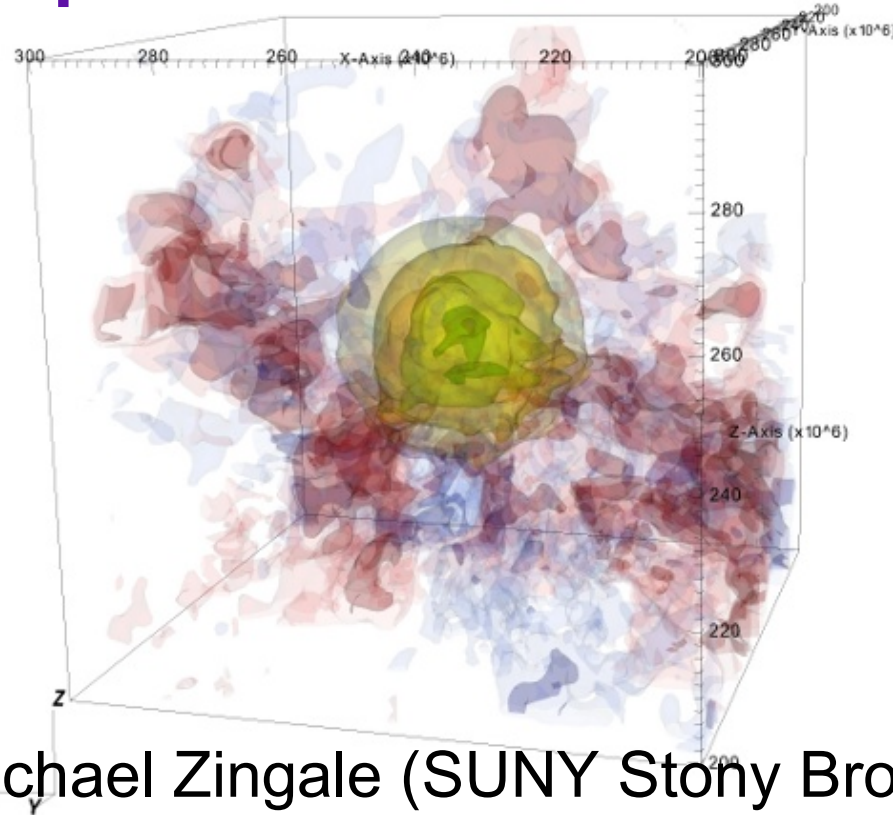


# The Challenges of Modeling Explosive Phenomena



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in collaboration with

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# Convection in Astrophysics

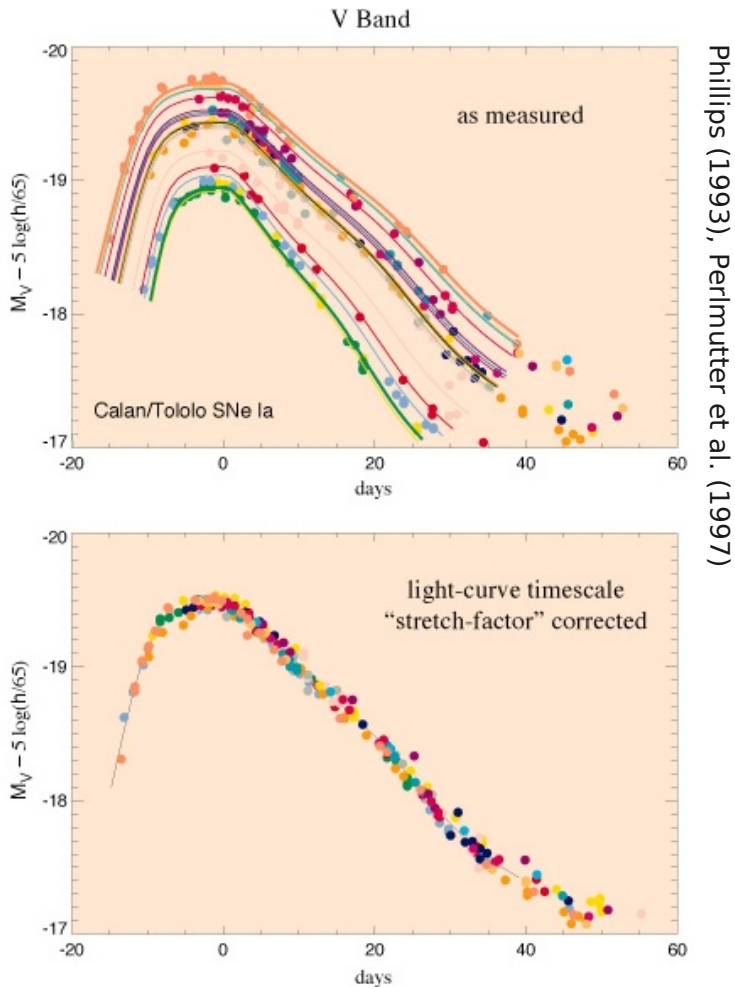
- Evolution of many stellar systems dominated by convective transport of energy
  - Supernovae (both thermonuclear and gravitational)
  - X-ray bursts and novae (thermonuclear explosion of accreted material on a surface of compact object)
  - General stellar evolution, including post main-sequence evolution of massive stars
- Often the convection is highly subsonic
  - Challenging for traditional astrophysical hydrodynamics codes
- **New algorithms are needed for efficient simulation of convective astrophysical flows**

# Type Ia Supernovae Observations

- Bright as host galaxy,  $L \sim 10^{43}$  erg s<sup>-1</sup>
- Large amounts of <sup>56</sup>Ni produced
  - Radioactivity powers the lightcurve



SN 1994D (High-Z SN Search team)



- No H seen in spectra, but strong Si, Ca, and Fe lines
- Occur in old stellar populations
- Lightcurve is robust
  - Variations can be corrected for via a single parameter function.
  - SNe Ia act as **standard candles**.

# Type Ia Supernovae

(single-degenerate scenario)

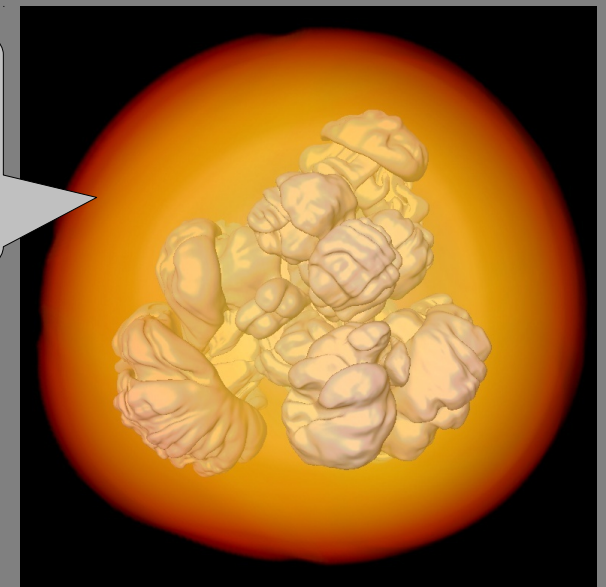
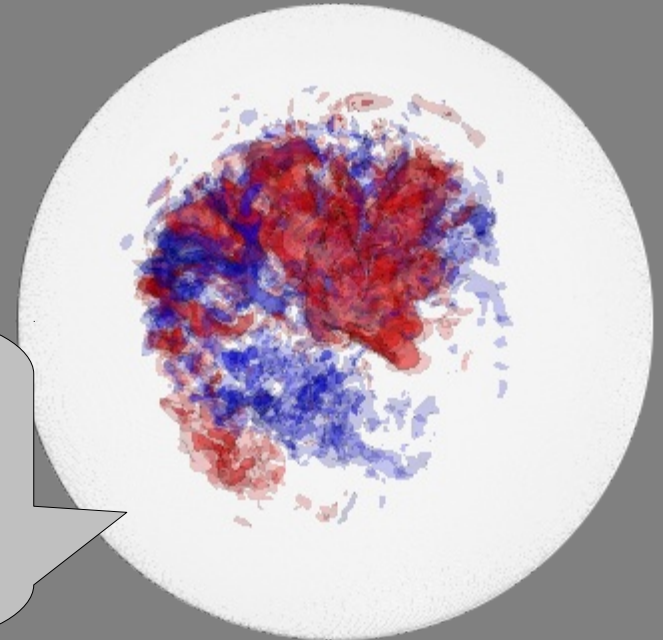


1 Accretion from binary companion. Grows to  $M_{\text{ch}}$

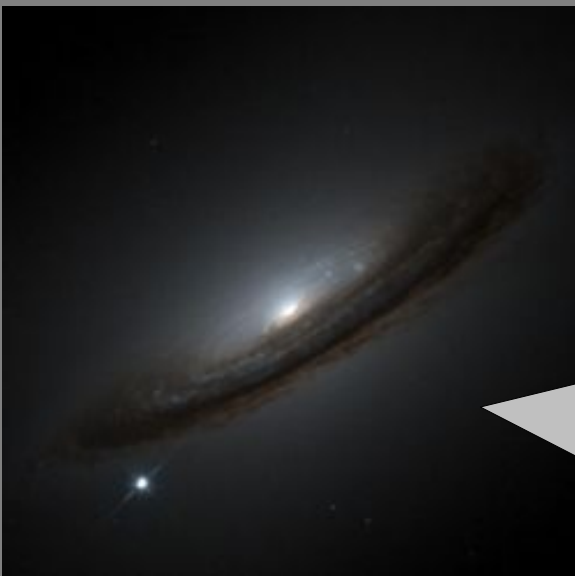
2 “Smoldering” phase—central T rises → flame born

3 Flame propagation. Initially subsonic, but detonation transition?

4 Explosion!  
Lightcurve powered by Ni decay. Width / luminosity relation.



(David A. Hardy & PPARC)



SN 1994D (High-Z SN Search team)

(Roepke and Hillebrandt 2005)

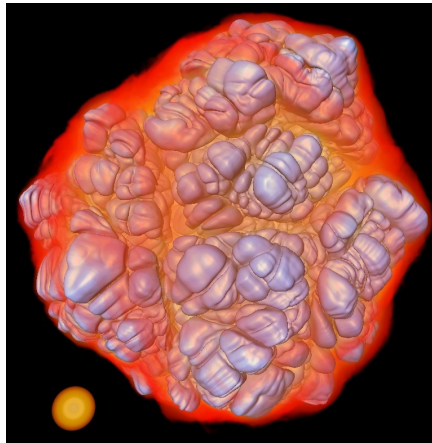
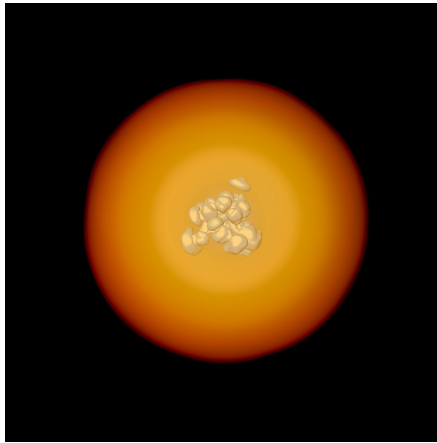
# Outstanding Questions in SNe Ia

- What is the progenitor?
  - Alternate models exist, including the merger of two white dwarfs
- Does the burning front remain subsonic or does it transition to a detonation?
  - A late time transition to a supersonic burning front (detonation) appears to give the best match to observations. Turbulence likely plays a key role in this transition.
- What are the initial conditions?
  - Variations in the spatial and temporal distribution of hot spots gives different explosion outcomes (Gracia-Senz & Bravo 2005, Plewa et al. 2004, Roepke et al. 2007, ...)
- What is the physical basis for the width-luminosity relationship in the lightcurve?
  - Some variation in the explosion is needed to account for the diversity in explosions.

Each of these questions requires a unique code.

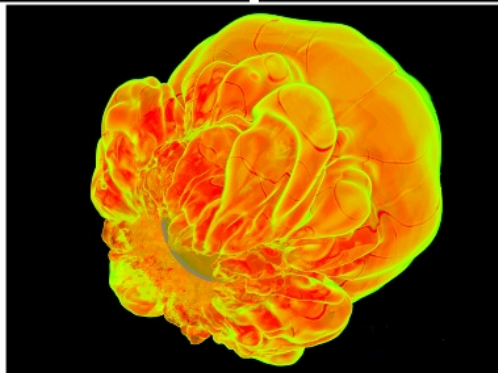
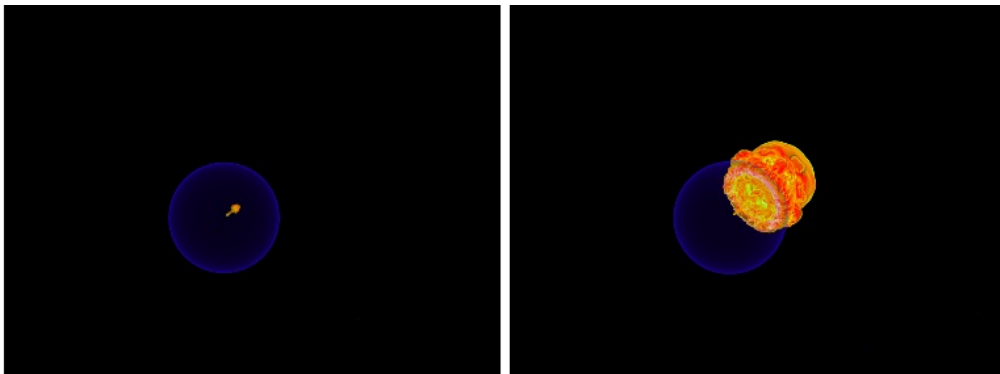
# Why Study Ignition?

▼ Roepke and Hillebrandt: ignition seeds in many points distributed around the center.



(Roepke and Hillebrandt 2005)

- Explosion outcome very sensitive to spatial and temporal distribution of initial flames (ignition points)
  - Single point on/off-center vs. multi-point explored by various groups
- Majority of explosion calculations begin with no initial velocity field



(Jordan et al. 2007)

◀ Jordan et al. 2007: Single off-centered ignition point leads to very asymmetric explosion. Also discussed in Plewa et al. 2004, Roepke and Woosley 2006.

... what does nature do?

# Multidimensional Simulations

- Nature is 3-d
  - Convection driven by nuclear energy release
  - Fluid instabilities / turbulence
  - Localized burning/runaway
  - Rotation
- Challenging simulations
  - Large computing / memory requirements
  - Making sense of enormous amounts of data
- SNe Ia begin with periods of low speed convection driven by nuclear energy release
  - Requires ability to model the domain for long timescales
- Requires a different algorithmic approach than those traditionally used in astrophysics

# Simulating Low Mach Phenomena

With explicit timestepping, information cannot propagate more than one zone per step:

$$\Delta t = \min \left\{ \frac{\Delta x}{|u| + c} \right\}$$

For  $M \equiv |u|/c \ll 1$  this is

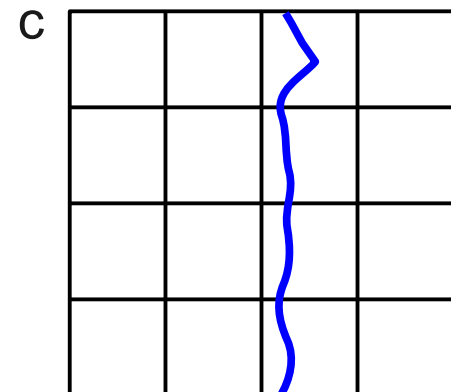
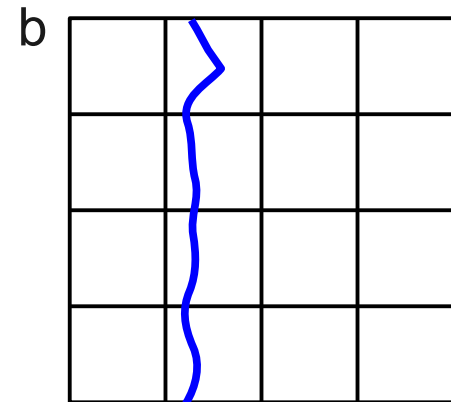
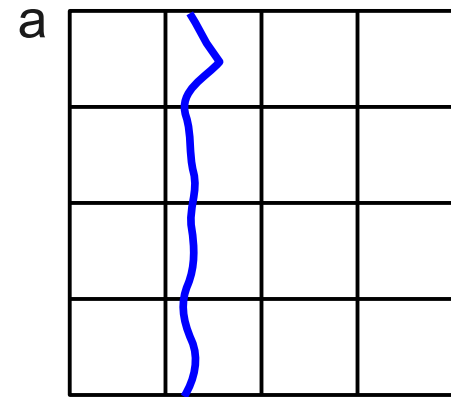
$$\Delta t \approx \frac{\Delta x}{c}$$

We would like to have

$$\Delta t \approx \frac{\Delta x}{|u|}$$

For very low Mach number flows, **it takes  $\sim 1/M$  timesteps for a fluid element to move more than one zone. Can't we do better?**

► A Mach 0.01 front moving to the right (a) initially, (b) after 1 step, (c) after 100 steps.





# MAESTRO: Low Mach Number Hydrodynamics

Almgren, Bell, Rendleman, & Zingale 2006 ApJ, 637, 922  
Almgren, Bell, Rendleman, & Zingale 2006, ApJ, 649, 927  
Almgren, Bell, Nonaka, & Zingale 2008, ApJ, 684, 449

- Reformulation of compressible Euler equations
  - Retain compressibility effects due to heating and stratification
  - Asymptotic expansion in Mach number decomposes pressure into thermodynamic and dynamic parts
  - Analytically enforce hydrostatic equilibrium through base state:

$$\nabla p_0 = \rho_0 g$$

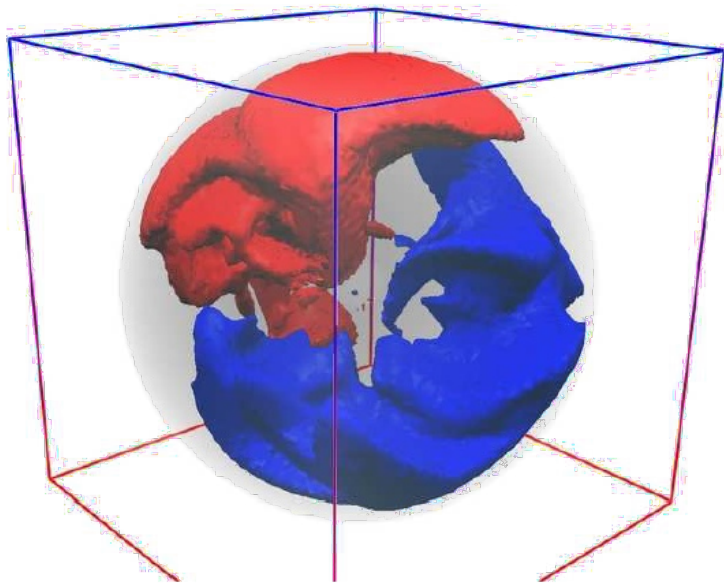
- Elliptic constraint on velocity field

$$\nabla \cdot (\beta_0 \mathbf{U}) = \beta_0 \left( S - \frac{1}{\bar{\Gamma}_1 p_0} \frac{\partial p_0}{\partial t} \right)$$

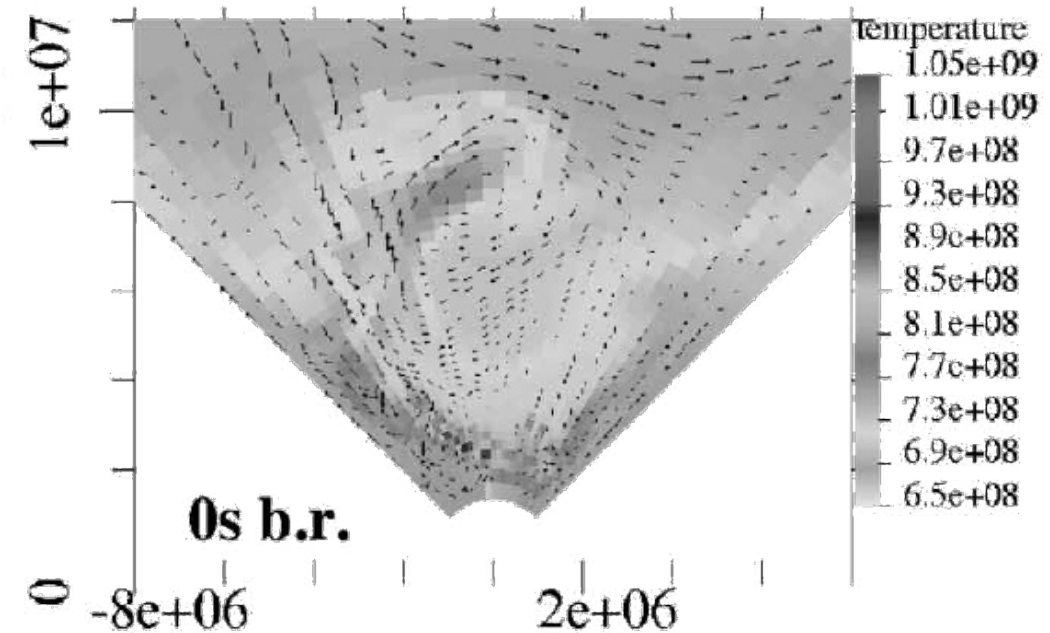
- $\beta_0$  is a density-like variable
  - $S$  represents heating sources
- **Timestep based on bulk fluid velocity, not sound speed**
- Weak scaling to  $\sim 100,000$  processors

# Previous SNe Ia Convection Calculations

► Hoflich and Stein modeled a 2-d wedge using an implicit code. Found flow caused compression near the center. Suggested ignition near the center.



(Kuhlen et al. 2006)



(Hoflich and Stein 2002)

◄ Kuhlen et al. modeled the convectively unstable region, with the very center cut out. They observed a characteristic dipole feature and suggested that off-center ignition was likely.

No previous calculations have modeled the entire star.

# Computational Demands

- Computer time measured in CPU-hours
- Single  $384^3$  run: ~1 million CPU-hours
- Single  $576^3$  run: ~7 million CPU-hours
  - 10368 processors (1728 MPI tasks  $\times$  6 OpenMP threads/MPI task)
  - 2100 plotfiles, each 18 GB in size = ~40 TB of data for a single run

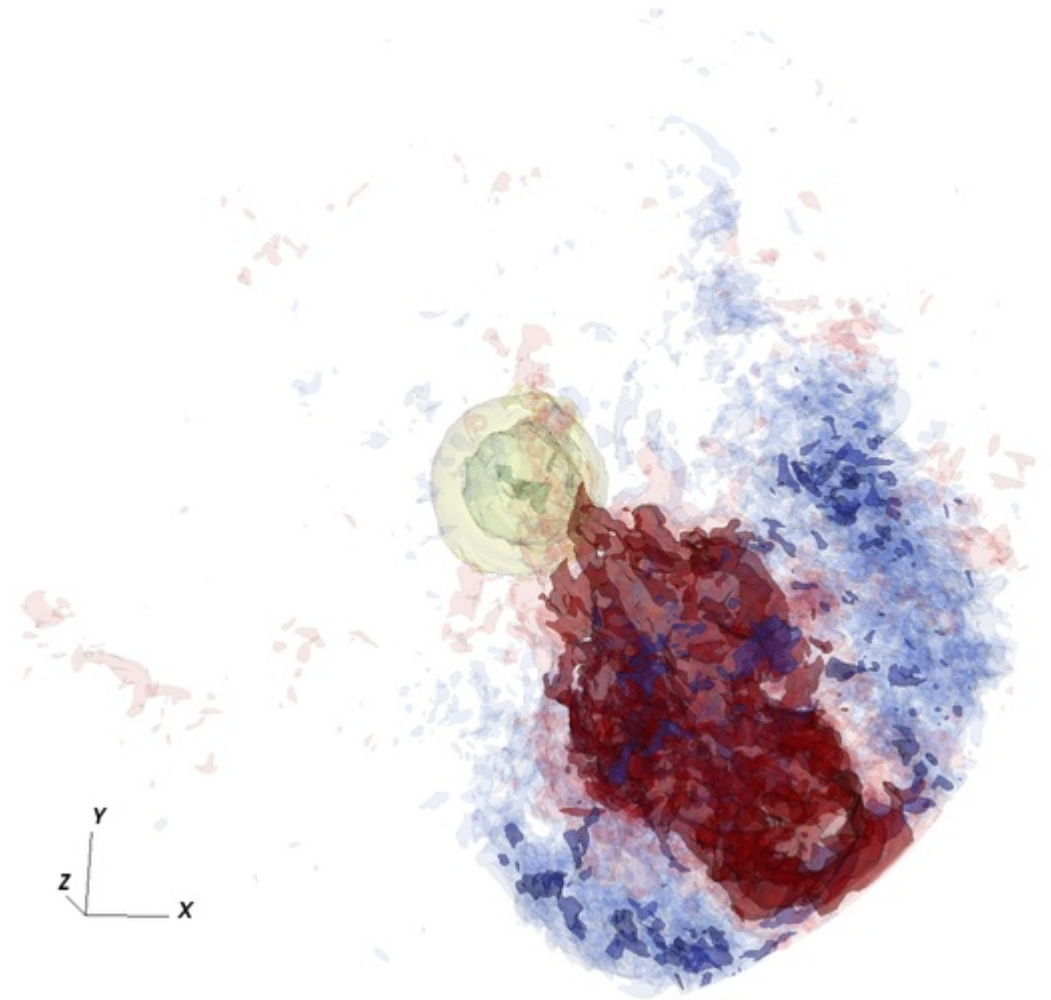


► The OLCF Cray XT5 jaguarpf machine at ORNL. This machine has 224,000 cores and is currently ranked #2 on the Top500 list.

# Pre-SNe Ia Convection: Dipole Convection

Zingale, Almgren, Bell, Nonaka, & Woosley 2009, ApJ, 704, 196.  
Nonaka, Aspden, Zingale, Almgren, Bell, & Woosley 2011, in preparation

- Dipole feature seen in previous calculations better described as a jet
  - Asymmetry in radial velocity field
- Direction changes rapidly

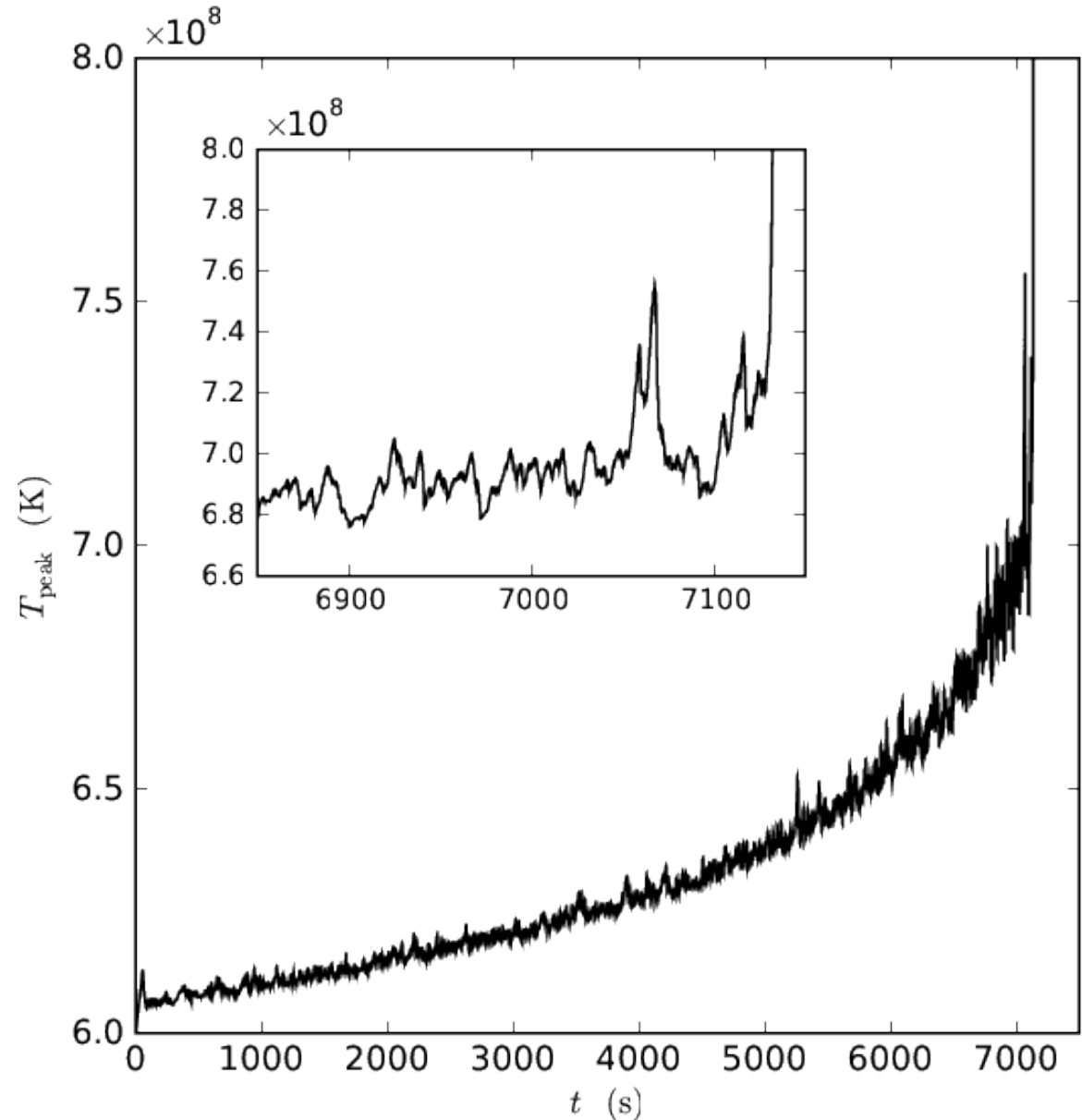


Radial velocity field (red = outflow; blue = inflow) in an  $1152^3$  non-rotating WD simulation.

# Pre-SNe Ia Convection: Runaway

Zingale, Almgren, Bell, Nonaka, & Woosley 2009, ApJ, 704, 196.

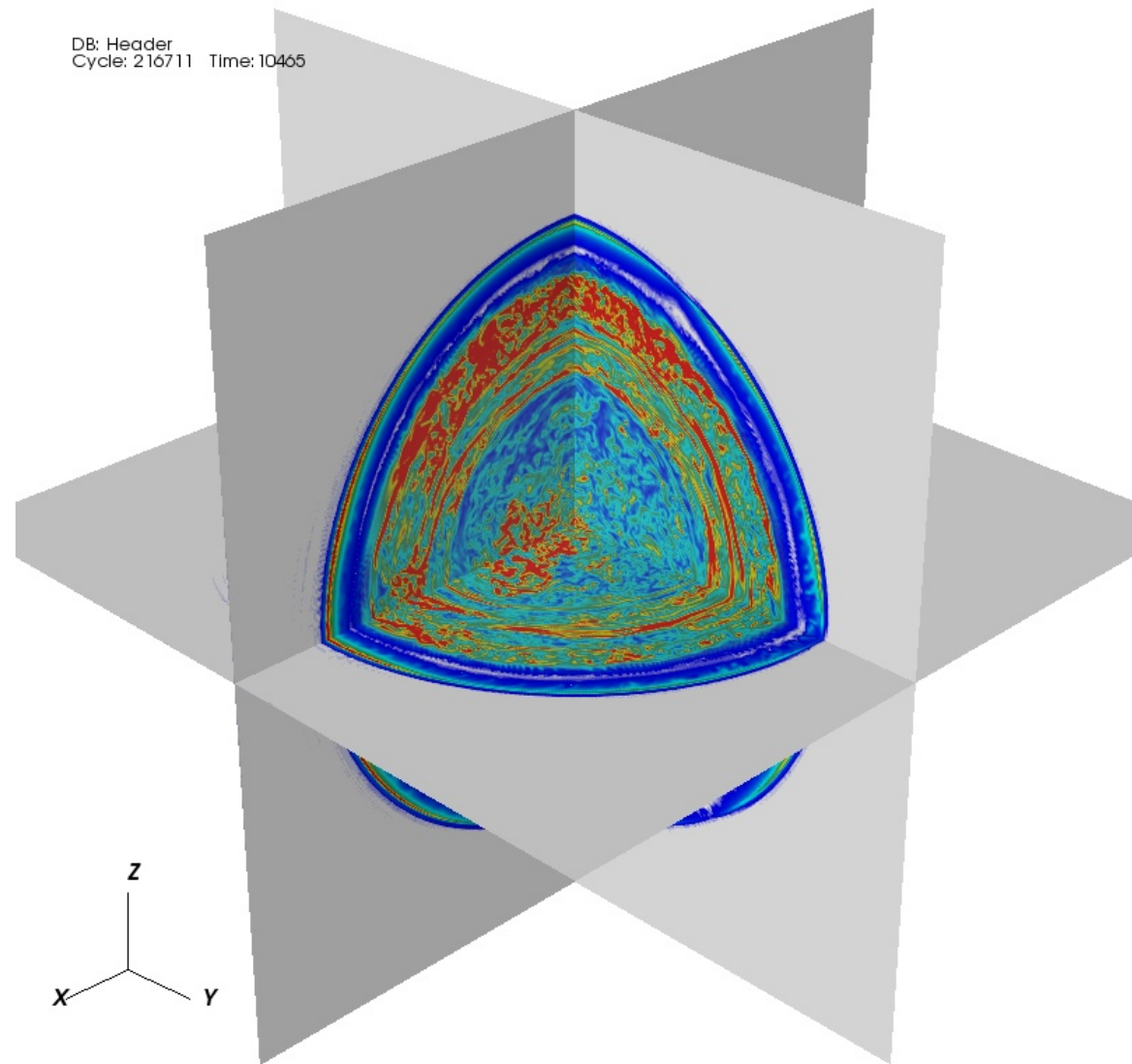
- Temperature increase nonlinear
  - Ignition occurs as  $T$  crosses  $8 \times 10^8$  K
  - “Failed” hotspots seen toward the end.



# Pre-SNe Ia Convection: Shear Layer

Zingale, Nonaka, Almgren, Bell, Malone, Woosley 2011, accepted to ApJ

- Clear separation between the convecting and stable regions
- Persists up to ignition
  - Strong shearing here will greatly affect the flame evolution



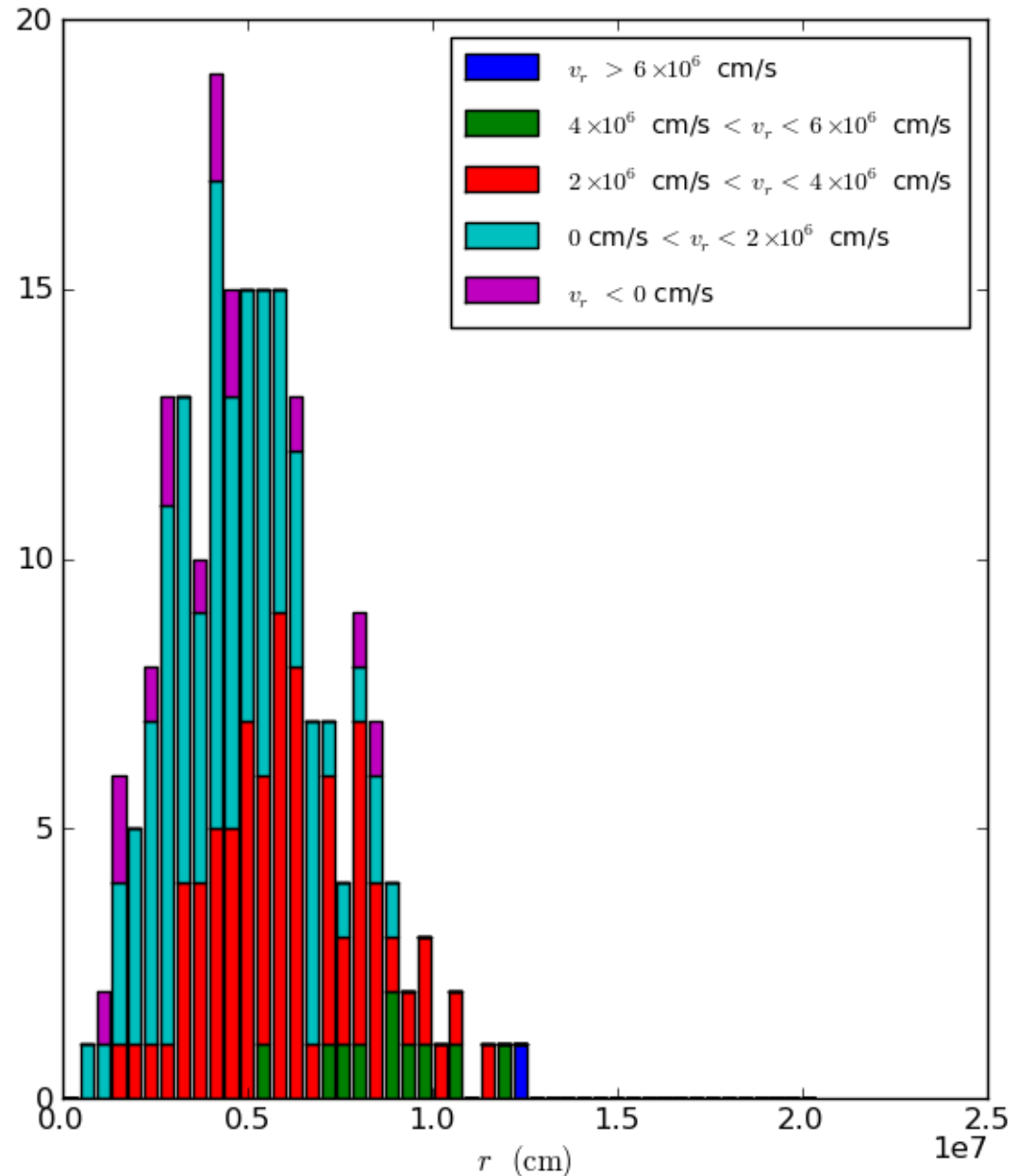
Vorticity field in a non-rotating model.

# Pre-SNe Ia Convection: Ignition Radius Likelihood

Zingale, Nonaka, Almgren, Bell, Malone, Woosley 2011, accepted to ApJ

- Distribution of likely ignition locations
  - Average hotspot radius over 1 s intervals
  - Consider final 200 s of evolution
- Vast majority of hotspots are moving outward from the center
- **Off-center ignition likely**

► Histogram of likely ignition radii from 576<sup>3</sup> non-rotating model. Hotspot radii are averaged into 1 s intervals and colored by radial velocity.

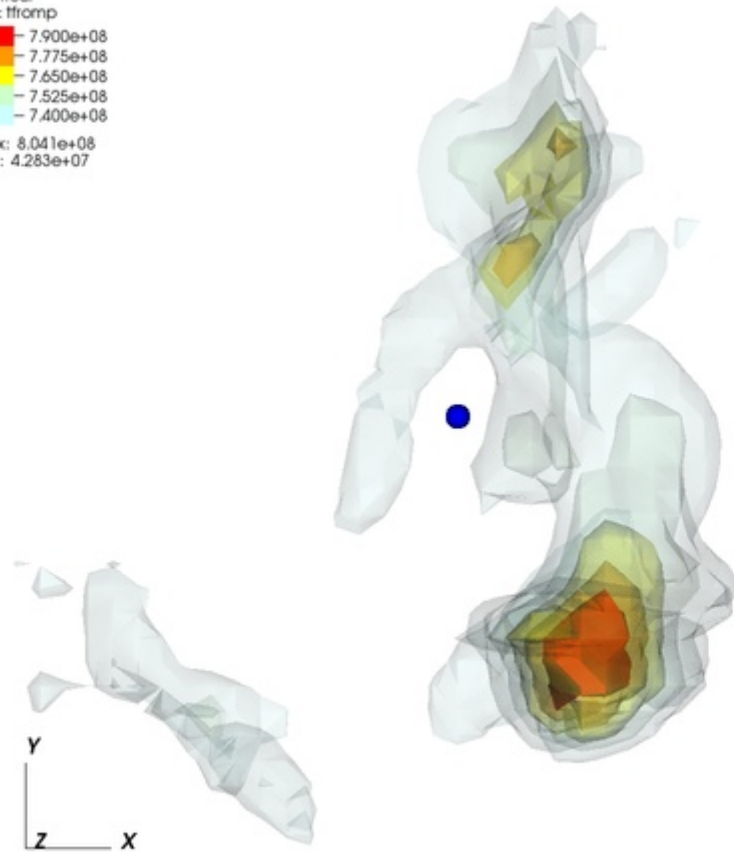


# Pre-SNe Ia Convection: Multiple Ignition?

Nonaka, Aspden, Zingale, Almgren, Bell, Woosley 2011, in preparation

- Disable burning in a hot spot once it ignites to allow further evolution
- Second hot spot is not present over a short timescale
- Single-point, off-center ignition most likely.

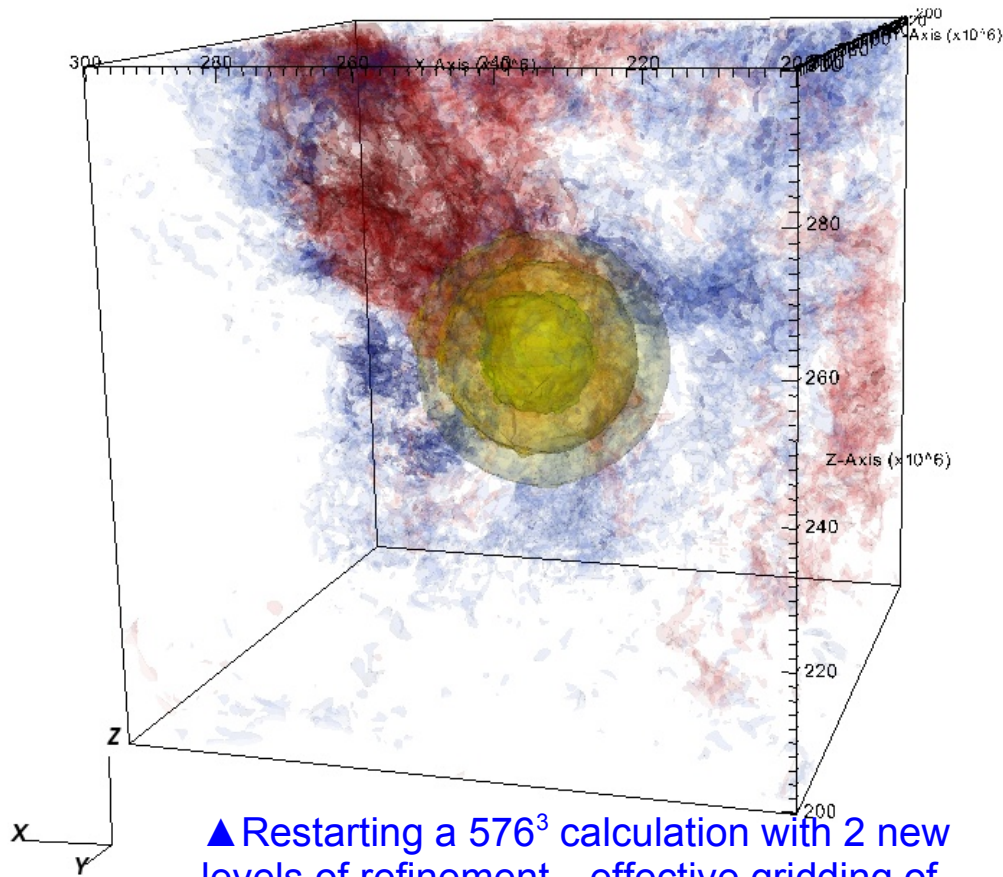
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Cycle: 231637 Time:10563  
Contour  
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Min: 4.283e+07



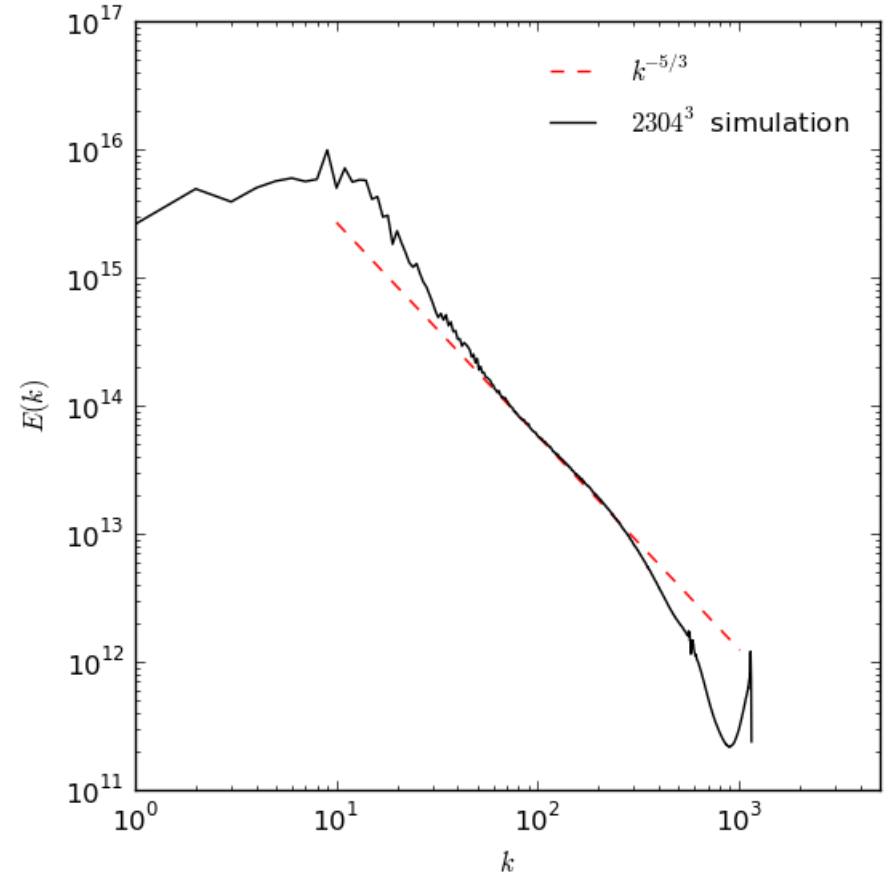


# Current Work: Turbulent Properties

Nonaka, Aspden, Zingale, Almgren, Bell, Woosley 2011, in preparation



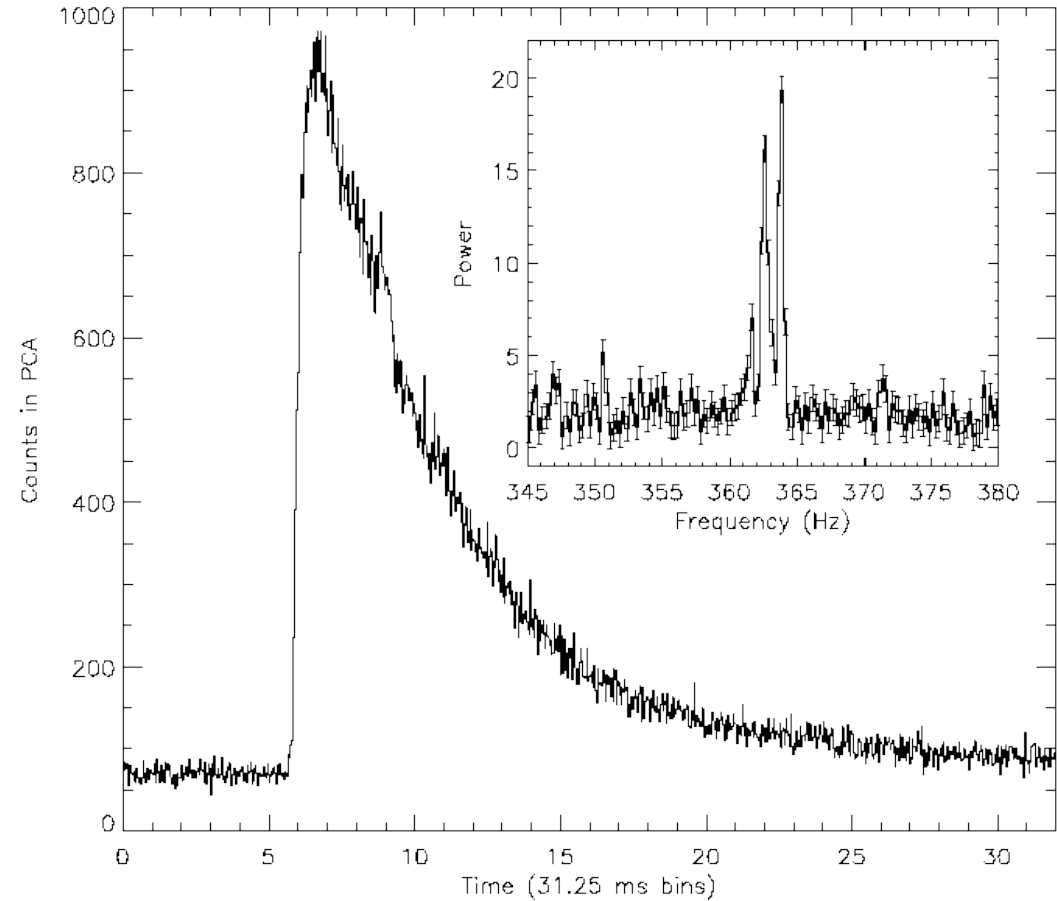
▲ Restarting a  $576^3$  calculation with 2 new levels of refinement—effective gridding of  $2304^3$  (~2 km resolution)



- High resolution simulations show a well-resolved turbulent cascade
- Integral scale large/turbulent intensity small → turbulence unlikely to affect flame propagation.
- Velocities in stable region are much higher/shearing.

# X-ray Bursts

- Thermonuclear runaway in thin accreted H/He layer on surface of a neutron star
- Accretion timescale  $\sim$  hours to days
- Runaway timescale  $\sim$  seconds
- $> 70$  sources known, some with 10s or more individual bursts.
- Potential site for rp-process nucleosynthesis



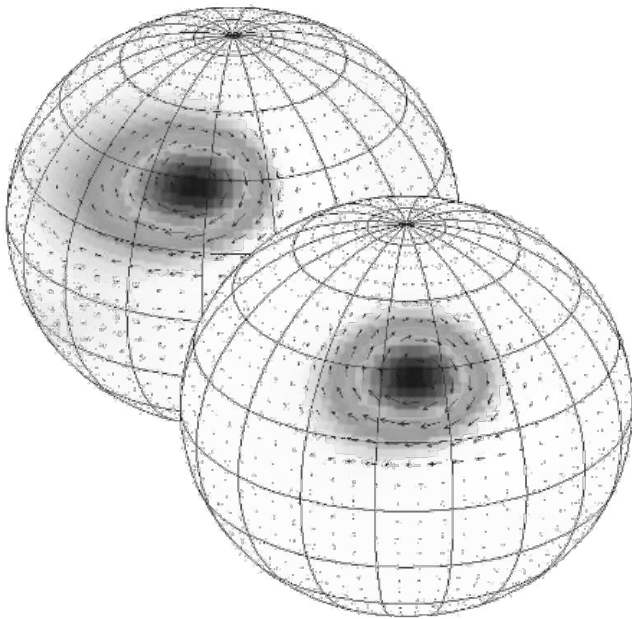
Strohmayer et al., 1996, ApJ, 469:L9

# Outstanding Questions in XRBs

- How does the fuel spread over the surface?
- How does the ignition begin?
- Is the burning localized?
- Does convection modify the nucleosynthesis?
- What are the effects of rotation?
- Does convection bring ash to the surface?

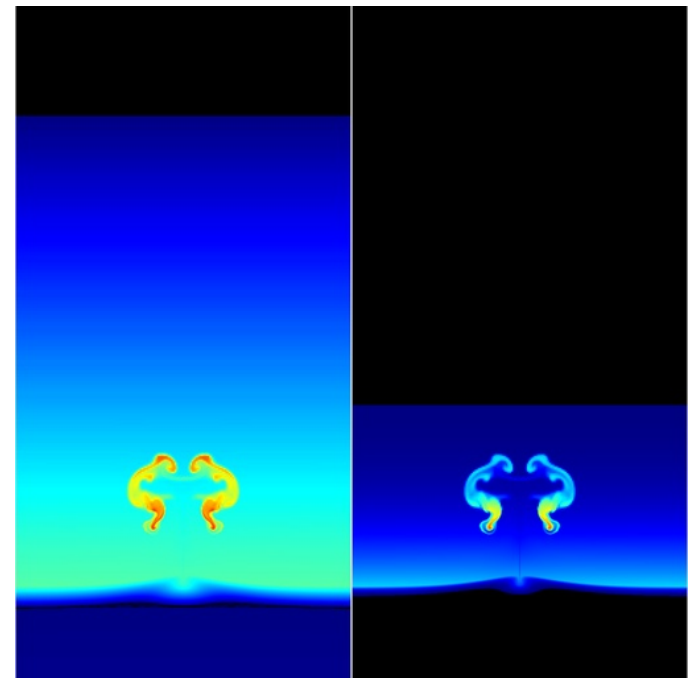
# Localization

- Accreted layer not degenerate enough to localize a hot spot
  - Fizzles out, maybe stirs
  - Similar to nova (Shankar & Arnett 1994)



(Adapted from Strohmayer and Bildsten 2003)

Fig. 3.13. Initial evolution of a burning hot spot ignited off the equator as seen in a frame rotating with the neutron star. Velocity vectors show the circulation of the fluid induced by the Coriolis forces. The hot spot expands due to burning and drifts west-southwest because of the latitude dependence of the Coriolis force (after Spitkovsky, Levin & Ushomirsky 2002).



MAESTRO simulation ( $L = 3.84$  m,  $\Delta x = 0.5$  cm) evolved to  $t = 1.5 \times 10^{-5}$  s showing dissipation of a hot spot (initial  $T = 10^9$  K) in a He NS accreted layer. Temperature is shown on the left, nuclear energy generation rate is shown on the right.

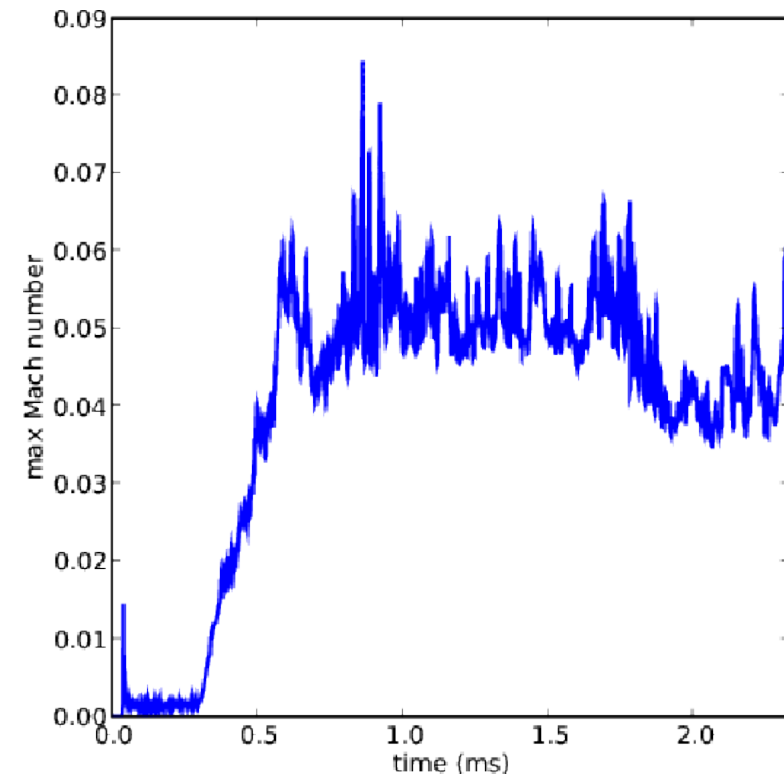
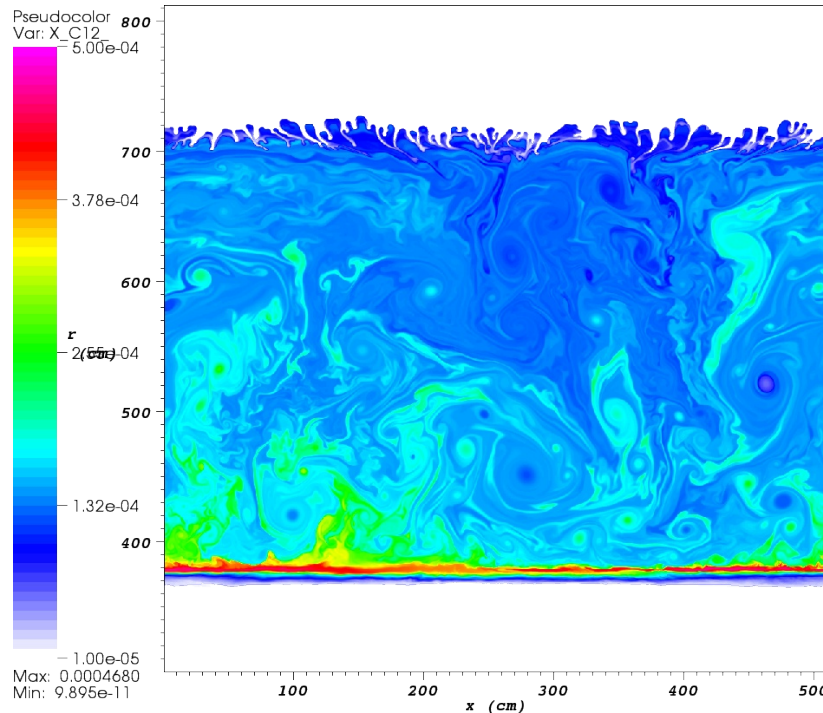
- Spitkovsky et al. (2001)
  - Shallow-water calculations of spreading on NS
  - Coriolis force balances lateral spreading of burning front
  - Simplified vertical structure

# X-ray Burst Modeling

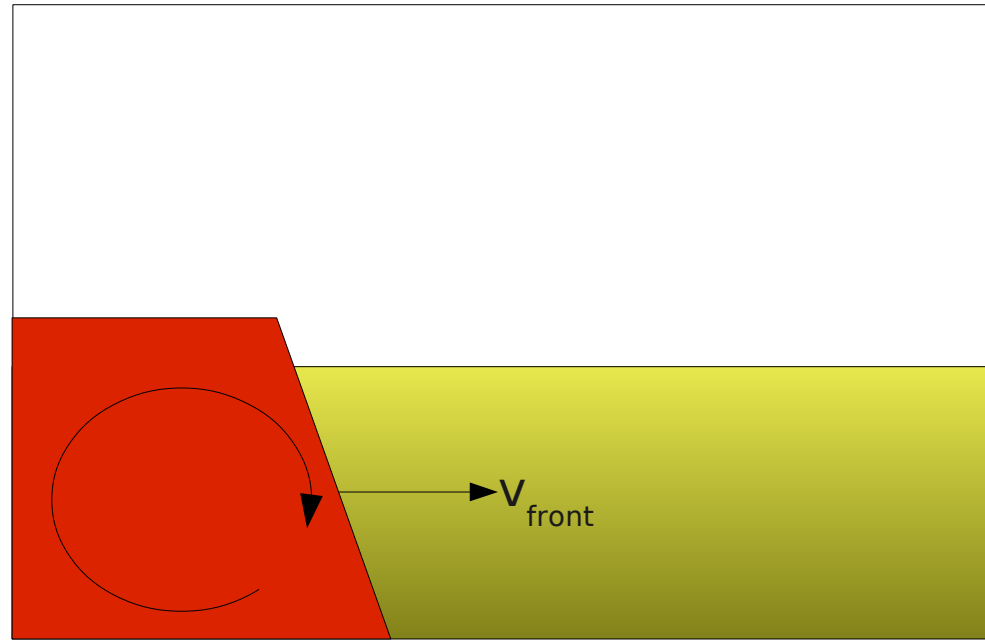
Malone et al. 2011, ApJ, 728, 118

- Pure He layers
  - Convective energy transport develops quickly
  - Resolution requirements much higher than previously thought
  - 2-d simulations challenging. 3-d?
- Mixed H/He bursts underway
  - Nuclear physics more time consuming
  - Steep composition change challenging

► Convection in an He layer on a neutron star, modeled by graduate student Chris Malone.



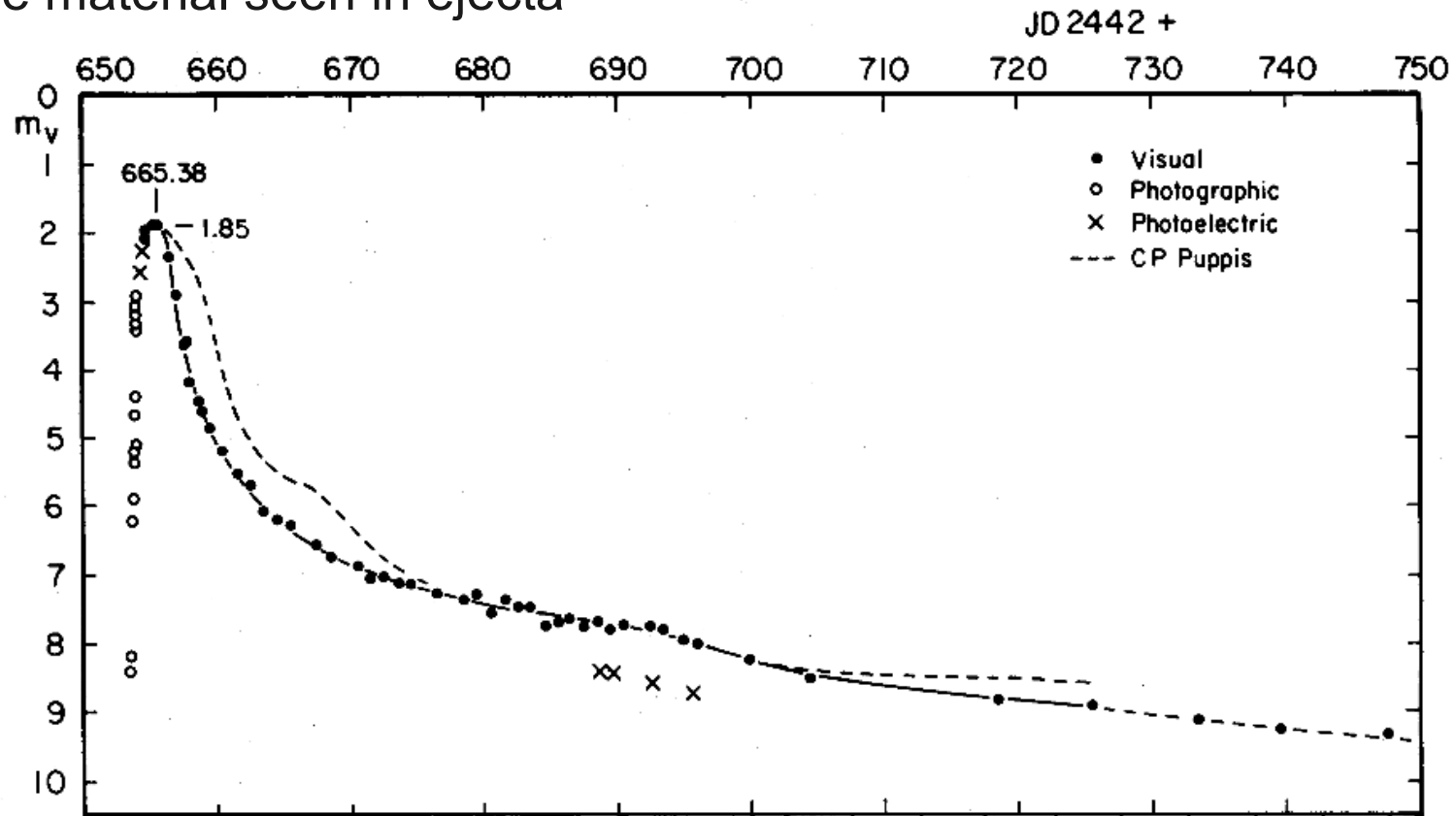
# What Can't We Do (Now)?



- Lateral flame propagation w/ resolved nuclear physics
  - Low Mach methods cannot (currently) describe two different scale heights (fuel and ash)
  - Lengthscale for Coriolis force to balance pressure gradient (Rossby length):  $L = \sqrt{gH_0/f} \sim \text{few km}$ 
    - Much bigger domain that we currently use

# Novae

- Explosion of surface H layer on white dwarf
  - Similar progenitor system to SNe Ia (but much fainter)
  - Recur when new layer of fuel is accreted (recurrence times of decades to 1000s of years, depending on white dwarf mass)
  - CNO burning required to explain luminosity
  - Core material seen in ejecta



(Young, Corwin, Bryan, and De Vaucouleurs)

# Novae

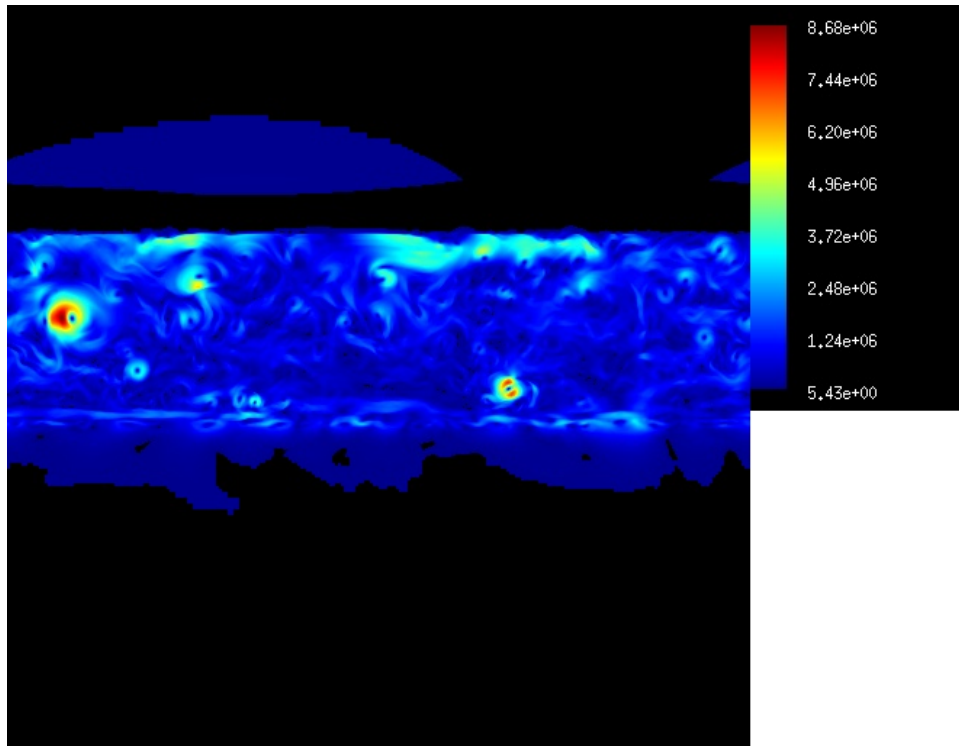
- **Biggest issue: dredge-up**
  - Underlying C/O needed to catalyze the reaction—enrichment by at least order-of-magnitude
  - Convection? Shear instabilities during accretion? Mass diffusion?  
(Livio and Truran 1990)
- Does the WD gain or lose mass as a result of the explosion?
- Can novae be SNe Ia progenitors?



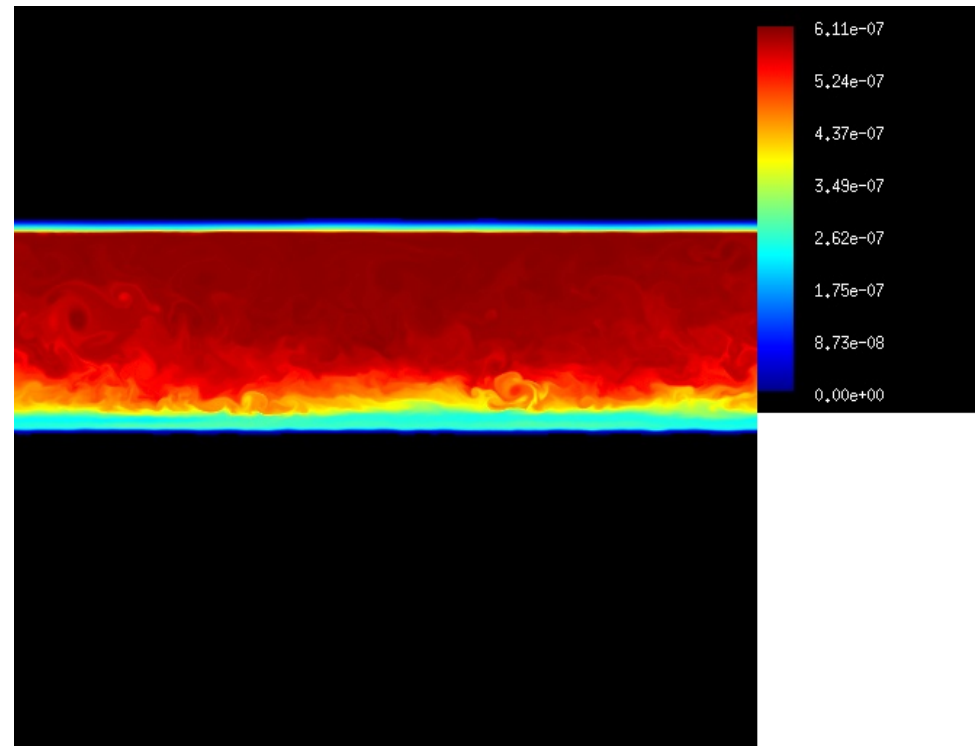
# Novae

- Numerical challenges

- Numerical mixing at base of accretion layer can artificially enhance burning
- Expansion is significant—needs to be tracked to accurately model dynamics.



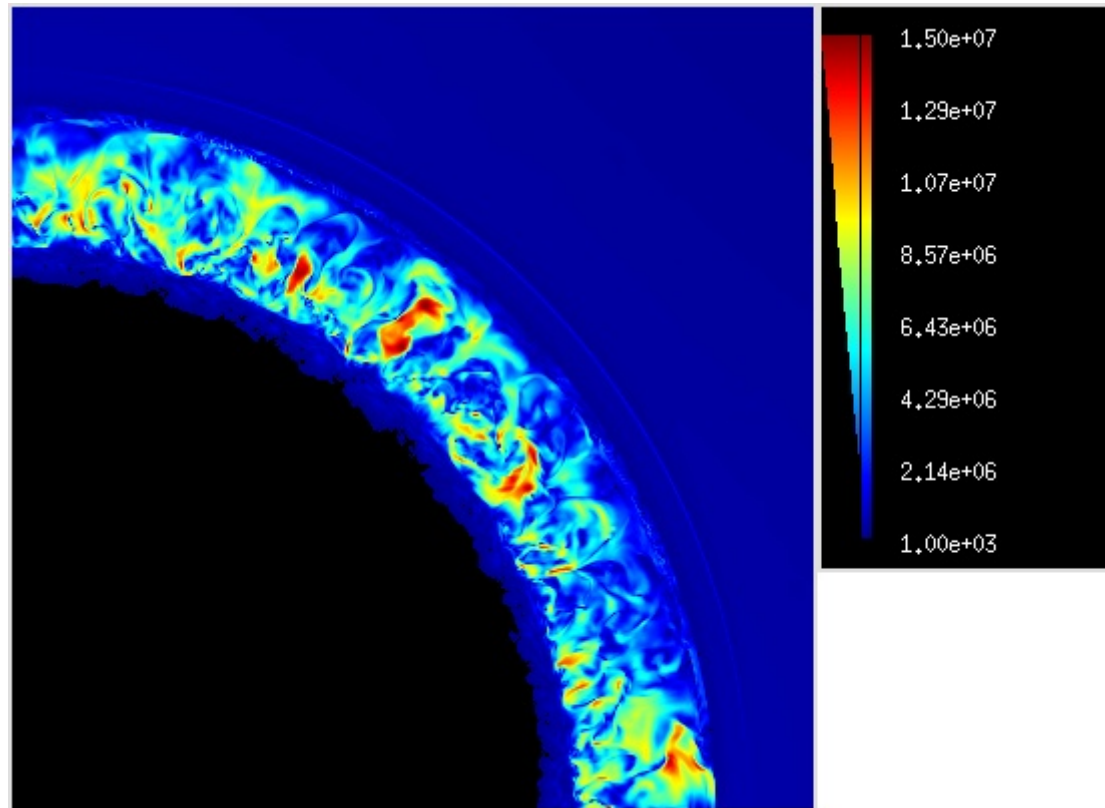
Velocity magnitude



$^{15}\text{N}$  abundance

# sub-Chandra SNe Ia Models

- Numerical challenges
  - Convective region potentially extends to the “top” of the star—difficult to capture steep gradient.



Slice through 3-d domain of vorticity in He layer on surface of  $1.0 M_{\odot}$  WD.

# Summary / What's Next?

- Modern algorithms / supercomputers can model convective astrophysical flows for many turnover times in 3-d.
  - Requires involvement of many different disciplines: mathematics, computational science, application scientists.
- Convection in pre-SNe Ia white dwarfs:
  - Rapidly changing convective field
  - Range of ignition locations: between central and ~80 km off-center
  - Details of ignition distribution can be learn by looking at late time fluctuations
  - Single-point, off-center ignition likely

# Summary / What's Next?

- X-ray bursts
  - Low Mach number hydrodynamics provides an efficient means for modeling convection on neutron stars
  - Exploring mixed H/He burning underway.
- Applications to nova, sub-Chandra SNe Ia ignition, and H core convection in massive stars underway.
- Future Work
  - Addition of long wavelength acoustics to extend range of validity of low Mach number model
  - Work on understanding limits to method
  - Restart ignition calculation in compressible code to follow the subsequent flame evolution.