

# Relativistic Core-Collapse Supernova Models

Identifying the Key Elements for Successful  
Neutrino-Driven Explosions

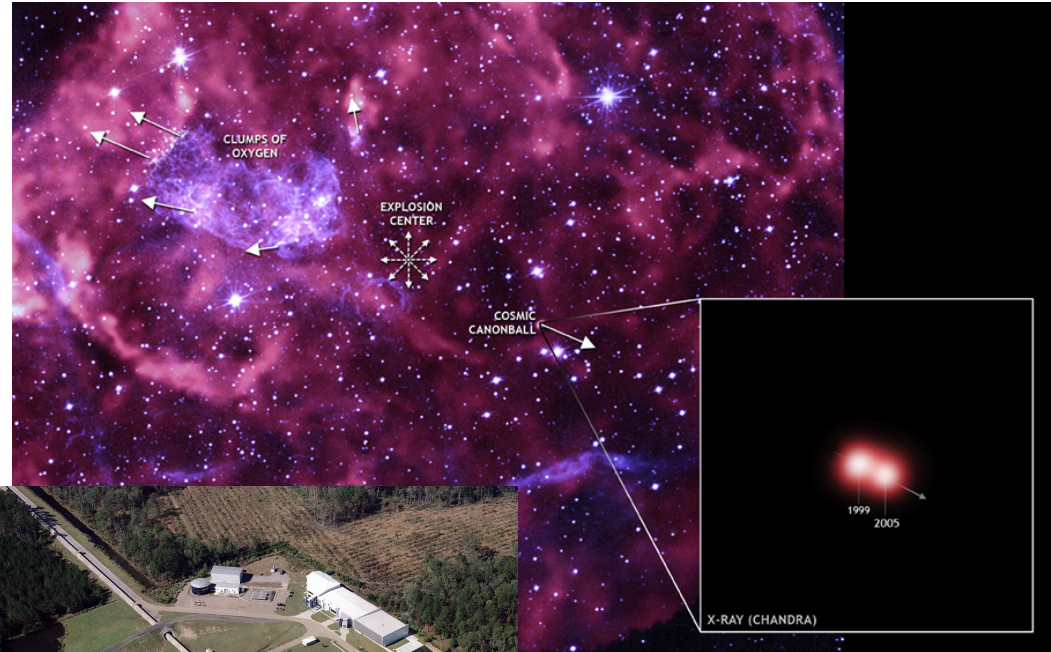
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With H.-Th. Janka, A. Marek, A. Heger

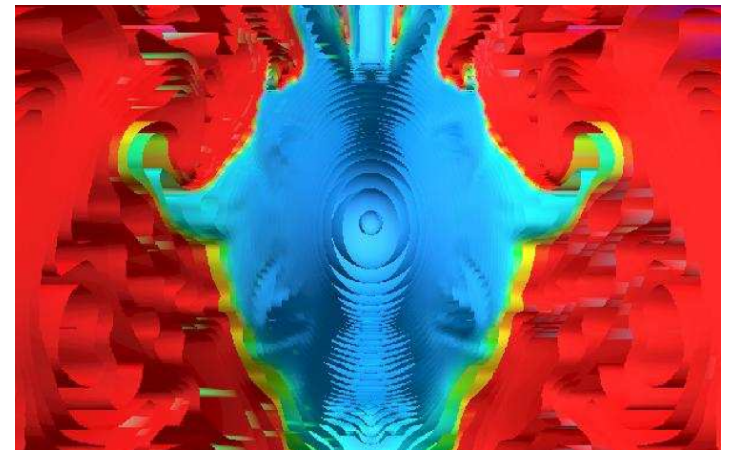
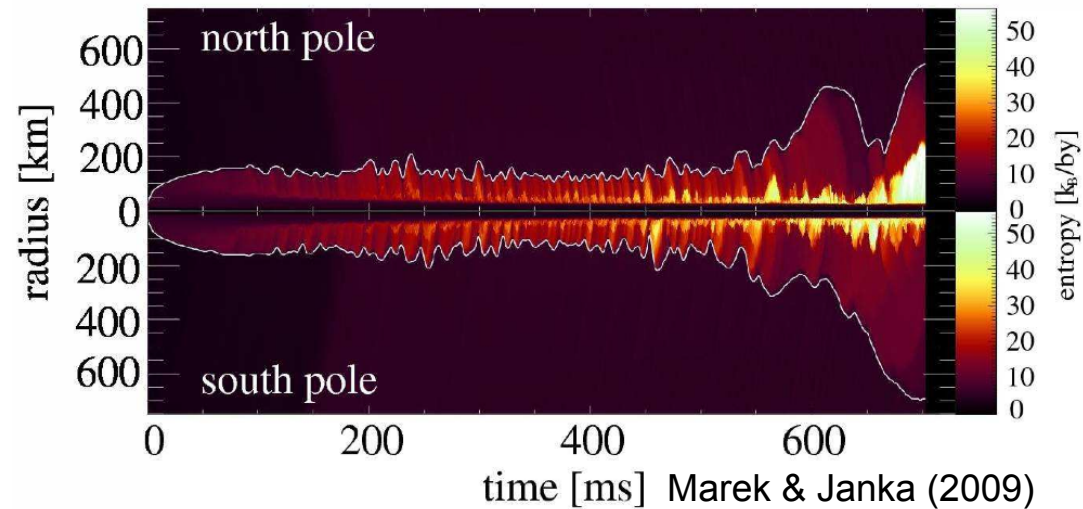
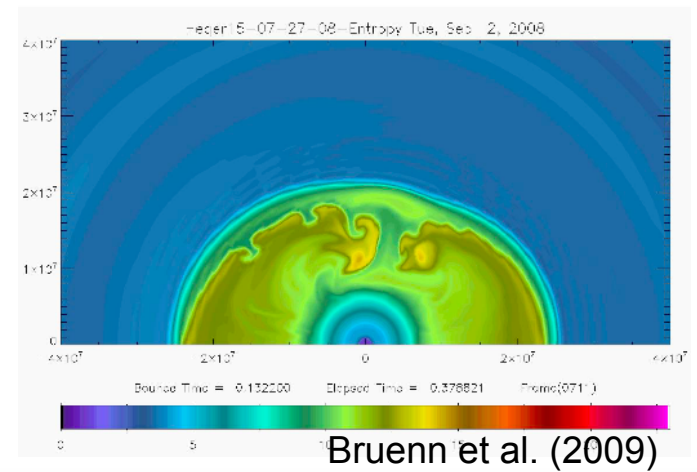
# Major Questions

- How does the “engine” work? Do  $\nu$ -driven explosions work or do we need an alternative?
- What can we observe?
  - Neutrinos – from bounce to cooling
  - Gravitational waves (?)
  - Ejecta morphology
  - Pulsar kicks
  - Nucleosynthesis yields



# Status of Neutrino-Driven Explosions

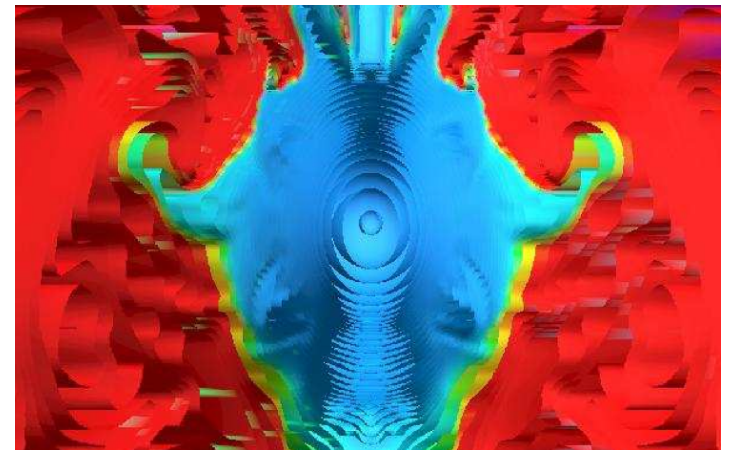
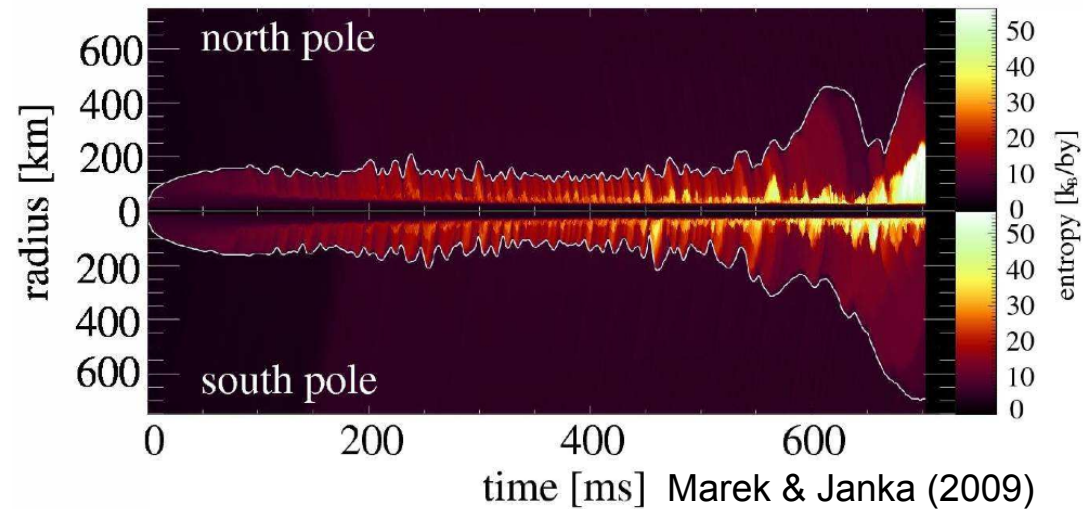
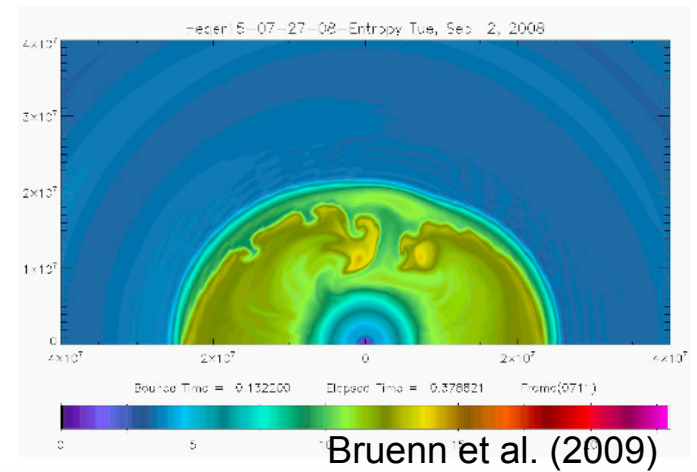
- Axisymmetric multi-group simulations by different groups not yet in agreement
- Concerns: only few weak & late explosions, limited range of progenitors
- Potential ingredients for neutrino-driven explosions to be investigated in more detail:
  - General relativity
  - Neutrino physics
  - 3D effects
  - Equation of state



Burrows et al. 2006: explosion **not** by  $\nu$ -heating, but by "acoustic mechanism"

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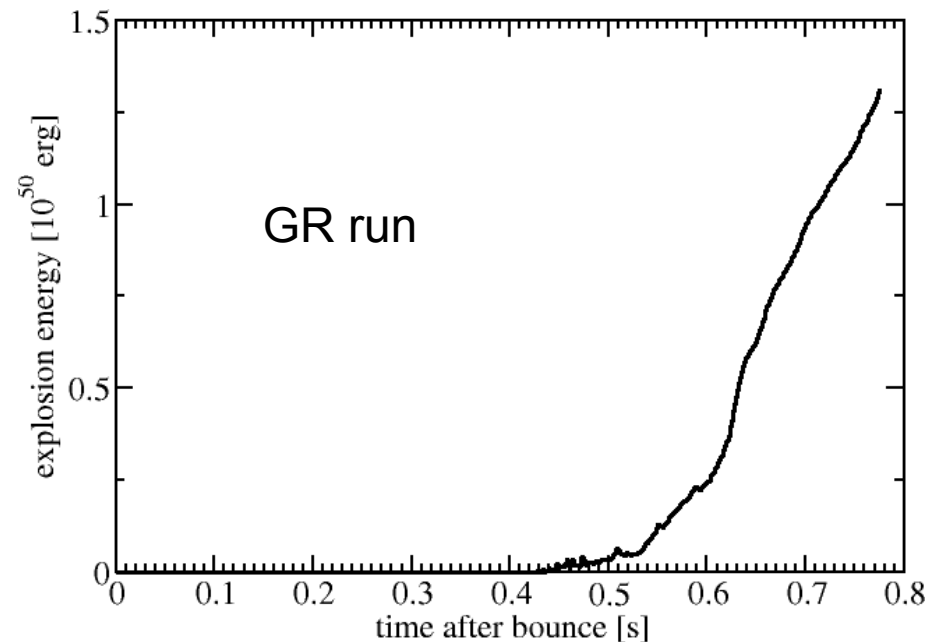
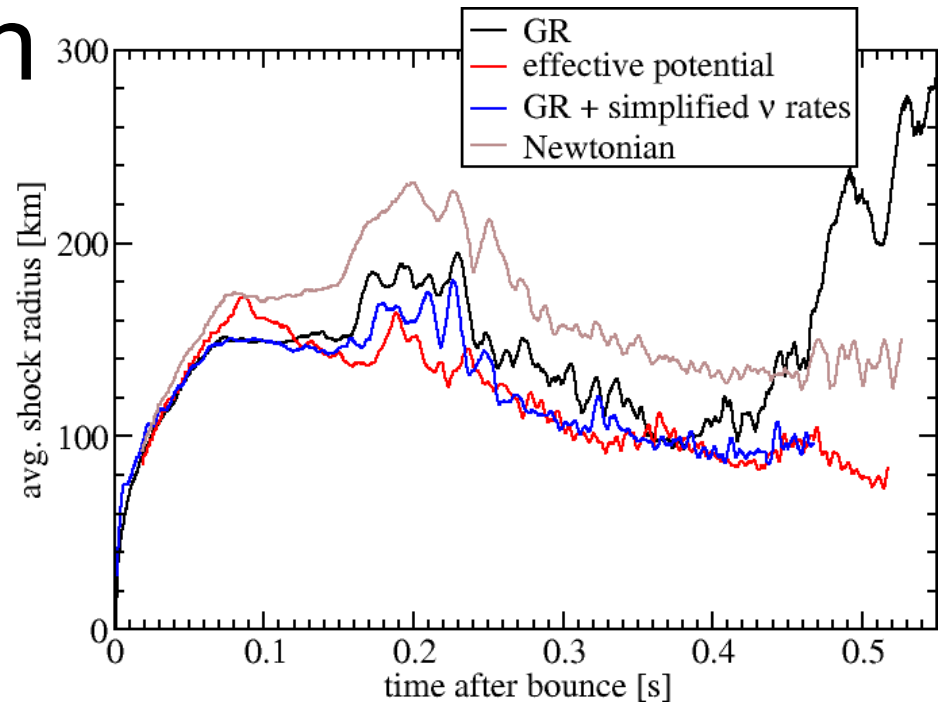
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  - **Neutrino physics**
  - 3D effects —————▶ still controversial, see for example Florian Hanke's talk this afternoon
  - Equation of state

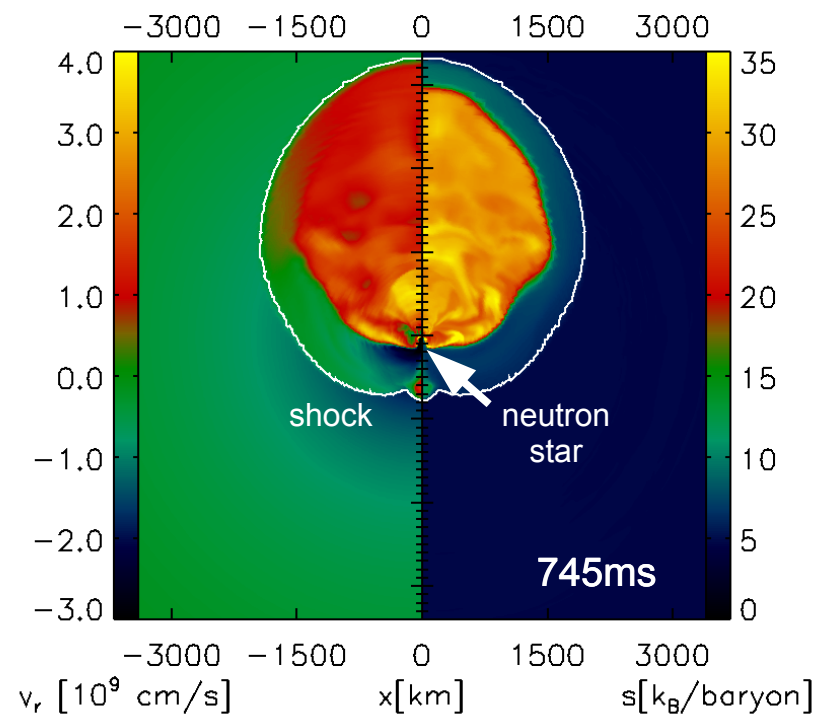
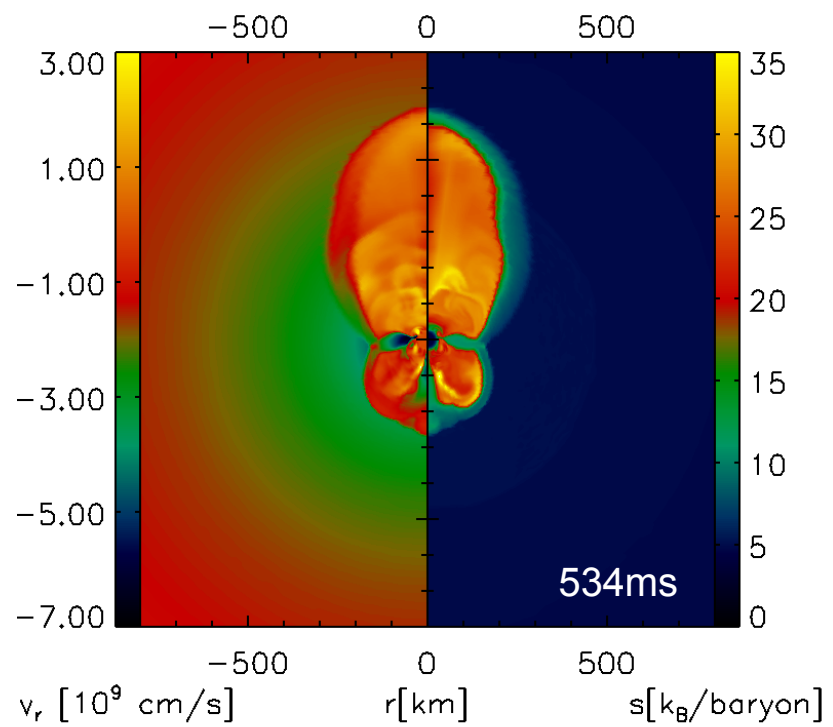
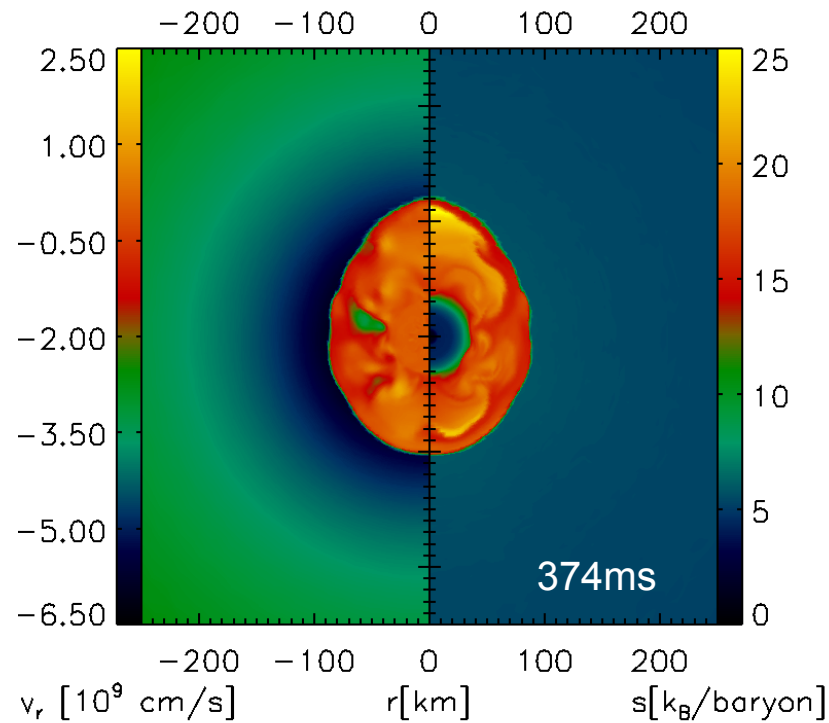
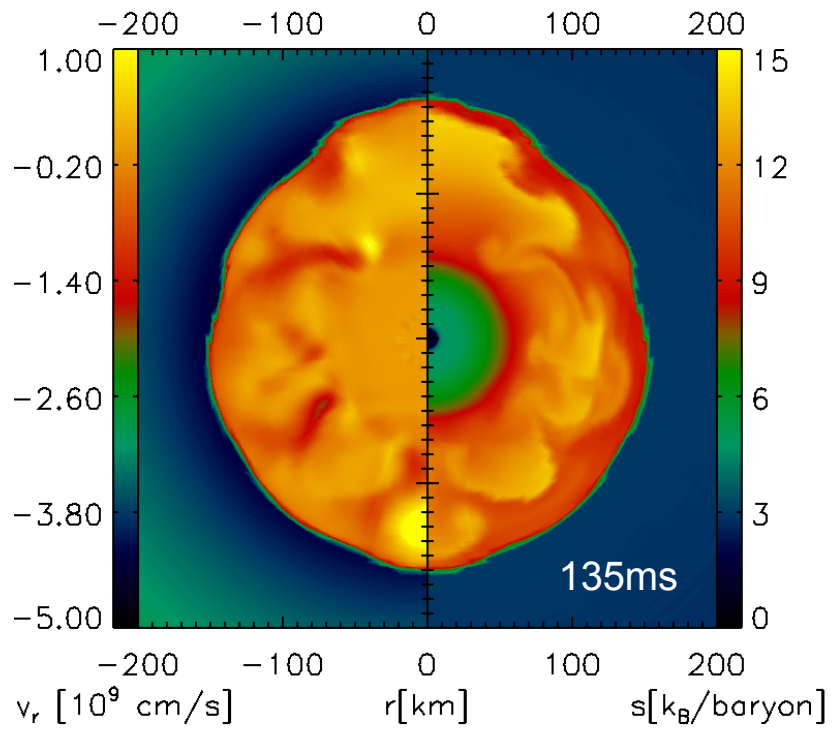


Burrows et al. 2006: explosion **not** by  $\nu$ -heating, but by "acoustic mechanism"

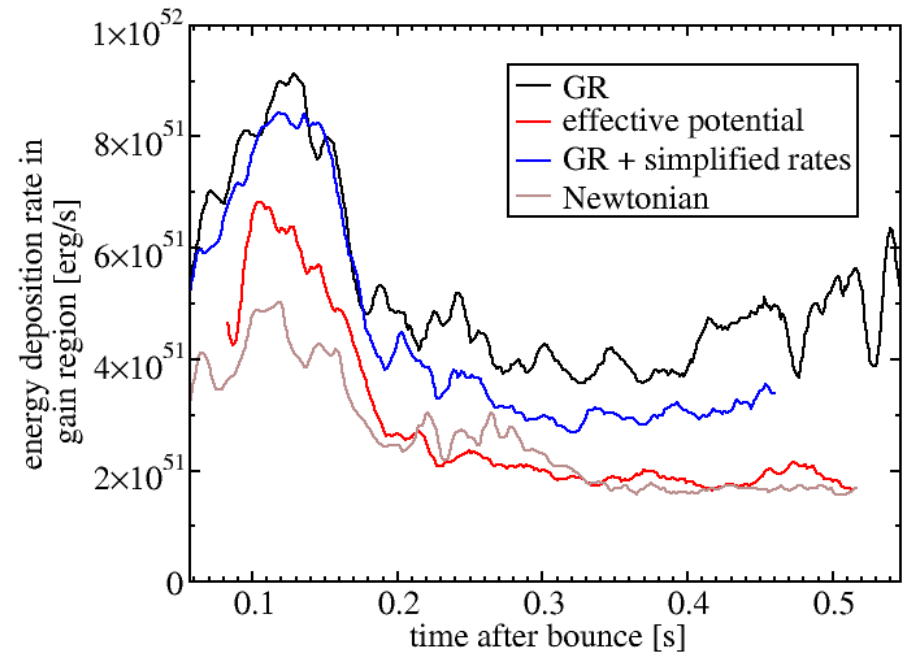
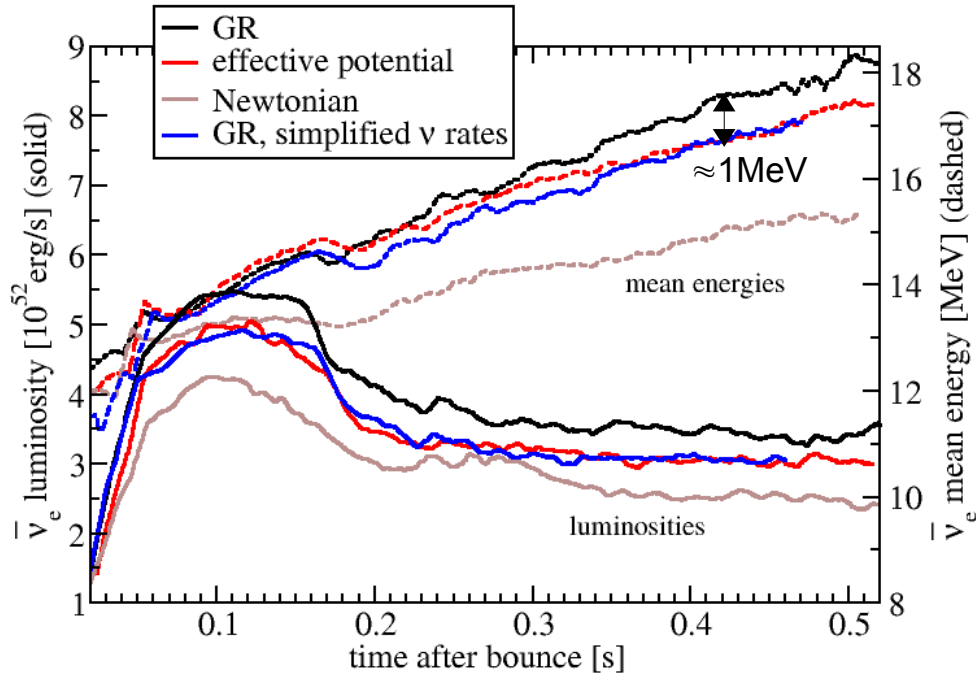
# Ingredients for $\nu$ -driven Explosions

- Detailed neutrino physics & general relativity sometimes dismissed as unimportant, but tests in multi-D required!
- Müller et al. (2012): Detailed comparison of four models using the  $15M_{\odot}$  progenitor of Woosley & Weaver (1995)
  - Newtonian vs. GR
  - Newtonian + “effective” pseudo-GR potential vs. GR
  - Up-to-date neutrino reaction rates vs. simplified rates (e.g. no recoil energy transfer in  $\nu$ -nucleon reactions)
- Only GR model with up-to-date rates explodes  $\rightarrow$  GR and  $\nu$  rates can make a difference!

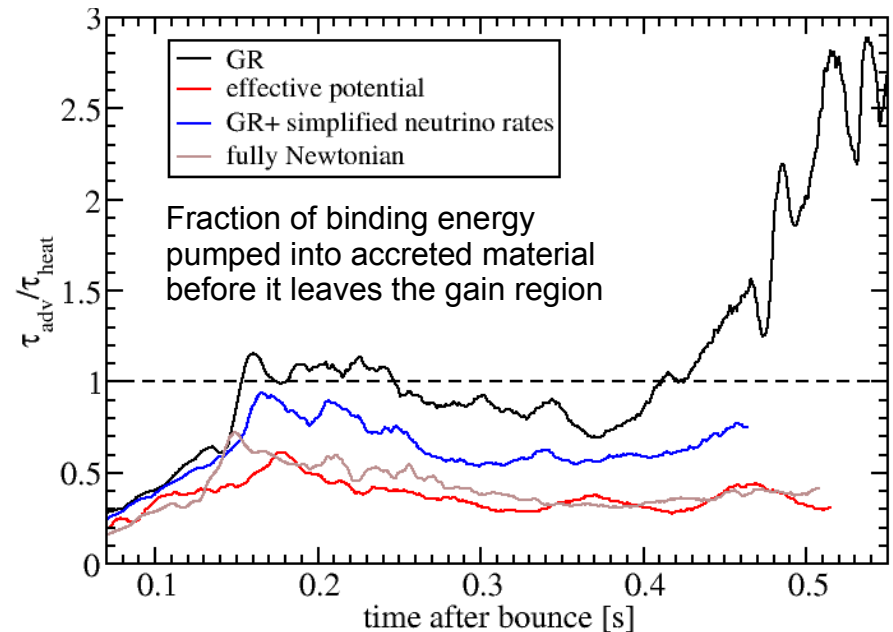




# Systematic Differences in the Heating Conditions

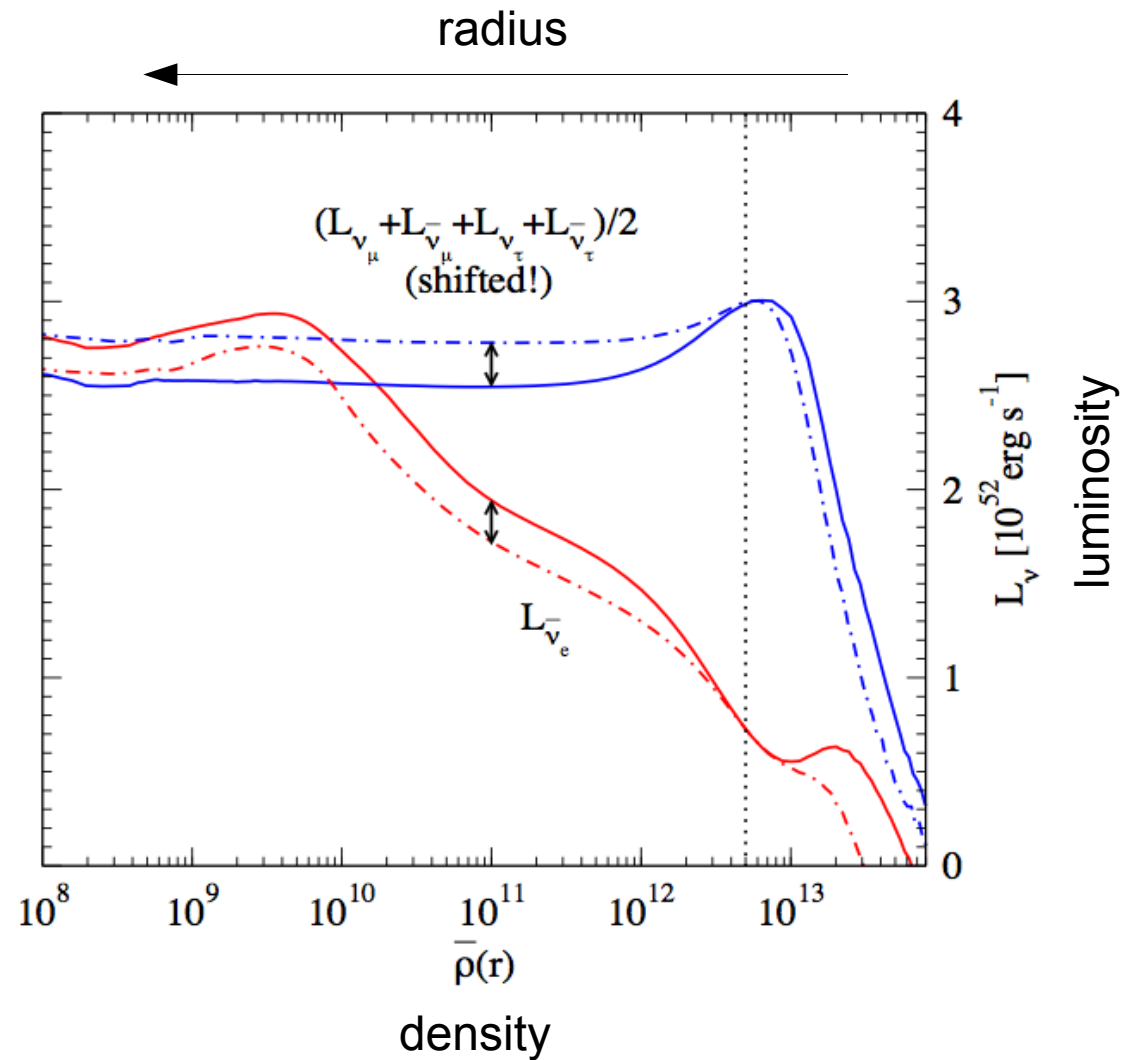
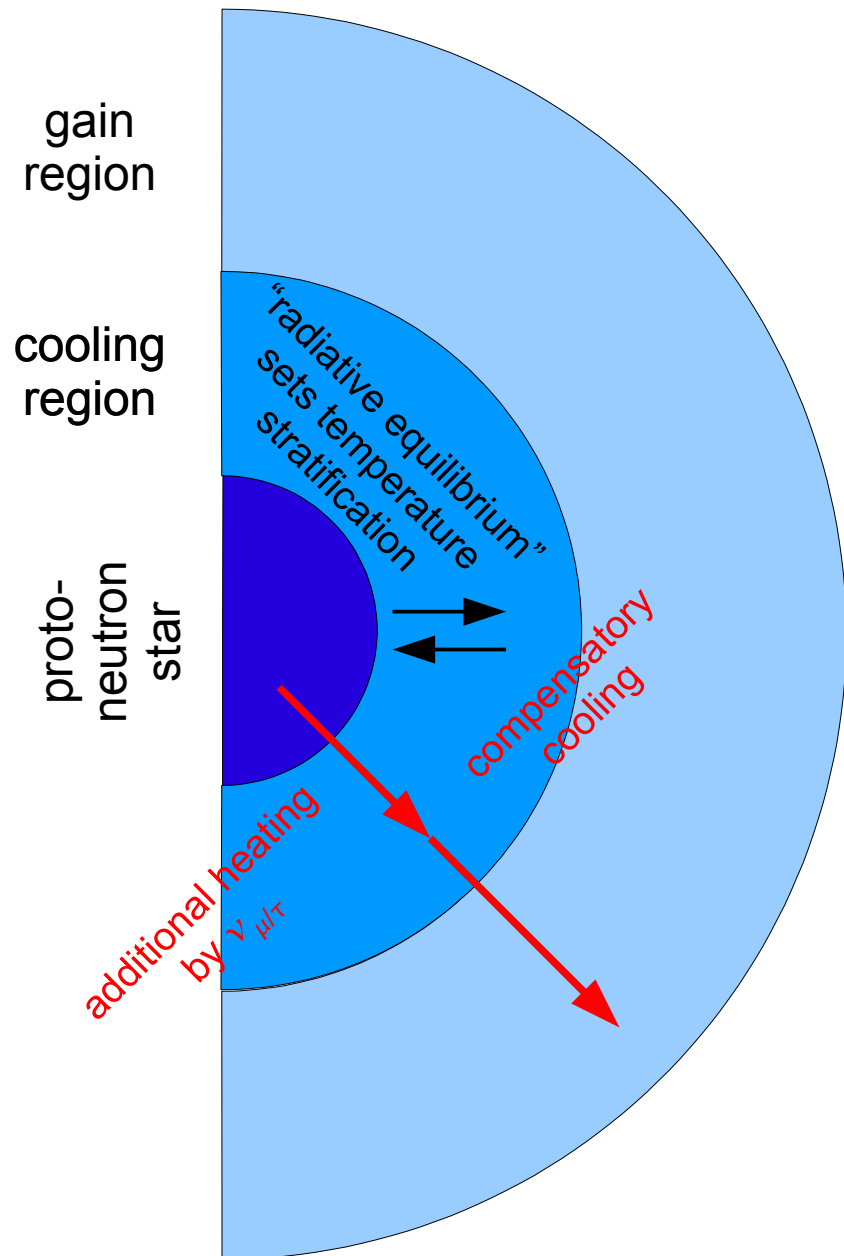


- Increased electron (anti-)neutrino luminosity  $L$  and mean energies  $\langle E_\nu \rangle$  in GR (hotter neutron star surface)
- Local heating rate  $\sim L \langle E_\nu \rangle^2$ , but feedback effects (stronger convection, larger shock radius) further increase the integrated heating rates (up to  $\sim 100\%$ )
- Improved microphysics: energy transfer from  $\nu_{\mu/\tau}$  to the medium allows stronger (anti-) $\nu_e$  emission in cooling region  $\rightarrow$  similar increase in heating in gain region



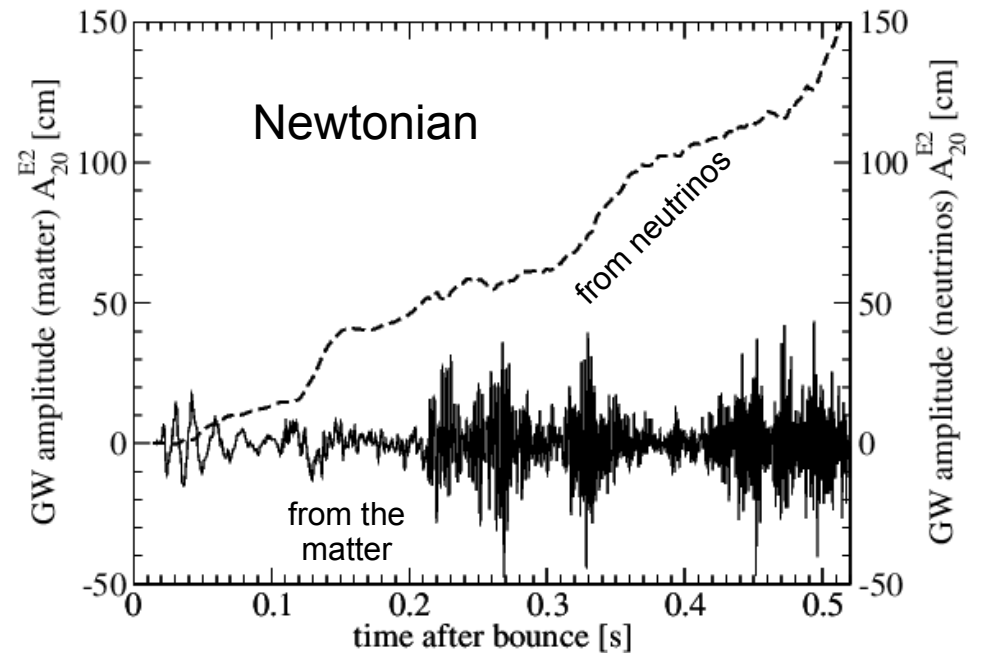
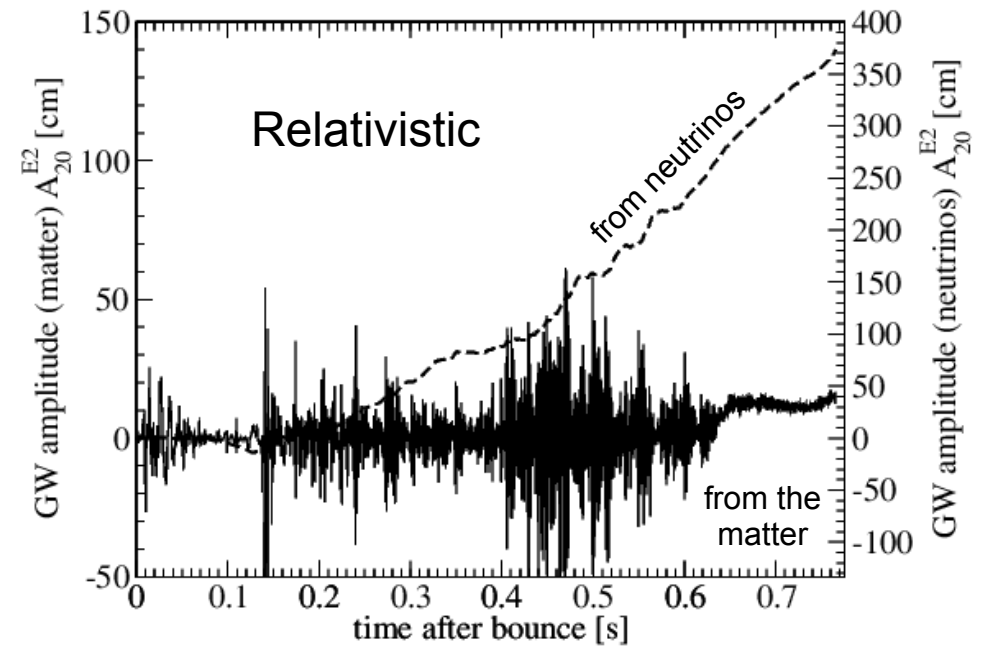


# The Role of Non-Isoenergetic Neutrino-Nucleon Scattering

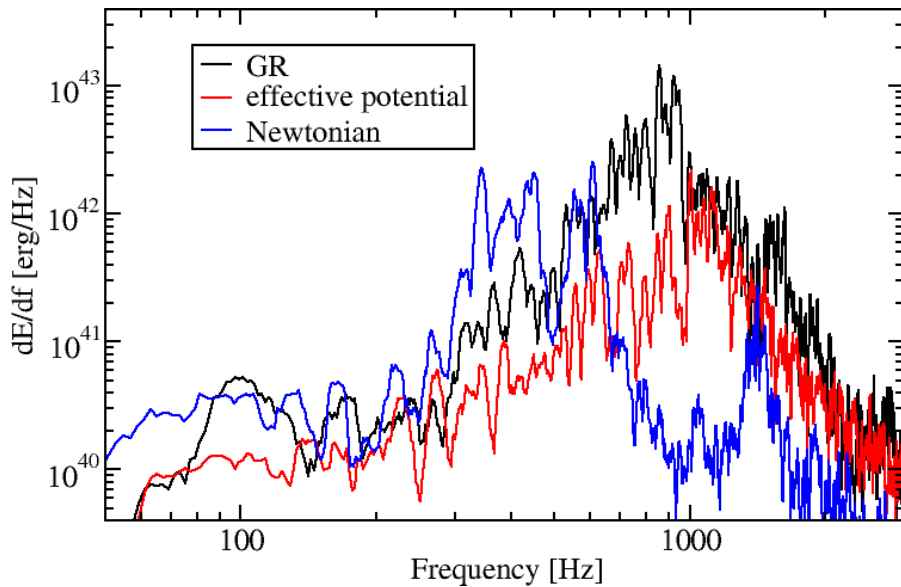


# GR and the Gravitational Wave Signals

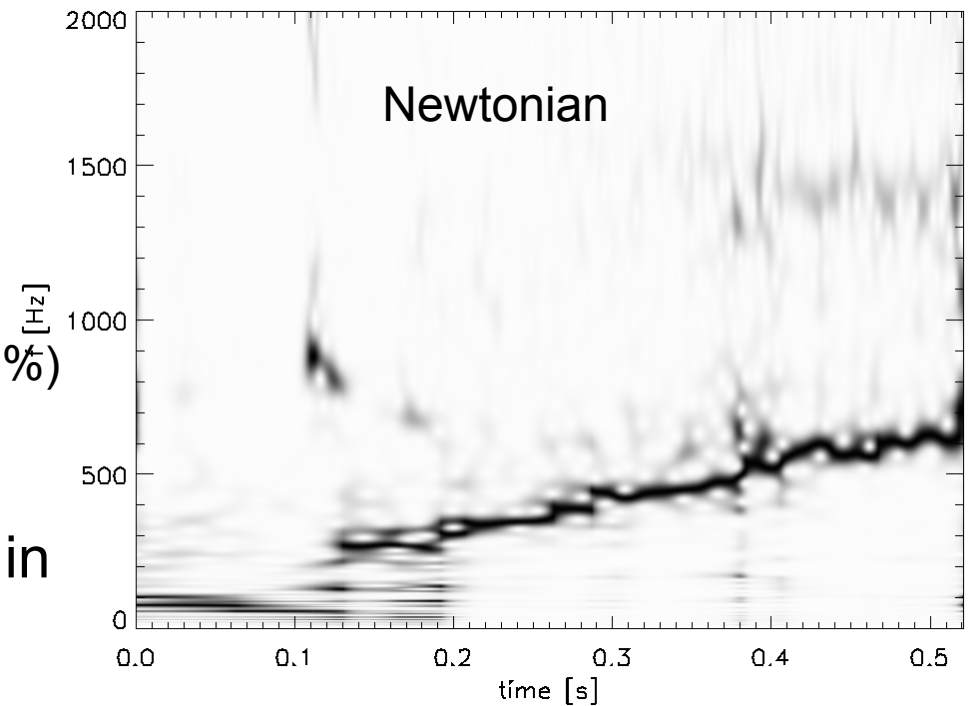
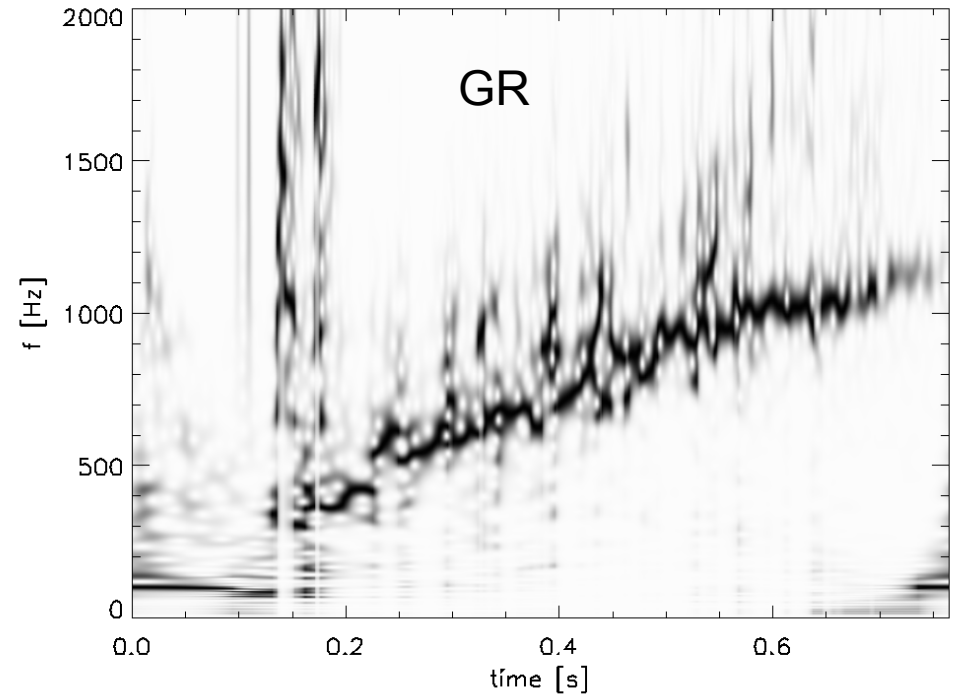
- GR is important for the dynamics, so what about the gravitational wave signal?
- Overall signal structure and amplitudes similar in GR & in the Newtonian approximation
- Signal from convection shows stochastic amplitude variations → model properties better reflected in the spectra
- Reference scale: typical frequencies vary by  $\sim 30\%$  for different equations of state (Marek et al. 2008)



Note: GW extraction with modified quadrupole formula for strong-field background metric



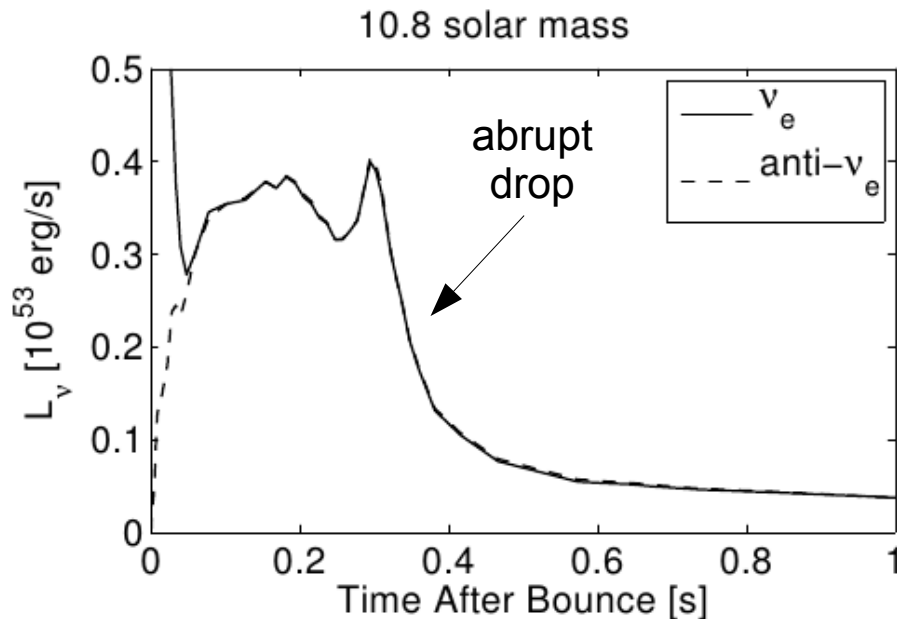
Gravitational wave energy spectrum for the first 500ms.



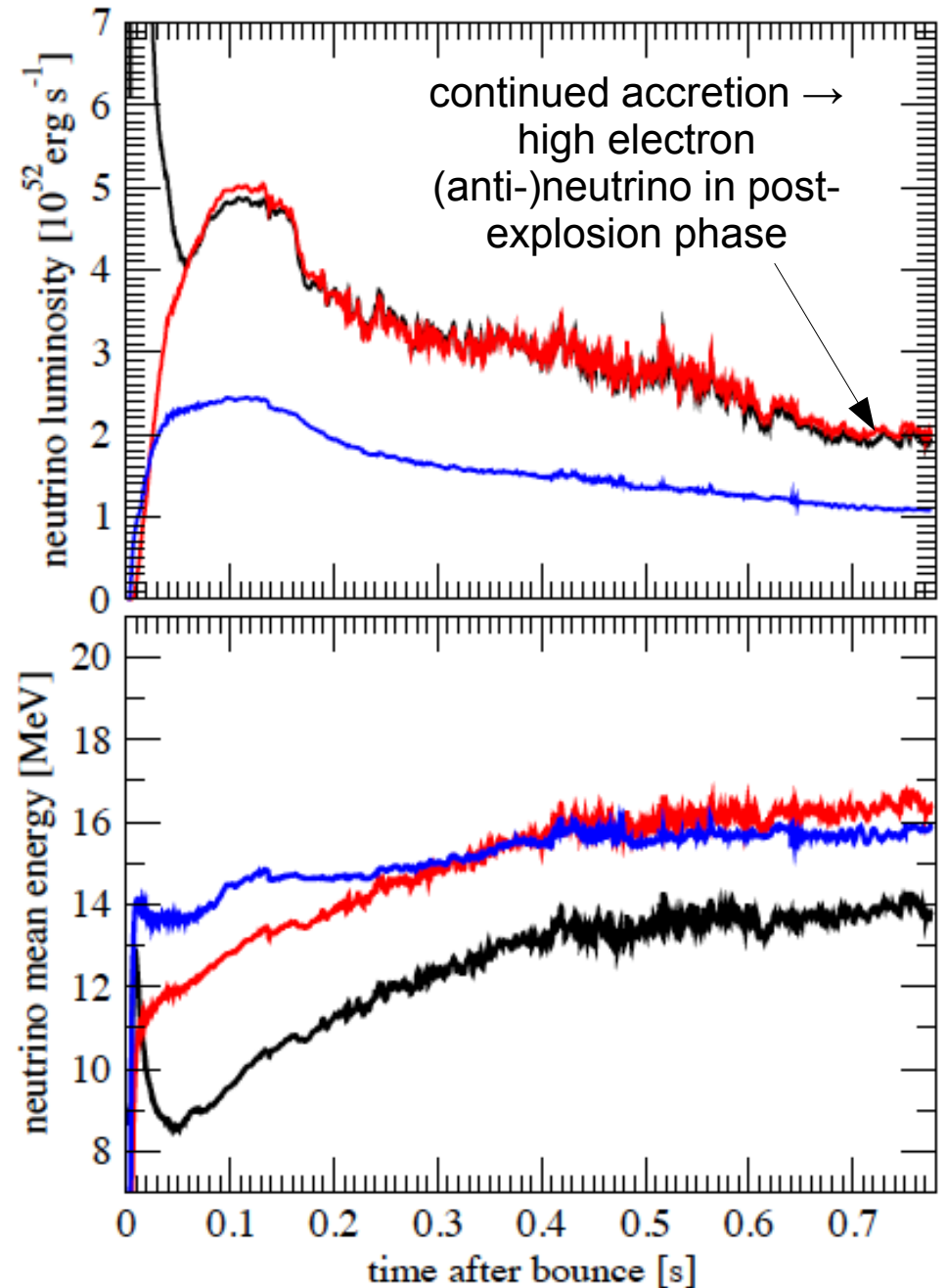
- Frequency shift in the GW energy spectra depending on the GR treatment (measured by the median)
  - GR: 900Hz
  - Newtonian: 500 Hz (woefully low...)
  - effective potential: 1100Hz (accurate to ~20%)
- Comparable to EoS effects!
- Result of different buoyancy frequency in neutron star surface region: This is a systematic effect!

# After Shock Revival: The Neutrino Signal

- Accretion can subsist long after the shock has been revived
- Decay of  $\nu_e$  and anti- $\nu_e$  luminosities is slow – **no abrupt drop**

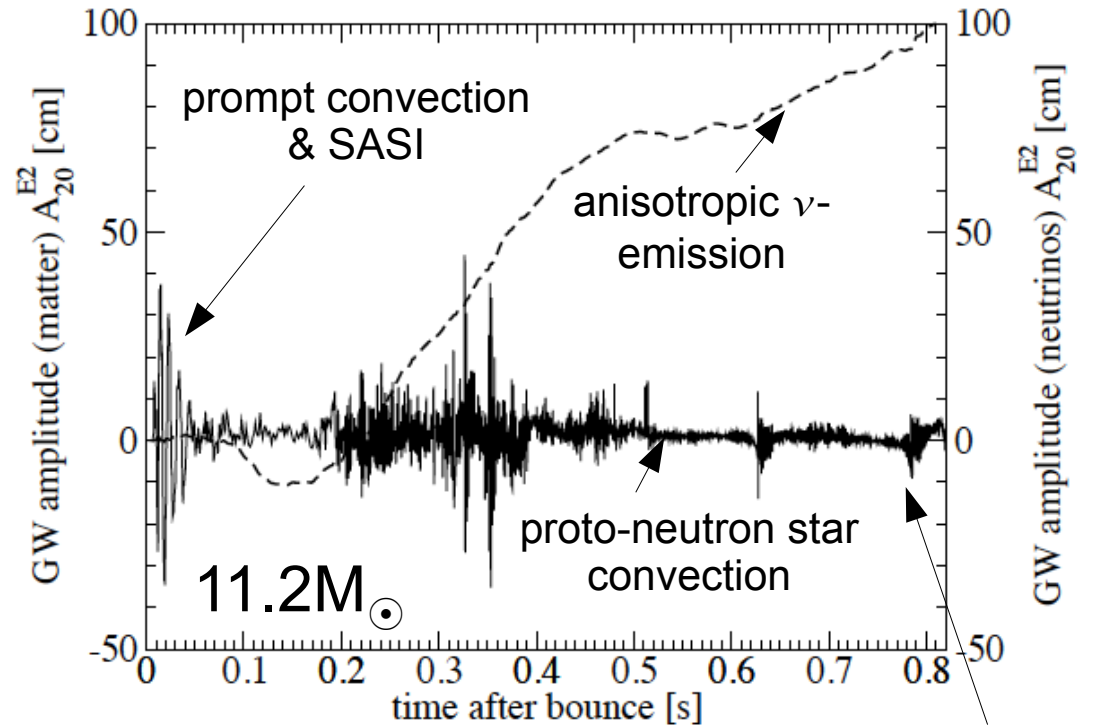
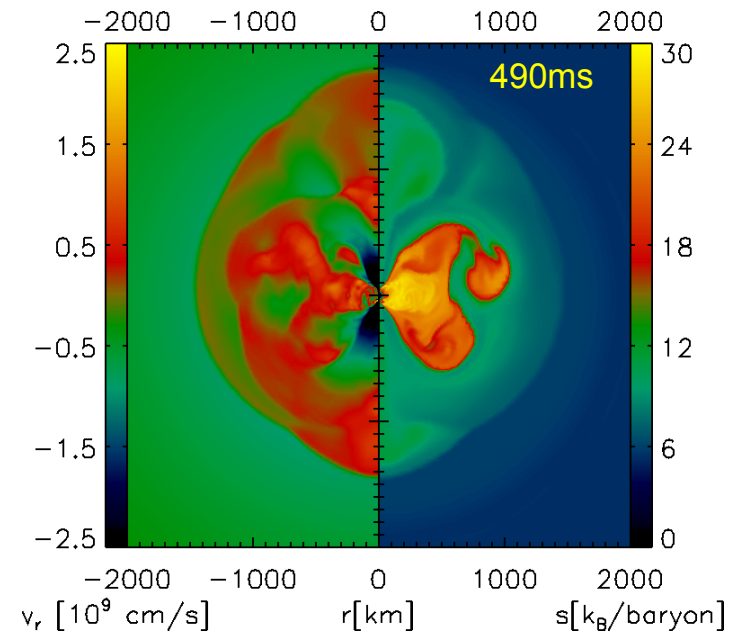
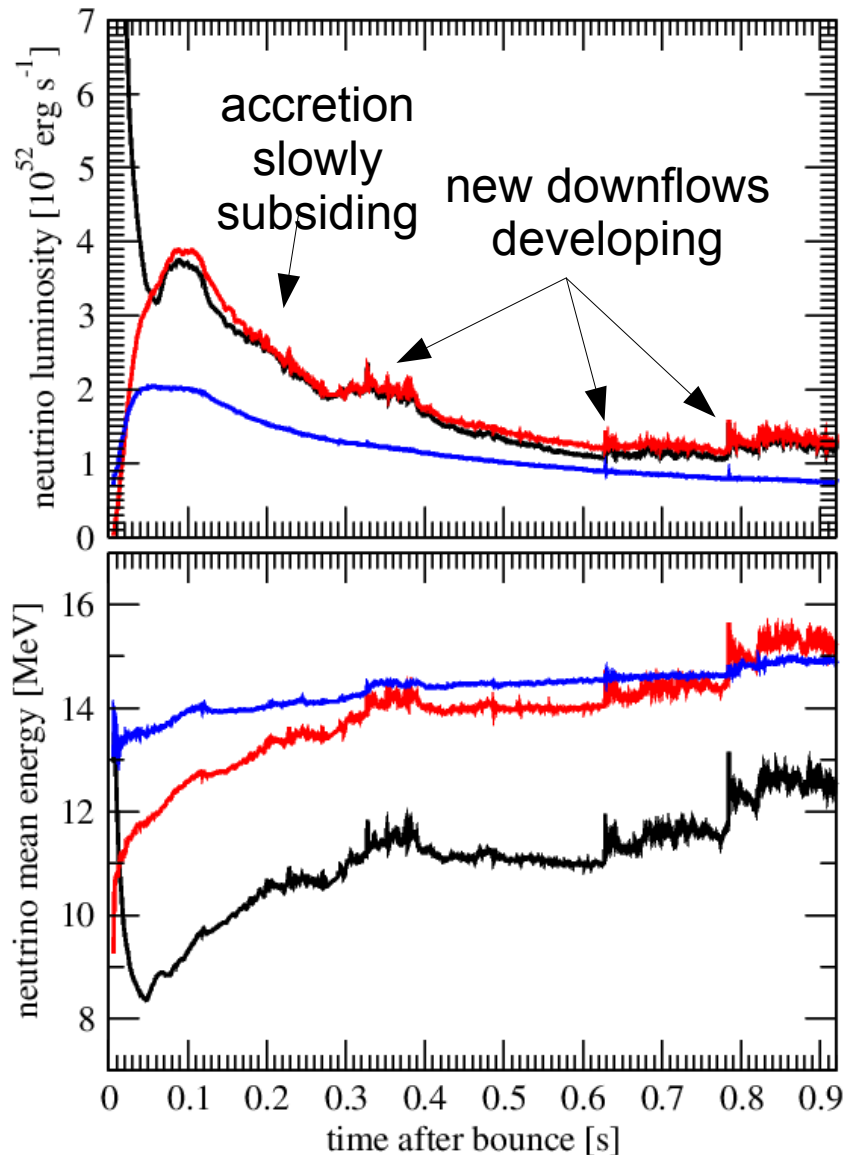


For comparison: artificial 1D explosion from  
Fischer et al. 2010



see Müller et al. (2012) in Proceedings  
of HaVse Workshop 2011

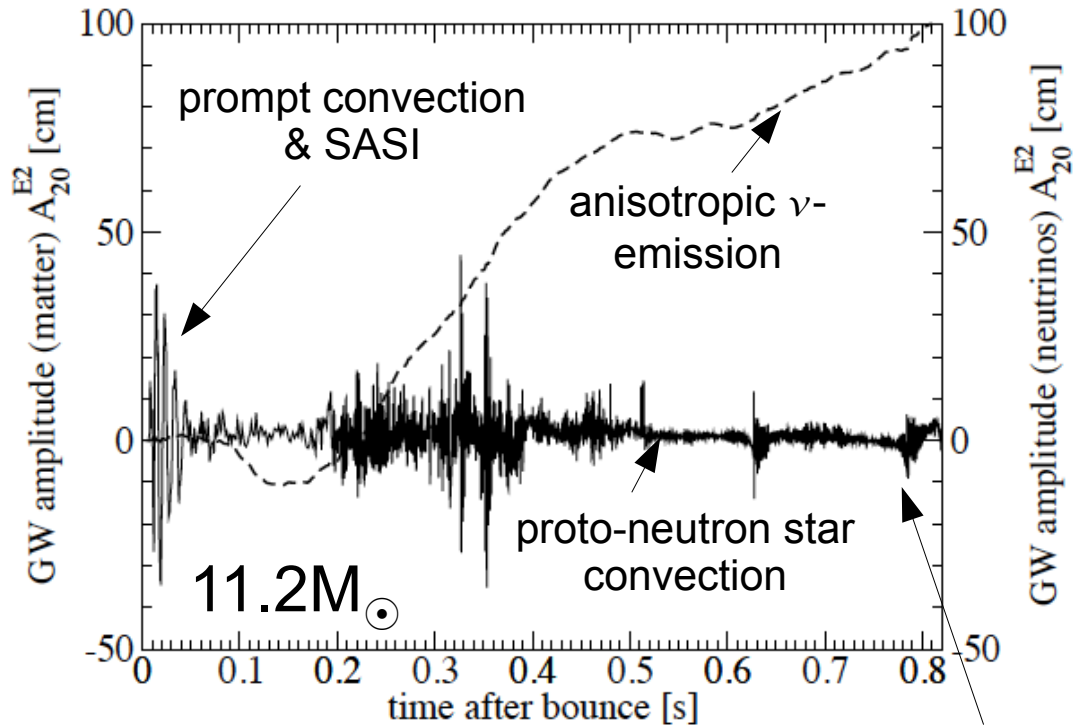
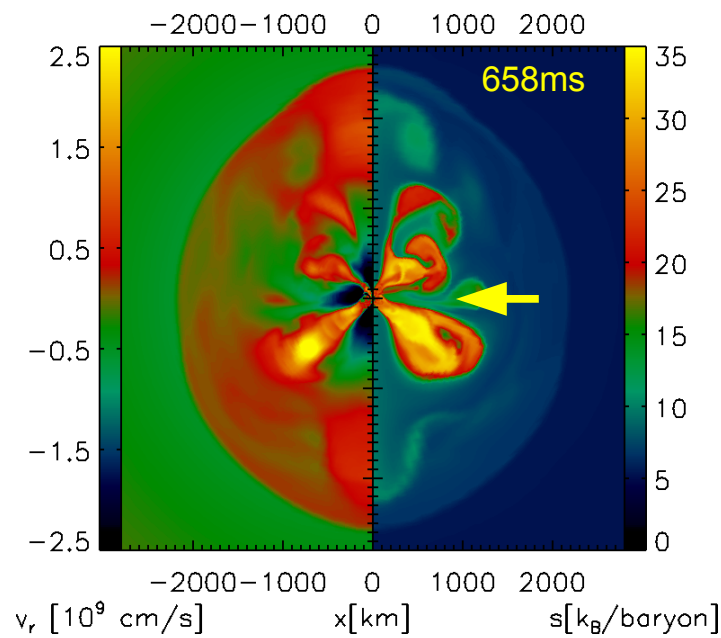
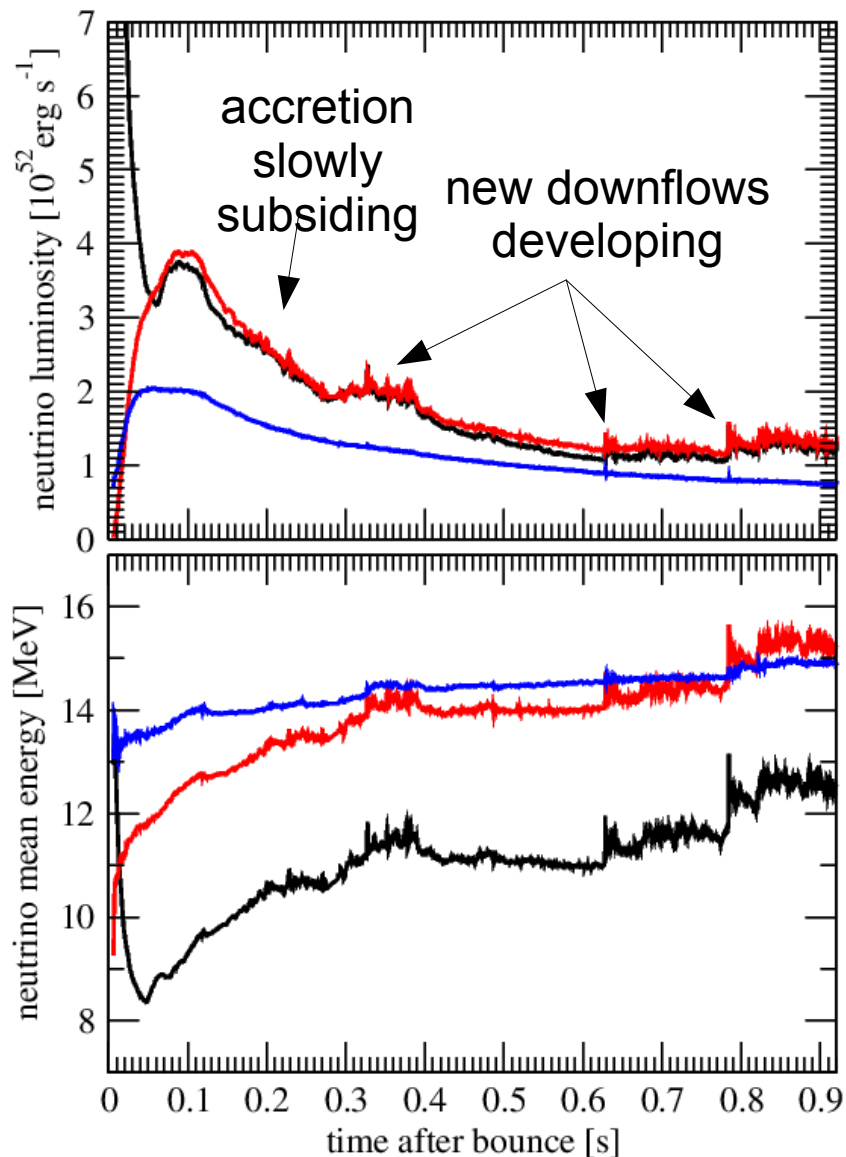
# Neutrino & Gravitational Wave Signals after Shock Revival



see Müller et al. (2012) in Proceedings of HaVse Workshop 2011

excitation of g-modes by newly-formed downflows

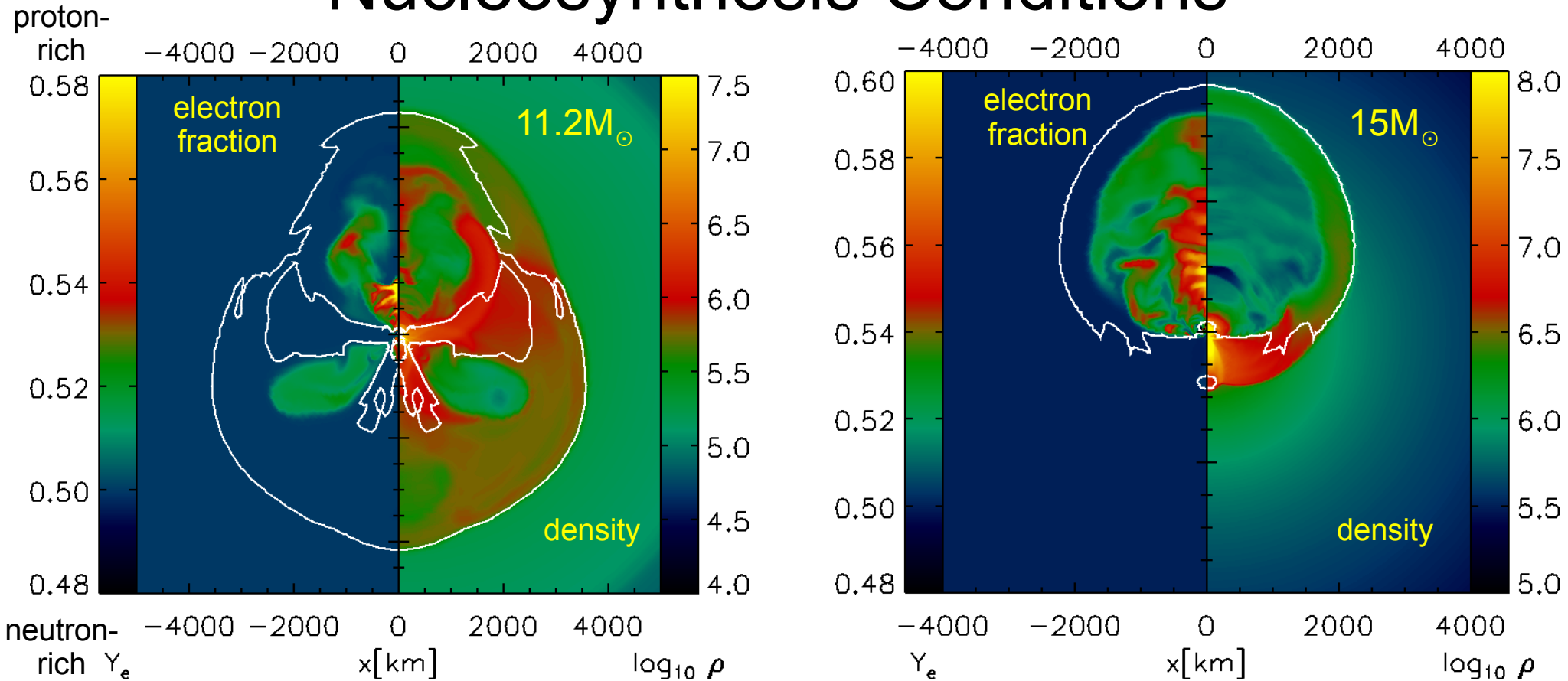
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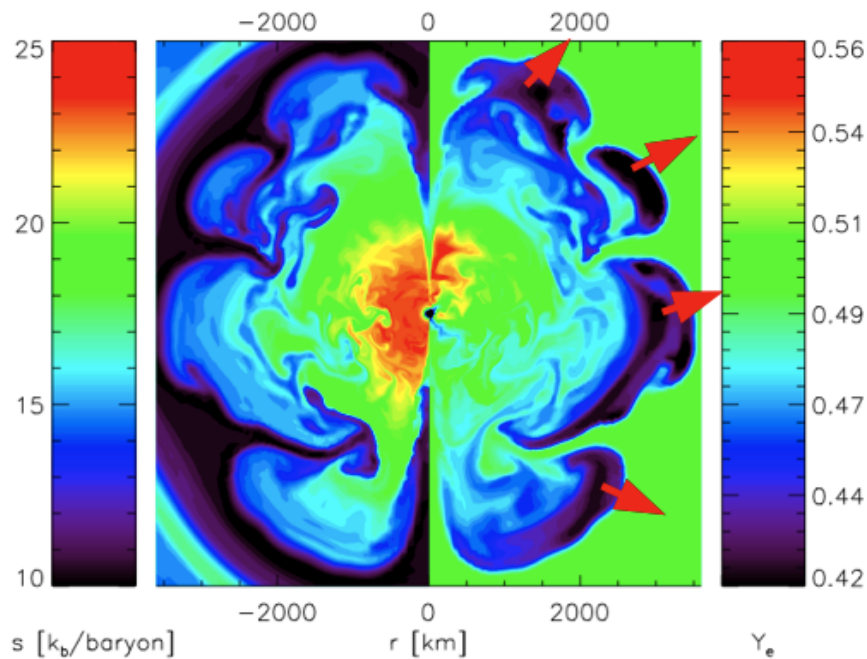
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# Nucleosynthesis Conditions

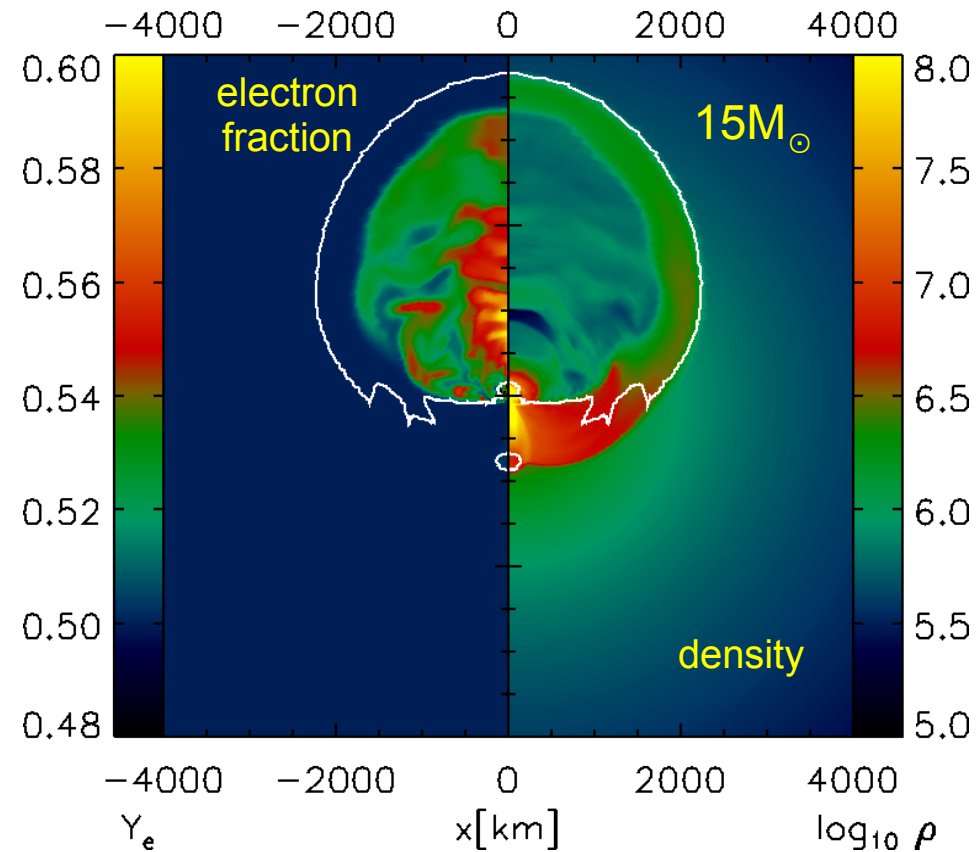


- Proton-rich ejecta at least for several 100ms
- Potential for  $\nu p$ -process (Fröhlich et al. 2006, Pruet et al. 2006) to be investigated
- Note: simple wind models inapplicable during this phase due to high accretion luminosity & aspherical dynamics

# Nucleosynthesis Conditions



8.8 $M_{\odot}$  progenitor with O-Ne-Mg-core:  
neutron-rich plumes (Wanajo et al. 2011)



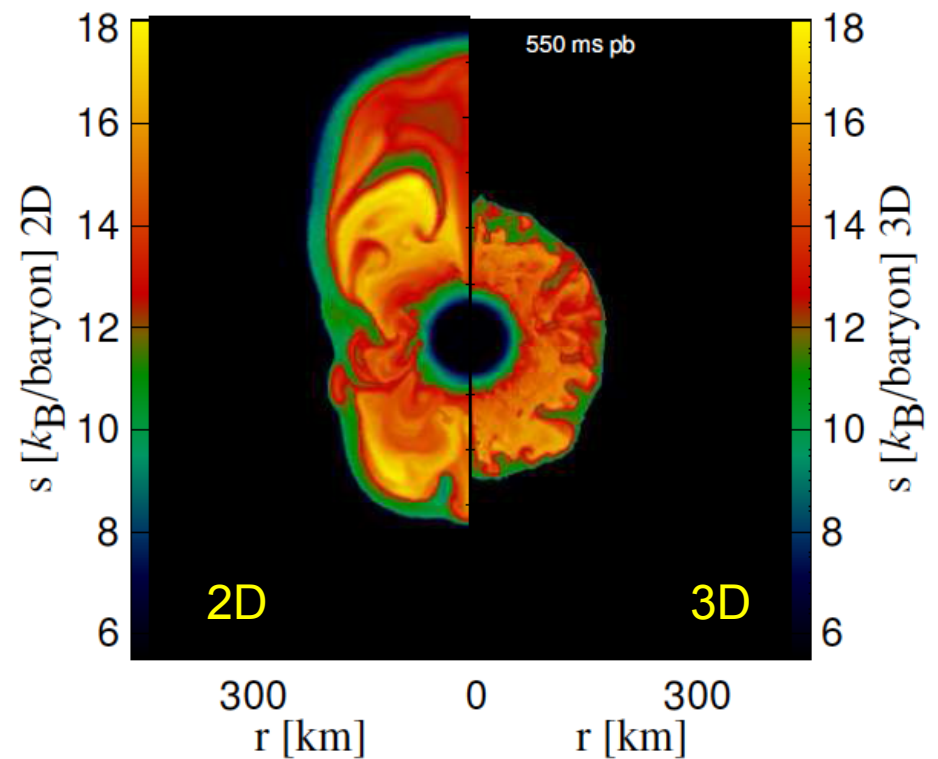
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- **Pronounced difference** between massive progenitors and low-mass progenitors (for which case see Wanajo et al. 2011)



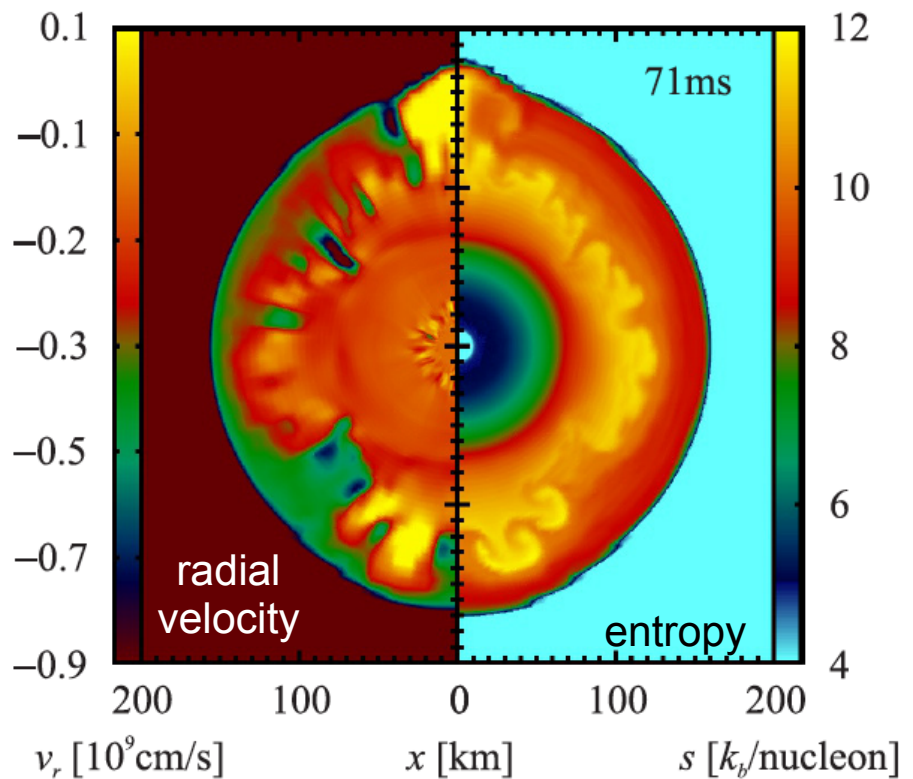
# Convection vs. SASI and the Possible Role of General Relativity in the Debate

# Convection vs. SASI

- Instabilities well-distinguished in linear regime only
- Large-scale structures and kinetic energy of convection may be reduced in 3D due to turbulent cascade (Hanke et al. 2012)
- But: large-scale modes may be important for explosion (more energy stored)
- Convection usually grows first



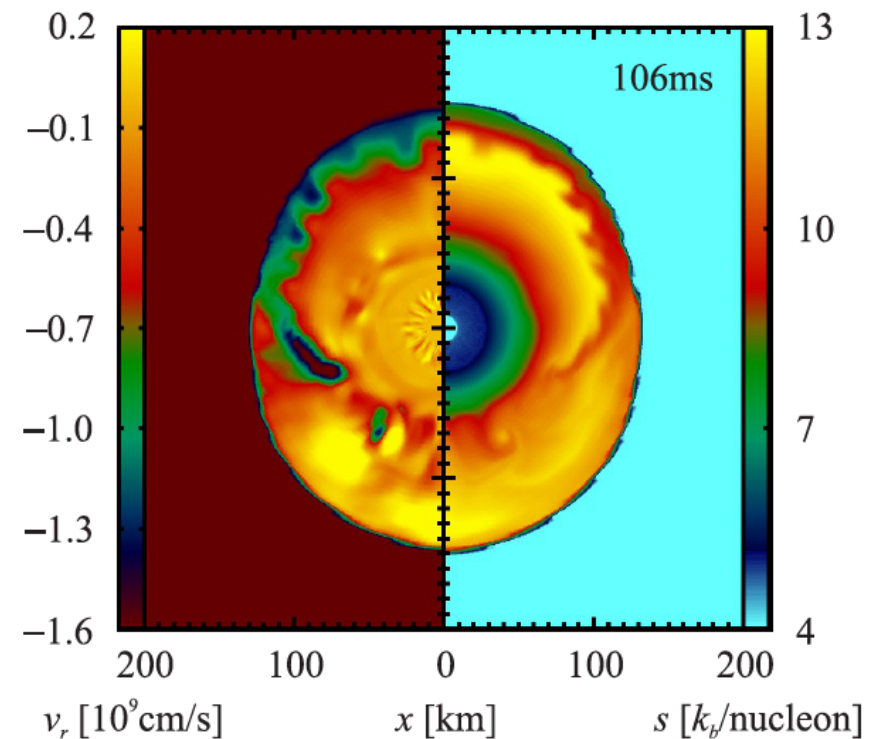
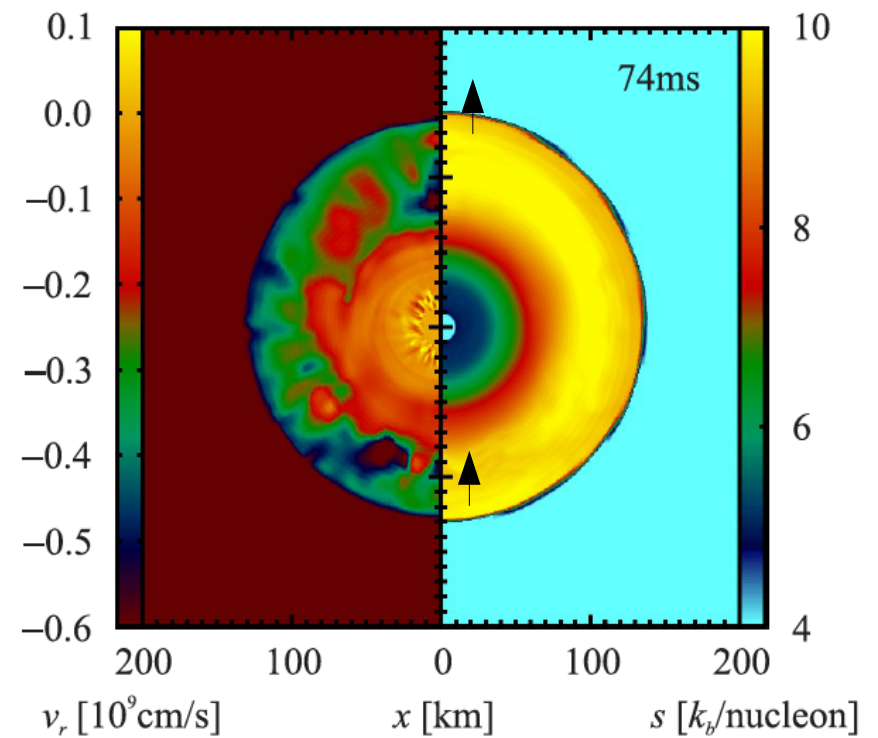
Hanke et al. (2011),  
arXiv:arXiv:1108.4355



Müller, Janka & Heger (2012)  
arXiv:1205.7078

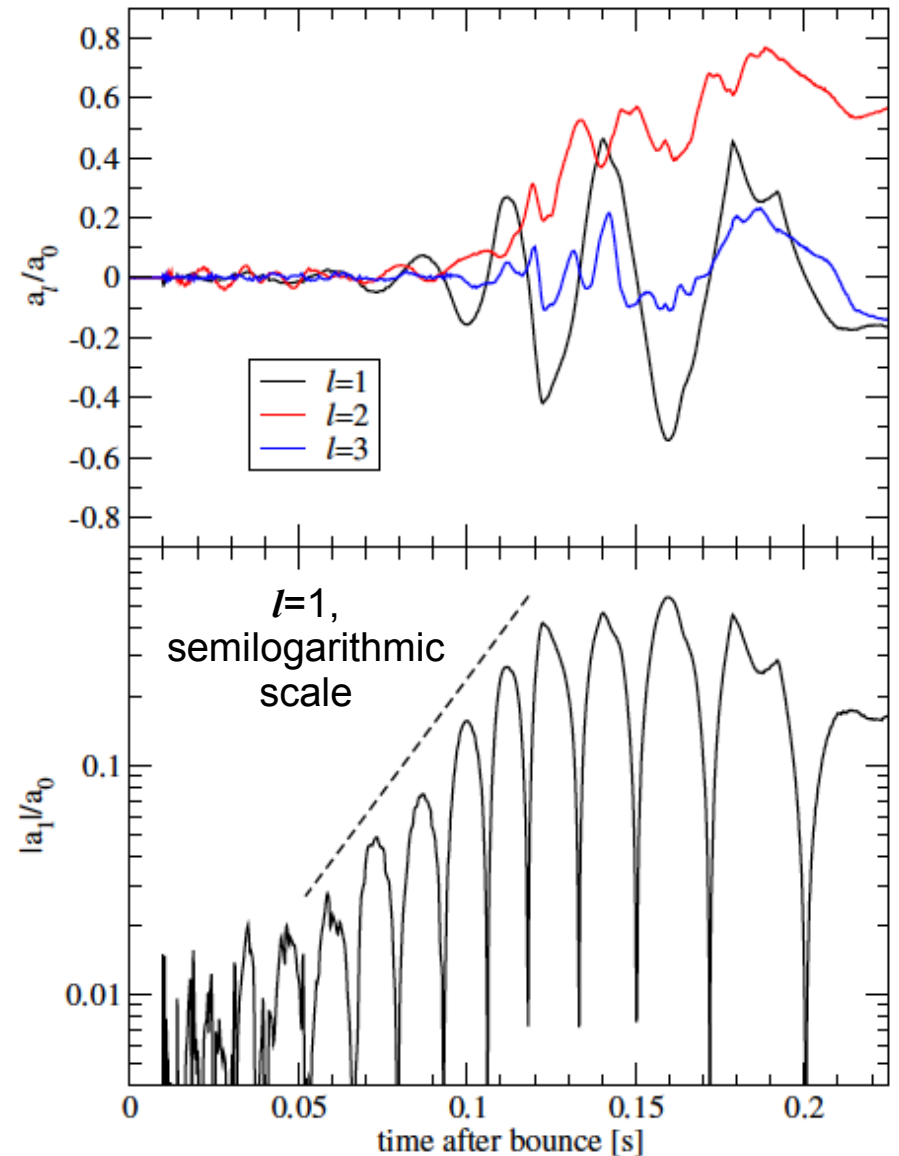
# Convection vs. SASI

- Can we find conditions for strong SASI growth in supernova cores?
- Recent relativistic  $27M_{\odot}$  explosion model (Müller et al. 2012) constitutes such a case
- Incidentally: Explosions now also with LS220 equation of state



# Convection vs. SASI

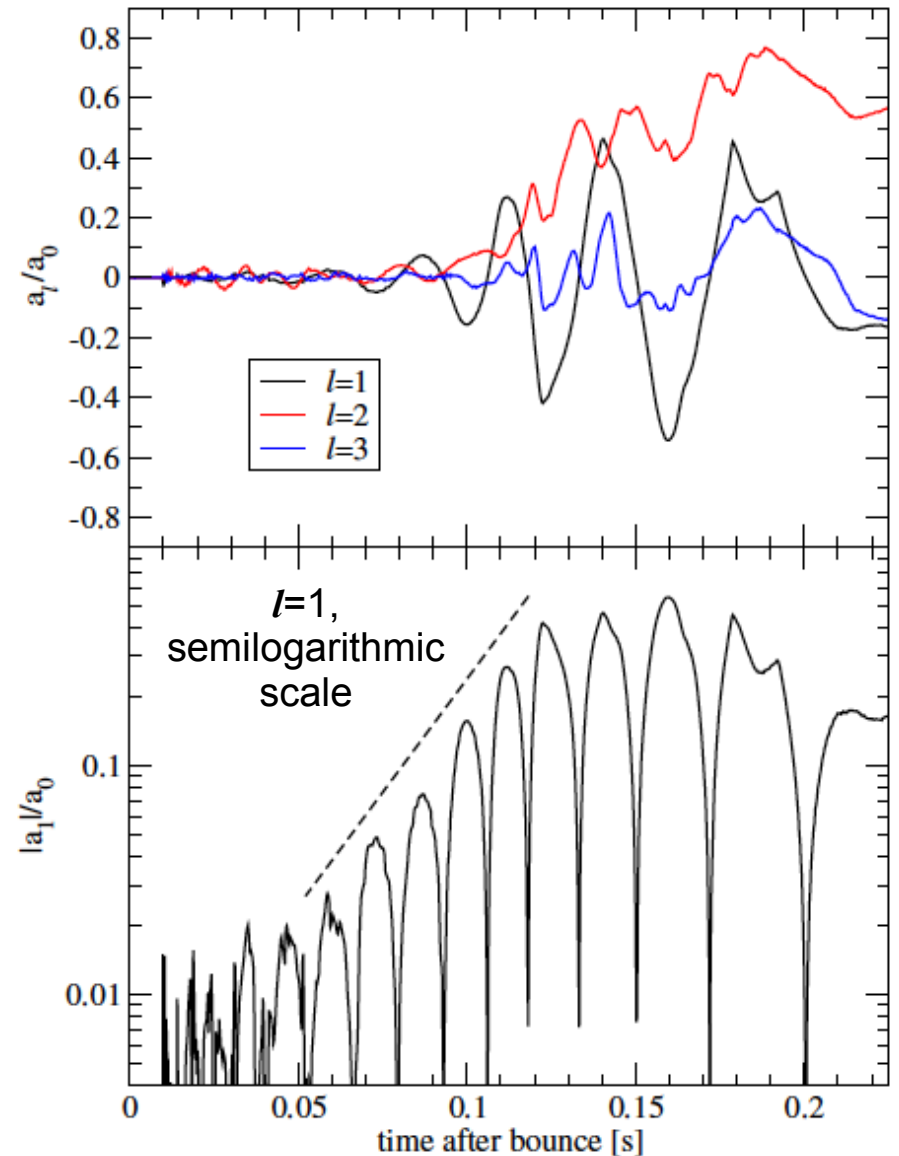
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- Suppression of convection due to fast advection through the gain region



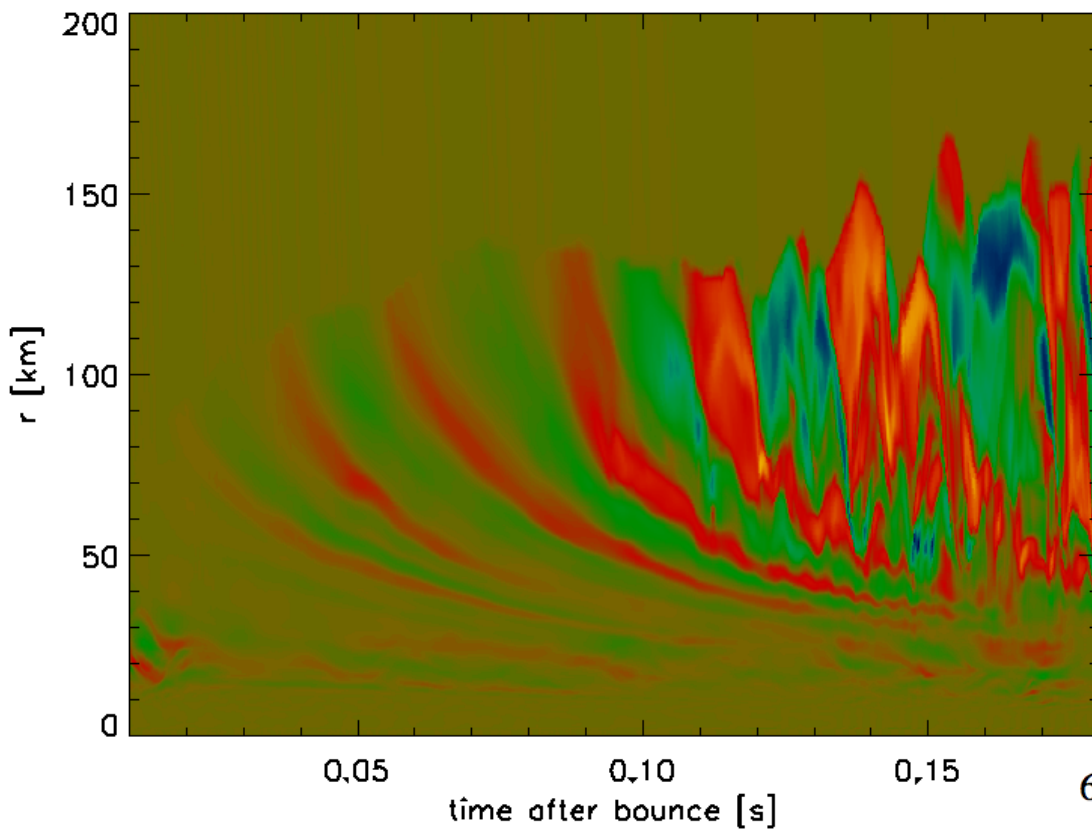
Decomposition of the shock surface into spherical harmonics

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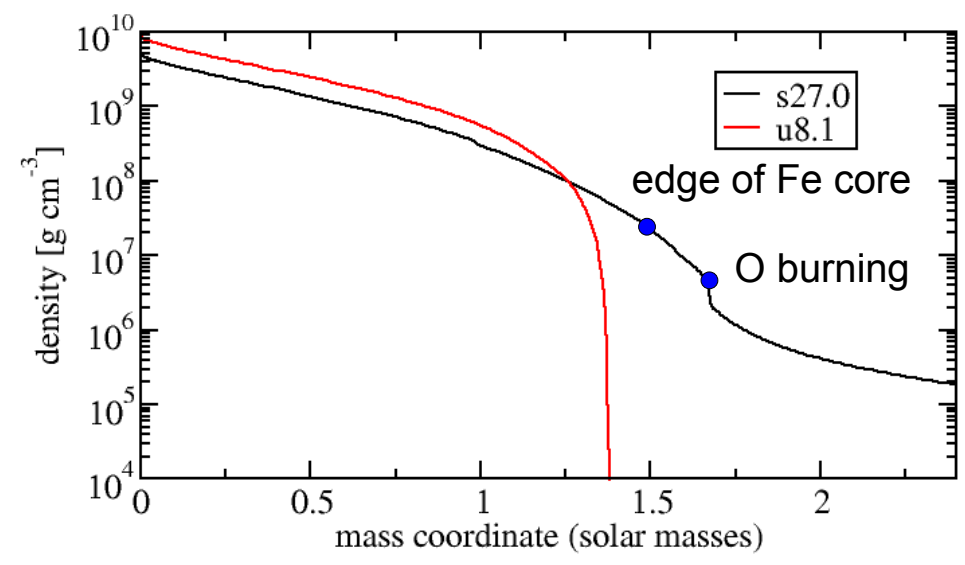


Decomposition of the shock surface into spherical harmonics

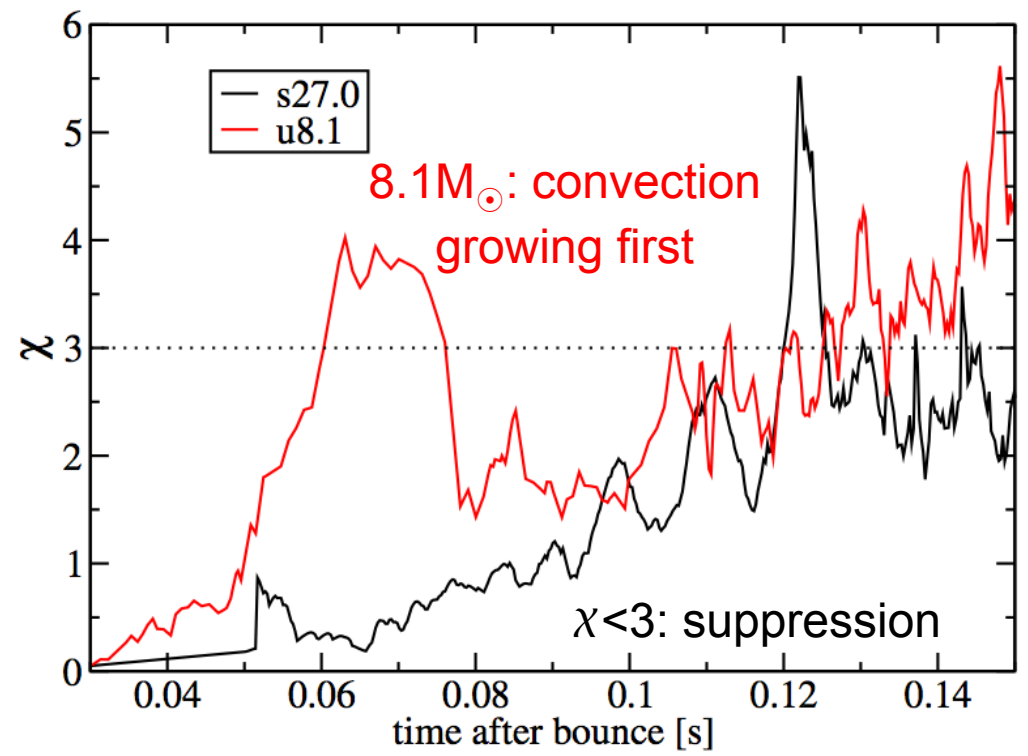


lateral velocity in equatorial plane revealing vorticity perturbation in SASI cycle

critical parameter  $\chi$  for growth of convection ( $\sim$ buoyancy time scale/advection time scale)



comparison of density profiles

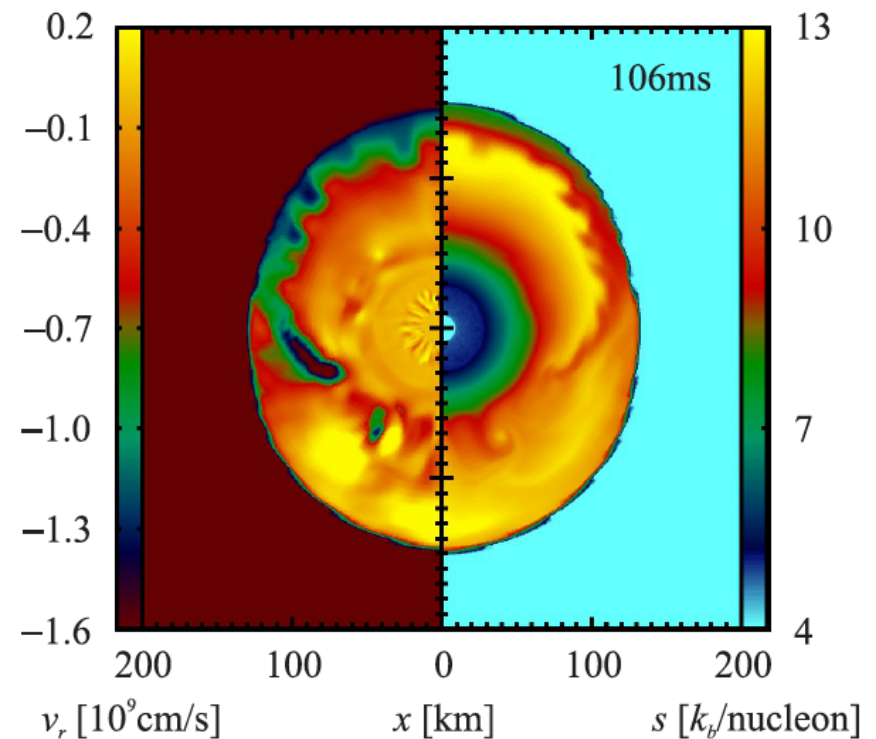
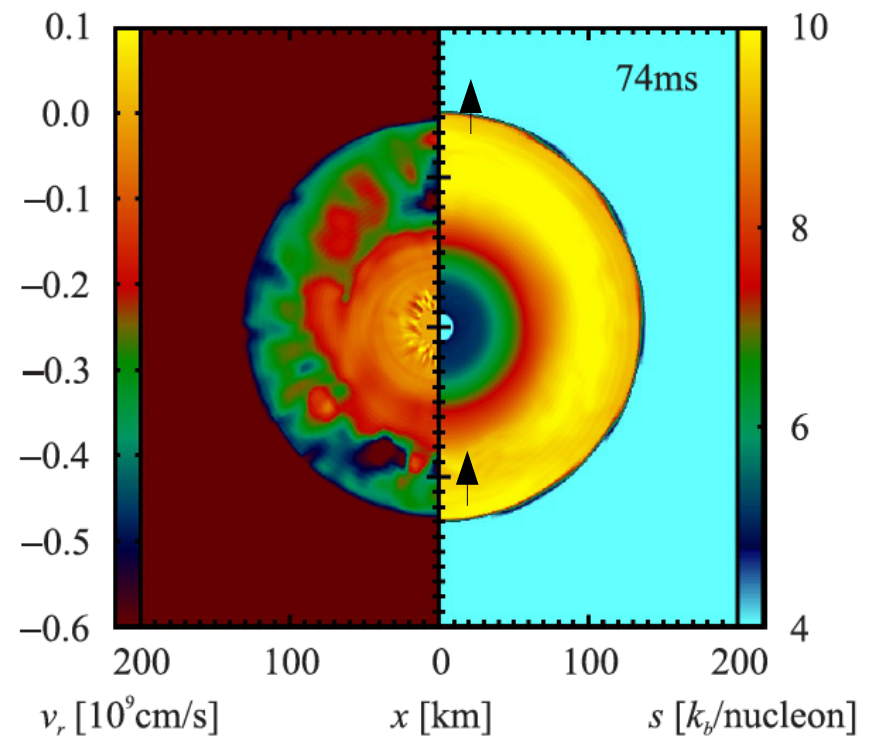


$8.1M_{\odot}$ : convection growing first

$\chi < 3$ : suppression

# Implications & Questions

- Compact proto-neutron stars with strong gravitational field beneficial for SASI growth ( $\rightarrow$  short advection time-scale)
- General relativity, the progenitor structure, the equation of state and a correct neutrino treatment at high optical depth ( $\rightarrow$  PNS contraction) may be crucial for vigorous SASI activity
- Is there an *intermediate* regime (SASI+convection)?
- Can “convectively-dominated” flows become “SASI-dominated” as the conditions change?
- What happens in 3D? Comparable or lower amplitudes? Spiral mode?



# Summary

- General relativity (GR) and a good neutrino treatment emerge as important ingredients for successful explosions:
  - Higher neutrino luminosities & mean energies due to hotter proto-neutron star result in **more heating in GR**; effect outweighs different accretion shock radius
  - GR may even play a role for obtaining conditions conducive to strong SASI growth (behaviour in 3D to be investigated)
  - Seemingly minor rate effects (nucleon recoil in  $\nu$ -nucleon scattering) may have an appreciable impact as well
- Large (50%) systematic GR effect on the typical gravitational wave frequency
- Conclusion: GR (at least on the level of the “effective potential approximation”) and up-to-date neutrino rates should be included for correct dynamics & accurate signal predictions
- Progress of explosion models: Growing set of progenitors, GW & neutrino signal predictions beyond shock revival now available, better connection to nucleosynthesis studies