

INT program Interfaces between structure and reactions for rare isotopes and nuclear astrophysics

Seattle, August 8 - September 2, 2011

Exploring the isovector equation of state at high densities with HIC



Vaia D. Prassa



Aristotle University of Thessaloniki

Department of Physics

Outline

- 1 Introduction**
 - Nuclear Equation of state
 - Symmetry Energy
 - Phase diagram
 - Spacetime evolution
- 2 Quantum Hadrodynamics (QHD)**
 - Meson exchange model
 - Asymmetric Nuclear Equation of State
- 3 Transport theory**
 - Vlasov term
 - Collision term
- 4 Particle Production**
 - Cross sections
 - Kaon-nucleon potential
- 5 Summary & Outlook**

First questions to be answered:

Why is the Symmetry Energy so important?

- At *low densities*: Nuclear structure (neutron skins, pigmy resonances), Nuclear Reactions (neutron distillation in fragmentation, charge equilibration), and Astrophysics, (neutron star formation, and crust),
- At *high densities*: Relativistic Heavy ion collisions (isospin flows, particle production), Compact stars (neutron star structure), and for fundamental properties of strong interacting systems (transition to new phases of the matter).

Why HIC?

- Probing the in-medium nuclear interaction in regions away from saturation.
- Reaction observables sensitive to the symmetry term of the nuclear equation of state.
- High density symmetry term probed from isospin effects on heavy ion reactions at relativistic energies.

In this talk:

- HIC at intermediate energies 400A MeV-2A GeV.
- Investigation of particle ratios: Probes for the symmetry energy density dependence. In-medium effects in inelastic cross sections & Kaon potential choices.

First questions to be answered:

Why is the Symmetry Energy so important?

- At *low densities*: Nuclear structure (neutron skins, pigmy resonances), Nuclear Reactions (neutron distillation in fragmentation, charge equilibration), and Astrophysics, (neutron star formation, and crust),
- At *high densities*: Relativistic Heavy ion collisions (isospin flows, particle production), Compact stars (neutron star structure), and for fundamental properties of strong interacting systems (transition to new phases of the matter).

Why HIC?

- Probing the in-medium nuclear interaction in regions away from saturation.
- Reaction observables sensitive to the symmetry term of the nuclear equation of state.
- High density symmetry term probed from isospin effects on heavy ion reactions at relativistic energies.

In this talk:

- HIC at intermediate energies 400A MeV-2A GeV.
- Investigation of particle ratios: Probes for the symmetry energy density dependence. In-medium effects in inelastic cross sections & Kaon potential choices.

First questions to be answered:

Why is the Symmetry Energy so important?

- At *low densities*: Nuclear structure (neutron skins, pigmy resonances), Nuclear Reactions (neutron distillation in fragmentation, charge equilibration), and Astrophysics, (neutron star formation, and crust),
- At *high densities*: Relativistic Heavy ion collisions (isospin flows, particle production), Compact stars (neutron star structure), and for fundamental properties of strong interacting systems (transition to new phases of the matter).

Why HIC?

- Probing the in-medium nuclear interaction in regions away from saturation.
- Reaction observables sensitive to the symmetry term of the nuclear equation of state.
- High density symmetry term probed from isospin effects on heavy ion reactions at relativistic energies.

In this talk:

- HIC at intermediate energies 400A MeV-2A GeV.
- Investigation of particle ratios: Probes for the symmetry energy density dependence. In-medium effects in inelastic cross sections & Kaon potential choices.

Equation of State (EOS)

The nuclear matter thermodynamical properties are described by an equation of state.

The nuclear EOS gives the **binding energy E/A** or the **pressure P** of the system per nucleon, as a function of the **baryon density** or the **temperature**.

$$E(\rho, T) = E_{th}(\rho, T) + E_c(\rho, T = 0) + E_0$$

$E_{th}(\rho, T)$: thermic energy, consists of a kinetic and a dynamic term.

$E_c(\rho, T = 0)$: compression energy at $T = 0$.

E_0 : binding energy at $T = 0$ and ρ_0 .

Incompressibility: $K = 9\rho_0^2 \left(\frac{\partial^2 E}{\partial \rho_B^2} \right) \Big|_{\rho_B = \rho_0}$

Equation of State (EOS)

The nuclear matter thermodynamical properties are described by an equation of state.

The nuclear EOS gives the **binding energy** E/A or the **pressure** P of the system per nucleon, as a function of the **baryon density** or the **temperature**.

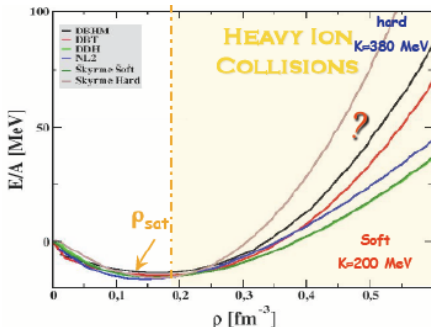
$$E(\rho, T) = E_{th}(\rho, T) + E_c(\rho, T = 0) + E_0$$

$E_{th}(\rho, T)$: thermic energy, consists of a kinetic and a dynamic term.

$E_c(\rho, T = 0)$: compression energy at $T = 0$.

E_0 : binding energy at $T = 0$ and ρ_0 .

Incompressibility: $K = 9\rho_0^2 \left(\frac{\partial^2 E}{\partial \rho_B^2} \right) \Big|_{\rho_B = \rho_0}$



At ρ_{sat} : well defined by studies on stable nuclei.

High ρ_B : is predicted by the theoretical models and is adjusted to fit the HIC data.

Constraints from HIC:

Multiplicities and Flows of n and p .

Symmetry Energy

The EOS depends on the asymmetry parameter $\alpha = \frac{N-Z}{N+Z}$:

$$E(\rho_B, \alpha) \equiv \frac{\epsilon(\rho_B, \alpha)}{\rho_B} = E(\rho_B, 0) + E_{sym}(\rho_B)\alpha^2$$

Thus, it gives a definition of the symmetry energy:

$$E_{sym} \equiv \frac{1}{2} \frac{\partial^2 E(\rho_B, \alpha)}{\partial \alpha^2} \Big|_{\alpha=0} = \frac{1}{2} \rho_B \frac{\partial^2 \epsilon}{\partial \rho_B^2} \Big|_{\rho_B=0}$$

$$K_{sym} = 9\rho_0^2 \left(\frac{\partial^2 E_{sym}}{\partial \rho_B^2} \right) \Big|_{\rho_B=\rho_0}$$

The symmetry energy describes the difference between the binding energy of the symmetric matter and that of the pure neutron matter.

Symmetry Energy

The EOS depends on the asymmetry parameter $\alpha = \frac{N-Z}{N+Z}$:

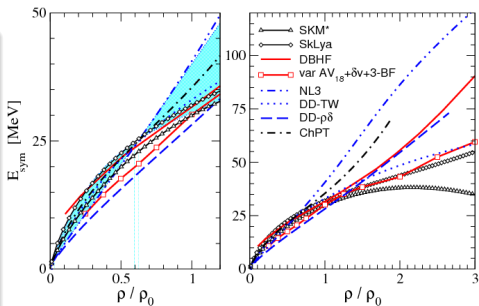
$$E(\rho_B, \alpha) \equiv \frac{\epsilon(\rho_B, \alpha)}{\rho_B} = E(\rho_B, 0) + E_{\text{sym}}(\rho_B)\alpha^2$$

Thus, it gives a definition of the symmetry energy:

$$E_{\text{sym}} \equiv \frac{1}{2} \frac{\partial^2 E(\rho_B, \alpha)}{\partial \alpha^2} \Big|_{\alpha=0} = \frac{1}{2} \rho_B \frac{\partial^2 \epsilon}{\partial \rho_B^2} \Big|_{\rho_B=0}$$

$$K_{\text{sym}} = 9\rho_0^2 \left(\frac{\partial^2 E_{\text{sym}}}{\partial \rho_B^2} \right) \Big|_{\rho_B=\rho_0}$$

The symmetry energy describes the difference between the binding energy of the symmetric matter and that of the pure neutron matter.

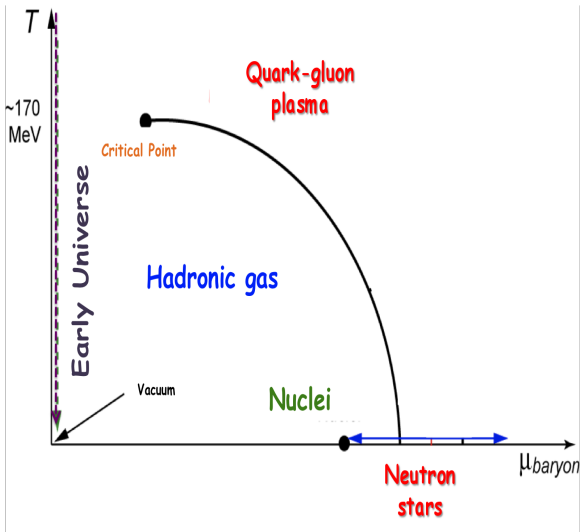


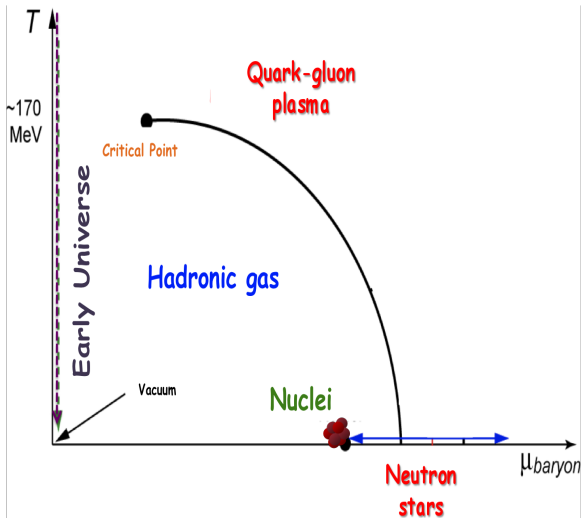
Different behavior even at saturation point.

High ρ_B , discrepancies between the models increases.

Constraints from HIC:

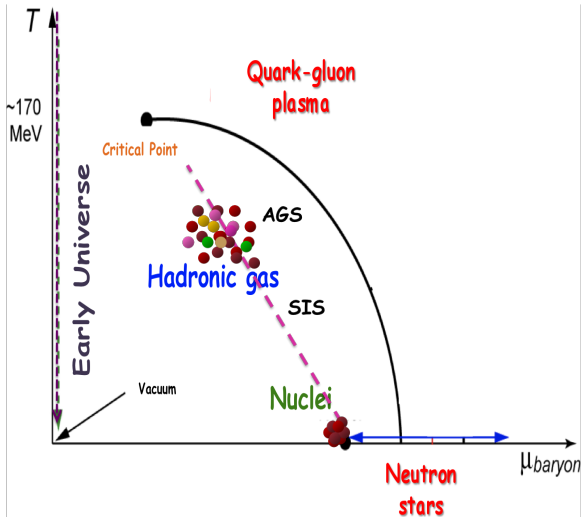
Multiplicities and Differential flows of n and p.
Pion flows and Isospin ratios π^-/π^+ , K^0/K^+ .



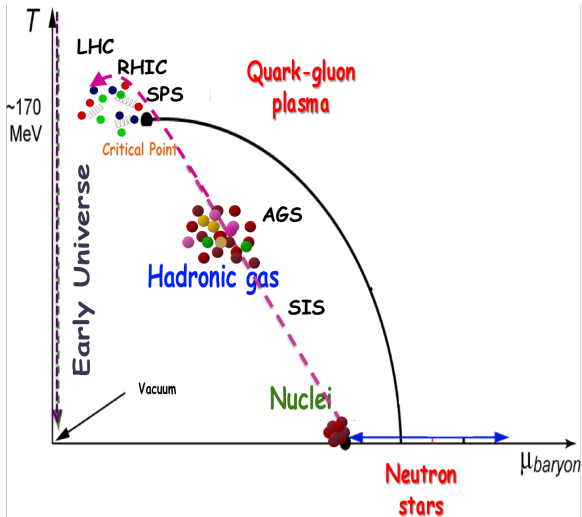


- **Liquid phase:**

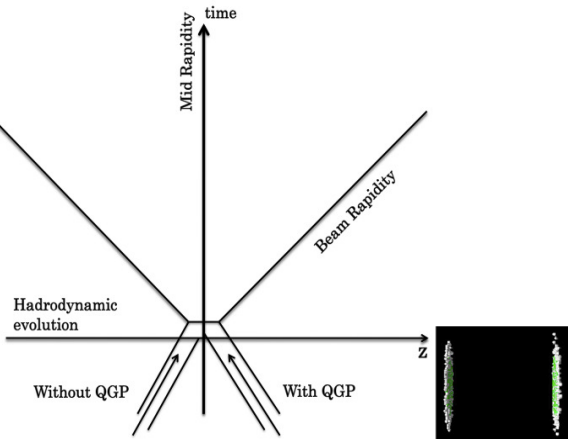
$T \approx 10 \text{ MeV}$.



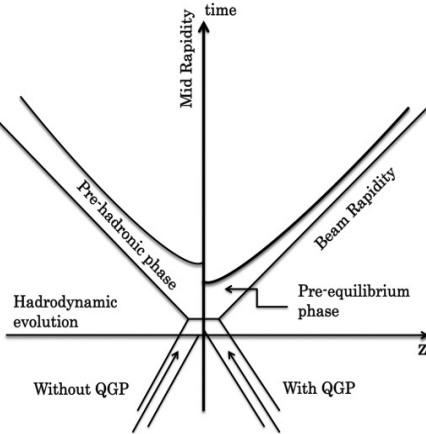
- **Gas phase:** RHIC
 $T \approx 10 - 100 \text{ MeV}$.
- **Liquid phase:**
 $T \approx 10 \text{ MeV}$.



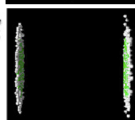
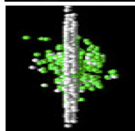
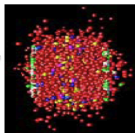
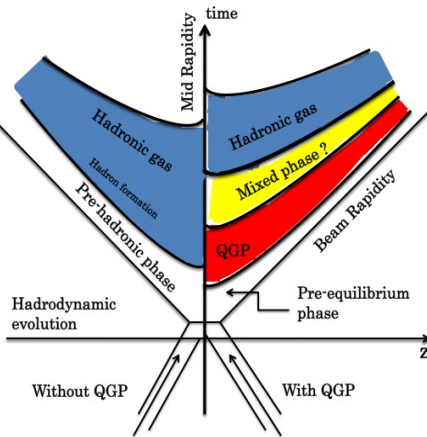
- **Quark-gluon plasma:** Ultra RHIC
 $T > 100 \text{ MeV}$
- **Gas phase:** RHIC
 $T \approx 10 - 100 \text{ MeV}$
- **Liquid phase:**
 $T \approx 10 \text{ MeV}$



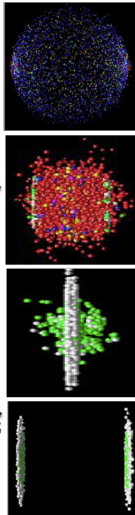
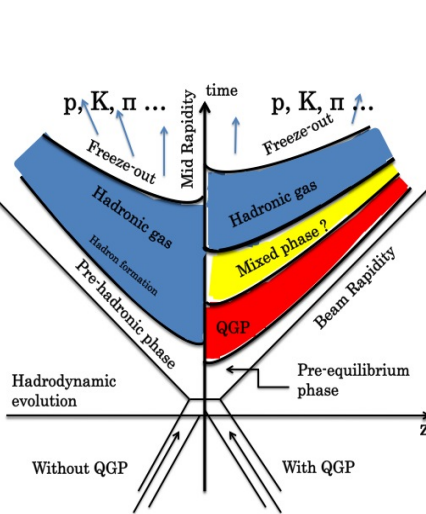
- **Initial stage.** Nuclei at ground state. $P = 0, T = 0, \rho = \rho_0$.



- **Compression.** Sequential N-N binary collisions. Incoming matter of the target & the projectile is **mixed & compressed** forming a short-lived stage of nuclear matter of high ρ_B that depends on the EOS.
 $E = 1A \text{ GeV}$, $T \approx 30 - 60 \text{ MeV}$,
 $\rho_B \approx 2 - 3\rho_0$.
- **Initial stage.** Nuclei at ground state. $P = 0$, $T = 0$, $\rho = \rho_0$.

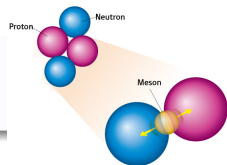


- Expansion.** Expansion of the density energy. $T, \rho \downarrow$.
Hot matter interacts with the **cold matter** of the spectator.
 $E_{beam} > 10A\text{GeV} \Rightarrow QGP_{limit}$,
 P lower than $P_{hadronic phase}$.
- Compression.** Sequential N-N binary collisions. Incoming matter of the target & the projectile is **mixed & compressed** forming a short-lived stage of nuclear matter of high ρ_B that depends on the EOS.
 $E = 1A\text{GeV}$, $T \approx 30 - 60\text{MeV}$,
 $\rho_B \approx 2 - 3\rho_0$.
- Initial stage.** Nuclei at ground state. $P = 0, T = 0, \rho = \rho_0$.

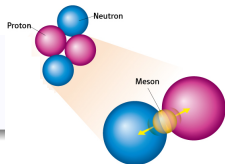


- **Freeze-out.** Low $\rho_B \Rightarrow$ no further interaction.
- **Expansion.** Expansion of the density energy. $T, \rho \downarrow$. **Hot matter** interacts with the **cold matter** of the spectator. $E_{beam} > 10A\text{GeV} \Rightarrow QGP_{limit}$, P lower than $P_{hadronic phase}$.
- **Compression.** Sequential N-N binary collisions. Incoming matter of the target & the projectile is **mixed & compressed** forming a short-lived stage of nuclear matter of high ρ_B that depends on the EOS. $E = 1A\text{GeV}$, $T \approx 30 - 60\text{MeV}$, $\rho_B \approx 2 - 3\rho_0$.
- **Initial stage.** Nuclei at ground state. $P = 0, T = 0, \rho = \rho_0$.

The NN Interaction is described by the exchange of **mesons**.
SCALAR (attraction): σ , δ (isospin dependence).
VECTOR (repulsion): ω , ρ (isospin dependence).



The NN Interaction is described by the exchange of **mesons**.
SCALAR (attraction): σ, δ (isospin dependence).
VECTOR (repulsion): ω, ρ (isospin dependence).



Lagrangian density

$$\begin{aligned} \mathcal{L} = & \bar{\psi}(i\gamma^\mu \partial_\mu - m)\psi + \frac{1}{2}\partial_\mu\sigma\partial^\mu\sigma - U(\sigma) + \frac{1}{2}m_\omega^2\omega_\mu\omega^\mu - \frac{1}{4}\Omega_{\mu\nu}\Omega^{\mu\nu} \\ & + \frac{1}{2}m_\rho^2\vec{\rho}_\mu \cdot \vec{\rho}^\mu - \frac{1}{4}\vec{R}_{\mu\nu}\vec{R}^{\mu\nu} + \frac{1}{2}(\partial_\mu\vec{\delta} \cdot \partial^\mu\vec{\delta} - m_\delta^2\vec{\delta}^2) \\ & + \bar{\psi}(-g_\omega\omega_\mu - g_\rho\vec{\gamma}\vec{\tau} \cdot \vec{\rho}_\mu + g_\sigma\sigma + g_\delta\vec{\tau} \cdot \vec{\delta})\psi \end{aligned}$$

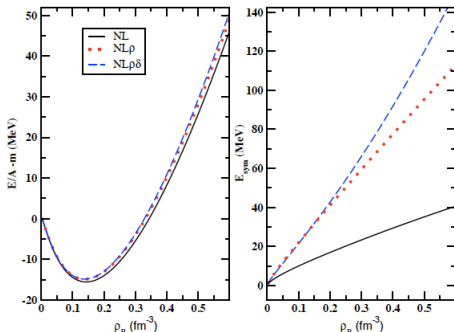
Lagrangian density of: the **free nucleons**, the σ **meson** with $U(\sigma) = \frac{1}{2}m_\sigma^2\sigma^2 + \frac{1}{3}g_2\sigma^3 + \frac{1}{4}g_3\sigma^4$, the ω **meson** with the field tensor $\Omega_{\mu\nu} \equiv \partial_\mu\omega_\nu - \partial_\nu\omega_\mu$, the ρ meson with the field tensor $\vec{R}_{\mu\nu} \equiv \partial_\mu\vec{\rho}_\nu - \partial_\nu\vec{\rho}_\mu$, the δ **meson** and of their **interaction**.

The *nuclear EOS* for asymmetric nuclear matter in the QHD picture:

$$\mathcal{E} = \sum_{i=n,p} 2 \int \frac{d^3k}{(2\pi)^3} E_i^*(k) + U(\Phi) + \frac{1}{2} f_V \rho_B^2 + \frac{1}{2} f_\rho \rho_B^2 + \frac{1}{2} f_\delta \rho_S^2$$

The nuclear *Symmetry energy* in the QHD picture :

$$E_{sym} = \frac{1}{6} \frac{k_F^2}{E_F^*} + \frac{1}{2} \left[f_\rho - f_\delta \left(\frac{m^*}{E_F^*} \right)^2 \right] \rho_B$$



Relativistic transport equation

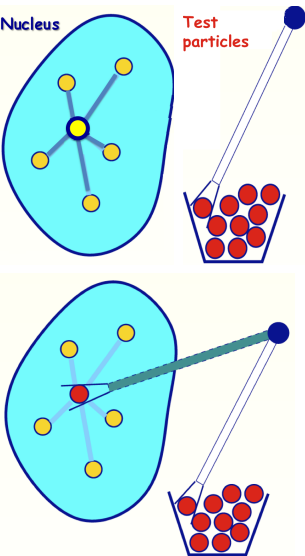
Relativistic Boltzmann-Uehling-Uhlenbeck (RBUU)

$$\begin{aligned}
 & [p_{\mu i}^* \partial_x^\mu + (g_\omega p_{\nu i}^* F_i^{\mu\nu} + m_i^* (\partial_x^\mu m_i^*)) \partial_\mu^p] f_i(x, p^*) = \\
 & \frac{g}{(2\pi)^3} \int \frac{d^3 p_2^*}{p_2^{*0}} \frac{d^3 p_3^*}{p_3^{*0}} \frac{d^3 p_4^*}{p_4^{*0}} W(p^*, p_2^*, p_3^*, p_4^*) \\
 & \{ f_3 f_4 [1 - f] [1 - f_2] - f f_2 [1 - f_3] [1 - f_4] \}
 \end{aligned}$$

- **Vlasov term.** Temporal evolution of the system, which is described by the phase-space distribution function $f(x, p^*)$, under the influence of a mean field (m_i^*, p_i^*) .
- **Collision term.** Transition rate W , is expressed by the differential cross section $(\frac{d\sigma}{d\Omega(s, \Theta)})$,

$$W(p^*, p_2^*, p_3^*, p_4^*) = (p^* + p_2^*)^2 \frac{d\sigma}{d\Omega} \delta^4(p^* + p_2^* - p_3^* - p_4^*)$$

where Θ is the scattering angle in the cms frame and s the square of the total energy, $s = (p^* + p_2^*)^2$.



Test particle method

Representation of the phase-space distribution function by a number of test particles.

Gaussian test particles

$$g(p^* - p_i^*(\tau)) = \alpha_p e^{(p^* - p_i^*(\tau))^2 / \sigma_p^2} \delta[p_{\mu}^* p_i^{*\mu}(\tau) - m_i^{*2}]$$

Distribution function

$$f(x, p^*) = \frac{1}{N(\pi\sigma\sigma_p)} \sum_{i=1}^{A \cdot N} \int_{-\infty}^{+\infty} d\tau e^{R_{i\mu}(x) R_i^{\mu}(x) / \sigma^2} e^{(p^* - p_i^*(\tau))^2 / \sigma_p^2} \times \delta[(x_{\mu} - x_{i\mu}(\tau)) u_i^{\mu}(\tau)] \delta[p_{\mu}^* p_i^{*\mu}(\tau) - m_i^{*2}]$$

Test particles equations of motions

$$\frac{d}{d\tau} x_i^{\mu} = \frac{p_i^{*\mu}(\tau)}{m_i^*(x_i)},$$

$$\frac{d}{d\tau} p_i^{*\mu} = \frac{p_{i\nu}^*(\tau)}{m_i^*(x_i)} F_i^{\mu\nu}(x_i(\tau)) + \partial^{\mu} m_i^*(x_i)$$

Collision term

$$\mathcal{I}_c = \frac{g}{(2\pi)^3} \int \frac{d^3 p_2^*}{p_2^{*0}} \frac{d^3 p_3^*}{p_3^{*0}} \frac{d^3 p_4^*}{p_4^{*0}} W(p^*, p_2^*, p_3^*, p_4^*)$$

$$\{ f(x, p_3^*) f(x, p_4^*) [1 - f(x, p^*)] [1 - f(x, p_2^*)] - f(x, p^*) f(x, p_2^*) [1 - f(x, p_3^*)] [1 - f(x, p_4^*)] \}$$

- Factors $(1 - f_i)$, ($f_i = f(x, p_i^*)$), Pauli principle.
- Transition rate:**
 $W = (2\pi)^4 \delta^4(k + k_2 - k_3 - k_4) (m^*)^4 |T|^2$.
- Two particles collide if:
 $d < d_0 = \sqrt{\frac{\sigma_{tot}}{\pi}}$.

Elastic channels

- $NN \iff NN$
- $N\Delta \iff N\Delta$
- $\Delta\Delta \iff \Delta\Delta$

Inelastic channels

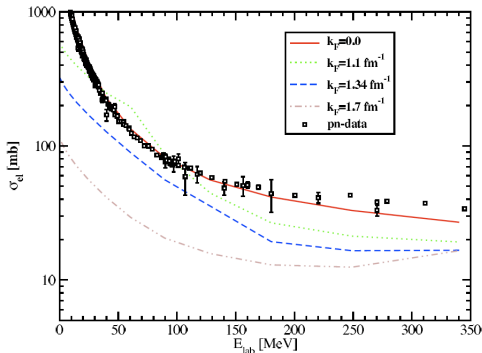
Ingoing channel	Outgoing Channel	Isospin coefficients
nn	$p\Delta^-$	1
	$n\Delta^0$	2/3
np	$p\Delta^0$	1/3
	$n\Delta^+$	2/3
pp	$p\Delta^+$	1/3
	$n\Delta^{++}$	1

Decay width:

$$\Gamma(q) = \tilde{\Gamma} \frac{q^3 R^2}{1 + q^2 R^2} z(q), \quad z(q) = \frac{q_r^2 + \delta^2}{q^2 + \delta^2}$$

Resonance decay probability P ,

$$P = 1 - \exp \left[-\frac{\Gamma(M)\Delta t}{\gamma \hbar c} \right]$$



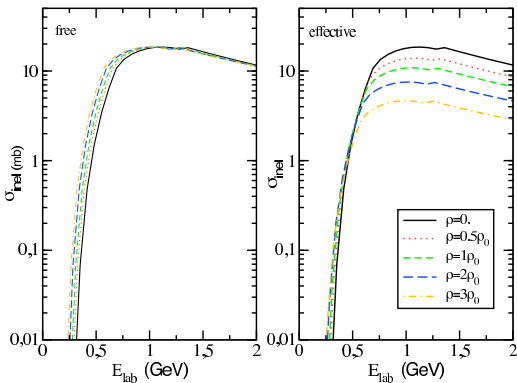
Elastic Baryon-Baryon collisions

In-medium effects: Dirac-Brueckner.

Suppression of cross sections at $E_{beam} < 300 A \text{ MeV}$ and high ρ_B .

At high E_{lab} , the σ_{eff} approaches asymptotically σ_{free}

Fuchs et al. Phys. Rev. C64 (2001), 024003.



Inelastic Baryon-Baryon collisions

In-medium effects: DBHF.

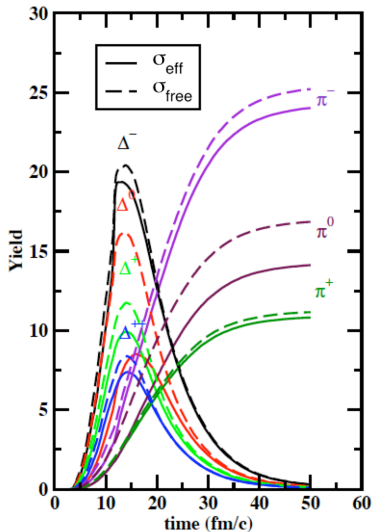
Ter Haar and Malfliet, Phys.Rev.C36, 4 (1987)

$$\sigma_{eff}^{inel} = f(\rho) \sigma_{free}^{inel}(E_{lab})$$

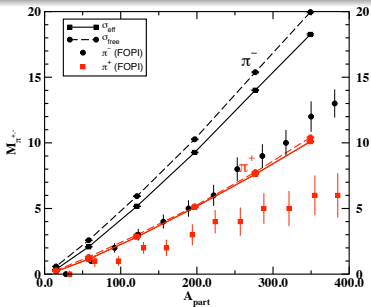
$$f(\rho) = 1 + a_0(\rho_B/\rho_0) + a_1(\rho_B/\rho_0)^2 + a_2(\rho_B/\rho_0)^3.$$

Inverse channel:

$$\sigma_{N\Delta \rightarrow NN} = \frac{(2S_N+1)(2S_N+1)}{(2S_N+1)(2S_\Delta+1)} \frac{q_f^2}{q_i^2} \sigma_{NN \rightarrow N\Delta}.$$



State	I_3	Decay channel	Weights
Δ^-	$-3/2$	$n\pi^-$	1
Δ^0	$-1/2$	$p\pi^-$	1/3
		$n\pi^0$	2/3
Δ^+	$+1/2$	$p\pi^0$	2/3
		$n\pi^+$	1/3
Δ^{++}	$+3/2$	$p\pi^+$	1

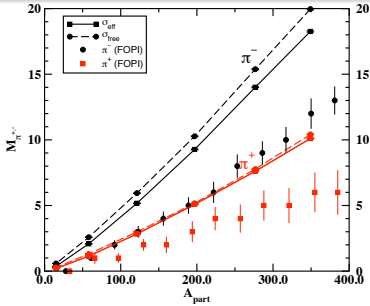


Centrality dependence

$Au + Au$ collision at 1A GeV.

A_{part} : number of participants in a collision.

Overestimation of data.

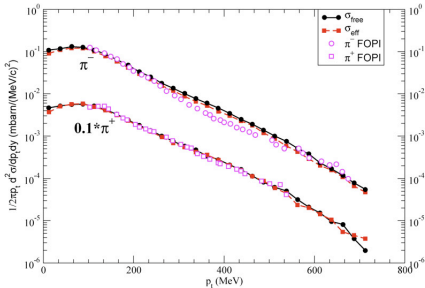


Centrality dependence

$Au + Au$ collision at 1 AGeV.

A_{part} : number of participants in a collision.

Overestimation of data.



Transverse momentum spectra

$Au + Au$ collision at 1 AGeV, at mid-rapidity
 $(-0.2 < y^0 < 0.2)$.

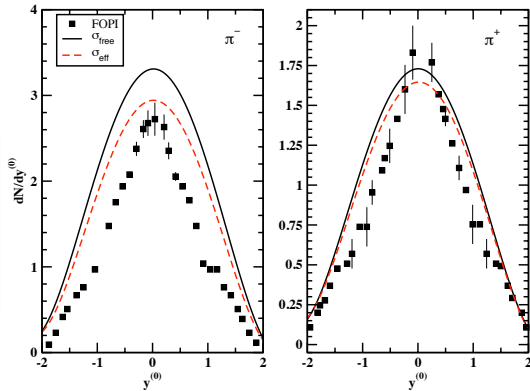
Very good agreement with data.

Pion rapidity distribution

$Au + Au$ collision at $E_{\text{beam}} = 1 \text{ AGeV}$,
with $p_t > 0.1 \text{ GeV}/c$.

Mid rapidity region: good agreement.

Spectator region: overestimation.

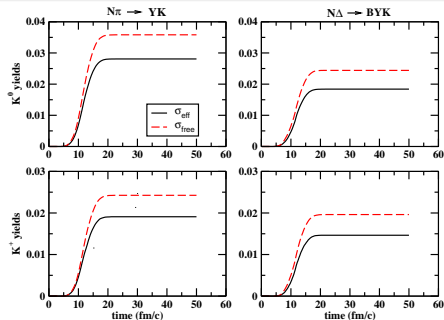


Kaon production

1 $\pi B \rightarrow YK$

2 $BB \rightarrow BYK$

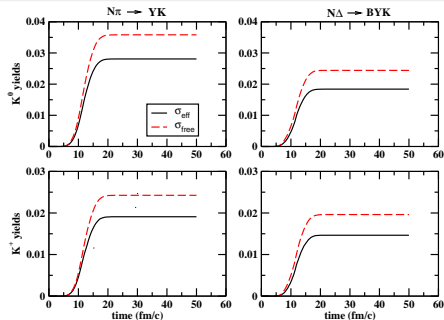
$Au + Au$ central collision at 1A GeV.



Kaon production

- 1 $\pi B \rightarrow YK$
- 2 $BB \rightarrow BYK$

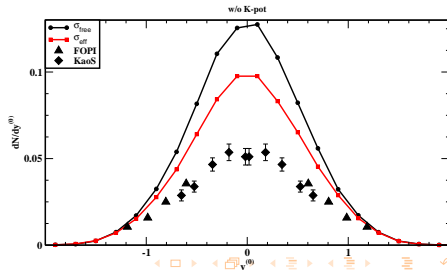
$Au + Au$ central collision at 1A GeV.



Rapidity distribution of K^+

$Ni + Ni$ collision at 1.93A GeV.

σ_{eff} : reduction of $K^+ \Rightarrow$ towards a better agreement with data.

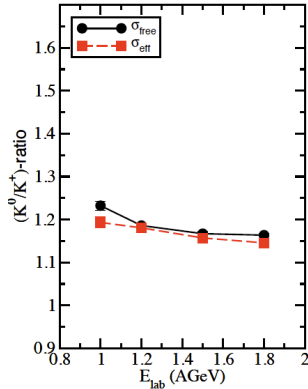
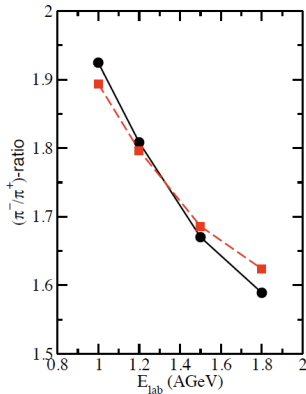


Yield ratios: **Determination** of the E_{sym} behavior.

π^-/π^+ : partially affected from the in-medium cross sections.

K^0/K^+ : appears **robust** against the in-medium cross sections.

V. Prassa et al, Nucl.Phys. A789, 311-333 (2007)



Kaons equation of motion

$$[(\partial^\mu + iV_\mu)^2 + m_K^{*2}] \phi_K(x) = 0$$

Kaon in-medium energy

$$E_K(\mathbf{k}) = k_0 = \sqrt{\mathbf{k}^2 + m_K^{*2}} + V_0$$

Chiral perturbation theory potential

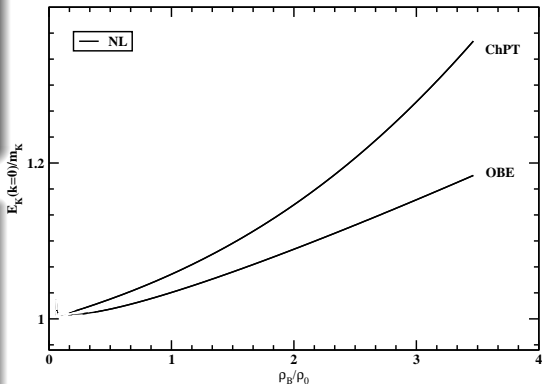
$$V_\mu = \frac{3}{8f_\pi^2} j_\mu$$

$$m_K^* = \sqrt{m_K^2 - \frac{\Sigma_{KN}}{f_\pi^2} \rho_s + V_\mu V^\mu}$$

One boson exchange model potential

$$V^\mu = \frac{1}{3} f_\omega^* j^\mu$$

$$m_K^* = \sqrt{m_K^2 + \frac{m_K}{3} g_{\sigma N \sigma}}$$



Kaons equation of motion

$$[(\partial^\mu + iV_\mu)^2 + m_K^{*2}] \phi_K(x) = 0$$

Chiral perturbation theory potential

$$V_\mu = \frac{3}{8f_\pi^{*2}} j_\mu \pm \frac{1}{8f_\pi^{*2}} j_{\mu 3}$$

$$m_K^* = \sqrt{m_K^2 - \frac{\Sigma_{KN}}{f_\pi^2} \rho_s + V_\mu V^\mu \mp \frac{C}{f_\pi^2} \rho_{s3}}$$

One boson exchange model potential

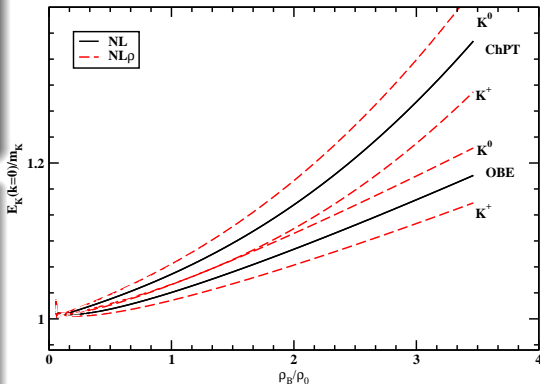
$$V^\mu = \frac{1}{3} (f_\omega^* j^\mu \pm f_\rho j_3^\mu)$$

$$m_K^* = \sqrt{m_K^2 + \frac{m_K}{3} g_{\sigma N \sigma}}$$

upper sign K^+

Kaon in-medium energy

$$E_K(\mathbf{k}) = k_0 = \sqrt{\mathbf{k}^2 + m_K^{*2}} + V_0$$



Kaons equation of motion

$$[(\partial^\mu + iV_\mu)^2 + m_K^{*2}] \phi_K(x) = 0$$

Chiral perturbation theory potential

$$V_\mu = \frac{3}{8f_\pi^{*2}} j_\mu \pm \frac{1}{8f_\pi^{*2}} j_{\mu 3}$$

$$m_K^* = \sqrt{m_K^2 - \frac{\Sigma_{KN}}{f_\pi^2} \rho_s + V_\mu V^\mu \mp \frac{C}{f_\pi^2} \rho_{s3}}$$

One boson exchange model potential

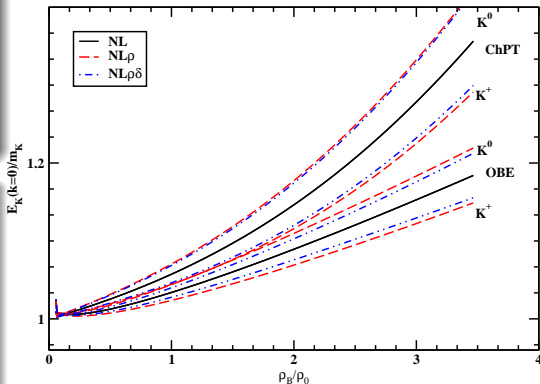
$$V^\mu = \frac{1}{3} (f_\omega^* j^\mu \pm f_\rho j_3^\mu)$$

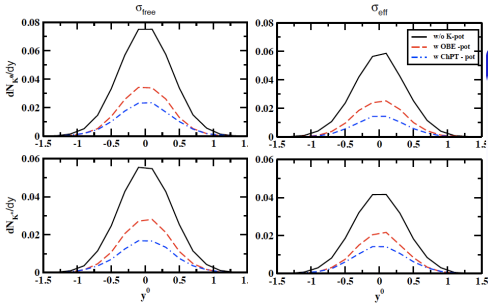
$$m_K^* = \sqrt{m_K^2 + \frac{m_K}{3} (g_{\sigma N} \sigma \mp f_\delta \rho_{s3})}$$

upper sign K^+

Kaon in-medium energy

$$E_K(\mathbf{k}) = k_0 = \sqrt{\mathbf{k}^2 + m_K^{*2}} + V_0$$





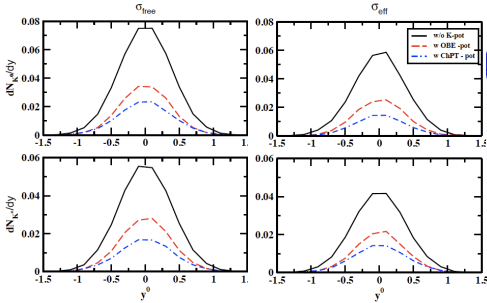
Rapidity distribution: Dependence on the V_K

Central $Au + Au@1A\text{GeV}$.

Reduction in the whole rapidity region.

OBE: *less stopping*.

Combination of V_K and σ_{eff} : further reduction.

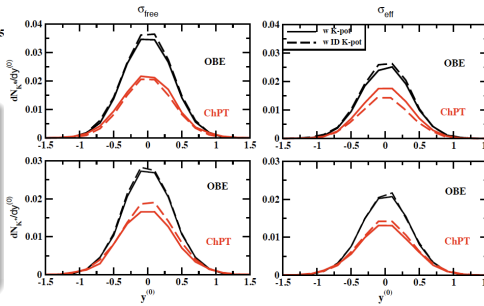


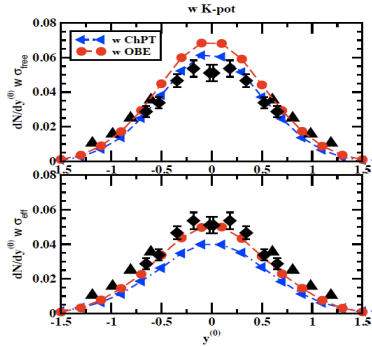
Rapidity distribution: Dependence on the V_K

Central $Au + Au@1A\text{GeV}$.
 Reduction in the whole rapidity region.
 OBE: less stopping.
 Combination of V_K and σ_{eff} : further reduction.

Rapidity distribution: Isospin dependent- V_K

Central $Au + Au@1A\text{GeV}$.
 Rapidity distributions *not* affected.
 Main contribution: *mid-rapidity* region.
 Combination V_K and σ_{eff} : further reduction.





Rapidity distributions of K^+

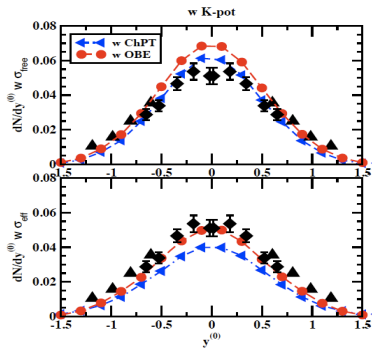
$Ni + Ni @ 1.93 A GeV$ $b < 4 fm$.

ChPT: σ_{free} good agreement with exp. data.

σ_{eff} : underestimation of the exp. data.

OBE: σ_{free} good agreement with exp. data.

σ_{eff} : on the exp. data.



Rapidity distributions of K^+

$Ni + Ni @ 1.93 A GeV$ $b < 4 fm$.

ChPT: σ_{free} good agreement with exp. data.

σ_{eff} : underestimation of the exp. data.

OBE: σ_{free} good agreement with exp. data.

σ_{eff} : on the exp. data.

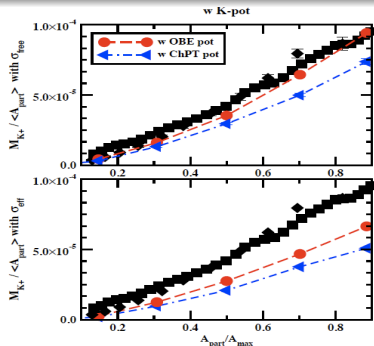
Centrality dependence K^+

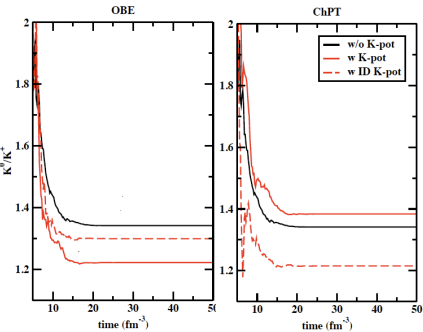
$Au + Au @ 1 A GeV$ collision.

Underestimation of the experimental data.

OBE: closer to the exp. data.

V. Prassa et al, Nucl.Phys. **A832** 88-99 (2010)





Temporal evolution of K^0/K^+

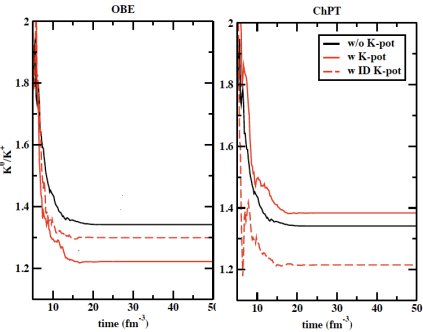
Central $Au + Au@1A\text{GeV}$.

OBE: reduction K^0/K^+ . Favors K^+ production.

ChPT: raise. Favors K^0 production.

IOBE: raise K^0/K^+ .

IChPT: sharp drop.

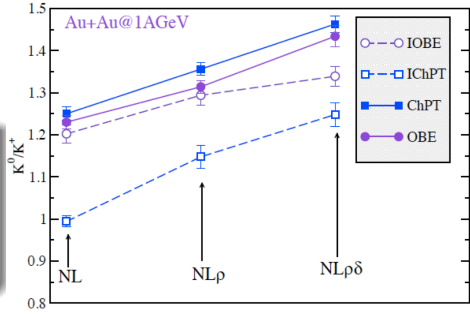


Temporal evolution of K^0/K^+

Central $Au + Au@1A\text{GeV}$.
OBE: reduction K^0/K^+ . Favors K^+ production.
ChPT: raise. Favors K^0 production.
IOBE: raise K^0/K^+ .
IChPT: sharp drop.

K^0/K^+ dependence on the EOS

Central $Au + Au@1A\text{GeV}$.
IChPT: reduction $\approx 20\%$.
IOBE: $NL\rho \approx 3\%$, while $NL\rho\delta \approx 5\%$.



Summary

● **Effective N-N cross sections:**

Dirac Brueckner Hartree Fock.

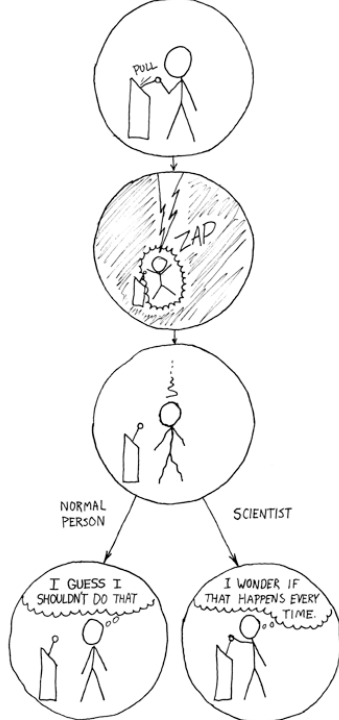
- **Pions:** reduction of production. At mid-rapidity good agreement with the data.
- π^-/π^+ : depends on the effective inelastic cross sections.
- **Kaons:** more affected ($\approx 30\%$).
- K^0/K^+ almost unchanged (large mean free path).

● **Kaon-nucleon potential**

- 1 Chiral Perturbation Theory, ChPT.
- 2 **One-Boson-Exchange, OBE.**
 - Reduction of kaon production.
 - Good agreement with the data (particularly with OBE).
 - **ChPT:** K^0/K^+ depends on the parametrization of the EOS.
 - **OBE:** K^0/K^+ more robust against the EOS parametrization.

Outlook

- Inclusion of momentum dependence.
T. Gaitanos, et al. Nucl.Phys. A828, 9-28 (2009).
- Improvement of NN-interactions.



THANK YOU FOR YOUR ATTENTION

Collaborations:

M. Di Toro, M. Colonna

LNS, Catania

H. H. Wolter

LMU, Muenchen

Theo Gaitanos

U. Giessen

G. A. Lalazisis

U. Thessaloniki