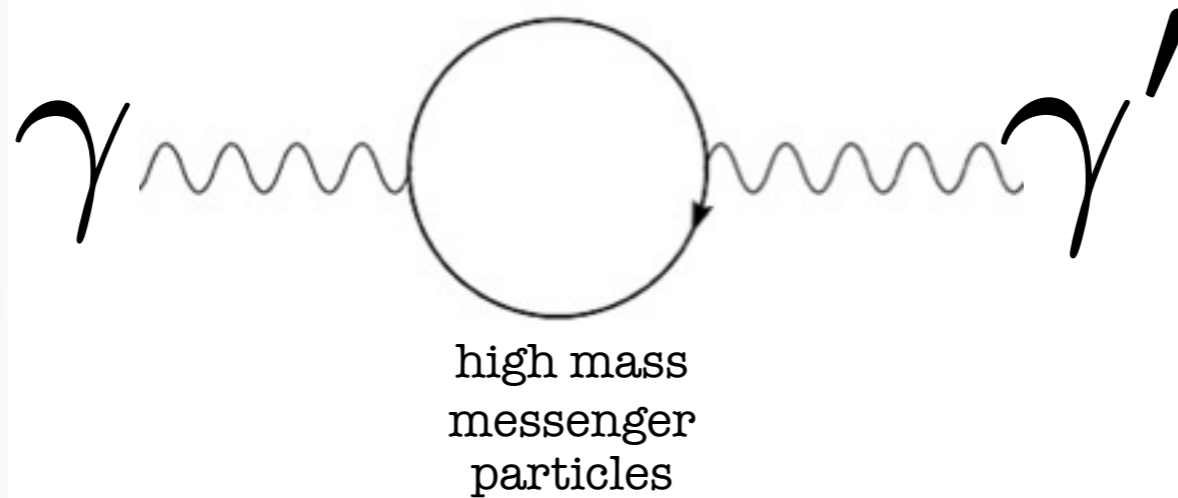
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Local U(1)'s: Hidden Photons & kinetic mixing

Extra U(1) symmetries are ubiquitous BSM (for instance in String Theory)

If the corresponding Hidden photon does not couple to SM particles ->
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Kinetic mixing is the most relevant interaction at low energies

$$\mathcal{L}_I = -\frac{1}{2}\chi F_{\mu\nu} B^{\mu\nu}$$

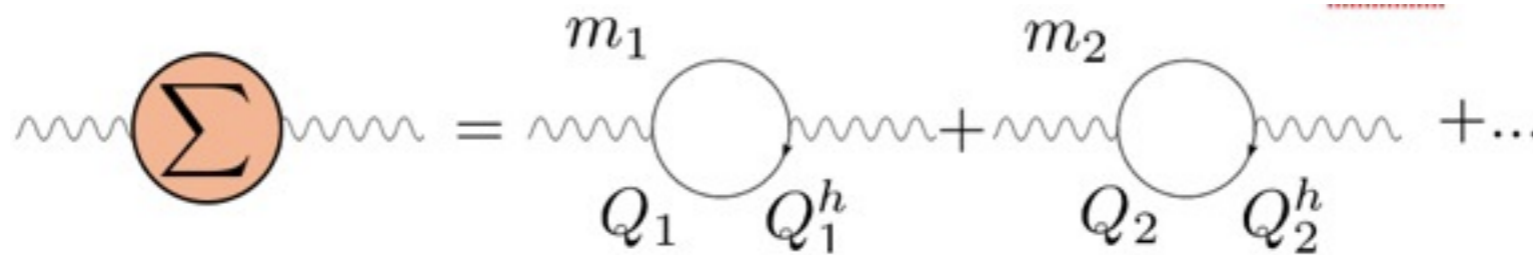
Size of kinetic mixing

Natural size: radiative correction

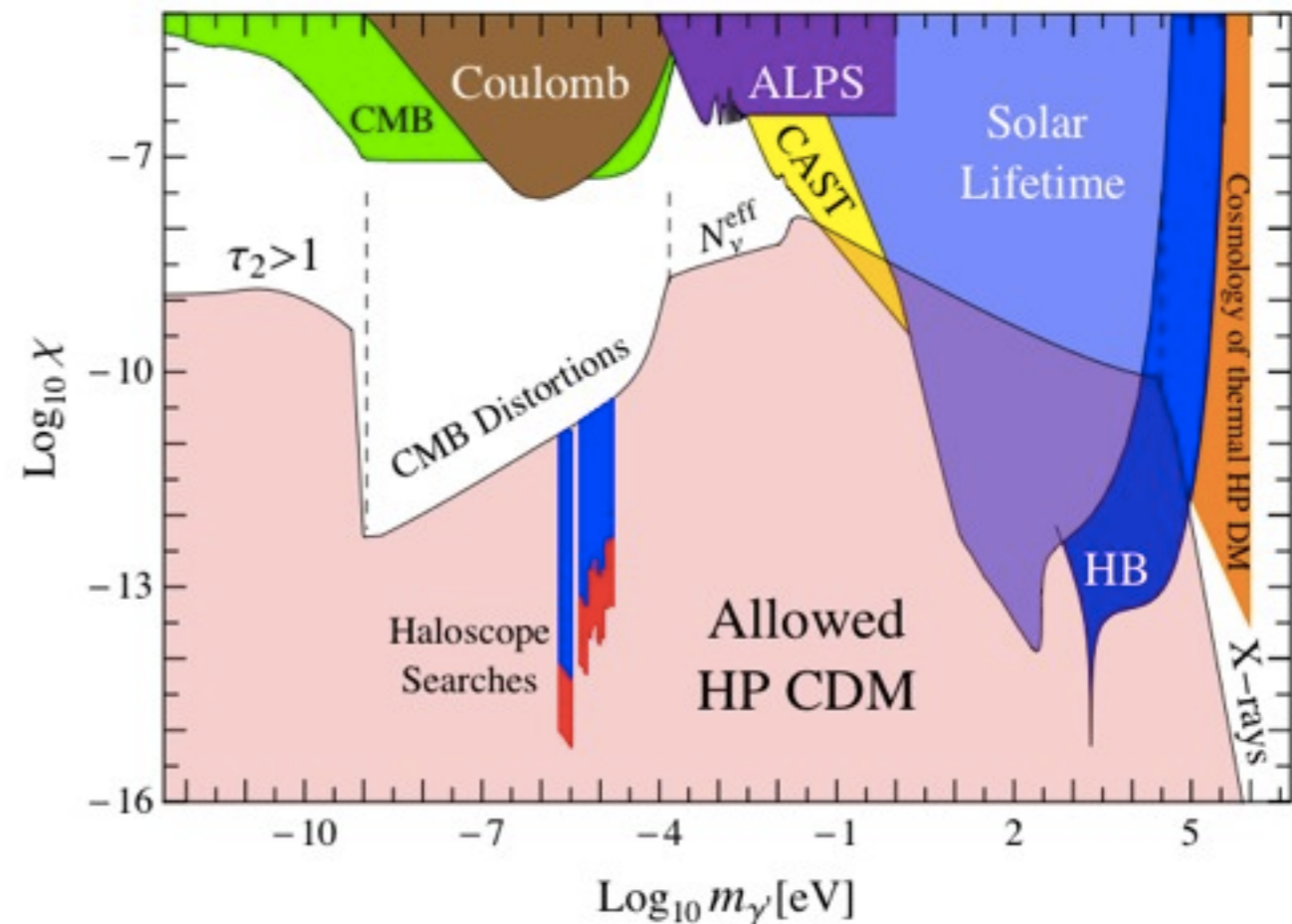
$$\chi \sim \frac{egh}{16\pi^2} \log \frac{m}{\mu} \sim 10^{-3}$$

But can be much smaller !!!!
if hyperweak hidden gauge coupling
or cancelations between contributions

natural value
not soooo small!

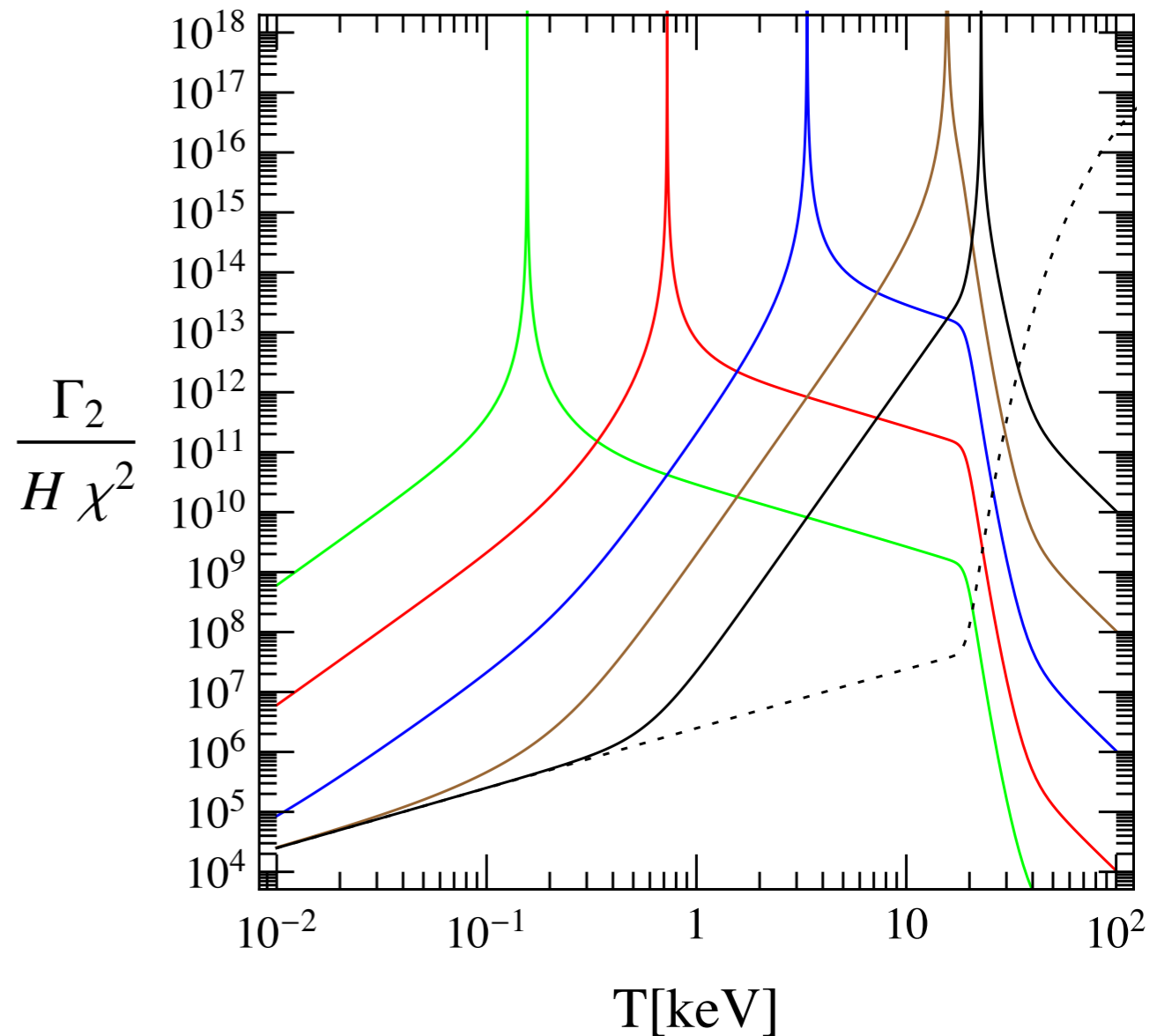


Again a huge parameter space to explore, even in the minimal case!



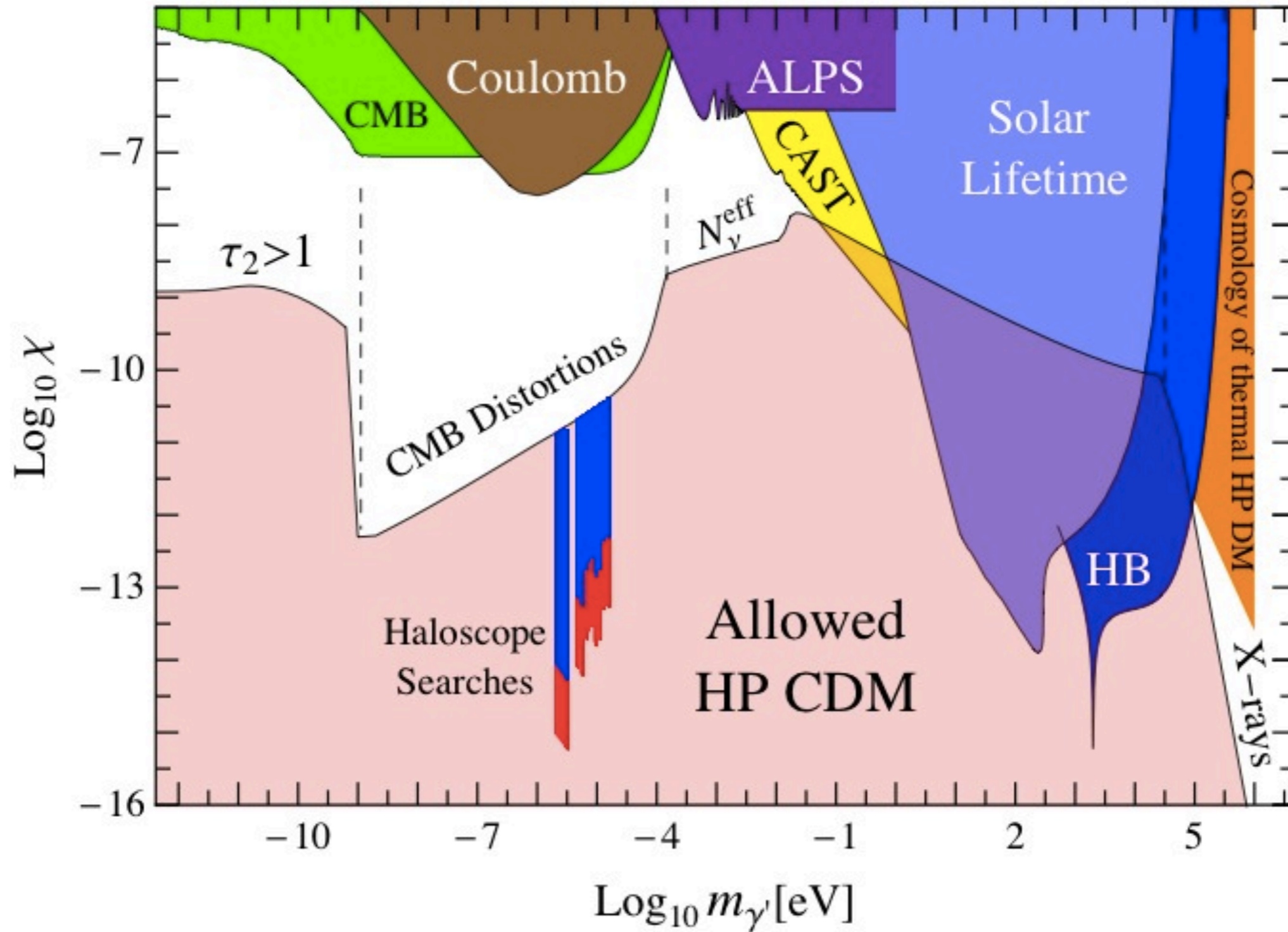
Crucial Differences

- The initial value of amplitude is not bounded!
- No phase transitions (no CSs, DWs ... well...)
- HPs mix directly with Photons (no need for B) (resonance transitions can evaporate HP CDM)
- Small E field in the universe
- ADMX-like exps. do not need B field



WISPy Dark matter: Example II (Hidden Photon)

Nelson & Scholtz, Arias et al.



Conclusions

- Extensions of the SM might well accommodate WISPs

The Strong CP problem cries for an axion

- Cosmology cries for WISPs!

Dark Matter, (Dark Radiation, Dark Energy)

- Astrophysics shouts WISP loud!

White dwarfs, Universe transparency

- WISPs can be searched experimentally

New Axion/ALP/HP cold dark matter experiments !!!

Next generation experiments (ALPS II, IAXO)