

TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

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1. Mass Table Calculations
2. Optimal parameters of the functional
3. Improving the functional
4. Visualization and development tools

SciDAC UNEDF Project

Building a Universal Nuclear Energy Density Functional

A Low-Energy Nuclear Physics National HPC Initiative

George F. Bertsch, University of Washington

The mission of the project is three-fold:

First, to find an optimal functional using all our knowledge of the nucleonic Hamiltonian and basic nuclear properties.

Second, to apply the EDF theory and its extensions to validate the functional using all the available relevant nuclear structure data.

Third, to apply the validated theory to properties of interest that cannot be measured, in particular the transition properties needed for reaction theory.

The activities to be supported fall into different areas of nuclear theory and computer science, but the goal can only be achieved by working at the interfaces among these areas. They are: ab initio theory of nuclear wave functions, Effective Field Theory (EFT) and its extensions, self-consistent mean-field description of ground and excited states, large amplitude collective motion, low-energy reaction theory and computer science.

Science Application: Nuclear Physics

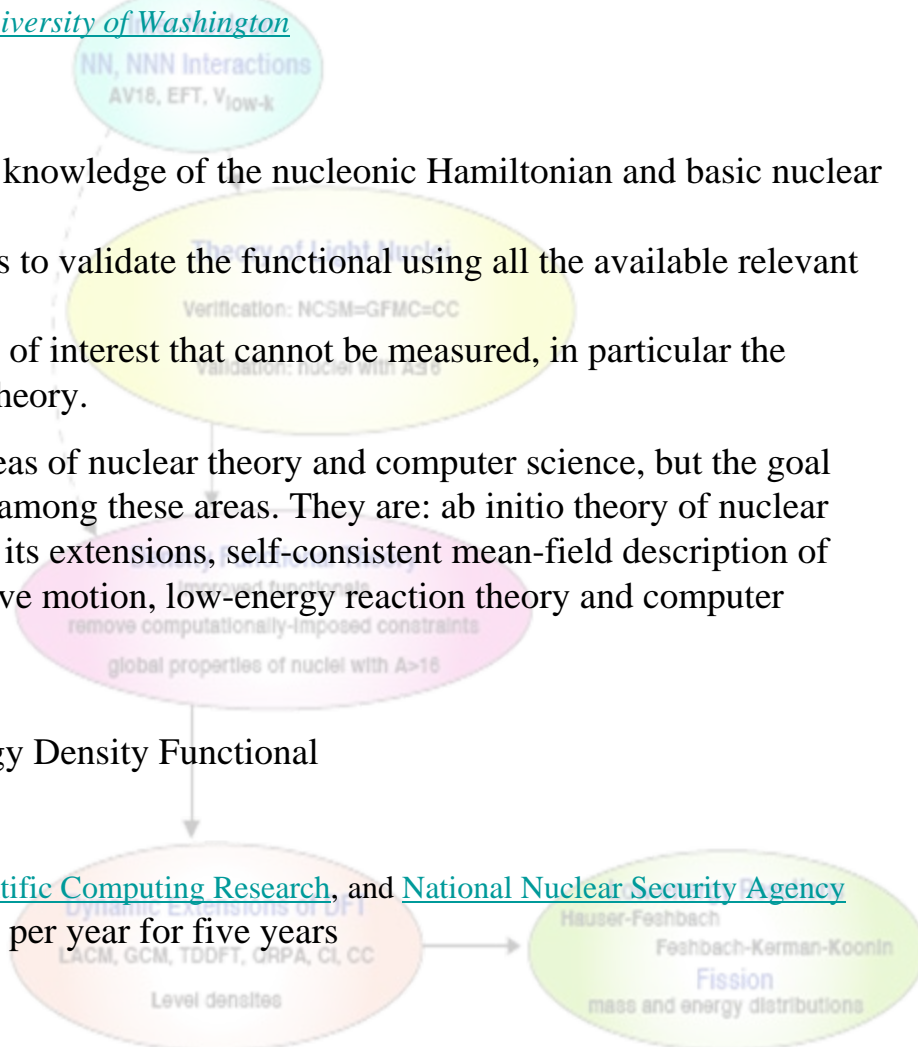
Project Title: Building a Universal Nuclear Energy Density Functional

Principal Investigator: George F. Bertsch

Affiliation: University of Washington

Funding Partners: [Office of Science](#), [Advanced Scientific Computing Research](#), and [National Nuclear Security Agency](#)

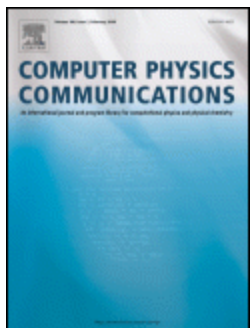
Budget and Duration: Approximately \$3 Million per year for five years



SciDAC

Scientific Discovery through Advanced Computing

<http://unedf.org>



HFBTHO

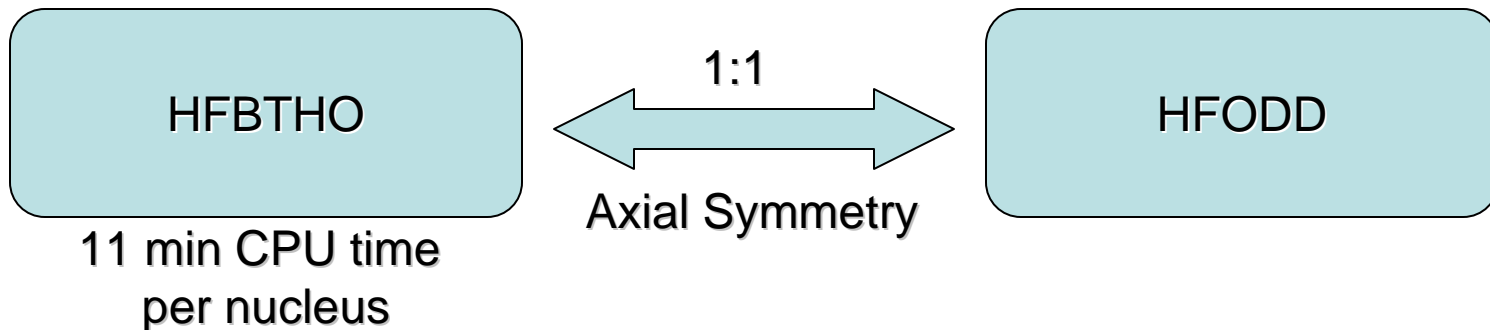
M.V. Stoitsov, J. Dobaczewski, W. Nazarewicz, P. Ring

Axially Deformed Solution of the Skyrme-Hartree-Fock-Bogolyubov Equations
Using The Transformed Harmonic Oscillator Basis. The program HFBTHO

Computer Physics Communications Volume 167, Issue 1, 1 April 2005, Pages 43-63

<http://massexplorer.org/svn/HFBTHO/trunk>

- 2D HFB in HO/THO basis (cylindrical coordinates)
- Time-reversal, axial and parity symmetries
- Skyrme type functional and contact delta pairing
- Even-even, odd-even and odd-odd nuclei
- Easily extendable to arbitrary functional
- Fast alternative for ground-state calculations
- 💡 Continuum as coming from the diagonalization



HFBTHO/HFODD (even-even nuclei)

Nucleus:	^{208}Pb		^{168}Er		^{120}Sn	
Code:	HFBTHO	HFODD	HFBTHO	HFODD	HFBTHO	HFODD
Basis:	2D-HO	3D-HO	2D-HO	3D-HO	2D-HO	3D-HO
N_0	14	14	14	14	14	14
N_{st}	680	680	680	680	680	680
$b_{\perp} = b_z$	2.2348121	2.2348121	2.1566616	2.1566616	2.039048	2.039048
λ_n	-8.114 078	-8.114 02	-6.93605 9	-6.93605 8	-8.015208	-8.015208
λ_p	-8.8104 77	-8.8104 45	-7.15648 6	-7.15647 7	-8.25 1999	-8.24 5192
Δ_n	0	0	0.3945 72	0.3945 78	1.24464 4	1.24464 5
Δ_p	0	0	0.3906 02	0.3906 05	0	0
E_n^{pair}	0	0	-1.716 979	-1.717 024	-12.4263 88	-12.4263 97
E_p^{pair}	0	0	-1.5286 16	-1.5286 43	0	0
R_n	5.61975 6	5.61975 7	5.357578	5.357578	4.7330 88	4.7331
R_p	5.4600 78	5.4600 90	5.22553 8	5.22553 9	4.5962 94	4.5963
Q_n	-0.00000 1	6.6E-11	11.47391 8	11.47392 0	-0.000000 1	6.6E-11
Q_p	-0.00000 1	4.7E-11	7.88022 1	7.88022 4	-0.000000 1	6.6E-11
E_n^{kin}	2525.99 2765	2525.99 1925	1974.614 008	1974.613 824	1338.2104 78	1338.2105 01
E_p^{kin}	1334.85 5572	1334.85 4465	1118.31 3683	1118.31 3442	829.438 221	829.438 221
E_{SO}	-96.375 045	-96.375 003	-80.1868 09	-80.1868 26	-49.0023 07	-49.0023 16
E_{dir}	827.60 7375	827.60 7885	602.810 248	602.810 352	366.326 962	366.326 917
E_{exc}	-31.2484 79	-31.2484 62	-25.93591 0	-25.93590 5	-19.08958	-19.08958
E_{tot}	-1634.14 8867	-1634.14 8120	-1357.658 500	-1357.658 322	-1018.141 626	-1018.141 673

HFBTHO/HFODD (odd nuclei)

state:	1/2+[4,4,0]		1/2+[4,0,0]		3/2-[5,2,1]	
code:	HFBTHO	HFODD	HFBTHO	HFODD	HFBTHO	HFODD
N_0	14	14	14	14	14	14
N_{st}	680	680	680	680	680	680
$b_{\perp} = b_z$	2.0418697	2.0418697	2.0418697	2.0418697	2.0418697	2.0418697
E_{qp}	1.007 644	1.008	1.611 961	1.612	1.38 8951	1.387
λ_n	-7.74 9566	-7.74 94	-7.6961 79	-7.6962	-7.97 2801	-7.97 42
E_n^{pair}	-9.29 4443	-9.29 64	-10.397 019	-10.398 3	-8.703 141	-8.703 5
Δ_n	1.057 516	1.057 6	1.120 611	1.120 7	1.037 402	1.037 3
r_t	4.6895 35	4.6895	4.6904 59	4.6905	4.6895 10	4.6895
β	-0.025 699	-0.0256	0.000 000	0.000 1	0.0 15789	0.0 147
Q_t	-0.86 2706	-0.86 04	0.00 0000	0.00 36	0. 530038	0. 4921
E_n^{kin}	1360.43 7867	1360.442 751	1362.40 7077	1362.40 9601	1358.9 12567	1358.8 86614
E_p^{kin}	827.317 590	827.317 961	827.12 3364	827.12 3676	827.19 5176	827.19 1207
E_{SO}	-50.4 83676	-50.4 85916	-50.92 2860	-50.92 3940	-49.6 07742	-49.5 92026
E_{dir}	365.7436 76	365.7437 74	365.6210 13	365.6210 31	365.736 277	365.735 680
E_{tot}	-1024.70727 5	-1024.70727 2	-1024.301 233	-1024.301 252	-1024.41 5866	-1024.41 6901

¹²⁰Sn: HFBODD: 6 h 39 min CPU / HFBTHO: 3 min CPU

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Calculating the whole Mass Table



↑
protons

2 8 20 28
2 8 20 28
↓
neutrons

proton drip line

neutron drip line

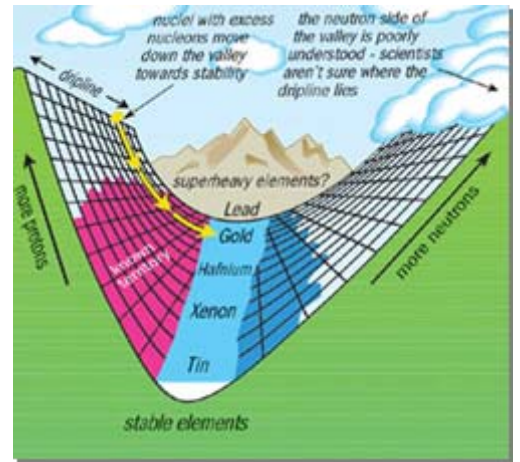
stable nuclei

known nuclei

super heavy nuclei

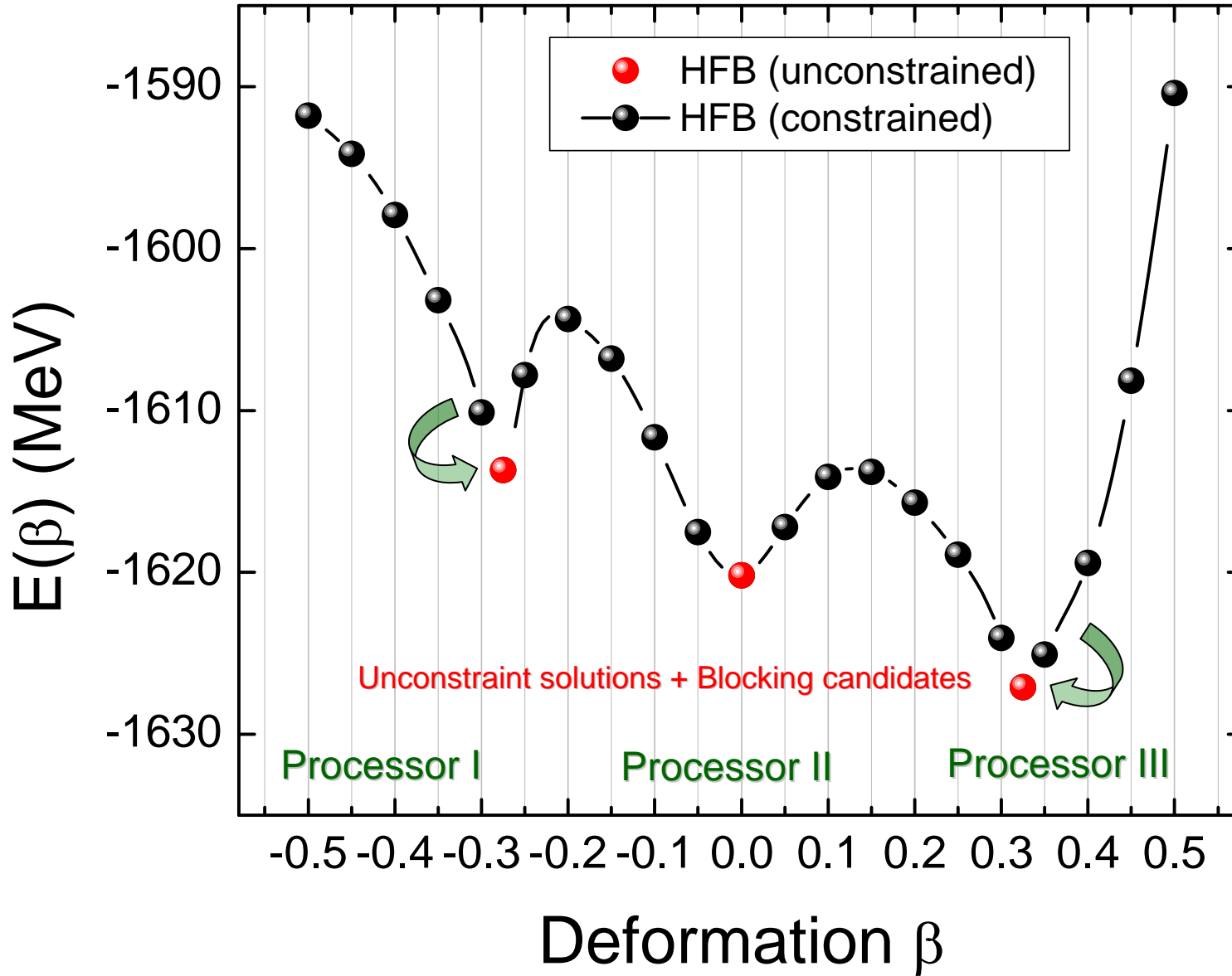
terra incognita

$B(N,Z)/A$



Large-Scale Calculations

Constrained calculations for about 9059 even-even nuclei



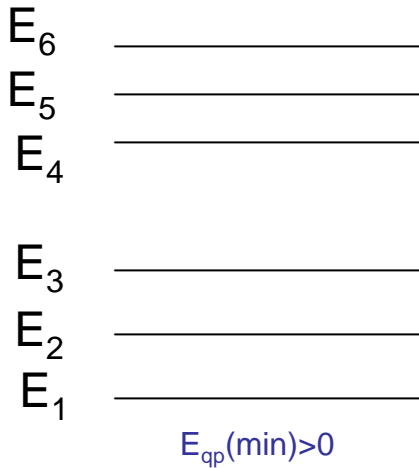
Large-Scale Calculations

Blocking calculations for about 837 220 configurations odd nuclei

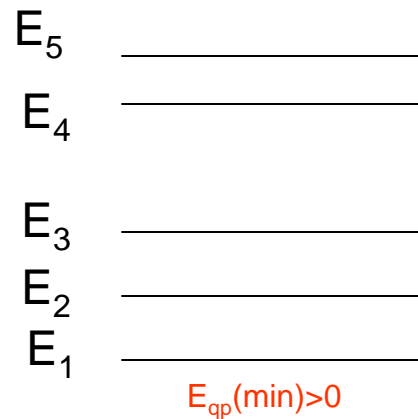
Parent even-even nucleus (N,Z)



neutrons N



protons Z



Self-consistent calculations
for odd nuclei with blocking

odd-even nucleus (N+1,Z)
6 configurations

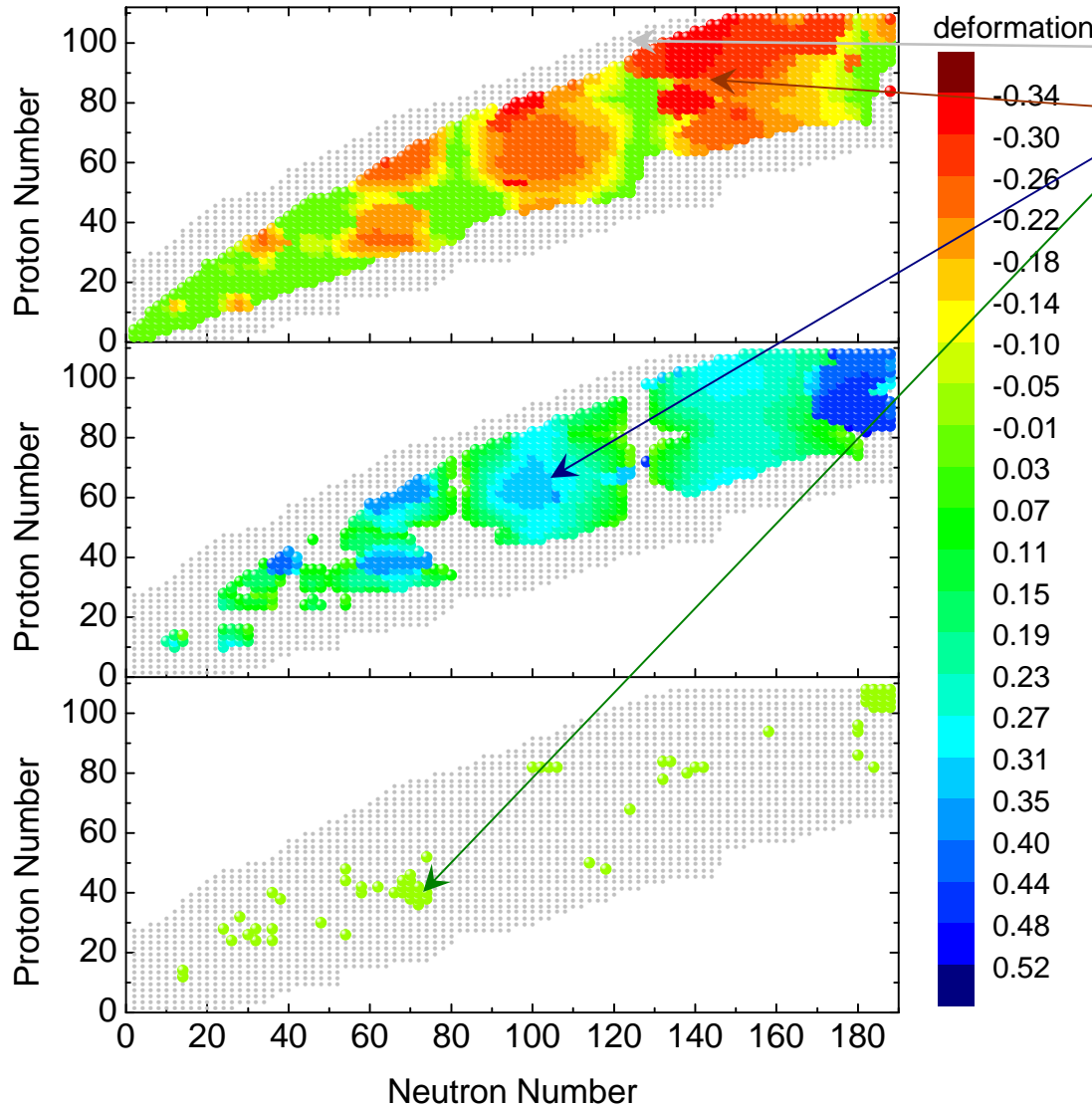
odd-even nucleus (N,Z+1)
5 configurations

odd-odd nucleus (N+1,Z+1)
 $6 \times 5 = 30$ configurations

41 processors

Large-Scale Mass Table Calculations

Calculating the whole Mass Table including even-even, odd-even, odd-odd nuclei



Constrained calculations for
9059 even-even nuclei
2971 even-even bound states

2 CPU hours
using 9060 processors



837 220 blocking candidates for
odd-even and odd-odd nuclei

12 CPU hours
using 9060 processors

- After implementing Broyden method
- all even-even nuclear states converge
 - for odd nuclei: about 0.5%, usually high lying configurations, still diverge

A single 14 CPU hours run

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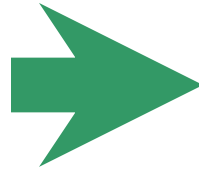
Towards an Optimal Set of Parameters for a Given Functional

Standard Skyrme functional - 13 parameters in ph-part

$$\begin{aligned}
 \mathcal{H}(\mathbf{r}) = & \frac{\hbar^2}{2m} \tau \\
 & + \frac{1}{2} t_0 \left(\left(\frac{x_0}{2} + 1 \right) \rho^2 - \left(x_0 + \frac{1}{2} \right) \sum_q \rho_q^2 \right) \\
 & + \frac{1}{4} t_1 \left(\left(\frac{x_1}{2} + 1 \right) \rho \tau - \left(x_1 + \frac{1}{2} \right) \sum_q \rho_q \tau_q \right) \\
 & + \frac{1}{4} t_2 \left(\left(\frac{x_2}{2} + 1 \right) \rho \tau + \left(x_2 + \frac{1}{2} \right) \sum_q \rho_q \tau_q \right) \\
 & - \frac{3}{16} t_1 \left(\left(\frac{x_1}{2} + 1 \right) \rho \Delta \rho + \left(x_1 + \frac{1}{2} \right) \sum_q \rho_q \Delta \rho_q \right) \\
 & + \frac{1}{16} t_2 \left(\left(\frac{x_2}{2} + 1 \right) \rho \Delta \rho + \left(x_2 + \frac{1}{2} \right) \sum_q \rho_q \Delta \rho_q \right) \\
 & + \frac{1}{12} t_3 \left(\left(\frac{x_3}{2} + 1 \right) \rho^2 - \left(x_3 + \frac{1}{2} \right) \sum_q \rho_q^2 \right) \rho^\gamma \\
 & - \frac{1}{8} (t_1 x_1 + t_2 x_2 - 5(t_0 + t_e)) \sum_q \mathbf{J}_q^2 \\
 & - \frac{1}{16} (t_1 (x_1 - 1) + t_2 (x_2 + 1) - 10t_0) \mathbf{J}_n \cdot \mathbf{J}_p \\
 & - (b_4 \rho \nabla \cdot \mathbf{J} + b'_4 \sum_q \rho_q \nabla \cdot \mathbf{J}_q),
 \end{aligned}$$

t-parameters

{ $t_0, t_1, t_2, t_3, x_0, x_1, x_2, x_3, t_0, t_e, b_4, b'_4, \gamma$ }



{ $C_{t_0}^\rho, C_{t_1D}^\rho, C_{t_2D}^{\Delta\rho}, C_{t_1}^{\Delta\rho}, C_{t_1}^{\tau}, C_{t_1}^J, C_{t_1}^{\nabla J}, \gamma$ }

C-parameters

$$\begin{aligned}
 \mathcal{H}(\mathbf{r}) = & \frac{\hbar^2}{2m} \tau_0 + \mathcal{H}_0(\mathbf{r}) + \mathcal{H}_1(\mathbf{r}), \\
 \mathcal{H}_t(\mathbf{r}) = & C_t^\rho \rho_t^2 + C_t^{\Delta\rho} \rho_t \Delta \rho_t + C_t^\tau \rho_t \tau_t \\
 & + \frac{1}{2} C_t^J \mathbf{J}_t^2 + C_t^{\nabla J} \rho_t \nabla \cdot \mathbf{J}_t,
 \end{aligned}$$

$$C_t^\rho = C_{t_0}^\rho + C_{t_1D}^\rho \rho_0^\gamma, \quad (t = 0, 1).$$

$$\begin{aligned}
 C_{00}^\rho &= \frac{3}{8} t_0, & C_{10}^\rho &= -\frac{1}{4} t_0 \left(x_0 + \frac{1}{2} \right), \\
 C_{0D}^\rho &= \frac{1}{16} t_3, & C_{1D}^\rho &= -\frac{1}{24} t_3 \left(x_3 + \frac{1}{2} \right), \\
 C_0^{\Delta\rho} &= \frac{1}{16} t_2 \left(x_2 + \frac{5}{4} \right) - \frac{9}{64} t_1, \\
 C_1^{\Delta\rho} &= \frac{3}{32} t_1 \left(x_1 + \frac{1}{2} \right) + \frac{1}{32} t_2 \left(x_2 + \frac{1}{2} \right) \\
 C_0^\tau &= \frac{3}{16} t_1 + \frac{1}{4} t_2 \left(x_2 + \frac{5}{4} \right), \\
 C_1^\tau &= -\frac{1}{8} t_1 \left(x_1 + \frac{1}{2} \right) + \frac{1}{8} t_2 \left(x_2 + \frac{1}{2} \right), \\
 C_0^J &= -\frac{1}{8} (t_1 (x_1 - \frac{1}{2}) + t_2 (x_2 + \frac{1}{2})) + \frac{5}{16} (3 t_0 + t_e), \\
 C_1^J &= \frac{1}{16} (t_1 - t_2) + \frac{5}{16} (t_0 - t_e), \\
 C_0^{\nabla J} &= -b_4 - \frac{1}{2} b'_4, & C_1^{\nabla J} &= -\frac{1}{2} b'_4,
 \end{aligned}$$

Optimization in Terms of Infinite Nuclear Matter Properties

$$\frac{E^{NM}}{A} \equiv W(\rho_c) \approx -16 \text{ MeV},$$

$$P^{NM} \equiv \rho^2 \frac{dW(\rho)}{d\rho} \Big|_{\rho=\rho_c} = 0, \quad \rho_c \approx 0.16 \text{ fm}^{-3}$$

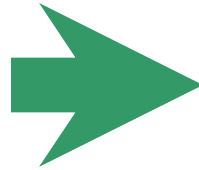
$$K^{NM} = 9\rho^2 \frac{d^2W(\rho)}{d\rho^2} \Big|_{\rho=\rho_c} \approx 220 \text{ MeV},$$

$$M_s^{*NM} = \frac{2m}{\hbar^2} \frac{dW}{d\tau} \Big|_{\rho=\rho_c} \approx 1,$$

$$a_{sym}^{NM} \equiv \frac{1}{2} \frac{d^2W(I, \rho)}{dI^2} \Big|_{\substack{\rho=\rho_c \\ I=0}} = 32.5 \text{ MeV},$$

$$L^{NM} \equiv 3\rho_c \frac{da_{sym}^{NM}}{d\rho_c} \approx 50 \text{ MeV},$$

$$M_v^{*NM} \approx 1,$$



$$\gamma = \frac{-K^{NM} + \frac{\hbar^2}{2m} (4M_s^{*NM} - 3) \tau_c - 9 \frac{E^{NM}}{A}}{\frac{\hbar^2}{2m} (6M_s^{*NM} - 9) \tau_c + 9 \frac{E^{NM}}{A}},$$

$$C_{00}^\rho = \frac{\frac{\hbar^2}{2m} ((2 - 3\gamma) M_s^{*NM} - 3) \tau_c + 3(1 + \gamma) \frac{E^{NM}}{A}}{3\gamma\rho_c},$$

$$C_{0D}^\rho = \frac{\frac{\hbar^2}{2m} (3 - 2M_s^{*NM}) \tau_c - 3 \frac{E^{NM}}{A}}{3\gamma\rho_c^{1+\gamma}},$$

$$C_0^\tau = \frac{\hbar^2}{2m} (M_s^{*NM} - 1) \frac{1}{\rho_c}.$$

$$C_1^\tau = C_0^\tau - \frac{\hbar^2}{2m} (M_v^{*NM} - 1) \frac{1}{\rho_c}$$

$$= \frac{\hbar^2}{2m} (M_s^{*NM} - M_v^{*NM}) \frac{1}{\rho_c},$$

$$C_{10}^\rho = \frac{1}{27\gamma\rho_c} \left[27(1 + \gamma) a_{sym}^{NM} C - 9L^{NM} \right.$$

$$\left. - 5 \left((1 + 3\gamma) \frac{\hbar^2}{2m} - (2 - 3\gamma) (C_0^\tau + 3C_1^\tau) \rho_c \right) \tau_c \right],$$

$$C_{1D}^\rho = \frac{1}{27\gamma\rho_c^{\gamma+1}} \left[-27a_{sym}^{NM} C + 9L^{NM} \right.$$

$$\left. + 5 \left(\frac{\hbar^2}{2m} - 2\rho_c (C_0^\tau + 3C_1^\tau) \right) \tau_c \right],$$

Skyrme functional fitting at 13% of the computational expense

Jorge Moré, Jason Sarich, and **Stefan Wild**

Mathematics and
Computer Science Division
Argonne National Laboratory



3rd LACM-EFES-JUSTIPEN Workshop
February 25, 2009

Our Optimization/NLS/NLR Problem

2 measurement types: binding energy (E), radius (R)

$\mathcal{N}_E = 63$ nuclei (27 spherical, 36 deformed)

$\mathcal{N}_R =$ the spherical nuclei from \mathcal{N}_E

$d_{t,i}$ experimental data ($t \in \{E, R\}$) for i th nucleus

$s_{t,i}(\theta)$ HFBTHO simulation of type t for i th nucleus

θ 9 simulation parameters from intervals of interest

$$f(\theta) = \frac{1}{\sigma_E^2} \sum_{i=1}^{63} (d_{E,i} - s_{E,i}(\theta))^2 + \frac{1}{\sigma_R^2} \sum_{i=1}^{27} (d_{R,i} - s_{R,i}(\theta))^2,$$

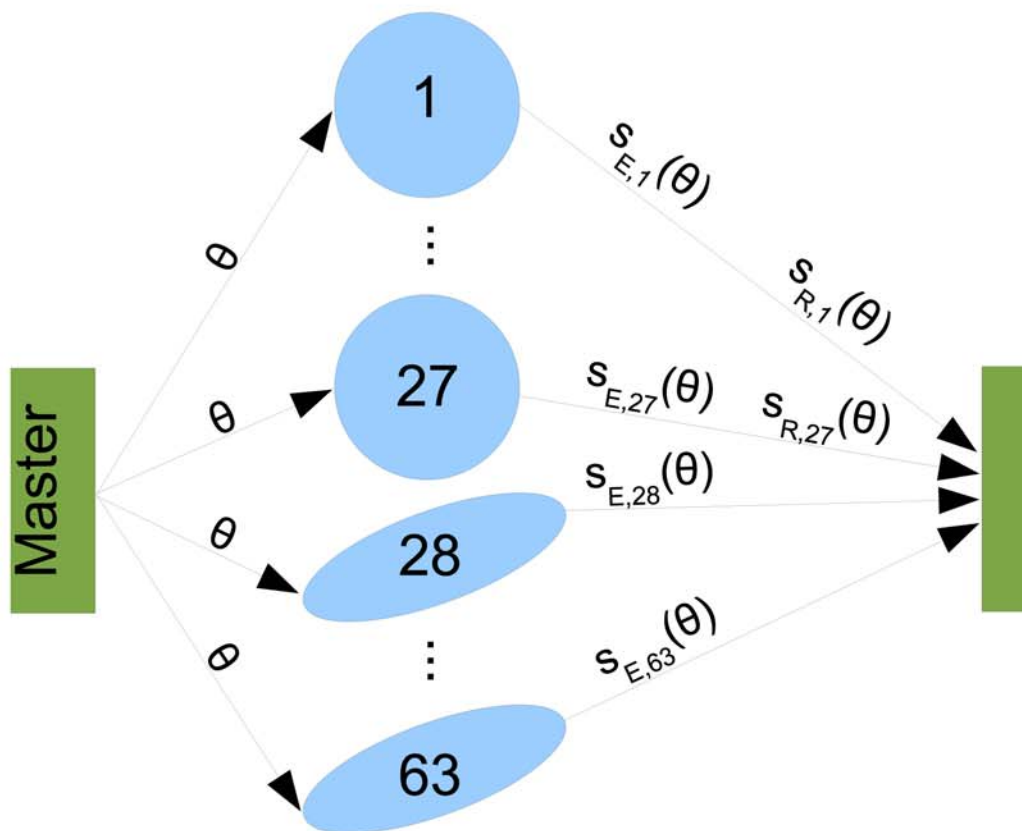
σ_t weights: $\sigma_E = 2$ [MeV], $\sigma_R = .02$ [fm]

Chosen to balance goals of energy and radius fitting

We Cannot Afford 9 Hours per Evaluation!

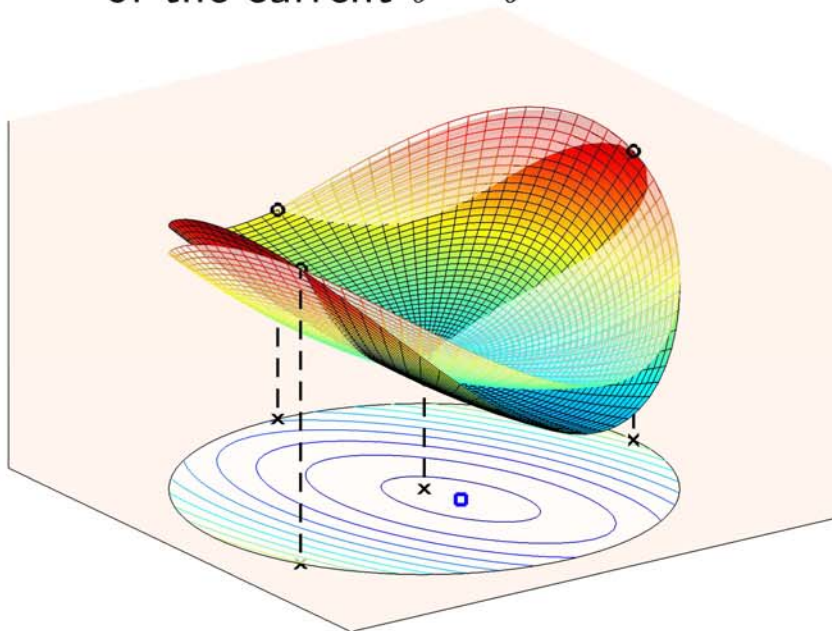
Move to a cluster

- ▶ 64 processors for 63 nuclei
- ▶ Simulate each nucleus independently
- ▶ Will be bound by the longest HFBTHO simulation time



A Sketch of MFQnls

Idea: Build a quadratic model of the objective f in a neighborhood of the current $\theta = \theta^{(k)}$



$$q(\theta^{(k)} + s) = c + g^T s + \frac{1}{2} s^T H s:$$

Find the $\frac{(n+1)(n+2)}{2}$ model coefficients $c, g, H = H^T$ so:

$$q(\hat{\theta}^{(i)}) = f(\hat{\theta}^{(i)}) \quad \forall \hat{\theta}^{(i)} \in \mathcal{Y}$$

\mathcal{Y} = interpolation set based on the θ at which we've previously evaluated f

Taking Advantage of the Structure of f

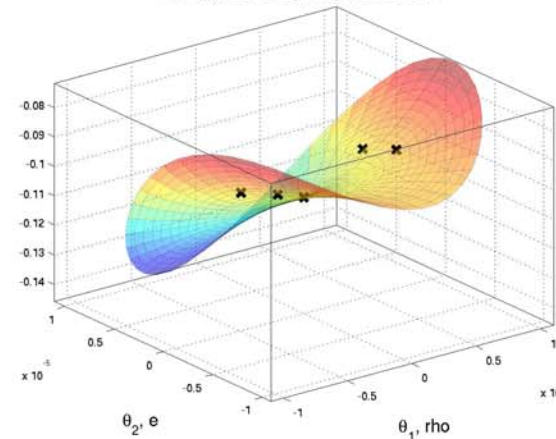
Build an interpolation model for

each residual $\frac{d_i - s_{t,i}(\theta)}{\sigma_i}$.

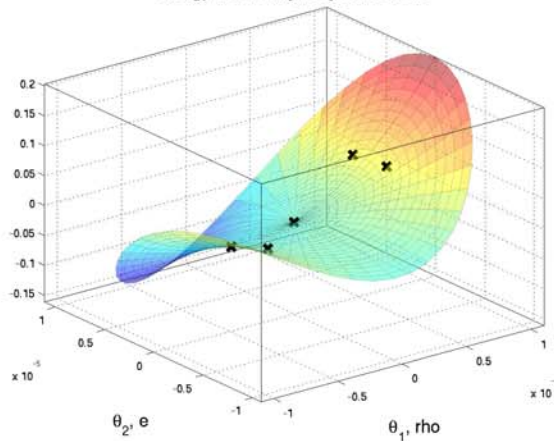
Allows us to obtain an approximate

Jacobian, $J \approx \begin{bmatrix} g_1^T \\ \vdots \\ g_m^T \end{bmatrix}$

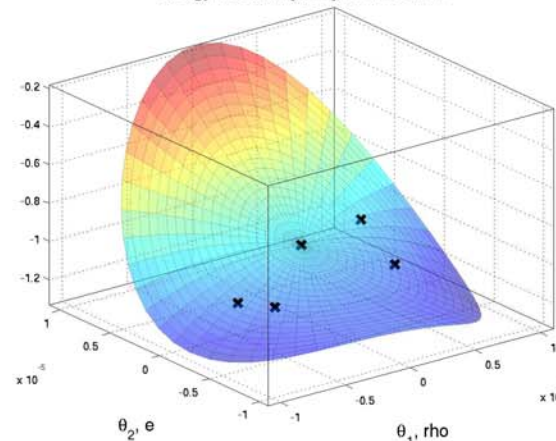
Energy Residual [MeV], Nucleus #10



Energy Residual [MeV], Nucleus #9



Energy Residual [MeV], Nucleus #22



Sensitivity

Assuming the errors $\frac{d_{t,i} - s_{t,i}(\theta)}{\sigma_t}$ are

- ▶ iid Normal with mean zero (← big assumption?)

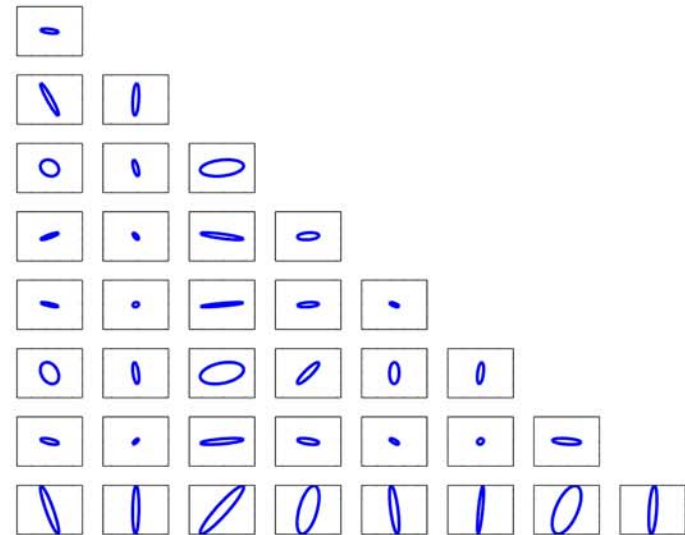
Use Jacobian approximation at $\hat{\theta}$ to estimate the covariance matrix

$$\text{Cov}(\hat{\theta}) \approx 2 \left(\nabla^2 f(\hat{\theta}) \right)^{-1} \approx \left(\hat{J}^T \hat{J} \right)^{-1}$$

Correlations

$$\text{Cor}(\theta_i, \theta_j) = \frac{\text{Cov}(\theta)_{i,j}}{\sqrt{\text{Cov}(\theta)_{i,i} \text{Cov}(\theta)_{j,j}}}$$

Reduce the problem by accounting for strong correlations.



Towards the optimal parameters of a given functional

$$\rho_c, \frac{E^{NM}}{A}, K^{NM}, M_s^{*NM}, a_{sym}^{NM}, L^{NM}, M_v^{*NM}, C_t^{\Delta\rho}, C_t^J, C_t^{\nabla J}$$

Correlation Matrix

1	0.0117	0.0168	0.0203	0.0282	0.0164	0.0020
1	-0.036	-0.035	-0.032	0.026	-0.0004	
1	-0.020	-0.018	0.0168	-0.0009		
1	-0.019	0.0166	-0.0008			
1	0.0125	-0.0012				
1	0.0010					
1						

Preliminary estimates

$$\frac{E^{NM}}{A} \approx -16.05 \text{ MeV},$$

$$\rho_c \approx 0.157 \text{ fm}^{-3},$$

$$K^{NM} \approx 218.5 \text{ MeV},$$

$$M_s^{*NM} \approx 0.997,$$

$$a_{sym}^{NM} = 32.36 \text{ MeV},$$

$$L^{NM} \approx 46.3 \text{ MeV},$$

$$M_v^{*NM} \approx 1.37,$$

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Most general form of the functional one can consider by now

$$\mathcal{H}(r) = \frac{\hbar^2}{2m} \tau_0 + \mathcal{H}_0(r) + \mathcal{H}_1(r),$$

$$\mathcal{H}_t(r) = U_t^{\rho\rho} \rho_t^2 + U_t^{\rho\tau} \rho_t \tau_t + U_t^{J^2} J_t^2$$

$t=(0,1)$, e.g.,

$$\rho_0 = \rho_n + \rho_p,$$

$$\rho_1 = \rho_n - \rho_p$$

$$+ U_t^{\rho\Delta\rho} \rho_t \Delta\rho_t + U_t^{\nabla\rho\nabla\rho} (\nabla\rho_t)^2$$

$$+ U_t^{\rho\nabla J} \rho_t \nabla \cdot J_t + U_t^{J\nabla\rho} J_t \cdot \nabla\rho_t,$$

six densities

$$\rho_t, \tau_t, J_t,$$

grouped in fifteen terms proportional to

$$\tau_0, \rho_t^2, \rho_t \tau_t, J_t^2, \rho_t \Delta\rho_t, (\nabla\rho_t)^2, \rho_t \nabla \cdot J_t, \nabla\rho_t \cdot J_t$$

and multiplied by fifteen amplitudes

$$\frac{\hbar^2}{2m}, U_t^{\rho\rho}, U_t^{\rho\tau}, U_t^{J^2}, U_t^{\rho\Delta\rho}, U_t^{\nabla\rho\nabla\rho}, U_t^{\rho\nabla J}, U_t^{J\nabla\rho},$$

U → C : Standard Skyrme functional

U → D : Functional with density dependent coupling constants

U → G : DME functional

U → F : Fayans functional

TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

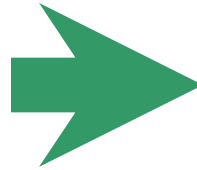
Standard Skyrme functional

U-functions: C-parameters

$$\begin{aligned} \mathcal{H}(\mathbf{r}) &= \frac{\hbar^2}{2m} \tau_0 + \mathcal{H}_0(\mathbf{r}) + \mathcal{H}_1(\mathbf{r}), \\ \mathcal{H}_t(\mathbf{r}) &= C_t^\rho \rho_t^2 + C_t^{\Delta\rho} \rho_t \Delta\rho_t + C_t^\tau \rho_t \tau_t \\ &\quad + \frac{1}{2} C_t^J \mathbf{J}_t^2 + C_t^{\nabla J} \rho_t \nabla \cdot \mathbf{J}_t, \end{aligned}$$

$$C_t^\rho = C_{t0}^\rho + C_{tD}^\rho \rho_0^\gamma, \quad (t = 0, 1).$$

$$\begin{aligned} C_{00}^\rho &= \frac{3}{8} t_0, & C_{10}^\rho &= -\frac{1}{4} t_0 \left(x_0 + \frac{1}{2}\right), \\ C_{0D}^\rho &= \frac{1}{16} t_3, & C_{1D}^\rho &= -\frac{1}{24} t_3 \left(x_3 + \frac{1}{2}\right), \\ C_0^{\Delta\rho} &= \frac{1}{16} t_2 \left(x_2 + \frac{5}{4}\right) - \frac{9}{64} t_1, \\ C_1^{\Delta\rho} &= \frac{3}{32} t_1 \left(x_1 + \frac{1}{2}\right) + \frac{1}{32} t_2 \left(x_2 + \frac{1}{2}\right), \\ C_0^\tau &= \frac{3}{16} t_1 + \frac{1}{4} t_2 \left(x_2 + \frac{5}{4}\right), \\ C_1^\tau &= -\frac{1}{8} t_1 \left(x_1 + \frac{1}{2}\right) + \frac{1}{8} t_2 \left(x_2 + \frac{1}{2}\right), \\ C_0^J &= -\frac{1}{8} (t_1(x_1 - \frac{1}{2}) + t_2(x_2 + \frac{1}{2})) + \frac{5}{16} (3t_0 + t_e), \\ C_1^J &= \frac{1}{16} (t_1 - t_2) + \frac{5}{16} (t_0 - t_e), \\ C_0^{\nabla J} &= -b_4 - \frac{1}{2} b'_4, & C_1^{\nabla J} &= -\frac{1}{2} b'_4, \end{aligned}$$



$$\begin{aligned} \mathcal{H}(\mathbf{r}) &= \frac{\hbar^2}{2m} \tau \\ &\quad + \frac{1}{2} t_0 \left(\left(\frac{x_0}{2} + 1\right) \rho^2 - \left(x_0 + \frac{1}{2}\right) \sum_q \rho_q^2 \right) \\ &\quad + \frac{1}{4} t_1 \left(\left(\frac{x_1}{2} + 1\right) \rho \tau - \left(x_1 + \frac{1}{2}\right) \sum_q \rho_q \tau_q \right) \\ &\quad + \frac{1}{4} t_2 \left(\left(\frac{x_2}{2} + 1\right) \rho \tau + \left(x_2 + \frac{1}{2}\right) \sum_q \rho_q \tau_q \right) \\ &\quad - \frac{3}{16} t_1 \left(\left(\frac{x_1}{2} + 1\right) \rho \Delta\rho + \left(x_1 + \frac{1}{2}\right) \sum_q \rho_q \Delta\rho_q \right) \\ &\quad + \frac{1}{16} t_2 \left(\left(\frac{x_2}{2} + 1\right) \rho \Delta\rho + \left(x_2 + \frac{1}{2}\right) \sum_q \rho_q \Delta\rho_q \right) \\ &\quad + \frac{1}{12} t_3 \left(\left(\frac{x_3}{2} + 1\right) \rho^2 - \left(x_3 + \frac{1}{2}\right) \sum_q \rho_q^2 \right) \rho^\gamma \\ &\quad - \frac{1}{8} (t_1 x_1 + t_2 x_2 - 5(t_0 + t_e)) \sum_q \mathbf{J}_q^2 \\ &\quad - \frac{1}{16} (t_1 (x_1 - 1) + t_2 (x_2 + 1) - 10t_0) \mathbf{J}_n \cdot \mathbf{J}_p \\ &\quad - (b_4 \rho \nabla \cdot \mathbf{J} + b'_4 \sum_q \rho_q \nabla \cdot \mathbf{J}_q), \end{aligned}$$

TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

Density Dependent Coupling Constants

I. Density dependence of all the coupling constants

For the time-reversal and spherical symmetries imposed, the extended EDF reads

$$\mathcal{H}_t(r) = C_t^\rho \rho_t^2 + C_t^\tau \rho_t \tau_t + C_t^{\Delta\rho} \rho_t \Delta\rho_t + \frac{1}{2} C_t^J J_t^2 + C_t^{\nabla J} \rho_t \nabla \cdot J_t \\ + C_t^{\nabla\rho} (\nabla\rho_t)^2 + C_t^{\nabla\rho'} (\nabla\rho_t) \cdot J_t$$

and depends linearly on 38 coupling constants,

$$C_t^\rho, C_t^\tau, C_t^{\Delta\rho}, C_t^J, \text{ and } C_t^{\nabla J},$$

$$\alpha_t^\rho, \alpha_t^\tau, \alpha_t^{\Delta\rho}, \alpha_t^J, \alpha_t^{\nabla J}, \alpha_t^{\nabla\rho}, \text{ and } \alpha_t^{\nabla\rho'},$$

$$\beta_t^\rho, \beta_t^\tau, \beta_t^{\Delta\rho}, \beta_t^J, \beta_t^{\nabla J}, \beta_t^{\nabla\rho}, \text{ and } \beta_t^{\nabla\rho'},$$

for $t = 0$ and 1 , i.e.,

$$C_t^m(\rho_0, \rho_1) = C_t^m \left[1 + \alpha_t^m \left(1 - \left(\frac{\rho_0}{\rho_{\text{sat}}} \right)^{\gamma_t^m} \right) + \beta_t^m \left(\left(\frac{\rho_1}{\rho_{\text{sat}}} \right)^2 \right)^{\eta_t^m} \right]$$

and on 28 powers γ_t^m and η_t^m .

TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

Density Dependent Coupling Constants

$$U \longrightarrow D_t^m = C_t^m \left(1 + \tilde{\alpha}_t^m \left(1 - y_0^{\gamma_t^m} \right) + \tilde{\beta}_t^m y_1^{\eta_t^m} \right)$$

$$= C_t^m + \alpha_t^m \left(1 - y_0^{\gamma_t^m} \right) + \beta_t^m y_1^{\eta_t^m},$$

$$y_0 = \left(\frac{\rho_0}{\rho_c} \right), \quad y_1 = \left(\frac{\rho_1}{\rho_c} \right)^2.$$

$$m = \{ \rho\rho, \rho\tau, J^2, \rho\Delta\rho, \nabla\rho\nabla\rho, \rho\nabla J, J\nabla\rho \}$$

A set of 66 independent parameters
38 coupling constants $\{C, \alpha, \beta\}$, and 28 powers $\{\gamma, \eta\}$

$$\{C_t^{\rho\rho}, C_t^{\rho\Delta\rho}, C_t^{\rho\tau}, C_t^{J^2}, C_t^{\rho\nabla J}\}$$

$$\{\alpha_t^m, \beta_t^m, \gamma_t^m, \eta_t^m\}.$$

Microscopically Based Nuclear Energy Functionals

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Abstract. A major goal of the SciDAC project “Building a Universal Nuclear Energy Density Functional” is to develop next-generation nuclear energy density functionals that give controlled extrapolations away from stability with improved performance across the mass table. One strategy is to identify missing physics in phenomenological Skyrme functionals based on our understanding of the underlying internucleon interactions and microscopic many-body theory. In this contribution, I describe ongoing efforts to use the density matrix expansion of Negele and Vautherin to incorporate missing finite-range effects from the underlying two- and three-nucleon interactions into phenomenological Skyrme functionals.

DENSITY MATRIX EXPANSION

The dominant many-body perturbation theory (MBPT) contributions to bulk nuclear properties like ground state energies take the generic form

$$\langle V \rangle = \frac{1}{2} \sum_{\{\sigma\tau\}} \int d\mathbf{r}_1 \cdots \int d\mathbf{r}_4 \langle \mathbf{r}_1 \sigma_1 \tau_1 \mathbf{r}_2 \sigma_2 \tau_2 | \hat{\mathcal{V}} | \mathbf{r}_3 \sigma_3 \tau_3 \mathbf{r}_4 \sigma_4 \tau_4 \rangle \\ \times \rho(\mathbf{r}_3 \sigma_3 \tau_3, \mathbf{r}_1 \sigma_1 \tau_1) \rho(\mathbf{r}_4 \sigma_4 \tau_4, \mathbf{r}_2 \sigma_2 \tau_2)$$

but any truncation will give results depending on the particular choice for k_F . The standard LDA choice of Negele and Vautherin corresponds to:

$$k_F(\mathbf{R}) = (3\pi^2 \rho(\mathbf{R})/2)^{1/3}, \quad (10)$$

though alternative choices such as the one introduced by Campi and Bouyssy [33]

$$k_F(\mathbf{R}) = \sqrt{\frac{5}{3} \frac{\tau(\mathbf{R}) - \frac{1}{4} \nabla^2 \rho(\mathbf{R})}{\rho(\mathbf{R})}}, \quad (11)$$

may be useful to optimize the convergence of truncated expansions of Eq. (9), and to introduce novel τ and $\nabla^2 \rho$ dependencies analogous to those found in Coulomb Meta-GGA functionals [19]. Truncating Eq. (9) to terms with $n \leq 1$ yields the fundamental equation of the DME,

$$\hat{\rho}(\mathbf{R} + \frac{\mathbf{r}}{2}, \mathbf{R} - \frac{\mathbf{r}}{2}) \approx \rho_{\text{SL}}(k_F(\mathbf{R})r) \rho(\mathbf{R}) \\ + r^2 g(k_F(\mathbf{R})r) \left[\frac{1}{4} \nabla^2 \rho(\mathbf{R}) - \tau(\mathbf{R}) + \frac{3}{5} k_F(\mathbf{R})^2 \rho(\mathbf{R}) \right], \quad (12)$$

where

$$\rho_{\text{SL}}(x) \equiv 3j_1(x)/x, \quad g(x) \equiv 35j_3(x)/2x^3, \quad (13)$$

To illustrate some of the non-trivial density dependencies that arise from finite-range effects, we give a sampling of results that are obtained by applying the DME to the Hartree-Fock contributions of the long-range parts of the chiral EFT NN interaction thru N²LO [34]. Thru this order, the finite-range interactions can be decomposed as

$$V_{NN} = V_C + \tau_1 \cdot \tau_2 W_C + [V_S + \tau_1 \cdot \tau_2 W_S] \vec{\sigma}_1 \cdot \vec{\sigma}_2 + [V_T + \tau_1 \cdot \tau_2 W_T] \vec{\sigma}_1 \cdot \vec{q} \vec{\sigma}_2 \cdot \vec{q} + i [V_{LS} + \tau_1 \cdot \tau_2 W_{LS}] (\vec{\sigma}_1 + \vec{\sigma}_2) \cdot (\vec{q} \times \vec{k}), \quad (15)$$

Skyrme-like EDF's from the DME

$$\mathcal{E} = \frac{\tau}{2M} + \frac{3}{8}t_0\rho^2 + \frac{1}{16}t_3\rho^{2+\alpha} + \frac{1}{16}(3t_1 + 5t_2)\rho\tau + \frac{1}{64}(9t_1 - 5t_2)|\nabla\rho|^2 + \dots \quad \text{Skyrme}$$

$$\mathcal{E} = \frac{\tau}{2M} + A[\rho] + B[\rho]\tau + C[\rho]|\nabla\rho|^2 + \dots \quad \text{DME}$$

- coupling *constants* --> coupling *functions*
 - finite range effects encoded as ρ -dependence in **ABC**
 - microscopic isovector, spin-orbit terms
 - well-suited for existing SkyHF codes

Novel density-dependencies in EDF from 1π and 2π exchanges:

$$\rho^{7/3}, \rho^{4/3}, \rho^{2/3}, \frac{1}{\rho^{2/3}} \log(1 + c\rho^{2/3}), \dots$$

TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

DME FUNCTIONAL

$$\mathbf{U} \longrightarrow G_t^{\rho\rho} = C_t^{\rho\rho} + G g_t^{\rho\rho}(\rho_0),$$

$$G_t^{\rho\tau} = C_t^{\rho\tau} + G g_t^{\rho\tau}(\rho_0),$$

$$G_t^{J^2} = C_t^{J^2} + G g_t^{J^2}(\rho_0),$$

$$G_t^{\rho\Delta\rho} = C_t^{\rho\Delta\rho} + G g_t^{\rho\Delta\rho}(\rho_0),$$

$$G_t^{\nabla\rho\nabla\rho} = C_t^{\nabla\rho\nabla\rho} + G g_t^{\nabla\rho\nabla\rho}(\rho_0),$$

$$G_t^{\rho\nabla J} = C_t^{\rho\nabla J} + G g_t^{\rho\nabla J}(\rho_0),$$

$$G_t^{J\nabla\rho} = C_t^{J\nabla\rho} + G g_t^{J\nabla\rho}(\rho_0).$$

$$g_t^m(\rho_0) = \frac{1}{2} (A^m(\rho_0) + (-1)^t B^m(\rho_0)),$$

$$m = \{\rho\rho, \rho\tau, J^2, \rho\Delta\rho, \nabla\rho\nabla\rho, \rho\nabla J, J\nabla\rho\}$$

$$A^{\rho\rho} = \frac{1}{256 u^6} \{12u (35 + 4u^2) \tan^{-1}(2u)$$

$$- \frac{3}{4u^2} (7 + 16u^2 (8 - 9u^2)) \log(4u^2 + 1)$$

$$+ (21 - 498u^2 - 64u^4 + 16u^6)\},$$

$$A^{\rho\Delta\rho} = \frac{35}{3072 m_\pi^2 u^8} \{3 - 72u^2 - 4u^4$$

$$- \frac{1}{4u^2} (3 + 54u^2 - 72u^4) \log(1 + 4u^2)$$

$$+ 60 \tan^{-1}(2u)u\}, \quad B^{\rho\Delta\rho} = 2A^{\rho\Delta\rho},$$

$$A^{J^2} = \frac{1}{48 m_\pi^2} \left(\frac{5 + 12u^2}{(1 + 4u^2)^2} + \frac{\log(4u^2 + 1)}{4u^2} \right),$$

$$A^{\rho\tau} = -4A^{\rho\Delta\rho}, \quad B^{\rho\tau} = 2A^{\rho\Delta\rho}, \quad B^{J^2} = 2A^{J^2},$$

$$A^{\rho\nabla J} = B^{\rho\nabla J} = 0, \quad A^{J\nabla\rho} = B^{J\nabla\rho} = 0,$$

$$u = k_F/m_\pi \quad G = g_A^2/f_\pi^2$$

$$\{C_{t0}^{\rho\rho}, C_{tD}^{\rho\rho}, C_t^{\rho\Delta\rho}, C_t^{\rho\tau}, C_t^{J^2}, C_t^{\rho\nabla J}, \gamma, G\},$$

TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

Density Dependent Coupling Constants

$$W(\rho, I) = W(\rho) + S_2(\rho)I^2 + S_4(\rho)I^4,$$

$$W(\rho) = \frac{E^{NM}}{A} + \frac{P^{NM}}{\rho_c^2} (\rho - \rho_c) + \frac{K^{NM}}{18\rho_c^2} (\rho - \rho_c)^2$$

$$S_2(\rho) = a_{sym}^{NM} + \frac{L^{NM}}{3\rho_c} (\rho - \rho_c) + \frac{\Delta K^{NM}}{18\rho_c^2} (\rho - \rho_c)$$

SLY4

$$\frac{E^{NM}}{A} = -15.972 \text{ MeV}, \quad a_{sym}^{NM} = 32.0 \text{ MeV},$$

$$\rho_c = 0.15954 \text{ fm}^{-3}, \quad L^{NM} = 45.962 \text{ MeV},$$

$$K^{NM} = 229.9 \text{ MeV}, \quad \Delta K^{NM} = -119.696 \text{ MeV},$$

$$M_s^{*NM} = 1.4396, \quad M_v^{*NM} = 1.24984.$$

$$G = \frac{K^{NM} + 9(\gamma+1) \frac{E^{NM}}{A} + \frac{\hbar^2}{2m} (3(1-3\gamma)\tau_c - 2(2-3\gamma)M_s^{*NM})}{\tilde{k}_F^c \rho_c \left((1-3\gamma)g_0^{\rho\rho'} + \tilde{k}_F^c g_0^{\rho\rho''} + \left((5-3\gamma)g_0^{\rho\tau'} + \tilde{k}_F^c g_0^{\rho\tau''} \right) \tau_c \right)}$$

$$C_{00}^{\rho\rho} = \frac{\frac{\hbar^2}{2m} ((2-3\gamma)M_s^{*NM} - 3)\tau_c + 3(1+\gamma) \frac{E^{NM}}{A}}{3\gamma\rho_c}$$

$$+ G \frac{-3g_0^{\rho\rho} + \tilde{k}_F^c (g_0^{\rho\rho'} + \tau_c g_0^{\rho\tau'})}{3\gamma},$$

$$C_{0D}^{\rho\rho} = \frac{\frac{\hbar^2}{2m} (3 - 2M_s^{*NM}) \tau_c - 3 \frac{E^{NM}}{A}}{3\gamma\rho_c^{1+\gamma}}$$

$$- G \frac{\tilde{k}_F^c (g_0^{\rho\rho'} + \tau_c g_0^{\rho\tau'})}{3\gamma\rho_c^\gamma},$$

$$C_1^{\rho\tau} = C_0^\tau - \frac{\hbar^2}{2m} (M_v^{*NM} - 1) \frac{1}{\rho_c}$$

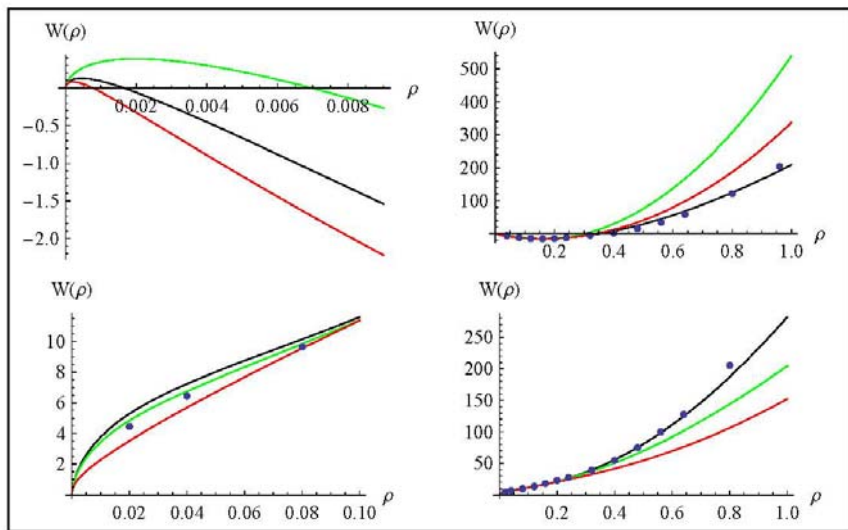
$$+ G (g_0^{\rho\tau} - g_1^{\rho\tau}),$$

$$C_{10}^{\rho\rho} = \frac{1}{27\gamma\rho_c} \left[27(1+\gamma) a_{sym}^{NM} C - 9L^{NM} \right]$$

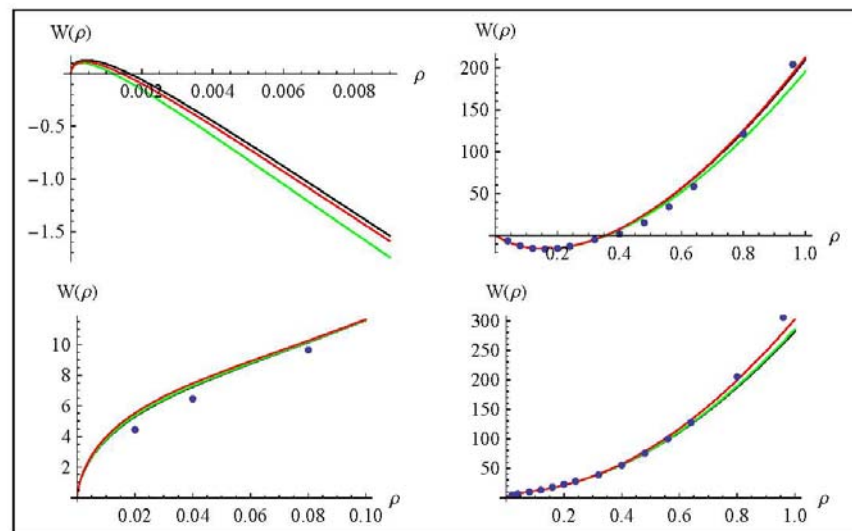
$$- 5 \left((1+3\gamma) \frac{\hbar^2}{2m} - (2-3\gamma) (C_0^\tau + 3C_1^\tau) \rho_c \right) \tau_c \Big]$$

$$- G \frac{27\gamma g_1^{\rho\rho} + (60\gamma - 40) g_0^{\rho\tau} \tau_c}{27\gamma}$$

$\gamma=1, G=9454.9$



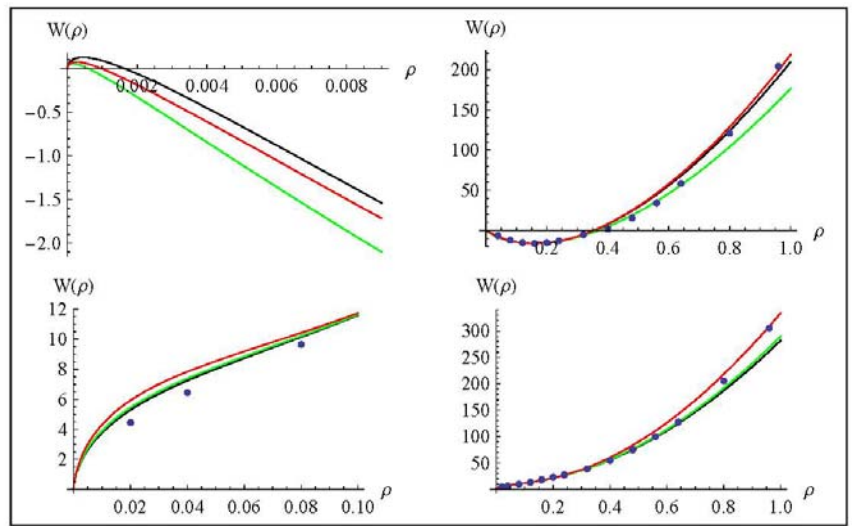
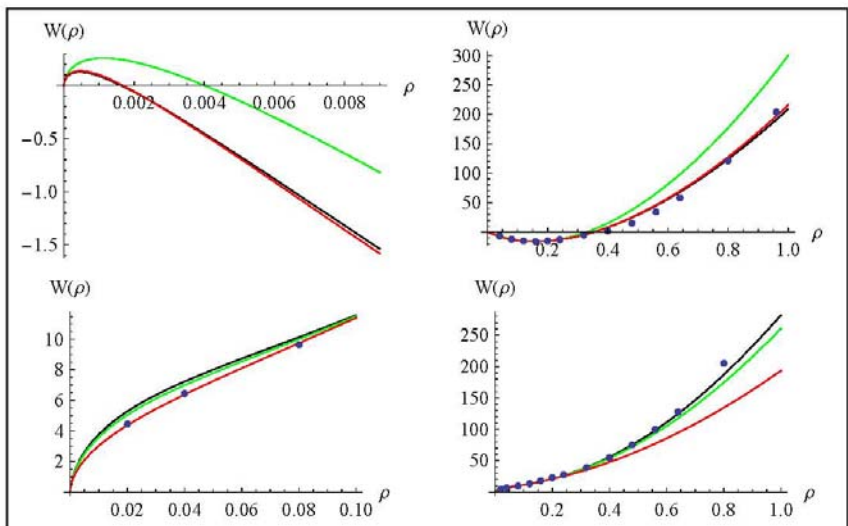
$\gamma=0.1, G=-703.79$



$\gamma=0.5, G=3631.$

$G_{DME}=1496.98$

$\gamma=0.000, G=-1744.9$



Odd-even mass differences from self-consistent mean field theory

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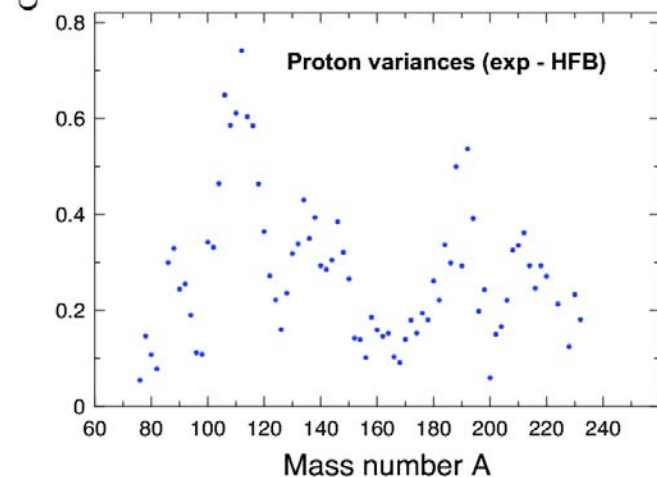
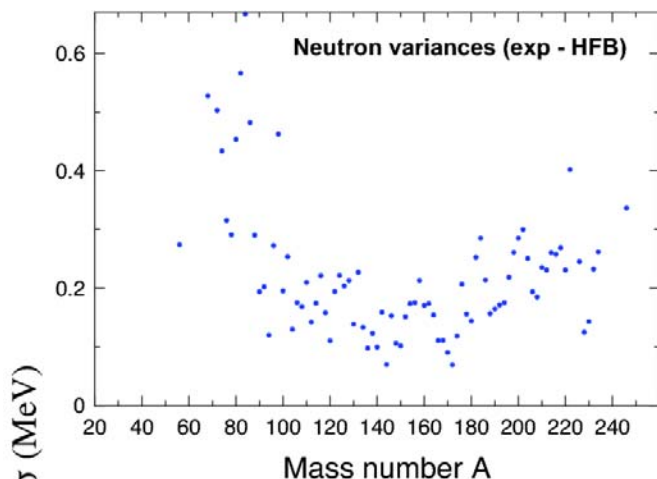
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As expected, best agreement for well deformed rare earths and actinides whose properties vary smoothly with particle number

Largest deviations around shell closures and in the regions of shape coexistence ($A=90$ for neutrons and $A=110$ and 190 for protons) where dynamic shape fluctuations are known to strongly impact masses

- There is a weak preference for a surface-peaked n-n pairing, which might be attributable to many-body effects
- A larger strength is required in the proton pairing channel than in the neutron pairing channel
- Pairing strengths adjusted to the isotope chains are too weak to give a good overall fit to the mass differences
- The results supports the recent attempts to directly parametrize the pairing functional in terms of isovector densities

TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

Isvector Density Dependent Contact Pairing Force

$$v_{pair}(1, 2) = \frac{1 - P_\sigma}{2} V_0 g_{\tau_3}[\rho, \rho_1] \delta(\mathbf{r}_1 - \mathbf{r}_2).$$

$$\rho_1(r) = (\rho_n - \rho_p), \quad \rho(r) = (\rho_n + \rho_p)$$

Hiroyuki Sagawa (SLYS)

$$g_n[\rho, \rho_1] = 1 - (1 - \beta)\eta_s \left(\frac{\rho}{\rho_0}\right)^{\alpha_s} - \beta\eta_n \left(\frac{\rho}{\rho_0}\right)^{\alpha_n}$$

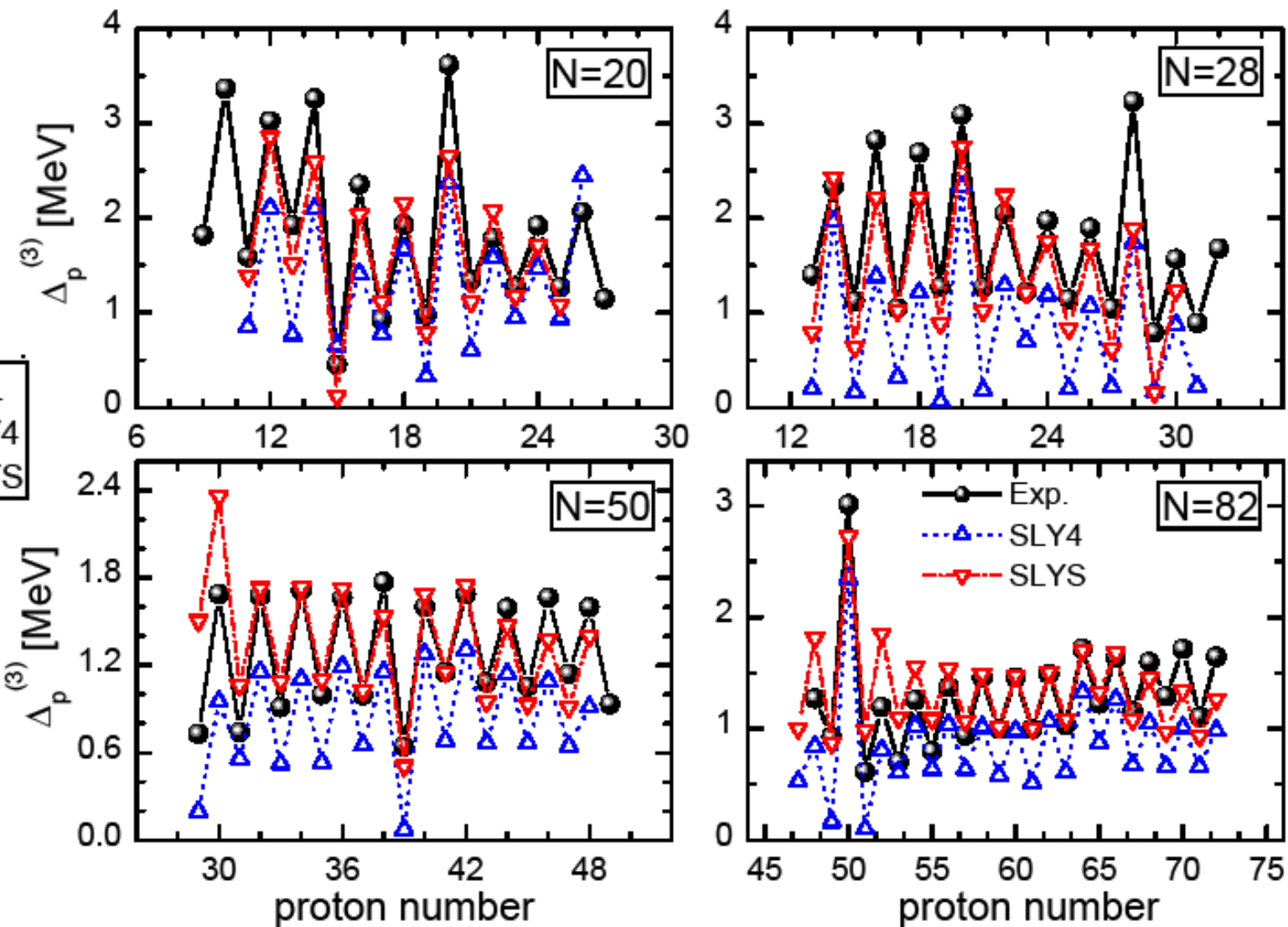
$$g_p[\rho, \rho_1] = 1 - (1 + \beta)\eta_s \left(\frac{\rho}{\rho_0}\right)^{\alpha_s} + \beta\eta_n \left(\frac{\rho}{\rho_0}\right)^{\alpha_n}$$

$$\beta(r) = \rho_1(r)/\rho(r), \quad \eta_s = 0.664, \quad \alpha_s = 0.522, \quad \eta_n = 1.01, \quad \alpha_n = 0.525, \quad \rho_0 = 0.16 \text{ fm}^{-3}$$

Masayuki Yamagami (SLYY)

$$g_{\tau_3}[\rho, \rho_1] = 1 - \frac{1}{2} \left(\frac{\rho}{\rho_0}\right) - \frac{\tau_3}{4} \left(\frac{\rho_1}{\rho_0}\right) - \frac{5}{2} \left(\frac{\rho_1}{\rho_0}\right)^2$$

Isovector Density Dependent Contact Pairing Force (preliminary results)



TOWARDS A UNIVERSAL NUCLEAR ENERGY DENSITY FUNCTIONAL

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1. Mass Table Calculations
2. Optimal parameters of the functional
3. Improving the functional
4. Visualization and development tools

Visualization and Development Tools

Mass Table Explorer

<http://massexplorer.org>

Off-Line Version

- Written in Java
- Can work on any computer
- Large sets of visualization tools
- One can compare with his own data
- Saves data and images in many formats

On-Line Version

- Uses Python, Gnuplot, PHP, Ajax
- Visualization right from the browser
 - mass filters
 - 2D and 3D charts
 - plot nuclear characteristics
 - rms errors with exp. data

Subversion Control System (SVN)

<http://massexplorer.org/websvn/>

- <http://massexplorer.org/svn/FitDME>
- <http://massexplorer.org/svn/HFBTHO>
- <http://massexplorer.org/svn/HFODD>
- http://massexplorer.org/svn/MPI_HFODD

News

Recent MTEx 4.1beta release can be downloaded [here](#)

Additional data files available for Mass Tables calculated with different functionals can be downloaded [here](#)

Screenshots from MTEx can be seen [here](#)

Journal iFrames

- [Nature](#)
- [Phys.Rev.Let.](#)
- [Phys.Rev. C](#)
- [arXiv.org](#)

[Periodic Table](#)

Mass Table explorer

... science scales with processors ...

Mass Table Explorer is a java application aimed to facilitate the visualization of the huge array of data coming from modern multiprocessors computers helping to understand challenging phenomena seen across the nuclear mass chart.

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Mass Tables

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- [Map of the Nuclides](#)
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Java Tools

- [Janis](#)
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✓ 1. Mass Table Calculations

2. Optimal parameters of the functional
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