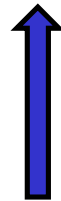
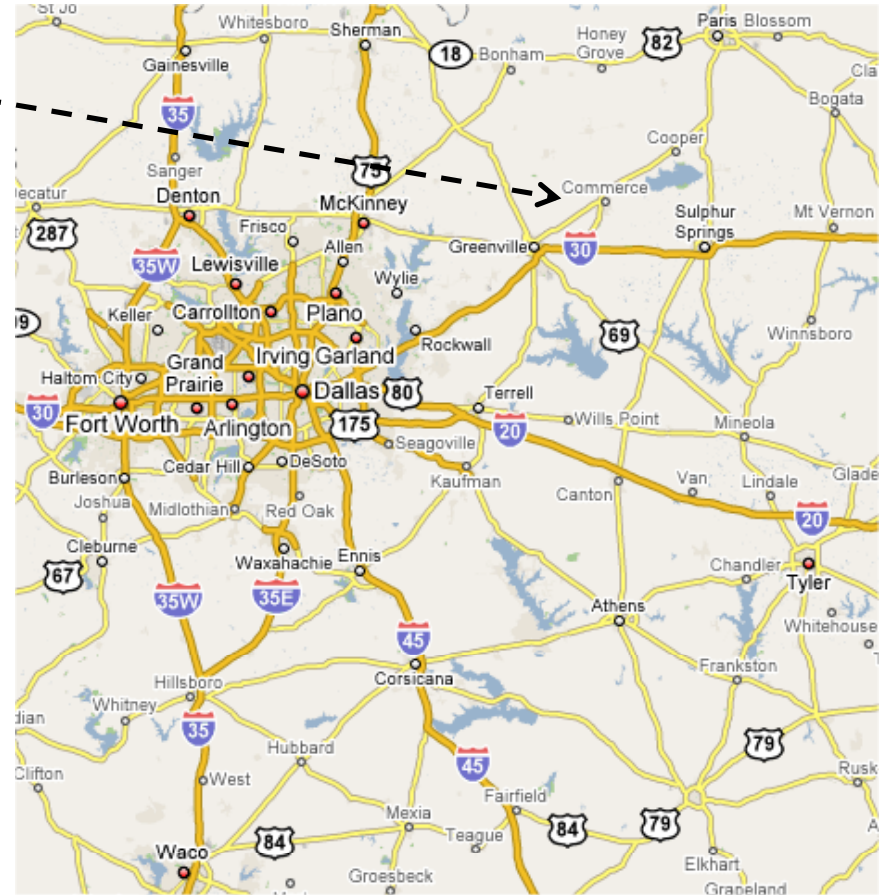
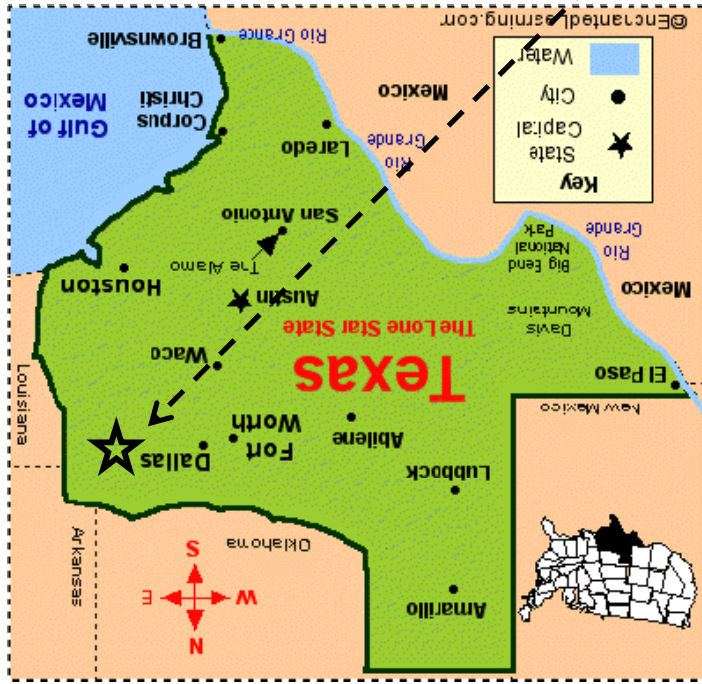


# Benchmark calculations of nuclear mass tables

C.A. Bertulani (Texas A&M - Commerce)



As seen from Seattle



Physics – TAMU-Commerce

# Mass tables with HFODD (J. Dobaczewski)

<http://www.fuw.edu.pl/~dobaczew/hfodd/hfodd.html>

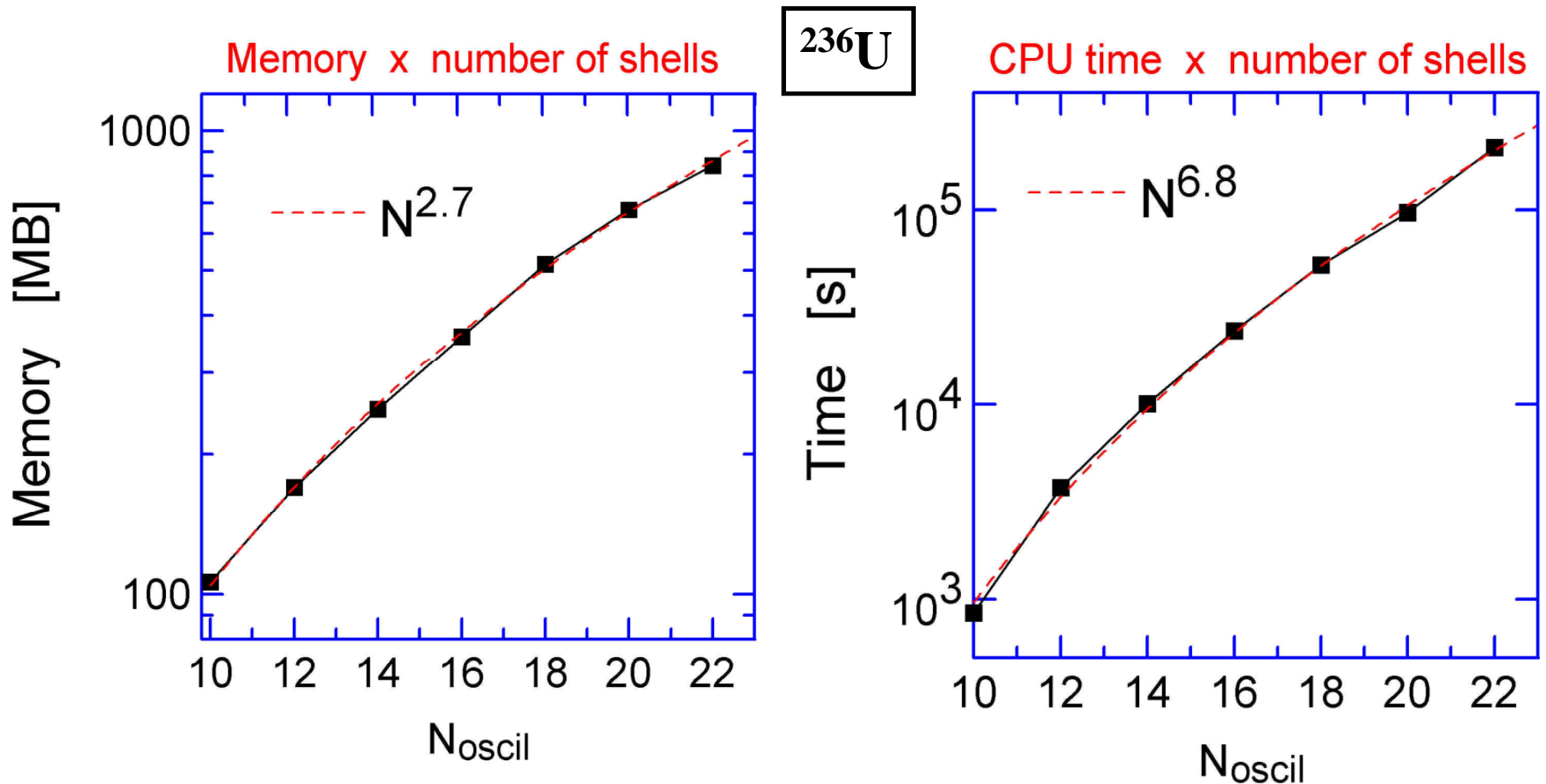
- 1 – Code has ~ 60,000 lines.
- 2 - HF $\bar{B}$ , h.o. expansion, breaks all self-consistent symmetries, and t-symmetry.
- 3 - Includes t-odd terms in Skyrme functional.
- 4 – Large continuum space included
- 5 - Blocking and Lipkin-Nogami (LN) implemented recently by J. Dobaczewski.

Blocking still has convergence problems.

- 6 – People involved: Nazarewicz, Stoitsov, Schunck (ORNL), Dobaczewski (Poland), More, Sarich (Argonne), Bertulani (Tamu-Commerce)

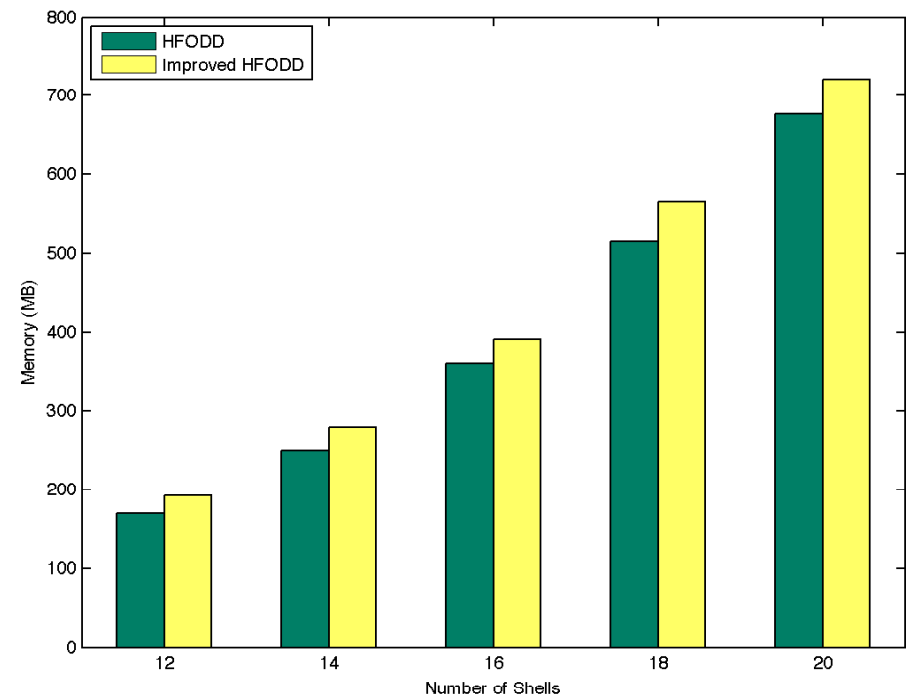
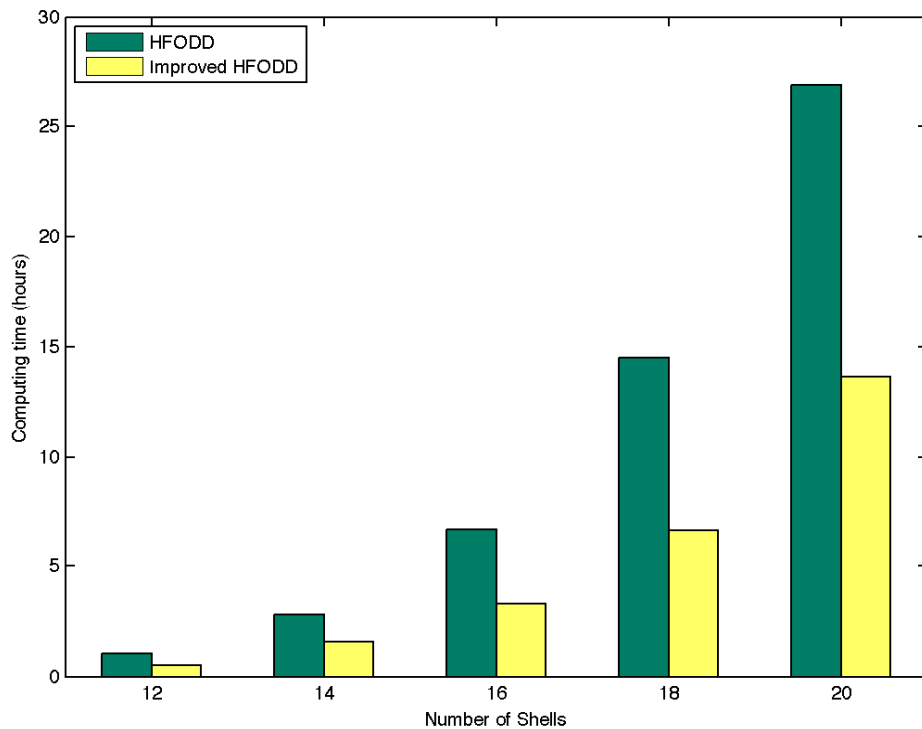
# Warming up with HFODD

- 1 - Benchmarking Jan-March/2007 version, HFODD vs. 2.24 - 2.27
- 2 - ~ 55 cases (nuclei, different parameters)
- 3 - Tests done at INT/Washington workstations and Jaguar/ORNL (on one single processor). Both ~ 3 GHz clock speed.
- 4 - On Jaguar (5 GFlops/s): HFODD = 1.25 GFlops/s = 25% capacity



# Improvements by **Jason Sarich**, incorporated in code by **Jacek Dobaczewski**

- 1 - Loops of matrix multiplications replaced by BLAS and LAPACK routines
- 2 - Similarly for eigenvalue problem
- 3 - Presently: routines incorporated in a standalone code (portable), or links to BLAS and LAPACK (faster, platform optimized)



Figures from **Jorge More's** presentation at SciDAC meeting, June/2007

Numerous benchmarks done for the SciDAC project

# Goals for HFODD

- 1 - Present version 2.31 (08/2007) include optimizations (**Sarich+Dobaczewski**), blocking and LN treatment of pairing (**Dobaczewski+Stoitsov**)
- 2 - Benchmarks with version 2.31 show similar improvements in speed.
- 3 - **Schunck + Sarich + Stoitsov**: N-Z walk on Jaguar
- 4 - UT/ORNL DFT-group + Texas (Bertulani): data analysis (chi-square's) and graphics interface.

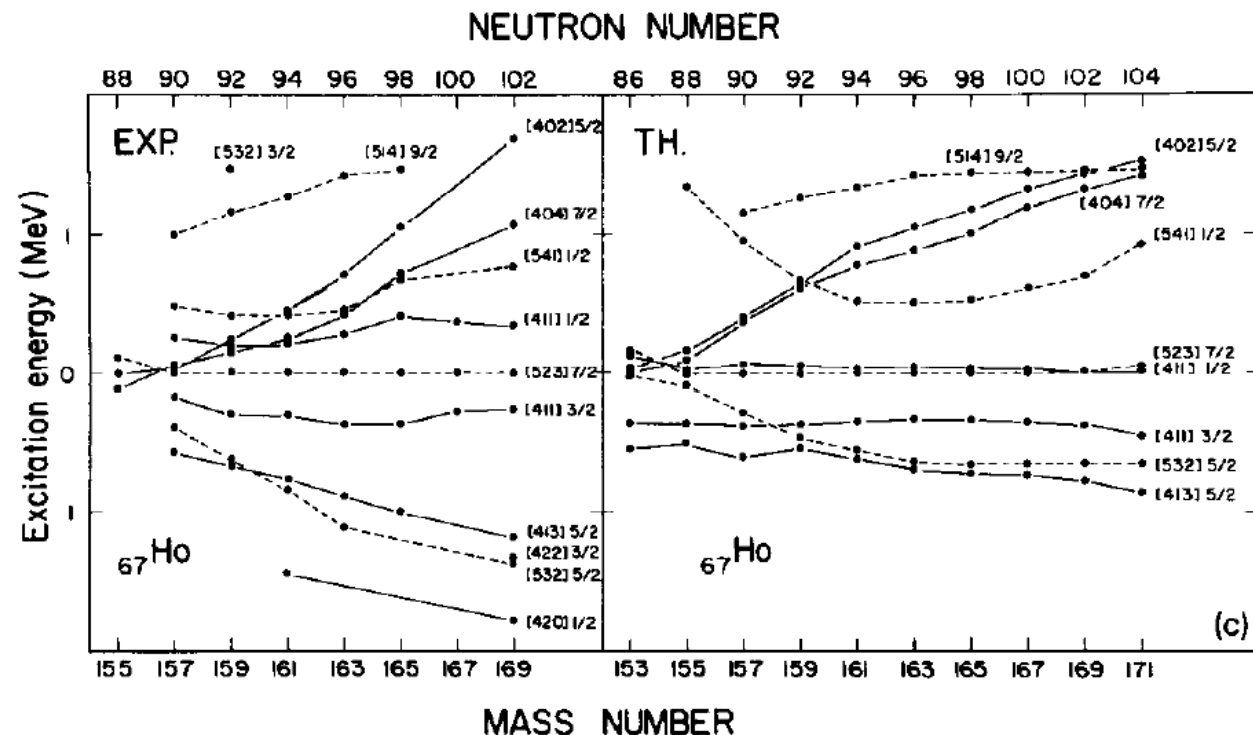
5 - Goals for 2008, using 3+4:

• Analysis of equilibrium deformations and excitation energies for odd-nuclei:

e.g., improving upon Nazarewicz, Riley, Garret, NPA 512 (1990) 61

• Preliminary mass tables for odd-nuclei:

e.g., improving upon Dobaczewski, Stoitsov, Nazarewicz, nucl-th/0404077



# Mass tables with EV8-ODD

**EV8 (P. Bonche, H. Flocard and P.H. Heenen, CPC 171 (2005) 49)**

1 – code has only 6,500 lines

2 - HF+BCS, 3-d coordinate mesh, axial symmetry, small continuum space

## **EV8 ODD:**

3 – Blocking implemented recently by Bertsch.

4 - N-Z walker by Bertulani.

# Binding energy residuals

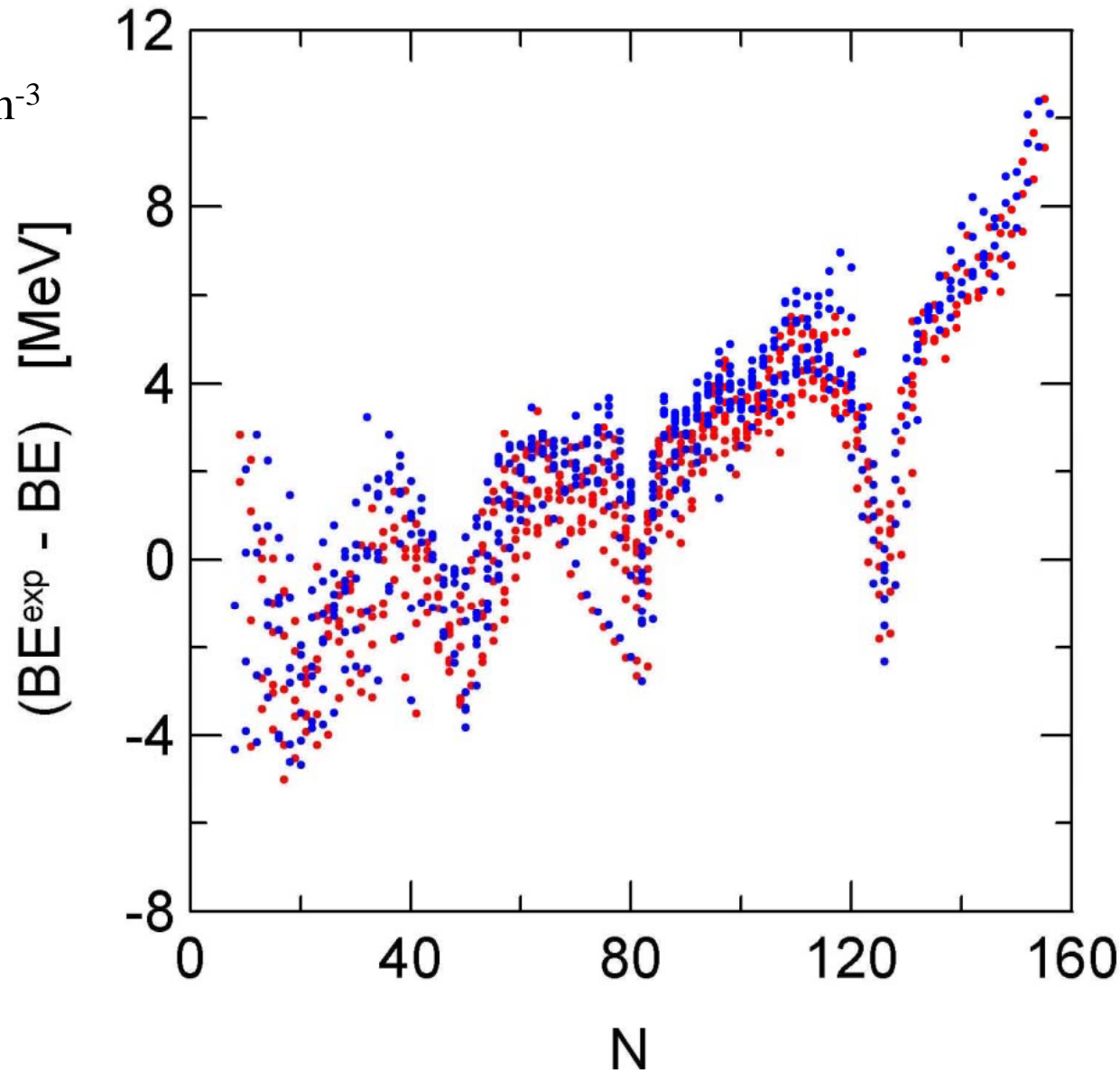
Example: Skyrme = SLy4

$$V_{\text{pairing}} = g \cdot \delta(r_{12}) \cdot [1 - \rho(r)/\alpha]$$

Surface pairing:

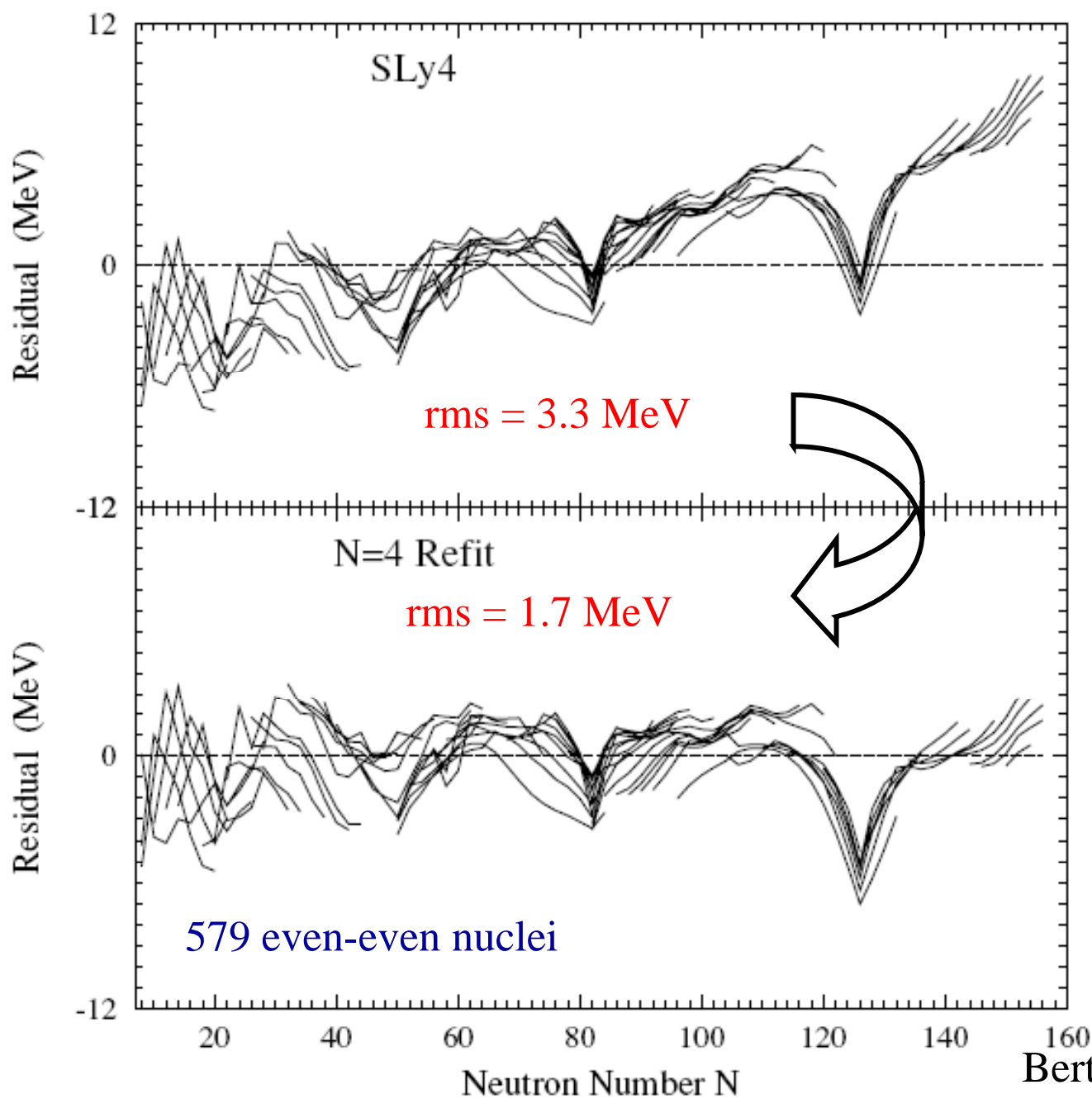
$$g_n = g_p = 1000 \text{ MeV fm}^3, \alpha = 0.16 \text{ fm}^{-3}$$

- N-even, 521 nuclei, rms = 2.83 MeV
- N-odd, 498 nuclei, rms = 2.71 MeV





# Goal: reduce rms by refitting interactions

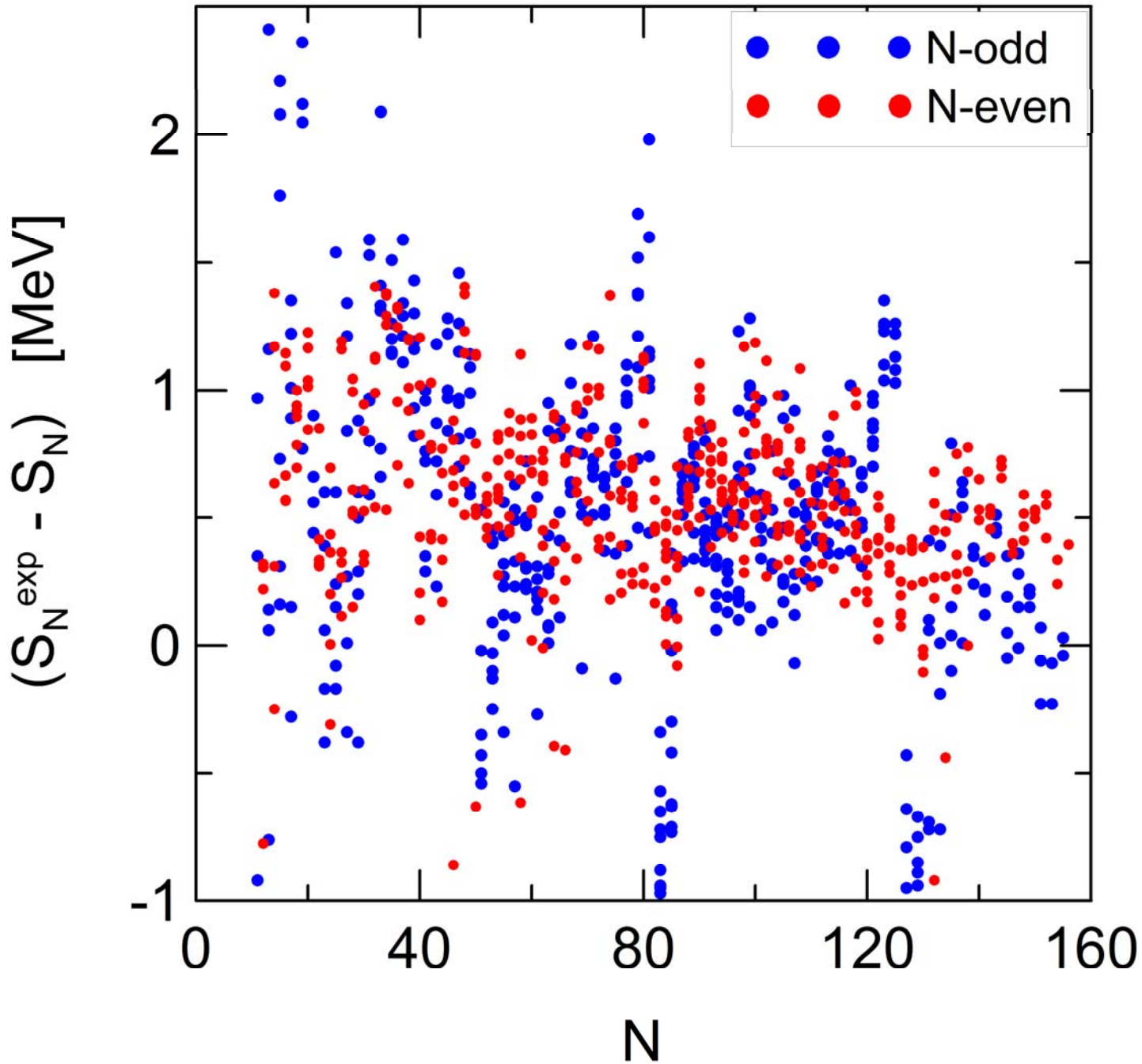


Bertsch, Sabbey, Uusnaki,  
PRC 71, 054311 (2005)

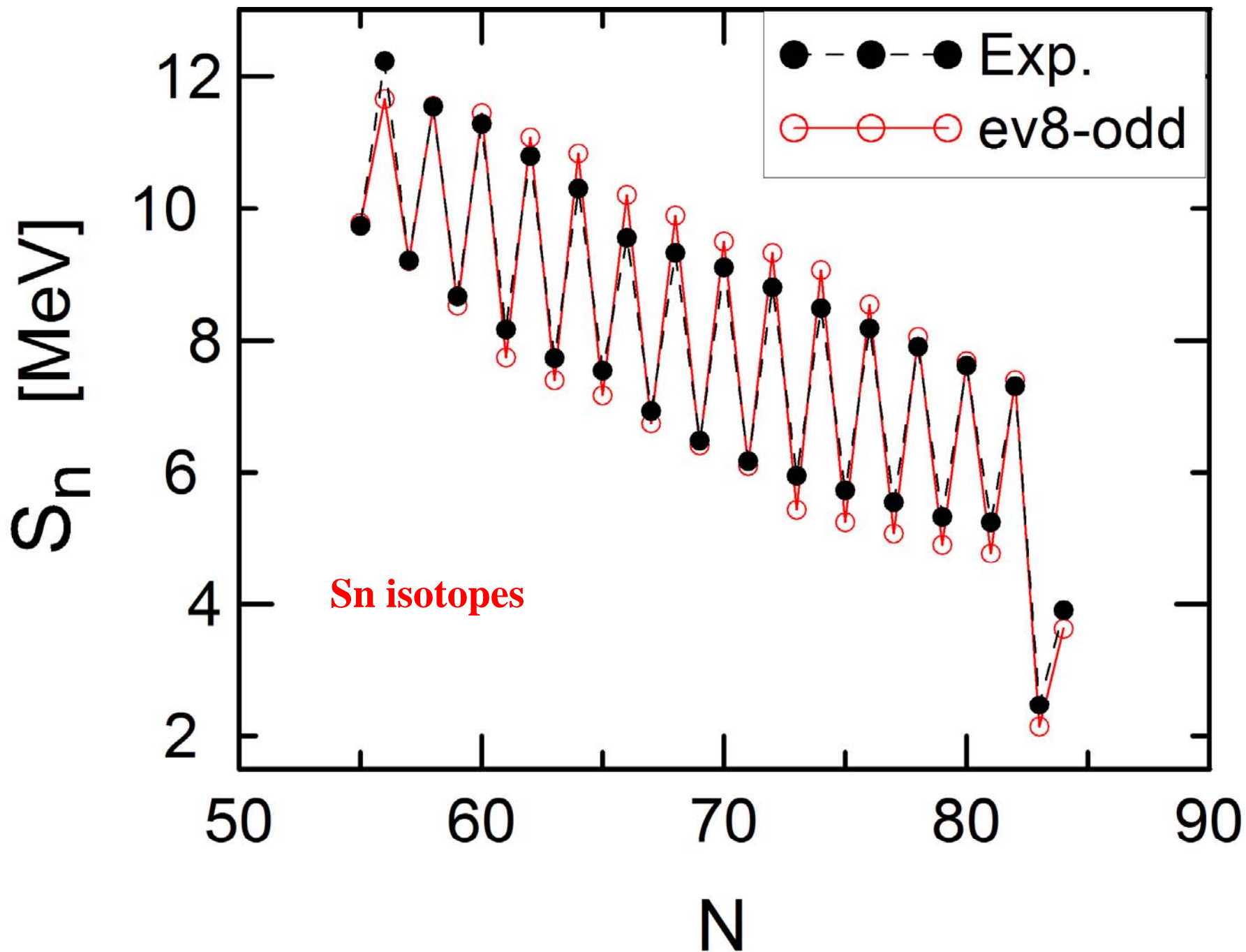


# Separation energy residuals

$$S(N,Z) = M(N-1,Z) + M_n - M(N, Z)$$



## Odd-even staggering



# Odd-even staggering and pairing strength

3-point filter:  $\Delta = 1/2 \cdot (-1)^N [S(N,Z) - S(N-1, Z)] \cong 1/2 \cdot (-1)^N \partial^2 B / \partial^2 N$   
 $N = \text{odd(o), even(e)}$

Mechanism	$\Delta_o^{(3)}$	$\Delta_e^{(3)}$
Single-particle	0	$(e_i - e_{i-1})/2$
BCS correlation	$\Delta_{BCS}$	$\Delta_{BCS}$
T-odd pp	$-v_{i\bar{i},i\bar{i}}/2$	$\bar{v} - v_{i\bar{i},i\bar{i}}/2$
T-odd DFT		
T-even polarization	$-e_{cp}$	0

Table by Bertsch

Satula, Dobaczewski, Nazarewicz,  
PRL.81,3599 (1998).

Rutz, Bender, Reinhard, Maruhn,  
PL B468, 1 (1999).

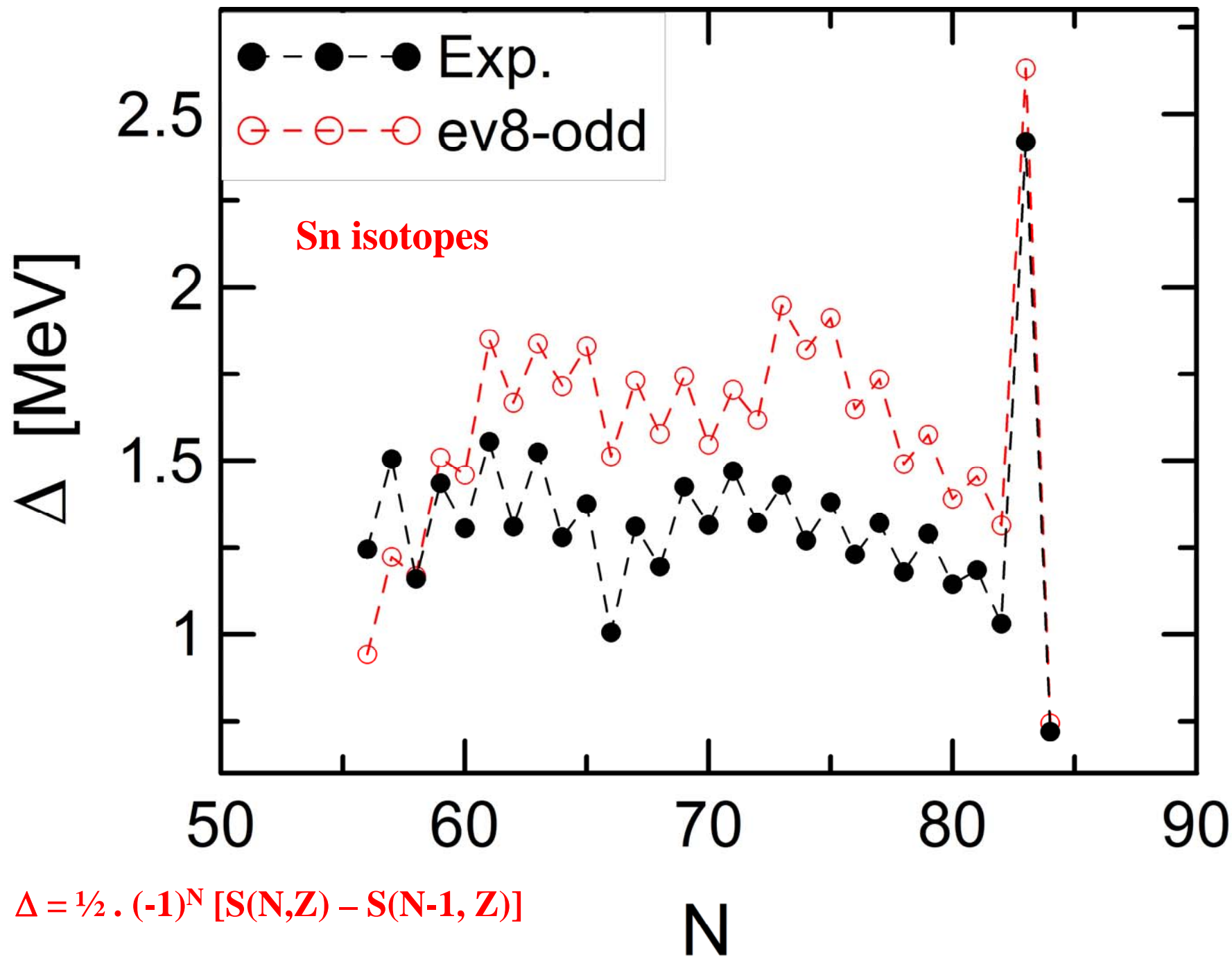
$$B = E_{sp} - \tilde{E}_{sp} + E_{macro}$$

$$E_{sp} = \sum_k e_k$$

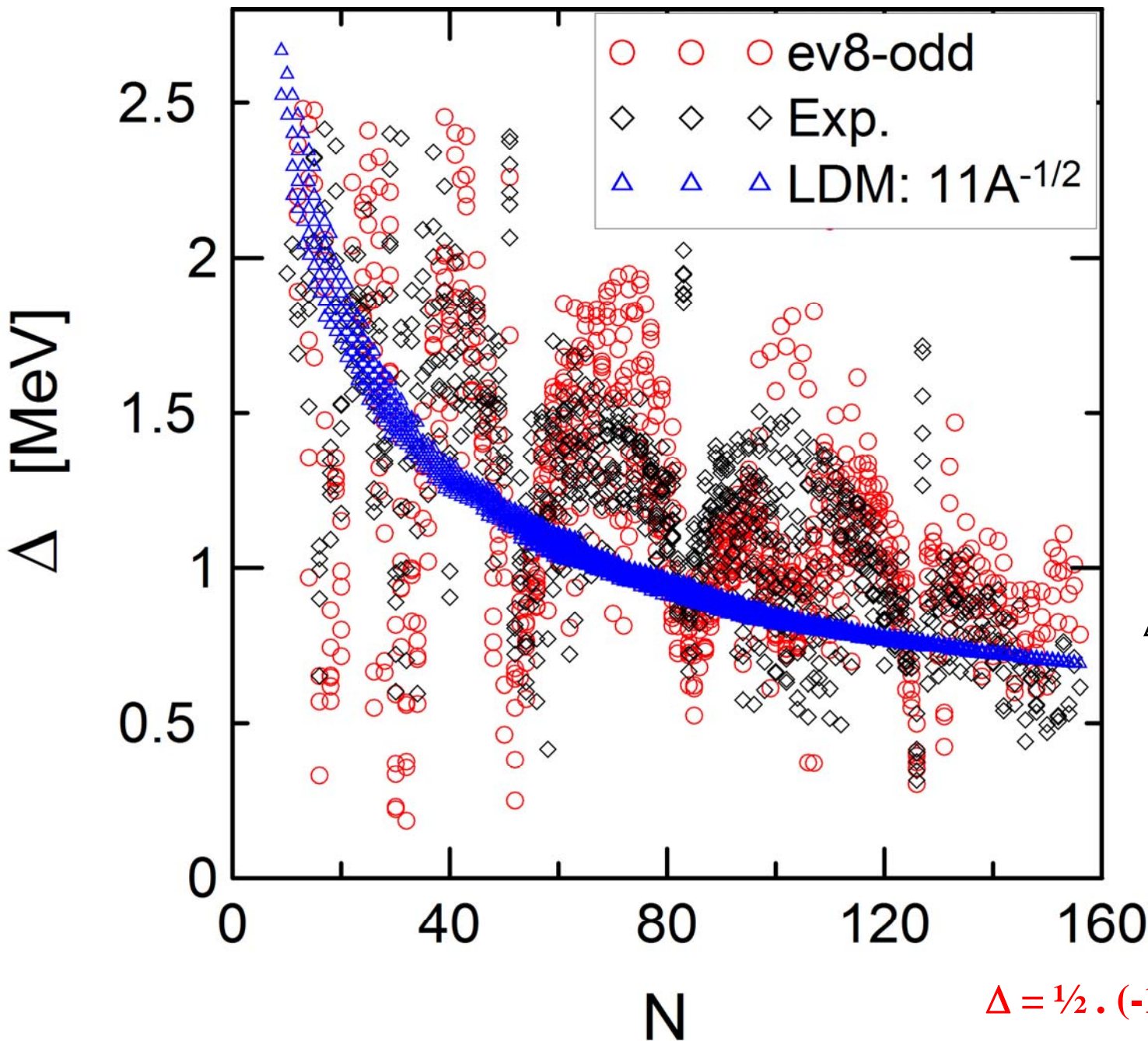
$$\Delta^{(o)}_{sp} \approx 0, \quad \Delta^{(e)}_{sp} \approx \frac{e_n - e_{n-1}}{2}$$

$$\partial^2 B_{\tilde{E}_{sp}} / \partial N^2 \approx \partial^2 B_{macro} / \partial N^2$$

## Odd-even staggering from ev8-odd



# Odd-even staggering with 967 masses!



From even-even  
to even-odd and  
odd-odd  
(absolute value):

$$\Delta_{LDM} = \frac{11}{A^{1/2}} \text{ MeV}$$

$$\Delta = \frac{1}{2} \cdot (-1)^N [S(N, Z) - S(N-1, Z)]$$



# Dependence on pairing strength

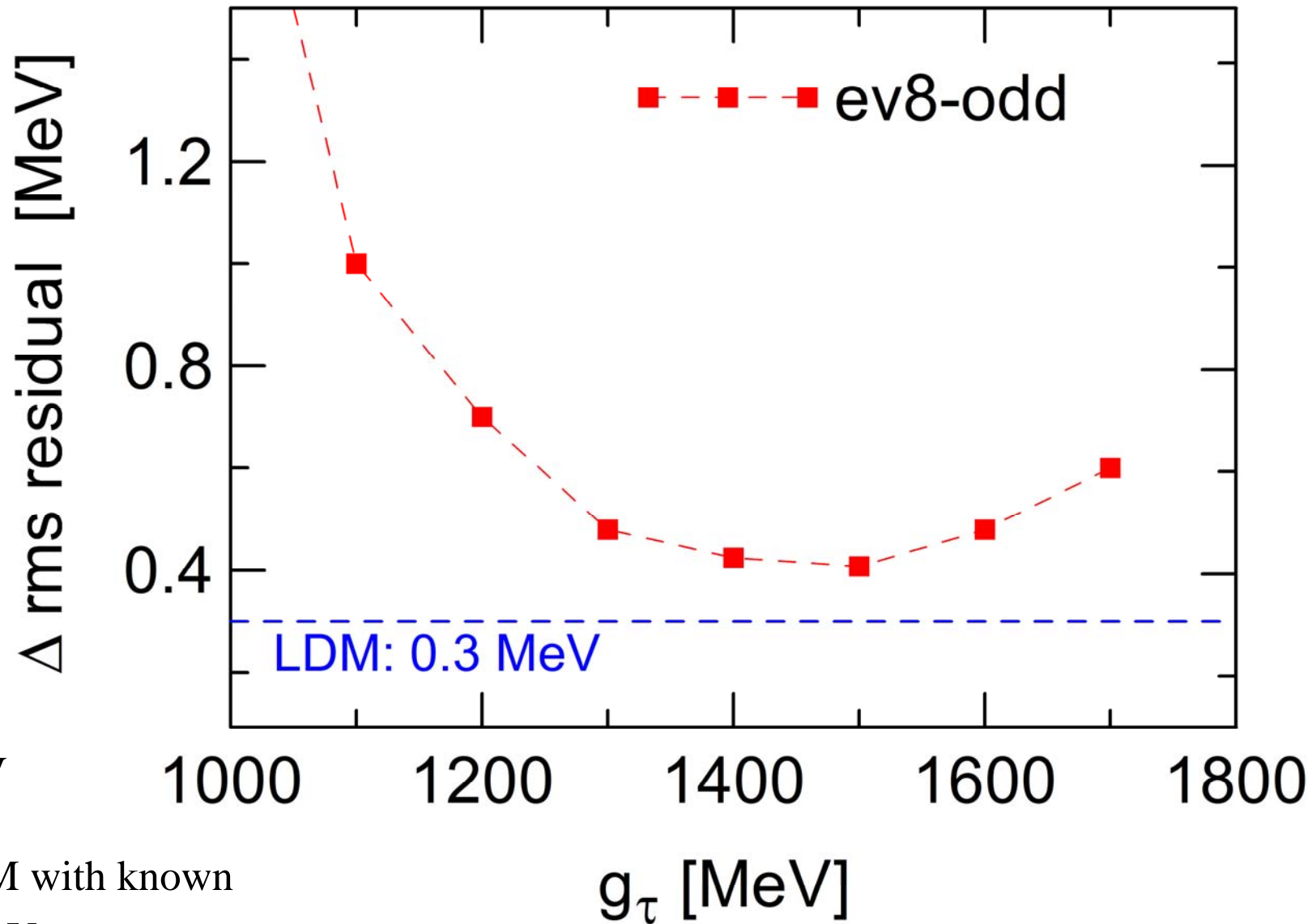
Skyrme = SLy4

$$V_{\text{pairing}} = g \cdot \delta(r_{12}) \cdot [1 - \rho(r)/\alpha]$$

$$\alpha = 0.16 \text{ fm}^{-3}$$

search for  $g_n - g_p$

$$\Delta = \frac{1}{2} \cdot (-1)^N [S(N, Z) - S(N-1, Z)]$$



$$\Delta_{LDM} = \frac{11}{A^{1/2}} \text{ MeV}$$

rms residual for LDM with known exp. data = 0.299 MeV

## In progress

- 1 - BCS+Lipkin-Nogami mass table.
- 2 - Functional parameters chi-square including odd isotopes and isotones.
- 3 - Mass table in one-two weeks on a single processor.
- 4- Runs on NERSC supercomputers for minima search.