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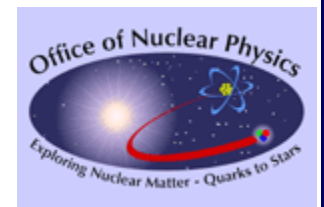
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## Can EFT help $p+A$ scattering

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5/19/2009

Supported by: U.S. DOE, OSC



# Observables in p+A elastic scattering

- p == proton or neutron
- A == spin-zero nucleus (closed shell)
- Independent vectors:  $\vec{k}, \vec{k}', \vec{k} \times \vec{k}'$  or  $\vec{k} \pm \vec{k}, \vec{k} \times \vec{k}'$
- Elastic scattering:  $|\vec{k}| = |\vec{k}'|$
- Most general form of scattering amplitude
- spin-1/2  $\rightarrow$  spin-0:  
$$A \cdot 1 + \vec{\sigma} \cdot \vec{C}$$
- Assuming rotational invariance and parity conservation

$$\begin{aligned} M &= A \cdot 1 + C \vec{\sigma} \cdot (\hat{\mathbf{k}} \times \hat{\mathbf{k}}') \\ &= A(\mathbf{k}, \theta) + \underline{C(\mathbf{k}, \theta)} \vec{\sigma} \cdot \hat{\mathbf{N}} \end{aligned}$$

Spin-flip amplitude

## Explicitly:

- $k$  and  $k'$  span scattering plane (x-z - plane)
- y-plane  $\vec{\sigma} \cdot \hat{N} = \sigma_y$
- With standard Pauli spinors:

$$\frac{d\sigma}{d\Omega}(\theta, +\hat{y} \rightarrow +\hat{y}) = |\chi_{+y}(A + C\sigma_y)\chi_{+y}| = |A + C|^2$$

$$\frac{d\sigma}{d\Omega}(\theta, +\hat{y} \rightarrow -\hat{y}) = 0$$

- **Unpolarized cross section:**
  - Average of initial states and sum of all final states

$$\begin{aligned} \frac{d\sigma}{d\Omega}(\theta) &= \frac{1}{2} \left[ \frac{d\sigma}{d\Omega}(\theta, i \rightarrow +\hat{y}) + \frac{d\sigma}{d\Omega}(\theta, i \rightarrow -\hat{y}) \right] \\ &= |A(\theta)|^2 + |C(\theta)|^2 \end{aligned}$$

# Analyzing Power $A_y$

- Spin of the outgoing projectile is measured
- Incident beam is unpolarized

$$A_y = \frac{\frac{d\sigma}{d\Omega}(\theta, i \rightarrow +\hat{y}) - \frac{d\sigma}{d\Omega}(\theta, i \rightarrow -\hat{y})}{\frac{d\sigma}{d\Omega}(\theta, i \rightarrow +\hat{y}) + \frac{d\sigma}{d\Omega}(\theta, i \rightarrow -\hat{y})} = \frac{2 \Re(A^*(\theta)C(\theta))}{|A(\theta)|^2 + |C(\theta)|^2}$$

**$\Rightarrow$  Spin dependence out of the scattering plane**

# Spin rotation parameter Q

- Measures the rotation of the spin vector in the scattering plane
- $+x \rightarrow \pm z$

$$Q = \frac{\frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow +\hat{z}) - \frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow -\hat{z})}{\frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow +\hat{z}) + \frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow -\hat{z})} = \frac{2 \Im(A(\theta)C^*(\theta))}{|A(\theta)|^2 + |C(\theta)|^2}$$

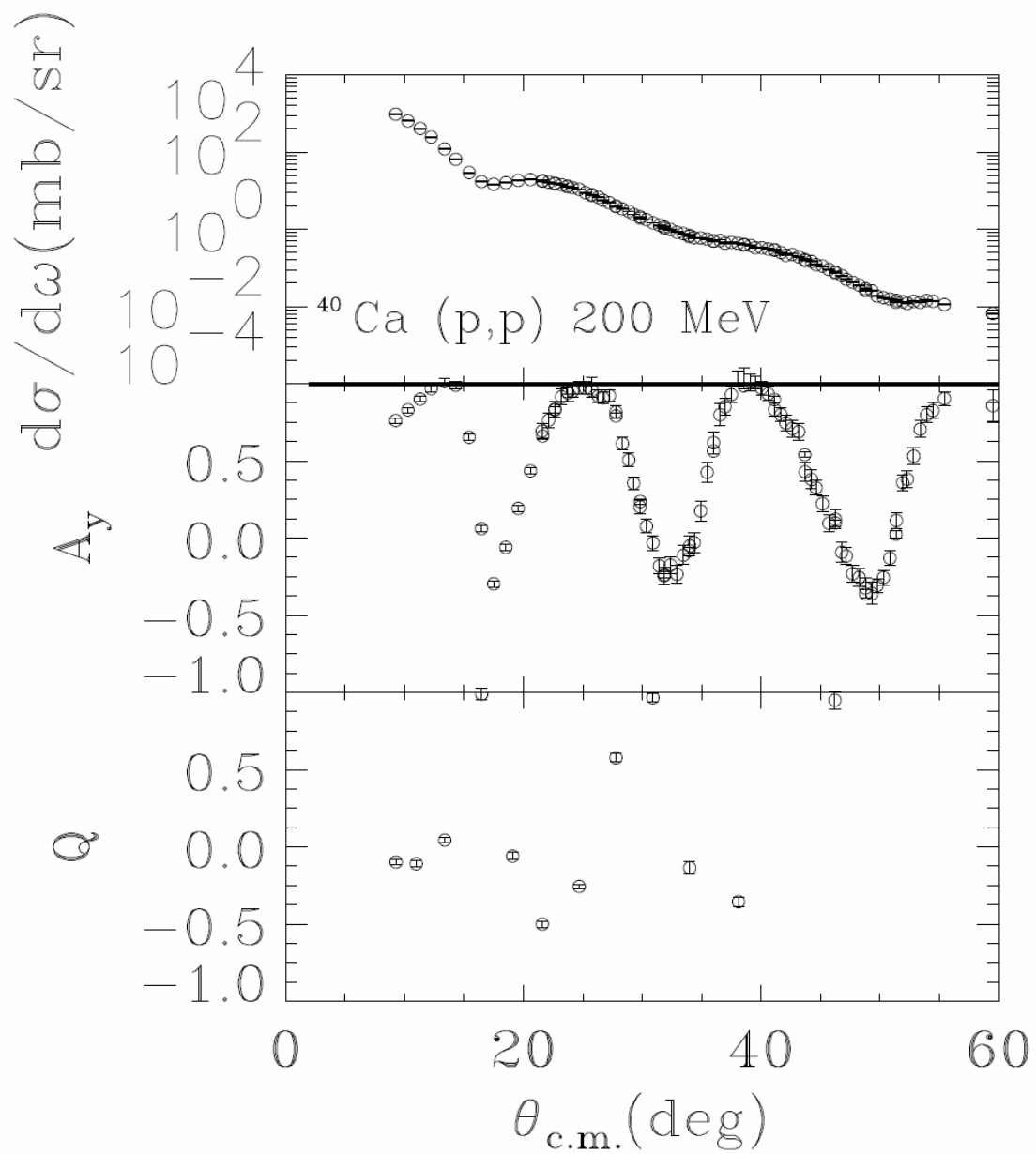
$\Rightarrow$  Spin dependence within the scattering plane

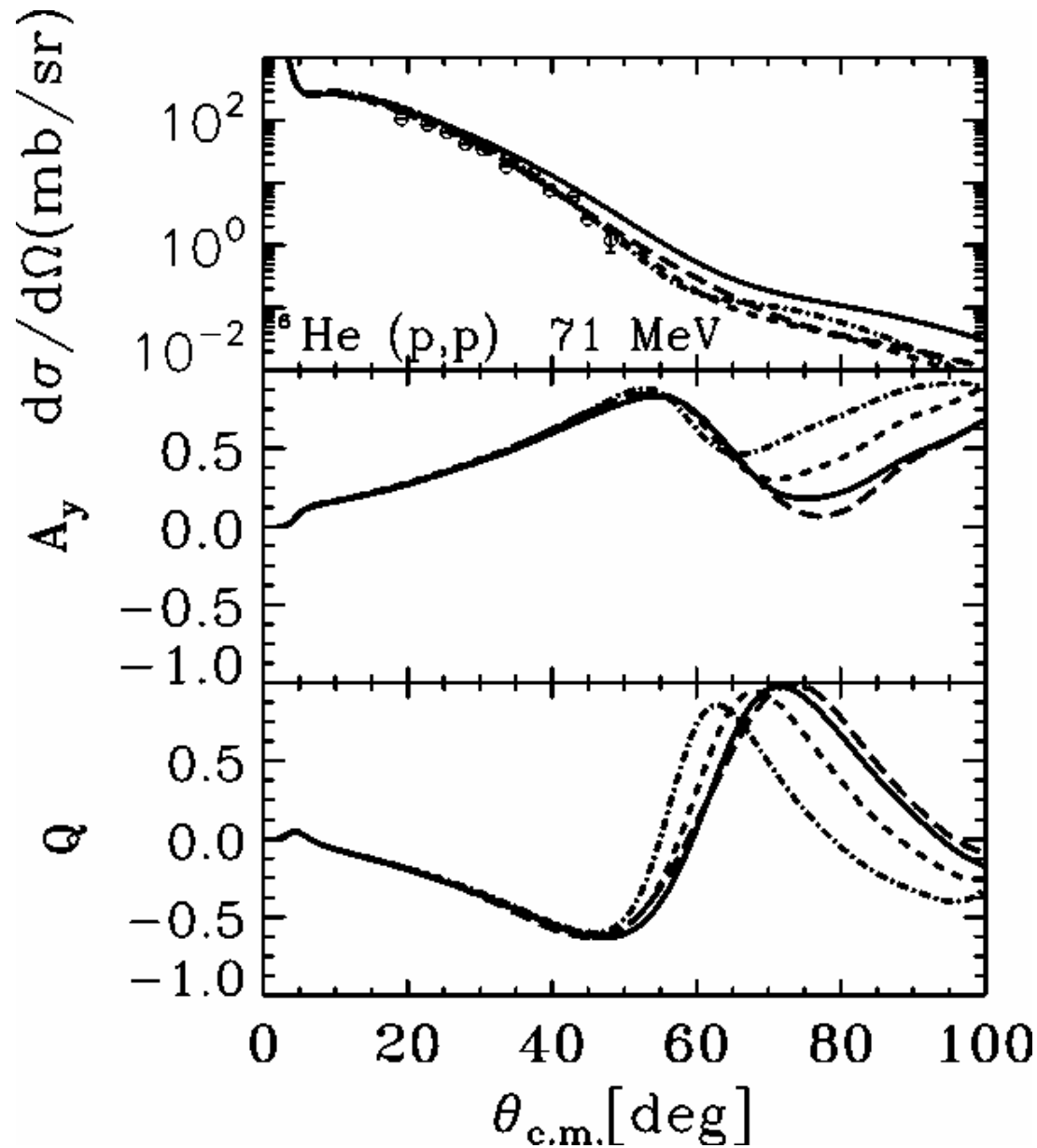
# Spin rotation parameter Q

- Measures the rotation of the spin vector in the scattering plane
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$$Q = \frac{\frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow +\hat{z}) - \frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow -\hat{z})}{\frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow +\hat{z}) + \frac{d\sigma}{d\Omega}(\theta, \hat{x} \rightarrow -\hat{z})} = \frac{2 \Im(A(\theta)C^*(\theta))}{|A(\theta)|^2 + |C(\theta)|^2}$$

$\Rightarrow$  Spin dependence within the scattering plane





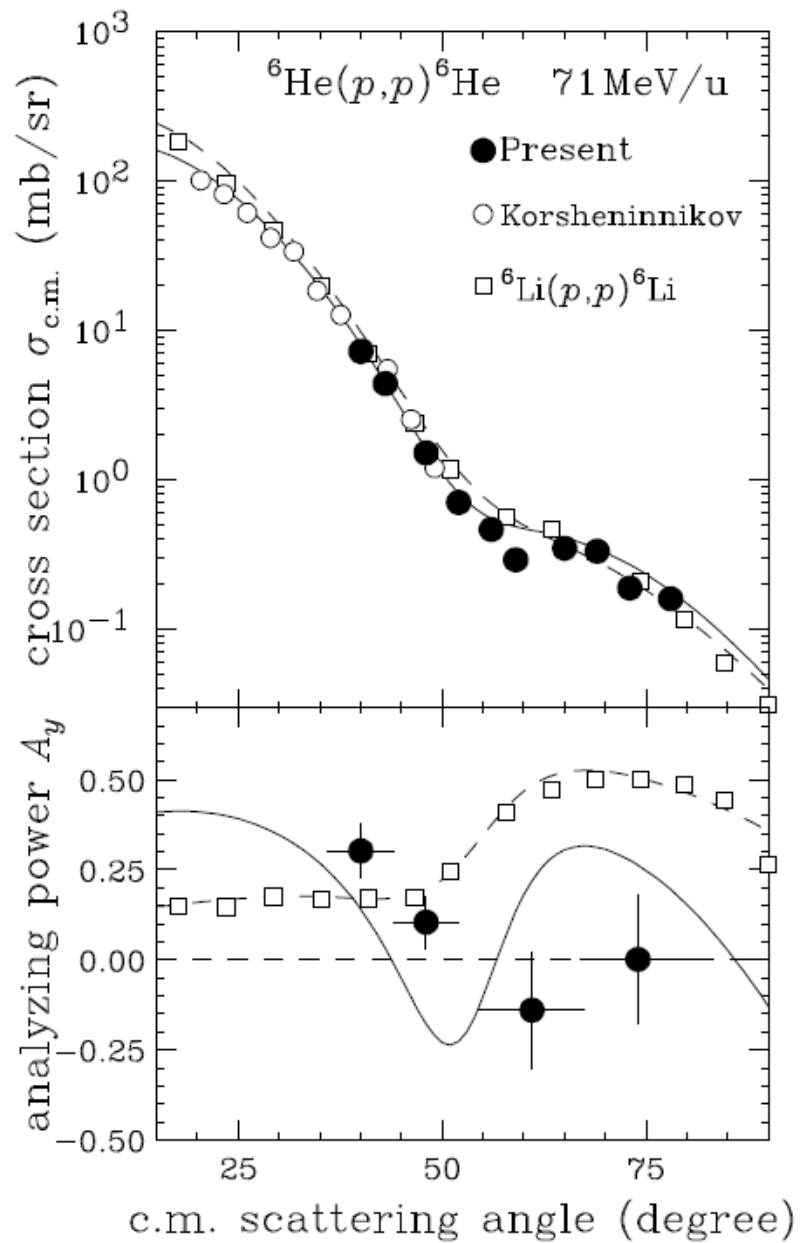
${}^6\text{He} + p$

S.P. Weppner, O.  
Garcia, Ch. Elster

PRC 61, 044601(2000)

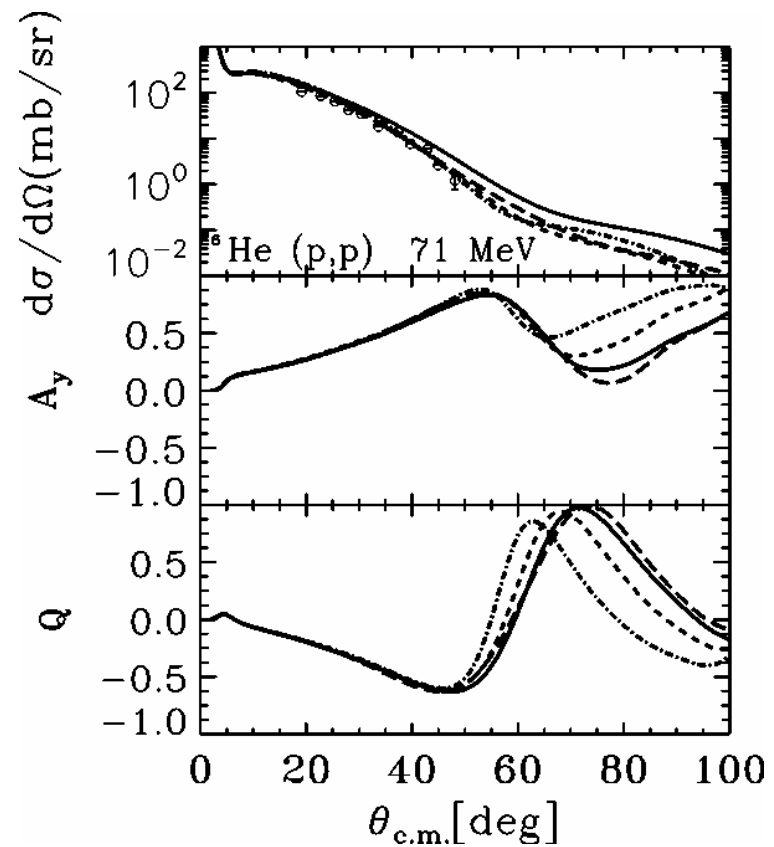
Simple densities,  
adjusted such that  
radius of  ${}^6\text{He}$  is  
captured

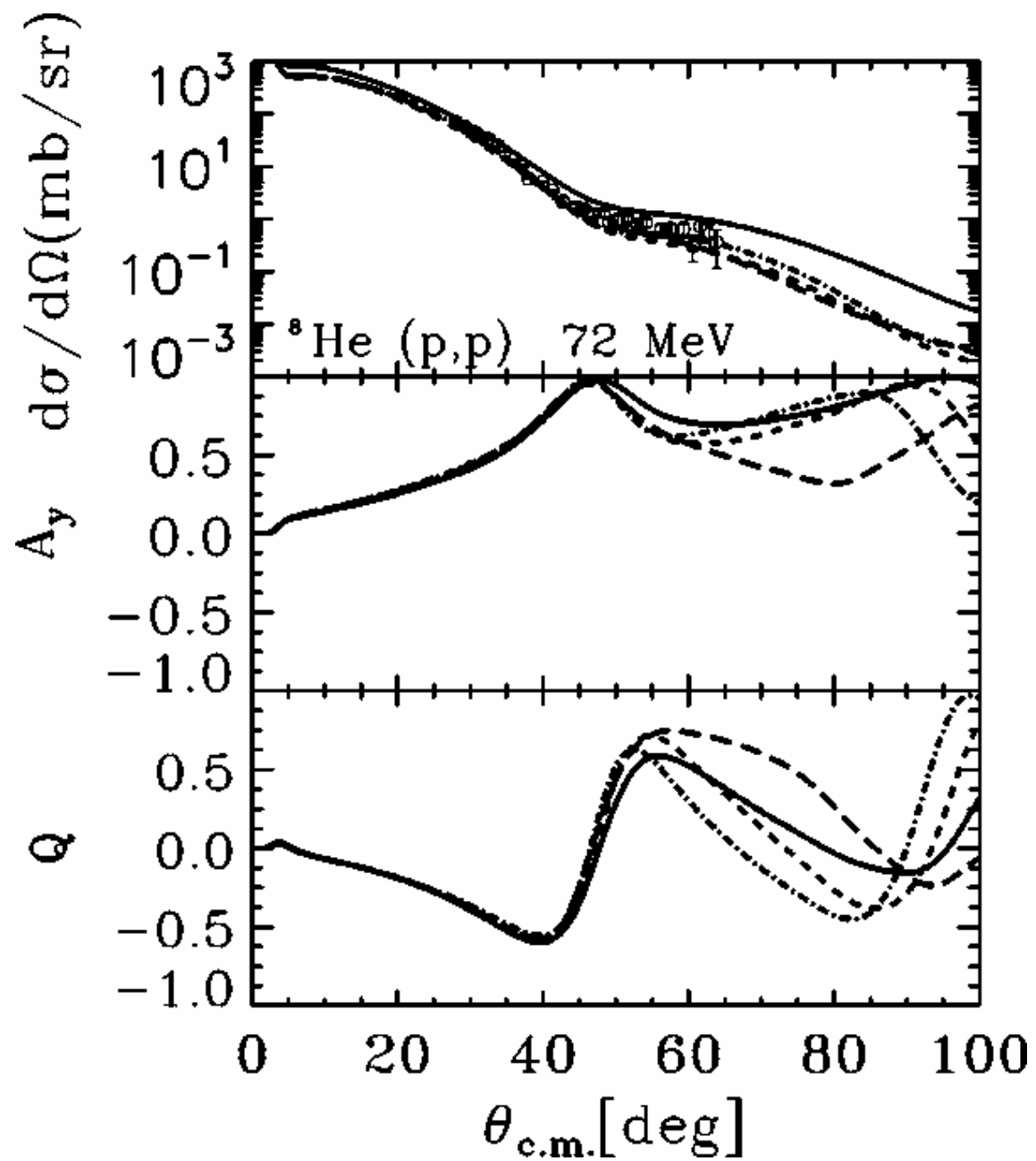




## Measurement:

M. Satano, H. Sakai et al.  
 Eur. Phys. J A25 255 (2005)





# Scattering: Lippmann-Schwinger Equation

- LSE:  $T = V + V G_0 T$
- Hamiltonian:  $H = H_0 + V$
- Free Hamiltonian:  $H_0 = h_0 + H_A$ 
  - $h_0$ : kinetic energy of projectile '0'
  - $H_A$ : target hamiltonian with  $H_A |\Phi\rangle = E_A |\Phi\rangle$
- $V$ : interactions between projectile '0' and target nucleons 'i'  $V = \sum_{i=0}^A v_{0i}$
- Propagator is  $(A+1)$  body operator
  - $G_0(E) = (E - h_0 - H_A + i\varepsilon)^{-1}$

## Standard Ansatz:

- $T = \sum_{i=0}^A T_{0i}$   
– with  $T_{0i} = v_{0i} + v_{0i} G_0(E) T$

$$T_{0i} = v_{0i} + v_{0i} G_0(E) \sum_j T_{0j}$$

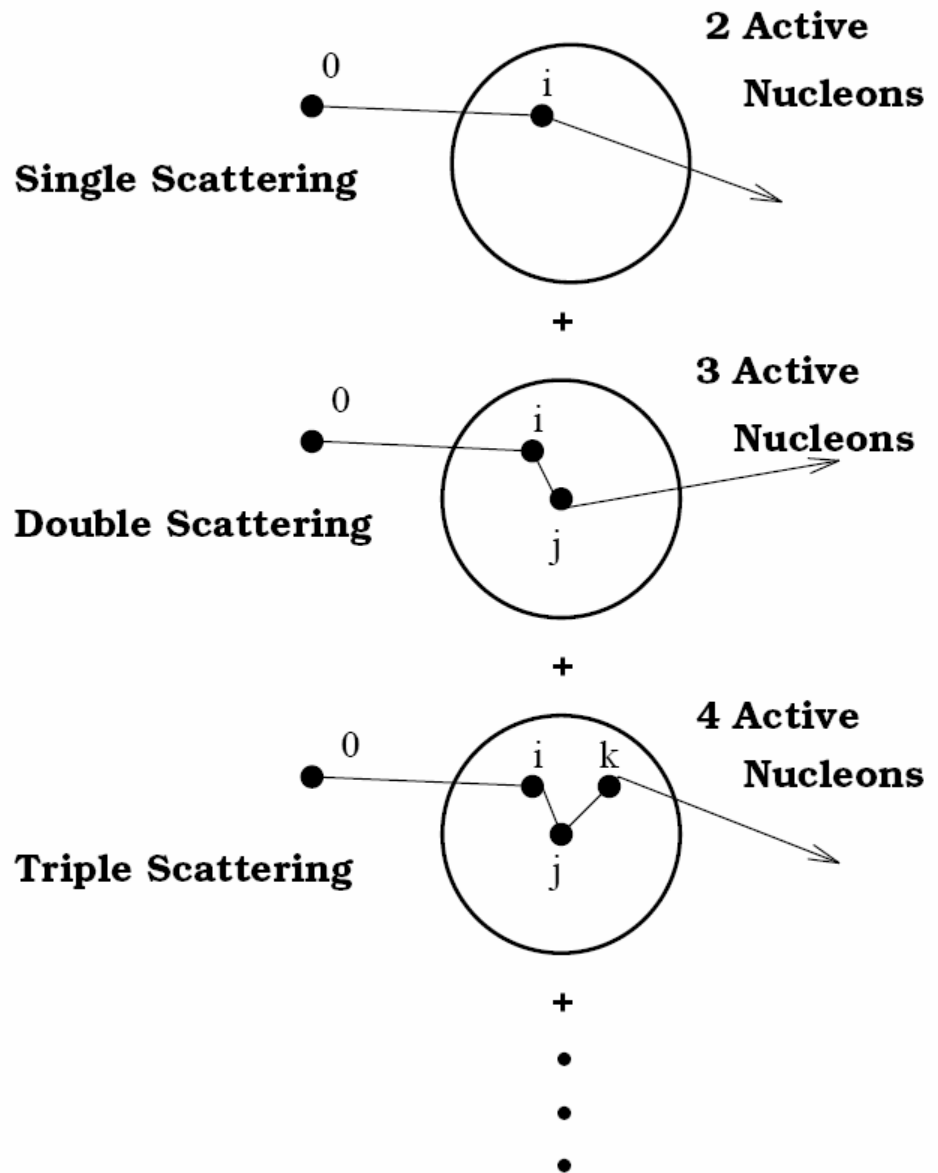
$$= v_{0i} + v_{0i} G_0(E) T_{0i} + v_{0i} G_0(E) \sum_{j \neq i} T_{0j}$$

$$(1 - v_{0i} G_0(E)) T_{0i} = v_{0i} + v_{0i} G_0(E) \sum_{j \neq i} T_{0j}$$

$$T_{0i} = t_{0i} + t_{0i} G_0(E) \sum_{j \neq i} T_{0j}.$$

with  $t_{0i} = v_{0i} + v_{0i} G_0(E) t_{0i}$

# Spectator Expansion:



Written down by

Siciliano, Thaler (1977)

Picklesimer, Thaler (1981)

# Spectator Expansion in eqs.

$$T = \sum_{i=1}^A t_{0i} + \sum_{i<j} (t_{ij} - t_{0i} - t_{0j}) \leftarrow \text{Scattering from pairs}$$
$$+ \sum_{i<j<k} (t_{ijk} - t_{ij} - t_{ik} - t_{jk} + t_{0i} + t_{0j} + t_{0k}) + \dots$$

2<sup>nd</sup> order term:  $t_{ij} = (v_{0i} + v_{0j}) + (v_{0i} + v_{0j})G_0(E)t_{ij},$

**Single scattering approximation:**

$$T = \sum_{i=1}^A T_{0i} \approx \sum_{i=1}^A t_{0i}.$$

Pauli Principle:

Antisymmetrize in active pairs

# Elastic Scattering

- In- and Out-States have the target in ground state  $\Phi_0$
- Projector on ground state  $P = |\Phi_0\rangle\langle\Phi_0|$ 
  - With  $1=P+Q$  and  $[P,G_0]=0$
- For elastic scattering one needs
- $P T P = P U P + P U P G_0(E) P T P$
- Or

$$- \quad \mathbf{T} = \mathbf{U} + \mathbf{U} \mathbf{G}_0(\mathbf{E}) \mathbf{P} \mathbf{T}$$

$$- \quad \mathbf{U} = \mathbf{V} + \mathbf{V} \mathbf{G}_0(\mathbf{E}) \mathbf{Q} \mathbf{U} \quad \Leftarrow \text{optical potential}$$

Standard:  $\mathbf{U}^{(1)} \approx \sum_{i=0}^A \tau_{0i}$  (1<sup>st</sup> order)

with

$$\tau_{0i} = \mathbf{v}_{0i} + \mathbf{v}_{0i} \mathbf{G}_0(\mathbf{E}) \mathbf{Q} \tau_{0i}$$

$$\tau_{0i} = v_{0i} + v_{0i} \mathbf{G}_0(\mathbf{E}) \mathbf{Q} \tau_{0i}$$

- $\mathbf{G}_0(\mathbf{E}) = (\mathbf{E} - h_0 - H_A + i\varepsilon)^{-1} == (A+1)$  body operator
  - Standard “**impulse approximation**”:
  - Average over  $H_A \Rightarrow$  c-number
  - $\rightarrow \mathbf{G}_0(\mathbf{e}) ==$ : two body operator
- Deal with  $\mathbf{Q}$ 
  - Define “two-body” operator  $\mathbf{t}_{0i}^{\text{free}}$  by
  - $\mathbf{t}_{0i}^{\text{free}} = v_{0i} + v_{0i} \mathbf{G}_0(\mathbf{e}) \mathbf{t}_{0i}^{\text{free}}$
  - and relate via integral equation to  $\tau_{0i}$
  - $\tau_{0i} = \mathbf{t}_{0i}^{\text{free}} - \mathbf{t}_{0i}^{\text{free}} \mathbf{G}_0(\mathbf{e}) \tau_{0i}$  [integral equation]
  - Important for keeping correct iso-spin character of optical potential
  - $\mathbf{U}^{(1)} = \sum_{i=1}^A \tau_{0i} =: \mathbf{N} \tau_n + \mathbf{Z} \tau_p$



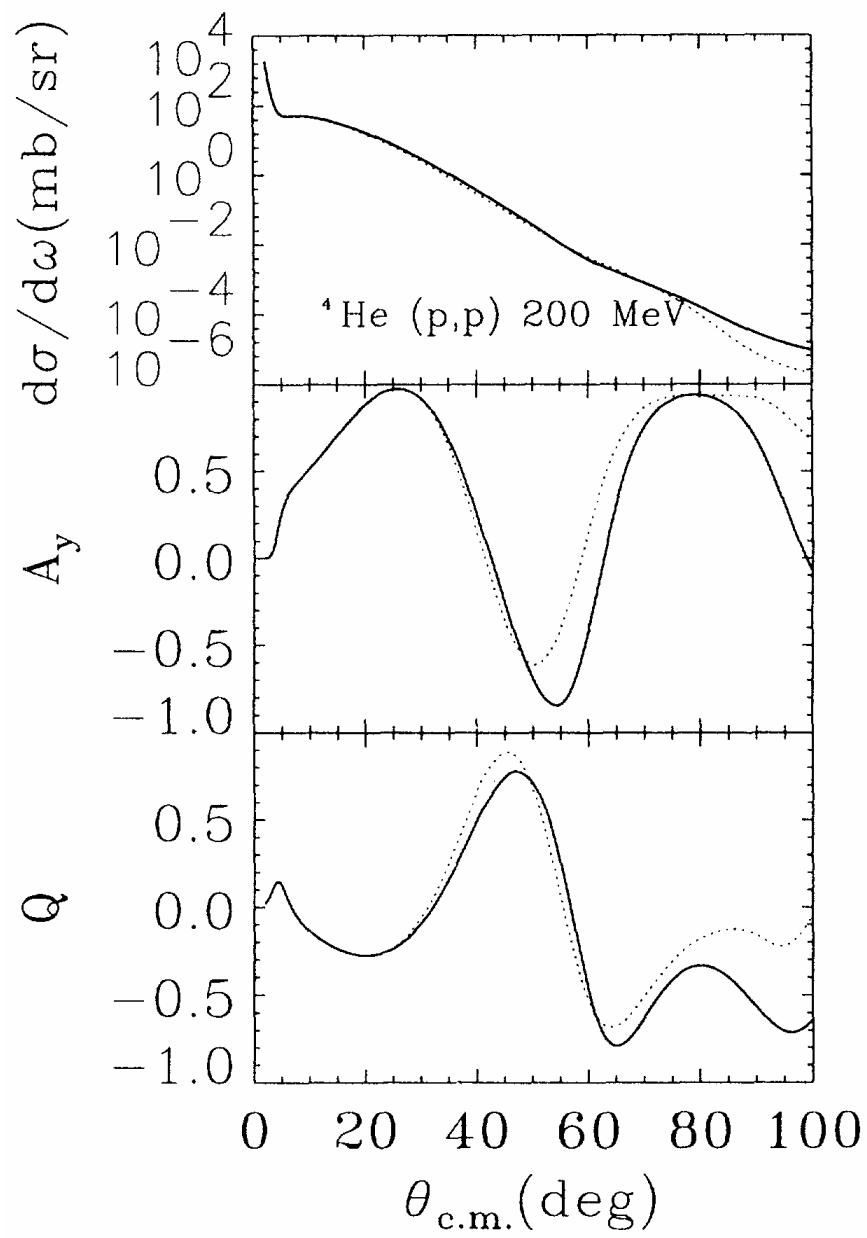
## First order Watson optical potential

$$U^{(1)} = \sum_{i=1}^A \tau_{oi} =: \sum_{i=1}^N \tau_n + \sum_{i=1}^P \tau_p$$

- Important for treating  $N \neq Z$  nuclei
- Be sensitive to proton vs. neutron scattering
- In general
  - $t_{pp} \neq t_{np}$
  - $\rho_p \neq \rho_n$
- These differences enter in a non-linear fashion into first order Watson optical potential

$$\tau_\alpha = t_\alpha - t_\alpha G_0^\alpha(\mathbf{e}) \tau_\alpha, \quad \alpha = n, p$$

Isospin effects in elastic p+A scattering, Chinn, Elster, Thaler, PRC47, 2242 (1993)



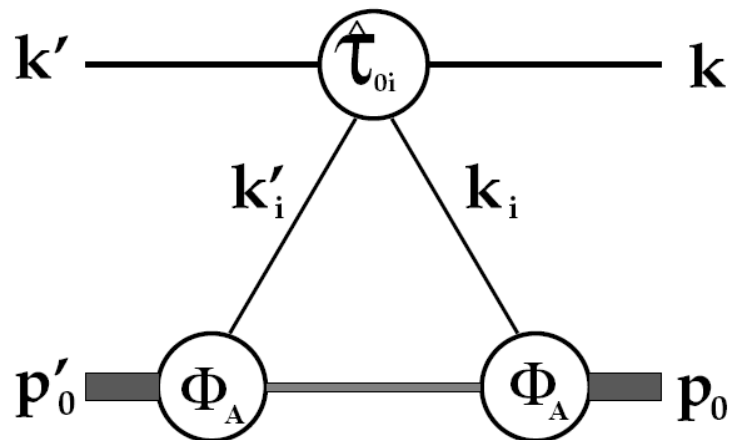
Solid: Watson

Dotted:  $\tau = t$

## More formal:

- Elastic scattering :  $T_{el} = PUP + PUPG_0(E)PT_{el}$ .
- First order Watson O.P.:

$$\langle \mathbf{k}' | \langle \phi_A | PUP | \phi_A \rangle \mathbf{k} \rangle \equiv U_{el}(\mathbf{k}', \mathbf{k}) = \sum_{i=n,p} \langle \mathbf{k}' | \langle \phi_A | \hat{\tau}_{0i}(\mathcal{E}) | \phi_A \rangle \mathbf{k} \rangle$$



$$\langle \hat{\tau}_{01} \rangle \equiv \langle \mathbf{k}' | \langle \phi_A | \hat{\tau}_{01}(\mathcal{E}) | \phi_A \rangle \mathbf{k} \rangle$$

Proton scattering:  $U_{el}(\mathbf{k}', \mathbf{k}) = Z \langle \hat{\tau}_{01}^{pp} \rangle + N \langle \hat{\tau}_{01}^{np} \rangle$

**Calculate:**

$$\langle \hat{\tau}_{01} \rangle \equiv \langle \mathbf{k}' | \langle \phi_A | \hat{\tau}_{01}(\mathcal{E}) | \phi_A \rangle \mathbf{k} \rangle$$

$$\langle \mathbf{k}_1 \mathbf{k}_2 \mathbf{k}_3 \mathbf{k}_4 \dots \mathbf{k}_A | \phi_A \rangle = \delta(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3 + \mathbf{k}_4 \dots + \mathbf{k}_A - \mathbf{p}_0) \langle \zeta_1 \zeta_2 \zeta_3 \zeta_4 \dots \zeta_{A-1} | \phi_A \rangle.$$

$$\begin{aligned} \langle \hat{\tau}_{01} \rangle &= \int \prod_{j=1}^A d\mathbf{k}'_j \int \prod_{l=1}^A d\mathbf{k}_l \langle \phi_A | \zeta'_1 \zeta'_2 \zeta'_3 \zeta'_4 \dots \zeta'_{A-1} \rangle \delta(\mathbf{p}' - \mathbf{p}_0) \langle \mathbf{k}' \mathbf{k}'_1 | \hat{\tau}_{01}(\mathcal{E}) | \mathbf{k} \mathbf{k}_1 \rangle \\ &\prod_{j=2}^A \delta(\mathbf{k}'_j - \mathbf{k}_j) \delta(\mathbf{p} - \mathbf{p}_0) \langle \zeta_1 \zeta_2 \zeta_3 \zeta_4 \dots \zeta_{A-1} | \phi_A \rangle, \end{aligned} \quad (2.48)$$

**With single particle density matrix :**

$$\rho(\zeta'_1, \zeta_1) \equiv \int \prod_{l=2}^{A-1} d\zeta'_l \int \prod_{j=2}^{A-1} d\zeta_j \langle \phi_A | \zeta'_1 \zeta'_2 \zeta'_3 \zeta'_4 \dots \zeta'_{A-1} \rangle \langle \zeta_1 \zeta_2 \zeta_3 \zeta_4 \dots \zeta_{A-1} | \phi_A \rangle.$$

$$\langle \hat{\tau}_{01} \rangle = \int d\zeta'_1 \int d\zeta_1 \langle \mathbf{k}' \zeta'_1 + \frac{\mathbf{p}'_0}{A} | \hat{\tau}_{01}(\mathcal{E}) | \mathbf{k} \zeta_1 + \frac{\mathbf{p}_0}{A} \rangle \rho(\zeta'_1, \zeta_1)$$

$$\delta\left(\frac{A-1}{A} \mathbf{p}'_0 - \zeta'_1 - \frac{A-1}{A} \mathbf{p}_0 + \zeta_1\right).$$

Better Variables:

$$\begin{aligned} \mathbf{k} &= \mathbf{K} - \frac{1}{2}\mathbf{q} & \zeta_1 &= \mathbf{P} + \frac{A-1}{2A}\mathbf{q} \\ \mathbf{k}' &= \mathbf{K} + \frac{1}{2}\mathbf{q} & \zeta_1' &= \mathbf{P} - \frac{A-1}{2A}\mathbf{q}. \end{aligned}$$

$$\begin{aligned} \langle \hat{\tau}_{01} \rangle &= \left\langle \frac{1}{2} \left( \mathbf{K} - \mathbf{P} + \frac{2A-1}{2A}\mathbf{q} - \frac{\mathbf{p}'_0}{A} \right) \middle| \hat{\tau}_{01}(\hat{\mathcal{E}}) \middle| \frac{1}{2} \left( \mathbf{K} - \mathbf{P} - \frac{2A-1}{2A}\mathbf{q} - \frac{\mathbf{p}_0}{A} \right) \right\rangle \\ \rho \left( \mathbf{P} - \frac{A-1}{2A}\mathbf{q}, \mathbf{P} + \frac{A-1}{2A}\mathbf{q} \right). \end{aligned} \quad (2.59)$$

$$U_{el}(\mathbf{q}, \mathbf{K}) = \sum_{i=n,p} \int d\mathbf{P} \hat{\tau}_{0i}(\mathbf{q}, \frac{1}{2}(\frac{A+1}{A}\mathbf{K} - \mathbf{P}), \hat{\mathcal{E}}) \rho_i(\mathbf{P} - \frac{A-1}{2A}\mathbf{q}, \mathbf{P} + \frac{A-1}{2A}\mathbf{q})$$

$$\hat{\mathcal{E}} = E_{NA} - \frac{(\mathbf{k} + \mathbf{k}_1)^2}{4m} = E_{NA} - \left( \frac{(\frac{A-1}{A}\mathbf{K} + \mathbf{P})^2}{4m} \right)$$

# Full-Folding Optical Potential

$$U_{el}(\mathbf{q}, \mathbf{K}) = \sum_{i=n,p} \int d\mathbf{P} \hat{\tau}_{0i}(\mathbf{q}, \frac{1}{2}(\frac{A+1}{A}\mathbf{K} - \mathbf{P}), \hat{\mathcal{E}}) \rho_i(\mathbf{P} - \frac{A-1}{2A}\mathbf{q}, \mathbf{P} + \frac{A-1}{2A}\mathbf{q})$$

Depends on  $|\mathbf{q}|$ ,  $|\mathbf{K}|$ ,  $\cos(\theta)_{\mathbf{q}\mathbf{K}}$

Stored on grids 80x80x5 for low energies  
and 360x360x5 for high energies

Study of approximations and simplifications (like fixed energy  $\varepsilon$ , on-shell density ....) to get to “text-book” expression for optical potential

$$U(\mathbf{q}) = t(\mathbf{q}) \rho(\mathbf{q})$$

See Thesis Stephen Weppner @ [www.phy.ohiou.edu/~elster/HE6](http://www.phy.ohiou.edu/~elster/HE6)

# NN amplitude $f_{NN}(k'k;E) = C \langle k' | t_{NN}(E) | k \rangle$

Variables  $(E, k', k, \varphi) \Rightarrow (E, q, K, \theta)$  with  $q = k' - k$   
 $K = 1/2(k' + k)$

Invariant $J_\alpha$	Amplitude $A_\alpha$
$\mathbb{1}$	$A(q, \mathcal{X}, \vec{q} \cdot \vec{\mathcal{X}})$
$(\vec{\sigma}_1 + \vec{\sigma}_2) \cdot \vec{w}$	$C(q, \mathcal{X}, \vec{q} \cdot \vec{\mathcal{X}})$
.....	.....
$\vec{\sigma}_1 \cdot \vec{w} \quad \vec{\sigma}_2 \cdot \vec{w}$	$B(q, \mathcal{X}, \vec{q} \cdot \vec{\mathcal{X}}) \quad M(\dots)$
$\vec{\sigma}_1 \cdot \hat{q} \quad \vec{\sigma}_2 \cdot \hat{q}$	$E(q, \mathcal{X}, \vec{q} \cdot \vec{\mathcal{X}}) \quad \text{or} \quad G(\dots)$
$\vec{\sigma}_1 \cdot \hat{\mathcal{X}} \quad \vec{\sigma}_2 \cdot \hat{\mathcal{X}}$	$F(q, \mathcal{X}, \vec{q} \cdot \vec{\mathcal{X}}) \quad H(\dots)$ <small>(Wolfenstein)                      (Hoshizaki)</small>
$(\vec{\sigma}_1 \cdot \hat{q} \vec{\sigma}_2 \cdot \hat{\mathcal{X}} + \vec{\sigma}_1 \cdot \hat{\mathcal{X}} \vec{\sigma}_2 \cdot \hat{q}) \vec{q} \cdot \vec{\mathcal{X}}$	$D(q, \mathcal{X}, \vec{q} \cdot \vec{\mathcal{X}}) = 0 \text{ on-shell}$

## Densities used in 1997:

- Dirac-Hartree

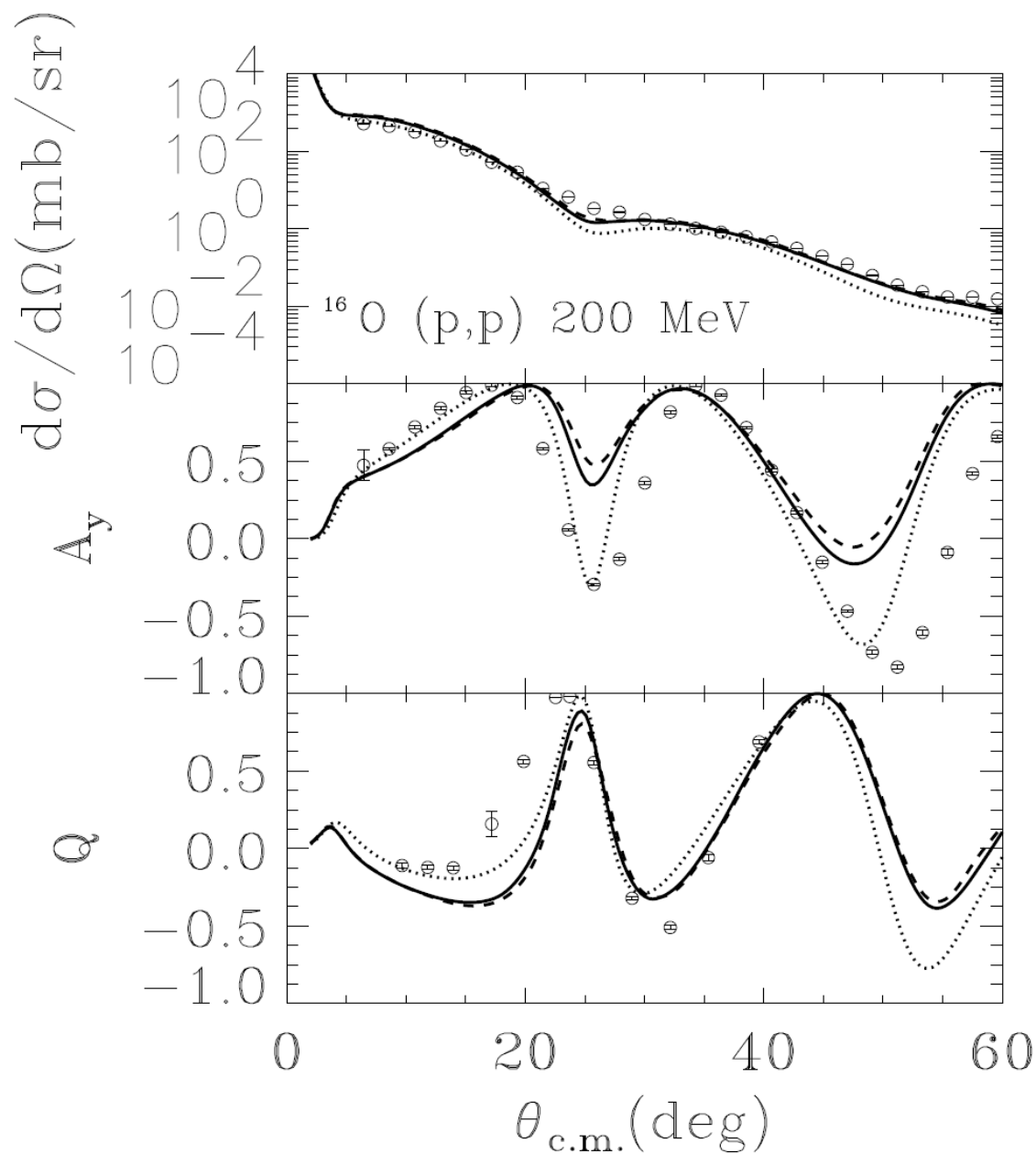
$$\rho_{t_z}(\mathbf{r}', \mathbf{r}) = \sum_{n\nu} \left[ \frac{G_{n,\nu,t_z}(r')}{r'} \frac{G_{n,\nu,t_z}(r)}{r} + \frac{F_{n,\nu,t_z}(r')}{r'} \frac{F_{n,\nu,t_z}(r)}{r} \right] \frac{2J+1}{2l+1} \sum_{m_l} Y_l^{*m_l}(\hat{\mathbf{r}}') Y_l^{m_l}(\hat{\mathbf{r}}).$$

- Gogny
- Harmonic Oscillator (home-brew)

$$\rho_s(\mathbf{q}, \mathbf{P}) = \frac{4\pi}{\nu_s} e^{-(P^2/\nu_s + q^2/4\nu_s)},$$

$$\rho_p(\mathbf{q}, \mathbf{P}) = \frac{2}{3} \frac{4\pi}{\nu_p} (P^2/\nu_p - q^2/4\nu_p) e^{-(P^2/\nu_p + q^2/4\nu_p)}$$





Solid: fixed  $\varepsilon$

Dashed: integrated  $\varepsilon$   
and  $\langle H_A \rangle = 0 \text{ MeV}$

Dotted: integrated  $\varepsilon$   
and  $\langle H_A \rangle = -8 \text{ MeV}$

$$\tau_{0i} = v_{0i} + v_{0i} G_0(E) Q \tau_{0i}$$

- $G_0(E) = (E - h_0 - H_A + i\varepsilon)^{-1} == (A+1)$  body operator
  - Standard “**impulse approximation**”:
  - Average over  $H_A \Rightarrow$  c-number
  - $\rightarrow G_0(e) ==$ : two body operator
- Deal with **Q**
  - Define “two-body” operator  $t_{0i}^{\text{free}}$  by
  - $t_{0i}^{\text{free}} = v_{0i} + v_{0i} G_0(e) t_{0i}^{\text{free}}$  **Exact**
  - and relate via integral equation to  $\tau_{0i}$
  - $\tau_{0i} = t_{0i}^{\text{free}} - t_{0i}^{\text{free}} G_0(e) \tau_{0i}$  **[integral equation]**
  - Important for keeping correct iso-spin character of optical potential
  - $U^{(1)} = \sum_{i=1}^A \tau_{0i} =: N \tau_n + Z \tau_p$

## Propagator (A+1) body operator:

$$G_0(E) = (E - h_0 - H_A + i\varepsilon)^{-1}$$

$$H_A = h_i + \sum_{j \neq i}^A v_{ij} + H^i$$

Chinn, Elster, Thaler  
PRC 48, 2956 (1993)

$h_i$  : kinetic energy of nucleon  $i$

$v_{ij}$  : interaction potential between  $i$  and  $j$

$H^i$  : (A-1) Hamiltonian  $\rightarrow \langle H^i \rangle \equiv \varepsilon^i \equiv$  c-number

$\langle \sum_{j \neq i}^A v_{ij} \rangle \equiv U_i \equiv$  mean field

$$\varepsilon^i + \varepsilon_i = \langle H_A \rangle = 0$$

Two-body  
operator via  
construction:

$$G_0(E_i, i)^{-1} = (E - \varepsilon^i) - h_0 - h_i - U_i$$
$$E_i \equiv E - [\varepsilon^i + \varepsilon_i] + \varepsilon_i$$

$$\tilde{t}_{0i} = v_{0i} + v_{0i} G_0(E_i, i) \tilde{t}_{0i}$$

$$t_{0i}^{\text{free}} = v_{0i} + v_{0i} g_0(e) t_{0i}^{\text{free}} \quad e = \text{arbitrary for now}$$

$$\tilde{t}_{0i} = t_{0i}^{\text{free}} + t_{0i}^{\text{free}} [G_0(E_i, i) - g_0(e)] \tilde{t}_{0i}$$

## Resolvent Identities:

$$\begin{aligned} G_0(E_i, i) - g_0(e) &= G_0(E_i, i) [g_0(e)^{-1} - G_0^{-1}(E_i, i)] g_0(e) \\ &= G_0(E_i, i) [e - h_0 - h_i - (E_i - h_0 - h_i - U_i)] g_0(e) \end{aligned}$$

$$\begin{aligned} \text{for } e = E_i & \\ &= G_0(E_i, i) U_i g_0(E_i) \\ &= g_0(E_i) T_i(E_i) g_0(E_i) \end{aligned}$$

$$\text{with } T_i(E_i) = U_i + U_i g_0(E_i) T_i(E_i)$$

$$\begin{aligned}\tilde{t}_{0i}(\mathbf{E}_i) &= t_{0i}^{\text{free}}(\mathbf{E}_i) + t_{0i}^{\text{free}}(\mathbf{E}_i)g_0(\mathbf{E}_i)T(\mathbf{E}_i)g_0(\mathbf{E}_i)\tilde{t}_{0i}(\mathbf{E}_i) \\ &= t_{0i}^{\text{free}}(\mathbf{E}_i) + \omega_{0i}(\mathbf{E}_i)g_0(\mathbf{E}_i)\tilde{t}_{0i}(\mathbf{E}_i)\end{aligned}$$

$$\tilde{t}_{0i}(\mathbf{E}_i) = t_{0i}^{\text{free}}(\mathbf{E}_i) + \Delta_{0i}$$

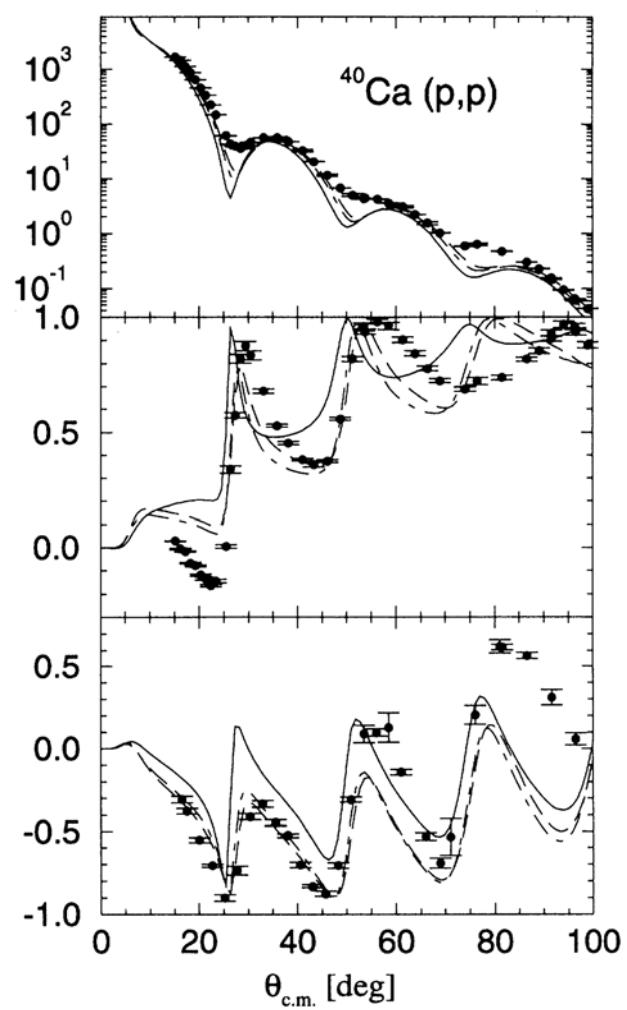
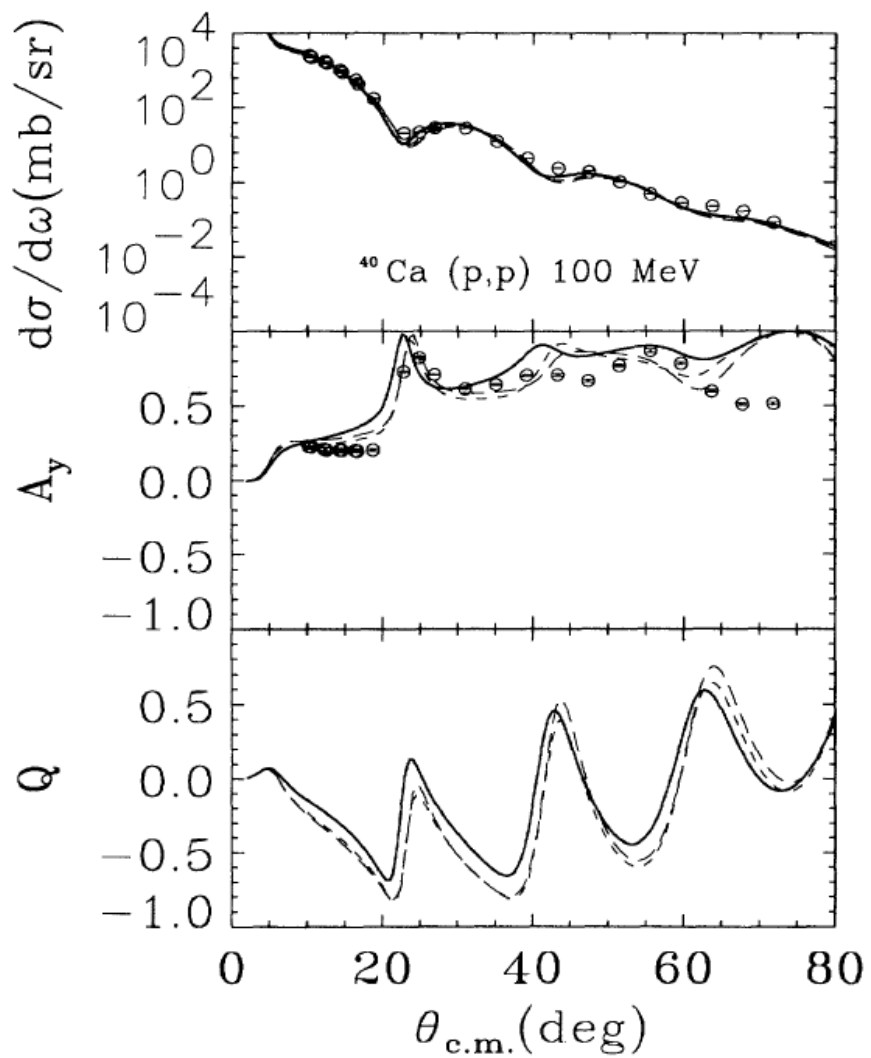
$$\begin{aligned}\Delta_{0i} &= \omega_{0i}(\mathbf{E}_i)g_0(\mathbf{E}_i)\tilde{t}_{0i}(\mathbf{E}_i) \\ &= t_{0i}^{\text{free}}(\mathbf{E}_i)g_0(\mathbf{E}_i)T(\mathbf{E}_i)g_0(\mathbf{E}_i)\tilde{t}_{0i}(\mathbf{E}_i) \\ &= t_{0i}^{\text{free}}(\mathbf{E}_i)g_0(\mathbf{E}_i)\eta_{0i}(\mathbf{E}_i)\end{aligned}$$

*with*  $\eta_{0i}(\mathbf{E}_i) = \omega_{0i}(\mathbf{E}_i) + \omega_{0i}(\mathbf{E}_i)g_0(\mathbf{E}_i)\eta_{0i}(\mathbf{E}_i)$

## Modification of propagator $G_0$ :

- Choose mean field potential  $U_i$  (consistent with density)
- Solve integral equation for  $T_{0i}$
- Construct  $\omega_{0i}(E_i)$ 
  - Approximation: variables are not “right”
  - i.e.  $\omega_{0i}(k'_0, k'_i, k_0, k_i)$  – needed  $\omega_{0i}(k'_0 - k'_i, k_0 - k_i)$
- Solve integral equation for  $\eta_{0i}(E_i)$
- Construct  $\Delta_{0i}$
- Add  $\Delta_{0i}$  to  $t_{0i}^{\text{free}} \rightarrow \tilde{t}_{0i}$
- Fold  $\tilde{t}_{0i}$  with the nuclear density matrix
- Solve integral equation for Watson first order potential

65 MeV



65 MeV

