

Breakup as a tool to study exotic nuclear structures

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Outline

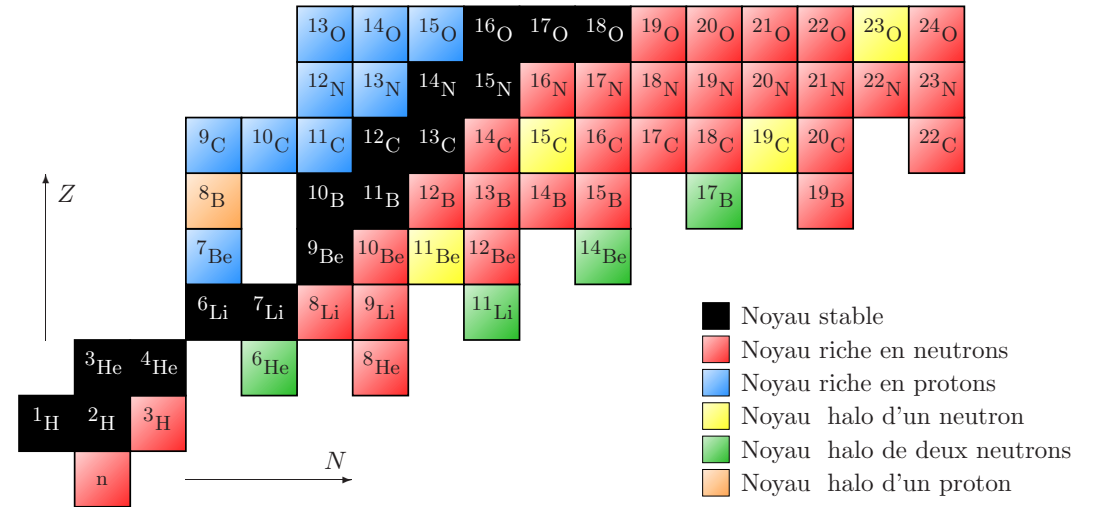
- Introduction: Halo nuclei
- Theoretical **framework** of reaction modelling
- Reaction models
 - Continuum-discretised coupled channel (**CDCC**)
 - Time-dependent technique (**TDSE**)
 - Dynamical eikonal approximation (**DEA**)
- New observable: **Ratio** technique
 - Similarity between **angular distributions** for elastic scattering and breakup
 - Ratio idea
- Summary

Introduction

Exotic nuclear structures are found far from stability

E.g. halo nuclei with peculiar quantal structure:

- Light, **n-rich** nuclei
- Large **matter radius**
- Low S_n or S_{2n}



⇒ strongly clusterised system:

neutrons **tunnel** far from the **core** and form a **halo**

Far from stability nuclei are **short-lived**

⇒ studied in **indirect** ways, e.g. through reactions

⇒ need accurate **reaction models**

and **observables** sensitive to nuclear structure

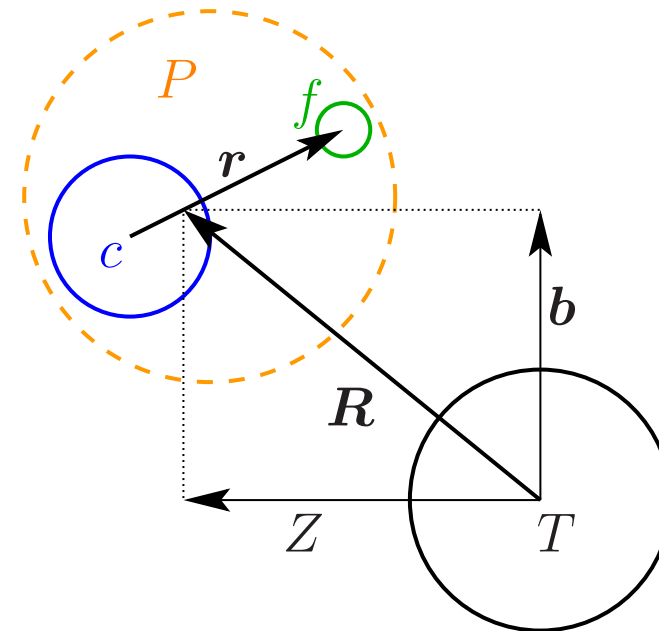
Framework

Projectile (P) modelled as a two-body system:
 core (c)+loosely bound nucleon (f) described by

$$H_0 = T_r + V_{cf}(\mathbf{r})$$

V_{cf} adjusted to reproduce
 bound state Φ_0
 and resonances

Target T seen as
 structureless particle



P - T interaction simulated by optical potentials
 \Rightarrow breakup reduces to **three-body** scattering problem:

$$[T_R + H_0 + V_{cT} + V_{fT}] \Psi(\mathbf{R}, \mathbf{r}) = E_T \Psi(\mathbf{R}, \mathbf{r})$$

with initial condition $\Psi(\mathbf{r}, \mathbf{R}) \xrightarrow{Z \rightarrow -\infty} e^{iKZ} \Phi_0(\mathbf{r})$

CDCC

Solve the three-body scattering problem:

$$[T_R + H_0 + V_{cT} + V_{fT}] \Psi(\mathbf{r}, \mathbf{R}) = E_T \Psi(\mathbf{r}, \mathbf{R})$$

by expanding Ψ on eigenstates of H_0

$$\Psi(\mathbf{r}, \mathbf{R}) = \sum_i \chi_i(\mathbf{R}) \Phi_i(\mathbf{r}) \quad \text{with } H_0 \Phi_i = \epsilon_i \Phi_i$$

Leads to set of coupled-channel equations (hence **CC**)

$$[T_R + \epsilon_i + V_{ii}] \chi_i + \sum_{j \neq i} V_{ij} \chi_j = E_T \chi_i,$$

with $V_{ij} = \langle \Phi_i | V_{cT} + V_{fT} | \Phi_j \rangle$

The continuum has to be **discretised** (hence **CD**)

[Kamimura *et al.* Prog. Theor. Phys. Suppl. 89, 1 (1986)]

code FRESKO [Thompson, Comp. Phys. Rep. 7, 167 (1988)]

Fully quantal approximation

No approx. on P - T motion, nor restriction on energy

But **expensive** computationally (at high energies)

Time-dependent model

P - T motion described by classical trajectory $\mathbf{R}(t)$

Time-dependent potentials simulate P - T interaction

P structure described quantum-mechanically by H_0

\Rightarrow Time-dependent Schrödinger equation (TDSE)

$$i\hbar \frac{\partial}{\partial t} \Psi(\mathbf{r}, \mathbf{b}, t) = [H_0 + V_{cT}(t) + V_{fT}(t)] \Psi(\mathbf{r}, \mathbf{b}, t)$$

solved for each \mathbf{b} with initial condition $\Psi \xrightarrow[t \rightarrow -\infty]{} \Phi_0$

Many codes have been written to solve TDSE

[Esbensen, Bertsch and Bertulani, NPA 581, 107 (1995)]

[Typel and Wolter, Z. Naturforsch. A54, 63 (1999)]

[P.C., Baye and Melezhik, PRC 68, 014612 (2003)]

Lacks quantum interferences between trajectories

Dynamical eikonal approximation

Three-body scattering problem:

$$[T_R + H_0 + V_{cT} + V_{fT}] \Psi(\mathbf{r}, \mathbf{R}) = E_T \Psi(\mathbf{r}, \mathbf{R})$$

with condition $\Psi \xrightarrow{Z \rightarrow -\infty} e^{iKZ} \Phi_0$

Eikonal approximation: factorise $\Psi = e^{iKZ} \hat{\Psi}$

$$T_R \Psi = e^{iKZ} [T_R + vP_Z + \frac{\mu_{PT}}{2} v^2] \hat{\Psi}$$

Neglecting T_R vs P_Z and using $E_T = \frac{1}{2} \mu_{PT} v^2 + \epsilon_0$

$$i\hbar v \frac{\partial}{\partial Z} \hat{\Psi}(\mathbf{r}, \mathbf{b}, Z) = [H_0 - \epsilon_0 + V_{cT} + V_{fT}] \hat{\Psi}(\mathbf{r}, \mathbf{b}, Z)$$

solved for each \mathbf{b} with condition $\hat{\Psi} \xrightarrow{Z \rightarrow -\infty} \Phi_0(\mathbf{r})$

This is the dynamical eikonal approximation (**DEA**)

[Baye, P. C., Goldstein, PRL 95, 082502 (2005)]

Same equation as **TDSE** with straight line trajectories

DEA, TDSE and eikonal

$$i\hbar v \frac{\partial}{\partial Z} \hat{\Psi}(\mathbf{r}, \mathbf{b}, Z) = [H_0 - \epsilon_0 + V_{cT} + V_{fT}] \hat{\Psi}(\mathbf{r}, \mathbf{b}, Z)$$

DEA \neq **TDSE** because \mathbf{b} and Z are quantal
 \Rightarrow includes interference between *trajectories*

The usual **eikonal** uses adiabatic approx. $H_0 - \epsilon_0 \sim 0$
 \Rightarrow neglects internal dynamics of projectile

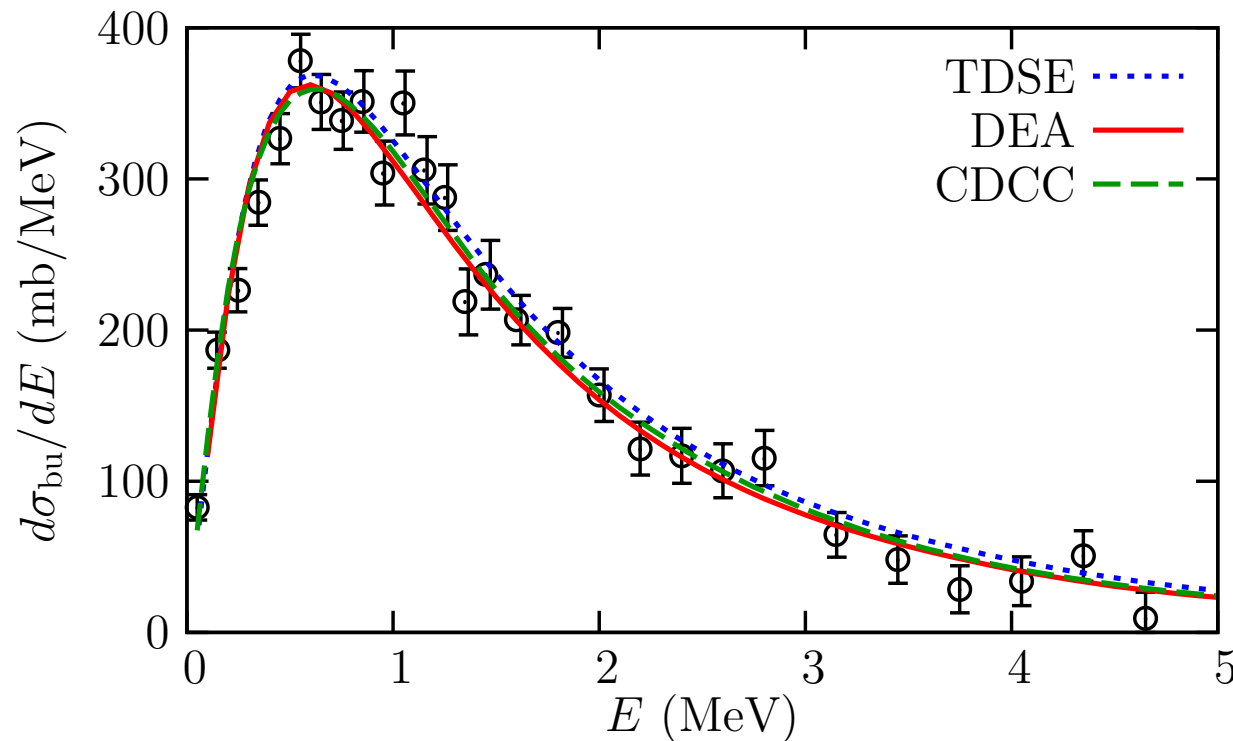
$$\hat{\Psi}^{\text{eik}}(\mathbf{r}, \mathbf{b}, Z) = e^{-\frac{i}{\hbar v} \int_{-\infty}^Z dZ' [V_{cT}(\mathbf{r}, \mathbf{b}, Z') + V_{fT}(\mathbf{r}, \mathbf{b}, Z')]} \Phi_0(\mathbf{r})$$

\Rightarrow dynamical eikonal generalises TDSE and eikonal

- improves TDSE by including **quantal** interferences
- improves eikonal by including **dynamical** effects

How do **CDCC**, **TDSE** and **DEA** compare?

Energy distribution: $^{15}\text{C}+\text{Pb}$ @ 68 A MeV



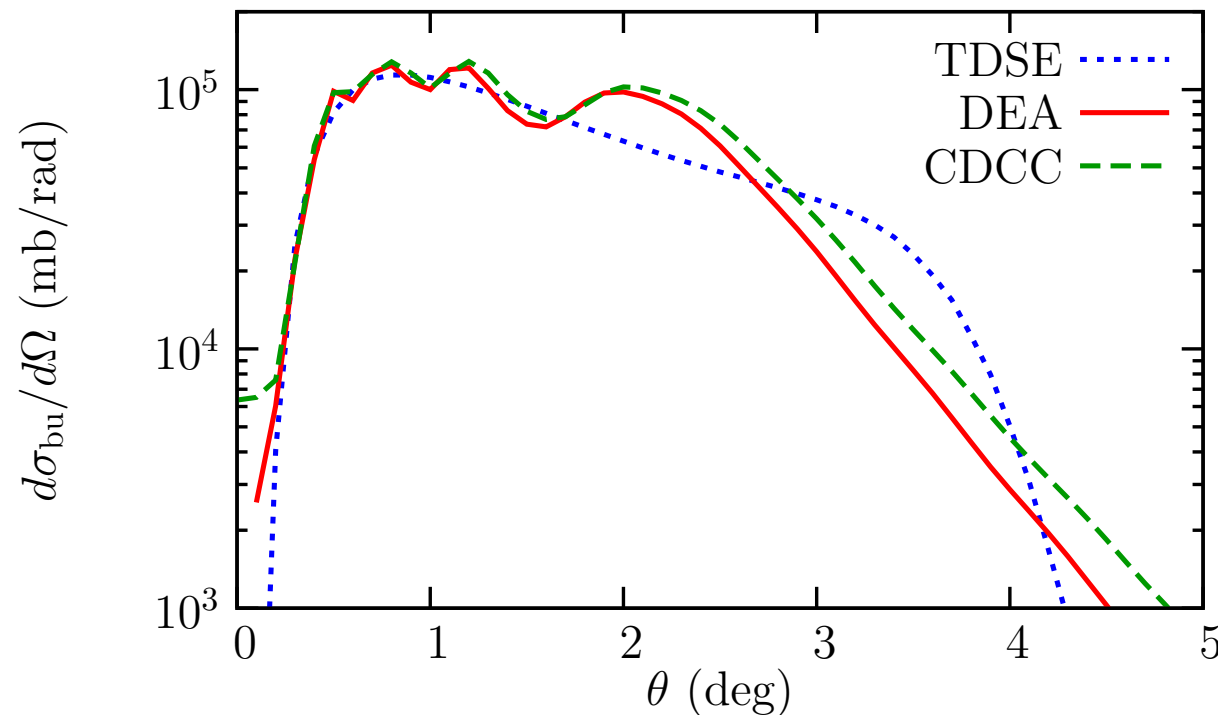
- Excellent agreement between all three models
- Excellent agreement with experiment

[Nakamura *et al.* PRC 79, 035805 (2009)]

⇒ Confirms the validity of the approximations

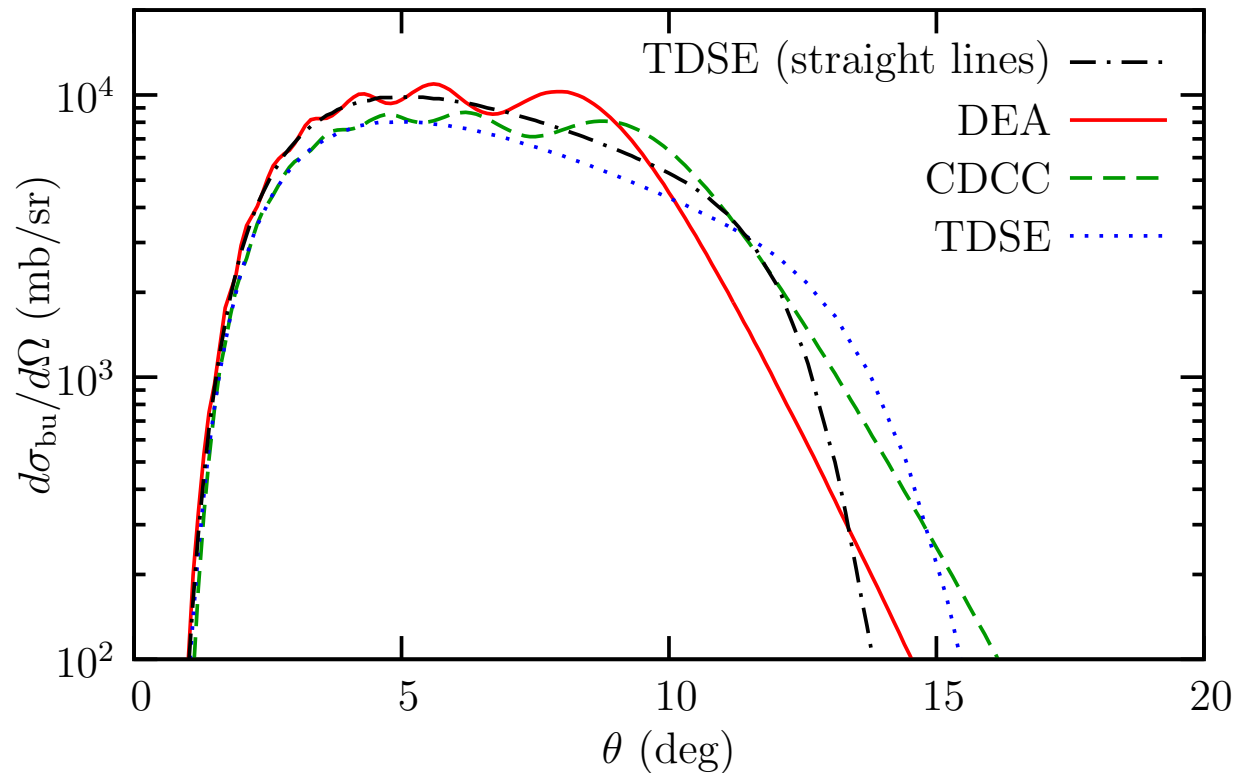
... and the two-body structure of ^{15}C

Angular distribution: $^{15}\text{C}+\text{Pb}$ @ 68 A MeV



- **TDSE** lacks quantum interferences but **reproduces** the general trend at small θ and observables integrated over angles
- **DEA** exhibits the quantum interferences much less time consuming than **CDCC**

$^{15}\text{C} + \text{Pb}$ @ 20 A MeV



- Disagreement between **DEA** and **CDCC** increases
- With **Coulomb trajectories** TDSE follows CDCC
- With straight lines TDSE follows DEA

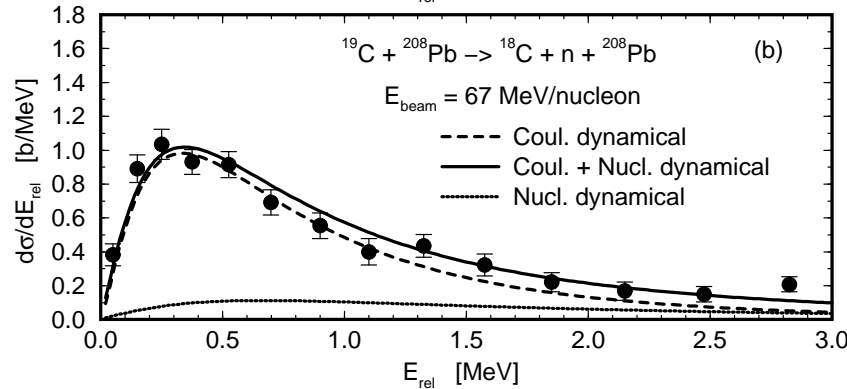
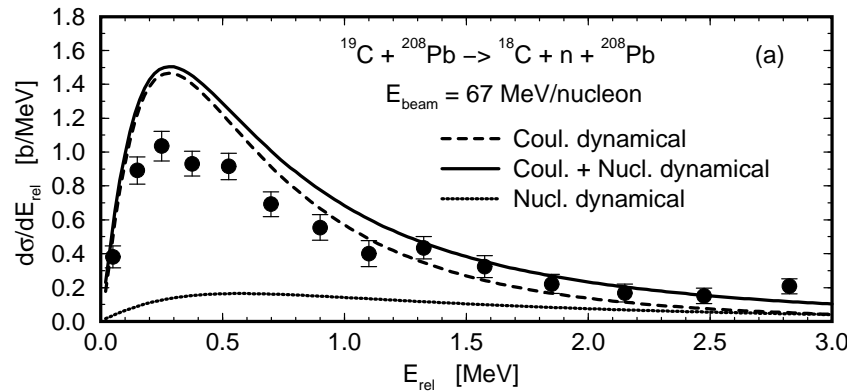
⇒ **DEA** lacks Coulomb deflection

Conclusion of the comparison

- Various nuclear-reaction models exist
Built on simple description of nuclei
using **phenomenological** potentials
see review article [Baye, P.C. arXiv:1011.6427 (2010)]
 - All models agree in energy distribution
agree with exp. \Rightarrow mechanism well understood
 - **TDSE** lacks **interferences** in angular distribution
because of semiclassical approximation
 - **DEA** reproduces **CDCC** results
while less time consuming
but lacks Coulomb deflection
- \Rightarrow **CDCC** can be replaced by **DEA** at high energies

Study of halo nuclei (TDSE)

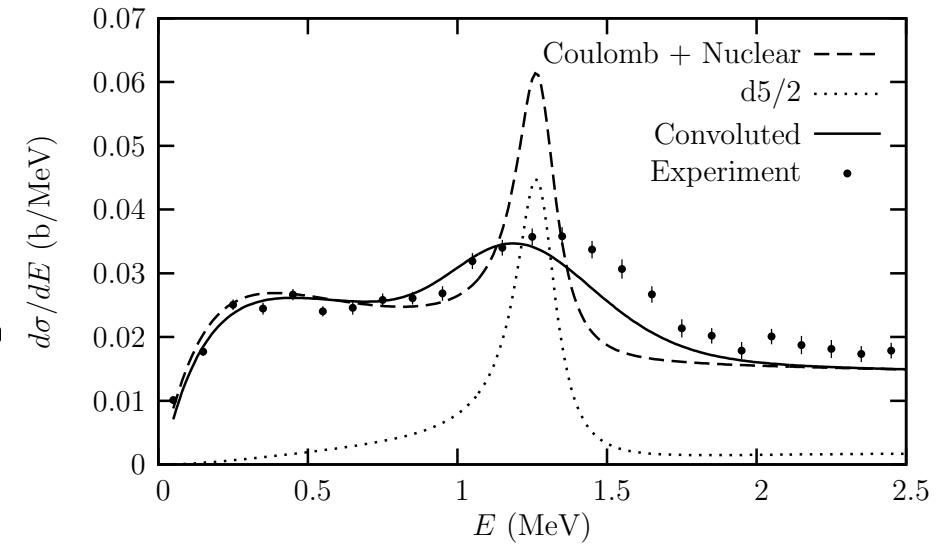
^{19}C on Pb @ 67 A MeV



[Typel and Shyam, PRC 64, 024605 (2001)]

Exp. [Nakamura *et al.*, PRL 83, 1112 (1999)]

^{11}Be on C @ 67 A MeV



[P.C., Goldstein, Baye, PRC 70, 064605 (2004)]

Exp. [Nakamura *et al.* PRC 70, 054606 (2004)]

- Sensitive to **binding energy**

$$S_n = \text{(a) } 530\text{keV}; \text{(b) } 650\text{keV}$$

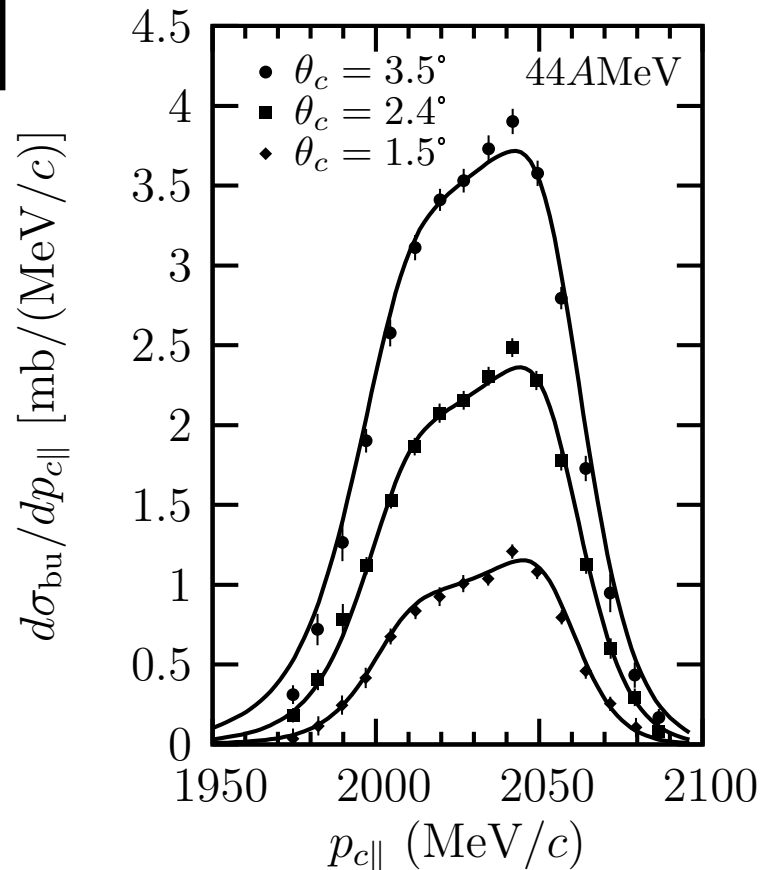
- Probes structure of **continuum** ($5/2^+$ resonance)

Reaction dynamics (DEA)

^8B on Pb @ 44 A MeV

DEA calculations

[Goldstein, P.C. and Baye, PRC 76, 024608 (2007)]



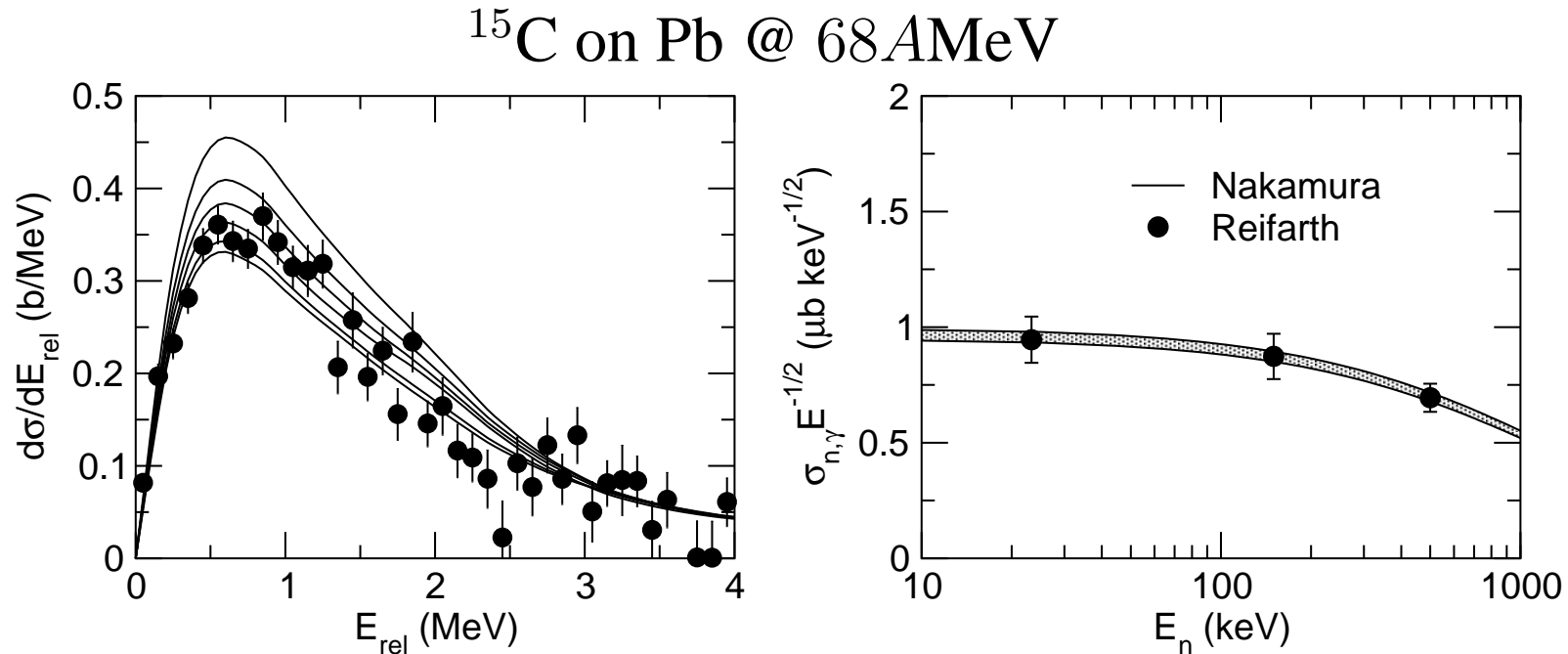
- agree with data
[Davids *et al.* PRL 81, 2209 (98)]
- validate $^7\text{Be} + \text{p}$ structure of ^8B
- presence of E2 transitions
- higher-order effects
(couplings in continuum)

⇒ significant reaction dynamics

⇒ attention when extracting info. from breakup data

(e.g. $dB(E1)/dE$)

Application to astrophysics (CDCC)



[Summers and Nunes, PRC 78, 011601(R) (2008)]

CDCC calculations with various ^{15}C models

Extract ANC from comparison with data

[Nakamura *et al.* PRC 79, 035805 (2009)]

Deduce σ_{capt} for $^{14}\text{C}(n, \gamma)$, agrees with direct measure

Same analysis with TDSE [Esbensen PRC 80, 024608 ('09)]

Sensitivity to model inputs

Breakup is used to infer information about

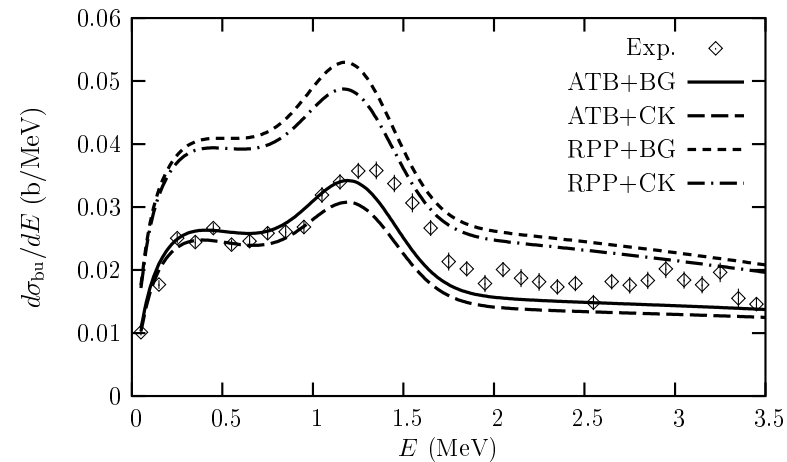
- exotic nuclear structure (halo nuclei)
- radiative capture of astrophysical interest

Reaction process is complex (E2, higher-orders...)

Calculations sensitive to optical potentials V_{PT}

Ex. $^{11}\text{Be} + \text{C}$ @ 69 A MeV

[P.C., Goldstein, Baye, PRC 70, 064605 (2004)]

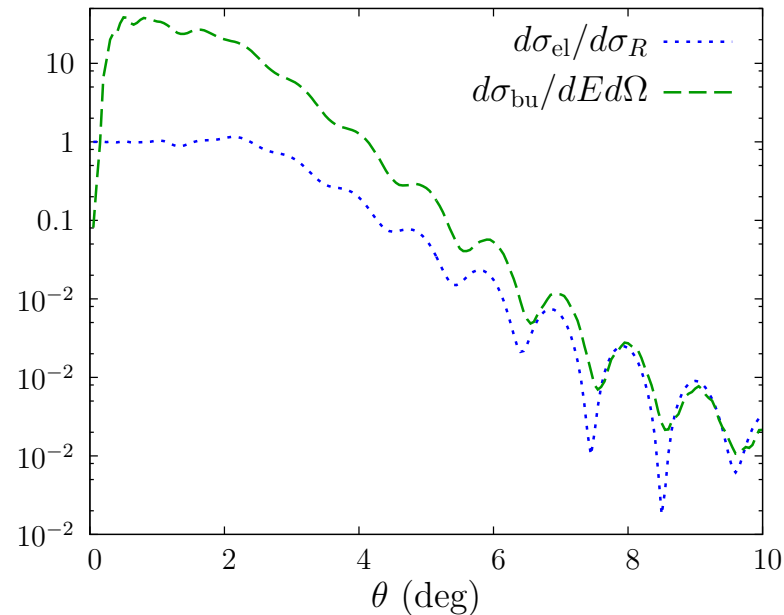


Is there an observable **insensitive** to reaction process, V_{PT} , and that gives direct access to nuclear structure ?

Angular distributions

$^{11}\text{Be}+\text{Pb}$ @ 69 A MeV

[P. C., M. Hussein, D. Baye, PLB 693, 448 (2010)]



Very **similar** features for **scattering** and **breakup**:

- oscillations at forward angles
- Coulomb rainbow ($\sim 2^\circ$)
- oscillations at large angles

\Rightarrow projectile scattered similarly bound or broken up

Recoil Excitation and Breakup

Assumes [R. Johnson *et al.* PRL 79, 2771 (1997)]

- adiabatic approximation
- $V_{fT} = 0$

⇒ excitation and breakup due to **recoil** of the core

Elastic scattering: $\frac{d\sigma_{el}}{d\Omega} = |F_{00}|^2 \left(\frac{d\sigma}{d\Omega}\right)_{pt}$

$$F_{00} = \int |\Phi_0|^2 e^{i\mathbf{Q} \cdot \mathbf{r}} d\mathbf{r} \quad \mathbf{Q} \propto (\mathbf{K} - \mathbf{K}')$$

⇒ scattering of **compound nucleus** ≡

form factor × scattering of **pointlike nucleus**

Similarly for breakup: $\frac{d\sigma_{bu}}{dE d\Omega} = |F_{E,0}|^2 \left(\frac{d\sigma}{d\Omega}\right)_{pt}$

$$|F_{E,0}|^2 = \sum_{ljm} \left| \int \Phi_{ljm}(E) \Phi_0 e^{i\mathbf{Q} \cdot \mathbf{r}} d\mathbf{r} \right|^2$$

⇒ explains similarities in angular distributions

provides the idea for the **ratio** technique...

Ratio technique

$$d\sigma_{\text{bu}}/d\sigma_{\text{el}} = |F_{E,0}(\mathbf{Q})|^2 / |F_{00}(\mathbf{Q})|^2$$

- completely **independent** of reaction process
not affected by V_{cT}
- probes only projectile structure
- no need to normalise exp. cross sections

Test this using **DEA**

- without adiabatic approximation
- including V_{fT}

Alternative: $d\sigma_{\text{bu}}/d\sigma_{\text{sum}} = |F_{E,0}|^2$

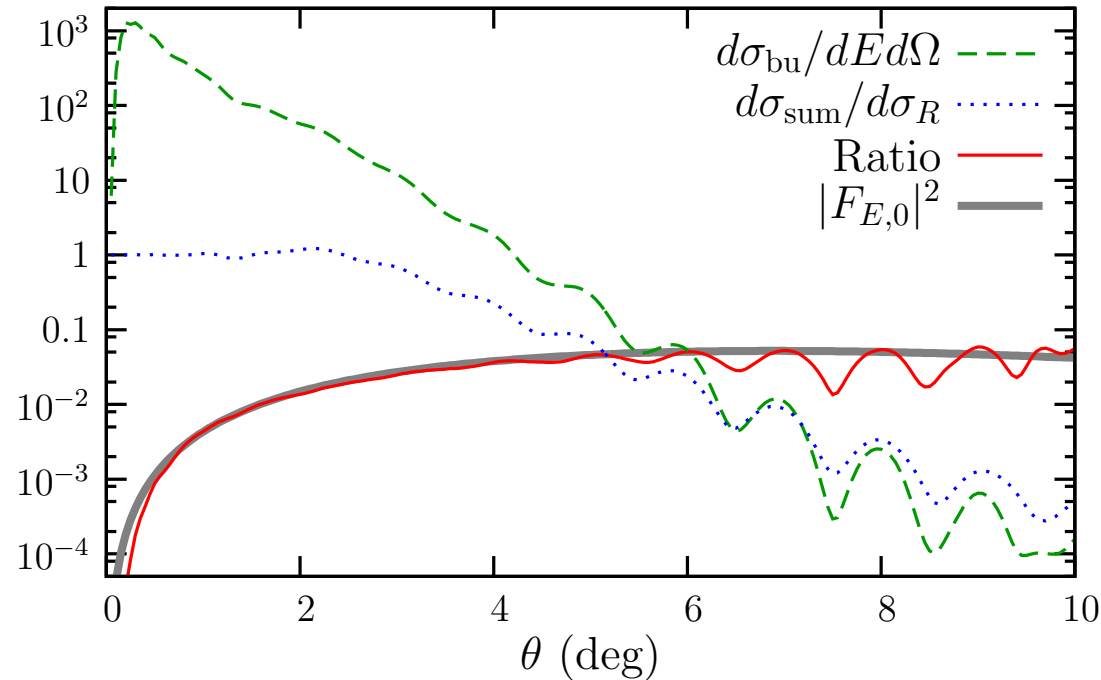
$$= \sum_{ljm} \left| \int \Phi_{ljm}(E) \Phi_0 e^{i\mathbf{Q} \cdot \mathbf{r}} d\mathbf{r} \right|^2$$

with $\frac{d\sigma_{\text{sum}}}{d\Omega} = \frac{d\sigma_{\text{el}}}{d\Omega} + \frac{d\sigma_{\text{inel}}}{d\Omega} + \int \frac{d\sigma_{\text{bu}}}{dE d\Omega} dE$

Testing with DEA

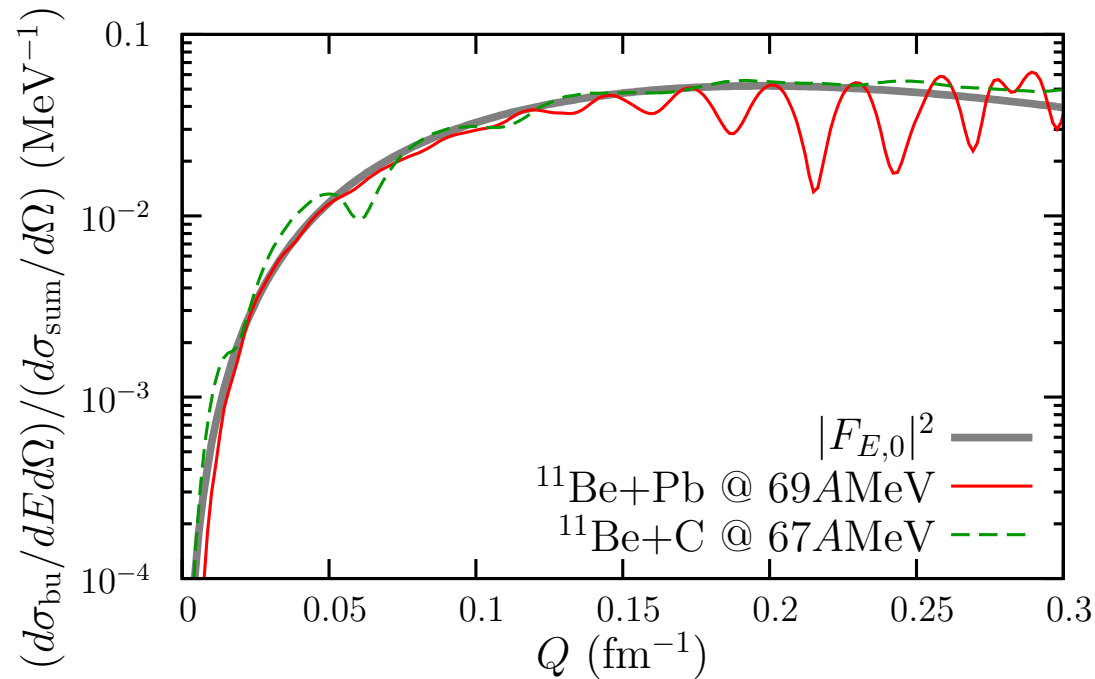
$^{11}\text{Be}+\text{Pb}$ @ 69 A MeV

[P. C., R. Johnson, F. Nunes, arXiv:1104.2228 (2011)]



- removes most of the angular dependence
 - REB predicts ratio = $|F_{E,0}|^2$
confirmed by DEA calculations
- ⇒ probe **structure** with little dependence on **reaction**

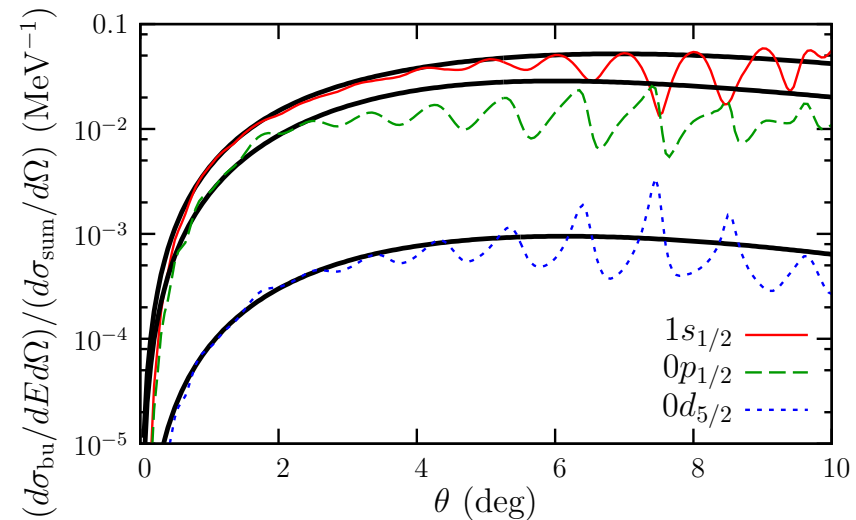
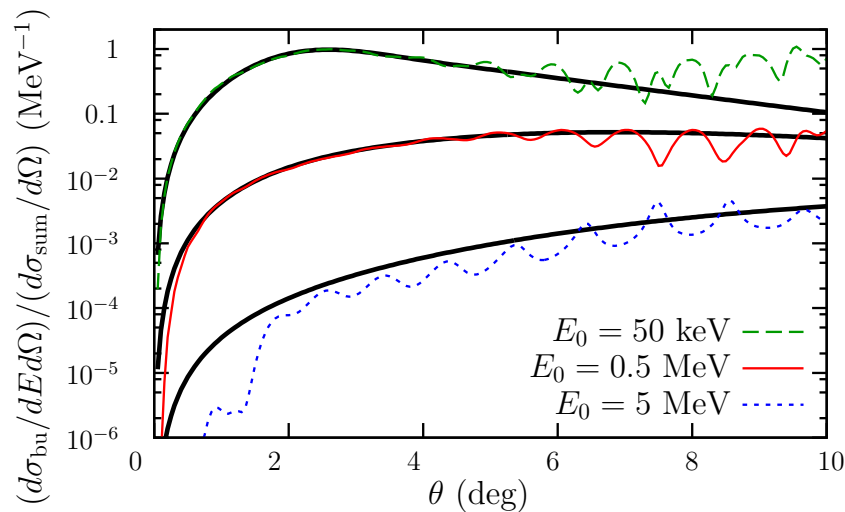
(In)sensitivity to reaction process



Similar for **Coulomb** and **nuclear** dominated collisions
⇒ nearly **independent** of the reaction process

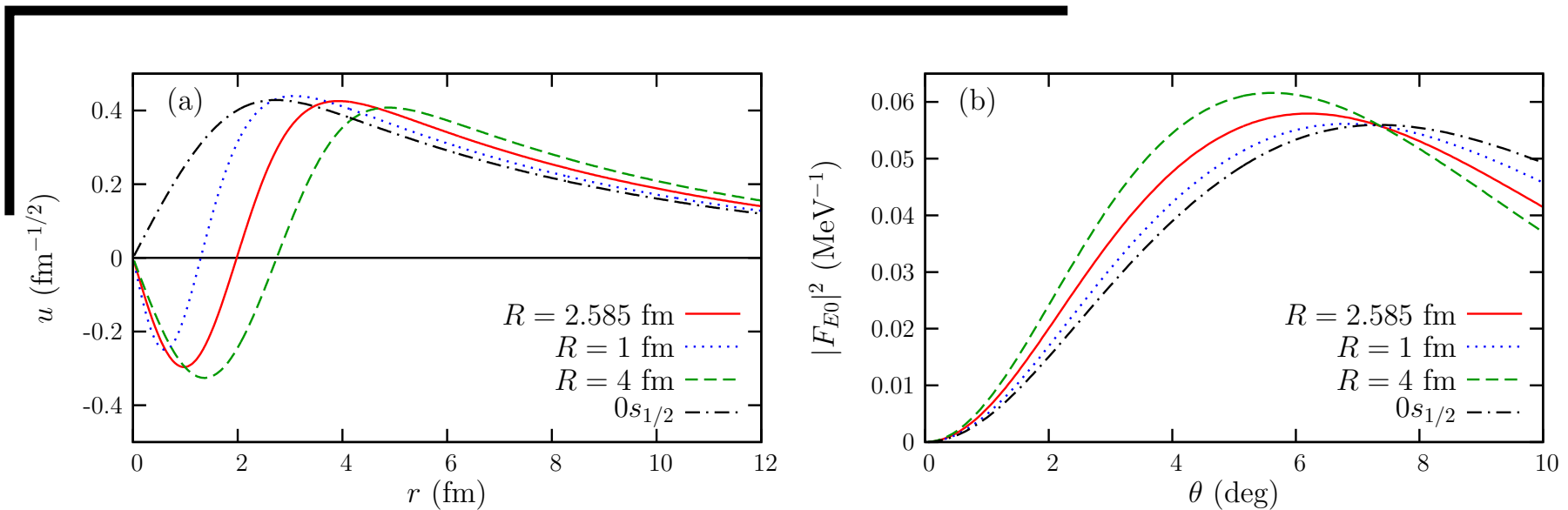
Sensitivity to projectile description

Study sensitivity to
binding energy bound-state orbital



- Sensitive to both binding energy and orbital in both shape and magnitude
- Works better for loosely-bound projectile (adiabatic approximation ?)

Sensitivity to radial wave function



- Changes in $|F_{E,0}|^2$ similar to those in u_{lj}
- Forward angles probe **asymptotics** of u_{lj}
- Large angles probe the **interior** of u_{lj}
may be difficult to distinguish experimentally

Summary of the ratio method

Breakup is a tool to study halo nuclei

Study hindered by reaction mechanism, V_{PT} ...

We propose a **ratio** of angular distributions

[P. C., R. Johnson, F. Nunes, arXiv:1104.2228 (2011)]

Removes most of the dependence on reaction process

Probes

- binding energy
- partial-wave configuration
- radial wave function

Open questions

- What happens for $SF < 1$?
- Is this valid for two-neutron haloes ?
- Can we extend this to proton haloes ?

Perspectives

Most reaction models built on
simple projectile description
using **phenomenological** V_{PT}

Ratio technique **removes** dependence on V_{PT}
 \Rightarrow gives access to finer information about projectile

Future: improve the description of projectile

- include configuration mixing
 - **XCDCC** [Summers *et al.* PRC 74, 014606 (2006)]
 - use **DEA**, as less expensive than CDCC
- three-body projectiles
 - CCE [Baye *et al.* PRC 79, 024607 (2009)]
 - **CDCC** [Rodríguez-Gallardo *et al.* PRC 80, 051601 ('09)]

Thanks...

- to you for your attention
- to my collaborators

Filomena Nunes



Daniel Baye



Mahir Hussein



Ron Johnson



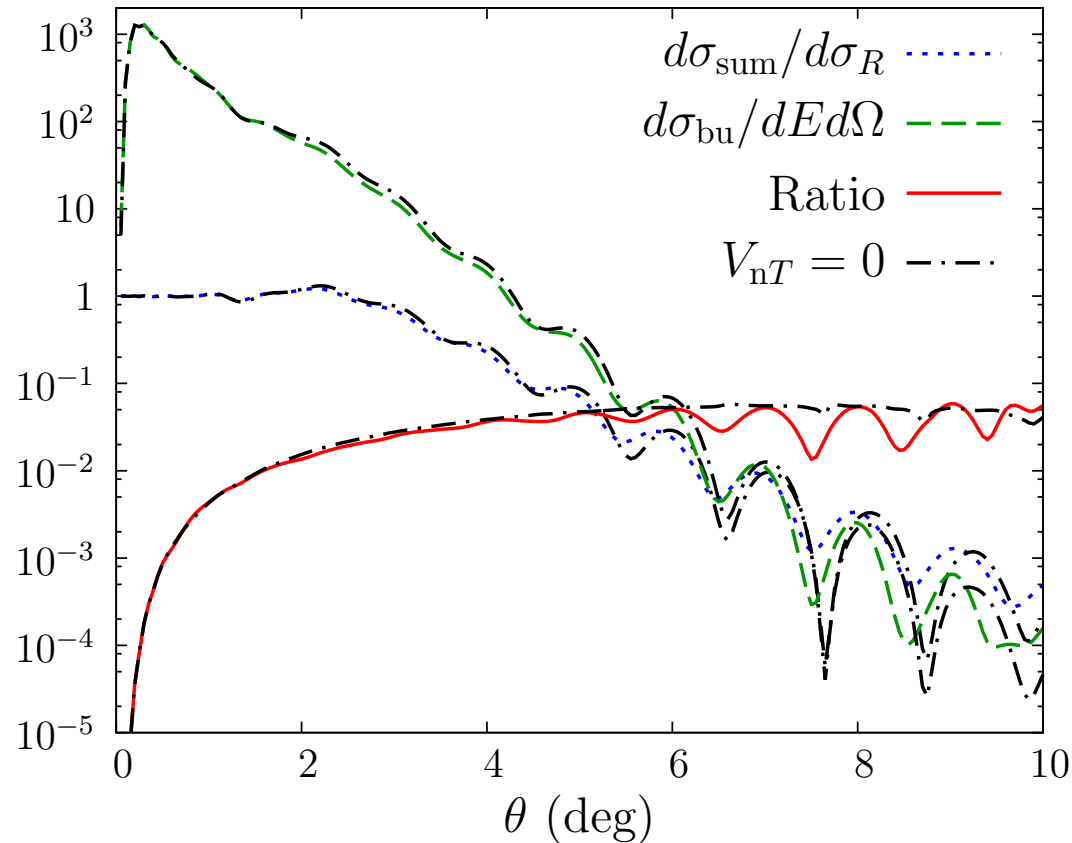
Henning Esbensen



Ian Thompson



Role of V_{nT}



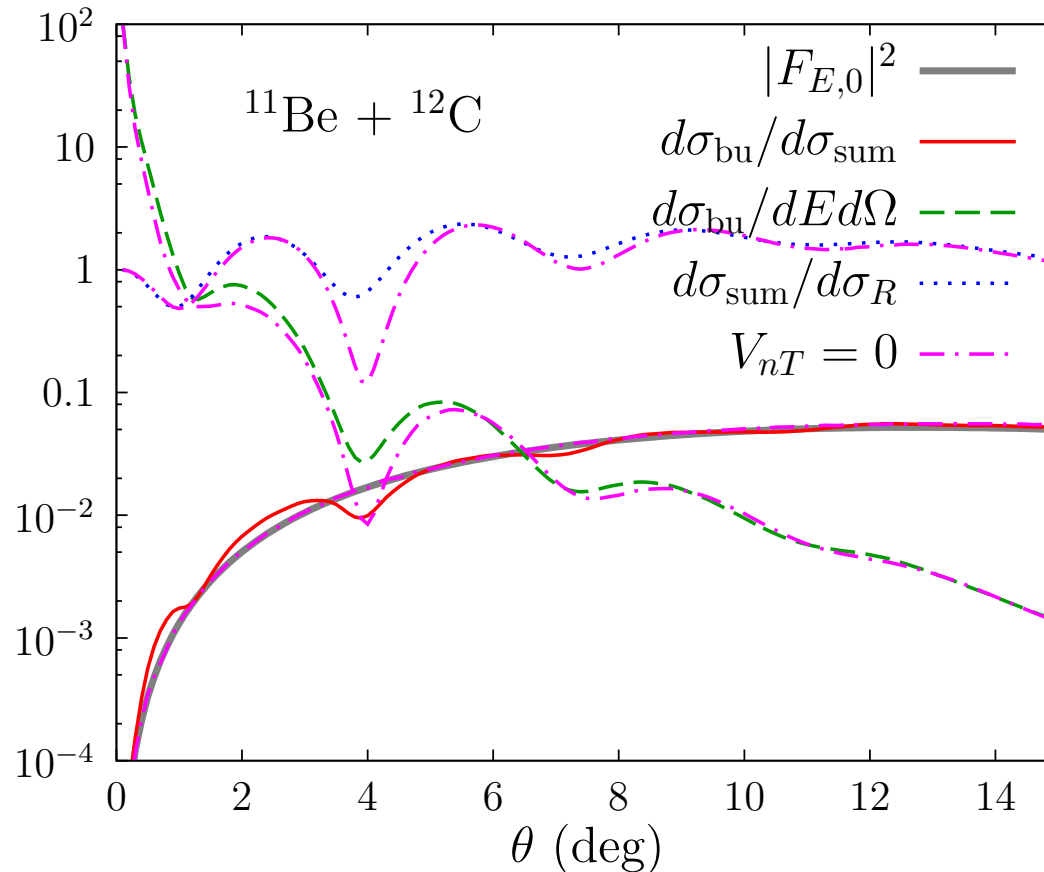
Large-angle oscillations due to V_{nT}

V_{nT} shifts oscillations [R. Johnson *et al.* PRL 79, 2771 (97)]

shift vary with excitation energy E

V_{nT} known \Rightarrow well under control

Role of V_{nT} on C



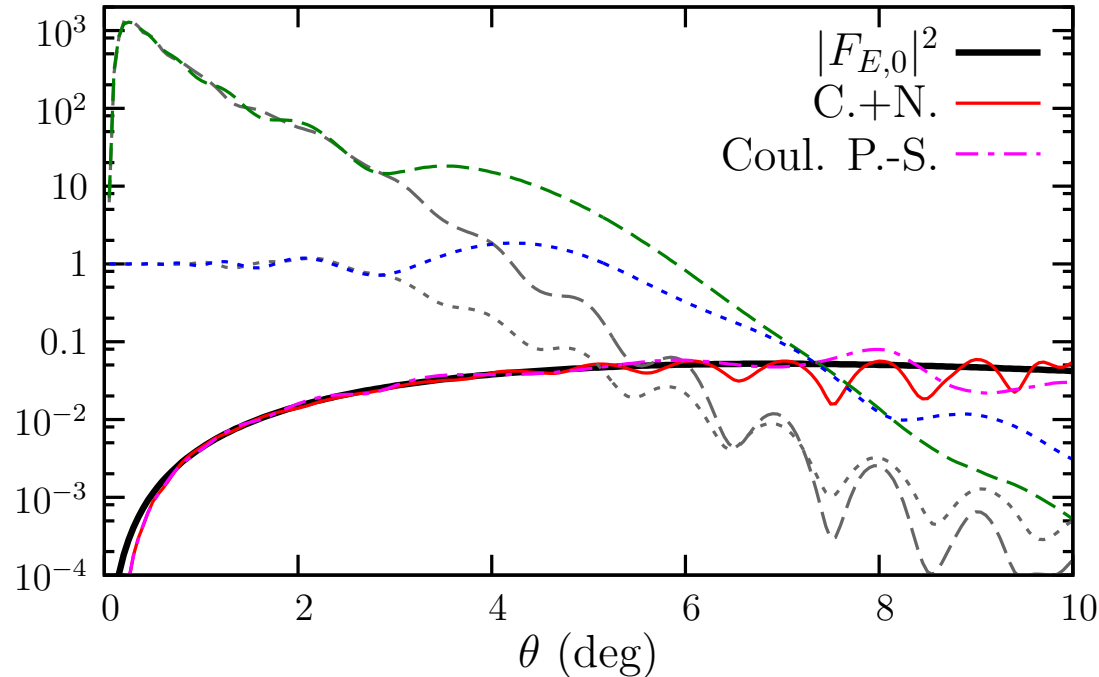
Oscillations at $2-4^\circ$ due to V_{nT}

V_{nT} shifts oscillations [R. Johnson *et al.* PRL 79, 2771 (97)]

shift vary with excitation energy E

V_{nT} known \Rightarrow well under control

Inensitivity to V_{PT} (1)

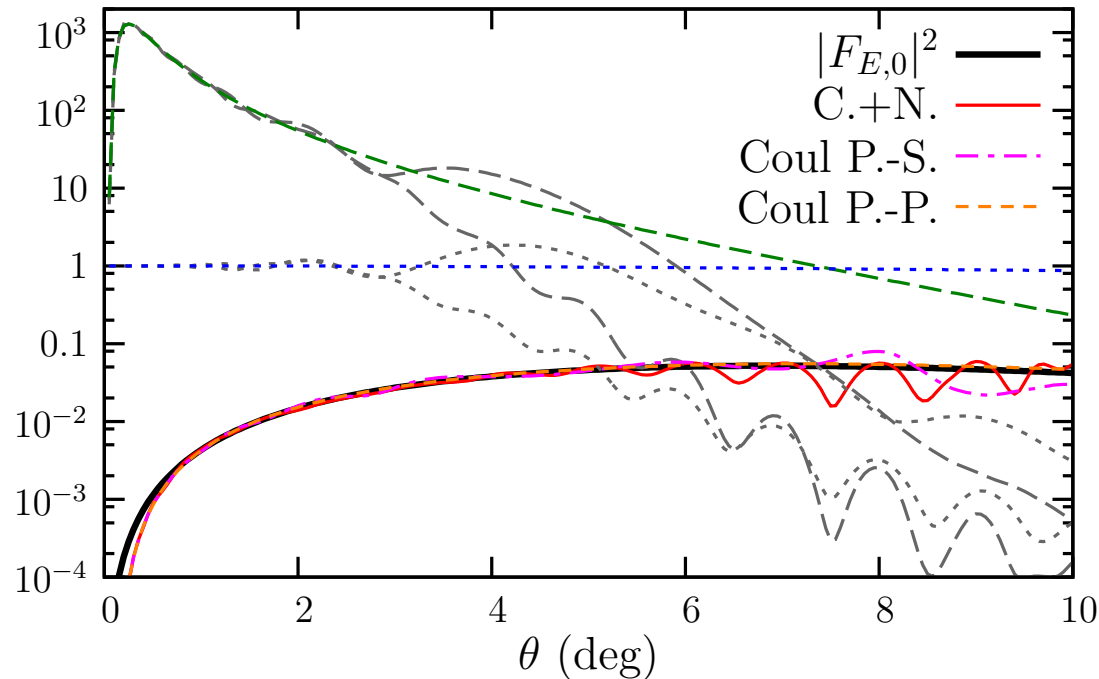


Without nuclear part of V_{PT} , **different** distributions:

- different Coulomb **rainbow**
- different **oscillations**

However, **same ratio**

Insenitivity to V_{PT} (2)

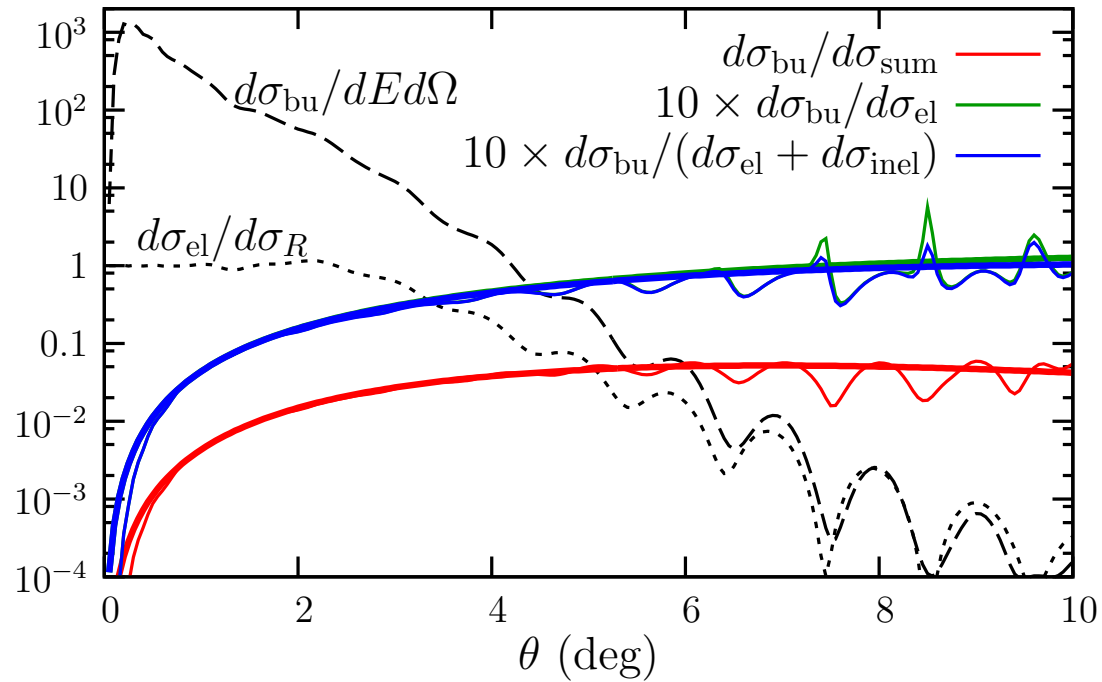


With $V_{PT} = \frac{Z_c Z_T e^2}{R_{cT}}$, very **different** distributions:

- No Coulomb **rainbow**
- No **oscillations**

However, **same ratio**

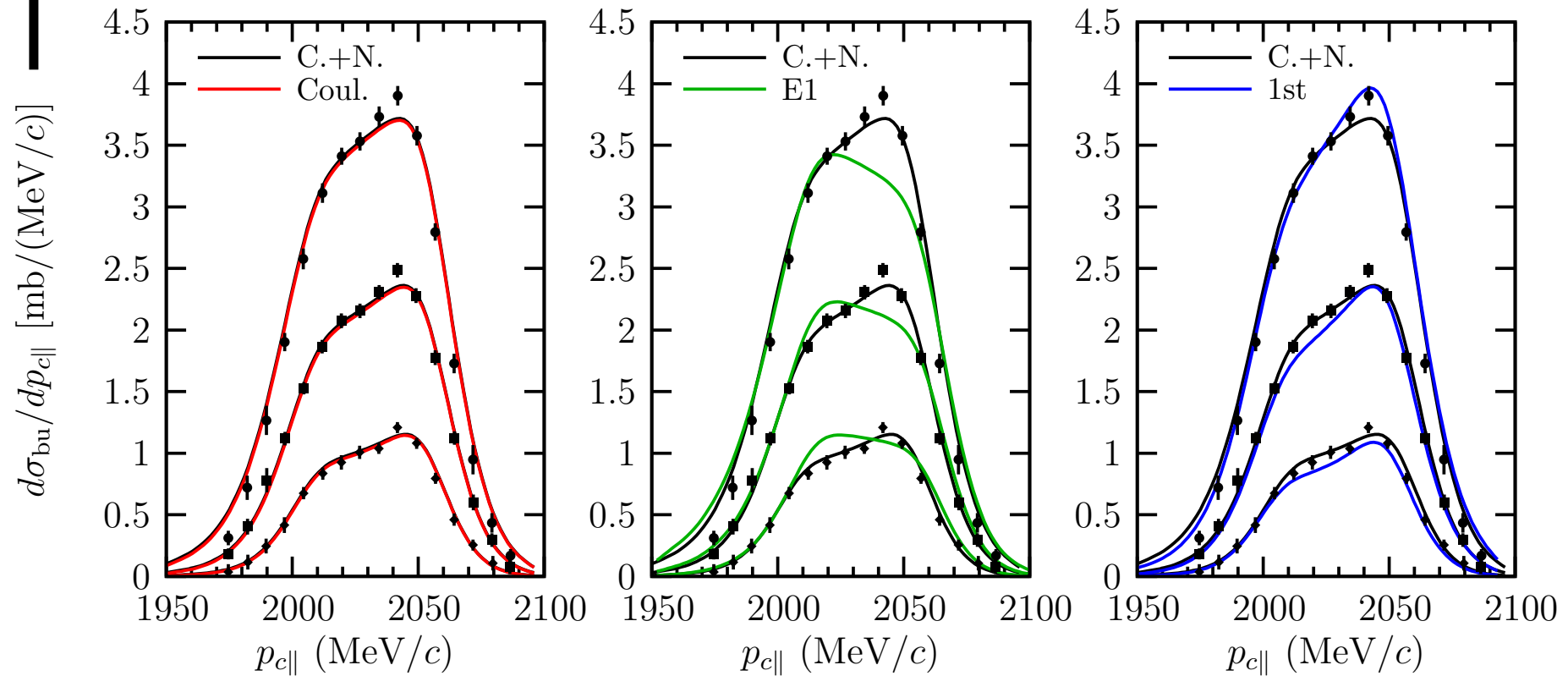
Other ratios



- $d\sigma_{bu}/d\sigma_{sum}$
- $d\sigma_{bu}/d\sigma_{el}$
- $d\sigma_{bu}/(d\sigma_{el} + d\sigma_{inel})$

Analysis

$^8\text{B} + \text{Pb} @ 44 \text{ AMeV (MSU)}$ [Davids PRL 81, 2209 (01)]



Nuclear interaction
negligible
at forward angles

**Significant E1-E2
interference**
(asymmetry)

First-order:
more asymmetric
⇒ **higher-order**