

The timelike Compton scattering at high and medium energies

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in collaboration with

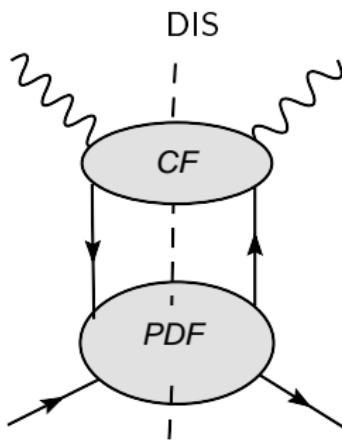
B. Pire (CPhT, Palaiseau) and J. Wagner (NCBJ, Warsaw)

Phys.Rev.D79:014010 (2009), Phys.Rev.D83:034009 (2011)

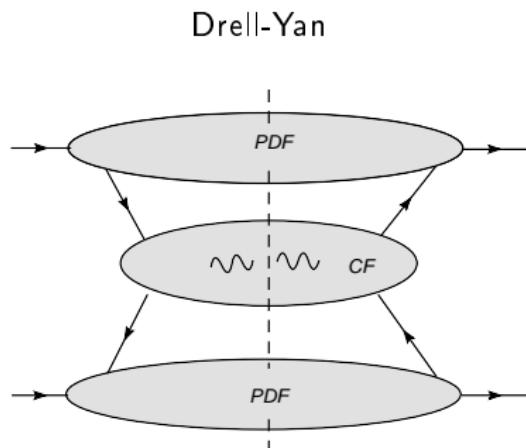
Frontiers in QCD (INT-11-3), September 19 - November 18, 2011

Motivation

In 80's, lot of studies of **INCLUSIVE**:



versus



- parton model from QCD factorization
- $\text{CF}_{\text{DIS}}(q^2 < 0)$ with **SPACELIKE** γ^* versus
 $\text{CF}_{\text{DY}}(q^2 > 0)$ with **TIMELIKE** γ^*
- at NLO order: 1-loop corrections to $\text{CF}_{\text{DY}}(q^2 > 0)$ are very big
 necessity of resummation to all orders before comparison with data

Motivation

Now: intensive studies of **EXCLUSIVE** processes

- Deeply Virtual Compton Scattering (**DVCS**) with $q^2 < 0$, i.e. with **SPACELIKE** γ^*
 - high energies: DESY: H1 and ZEUS; EIC
 - medium energies: HERMES, JLAB
- within ongoing, accepted and planned Drell-Yan (**DY**) programs with $q^2 > 0$, i.e. with **TIMELIKE** γ^*
 - high energies: ultraperipheral scattering at LHC and RHIC, COMPASS
 - medium energies: HERMES, JLAB@12GeV, GSI-FAIR

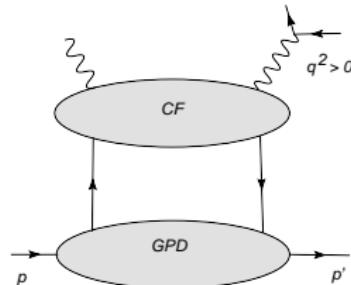
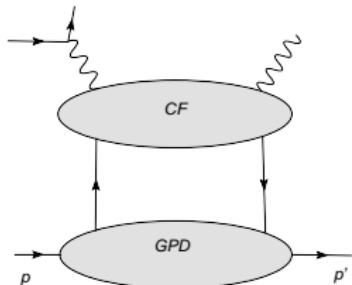
Motivation

Two phenomenologically important **EXCLUSIVE** processes:

DVCS

versus

Timelike Compton Scattering (TCS)

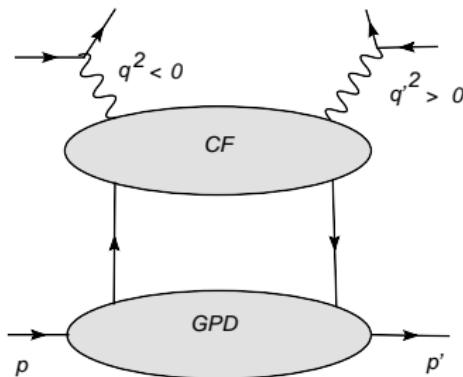


- QCD factorization with **Generalized Parton Distributions (GPDs)**
- $\text{CF}_{DVCS}(q^2 < 0)$ known at NLO since 98 Mankiewicz et al, Belitsky et al
- $\text{CF}_{TCS}(q^2 > 0)$ at NLO derived in 2011 B. Pire et al Phys. Rev. D83
- resummation of large contributions in **EXCLUSIVE** processes in progress

Motivation

Additional phenomenologically important EXCLUSIVE process:
Double Deeply Virtual Compton Scattering (DDVCS)

Guidal et al Phys. Rev. Lett. 90 (2003)



- analysis started by HERMES, soon in JLab
 - $\text{CF}_{DDVCS}(q^2 > 0)$ at NLO derived in 2011 B. Pire et al Phys. Rev. D83

Kinematics of TCS

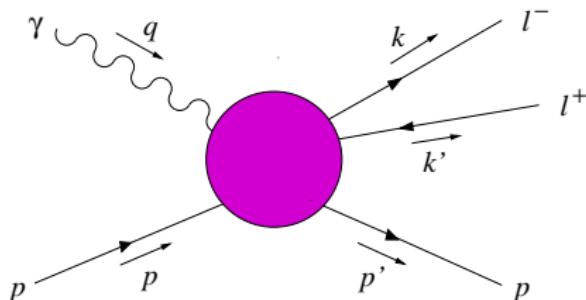


Figure: Real photon-proton scattering into a lepton pair and a proton.

$$\gamma(q)N(p) \rightarrow \gamma^*(q')N(p') \rightarrow l^-(k)l^+(k')N(p')$$

at small $t = (p' - p)^2$ and large *timelike* virtuality $(k + k')^2 = q'^2 = Q'^2$ of the final state dilepton

Experiments:

- high energies: at LHC, RHIC small- x physics
as ultraperipheral scattering (with B-W real γ 's)
- lower energies: JLab

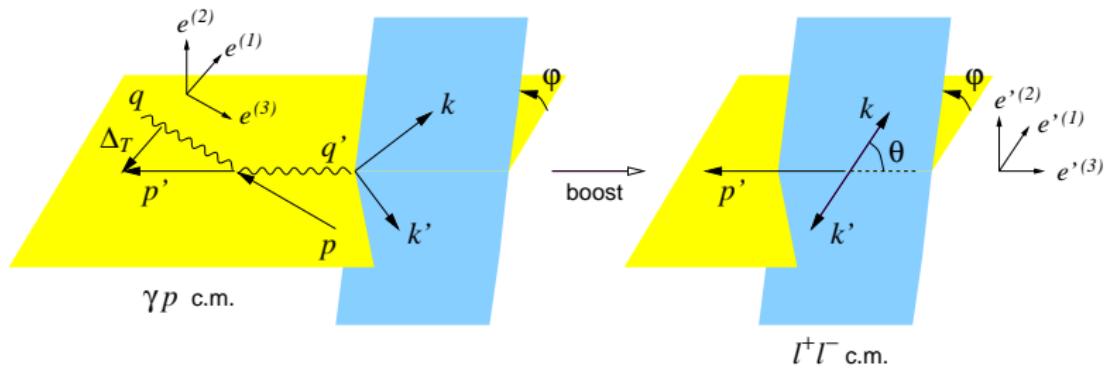


Figure: Kinematical variables and coordinate axes in the γp and $\ell^+ \ell^-$ c.m. frames.

The Bethe-Heitler contribution

purely electromagnetic contribution

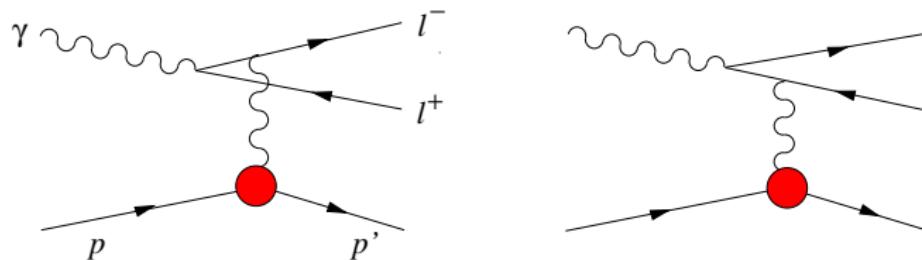


Figure: The Feynman diagrams for the Bethe-Heitler amplitude.

$$\frac{d\sigma_{BH}}{dQ'^2 dt d(\cos \theta) d\varphi} \approx \frac{\alpha_{em}^3}{2\pi s^2} \frac{1}{-t} \frac{1 + \cos^2 \theta}{\sin^2 \theta} \left[\left(F_1^2 - \frac{t}{4M^2} F_2^2 \right) \frac{2}{\tau^2} \frac{\Delta_T^2}{-t} + (F_1 + F_2)^2 \right]$$

For small θ BH contribution becomes very large

The Compton contribution

Born contribution

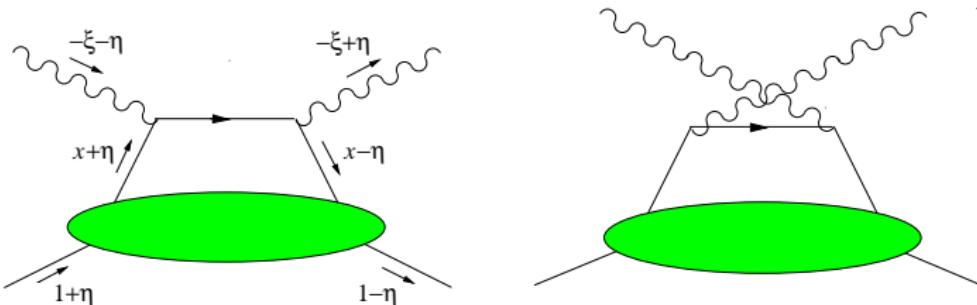


Figure: Handbag diagrams for the Compton process in the scaling limit. The plus-momentum fractions x, ξ, η refer to the average proton momentum $\frac{1}{2}(p + p')$.

$$x = \frac{(k + k')^+}{(p + p')^+}, \quad \xi \approx -\frac{(q + q')^+}{(p + p')^+}, \quad \eta \approx \frac{(p - p')^+}{(p + p')^+}.$$

To leading-twist accuracy one has $\xi = -\eta = -\tau/(2 - \tau)$, where $\tau = Q'^2/s$ is Björken variable.

Quark (unpolarised) GPDs:

$$\begin{aligned} F^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle|_{z^+=0, \mathbf{z}=0} \\ &= \frac{1}{2P^+} \left[H^q(x, \eta, t) \bar{u}(p') \gamma^+ u(p) + E^q(x, \eta, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right] \end{aligned}$$

Gluon (unpolarized) GPDs:

$$\begin{aligned} F^g &= \frac{1}{P^+} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | G^{+\mu}(-\frac{1}{2}z) G_\mu^+(\frac{1}{2}z) | p \rangle|_{z^+=0, \mathbf{z}=0} \\ &= \frac{1}{2P^+} \left[H^g(x, \eta, t) \bar{u}(p') \gamma^+ u(p) + E^g(x, \eta, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right] \end{aligned}$$

the Compton form factors:

$$\mathcal{H}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left(\frac{1}{\xi - x - i\epsilon} - \frac{1}{\xi + x - i\epsilon} \right) H^q(x, \eta, t),$$

$$\mathcal{E}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left(\frac{1}{\xi - x - i\epsilon} - \frac{1}{\xi + x - i\epsilon} \right) E^q(x, \eta, t),$$

$$\tilde{\mathcal{H}}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left(\frac{1}{\xi - x - i\epsilon} + \frac{1}{\xi + x - i\epsilon} \right) \tilde{H}^q(x, \eta, t),$$

$$\tilde{\mathcal{E}}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left(\frac{1}{\xi - x - i\epsilon} + \frac{1}{\xi + x - i\epsilon} \right) \cdot \tilde{E}^q(x, \eta, t)$$

For example:

$$M^{\lambda' \lambda \gamma^*, \lambda \lambda \gamma}$$

$$M^{+-,+-} \Big|_{TCS} =$$

$$\sqrt{1 - \eta^2} (\mathcal{H}_1(-\eta, \eta, t) + \tilde{\mathcal{H}}_1(-\eta, \eta, t) - \frac{\eta^2}{1 - \eta^2} (\mathcal{E}_1(-\eta, \eta, t) + \tilde{\mathcal{E}}_1(-\eta, \eta, t)))$$

Modelizing GPDs for Ultraperipheral Collisions (UPC)

small- x

Factorized ansatz for t -dependence:

$$\begin{aligned} H^u(x, \eta, t) &= h^u(x, \eta) \frac{1}{2} F_1^u(t) \\ H^d(x, \eta, t) &= h^d(x, \eta) F_1^d(t) \\ H^s(x, \eta, t) &= h^s(x, \eta) F_D(t) \end{aligned}$$

Double distribution ansatz for h^q without any D-term:

$$\begin{aligned} h^q(x, \eta) &= \int_0^1 dx' \int_{-1+x'}^{1-x'} dy' \\ &\quad \left[\delta(x - x' - \eta y') q(x') - \delta(x + x' - \eta y') \bar{q}(x') \right] \pi(x', y') \\ \pi(x', y') &= \frac{3}{4} \frac{(1-x')^2 - y'^2}{(1-x')^3} \end{aligned}$$

For the unpolarized distributions $q(x)$ and $\bar{q}(x)$ we take NLO($\overline{\text{MS}}$) GRV GJR 2008 parametrization.

They have strong dependence of the factorization scale choice for small x :

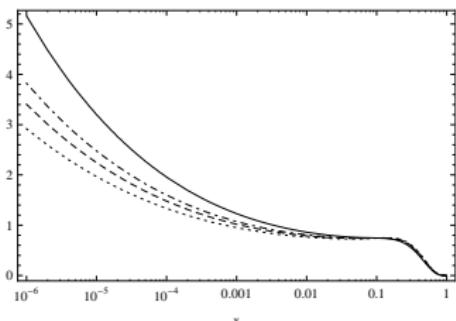


Figure: The NLO($\overline{\text{MS}}$) GRV GJR 2008 parametrization of $u(x) + \bar{u}(x)$ for different factorization scales $\mu_F^2 = 4$ (dotted), 5 (dashed), 6 (dash-dotted), 10 (solid) GeV^2 .

This results in the strong dependence of h^q for small values of η :

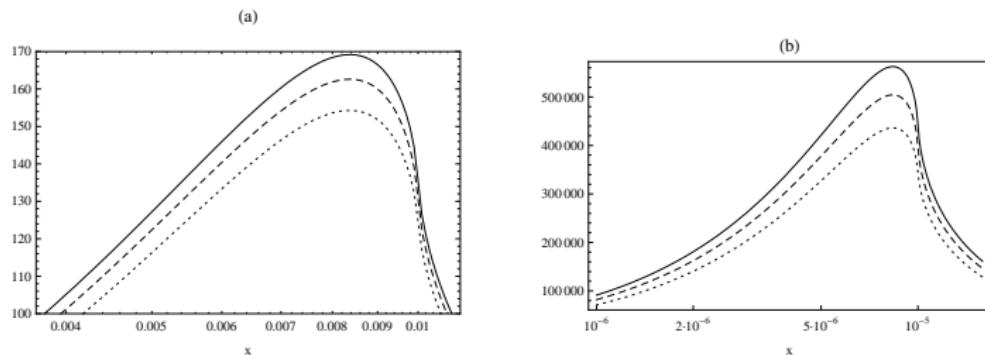


Figure: $h_+^u(x, \eta) = h^u(x, \eta) - h^u(-x, \eta)$ for $\eta = 10^{-2}$ (a) and for $\eta = 10^{-5}$ (b) for different factorization scales $\mu_F^2 = 4$ (dotted), 5 (dashed), 6 (solid) GeV^2 .

B-H cross section at UPC

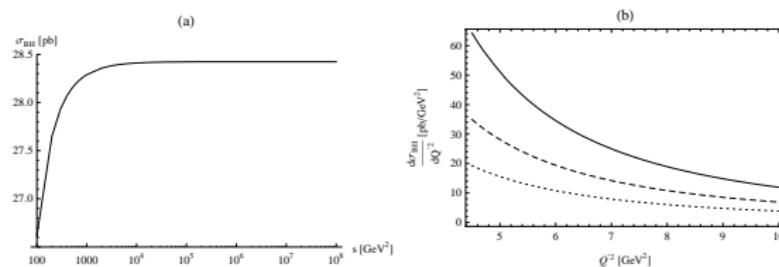


Figure: (a) The BH cross section integrated over $\theta \in [\pi/4, 3\pi/4]$, $\varphi \in [0, 2\pi]$, $Q'^2 \in [4.5, 5.5] \text{ GeV}^2$, $|t| \in [0.05, 0.25] \text{ GeV}^2$, as a function of γp c.m. energy squared s . (b) The BH cross section integrated over $\varphi \in [0, 2\pi]$, $|t| \in [0.05, 0.25] \text{ GeV}^2$, and various ranges of θ : $[\pi/3, 2\pi/3]$ (dotted), $[\pi/4, 3\pi/4]$ (dashed) and $[\pi/6, 5\pi/6]$ (solid), as a function of Q'^2 for $s = 10^5 \text{ GeV}^2$

TCS cross section at UPC

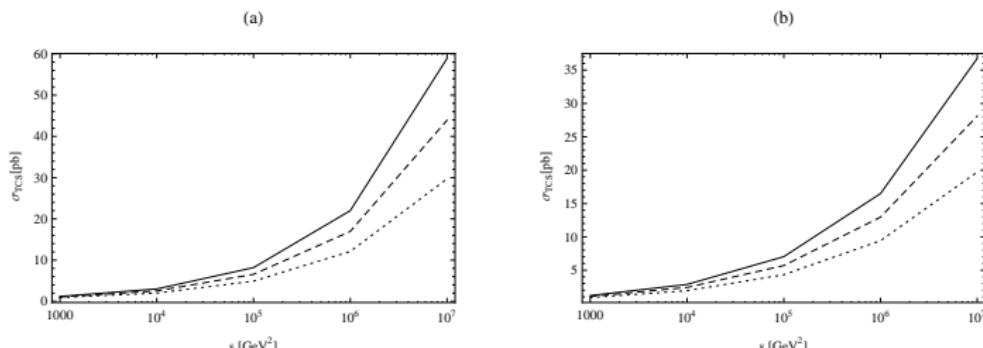


Figure: σ_{TCS} as a function of γp c.m. energy squared s , for GRVGJR2008 LO (a) and NLO (b) parametrizations, for different factorization scales $\mu_F^2 = 4$ (dotted), 5 (dashed), 6 (solid) GeV^2 .

For very high energies σ_{TCS} calculated with $\mu_F^2 = 6 \text{ GeV}^2$ is much bigger than with $\mu_F^2 = 4 \text{ GeV}^2$. Also predictions obtained using LO and NLO GRVGJR2008 PDFs differ significantly.

The interference cross section at UPC

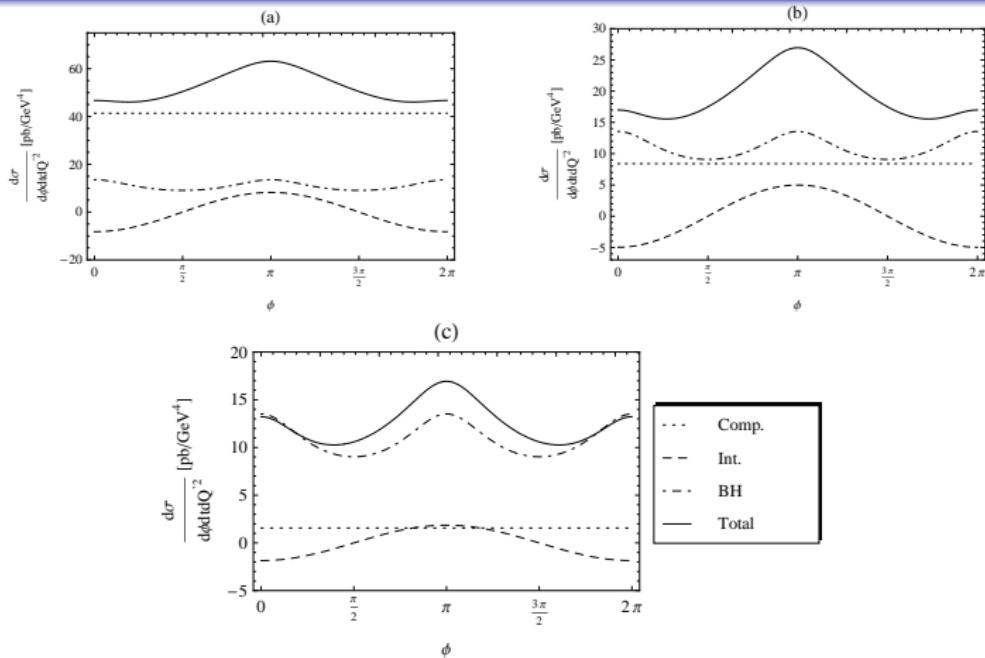


Figure: The differential cross sections (solid lines) for $t = -0.2 \text{ GeV}^2$, $Q'^2 = 5 \text{ GeV}^2$ and integrated over $\theta = [\pi/4, 3\pi/4]$, as a function of φ , for $s = 10^7 \text{ GeV}^2$ (a), $s = 10^5 \text{ GeV}^2$ (b), $s = 10^3 \text{ GeV}^2$ (c) with $\mu_F^2 = 5 \text{ GeV}^2$. We also display the Compton (dotted), Bethe-Heitler (dash-dotted) and Interference (dashed) contributions.

Rate estimates for UPC

$$\sigma_{pp} = 2 \int \frac{dn(k)}{dk} \sigma_{\gamma p}(k) dk$$

$\sigma_{\gamma p}(k)$ is the cross section for the $\gamma p \rightarrow pl^+l^-$ process and k is the γ 's energy.

$\frac{dn(k)}{dk}$ is an equivalent photon flux

$$\frac{dn(k)}{dk} = \frac{\alpha}{2\pi k} \left[1 + \left(1 - \frac{2k}{\sqrt{s_{pp}}} \right)^2 \right] \left(\ln A - \frac{11}{6} + \frac{3}{A} - \frac{3}{2A^2} + \frac{1}{3A^3} \right)$$

$A = 1 + \frac{0.71 \text{ GeV}^2}{Q_{min}^2}$, $Q_{min}^2 \approx \frac{4M_p^2 k^2}{s_{pp}}$ is the minimal $-t$

s_{pp} is the proton-proton energy squared ($\sqrt{s_{pp}} = 14 \text{ TeV}$): $s \approx 2\sqrt{s_{pp}}k$

The pure Bethe - Heitler contribution to σ_{pp} , integrated over $\theta = [\pi/4, 3\pi/4]$, $\phi = [0, 2\pi]$, $t = [-0.05 \text{ GeV}^2, -0.25 \text{ GeV}^2]$, $Q'^2 = [4.5 \text{ GeV}^2, 5.5 \text{ GeV}^2]$, and photon energies $k = [20, 900] \text{ GeV}$ gives:

$$\sigma_{pp}^{BH} = 2.9 \text{ pb} .$$

The Compton contribution (calculated with NLO GRVGJR2008 PDFs, and $\mu_F^2 = 5 \text{ GeV}^2$) gives:

$$\sigma_{pp}^{TCS} = 1.9 \text{ pb} .$$

LHC: rate $\sim 10^5$ events/year with nominal luminosity ($10^{34} \text{ cm}^{-2} \text{ s}^{-1}$)

TCS at lower energies

Berger, Diehl, Pire, 2002

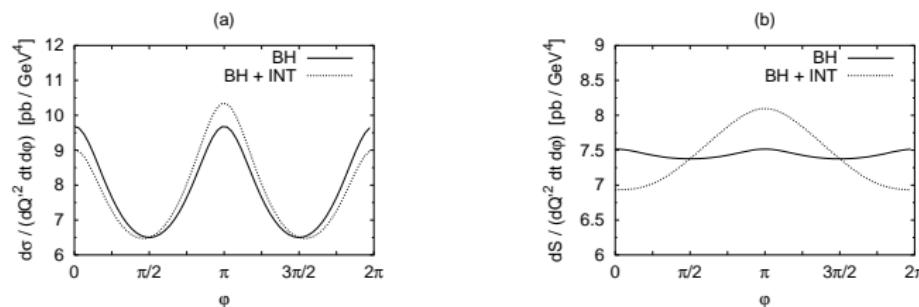


Figure:

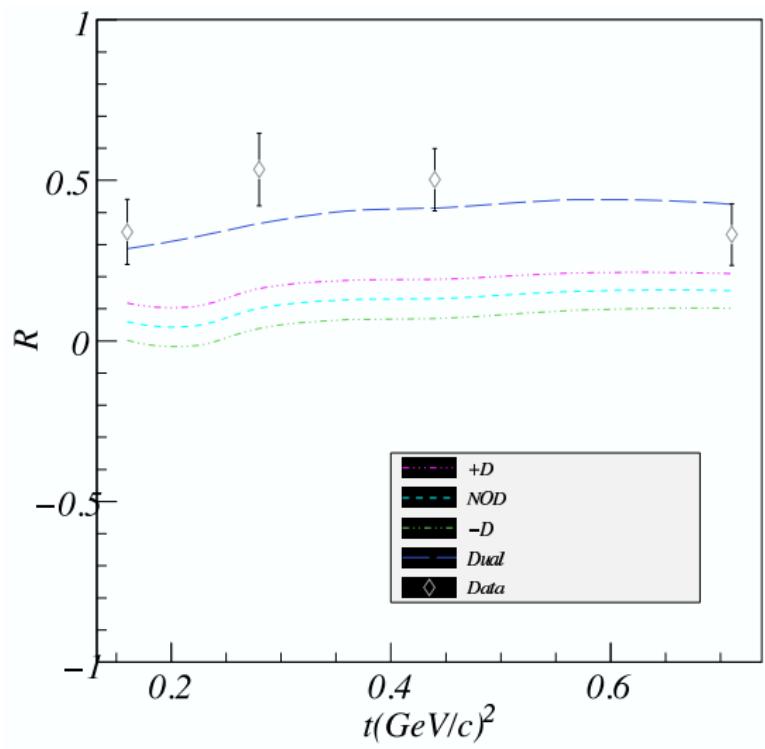
B-H dominant; TCS dominated by quark GPDs

Charge asymmetry \sim interference of B-H and TCS

TCS at lower energies

NLO corrections necessary:

$$R = \frac{\int d\phi \cos(\phi) d\sigma}{\int d\phi d\sigma}$$



NLO corrections

$$\gamma^*(q_{in})N \rightarrow \gamma^*(q_{out})N'$$

DVCS versus TCS versus DDVCS:

- DVCS: $q_{in}^2 < 0, q_{out}^2 = 0$
- TCS: $q_{in}^2 = 0, q_{out}^2 > 0$
- DDVCS: $q_{in}^2 < 0, q_{out}^2 > 0$

Why NLO corrections of TCS are interested:

- at high energies gluons important, they enter at NLO
- DIS versus Drell-Yan: big K-factors $\log \frac{-Q^2}{\mu_F^2} \rightarrow \log \frac{Q^2}{\mu_F^2} \pm i\pi$
- dependence (strong ?? or weak ??) on the factorization scale μ_F
- DVCS_{unphysicalregion} $\xi \rightarrow \xi - i\varepsilon$ DVCS_{physicalregion}

in TCS and DDVCS it is not enough

Kinematics in Ji's (symmetric) notation

incoming photon $q_{in} = (q - \xi p)$

incoming proton $P = (1 + \xi)p$

outgoing photon ($q_{out} = q + \xi p$)

outgoing proton $P' = (1 - \xi)p$

$$p = p^+(1, 0, 0, 1),$$

$$n = \frac{1}{2p^+}(1, 0, 0, -1),$$

$$q = -x_B p + \frac{Q^2}{2x_B} n$$

so: $pn = 1$, $s = (p + q)^2 = \frac{1-x_B}{x_B} Q^2$ and $x_B = \frac{Q^2}{s+Q^2}$

$$q_{in}^2 = -Q^2 \left(1 + \frac{\xi}{x_B}\right) \quad q_{out}^2 = -Q^2 \left(1 - \frac{\xi}{x_B}\right)$$

DVCS: $x_B = \xi$, $Q^2 > 0$

TCS: $x_B = -\xi$, $Q^2 = -Q'^2 < 0$

DDVCS: $0 < x_B < \xi$ and $Q^2 > 0$ OR $0 > x_B > -\xi$ and $Q^2 < 0$

Amplitude:

$$\mathcal{A}^{\mu\nu} = g_T^{\mu\nu} \int_{-1}^1 dx \left[\sum_q^{n_F} T^q(x) F^q(x) + T^g(x) F^g(x) \right]$$

where renormalized coefficient functions are given by:

$$T^q = C_0^q + C_1^q + \frac{1}{2} \ln \left(\frac{|Q^2|}{\mu_F^2} \right) \cdot C_{coll}^q ,$$

$$T^g = C_1^g + \frac{1}{2} \ln \left(\frac{|Q^2|}{\mu_F^2} \right) \cdot C_{coll}^g$$

and the GPDs are

$$F^q(x, \xi) = \frac{1}{2} \int \frac{d\lambda}{2\pi} e^{-i\lambda x} \left\langle P' \left| \bar{\psi}_q \left(\frac{\lambda}{2} n \right) \gamma^\mu \psi_q \left(-\frac{\lambda}{2} n \right) \right| P \right\rangle n_\mu ,$$

$$F^g(x, \xi) = -\frac{1}{2x} \int \frac{d\lambda}{2\pi} e^{-i\lambda x} \left\langle P' \left| G_a^{\mu\alpha} \left(\frac{\lambda}{2} n \right) G_{a\alpha}^\nu \left(-\frac{\lambda}{2} n \right) \right| P \right\rangle n_\mu n_\nu$$

Diagrams

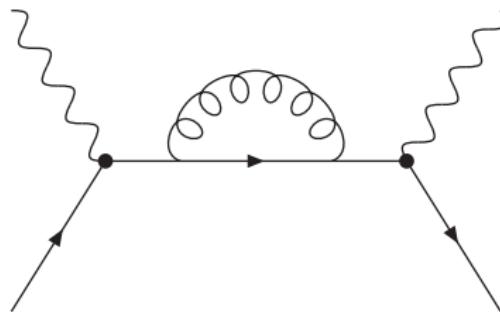


Figure: Self energy correction to $q\gamma \rightarrow q\gamma$ scattering amplitude

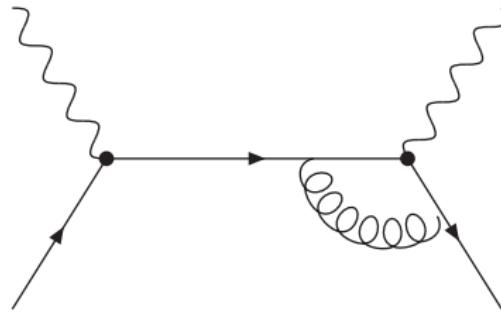


Figure: Right vertex correction to $q\gamma \rightarrow q\gamma$ scattering amplitude

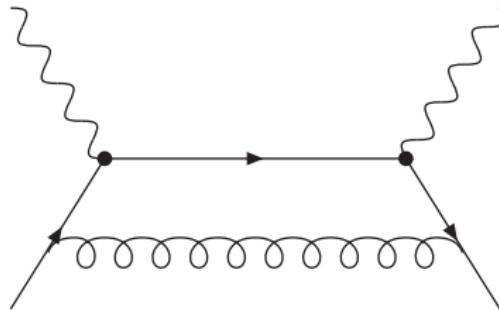


Figure: Box diagram correction to $q\gamma \rightarrow q\gamma$ scattering amplitude

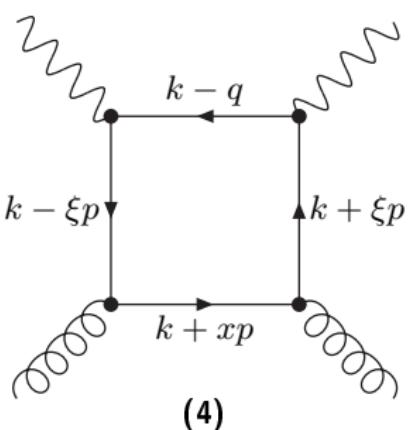
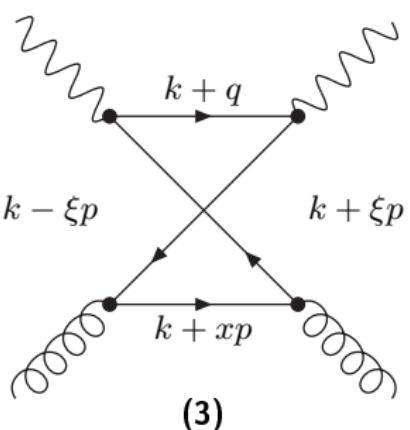
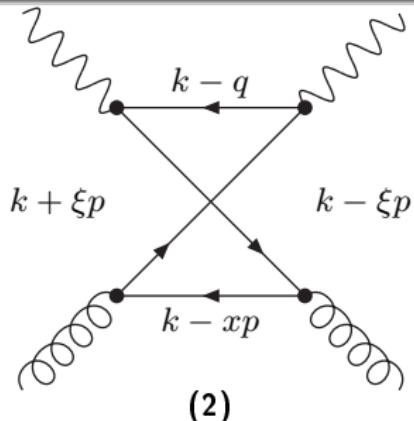
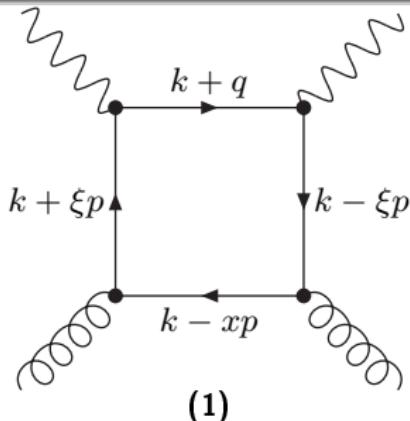


Figure: First group of diagrams describing $\gamma g \rightarrow \gamma g$ scattering.

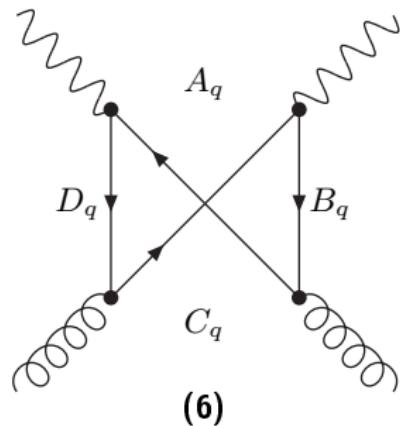
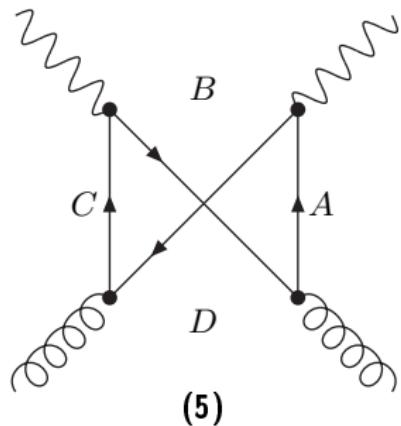


Figure: Second group of diagrams describing $\gamma g \rightarrow \gamma g$ scattering.

Results: TCS + DVCS + DDVCS

TCS:

Quark coefficient functions:

$$\begin{aligned} C_0^q &= e_q^2 \left(\frac{1}{x - \xi - i\varepsilon} + \frac{1}{x + \xi + i\varepsilon} \right), \\ C_1^q &= \frac{e_q^2 \alpha_S C_F}{4\pi} \\ &\left\{ \frac{1}{x - \xi - i\varepsilon} \left[-9 + 3 \log(-1 + \frac{x}{\xi} - i\varepsilon) - 6 \frac{\xi}{x + \xi} \log(-1 + \frac{x}{\xi} - i\varepsilon) + 6 \frac{\xi}{x + \xi} \log(-2 - i\varepsilon) \right. \right. \\ &\quad \left. \left. + \log^2(-1 + \frac{x}{\xi} - i\varepsilon) - \log^2(-2 - i\varepsilon) \right] \right. \\ &\quad \left. + \frac{1}{x + \xi + i\varepsilon} \left[-9 + 3 \log(-1 - \frac{x}{\xi} - i\varepsilon) + 6 \frac{\xi}{x - \xi} \log(-1 - \frac{x}{\xi} - i\varepsilon) - 6 \frac{\xi}{x - \xi} \log(-2 - i\varepsilon) \right. \right. \\ &\quad \left. \left. + \log^2(-1 - \frac{x}{\xi} - i\varepsilon) - \log^2(-2 - i\varepsilon) \right] \right\}, \\ C_{coll}^q &= \frac{e_q^2 \alpha_S C_F}{4\pi} \left\{ \frac{1}{x - \xi - i\varepsilon} \left[6 + 4 \log(-1 + \frac{x}{\xi} - i\varepsilon) - 4 \log(-2 - i\varepsilon) \right] \right. \\ &\quad \left. + \frac{1}{x + \xi + i\varepsilon} \left[6 + 4 \log(-1 - \frac{x}{\xi} - i\varepsilon) - 4 \log(-2 - i\varepsilon) \right] \right\} \end{aligned}$$

Gluon coefficient functions:

$$\begin{aligned}
 C_{coll}^g &= \frac{\left(\sum_q e_q^2\right) \alpha_S T_F}{4\pi} \frac{8x}{(x + \xi + i\varepsilon)(x - \xi - i\varepsilon)} . \\
 &\left[\frac{x - \xi}{x + \xi} \log \left(-1 + \frac{x}{\xi} - i\varepsilon \right) + \frac{x + \xi}{x - \xi} \log \left(-1 - \frac{x}{\xi} - i\varepsilon \right) - 2 \frac{x^2 + \xi^2}{x^2 - \xi^2} \log(-2 - i\varepsilon) \right] , \\
 C_1^g &= \frac{\left(\sum_q e_q^2\right) \alpha_S T_F}{4\pi} \frac{2x}{(x + \xi + i\varepsilon)(x - \xi - i\varepsilon)} . \\
 &\left[-2 \frac{x - 3\xi}{x + \xi} \log \left(-1 + \frac{x}{\xi} - i\varepsilon \right) + \frac{x - \xi}{x + \xi} \log^2 \left(-1 + \frac{x}{\xi} - i\varepsilon \right) \right. \\
 &- 2 \frac{x + 3\xi}{x - \xi} \log \left(-1 - \frac{x}{\xi} - i\varepsilon \right) + \frac{x + \xi}{x - \xi} \log^2 \left(-1 - \frac{x}{\xi} - i\varepsilon \right) \\
 &\left. + 4 \frac{x^2 + 3\xi^2}{x^2 - \xi^2} \log(-2 - i\varepsilon) - 2 \frac{x^2 + \xi^2}{x^2 - \xi^2} \log^2(-2 - i\varepsilon) \right]
 \end{aligned}$$

Discussion

- DVCS: the imaginary parts from $\xi \rightarrow \xi - i\varepsilon$
- TCS:
 - part of imaginary parts from $\xi \rightarrow \xi + i\varepsilon$
 - there appear e.g. $\log^2(-2 - i\varepsilon)$ which contribute to imaginary parts
 - in DVCS the imaginary part are in DGLAP region
in TCS they are in DGLAP AND ERBL
- at LO: $C_{0(DVCS)}^q = {C_{0(TCS)}^q}^*$
at NLO: $C_{coll(DVCS)}^q = {C_{coll(TCS)}^q}^*$ and $C_{coll(DVCS)}^g = {C_{coll(TCS)}^g}^*$

NLO quark:

$$\frac{C_{1(TCS)}^q - C_{1(DVCS)}^q}{\frac{e^2 \alpha_S C_F}{4\pi}} =$$
$$\frac{1}{x - \xi + i\varepsilon} \left[\left(3 - 2 \log 2 + 2 \log \left| 1 - \frac{x}{\xi} \right| \right) (i\pi) + \pi^2 (1 + \theta(x - \xi) - \theta(-x + \xi)) \right]$$
$$+ \frac{1}{x + \xi - i\varepsilon} \left[\left(3 - 2 \log 2 + 2 \log \left| 1 + \frac{x}{\xi} \right| \right) (i\pi) + \pi^2 (1 + \theta(-x - \xi) - \theta(x + \xi)) \right]$$

NLO gluon in DGLAP region:

$$\frac{C_{1(TCS)}^g - C_{1(DVCS)}^g}{\frac{(\sum_q e_q^2) \alpha_S T_F}{4\pi}} \stackrel{x \geq \xi}{=} \frac{2x}{x^2 - \xi^2} \left[2 \frac{x - \xi}{x + \xi} \pi^2 \right.$$
$$\left. + \left(-4 \frac{x - 3\xi}{x + \xi} + 2 \frac{x - \xi}{x + \xi} \log \left| 1 - \frac{x}{\xi} \right| - 2 \frac{x + \xi}{x - \xi} \log \left| 1 + \frac{x}{\xi} \right| + 4 \frac{x^2 + \xi^2}{x^2 - \xi^2} \log 2 \right) (-i\pi) \right]$$

$$\text{quark ratio: } R^q = \frac{C_1^q + \frac{1}{2} \log\left(\frac{|Q^2|}{\mu_F^2}\right) \cdot C_{coll}^q}{C_0^q}$$

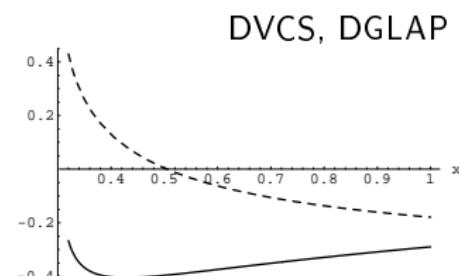
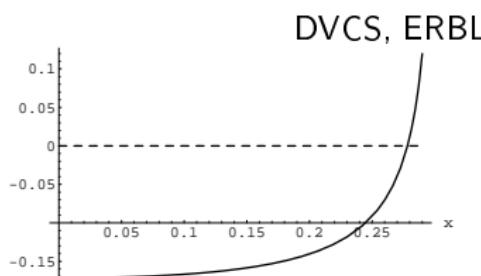
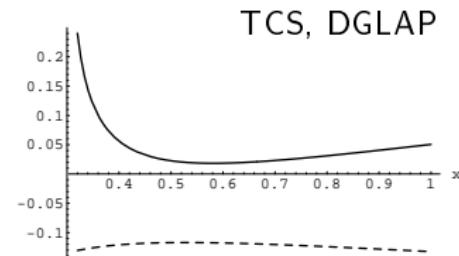
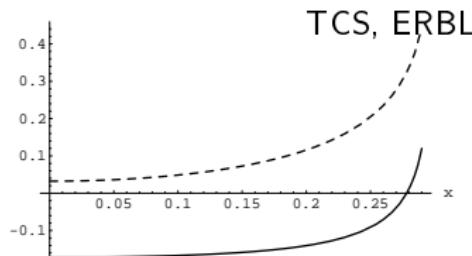


Figure: Real (solid line) and imaginary (dashed line) part of the ratio R^q of the NLO quark coefficient function to the Born term in Timelike Compton Scattering (up) and Deeply Virtual Compton Scattering (down) as a function of x in the ERBL (left) and DGLAP (right) region for $\xi = 0.3$, for $\mu_F^2 = |Q^2|$.

another quark ratio: $R_{T-S}^q = \frac{C_{1(TCS)}^q - C_{1(DVCS)}^{q*}}{C_0^q}$

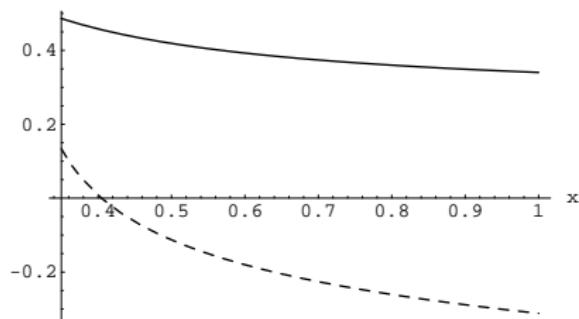


Figure: Real (solid line) and imaginary (dashed line) part of the ratio R_{T-S}^q of difference of NLO quark coefficient functions to the LO coefficient functions in the TCS and DVCS as a function of x in the DGLAP region for $\xi = 0.3$.

gluonic ratios:

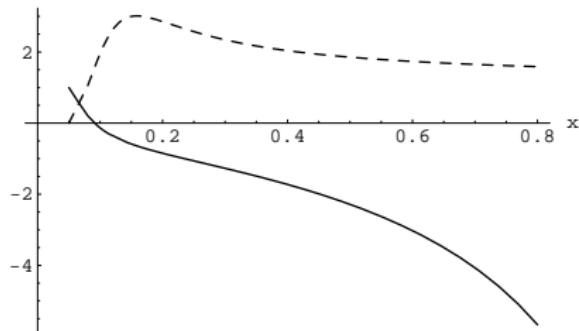


Figure: Ratio of the real (solid line) and imaginary (dashed line) part of the NLO gluon coefficient function in TCS to the same quantity in DVCS as a function of x in the DGLAP region for $\xi = 0.05$ for $\mu_F^2 = |Q^2|$.

Factorisation scale dependence of quark CF:

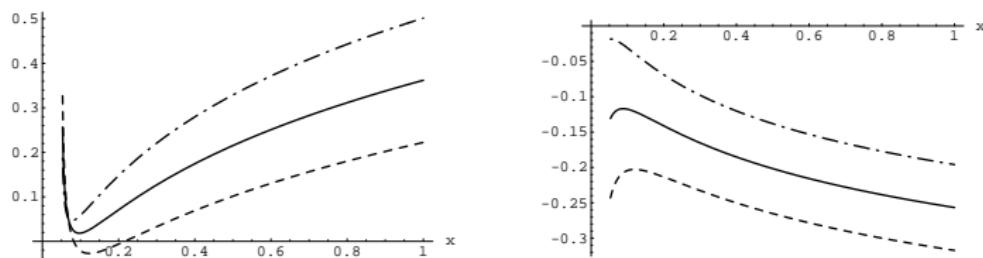


Figure: Factorization scale dependence of the real (left) and imaginary (right) parts of ratio R^q of NLO quark correction to hard scattering amplitudes to Born level coefficient function of the Timelike Compton Scattering as a function of x in the DGLAP region for $\xi = 0.05$. The ratios are plotted for the values of $\frac{|Q^2|}{\mu_F^2}$ equal 0.5 (dashed), 1 (solid) and 2 (dash-dotted line).

Factorisation scale dependence of gluonic CF:

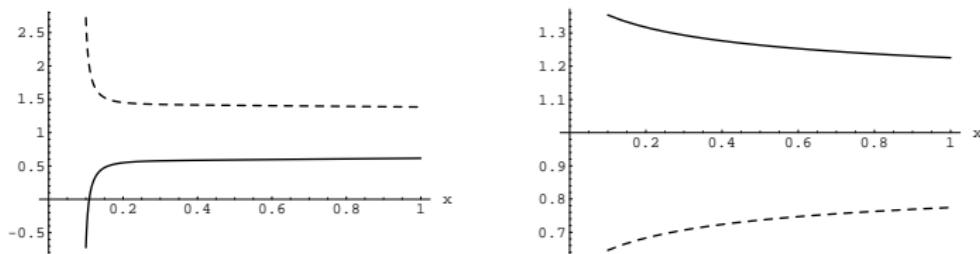


Figure: Ratios of the real (left) and imaginary (right) parts of NLO gluon coefficient function for $|Q^2| = 1/2\mu_F^2$ (solid line) and $|Q^2| = 2\mu_F^2$ (dashed line) to the same quantities with $|Q^2| = \mu_F^2$. Those quantities are calculated for the timelike Compton scattering and plotted as a function of x in the DGLAP region for $\xi = 0.05$.

Estimates for DVCS

ξ dependence of Compton form factors for DVCS with GPDs obtained from double distribution

solid line: LO $\text{Re } H_u$

dotted line: LO $\text{Im } H_u$

dashed line: Full NLO $\text{Re } H_u$

dot-dashed line: Full NLO $\text{Im } H_u$

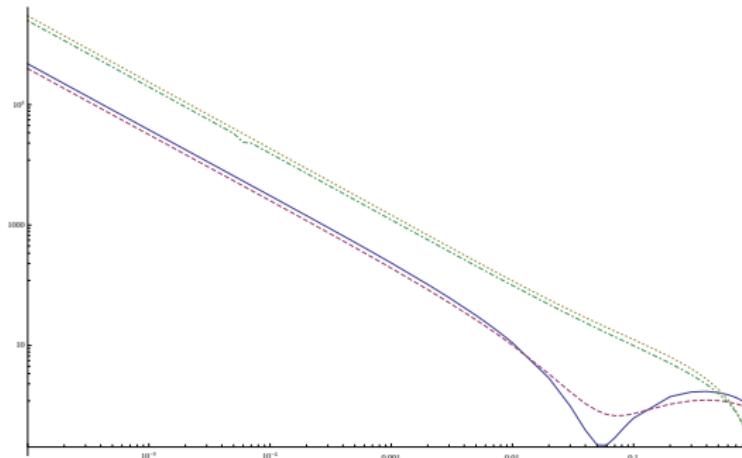


Figure: Double distr. with PDF by Goloskokov-Kroll for $Q^2 = 4\text{GeV}^2$, $\mu_F = Q$ and $t = 0$

Estimates for DVCS cntd

ξ dependence of Compton form factors for DVCS with GPDs obtained from double distribution

solid line: LO $\text{Re } H_u$

dotted line: LO $\text{Im } H_u$ dashed line: Full NLO $\text{Re } H_u$

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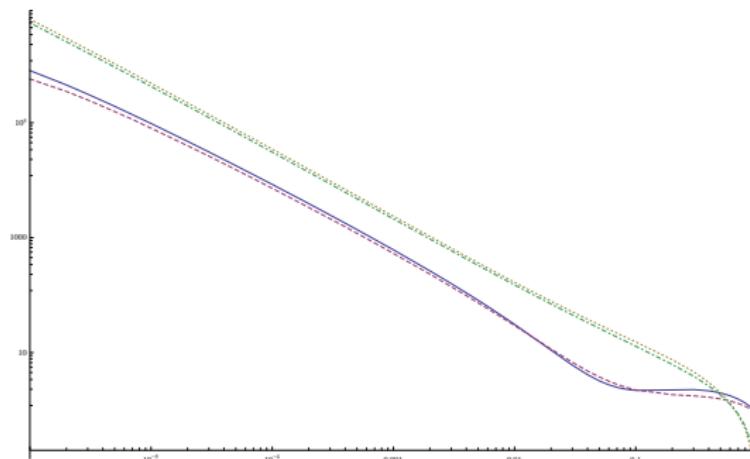


Figure: Double distr. with PDF by MSTW for $Q^2 = 4\text{GeV}^2$, $\mu_F = Q$ and $t = 0$

Estimates for DVCS cntd

ξ dependence of Compton form factors for DVCS with GPDs obtained from double distribution obtained with MSTW PDFs

$$CFF = LO + NLO \quad \text{Ratio} = \frac{NLO}{LO}$$

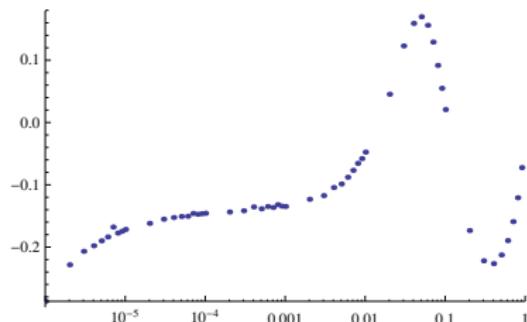
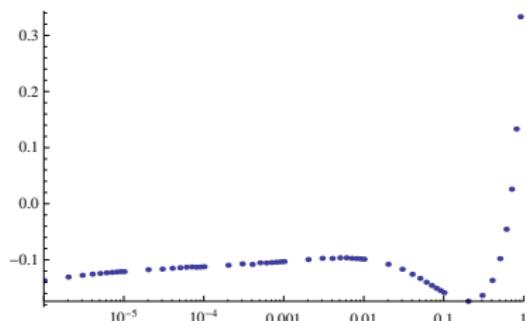


Figure: Ratios of NLO correction to Born contribution for imaginary (left figure) and real (right figure) parts for $Q^2 = 4\text{GeV}^2$, $\mu_F = Q$, $t = 0$

Estimates for TCS

ξ dependence of Compton form factors for TCS with GPDs obtained from double distribution obtained with MSTW PDFs

$$CFF = LO + NLO \quad \text{Ratio} = \frac{NLO}{LO}$$

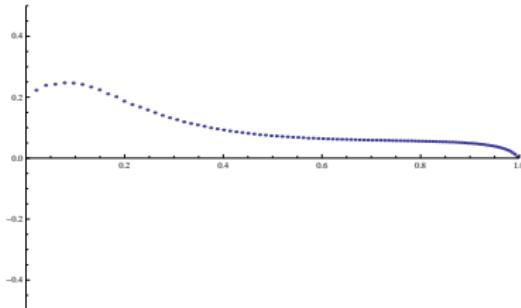
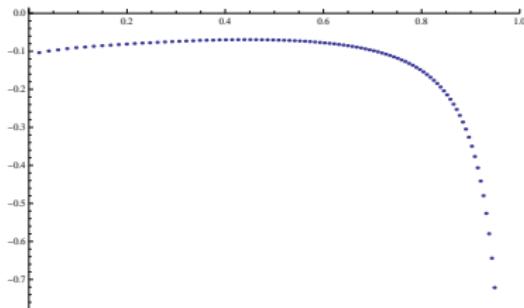


Figure: Ratios of NLO correction to Born contribution for imaginary (left figure) and real (right figure) parts for $Q^2 = 5\text{GeV}^2$, $\mu_F = Q$, $t = 0$

Resummation of large terms

Reminder: **INCLUSIVE** DIS vs. DY case G. Parisi Phys. Lett. 90B (1980)

$$\sigma_{DY}^n = \sigma_{PM}^n R(\alpha, n)$$

$$R(\alpha, n) = 1 + \frac{\alpha(Q^2)}{2\pi} f(n) + \mathcal{O}(\alpha^2(Q^2))$$

σ_{DY}^n moments in $\tau = Q^2/s$

σ_{PM}^n predictions of naive parton model at $q^2 = -Q^2$

$$f(n) \sim \frac{4}{3} \left(\frac{4}{3} \pi^2 + 2 \ln^2 n \right) \quad \text{for } n \gg 1$$

π^2 terms: analytic continuation from $q^2 < 0$ to $q^2 > 0$

$\ln^2 n$ terms: soft gluons

⇒ large terms exponentiate into quark e-m. form factor

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Resummation in case of **EXCLUSIVE** processes:

e.g. DVCS vs. TCS case: no results

work in progress

Conclusions of the NLO part:

- new results: NLO corrections to DVCS, TCS and to DDVCS
- corrections seem to be big ...
- better understanding of large terms (π^2 , ??) is needed resummation
- realistic phenomenology needed: (in progress)
 - realistic GPD convoluted with our NLO CFs
 - calculation of relevant observables
- NICE DATA FROM LHC, RHIC and JLab ON TCS, DDVCS
ARE VERY NEEDED !!

THANK YOU FOR YOUR ATTENTION