

The Questions of Hadronic Physics

L: parton OAM

- Can we **quantitatively** describe the **non-perturbative** problems of hadron substructure and hadron formation?
→ experiment vs lattice QCD
- Can we achieve an **intuitive understanding** of hadron structure and formation? What are the best **degrees of freedom** with which to think about the strong force in confined systems?
→ experiment vs phenomenology / effective theories
- Are the **theoretical tools** we use to describe our data accurate and well-understood, for both familiar and novel distribution and fragmentation functions?
→ experiment vs pQCD, factorization, & evolution
- How does the **nuclear environment** affect the partonic structure of the nucleon?
→ experiment vs medium-effect models

L + Relativity = Weirdness

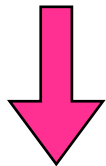
Dirac free plane-wave particle with spin $\mathbf{S}_z = +1$

Boosting a Dirac Spinor

How is L_z affected by boosts?

at rest $\vec{p} = 0$

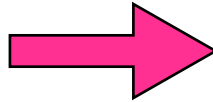
$$\psi = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-imt}$$



$$\frac{\psi^\dagger \vec{\Sigma} \psi}{\psi^\dagger \psi} = \hat{z}$$

BOOST

in $-\hat{x}$ direcⁿ with



$$\beta = p'/E' = \tanh \phi$$

$$\hat{B}(\hat{x}, \phi) = e^{\frac{\phi}{2} \vec{\alpha} \cdot \hat{x}} = \cosh \frac{\phi}{2} \mathbf{1} + \sinh \frac{\phi}{2} \alpha_x$$

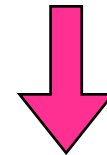
What's its spin?

$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix}$$

$$\vec{\sigma} = \begin{pmatrix} \hat{z} & \hat{x} - i\hat{y} \\ \hat{x} + i\hat{y} & -\hat{z} \end{pmatrix}$$

$\vec{p}' = p' \hat{x}$

$$\psi' = N \begin{pmatrix} 1 \\ 0 \\ 0 \\ \frac{p'}{E' + m} \end{pmatrix} e^{i(p'x' - E't')}$$



$$\frac{\psi'^\dagger \vec{\Sigma} \psi'}{\psi'^\dagger \psi'} = \hat{z} \left[1 - \left(\frac{p'}{E' + m} \right)^2 \right]$$

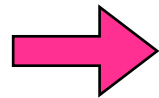
$$\approx \hat{z} \frac{1}{\gamma^2} \text{ for } \gamma \gg 1$$

Why there are no transversely polarized electron machines!

Spin, L, and the free Dirac Hamiltonian

$$\mathbf{H} = \boldsymbol{\alpha} \cdot \vec{p} + \beta m = \begin{pmatrix} m\mathbf{1} & -i\vec{\sigma} \cdot \vec{\nabla} \\ -i\vec{\sigma} \cdot \vec{\nabla} & m\mathbf{1} \end{pmatrix}$$

$$\begin{aligned} \vec{\mathbf{L}}(\vec{x}) &= \mathbf{1} \vec{x} \times \vec{p} \\ &= -i \vec{x} \times \vec{\nabla} \end{aligned}$$



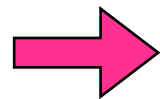
L position-dependent, doesn't commute w $\hat{\partial}_i$ in **H**

$$[\mathbf{H}, \vec{\mathbf{L}}(x_i)] = -\vec{\alpha} \times \vec{\nabla}$$

L NOT CONSERVED

no shells!

$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix}$$



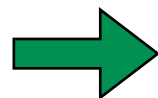
Pauli matrices in **Σ** and **H** don't commute

$$[\mathbf{H}, \vec{\Sigma}] = 2\vec{\alpha} \times \vec{\nabla}$$

SPIN NOT CONSERVED

intuition?

$$[\sigma_i, \sigma_j] = 2i \epsilon_{ijk} \sigma_k$$



$$[\mathbf{H}, \vec{\mathbf{L}} + \frac{1}{2} \vec{\Sigma}] = [\mathbf{H}, \vec{\mathbf{J}}] = 0$$

J CONSERVED

Dirac particle in a central potential

We denote the solution of the above-mentioned equation by the Dirac four-spinor ψ and/or its upper- and lower-component, the corresponding two-spinors φ and χ . The stationary states are characterized by the following set of quantum numbers ε , j , m and P which are respectively the eigenvalues of the operators \hat{H} (the Hamiltonian), $\hat{\mathbf{j}}^2$, \hat{j}_z (total angular momentum and its z-component) and \hat{P} (the parity). Since every eigenstate of the valence quark characterized by ε , j , m and P corresponds to two different orbital angular momenta l and $l' = l \pm 1$, (see Appendix A), it is clear that *orbital motion is involved in every stationary state*. This is true *also when the valence quark is in its ground state* ($\psi_{\varepsilon j m P}$ where $\varepsilon = \varepsilon_0$, $j = 1/2$, $m = \pm 1/2$, $P = +^2$). This state can be expressed as follows:

$$\psi_{\varepsilon_0 1/2 m+}(r, \theta, \phi) = \begin{pmatrix} f_0(r) \Omega_0^{1/2 m}(\theta, \phi) \\ g_1(r) \Omega_1^{1/2 m}(\theta, \phi) \end{pmatrix}. \quad (2.1)$$

The angular part of the two-spinors can be written in terms of spherical functions $Y_{ll_z}(\theta, \phi)$ and (non-relativistic) spin-eigenfunctions which are nothing else but the Pauli-spinors $\xi(\pm 1/2)$:

$$\Omega_0^{1/2 m}(\theta, \phi) = Y_{00}(\theta, \phi) \xi(m),$$

The spherical solutions of a Dirac particle in a central potential are discussed in some of the text books (see, for example, Landau, L.D., Lifshitz, E.M.: Course of theoretical physics. Vol. 4: Relativistic quantum theory. New York: Pergamon 1971). The notations and conventions we use here are slightly different. In order to avoid possible misunderstanding, we list the general form of some of the key formulae in the following:

In terms of spherical variables, a state with given ε , j , m and P can be written as:

$$\psi_{\varepsilon j m P}(r, \theta, \phi) = \begin{pmatrix} f_{\varepsilon l}(r) \Omega_l^{j m}(\theta, \phi) \\ (-1)^{(l-l'+1)/2} g_{\varepsilon l'}(r) \Omega_{l'}^{j m}(\theta, \phi) \end{pmatrix}. \quad (A1)$$

Here $l = j \pm 1/2$, $l' = 2j - l$ and $P = (-1)^l$; $\Omega_l^{j m}$ and $\Omega_{l'}^{j m}$ are two-spinors which, for the possible values of l , are given by:

$$\begin{aligned} \Omega_{l=j-1/2}^{j m}(\theta, \phi) &= \sqrt{\frac{j+m}{2j}} Y_{l l_z=m-1/2}(\theta, \phi) \xi(1/2) \\ &+ \sqrt{\frac{j-m}{2j}} Y_{l l_z=m+1/2}(\theta, \phi) \xi(-1/2), \end{aligned} \quad (A2)$$

$$\begin{aligned} \Omega_{l=j+1/2}^{j m}(\theta, \phi) &= -\sqrt{\frac{j-m+1}{2j+2}} Y_{l l_z=m-1/2}(\theta, \phi) \xi(1/2) \\ &+ \sqrt{\frac{j+m+1}{2j+2}} Y_{l l_z=m+1/2}(\theta, \phi) \xi(-1/2). \end{aligned} \quad (A3)$$

Here, $\xi(\pm 1/2)$ stand for the eigenfunctions for the spin-operator $\hat{\sigma}_z$ with eigenvalues ± 1 , and $Y_{ll_z}(\theta, \phi)$ for the spherical harmonics which form a standard basis for the orbital angular momentum operators ($\hat{\mathbf{l}}^2, \hat{l}_z$). The functions $f_{\varepsilon l}(r)$ and $g_{\varepsilon l'}(r)$ are solutions of the coupled differential equations:

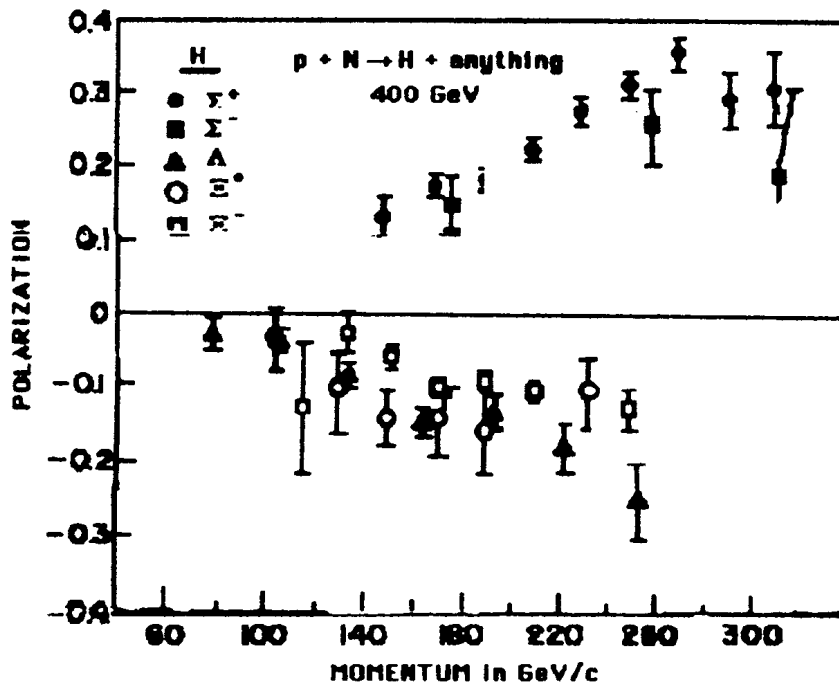
The Wacky World of Hyperon Polarization

Unpolarized beams on unpolarized targets produce hyperons which are strongly polarized!

... direction is $\hat{n} = \mathbf{p}_{\text{beam}} \times \mathbf{p}_Y$

$$d\sigma_{UUT} \sim \sin(\phi_h^l - \phi_{S_h}^l) \cdot f_1(x) D_{1T}^{\perp(1)}(z) = \text{Diagram}$$

$pN \rightarrow Y^{\uparrow} X$ data



Hyperon spin structure in CQM:

$$p \quad \Delta u = +4/3, \quad \Delta d = -1/3, \quad \Delta s = 0$$

$$\Lambda \quad \Delta s = +1, \quad \Delta u = \Delta d = 0$$

$$\Sigma^{\pm} \quad \Delta s = -1/3, \quad \Delta u, d = +4/3$$

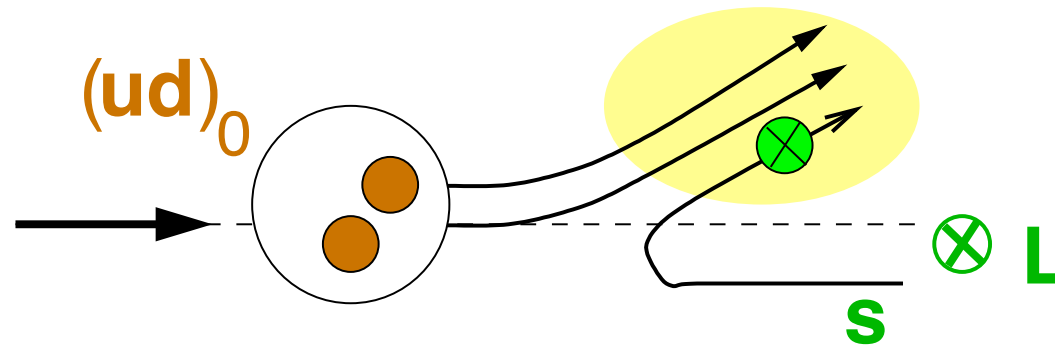
$$\Xi^{\pm} \quad \Delta s = +4/3, \quad \Delta u, d = -1/3$$

\Rightarrow **sign of polarization is opposite to Δs ...**

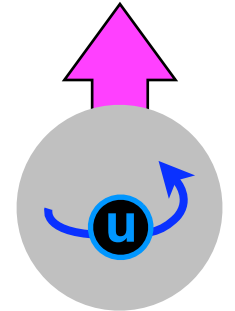
Thomas Precession & the DGM Model

Thomas precession: relativistic effect due [boost, rotation] $\neq 0$...
 → ‘**spin-orbit**’ pseudo-force that **aligns** L and S of **accelerating particle**

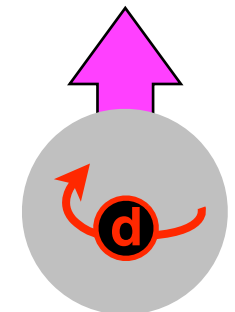
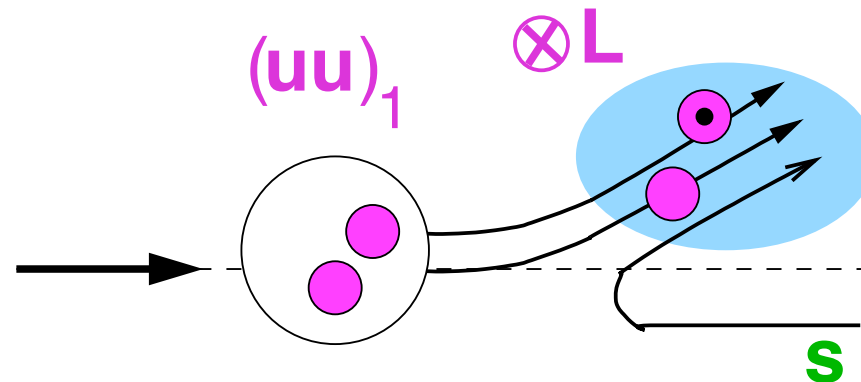
Λ : $\Delta s = +1$ P_Λ from accelerated sea s quark



relevant?



Σ^+ : $\Delta u = +4/3$ P_Σ from accelerated valence $(uu)_1$ diquark



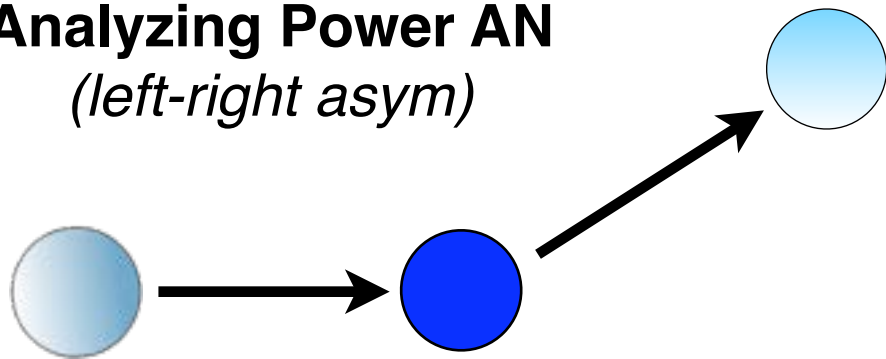
DGM model did pretty well

Non-Relativistic SSA's:
Any lessons?

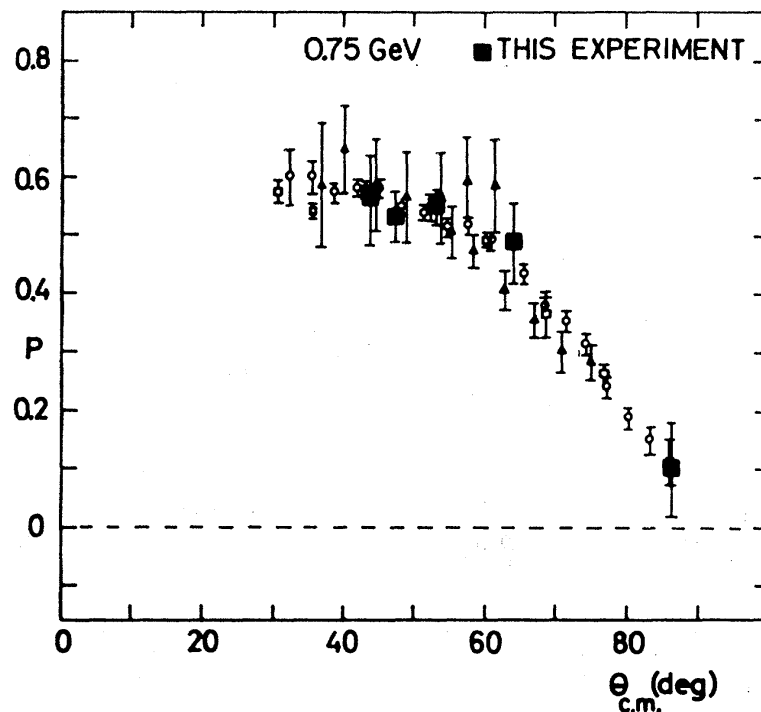
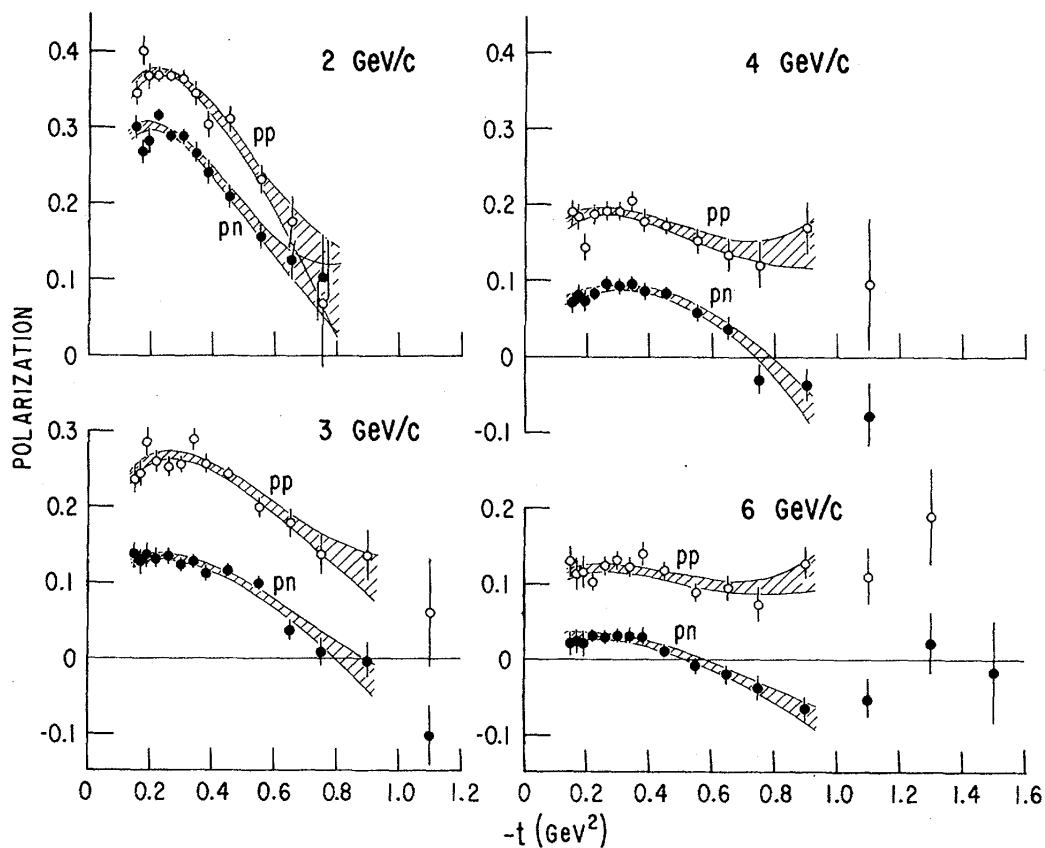
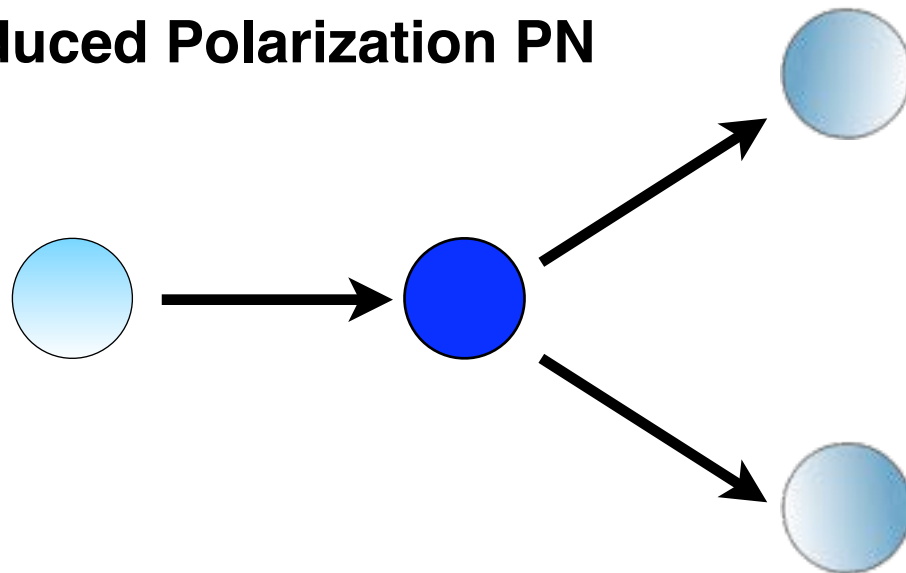
Well-known effects!

SSA's in Low-energy Elastic pp Scattering

Analyzing Power AN
(left-right asym)

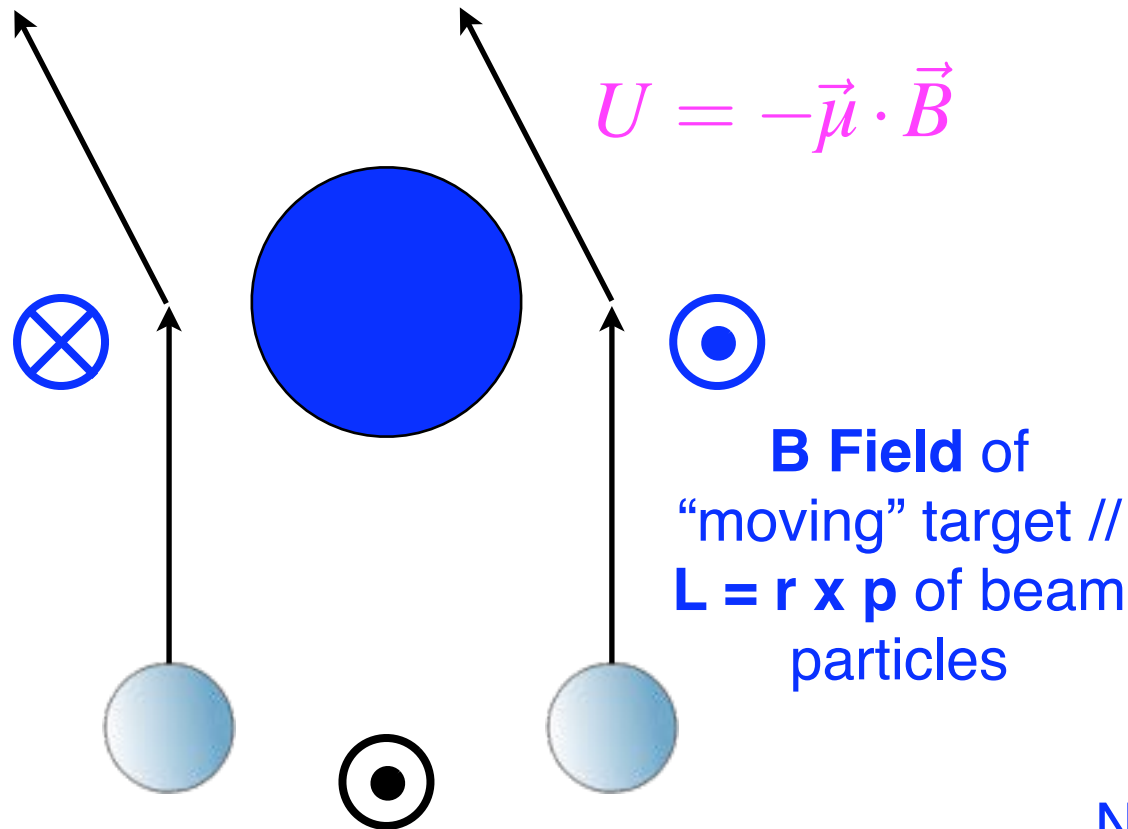


Induced Polarization PN



The Spin-Orbit Interaction in Good-Old E&M

particles on left / right sides
head for stronger / weaker B



Spin \mathbf{S} // Magnetic Moment
of beam polarized

Let $V(r) =$ target’s potential field,
in target rest frame.

Lorentz boost to beam frame:

$$\vec{B}' = -\gamma \frac{\vec{v}}{c^2} \times \vec{E} = \frac{\vec{p}}{mc^2} \times \frac{\vec{r} dV}{r dr}$$

Using $\vec{r} \times \vec{p} = \vec{l} \hbar$ and

$$U = -\vec{\mu} \cdot \vec{B}' \sim -\vec{s} \cdot \vec{B}'$$

➔ **spin-orbit interaction**

$$U_{s-o} = \frac{\text{const}}{r} \frac{dV}{dr} \vec{s} \cdot \vec{l}$$

Note: The **origin** of the underlying
potential $V(r)$ doesn’t matter!

➔ the result follows from **relativity**

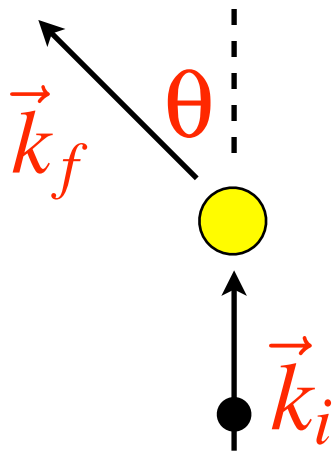
Spin-Orbit Interaction: Nuclear Force

The **strong interaction** between nucleons is **short-range** ...
 can approximate as a **contact interaction** (unlike E&M!)

With $\rho(r)$ = target density,

$$U_{s-o} \sim \frac{dV}{dr} \vec{s} \cdot \vec{l} \sim \frac{d\rho}{dr} \vec{s} \cdot \vec{l}$$

nuclear s-o interaction
 active at **target surfaces**

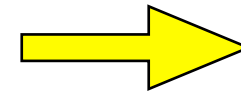


Let's calculate! Non-relativistic scattering:

$$\psi = e^{ikz} + f(\theta) \frac{e^{ikr}}{r}$$

INCOMING
PLANE WAVE

OUTGOING
SPHERICAL WAVE



Cross-section:

$$\frac{d\sigma}{d\theta} = |f(\theta)|^2$$

Short-range Born approximation:

$$f(\theta) = -\frac{\mu}{2\pi\hbar^2} \int e^{i(\vec{k}_i - \vec{k}_f) \cdot \vec{r}'} V(r') d^3r'$$

Angular pattern of scatt amplitude
 ➔ **Fourier transform** of target V

Spin-Orbit Interaction: Nuclear Force

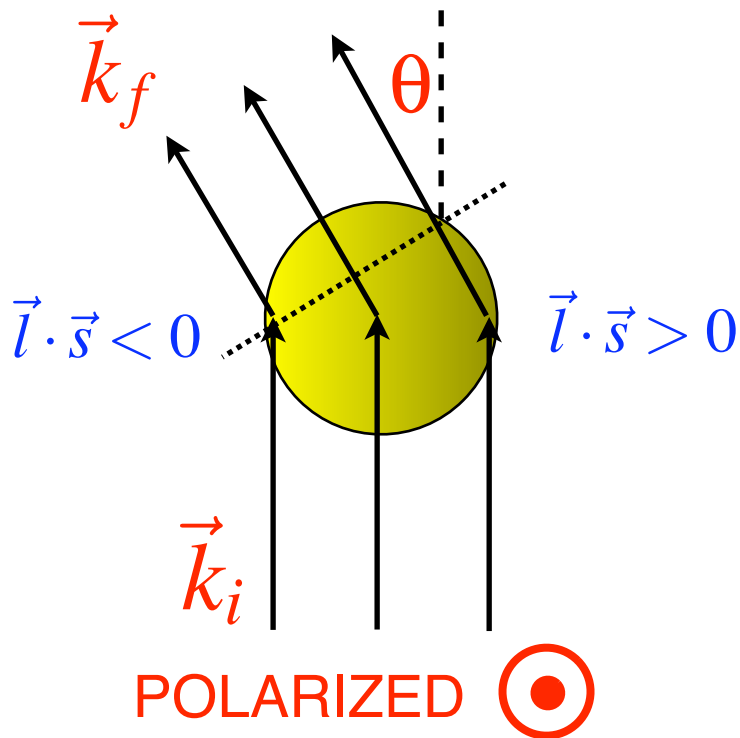
Now for a **polarized proton beam!**

.....

$$\begin{aligned} \psi_{\text{scat}} &\sim (U_1 + iU_2)e^{ikr} - D_{s-o}e^{ik(r-R\theta)} + D_{s-o}e^{ik(r+R\theta)} \\ &= (U_1 + iU_2 + 2iD_{s-o}\sin k\theta R)e^{ikr} \end{aligned}$$

Analyzing power
→ $\sin(\theta)$ term in xsec

$$\begin{aligned} \Rightarrow \frac{d\sigma}{d\Omega} &\sim |\psi_{\text{scat}}|^2 \sim U_1^2 + U_2^2 + 4D_{s-o}^2 \sin^2 k\theta R \\ &\quad + 4U_2 D_{s-o} \sin k\theta R \end{aligned}$$



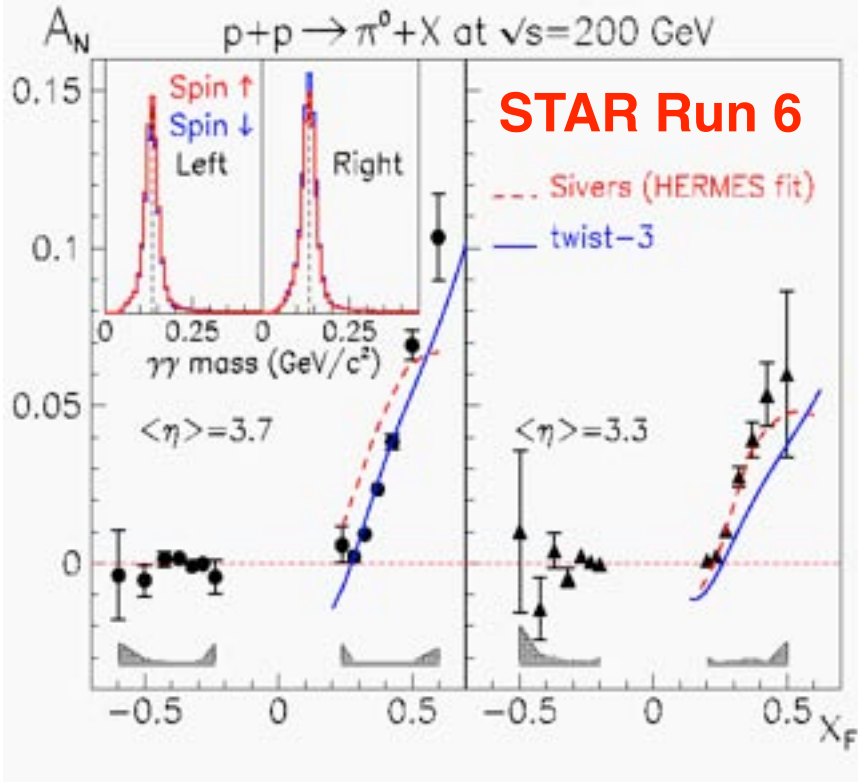
Single-spin asym in $p^\uparrow p \rightarrow pp$ involves:

- **Interference:** between an **imaginary, spin-independent** term U_2 in volume potential and a **spin-dependent** spin-orbit term D_{s-o}
- **Surfaces:** where target density has a gradient → target with structure

SSA's at high-energies

Large SSAs persist at very high RHIC energies

T-odd observables

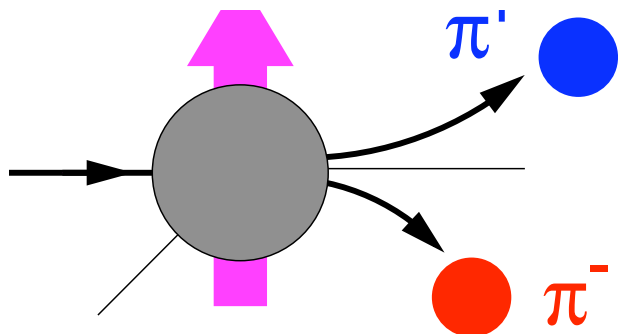


SSA observables $\sim \vec{J} \cdot (\vec{p}_1 \times \vec{p}_2)$
 \Rightarrow **odd** under naive **time-reversal**

Since QCD amplitudes are T-even, must arise from **interference** between **spin-flip** and non-flip amplitudes with **different phases**

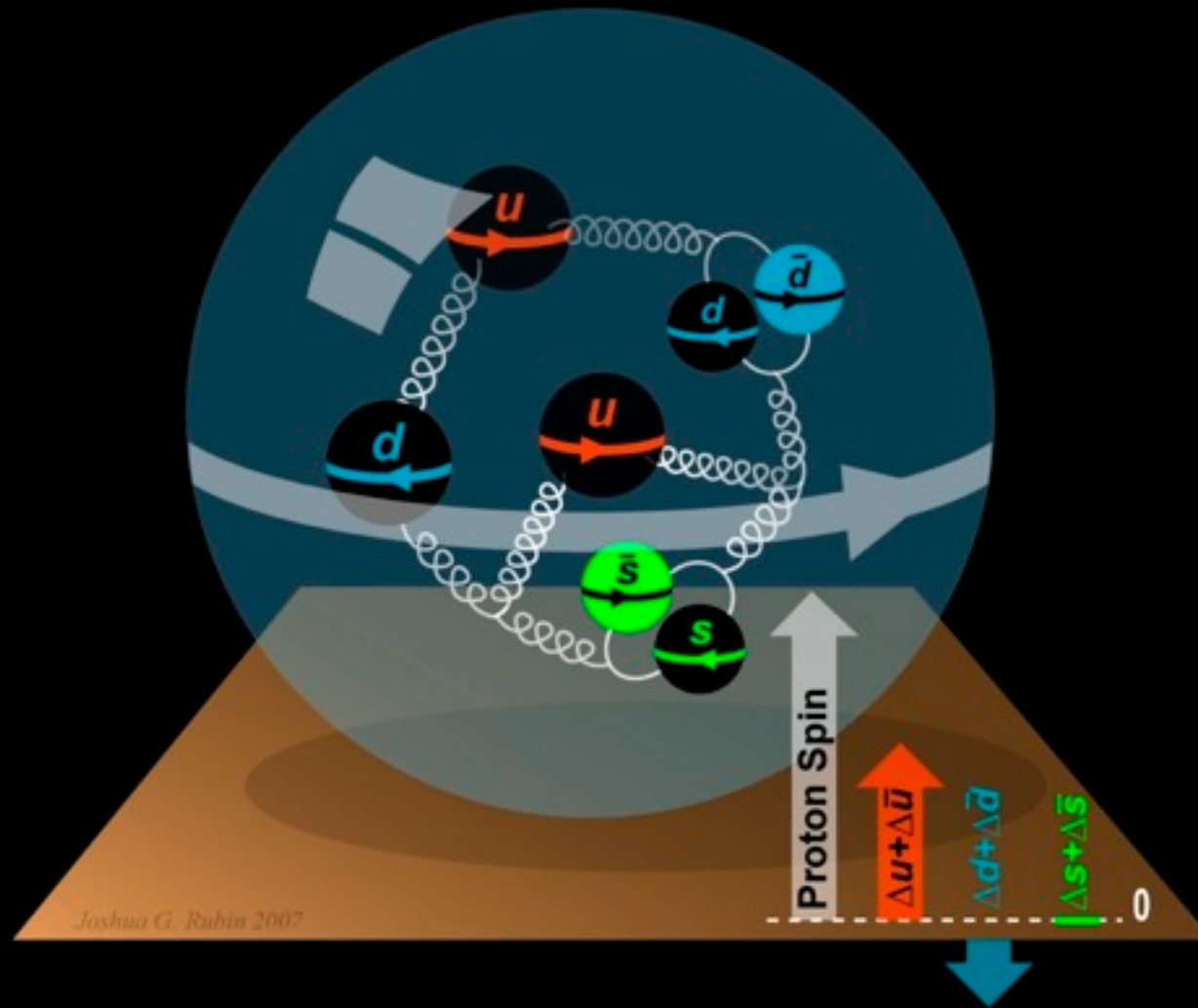
Can't come from perturbative subprocess:

- q helicity flip suppressed by m_q/\sqrt{s}
- need α_s -suppressed loop-diagram to generate necessary phase



At hard (enough) scales, SSA's must arise from soft physics: T-odd distribution / fragmentation functions

Models: seeking an intuitive picture



Joshua G. Rubin 2007

Flavor Structure of the Proton

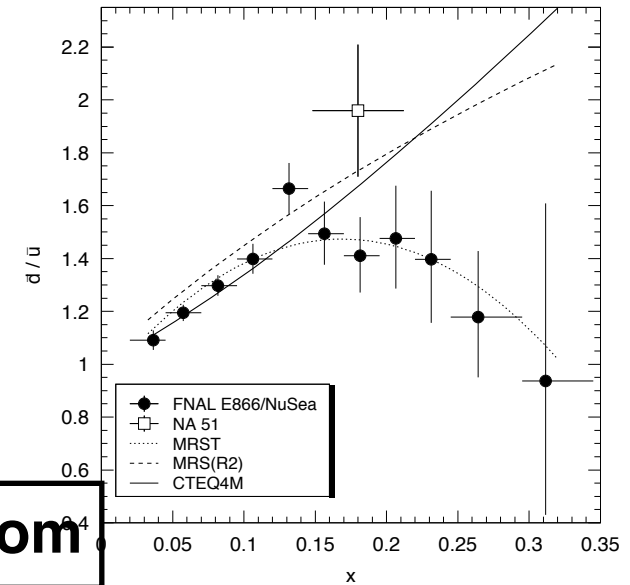
E866: $\bar{d}/\bar{u} > 1$

Constituent Quark Model

Pure valence description: proton = $2u + d$

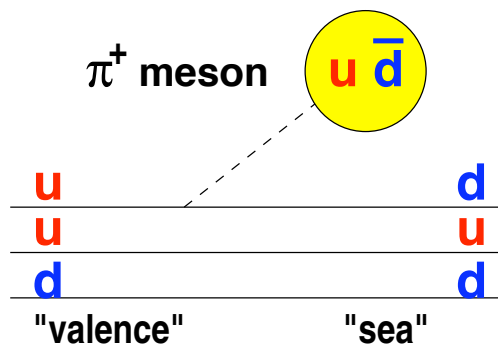
Perturbative Sea Sea quark pairs from $g \rightarrow q\bar{q}$ should be flavor symmetric:

$$\bar{u} = \bar{d}$$



Non-perturbative models: alternate deg's of freedom

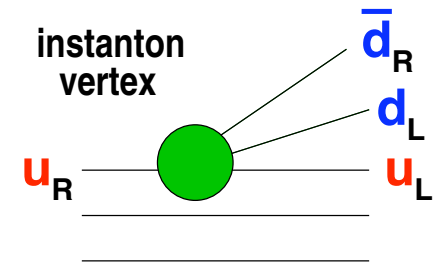
Meson Cloud Models



Quark sea from cloud of 0^- mesons: $\bar{d} > \bar{u}$

Chiral-Quark Soliton Model

- quark degrees of freedom in a pion mean-field
- nucleon = chiral soliton
- one parameter: dynamically-generated quark mass
- expand in $1/N_c$



'tHooft instanton vertex

$$\sim \bar{u}_R u_L \bar{d}_R d_L$$

$$\bar{d} > \bar{u}$$

Spin of the Sea Quarks

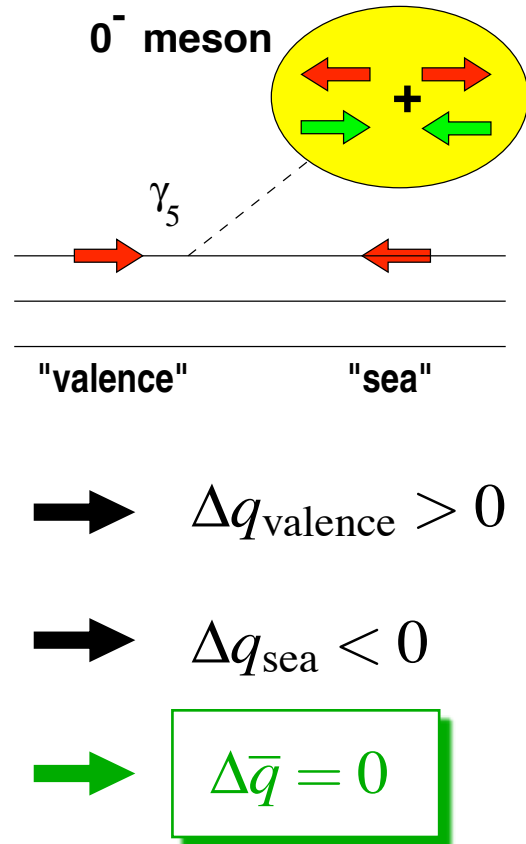
Constituent Quark Model

$$\Delta u = +\frac{4}{3}, \quad \Delta d = -\frac{1}{3}$$

$$\Delta q \equiv N^\uparrow - N^\downarrow$$

Meson Cloud Models

Li, Cheng, hep-ph/9709293



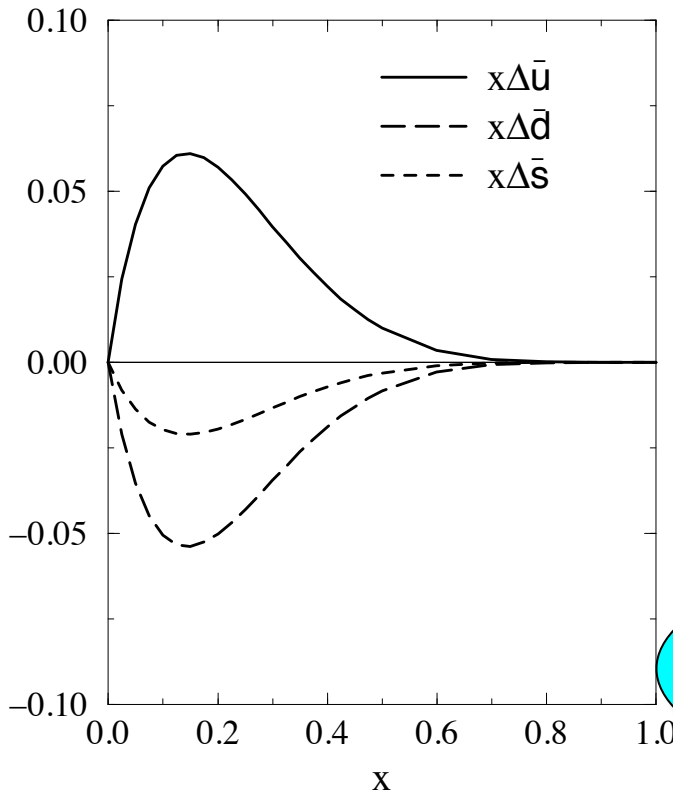
“Higher-order” cloud of vector mesons can generate a small polarization.

Chiral-Quark Soliton Model

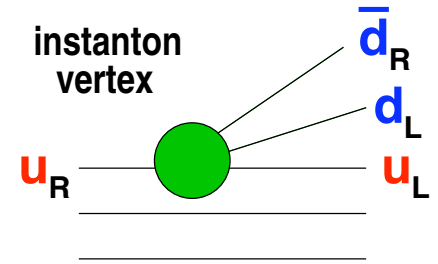
Light sea quarks polarized:

$$\Delta \bar{u} \simeq -\Delta \bar{d} > 0$$

Goeke et al, hep-ph/0003324



Instanton Mechanism

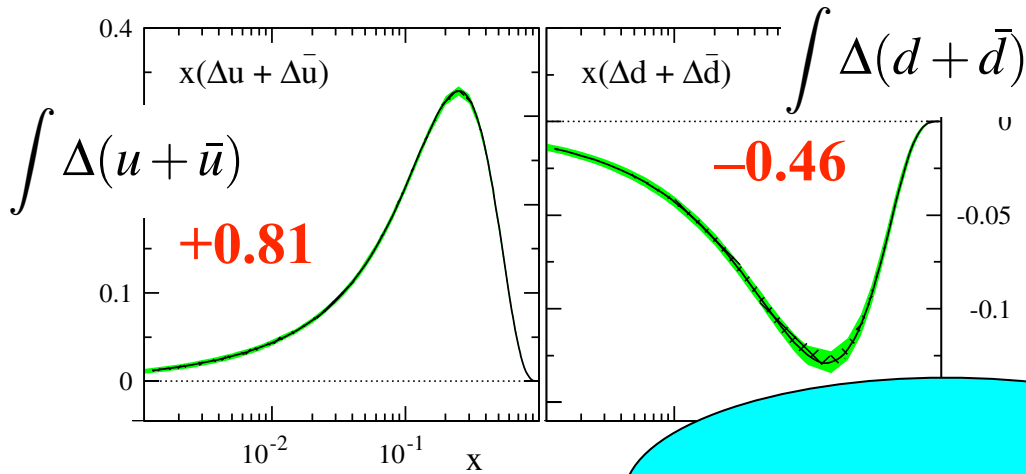


‘tHooft instanton vertex $\sim \bar{u}_R u_L \bar{d}_R d_L$ transfers helicity from valence u quarks to $d\bar{d}$ pairs

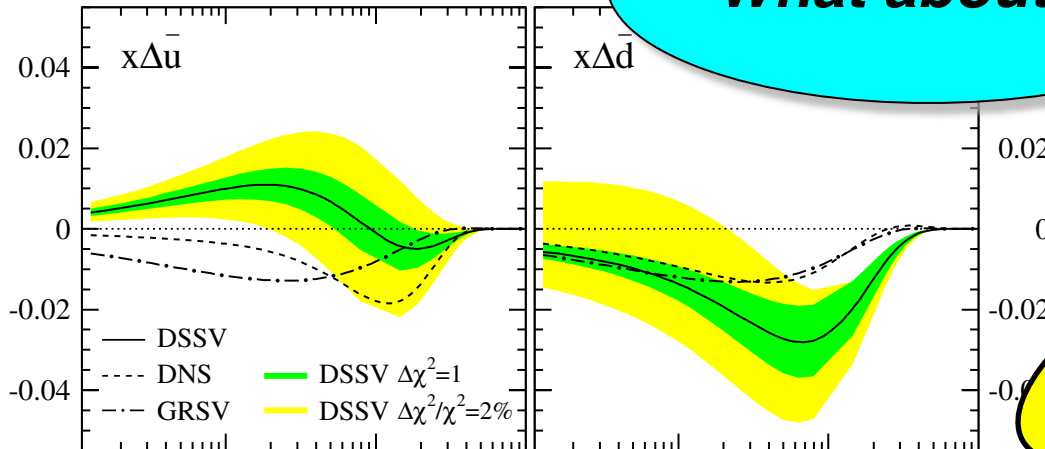
What about gluon spin?

DSSV NLO global fit: Δq & Δg

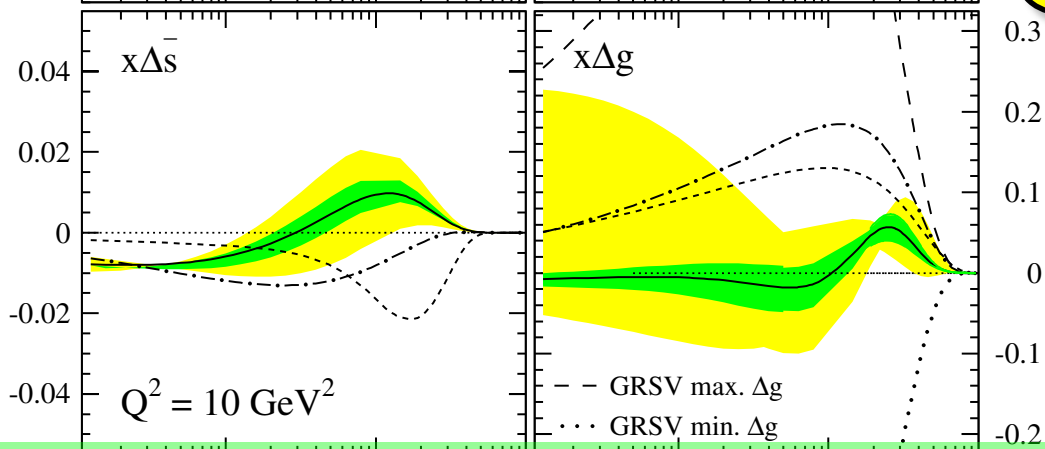
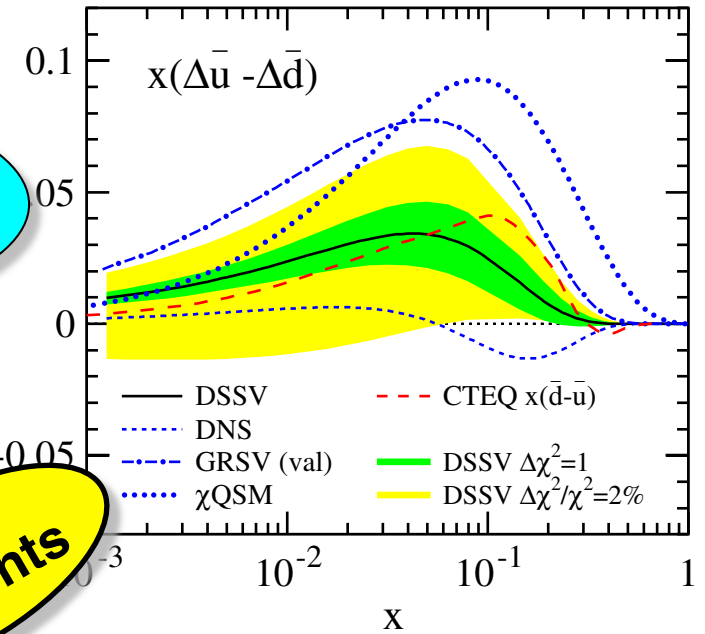
DeFlorian, Sassot, Stratmann, Vogelsang,
PRL 101 (2008) 071001, PRD 80 (2009) 034030



What about \underline{L} ?



1st moments

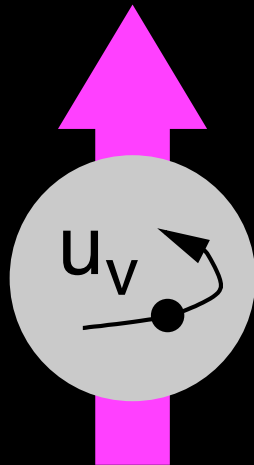
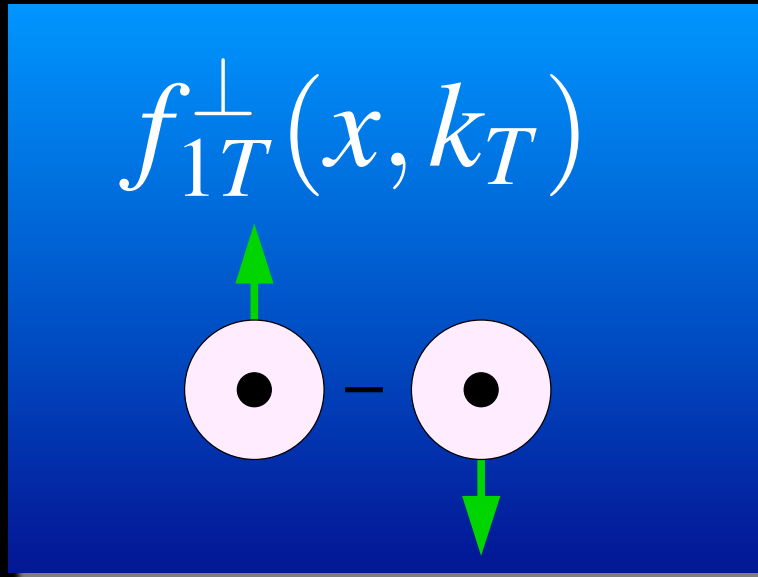


gluons & sea: spin-polarizations
all negative-ish zeros

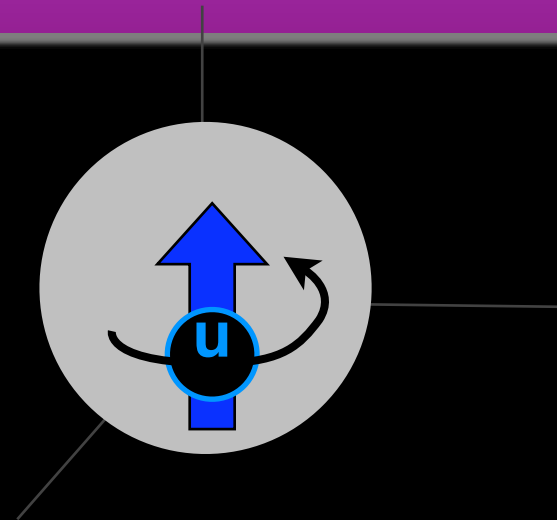
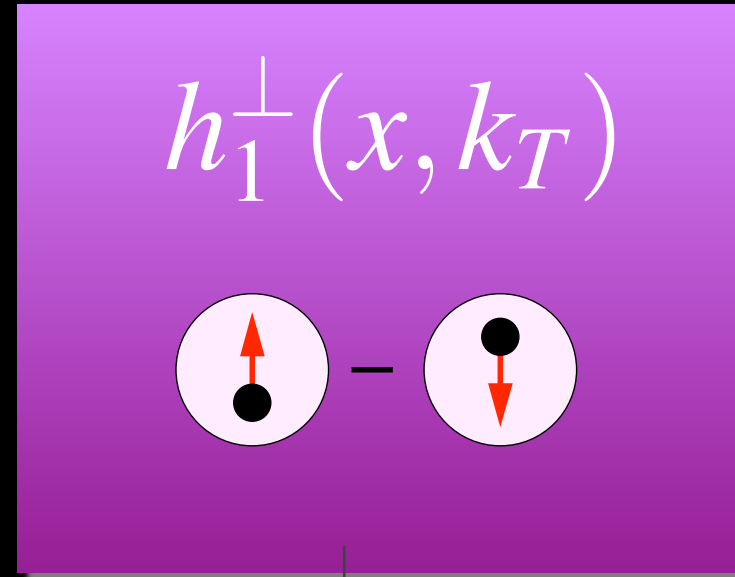
	meas: $x > .001$	extrap: all x	error
$\Delta\Sigma$	0.37	0.24	+0.04 -0.06
$\Delta\bar{u}$	0.03	0.04	± 0.06
$\Delta\bar{d}$	-0.09	-0.12	± 0.09
Δs	-0.01	-0.06	± 0.03
ΔG	0.01	-0.08	+0.7 -0.3

Models: a tantalizing strawman for L

Sivers



Boer-Mulders





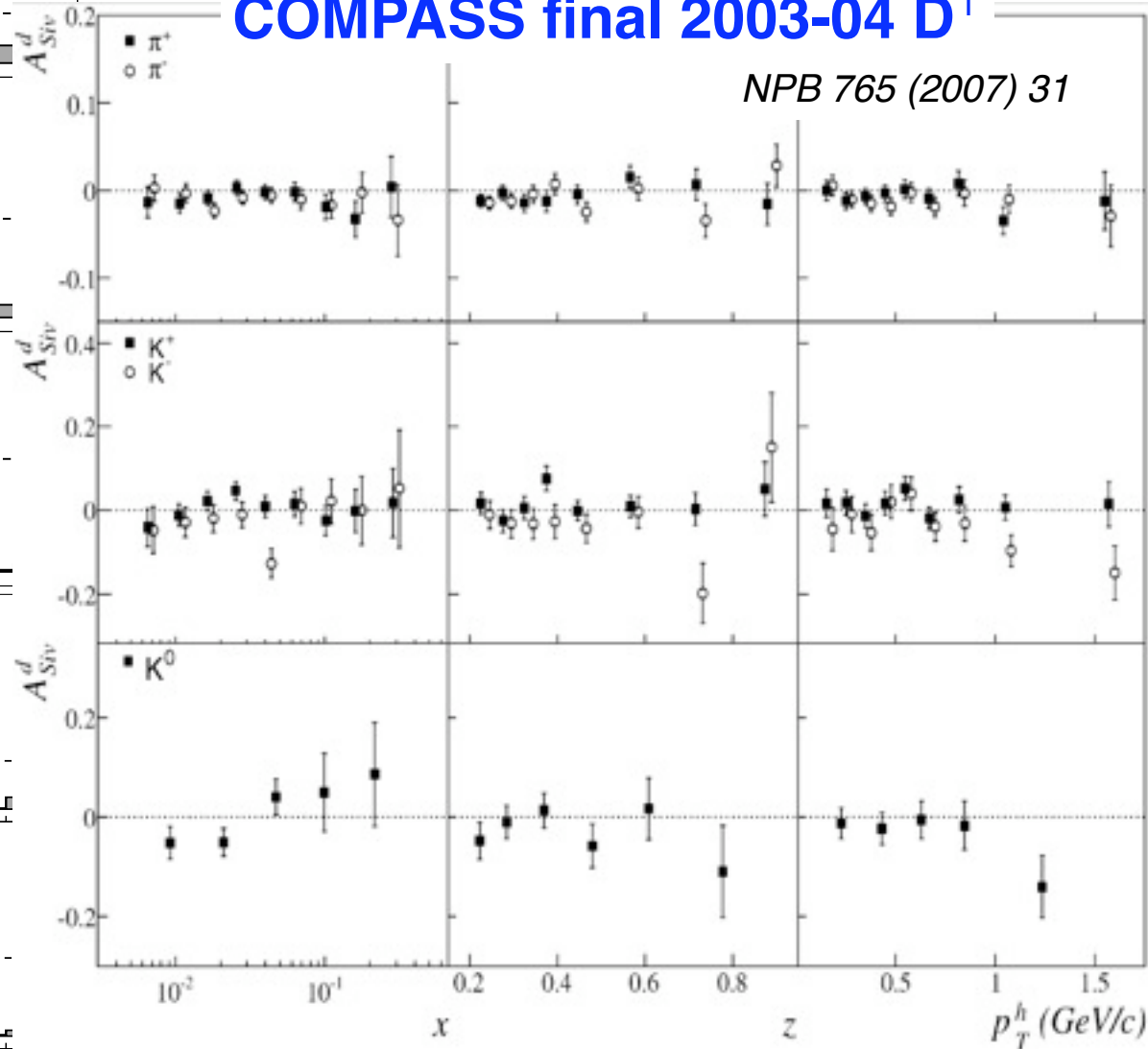
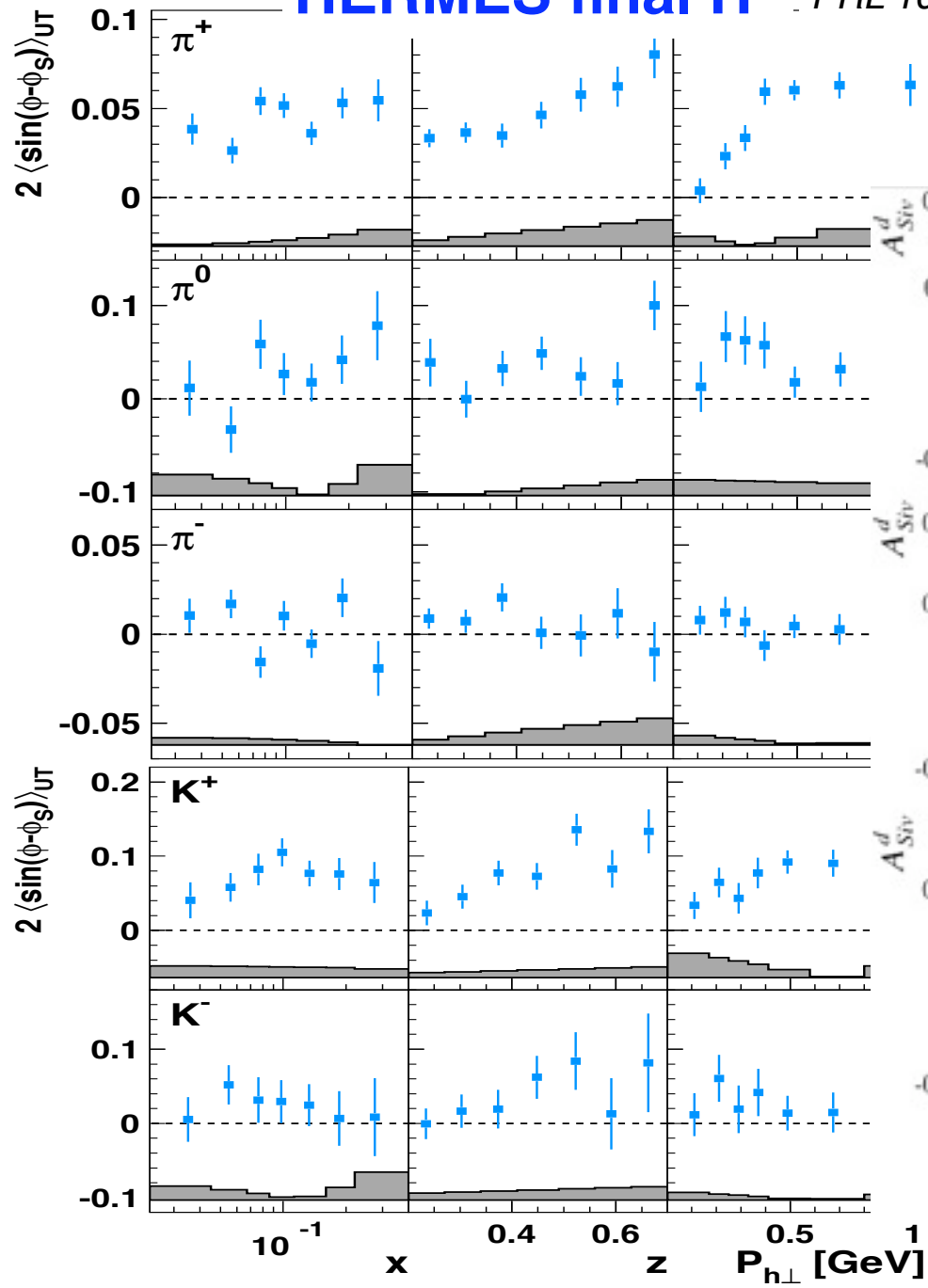
Sivers Moments for π and K from H^\uparrow & D^\uparrow

HERMES final H^\uparrow PRL 103 (2009)

$$f_{1T}^\perp(x, k_T) \otimes D_1^\perp(z)$$



COMPASS final 2003-04 D^\uparrow





Global Fit to Sivvers Asymmetries

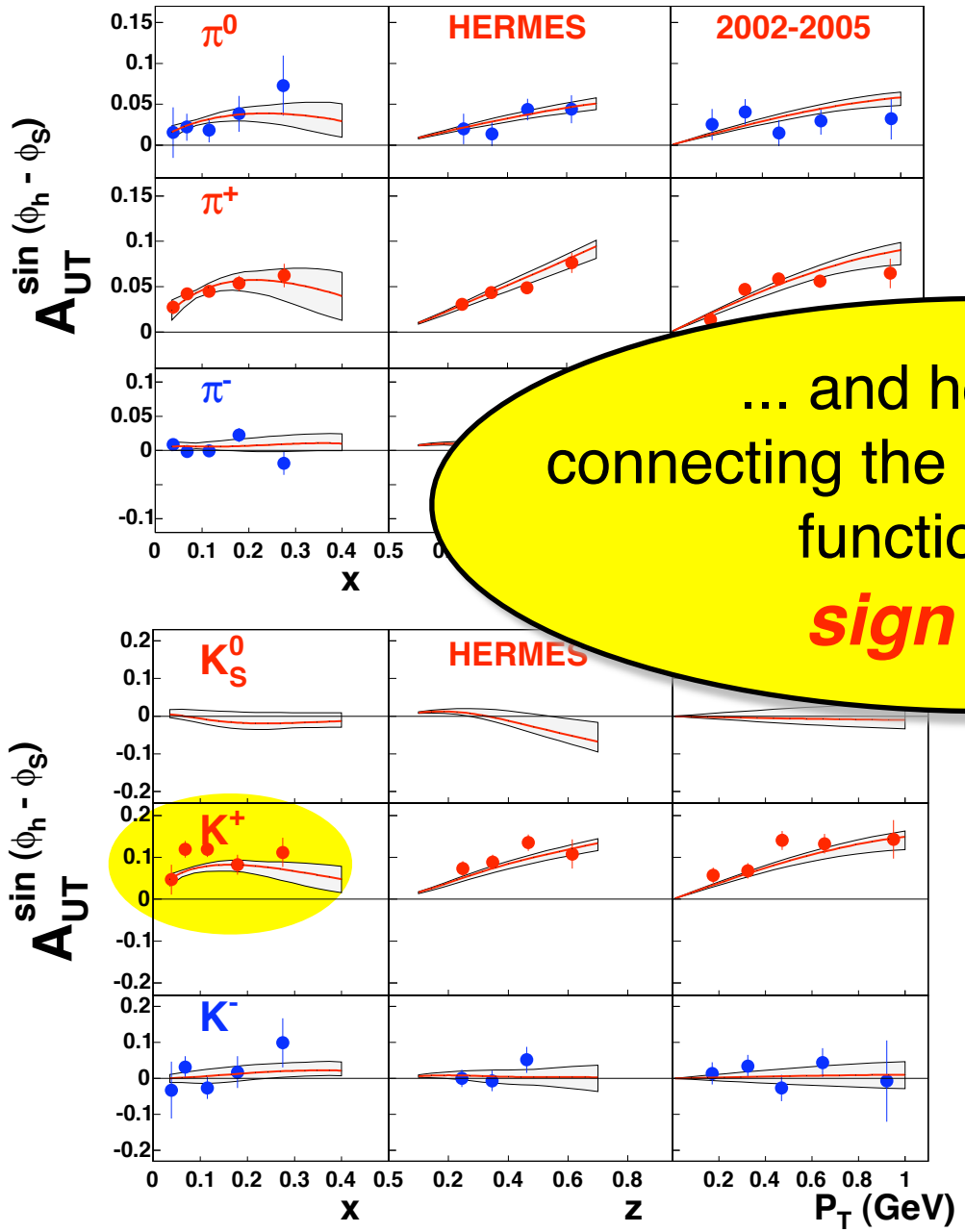
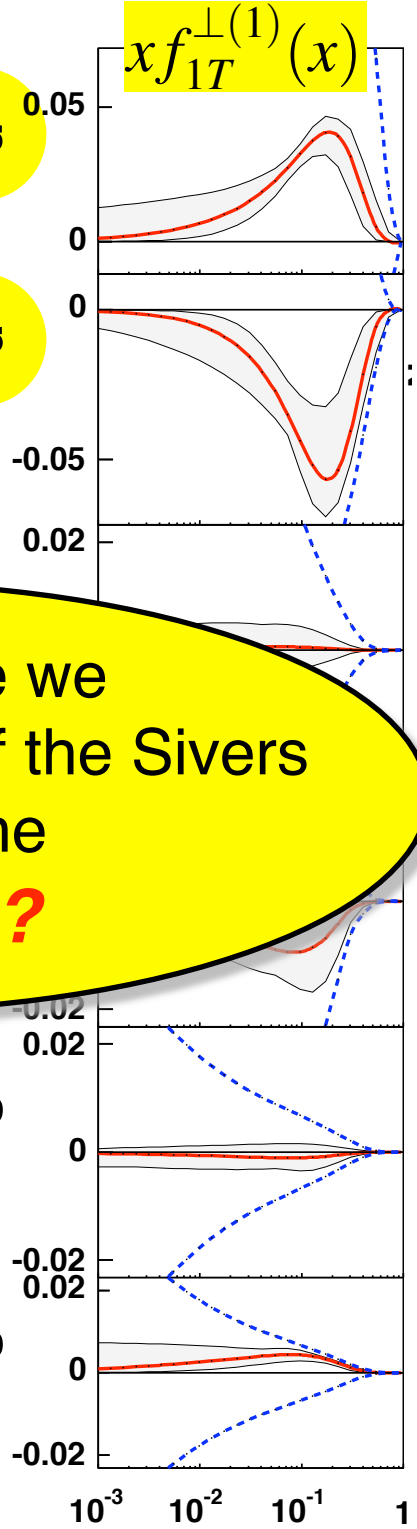


E. Boglione,
Transversity2008

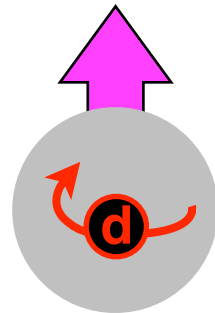
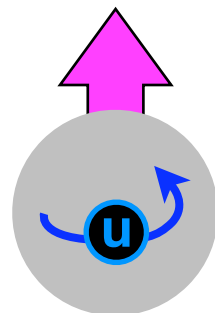
Anselmino et al,
arXiv:0805.2677

u

d



... and how are we connecting the sign of the Sivvers function to the *sign of L_q* ?



antiquark orbital $L \neq 0$ favoured

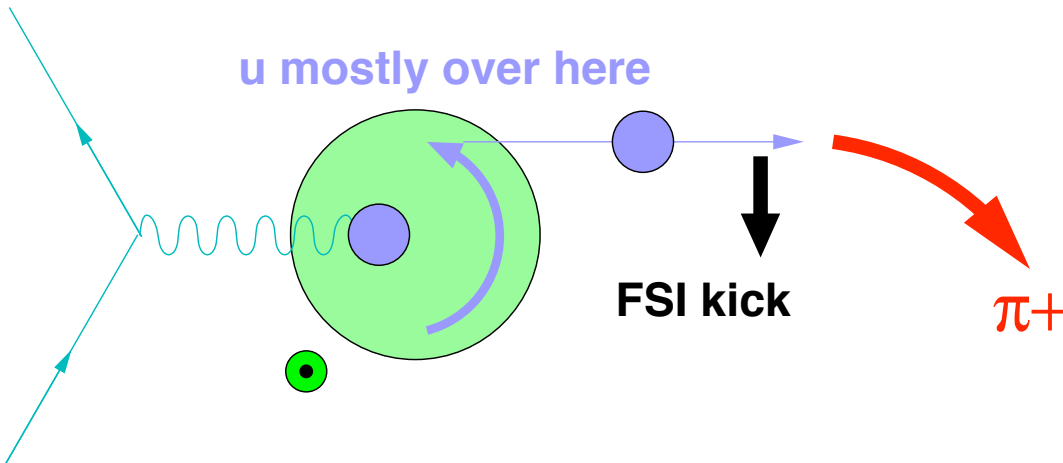
Phenomenology: Sivers Mechanism

Assuming
 $L_u > 0$

Why?

M. Burkardt: Chromodynamic lensing

Electromagnetic coupling $\sim (J_0 + J_3)$ **stronger for *oncoming* quarks**



We observe $\langle \sin(\phi_h^l - \phi_S^l) \rangle_{\pi^+} > 0$
(and opposite for π^-)
 \therefore for $\phi_S^l = 0$, $\phi_h^l = \pi/2$ preferred

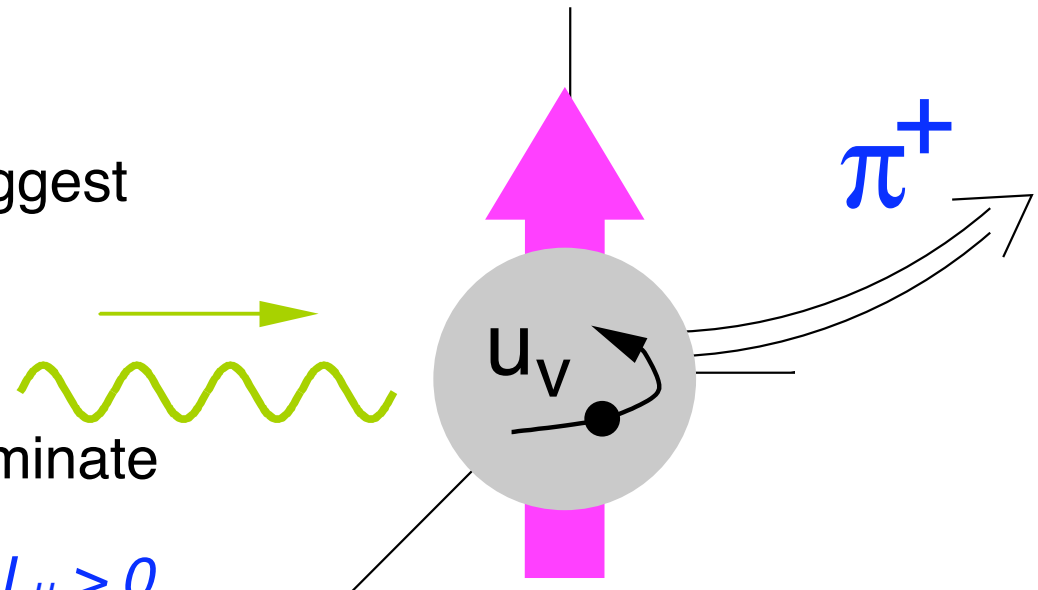
Model agrees!

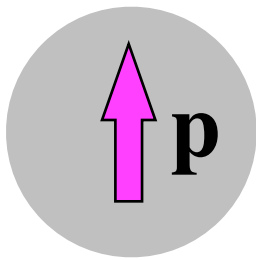
D. Sivers: Jet Shadowing

Parton energy loss considerations suggest
quenching of jets from
“near” surface of target

→ quarks from “far” surface should dominate

Opposite sign to data ... *assuming $L_u > 0$...*





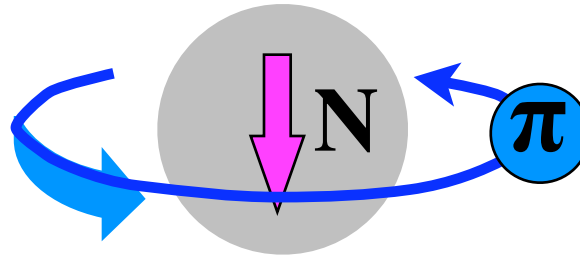
Meson Cloud on an Envelope

$|p\rangle = p + N\pi + \Delta\pi + \dots$ Pions have $J^P = 0^- = \text{negative parity} \dots$
 \rightarrow **need $L = 1$** to get proton's $J^P = 1/2^+$

$N\pi$ cloud:



$2/3 \quad n \pi^+$
 $1/3 \quad p \pi^0$

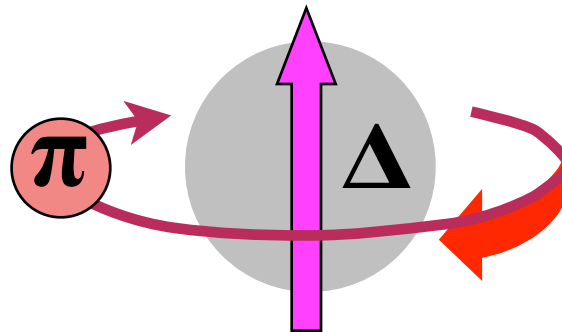


$2/3 \quad L_z = +1$
 $1/3 \quad L_z = 0$

$\Delta\pi$ cloud:



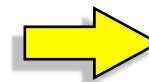
$1/2 \quad \Delta^{++} \pi^-$
 $1/3 \quad \Delta^+ \pi^0$
 $1/6 \quad \Delta^0 \pi^+$



$1/2 \quad L_z = -1$
 $1/3 \quad L_z = 0$
 $1/6 \quad L_z = +1$

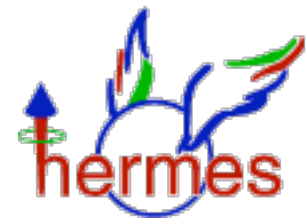
Dominant source of:

orbiting u: $n \pi^+$ with $L_z(\pi) > 0$
 orbiting d: $\Delta^{++} \pi^-$ with $L_z(\pi) < 0$

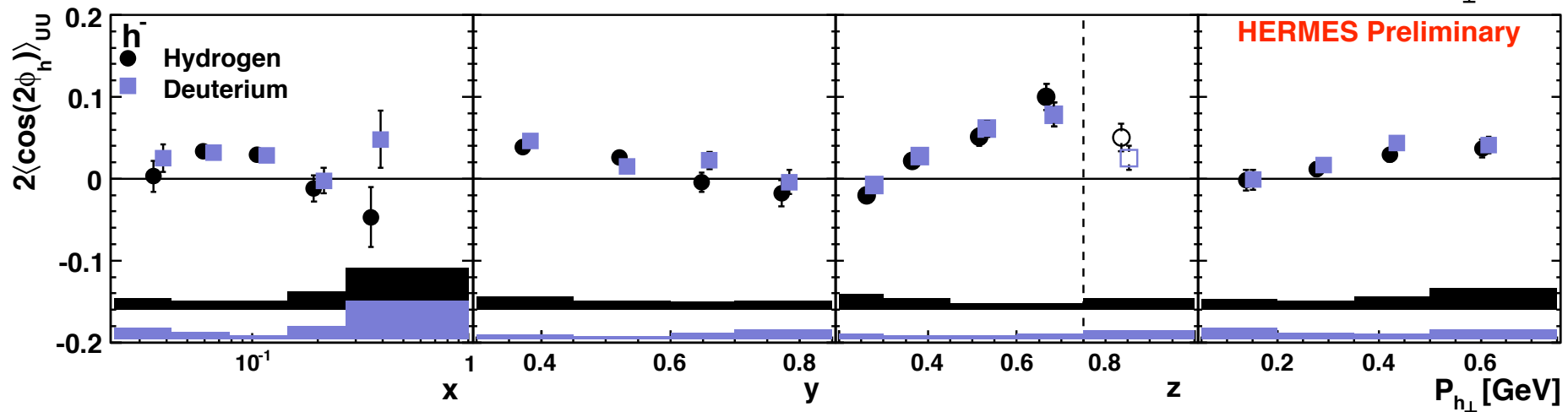
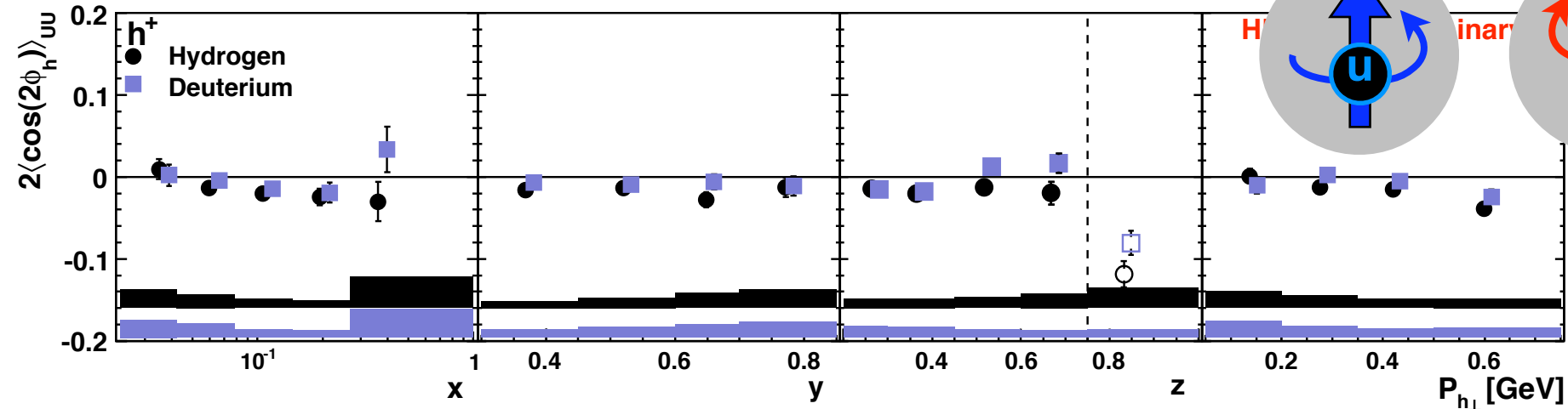


$L_u > 0$
 $L_d < 0$
 $L_{qbar} \neq 0$

Boer-Mulders: $\langle \cos(2\Phi) \rangle_{UU}$ from HERMES



$$h_1^\perp(x, k_T) \otimes H_1^\perp(z, p_T) \rightarrow \cos(2\phi) \text{ modulation}$$

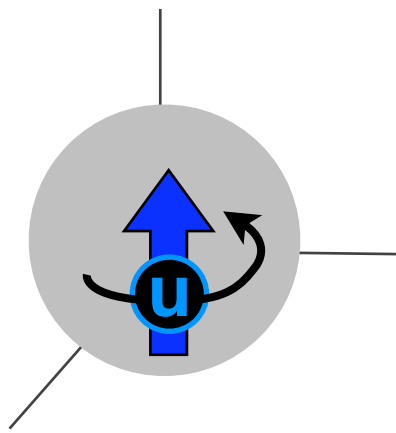


*deuterium \approx hydrogen values \rightarrow indicate **Boer-Mulders** functions of **SAME SIGN** for **up** and **down** quarks (both negative, similar magnitudes)*

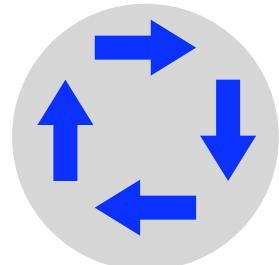
$\cos(2\Phi)$

Boer-Mulders: correlation between S_q and L_q

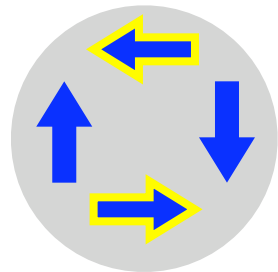
$$h_1^\perp(x, k_T) \otimes H_1^\perp(z, p_T) \rightarrow \cos(2\phi) \text{ modulation}$$



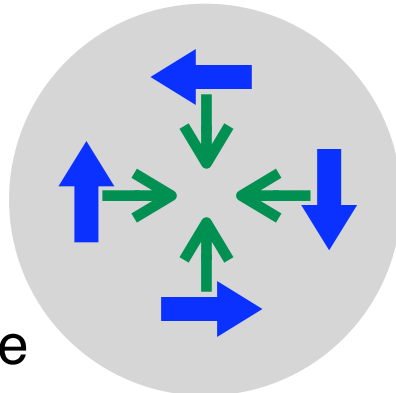
assume $S_u // L_u$



lepton plane

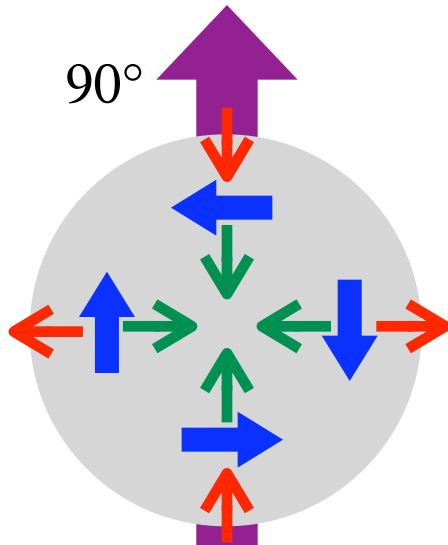


② γ^* absorbed
quark spin flip // lepton plane

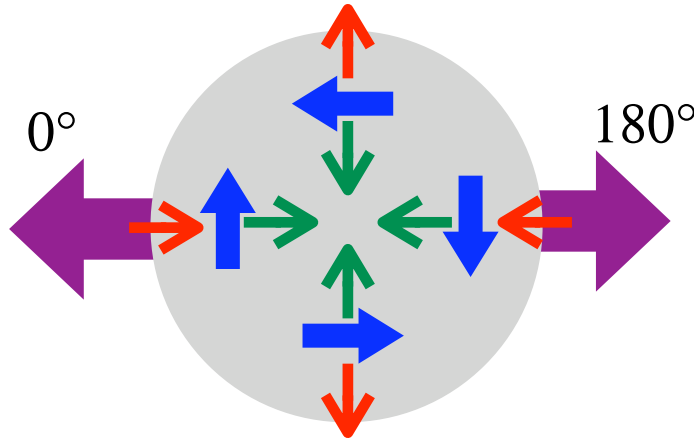


③ FSI kick
back to remnant

① oncoming quarks
scatter most ...
 h_1^\perp sets spin direc's



favoured $u \rightarrow \pi^+$
 $\langle \cos 2\phi \rangle$ negative



disfavoured $u \rightarrow \pi^-$
 $\langle \cos 2\phi \rangle$ positive

④ **Collins!**

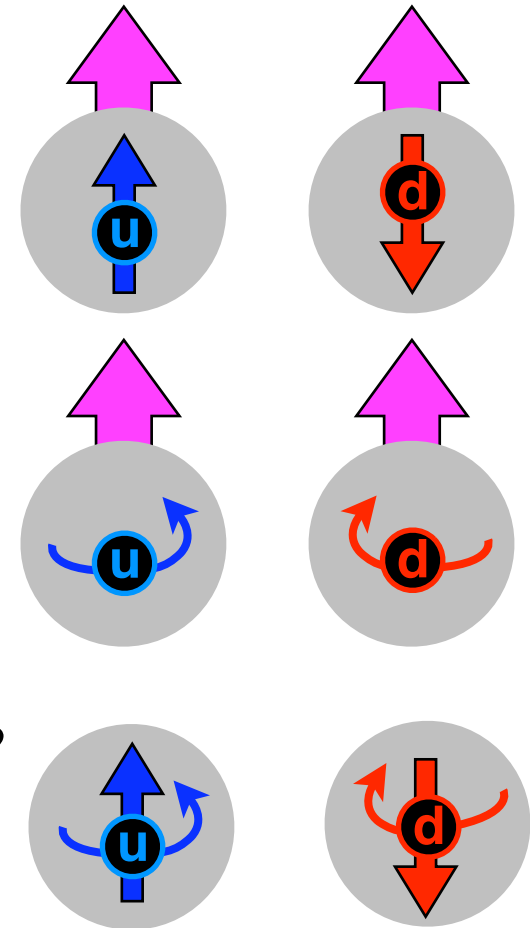
The Tantalizing Strawman

- **Transversity:** $h_{1,u} > 0$ $h_{1,d} < 0$
 → same as $g_{1,u}$ and $g_{1,d}$ in NR limit

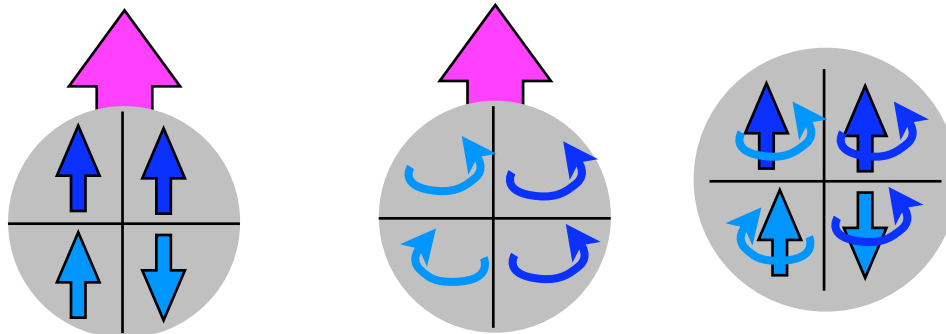
- **Sivers:** $f_{1T^\perp,u} < 0$ $f_{1T^\perp,d} > 0$
 → relatⁿ to **anomalous magnetic moment***

$f_{1T^\perp,q} \sim \kappa_q$ where $\kappa_u \approx +1.67$ $\kappa_d \approx -2.03$
 values achieve $\kappa^{p,n} = \sum_q e_q \kappa_q$ with u,d only

- **Boer-Mulders:** follows that $h_{1^\perp,u}$ and $h_{1^\perp,d} < 0$?
 → **results** on $\langle \cos(2\Phi) \rangle_{UU}$ suggest yes:



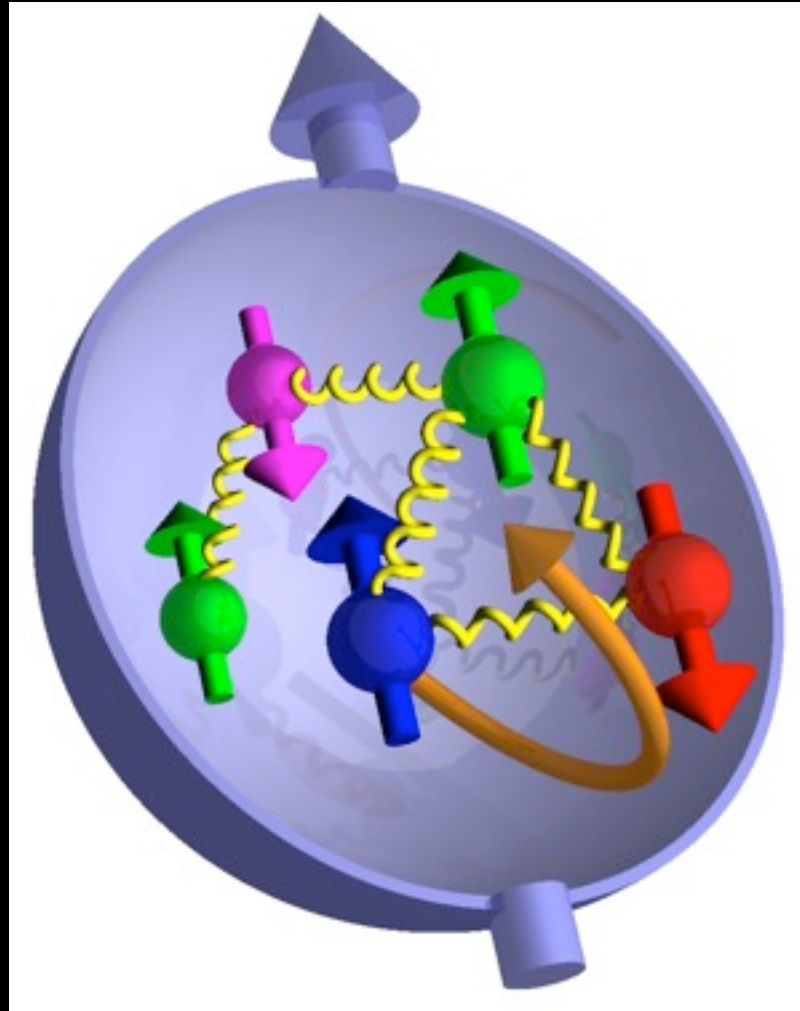
*but these
TMDs are all
independent*



$$\langle \vec{s}_u \cdot \vec{S}_p \rangle = +0.5 \quad \langle \vec{l}_u \cdot \vec{S}_p \rangle = +0.5 \quad \langle \vec{s}_u \cdot \vec{l}_u \rangle = 0$$

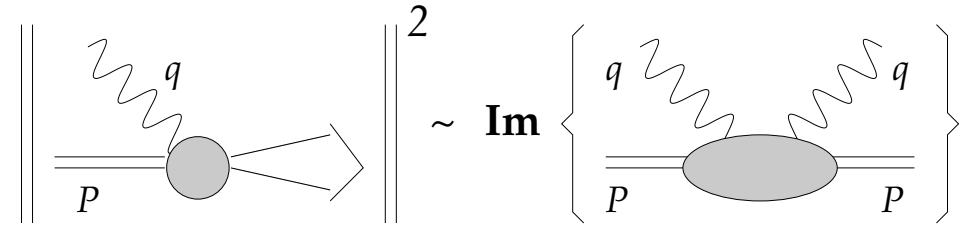
* Burkardt PRD72 (2005) 094020;
 Barone et al PRD78 (1008) 045022;

Models: can we calculate Sivers & Boer-Mulders reliably from a model wavefuncⁿ + gauge links?

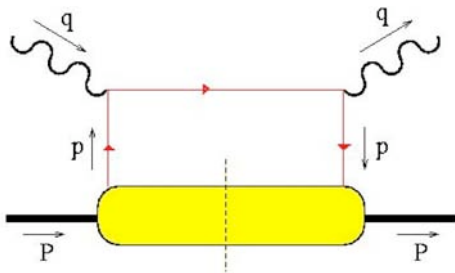


The Leading-Twist Sivers Function: Can it Exist in DIS?

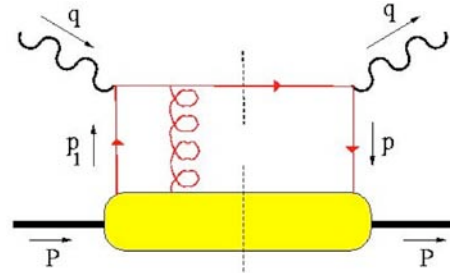
A T-odd function like f_{1T}^\perp **must** arise from **interference** ... but a distribution function is just a forward scattering amplitude, how can it contain an interference?



Brodsky, Hwang, & Schmidt 2002



can interfere with

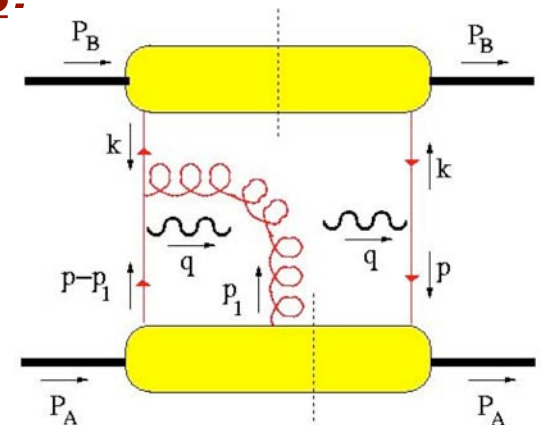


and produce a T-odd effect!
(also need $L_z \neq 0$)

It looks like higher-twist ... but no, these are soft gluons: “gauge links” required for color gauge invariance

Such soft-gluon reinteractions with the soft wavefunction are **final / initial state interactions** ... and **process-dependent** ...

e.g. **Drell-Yan**: → Sivers effect should have **opposite sign** cf. SIDIS



Modelling the T-odd dist and frag functions

Ancient slide
from 2004

Many groups now calculating these functions
via the *Brodsky-Hwang-Schmidt gauge-link*

T-Odd Distribution Functions

- **Yuan**: MIT bag model
+ 1-gluon exchange
- **Bacchetta**: quark-diquark spectator
model + 1-gluon exchange

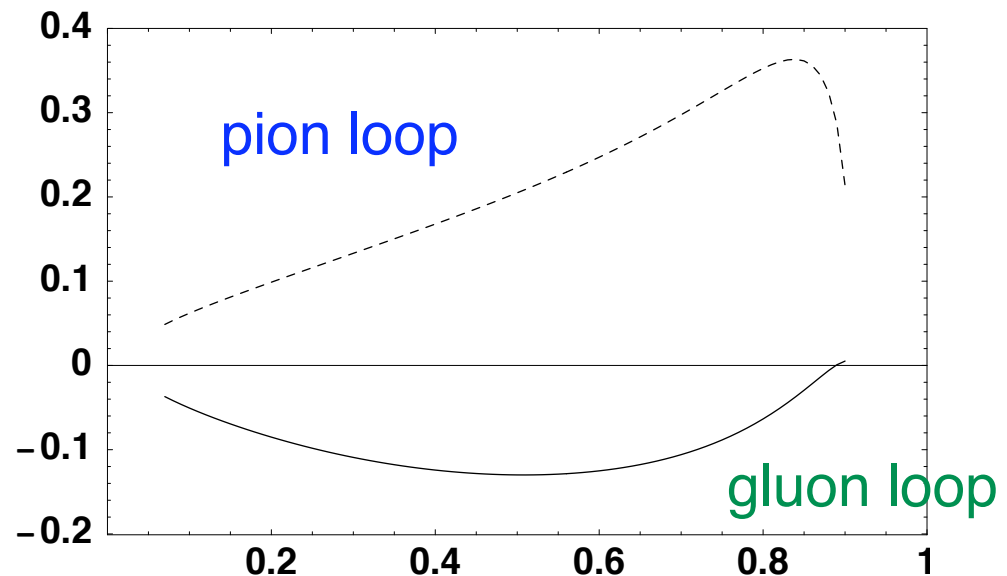
$$f_{1T}^{\perp(1)u} = -0.01 \quad f_{1T}^{\perp(1)d} = +0.003$$

$$f_{1T}^{\perp(1)u} = +0.037 \quad f_{1T}^{\perp(1)d} = -0.011$$

T-Odd Fragmentation Functions

e.g. **Metz et al**: Collins FF via
1-gluon and 1-pion exchange in
Georgi-Manohar model

$$H_1^{\perp(1/2)}(z)/D_1(z) \quad \rightarrow$$

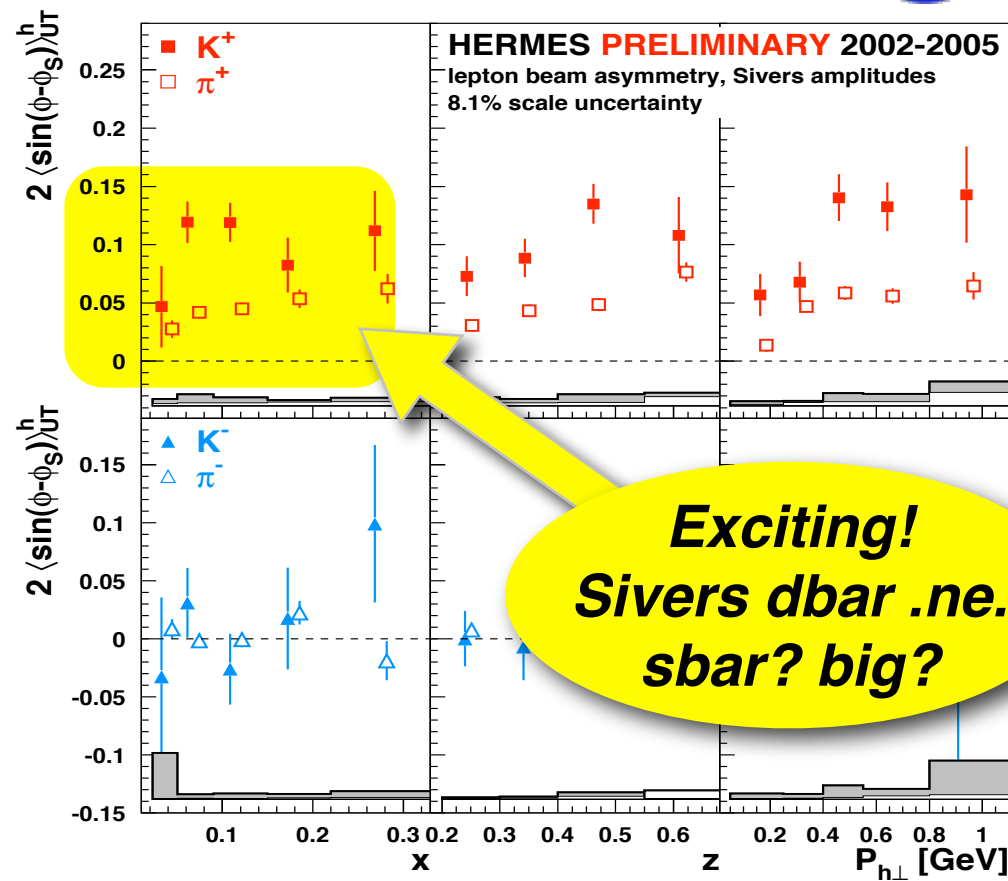
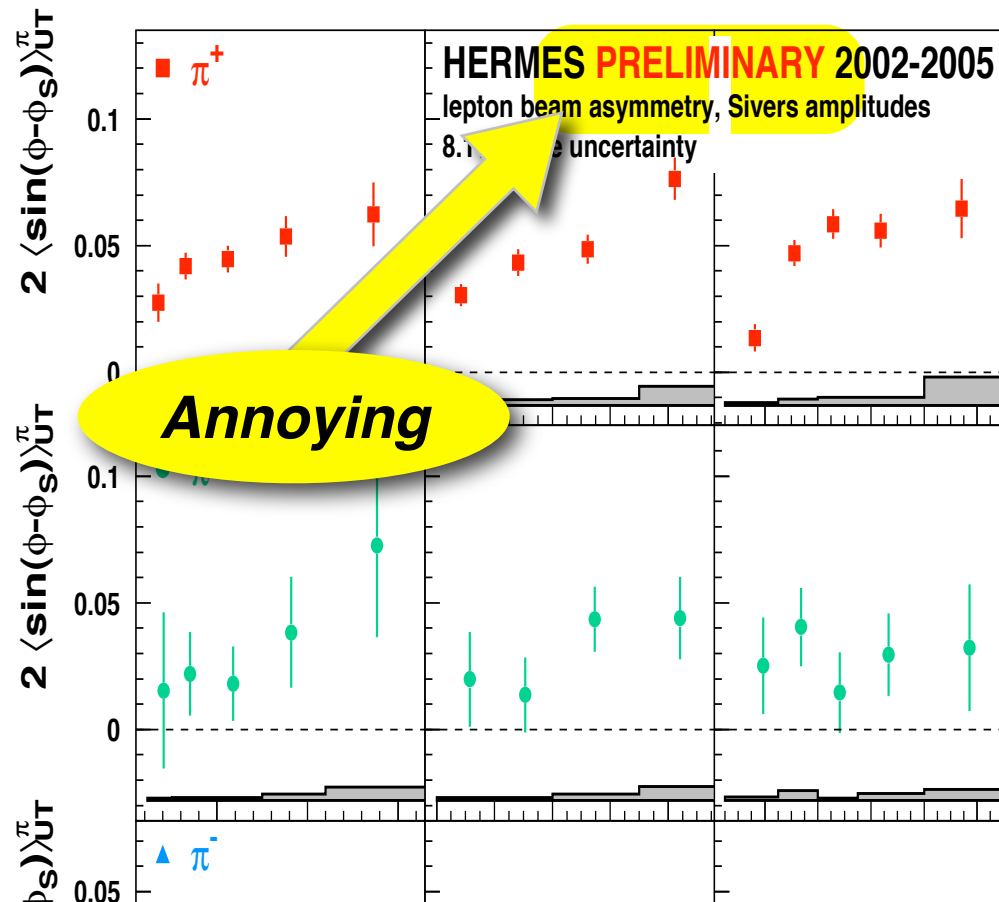
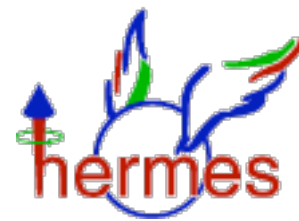


How good an approximation is one-anything exchange?

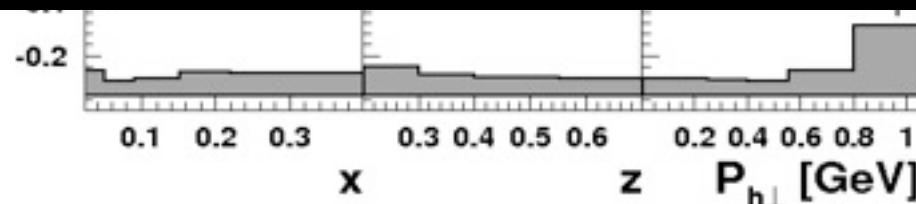
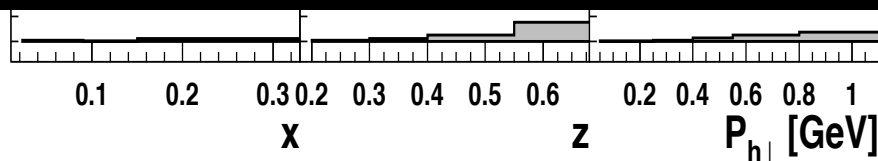
“Experimental” Issues

- The Kaon Collection
- Scale-dependence:
 - Evolution & Higher Twist
- The Missing Spin Programme

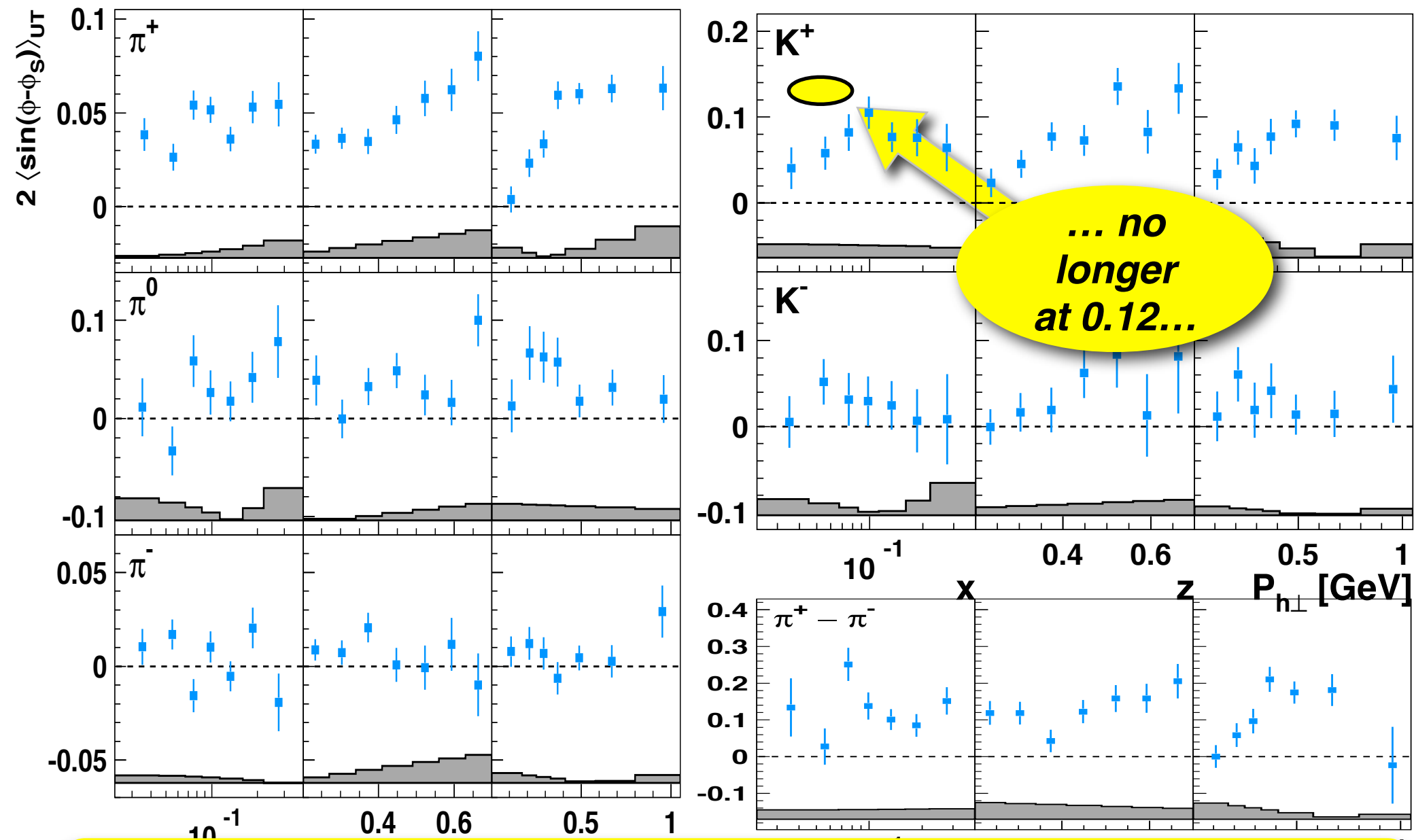
Sivers Moments for π, K from $H \uparrow$ Data



... 2.5 years of exhausting analysis later ...

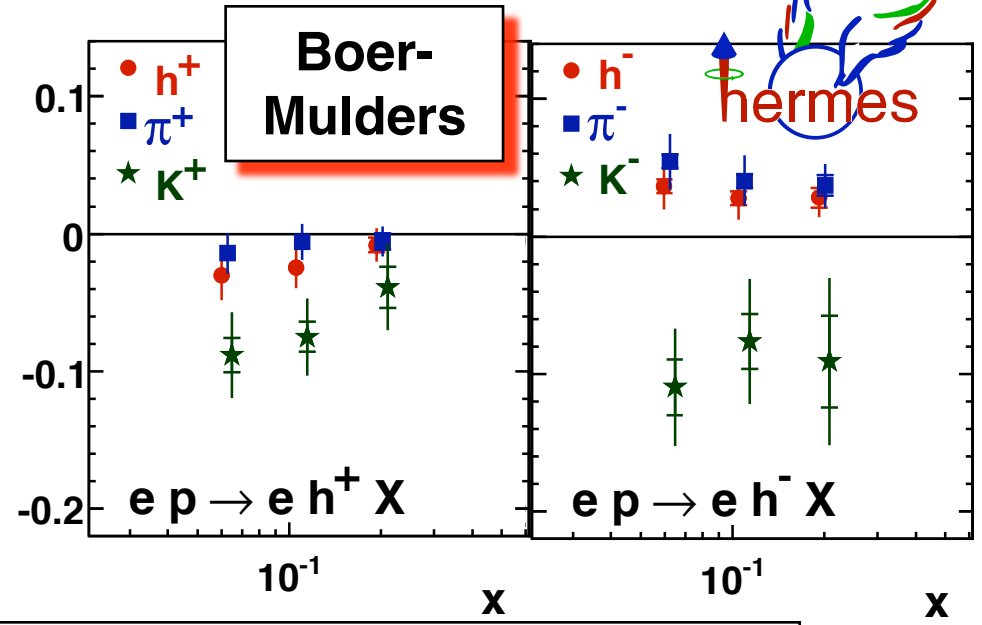
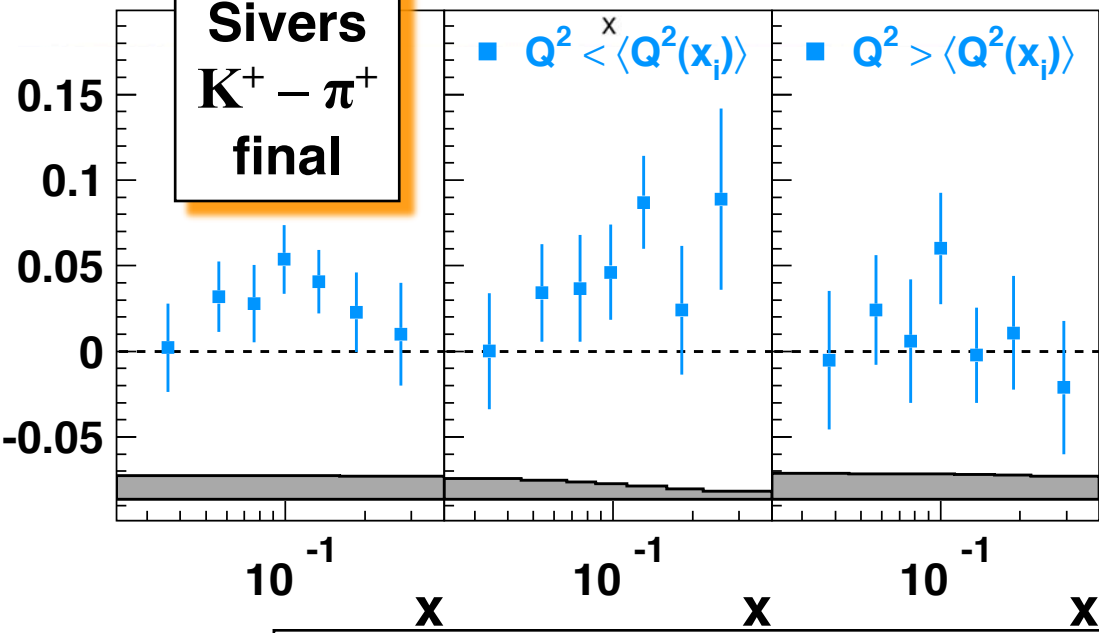
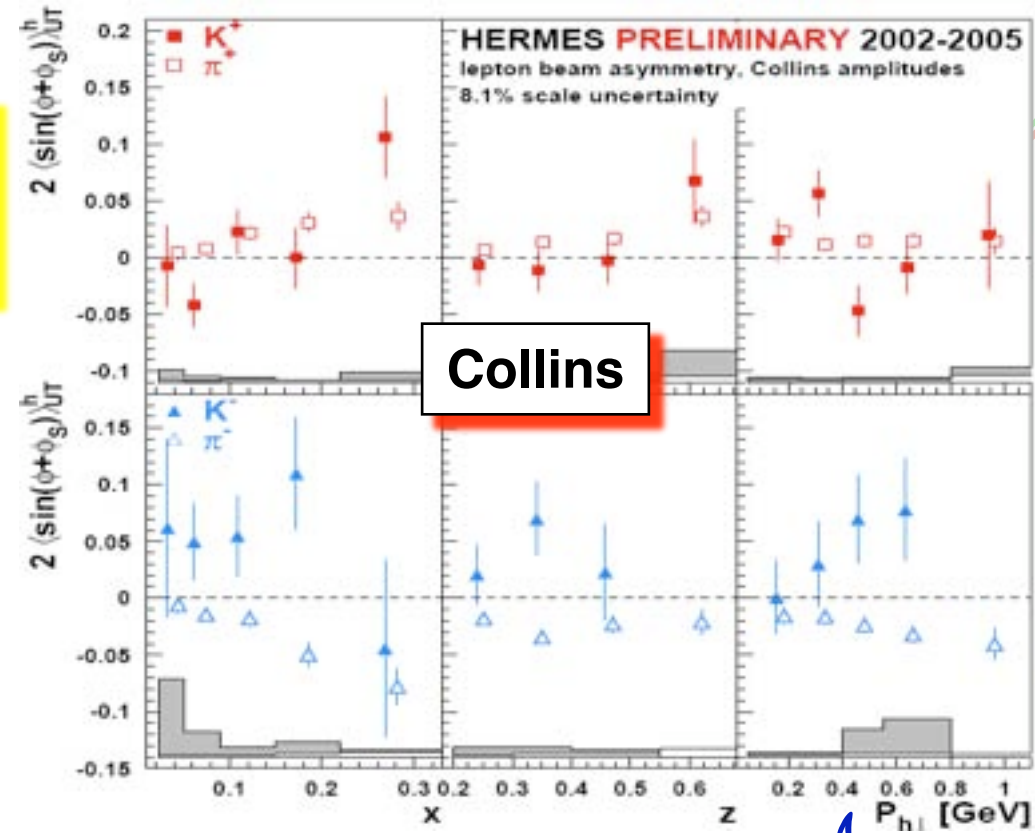
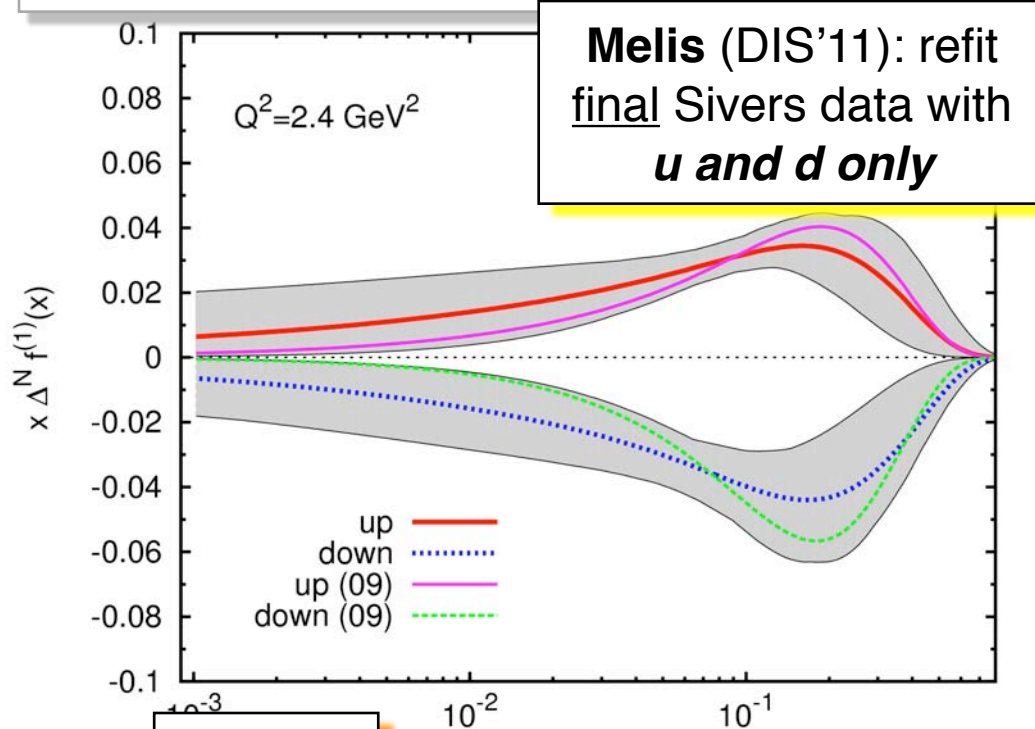


Published Sivers Moments from $H \uparrow$: PRL 103 (2009)



Finer binning, better systematics evaluation, ... message unchanged

The Kaon Collection



... and **BRAHMS** SSA's for kaons, never explained ...

SIDIS Multiplicities → Understanding Fragmentation

- How well do the **favored / disfavored** symmetries & **x-z factorizⁿ** hold?
 ... assumed in \approx all FF global fits & PDF extractions
 ... not exact at HERMES energies, acc to Lund MC

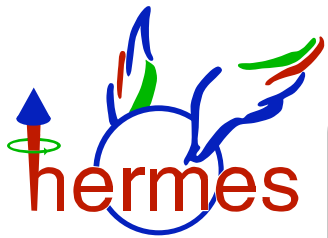
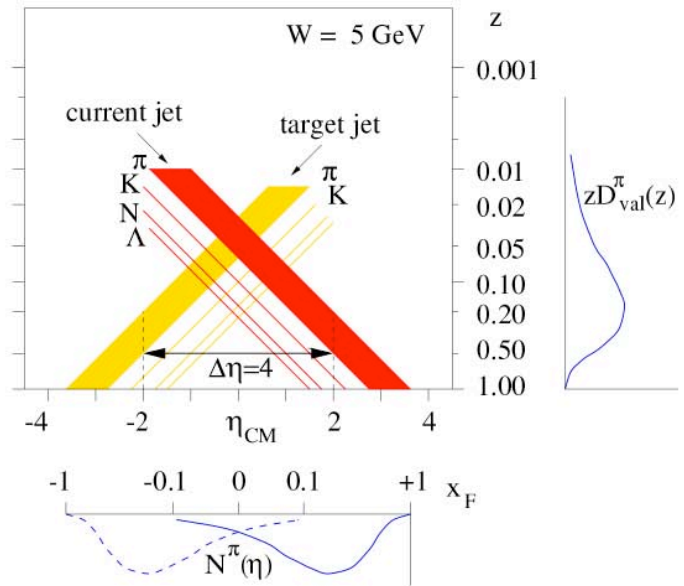
$$D_{\text{fav}} \equiv D_u^{\pi^+} = D_d^{\pi^-} = \dots$$

$$D_{\text{disfav}} \equiv D_u^{\pi^-} = D_d^{\pi^+} = \dots$$

- Are there **any** such FF symmetries for ***Kaons***?

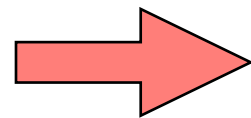
- Does **intrinsic quark $\langle k_T \rangle$** vary with **x**?
 ... with ***flavor***? (holy grail!)

- Can the **Lund model** describe fragmentation at different **energies** / different **processes** (SIDIS vs e+e-) ***without retuning***?



*paper permanently
in progress*

$d\sigma(x, z, p_T)$
 $d\sigma(Q^2, z, p_T)$ for $\pi^{\pm}, \pi^0, K^{\pm}, p, pbar$



compare

COMPASS-II $\mu^{\pm}p$

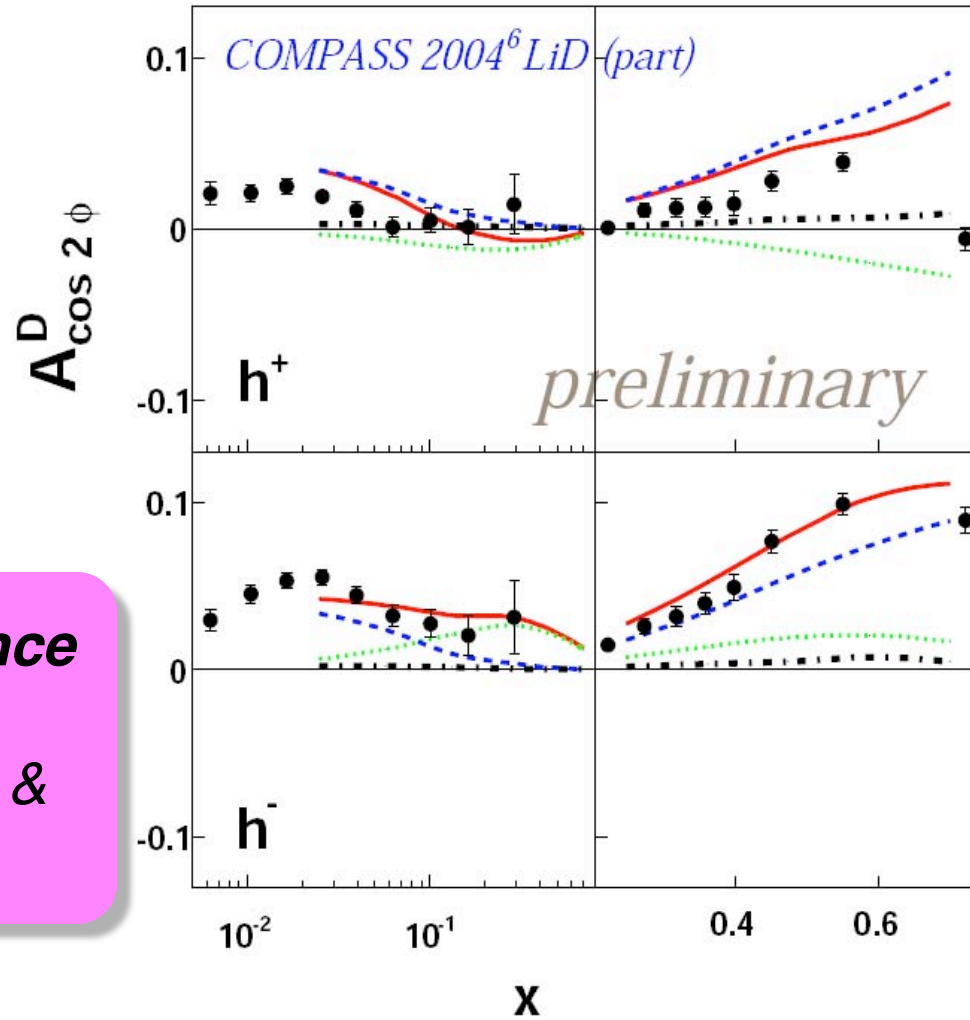
- pure LH2 target
- higher energy
- RICH upgrade
- full 4D binning



Boer-Mulders #2: $\langle \cos(2\Phi) \rangle_{UU}$ from COMPASS

different picture @ higher Q^2

Scale-dependence challenges: TMD evolution & higher twist



COMPASS $\cos(2\Phi)$ well explained by dominant twist-4 Cahn effect

... but Cahn contribⁿ seems small in HERMES data, at lower Q^2

... Can **BELLE** data on Collins FF be evolved to all SIDIS scales?

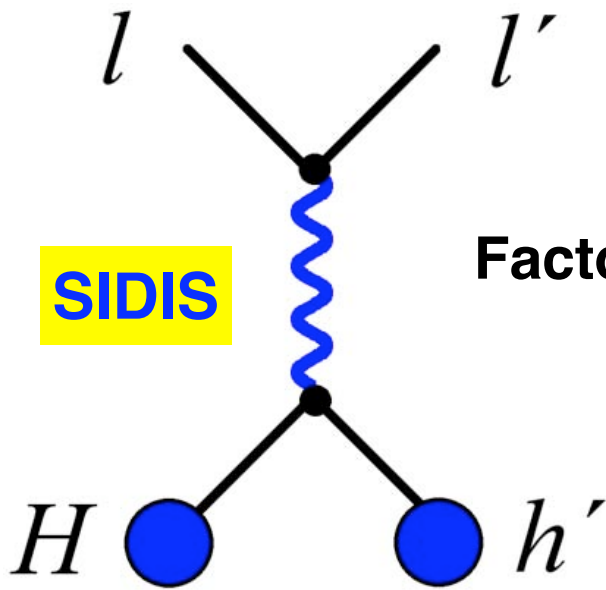
V.Barone, A.Prokudin, B.Q.Ma
arXiv:0804.3024 [hep-ph]

— total ⋯ Boer Mulders
- - - Cahn ⋯ pQCD

errors shown are statistical only

Leptons: clean, surgical tools

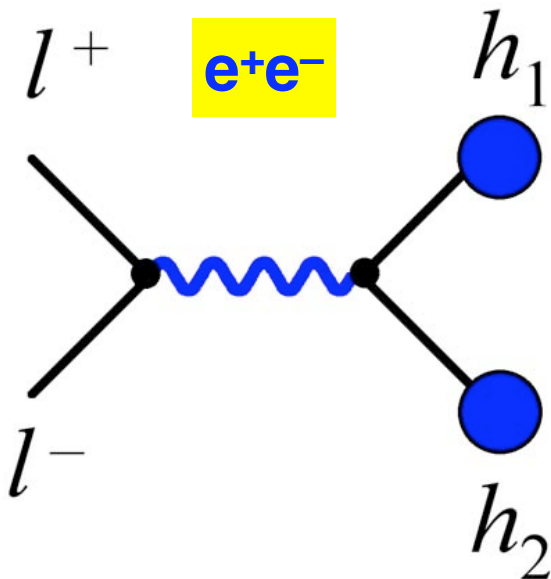
SIDIS



Factorization: $d\sigma \sim \sum_q e_q^2 \mathbf{f}_q^{(H)}(x) \mathbf{D}_q^{h'}(z)$

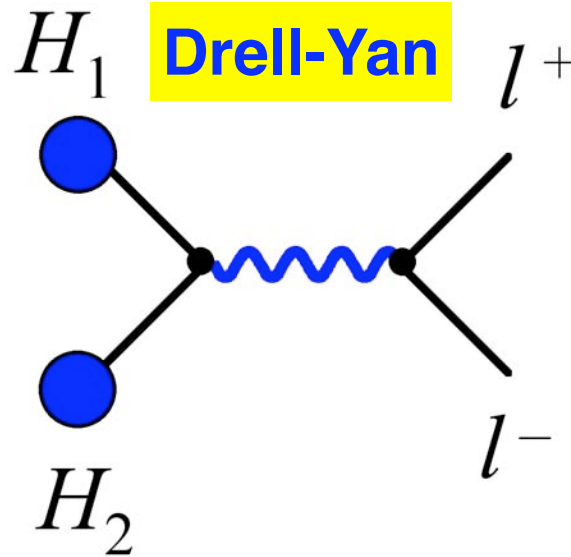
- Disentangle **distribution** (f) and **fragmentation** (D) functions \rightarrow measure **all process**
- Disentangle **quark flavours** $q \rightarrow$ measure as many **hadron species** H, h as possible

e^+e^-



$$\sum_q e_q^2 \mathbf{D}_q^{h_1}(z_1) \mathbf{D}_{\bar{q}}^{h_2}(z_2)$$

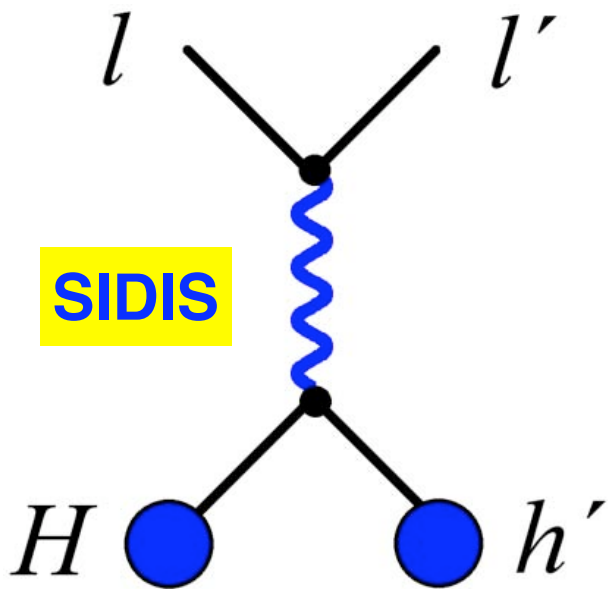
Drell-Yan



$$\sum_q e_q^2 \mathbf{f}_q^{(H_1)}(x_1) \mathbf{f}_{\bar{q}}^{(H_2)}(x_2)$$

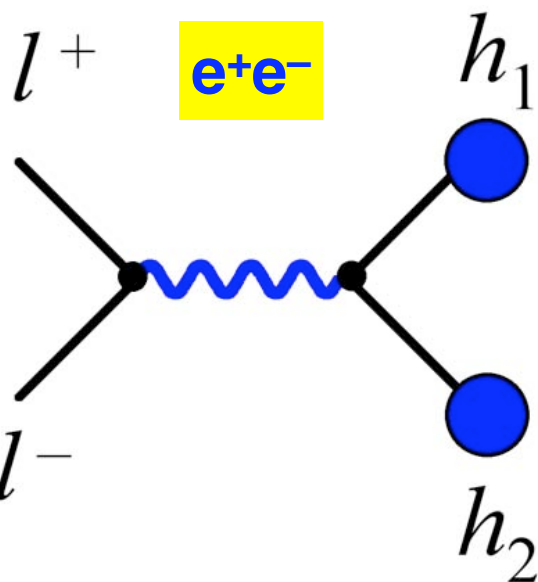
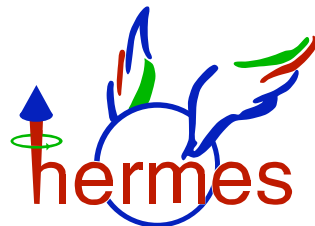
Leptons: clean, surgical tools

SIDIS

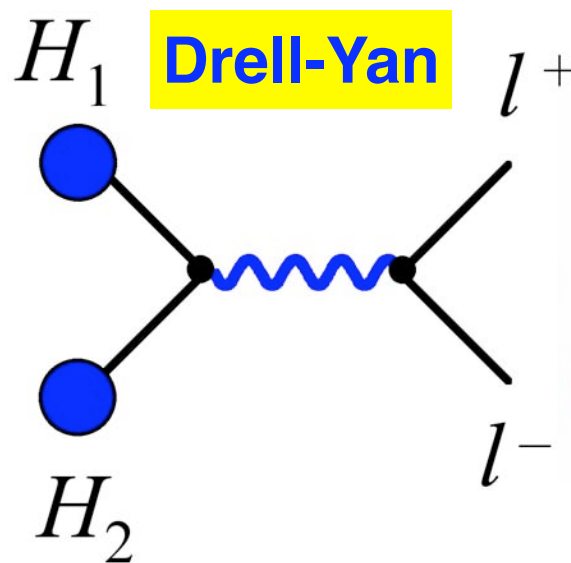


$$\sum_q e_q^2 f_q^{(H)}(x) D_q^{h'}(z)$$

Spin Programs



e⁺e⁻



Drell-Yan



$$\sum_q e_q^2 D_q^{h_1}(z_1) D_{\bar{q}}^{h_2}(z_2)$$

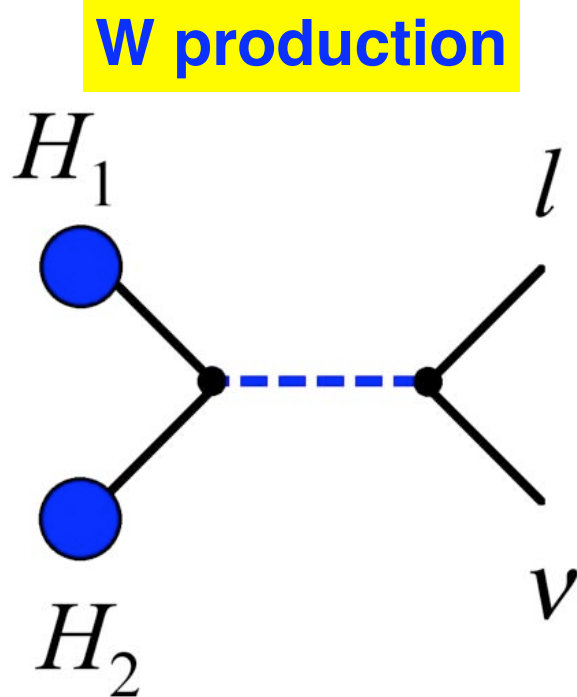
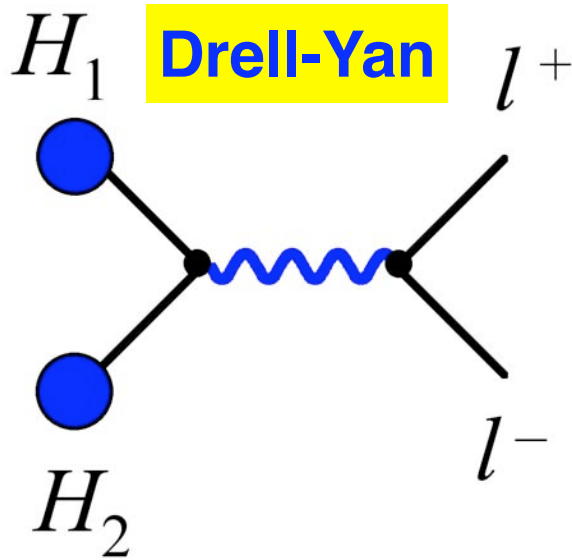
$$\sum_q e_q^2 f_q^{(H_1)}(x_1) f_{\bar{q}}^{(H_2)}(x_2)$$

The Missing Spin Program: Drell-Yan



$$\sum_q e_q^2 \mathbf{f}_q^{(H_1)}(x_1) \mathbf{f}_{\bar{q}}^{(H_2)}(x_2)$$

- Clean access to **sea quarks**
e.g. $\Delta\bar{u}(x), \Delta\bar{d}(x)$ at RHIC
- Crucial test of **TMD formalism**
→ sign change of T-odd functions
- A **complete** spin program
requires multiple hadron species
→ **nucleon & meson beams**



Theory Issues

- The TMD-GPD Connection
... or lack thereof
- The Transverse Spin Sum Rule
... elusive unicorn
- The Definition of L



PDFs and the Optical Theorem

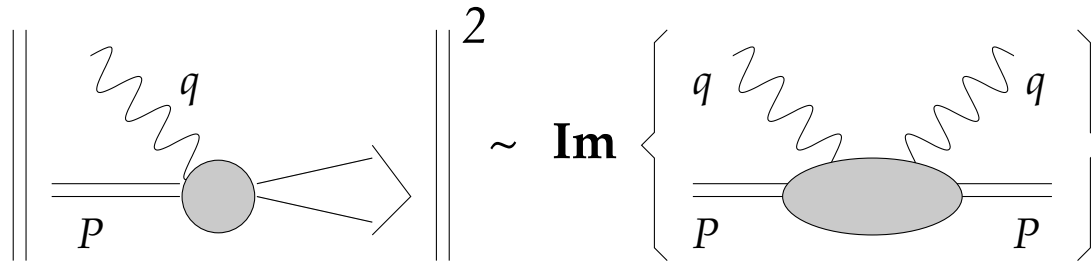
Proton
Matrix
Elements

vector charge $\langle PS | \bar{\psi} \gamma^\mu \psi | PS \rangle = \int_0^1 dx q(x) - \bar{q}(x) \rightarrow \# \text{ valence quarks}$

axial charge $\langle PS | \bar{\psi} \gamma^\mu \gamma_5 \psi | PS \rangle = \int_0^1 dx \Delta q(x) + \Delta \bar{q}(x) \rightarrow \text{net quark spin}$

tensor charge $\langle PS | \bar{\psi} \sigma^{\mu\nu} \gamma_5 \psi | PS \rangle = \int_0^1 dx \delta q(x) - \delta \bar{q}(x) \rightarrow ???$

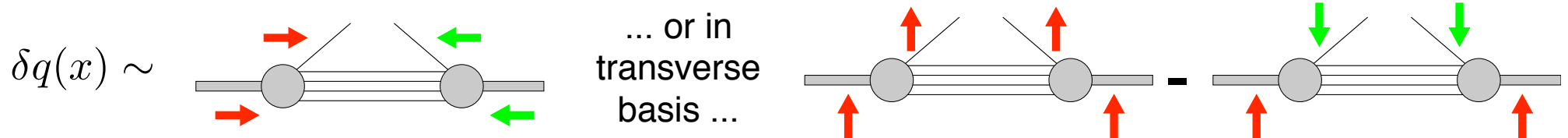
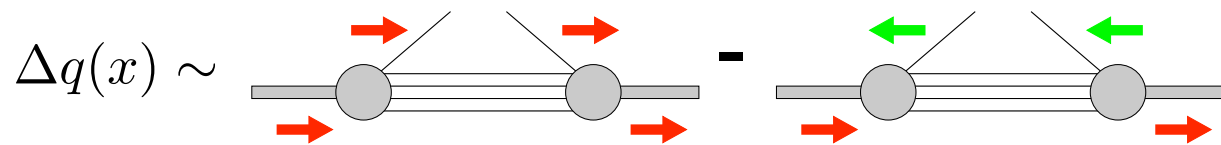
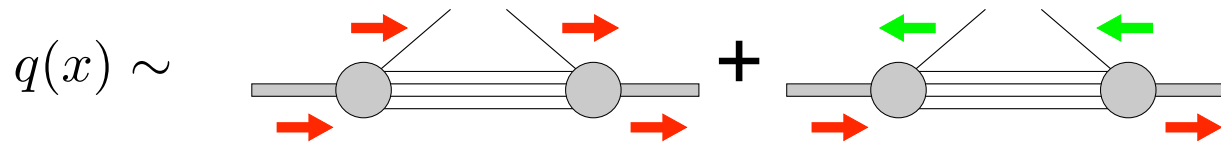
the Optical
Theorem



Forward
Scattering
Amplitudes

the DIS xsec

... can be calculated from ...



Danger !
"Pauli-Lubanski" ...
 h_1 is **not** $\langle \Sigma_\perp \rangle$

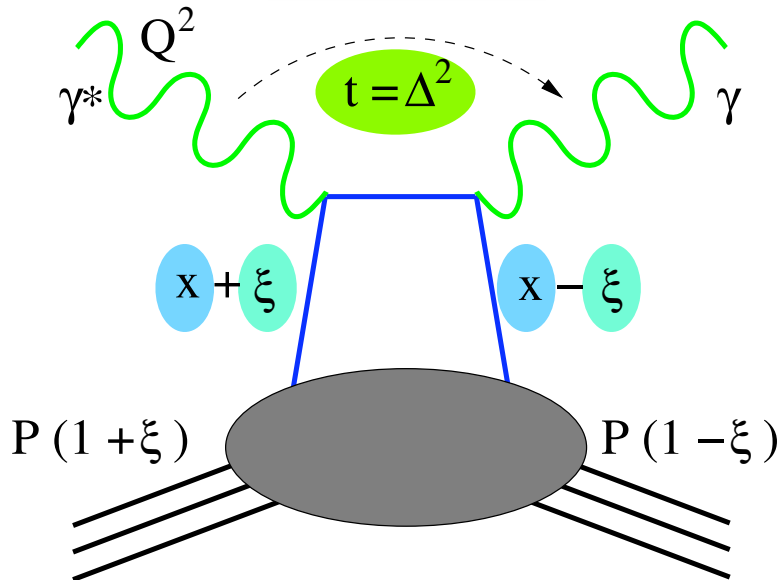
TRANSVERSITY

Generalized Parton Distributions

Analysis of hard exclusive processes leads to a new class of parton distributions

Cleanest example: Deeply Virtual Compton scattering

DVCS



- \mathbf{x} : average quark momentum fracⁿ
- ξ : “skewing parameter” = $x_1 - x_2$
- \mathbf{t} : 4-momentum transfer²

Four new distributions = “GPDs”

$$\begin{aligned} \text{q helicity sum} &\rightarrow H(x, \xi, t), E(x, \xi, t) \\ \text{q helicity difference} &\rightarrow \tilde{H}(x, \xi, t), \tilde{E}(x, \xi, t) \end{aligned}$$

- involve quark helicity-conserving amplitudes

Four with q helicity flip = “GTDs”

$$\begin{aligned} \text{q helicity sum} &\rightarrow H_T(x, \xi, t), E_T(x, \xi, t) \\ \text{q helicity difference} &\rightarrow \tilde{H}_T(x, \xi, t), \tilde{E}_T(x, \xi, t) \end{aligned}$$

Generalized Transversity Distributions are

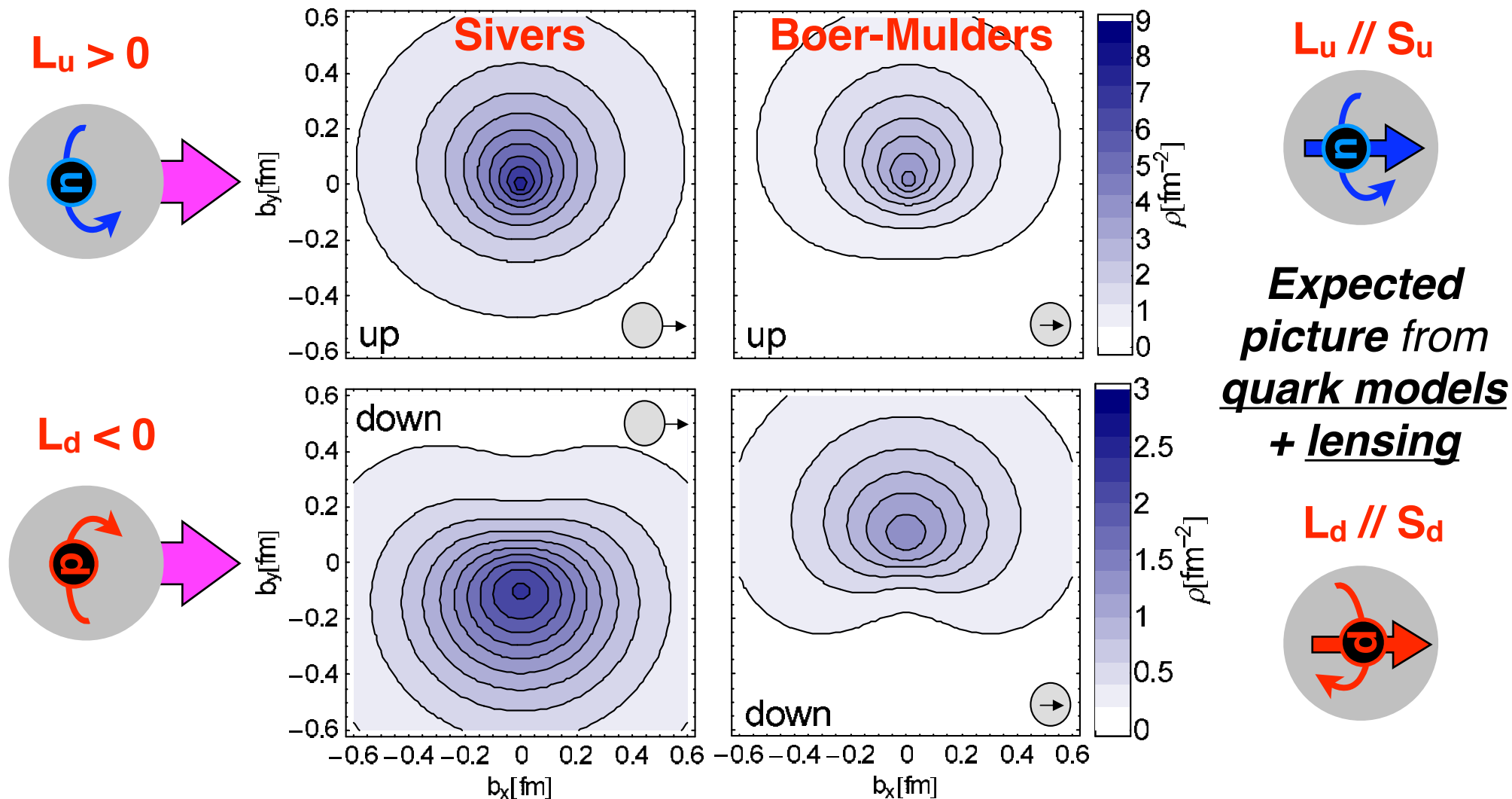
- chiral odd
- also called “tensor GPDs” because of presence of $\sigma^{\mu\nu}$ in their definition

Transverse spin on the lattice

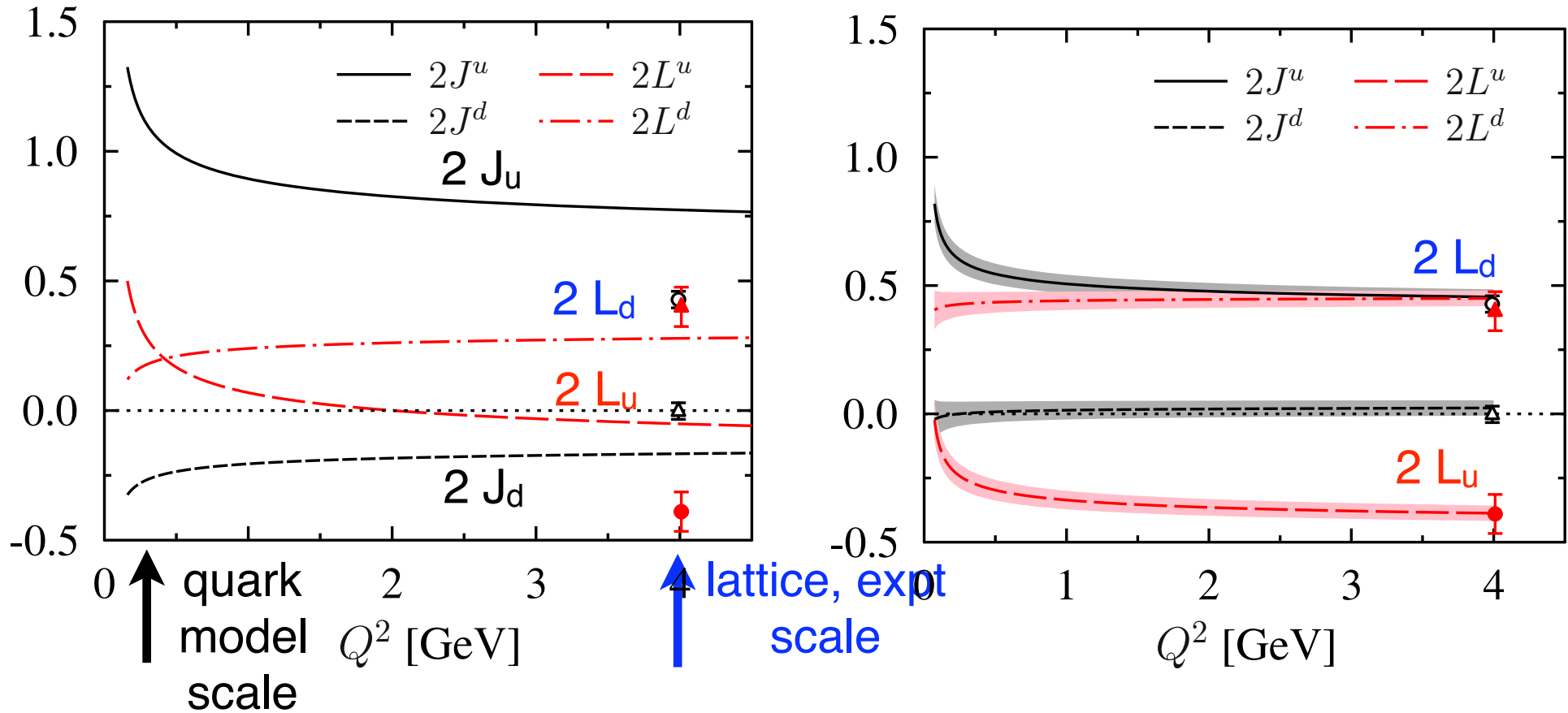
Hagler et al,
PRL98 (2007)

Compute **quark densities** in **impact-parameter space** via GPD formalism

nucleon coming out of page ... observe spin-dependent **shifts** in quark densities:



Thomas: **cloudy bag model** evolved up to Q^2 of expt / lattice



→ lattice shows $L_u < 0$ and $L_d > 0$ in longitudinal case at expt'al scales!

Evolution might explain disagreement with quark models ...

or not. Wakamatsu evolves down → insensitive to uncertain scale of quark models

• **Density shifts** seen on lattice due to GPD $E_q(x, \xi, t)$

• **E requires L**

Brodksy, Drell (1980) ; Burkardt, Schnell, PRD 74 (2006)

• $\int E dx = \text{Pauli } F_2 \rightarrow_{(t=0)}$ anomalous magnetic moment $\kappa \quad \therefore$ GPD basics

• both F_2 and κ **require $L \neq 0$** \therefore N spin-flip amplitudes

Jaffe L?

• **E is not L**

Ji Sum Rule

$$2 J_q = \int x H_q|_{t=0} dx + \int x E_q|_{t=0} dx$$

momentum fraction $\int x q(x) dx$

$$\leftarrow \langle \mathbf{X} \rangle_q + E_q^{(2)} \rightarrow \text{“anomalous gravito-magnetic moment”}$$

Spin Sum Rule

$$2 J_q = \Delta q + 2 L_q$$

$$\therefore 2 L_q = \left[\langle x \rangle_q + E_q^{(2)} \right]_{=J_q} - \Delta q$$

“L” not uniquely defined

Contradiction?

Ji L

Proton Spin Decompositions

$$J^{\text{Ji}} = \underbrace{\frac{i}{2} q^\dagger (\vec{r} \times \vec{D})^z q}_{L_q} + \underbrace{\frac{1}{2} q^\dagger \sigma^z q}_{\Delta q} + \underbrace{2 \text{Tr} E^j (\vec{r} \times \vec{D})^z A^j}_{L_g} + \underbrace{\text{Tr} (\vec{E} \times \vec{A})^z}_{\Delta g}$$

$$J^{\text{Jaffe}} = \frac{1}{2} q_+^\dagger (\vec{r} \times i\vec{\nabla})^z q_+ + \frac{1}{2} q_+^\dagger \gamma_5 q_+ + 2 \text{Tr} F^{+j} (\vec{r} \times i\vec{\nabla})^z A^j + \epsilon^{+-ij} \text{Tr} F^{+i} \vec{A}^j$$

Ji: ③ gauge invariant $\Delta q, L_q, J_g$

Jaffe: ④ gauge invar $\Delta q, L_q, \Delta g, L_g$

✗ **access Δg :** no GI sepⁿ of $\Delta g, L_g$

✓ **access Δg :** this is what's being measured at RHIC, COMPASS

✓ **measure L_q** (expt & lattice):
yes → via GPDs & DVCS

✓ **interpret L_q :** $\vec{r} \times \vec{p} \rightarrow$ field-free OAM ... in ∞ momentum frame

✗ **interpret L_q :** covariant derivative
 $D^\mu = \partial^\mu + ig^\mu \leftarrow$ **gluon interac's**

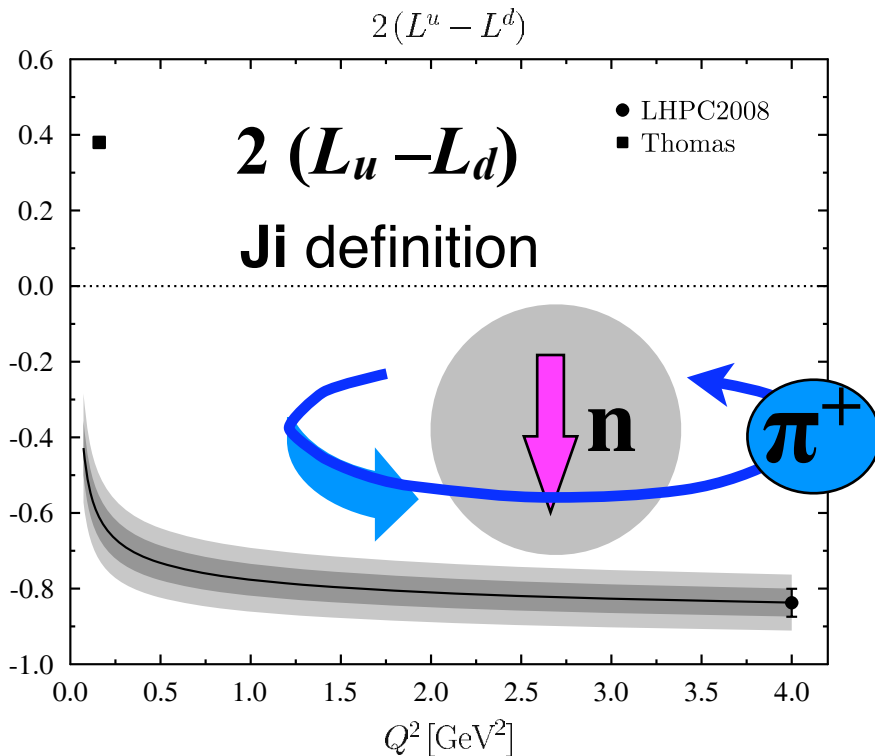
✗ **measure L_q** (expt & lattice):
involves **non-local** operators
except in **lightcone gauge** $A^+=0$



Ongoing work of **Chen et al** PRL 100 (2008), 103 (2009)
& **Wakamatsu** PRD 81 (2010), 83 (2011)

Theory: Ji's L_{u-d} is rock-solid & **negative**

Compare Jaffe & Ji
calculate explicitly in χ QSM;
at quark-model scale:



$$2L_q^{\text{Ji}} = \left[\langle x \rangle_q + E_q^{(2)} \right]_{=J_q} - \Delta q$$

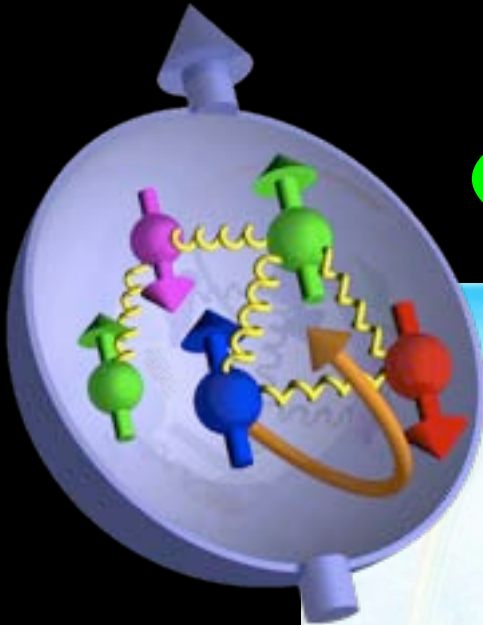
- $\langle x \rangle_{u-d}$: well known
- $\Delta u - \Delta d = g_A$: well known
- $E_{u-d}^{(2)}$: **all lattice** calculat^{ns}
and XQSM agree

	L_{u-d} Jaffe	L_{u-d} Ji
Valence	+0.147	-0.142
Sea	-0.265	-0.188
Total	-0.115	-0.330

**Negative model value
dominated by sea quark L !**

**Need direct measurement of
Sivers for sea quarks:**

**spin-dependent Drell-Yan
with p or π^+ beam**



Hmmm

