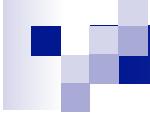


VM production and GPDs : polarization, angular momentum,...

Marc Vanderhaeghen
Johannes Gutenberg Universität, Mainz

INT Workshop “Orbital Angular Momentum in QCD”
Seattle, February 6 - 17, 2012



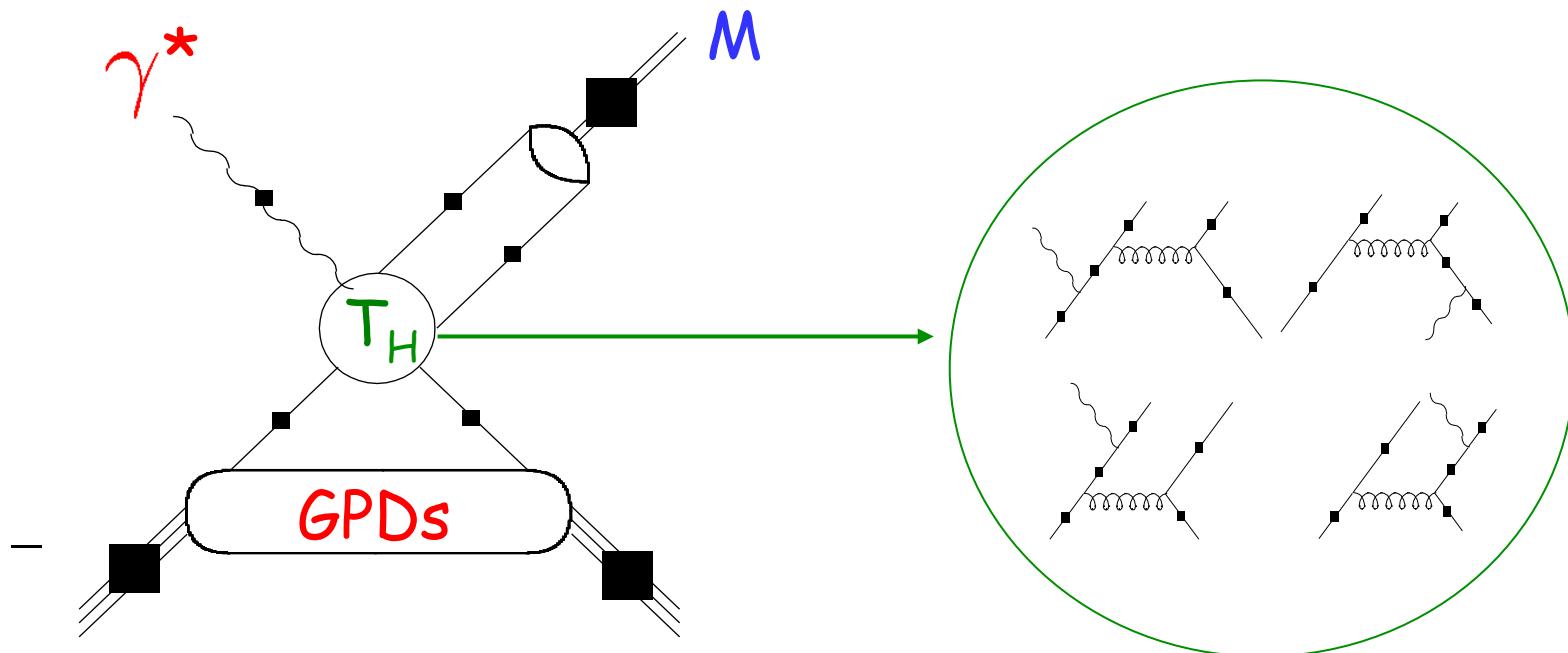
Outline

- ➡ Vector meson production in the **GPD framework**
- ➡ Modeling the **GPD E** and its connection to J_q
- ➡ Observables
- ➡ $N \rightarrow \Delta$ DVCS



Vector meson production in the GPD framework

Hard electroproduction of mesons ($\rho^{0,\pm}$, ω , φ , π , ...)



Factorization theorem shown for longitudinal photon

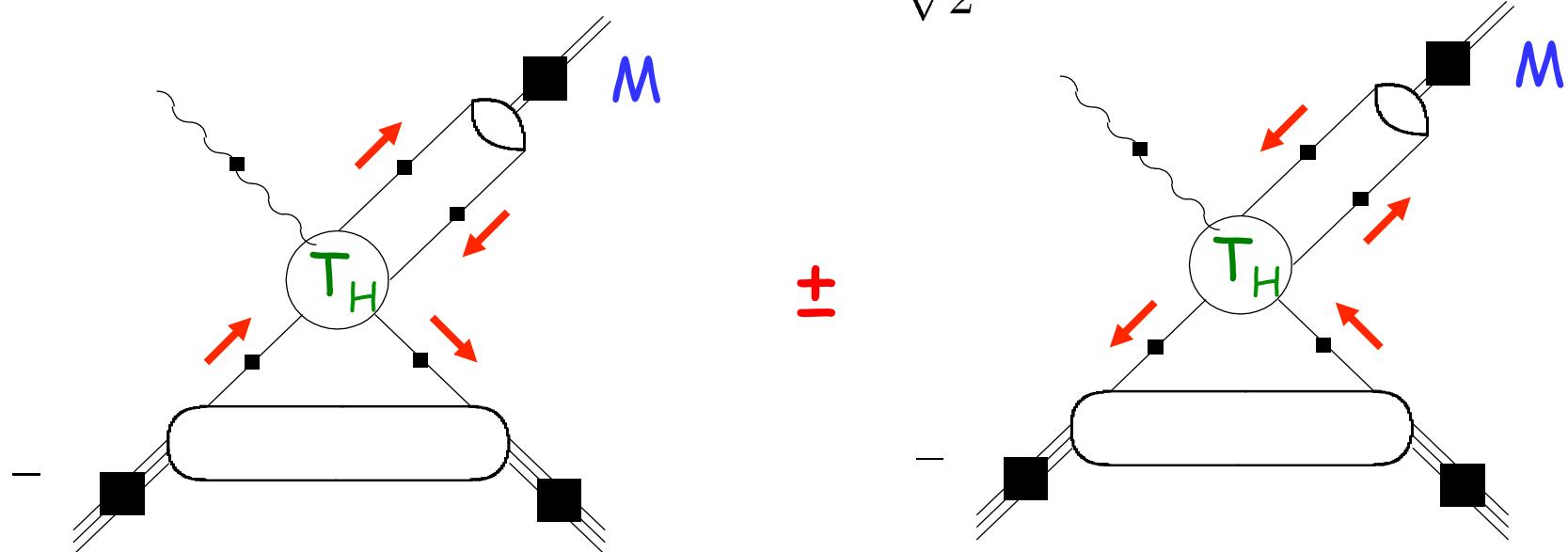
hard scattering amplitude

Collins, Frankfurt, Strikman (1997)

Meson acts as helicity filter

longitudinally pol. Vector meson $|\rho_L\rangle = \frac{1}{\sqrt{2}} |\uparrow\downarrow + \downarrow\uparrow\rangle$

PseudoScalar meson $|\pi\rangle = \frac{1}{\sqrt{2}} |\uparrow\downarrow - \downarrow\uparrow\rangle$



- Vector meson : accesses unpolarized GPDs H and E
- PseudoScalar meson : accesses polarized GPDs \tilde{H} and \tilde{E}

Hard electroproduction of vector mesons ($\rho^{0,\pm}$, ω , φ)

→ amplitude for longitudinally polarized vector meson

$$\begin{aligned}\mathcal{M}_{V_L}^L &= -ie \frac{4}{9} \frac{1}{Q} \left[\int_0^1 dz \frac{\Phi_{V_L}(z)}{z} \right] \frac{1}{2} (4\pi\alpha_s) \\ &\times \left\{ A_{V_L N} \bar{N}(p') \gamma \cdot n N(p) + B_{V_L N} \bar{N}(p') i\sigma^{\kappa\lambda} \frac{n_\kappa \Delta_\lambda}{2m_N} N(p) \right\}\end{aligned}$$

→ leading (1 gluon exchange) amplitude depends on α_s goes as $1/Q$

→ dependence on meson distribution amplitude Φ_V

$$\Phi_{V_L}(z) = f_V 6z(1-z)$$

with $f_\rho = 0.216$ GeV, $f_\omega = 0.195$ GeV, from $V \rightarrow e^+e^-$

Mankiewicz, Piller, Weigl (1998)

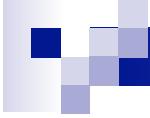
Vdh, Guichon, Guidal (1998)

Flavor decomposition of GPDs H and E

$$\rho^0 \quad \begin{aligned} A_{\rho_L^0 p} &= \int_{-1}^1 dx \quad \frac{1}{\sqrt{2}} (e_u H^u - e_d H^d) \quad \left\{ \frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right\} \\ B_{\rho_L^0 p} &= \int_{-1}^1 dx \quad \frac{1}{\sqrt{2}} (e_u E^u - e_d E^d) \quad \left\{ \frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right\} \end{aligned}$$

$$\rho^\pm \quad \begin{aligned} A_{\rho_L^\pm n} &= - \int_{-1}^1 dx \quad (H^u - H^d) \quad \left\{ \frac{e_u}{x - \xi + i\epsilon} + \frac{e_d}{x + \xi - i\epsilon} \right\} \\ B_{\rho_L^\pm n} &= - \int_{-1}^1 dx \quad (E^u - E^d) \quad \left\{ \frac{e_u}{x - \xi + i\epsilon} + \frac{e_d}{x + \xi - i\epsilon} \right\} \end{aligned}$$

$$\omega \quad \begin{aligned} A_{\omega_L p} &= \int_{-1}^1 dx \quad \frac{1}{\sqrt{2}} (e_u H^u + e_d H^d) \quad \left\{ \frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right\} \\ B_{\omega_L p} &= \int_{-1}^1 dx \quad \frac{1}{\sqrt{2}} (e_u E^u + e_d E^d) \quad \left\{ \frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right\} \end{aligned}$$



Modeling the GPD E and its connection to J_q

GPDs : t dependence (small - t)

→ $F_1^q(t) = \int_{-1}^1 dx H^q(x, \xi, t) \quad F_2^q(t) = \int_{-1}^1 dx E^q(x, \xi, t)$

evaluate for $\xi = 0$: model $H^q(x, 0, t)$ and $E^q(x, 0, t)$

→ small - t ($-t < 1 \text{ GeV}^2$) : Regge model Goeke, Polyakov, vdh (2001)

- $t = 0$: $H^q(x, 0, 0) + H^q(-x, 0, 0) = q_v(x) \sim \frac{1}{x^{\alpha(0)}} \quad \alpha(0) \simeq 0.5$

- $t \neq 0$: $H^q(x, 0, t) + H^q(-x, 0, t) \sim \frac{1}{x^{\alpha(t)}} \quad \alpha(t) = \alpha(0) + \alpha' t$

Regge trajectory $\alpha' \simeq 0.9 \text{ GeV}^{-2}$

→
$$F_1^q(t) = \int_0^1 dx q_v(x) \frac{1}{x^{\alpha'_1 t}} \quad F_2^q(t) = \int_0^1 dx \kappa_q q_v(x) \frac{1}{x^{\alpha'_2 t}}$$

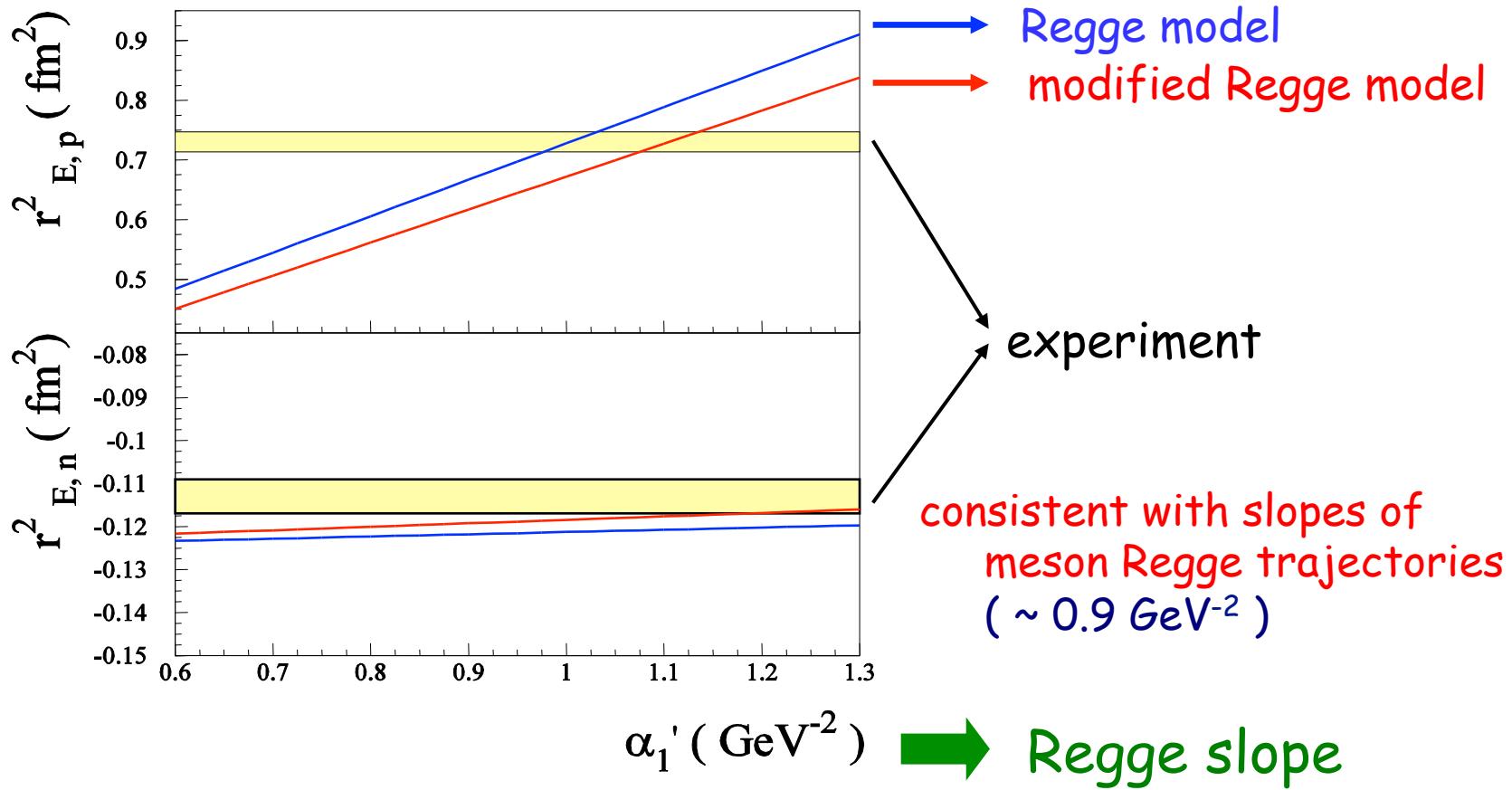
regge slopes : α'_1, α'_2 determined from rms radii

valence model
for E

proton & neutron charge radii

$$r_{E,p}^2 = r_{1,p}^2 + \frac{3}{2} \frac{\kappa_p}{M_N^2} \quad r_{1,p}^2 = -6 \alpha_1' \int_0^1 dx \left\{ e_u u_v(x) + e_d d_v(x) \right\} \ln x$$

$$r_{E,n}^2 = r_{1,n}^2 + \frac{3}{2} \frac{\kappa_n}{M_N^2} \quad r_{1,n}^2 = -6 \alpha_1' \int_0^1 dx \left\{ e_u d_v(x) + e_d u_v(x) \right\} \ln x$$



GPDs : t dependence (large $-t$)

modified Regge parametrization : Guidal, Polyakov, Radyushkin, vdh (2005)

$$\boxed{\begin{aligned} H^q(x, 0, t) &= q_v(x) x^{-\alpha'_1 (1-x) t} \\ E^q(x, 0, t) &= \frac{\kappa_q}{N_q} (1 - x)^{\eta_q} q_v(x) x^{-\alpha'_2 (1-x) t} \end{aligned}}$$

- Input : forward parton distributions at $\mu^2 = 1 \text{ GeV}^2$ (MRST2002 NNLO)
- Drell-Yan-West relation : $\exp(-\alpha' t) \rightarrow \exp(-\alpha' (1-x) t)$ Burkardt (2001)
- parameters :
 - regge slopes : α'_1, α'_2 determined from rms radii
 - η_u, η_d determined from F_2 / F_1 at large $-t$
- future constraints : moments from lattice QCD

connection large Q^2 of FF \leftrightarrow large x of GPD

$$\begin{aligned} I &= \int_0^1 dx (1-x)^\nu e^{\alpha' Q^2 (1-x) \ln x} = \int_0^1 dx e^{\nu \ln(1-x) + \alpha' Q^2 (1-x) \ln x} \\ &= \int_0^1 dx e^{f(x, Q^2)} \end{aligned}$$

at large Q^2 : integral dominated by maximum of $f(x, Q^2)$, remainder region is exp. suppressed (method of steepest descent)

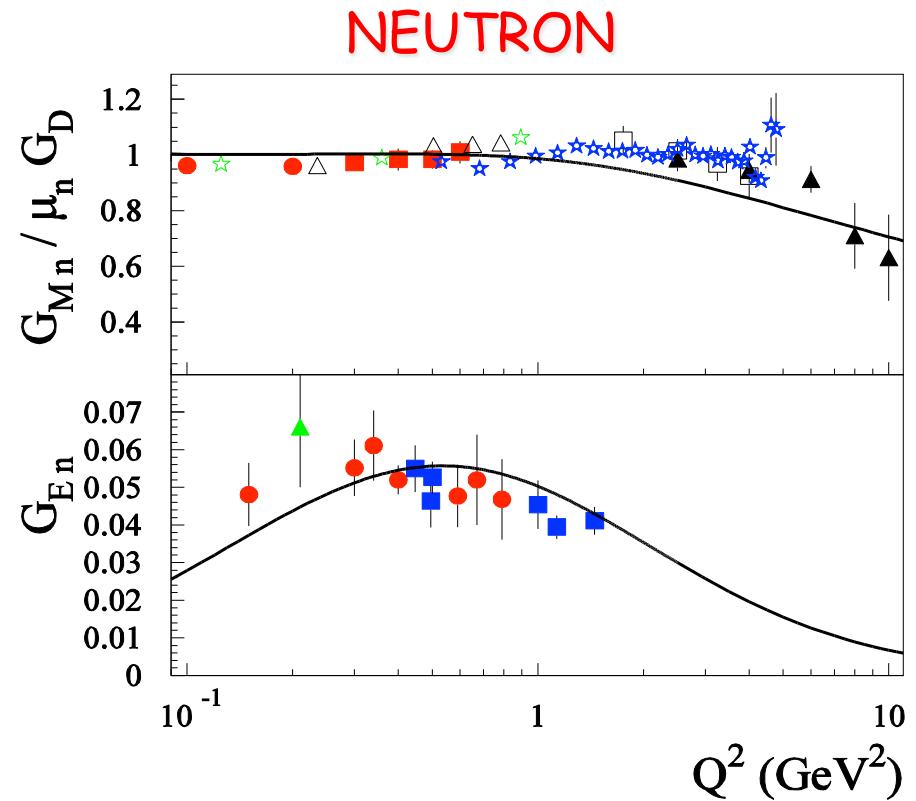
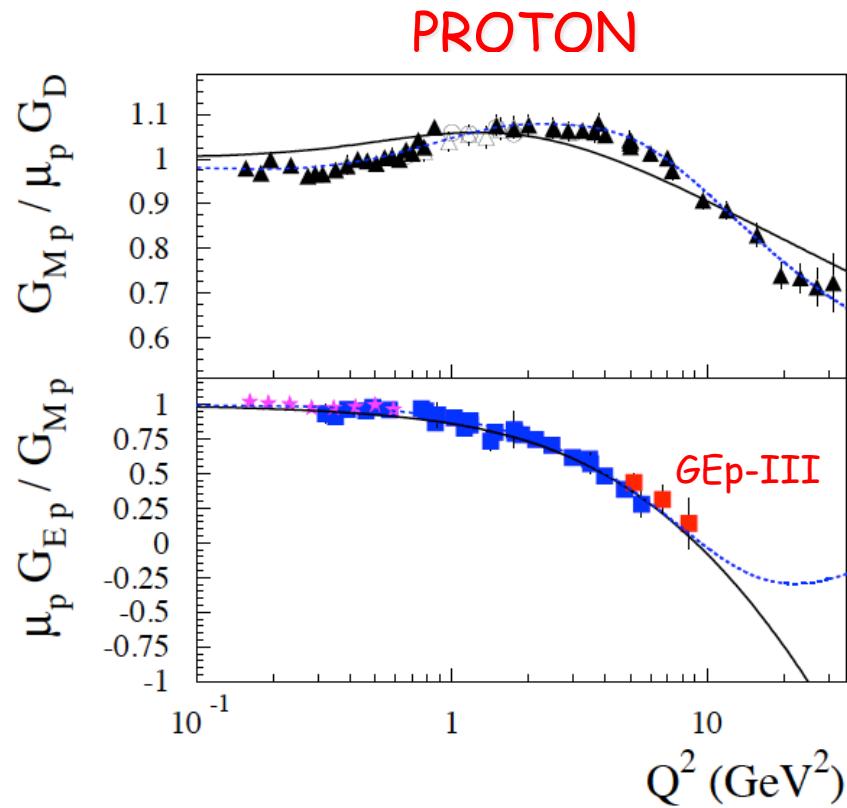
$$f(x, Q^2) \text{ reaches maximum for : } x = x_0 \simeq 1 - \frac{\nu}{\alpha' Q^2}$$

"Drell-Yan-West" relation for PDF/GPD :

at large Q^2 : I is dominated by its behavior around $x \rightarrow 1$

$$I \simeq e^{f(x_0, Q^2)} \left(\frac{2}{f''(x_0, Q^2)} \right)^{1/2} \frac{\sqrt{\pi}}{2} \sim \left(\frac{1}{\alpha' Q^2} \right)^{(\nu+1)/2}$$

Nucleon electromagnetic form factors



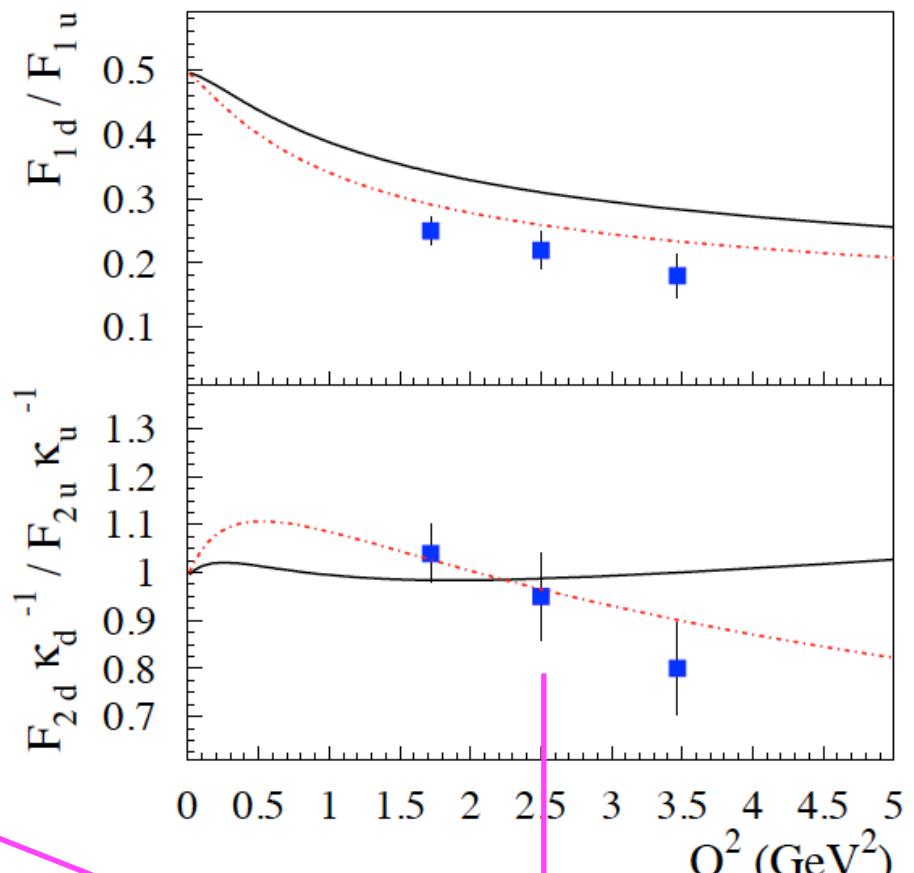
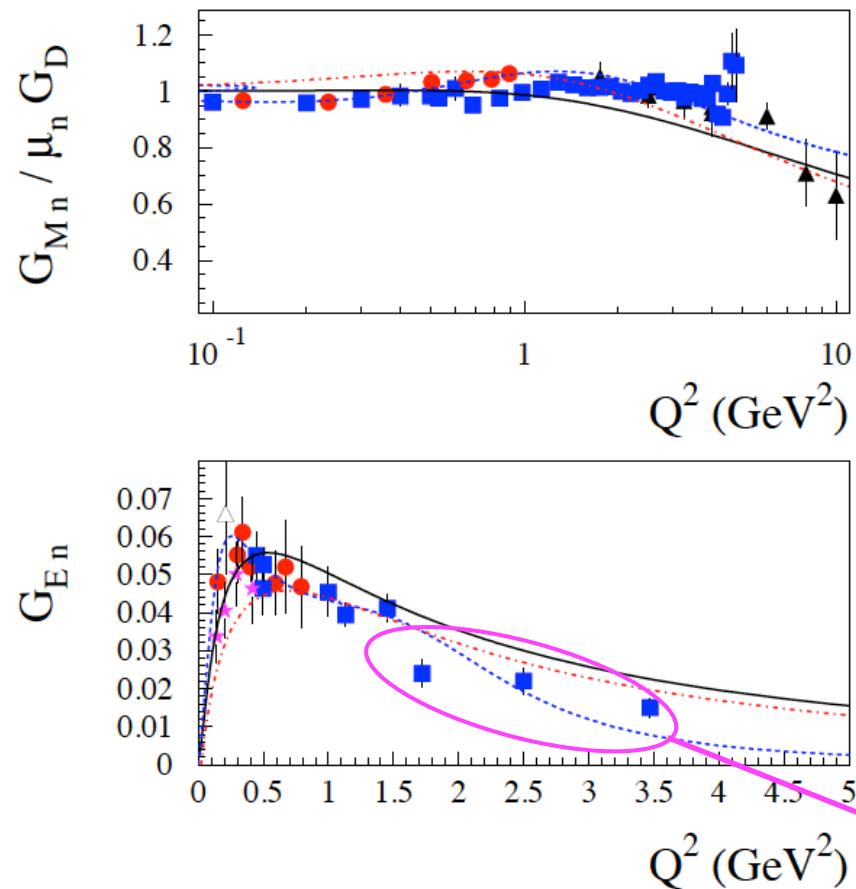
→ modified Regge GPD parameterization

3-parameter fit $\begin{cases} 1 : \text{Regge slope} \rightarrow \text{proton Dirac (Pauli) radius} \\ 2, 3 : \text{large } x \text{ behavior of GPD } E^u, E^d \rightarrow \text{large } Q^2 \text{ behavior of } F2p, F2n \end{cases}$

Guidal, Polyakov, Radyushkin, Vdh (2005)

also Diehl, Feldmann, Jakob, Kroll (2005)

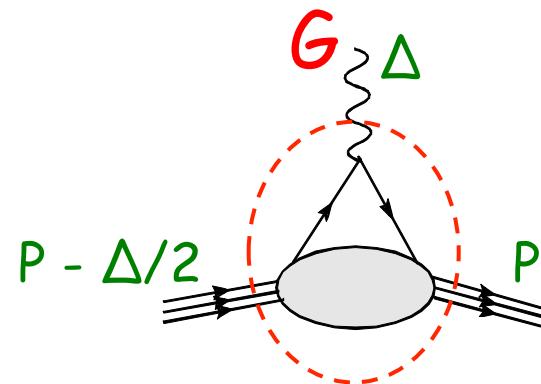
neutron e.m. form factors



- — — — — Phenomenological fit : Bradford et al.
- — — — — modified Regge GPD parameterization (3 parameters)
- - - - - modified Regge GPD parameterization (6 parameters)

Jlab/HallA E02-013
preliminary

Energy momentum form factors / spin of nucleon



nucleon in external classical gravitational field

$P - \Delta/2$ $P + \Delta/2$ $\rightarrow G$ couples to energy-momentum tensor

$$(\mu, \nu) \equiv \frac{1}{2}(\mu\nu + \nu\mu)$$

$$\langle N | T^{\mu\nu}(0) | N \rangle = \bar{N} \left\{ A(t) \gamma^{(\mu} P^{\nu)} + B(t) P^{(\mu} i\sigma^{\nu)\alpha} \frac{\Delta_\alpha}{2M} + C(t) (\Delta^\mu \Delta^\nu - \Delta^2 g^{\mu\nu}) \frac{1}{M} \right\} N$$

→ link to GPDs :

x. Ji (1997)

$$\int_{-1}^1 dx x H(x, \xi, t) = A(t) + 4\xi^2 C(t)$$

$$\int_{-1}^1 dx x E(x, \xi, t) = B(t) - 4\xi^2 C(t)$$

→ SPIN
"relation"

$$\boxed{\int_{-1}^1 dx x \left\{ H^q(x, \xi, 0) + E^q(x, \xi, 0) \right\} = A(0) + B(0) = 2 J^q}$$

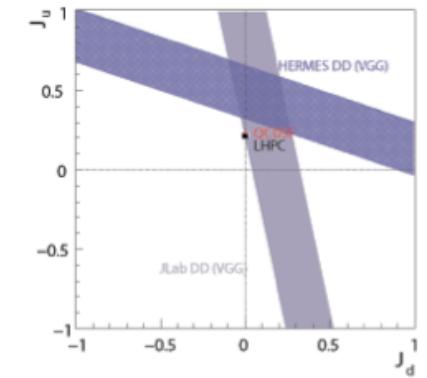
quark contribution to proton spin

$$\rightarrow 2 J^q = \int_{-1}^1 dx x \left\{ H^q(x, 0, 0) + E^q(x, 0, 0) \right\}$$

x. Ji
(1997)

$$2 J^q = M_2^q + \int_{-1}^1 dx x E^q(x, 0, 0)$$

with $M_2^q = \int_0^1 dx x [q(x) + \bar{q}(x)]$



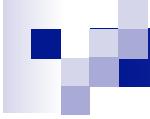
$$\rightarrow \text{parametrizations for } E^q : E^q(x, 0, 0) = \kappa_q / N_q (1 - x)^{\eta_q} q_v(x)$$

PROTON	M_2^q	$2 J^q$ GPD valence model	$2 J^q$ Lattice (LHPC) (4 GeV^2)
u	0.37	0.58	≈ 0.47
d	0.20	-0.06	≈ 0.00
s	0.04	0.04	
u + d + s	0.61	0.56	

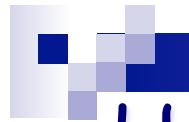
GPD model
($\mu^2 = 2 \text{ GeV}^2$)

Goeke, Polyakov, Vdh
(2001)

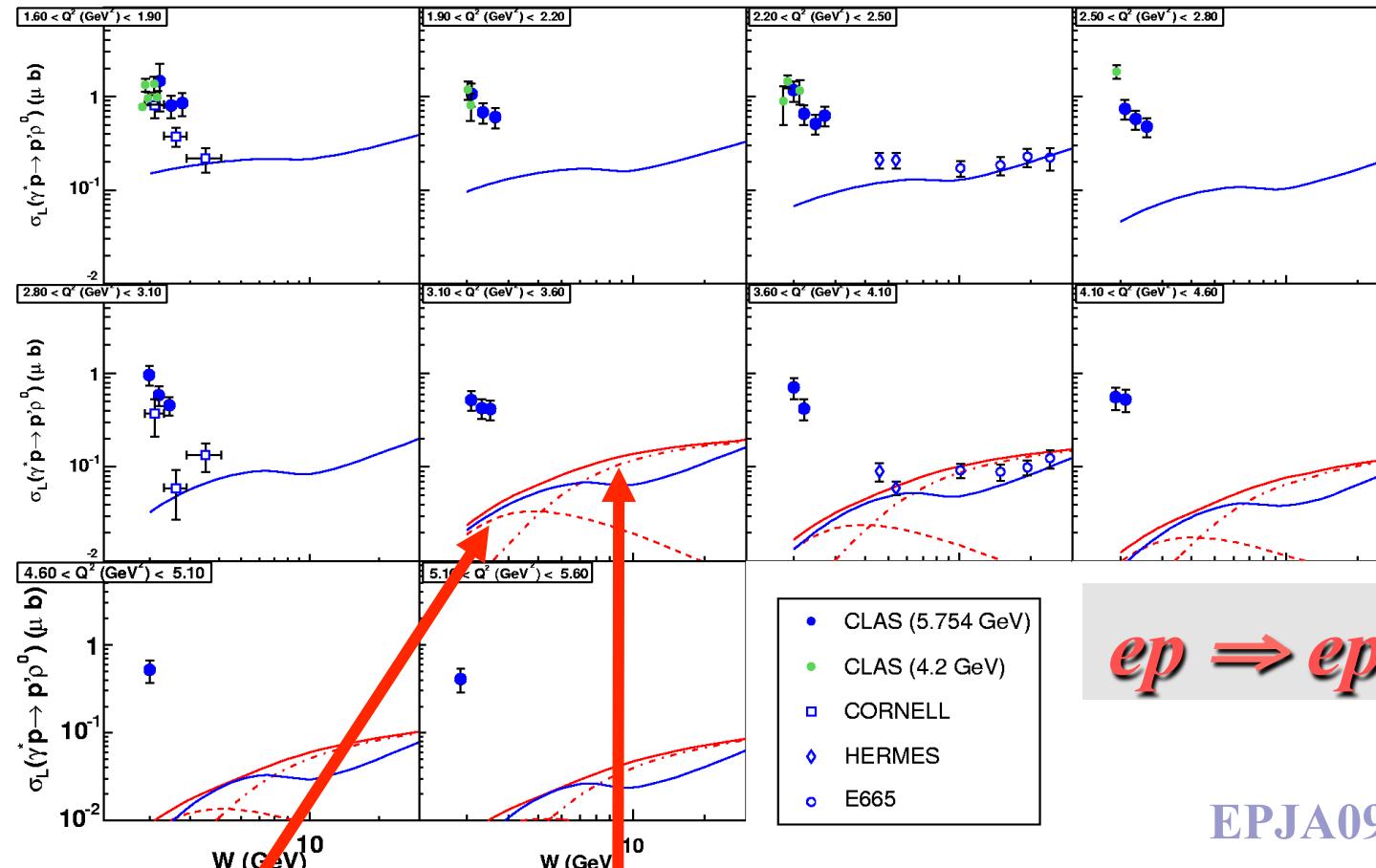
lattice : full QCD,
no disconnected
diagrams so far



Observables

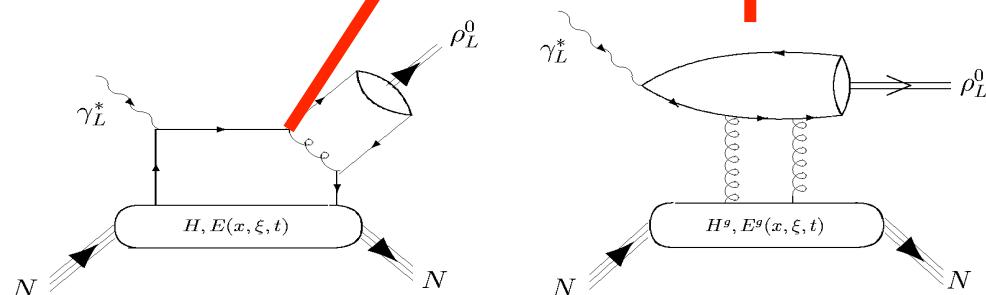


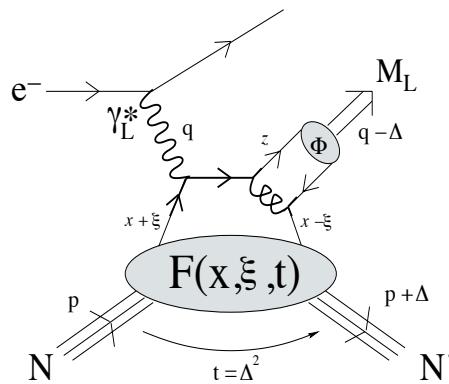
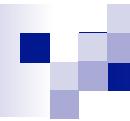
Hard electroproduction of ρ^0 : cross sections



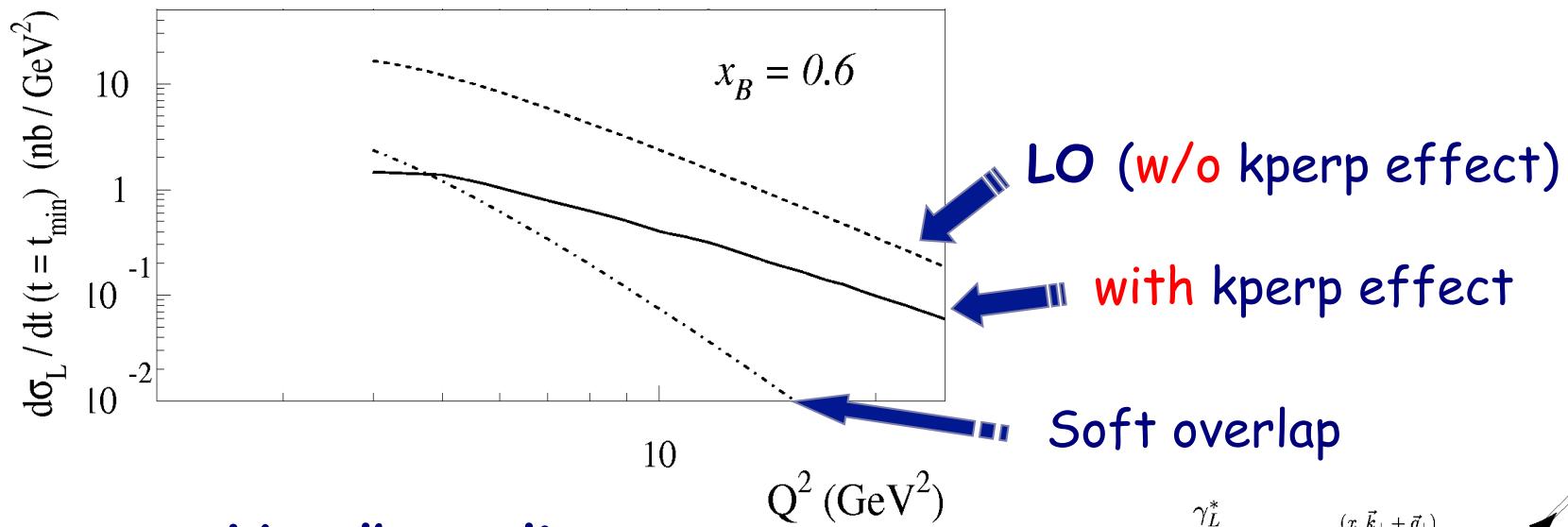
EPJA09

VGG GPD model
GK GPD model

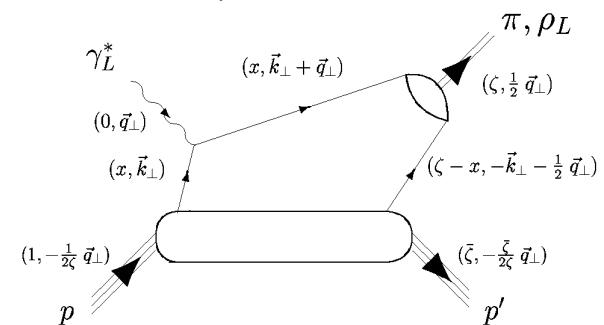




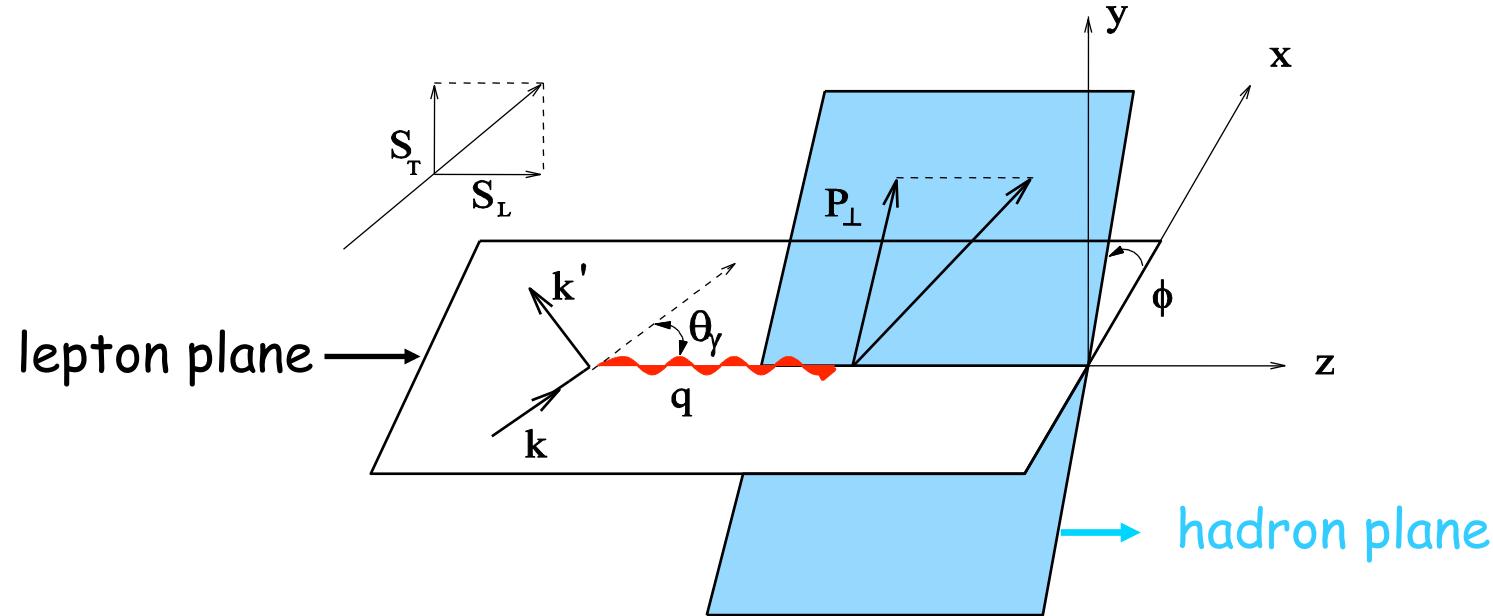
Interpretation in terms of GPDs ?



Handbag diagram
calculation requires
large correction
factors



Hard electroproduction of mesons : target normal spin asymmetry



in leading order (in Q) \rightarrow 2 observables $\sigma = \sigma_L + P_n \sigma_L^n$

\rightarrow Asymmetry :

$$A = \frac{2 \sigma_L^n}{\pi \sigma_L}$$

Target polarization normal
to hadron plane

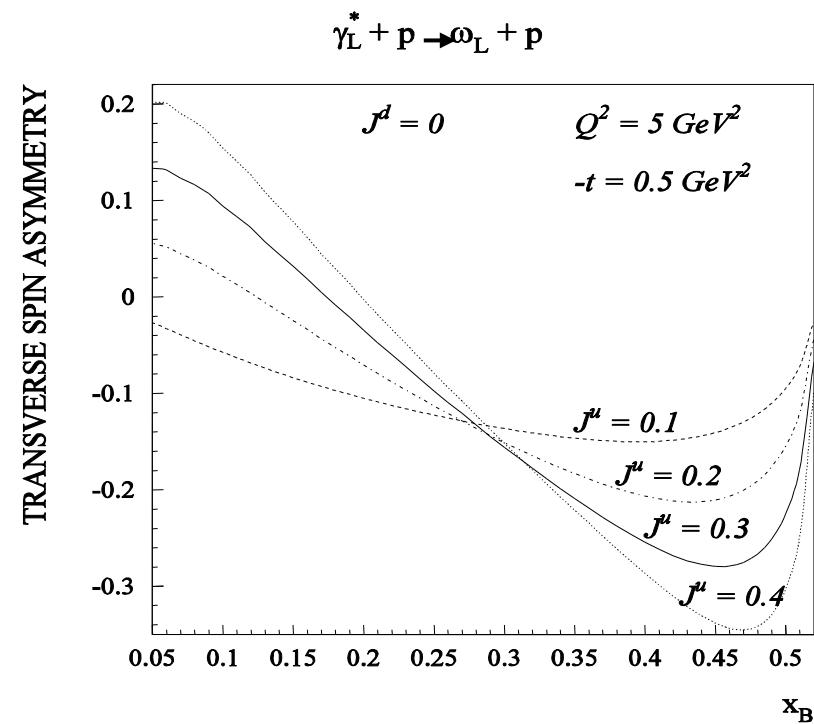
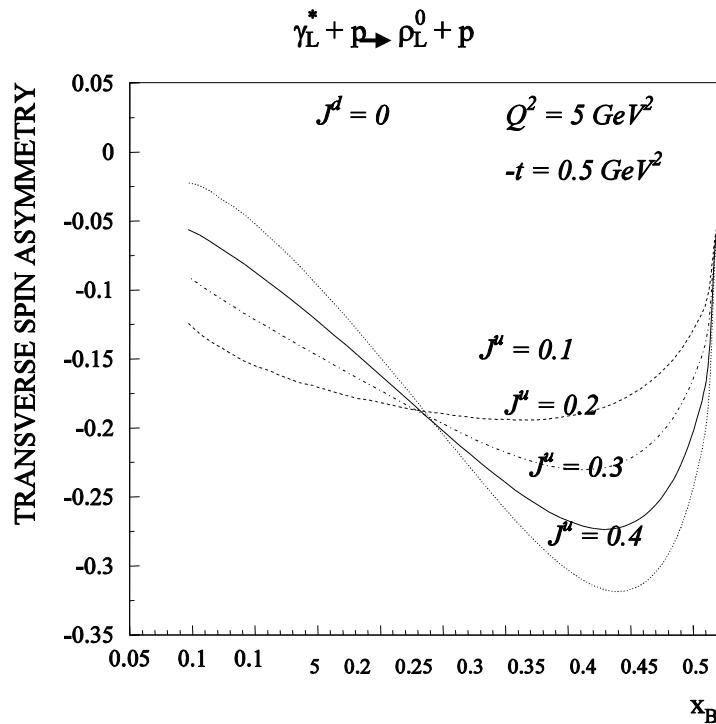
Hard electroprod. of vector mesons : target normal spin asymmetry

$$\begin{aligned} \mathcal{A}_{VN} &= -\frac{2|\Delta_\perp|}{\pi} \\ &\times \frac{\text{Im}(AB^*) / m_N}{|A|^2(1-\xi^2) - |B|^2(\xi^2 + t/(4m_N^2)) - \text{Re}(AB^*) 2\xi^2} \end{aligned}$$

- $A \rightarrow \text{GPD H}$ $B \rightarrow \text{GPD E}$
- linear dependence on GPD E \longleftrightarrow unpolarized cross section
- ratio : less sensitive to NLO and higher twist effects
- sensitivity to J^u and J^d
measure of TOTAL angular momentum contribution to proton spin

Hard electroprod. of vector mesons : target normal spin asymmetry

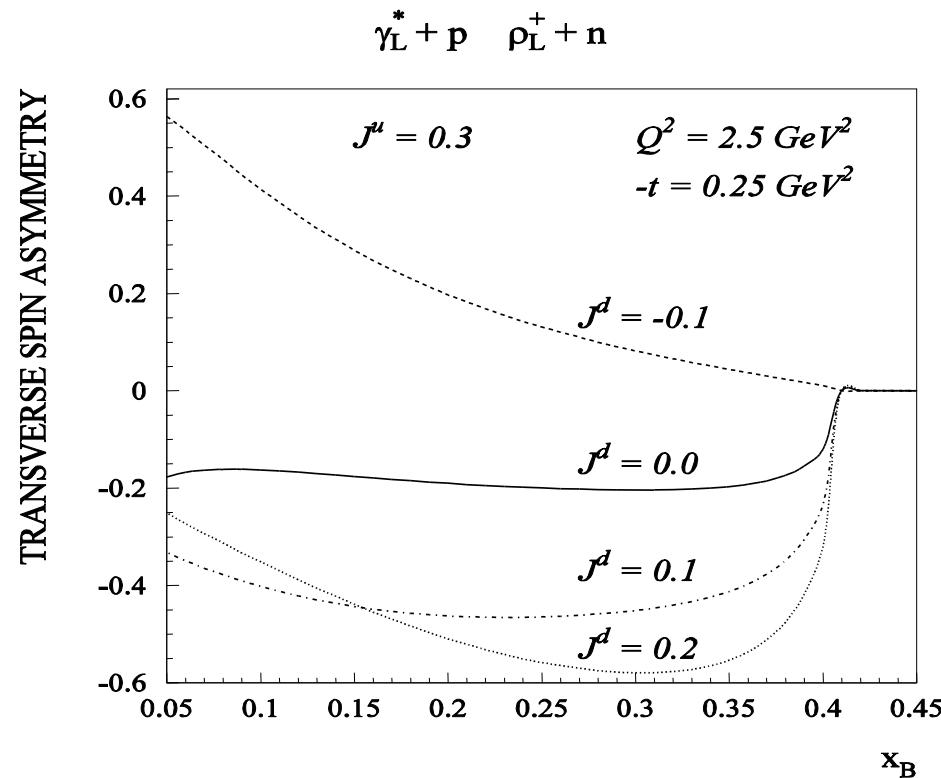
target polarized normal to hadronic plane



ρ_L^0 sensitive to $(2 J^u + J^d)$

ω_L sensitive to $(2 J^u - J^d)$

Hard electroprod. of vector mesons : target normal spin asymmetry



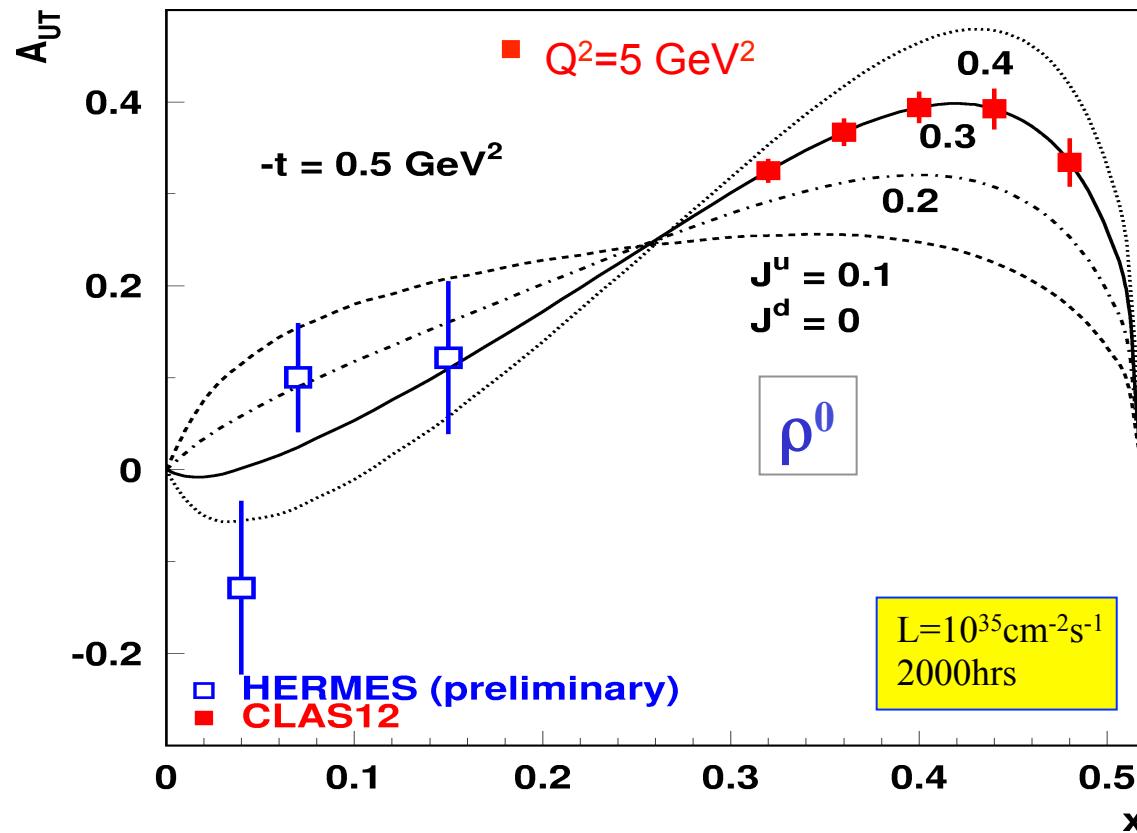
ρ_L^+ sensitive to ($J^u - J^d$)

exclusive ρ^0 prod. with transverse target

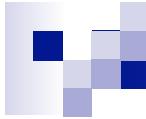
$$A_{UT} = - \frac{2\Delta (\text{Im}(AB^*))/\pi}{|A|^2(1-\xi^2) - |B|^2(\xi^2+t/4m^2) - \text{Re}(AB^*)2\xi^2}$$

ρ^0

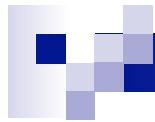
$$\begin{aligned} A &\sim (2H^u + H^d) \\ B &\sim (2E^u + E^d) \end{aligned}$$



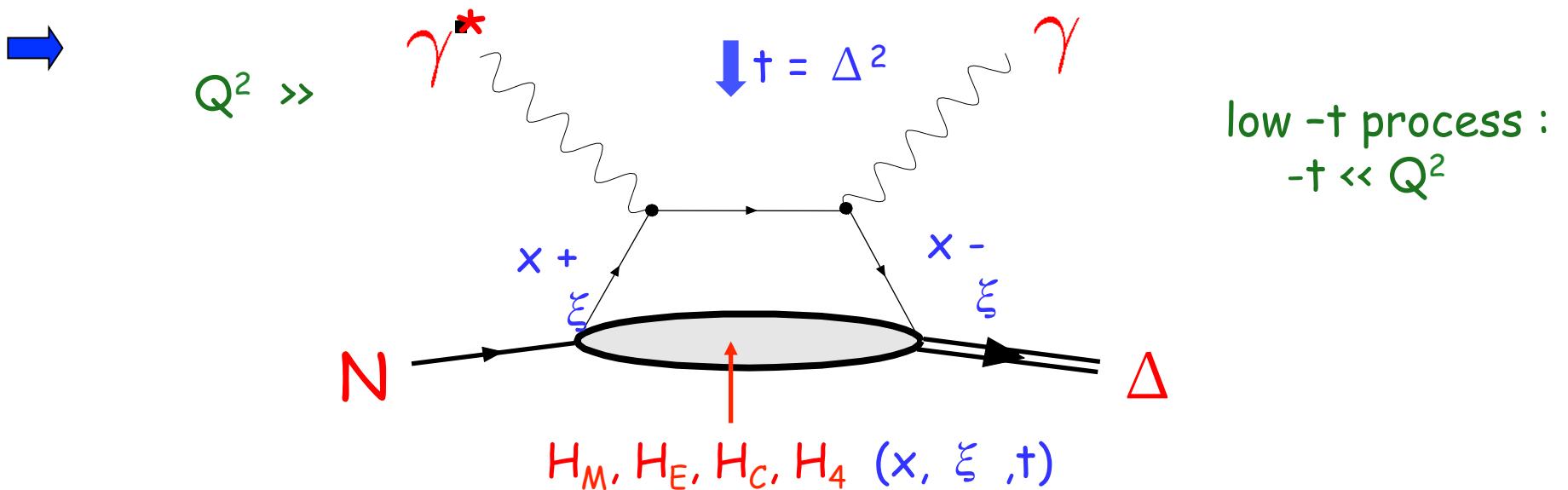
Asymmetry depends
linearly on the GPD E ,
which enters
Ji's sum rule.



$N \rightarrow \Delta$ DVCS



$N \rightarrow \Delta$ DVCS and GPDs



→

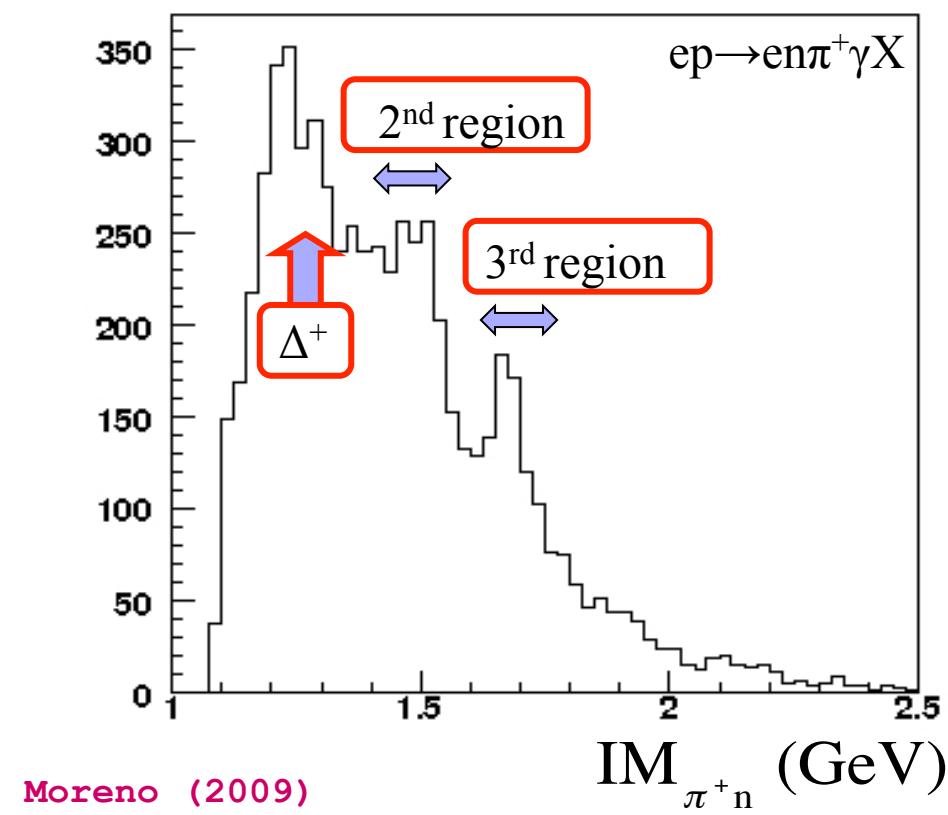
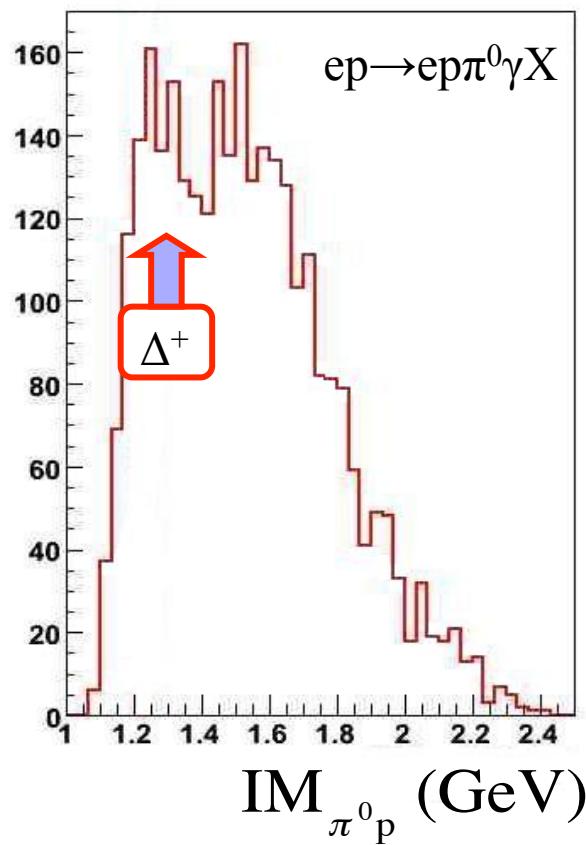
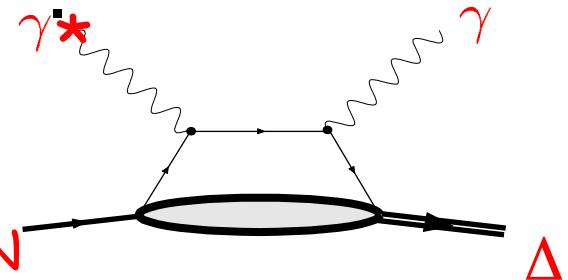
$$\left. \begin{aligned} \int_{-1}^1 dx H_M(x, \xi, t) &= 2 G_M^*(t) \\ \int_{-1}^1 dx H_E(x, \xi, t) &= 2 G_E^*(t) \\ \int_{-1}^1 dx H_C(x, \xi, t) &= 2 G_C^*(t) \\ \int_{-1}^1 dx H_4(x, \xi, t) &= 0 \end{aligned} \right\}$$

Jones-Scadron
 $N \rightarrow \Delta$ form
factors

$N \rightarrow \Delta$ DVCS events in CLAS

$W > 2 \text{ GeV}$

$Q^2 \approx 2.5 \text{ GeV}^2$



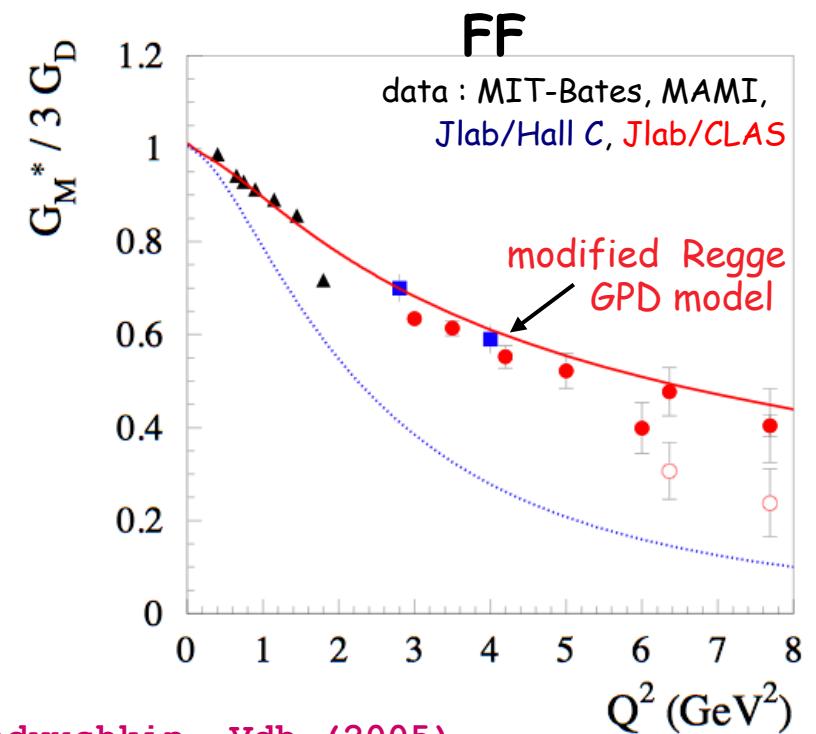
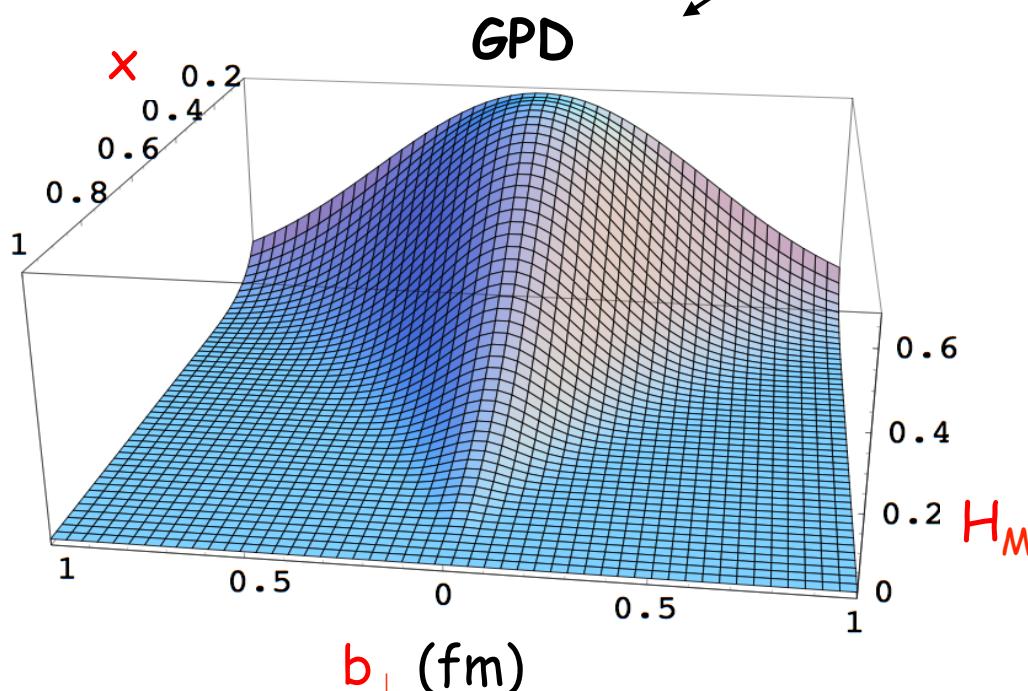
$N \rightarrow \Delta$ magnetic dipole GPD and FF

large N_c : $G_M^*(0) = \kappa_V / \sqrt{2} = 2.62$

large N_c limit

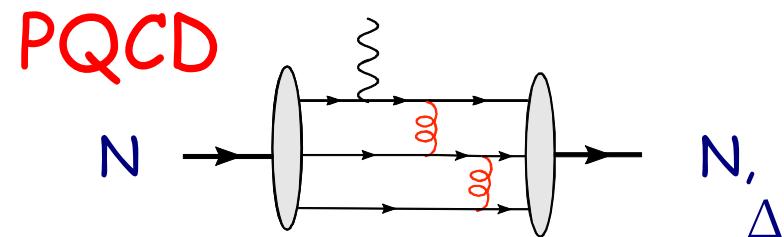
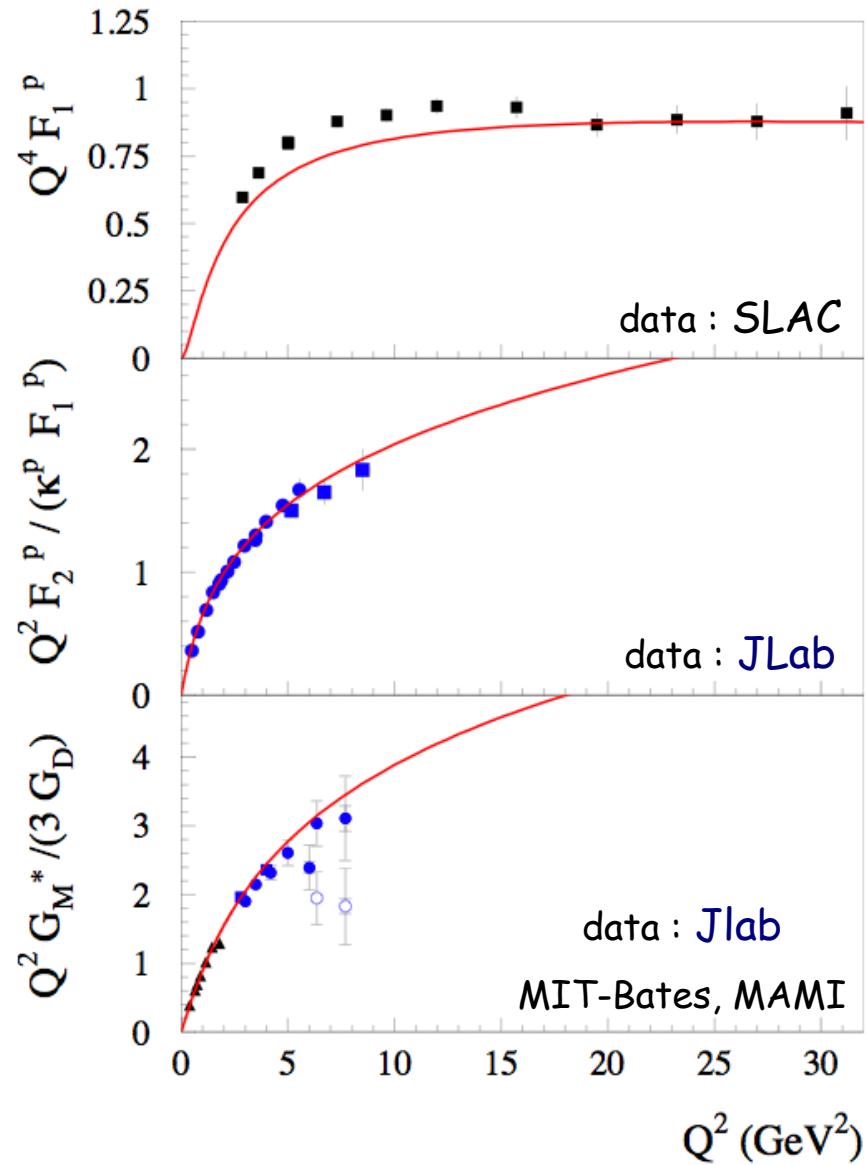
EXP: $G_M^*(0) = 3.02$

$$G_M^*(t) = \frac{G_M^*(0)}{\kappa_V} \int_{-1}^{+1} dx \left\{ E^u(x, \xi, t) - E^d(x, \xi, t) \right\} = \frac{G_M^*(0)}{\kappa_V} \left\{ F_2^p(t) - F_2^n(t) \right\}$$



Guidal, Polyakov, Radyushkin, Vdh (2005)

scaling behavior of N and $N \rightarrow \Delta$ FF



+ collinear quarks

$$F_1^p \sim 1/Q^4$$

$$F_2^p / F_1^p \sim 1/Q^2$$

$$G_M^* \sim 1/Q^4$$

GPD — modified Regge GPD model

Guidal, Polyakov, Radyushkin, Vdh
(2005)

Challenges / outlook

- Physics of light vector meson production
 - in the **valence region** : remains to be understood
 - (u-quark dominance, meson exchanges, higher twist, ... ?)
 - for **gluons** : large correction factors needed
- Transverse target spin asymmetry seems a promising observable to minimize higher order/
higher twist corrections
 - Linear dependence on **GPD E (J_q)**
- $N \rightarrow \Delta$ DVCS : quark GPDs in excited state,
test of dynamical relations (large N_c)
relation with **GPD E_q**