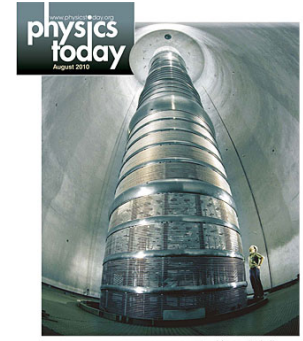


Recent progress and new challenges
in *ab initio* nuclear structure and nuclear reactions

James P. Vary
Iowa State University

Extreme Computing and its Applications
Institute of Nuclear Theory
June 6, 2011

Ab initio nuclear physics - fundamental questions



- What controls nuclear saturation?
- How the nuclear shell model emerges from the underlying theory?
- What are the properties of nuclei with extreme neutron/proton ratios?
- Can we predict useful cross sections that cannot be measured?
- Can nuclei provide precision tests of the fundamental laws of nature?
- Under what conditions do we need QCD to describe nuclear structure?



Jaguar



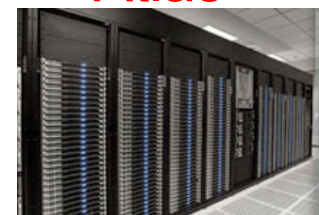
Franklin



Blue Gene/p



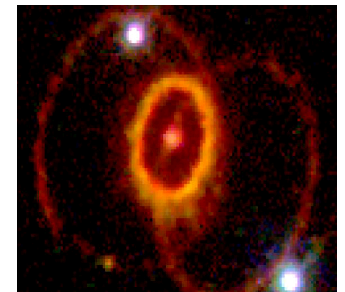
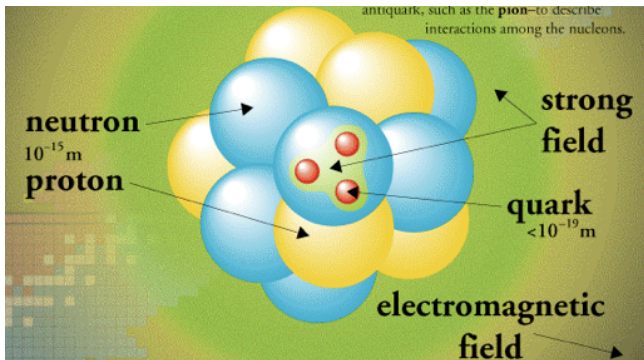
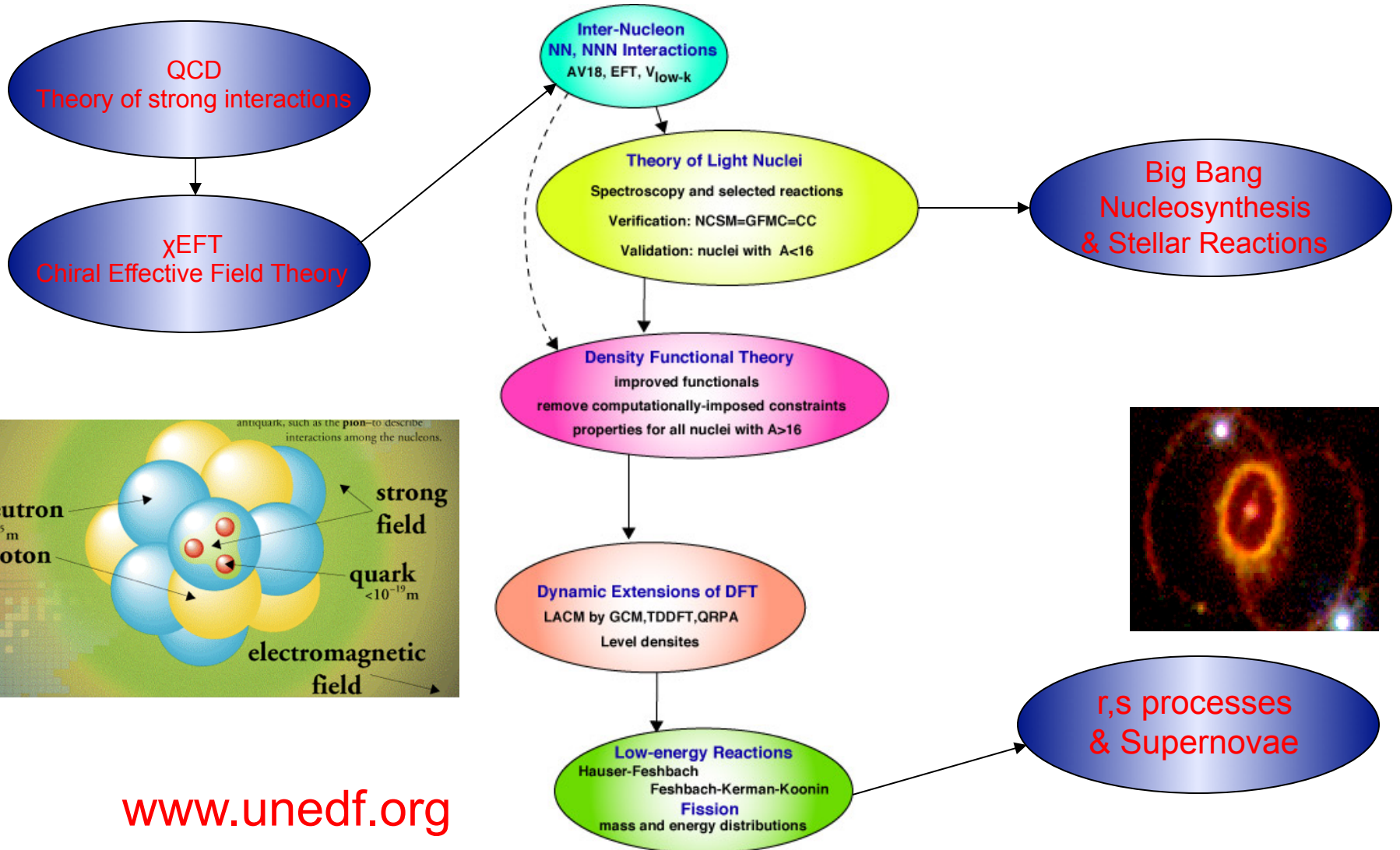
Atlas





UNEDF SciDAC Collaboration

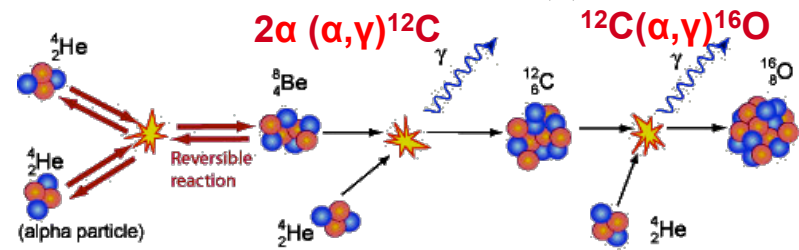
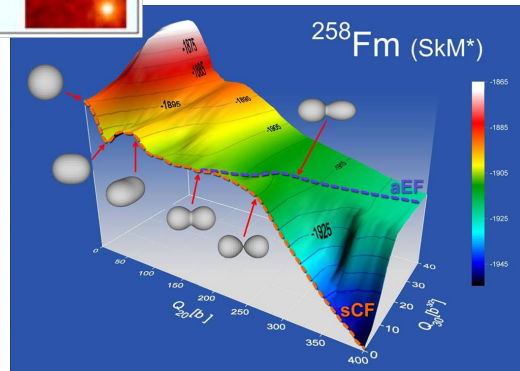
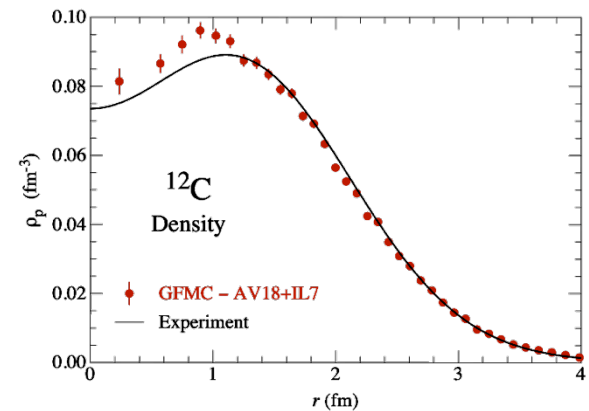
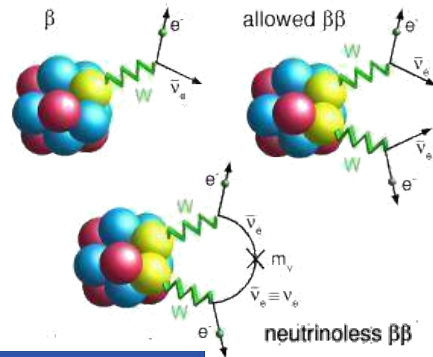
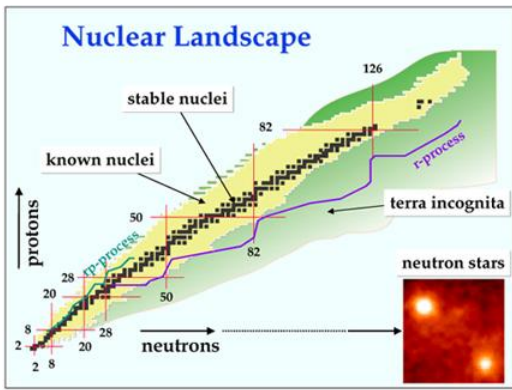
Universal Nuclear Energy Density Functional

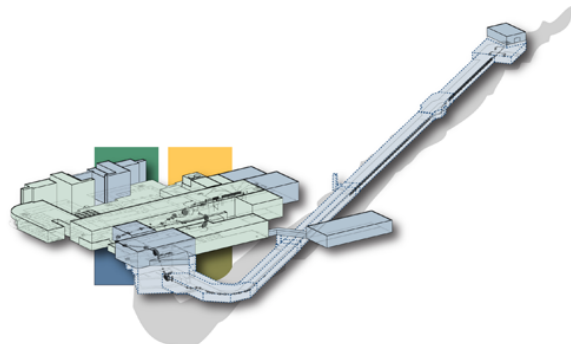
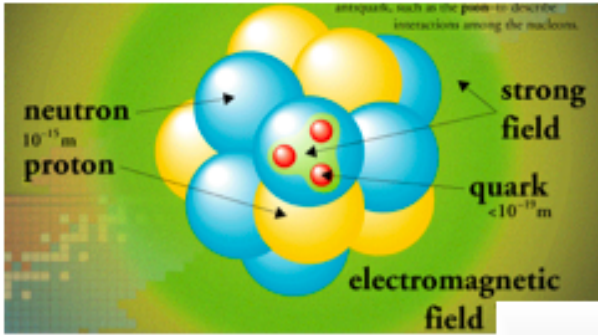


DOE Workshop on Forefront Questions in Nuclear Science
 and the Role of High Performance Computing,
 Gaithersburg, MD, January 26-28, 2009
Nuclear Structure and Nuclear Reactions

List of Priority Research Directions

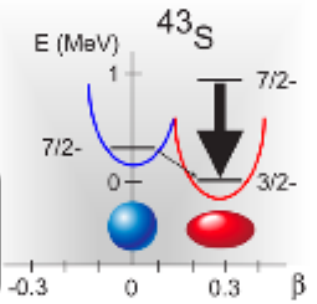
- Physics of extreme neutron-rich nuclei and matter
- Microscopic description of nuclear fission
- Nuclei as neutrino physics laboratories
- Reactions that made us – triple α process and $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$





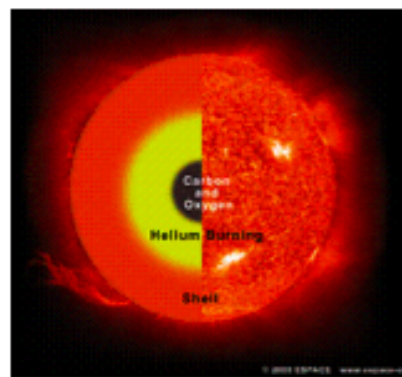
$^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$
 ^{132}Sn structure

Ab initio structure
in light nuclei



^{78}Ni structure

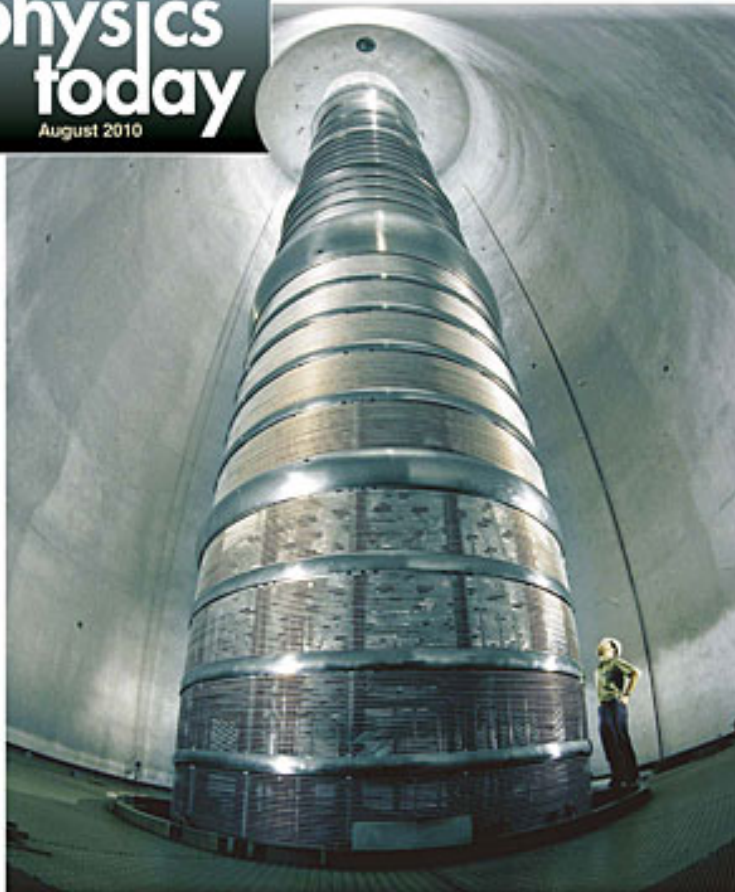
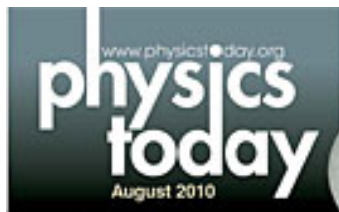
$^8\text{Be}(\alpha,\gamma)^{12}\text{C}$



10x tera 100x tera peta 10x peta 100x peta 1 exaflop year

Testing the doubly magic character of tin-132

Adding an extra neutron to a nucleus with magic numbers of both neutrons and protons, and watching how it settles in, tests the shell model and can help elucidate the creation of heavy elements in supernovae.



Doubly magic shell game

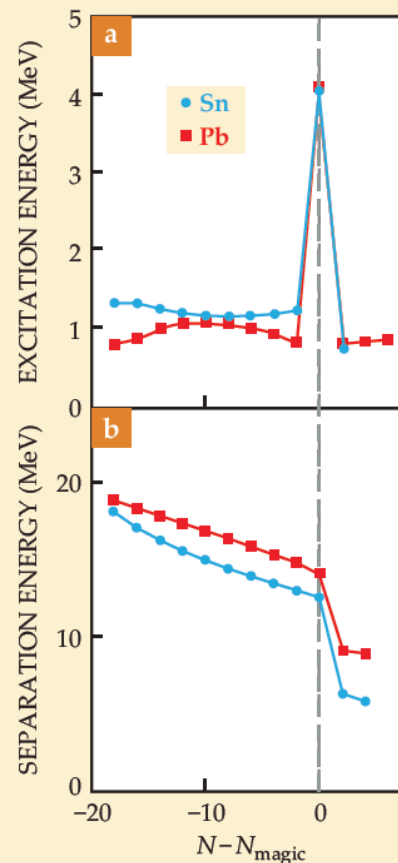


Figure 2. Doubly magic nuclides tin-132 and lead-208 clearly manifest special properties when compared, from archival data, with lighter isotopes that also have even neutron numbers N . **(a)** The energy of the first electric-quadrupole excitation peaks dramatically at N_{magic} (82 for Sn, 126 for Pb). **(b)** The energy cost of removing a neutron pair falls abruptly after N_{magic} . (Adapted from ref. 1.)

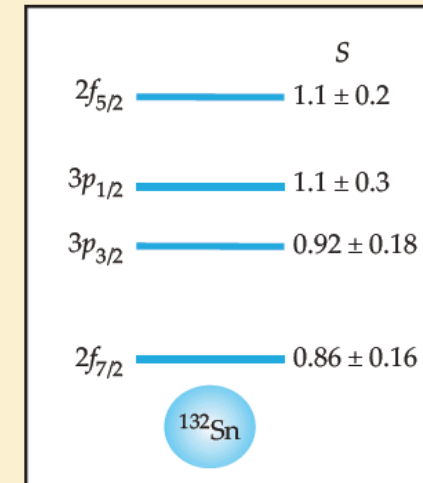


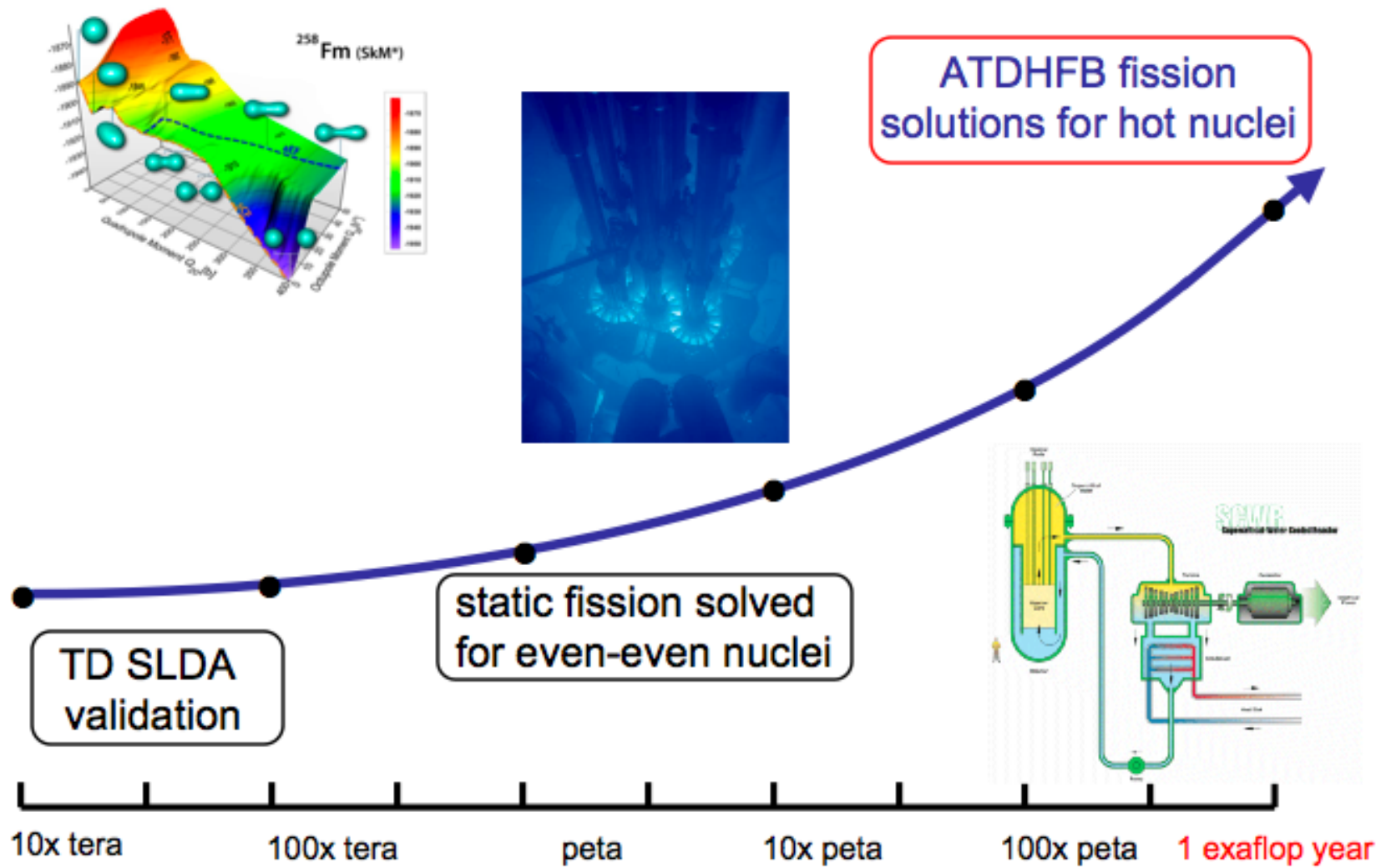
Figure 4. Valence states of the extra tin-133 neutron. For each of the valence levels observed in the Oak Ridge experiment, schematically shown above the doubly magic ^{132}Sn core, the best-fit quantum state is given (left) together with its spectroscopic factor S (right), a measure of spectral purity. In the spectroscopic notation, p and f denote, respectively, orbital angular momenta 1 and 3. If the best-fit state is pure, with no admixture of other quantum states due to core excitations, $S = 1$. (Adapted from ref. 1.)

Based on:

K.L. Jones, et al., *Nature* **465**, 454 (2010)

P. Cottle, *Nature* **465**, 430 (2010)

A publication of the American Institute of Physics



All interactions are “effective” until the ultimate theory unifying all forces in nature is attained.

Thus, even the Standard Model, incorporating QCD, is an effective theory valid below the Planck scale
 $\lambda < 10^{19} \text{ GeV}/c$

The “bare” NN interaction, usually with derived quantities, is thus an effective interaction valid up to some scale, typically the scale of the known NN phase shifts and Deuteron gs properties
 $\lambda \sim 600 \text{ MeV}/c (3.0 \text{ fm}^{-1})$

Effective NN interactions can be further renormalized to lower scales and this can enhance convergence of the many-body applications
 $\lambda \sim 300 \text{ MeV}/c (1.5 \text{ fm}^{-1})$

“Consistent” NNN and higher-body forces are those valid to the same scale as their corresponding NN partner, and obtained in the same renormalization scheme.

ab initio renormalization schemes

SRG: Similarity Renormalization Group

LSO: Lee-Suzuki-Okamoto

Vlowk: V with low k scale limit

UCOM: Unitary Correlation Operator Method
and there are more!

The Nuclear Many-Body Problem

The many-body Schroedinger equation for bound states consists of $2^A \binom{A}{Z}$ coupled second-order differential equations in $3A$ coordinates using strong (NN & NNN) and electromagnetic interactions.

Successful *ab initio* quantum many-body approaches ($A > 6$)

Stochastic approach in coordinate space
Greens Function Monte Carlo (**GFMC**)

Hamiltonian matrix in basis function space
No Core Shell Model (**NCSM**)
No Core Full Configuration (**NCFC**)

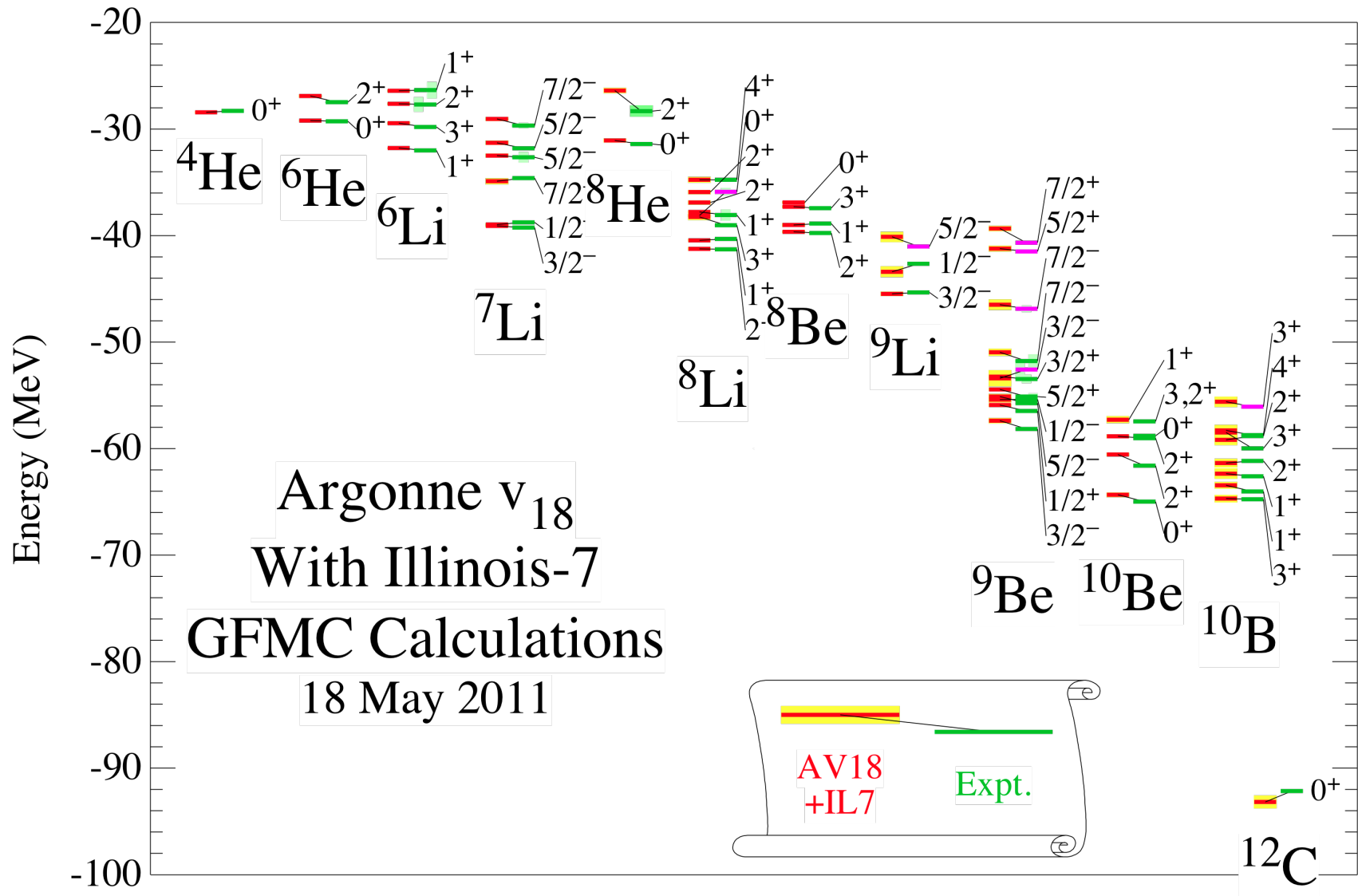
Cluster hierarchy in basis function space
Coupled Cluster (**CC**)

Lattice + EFT approach (New)

Comments

All work to preserve and exploit symmetries
Extensions of each to scattering/reactions are well-underway
They have different advantages and limitations

REPRODUCTION OF NUCLEAR LEVELS



AV18+IL7 reproduces ~50 levels (+ ~60 isobaric analogs) up to ¹²C with rms error ~0.6 MeV
 We have motivated or supported experimental work in almost all these nuclei

VMC FOR ASYMPTOTIC NORMALIZATION COEFFICIENTS (ANC)

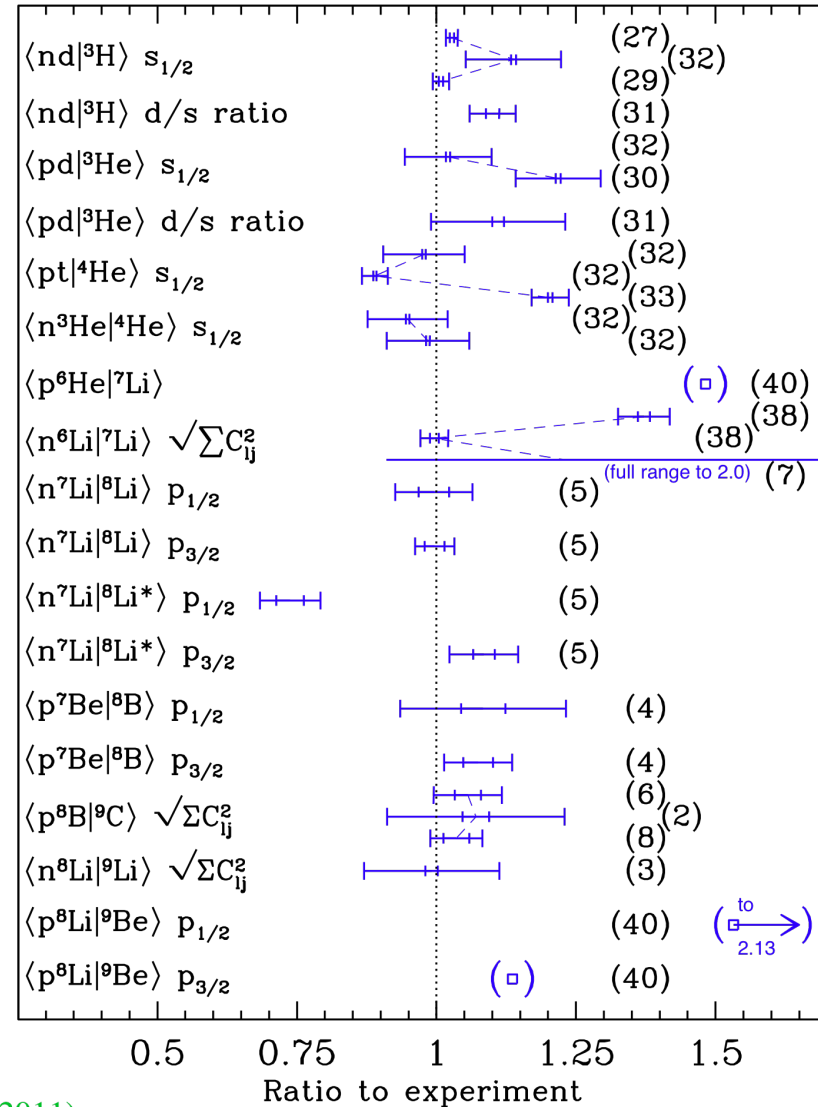
$$\Phi(r \rightarrow \infty) = \langle \Psi_{A-1} | a_{\ell j}(r \rightarrow \infty) | \Psi_A \rangle = C_{\ell j} W_{-\eta, \ell + \frac{1}{2}}(2kr)/r$$

- Best laboratory handle on many astrophysical reactions
- Much recent expt. interest
- Normalization to overlap tails is difficult
- The ANC can be recast into a short-ranged integral

$$C_{\ell j} \sim \mathcal{A} \int M_{-\eta, \ell + \frac{1}{2}}(2kr)/r$$

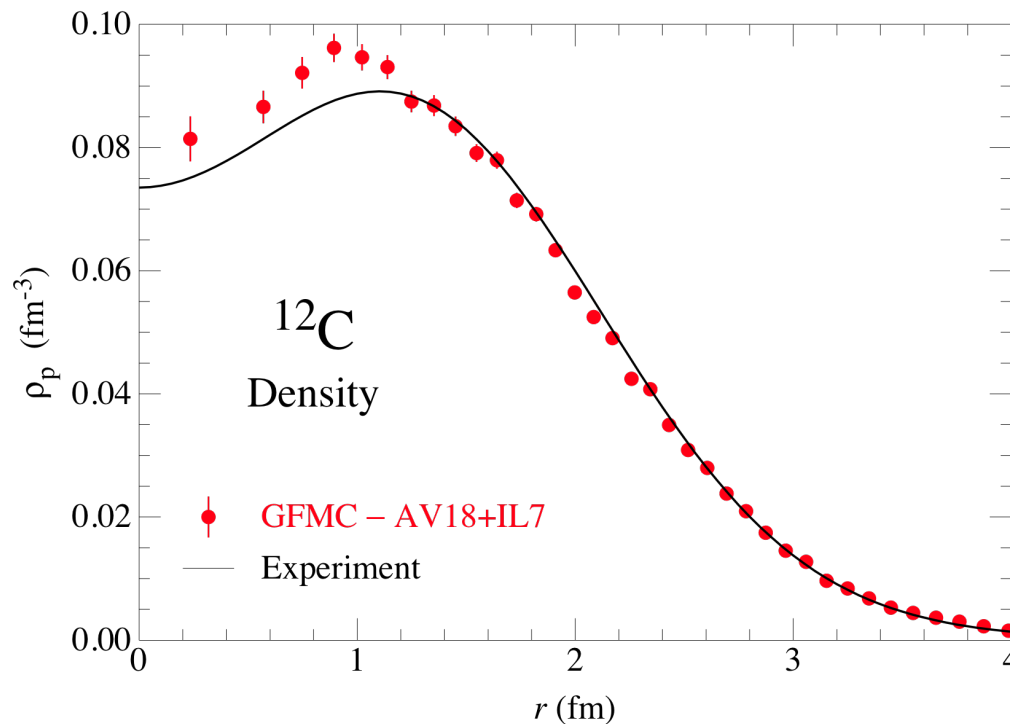
$$\times \Psi_{A-1}^\dagger \chi^\dagger Y_{lm}^\dagger(\hat{\mathbf{r}}) (U_{\text{rel}} - V_C) \Psi_A d\mathbf{R}$$

- This integral is ideal for QMC evaluation



UNEDF AND INCITE COMPUTATIONS OF ^{12}C ON ARGONNE'S IBM BLUE GENE/P

- Under the UNEDF SciDAC, Rusty Lusk (Math. & Comp. Sci.), Ralph Butler (MSTU) have developed ADLB to enable parallelization of GFMC to $>100,000$ cores
- Very successful calculation of $^{12}\text{C}(\text{gs})$ $E(\text{GFMC}) = -93.2(6)$ vs $\text{expt} = -92.16$ MeV
 - Done with Argonne v18 NN & Illinois-7 NNN potentials
 - RMS radius also very good – 2.35 fm vs experiment of 2.33 fm



Phys. Rev. Lett. 104, 182501 (2010) [4 pages]

Ab Initio Computation of the ^{17}F Proton Halo State and Resonances in $A=17$ Nuclei

G. Hagen¹, T. Papenbrock^{2,1}, and M. Hjorth-Jensen³¹Physics Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA²Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA³Department of Physics and Center of Mathematics for Applications, University of Oslo, N-0316 Oslo, Norway

Received 9 March 2010; published 4 May 2010

	^{17}O			^{17}F		
	$1/2^+$	$5/2^+$	E_{so}	$1/2^+$	$5/2^+$	E_{so}
GHF	-2.8	-3.2	4.3	-0.082	0.11	3.7
Exp.	-3.272	-4.143	5.084	-0.105	-0.600	5.000

TABLE I: Single-particle energies of the $1/2^+$ and $5/2^+$ states, and the spin-orbit splitting $E_{\text{so}}(d_{3/2}-d_{5/2})$ (in units of MeV) in ^{17}O and ^{17}F calculated in a Berggren (Gamow) basis (GHF), and the comparison to experiment [31].

	$^{17}\text{O } 3/2^+$		$^{17}\text{F } 3/2^+$	
	E_{sp}	Γ	E_{sp}	Γ
This work	1.1	0.014	3.9	1.0
Experiment	0.942	0.096	4.399	1.530

TABLE II: Computed $3/2^+$ single-particle resonance energies in ^{17}O and ^{17}F compared to data [31]. The real part $E_{\text{sp}} = \text{Re}[E]$, and the width $\Gamma = 2\text{Im}[E]$ are given in units of MeV.

Coupled-cluster theory for open-shell nuclei

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¹*Department of Physics and Center of Mathematics for Applications, University of Oslo, N-0316 Oslo, Norway*

²*Physics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA*

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⁴*GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany*

⁵*Institut für Kernphysik, Technische Universität Darmstadt, 64289 Darmstadt, Germany*

We develop a new method to describe properties of truly open-shell nuclei. This method is based on single-reference coupled-cluster theory and the equation-of-motion method with extensions to nuclei with $A \pm 2$ nucleons outside a closed shell. We perform proof-of-principle calculations for the ground states of the helium isotopes $^3\text{--}^6\text{He}$ and the first excited 2^+ state in ^6He . The comparison with exact results from matrix diagonalization in small model spaces demonstrates the accuracy of the coupled-cluster methods. Three-particle-one-hole excitations of ^4He play an important role for the accurate description of ^6He . For the open-shell nucleus ^6He , the computational cost of the method is comparable with the coupled-cluster singles-and-doubles approximation while its accuracy is similar to coupled-cluster with singles, doubles and triples excitations.

Chiral NN (SRG, 1.9 fm^{-1}), $hw = 24 \text{ MeV}$, $N_{\text{shell}}=5$, $l_{\text{max}}=2$

	^3He	^4He	^5He
CCSD	-6.624	-27.468	-22.997
CCSDT-1	-6.829	-27.600	-23.381
CCSDT	-6.911	-27.619	-23.474
EOM-CCSD	-6.357	-27.468	-23.382
FCI	-6.911	-27.640	-23.640

	^6He	0_1^+	2_1^+	$0^+ \langle J \rangle$	$2_1^+ \langle J \rangle$
CCSD	-22.732	-20.905	0.78	2	
CCSDT-1	-24.617	-21.586	0.25	2	
CCSDT	-24.530	-21.786	0.01	2	
2PA-EOM-CCSD(2p-0h)	-21.185	-18.996	0	2	
2PA-EOM-CCSD(3p-1h)	-24.543	-21.634	0	2	
FCI	-24.853	-21.994	0	2	

Table VII: Ground-state energies (in MeV) for ^3He , ^4He and ^5He , calculated with coupled-cluster methods truncated at the 2-particle-2-hole (CCSD) level, 3-particle-3-hole (CCSDT) and a hybrid (CCSDT-1) where a small subset of the leading diagrams in CCSDT are included. For the EOM-CCSD approach, truncations has been made at the 1-particle-2-hole level, the 2-particle-2-hole level, and the 2-particle-1-hole level for ^3He , ^4He and ^5He respectively. The energies are

Table VIII: Energies (in MeV) for the ground state and first excited state of ^6He and the expectation value of the total angular momentum, calculated with coupled-cluster methods truncated at the 2-particle-2-hole (CCSD) level, 3-particle-3-hole (CCSDT) and a hybrid (CCSDT-1) where the 3-particle-3-hole amplitudes are treated perturbatively. The 2PA-EOM-CCSD results are calculated with a truncation at the 2-

No Core Shell Model

A large sparse matrix eigenvalue problem

$$H = T_{rel} + V_{NN} + V_{3N} + \dots$$

$$H|\Psi_i\rangle = E_i|\Psi_i\rangle$$

$$|\Psi_i\rangle = \sum_{n=0}^{\infty} A_n^i |\Phi_n\rangle$$

$$\text{Diagonalize } \{ \langle \Phi_m | H | \Phi_n \rangle \}$$

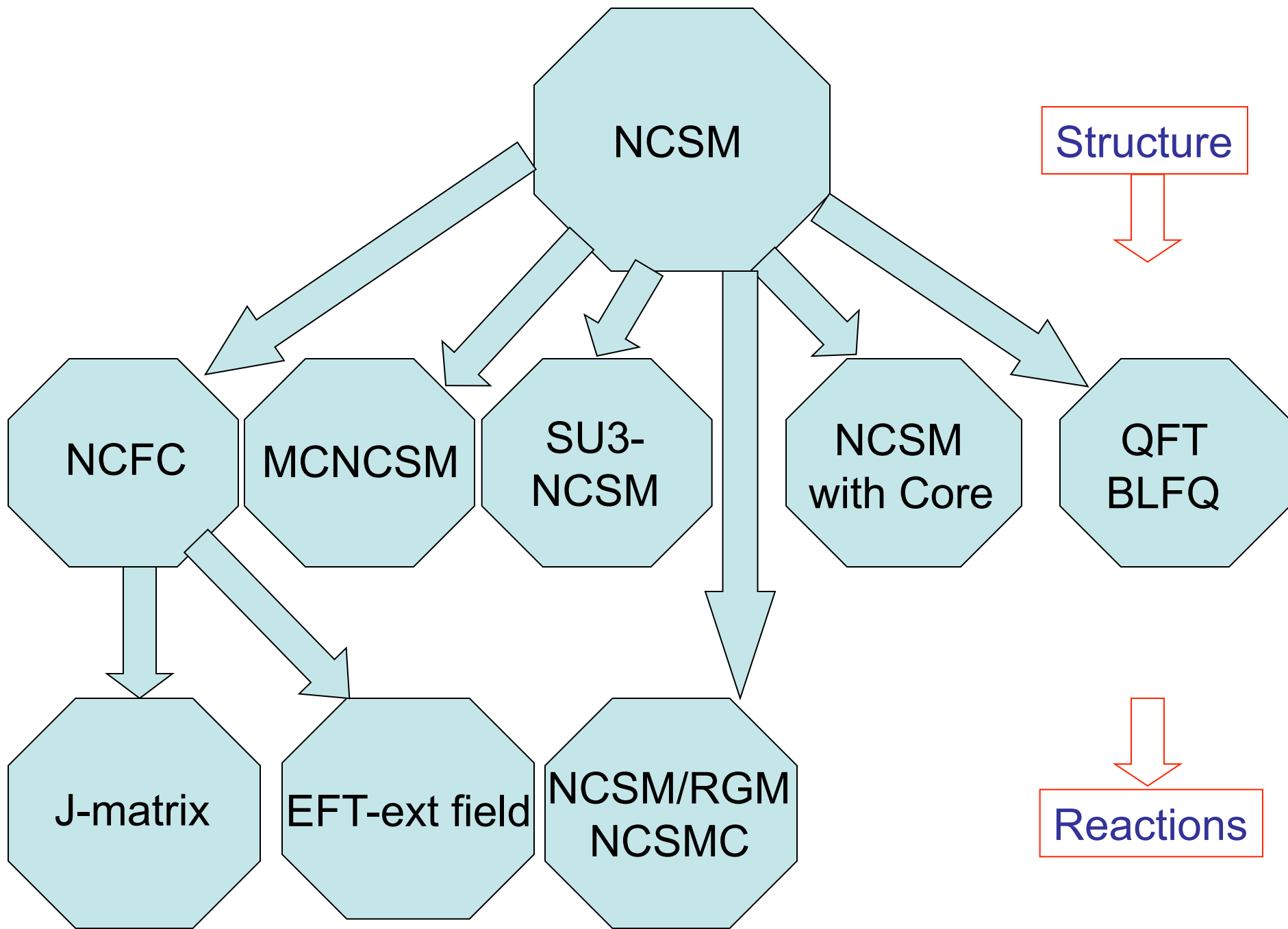
- Adopt realistic NN (and NNN) interaction(s) & renormalize as needed - retain induced many-body interactions: **Chiral EFT interactions and JISP16**
- Adopt the 3-D Harmonic Oscillator (HO) for the single-nucleon basis states, α, β, \dots
- Evaluate the nuclear Hamiltonian, H, in basis space of HO (Slater) determinants (manages the bookkeeping of anti-symmetrization)
- Diagonalize this sparse many-body H in its “m-scheme” basis where [$\alpha = (n, l, j, m_j, \tau_z)$]

$$|\Phi_n\rangle = [a_{\alpha}^+ \dots a_{\zeta}^+]_n |0\rangle$$
$$n = 1, 2, \dots, 10^{10} \text{ or more!}$$

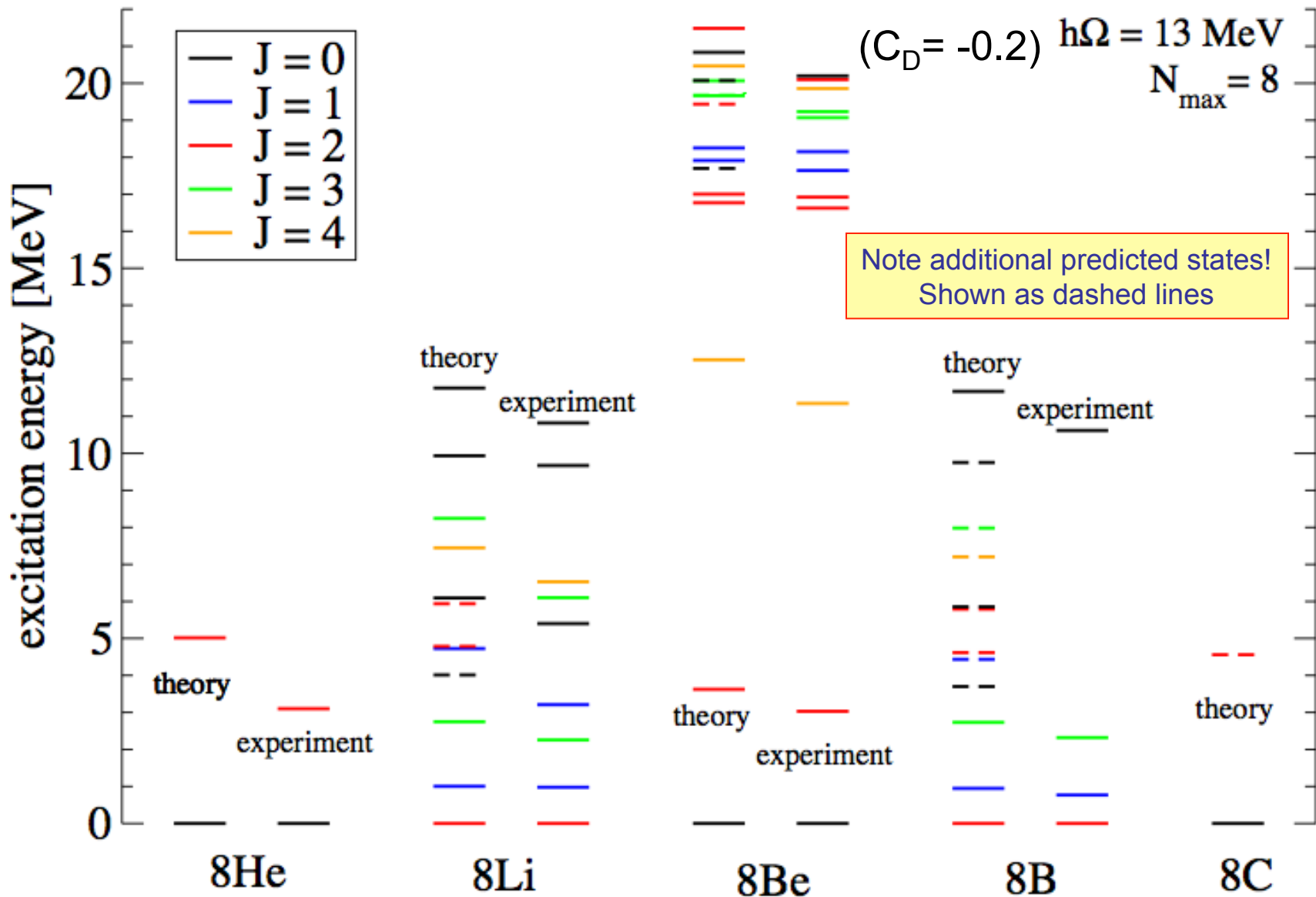
- Evaluate observables and compare with experiment

Comments

- Straightforward but computationally demanding => new algorithms/computers
- Requires convergence assessments and extrapolation tools
- Achievable for nuclei up to A=16 (40) today with largest computers available



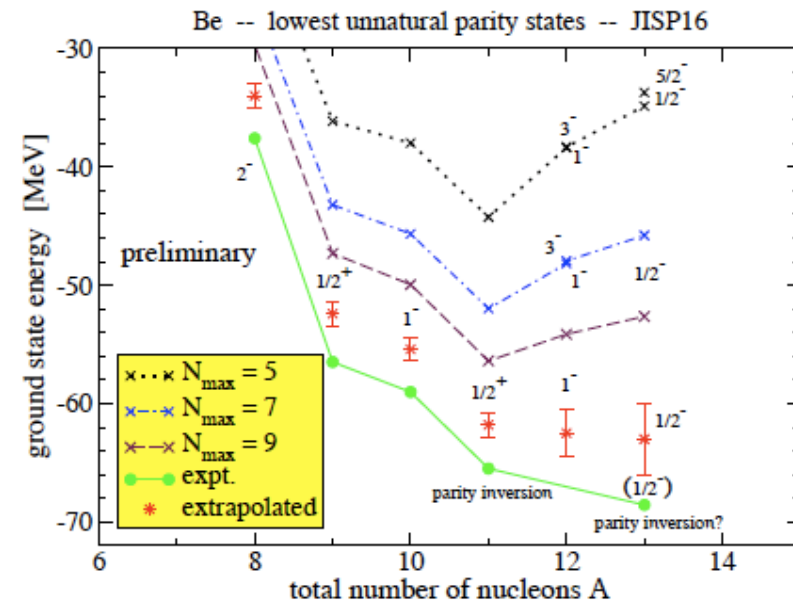
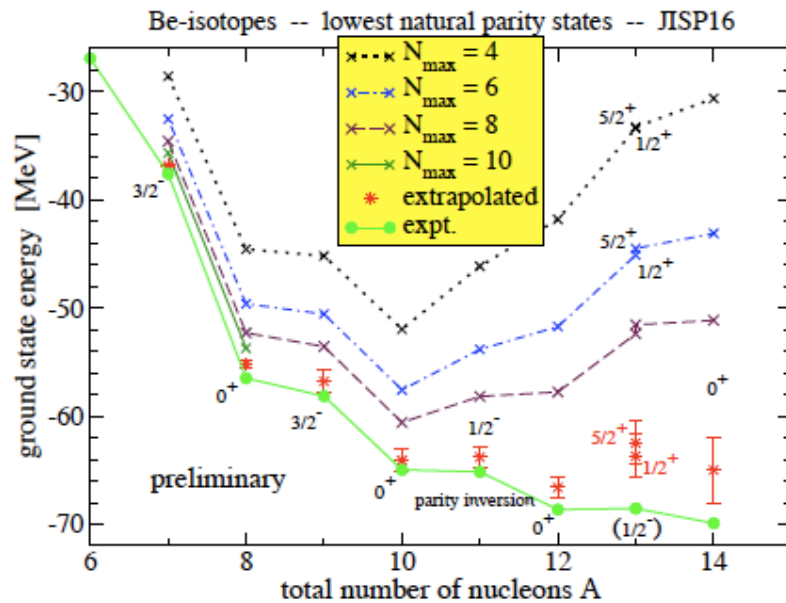
spectrum A=8 nuclei with N3LO 2-body + N2LO 3-body



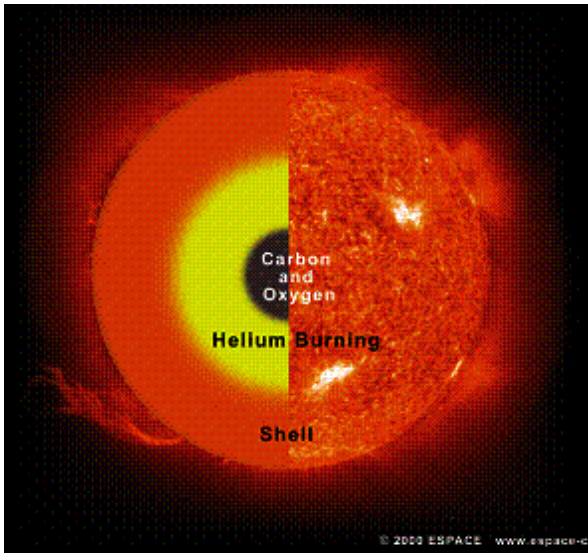
Beryllium isotopes

updated from Vary, Maris, Ng, Yang, Sosonkina, arXiv:0907.0209 [nucl-th],

J. Phys. Conf. Ser. 180, 012083 (2009)



- Exploring physics near the neutron drip line – in progress
- Un-natural parity states systematically underbound with JISP16
- Similar results for He- and Li-isotopes



^{12}C - At the heart of matter

The first excited 0^+ state of ^{12}C , the “Hoyle state”, is the key state of ^{12}C formation in the triple-alpha fusion process that occurs in stars.

Due to its role in astrophysics and the fact that carbon is central to life, some refer to this as one of the “holy grails” of nuclear theory.

Many important unsolved problems of the Hoyle state:

Microscopic origins of the triple-alpha structure are unsolved

Breathing mode puzzle - experiments disagree on sum rule fraction

Laboratory experiments to measure the formation rate are very difficult - resulting uncertainties are too large for predicting the ^{12}C formation rate through this state that dictates the size of the iron core in pre-supernova stars

Conclusion: Need *ab initio* solutions of the Hoyle state with no-core method that accurately predicts the ground state binding energy

**==> parameter free predictions for the Hoyle state
achievable with petascale within 1-2 years**

Lattice + EFT results [Adjusted to 4He, predict rest]

PRL 106, 192501 (2011)

PHYSICAL REVIEW LETTERS

13 MAY 2011



Ab Initio Calculation of the Hoyle State

Evgeny Epelbaum,¹ Hermann Krebs,¹ Dean Lee,² and Ulf-G. Meißner^{3,4}

TABLE I. Lattice results for the ground state energies for ⁴He, ⁸Be, and ¹²C. For comparison we also exhibit the experimentally observed energies. All energies are in units of MeV.

	⁴ He	⁸ Be	¹² C
LO [$O(Q^0)$]	-24.8(2)	-60.9(7)	-110(2)
NLO [$O(Q^2)$]	-24.7(2)	-60(2)	-93(3)
IB + EM [$O(Q^2)$]	-23.8(2)	-55(2)	-85(3)
NNLO [$O(Q^3)$]	-28.4(3)	-58(2)	-91(3)
Experiment	-28.30	-56.50	-92.16

TABLE II. Lattice results for the low-lying excited states of ¹²C. For comparison the experimentally observed energies are shown. All energies are in units of MeV.

	0_2^+	E_{ex}	$2_1^+, J_z = 0$	$2_1^+, J_z = 2$
LO [$O(Q^0)$]	-94(2)	16	-92(2)	-89(2)
NLO [$O(Q^2)$]	-82(3)	11	-87(3)	-85(3)
IB + EM [$O(Q^2)$]	-74(3)	11	-80(3)	-78(3)
NNLO [$O(Q^3)$]	-85(3)	6	-88(3)	-90(4)
Experiment	-84.51		-87.72	

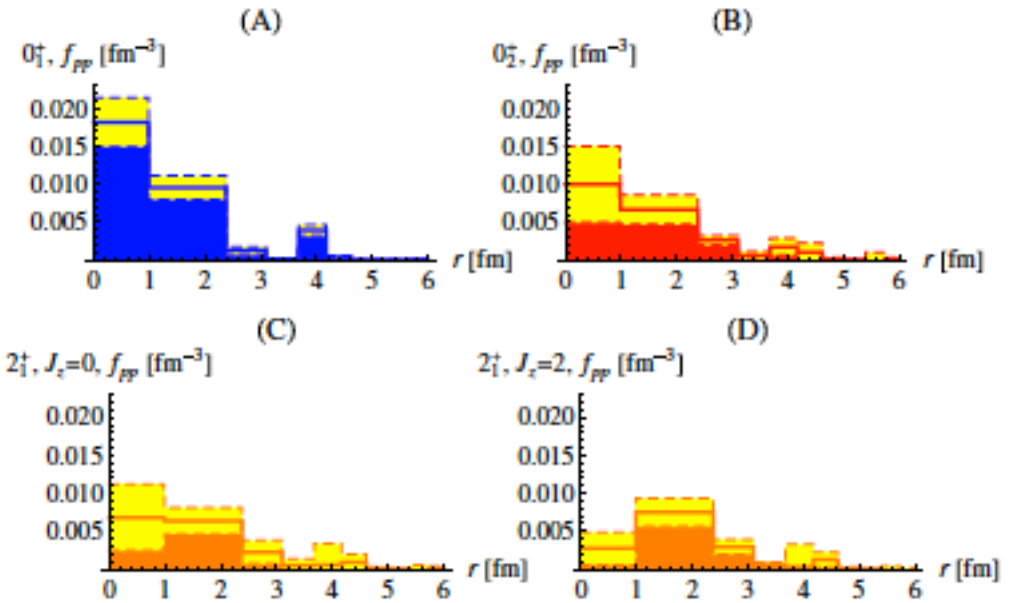
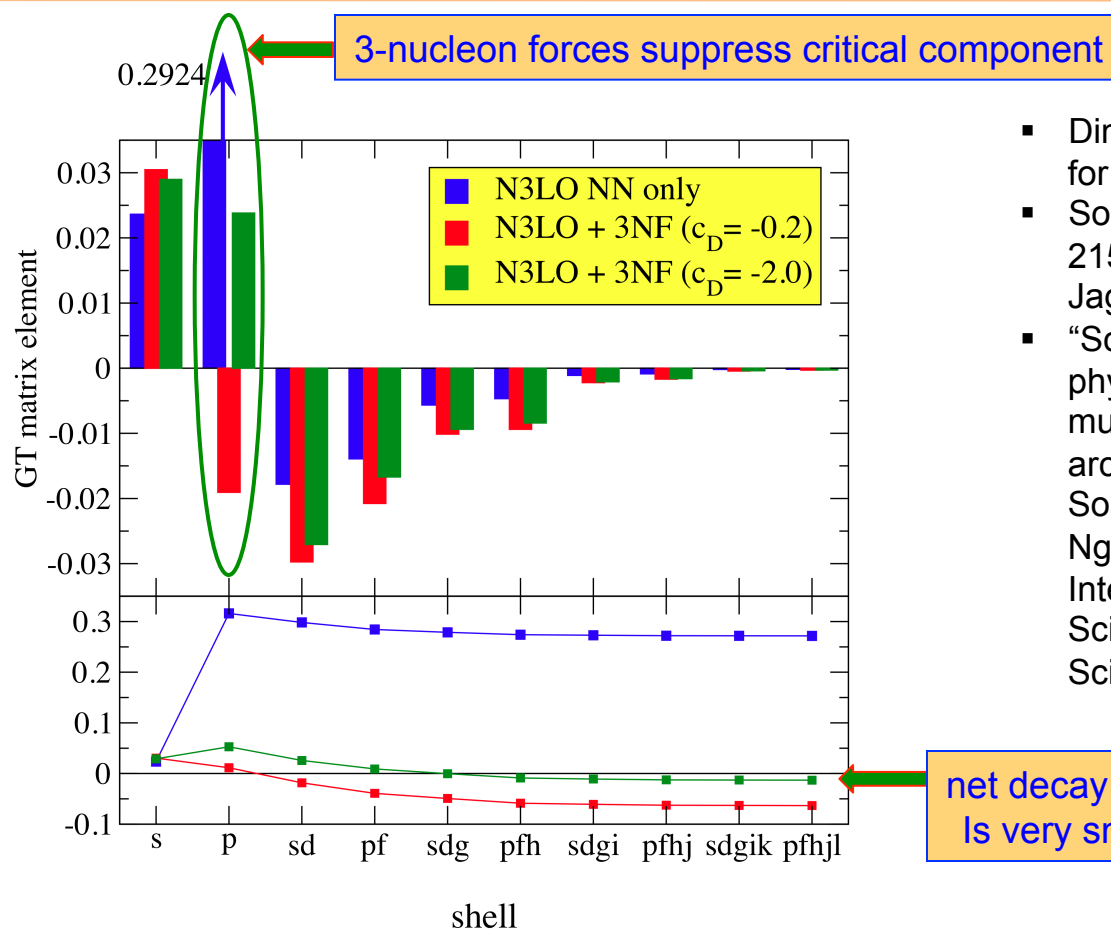
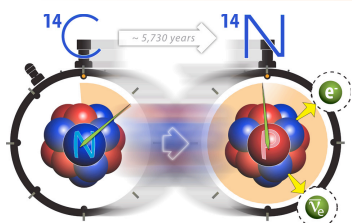


FIG. 3 (color online). The radial distribution function $f_{pp}(r)$ for the ground state (A), Hoyle state (B), and in the $J_z = 0$ (C) and $J_z = 2$ (D) projections of the spin-2 state. The yellow bands denote error bars.

NB: Lattice spacing ~ 2 fm, ~ 3 MeV uncertainty in energies

Origin of the Anomalous Long Lifetime of ^{14}C P. Maris,¹ J.P. Vary,¹ P. Navrátil,^{2,3} W.E. Ormand,^{3,4} H. Nam,⁵ and D.J. Dean⁵

- Solves the puzzle of the long but useful lifetime of ^{14}C
- Establishes a major role for strong 3-nucleon forces in nuclei
- Strengthens foundation for guiding DOE-supported experiments



- Dimension of matrix solved for 8 lowest states $\sim 1 \times 10^9$
- Solution takes ~ 6 hours on 215,000 cores on Cray XT5 Jaguar at ORNL
- "Scaling of *ab initio* nuclear physics calculations on multicore computer architectures," P. Maris, M. Sosonkina, J. P. Vary, E. G. Ng and C. Yang, 2010 Intern. Conf. on Computer Science, Procedia Computer Science 1, 97 (2010)

But how to progress to heavier nuclei – structure & reactions?

IT-NCSM (Roth, Navratil, . . .)

SU3-NCSM (LSU-ISU-OSU-Ames Lab NSF PetaApps collab)

MCNCSM (Japan-US collaboration)

NCSM *with* a core (Barrett)

Energy-Density Functional theory (SciDAC/UNEDF collab)

EFT with achievable basis spaces (van Kolck)

TDSLDA (Bulgac)

Innovations underway to improve the NCSM with aims:

(1) improve treatment of clusters and intruders

(2) enable *ab initio* solutions of heavier nuclei

Initially, all follow the NCFC approach = extrapolations

Importance Truncated – NCSM

Separate spurious CM motion in same way as CC approach

Robert Roth and collaborators

“Realistic” single-particle basis - Woods-Saxon example

Control the spurious CM motion with Lagrange multiplier term

A. Negoita, ISU PhD thesis project

Alternative sp basis spaces – Mark Caprio collaboration

SU(3) No Core Shell Model

Add symmetry-adapted many-body basis states

Preserve exactly the CM factorization

LSU - ISU – OSU collaboration

No Core Monte Carlo Shell Model

Invokes single particle basis (FCI) truncation

Separate spurious CM motion in same way as CC approach

Scales well to larger nuclei

U. Tokyo - ISU collaboration

Taming the scale explosion in nuclear calculations

NSF PetaApps - Louisiana State, Iowa State, Ohio State collaboration

❖ Goals

- Ab initio calculations of nuclei with unprecedented accuracy using basis-space expansions
- Current calculations limited to nuclei with $A \leq 16$ (up to 20 billion basis states with 2-body forces)

❖ Progress

- Scalable CI code for nuclei
- Sp(3,R)/SU(3)-symmetry vital

❖ Challenges/Promises

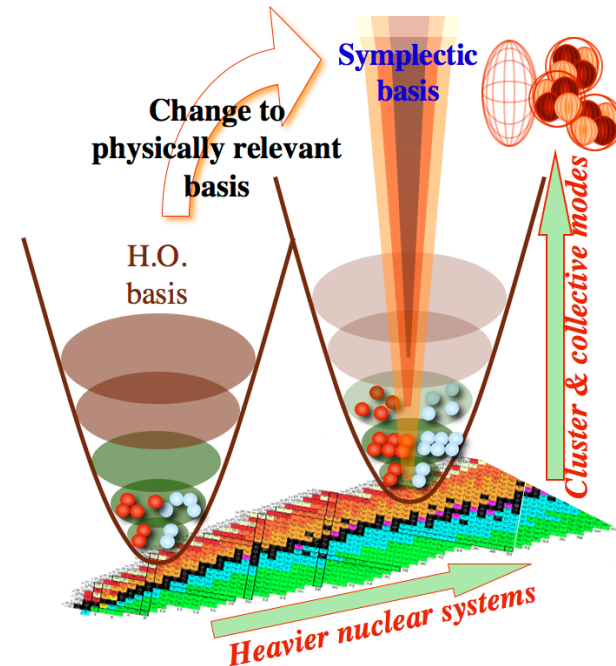
- Constructing hybrid Sp-CI code
- Publicly available peta-scale software for nuclear science

❖ Novel approach

- Sp-CI: exploiting symmetries of nuclear dynamics
- Innovative workload balancing techniques & representations of multiple levels of parallelism for ultra-large realistic problems

❖ Impact

- Applications for nuclear science and astrophysics



Ab initio NCSM reinstating the core!
Name: “Ab Initio Shell Model”?

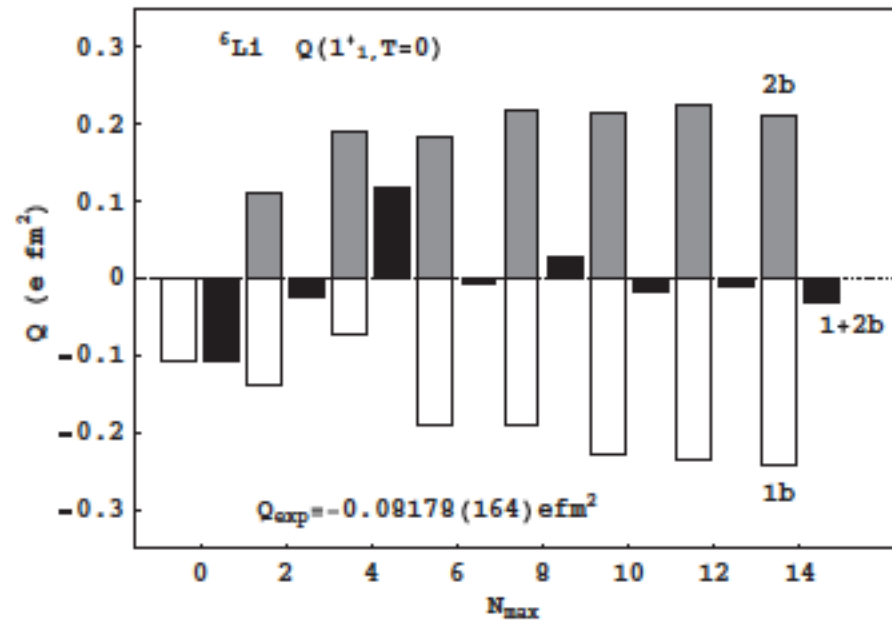


Figure 6. The quadrupole moment (Q) of the g.s. for ${}^6\text{Li}$ [$1^+(T=0)$] is shown in terms of one and two-body contributions, as a function of increasing model-space size. The one- and two-body contributions and total Q are depicted as white, gray and black histograms, respectively [18].

A. F. Lisetskiy, M. K. G. Kruse, B. R. Barrett, P. Navrátil, I. Stetcu, and J. P. Vary, *Phys. Rev. C* 80 (2009) 024315.

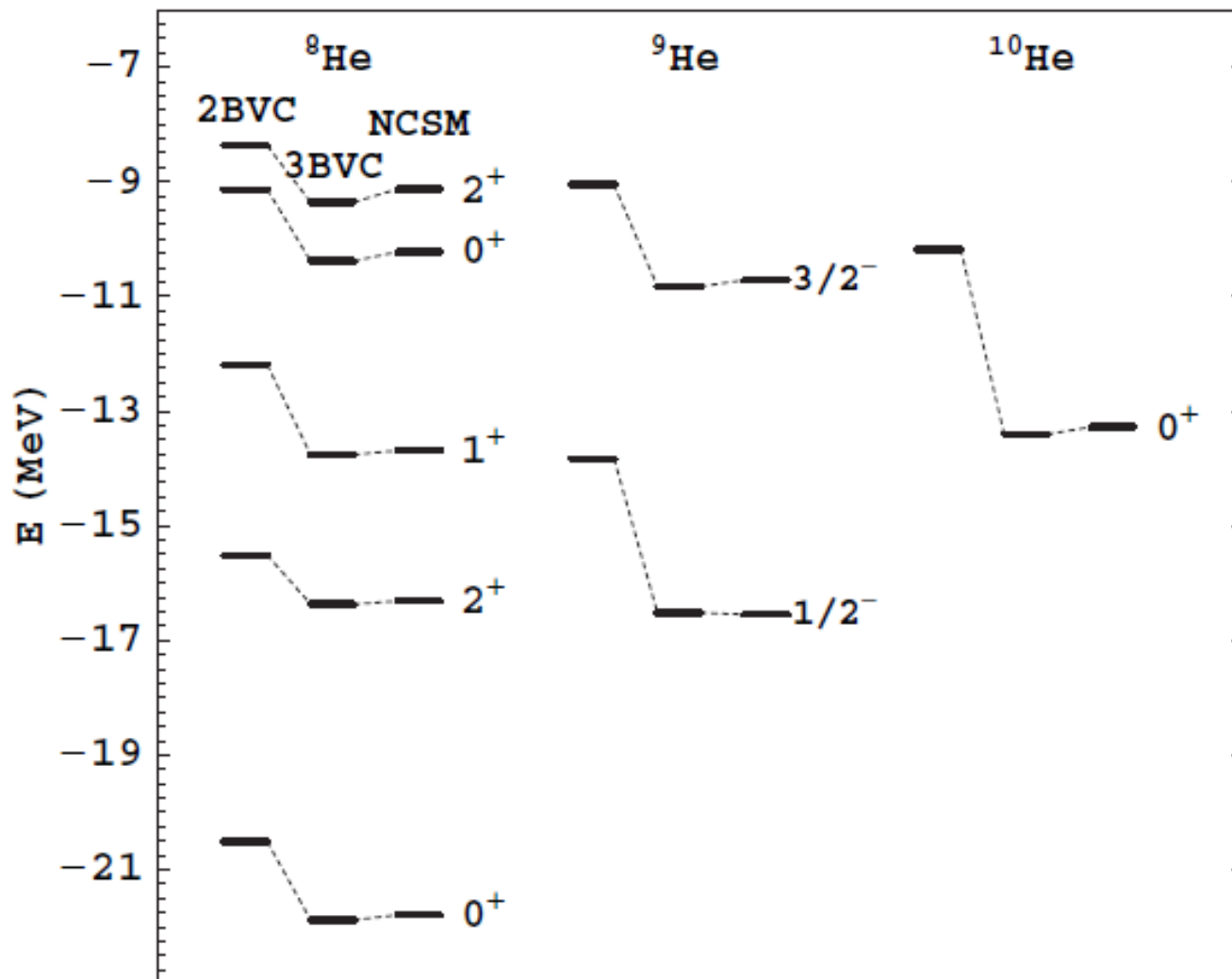
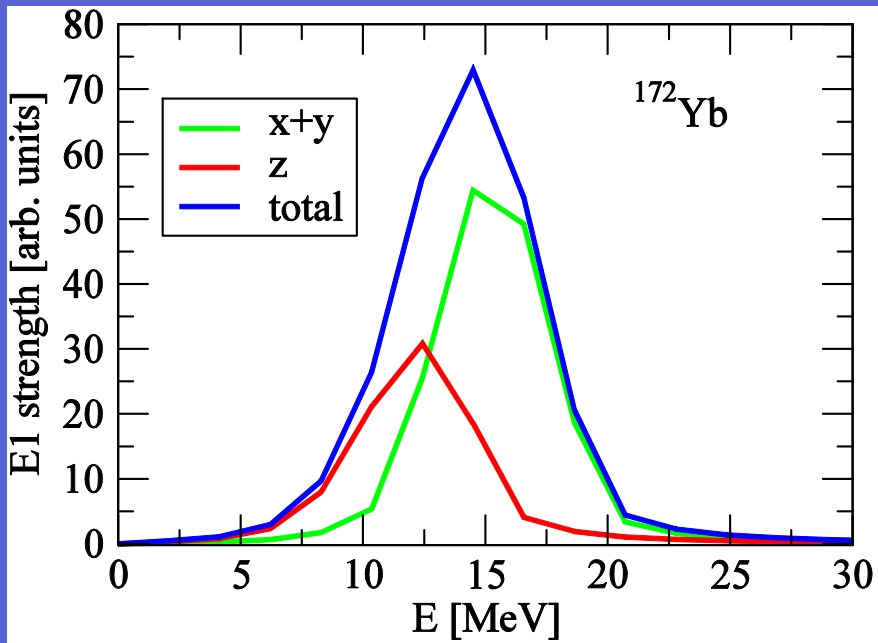
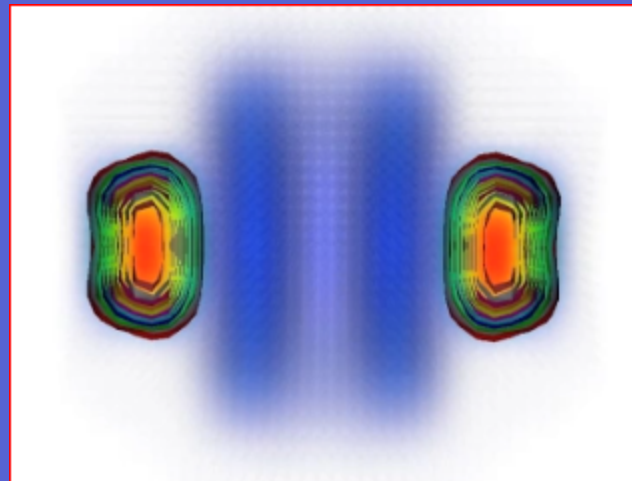
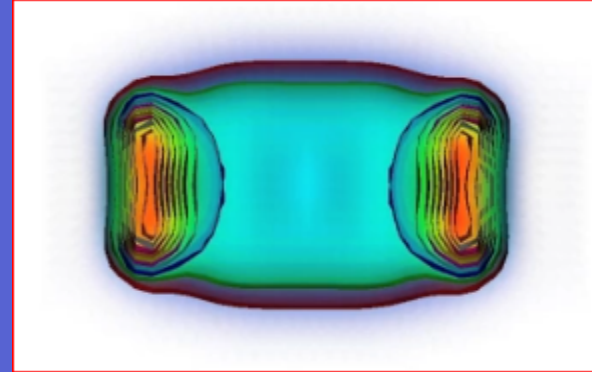
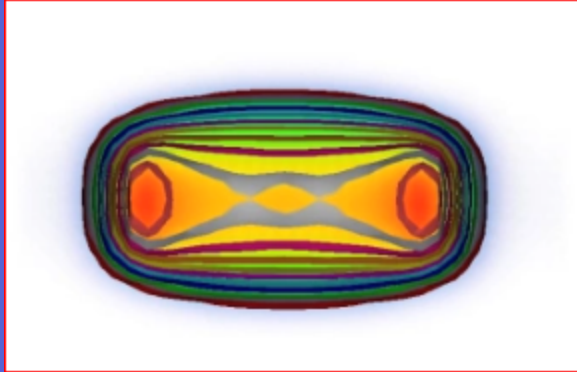


FIG. 9. Comparison of spectra for ${}^8\text{He}$, ${}^9\text{He}$, and ${}^{10}\text{He}$ from SSM calculations using the effective 2BVC and 3BVC Hamiltonians and from exact NCSM calculation for $N_{\text{max}} = 6$ and $\hbar\Omega = 20$ MeV using the CD-Bonn interaction.



Isovector dipole strength computed in TDSLDA
I. Stetcu *et al.*



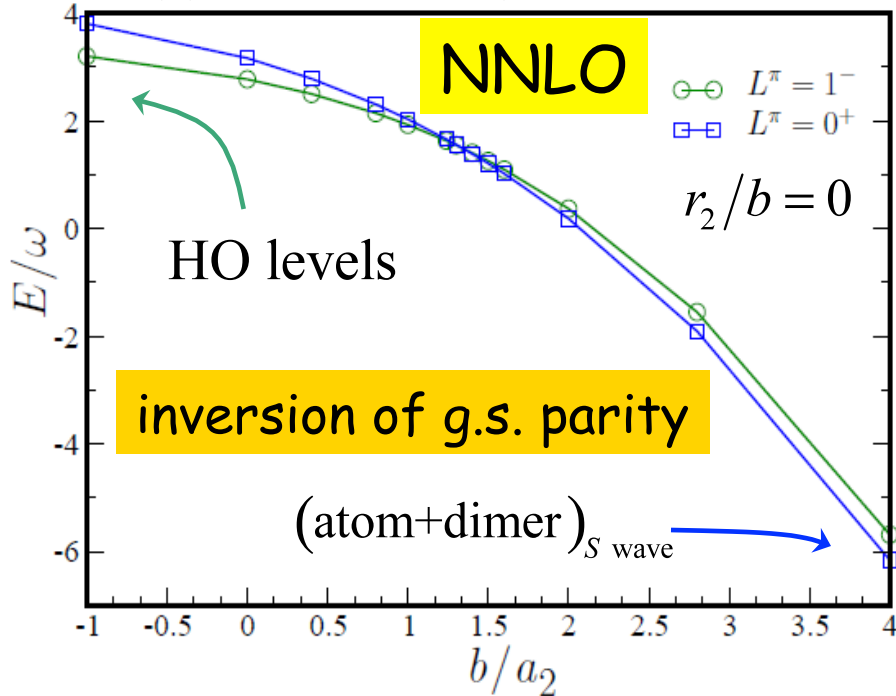
Several consecutive frames of real-time induced fission of ^{280}Cf computed in TDSLDA

I. Stetcu *et al.*

Harmonic EFT

U. van Kolck

Trapped two-component fermions

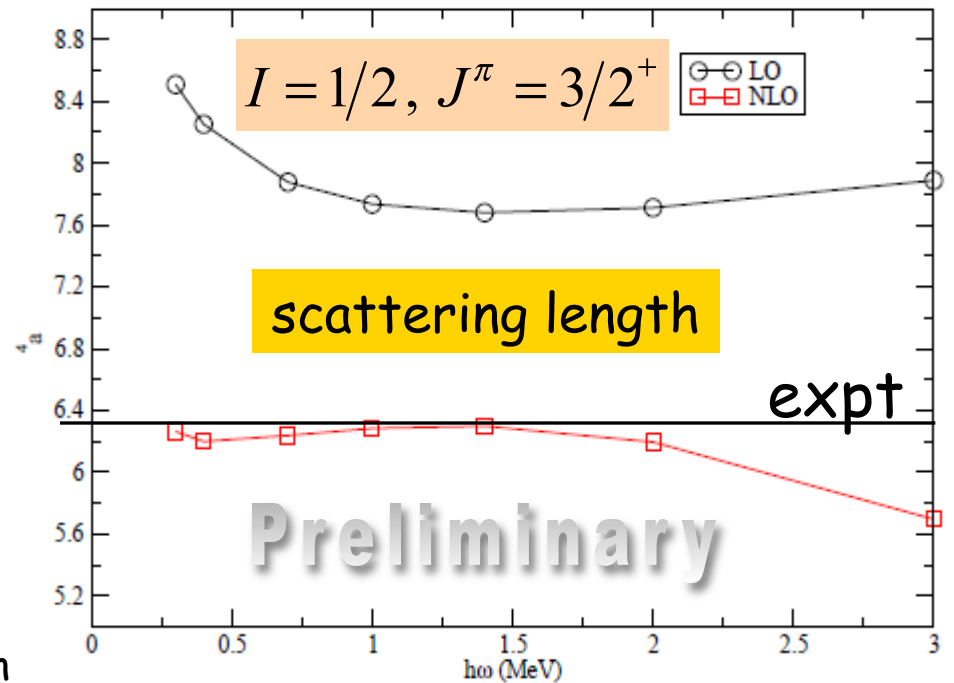


Rotureau, Stetcu, Barrett, Birse + v.K. '10

$$A = 3$$

Rotureau, Stetcu, Barrett + v.K. in preparation

Contact EFT in
harmonic-oscillator potential
with two-body scattering
parameters
as input
Nucleons



Descriptive Science



Predictive Science

“Proton-Dripping Fluorine-14”

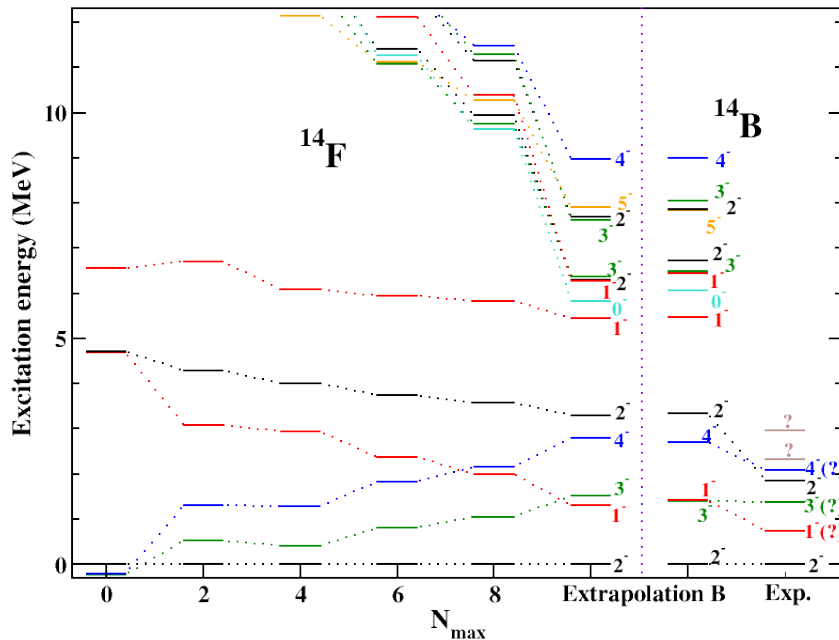
Objectives

- Apply *ab initio* microscopic nuclear theory’s predictive power to major test case

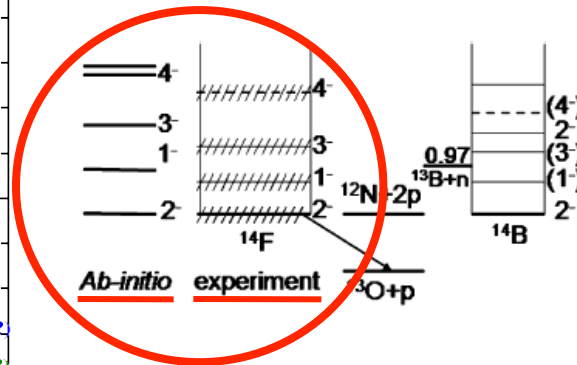
Impact

- Deliver robust predictions important for improved energy sources
- Provide important guidance for DOE-supported experiments
- Compare with new experiment to improve theory of strong interactions

P. Maris, A. Shirokov and J.P. Vary,
Phys. Rev. C 81 (2010) 021301(R)



**Experiment confirms
our published
predictions!**



V.Z. Goldberg et al.,
Phys. Lett. B 692, 307 (2010)

- Dimension of matrix solved for 14 lowest states $\sim 2 \times 10^9$
- Solution takes ~ 2.5 hours on 30,000 cores (Cray XT4 Jaguar at ORNL)
- “Scaling of ab-initio nuclear physics calculations on multicore computer architectures,” P. Maris, M. Sosonkina, J. P. Vary, E. G. Ng and C. Yang, 2010 Intern. Conf. on Computer Science, Procedia Computer Science 1, 97 (2010)

Ab Initio Neutron drops in traps

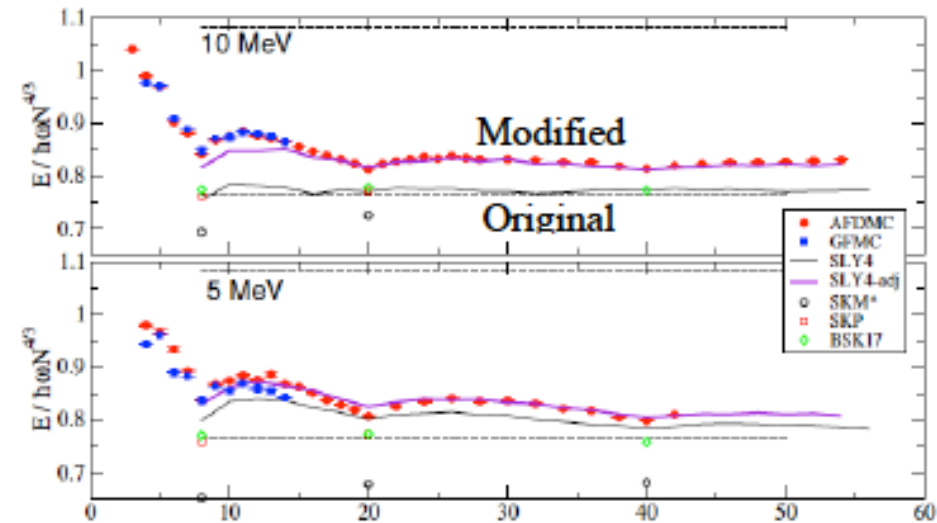


UNEDF

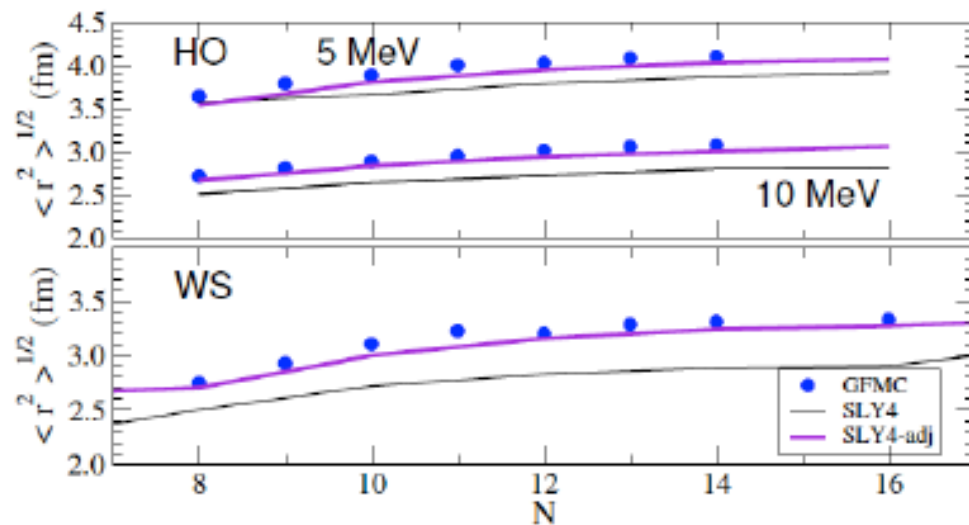
Cold Neutrons Trapped in External Fields

S. Gandolfi,¹ J. Carlson,¹ and Steven C. Pieper²Artificial Nuclei
with Neutrons only

Energies



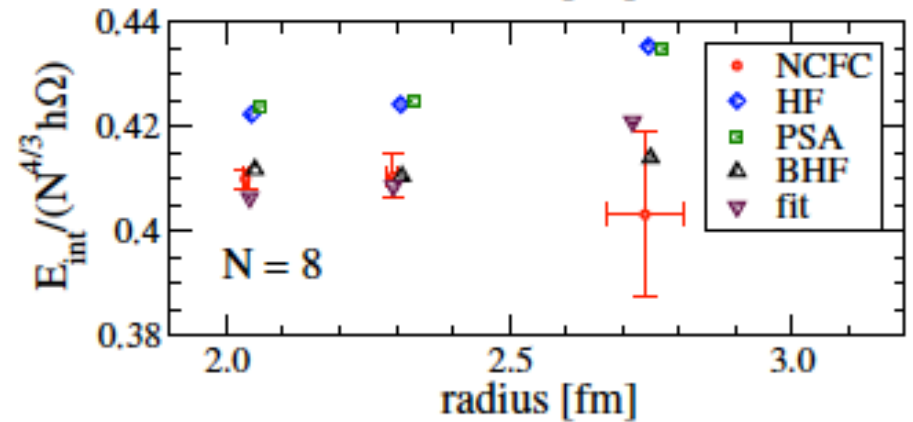
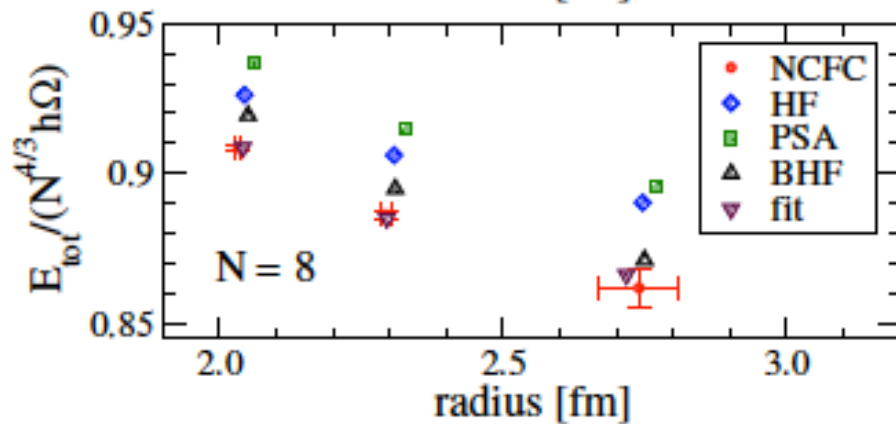
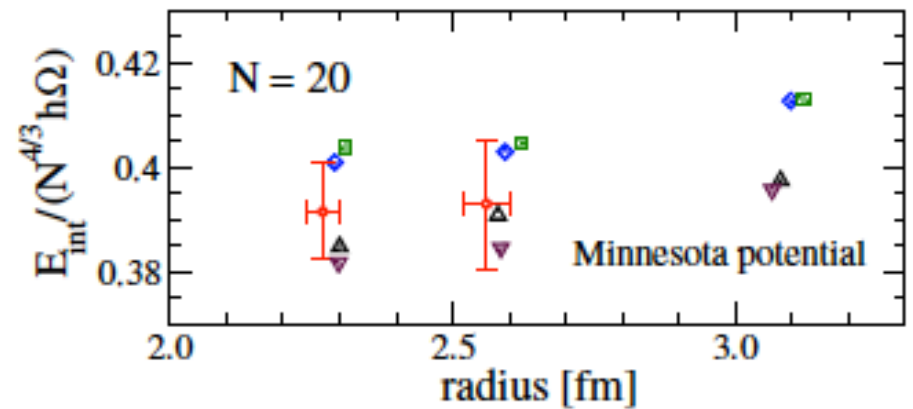
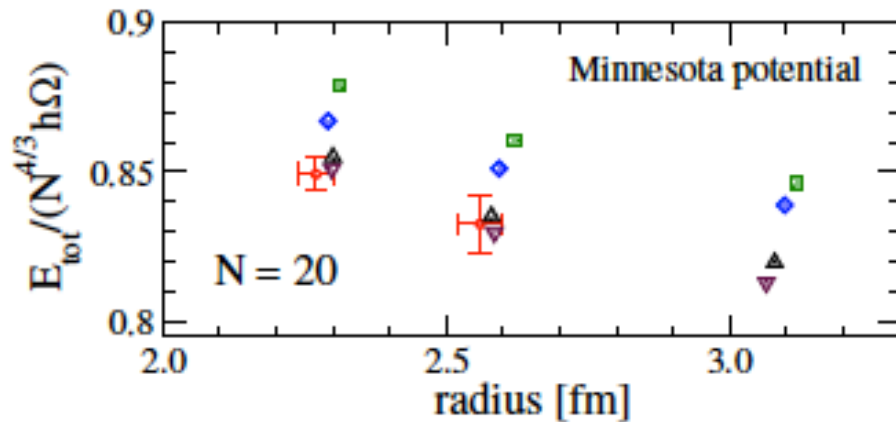
Radii



Testing the density matrix expansion against ab initio calculations of trapped neutron drops

S. Bogner,¹ R.J. Furnstahl,² M. Kortelainen,³ P. Maris,⁴ M. Stoitsov,³ and J.P. Vary⁴

Preliminary Results

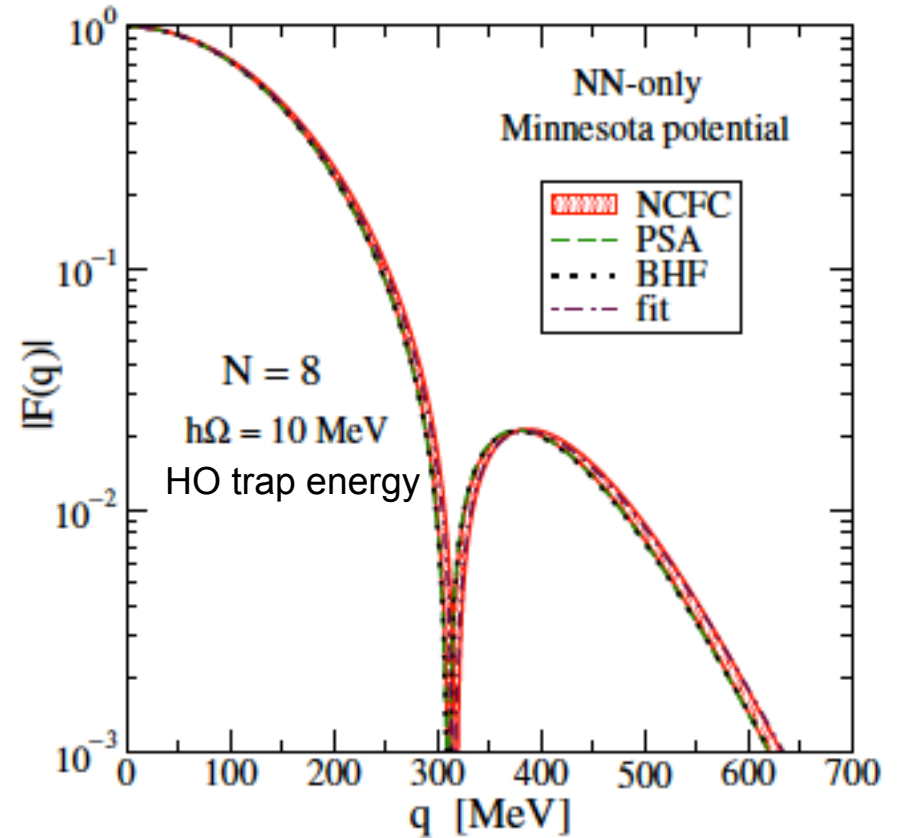
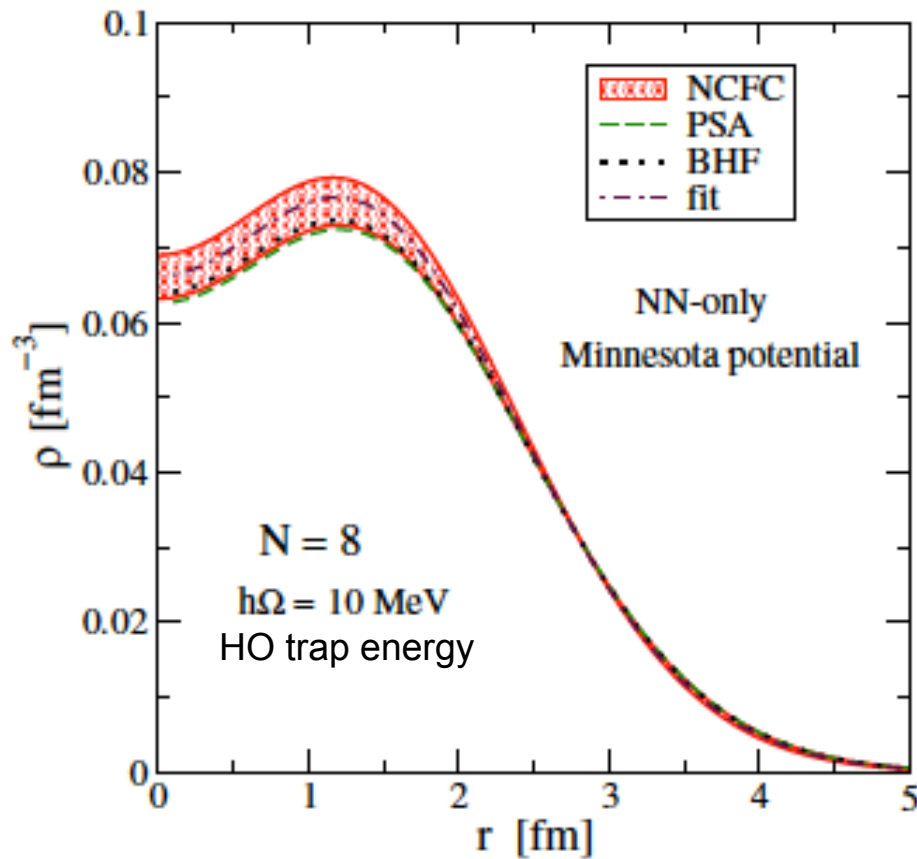


HO Traps with strengths of 10, 15 and 20 MeV

Testing the density matrix expansion against ab initio calculations of trapped neutron drops

S. Bogner,¹ R.J. Furnstahl,² M. Kortelainen,³ P. Maris,⁴ M. Stoitsov,³ and J.P. Vary⁴

Preliminary Results



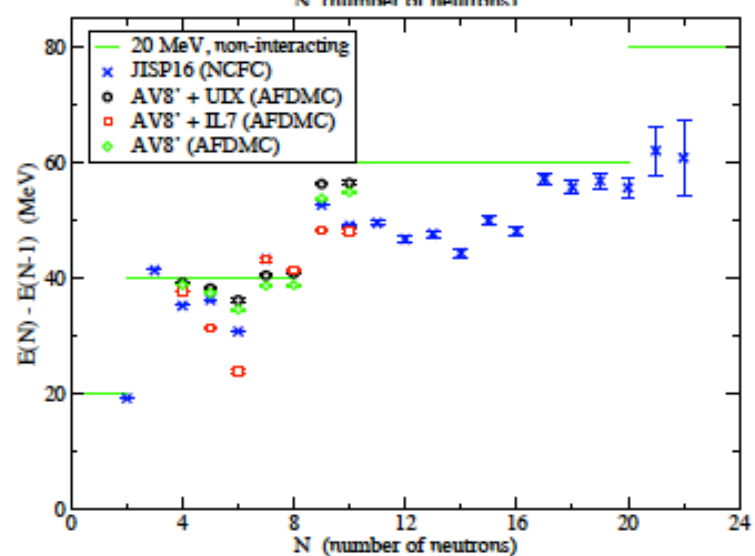
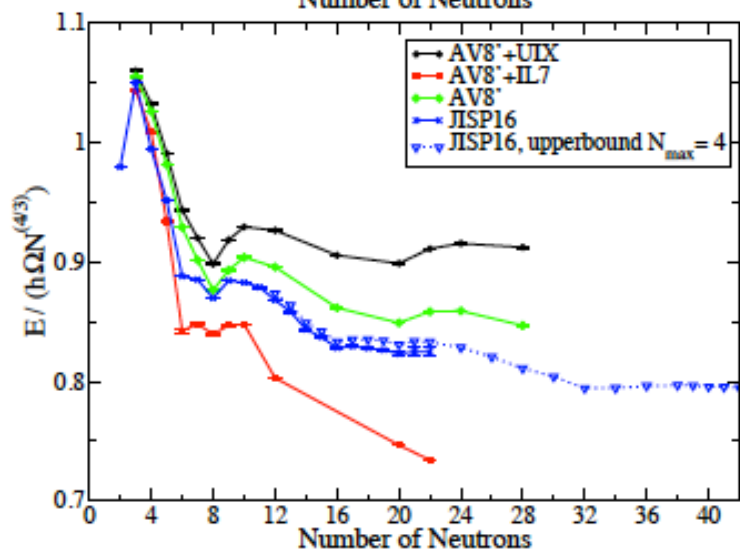
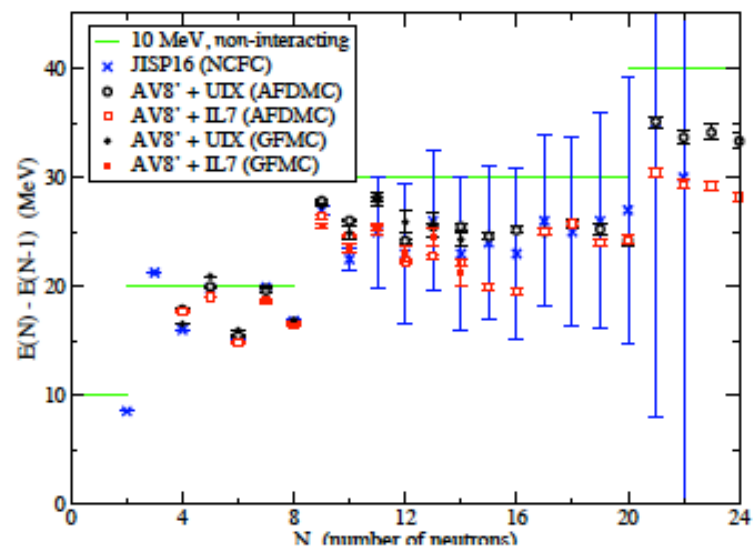
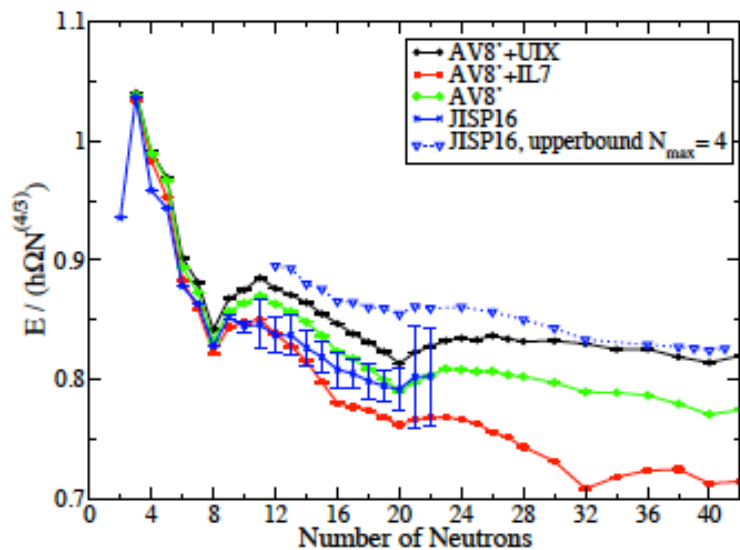
Properties of trapped neutrons interacting with realistic nuclear Hamiltonians

J. Carlson and S. Gandolfi
Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87545

Pieter Maris and James Vary
Iowa State University, Ames, Iowa, 50011

Preliminary

Steven C. Pieper
Physics Division, Argonne National Laboratory, Argonne, IL 61801
 (Dated: April 20, 2011)



Ab initio Nuclear Structure



Ab initio Nuclear Reactions

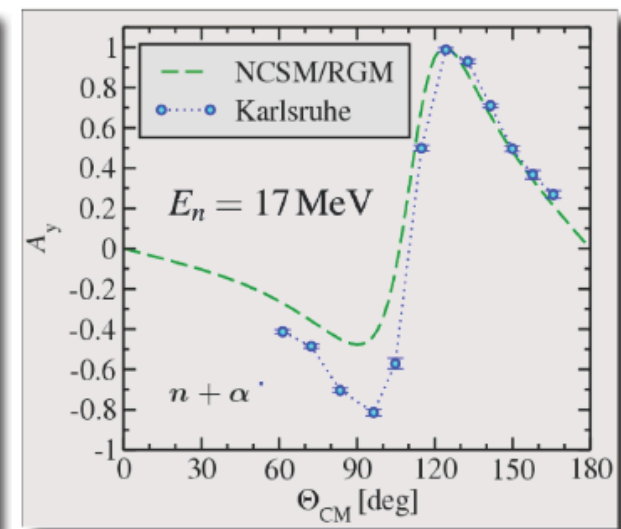
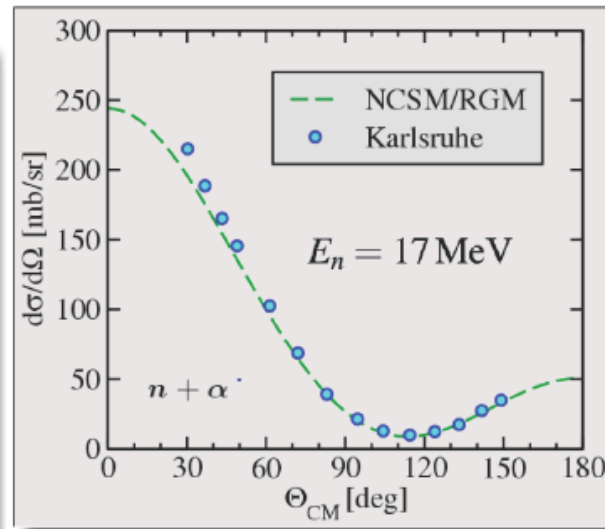
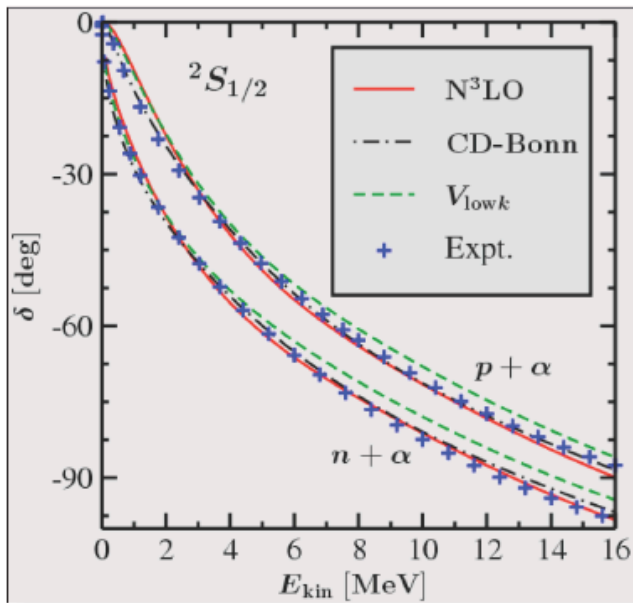
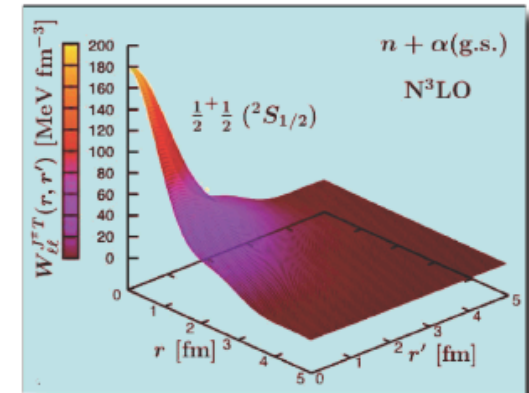
Ab initio NCSM/RGM: nucleon-⁴He scattering

Navratil

- The N -⁴He potential is calculated microscopically from the many-body realistic Hamiltonian and the NCSM eigenstates of the ⁴He

$$\left\langle \begin{array}{c} \text{4He} \\ r \end{array} \middle| \hat{A}(H-E)\hat{A} \middle| \begin{array}{c} \text{4He} \\ r' \end{array} \right\rangle \longrightarrow W_{VV'}(r, r')$$

- Solving the non-local integro-differential coupled-channel equations for the N -⁴He relative motion: phase shifts, cross sections, polarization observables



Phase shifts in PRL 101, 092501 (2008)
and PRC 79, 044606 (2009); arXiv 0901.0950;
Cross sections and polarizations to be published

NCSM/RGM

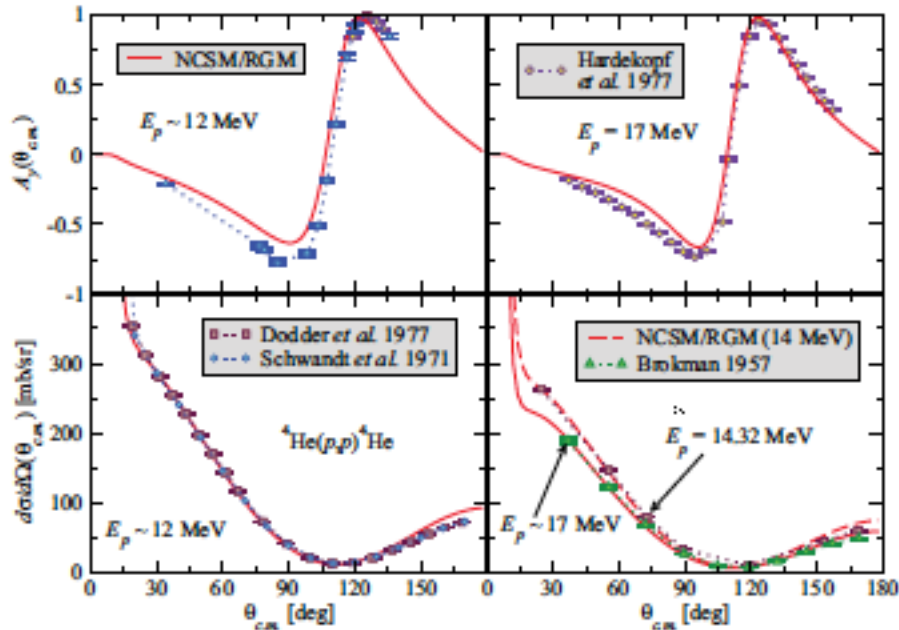


Figure 7. Calculated $p\text{-}^4\text{He}$ differential cross section (bottom panels) and analyzing power (top panels) for proton laboratory energies $E_p = 12, 14.32$ and 17 MeV compared to experimental data from Refs. [29, 30, 31, 32]. The SRG- $N^3\text{LO}$ NN potential with $\lambda = 2.02 \text{ fm}^{-1}$ was used.

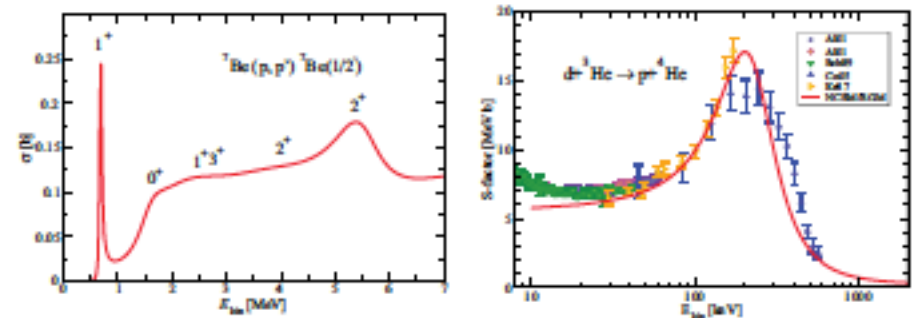


Figure 8. Calculated inelastic ${}^7\text{Be}(p,p'){}^7\text{Be}(1/2^-)$ cross section with indicated positions of the P -wave resonances (left figure). Calculated S -factor of the ${}^3\text{He}(d,p){}^4\text{He}$ fusion reaction compared to experimental data (right figure). Energies are in the center of mass. The SRG- $N^3\text{LO}$ NN potential with $\lambda = 1.85 \text{ fm}^{-1}$ ($\lambda = 1.5 \text{ fm}^{-1}$) was used, respectively.

Ab initio scattering via trapping the system then analytically removing effects of the trap

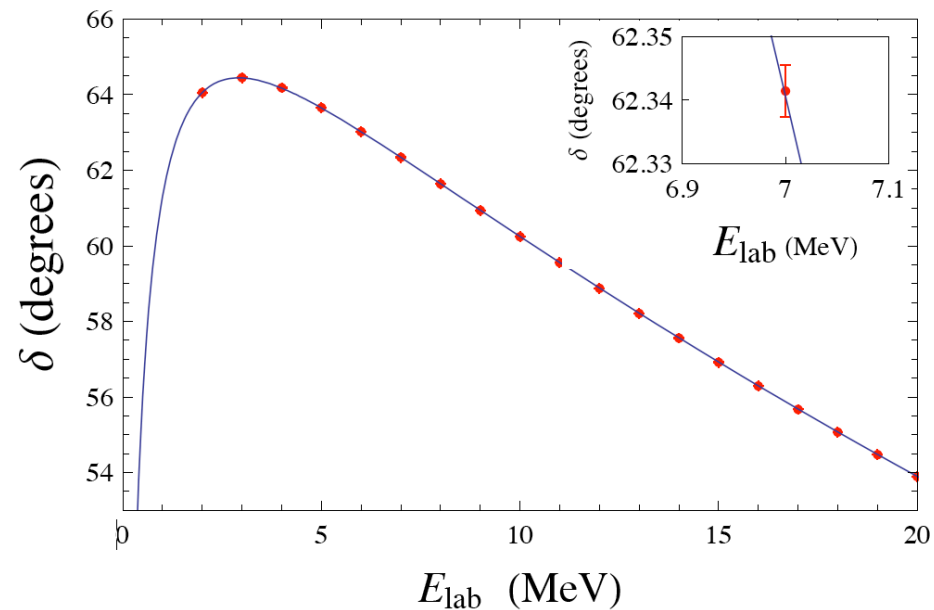


Figure 3 The extracted results agreed with those from solving the Schrodinger equation in the continuum as illustrated for the 1S0 partial wave with the JISP16 NN interaction.

Analogous to Luescher's method for extracting phase shifts from lattice-gauge results

T. Luu, M. Savage, A. Schwenk and J.P. Vary, Phys. Rev. C 82, 034003 (2010); arXiv:1006.0427

Resonances in NCSM

A. Shirokov

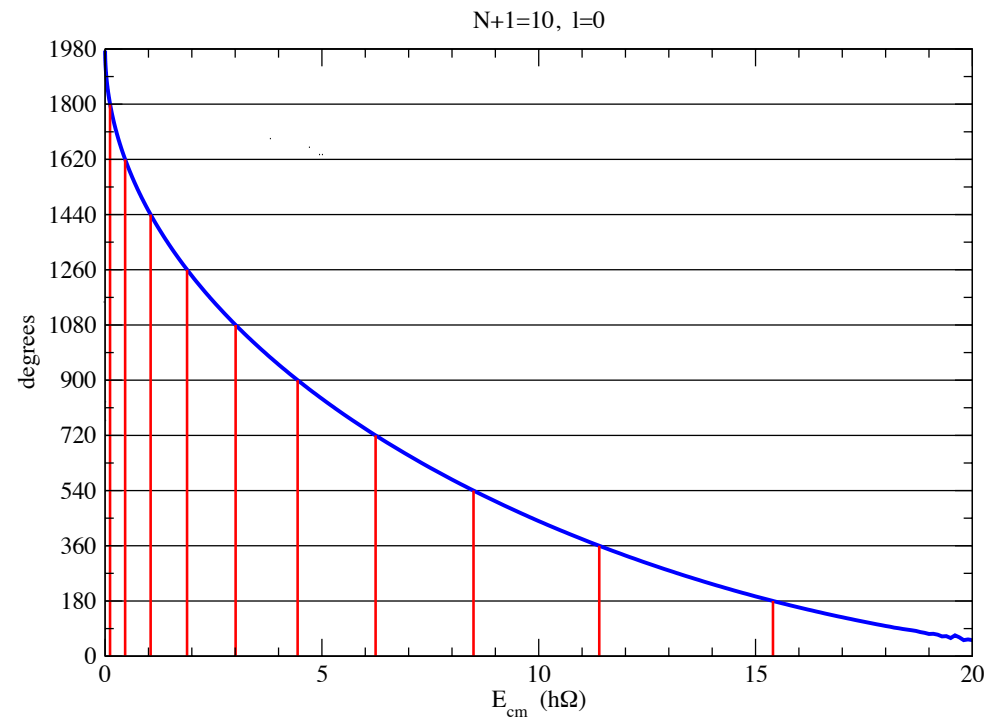
n -A scattering phase shift at NCSM eigenergy E_λ is expressed through known function $f_N(E)$:

$$\delta = f_{N_{\max}}(E_\lambda)$$

Varying $\hbar\Omega$ and hence E_λ , one can get resonance energy E_{res} and width Γ .

$$E_{res} = E_\lambda + \Delta$$

$$\tan f_{N_{\max}}(E_\lambda) = \frac{\Gamma/2}{\Delta}$$



Good description of E_{res} and Γ if $f_{N_{\max}}(E_\lambda)$ is around $\pi/2$, $3\pi/2$, etc.; if $f_{N_{\max}}(E_\lambda)$ is around 0 , π , 2π , etc., there is no hope to get resonance parameters with this approach.

Applications to Relativistic Quantum Field Theory QED (new) and QCD (under development)

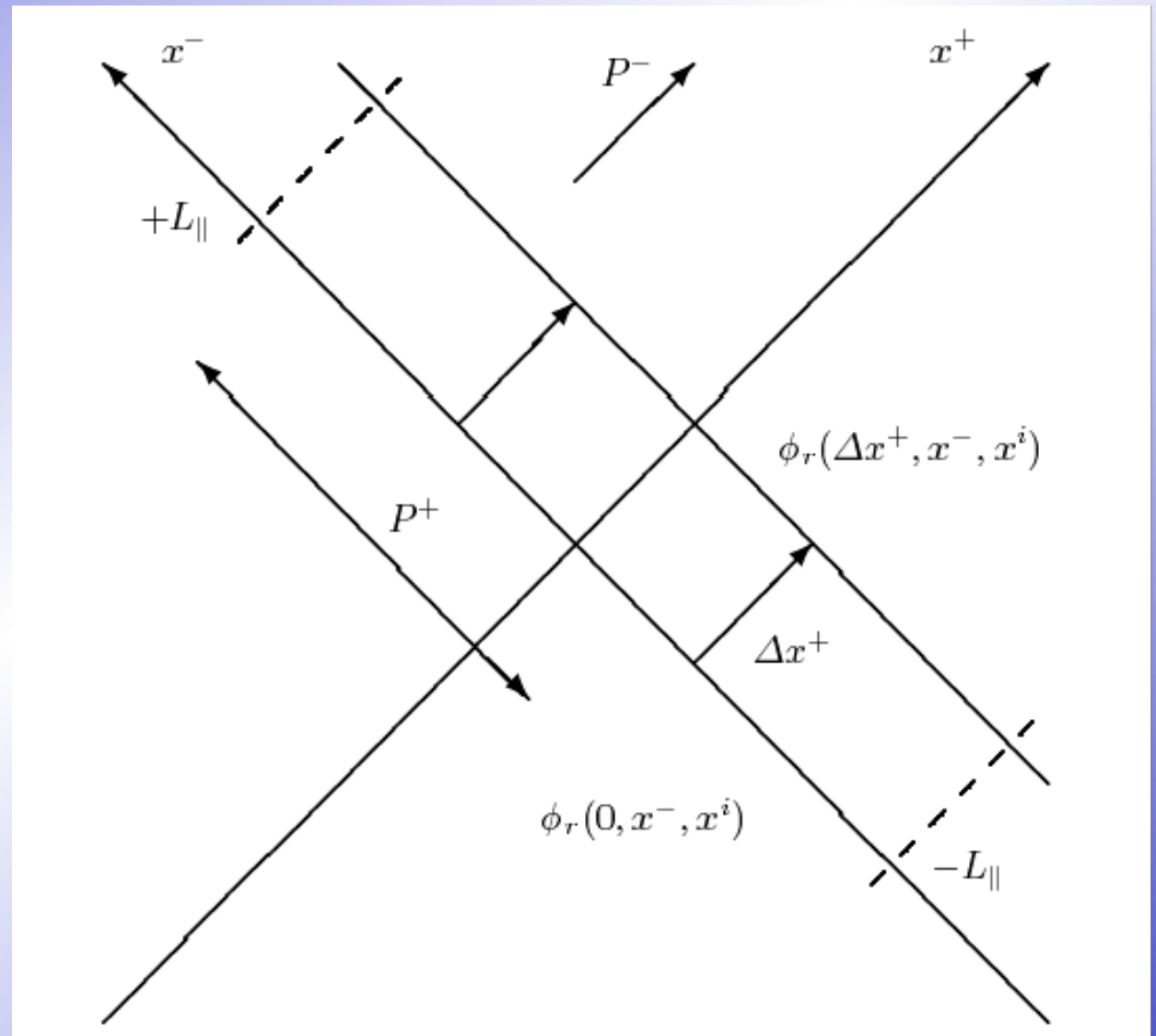
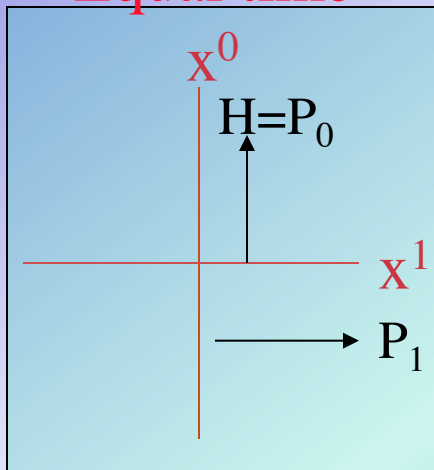
J. P. Vary, H. Honkanen, Jun Li, P. Maris, S. J. Brodsky, A. Harindranath,
G. F. de Teramond, P. Sternberg, E. G. Ng and C. Yang,
“Hamiltonian light-front field theory in a basis function approach”,
Phys. Rev. C 81, 035205 (2010); arXiv nucl-th 0905.1411

H. Honkanen, P. Maris, J. P. Vary and S. J. Brodsky,
“Electron in a transverse harmonic cavity”,
Phys. Rev. Lett. 106, 061603 (2011); arXiv: 1008.0068

Light cone coordinates and generators

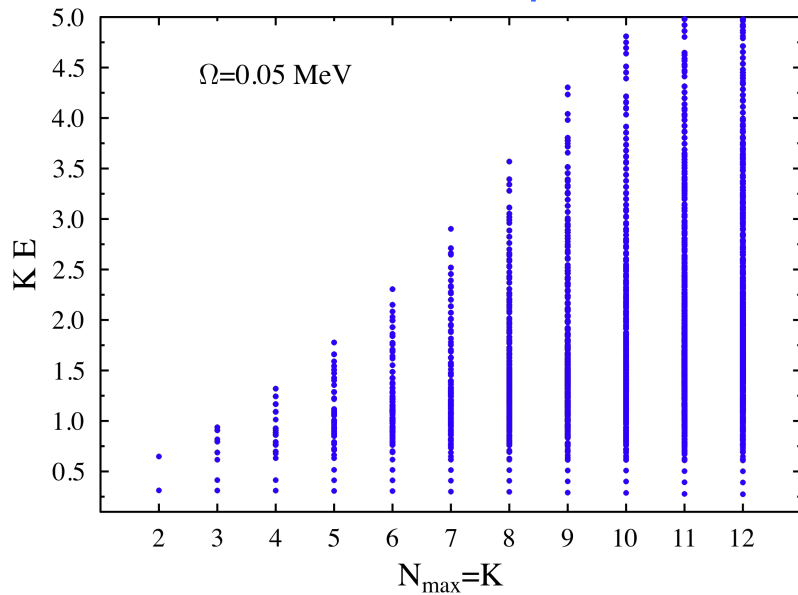
$$M^2 = P^0 P_0 - P^1 P_1 = (P^0 - P^1)(P_0 + P_1) = P^+ P^- = KE$$

Equal time

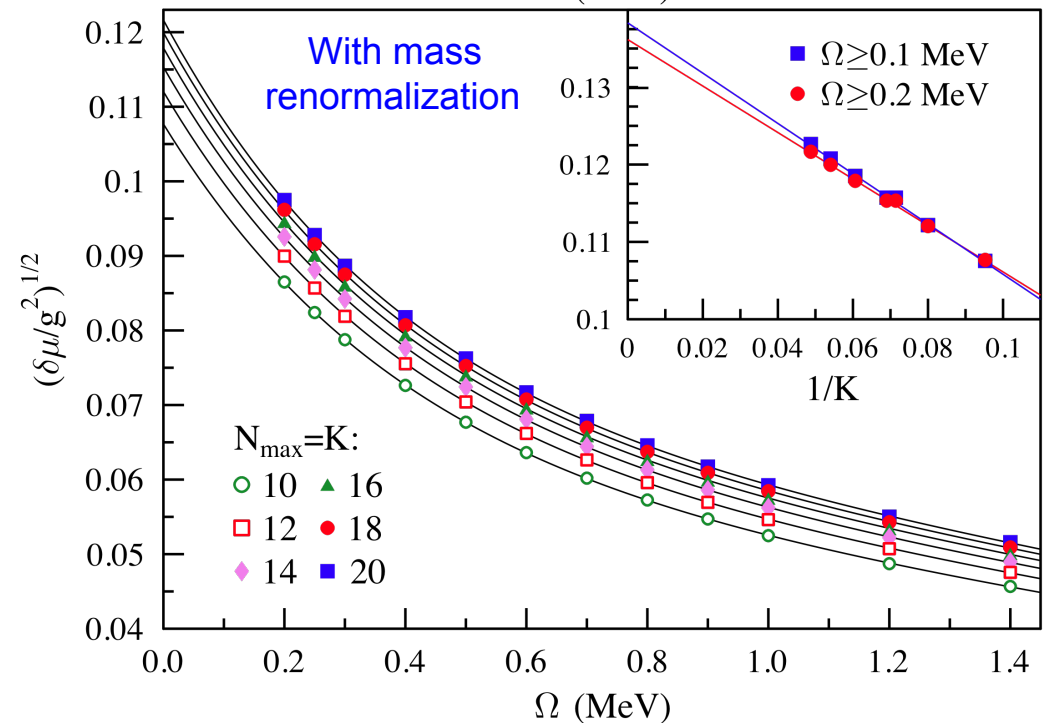
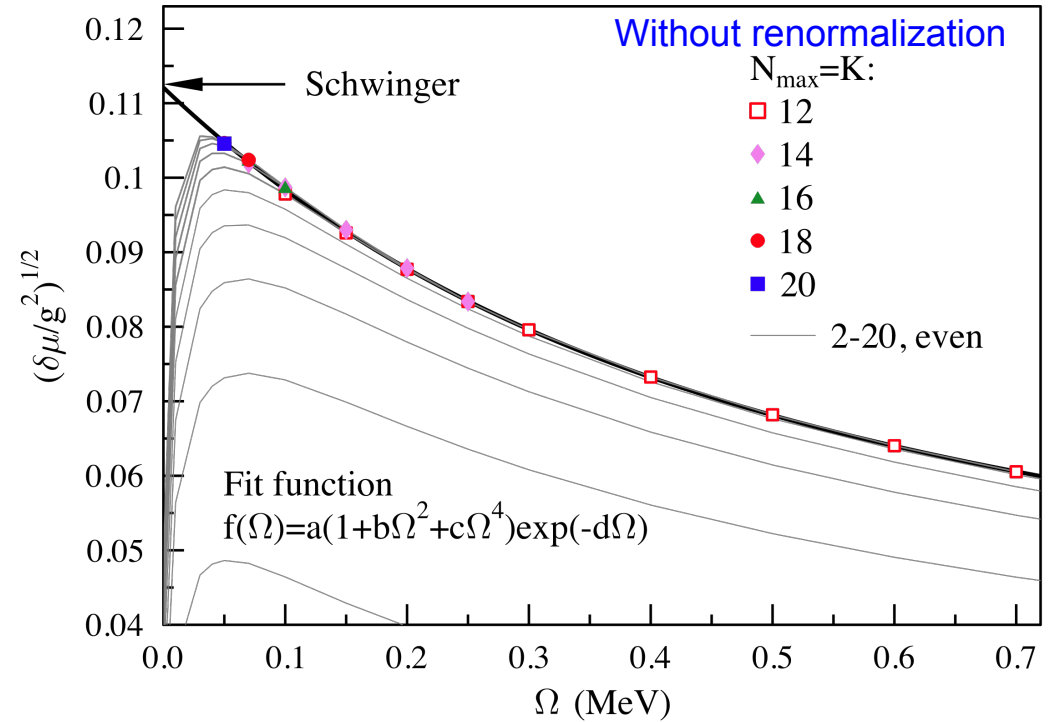


Initial QED problem
 Electron in a transverse
 harmonic trap*
 mass² spectra and
 anomalous moment

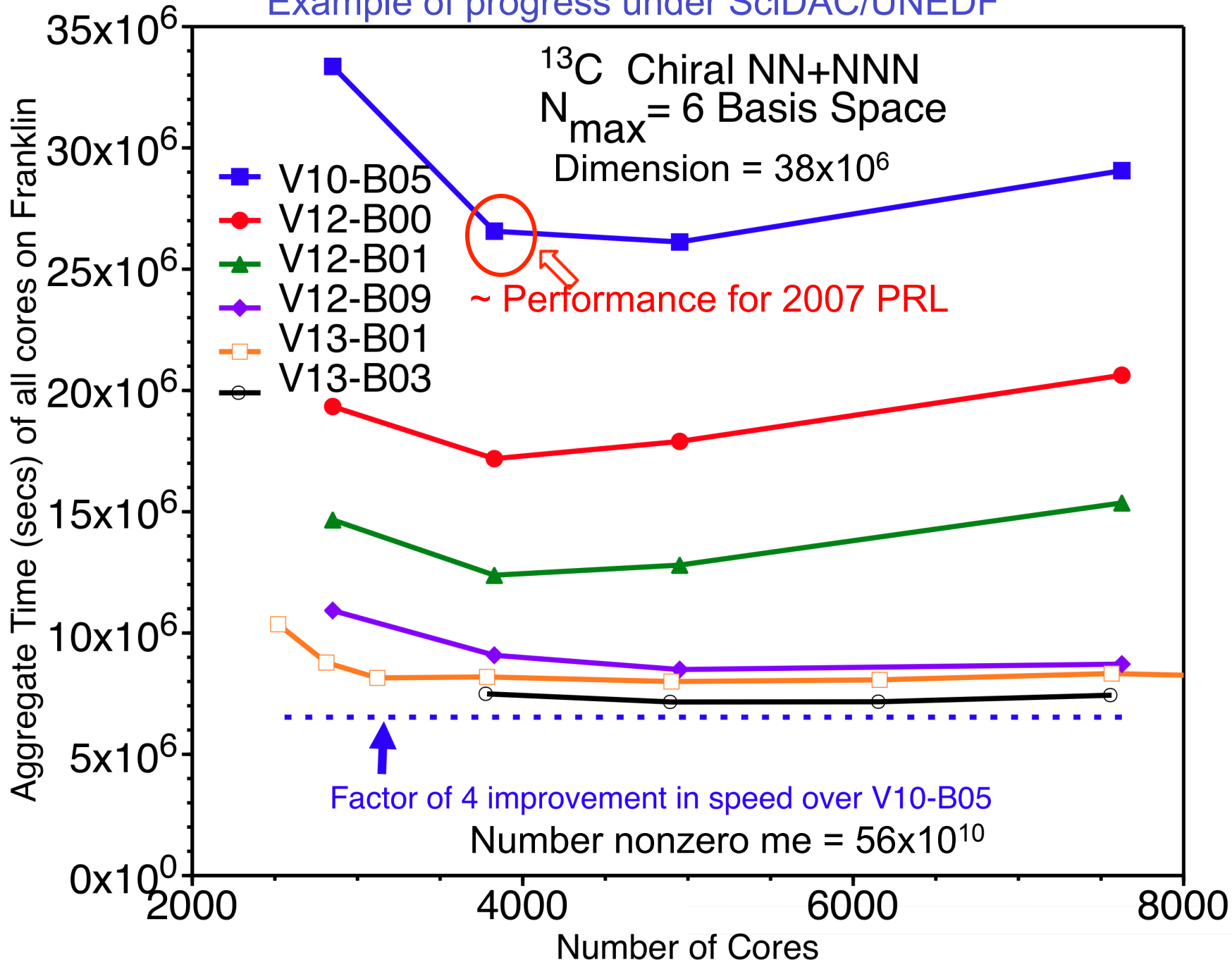
Invariant M² spectra



*H. Honkanen, P. Maris, J.P. Vary, S.J. Brodsky,
 Phys. Rev. Lett. 106, 061603 (2011);
 X. Zhao, P. Maris, J.P. Vary, S.J. Brodsky,
 LC2011 in preparation



Example of progress under SciDAC/UNEDF



Millions of CPU hours - Nuclear ab initio + EDF(fits only)

YEAR	INCITE	OTHER	TOTAL
2008	37	3	40
2009	30	34 ¹	64
2010	40	4	44
2011	43	15	58
2012	67 ²	8 ³	75
2013	109 ²	10 ³	119

¹Includes 30 from Jaguar “Early Science” Award

²Proposed based on current facilities

³Projected based on trends and current facilities

Additional notes:

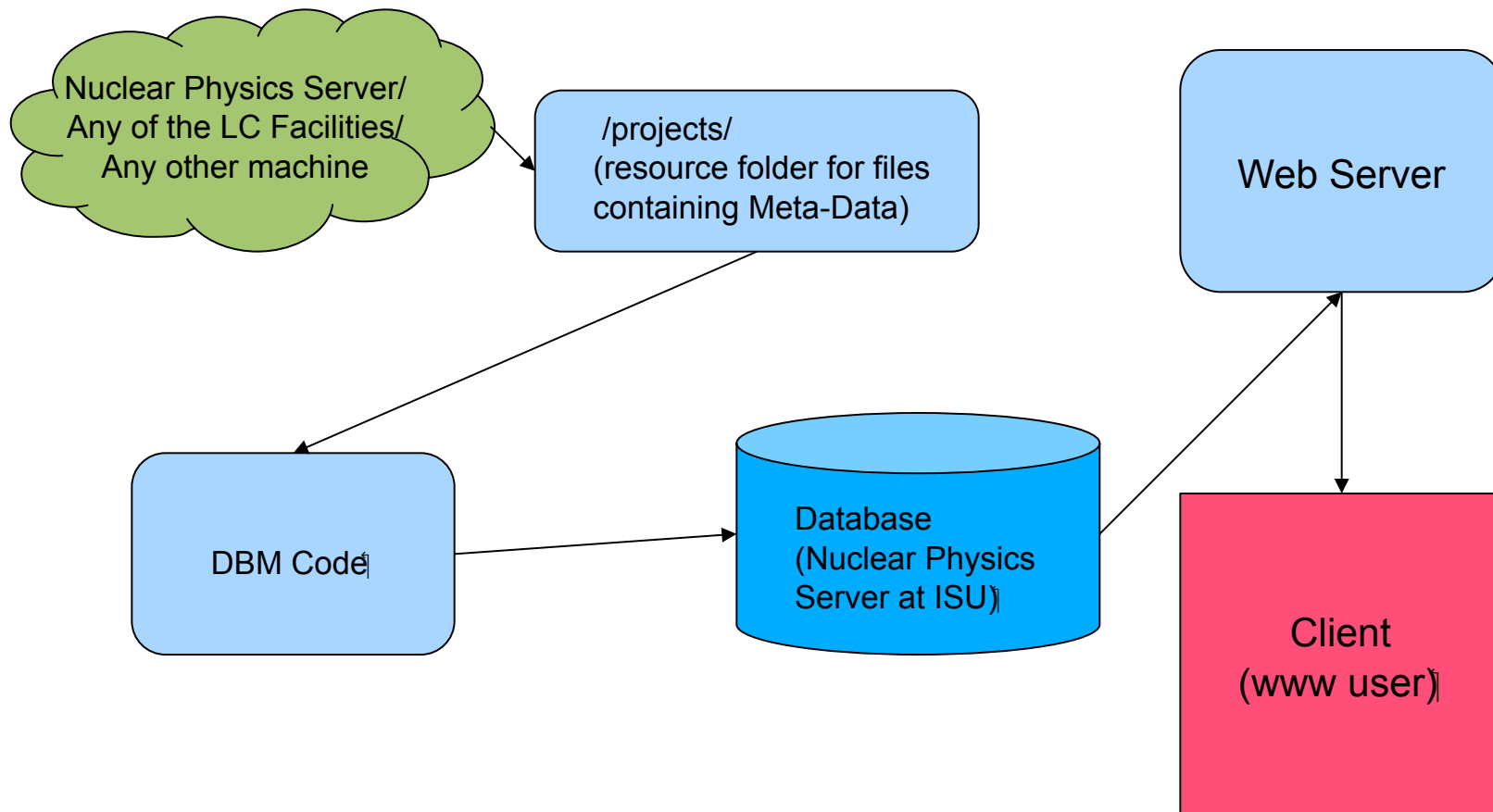
TDSLDA used 70 million in 2010 not included above

NSF PRAC pending and NSF Blue Waters potential data storage needs to reach 200TB by 2013

Data Base Management System - Prototype

First step for Provenance

nuclear.physics.iastate.edu/info/



Observation

Ab initio nuclear physics maximizes predictive power & represents a theoretical and computational physics challenge

Key issues

How to achieve the full physics potential of *ab initio* theory?
Can theory and experiment work more closely to define/solve fundamental physics problems?

Conclusions

We have entered an era of first principles, high precision, nuclear structure and nuclear reaction theory

Linking nuclear physics and the cosmos through the Standard Model is well underway

Pioneering collaborations between Physicists, Computer Scientists and Applied Mathematicians have become essential to progress

Challenges

- ❖ improve NN + NNN + NNNN interactions/renormalization
develop effective operators beyond the Hamiltonian
tests of fundamental symmetries
- ❖ achieve higher precision
quantify the uncertainties - justified through simulations
global dependencies mapped out
- ❖ proceed to heavier systems - breaking out of the p-shell
extend quantum many-body methods
- ❖ evaluate more complex projectile-target reactions
- ❖ achieve efficient use of computational resources – improve
scalability, load-balance, I/O, inter-process communications
- ❖ build a community aiming for investment preservation
support/sustain open libraries of codes/data
develop/implement provenance framework/practices