Attributes of molecule-like exotics in the heavy sector

- Interlude on EFTs
- The "Exotic" Spectrum X(3872), Y, Z, ...
- Observables that test the molecular hypothesis in
  - $X(3872) D^{(-)} 0, (*)$  scattering
  - $X(3872) \rightarrow \psi(2S)\gamma$
  - $\psi(4040) \rightarrow X(3872)\gamma$
  - $\psi(4160) \rightarrow X(3872)\gamma$
- (Example of a thing that is probably not a molecule)
- Candidates for molecules in the b-sector

R.P. Springer Duke University "Light Nuclei from First Principles" 4 Oct 2012



**Examples of Effective Theories** 

- Newton's laws
- Thermodynamics
- Fluid Dynamics
- Gravity
- Quantum Electrodynamics
- Standard Model of Nuclei and Particles

Attributes of Effective Field Theories (EFTs)

- Utilize separation of scales => create small parameter
- Based upon underlying (perhaps approximate) symmetries
- Reliable error estimates from order of calculation
- Systematically improvable
- May be used to probe unknown underlying theory
- May be used to simplify calculations in known theories
- Typically contain unknown (by the EFT) coefficients that have to be fixed via experiment or other means
- Coefficient fixed from any exp for which EFT is valid true for \*all\* observables in that EFT
- Typically valid only in a limited energy window

An Effective Quantum Field Theory for low energy light-light scattering Scales:  $m_e \sim 511 \text{ keV}$   $E_{\gamma} << m_e$  $\tilde{F}^{\mu\nu} = F_{\alpha\beta} \ \epsilon^{\mu\nu\alpha\beta}$ Symmetry: Lorentz invariance  $\mathcal{L} = -\frac{1}{4} F^{\mu\nu} F_{\mu\nu} + \frac{c_1}{m_{\perp}^4} (F^{\mu\nu} F_{\mu\nu})^2 + \frac{c_2}{m_{\perp}^4} (F^{\mu\nu} \tilde{F}_{\mu\nu})^2$  $F_{\mu\nu} = \frac{\partial A_{\mu}}{\partial x^{\nu}} - \frac{\partial A_{\nu}}{\partial x^{\mu}}$  $c = 1 \Rightarrow [L] = [T]$  $\hbar = 1 \Rightarrow [E] = [T]^{-1} = [L]^{-1}$  $\int_{-\infty}^{\infty} = c_1 \frac{E_{\gamma}^4}{m_e^4} \int_{-\infty}^{\infty} + \cdots$ (from J. Gasser, **MENU 07)** 



 $\alpha_s \stackrel{1}{[}$  Symmetry  $\alpha_s \sim 1$  Symmetry  $\alpha_s \ll 1$  but vert but vert  $\alpha_s \ll 1$   $\swarrow$  E (GeV)

In the absence of a

solution to QCD, use EFT

=> contains predictions

of QCD as a subset

Symmetry (group) structure works for ground states, but we need dynamics for excited states

# Limits of QCD where symmetries are enhanced $0 \leftarrow m_u < m_d < m_s \mid m_c < m_b < m_t \to \infty$ $^{\frown}\Lambda_{QCD}$ $\mathcal{L}_{QCD}^{light} = \sum \left( \overline{q}_{iL} i D q_{iL} + \overline{q}_{iR} i D q_{iR} \right)$ $-\sum \left[ (\overline{q}_{iL}m_{ij}q_{jR} + \overline{q}_{iR}m_{ij}q_{jL}) \right]$ ij $m_a = diag(m_u, m_d, m_s)$ $q_{iR} \to R_{ij}q_{jR}$ $q_{iL} \rightarrow L_{ij}q_{jL}$ $L \epsilon SU(3)_L$ $R \epsilon SU(3)_R$ $\frac{m_q, p}{\Lambda_{\gamma}}$

$$\mathcal{L}_{QCD}^{heavy} = \overline{Q}(i \not\!\!\!D - m_Q) Q \rightarrow \overline{h}_v^{(Q)} iv.Dh_v^{(Q)}$$

$$Q = e^{-im_Q v.x} (h_v^{(Q)} + \xi_v^{(Q)})$$
small
$$p_Q^{\mu} = m_Q v^{\mu} + k^{\mu}$$

$$\mathbf{Heavy Meson Multiplets} \quad c\overline{q}$$

$$s_l \text{ and } s_Q = 1/2 \text{ separately conserved}$$

$$|D(0^-)\rangle = |00\rangle = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) \qquad \text{ light}$$

$$\frac{k}{m_Q} \quad HQET + \chi PT = HH\chi PT \qquad \text{heavy}$$

# Collect into Supermultiplets

$$H_{a} = \frac{1 + \psi}{2} \begin{bmatrix} P_{a}^{*\mu} \gamma_{\mu} - P_{a} \gamma_{5} \end{bmatrix} \qquad S_{a} = \frac{1 + \psi}{2} \begin{bmatrix} \mathcal{P}_{a}^{*\mu} \gamma_{\mu} \gamma_{5} - \mathcal{P}_{a} \end{bmatrix} \\ \uparrow \qquad \qquad (D^{*(0,+)}, D_{s}^{*}) \qquad (D^{0,+}, D_{s}) \qquad \qquad (D_{1}^{(0,+)}, D_{s1})$$

$$\mathcal{L} = -\mathrm{Tr}[\overline{H}_{a}(iv.D_{ab} - \delta_{H})H_{b}] + Tr[\overline{S}_{a}(iv.D_{ab} - \delta_{S})S_{b}] + g\,\mathrm{Tr}[\overline{H}_{a}H_{b}A_{ba}\gamma_{5}] + g'\,\mathrm{Tr}[\overline{S}_{a}S_{b}A_{ba}\gamma_{5}] + h\,(\mathrm{Tr}[\overline{H}_{a}S_{b}A_{ba}\gamma_{5}] + h.c.)$$

$$D^{*+} \xrightarrow{p^{\mu}} D^{+}$$

$$\xi = e^{iM/f} \quad D^{\mu} = \partial^{\mu} + V^{\mu}$$

$$\int_{\pi^{0}}^{\pi^{0}} -\frac{g \ p.\epsilon}{f\sqrt{2}}$$

$$V^{\mu} = \frac{1}{2}(\xi \partial^{\mu} \xi^{\dagger} + \xi^{\dagger} \partial^{\mu} \xi)$$

$$A^{\mu} = \frac{i}{2}(\xi \partial^{\mu} \xi^{\dagger} - \xi^{\dagger} \partial^{\mu} \xi)$$





X,Y,Z states from Table 9, Brambilla et al. 1010.5827



Techniques/Descriptions/Strategies **OCD** Sum Rules Non-relativistic QCD Heavy Quark Effective Theory Heavy Hadron Chiral Perturbation Theory X-EFT **Potential Models** Lattice **Mixtures** Molecule Baryonium Tetraquark **Hybrids Coupled channels** Hadrocharmonium

# Molecules: do the constituents retain their identify as hadrons? (more details in the X(3872) section)

X(3872)	$\overline{D}^0 D^{*0}$	
X(3915)	$\overline{D}^{*0}D^{*0} + D^{*+}D^{*-}$	BGL
Y(4140)	$D_{s}^{*+}D_{s}^{*-}$	BGL
Y(4260)	$D_0 \overline{D}^*, \psi(2S) f_0(980)$ $\Lambda_c \overline{\Lambda}_c, \chi_{c0} \rho, \chi_{c1} \omega, D_1 \overline{D}$	AN,TKGO Q,LZL,YWM,R
$Z(4430)^+$	$D^{*+}\overline{D}_1^0$	LMNN/BGL
X(4630)	$\psi(2S)f_0(980)$	GHHM
Y(4660)	$\psi(2S)f_{0}(980)$	GHM

BGL=Branz,Gutsche,Lyubovitskij LMNN=Lee,Miharo,Navarro,Nielsen TKGO=Torres,Kehmchandari,Gamermann,Oset AN=Albuquerque,Nielsen Q=Qiao LZL=Liu,Zeng,Li YWM=Yuan,Wang,Mo R=Rosner GH(H)M=Guo,(Haidenbauer),Hanhart,Meissner

X(3872) as molecule  

$$\frac{1}{\sqrt{2}} \left( D^0 \overline{D}^{0*} + \overline{D}^0 D^{0*} \right) \qquad X(3872) \to J/\psi\gamma \Rightarrow C = +$$
S-wave  $X(3872) \to \pi^+ \pi^- J/\psi$ 

 $\Gamma < 1.2 \text{ MeV}$ 

Isospin issue:

 $\frac{\Gamma[X \to J/\psi \pi^+ \pi^- \pi^0]}{\Gamma[X \to J/\psi \pi^+ \pi^-]} =$ 

Belle 2011 PRD 84,052004 Hanhart et al 1111.6241

$$\frac{\Gamma[X \to J/\psi\omega]}{\Gamma[X \to J/\psi\pi^+\pi^-]} = 0.8 \pm 0.3 \qquad \text{BaBar 2010}$$

 $J^{PC} = 1^{++} \text{ or } 2^{-+}$  multipole question

 $m_{D^0\bar{D}^{0*}} - m_{X(3872)} = 0.16 \pm 0.33 \text{ MeV}$ 

Like the Deuteron? Systematic NN treatment: NN-EFT (no pions) Only now it is an infinite sum of  $(\overline{D}D^* + cc)$  or  $(\overline{B}^*B^{(*)} + cc)$  etc.  $\times$  +  $\times$ + $A = \mathcal{C} + i\mathcal{C}^2 \frac{Mp}{4\pi} + \mathcal{C}^3 \left(\frac{Mp}{4\pi}\right)^2$  $A = \frac{4\pi}{M} \left[ -a + ia^2 p + \frac{1}{2} (a^3 - a^2 r_0) p^2 + \cdots \right]$ does not converge NN system:  $a^{(^1S_0)} \sim -\frac{1}{8 \text{ MeV}}$  $a^{(^{3}S_{1})} \sim \frac{1}{36 \text{ MeV}}$ 

> Both S-wave scattering lengths anomalously large => momentum expansion fails = reorganize to treat C's nonperturbatively

$$A = -\frac{4\pi}{M} \frac{1}{1/a + ip} + \cdots$$

$$A = -\frac{4\pi}{M} \frac{1}{1/a + ip} + \cdots$$

with effective range:

 $A = -\frac{1}{M}\frac{1}{a - \frac{1}{2}rp^2 + ip} + \frac{1}{2}rp^2 + \frac$ EM effects easily included

#### Evidence that pionless EFT works in strong and EM sector Chen,Rupak,Savage nucl-th/9902056v4



FIG. 1. The phase shift  $\delta_0$  as a function of the center of mass momentum  $|\mathbf{k}|$ . The dashed curve corresponds to  $\delta_0^{(0)}$ , the dotted curve corresponds to  $\delta_0^{(0)} + \delta_0^{(1)}$ , the solid curve corresponds to  $\delta_0^{(0)} + \delta_0^{(1)} + \delta_0^{(2)}$ , and the dot-dashed curve is the Nijmegen partial wave analysis [35].





FIG. 3. The form factor  $A(q^2)$  as a function of  $|\mathbf{q}| = \sqrt{-q^2}$ . The dashed curve corresponds to the leading order prediction, the dotted curve corresponds to the next-to-leading order prediction, and the solid curve corresponds to the next-to-next-to-leading order prediction, in EFT( $\not{\pi}$ ).

X-Effective Field Theory: Fleming, Kusunoki, Mehen, van Kolck



Factorization theorems: Braaten/Kusunoki/Lu

Rate = 
$$\frac{1}{3} \sum_{\lambda} |\langle 0| \frac{1}{\sqrt{2}} \epsilon_i(\lambda) (V^i \bar{P} + \bar{V}^i P) |X(3872, \lambda) \rangle|^2$$
  
  $\times \text{ (phase space)} \times |\mathcal{C} (\overline{D} D^* \to f)|^2$ 

Universal shallow-bound-state properties from effective range theory: Braaten/Voloshin...

$$\psi_{DD^*}(r) \propto \frac{e^{-\gamma r}}{r} \quad B = \frac{1}{2\mu_{D^*D}a^2} \quad \begin{array}{l} \gamma \sim 20 \text{ MeV} \\ a \sim 10 \text{ fm} \\ \langle r \rangle \sim 12 \text{ fm} \end{array}$$

 $X(3872) - D^{(*)}$  scattering Canham/Hammer/RPS **IF**  $X(3872) \sim \frac{1}{\sqrt{2}} (D^0 \overline{D}^{*0} + D^{*0} \overline{D}^0)$  $m_X = (3871.68 \pm 0.17) \text{ MeV}$   $B_X = (0.16 \pm 0.36) \text{ MeV}$  $a^{-1} \sim \sqrt{2\mu_X B_X}$  $\mathcal{L} = \sum_{j=D^0, D^{*0}, \bar{D}^0, \bar{D}^{*0}} \psi_j^{\dagger} \left( i\partial_t + \frac{\nabla^2}{2m_j} \right) \psi_j + \Delta X^{\dagger} X$  $-\frac{g}{\sqrt{2}} \left( X^{\dagger}(\psi_{D^{0}}\psi_{\bar{D}^{*0}} + \psi_{D^{*0}}\psi_{\bar{D}^{0}}) + \text{h.c.} \right) + \cdots$ 

Integral equation:



Results depend only on scattering length  $a_{D^0X} = -9.7a$   $a_{D^{*0}X} = -16.6a$ 

#### Three body cross section vs scattering length



LHC possibilities: $B_c \sim 10^7$  per week $B\overline{B}$ final state interactions $\sigma(b\overline{b}) \sim 0.4$  mb $\sigma(b\overline{b}b\overline{b}) \sim 5$  fb





Polarization measurement would shed light on relative importance of decay mechanisms

• Polarization as function of  $\lambda \equiv \frac{3c_1}{g_2\beta} \approx 1.3 \frac{c_1}{\text{GeV}^{-5/2}} \sim O(1)$ 



• 
$$X(3872)$$
 as  $2^{-+}$  :  $\alpha = 0.08$ 



 $\psi(4040) \rightarrow X(3872)\gamma$ 

$$g_2 \to \tilde{g}_2; \quad c_1 \to \tilde{c}_1$$
  
 $E_\gamma \sim 165 \text{ MeV}$ 

Suppose g-like terms dominate:  $|M(X)|^2 > 0.09 \text{ GeV}^3$ from  $\Gamma(X(3872) \rightarrow \psi(2S)\gamma)$   $(\tilde{g}_2)^2 < 0.63 \text{ GeV}^{-3}$ from width of  $\psi(4040)$ 

 $(\tilde{g}_2)^2 \sim 0.17 \ {\rm GeV}^{-3}$ 

from quark model hep-ph/0511179

 $\Rightarrow \Gamma[\psi(4040) \rightarrow X(3872)\gamma] \\ \sim (0.005 - 0.02) \text{ MeV}$ 

 $\psi(4160) \rightarrow X(3872)\gamma$ 

$$n^{(2s+1)}L_J = 1^3 D_1 \qquad \qquad J^{PC} = 1^{--}$$
$$J^{ij} = \frac{1}{2}\sqrt{\frac{3}{5}} \left(\sigma^i \psi^j + \sigma^j \psi^i - \frac{2}{3}\delta^{ij}\sigma \cdot \psi\right) + \cdots$$

$$\mathcal{L} = i\frac{\bar{g}}{2} \operatorname{Tr} \left[ J^{ij} \bar{H}^{\dagger} \sigma^{i} \overleftrightarrow{\partial^{j}} H^{\dagger} \right] + \frac{\bar{c}}{2} \operatorname{Tr} \left[ J^{ij} \bar{H}^{\dagger} \sigma^{i} E^{j} H^{\dagger} \right] + \text{h.c.}$$



Preliminary Margaryan Mehen RPS

# An example of possible "exotics " that appear *not* to be molecules



$$1^+, 2^+$$
  $D_1^{(0,+)} D_{s1} D_2^{(0,+)} D_{s2}$ 

$$m_c \to \infty$$

$$m_u, m_d, m_s \to 0$$
  $0^+, 1^+ \overline{D_0^{(0,+)} D_{s0} D_1^{\prime(0,+)} D_s^{\prime}}$ 

$$0^-, 1^- \ \overline{D^{(0,+)} \ D_s \ D^{*(0,+)} \ D_s^*}$$

Corrections : 
$$\frac{(m_q, p)}{(\Lambda_{\chi}, m_Q)}$$
  $SU(3)?$ 

 $D^* - D \sim D_s^* - D_s \sim D_{s1}' - D_{s0} \sim 140 MeV$ 

# Electromagnetic Decays of $0_s^+$ and $1_s^+$



$$\frac{D_{s0}(2317) \to D_s^* \gamma}{D_{s0}(2317) \to D_s \pi^0} < 0.059$$
(CLEO)

$$\frac{D'_{s1}(2460) \to D^*_s \gamma}{D'_{s1}(2460) \to D^*_s \pi^0} < 0.16$$

 $Q^{\xi} = \frac{1}{2} (\xi Q \xi^{\dagger} + \xi^{\dagger} Q \xi)$ 

 $\frac{D'_{s1}(2460) \to D_s \gamma}{D'_{s1}(2460) \to D_s^* \pi^0} = 0.55 - 0.38 \quad \text{(Belle)}$  $0.38 - 0.27 \quad \text{(BaBar)}$ 

$$\mathcal{L}_{em} = \frac{e}{4} \tilde{\beta} \left[ \overline{H}_a S_b \sigma^{\mu\nu} F_{\mu\nu} Q_{ba}^{\xi} \right]$$
  
corrections :  $\frac{\Lambda_{QCD}}{m_c} \sim \frac{m_s}{\Lambda_{\chi}} \sim 30\%$ 

#### $D_{s0}, D'_{s1}$ as molecules?



 $\Gamma(D_{s1} \to D_s^* \gamma) = \frac{8g^2 \alpha^2}{3f^2} \frac{m_{D^*} m_{D_s^*}}{m_{Ds1}^3} |\Psi_{D^*K}(0)|^2 E_{\gamma}$   $\Gamma(D_{s1} \to D_s \gamma) = \frac{4g^2 \alpha^2}{3f^2} \frac{m_{D^*} m_{D_s}}{m_{Ds1}^3} |\Psi_{D^*K}(0)|^2 E_{\gamma}$  $\Gamma(D_{s0} \to D_s^* \gamma) = \frac{4g^2 \alpha^2}{f^2} \frac{m_{D} m_{D_s^*}}{m_{Ds0}^3} |\Psi_{DK}(0)|^2 E_{\gamma}$ 

 $m_Q \rightarrow \infty$  2:1:3 phase space  $1.57:1:R_{\Psi}1.58$  cf. to exp. limits

#### Strong Decay of Molecules



Predicts  $(\pm 30\%)$ :

$$\frac{D_{s1} \to D_s^* \gamma}{D_{s1} \to D_s^* \pi^0} = 3.23 \quad (\exp < 0.16)$$

problem ratios

 $\rightarrow$  molecular hypothesis

$$\frac{D_{s1} \to D_s \gamma}{D_{s1} \to D_s^* \pi^0} = 2.21 \quad (\exp \sim 0.44)$$

disfavored

$$\frac{D_{s0} \to D_s^* \gamma}{D_{s0} \to D_s \pi^0} = 2.96 \quad (\exp < 0.059)$$

$$\Gamma(D_{s1} \to D_s^* \pi^0) = \frac{3(m_K + E_{\pi^0})^2}{4\pi f^4} \theta^2 \frac{m_{D^*} m_{D_s^*}}{m_{Ds1}^3} |\Psi_{D^*K}(0)|^2 |\vec{p}_{\pi^0}|$$

$$\Gamma(D_{s0} \to D_s \pi^0) = \frac{3(m_K + E_{\pi^0})^2}{4\pi f^4} \theta^2 \frac{m_D m_{D_s}}{m_{D_{s0}}^3} |\Psi_{DK}(0)|^2 |\vec{p}_{\pi^0}|^2$$

#### b Exotics above threshold - Belle 1103.3419



Eidelman, Heltsley, Hernandez-Rey, Navas, Patrignani 1205.4189

#### $Z_b$ as a molecule

HQET predicts additional states (Voloshin...)

$$\begin{split} W_{0} &= 1^{-}(0^{+}) = \frac{1}{2}0^{-}_{b\bar{b}} \times 0^{-}_{l\bar{t}} - \frac{\sqrt{3}}{2} \left(1^{-}_{b\bar{b}} \otimes 1^{-}_{l\bar{t}}\right)_{J=0} \\ Z_{b} &= 1^{+}(1^{+}) = \frac{1}{\sqrt{2}} \left(0^{-}_{b\bar{b}} \times 1^{-}_{l\bar{t}} + 1^{-}_{b\bar{b}} \otimes 0^{-}_{l\bar{t}}\right) \\ Z'_{b} &= 1^{+}(1^{+}) = \frac{1}{\sqrt{2}} \left(0^{-}_{b\bar{b}} \times 1^{-}_{l\bar{t}} - 1^{-}_{b\bar{b}} \otimes 0^{-}_{l\bar{t}}\right) \\ W'_{0} &= 1^{-}(0^{+}) = \frac{\sqrt{3}}{2}0^{-}_{b\bar{b}} \times 0^{-}_{l\bar{t}} + \frac{1}{2} \left(1^{-}_{b\bar{b}} \otimes 1^{-}_{l\bar{t}}\right) \xrightarrow{\to} \eta_{b}\pi, \chi_{b}\pi, \Upsilon\rho \end{split}$$

Molecule treatment predicts decay ratios among them (Mehen/Powell)

$$\mathcal{L}_{eff} = \cdots - \frac{C_{10}}{4} \operatorname{Tr}[\bar{H}_{a}^{\dagger} \tau_{aa'}^{A} H_{a'}^{\dagger} H_{b} \tau_{bb'}^{A} \bar{H}_{b'}] + - \frac{C_{11}}{4} \operatorname{Tr}[\bar{H}_{a}^{\dagger} \tau_{aa'}^{A} \sigma^{i} H_{a'}^{\dagger} H_{b} \tau_{bb'}^{A} \sigma^{i} \bar{H}_{b'}].$$

$$H_{a} = P_{a} + \vec{V} \cdot \vec{\sigma} \qquad \text{now } B^{(*)} \text{ multiplet rather than } D^{(*)} \text{ multiplet}$$

$$\Gamma[W_{0} \to \chi_{b1}\ell]: \Gamma[W_{0}' \to \chi_{b1}\ell]: \Gamma[Z \to h_{b}\ell]: \Gamma[Z' \to h_{b}\ell] = \frac{3}{2}: \frac{1}{2}: 1:1$$

## Summary

Many new "exotic" unexpected particles discovered at B factories X(3872) may be a molecular bound state of the  $D^0$  and  $\overline{D}^{0*}$  mesons. If so, it must have  $J^{PC} = 1^{++}$ 

Measurements needed to check molecular hypothesis:

- a.  $D^{0(*)}, \overline{D}^{0(*)}$  scattering enhancement
- b. polarization of  $\psi(2S)$  in decay
- c. polarization of X(3872) in creation

Possible analogues seen in bottomonium-like system

Again, additional data needed to prove or disprove characterLHC, BESIII, ... exciting times ahead for heavy quark spectroscopy and our ability to understand bound states of QCDWill this "cleaner" system shed light on nuclear bound states?

## Additional Slides

#### Baru et al 1108.5644



#### Amplitudes

$$a) = -\frac{g_{2}e\beta}{3}\frac{1}{E_{\gamma} + \Delta}(\vec{k} \cdot \vec{\epsilon}_{\psi}^{*} \vec{\epsilon}_{D^{*}} \cdot \vec{k} \times \vec{\epsilon}_{\gamma}^{*} - \vec{k} \cdot \vec{\epsilon}_{D^{*}} \vec{\epsilon}_{\psi}^{*} \cdot \vec{k} \times \vec{\epsilon}_{\gamma}^{*})$$

$$b) = \frac{g_{2}e\beta}{3}\frac{1}{\Delta - E_{\gamma}}\vec{k} \cdot \vec{\epsilon}_{\psi}^{*} \vec{\epsilon}_{D^{*}} \cdot \vec{k} \times \vec{\epsilon}_{\gamma}^{*}$$

$$c) = \frac{g_{2}e\beta}{3}\frac{1}{E_{\gamma}}\vec{k} \cdot \vec{\epsilon}_{D^{*}} \vec{\epsilon}_{\psi}^{*} \cdot \vec{k} \times \vec{\epsilon}_{\gamma}^{*}$$

$$d) = -ec_{1}E_{\gamma}\vec{\epsilon}_{D^{*}} \cdot \vec{\epsilon}_{\psi}^{*} \times \vec{\epsilon}_{\gamma}^{*}$$

$$|\mathcal{M}|^{2} = g_{2}^{2}\beta^{2}F_{1}(\Delta, E_{\gamma}) + g_{2}\beta c_{1}F_{2}(\Delta, E_{\gamma}) + c_{1}^{2}F_{3}(E_{\gamma})$$

$$\mathcal{A}(\vec{\epsilon}_{\psi})|^{2} = (2g_{2}^{2}\beta^{2}A^{2}E_{\gamma}^{4} + 4g_{2}\beta c_{1}ACE_{\gamma}^{2} + 2c_{1}^{2}C^{2})|\hat{k} \cdot \vec{\epsilon}_{\psi}|^{2}$$

$$\begin{split} |\mathcal{M}(\vec{\epsilon}_{\psi})|^{2} &= \left(2g_{2}^{2}\beta^{2}A^{2}E_{\gamma}^{4} + 4g_{2}\beta c_{1}ACE_{\gamma}^{2} + 2c_{1}^{2}C^{2}\right)|k \cdot \vec{\epsilon}_{\psi}|^{2} \\ &+ \left(g_{2}^{2}\beta^{2}B^{2}E_{\gamma}^{4} - 2g_{2}\beta c_{1}BCE_{\gamma}^{2} + c_{1}^{2}C^{2}\right)|\hat{k} \times \vec{\epsilon}_{\psi}|^{2} \\ \Delta \sim 142 \text{ MeV}; \quad E_{\gamma} \sim 181 \text{ MeV} \end{split}$$

#### Hadrocharmonium

 $J/\psi, \psi(2S), \ldots$  even  $\Upsilon?$  affinity for light hadronic matter



# Strong Interaction Terms

$$\begin{split} \mathcal{L} &= N^{\dagger} (i\partial_{0} + \frac{\vec{\nabla}^{2}}{2M}) N - \frac{1}{8} \mathcal{C}_{0}^{(^{1}S_{0})} (N^{T} \tau_{2} \tau_{a} \sigma_{2} N)^{\dagger} (N \tau_{2} \tau_{a} \sigma_{2} N) \\ &- \frac{1}{8} \mathcal{C}_{0}^{(^{3}S_{1})} (N^{T} \tau_{2} \sigma_{2} \sigma_{i} N)^{\dagger} (N \tau_{2} \sigma_{2} \sigma_{i} N) + \dots, \\ P_{a}(^{1}S_{0}) &= \frac{1}{\sqrt{8}} \tau_{2} \tau_{a} \sigma_{2} ; \quad P_{i}(^{3}S_{1}) = \frac{1}{\sqrt{8}} \tau_{2} \sigma_{2} \sigma_{i} \\ \mathcal{L} &= N^{\dagger} \left( i\partial_{0} + \frac{\vec{\nabla}^{2}}{2M} \right) N - t_{i}^{\dagger} \left( i\partial_{0} + \frac{\nabla^{2}}{4M} - \Delta_{(^{3}S_{1})} \right) t_{i} \\ &- g_{(^{3}S_{1})} \left[ t_{i}^{\dagger} N^{T} P_{i}(^{3}S_{1}) N + \text{h.c.} \right] \\ \text{"dibaryon"} \\ \text{treatment} &- s_{a}^{\dagger} \left( i\partial_{0} + \frac{\nabla^{2}}{4M} - \Delta_{(^{1}S_{0})} \right) s_{a} \\ &- g_{(^{1}S_{0})} \left[ s_{a} N^{T} P_{a}(^{1}S_{0}) N + \text{h.c.} \right] \end{split}$$