

Role of the tensor correlation in neutron halo nuclei

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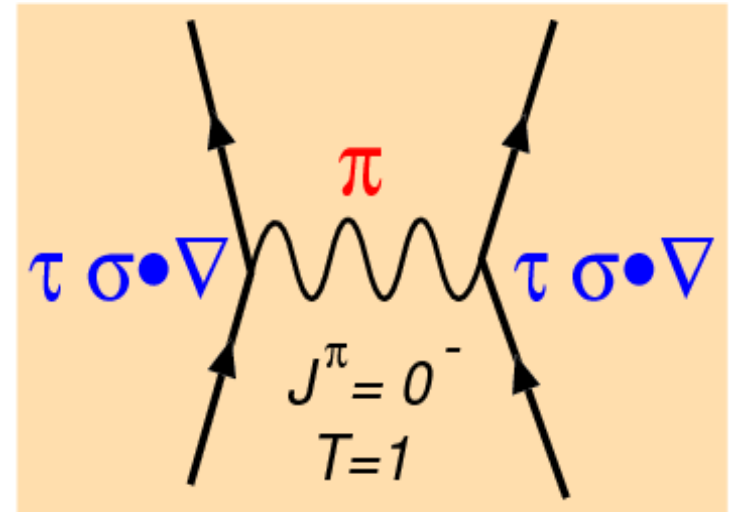
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Contents

- He isotopes with tensor correlation
 - Tensor-optimized shell model (TOSM)
- Li isotopes with tensor and pairing correlations
 - Breaking of magic number, halo formation
- Unitary Correlation Operator Method (UCOM) for short-range correlation
 - TOSM+UCOM with bare interaction

Motivation

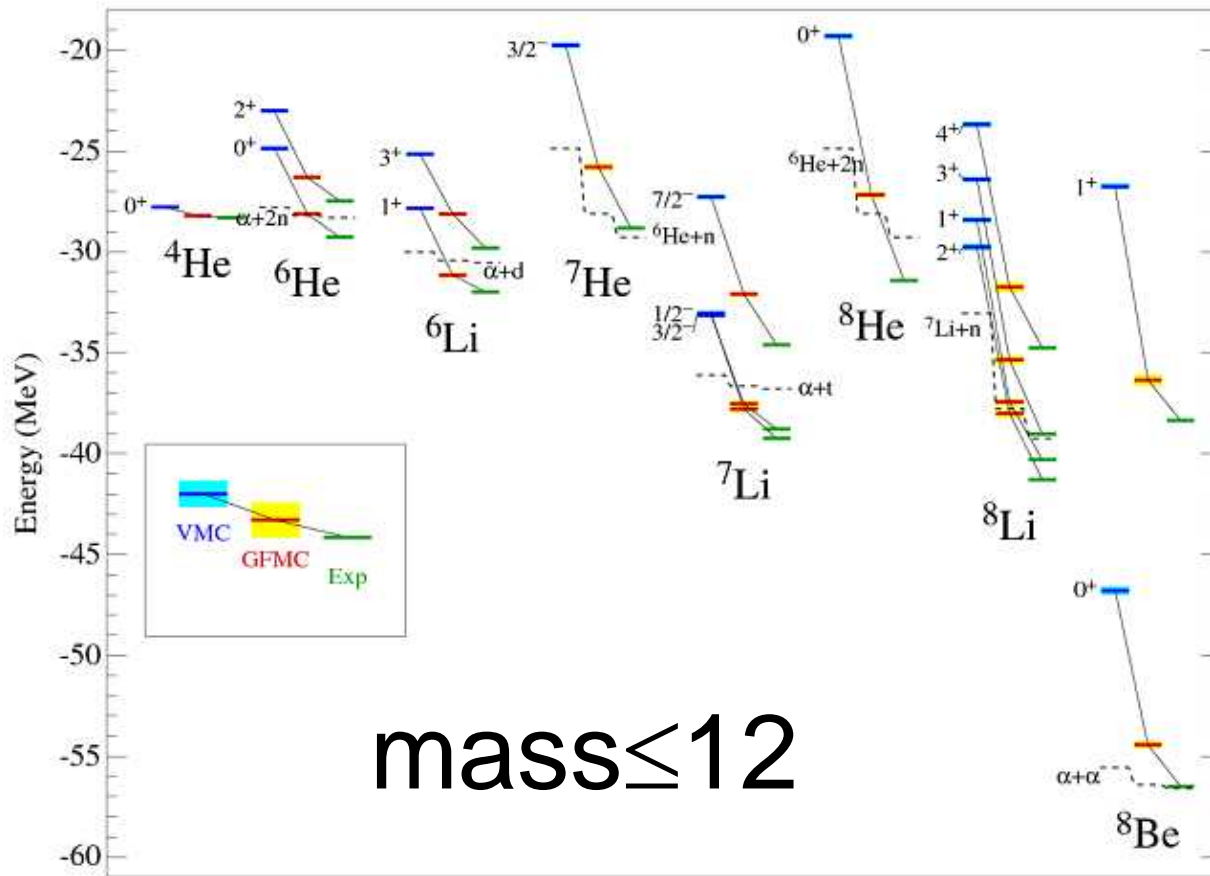
- Tensor force (V_{tensor}) plays a significant role in the nuclear structure.
 - In ${}^4\text{He}$, $\langle V_{tensor} \rangle \sim \langle V_{central} \rangle$
 - $\frac{V_{\pi}}{V_{NN}} \sim 80\%$ (GFMC)



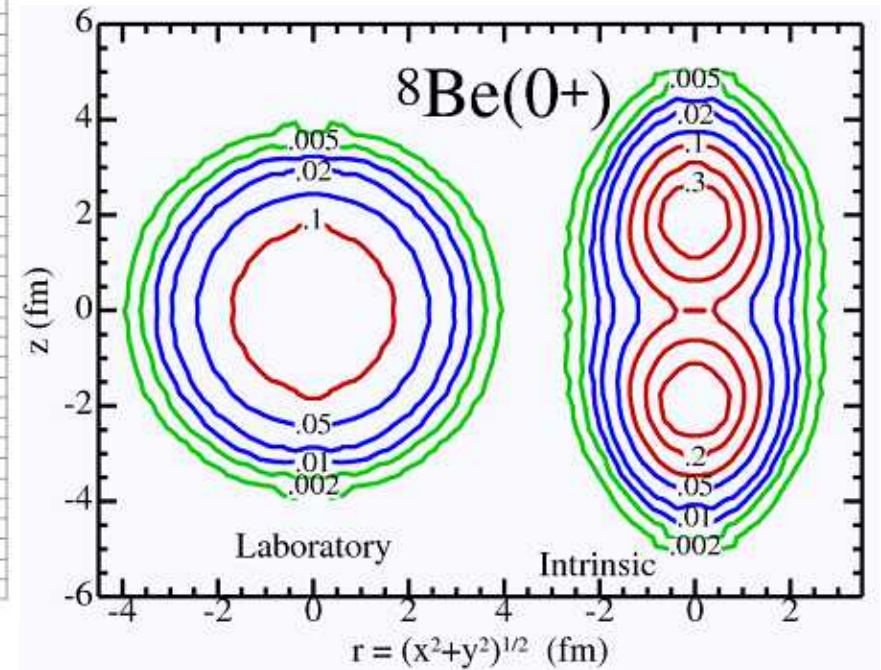
R.B. Wiringa, S.C. Pieper, J. Carlson, V.R. Pandharipande, PRC62(2001)

- We would like to understand the role of V_{tensor} in the nuclear structure **by describing tensor correlation explicitly.**
 - model wave function (shell model and cluster model).
 - spatial properties, p-h correlation, ...
- Spectroscopy of neutron-rich nuclei : He and Li isotopes

Variational calculation in real space



Green's function
Monte Carlo



α - α structure

C.Pieper, R.B.Wiringa,
Annu.Rev.Nucl.Part.Sci.51(2001)
R.B.Wilinga, S.C.Pieper, J.Carlson, V.R.Pandaripande,
PRC62(2000)014001.

Tensor-optimized shell model (TOSM)

- Tensor correlation in the shell model type approach.

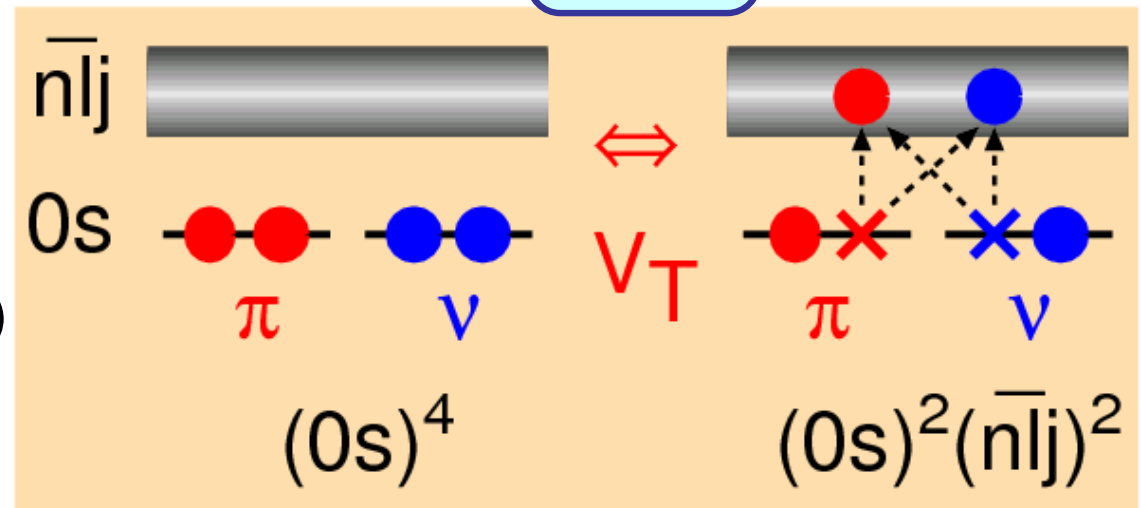
⁴He

- Configuration mixing with high-L orbit within **2p2h excitations**

TM, Kato, Ikeda, PTP113(2005)

TM et al., PTP117(2007)

T.Terasawa, PTP22(1959)



- Length parameters $\{b_\alpha\}$ such as $b_{0s}, b_{0p1/2}, \dots$ are determined **independently** and **variationally**.

– Describe **high momentum component** from V_{tensor}

CPPHF by Sugimoto et al.(NPA740) / Akaishi (NPA738)

CPP-RMF by Ogawa et al.(PRC73), CPP-AMD by Dote et al.(PTP115) 5

Hamiltonian and variational equations

$$H = \sum_{i=1}^A t_i - T_G + \sum_{i<j}^A v_{ij}, \quad v_{ij} : \text{central+tensor+LS+Coulomb}$$

$$\Phi = \sum_k C_k \cdot \psi_k \quad \psi_k : \text{shell model type configuration}$$

$$\delta \frac{\langle \Phi | H | \Phi \rangle}{\langle \Phi | \Phi \rangle} = 0 \Rightarrow \frac{\partial \langle H - E \rangle}{\partial b_\alpha} = 0, \quad \frac{\partial \langle H - E \rangle}{\partial C_k} = 0$$

TM, Kato, Ikeda, PTP113('05)763

TM, Sugimoto, Kato, Toki, Ikeda PTP117('07)257

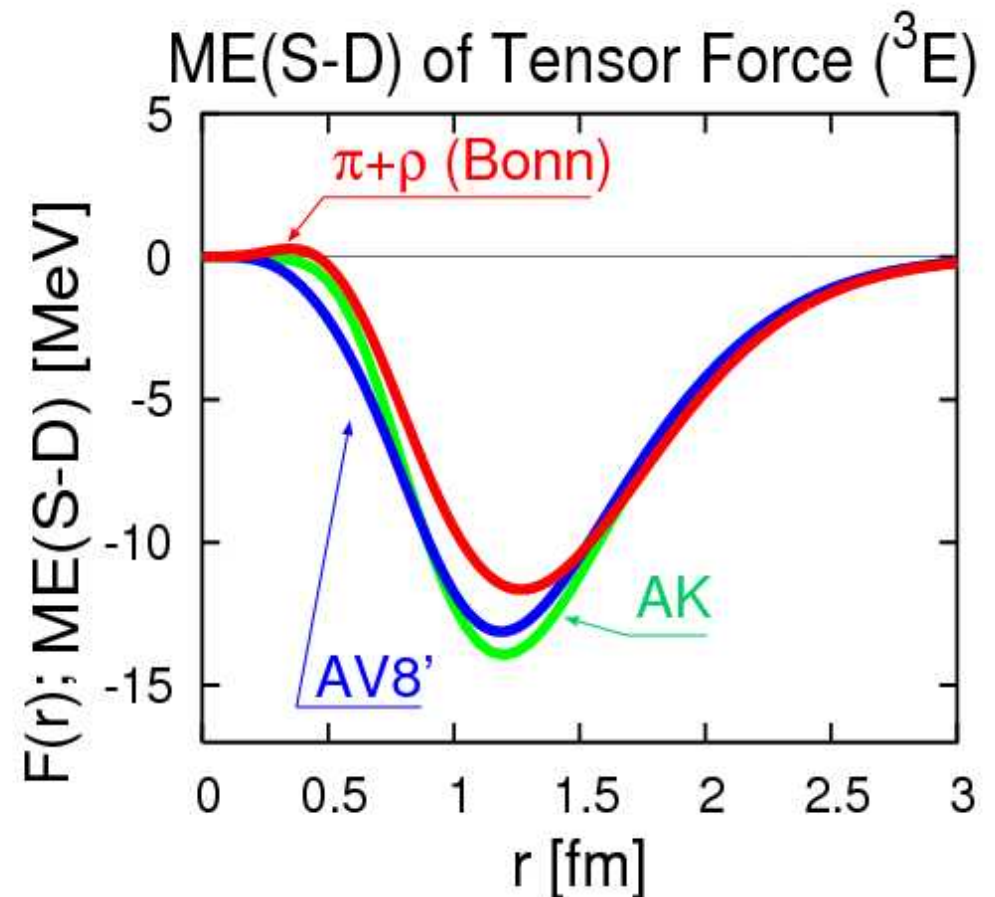
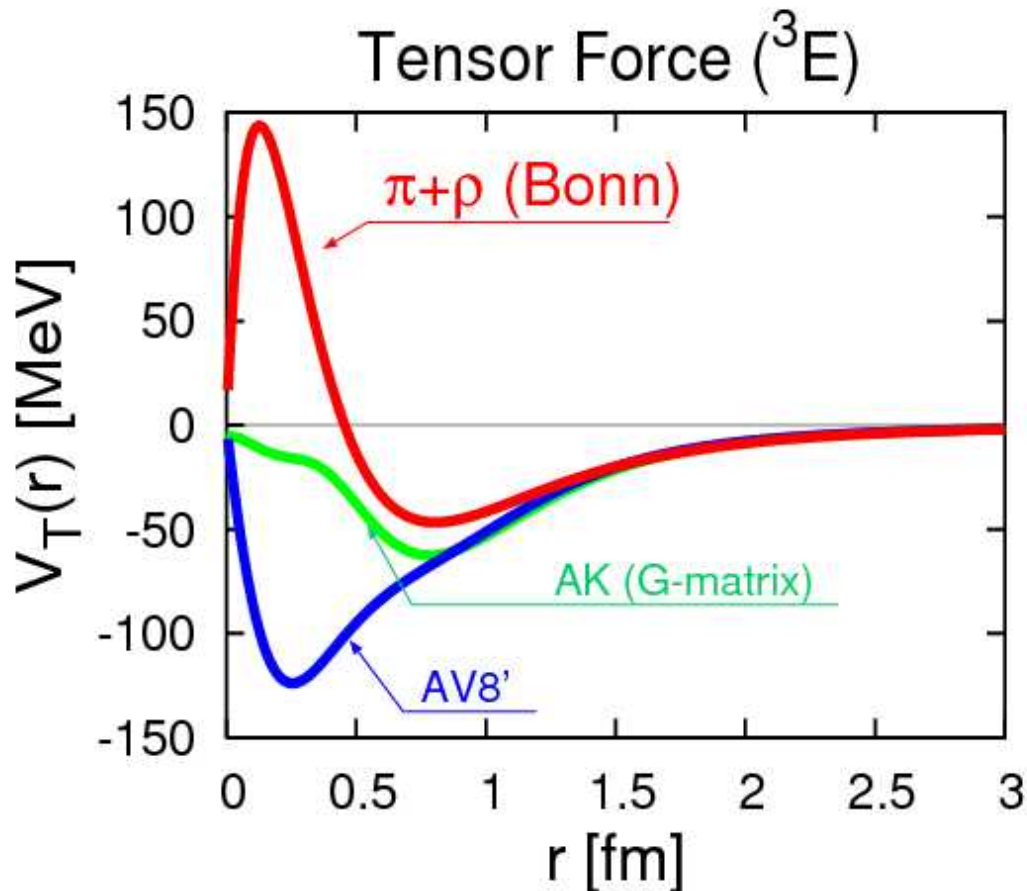
- Effective interaction : Akaishi force (NPA738)
 - G-matrix from AV8' with $k_Q=2.8 \text{ fm}^{-1}$
 - Long and intermediate ranges of V_{tensor} survive.
 - Adjust V_{central} to reproduce B.E. and radius of ${}^4\text{He}$

Property of the tensor force

$$F(r) = r^2 \cdot \phi_{0s}(r, b_{0s}) \cdot V_T(r) \cdot \phi_{0d}(r, b_{0d})$$

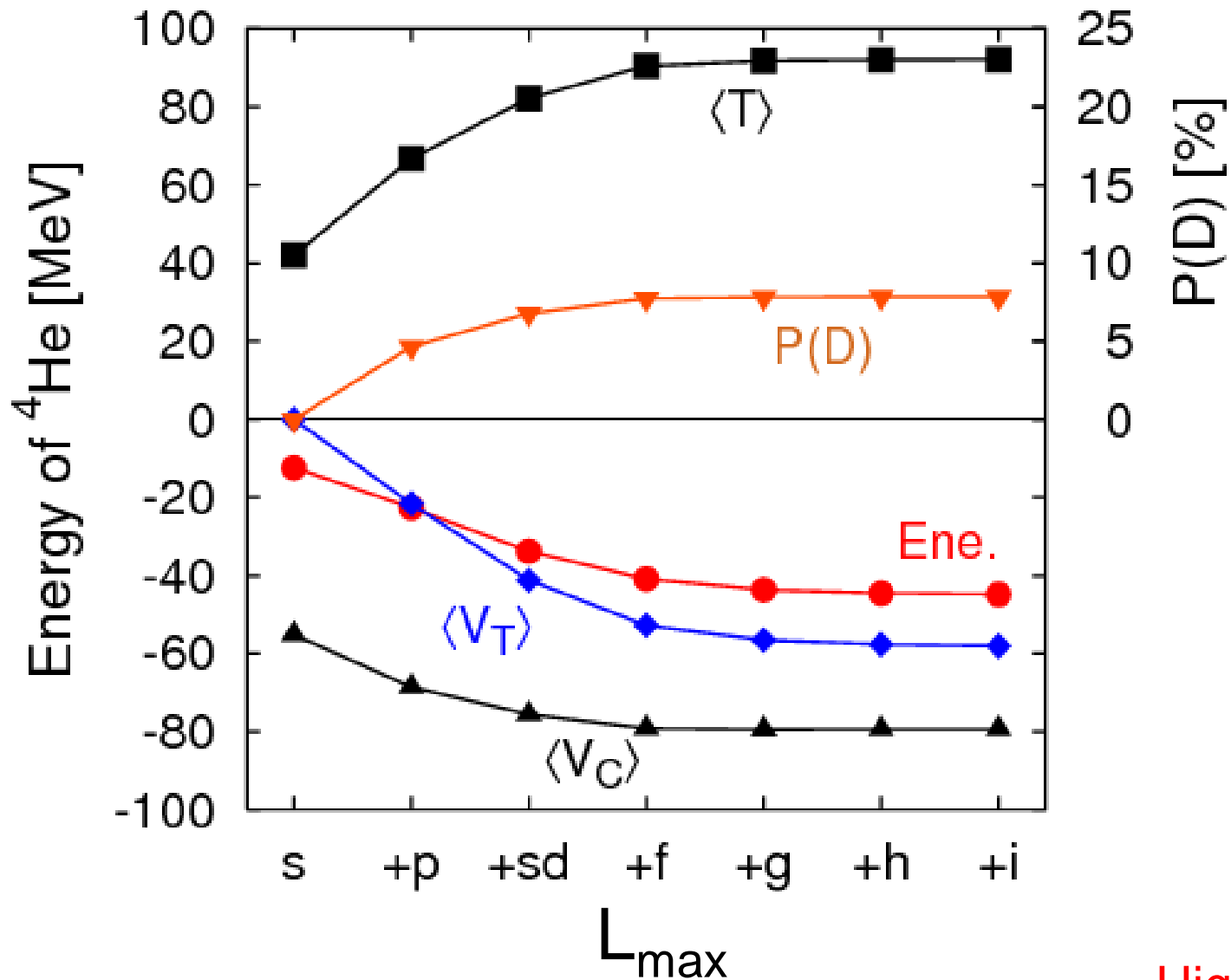
$$V_{\text{tensor}} = V_T(r) \cdot S_{12}$$

$$b_{0s} = 1.4 \cdot \sqrt{2} \text{ [fm]} \quad b_{0d} = b_{0s} / 2$$



- Centrifugal potential (1 GeV @ 0.5 fm) pushes away the L=2 wave function.

^4He with TOSM



good convergence

Length parameters

Orbit	b_{nlj}/b_{0s}
$0p_{1/2}$	0.65
$0p_{3/2}$	0.58
$1s_{1/2}$	0.63
$0d_{3/2}$	0.58
$0d_{5/2}$	0.53
$0f_{5/2}$	0.66
$0f_{7/2}$	0.55

Higher shell effect $\sim 16\hbar\omega$

Pion exchange interaction vs. V_{Tensor}

$$3(\vec{\sigma}_1 \cdot \hat{q})(\vec{\sigma}_2 \cdot \hat{q}) \frac{q^2}{m^2 + q^2} = (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \frac{q^2}{m^2 + q^2} + S_{12} \frac{q^2}{m^2 + q^2}$$

$$= (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \left[\frac{m^2 + q^2}{m^2 + q^2} - \frac{m^2}{m^2 + q^2} \right] + S_{12} \frac{q^2}{m^2 + q^2}$$

↑
Delta interaction

Involve large momentum

Tensor operator

↑
Yukawa interaction

$$S_{12} = 3(\vec{\sigma}_1 \cdot \hat{q})(\vec{\sigma}_2 \cdot \hat{q}) - (\vec{\sigma}_1 \cdot \vec{\sigma}_2)$$

- V_{tensor} produces the high momentum component.

^4He in TOSM

Energy (MeV)	- 28.0
$\langle V_{\text{tensor}} \rangle$	- 51.0
$(0s_{1/2})^4$	85.0 %
$(0s_{1/2})^2_{JT}(0p_{1/2})^2_{JT}$ JT=10	5.0
JT=01	0.3
$(0s_{1/2})^2_{10}(1s_{1/2})(0d_{3/2})_{10}$	2.4
$(0s_{1/2})^2_{10}(0p_{3/2})(0f_{5/2})_{10}$	2.0
P[D]	9.6

4 Gaussians instead of HO

$$\langle T \rangle = 71.2 \text{ MeV}$$

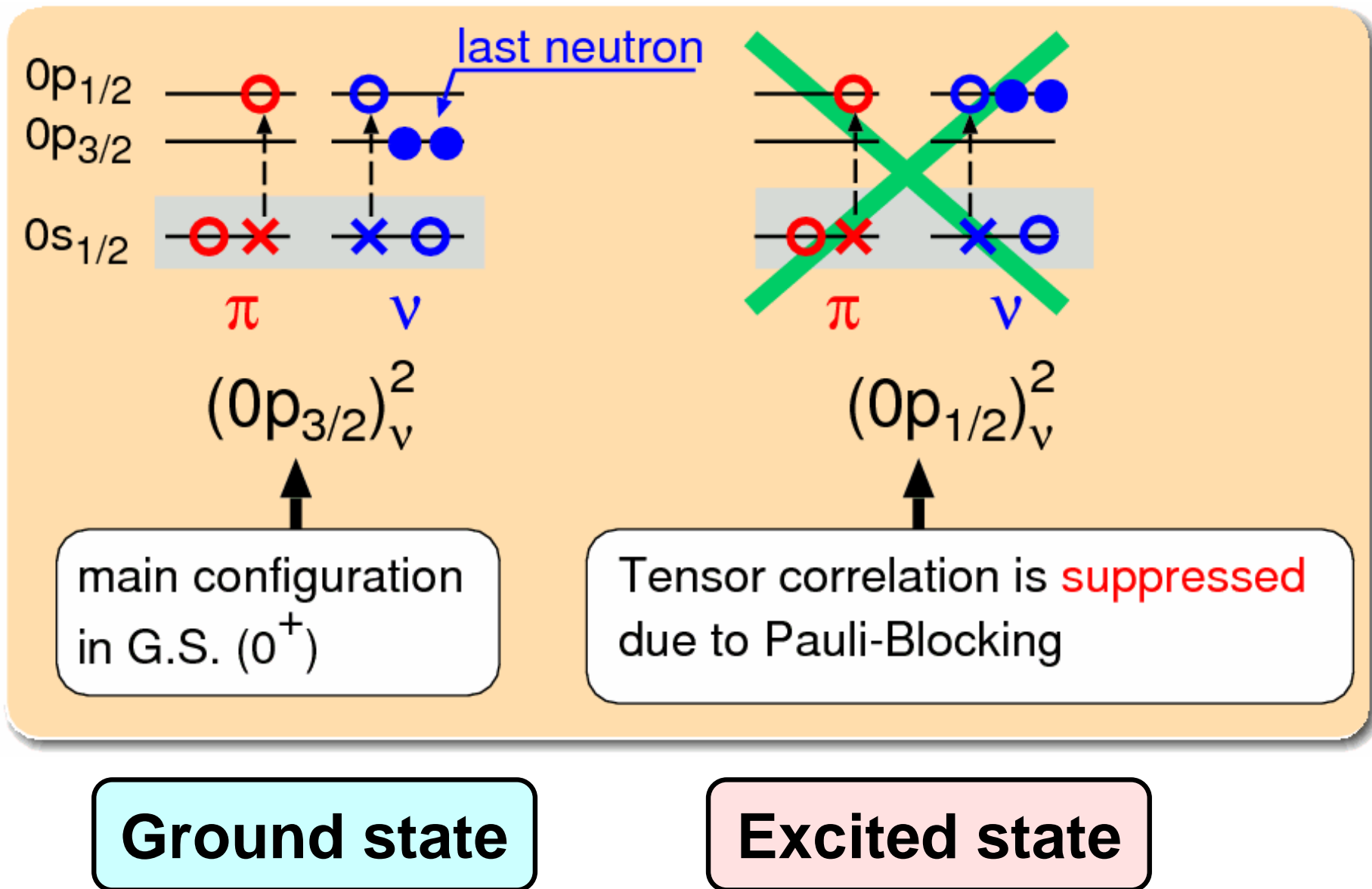
$$\langle V_{\text{central}} \rangle = -48.6 \text{ MeV}$$

c.m. excitation = 0.6 MeV

- 0^- of pion nature.
- deuteron correlation with $(J,T)=(1,0)$

Cf. R.Schiavilla et al. (GFMC)
PRL98('07)132501

Tensor correlation in ${}^6\text{He}$



${}^6\text{He}$ in coupled ${}^4\text{He}+n+n$ model

- System is solved based on RGM

$$H({}^6\text{He}) = H({}^4\text{He}) + H_{nn} \quad \Phi({}^6\text{He}) = \mathcal{A} \left\{ \sum_{i=1}^N \psi_i({}^4\text{He}) \cdot \chi_i(nn) \right\}$$

$$\sum_{i=1}^N \left\langle \psi_j({}^4\text{He}) \left| H({}^6\text{He}) - E \right| \mathcal{A} \left\{ \psi_i({}^4\text{He}) \cdot \chi_i(nn) \right\} \right\rangle = 0$$

$\psi_i({}^4\text{He})$: **shell model type configuration** \rightarrow **TOSM**

- Orthogonality Condition Model (OCM) is applied.

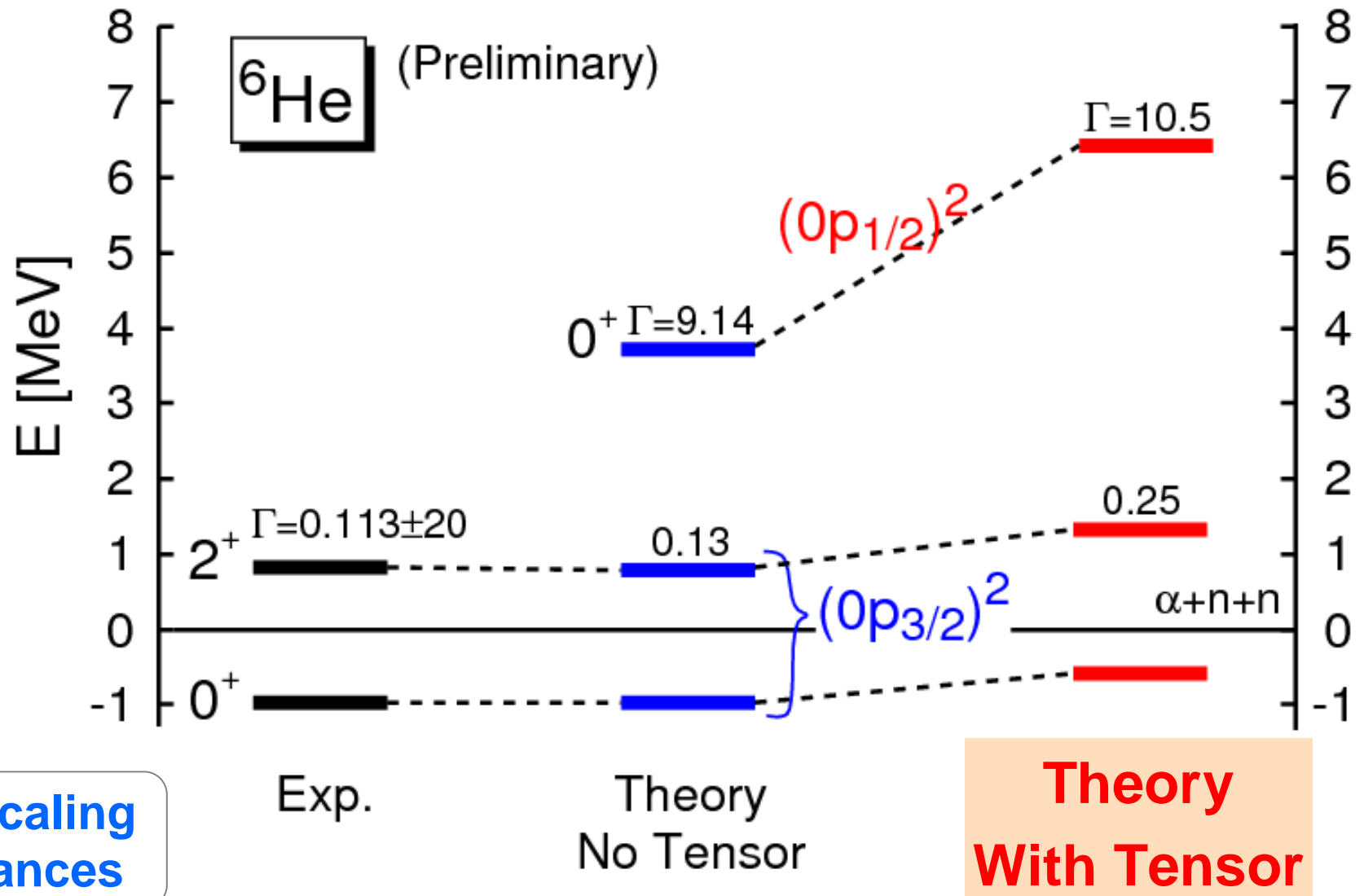
$$\sum_{i=1}^N \left[H_{ij}({}^4\text{He}) + (T_1 + T_2 + V_{c1} + V_{c2} + V_{12}) \cdot \delta_{ij} \right] \chi_j(nn) = E \chi_i(nn)$$

$$H_{ij}({}^4\text{He}) = \langle \psi_i | H({}^4\text{He}) | \psi_j \rangle : \text{Hamiltonian for } {}^4\text{He}$$

$$\chi(nn) = \mathcal{A} \{ \varphi_1 \varphi_2 \} : \text{2 neutrons with Gaussian expansion method}$$

$$\langle \varphi_i | \phi_\alpha \rangle = 0, \{ \phi_\alpha \in {}^4\text{He} \} : \text{Orthogonality to the Pauli-forbidden states}$$

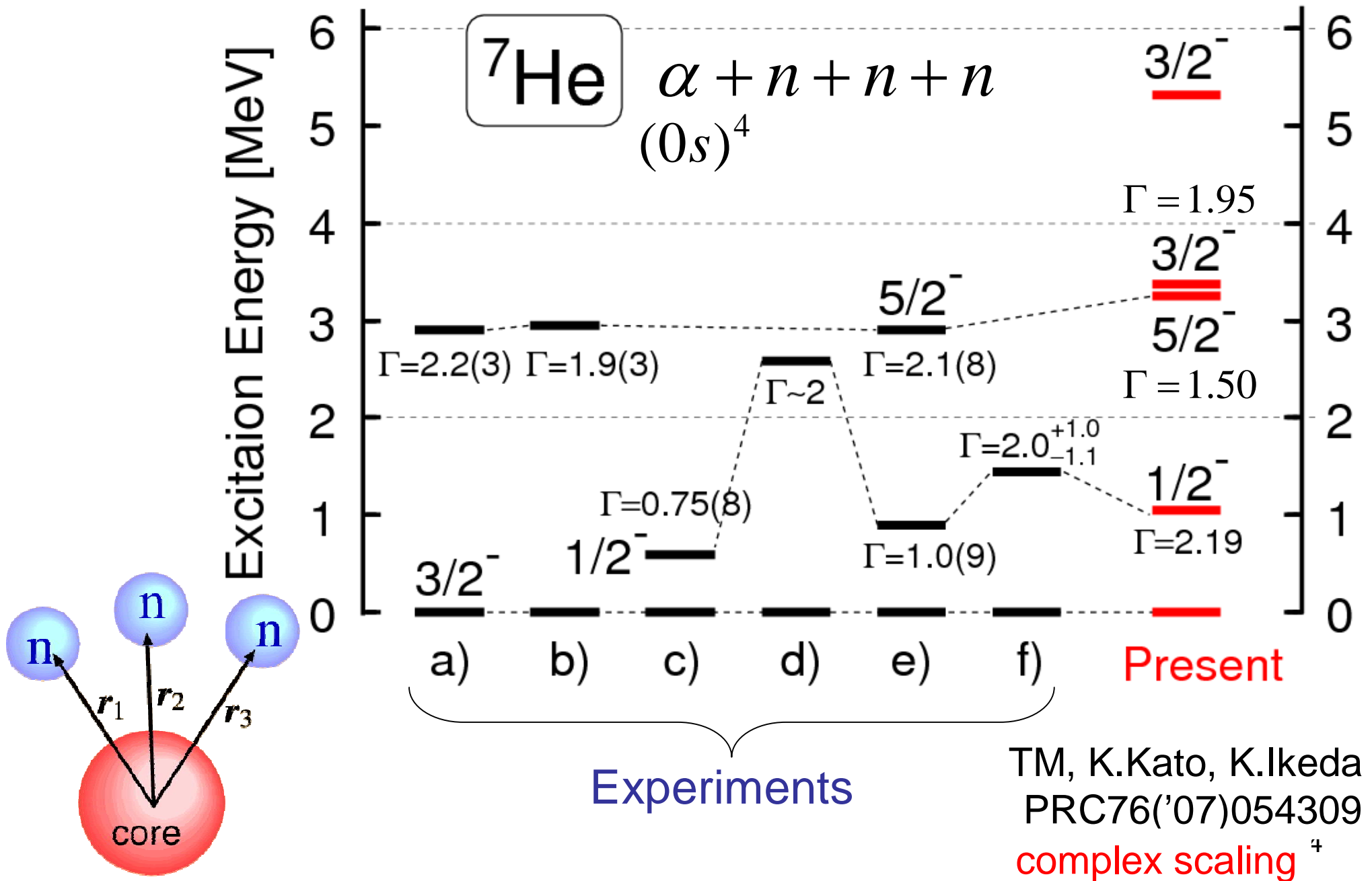
${}^6\text{He}$ in coupled ${}^4\text{He}+n+n$ model



Complex scaling
for resonances

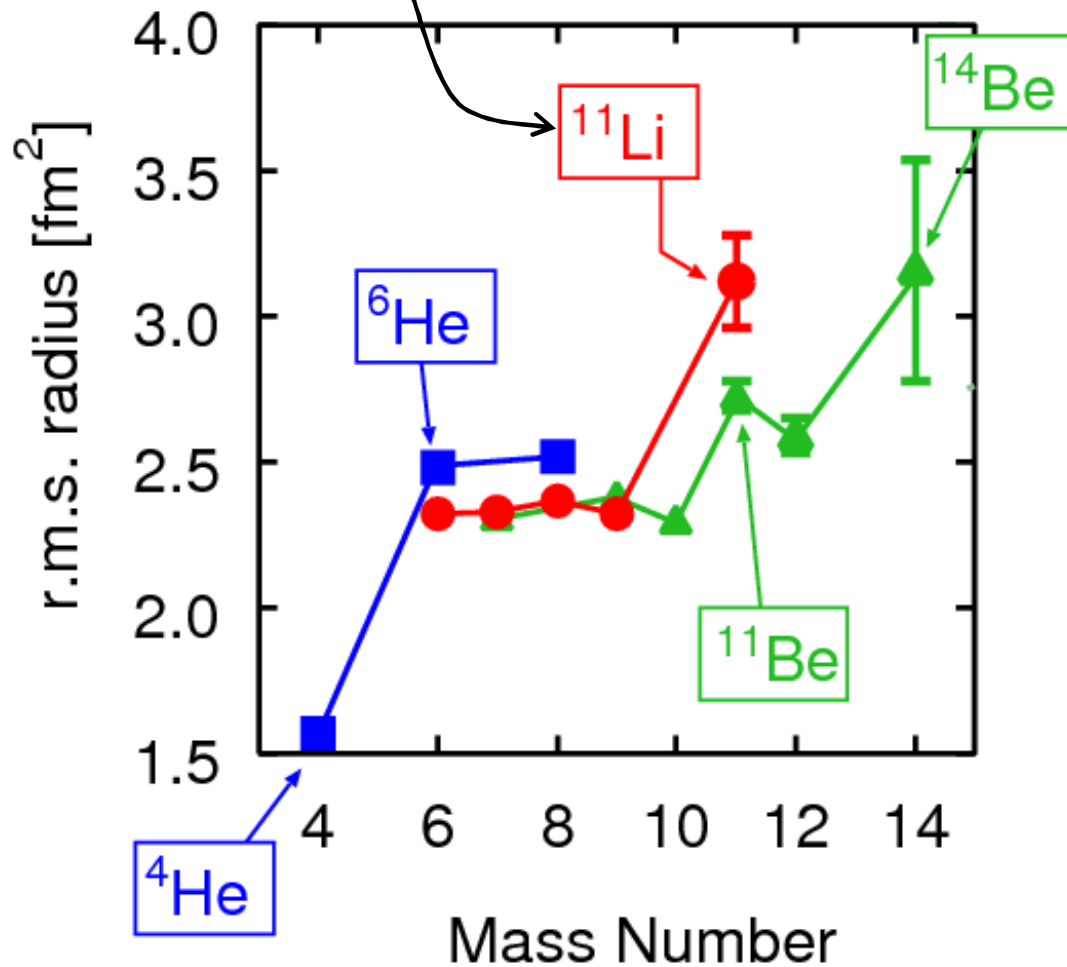
- $(0p_{3/2})^2$ can be described in Naive ${}^4\text{He}+n+n$ model
- $(0p_{1/2})^2$ loses the energy \longrightarrow Tensor suppression in $0^+_{2,13}$

${}^7\text{He}$ (unbound) : Expt vs. Theory



Characteristics of Li-isotopes

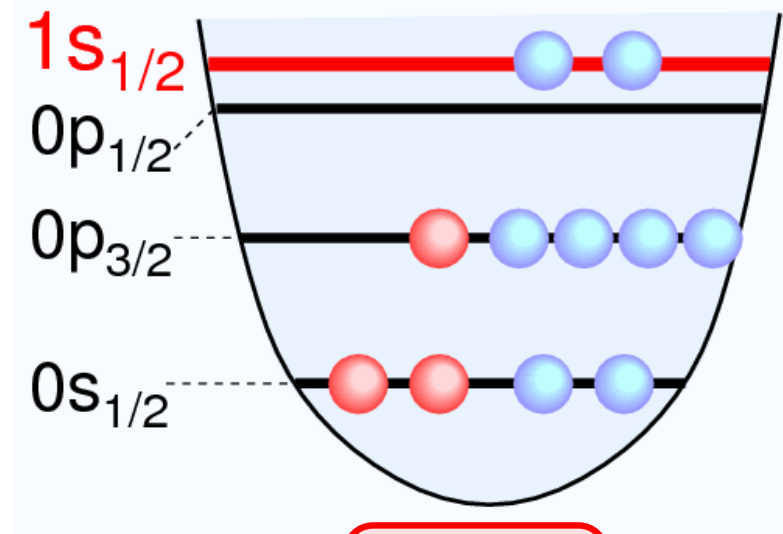
Halo structure



I. Tanihata et. al
PLB206(1988)592

► Breaking of magicity N=8

- ¹⁰⁻¹¹Li, ¹¹⁻¹²Be
- ¹¹Li ... (1s)² ~ 50%.
(Expt by Simon et al., PRL83)
- **Mechanism is unclear**



¹¹Li

^{11}Li in coupled $^9\text{Li}+n+n$ model

- System is solved based on RGM

$$H(^{11}\text{Li}) = H(^9\text{Li}) + H_{nn} \quad \Phi(^{11}\text{Li}) = \mathcal{A} \left\{ \sum_{i=1}^N \psi_i(^9\text{Li}) \cdot \chi_i(nn) \right\}$$

$$\sum_{i=1}^N \left\langle \psi_j(^9\text{Li}) \left| H(^{11}\text{Li}) - E \right| \mathcal{A} \left\{ \psi_i(^9\text{Li}) \cdot \chi_i(nn) \right\} \right\rangle = 0$$

$\psi_i(^9\text{Li})$: **shell model type configuration** \rightarrow

TOSM

- Orthogonality Condition Model (OCM) is applied.

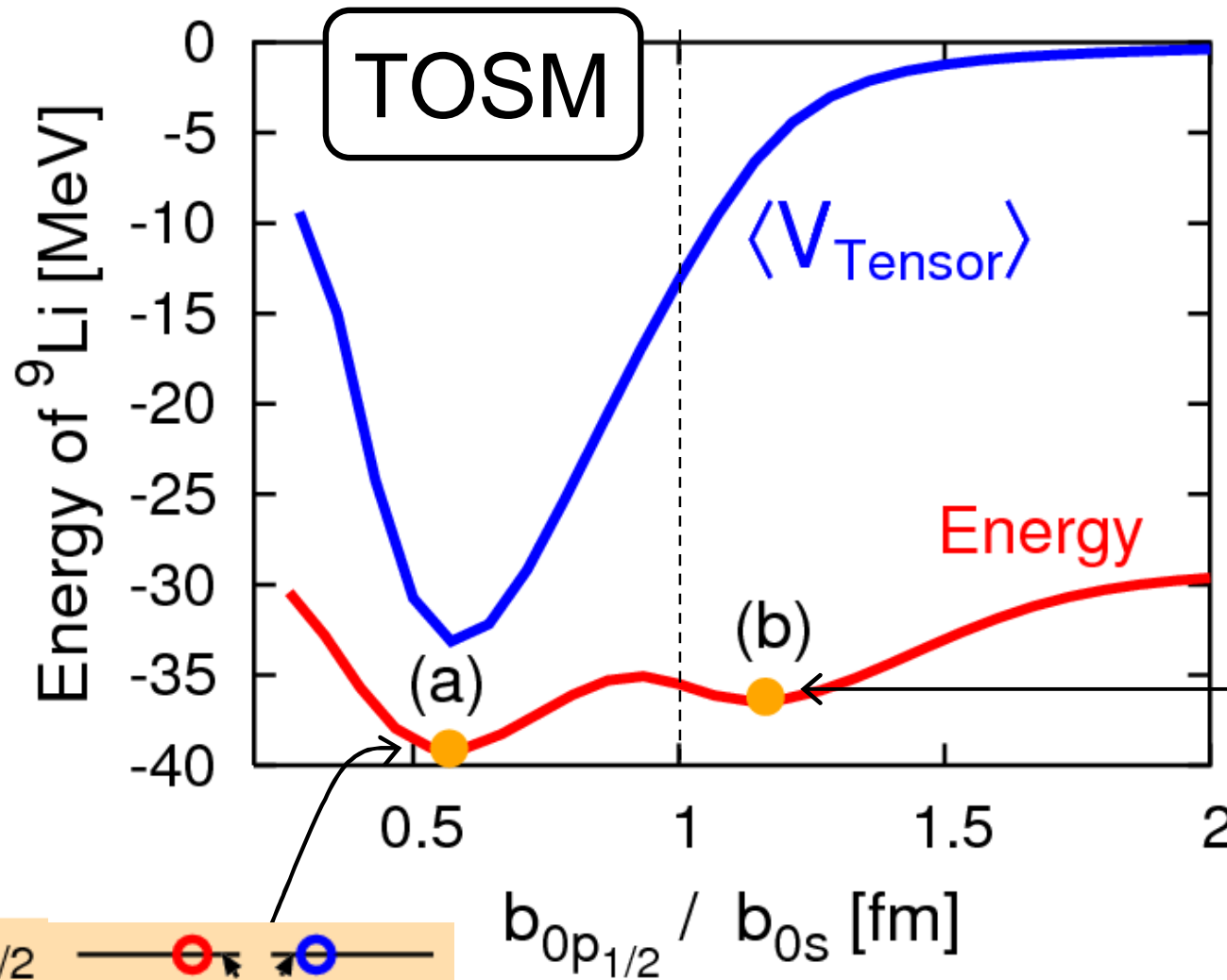
$$\sum_{i=1}^N \left[H_{ij} (^9\text{Li}) + (T_1 + T_2 + V_{c1} + V_{c2} + V_{12}) \cdot \delta_{ij} \right] \chi_j(nn) = E \chi_i(nn)$$

$$H_{ij} (^9\text{Li}) = \langle \psi_i | H(^9\text{Li}) | \psi_j \rangle : \text{Hamiltonian for } ^9\text{Li}$$

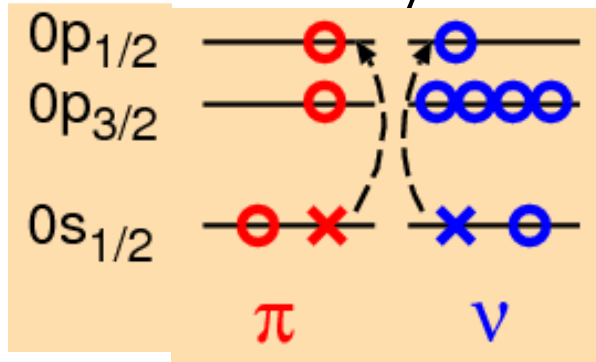
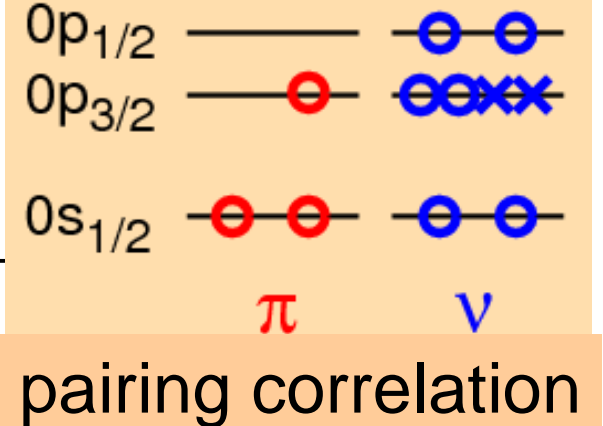
$$\chi(nn) = \mathcal{A} \{ \phi_1 \phi_2 \} : \text{2 neutrons with Gaussian expansion method}$$

$$\langle \phi_i | \phi_\alpha \rangle = 0, \{ \phi_\alpha \in ^9\text{Li} \} : \text{Orthogonality to the Pauli-forbidden states}^{16}$$

Energy surface for b-parameter in ${}^9\text{Li}$



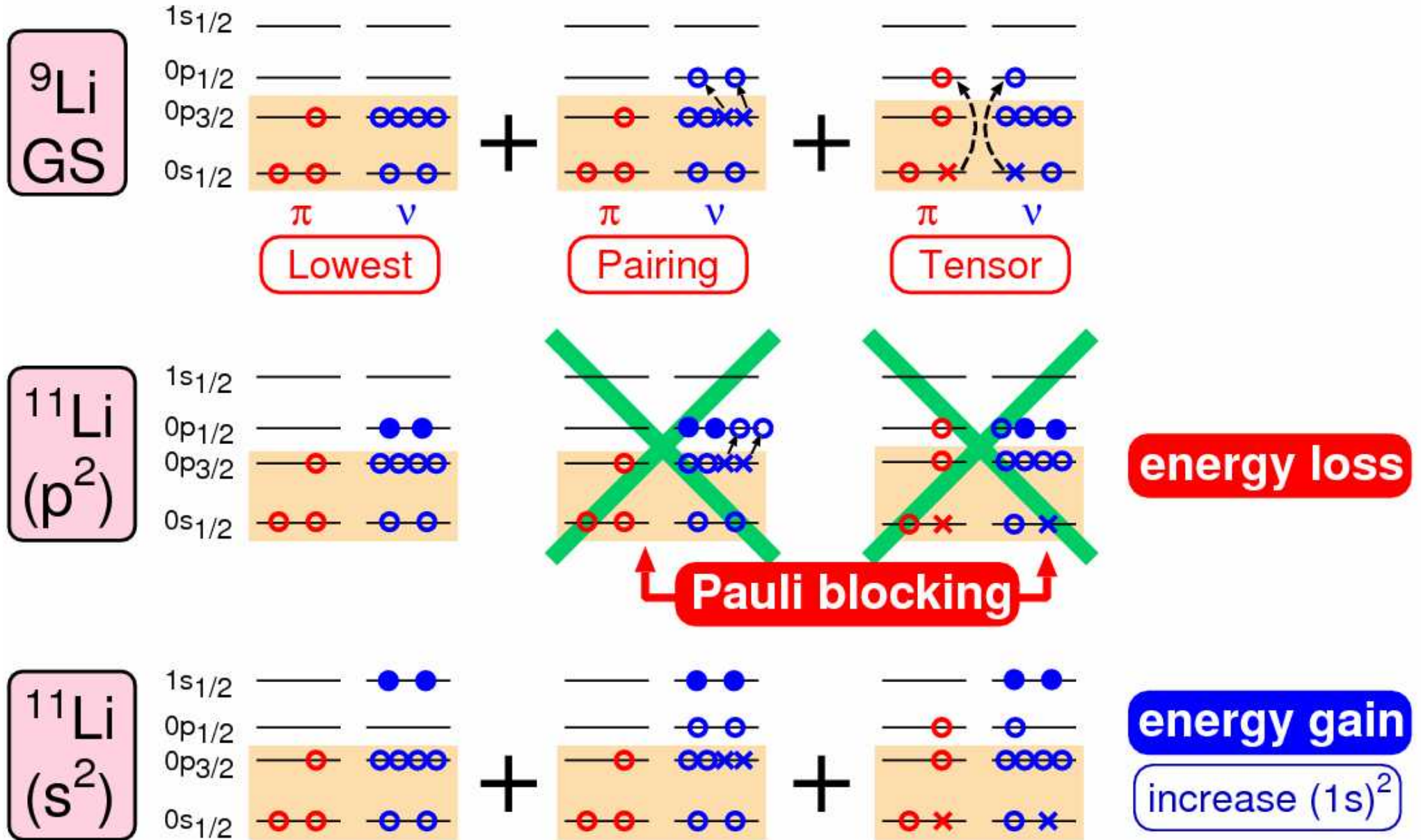
$0s+0p+1s0d$ within
2p2h excitations.



Dominant part of the tensor correlation

cf. 1st order (residual interaction): T. Otsuka et al.
PRL95(2005)232502.

Expected effects of pairing and tensor correlations in ^{11}Li

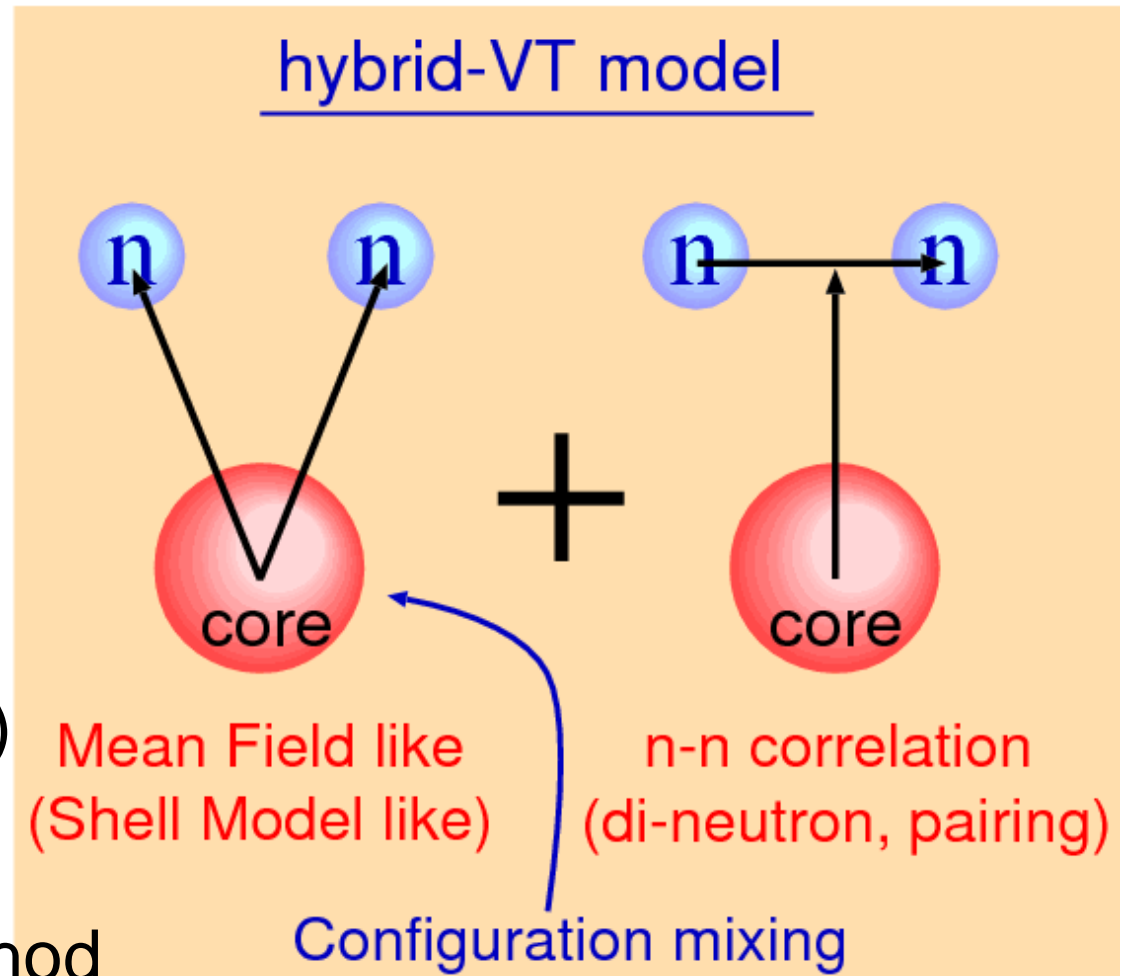


Pairing-blocking :

K.Kato,T.Yamada,K.Ikeda,PTP101('99)119, Masui,S.Aoyama,TM,K.Kato,K.Ikeda,NPA673('00)207.
 TM,S.Aoyama,K.Kato,K.Ikeda,PTP108('02)133, H.Sagawa,B.A.Brown,H.Esbensen,PLB309('93)1.

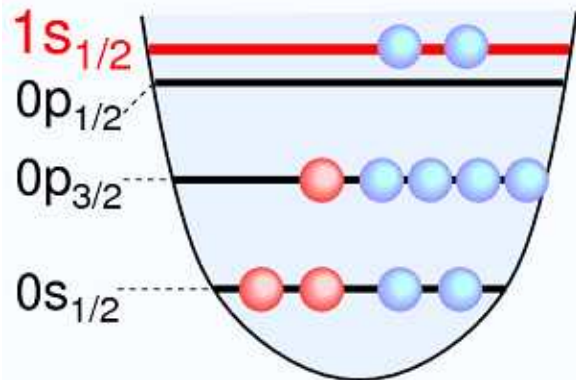
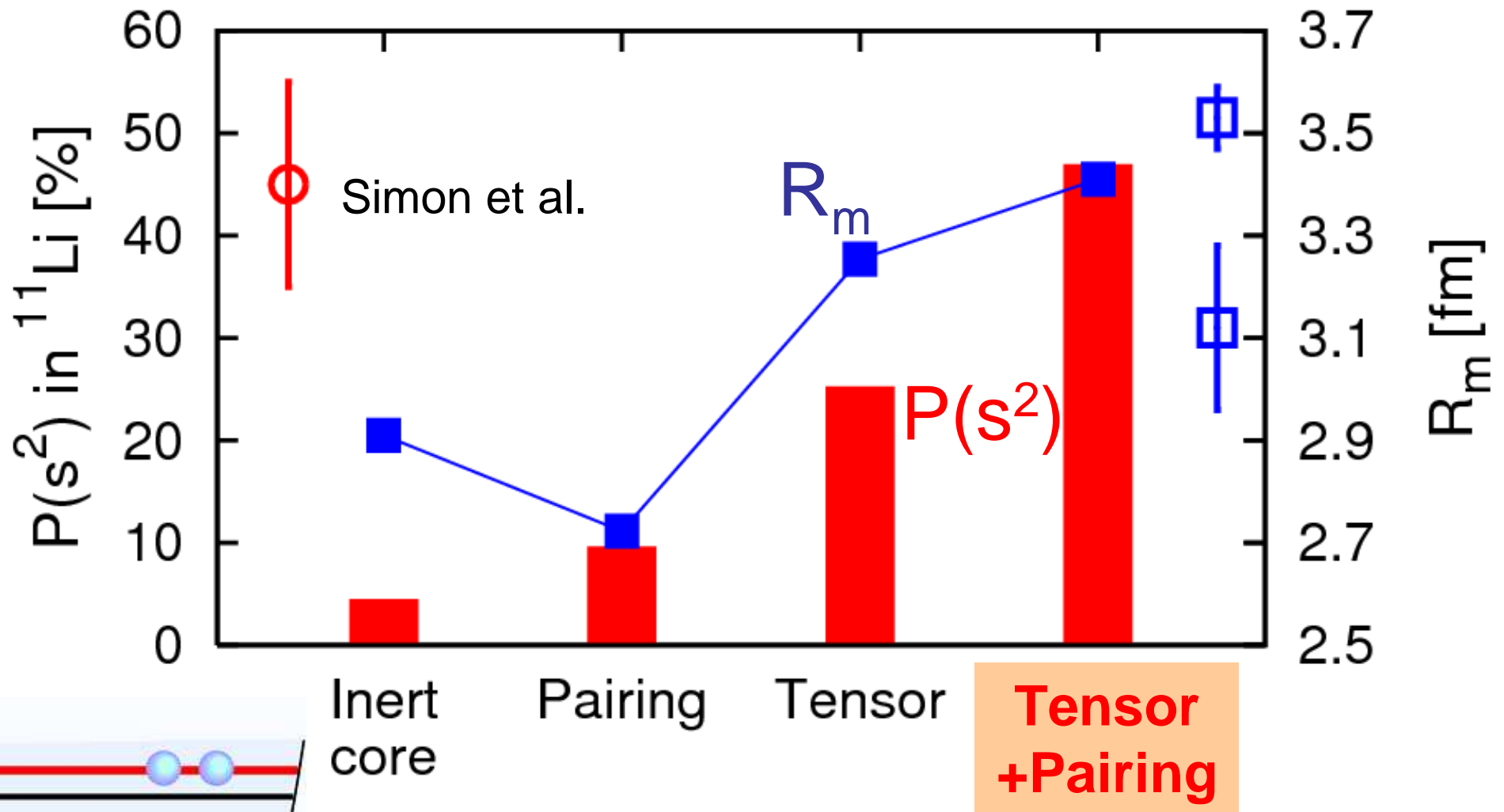
Hamiltonian for ^{11}Li

- $V_{9\text{Li-n}}$: folding potential
 - Same strength for s- and p-waves
 - Adjust to reproduce $S_{2n}=0.31$ MeV
- V_{n-n} : Argonne potential (AV8')
- $2n$: Gaussian expansion method



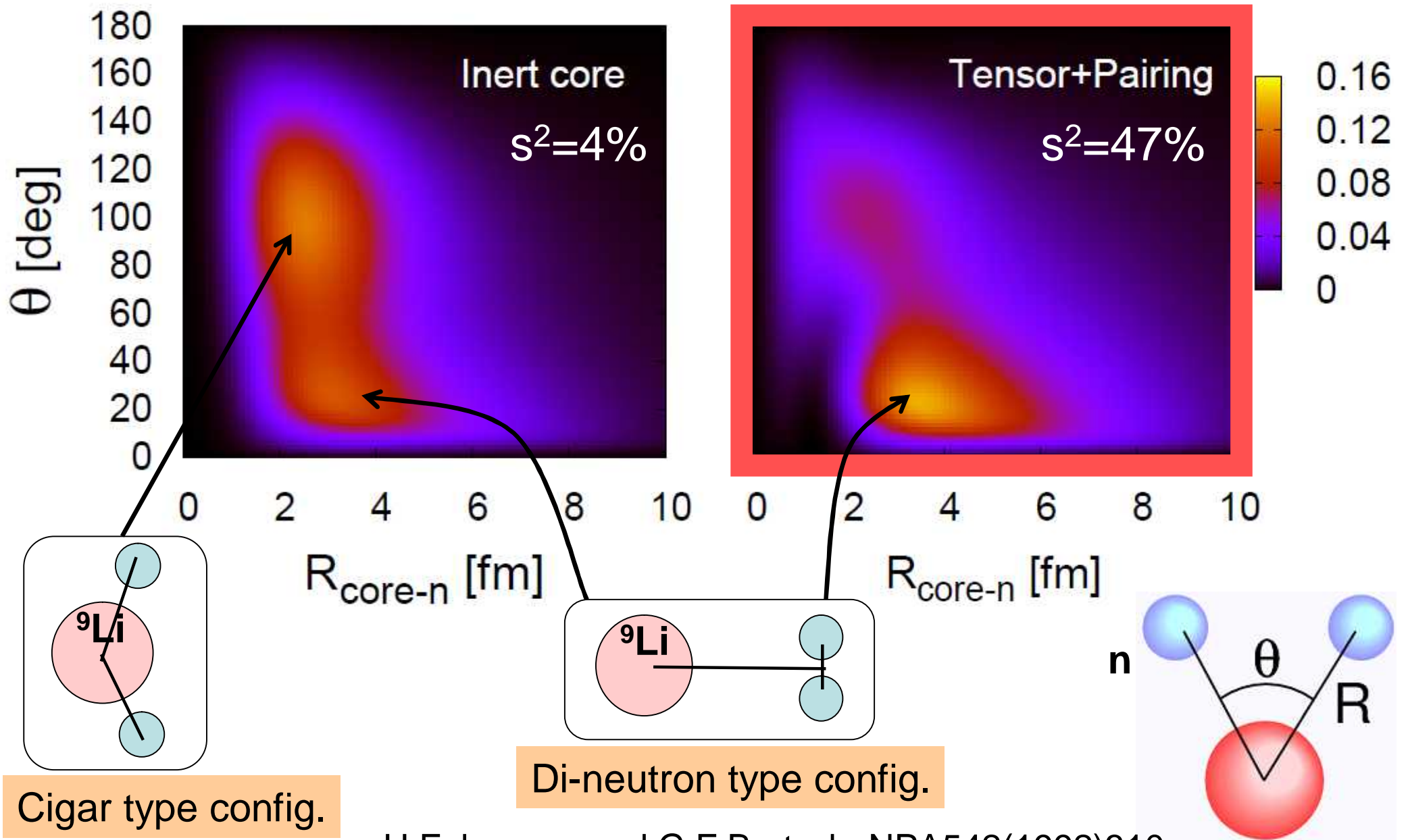
[Ref] TM, S. Aoyama, K. Kato, K. Ikeda, PTP108(2002)

^{11}Li G.S. properties ($S_{2n}=0.31$ MeV)



TM, K.Kato, H.Toki, K.Ikeda, PRC76('07)024305

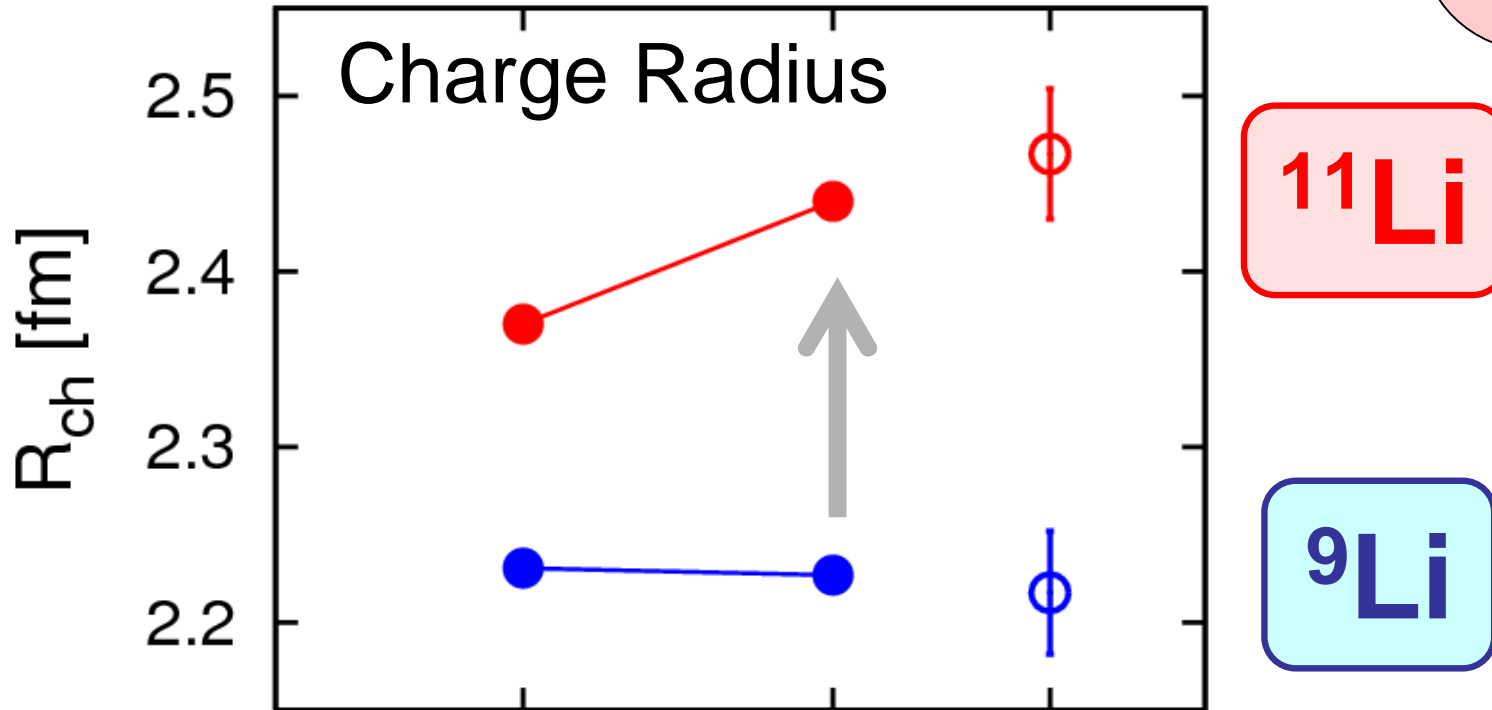
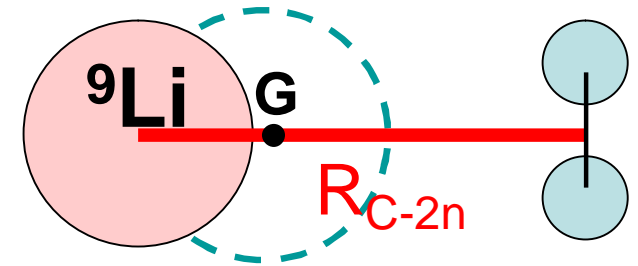
2n correlation density in ^{11}Li



H.Esbensen and G.F.Bertsch, NPA542(1992)310
K. Hagino and H. Sagawa, PRC72(2005)044321

Charge Radii of Li isotopes

$$R_{\text{proton}}^2(^{11}\text{Li}) = R_{\text{proton}}^2(^9\text{Li}) + \left(\frac{2}{11}\right)^2 R_{\text{C-2n}}^2$$



Inert
core

**Tensor
+Pairing**

Expt. (Sanchez et al., PRL96(2006))

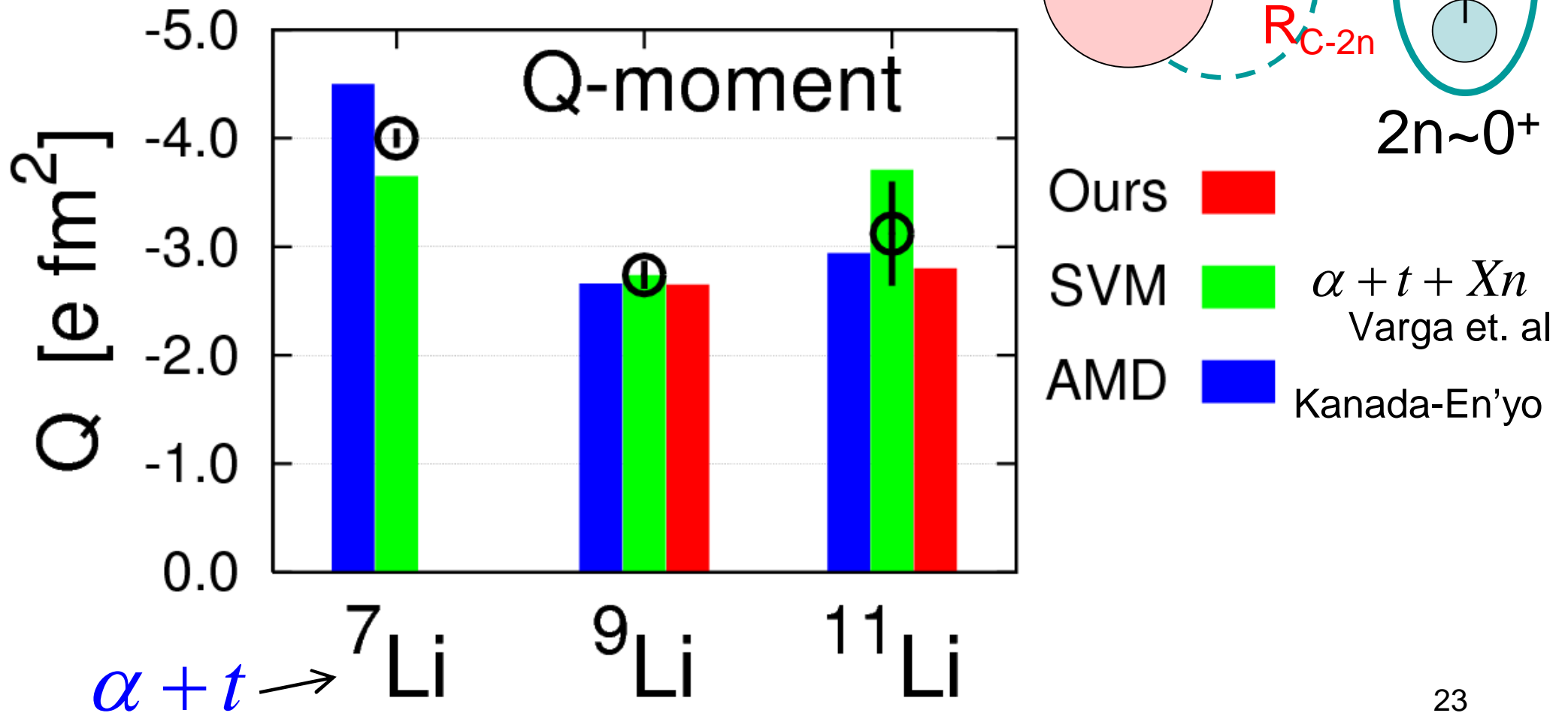
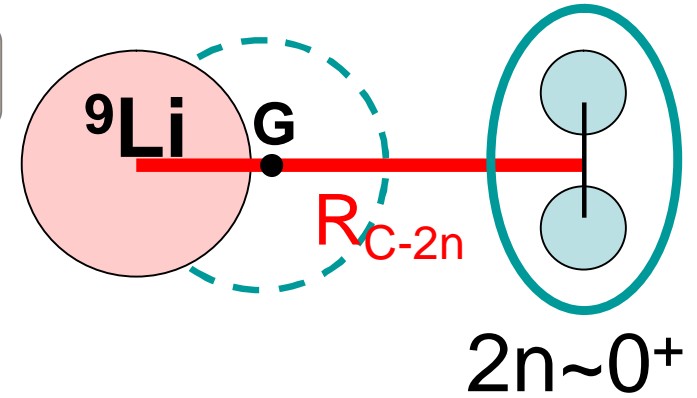
$R_{\text{C-2n}}$	4.67	5.69	[fm]
$P(s^2)$	4	47	%

Q-moment of Li-isotopes

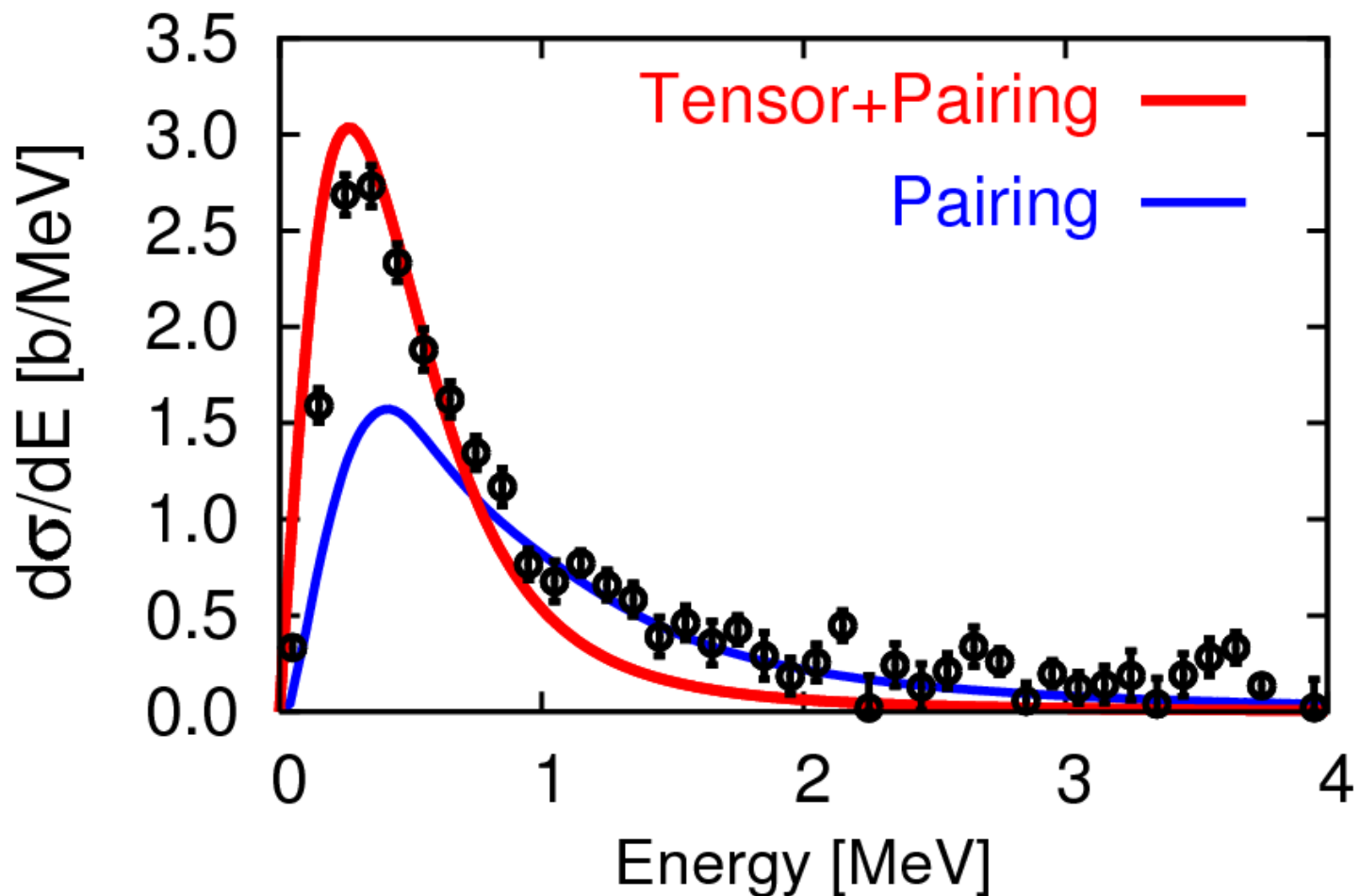
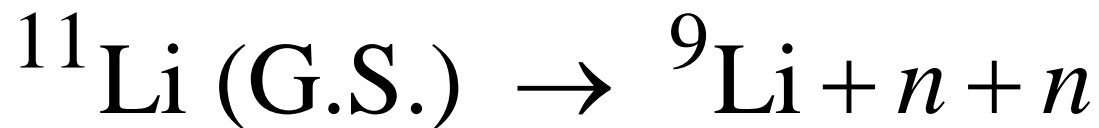
$$Q_2(^{11}\text{Li}) = Q_2(^9\text{Li}) + Q_2(R_{C-2n}) + \alpha \cdot [\mathcal{N}_1(^9\text{Li}), \mathcal{N}_1(R_{C-2n})]_2$$

$$\sim r^2 Y_2(\hat{r})$$

Vanish due to 0+ state of 2n



Coulomb breakup strength of ^{11}Li



No three-body resonance

E1 strength by using the Green's function method
+Complex scaling method
+Equivalent photon method
(TM, Aoyama, Kato, Ikeda, PRC63('01)054313)

- Expt: T. Nakamura et al. , PRL96,252502(2006)
- Energy resolution with $\sqrt{E} = 0.17$ MeV.

Virtual s-wave states in ^{10}Li

- $1s_{1/2}$ virtual state:

$$(0p_{3/2})_{\pi} (1s_{1/2})_{\nu} \rightarrow 1^{-}, 2^{-}$$

a_s : scattering length of $^9\text{Li}+n$

J^{π}	Inert core	Tensor +Pairing
1^{-}	+1.4 fm	-5.6 fm
2^{-}	+0.8 fm	-17.4 fm

T.M. et al., submitted to JPG

Expt. M. Thoennesen et al.,
PRC59 (1999)111.
M. Chartier et al.
PLB510(2001)24.
H.B. Jeppesen et al.
PLB642(2006)449.

$$a_s = -10 \sim -25 \text{ fm}$$

cf. $a_s(nn) : -18.5 \pm 0.5 \text{ fm}$

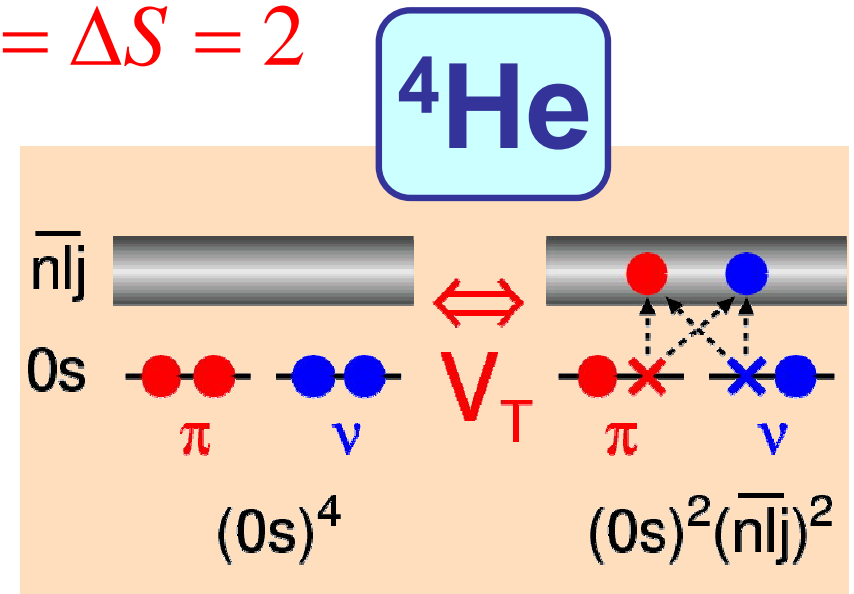
Pauli-blocking naturally describes virtual s-state in ^{10}Li

Tensor & Short-range correlations

- Tensor correlation in TOSM

- $S_{12} \propto [Y_2(\hat{r}), [\vec{\sigma}_1, \vec{\sigma}_2]_2]_0 \rightarrow \Delta L = \Delta S = 2$

- 2p2h mixing optimizing the particle states (radial & high-L)



- Short-range correlation

- Short-range repulsion of the bare NN force in the relative wave function of nuclei

- Unitary Correlation Operator Method (UCOM)

H. Feldmeier, T. Neff, R. Roth, J. Schnack, NPA632(1998)61

T. Neff, H. Feldmeier NPA713(2003)311

Unitary Correlation Operator Method

$$\Psi_{\text{corr.}} = \mathbf{C} \cdot \Phi_{\text{uncorr.}} \leftarrow \text{SM, HF, FMD}$$

short-range correlator

$$\mathbf{C}^\dagger = \mathbf{C}^{-1} \text{ (Unitary trans.)}$$

$$H\Psi = E\Psi \rightarrow \mathbf{C}^\dagger H\mathbf{C}\Phi \equiv \widehat{H}\Phi = E\Phi$$

Bare Hamiltonian

Shift operator depending on the relative distance \mathbf{r}

$$\mathbf{C} = \exp\left(-i \sum_{i < j} g_{ij}\right), \quad g_{ij} = \frac{1}{2} \left\{ p_r s(r_{ij}) + s(r_{ij}) p_r \right\} \quad \vec{p} = \vec{p}_r + \vec{p}_\Omega$$

$$g_{ij} = g_{ij}^\dagger : \text{Hermitian generator} \quad R'_+(r) = \frac{s(R_+(r))}{s(r)}$$

Short-range correlator : C

$C : r \rightarrow R_+(r)$ for Hamiltonian,
 $r \rightarrow R_-(r)$ for relative wave func.

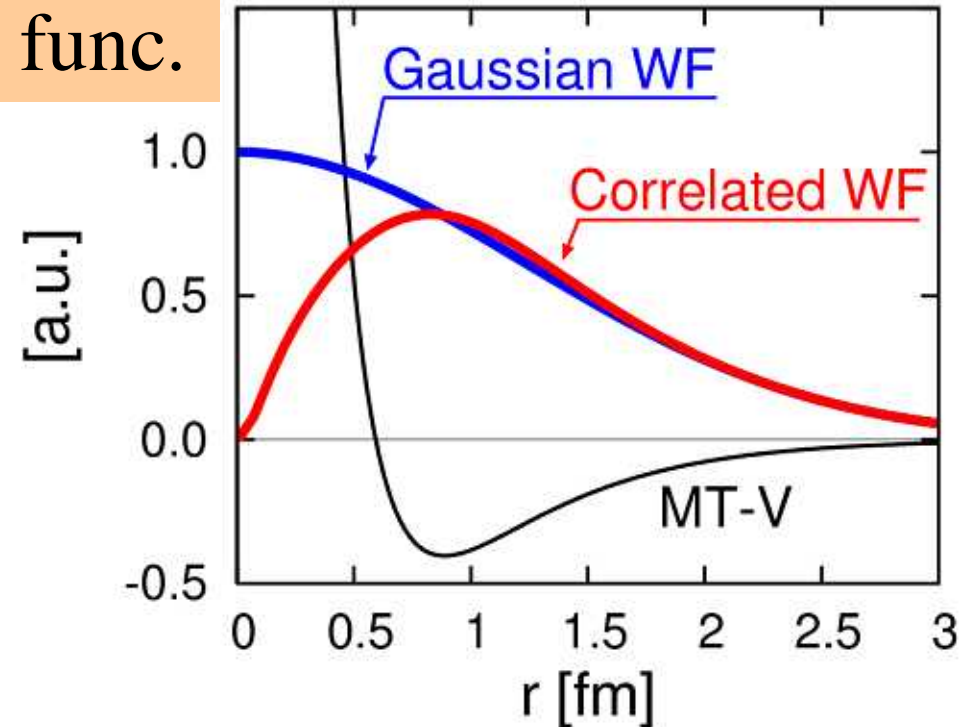
$$C^\dagger r C = R_+(r)$$

$$R_-(R_+(r)) = r$$

Hamiltonian in UCOM

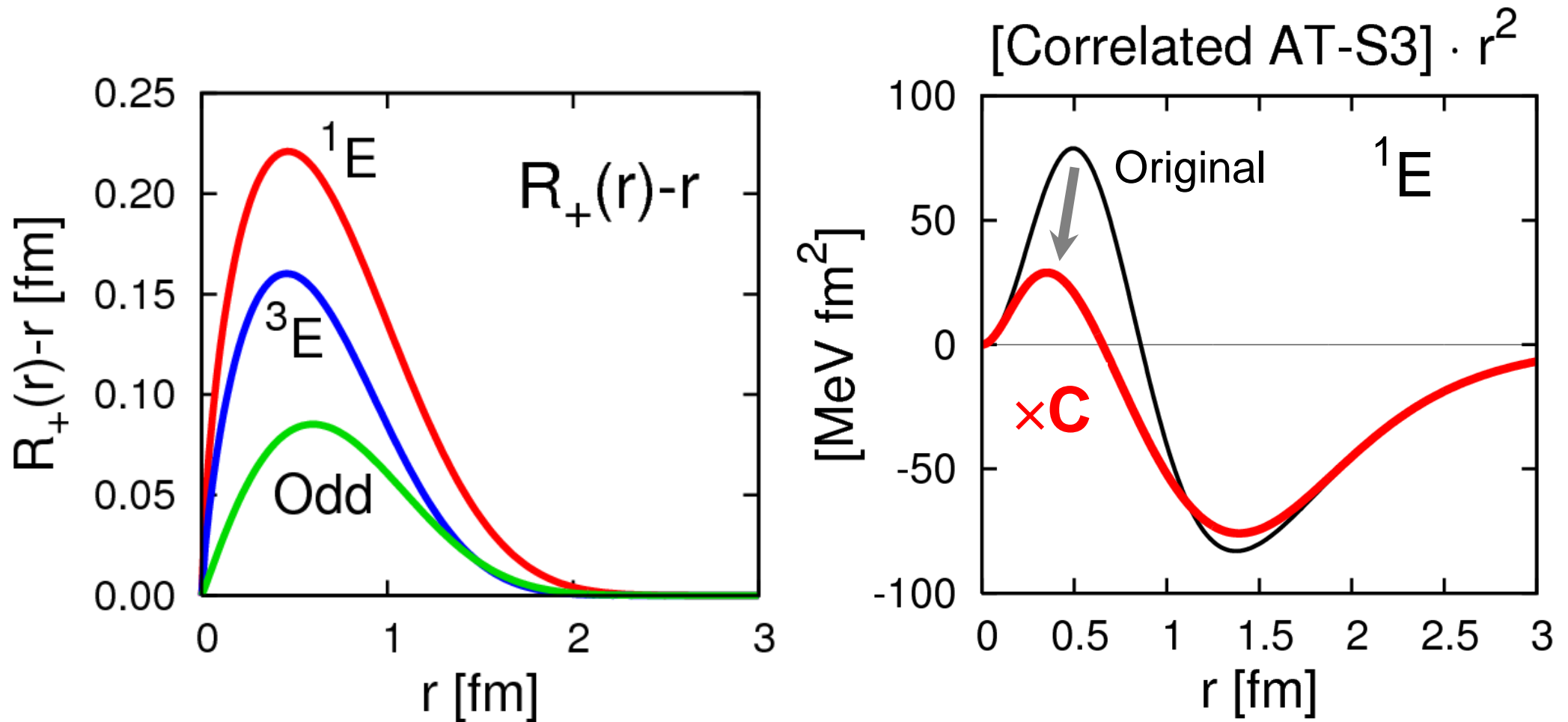
$$C^\dagger H C = \hat{H} = \hat{T} + \hat{V}$$

$$\hat{T} \simeq T + \Delta T, \quad \Delta T = \sum_{i < j} u_{ij}^2 \quad \hat{V} \simeq \sum_{i < j} v(R_+(r_{ij}))$$



2-body approximation in the cluster expansion of operator

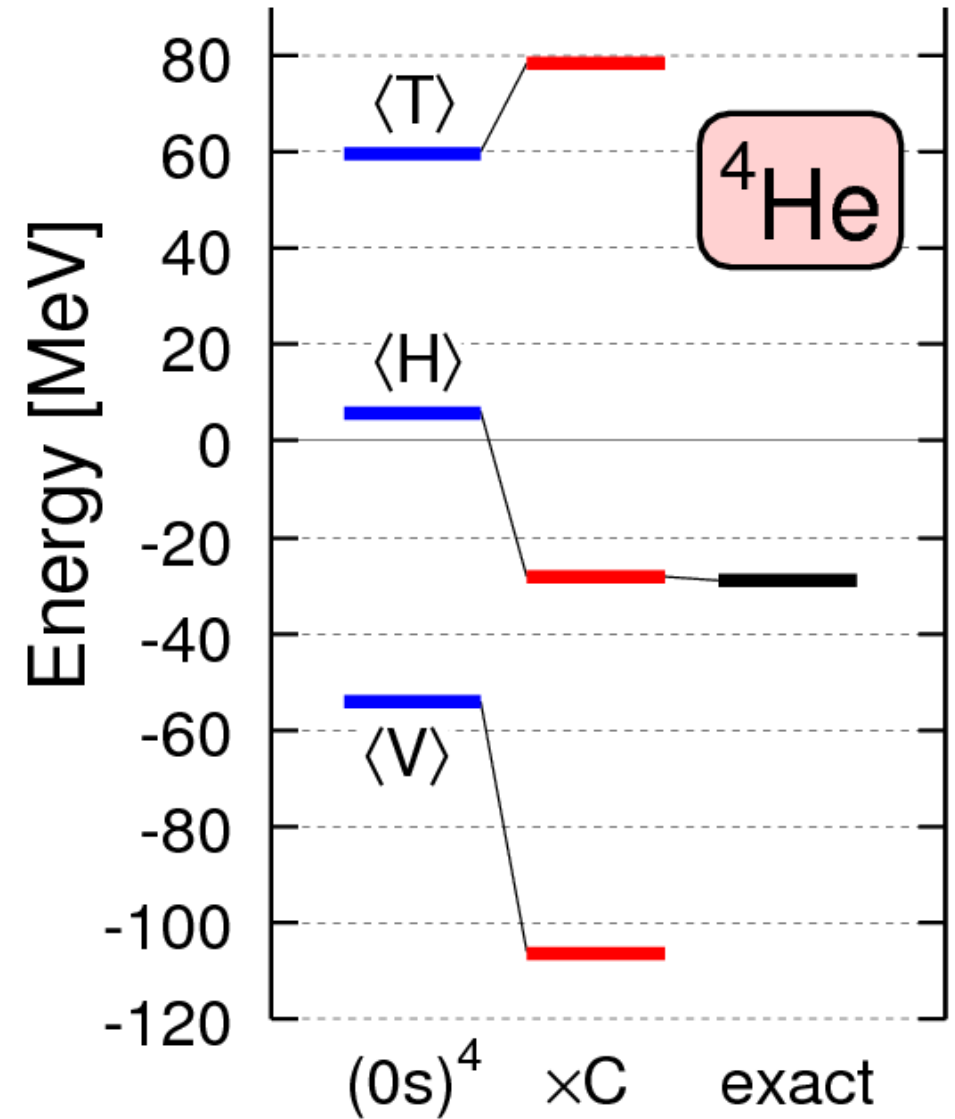
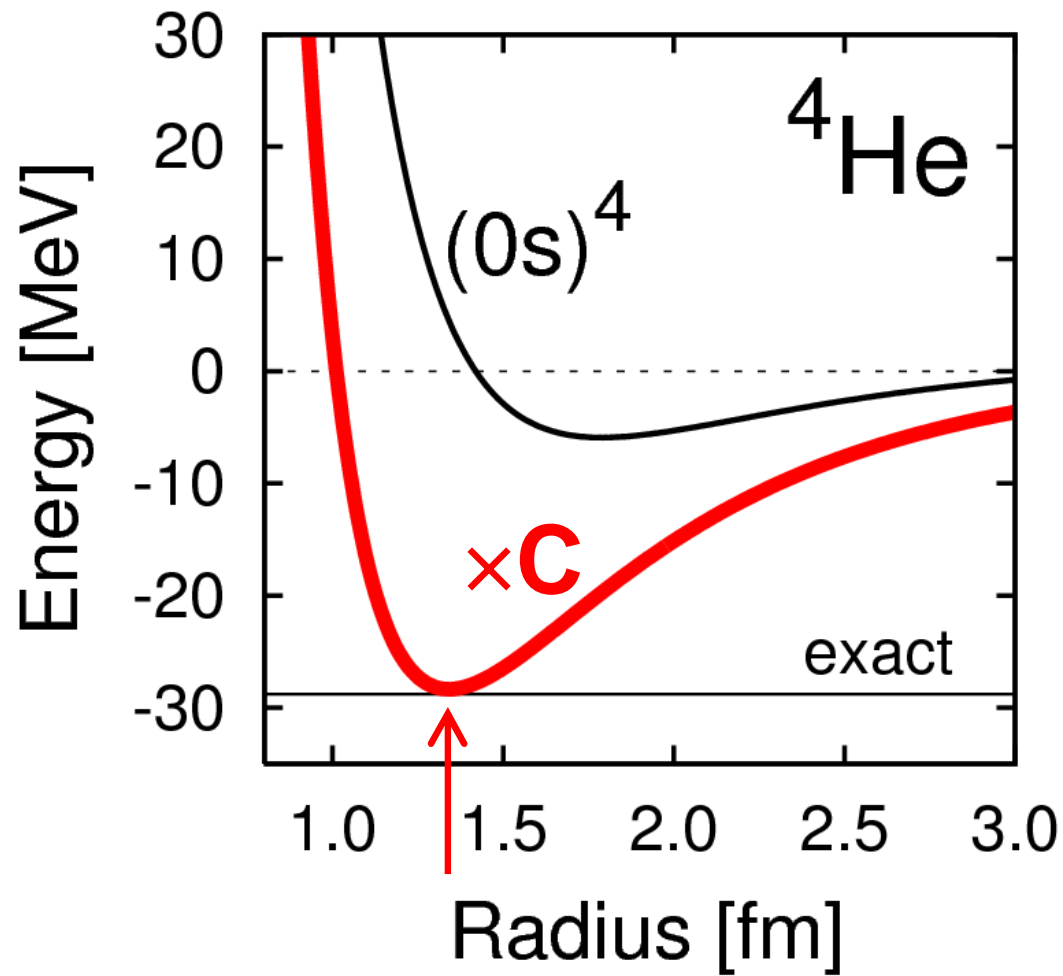
Form of R_+ in UCOM



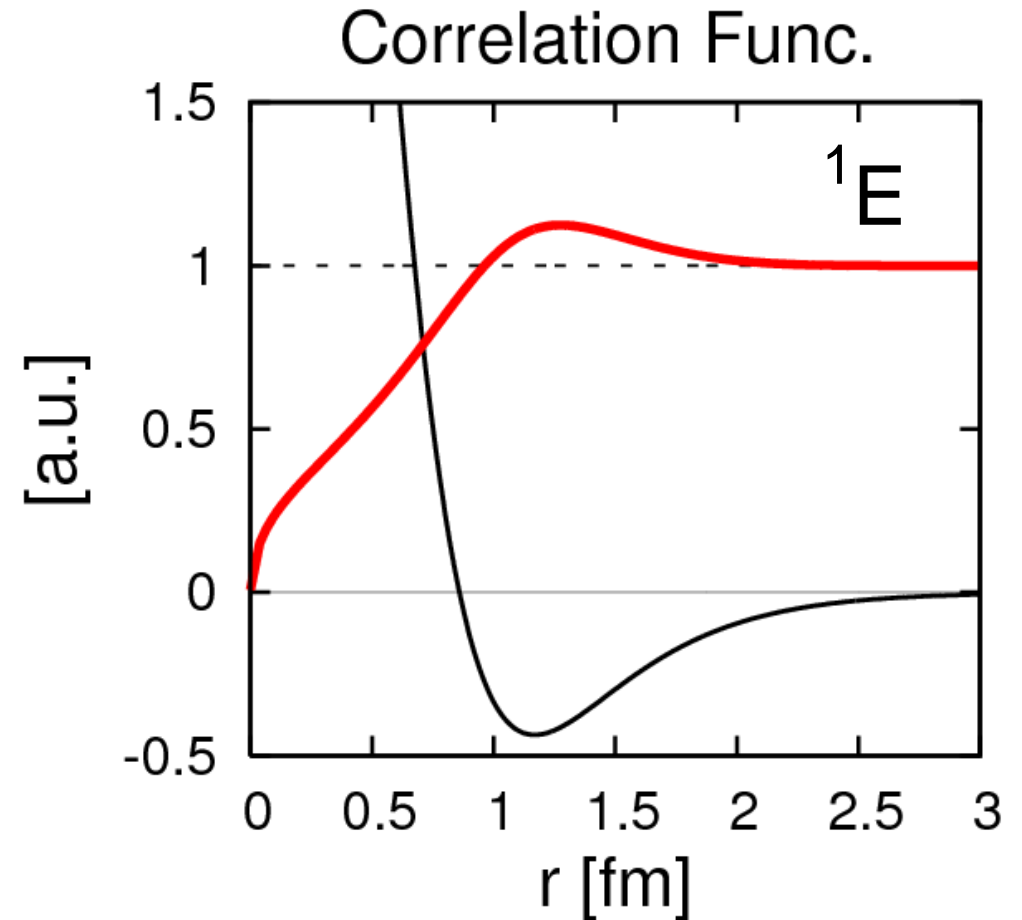
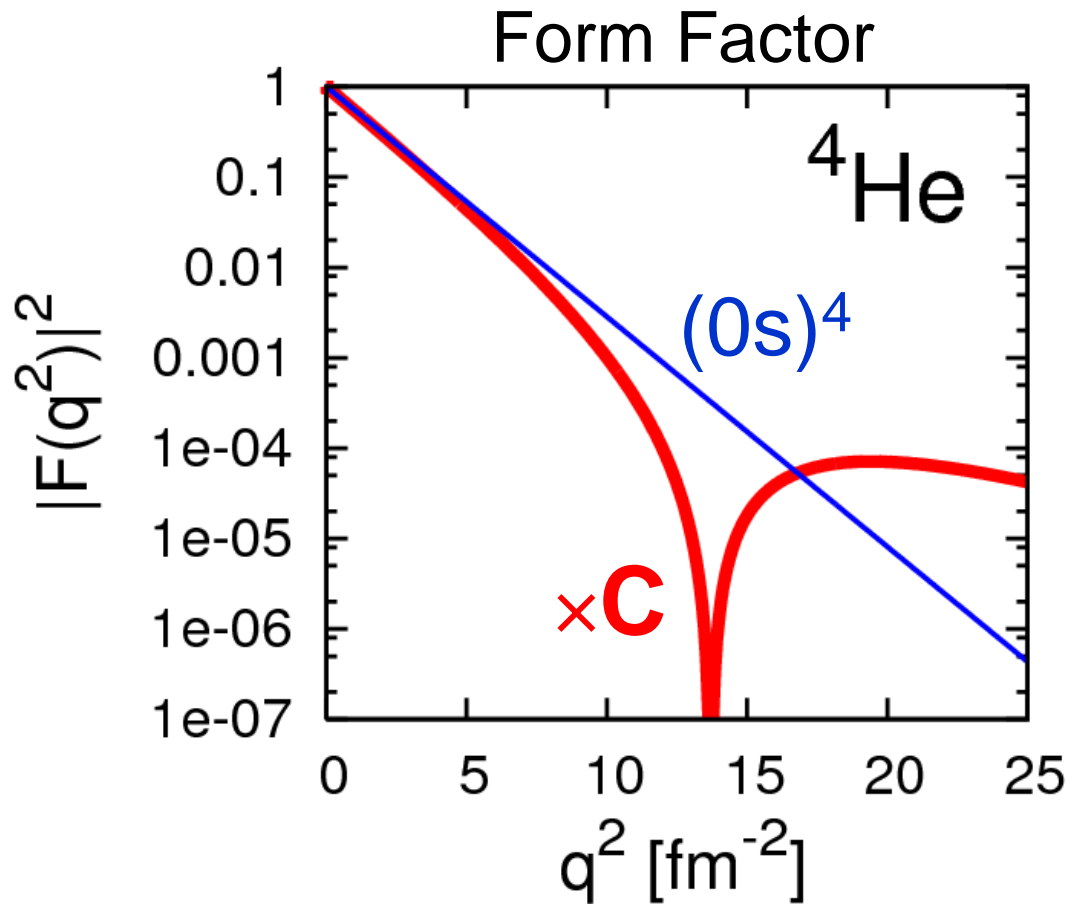
Functional form given by referring to the Deuteron's exact case

Afnan-Tang : central only
about **1 GeV repulsion**

^4He with UCOM (Afnan-Tang)

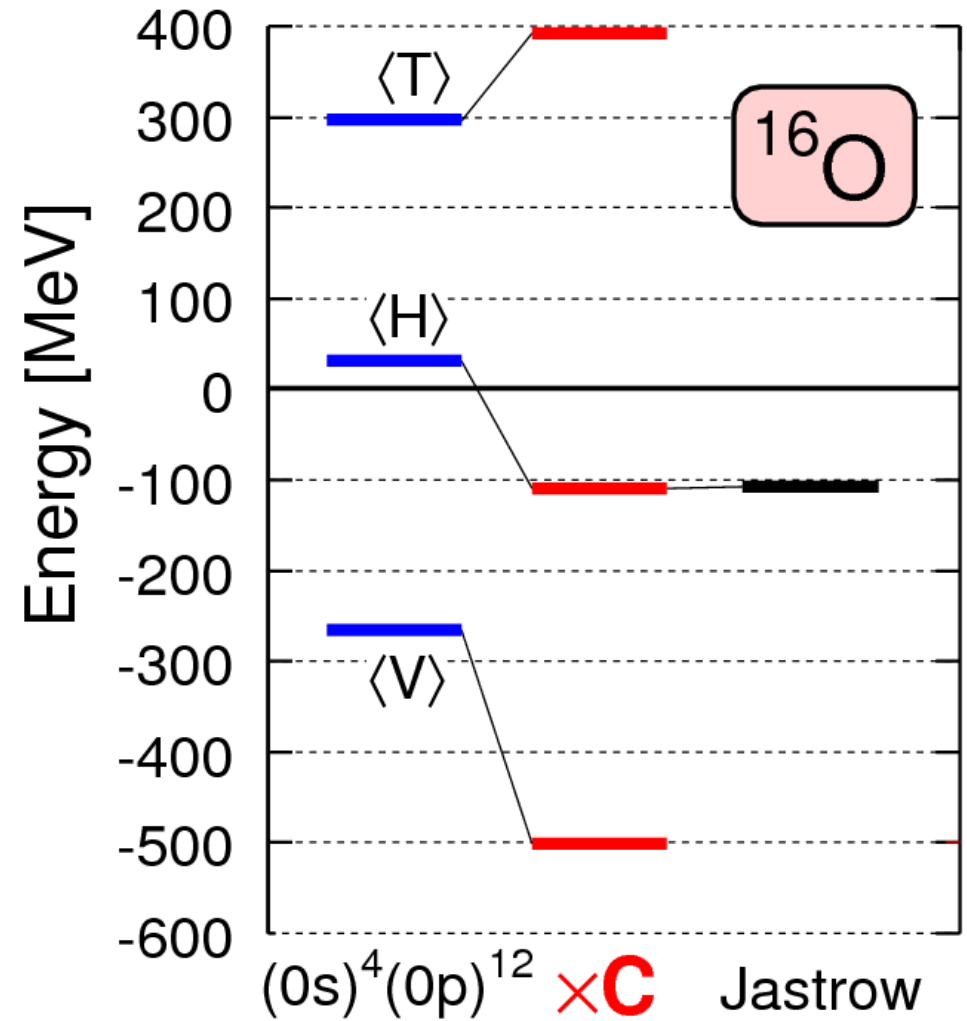
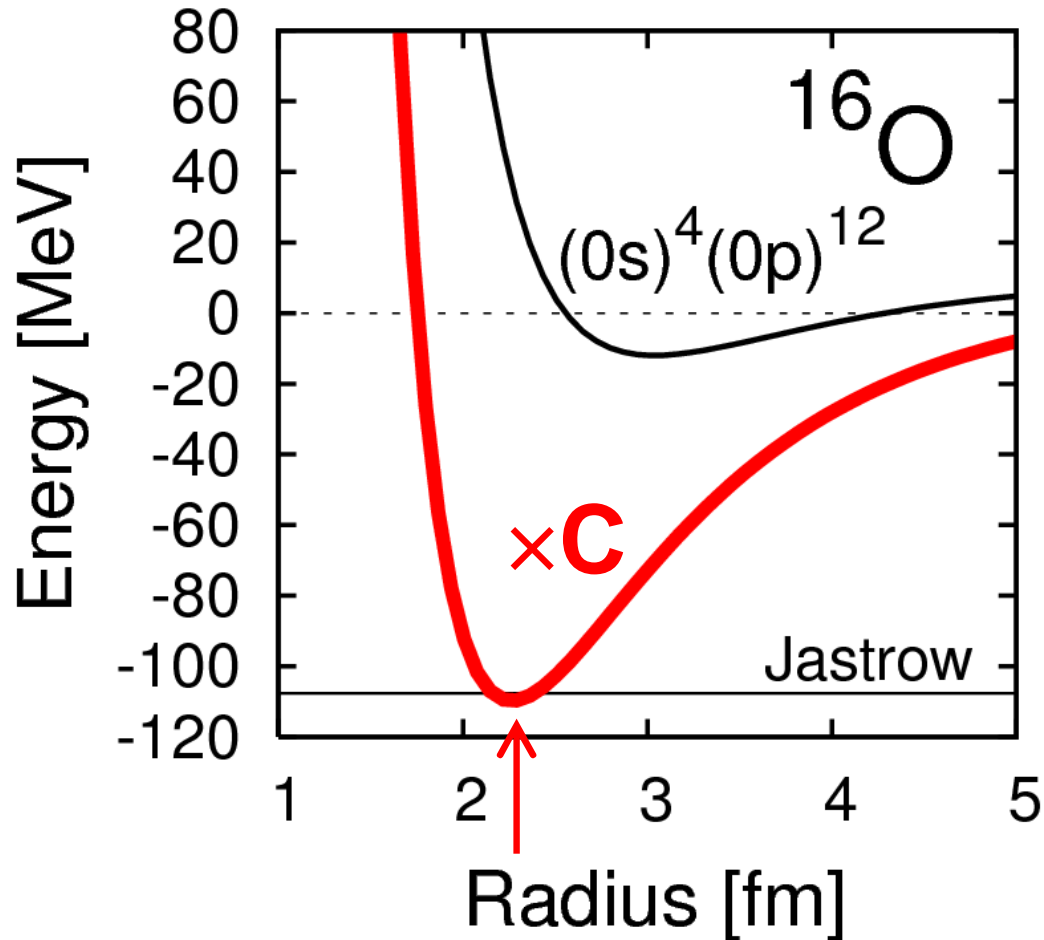


Charge form factor and Corr. Func.

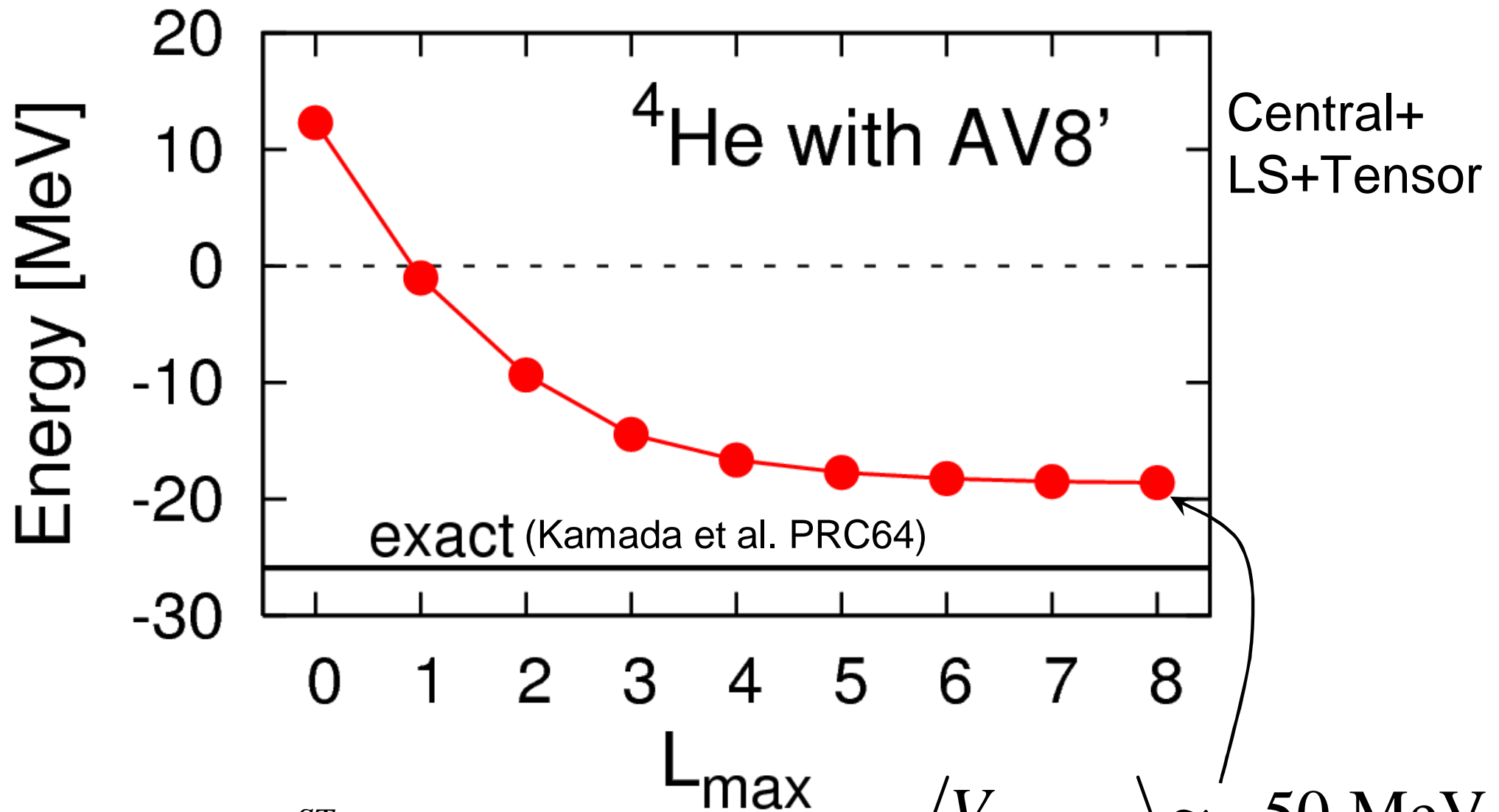


$$P[(0s)^4] = 0.95$$

^{16}O with UCOM (Afnan-Tang)



^4He in TOSM+UCOM



Choice of $R_+^{ST}(r)$

Summary

- Tensor correlation in nuclei.
 - Tensor-optimized shell model (TOSM).
 - He isotopes : LS splitting
 - Li isotopes: Magic number breaking and halo
- Short-range correlation
 - Unitary Correlation Operator Method (UCOM).
- In **TOSM+UCOM**, we can study the nuclear structure starting from the bare interaction.