

Transversity in electroproduction of pseudoscalar mesons

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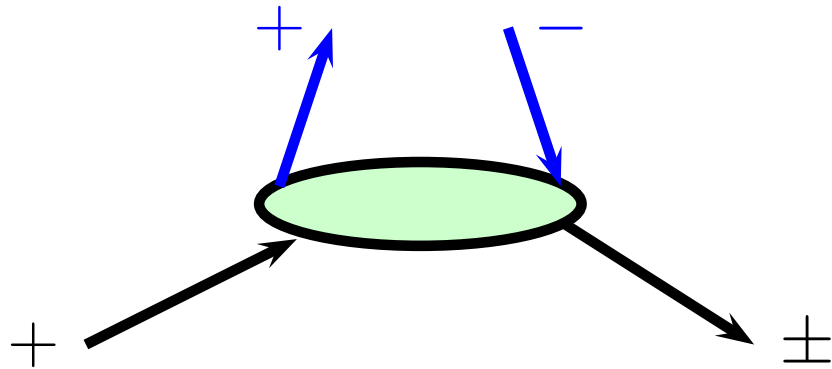
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INT Seattle, February 2012

Outline:

- **Transverse spin**
- **Evidence for strong $\gamma_T^* \rightarrow \pi$ transitions**
- **Transversity in the handbag approach**
- **Parametrizations of the GPDs**
- **Results**
- **Summary**

Transverse spin



transversely pol. quarks

EV of σ_2 (σ_1):

$$|\uparrow(\downarrow)\rangle = 1/\sqrt{2}[|+\rangle \pm i|-\rangle]$$

requires helicity flip

inclusive: transversity distributions $\Delta_T q(x)$ ($h_1(x)$)

not accessible in DIS but in SIDIS (analysis [Anselmino et al \(09\)](#))

exclusive: transv. GPDs $H_T, \tilde{H}_T, E_T, \tilde{E}_T$ (lead. twist)

soft matrix elements $\sim \langle p' | \bar{q}(-z/2) i\sigma^{+i} q(z/2) | p \rangle$ [Hoodbhoy-Ji \(98\)](#), [Diehl \(01\)](#)

reduction formula: $H_T^q(x, \xi = t = 0) = \Delta_T q(x)$

difficult to access in exp: helicity flip of light quarks suppressed

only a few applications: [Pire et al](#) electroproduction of ρ_T

[Liuti et al](#) production of π^0

[Goloskokov-K](#) production of pseudoscalar mesons

An almost model-independent argument

consider pion electroproduction

sum and difference of single-flip ampl. ($\sim \sqrt{-t'}$ for $t' \rightarrow 0$)

$$\mathcal{M}_{0+\mu+}^{N(U)} = \frac{1}{2} \left[\mathcal{M}_{0+\mu+} + (-) \mathcal{M}_{0+-\mu+} \right] \quad \mu = \pm 1$$

$$\implies \mathcal{M}_{0+-+}^{N(U)} = +(-) \mathcal{M}_{0+++}^{N(U)}$$

like a one-particle-exchange of either **N**atural or **U**nnatural parity

nucleon helicity flip: $\mathcal{M}_{0--+} \sim t'$ $\mathcal{M}_{0-++} \sim \text{const}$

sum and difference inconvenient

(const can be small (or zero) for dynamical reasons)

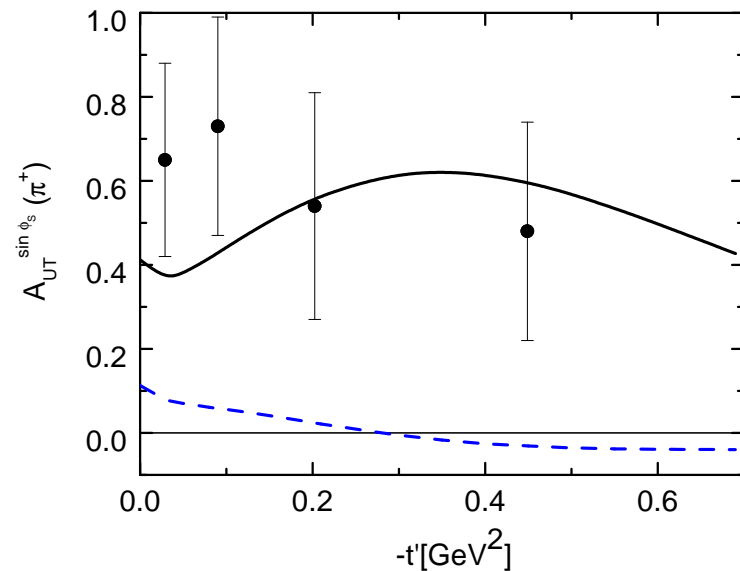
Experiment:

$\gamma p \rightarrow \pi^+ n$ cross section exhibits pronounced maximum

c cannot be small

Phillips (1967): Regge cuts necessary

Pion electroproduction



HERMES(09)

$Q^2 \simeq 2.5 \text{ GeV}^2$, $W = 3.99 \text{ GeV}$

$\sin \phi_s$ harmonic very large

does not seem to vanish for $t' \rightarrow 0$

$$A_{UT}^{\sin \phi_s} \propto \text{Im} \left[\mathcal{M}_{0-,++}^* \mathcal{M}_{0+,0+} \right]$$

n-f. ampl. $\mathcal{M}_{0-,++}$ required

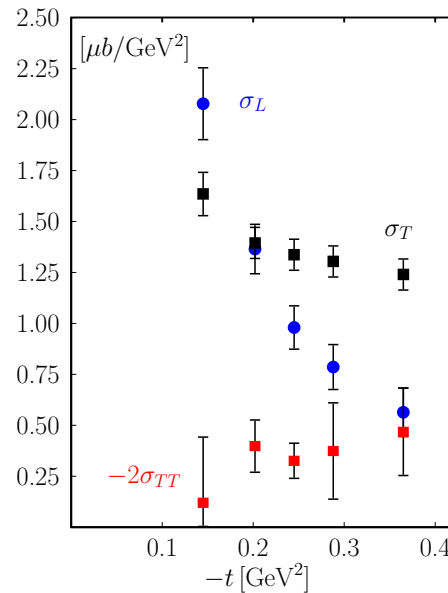
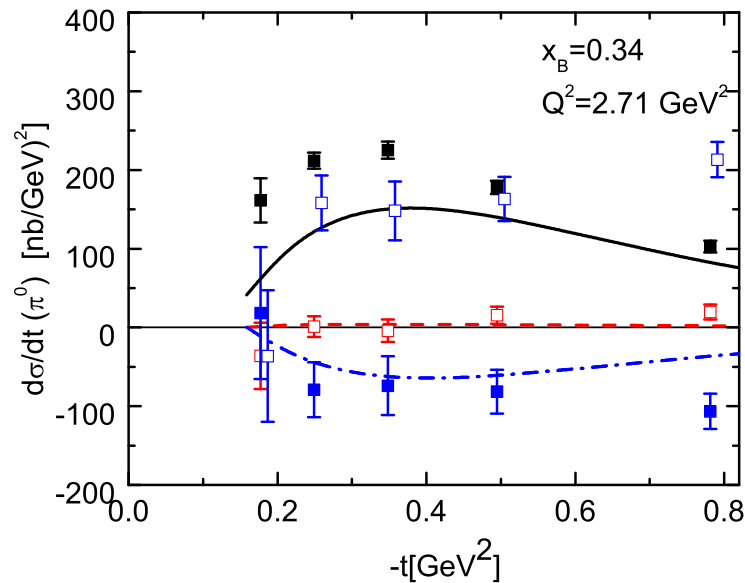
not vanishing in forward direction

assumption: $|\mathcal{M}_{0--}| \ll |\mathcal{M}_{0-++}|, |\mathcal{M}_{0+\pm}|$

Transverse cross sections

$$\frac{d\sigma_T}{dt} \simeq \frac{1}{2\kappa} \left[|\mathcal{M}_{0-+++}|^2 + 2|\mathcal{M}_{0++++}^N|^2 + 2|\mathcal{M}_{0++++}^U|^2 \right] \quad \frac{d\sigma_{TT}}{dt} \simeq -\frac{1}{2\kappa} \left[|\mathcal{M}_{0++++}^N|^2 - |\mathcal{M}_{0++++}^U|^2 \right]$$

$$\frac{d\sigma_T}{dt} + 2\frac{d\sigma_{TT}}{dt} \simeq \frac{1}{2\kappa} \left[|\mathcal{M}_{0-+++}|^2 + 4|\mathcal{M}_{0++++}^U|^2 \right] \quad \Rightarrow \quad -2\frac{d\sigma_{TT}}{dt} \leq \frac{d\sigma_T}{dt} \leq \frac{d\sigma}{dt}$$



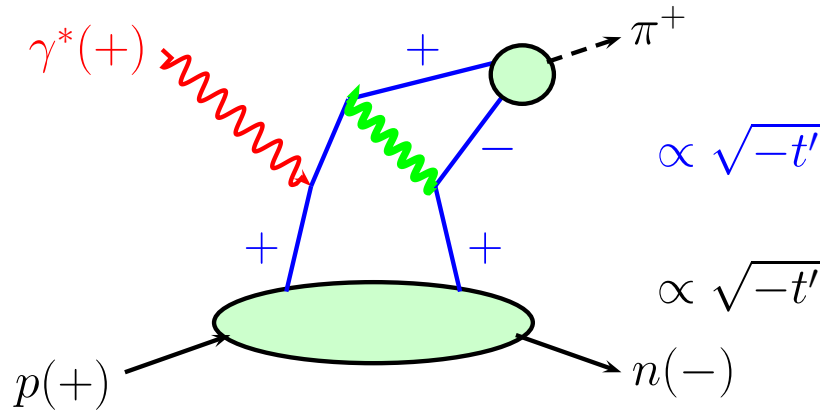
π^0 CLAS
unsep. cross sec.

π^+ $F - \pi$
 $Q^2 = 2.45 \text{ GeV}^2$
 $W = 2.22 \text{ GeV}$

$\pi^0 \implies |\mathcal{M}_{0++++}^N|$ dominant (for $-t' > 0$ see forward dip)

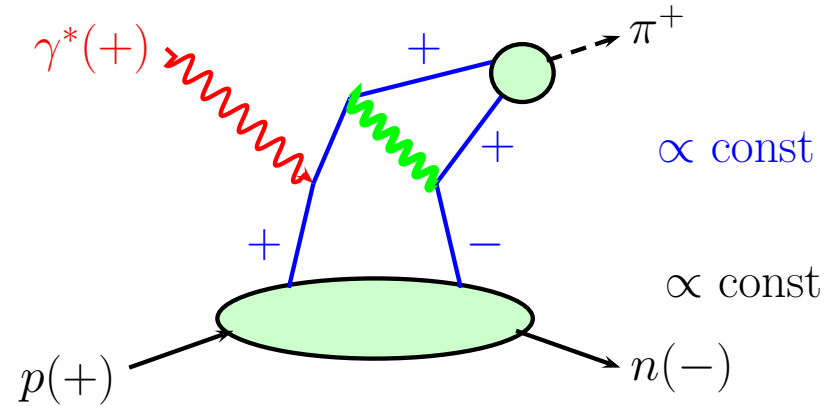
$(d\sigma_L/dt \ll d\sigma_T/dt)$

Handbag: can $\mathcal{M}_{0-,++}$ be fed by ordinary GPDs?



lead. twist pion wave fct. $\propto q' \cdot \gamma\gamma_5$
 (perhaps including \mathbf{k}_\perp)

$$\mathcal{M}_{0-,++} \propto t'$$



twist-3 w.f.
 (suppressed by μ_π/Q)

$$\mathcal{M}_{0-,++} \propto \text{const}$$

transv. GPDs in long. amplitudes suppressed by extra $\sqrt{-t'}/Q$

$\gamma_T^* \rightarrow \pi$ in the handbag approach

see Diehl01, GK10, GK11

$$\bar{E}_T \equiv 2\tilde{H}_T + E_T \quad \mu = \pm 1$$

$$\begin{aligned} \mathcal{M}_{0+\mu+} &= e_0 \frac{\sqrt{-t'}}{4m} \int d\bar{x} \left\{ (H_{0+\mu-} - H_{0-\mu+}) (\bar{E}_T - \xi \tilde{E}_T) \right. \\ &\quad \left. + (H_{0+\mu-} + H_{0-\mu+}) (\tilde{E}_T - \xi E_T) \right\} \end{aligned}$$

$$\begin{aligned} \mathcal{M}_{0-\mu+} &= e_0 \sqrt{1 - \xi^2} \int d\bar{x} \left\{ H_{0-\mu+} \left[H_T + \frac{\xi}{1 - \xi^2} (\tilde{E}_T - \xi E_T) \right] \right. \\ &\quad \left. + (H_{0+\mu-} - H_{0-\mu+}) \frac{t'}{4m^2} \tilde{H}_T \right\} \end{aligned}$$

with parity conservation: $\mathcal{M}_{0+\pm+} = \mathcal{M}_{0+++}^N \pm \mathcal{M}_{0+++}^U$

time-reversal invariance: \tilde{E}_T is odd function of ξ

N: \bar{E}_T with corrections of order ξ^2 U: order ξ

small $-t'$: \mathcal{M}_{0-++} mainly H_T with corrections of order ξ^2

\mathcal{M}_{0--+} suppressed by t/Q^2 due to H_{0--+}

The twist-3 pion distr. amplitude

projector $q\bar{q} \rightarrow \pi$ (3-part. $q\bar{q}g$ contr. neglected) Beneke-Feldmann (01)

$$\sim q' \cdot \gamma \gamma_5 \Phi + \mu_\pi \gamma_5 \left[\Phi_P - i \sigma_{\mu\nu} (\dots \Phi'_\sigma + \dots \Phi_\sigma \partial / \partial \mathbf{k}_\perp \nu) \right]$$

definition: $\langle \pi^+(q') | \bar{d}(x) \gamma_5 u(-x) | 0 \rangle = f_\pi \mu_\pi \int d\tau e^{iq'x\tau} \Phi_P(\tau)$

local limit $x \rightarrow 0$ related to divergency of axial vector current

$$\implies \mu_\pi = m_\pi^2 / (m_u + m_d) \simeq 2 \text{ GeV at scale } 2 \text{ GeV (conv. } \int d\tau \Phi_P(\tau) = 1)$$

Eq. of motion: $\tau \Phi_P = \Phi_\sigma / N_c - \tau \Phi'_\sigma / (2N_c)$

solution: $\Phi_P = 1, \quad \Phi_\sigma = \Phi_{AS}$ Braun-Filyanov (90)

$H_{0-,++} \neq 0$, Φ_P dominant, Φ_σ contr. $\propto t'/Q^2$

in coll. appr.: $H_{0-,++}$ singular \mathbf{k}_\perp factorization (m.p.a.) regular

$$M_{0-++} = e_0 \sqrt{1 - \xi^2} \int dx H_{0-++} H_T, \quad M_{0-++} = -e_0 \frac{\sqrt{-t'}}{4m} \int dx H_{0-++} \bar{E}_T$$

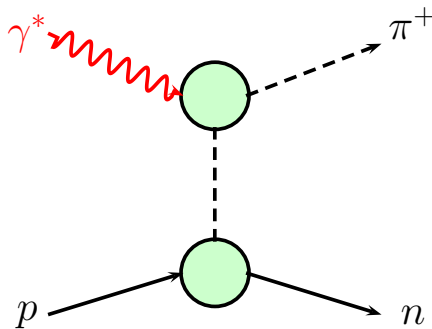
The $\gamma_L^* \rightarrow \pi$ amplitudes and pion pole

$$\mathcal{M}_{0+0+} = \frac{e_0}{2} \sqrt{1 - \xi^2} \int dx (H_{0+0+} - H_{0-0-}) \left(\tilde{H} - \frac{\xi^2}{1 - \xi^2} \tilde{E}_{\text{n.p.}} \right)$$

$$\mathcal{M}_{0-0+} = e_0 \frac{\sqrt{-t'}}{4m} \int dx (H_{0+0+} - H_{0-0-}) \xi \tilde{E}_{\text{n.p.}}$$

leading amplitudes for $Q^2 \rightarrow \infty$

For π^+ production - pion pole



$$\mathcal{M}_{0+0+}^{\text{pole}} = -e_0 \frac{2m\xi Q}{\sqrt{1 - \xi^2}} \frac{\rho_\pi}{t - m_\pi^2}$$

$$\mathcal{M}_{0-0+}^{\text{pole}} = -e_0 \sqrt{-t'} Q \frac{\rho_\pi}{t - m_\pi^2}$$

$$\mathcal{M}_{0+\pm+}^{\text{pole}} = \pm 2\sqrt{2} e_0 m \xi \sqrt{-t'} \frac{\rho_\pi}{t - m_\pi^2}$$

$$\mathcal{M}_{0-\pm+}^{\text{pole}} = \pm \sqrt{2} e_0 t' \sqrt{1 - \xi^2} \frac{\rho_\pi}{t - m_\pi^2} !$$

$$\rho_\pi = \sqrt{2} g_{\pi NN} F_\pi(Q^2) F_{\pi NN}(t)$$

(see assumption 1 and following remarks)

Double distributions

integral representation ($i = u, d$ valence quarks)

$$\tilde{H}^i(\bar{x}, \xi, t) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - \bar{x}) \tilde{f}_i(\beta, \alpha, t)$$

\tilde{f}_i double distributions Mueller *et al* (94), Radyushkin (99)

advantage - polynomiality automatically satisfied

useful ansatz with relation to PDFs (reduction formula respected)

$$\tilde{f}_i(\beta, \alpha, t) = \Delta q_i(\beta) \Theta(\beta) \exp[(\tilde{b}_i + \tilde{\alpha}'_i \ln(1/\beta))t] \frac{3}{4} \frac{[(1 - |\beta|)^2 - \alpha^2]}{(1 - |\beta|)}$$

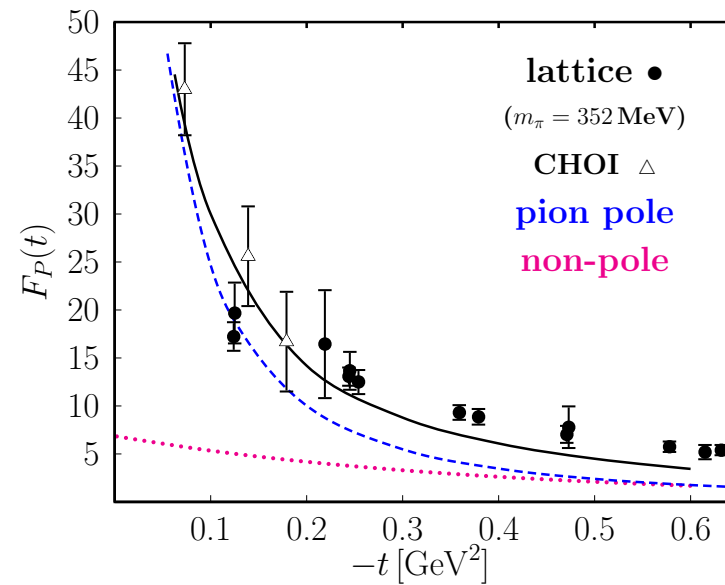
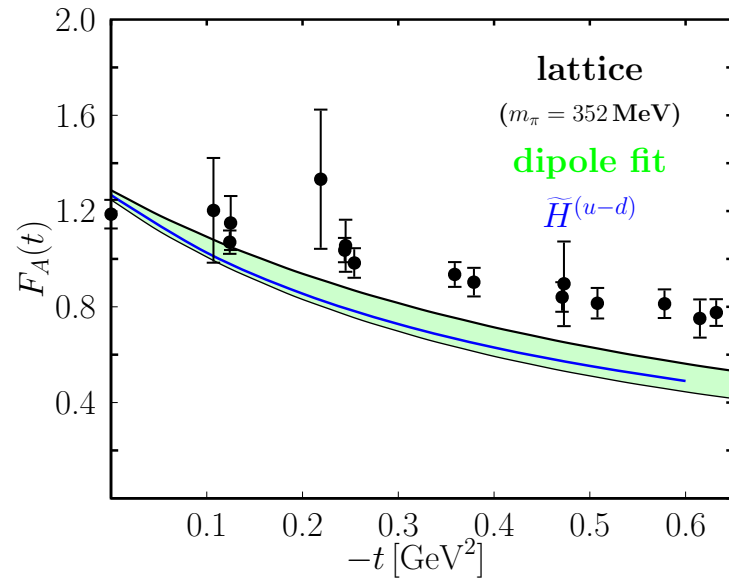
$\tilde{\alpha}'_{h'} = 0.45 \text{ GeV}^{-2}$ $\tilde{b}_{h'} = 0.0$ t -dependence of Regge residue

Regge intercept and residue at $t = 0$ included in PDF

$\tilde{E}_{n.p.}$ analogously, forward limit parameterized as $\tilde{e}_q = \tilde{N}_q \beta^{-0.48} (1 - \beta)^5$

$\tilde{N}_u = 14$ $\tilde{N}_d = 4$, $\tilde{\alpha}'_e = 0.45 \text{ GeV}^{-2}$, $\tilde{b}_e = 0.9 \text{ GeV}^{-2}$, values fitted to π^+ data

Comparison with lattice results



Hägler (07), Gockeler (05)

lowest pion mass 352 MeV, no chiral extrapolation

in general at $t \simeq 0$ reasonable agreement but t dependences flatter than DD ansatz (and form factor data)

relative t dependence of moments in good agreement

Parametrization of H_T and \bar{E}_T

H_T : transversity PDFs Anselmino et al(09)

$$\Delta_T q(x) = N_{H_T}^q \sqrt{x}(1-x) [q(x) + \Delta q(x)]$$

DD ansatz

parameters: $\alpha(0) = -0.02$, $\alpha' = 0.45 \text{ GeV}^{-2}$, $b = 0$, $N^u = 0.78$, $N^d = -1.01$

\bar{E}_T : Lattice result for moments of $\bar{E}_T = 2\tilde{H}_T + E_T$: QCDSF-UKQCD(06)

Large, same sign and almost same size for u and d quarks

\bar{E}_T parameterization (like $\tilde{E}_{\text{n.p.}}$):

$$e_T^a = \bar{N}_T^e e^{b_{eT} t} x^{-\alpha_T^e(t)} (1-x)^{\beta_{eT}^a}$$

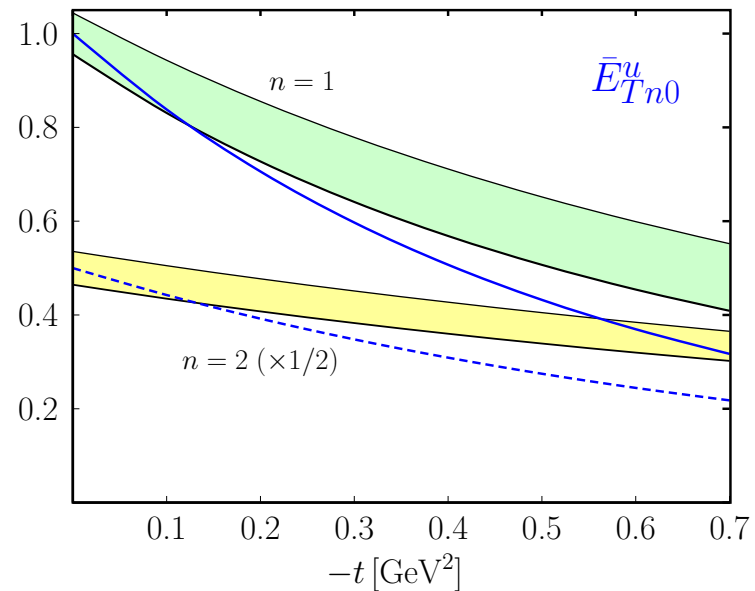
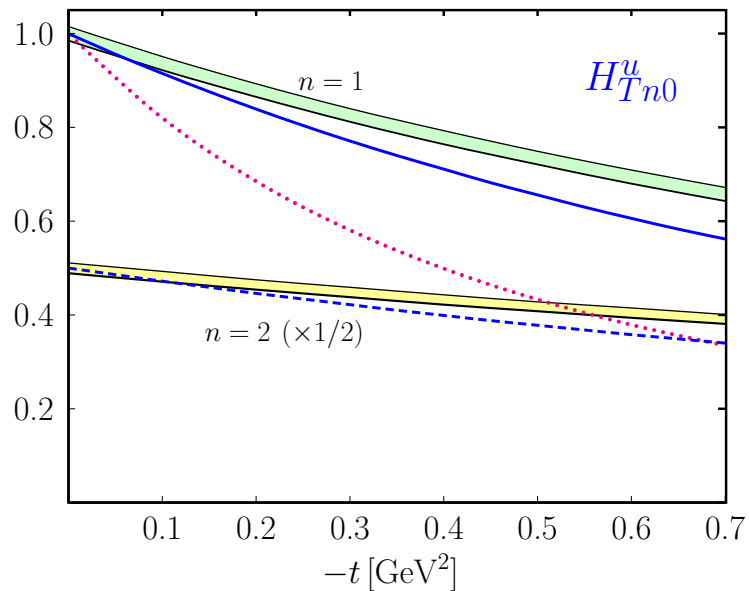
parameters: $\alpha(0) = 0.3$, $\alpha' = 0.45 \text{ GeV}^{-2}$, $b = 0.5 \text{ GeV}^{-2}$, $\bar{N}_T^u = 6.83$, $\bar{N}_T^d = 5.05$

adjusted to lattice results

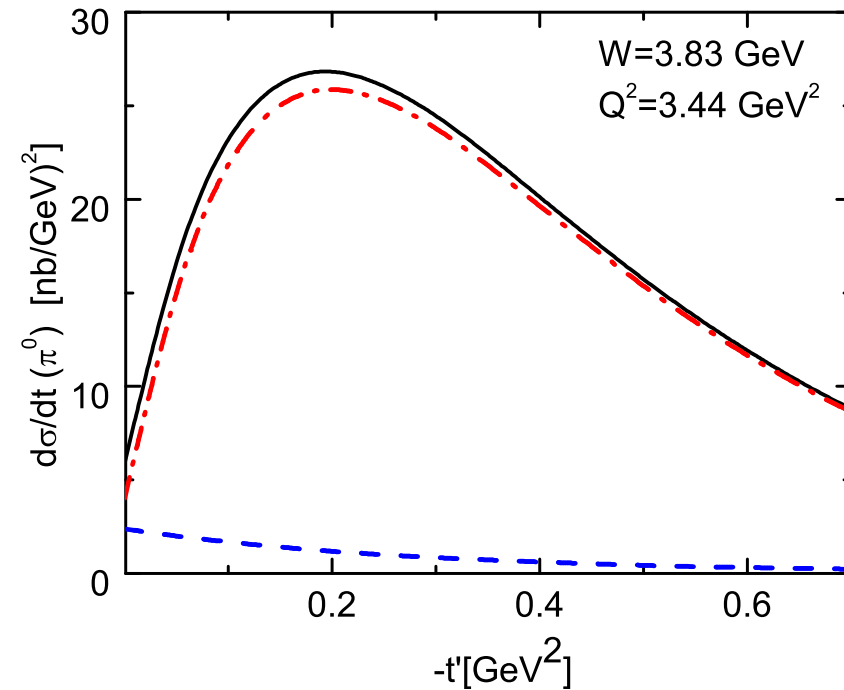
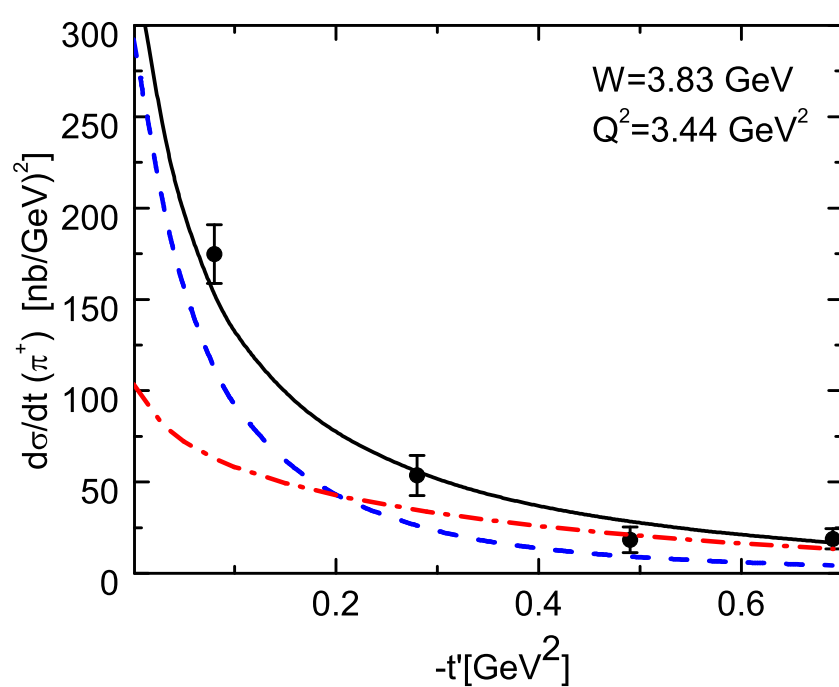
Burkardt related to Boer-Mulders fct $\langle \cos(2\phi) \rangle$ in SIDIS – same pattern

	lattice	this work		lattice	this work
H_{T10}^u	0.857(13)	0.585	E_{T10}^u	2.93(13)	2.93
H_{T20}^u	0.268(6)	0.123	\bar{E}_{T20}^u	0.420(31)	0.360
H_{T10}^d	-0.212(5)	-0.153	\bar{E}_{T10}^d	1.90(9)	1.90
H_{T20}^d	-0.052(2)	-0.021	\bar{E}_{T20}^d	0.260(23)	0.199

H_T lattice moments are larger by about factor of 2 as those constructed from transversity PDFs with help of DD ansatz



\bar{E}_T in pion electroproduction



unseparated (longitudinal, transverse) cross sections

π^+ : pion pole and $\propto F^u - F^d$

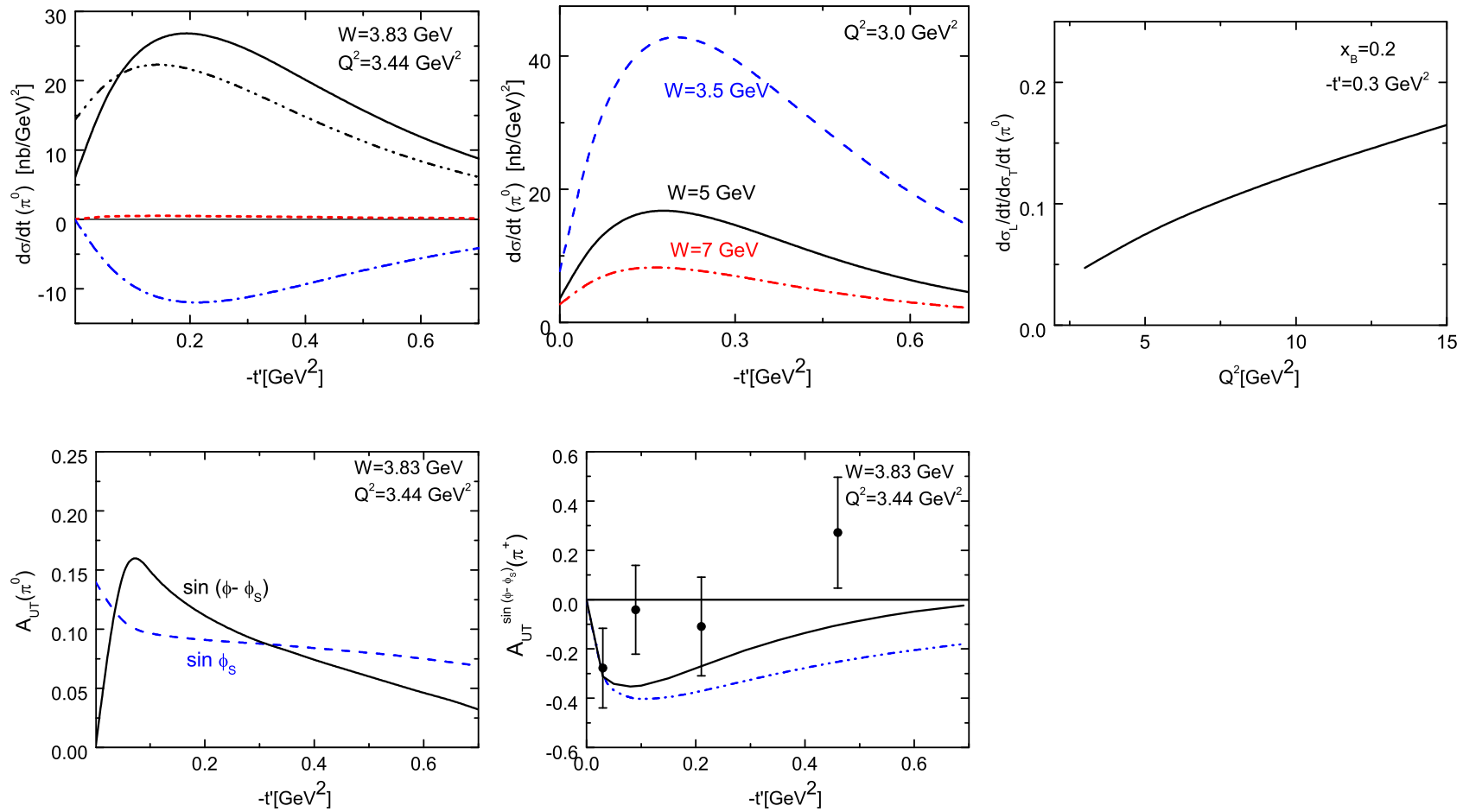
π^0 : no pion pole and $\propto 2F^u + F^d$

consider $u - d$ signs: $\bar{E}_T, \tilde{E}^{n.p.}$ same, \tilde{H}, H_T opposite sign

$\implies \tilde{H}$ and H_T large for π^+ , small for π^0

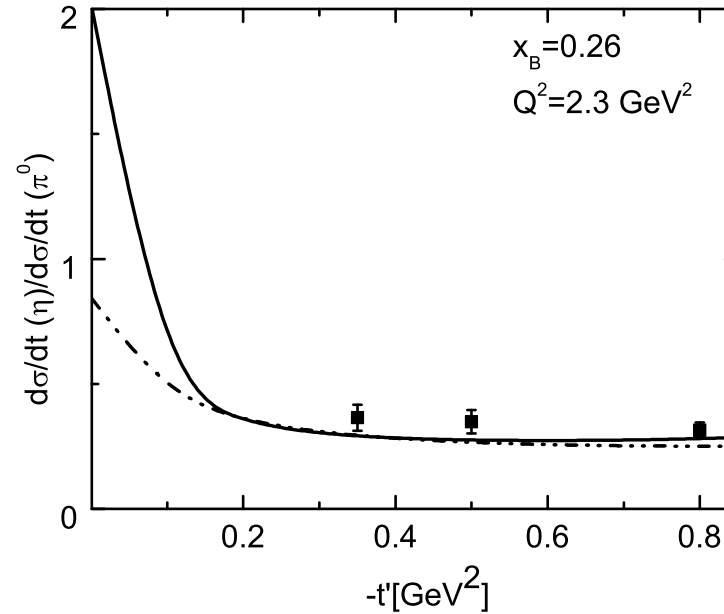
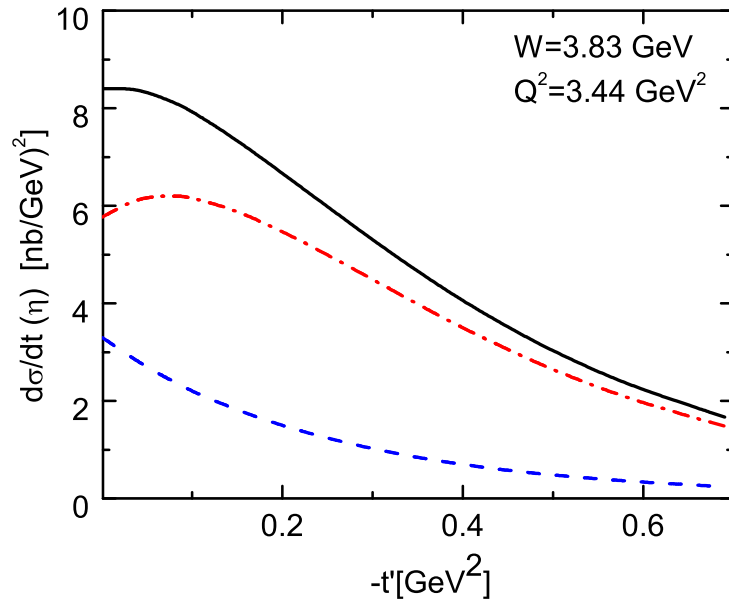
$\tilde{E}^{n.p.}$ and \bar{E}_T small for π^+ , large for π^0

Results for pion production



Goloskokov-K (10),(11) optimized for small ξ and large W

η/π^0 ratio



data CLAS (prel.)

$$\frac{d\sigma(\eta)}{d\sigma(\pi^0)} \simeq \left(\frac{f_\eta}{f_\pi}\right)^2 \frac{1}{3} \left| \frac{e_u \langle F^u \rangle + e_d \langle F^d \rangle}{e_u \langle F^u \rangle - e_d \langle F^d \rangle} \right|^2 \quad (f_\eta = 1.26 f_\pi)$$

if F^u and F^d have opposite sign: $\eta/\pi^0 \simeq 1$

if F^u and F^d have same sign: $\eta/\pi^0 < 1$

$t' \simeq 0$ \tilde{H}, H_T dominant (see also Eides et al(98))

$t' \neq 0$ \bar{E}_T dominant

Strangeness production

e.g. $\gamma^* p \rightarrow K^+ \Lambda(\Sigma^0)$

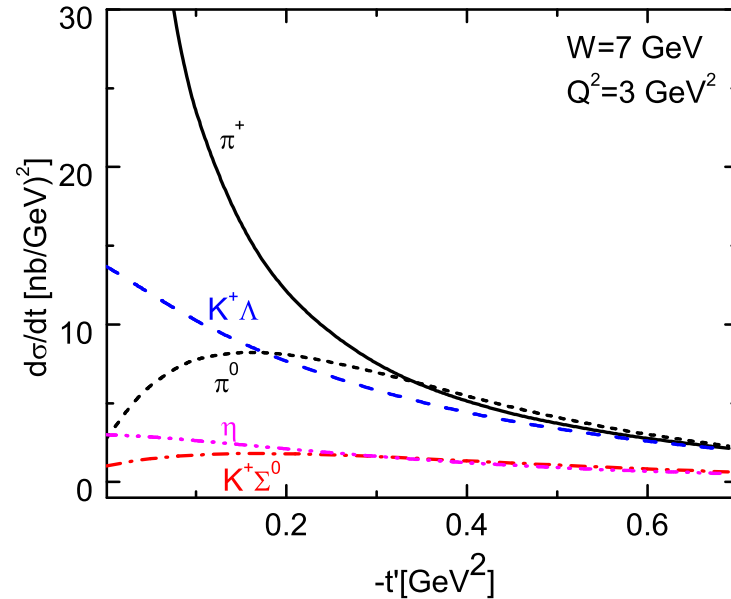
similar to π^+ production

Kaon pole (smaller than pion pole)

and

twist-3 effect with

$$\mu_K = m_K^2 / (m_u + m_s) \simeq 2.0 \text{ GeV}$$



would probe \tilde{H} , \tilde{E} and H_T for flavor symmetry breaking in sea

e.g.

$$F_{p \rightarrow \Sigma^0} = -F_v^d + (F^s - F^{\bar{d}}),$$

$$F_{p \rightarrow \Lambda} = -\frac{1}{\sqrt{6}} \left[2F_v^u - F_v^d + (2F^{\bar{u}} - F^{\bar{d}} - F^s) \right]$$

L-T interference

$$\frac{d\sigma_{LT}}{dt} \sim \text{Re} \left[M_{0-0+}^* M_{0-++} \right] \sim \text{Re} \left[\langle H_T \rangle \langle \tilde{E} \rangle^* \right]$$
$$A_{LU} \sigma_0 \sim \text{Im} \left[M_{0-0+}^* M_{0-++} \right] \sim \text{Im} \left[\langle H_T \rangle \langle \tilde{E} \rangle^* \right]$$

no data at small ξ

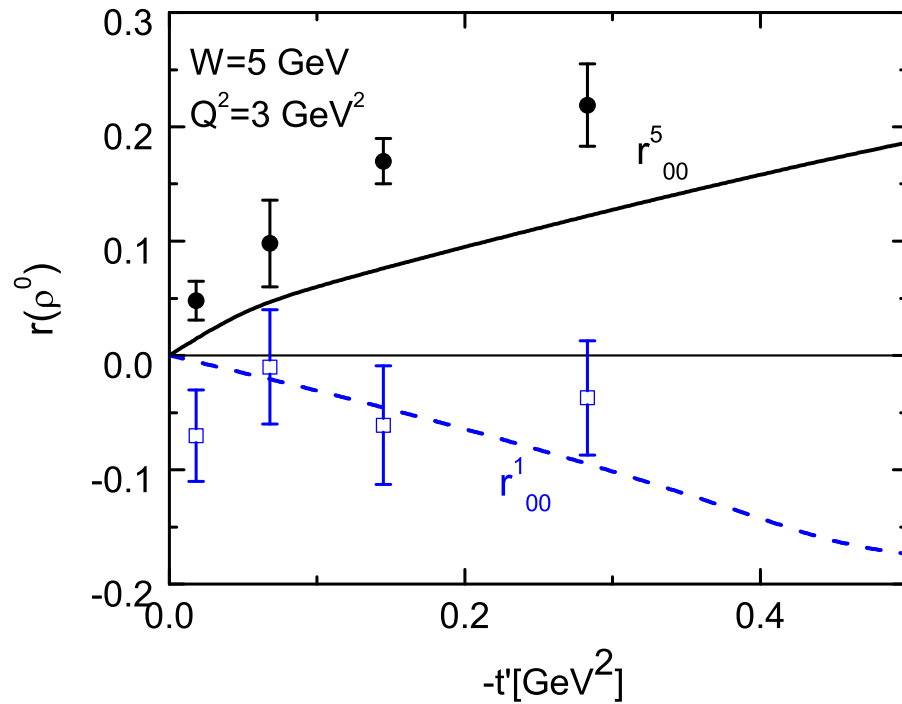
data on π^0 production at larger ξ from CLAS - small but non-zero

from our GPDs: both quantities practically zero -

underestimate of H_T and/or $\tilde{E}_{n.p.}$?

see als deep dip of forward cross section

Transversity in vector meson electroproduction?



SDME for ρ^0 production
data [HERMES](#)

$$r^5_{00} \sim \text{Re}[\mathcal{M}_{0+0+}\mathcal{M}^*_{0+++}]$$

$$r^1_{00} \sim -|\mathcal{M}_{0+++}|^2$$

twist-3 effect $\sim m_\rho/Q$ (not enhanced by chiral condensate)

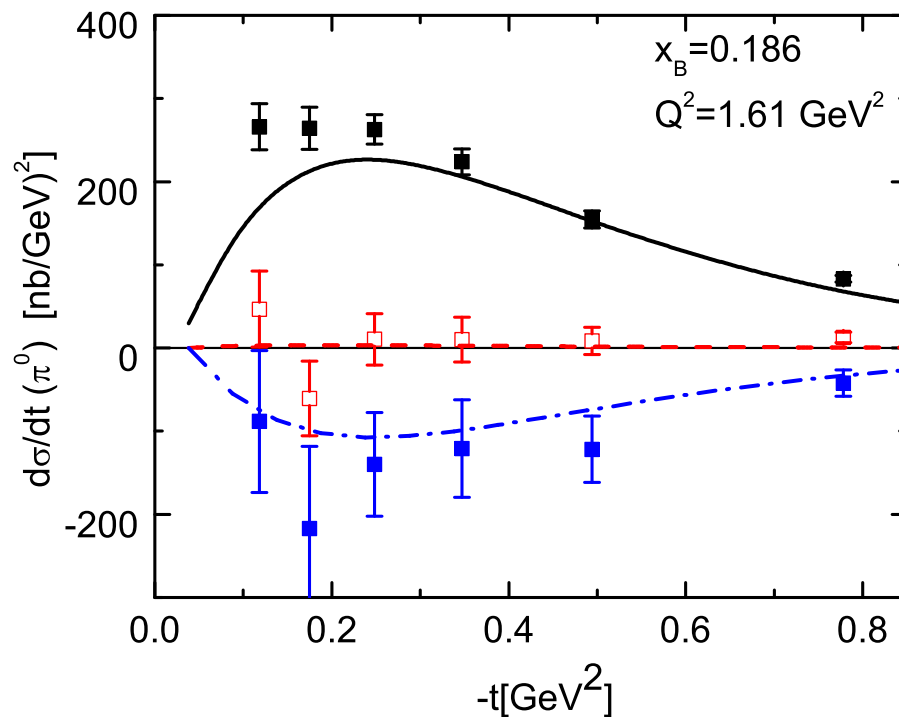
Summary

- analysis of pseudoscalar meson electroproduction within handbag approach complicated, many GPDs contribute
- clear indications in data (CLAS, HERMES) for strong contributions from $\gamma_T^* \rightarrow \pi$ transitions
- within handbag approach $\gamma_T^* \rightarrow \pi$ transitions are related to transversity (helicity-flip) GPDs accompanied by a twist-3 pion wave fct.
- H_T constrained by transversity PDFs - from analysis of A_{UT} for SIDIS
 \overline{E}_T constrained by lattice results
- fit to HERMES π^+ data and interesting predictions for other channels
- trends and magnitudes of large ξ CLAS data reproduced

CLAS result for π^0 production

CLAS results at low W , i.e. at large skewness

Quantitative comparison with our results is to be done with utmost caution (cf. difficulties with ρ^0 production)



prel. Data: CLAS

unseparated cross section

σ_{LT}

σ_{TT}

see also Hall A (dip)