

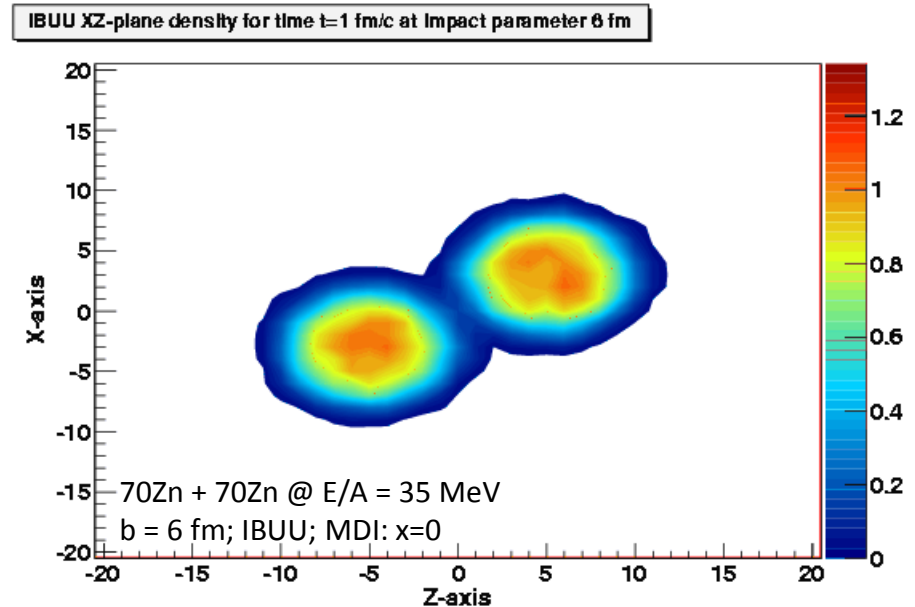
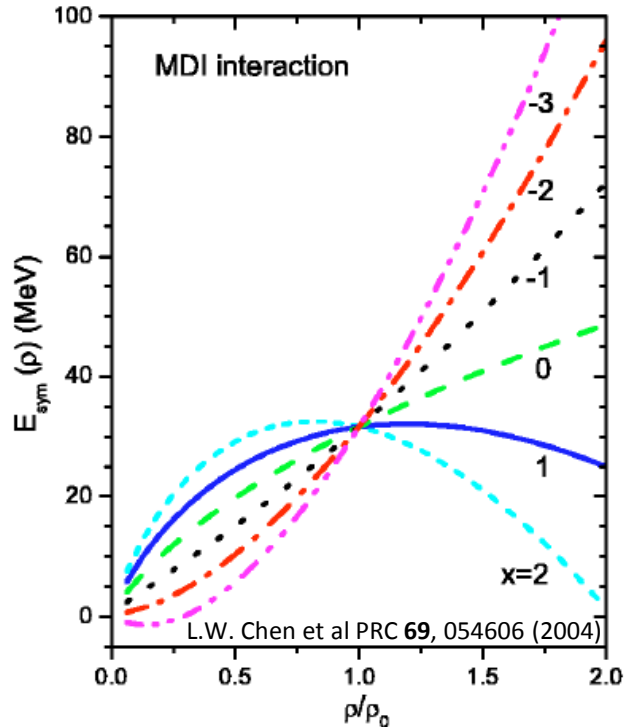
# Flow and Correlations

Recent Experimental Results on the  
Symmetry Energy and Reaction Dynamics

**Alan McIntosh**  
**Texas A&M University**

# Flow and Correlations

## Recent Experimental Results on the Symmetry Energy and Reaction Dynamics



*“Stiff” and “Soft” are relative, and have meaning within a particular model.*

- Extraction of information on  $E_{\text{sym}}(\rho)$ 
  - Experimental Data  $\leftrightarrow$  Theoretical Transport Model Calculations
- Reaction dynamics are critical
  - Mid-rapidity or neck emission
  - Emission from transiently deformed shapes.

## Directed Flow of Light Charged Particles and Intermediate-Mass Fragments

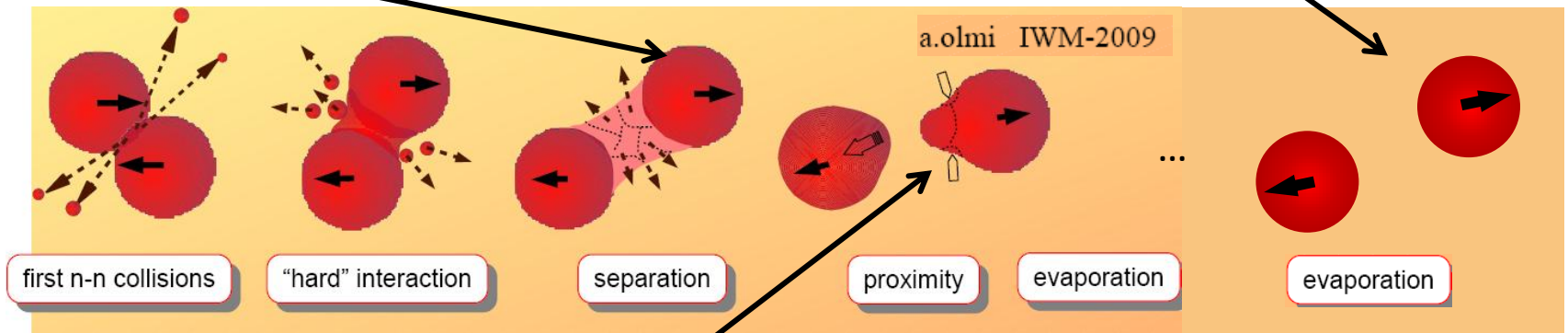
Sensitive to  $E_{\text{sym}}(\rho)$  – Model Dependent

- Dependence of Flow on Fragment N/Z
- Differential Flow ( ${}^3\text{He}:$  ${}^3\text{H}$ )
- Dependence of Flow on impact parameter

## Statistical Decay

Careful **reconstruction** of **equilibrated** source is needed. Info on  $E_{\text{sym}}(\rho)$  from:

- Caloric Curves (asymmetry, coulomb)
- Isoscaling



## Correlations Between Observables for Dynamically Produced Fragments

→ May provide useful new constrains for models

- Alignment
- Fragment Size
- Fragment Composition
- Yield
- Velocity Damping
- Breakup Timescale

# Experimental Descriptions

$^{70}\text{Zn} + ^{70}\text{Zn}$ ,  $^{64}\text{Zn} + ^{64}\text{Zn}$ ,  $^{64}\text{Ni} + ^{64}\text{Ni}$

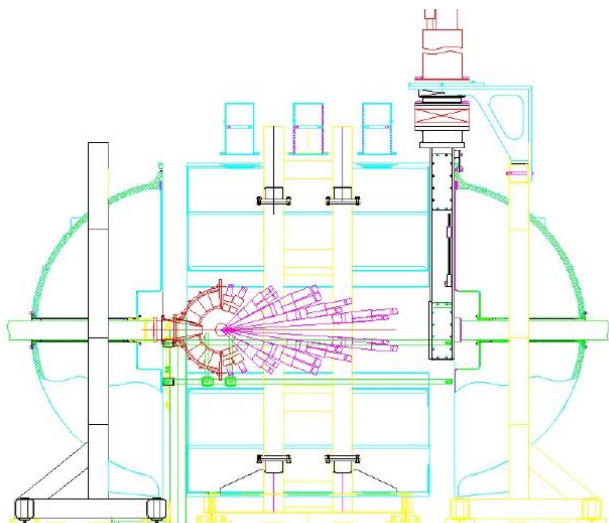
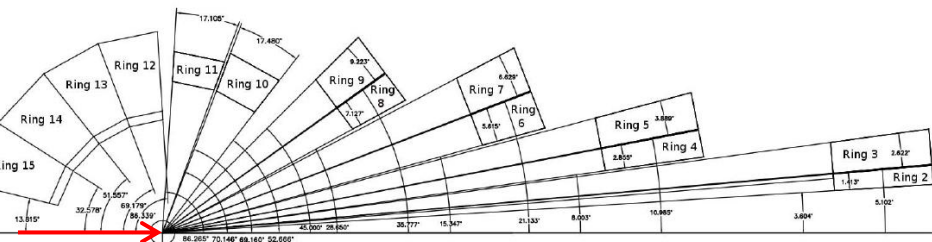
@  $E/A = 35$  MeV

$^{124,136}\text{Xe} + ^{112,124}\text{Sn}$

@  $E/A = 50$  MeV

## TAMU NIMROD-ISiS Array

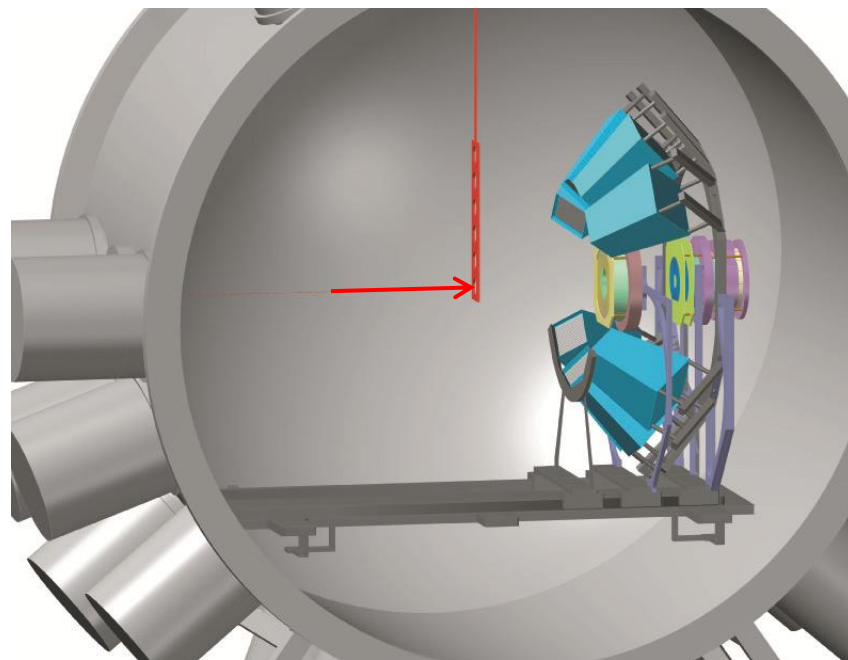
- Nearly  $4\pi$  coverage
- Isotopic Resolution for  $Z \leq 17$
- Free Neutron Multiplicity



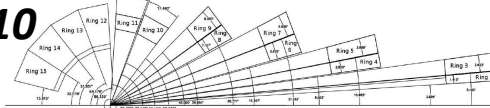
S. Wuenschel *et al.*, NIMA **604**, 578 (2009).

## Indiana University FIRST-LASSA Array

- Selection of  $2.8^\circ \leq \theta_{\text{lab}} \leq 6.6^\circ$  (for this analysis)
- High Angular Resolution ( $0.1^\circ$ )
- Isotopic Resolution for  $Z \leq 14$



T. Paduszynski *et al.*, NIMA **547**, 464 (2005)



## Directed Flow of Light Charged Particles and Intermediate-Mass Fragments

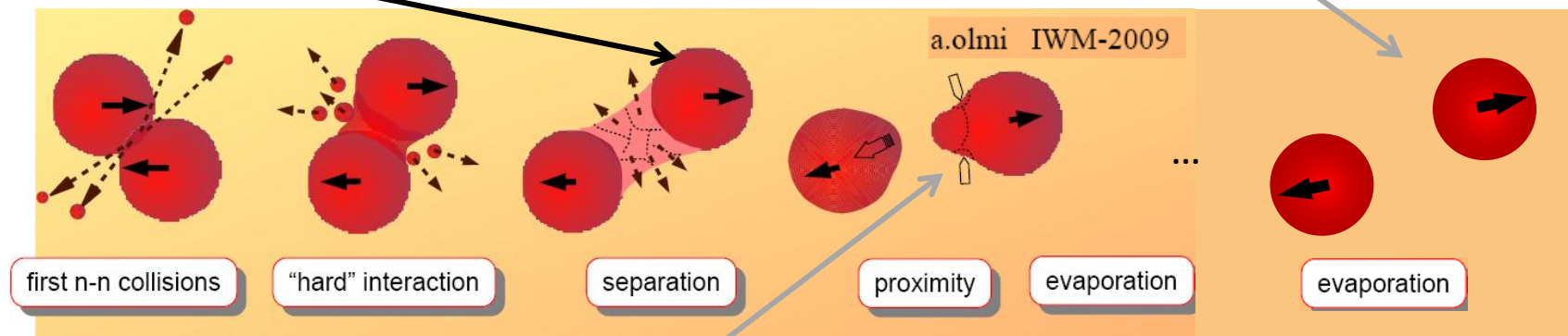
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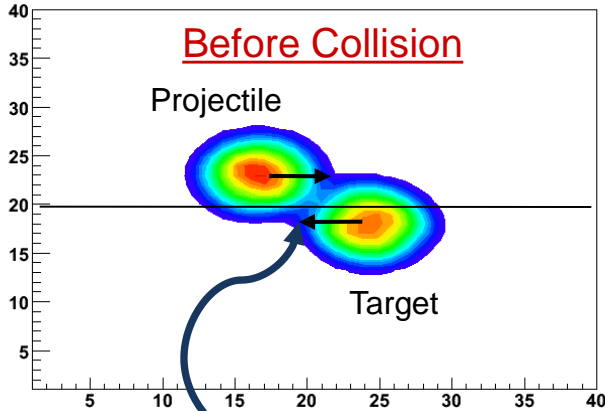
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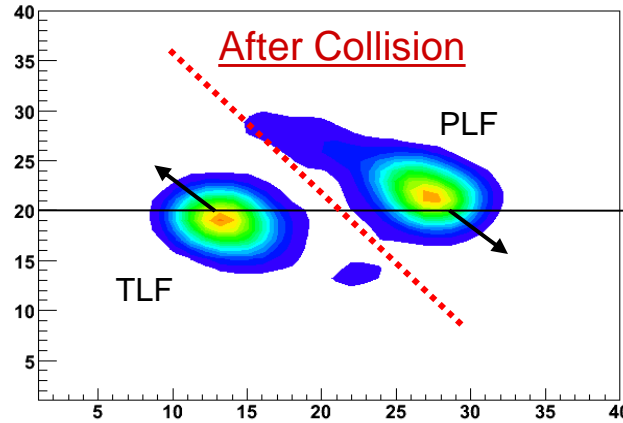
- Alignment
- Fragment Size
- Fragment Composition
- Yield
- Dissipation
- Decay Timescale

# Defining Transverse Flow

Reaction Time: 20 fm/c



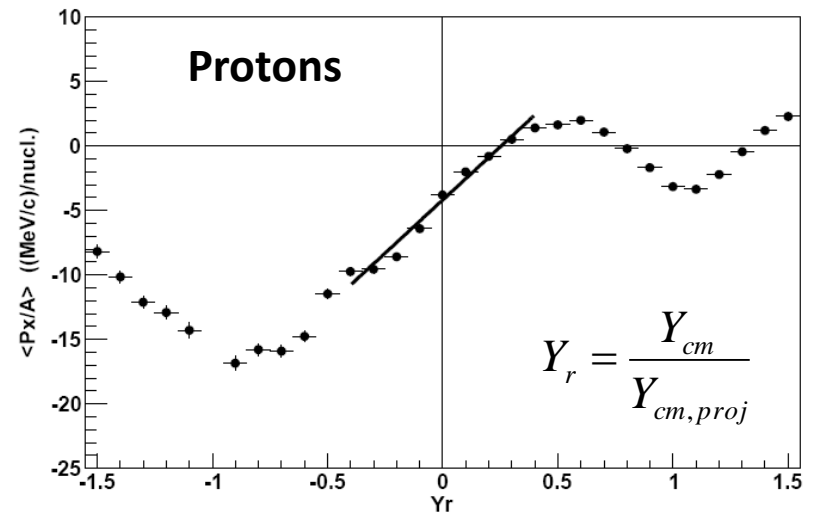
Reaction Time: 140 fm/c



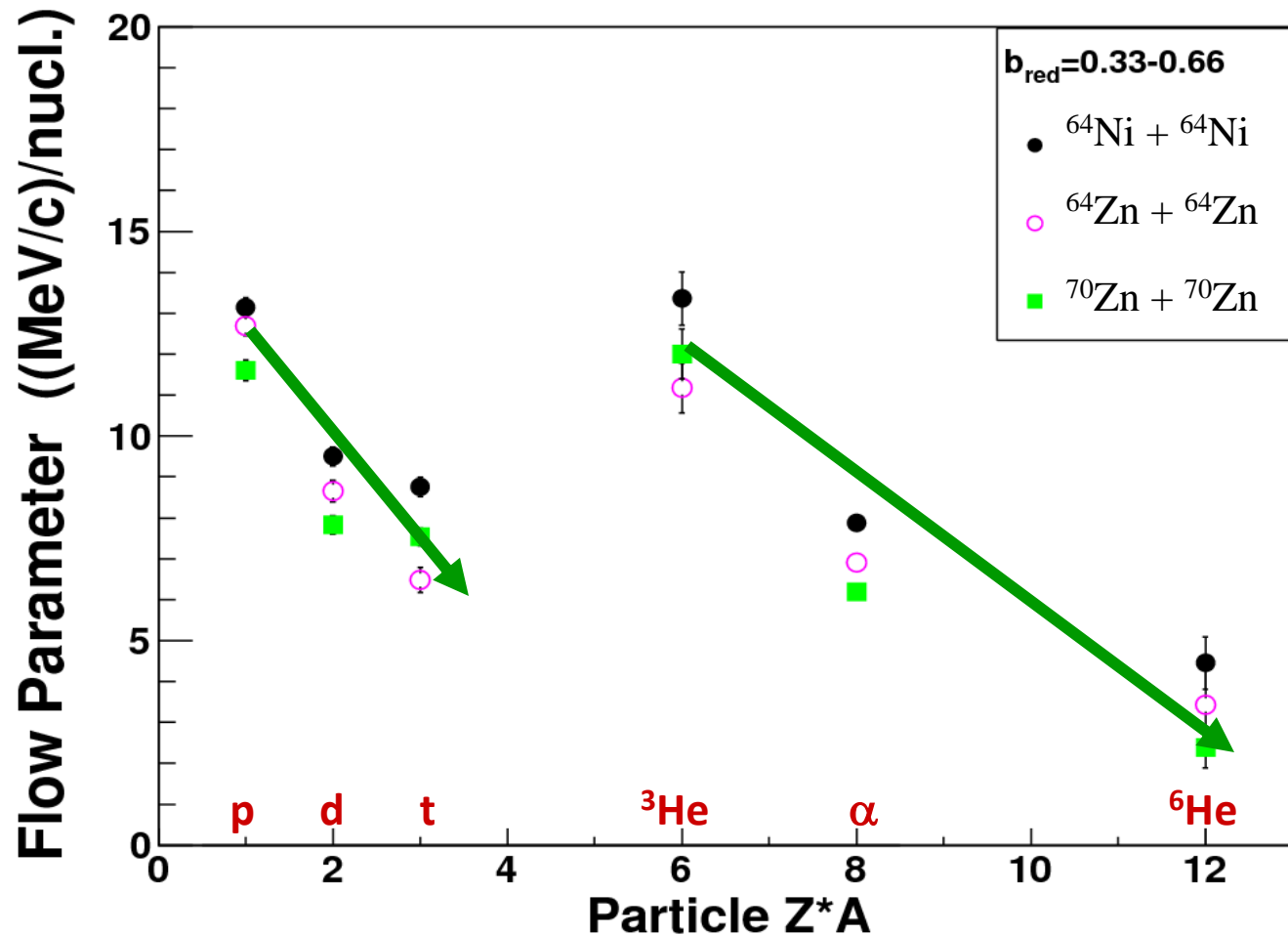
$$F = \frac{\partial \langle P_x / A \rangle}{\partial Y_r}$$

Attractive Mean Field  
- Isospin-dependent part

Repulsive NN-collisions  
Repulsive Coulomb



# Flow of Light Charge Particles

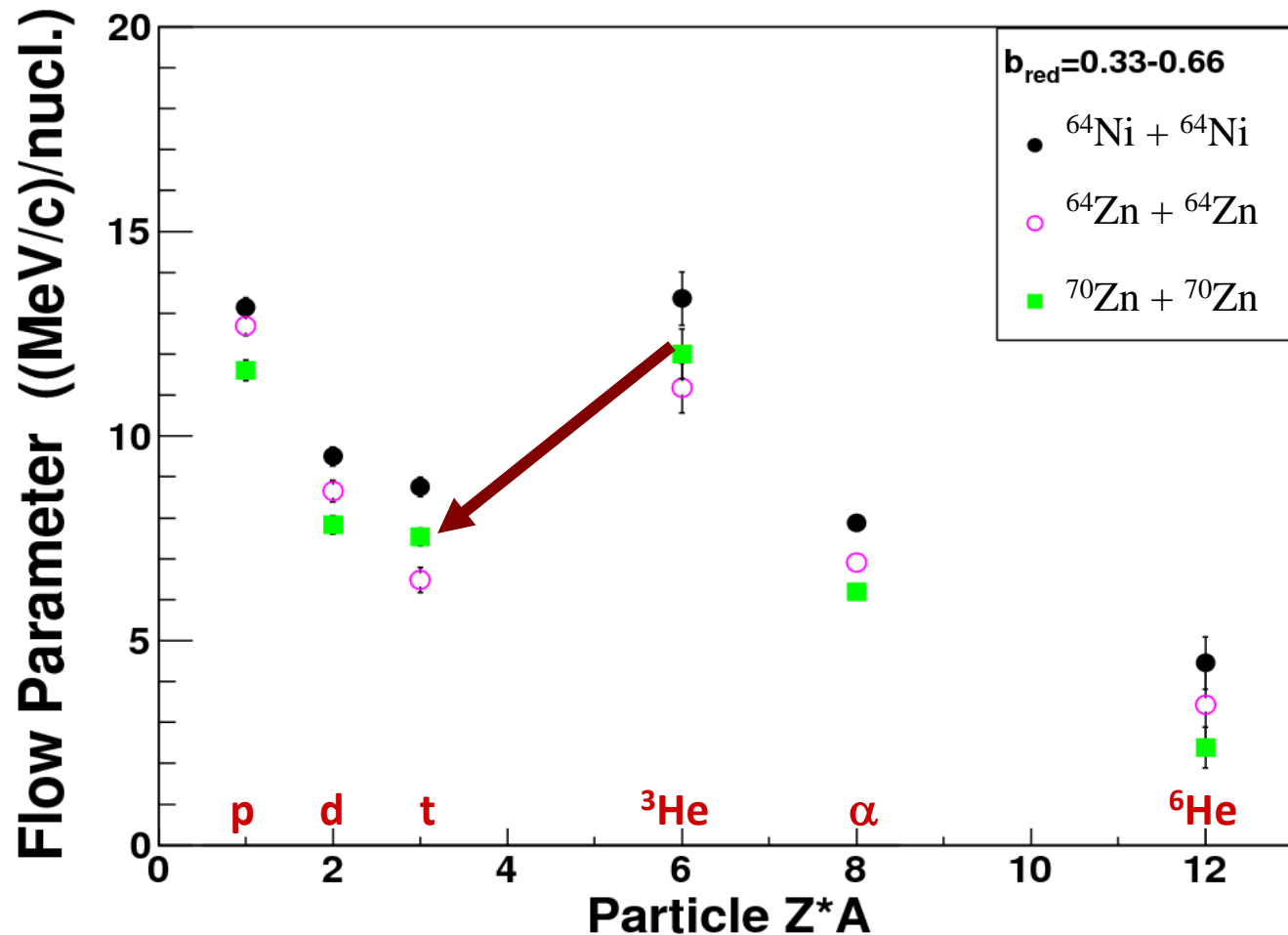


## Experimental Details

- TAMU Cyclotron Institute
- NIMROD-ISiS Detector
- 35 MeV/u (Fermi Energy)

- Strong Isotopic Trends
- $\downarrow$  Flow with  $\uparrow$  n-rich

# Flow of Light Charge Particles



## Experimental Details

- TAMU Cyclotron Institute
- NIMROD-ISiS Detector
- 35 MeV/u (Fermi Energy)

• Strong Isotopic Trends

•  $\downarrow$  Flow with  $\uparrow$  n-rich

• Isobaric Effects ( $A=3$ )

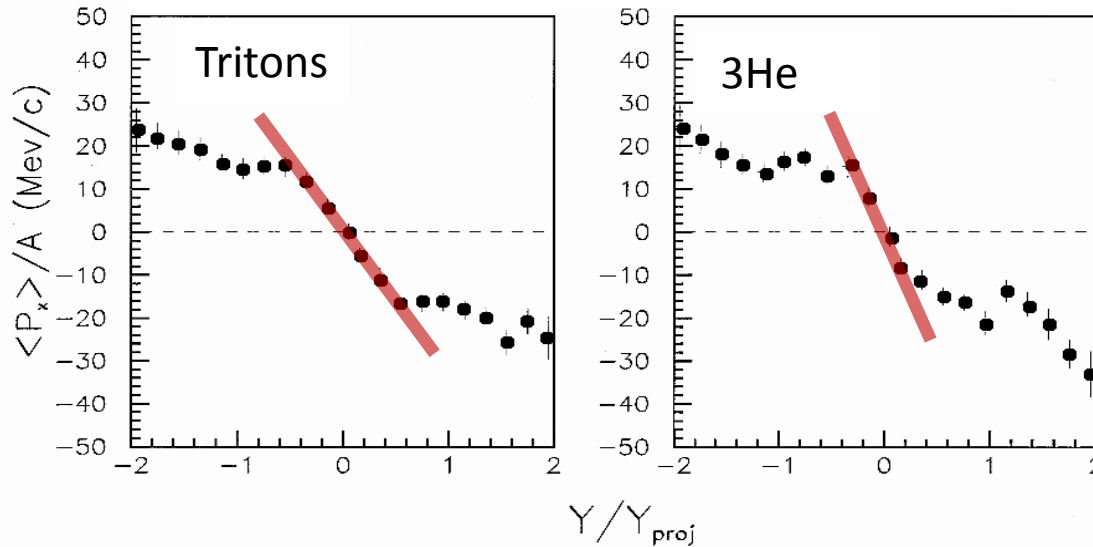
**Fragments are moving differently in HICs depending on their N/Z.  
(It's not just a mass or charge effect)**



# ${}^3\text{H}$ - ${}^3\text{He}$ Flow

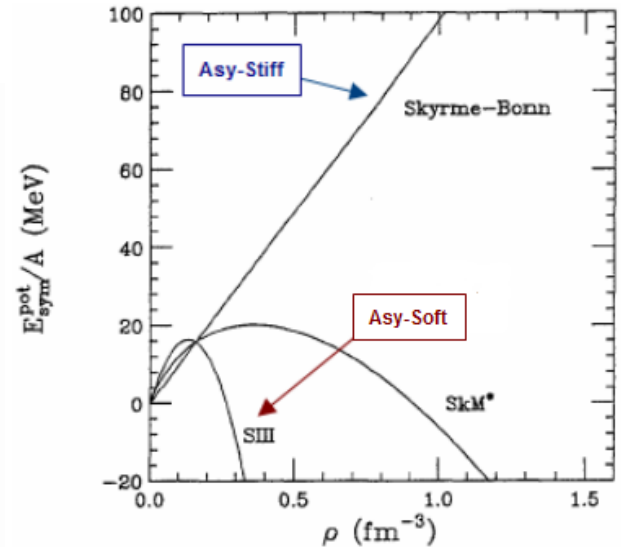
Motivation: t/ ${}^3\text{He}$  flow as surrogate for n/p flow

## BNV Simulation



M. Di Toro *et al.*, Prog. Part. Nucl. Phys. **42**, 125 (1999).

L. Scalone *et al.*, Phys. Lett. B **461**, 9 (1999).



Stiff  $E_{\text{sym}}(\rho)$      ${}^3\text{He} > {}^3\text{H}$

Soft  $E_{\text{sym}}(\rho)$      ${}^3\text{He} = {}^3\text{H}$

**Stiff symmetry potential drives neutrons into the low density neck.**

**This motion is counter to the net nucleon flow**

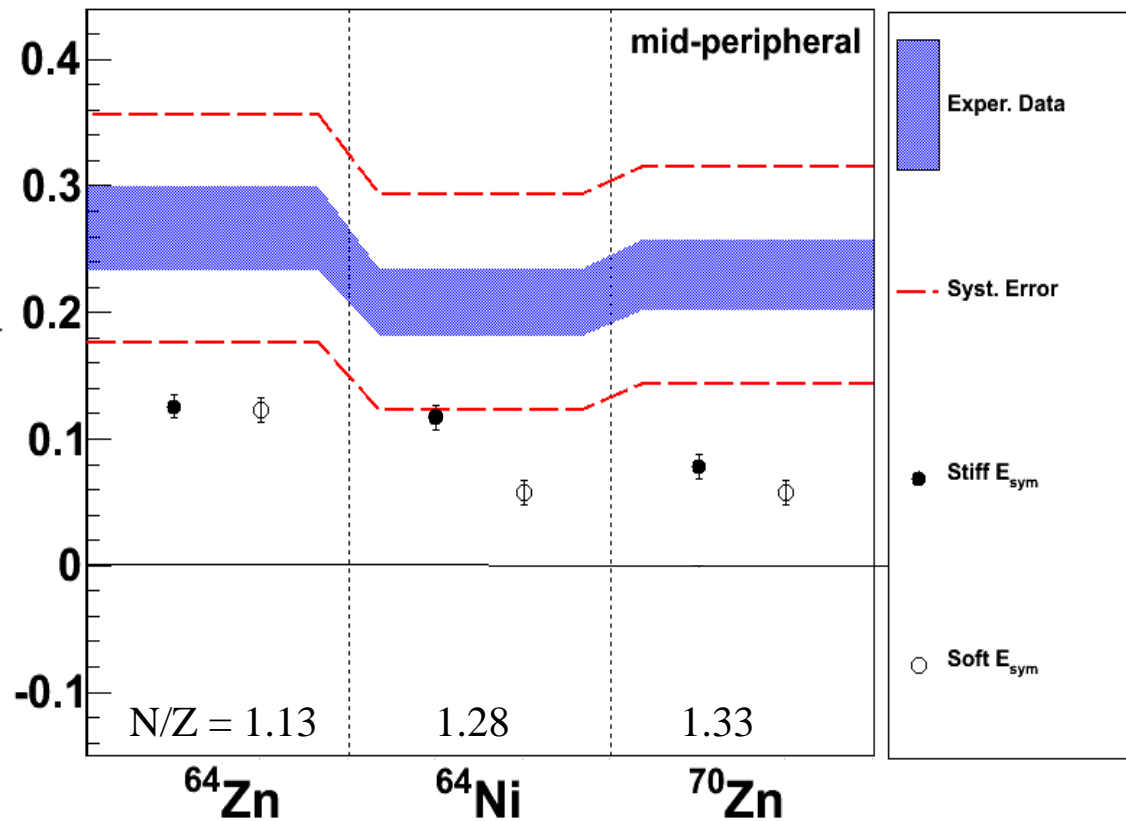
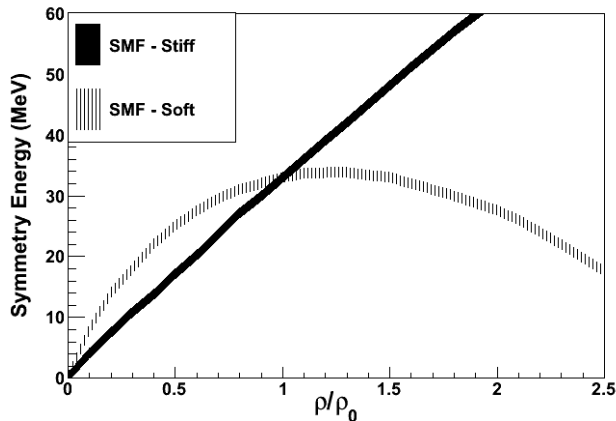
**“Stiff”  $\rightarrow$  Larger flow of  ${}^3\text{He}$  than tritons for “stiff”**

# ${}^3\text{H}$ - ${}^3\text{He}$ Flow

## Stochastic Mean-Field (SMF)

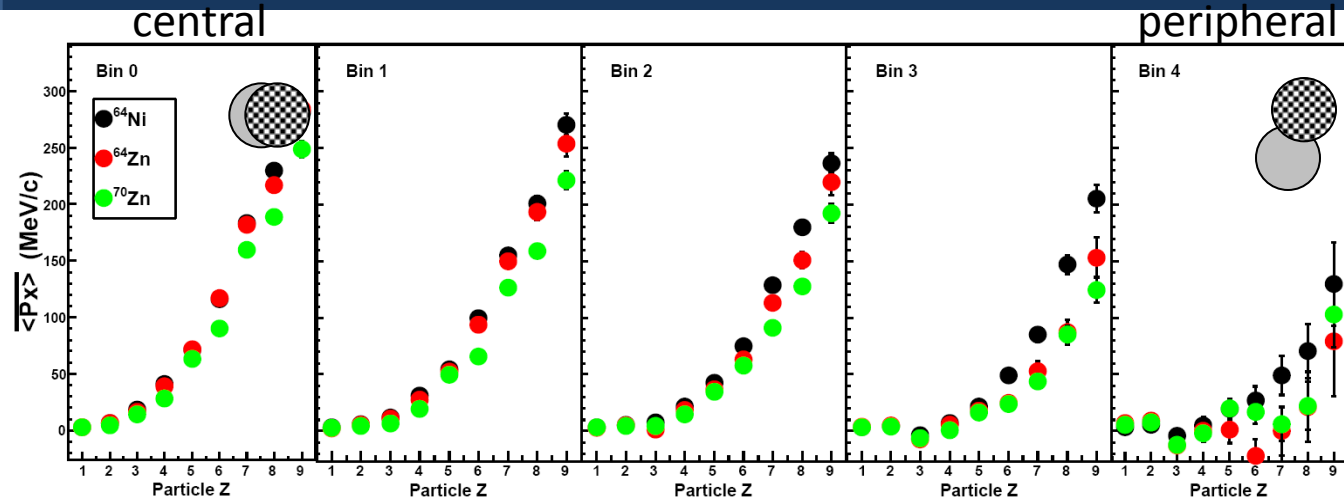
J. Rizzo *et al.* Nucl. Phys. **A806**, 79 (2008).

$$R_{{}^3\text{He}-{}^3\text{H}} = \frac{F_{{}^3\text{He}} - F_{{}^3\text{H}}}{F_{{}^3\text{He}} + F_{{}^3\text{H}}}$$



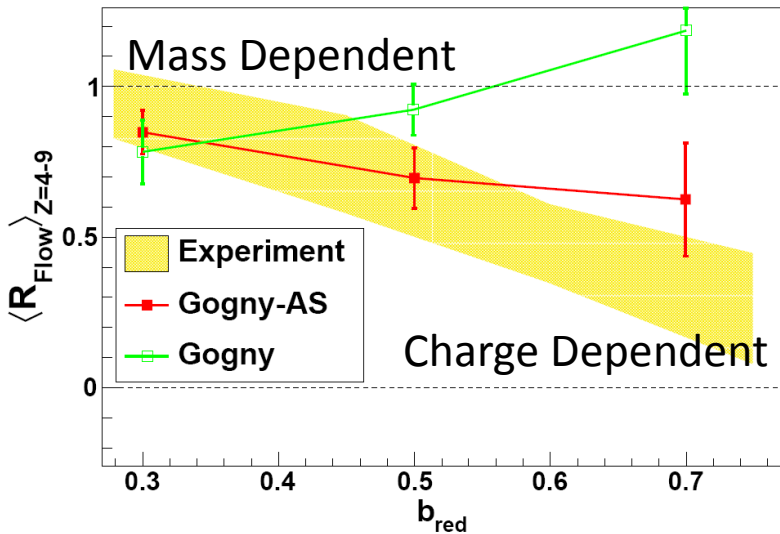
- Transverse flow is movement of particles following the PLF and TLF.
- Stiff symmetry energy propels neutrons away from the PLF and TLF into the neck, decreasing the flow for neutron-rich species.

# IMF Flow



$$R_{\text{flow}} = \frac{\langle Px \rangle_{^{64}\text{Zn}} - \langle Px \rangle_{^{70}\text{Zn}}}{\langle Px \rangle_{^{64}\text{Ni}} - \langle Px \rangle_{^{70}\text{Zn}}}$$

$$R_{\text{flow}} = \frac{\text{red} - \text{green}}{\text{black} - \text{green}}$$



## Violent Collisions

The heavier systems have more NN collisions (repulsive)

→ Lower  $E_{\text{bal}}$  and lower flow than the lighter system

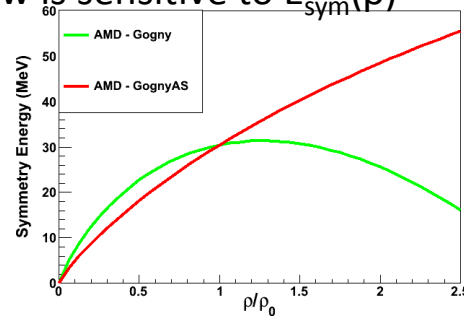
## Peripheral Collisions

Smaller interaction volume

→ Less mean-field component, but same Coulomb

Charge-dependent flow

Mean-field is isospin dependent, so the competition between mass-dependent and charge dependent flow is sensitive to  $E_{\text{sym}}(\rho)$

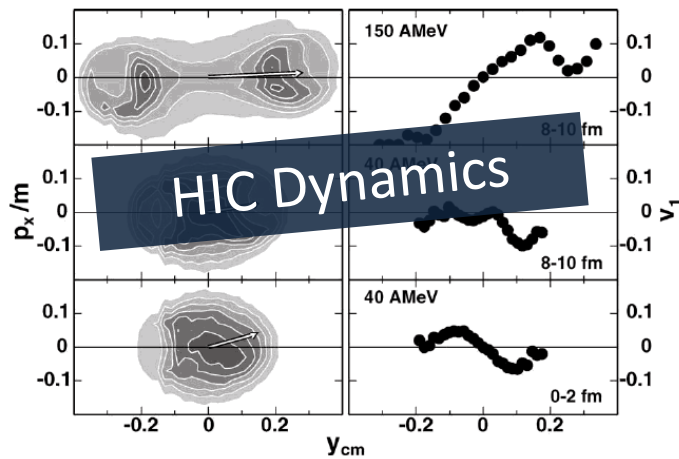


## AMD+GEMINI

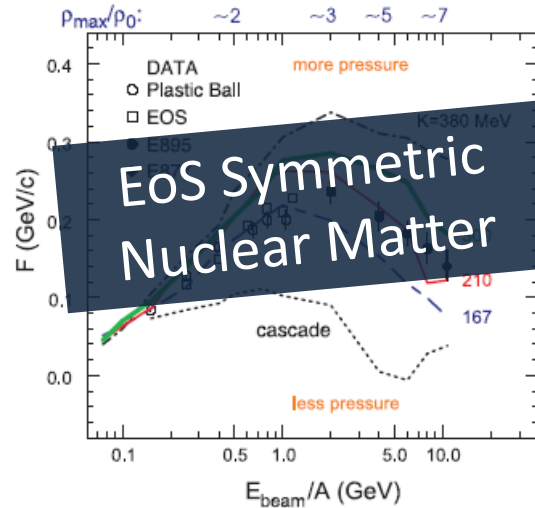
Molecular dynamics model coupled with statistical decay.

A. Ono and H. Horiuchi,  
Prog. Part. Nucl. Phys. 53,  
501, (2004).

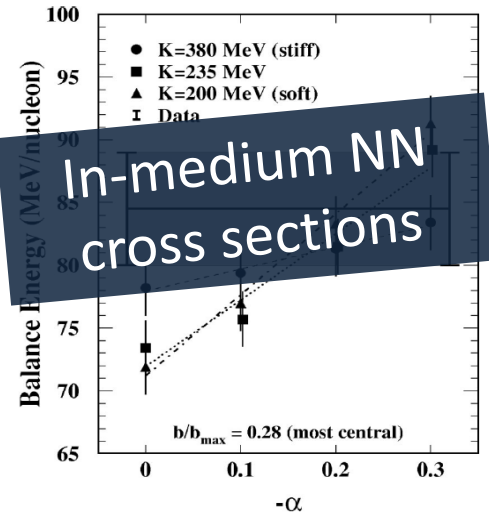
# Usefulness/Importance of Flow Measurements



J. Lukasik *et al.*, PLB (2005)



P. Danielewicz *et al.*, Science (2002)



D.J. Magestro *et al.*, (2000)

Probe of EoS for asymmetric nuclear matter.

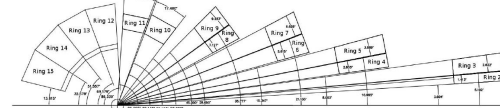
IMF flows

LCP flows (Ex. 3H-3He)

Balance energy

$\pi^+/\pi^-$  flows

N/P flows



## Directed Flow of Light Charged Particles and Intermediate-Mass Fragments

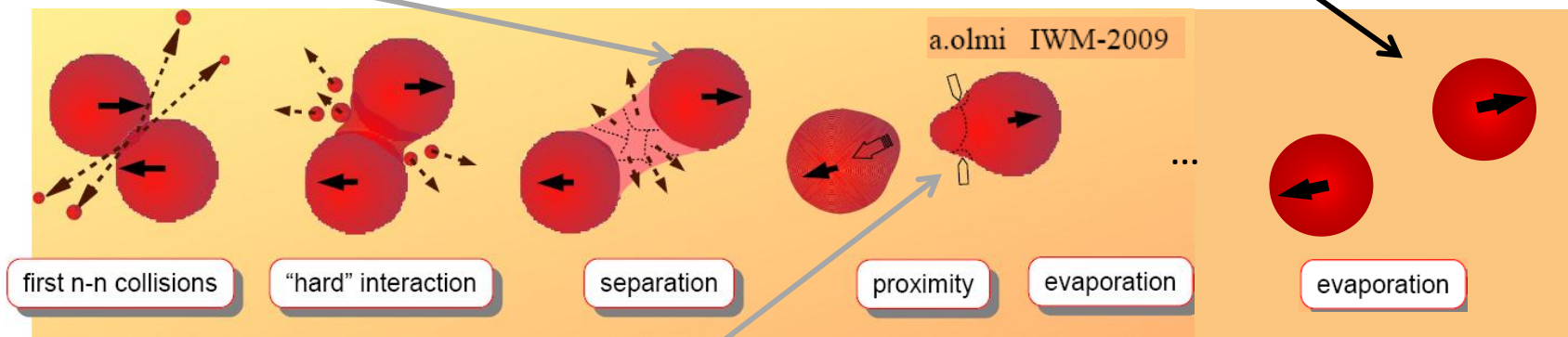
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# Source Selection

S. Wuenschel et al., PRC79, 061602 (2009)

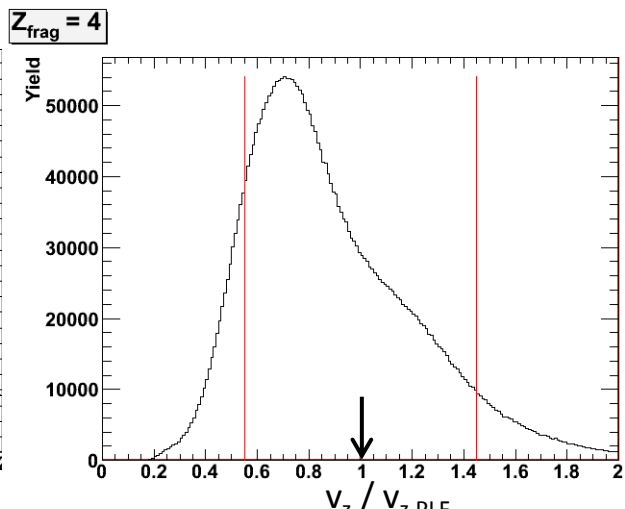
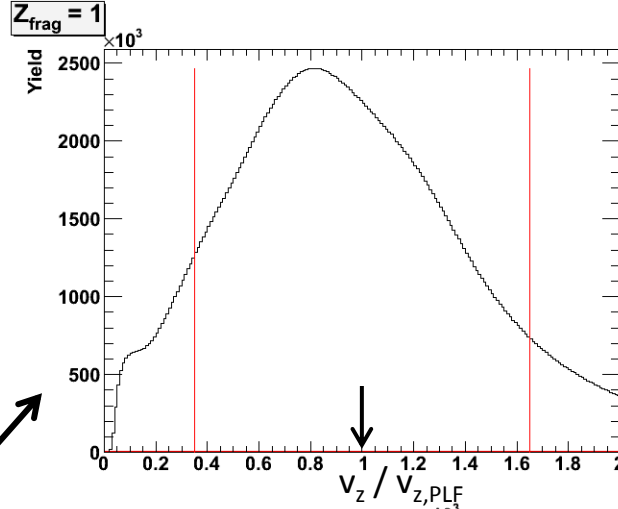
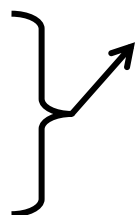
J.C. Steckmeyer et al., NPA686, 537 (2001)

Remove particles that clearly do not belong (on average) to a statistically emitting projectile-like source

$$Z = 1: 0.35 \leq v_z / v_{z,PLF} \leq 1.65$$

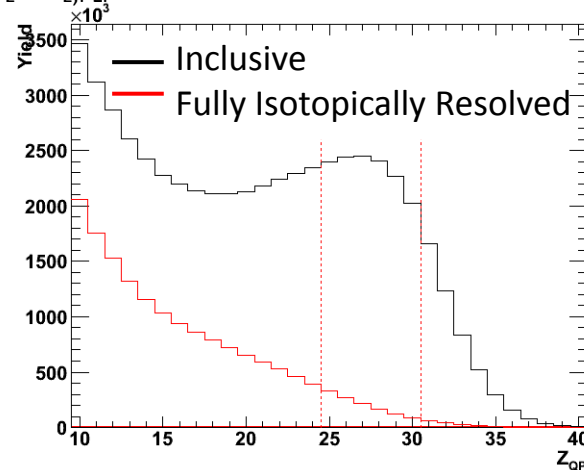
$$Z = 2: 0.40 \leq v_z / v_{z,PLF} \leq 1.60$$

$$Z \geq 3: 0.55 \leq v_z / v_{z,PLF} \leq 1.45$$



Select events with a well-measured QP:

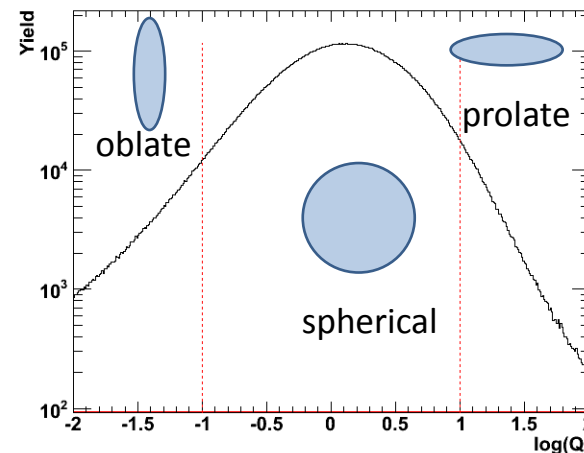
$$25 \leq \sum Z \leq 30$$



Select events with near-zero average momentum quadrupole.

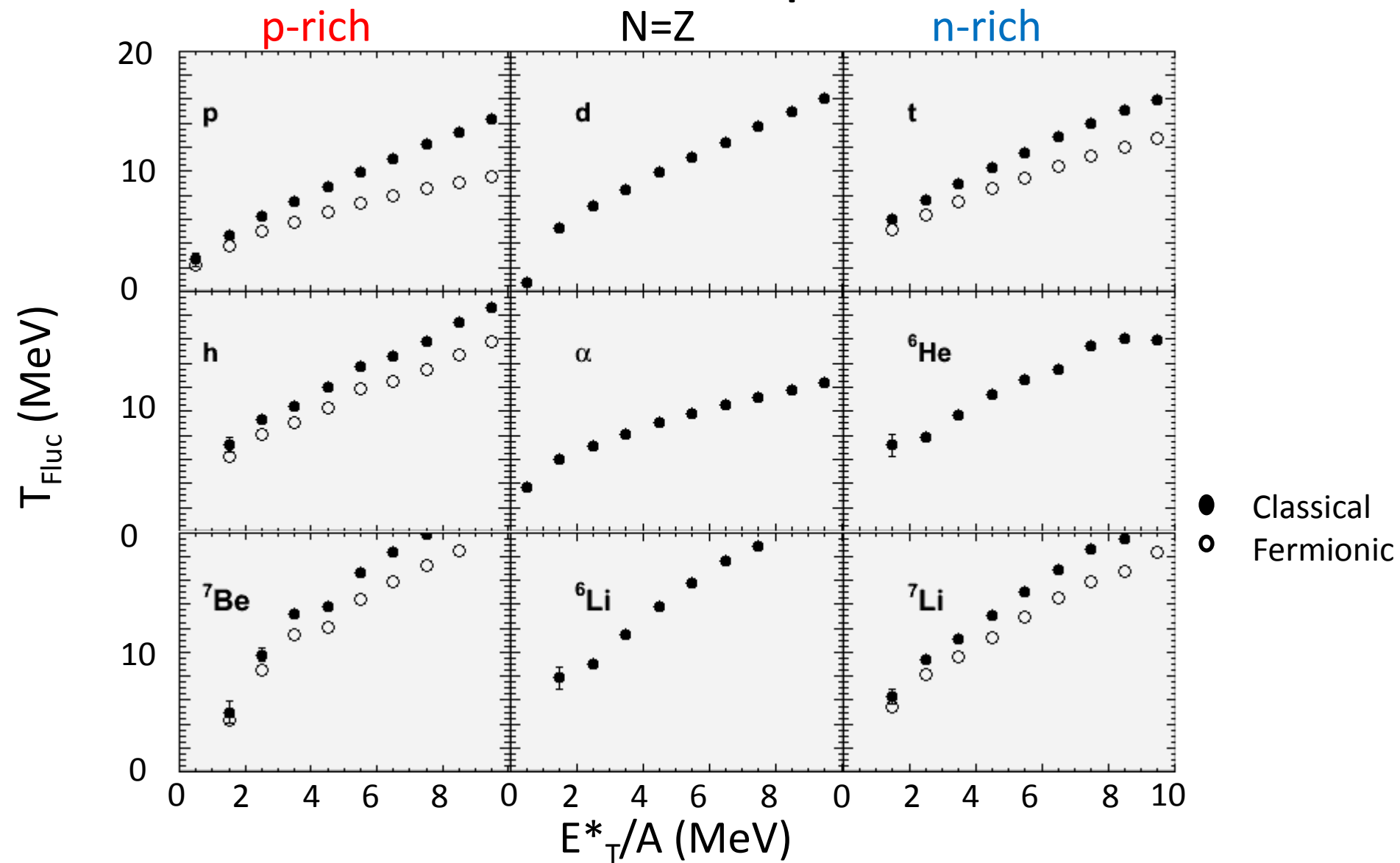
$$-1 \leq \log Q \leq 1$$

$$Q = \frac{\sum p_{z,i}^2}{\frac{1}{2} \sum p_{T,i}^2}$$



-- preliminary --

# Fluctuation Temperature



Classical:

$$\sigma_{xy}^2 = 4m^2 T_{cl}^2$$

Fermionic:

$$\sigma_{xy}^2 = \frac{16m^2 \epsilon_f^2}{35} \left( 1 + \frac{7}{6} \pi^2 \left( \frac{T}{\epsilon_f} \right)^2 \right)$$

$$\sigma_M^2 = \frac{3T}{2\epsilon_f}$$

# Isoscaling of Fragments from Reconstructed Quasi-Projectiles

$^{78,86}\text{Kr} + ^{58,64}\text{Ni}$  @  $E/A = 35$  MeV

Isoscaling over a very wide range of nuclides:

$$1 \leq Z \leq 17$$

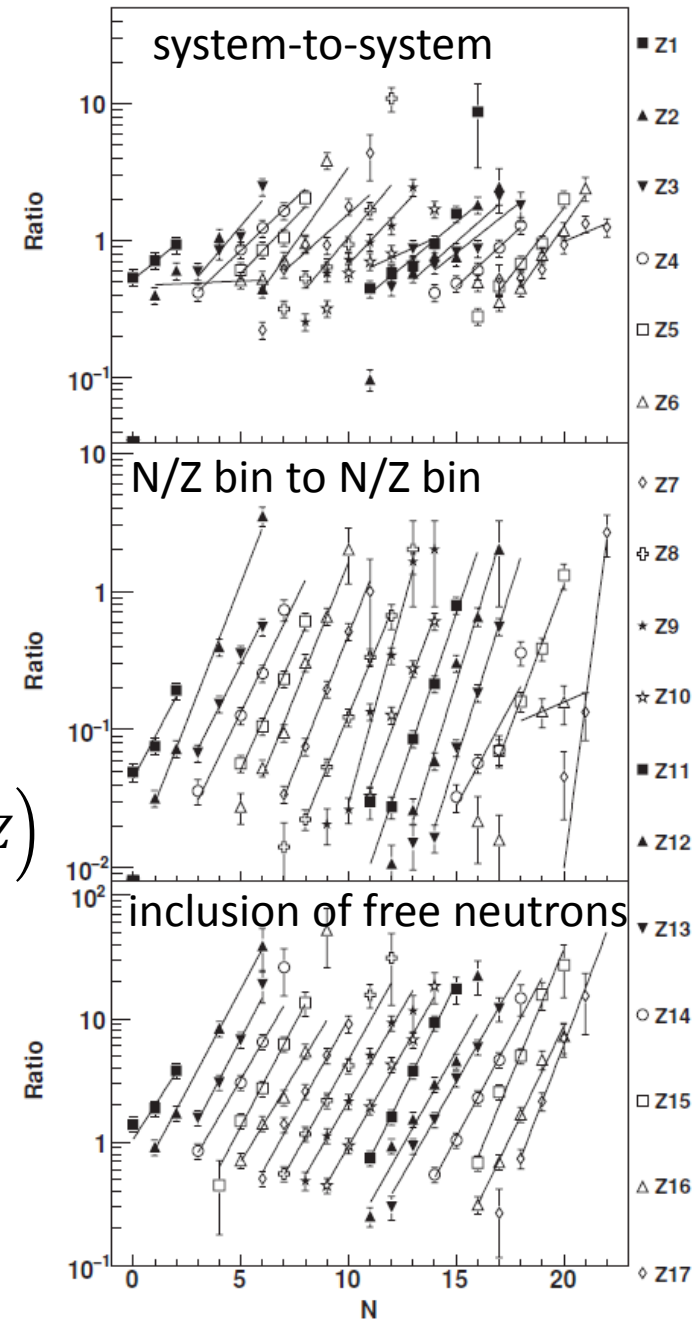
$$Y(N, Z) \propto \exp((-G(N, Z) + \mu_n N + \mu_p Z)/T)$$

$$R_{12}(N, Z) = \frac{Y_1(N, Z)}{Y_2(N, Z)} \propto \exp\left(\frac{\mu_{n,2} - \mu_{n,1}}{T} N - \frac{\mu_{p,2} - \mu_{p,1}}{T} Z\right)$$

$$R_{12}(N, Z) \propto \exp(\alpha N - \beta Z)$$

$$\frac{C_{sym}}{T} = \frac{\alpha}{\Delta}$$

**Careful source characterization is an integral part of this analysis!**

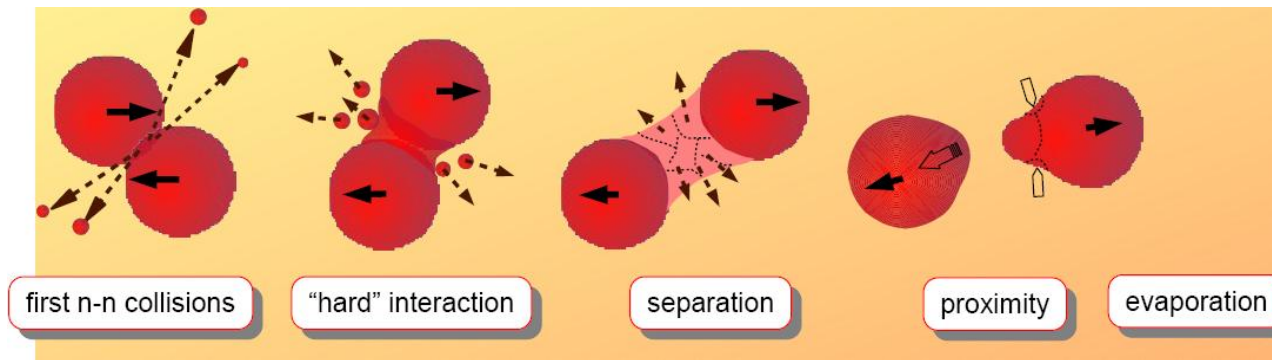


S. Wuenschel et al., PRC **79**, 061602 (2009)

see also P. Marini et al., submitted to PRC



- Challenge: to form a description of the heavy ion collisions that respects the dynamical and statistical evolution of the system



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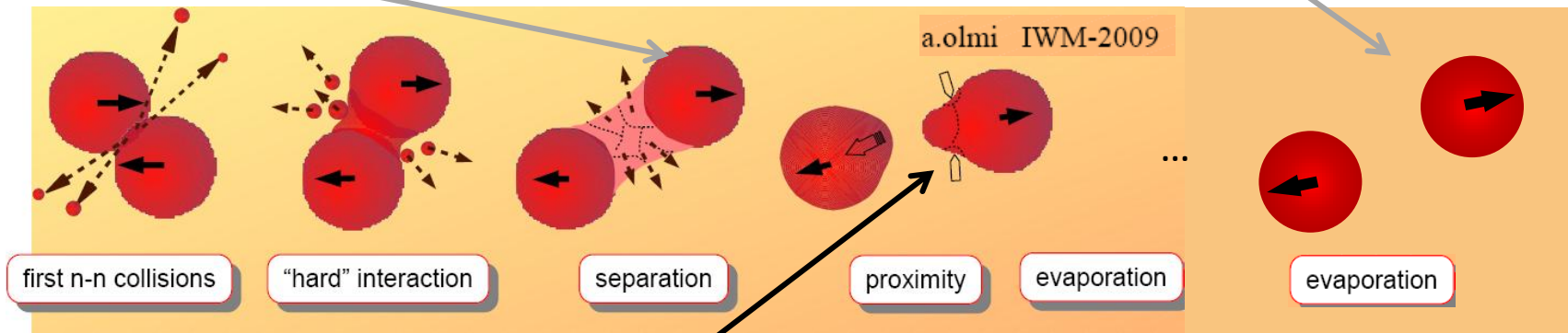
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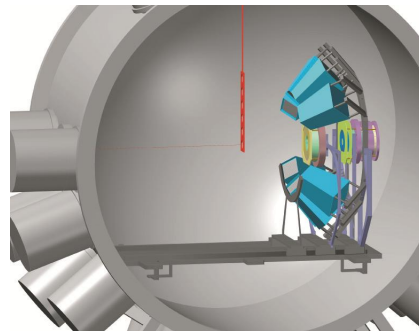
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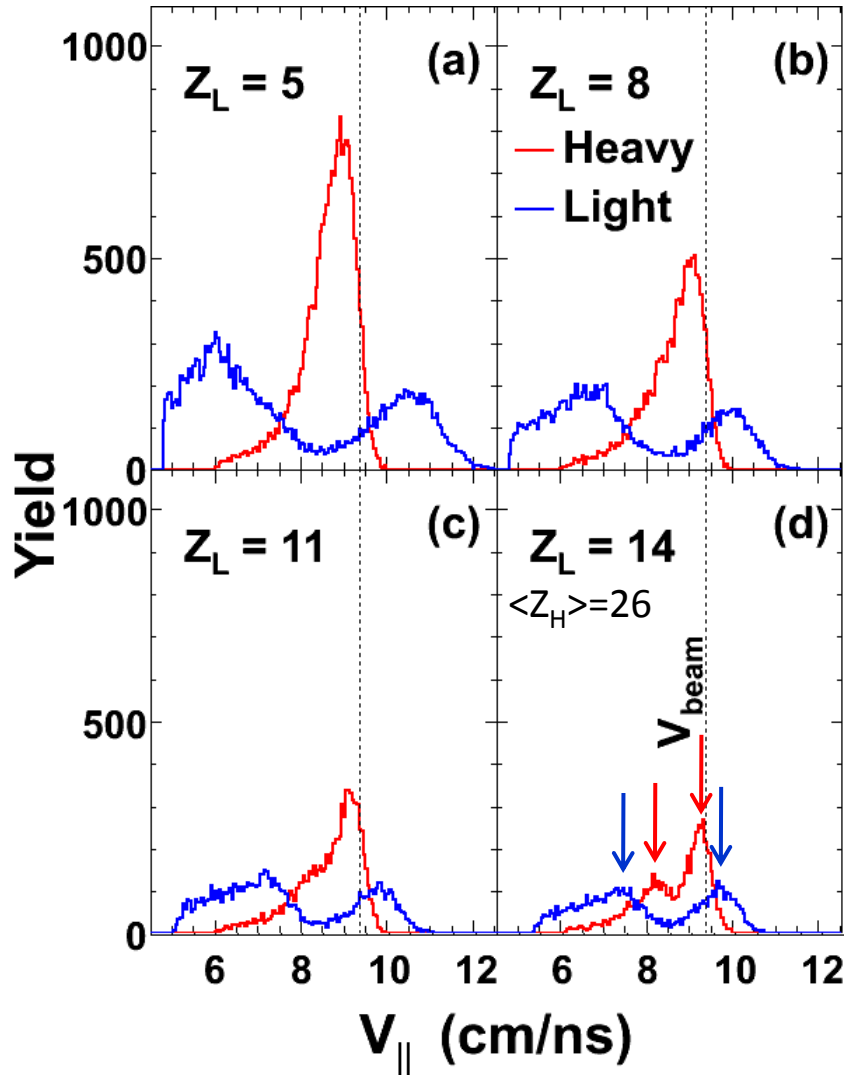
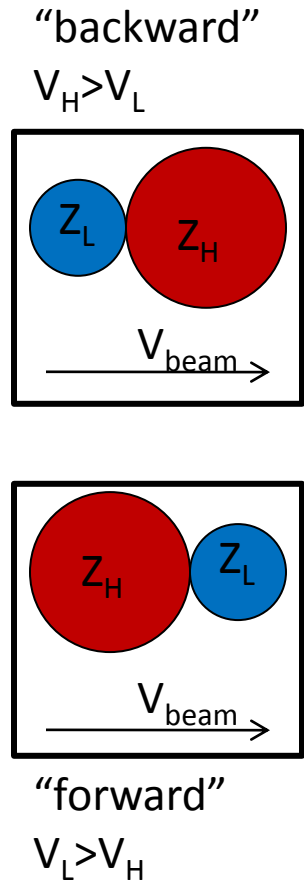
- Alignment
- Fragment Size
- Fragment Composition
- Yield
- Dissipation
- Decay Timescale



*Alan McIntosh, Ph.D. Thesis, 2010  
Indiana University*

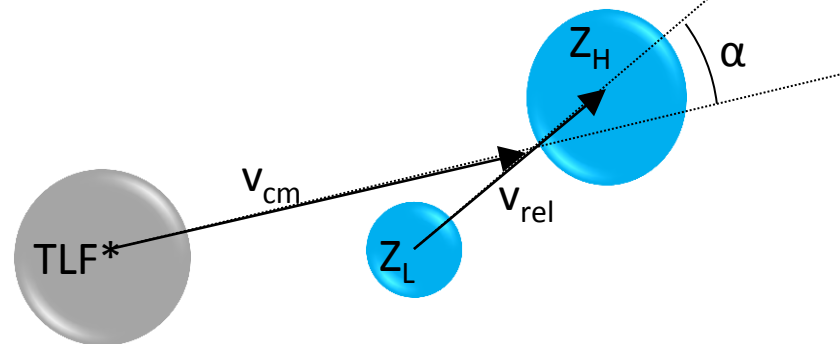
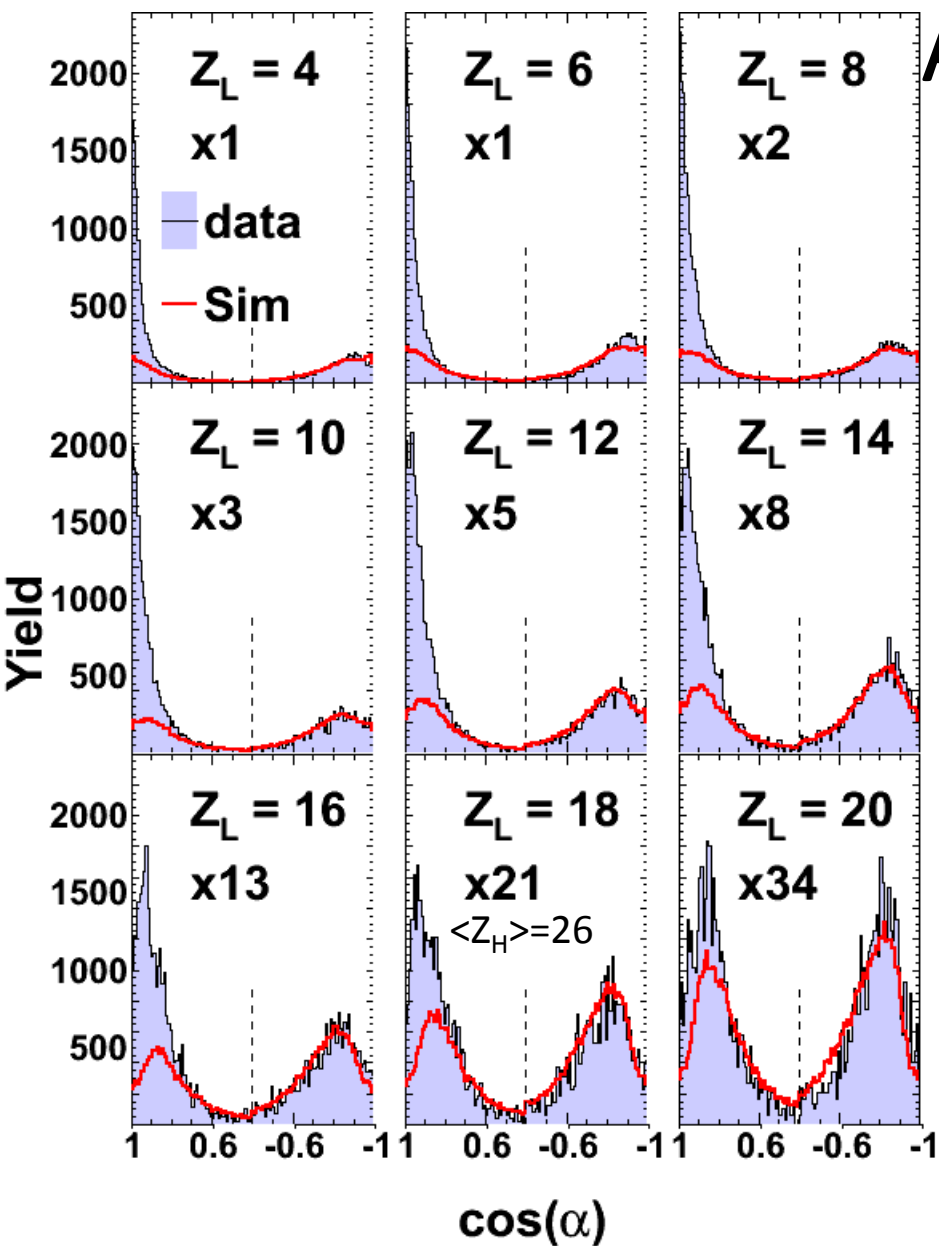
*Out-of-equilibrium  
fragment production*

# Recoil Effects Between $Z_{\text{Heavy}}$ and $Z_{\text{Light}}$



- Select events with at least **2 fragments** ( $Z_H \geq 21$ ,  $Z_L \geq 4$ )
- $3^\circ \leq \theta_{\text{lab}} \leq 7^\circ$  selects only “forward” and “backward” break-up
- Light fragment ( $Z_L$ ) is peaked forward of mid-velocity
- Recoil effects indicate a common parent

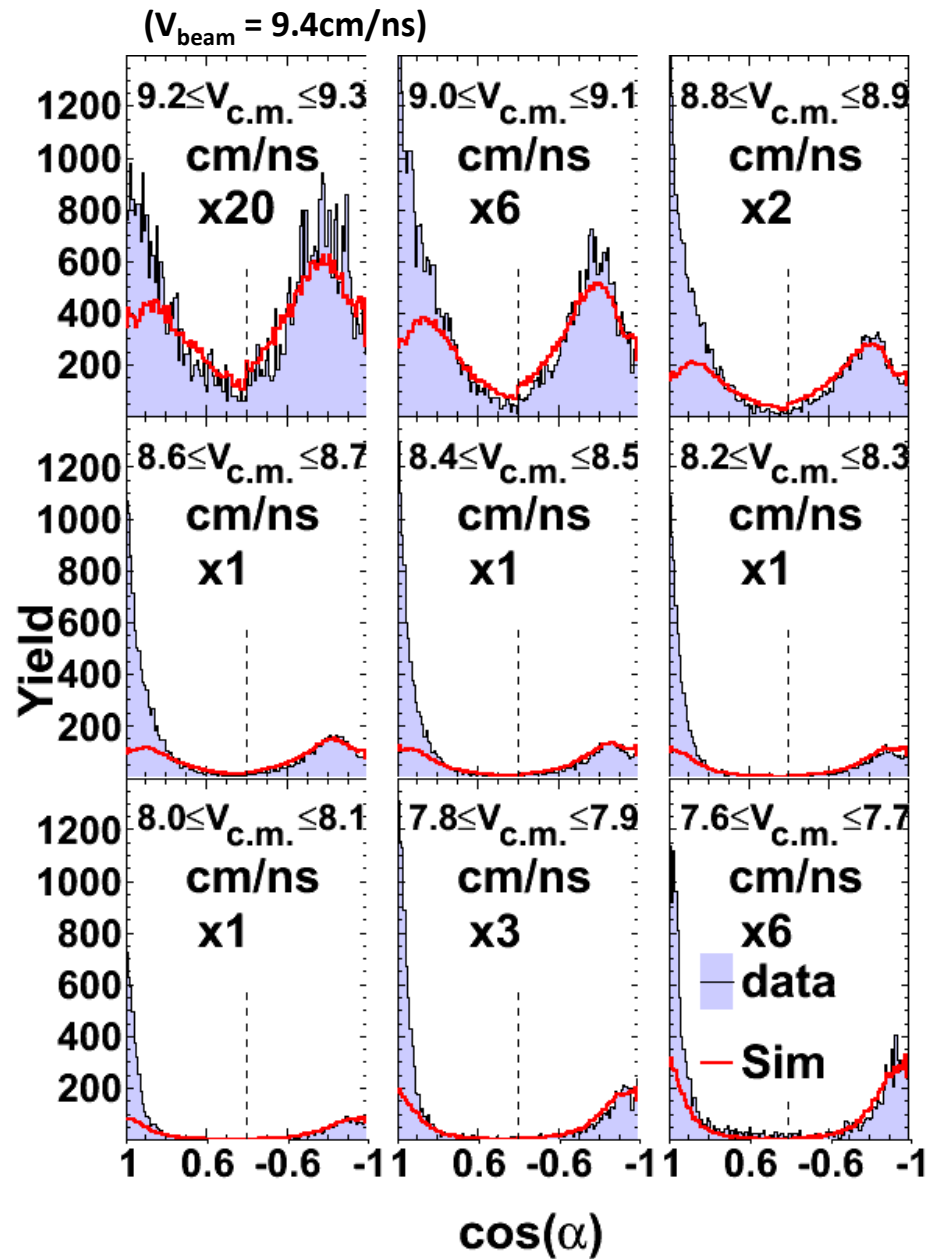
# Alignment and Size ( $Z_L$ )



- Excess yield of IMF emitted toward Target-Like Fragment
- — Isotropic emission cannot account for backward yield
- Strong alignment
- **Alignment decreases with  $Z_L$**
- **Persists to near-symmetric splits**
- Mechanism...

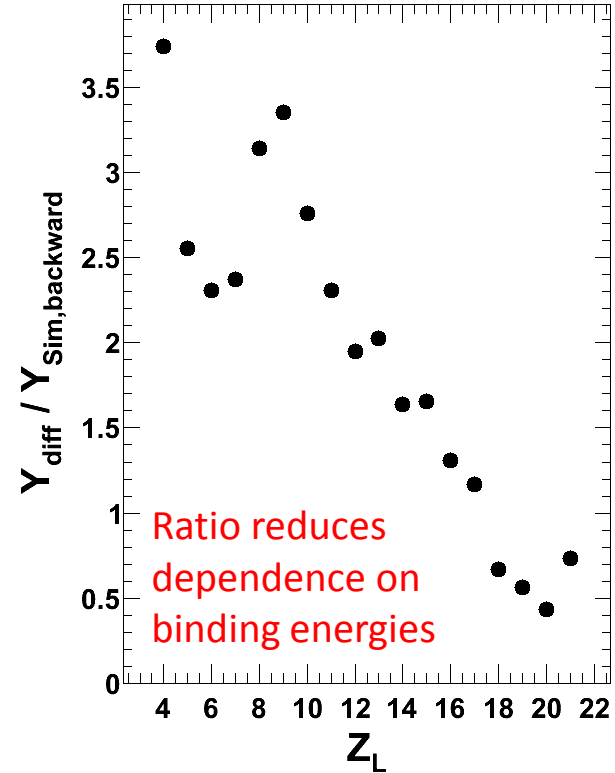
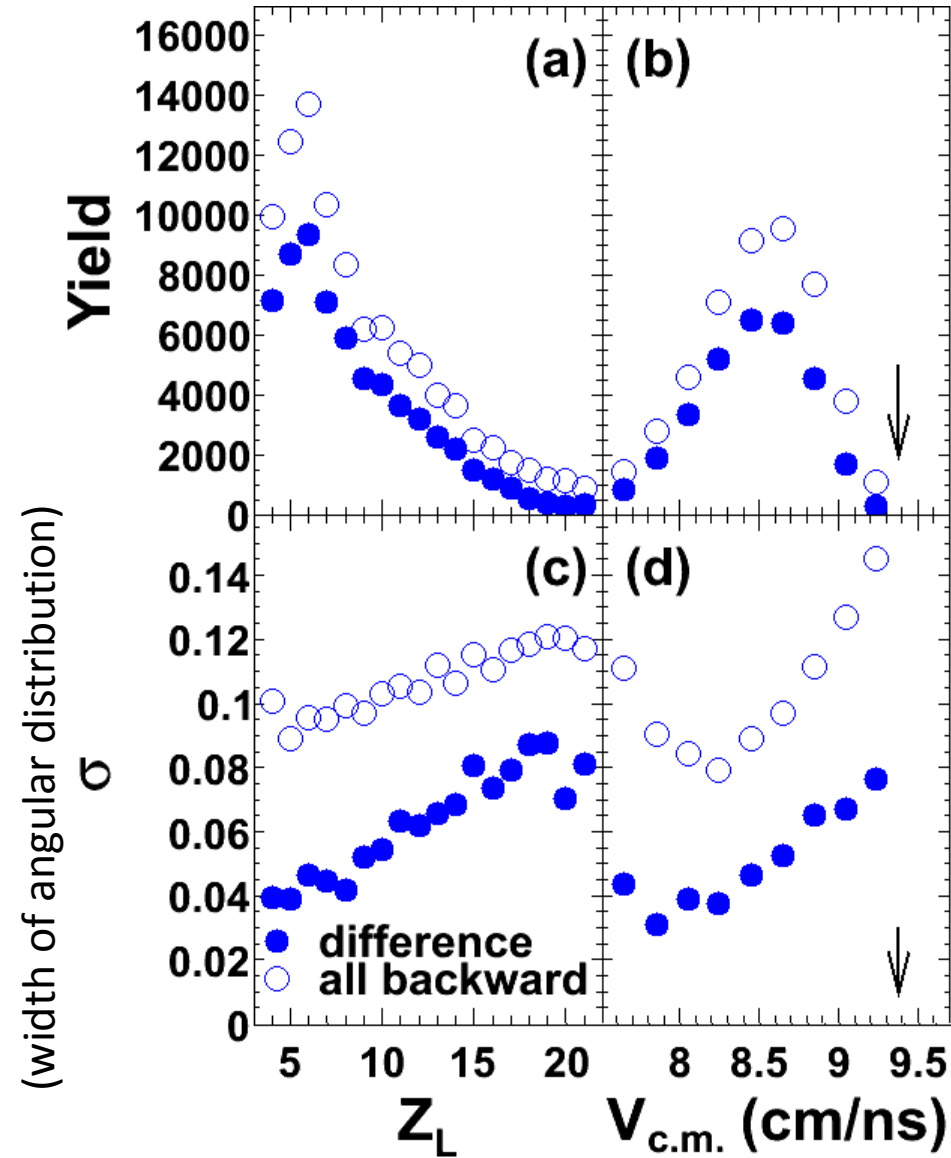
# Velocity Damping and Alignment

- Detector acceptance accounted for
- Isotropic emission describes forward emission, but not backward emission
- **Correlation: Alignment increases with damping**



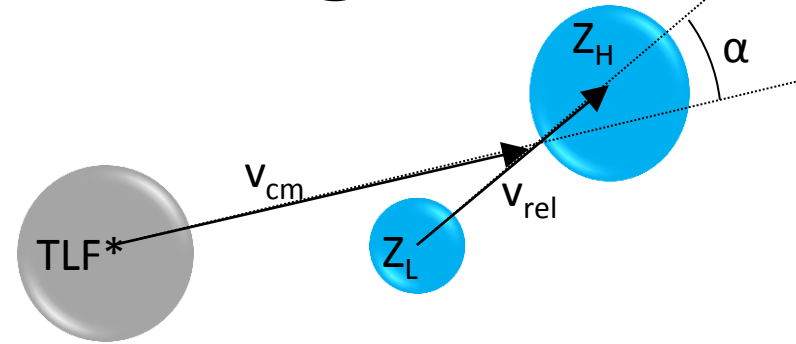
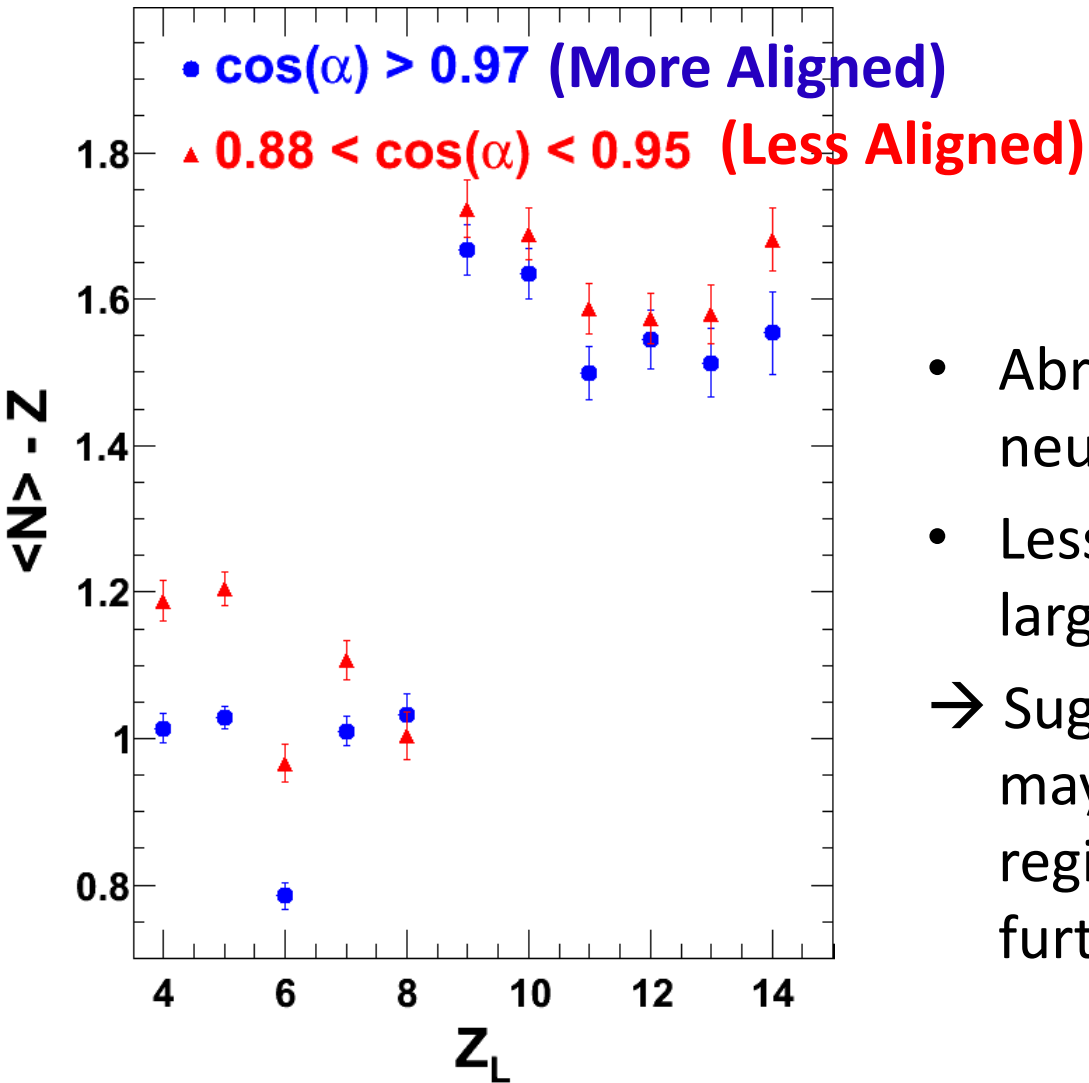
- Smooth evolution in both the yield and width

- Asymmetric  $\leftrightarrow$  Symmetric
- Small damping  $\leftrightarrow$  Large damping



Relative yield is peaked at  $Z_L=9$

# Composition of Aligned Fragments



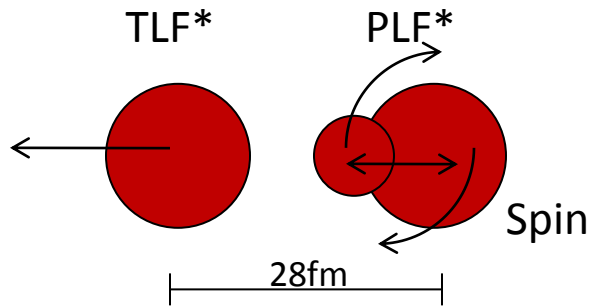
- Abrupt change in average neutron excess at  $Z_L=9$
  - Less aligned fragments have larger neutron excess
- Suggests isospin equilibration may not be reached between regions of the decaying PLF\*, further investigation needed

$^{124}\text{Xe} + ^{124}\text{Sn}$  @  $E/A = 50$  MeV

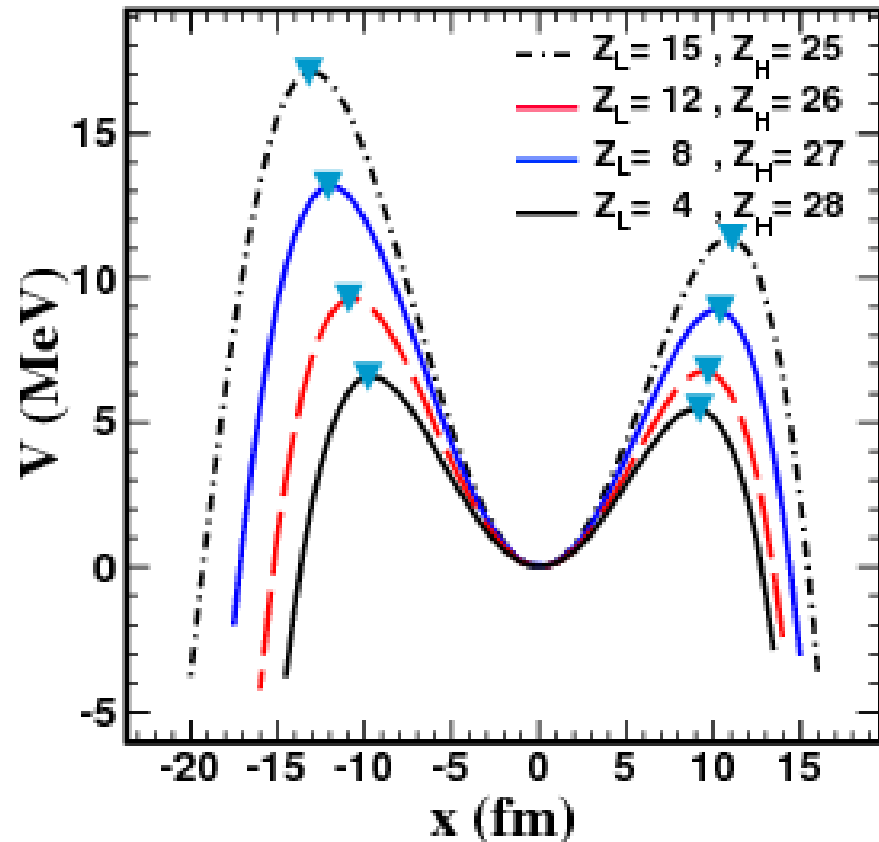
McIntosh et al., PRC 81, 034603 (2010)

# Langevin Model

- Separation of PLF\* into  $Z_L$  and  $Z_H$  evolves on a potential energy surface
- Nuclear between  $Z_H$  and  $Z_L$
- Coulomb between  $Z_H$ ,  $Z_L$  and the target-like fragment
- High-fraction Limit: Motion is over-damped
- Motion along the potential energy surface is stochastic (thermal)

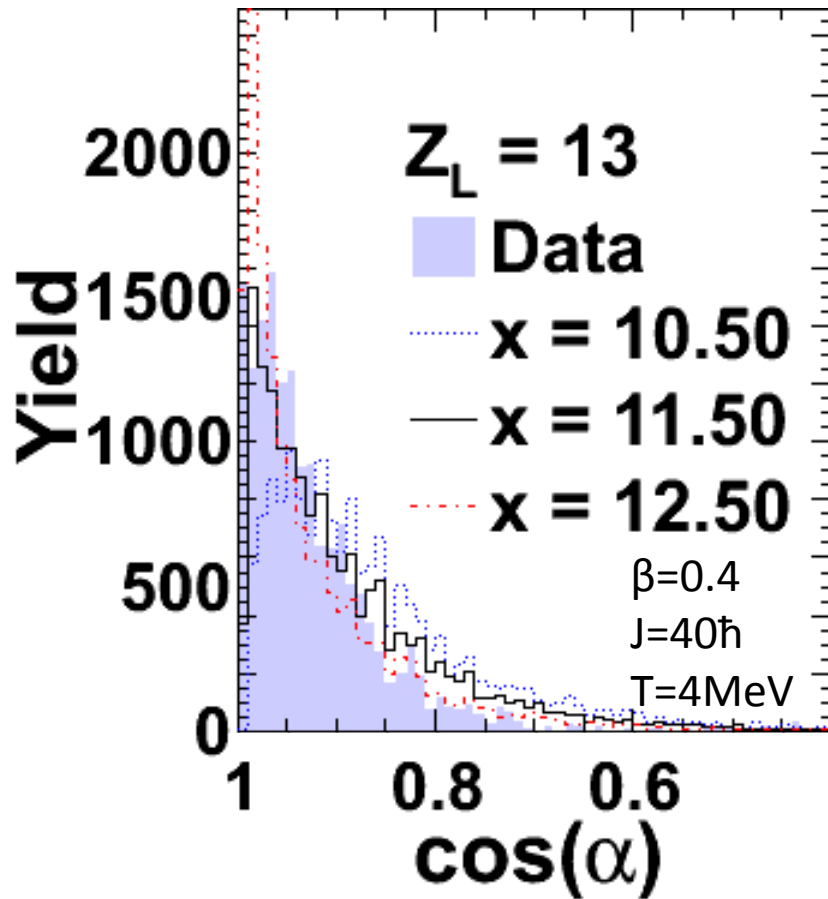


Langevin model courtesy of R. Charity

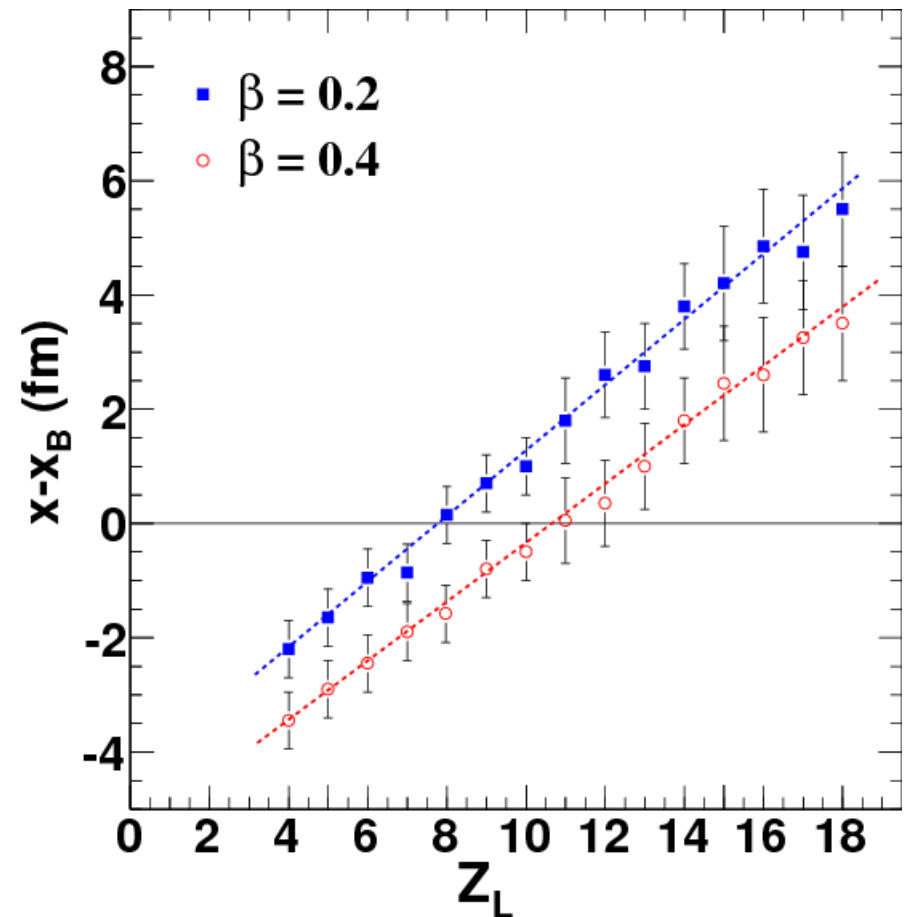




# Langevin Model

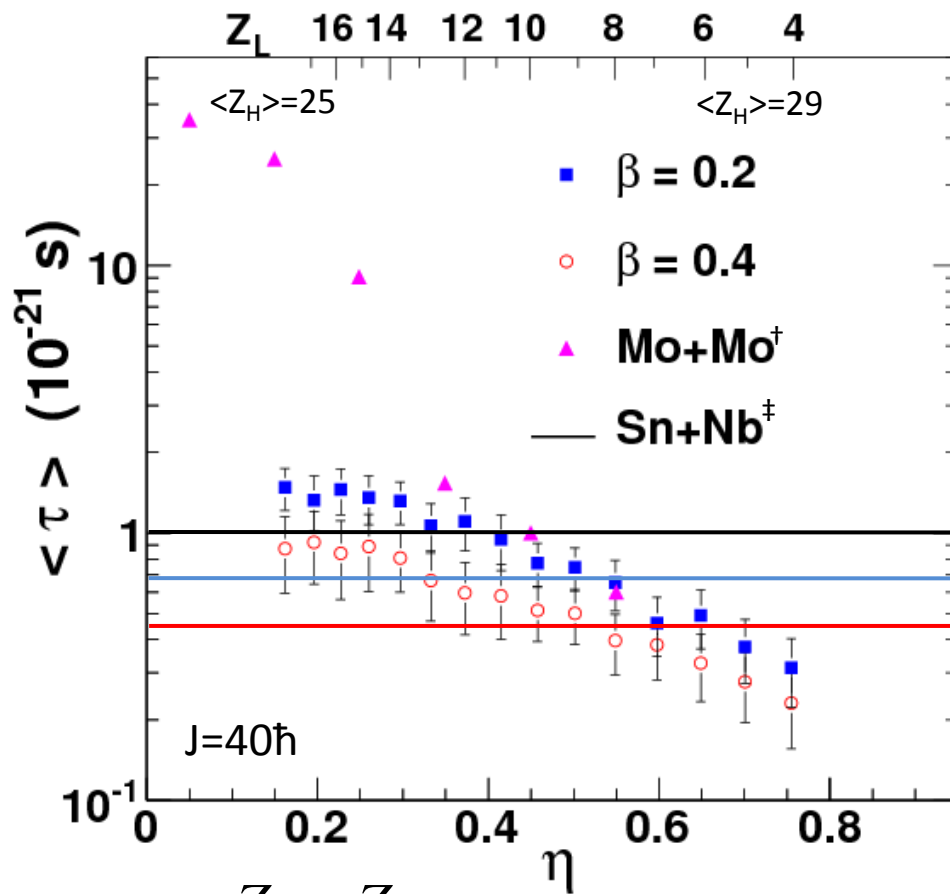


Account for detector acceptance & granularity.  
Vary the initial deformation ( $x$ ) to reproduce the experimental angular distributions.  
→ Sensitivity  $< 1.0\text{fm}$



Within the context of the model, the lightest fragments are produced from systems already deformed beyond the barrier

# Timescale of Aligned Decay



$$\eta = \frac{Z_H - Z_L}{Z_H + Z_L}$$

124Xe + 124Sn @ E/A = 50 MeV  
McIntosh et al., PRC 81, 034603 (2010)

$Z_L=4$ :

$\langle \tau \rangle = 0.25 - 0.35 \times 10^{-21} \text{ s}$   
(75-100fm/c)

$Z_L=18$ :

$\langle \tau \rangle = 0.90 - 1.5 \times 10^{-21} \text{ s}$   
(270-450fm/c)

For  $J=30\hbar \rightarrow$  increase  $\tau$  by 25%

† Mo + Mo at E/A = 20MeV  
Casini et al., PRL 71, 2567 (1993)

‡  $^{116}\text{Sn} + ^{93}\text{Nb}$  at E/A = 29MeV  
Piantelli et al., PRL 88, 052701 (2002)

# Correlations Summary

- Smooth evolution of aligned component with size ( $Z_L$ )
  - Stronger alignment for small  $Z_L$
  - Alignment persists for near-symmetric splits
- Smooth evolution of aligned component with damping
  - Alignment increases with damping
- Decay time-scale ( $0.25-1.5 \times 10^{-21}$ s) evolves with  $Z_L$  (or  $\eta$ )
- Transition around  $Z_L=9$  observed in:
  - Composition (N/Z), Relative Yield, Distance from the Barrier
- Observed dependence of composition on decay orientation
  - Suggests sensitivity to N/Z transport *within* an excited transiently-deformed nucleus – further investigation is needed.

# Final Remarks

- Dynamical transport models and molecular dynamics models are used to extract information on  $E_{\text{sym}}(\rho)$ .
- These models are successful in describing some aspects of fragment production – but a more complete description of the reaction is necessary to constrain  $E_{\text{sym}}(\rho)$
- Single description of the reaction needed – respect both dynamical & statistical nature
- Cluster production in the dynamical evolution
- Correlations between observables for dynamically produced fragments → Further constraints for models