Nano-eV Axions Beyond the Horizon



"Axion cosmology beyond the horizon" DBK, A.E. Nelson, arXiv:0809.1206 (2008)

1982: Abbott, Sikivie; Dine, Fischler; Preskill, Wilczek, Wise

1982: Abbott, Sikivie; Dine, Fischler; Preskill, Wilczek, Wise

 $for temperature T \gg 1 {
m GeV}$ the axion potential is flat



 a/f_a is an angle

1982: Abbott, Sikivie; Dine, Fischler; Preskill, Wilczek, Wise

 $for temperature T \gg 1 \text{ GeV}$ the axion potential is flat

The temperature $T \sim 1 \ {
m GeV}$ the axion potential starts to appear and the axion mass grows.



 a/f_a is an <u>angle</u>

1982: Abbott, Sikivie; Dine, Fischler; Preskill, Wilczek, Wise

 $for temperature T \gg 1 {
m GeV}$ the axion potential is flat

At temperature $T \sim 1 \text{ GeV}$ the axion potential starts to appear and the axion mass grows.

When the axion Compton wavelength crosses the horizon, axion field begins to oscillate, = Bose condensate of noninteracting particles = CDM

$$m_a(t_{\rm osc}) = H(t_{\rm osc})$$

 a/f_a is an angle

 $\theta = 0$

1982: Abbott, Sikivie; Dine, Fischler; Preskill, Wilczek, Wise

For temperature $T \gg 1 \text{ GeV}$ the axion potential is flat

At temperature $T \sim 1 \; {
m GeV}$ the axion potential starts to appear and the axion mass grows.

When the axion Compton wavelength crosses the horizon, axion field begins to oscillate, = Bose condensate of noninteracting particles = CDM

$$m_a(t_{\rm osc}) = H(t_{\rm osc})$$

 $\theta = 0^{\pi}$

😭 Axions can eventually dominate the universe $\rho_{\rm CDM} \propto R^{-3}, \quad \rho_{\rm rad} \propto R^{-4}$ a/f_a is an angle

How does the axion dark matter depend on f_a ?



Axion dark matter today:

$$\rho_a(t_0) \simeq \rho_{\rm dm} \theta_i^2 \left(\frac{f_a}{{\rm few} \times 10^{11} {\rm ~GeV}} \right)$$

observed dark matter density
Upper bound on f_a ...

...Assuming initial misalignment angle is O(I)

Axion dark matter today:

$$\rho_a(t_0) \simeq \rho_{\rm dm} \theta_i^2 \left(\frac{f_a}{{\rm few} \times 10^{11} {\rm GeV}} \right)$$
observed dark matter density
$$\frac{Jpper \text{ bound on } f_a...}{Jpper bound on f_a...}$$

...Assuming initial misalignment angle is O(I)

With f_a below inflation scale: causally disconnected at T~I GeV regions merge:

$$\theta_i^2 \to \langle \sin^2 \theta_i \rangle \simeq \frac{1}{2}$$

...always O(I)

Axion dark matter today:

$$\rho_a(t_0) \simeq \rho_{\rm dm} \theta_i^2 \left(\frac{f_a}{{\rm few} \times 10^{11} {\rm ~GeV}} \right)$$
observed dark matter density
$$\frac{f_a}{f_b per bound on f_a}$$

...Assuming initial misalignment angle is O(I)

With f_a below inflation scale: causally disconnected at T~I GeV regions merge:

$$\theta_i^2 \to \langle \sin^2 \theta_i \rangle \simeq \frac{1}{2}$$

...always O(I)

- upper bound: $f_a \lesssim 10^{12} {
 m GeV}$
- axions make good dark matter candidate for $f_a \simeq 10^{12} \text{ GeV}$ $\left(m_a \simeq 10^{-5} - 10^{-6} \text{ eV}\right)$

$$\rho_a(t_0) \simeq \rho_{\rm dm} \,\theta_i^2 \left(\frac{f_a}{\rm few \times 10^{11} \, GeV}\right)$$

$$\rho_a(t_0) \simeq \rho_{\rm dm} \,\theta_i^2 \left(\frac{f_a}{{\rm few} \times 10^{11} {\rm ~GeV}}\right)$$

Axions with PQ symmetry breaking before inflation:

$$\rho_a(t_0) \simeq \rho_{\rm dm} \,\theta_i^2 \left(\frac{f_a}{{\rm few} \times 10^{11} {\rm ~GeV}}\right)$$

Axions with PQ symmetry breaking before inflation:

 \bullet initial misalignment angle θ_i random

$$\rho_a(t_0) \simeq \rho_{\rm dm} \,\theta_i^2 \left(\frac{f_a}{{\rm few} \times 10^{11} {\rm ~GeV}}\right)$$

Axions with PQ symmetry breaking before inflation:

- initial misalignment angle θ_i random
- today our horizon comes from a single causally connected patch from before inflation with one particular value for θ_i

$$\rho_a(t_0) \simeq \rho_{\rm dm} \,\theta_i^2 \left(\frac{f_a}{{\rm few} \times 10^{11} {\rm ~GeV}}\right)$$

Axions with PQ symmetry breaking before inflation:

- initial misalignment angle θ_i random
- today our horizon comes from a single causally connected patch from before inflation with one particular value for θ_i

So the initial misalignment angle can assume any value, is a constant across our horizon, and there is no bound on f_a (but small θ_i required for large f_a ! Fine-tuned!)

[S.Y. Pi]



- Epoch of expansion much faster than speed of light
- Causal patch stretched to far outside the horizon
- Followed by reheating epoch & conventional Big Bang evolution
- Inhomogeneities eventually reenter horizon



- Epoch of expansion much faster than speed of light
- Causal patch stretched to far outside the horizon
- Followed by reheating epoch & conventional Big Bang evolution
- Inhomogeneities eventually reenter horizon





- Epoch of expansion much faster than speed of light
- Causal patch stretched to far outside the horizon
- Followed by reheating epoch & conventional Big Bang evolution
- Inhomogeneities eventually reenter horizon







horizon 🔘



Potential problems with **inflationary** axion cosmology with an ultralight axion ($f_a >> 10^{12}$ GeV):

Potential problems with **inflationary** axion cosmology with an ultralight axion ($f_a >> 10^{12}$ GeV):



Potential problems with **inflationary** axion cosmology with an ultralight axion ($f_a >> 10^{12}$ GeV):



• Can be fixed by anthropic principle

Potential problems with **inflationary** axion cosmology with an ultralight axion ($f_a >> 10^{12}$ GeV):



Fine tuning of initial axion misalignment angle

• Can be fixed by anthropic principle



Potential problems with **inflationary** axion cosmology with an ultralight axion ($f_a >> 10^{12}$ GeV):



- Fine tuning of initial axion misalignment angle
 - Can be fixed by anthropic principle



Can be fixed with sufficiently low inflation scale

Isocurvature axion fluctuations (Turner & Wilczek):

Inflation gives rise to fluctuations in massless fields

$$\left\langle \phi_{\mathbf{k}} \phi_{\mathbf{k}'}^* \right\rangle = \frac{2\pi^2}{k^3} \left(\frac{H_i}{2\pi}\right)^2 (2\pi)^3 \delta^3(\mathbf{k} - \mathbf{k}')$$

Socurvature axion fluctuations (Turner & Wilczek): Inflation gives rise to fluctuations in massless fields $\langle \phi_{\mathbf{k}} \phi_{\mathbf{k}'}^* \rangle = \frac{2\pi^2}{k^3} \left(\frac{H_i}{2\pi} \right)^2 (2\pi)^3 \delta^3(\mathbf{k} - \mathbf{k}')$

• Inflaton fluctuations give rise to adiabatic perturbations for structure formation

Socurvature axion fluctuations (Turner & Wilczek): Inflation gives rise to fluctuations in massless fields $\langle \phi_{\mathbf{k}} \phi_{\mathbf{k}'}^* \rangle = \frac{2\pi^2}{k^3} \left(\frac{H_i}{2\pi} \right)^2 (2\pi)^3 \delta^3(\mathbf{k} - \mathbf{k}')$

- Inflaton fluctuations give rise to adiabatic perturbations for structure formation ^(C)
- Fluctuations in the axion field (misalignment angle) give rise to isocurvature perturbations ⁽³⁾

Socurvature axion fluctuations (Turner & Wilczek): Inflation gives rise to fluctuations in massless fields $\langle \phi_{\mathbf{k}} \phi_{\mathbf{k}'}^* \rangle = \frac{2\pi^2}{k^3} \left(\frac{H_i}{2\pi} \right)^2 (2\pi)^3 \delta^3(\mathbf{k} - \mathbf{k}')$

- Inflaton fluctuations give rise to adiabatic perturbations for structure formation $\textcircled{\begin{tubel{$
- Fluctuations in the axion field (misalignment angle) give rise to isocurvature perturbations ⁽³⁾

Isocurvature perturbations:

- Fluctuations in energy density of matter & radiation
- **NO** fluctuations in total energy (matter + radiation)





Initial **adiabatic** perturbation spectrum agrees well with CMB observation



WMAP 5-yr results

David B. Kaplan ~ INT ~ April 25, 2012

Generation of isocurvature fluctuations

Initial isocurvature perturbation spectrum disagrees with CMB observation at small angles



Generation of isocurvature fluctuations

Initial isocurvature perturbation spectrum disagrees with CMB observation at small angles





Inflation induced fluctuations in axions: Hubble

If axions are the dark matter:

$$\theta_i \simeq \left(\frac{10^{12} \text{ GeV}}{f_a}\right)^{1/2}$$

and one gets an **upper** bound on H_I for a given f_a . E.g: $f_a = 10^{16}$ GeV -> $H_I < 10^8$ GeV

Inflation induced fluctuations in axions:

I fluctuations in axions: Hubble const

$$\frac{\delta n_a^{\text{iso}}}{n_a} \simeq \frac{H_I}{\pi a_i} = \frac{H_I}{\pi f_a \theta_i}$$

If axions are the dark matter:

$$\theta_i \simeq \left(\frac{10^{12} \text{ GeV}}{f_a}\right)^{1/2}$$

and one gets an **upper** bound on H_I for a given f_a . E.q: $f_a = 10^{16} \text{ GeV} \rightarrow H_I < 10^8 \text{ GeV}$

Small H_1 implies small tensor perturbations:

Observation of tensor perturbations in CMB would **rule out** $f_a > 10^{12}$ GeV

Fine tuning of initial axion misalignment angle: Can be fixed by anthropic principle



Anthropic selection of small initial axion angle (eg, of universe not over-dominated by axion dark matter)

Easy to abuse anthropic arguments!!

Sensible argument requires:

*ensemble of physical parameters to choose from

*****understanding of a priori probability distribution

★effect of evolution of cosmic structure, life...

Easy to abuse anthropic arguments!!

Sensible argument requires:

*ensemble of physical parameters to choose from

*****understanding of a priori probability distribution

★effect of evolution of cosmic structure, life...

Axion case ideal (why is θ_i small with inflation?)

*****different patches with different θ_i

\starinitial distribution flat on [0,2 π)

*affects evolution of cosmic structure through dark matter density Ω_{dm}





- Anthropic arguments for axions rely on a known initial probability distribution for the axion misalignment angle, and relatively simple cosmology to determine "viability"
- \bullet Inflation removes upper bound on $f_a,$ allows for GUT/string axions
- f_a> 10¹² GeV allows anthropic solution to dark matter coincidence

Could there be observable consequences from these ultra-light pre-inflationary axions?

Direct detection of ultralight axions $(f_a > 10^{12} \text{ GeV})$ very challenging!

Do you have any ideas?

Indirect detection through cosmology looks more promising now.

DBK, A.E. Nelson: arXiv:0809.1206



 \star = axion strings

 \bigstar = axion strings

There are axion strings outside our horizon

Distance to nearest cosmic axion string = d

$$d \lesssim r/H_0$$

Axion angle varies across our horizon:

$$\delta\theta \sim 2\pi \frac{1/H_0}{d} = \frac{2\pi}{r}$$

Axion strings are $\leq \mathbf{r}$ horizon lengths away = classical, superhorizon fluctuation ...so θ_i is not exactly constant in our horizon

Fine tuning with large f_a means enhanced sensitivity to fluctuations. How do we see them? How big does r have to be?

Today's dark matter distribution is sensitive to inhomogeneities in axion angle (axion strings!) at the beginning of inflation

- There are 25-60 e-foldings of inflation after our horizon leaves the inflationary horizon
- Relic pre-inflationary inhomogeneities and curvature today are sensitive to the amount of inflation r that precedes horizon departure
- What are current bounds on r?

Inflation must solve the flatness problem:

Curvature before inflation = O(1)

Inflation must solve the the horizon problem:

Assume: pre-inflation inhomogeneities = O(1) on scale of pre-inflation horizon

CMB multipoles will depend on

$$(kH_0)^{\ell} \sim \left(\frac{H_0}{rH_0}\right)^{\ell} = r^{-\ell}$$

So biggest effect of super-horizon fluctuations today are in lowest multipoles

Size of pre-inflationary causal patch today

Size of our $\sim 1/H_0$ horizon today

 $\left(\frac{\delta\rho}{\rho}\right)_{L}, \qquad k \ll \frac{1}{H_{0}}$

Find for CMB $\delta T/T$:

- Monopole moment unphysical
- Dipole moment cannot be distinguished from Doppler shift from local ("peculiar") velocity; and distant matter at rest in rest frame of CMB
- Quadrupole moment puts limit:

 $1/r^2 \lesssim (3 \times 10^{-5}) \qquad r \gtrsim 200$

 $\left(\frac{\delta\rho}{\rho}\right)_{L}, \qquad k \ll \frac{1}{H_{0}}$

Find for CMB $\delta T/T$:

- Monopole moment unphysical
- Dipole moment cannot be distinguished from Doppler shift from local ("peculiar") velocity; and distant matter at rest in rest frame of CMB

• Quadrupole moment puts limit:

$$1/r^2 \lesssim (3 \times 10^{-5}) \qquad r \gtrsim 200$$

 $\left(\frac{\delta\rho}{\rho}\right)_{L}, \qquad k \ll \frac{1}{H_{0}}$

Find for CMB $\delta T/T$:

- Monopole moment unphysical
- Dipole moment cannot be distinguished from Doppler shift from local ("peculiar") velocity; and distant matter at rest in rest frame of CMB

• Quadrupole moment puts limit:

$$1/r^2 \lesssim (3 \times 10^{-5})$$
 $r \gtrsim 200$
Observed quadrupole

 $\left(\frac{\delta\rho}{\rho}\right)_{I}, \quad k \ll \frac{1}{H_{0}}$

Find for CMB $\delta T/T$:

- Monopole moment unphysical
- Dipole moment cannot be distinguished from Doppler shift from local ("peculiar") velocity; and distant matter at rest in rest frame of CMB

• Quadrupole moment puts limit: $1/r^2 \lesssim (3 \times 10^{-5})$ $r \gtrsim 200$ Grishchuk-Zel'dovitch 1978 Observed quadrupole

 $\left(\frac{\delta\rho}{\rho}\right)_{L}, \qquad k \ll \frac{1}{H_{0}}$

Find for CMB $\delta T/T$:

- Monopole moment unphysical
- Dipole moment cannot be distinguished from Doppler shift from local ("peculiar") velocity; and distant matter at rest in rest $\frac{1}{r^2} \lesssim (3 \times 10^{-5}) \qquad r \gtrsim 200 \qquad \text{Grishchuk-Zel'dovitch} \\ \text{Observed quadrupole} \qquad \text{Castro et al. 2003} \\ \text{Phisticated: WMAP+CDMA} \qquad \text{Castro et al. 2003} \\ \text{Cast$ frame of CMB

• Quadrupole moment puts limit:

More sophisticated: WMAP+CDM Λ r>3900

If you plug in super-horizon <u>isocurvature</u> perturbation (eg: axions!) get non Sachs-Wolfe contribution:

$$\delta \rho_{\rm rad} = -\delta \rho_a$$

Find for CMB $\delta T/T$:

- Monopole moment unphysical
- Dipole moment **can** be distinguished from Doppler shift from local "peculiar" velocity (recall: δT_{γ} 180° out of phase)

Intrinsic dipole in CMB ≠ dipole in gravitational potential, so no corresponding flow of matter

We will see different dipole in CMB vs redshift of distant matter (Type 1 SN)

"Tilted Universe", M. Turner, 1990

Present and future bounds on tilted universe

- Tilted universe: gradient on matter density⇒photon rest frame ≠ matter rest frame
- CMB dipole gives our proper motion in photon rest frame
- SNI surveys give our proper motion in matter rest frame (currently rough agreement with CMB, Gordon, Land, Slozar, arXiv:0711.4196)

Gordon, Land, Slozar present and forecast for future peculiar velocity relative to matter measurements:

Figure 5. One sigma contours for the direction of the solar system velocity. The cases plotted are when correlated (solid) and uncorrelated (dashed) SNe peculiar velocities are used. The star shows the direction as determined by the CMB.

	l	b	$v_O ~(\rm km/s)$
Solar System uncorrelated	$238\pm26^\circ$	$45\pm14^{\circ}$	475 ± 134
Solar System correlated	$234\pm44^{\circ}$	$39 \pm 21^{\circ}$	468 ± 186
Local Group uncorrelated	$260\pm14^{\circ}$	$32 \pm 11^{\circ}$	697 ± 137
Local Group correlated	$257\pm24^{\circ}$	$29\pm16^\circ$	690 ± 201

 Table 1. The mean and standard deviation for the estimate of the solar system and local group velocity from current SNe data. The results for both the correlated and uncorrelated peculiar velocities are shown.

 Multiple

	l	b	$v_O \ (\rm km/s)$
GAIA Uncorrelated PVs	8°	5°	36
LSST Uncorrelated PVs	7°	5°	32
GAIA Correlated PVS	10°	6°	42
LSST Correlated PVS	8°	5°	34

Table 2. The forecasted marginalised standard deviation for the estimate of the solar system peculiar velocity from the future SNe surveys GAIA and LSST, where SNe peculiar velocities (PVs) are treated as uncorrelated and correlated.

current

Gordon, Land, Slozar present and forecast for future peculiar velocity relative to matter measurements:

Figure 5. One sigma contours for the direction of the solar system velocity. The cases plotted are when correlated (solid) and uncorrelated (dashed) SNe peculiar velocities are used. The star shows the direction as determined by the CMB.

Currently agree at $\approx 1 \sigma$

σ will be reduced by factor of ~ 4 with GAIA, LSST

	l	b	$v_O \ (\rm km/s)$
Solar System uncorrelated	$238\pm26^\circ$	$45\pm14^{\circ}$	475 ± 134
Solar System correlated	$234\pm44^{\circ}$	$39 \pm 21^{\circ}$	468 ± 186
Local Group uncorrelated	$260\pm14^{\circ}$	$32 \pm 11^{\circ}$	697 ± 137
Local Group correlated	$257\pm24^\circ$	$29\pm16^\circ$	690 ± 201

current

 Table 1. The mean and standard deviation for the estimate of the solar system and local group velocity from current SNe data. The results for both the correlated and uncorrelated peculiar velocities are shown.

 full
 full

	l	b	$v_O \ (\rm km/s)$
GAIA Uncorrelated PVs	8°	5°	36
LSST Uncorrelated PVs	7°	5°	32
GAIA Correlated PVS	10°	6°	42
LSST Correlated PVS	8°	5°	34

Table 2. The forecasted marginalised standard deviation for the estimate of the solar system peculiar velocity from the future SNe surveys GAIA and LSST, where SNe peculiar velocities (PVs) are treated as uncorrelated and correlated.

Many more recent papers indicating bulk flow of ~ 100 km/sec

e.g.:

Cosmic flows in the nearby universe from Type Ia Supernovae

Stephen Turnbull et al., 7 Nov 2011

bulk flow = 150 ± 43 km/sec

Measuring the cosmological bulk flow using the peculiar velocities of supernovae

De Chang Dai et al., 14 April 2011

bulk flow = 188 +119/-103 km/sec

Now: peculiar velocity measurements agree to $\delta v \sim 0.5 \times 10^{-3}$ Future: detect $\delta v \sim 1 \times 10^{-4}$

Fined tuned axion enhances isocurvature dipole moment

From axion strings:

$$\frac{\delta\Omega_a}{\Omega_a} \simeq 2 \frac{\delta\theta_i}{\theta_i} \simeq 2 \frac{(2\pi/r)}{\theta_i}$$

$$\approx \delta v$$
small θ_i enhances dipole
anisotropy of dark matter

Detectable if $\gtrsim 10^{-4}$

For $\underline{f_a \sim 10^{17} \text{ GeV}}$: $\theta_i \simeq 10^{-3} \implies \frac{\delta v = 10^{-4} \text{ sensitive to}}{r = 10^7 !}$

Now: peculiar velocity measurements agree to $\delta v \sim 0.5 \times 10^{-3}$ Future: detect $\delta v \sim 1 \times 10^{-4}$

Fined tuned axion enhances isocurvature dipole moment

From axion strings: $\frac{\delta\Omega_a}{\Omega_a} \simeq 2 \frac{\delta\theta_i}{\theta_i} \simeq 2 \frac{(2\pi/r)}{\theta_i}$ $\approx \delta v$ small θ_i enhances dipole anisotropy of dark matter

Detectable if $\gtrsim 10^{-4}$

For $\underline{f_a \sim 10^{17} \text{ GeV}}$: $\theta_i \simeq 10^{-3} \implies \frac{\delta v = 10^{-4} \text{ sensitive to}}{r = 10^7 !}$

We could detect an axion string 10,000,000 times horizon lengths away (6 x 10¹⁶ light-years)

Conclusions:

- Ultralight axions ($f_a \sim GUT$ scale, $m_a \sim 10^{-9} \text{ eV}$) remain a viable possibility for the dark matter
- Requires low scale inflation: they can be ruled out by observation of tensor perturbations in the CMB
- They may be indirectly detectable in large scale flow (Turner's Tilted Universe scenario)

if lucky, $r \leq 10^7$

 Black hole super-radiance another possible way to detect? (Arvanitaki, Dubovsky, 2010)