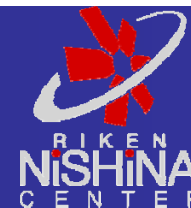


August 11, 2011 @ INT Workshop

Seattle



# Study of Spin-isospin Responses in the Continuum by Charge-Exchange Reactions

H. Sakai

RIKEN Nishina Center / Sungkyunkwan University

# Contents

1 How reliable are the spin-isospin responses in the **continuum** extracted by the **nucleon** CHEX reactions ?

- Measurement, analysis and associated uncertainties

- ✓ MDA

- ✓ unbound transition (shallow binding approx.) ?

- ✓  $L=0$ ,  $L=2$  and their interference effect ?

- ✓ interference between GT and IVSM ?

- ✓ proportionality ?

2 How are they in the case of composite projectiles ?

- ( $t, {}^3\text{He}$ ) reaction: measurement by Miki

- ✓ Exchange effects

- ( ${}^{12}\text{N}, {}^{12}\text{C}$ ) reaction: measurement by Noji

- ✓ Ambiguities by optical potentials(imaginary part)

3 **Brand-new**: measurement of the exothermic  ${}^{12}\text{Be}(p,n)$  reaction in inverse-kinematics at 200 MeV/A by Yako

- – *observation of GT giant resonance and SDR* –

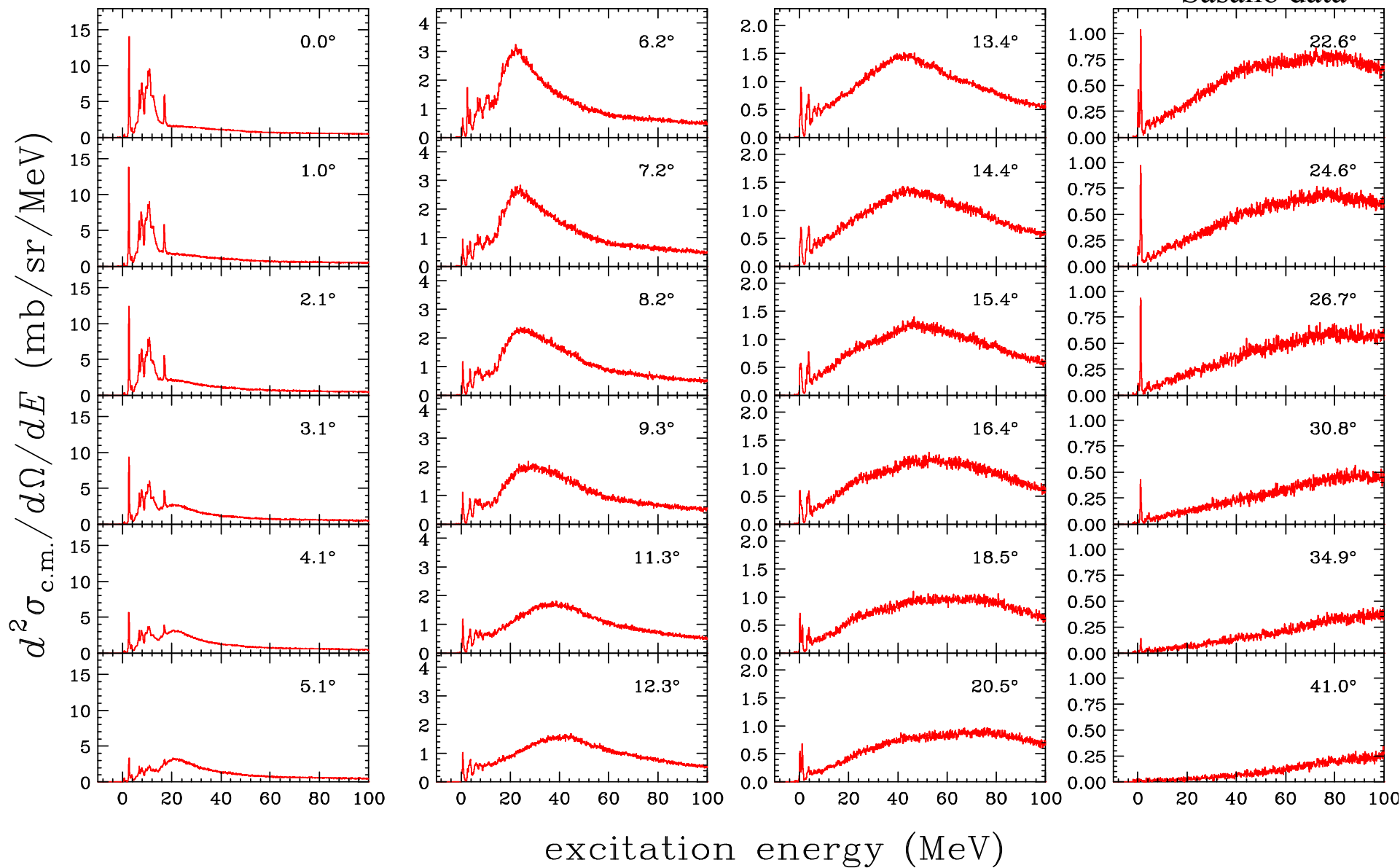
4 Summary and home works for theorists

# $^{48}\text{Ca}(p,n)$ data



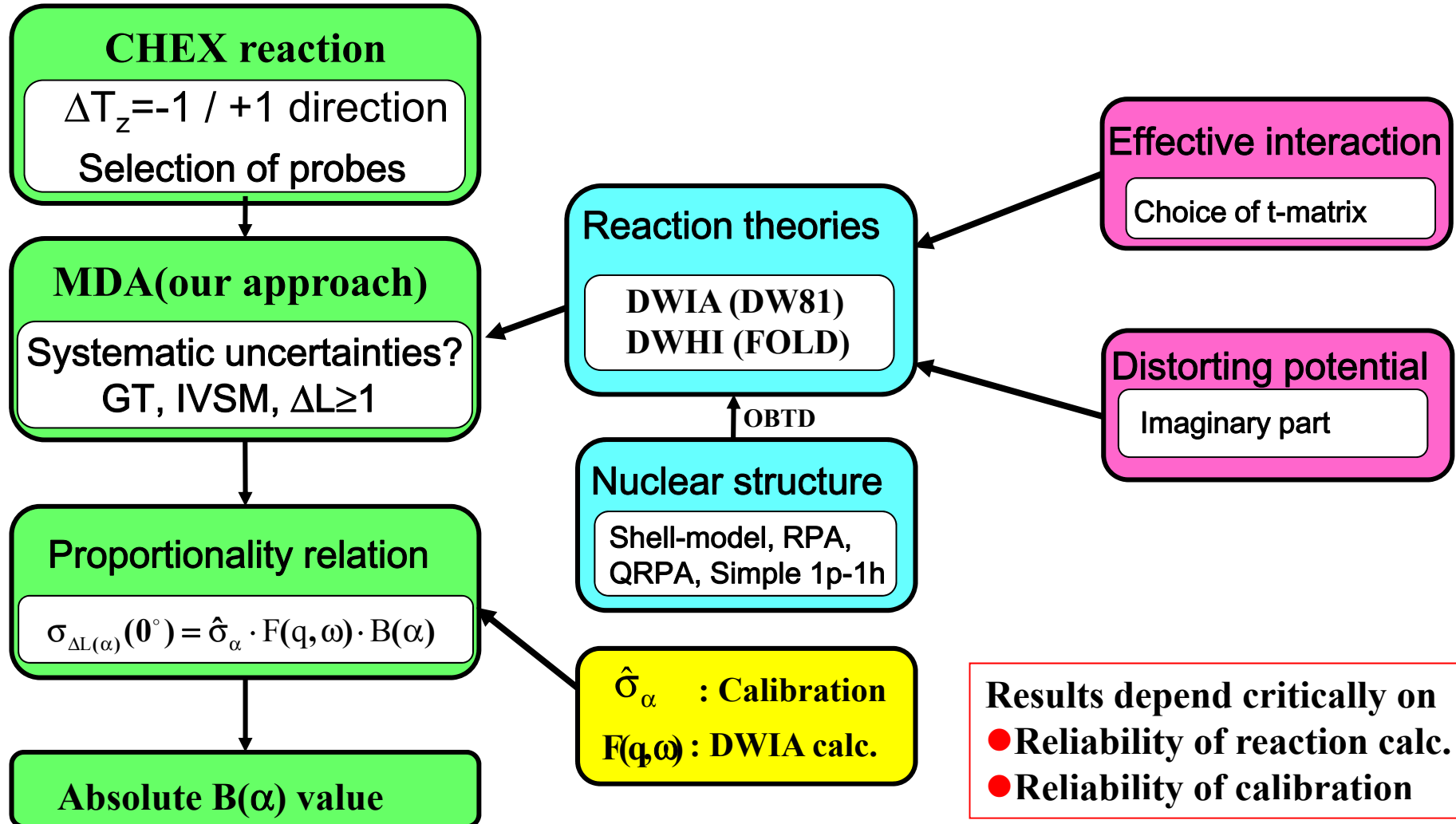
$^{48}\text{Ca}(p,n)^{48}\text{Sc}$  at 300 MeV

Sasano data



# How to cook the continuum ?

## Example: spin-isospin responses



# Multipole Decomposition Analysis

$$\sigma^{\text{exp}}(\theta_{\text{cm}}, E_x) \approx \sum_{J^\pi} a_{J^\pi} \sigma_{ph; J^\pi}^{\text{calc}}(\theta_{\text{cm}}, E_x)$$

↑ DWIA

$$\Delta L = 0, 1, 2, 3 \quad [J^\pi = 1^+, (0^-, 1^-, 2^-), (2^+, 3^+), 4^-]$$

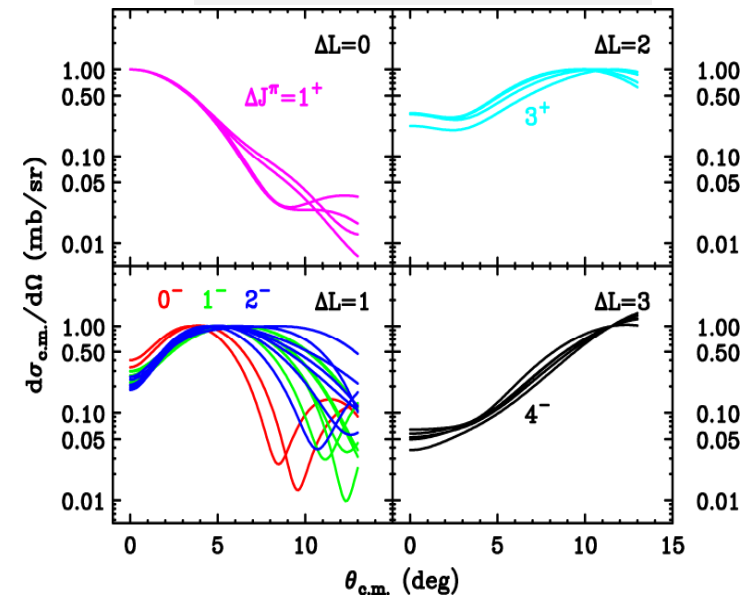
DWIA inputs

- NN interaction:
  - t-matrix by Franey & Love @325 MeV
- optical model parameters:
  - Global optical potential (phenomenological, Cooper et al.)
- one-body transition density:
  - pure 1p-1h configurations

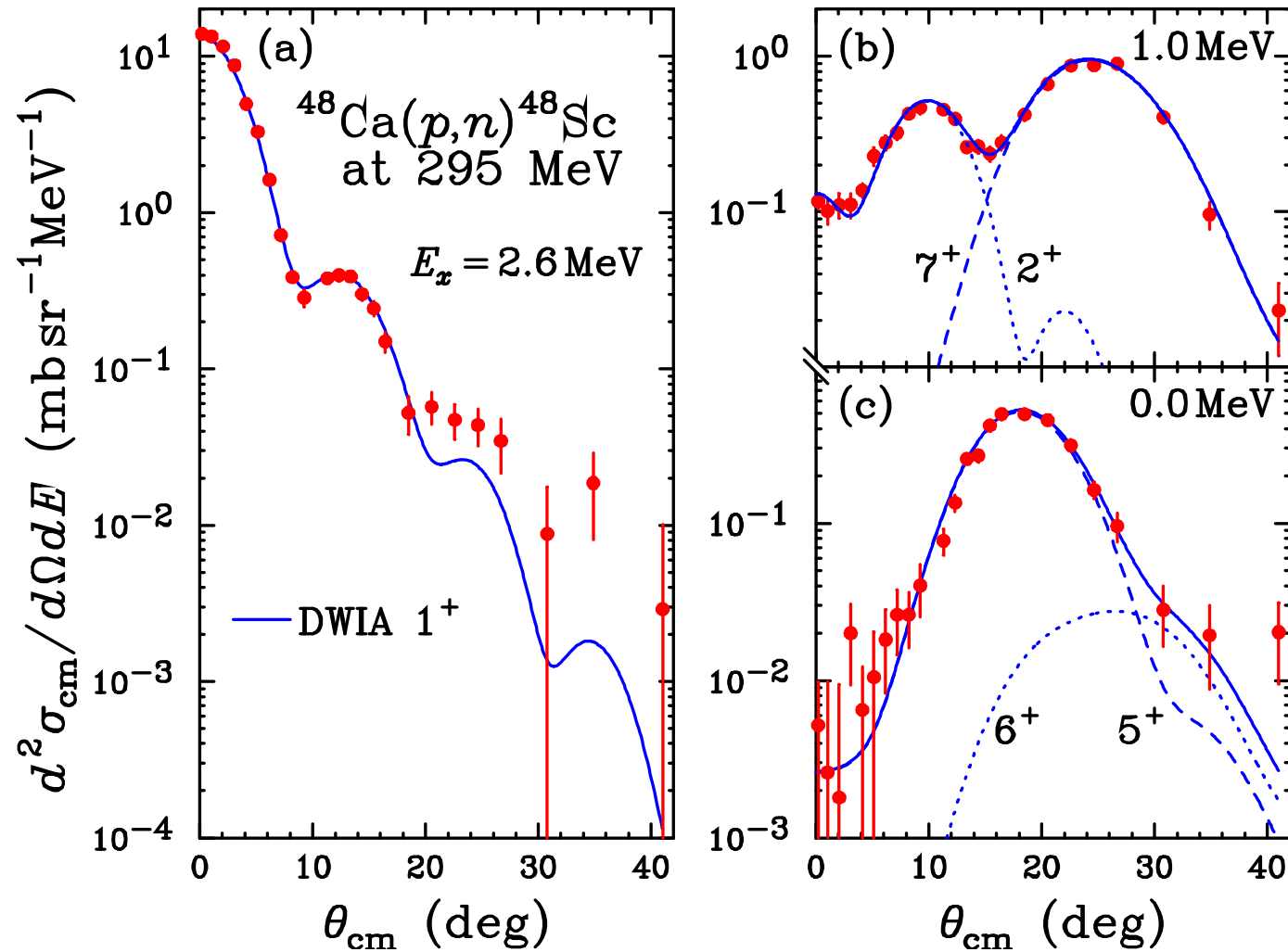
Particle:	1f, 2p, 1g, 2d, 3s, 1h11/2
Hole:	1p, 1d, 2s, 1f

radial wave functions ... W.S. / H.O.

$^{48}\text{Ti}(n,p)$  angular dist.  
 $E_x = 20 \text{ MeV}$

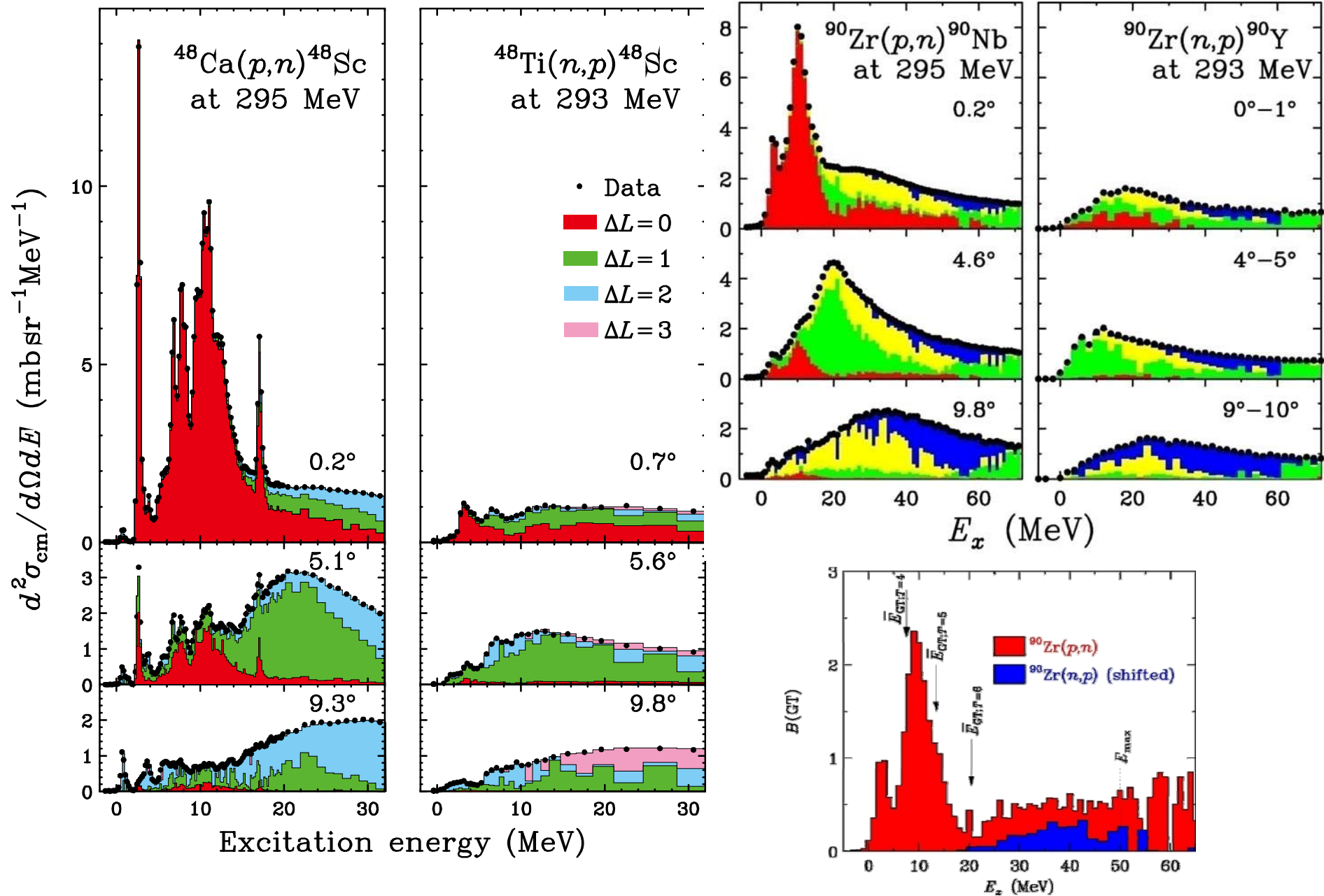


# How well does DWIA reproduce data ?



Reproduce very well at least low  $E_x$  !

# Decomposed spectra



## $^{90}\text{Zr}(p,n)/(n,p)$ cases

		$S^-$ (30.6)	$S^+$ (3.0)	$S^- - S^+$ (27.6)	$Q$ (0.92)
statistical		0.5	0.4	0.6	0.02
systematic	c.s. data	1.3	0.3	1.4	0.05
	unit c.s.	1.5	0.1	1.4	0.05
	MDA*	0.5	0.3	0.3	0.01
	IVSM*	0.9	0.3	0.7	0.02

\* : estimated within the 'standard' DWIA framework

- optical models: (contribution = 0.2 for  $S^-$  MDA)

phenomenological... EDAIZr(Cooper), n-global(Shen),  
folding... RH-RIA(Horowitz), DParis(von Geramb)

- radial w.f.:(0.2)

Woods-Saxon, Harmonic Oscillator, wine-bottle shapes

- effective NN interaction:(0.3)

Franey-Love @ 325 MeV & 270 MeV



## Uncertainties besides cross section of data

- unit cross section
- proportionality?
- unbound transition (shallow binding approx.) ?
- $L=0$ ,  $L=2$  and their interference effect ?
- interference between GT and IVSM ?

# Proportionality (relation between $\sigma_{\Delta L=0}$ and $B(GT)$ )

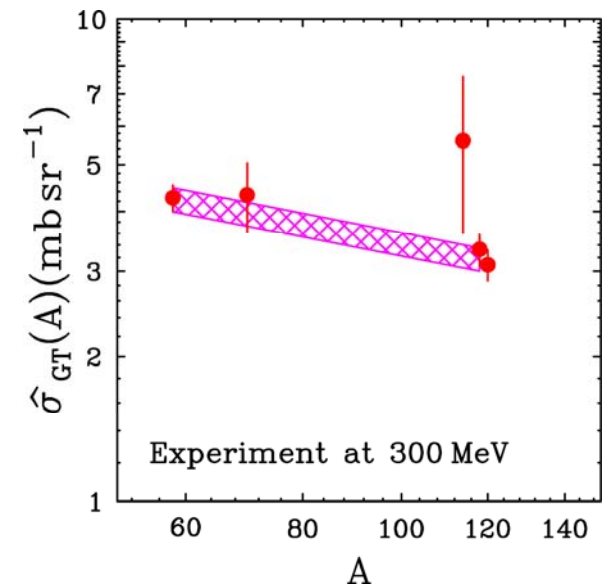
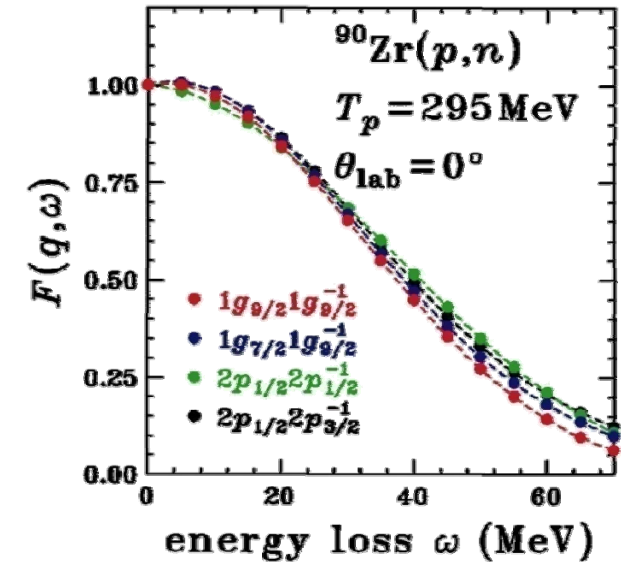
$$\sigma_{\Delta L=0}(0^\circ) = \hat{\sigma}_{GT} \cdot F(q, \omega) \cdot B(GT) \quad \sigma_{\Delta L=0}(q, \omega) \rightarrow B(GT)$$

- $F(q, \omega)$ : kinematical correction  
( $q, \omega$ )  $\rightarrow$  (0,0)  
estimated by DWIA calc.

- $\hat{\sigma}_{GT}$  : GT unit cross section  
should be measured, not easy  
systematic study by Sasano  
PRC 79, 024602 (2009)

$$\hat{\sigma}_{GT}(A = 48) = 4.69 \pm 0.40 \text{ mb/sr}$$

Same  $\hat{\sigma}_{GT}$  is used for both (p,n) / (n,p).



# Proportionality test by Sasano

$$\sigma_{\Delta L=0}(0^\circ) = \hat{\sigma}_{GT} \cdot F(q, \omega) \cdot B(GT)$$

## Proportionality test by shell model

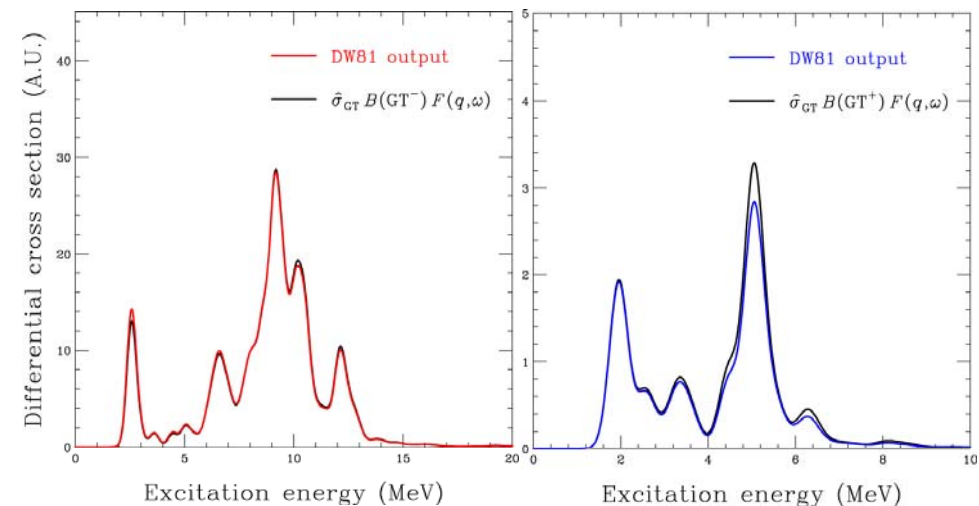
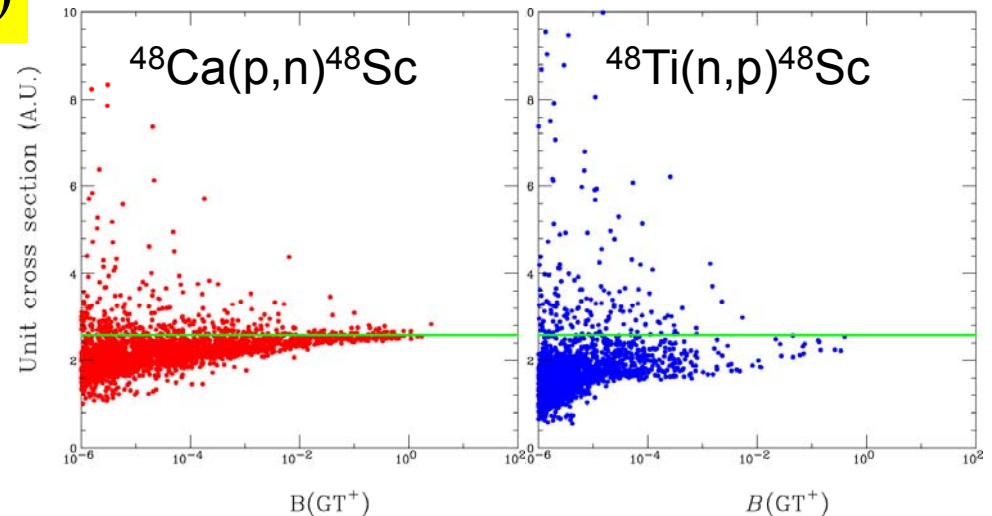
Exercise by using:

- ◆  $^{48}\text{Ca}$ -- $^{48}\text{Ti}$  system
- ◆ Shell model calculations
- ◆ Standard DWIA calc.

Deviations are large for small  $B(GT)$  for both sides.

Averaging could work.

Retain the proportionality (optimistic hope ?!).



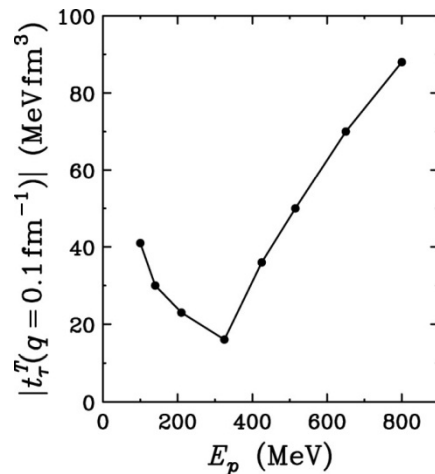
# Proportionality test-2 by Sasano

## Effects by tensor interaction

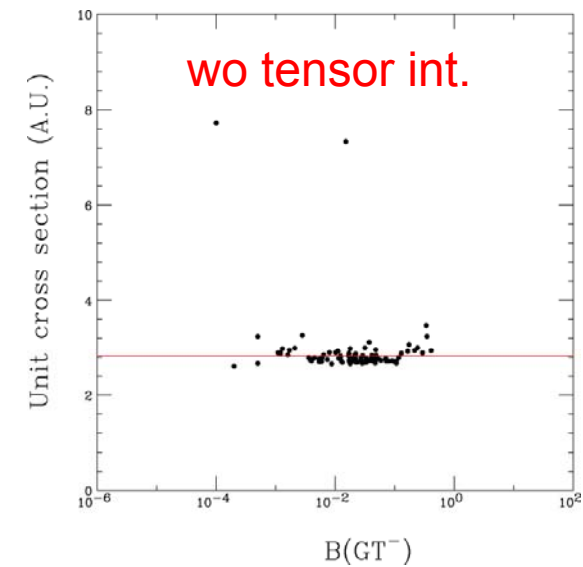
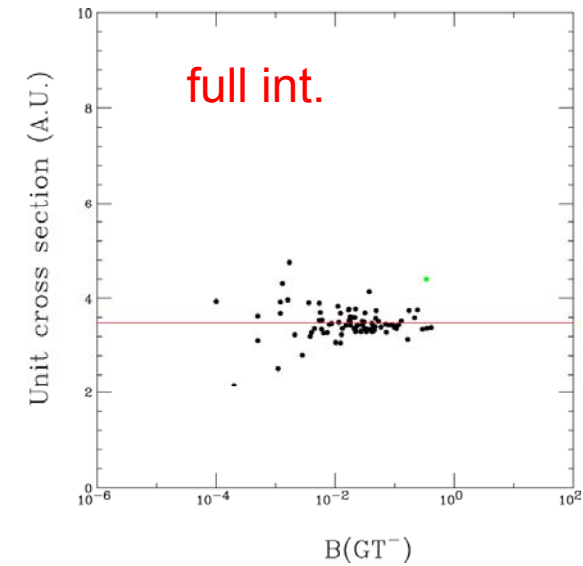
Exercise by using:

- ◆  $^{58}\text{Ni}$  system
- ◆ Shell model calculations
- ◆ Standard DWIA calc.  
with / without tensor interactions

Deviations are mainly due to the tensor interactions.



MDA might work best at 200-400 MeV.



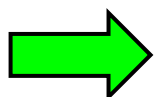
Continuum  $\rightarrow$  unbound transition density

Customary shallow binding approx. is used.

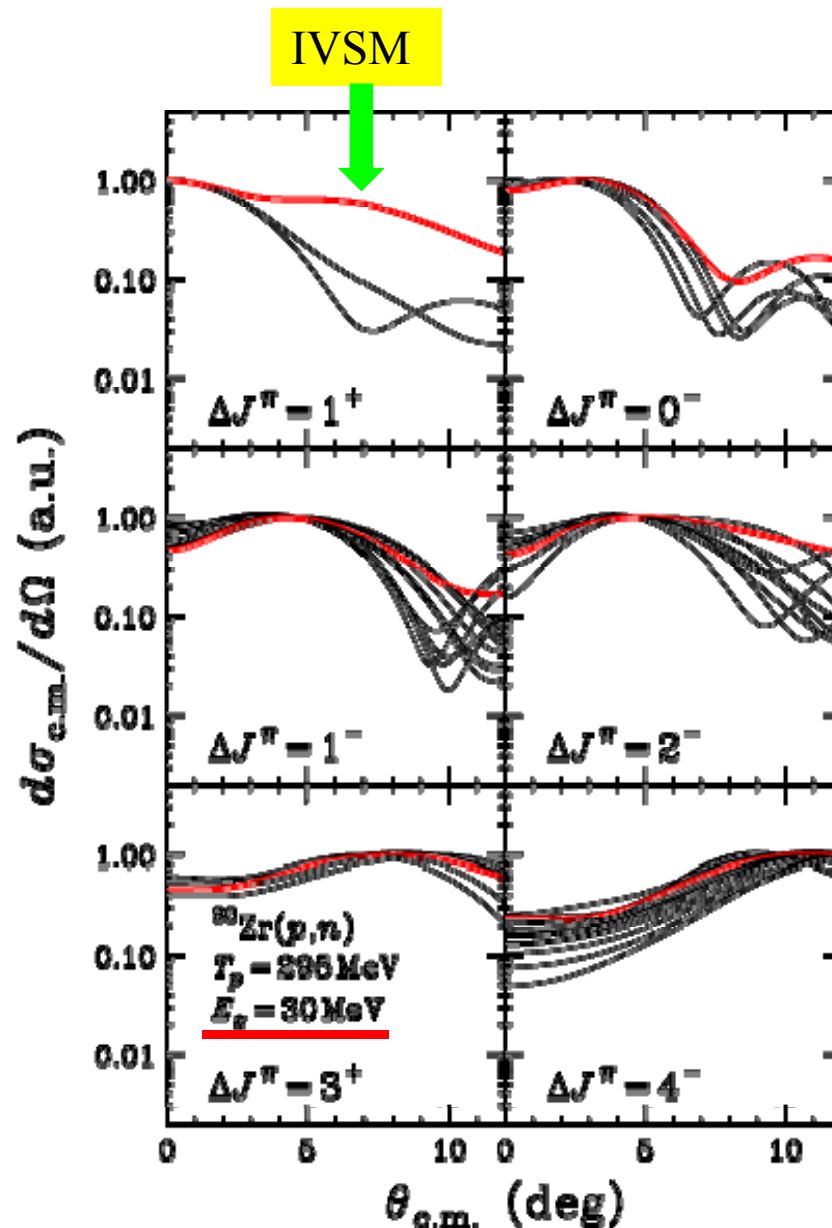
Need to check the validity

- **crdw code by Ichimura et al.**  
Phys.Rev. C 63, 044609 (2001).

➤ DWIA + continuum RPA



Shallow binding approx. seems to work well.



# Interferences

## GT vs. IVSM

$$\begin{aligned}\sigma_{\Delta L=0} &\propto \left| \langle \varphi_f | \langle \chi_f | V_{\text{int}} | \chi_i \rangle | \varphi_i \rangle \right|^2 \\ &\propto \left| \langle \varphi_f | C_{\text{GT}} O_{\text{GT}} + C_{\text{IVSM}} O_{\text{IVSM}} | \varphi_i \rangle \right|^2 \\ &\propto \underbrace{\left| \langle \varphi_f | C_{\text{GT}} O_{\text{GT}} | \varphi_i \rangle \right|^2}_{\sigma_{\text{GT}}} + \underbrace{\left| \langle \varphi_f | C_{\text{IVSM}} O_{\text{IVSM}} | \varphi_i \rangle \right|^2}_{\sigma_{\text{IVSM}}} + \underbrace{2 \operatorname{Re} \left( \langle \varphi_i | C_{\text{IVSM}}^* O_{\text{IVSM}}^* | \varphi_f \rangle \langle \varphi_f | C_{\text{GT}} O_{\text{GT}} | \varphi_i \rangle \right)}_{\sigma_{\text{int}'f} : \text{interference}}\end{aligned}$$

### ● $1^+$ state consists of:

$$\begin{aligned}|1^+\rangle &= | \text{GT}; \Delta S = 1, \Delta L = 0(2), 0\hbar\omega \rangle \\ &+ | \text{IVSM}; \Delta S = 1, \Delta L = 0, 2\hbar\omega \rangle \\ &+ | \text{SQR}; \Delta S = 1, \Delta L = 2, 2\hbar\omega \rangle\end{aligned}$$

Strictly speaking:  
 $|0 \hbar\omega\rangle$  and  $|2 \hbar\omega\rangle$  are  
not orthogonal.

→ In principle they all **interfere!**

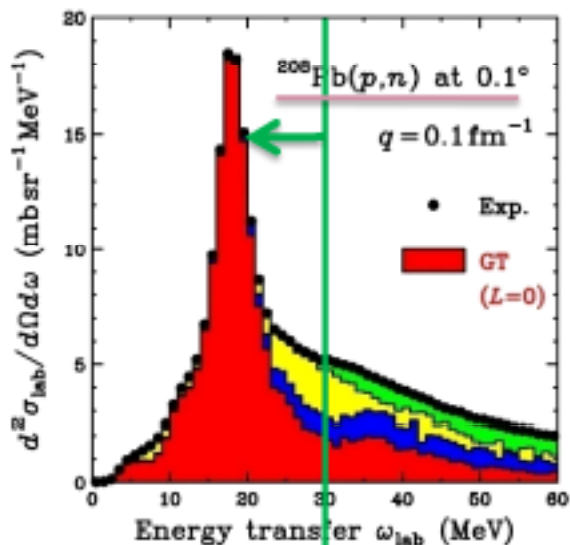
→ Two sources of interferences

- 1  $\Delta L=0$  and  $\Delta L=2$  within a mode
- 2 mode interference; GT vs. IVSM

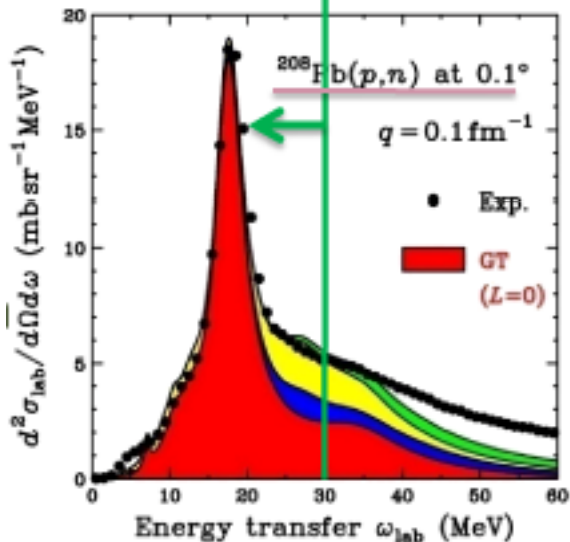
### ● How to disentangle experimentally?

## MDA vs. DWIA for $^{208}\text{Pb}(p,n)$ 300 MeV

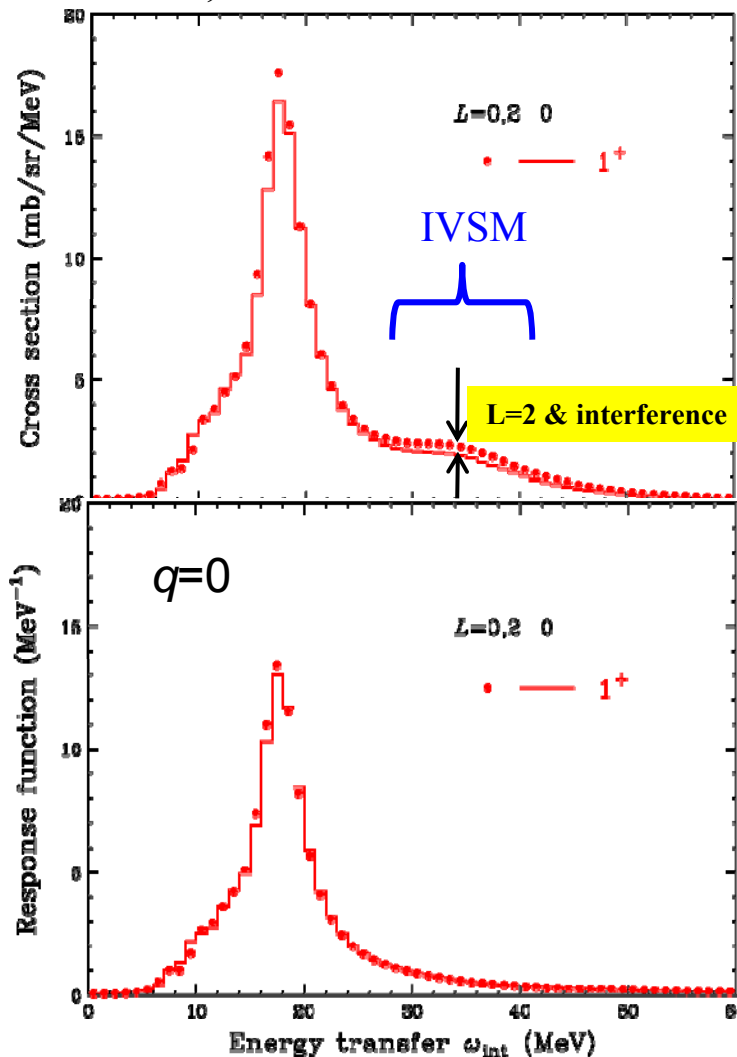
MDA



DWIA(crdw)



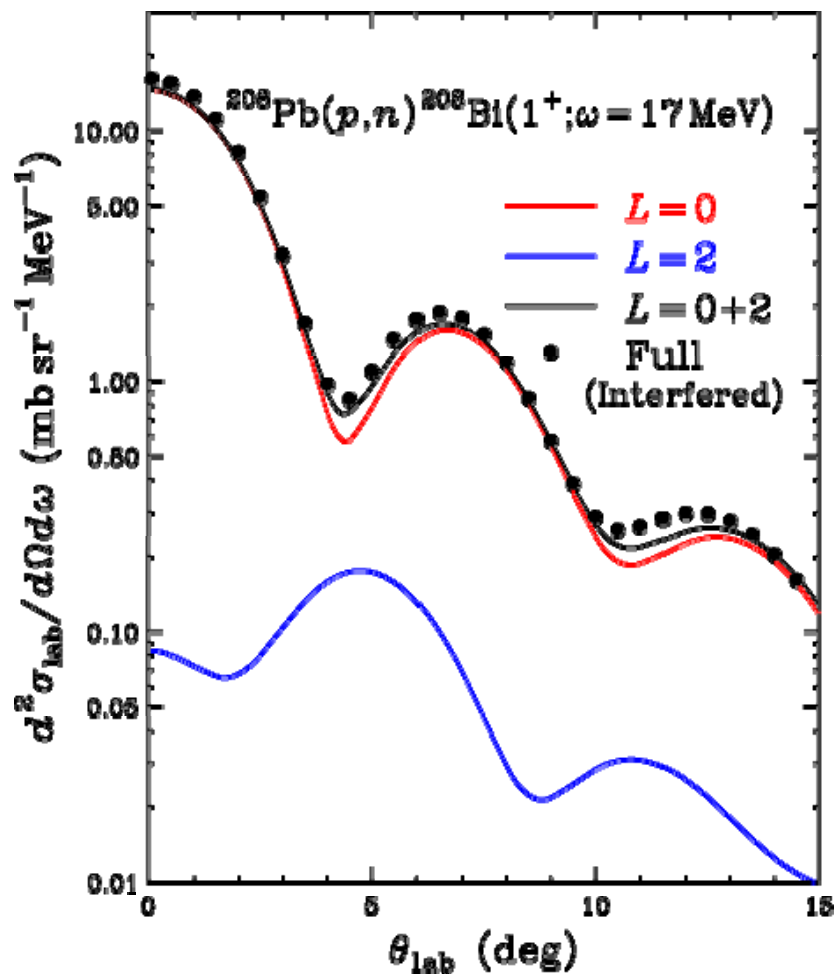
## L=0, L=2 and interference



$J^\pi=1^+$  response consists of  
 GT + IVSM + interference !

# L=0, L=2 and their interference (exercise by Wakasa)

L=0, L=2 and interference



Few % effect by interference is seen.

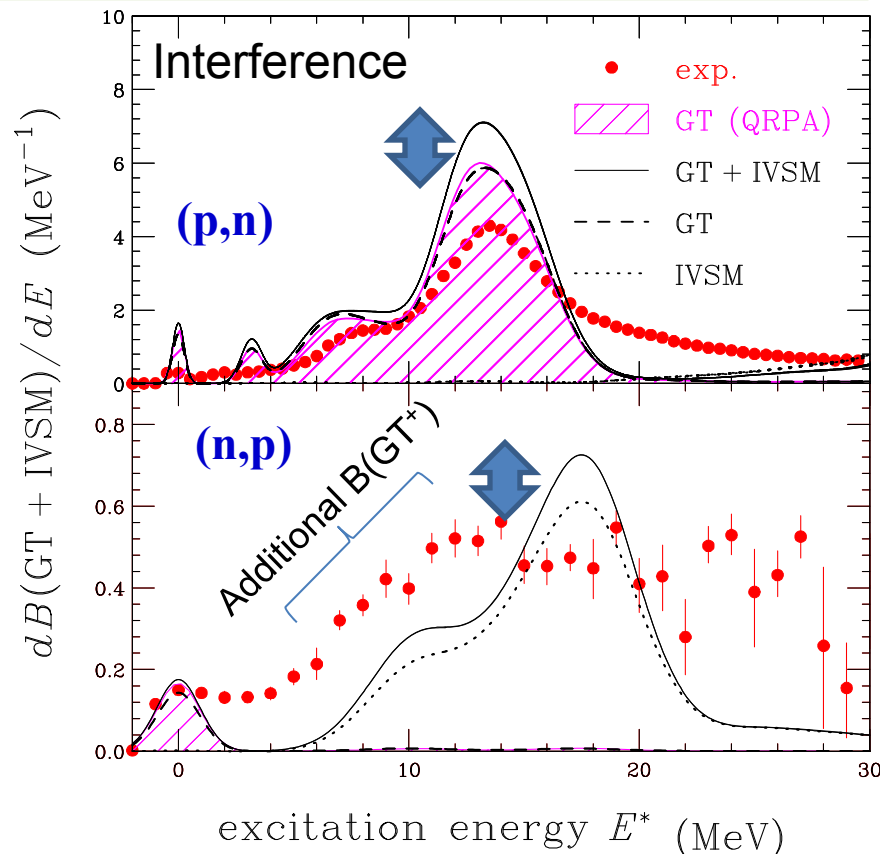


# Interference between GT+IVSM (Sasano data and calc.)

- $^{116}\text{Cd}(p,n)^{116}\text{In}$  at 300 MeV
- $^{116}\text{Sn}(n,p)^{116}\text{In}$

Scat. amp.:  $T = T_{0hw}(\text{GT}) + T_{2hw}(\text{IVSM})$   
 $|T|^2 = |T_{0hw}|^2 + |T_{2hw}|^2$   
 $+ 2 \text{Re}(T_{0hw}^* T_{2hw})$

QRPA (GT + IVSM)  
 (Rodin et al., Tuebingen Univ.)  
 Large model space (34 levels)  
 $\Rightarrow 2hw$   
 quenching factor, 0.843  
 &  $g_{pp} = 0.5$



	Theo.			Exp.
	GT	IVSM	GT+IVSM	GT+IVSM
$\beta^+$	0.4	5.4	6.8	$11 \pm 1$
$\beta^-$	42	4	52	$45 \pm 8$

Strengths around 10 MeV are partly reproduced, but still underestimated in the calculation.

- **Unit cross section**
  - **Must be experimentally calibrated**
- **Proportionality : recover (?) for the continuum**
  - **Poor  $\Delta E$  helps? (average over  $\Delta E$ )**
- **MDA**
  - **Shallow binding treatment seems to work**
- **Interference (exercise)**
  - **between  $L=0$  and  $L=2$ (IVSQ) : seems to be small**
  - **between GT and IVSM : ?**

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- – *observation of GT giant resonance and SDR* –

4 Summary

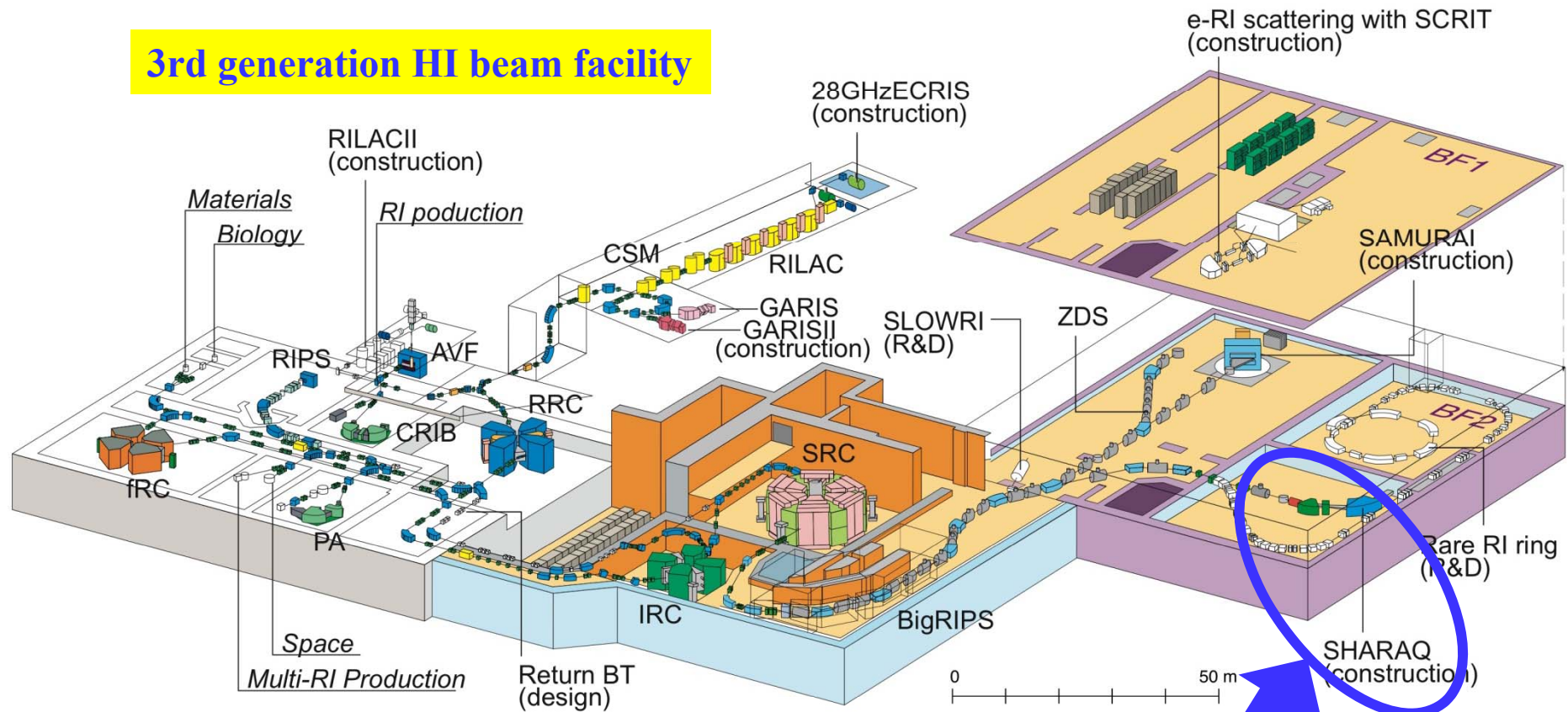
## Studies on spin-isospin responses by composite projectiles

- $\beta^+$  IVSM search by (t,  $^3\text{He}$ ) reaction
- $\beta^-$  IVSM search by ( $^{12}\text{N}$ ,  $^{12}\text{C}$ ) reaction

# RI Beam Facility of RIKEN



## 3rd generation HI beam facility



**SHARAQ**

## SHARAQ magnetic spectrometer :

Constructed by Univ. Tokyo under ICHOR project



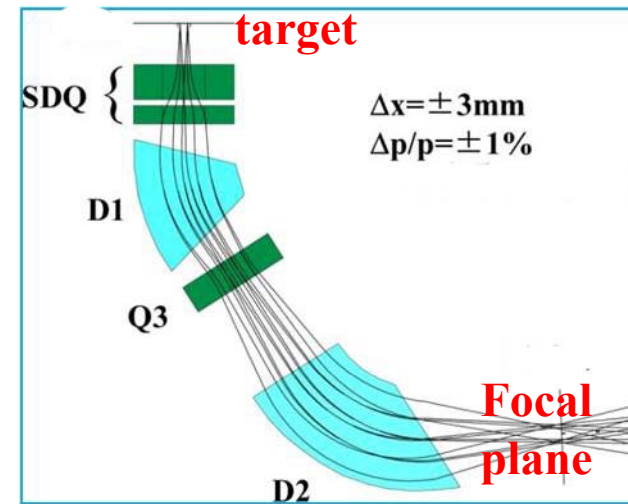
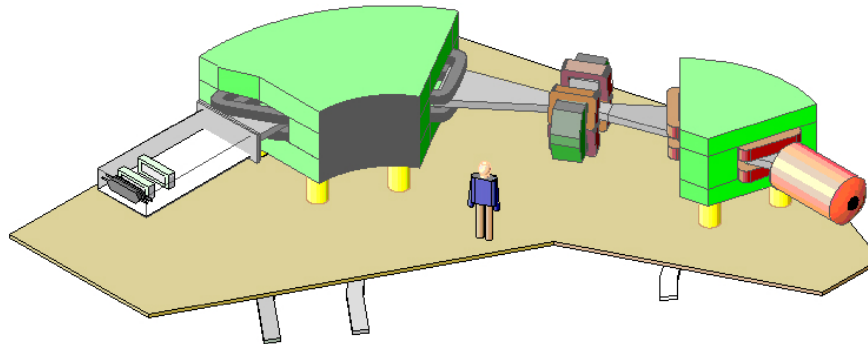
Sharaku

- Isospin-spin responses in CHarge-exchange exOthermic Reactions (ICHOR)
- Under the Grant-in-Aid for Specially Promoted Research of MEX
- Spokesperson: H. Sakai (University of Tokyo)
- Approved at 2005 for 5 years.
- Total budget: about \$5M.

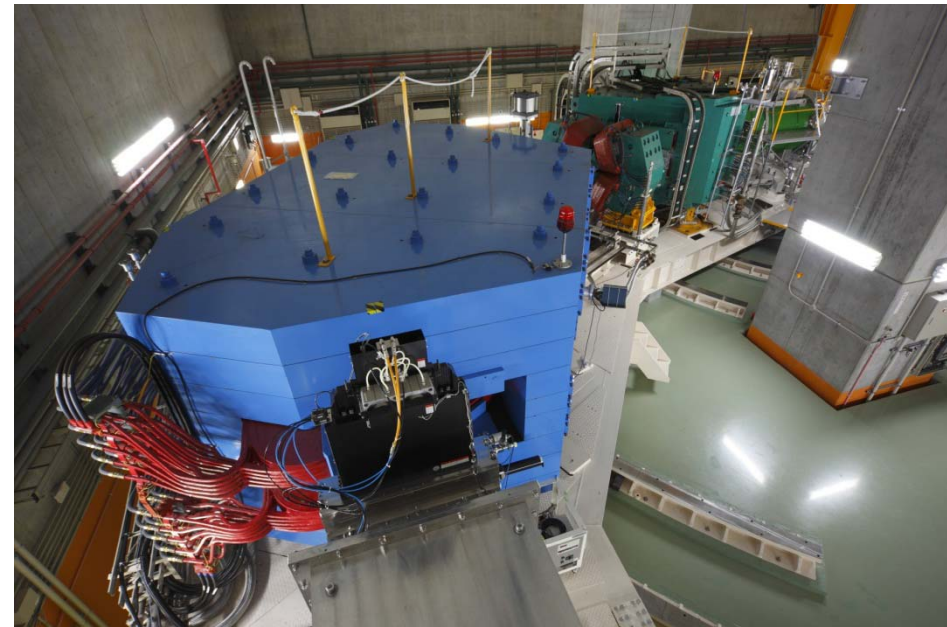


# SHARAQ Characteristic

Dedicated to the missing mass spectroscopy by unstable RI beams.



- QQDQD type
- Maximum rigidity 6.8 Tm
- $\delta p/p = 1/14700$
- Dispersion matching  $(x|\delta)$ ,  $(\theta|\delta)$
- Angular resolution  $< 1$  mrad
- Solid angle 2.7 msr
- Rotatable (-2 to 15 degree)
- Weight 500 tons



# Experiments at SHARAQ since 2009



- ◆ Measurement of the spin isovector monopole resonance via the (t,<sup>3</sup>He) reaction at 900 MeV (approved)

Spokesperson: K. Miki

Done in 2009. (First experiment!)

Search for IVSM  
 $\beta^+$  direction

- ◆ Studies of isovector non-spin-flip monopole resonance via the super-allowed Fermi type charge exchange reaction

Spokesperson: Y. Sasamoto

Done in 2010.

Search for IVM  
 $\beta^-$  direction

- ◆ Development of Exothermic charge-exchange reaction as a new spin-isospin probe and its application to the observation of the isovector spin monopole resonance in <sup>90</sup>Nb

Spokesperson: S. Noji

Done in 2010.

Search for IVSM  
 $\beta^-$  direction

- ◆ Direct mass measurement of neutron-rich Calcium isotopes at N~34

Spokesperson: S. Michimasa

(approved)

High resolution  
of SHARAQ

- ◆ Tetra-neutron system produced by exothermic double-charge exchange reaction

Spokesperson: S. Shimoura

(approved)

Tetra-neutron

- ◆ Spin-isospin excitations of <sup>12</sup>Be via the (p,n) reaction in inverse kinematics

Spokesperson: K. Yako

Done in June 2011. 2 months ago!

(p,n) in inverse-  
kinematic



**Search for the  $\beta^+$  IVSM by  $(t, {}^3\text{He})$  reactions at 300 MeV/A**

**Spokesperson: K. Miki, Univ. Tokyo**

# $\beta^+$ Iso-Vector Spin-Monopole Resonance

- Purpose : **search for IVSMR( $\beta^+$ )**

Isovector compression mode with spin

Previous Exp.

IVSMR( $\beta^-$ ) – a few signatures

IVSMR( $\beta^+$ ) – **no** clear signature

- Experiment

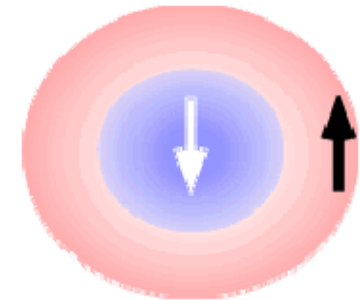
**( $t, ^3\text{He}$ )** reaction at **300 MeV/u** for  **$^{208}\text{Pb}$**  and  **$^{90}\text{Zr}$**

**BigRIPS + SHARAQ**

- Why ( $t, ^3\text{He}$ ) reaction at 300 MeV/u ?

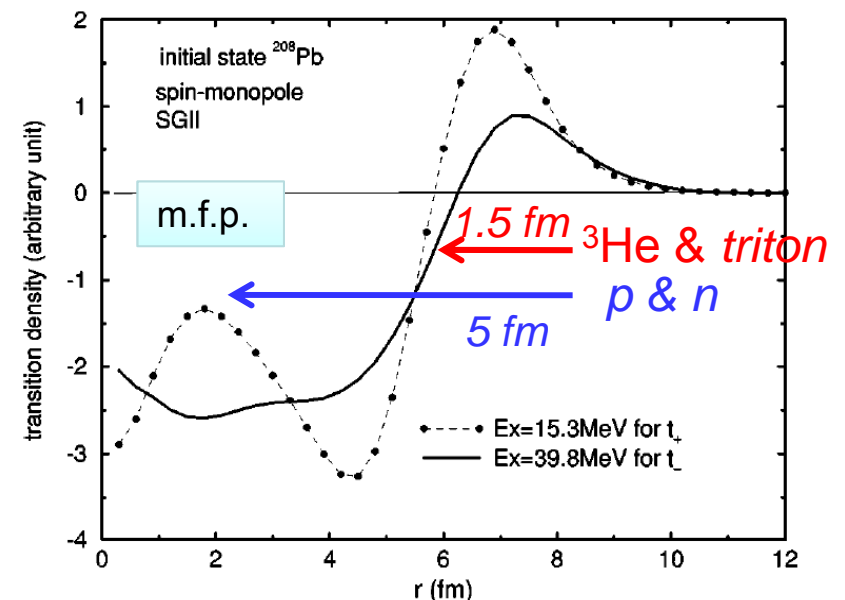
Why  $^{208}\text{Pb}$  and  $^{90}\text{Zr}$  targets ?

1. **strong spin-isospin excitation**
2. **large absorption effect**
3. **strong Pauli-blocking effect**



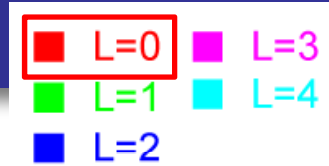
$$\Delta L=0, \Delta S=1$$

$$2\hbar\omega$$

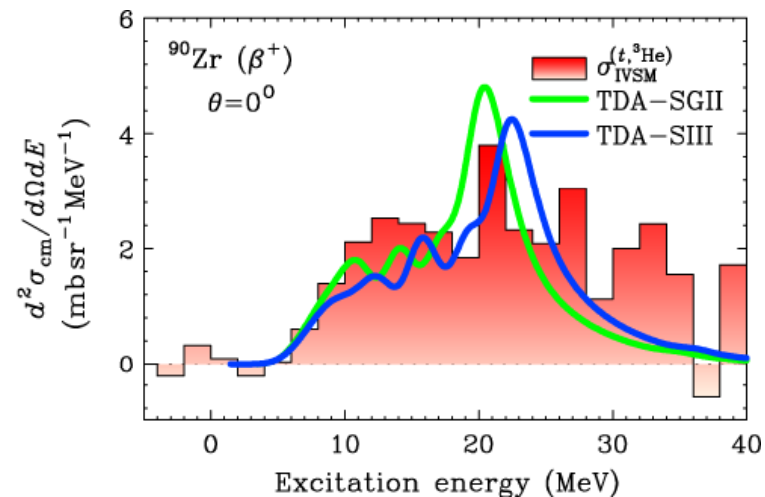
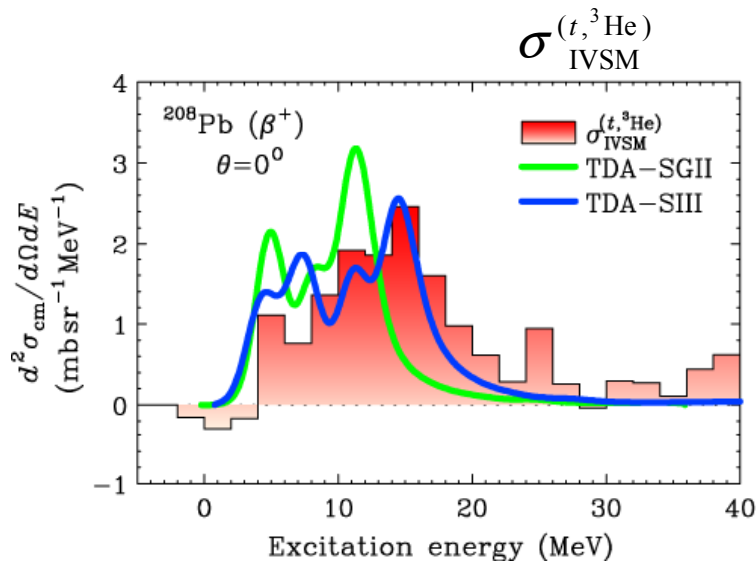
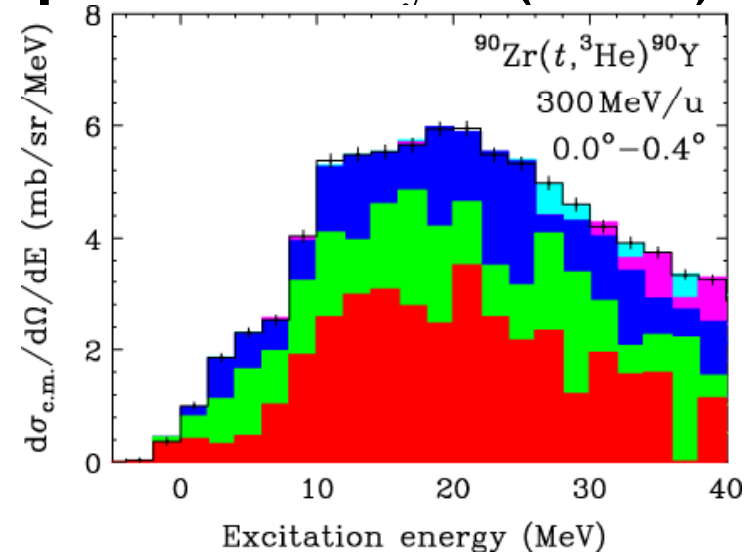
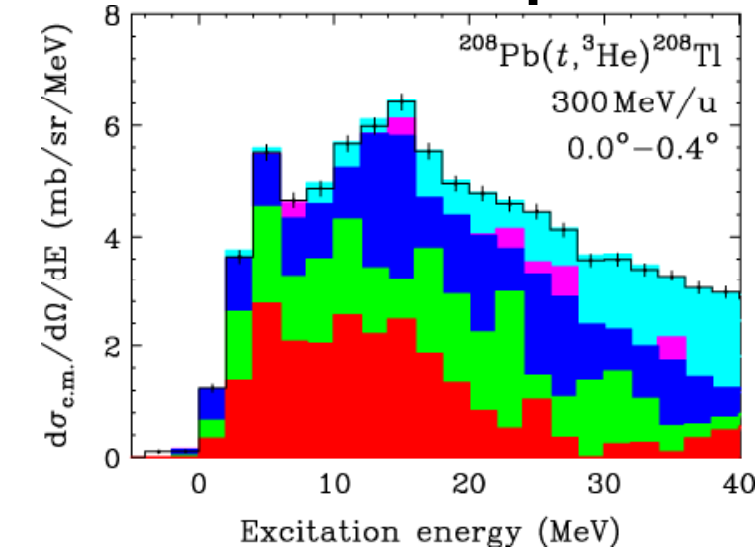


Hamamoto and Sagawa  
PRC 62 (2000) 024319

# IVSM study by ( $t, {}^3\text{He}$ ) reaction



## ● Result of the Multipole Decomposition Analysis (MDA)



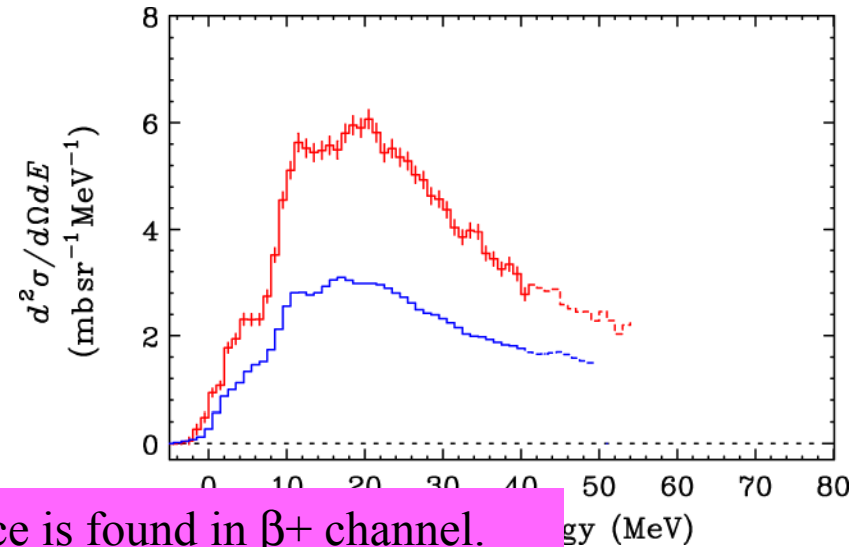
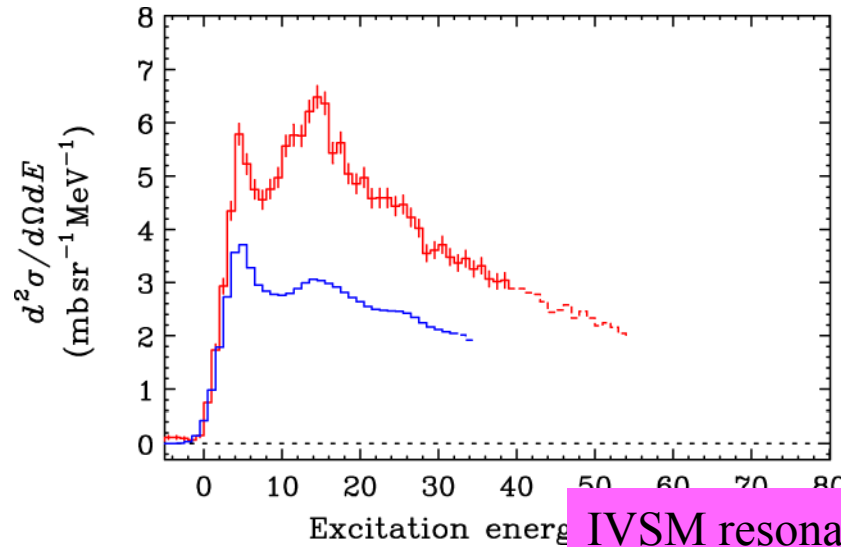
# Comparisons $(t, {}^3\text{He})/(n, p)$ vs. $({}^3\text{He}, t)/(p, n)$

${}^{208}\text{Pb}(t, {}^3\text{He})$  300MeV/u 0.0°-0.4° (RIBF)

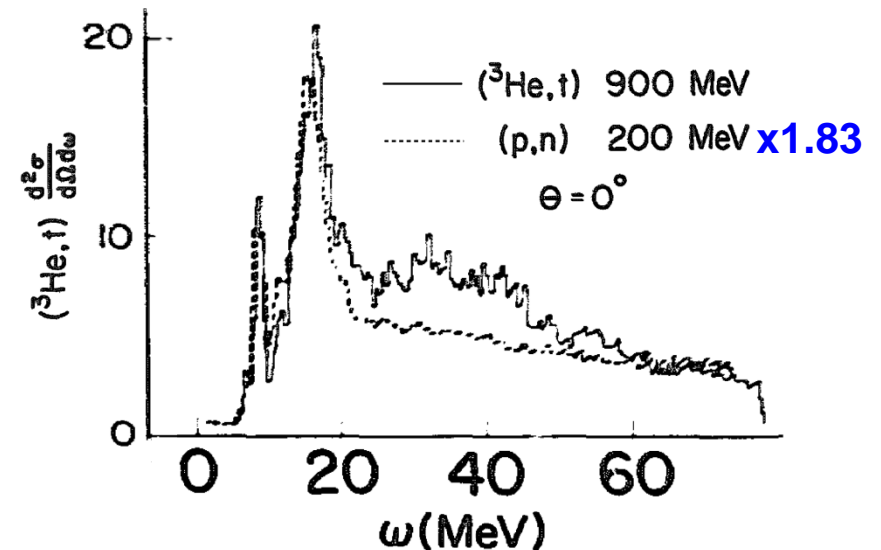
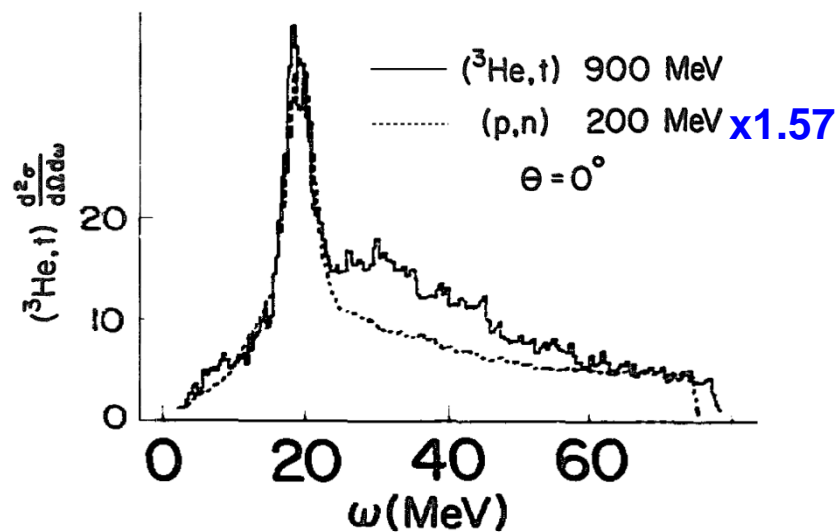
${}^{208}\text{Pb}(n, p)$  200MeV 0.0°-1.8° (TRIUMF) x1.57

${}^{90}\text{Zr}(t, {}^3\text{He})$  300MeV/u 0.0°-0.4° (RIBF)

${}^{90}\text{Zr}(n, p)$  300MeV 0.0°-1.0° (RCNP) x1.83



IVSM resonance is found in  $\beta^+$  channel.



## Exchange effects

- comparison between (p,n) and ( $^3\text{He}$ ,t) reactions

# Exchange

Anti-symmetrization (A simple case :  $N$ - $N$  system wo spin, isospin)

$\chi_{i,f}(\vec{r})$  --- Scattering wave function (proj, eject)

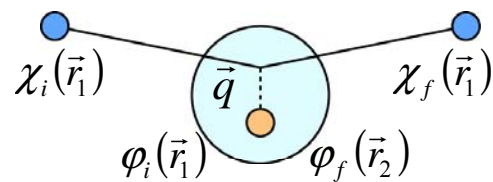
$\chi_f(\vec{r}_1)$  --- single-particle wave function (target)

$$\Psi_i = \frac{1}{\sqrt{2}} \begin{vmatrix} \chi_i(\vec{r}_1) & \varphi_i(\vec{r}_1) \\ \chi_i(\vec{r}_2) & \varphi_i(\vec{r}_2) \end{vmatrix}, \quad \Psi_f = \frac{1}{\sqrt{2}} \begin{vmatrix} \chi_f(\vec{r}_1) & \varphi_f(\vec{r}_1) \\ \chi_f(\vec{r}_2) & \varphi_f(\vec{r}_2) \end{vmatrix}$$

$$T = \langle \Psi_f | V_{\text{int}} | \Psi_i \rangle$$

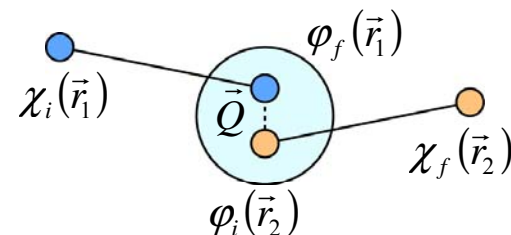
$$= \int d\vec{r}_1 \int d\vec{r}_2 \chi_f^*(\vec{r}_1) \varphi_f^*(\vec{r}_2) V_{\text{int}} \chi_i(\vec{r}_1) \varphi_i(\vec{r}_2) - \int d\vec{r}_1 \int d\vec{r}_2 \chi_f^*(\vec{r}_1) \varphi_f^*(\vec{r}_2) V_{\text{int}} \chi_i(\vec{r}_2) \varphi_i(\vec{r}_1)$$

Direct



Reducible down to  
2-dim. radial integral (easy)

Exchange (knock-on)



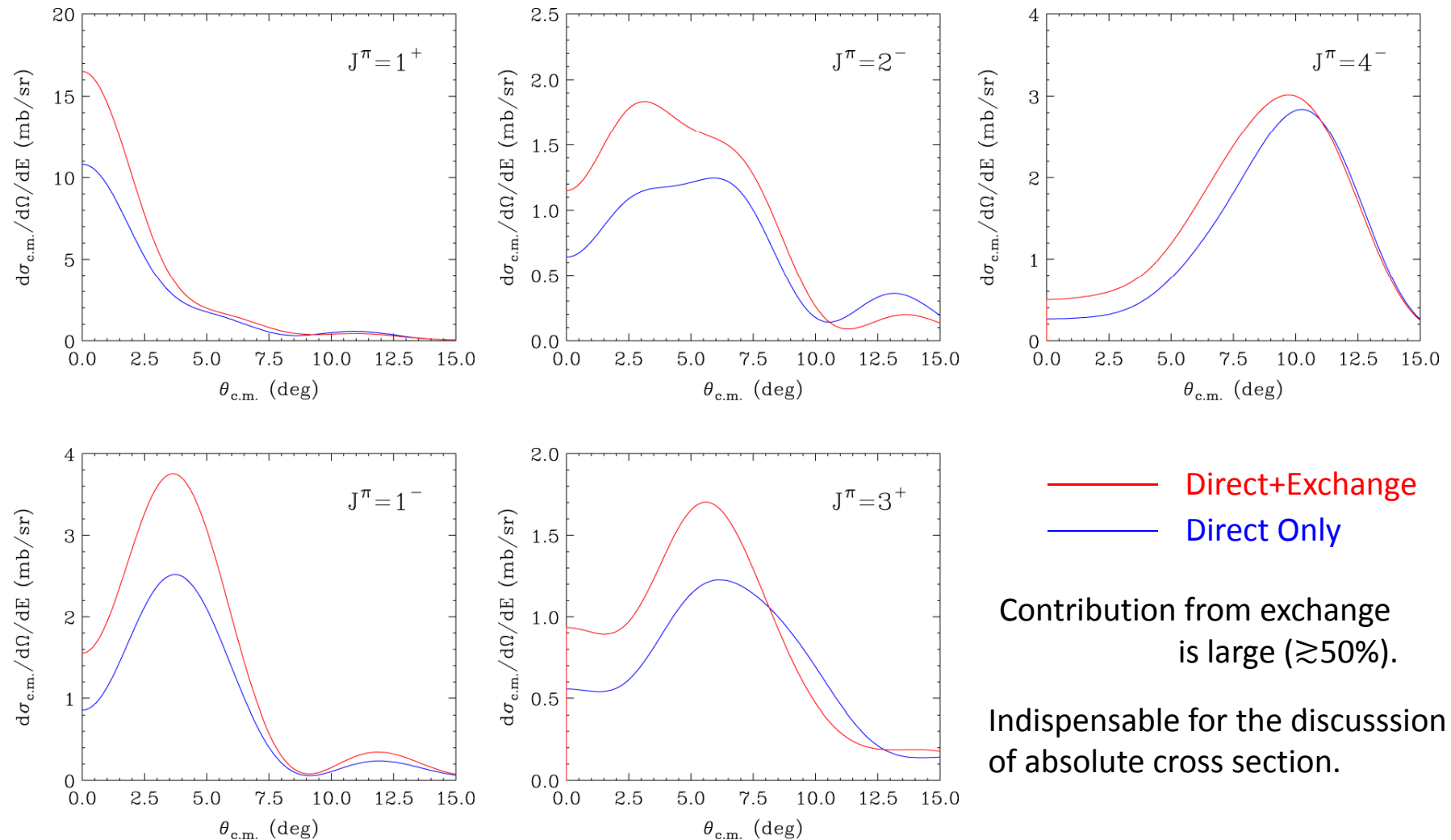
Irreducible...  
6-dim. integral (difficult)  
→ approx. : short-range, central only, ...

# $^{208}\text{Pb}(n,p)$ at 300MeV as an example

$^{208}\text{Pb}(n,p)$  at 300MeV

Computer Code : DW81 (“Knock-on exchange is calculated exactly”)

N-N interaction : Franey-Love 325MeV



# Direct and exchange effects in ( $^3\text{He}, t$ )

- DWHI+FOLD : rather difficult to calculate exchange effects
- DCP-1 code : includes knock-on exchange effects

(Distorted wave impulse approximation code for Composite-Particle scattering)

Udagawa, Schulte and Osterfeld, NP A474 (1987) 131.

Contributions from the Exchange Term in  
 $^{12}\text{C}(p, n)$  and  $(h, t)$  Reactions

$1^+, 0^0$

Reaction	E(MeV)	$\ell_t$	$\sigma(\text{D})$	$\sigma(\text{E})$	$\sigma(\text{D+E})$	$\sigma(\text{D+E})/\sigma(\text{D})$
(p,n)	200	0	14.0	1.02	7.46	0.53
		2	0.03	0.002	0.037	1.38
		0+2	14.0	1.02	7.50	0.54
(h,t)	600	0	47.4	0.028	27.5	0.58
		2	0.272	0.039	0.501	1.84
		0+2	47.7	0.067	28.0	0.59
(p,n)	300	0	4.59	0.426	6.10	1.33
		2	0.037	0.002	0.104	2.79
		0+2	4.63	0.428	6.20	1.34
(h,t)	900	0	16.2	1.40	20.3	1.25
		2	0.293	0.078	0.662	2.26
		0+2	16.5	1.48	21.0	1.27

Large exchange effects !  
→ However .....

Energy dependent! Very subtle  
→(p,n)~(3He,t), if this is a general  
feature, then ....



# Computer Codes for DWBA, DWIA



- Computer Codes (for experimentalist ?)

\* Only for KNOCK-ON exchange.  
No code available for FULL exchange.

	Author/Maintainer	N-A	A-A	Exchange (*)	Note.
DWUCK4	Kunz	O	$\Delta$	Short-range approx.	
TWOFNR	Igarashi et.al.	O	$\Delta$	Short-range approx.	
DW81	Comfort, Love	O	$\Delta$	Exact	
DWBA98	Raynal et.al.	O	$\Delta$	Exact	
DGP-1	Udagawa et.al.	O	O	Exact	Lost...?
FOLD	Zegers et.al.	O	O	Short-range approx.	Developing...?

Double folding

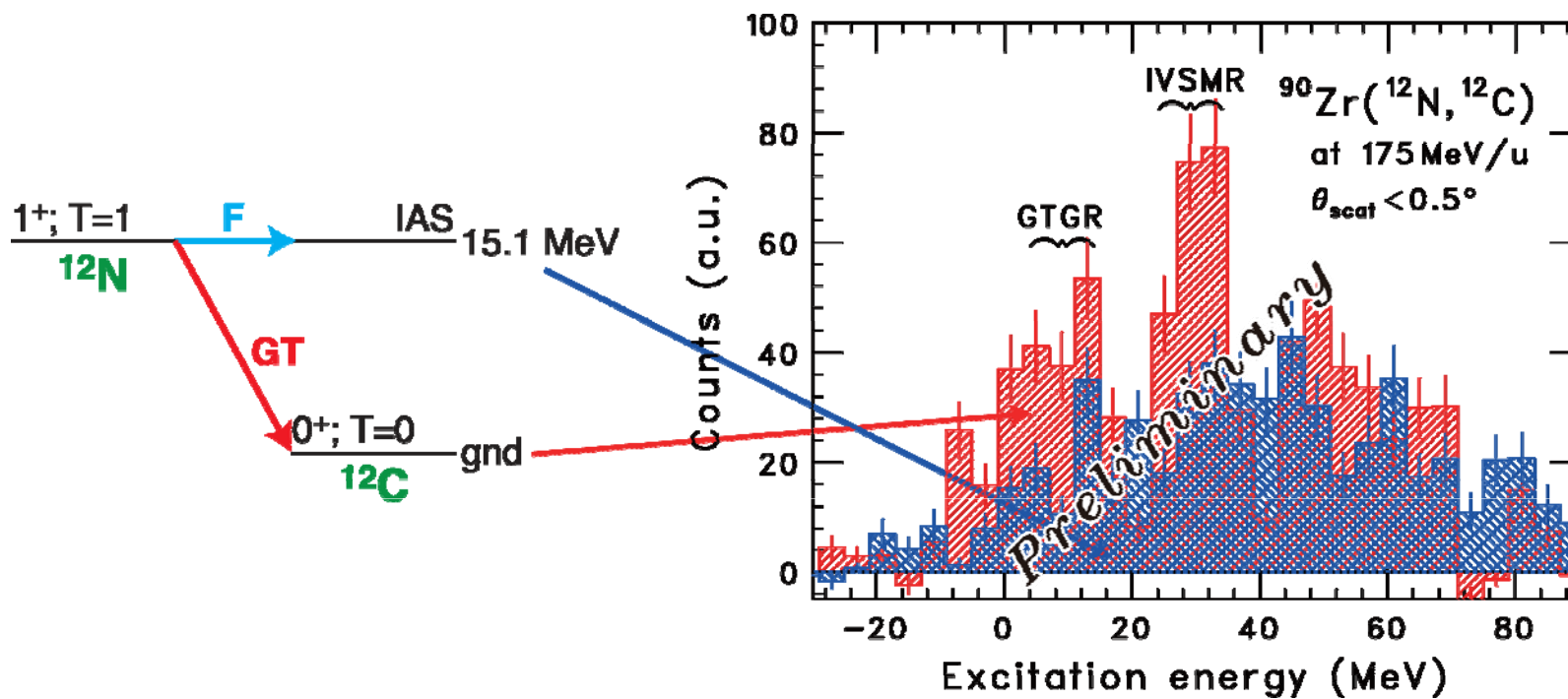
→ **Wanted** : Code for **A-A** scattering with **Exact** treatment of **Exchange**.

**Search for the  $\beta^-$  IVSM search via  $(^{12}\text{N},^{12}\text{C})$  reactions**

**Spokesperson: S. Noji, Univ. Tokyo**



# Very very preliminary result by Noji



# Optical potentials

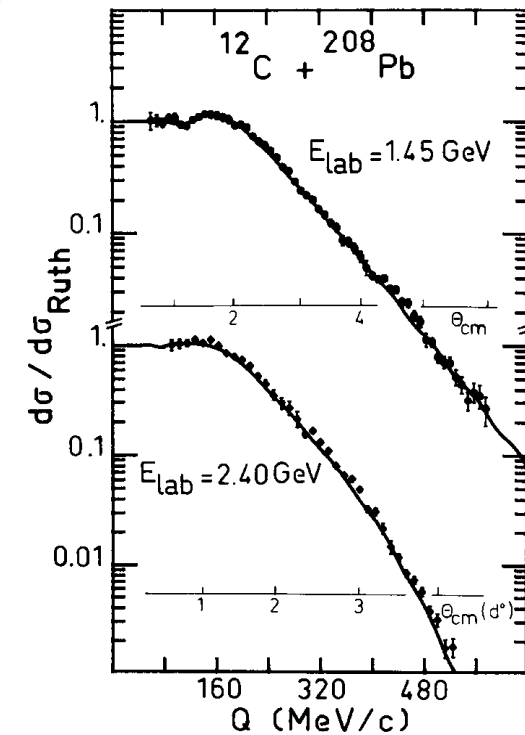
Nuclear Physics **A490** (1988) 441-470  
North-Holland, Amsterdam

## ELASTIC AND INELASTIC SCATTERING OF $^{12}\text{C}$ IONS AT INTERMEDIATE ENERGIES

J.Y. HOSTACHY, M. BUENERD, J. CHAUVIN, D. LEBRUN and Ph. MARTIN  
*ISN Grenoble, 53, Avenue des Martyrs, 38026 Grenoble Cedex, France*

J.C. LUGOL, L. PAPINEAU, P. ROUSSEL and N. ALAMANOS  
*DPhN, CEN Saclay, 91191 Gif-sur-Yvette Cedex, France*

J. ARVIEUX and C. CERRUTI  
*Laboratoire National Saturne, F-91191 Gif-sur-Yvette, France*



$E/A$ (MeV/u)	$V_0$ (MeV)	$r_R$ (fm)	$a_R$ (fm)	$W_0$ (MeV)	$r_I$ (fm)	$a_I$ (fm)	$\sigma_r$ (mb)	$\chi^2/N$
200	10	0.803	0.815	35.82	0.991	1.186	3.61	1.87
	20	0.869	0.345	16.59	1.234	0.739	3.58	1.50
	35.68	0.900	0.466	14.06	1.238	0.743	3.47	1.45
	40	0.748	0.649	26.17	1.080	1.063	3.59	1.64
	50	0.889	0.508	14.85	1.226	0.788	3.51	1.79
	72.15	0.195	1.275	95.28	0.692	1.526	3.75	1.92

# Ambiguities by $V_{\text{eff}}$ and optical potentials

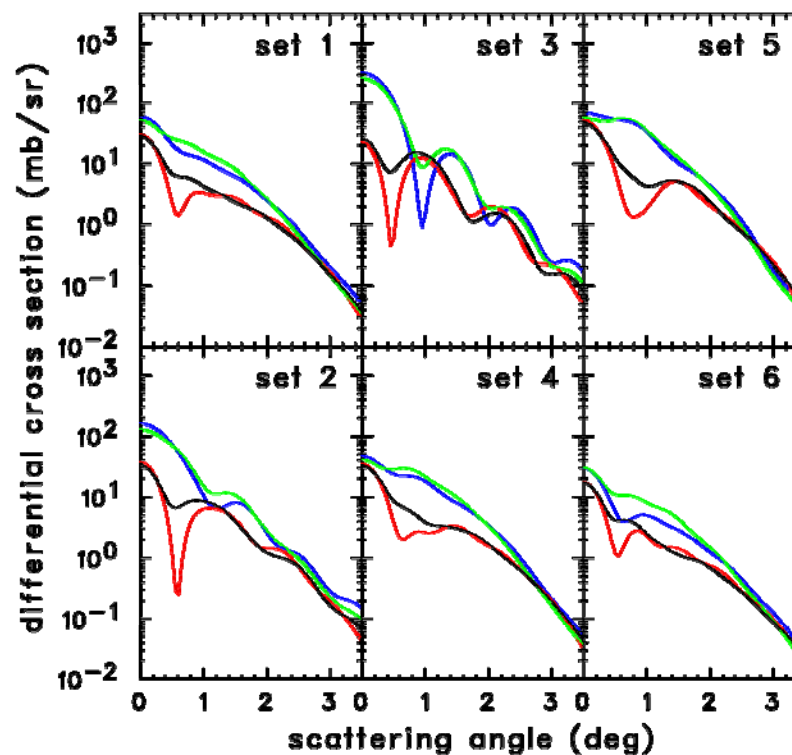
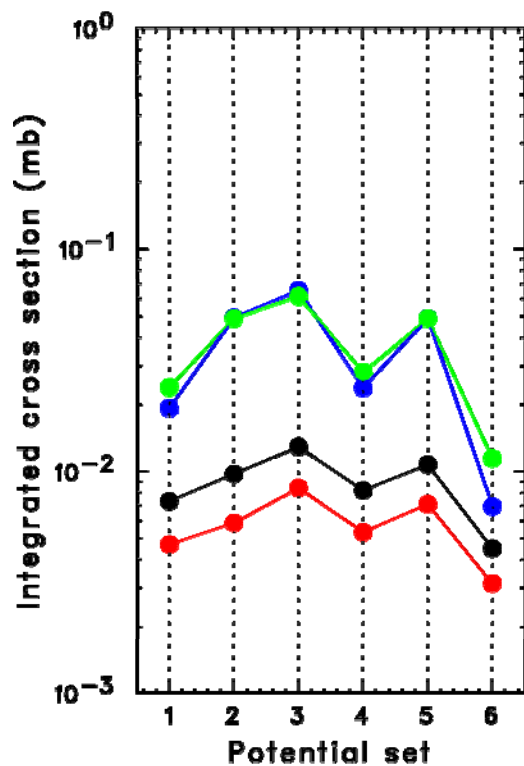
$^{90}\text{Zr}(^{12}\text{N}, ^{12}\text{C})^{90}\text{Nb}$  at  $E=200\text{A MeV}$   
NM-OBTD, FL100MeV  
OMP:  $^{12}\text{C} + ^{208}\text{Pb}$  at  $200\text{A MeV}$   
Hostachy et al., NP A490 (1988) 441

GT,  $E_x=9.0\text{ MeV}$

IVSM,  $E_x=32\text{ MeV}$

IAS,  $E_x=5.1\text{ MeV}$

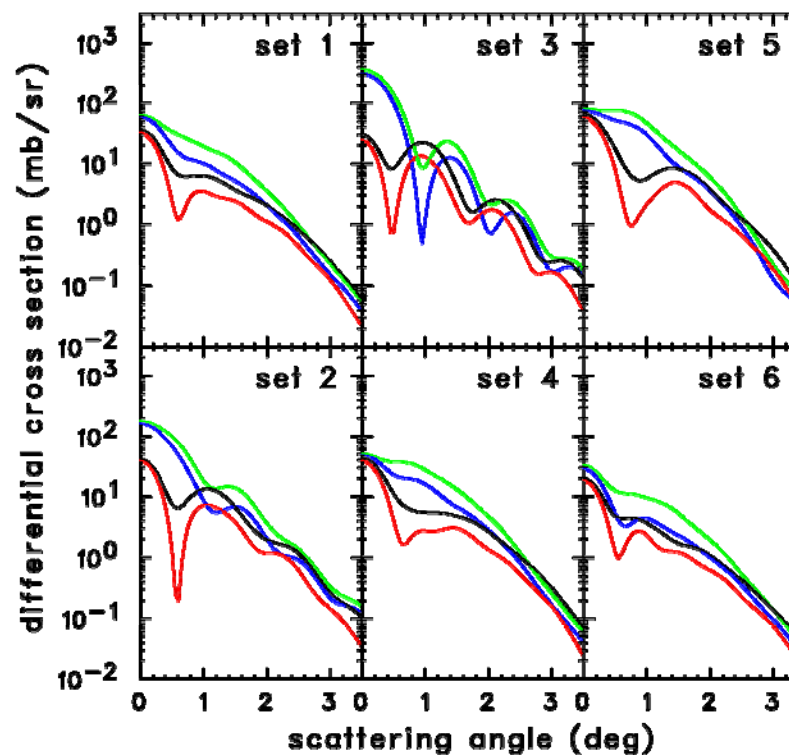
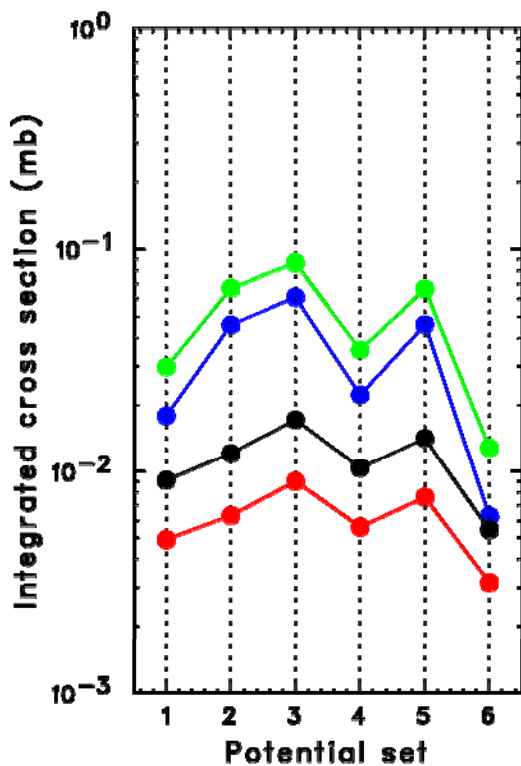
IVM,  $E_x=25\text{ MeV}$



# Ambiguities by $V_{\text{eff}}$ and optical potentials

$^{90}\text{Zr}(^{12}\text{N}, ^{12}\text{C})^{90}\text{Nb}$  at  $E=200\text{A MeV}$   
 NM-OBT, FL175MeV  
 OMP:  $^{12}\text{C} + ^{208}\text{Pb}$  at  $200\text{A MeV}$   
 Hostachy et al., NP A490 (1988) 441

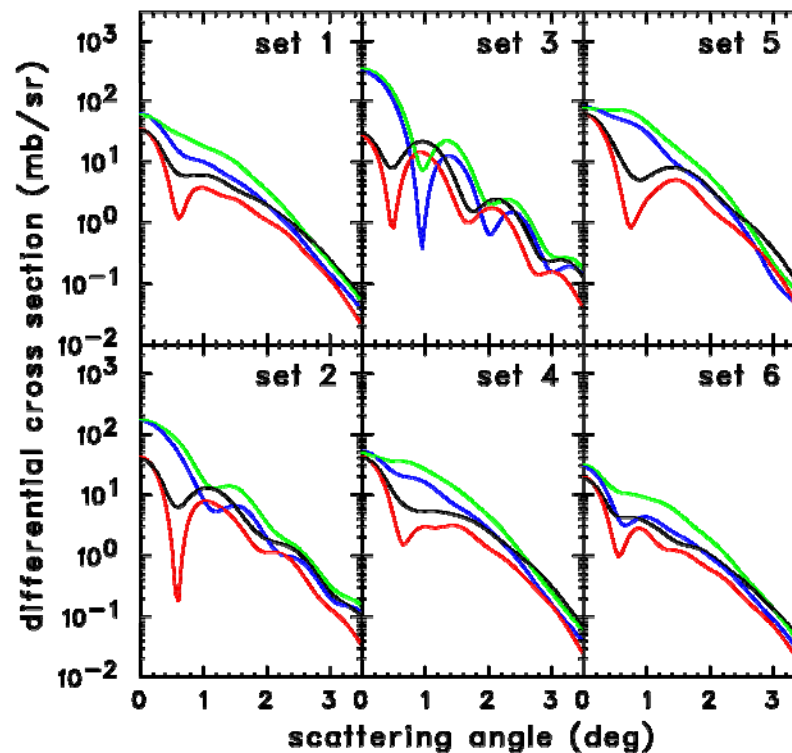
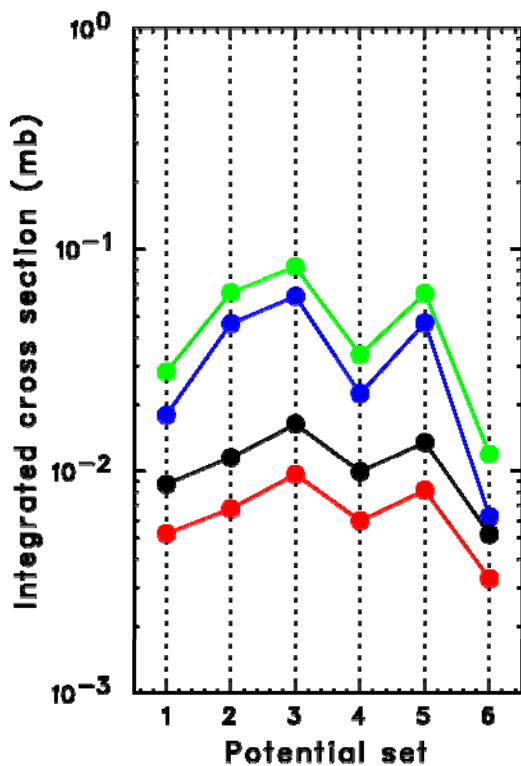
GT,  $E_x=9.0\text{ MeV}$   
 IVSM,  $E_x=32\text{ MeV}$   
 IAS,  $E_x=5.1\text{ MeV}$   
 IVM,  $E_x=25\text{ MeV}$



# Ambiguities by $V_{\text{eff}}$ and optical potentials

$^{90}\text{Zr}(^{12}\text{N}, ^{12}\text{C})^{90}\text{Nb}$  at  $E=200\text{A MeV}$   
 NM-OBT, FL210MeV  
 OMP:  $^{12}\text{C} + ^{208}\text{Pb}$  at  $200\text{A MeV}$   
 Hostachy et al., NP A490 (1988) 441

GT,  $E_x=9.0\text{ MeV}$   
 IVSM,  $E_x=32\text{ MeV}$   
 IAS,  $E_x=5.1\text{ MeV}$   
 IVM,  $E_x=25\text{ MeV}$

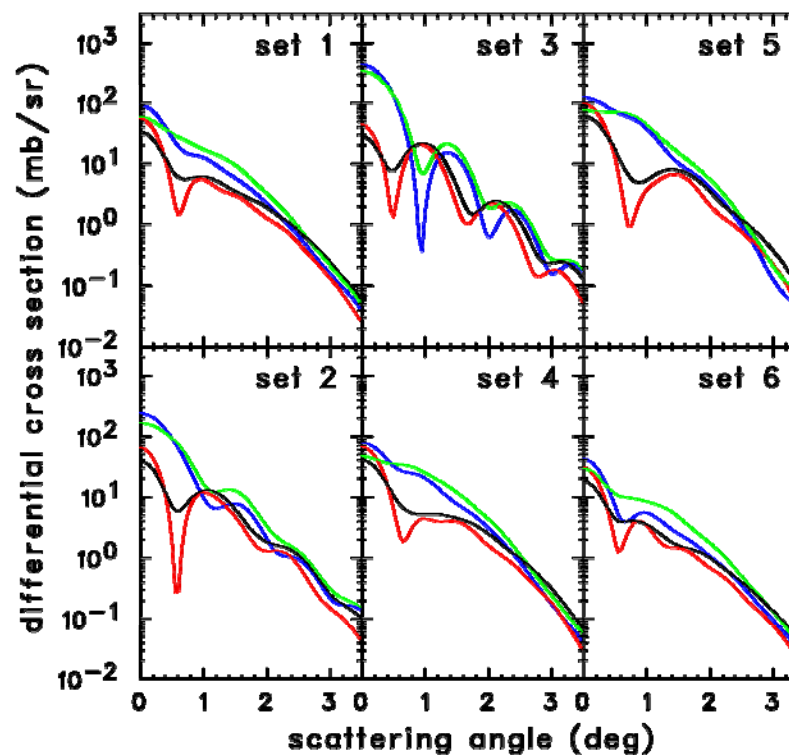
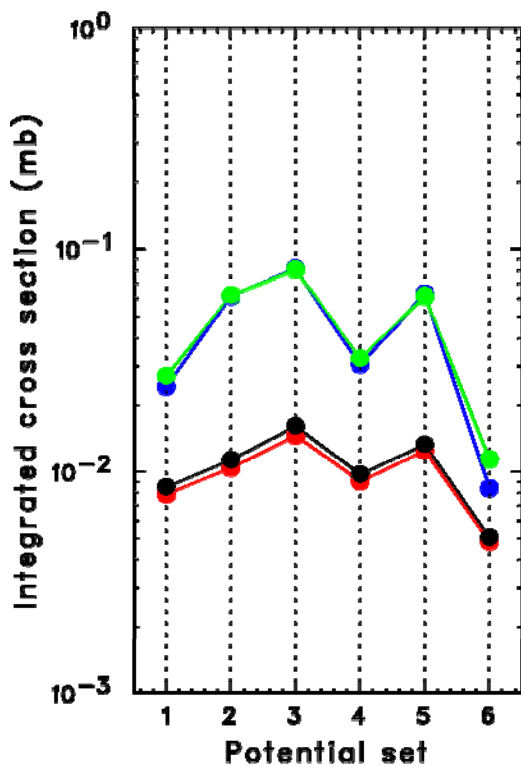




# Ambiguities by $V_{\text{eff}}$ and optical potentials

$^{90}\text{Zr}(^{12}\text{N}, ^{12}\text{C})^{90}\text{Nb}$  at  $E=200\text{A MeV}$   
NM-OBTD, FL270MeV  
OMP:  $^{12}\text{C} + ^{208}\text{Pb}$  at  $200\text{A MeV}$   
Hostachy et al., NP A490 (1988) 441

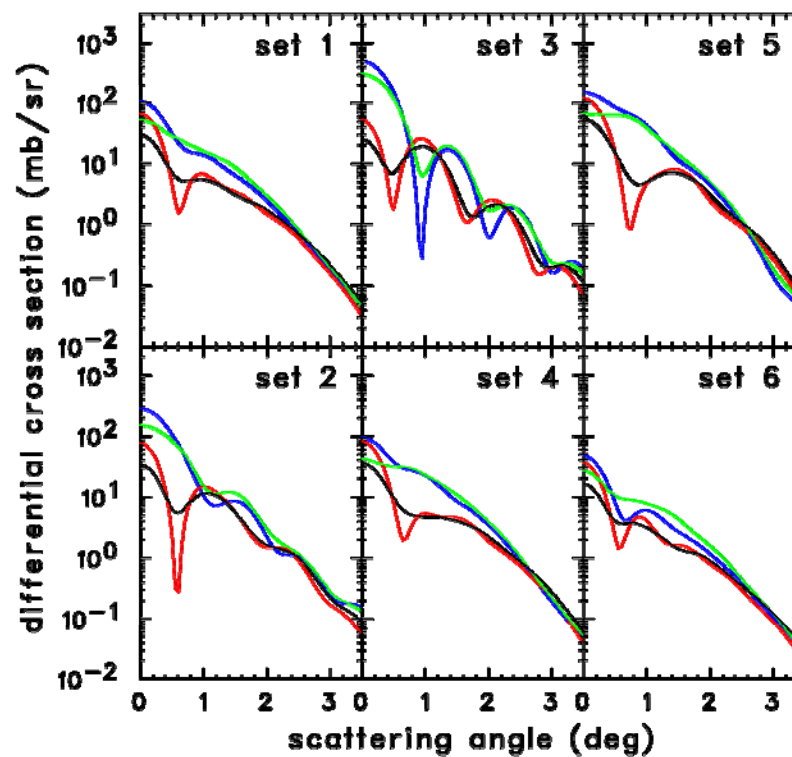
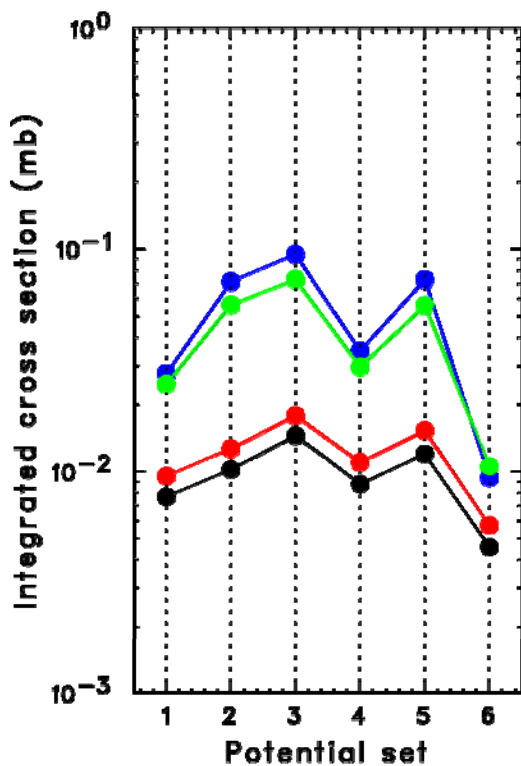
GT,  $E_x=9.0\text{ MeV}$   
IVSM,  $E_x=32\text{ MeV}$   
IAS,  $E_x=5.1\text{ MeV}$   
IVM,  $E_x=25\text{ MeV}$



# Ambiguities by $V_{\text{eff}}$ and optical potentials

$^{90}\text{Zr}(^{12}\text{N}, ^{12}\text{C})^{90}\text{Nb}$  at  $E=200\text{A MeV}$   
 NM-OBTD, FL325MeV  
 OMP:  $^{12}\text{C} + ^{208}\text{Pb}$  at  $200\text{A MeV}$   
 Hostachy et al., NP A490 (1988) 441

GT,  $E_x=9.0\text{ MeV}$   
 IVSM,  $E_x=32\text{ MeV}$   
 IAS,  $E_x=5.1\text{ MeV}$   
 IVM,  $E_x=25\text{ MeV}$



# Lessons by exercise



- Effective interaction dependence is rather small.
- An order of magnitude difference depending on optical pot. sets.
- Even angular distributions are different.
- How to choose optical potentials? → show a guideline

# Contents

1 How reliable are the spin-isospin responses in the **continuum** extracted by the **nucleon** CHEX reactions ?

- Measurement, analysis and associated uncertainties

- ✓ MDA

- ✓ unbound transition (shallow binding approx.) ?

- ✓ L=0, L=2 and their interference effect ?

- ✓ interference between GT and IVSM ?

- ✓ proportionality ?

2 How are they in the case of composite projectiles ?

- (t,<sup>3</sup>He,) reaction: measurement by Miki

- ✓ Exchange effects

- (<sup>12</sup>N,<sup>12</sup>C) reaction: measurement by Noji

- ✓ Ambiguities by optical potentials(imaginary part)

3 **Brand-new**: measurement of the exothermic <sup>12</sup>Be(p,n) reaction in inverse-kinematics at 200 MeV/A by Yako

- – *observation of GT giant resonance and SDR* –

4 Summary

**First measurement of the exothermic  
 $^{12}\text{Be}(p,n)$  reaction  
in inverse-kinematics at 200 MeV/A**

**Spokesperson: K. Yako**

# What is interesting in $^{12}\text{Be}$ ?

① large neutron asymmetry

$$\epsilon = \frac{(N-Z)}{A} = 0.33$$

② disappearance of closed shell N=8

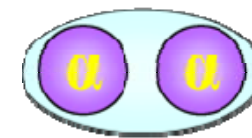
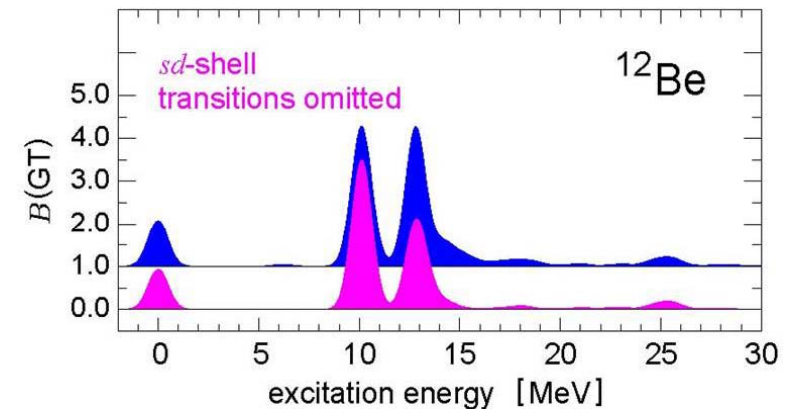
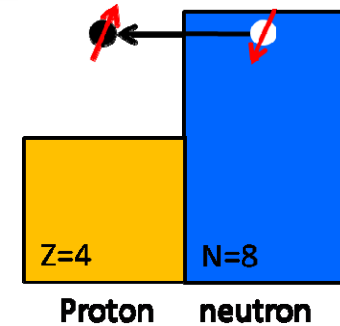
- 40% admixture of sd-orbits into p-orbits
- Effects on to GT transitions?
- Large effects on SDR transition?

$$O_{1\mu}^{\pm}(GT) = \sum_i \sigma_{\mu}(i) t_{\pm}(i)$$

$$\hat{O}^{\pm}(SDR) = \sum_{im\mu} t_{\pm}^i \sigma_m^i r_i Y_1^{\mu}(\hat{r}_i)$$

③ huge deformation (cluster structure)

- Ellipsoid ratio; long : short=2:1 !
- Large effects on SDR transition?
- Effects on GT transition?



**Aim: GT/SDR search in neutron rich nucleus  $^{12}\text{B}$**

⇒ collectivity of GT state

⇒ breaking of cluster structure by SDR

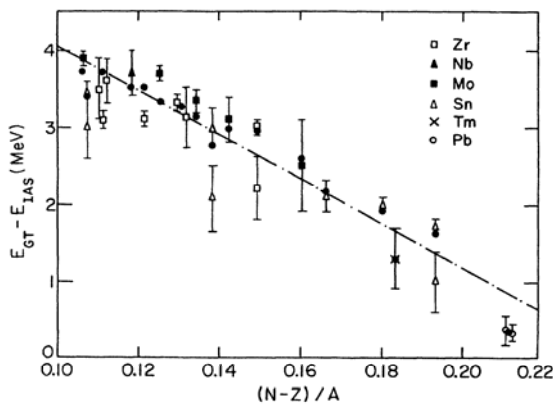
⇒ establish of new spectroscopic tool by unstable beams

# GTGR exists in light neutron-rich nuclei ?

Gamow-Teller state

$$|GTR\rangle = \sum_{i=1}^A \tau_-^{(i)} \sigma_-^{(i)} |0\rangle$$

$$\langle E_{GT} \rangle - \langle E_{IAS} \rangle = \Delta E_{ls} + 2(\tilde{\kappa}_{\sigma\tau} - \tilde{\kappa}_{\tau}) \frac{N-Z}{A}$$



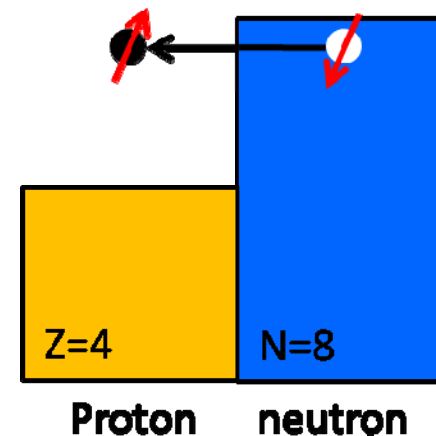
$\Delta E_{ls} = 1/2(\epsilon_{j>} - \epsilon_{j<})$ :  
Spin-orbit part of the  
single-particle energy

$\kappa_{\sigma\tau}(\kappa_{\tau})$ :  
particle-hole  
coupling constants

Nothing known beyond 0.22.

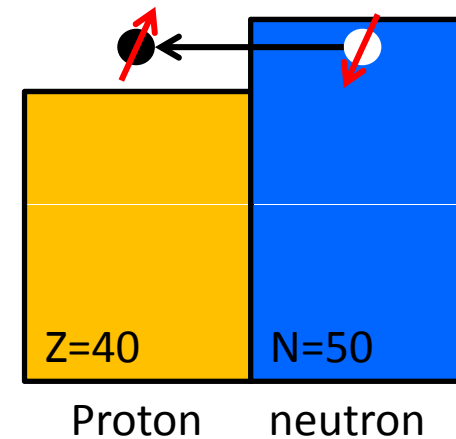
$^{12}\text{Be}$

$$\frac{N-Z}{A} = \underline{0.33}$$



$^{90}\text{Zr}$

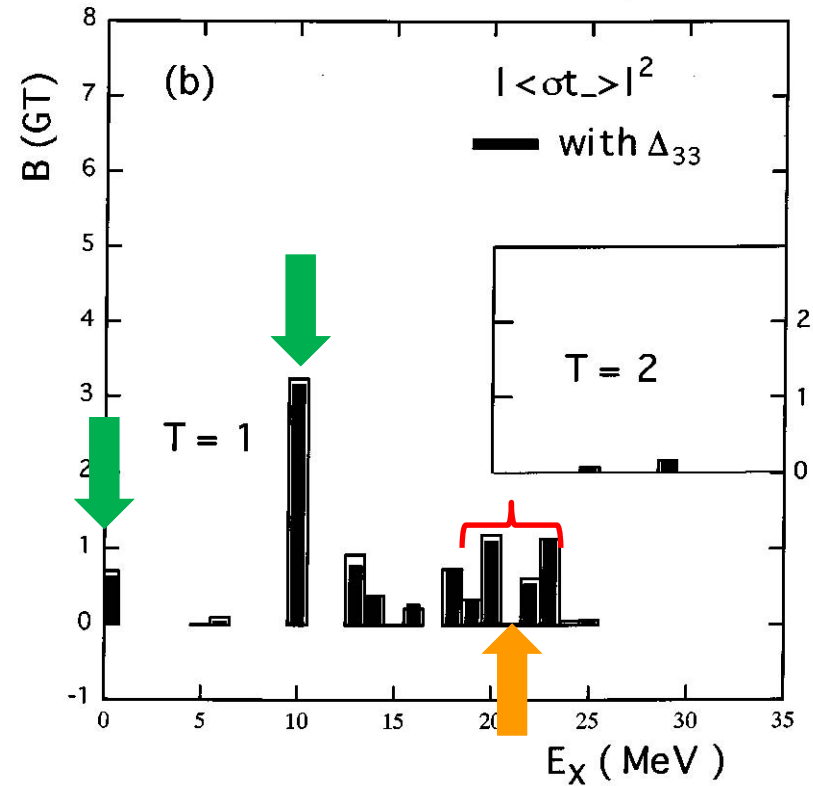
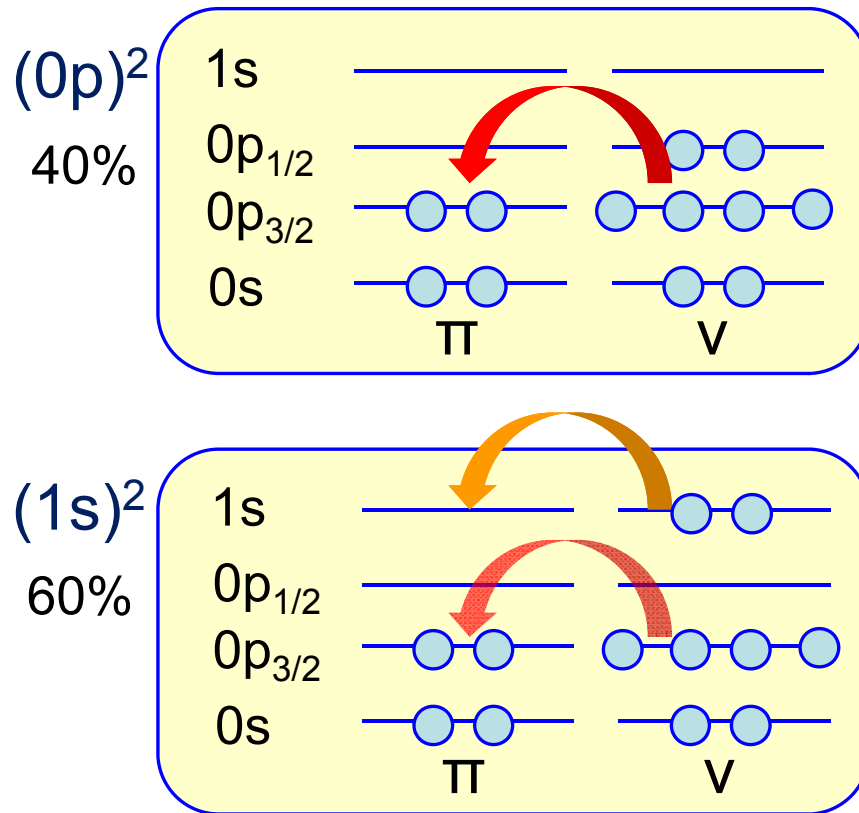
$$\frac{N-Z}{A} = 0.11$$



# Shell-model prediction: GT excitations

Suzuki & Otsuka, PRC56(1997)847

- Model space: p-sd
- $\Delta\varepsilon_{1s} = -3.4$  MeV
- logft value is reproduced.

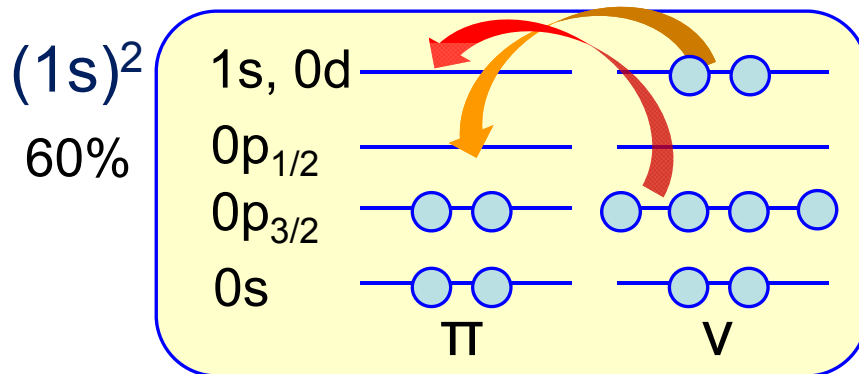
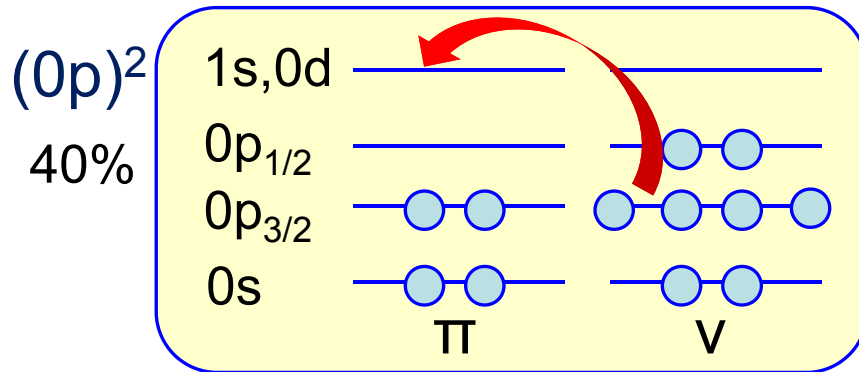


...Deformation-difference?  
...Cluster model?

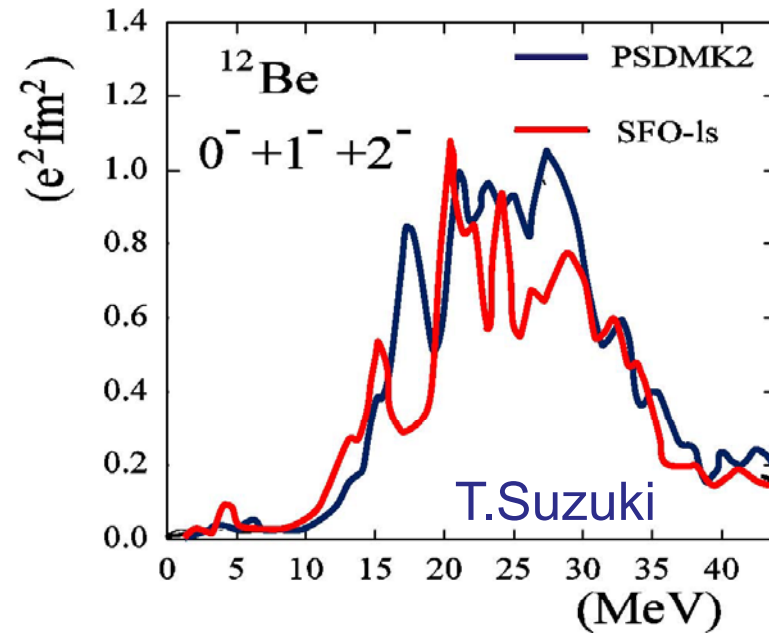


# SD excitations

- Spin dipole ...  $\Delta L = 1, 1\hbar\omega$   
change in L  $\rightarrow$  qualitative change in strength distribution



- Degeneracy between p- and sd- shell can be seen?
- SD excitations in low  $E_x$  region?

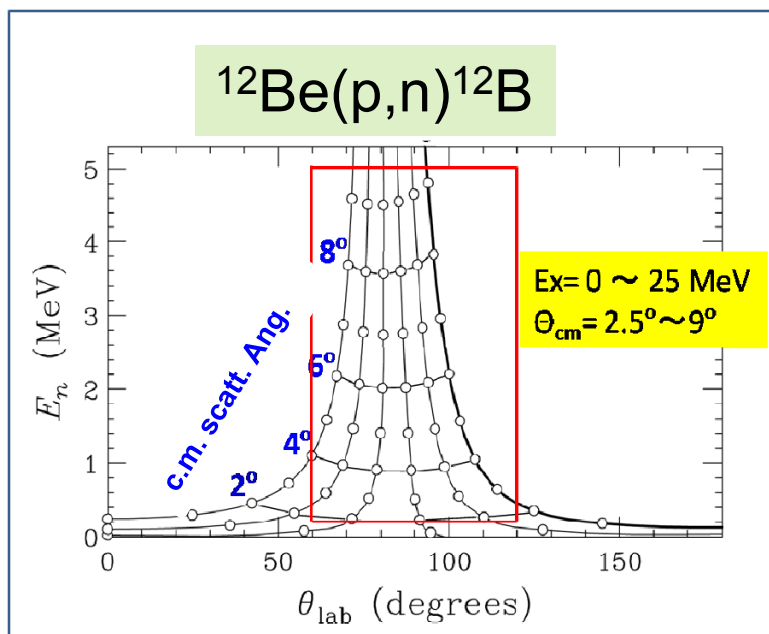
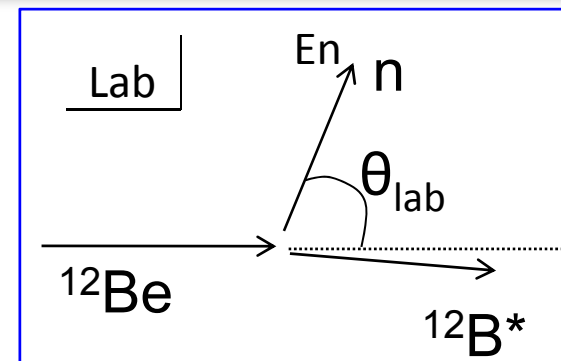


# $^{12}\text{Be}(p,n)^{12}\text{B}$ measurement

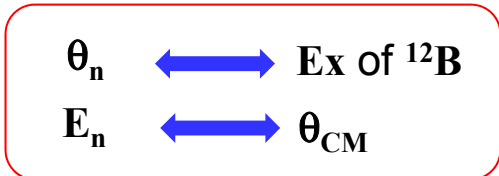
## Exothermic reaction in inverse kinematics!

$Q_{gs} = +11 \text{ MeV}$

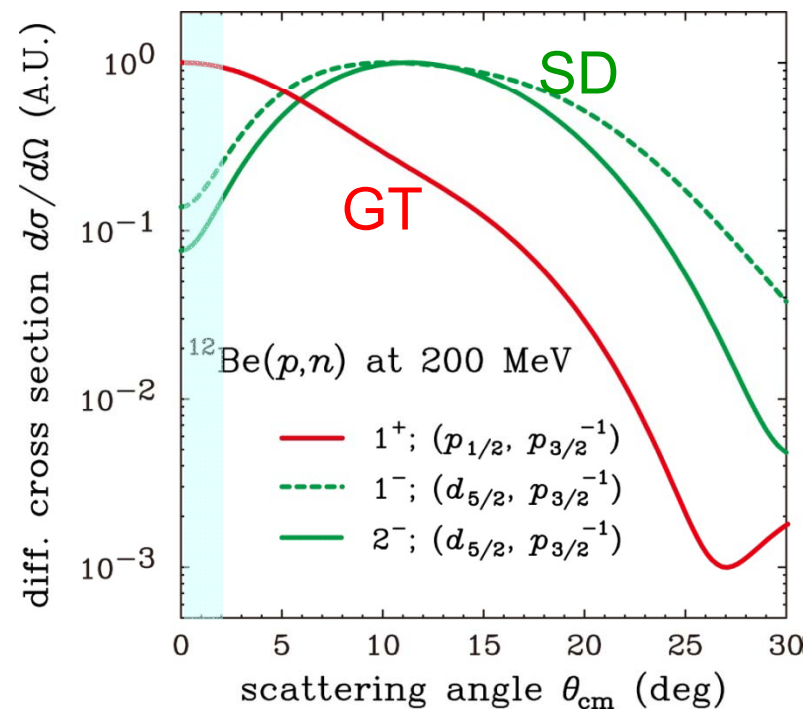
- resolution  $\delta E_x \sim 1 \text{ MeV}$ ,  $\delta \theta_{cm} \sim 1 \text{ deg}$
  - missing mass :  $(E_n, \theta_{lab}) \rightarrow (E_x, \theta_{cm})$
- $E_n$  ... Time-of-flight



$\delta E_n \sim 0.8 \text{ MeV}$ ,  $\delta \theta_{lab} \sim 1.3 \text{ deg}$

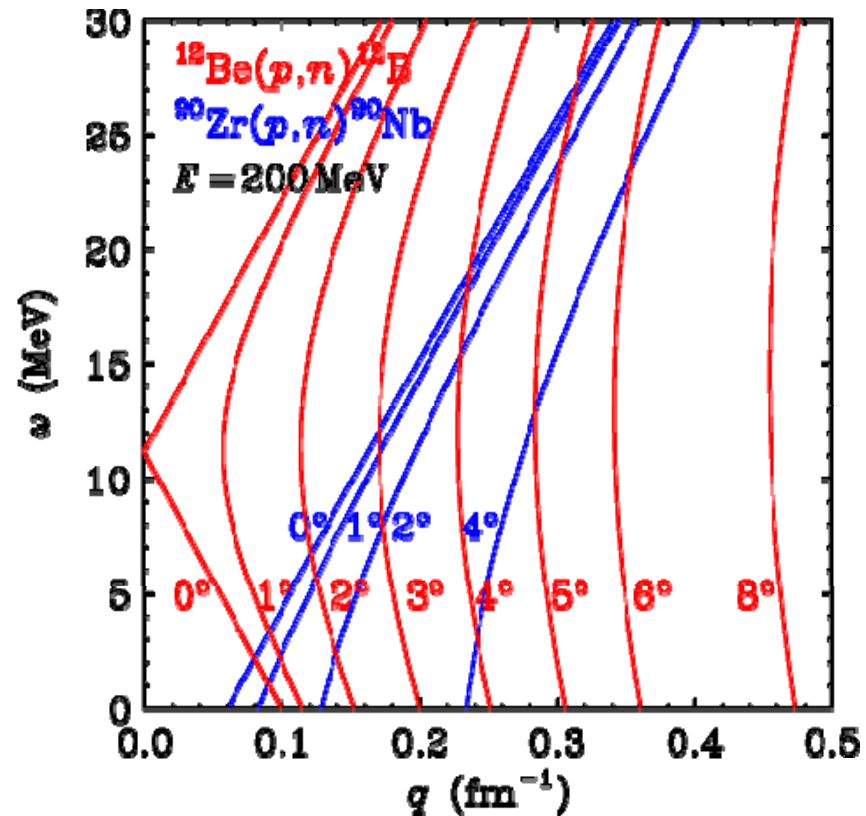


## Angular distribution



# Merit of exothermic $^{12}\text{Be}(p,n)^{12}\text{B}$ reaction

$^{12}\text{Be}(p,n)^{12}\text{B}$  reaction :  $Q_{\text{gs}} = +11 \text{ MeV}$



- $q=0.0 \text{ fm}^{-1}$  is achieved even at  $\omega=11 \text{ MeV}$ !
- $q=0.2 \text{ fm}^{-1}$  is achieved even at 3 degrees.

# Sketch of experiment

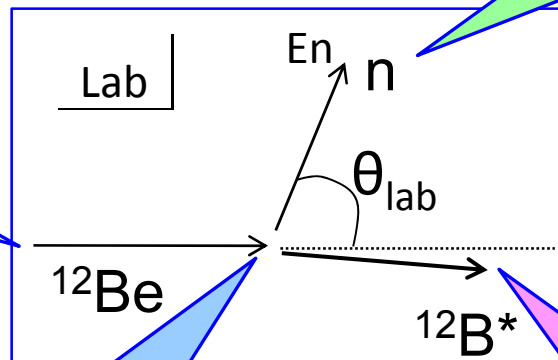
- (p,n) reaction in Inverse kinematics
- Beam preparation
- Target
- Neutron(TOF)
- Residual nucleus(SHARAQ)

Neutron detector  
TOF method



WINDS

$^{18}\text{O}$  beam + Be  
Achromatic transport



Liquid hydrogen target

SHARAQ  
 $^{12}\text{B}$ ,  $^{11}\text{B}$ ,  $^{10}\text{B}$



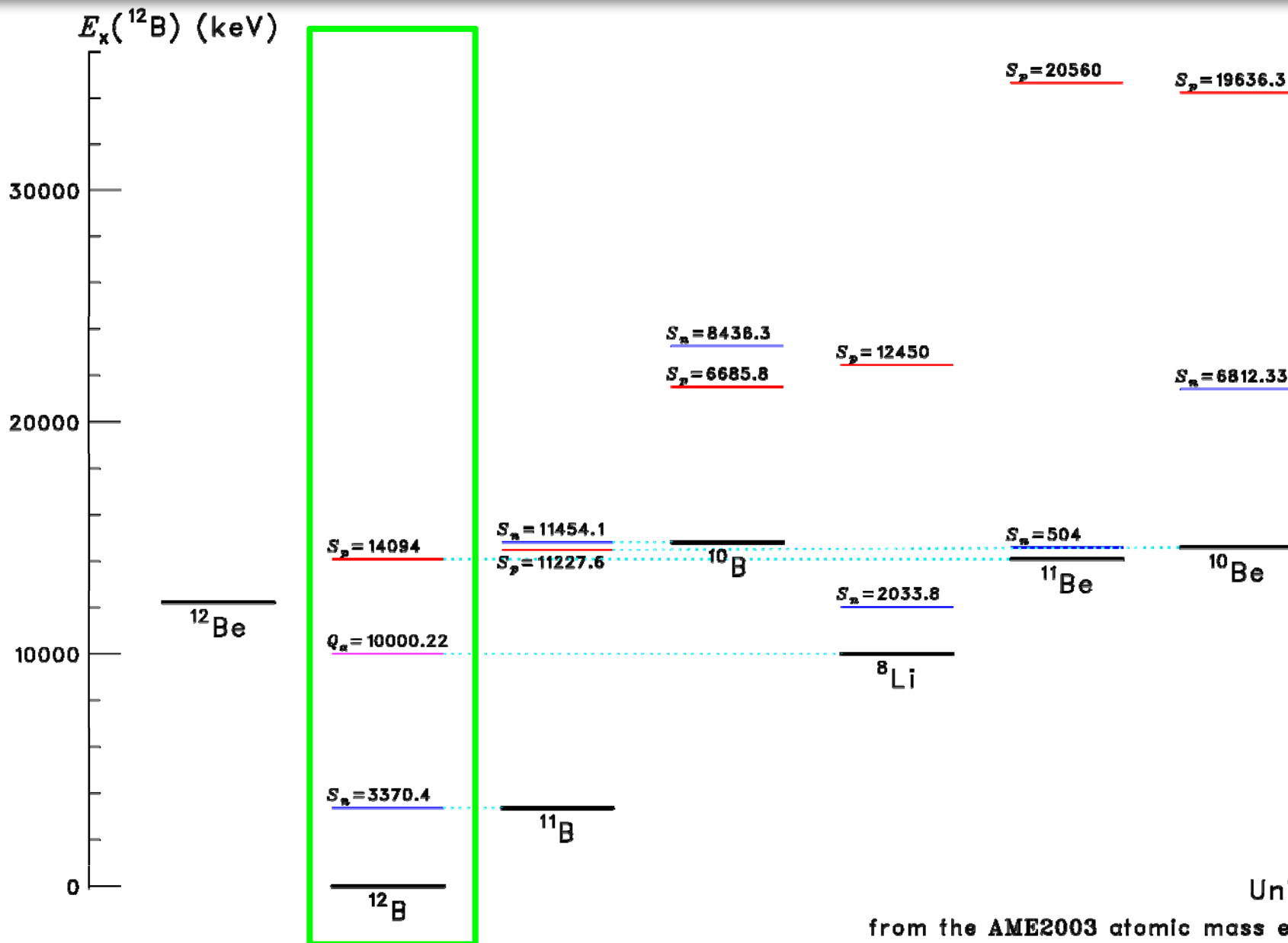
LHe

- Acceptances  
 $|\delta| < 1\%$   
 $|\theta| < 36 \text{ mr}$ ,  $|\Phi| < 68 \text{ mr}$



SHARAQ

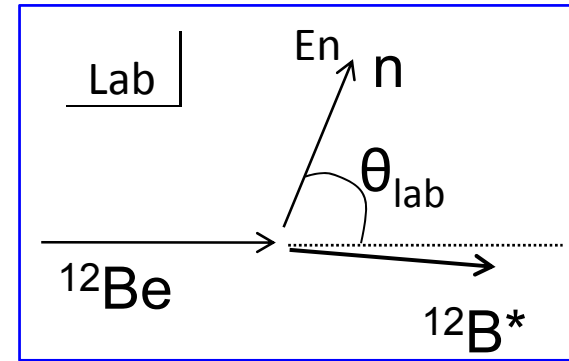
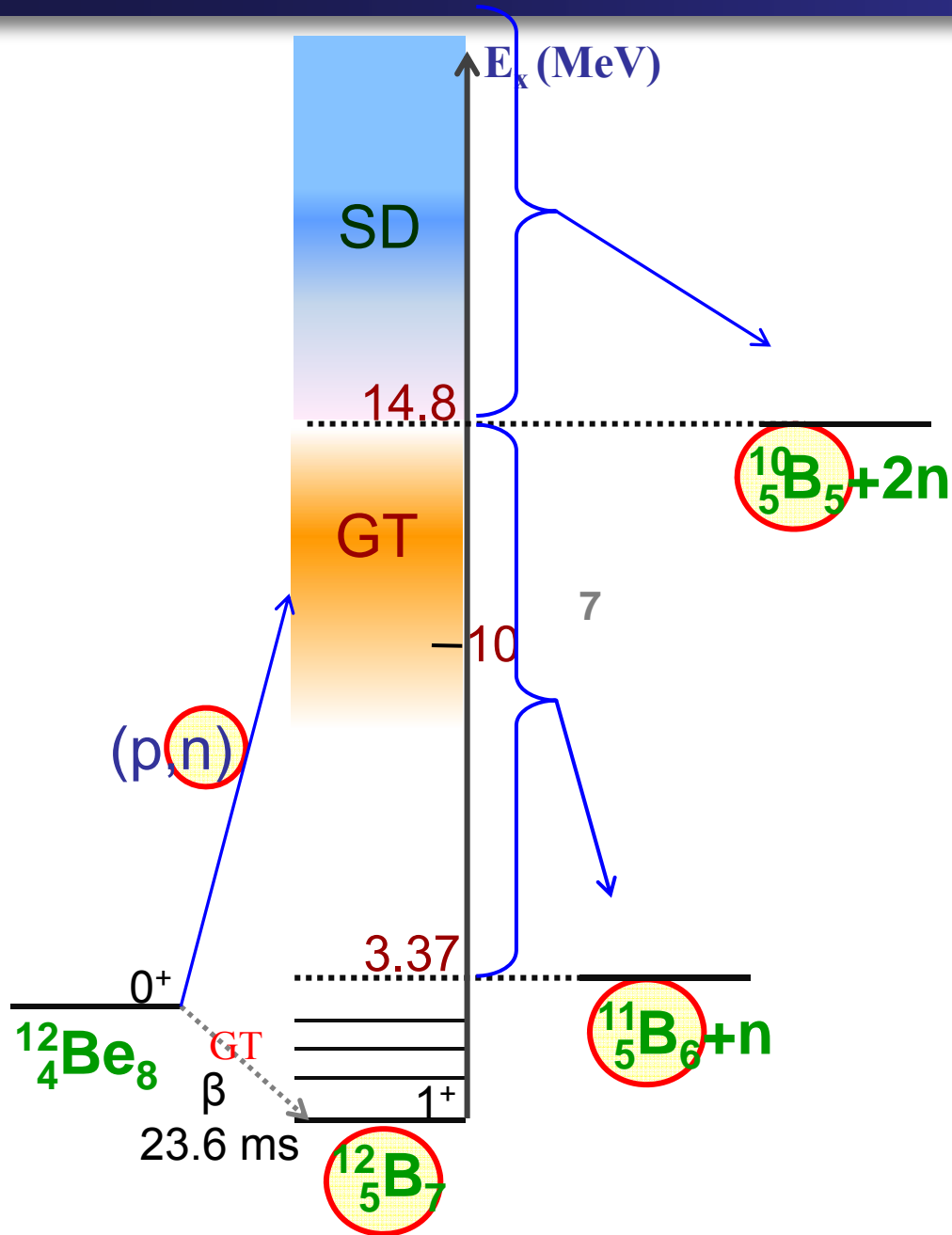
# Masses around $^{12}\text{Be}$



Units: keV

from the AME2003 atomic mass evaluation  
<http://www.nndc.bnl.gov/masses/rct2.mas03>

# Coincidence measurement



Neutron and residual particle coincidence meas.

### 3 settings of SHARAQ

- ◆  $0 < E_x < 3.4 \text{ MeV}$   
→  $^{12}\text{B}$  &  $n$
- ◆  $3.4 < E_x < 15 \text{ MeV}$   
→  $^{11}\text{B}$  &  $n$
- ◆  $15 < E_x < 22 \text{ MeV}$   
→  $^{10}\text{B}$  &  $n$

→ improves S/N

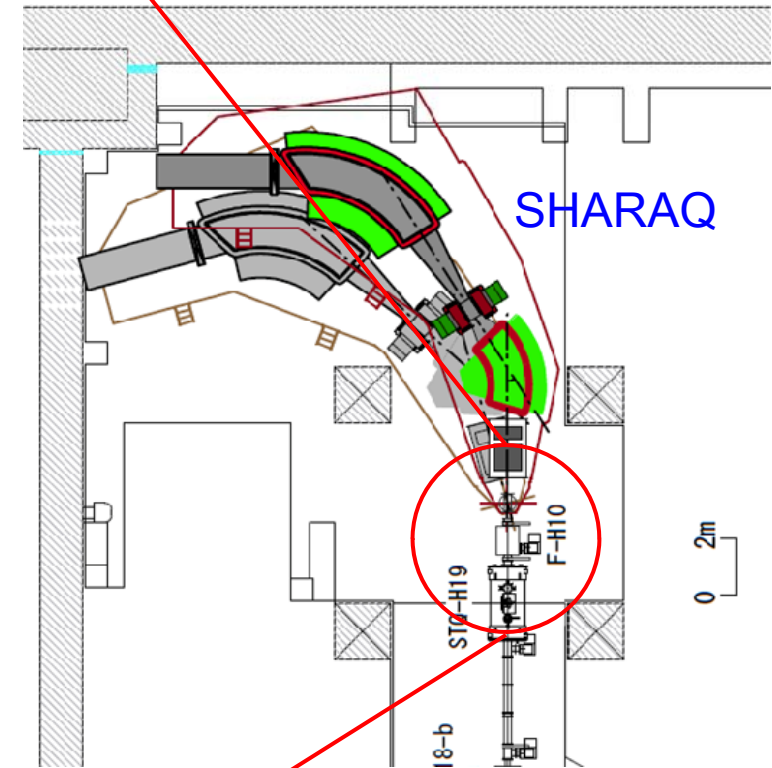
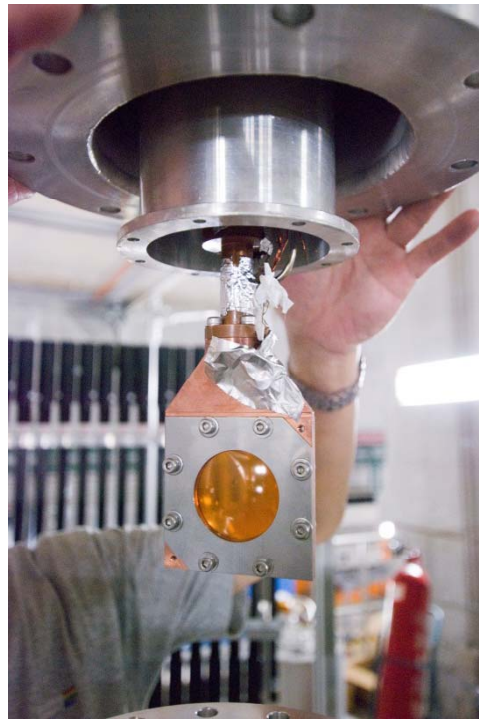
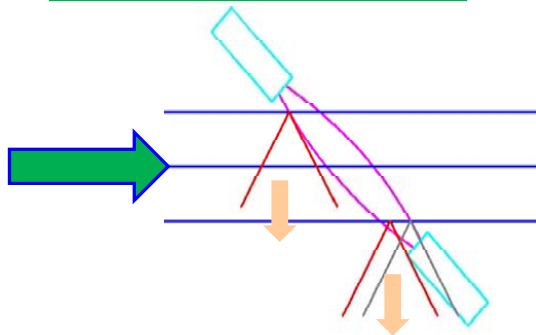
# Liquid Hydrogen target

- LH<sub>2</sub> target
  - 14 mm<sup>t</sup>
  - 40 mmΦ
  - Kapton window 25 μm

Beam size:

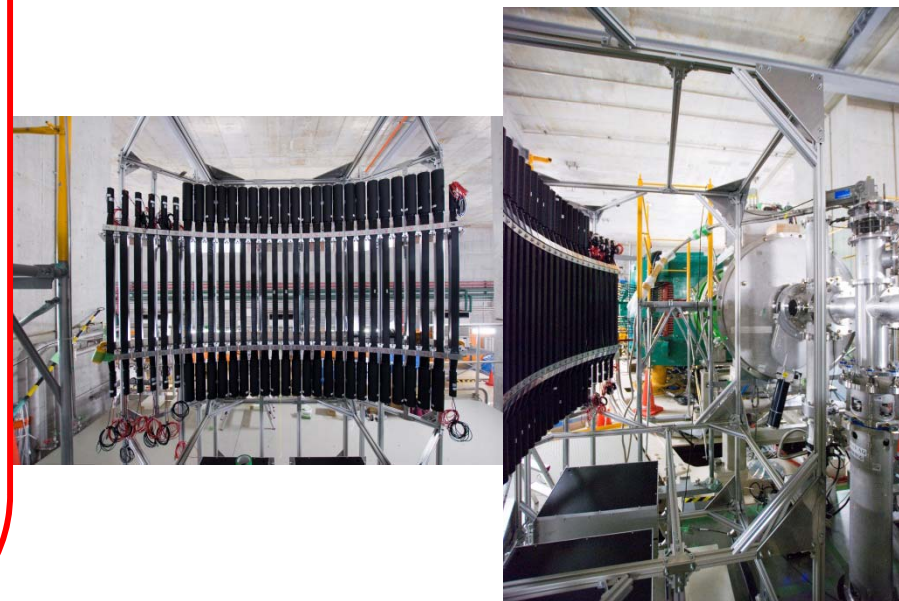
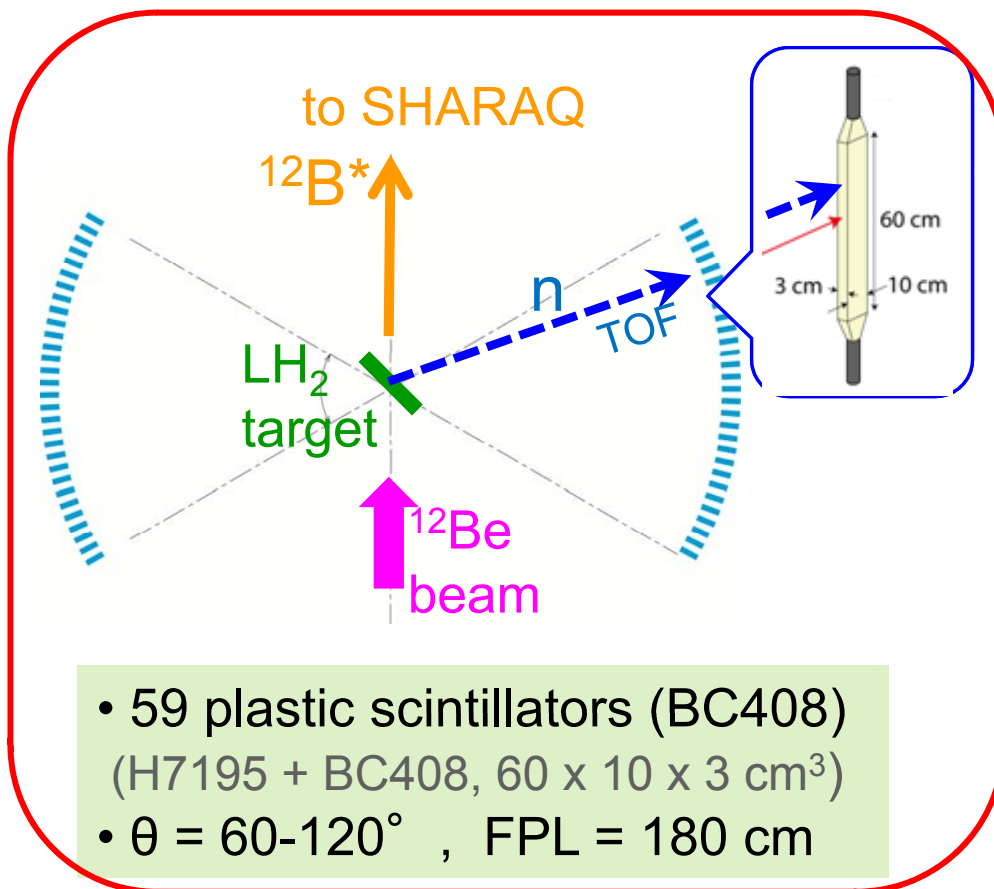
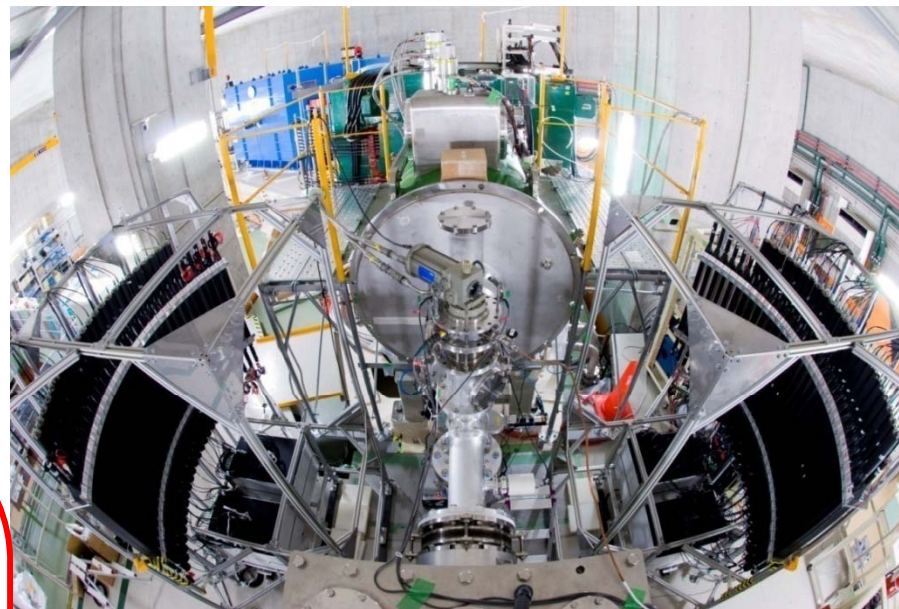
$$\Delta x = 7 \text{ mm (in } \sigma)$$

$$\Delta y = 5 \text{ mm}$$



# WINDS (neutron counter array)

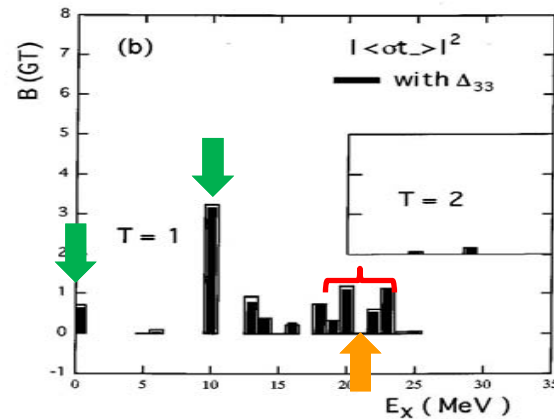
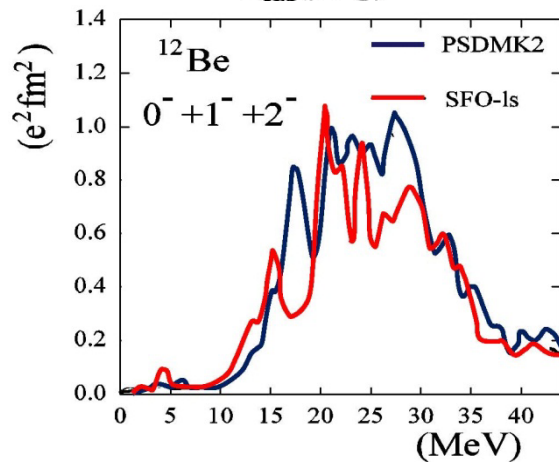
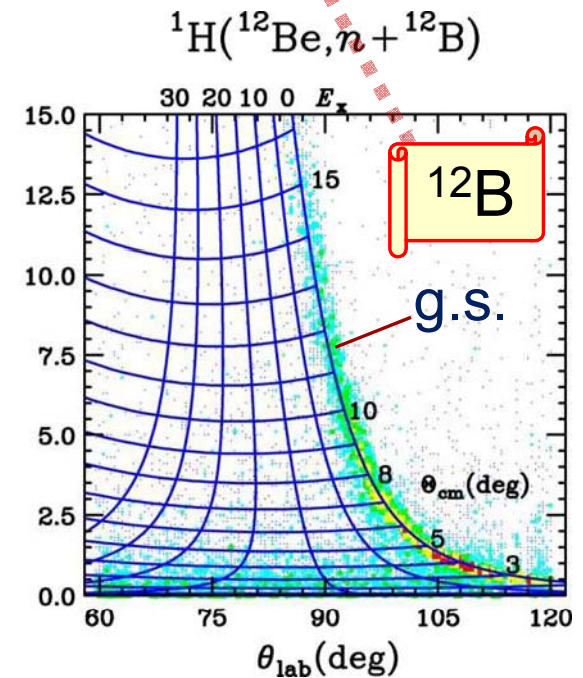
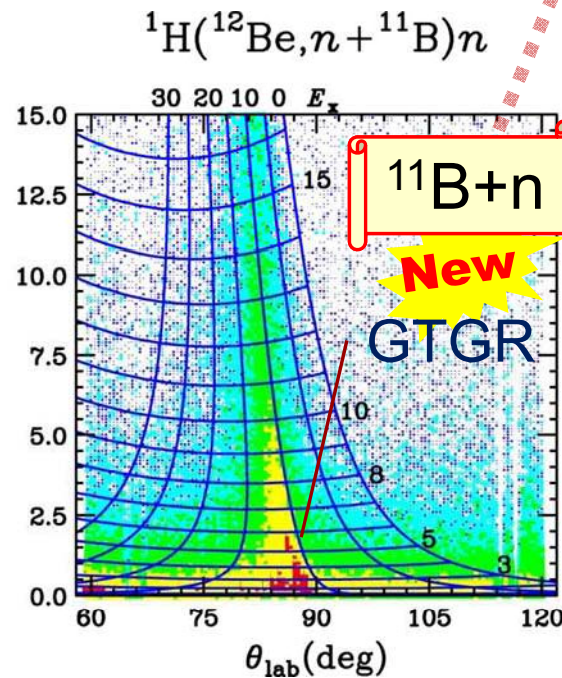
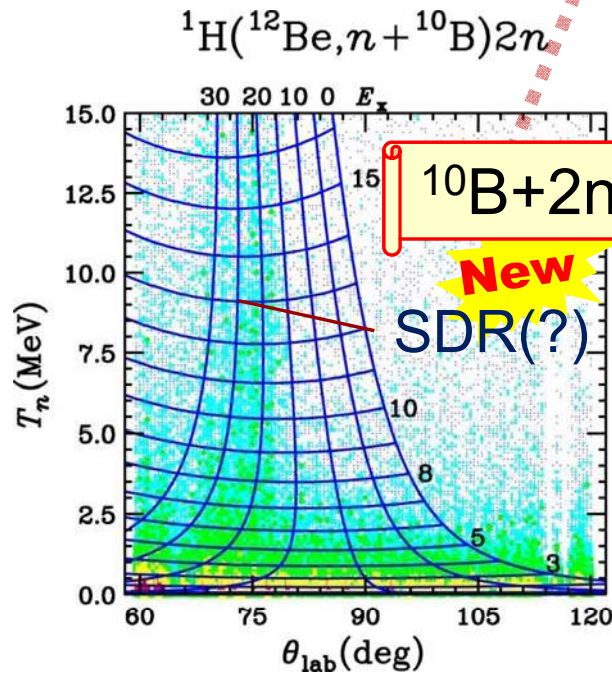
**Wide-angle**  
**Inverse-kinematics**  
**Neutron**  
**Detectors for**  
**SHARAQ**





- **Experiment : 6-12 June, 2011**
- **Primary beam:  $^{18}\text{O}$  250A MeV, 100-200 pnA**
  - $\frac{1}{4}$  -freq. buncher ... pulse separation of 122 ns
- **Primary target: Be, 20 mm<sup>t</sup>**
- **Secondary beam:  $^{12}\text{Be}$  200A MeV, 500 kcps on target**
  - contains few % isomer in  $^{12}\text{Be}$
- **Secondary target: Liq H<sub>2</sub>, 14 mm<sup>t</sup>**

# Result



First results on **GTGR** & **SDR** full distributions in  $^{12}\text{B}$  with unstable  $^{12}\text{Be}$  beam.

## 1 reliability of extracting the spin-isospin responses in the **continuum**

- **Unit cross section, proportionality, MDA(shallow binding)**
- **Interferences:  $L=0$  vs.  $L=2$  and GT vs. IVSM**

## 2 composite projectiles

- **( $t, {}^3\text{He}$ ) reaction: measurement by Miki**
  - **Large exchange effects**
- **( ${}^{12}\text{N}, {}^{12}\text{C}$ ) reaction: measurement by Noji**
  - **Large ambiguities by optical potentials(imaginary part)**

## 3 Brand-new: measurement of the exothermic ${}^{12}\text{Be}(p,n)$ reaction in inverse-kinematics at 200 MeV/A by Yako

- **Please stay tuned**

- **Mode interference (GT vs. IVSM )**
  - **How to disentangle?**
  - **Should compare in terms of cross sections ?**
  - **Requires structure + reaction collaboration**
  - **Provide us the predictions in terms of cross sections**
  - **Then, dilemma . . .**
  
- **Exchange effects**
  - **Please develop the reaction code which can handle the exchange**
  
- **Optical potentials**
  - **Indispensable for the quantitative analysis**
  - **Hard to carry out exp. for rare-isotopes**
  - **Please create a global OP**

**The End**

**Helps by K. Yako, K. Miki, S. Noji and M. Sasano are acknowledged.**