



# **Solving the Mysteries of Ultra-Magnetized Neutron Stars**

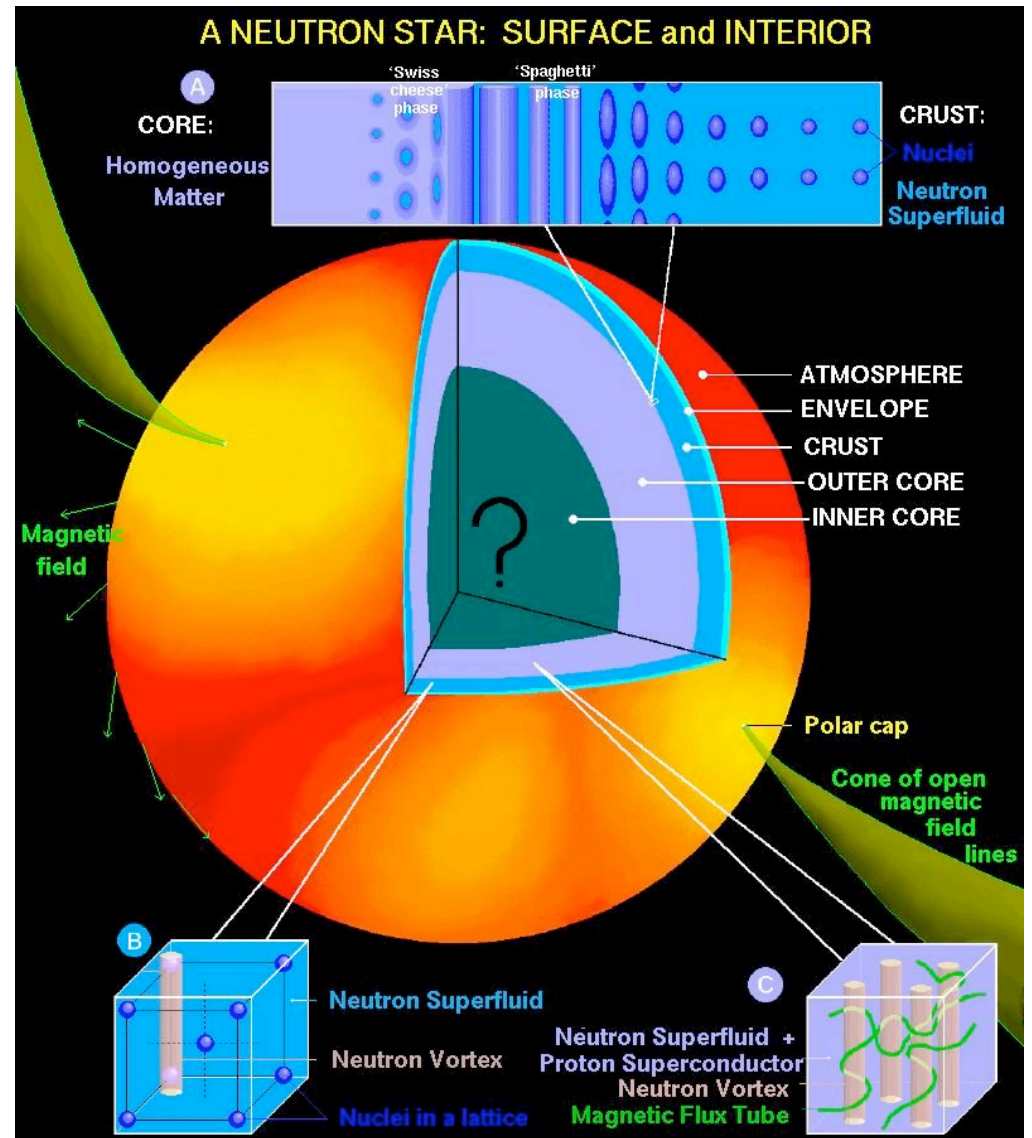
## **Heat Transport inside the Crust**

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IAUNAM  
(2007)

# Neutron Stars

## General characteristics:

- masses between 1.1 and 2.1  $M_{\text{sol}}$
- corresponding radii between 20 - 10km
- central density  $\sim 10^{15} \text{ g cm}^{-3}$
- **core**: superfluid of degenerate neutrons + superconductor of degenerate protons
- inner core ?
- crust  $\rightarrow$  envelope  $\rightarrow$  atmosphere



# Magnetic Breaking

Magnetic Dipole Model:

$$\dot{E} = -\frac{2}{3c^3} |\ddot{\mathbf{m}}|^2 = \frac{-B_p^2 R_{NS}^6 \Omega^4 \sin^2 \alpha}{6c^3}$$

Rotation Energy:

$$E = \frac{1}{2} I \Omega^2 \longrightarrow \dot{E} = I \Omega \dot{\Omega}$$

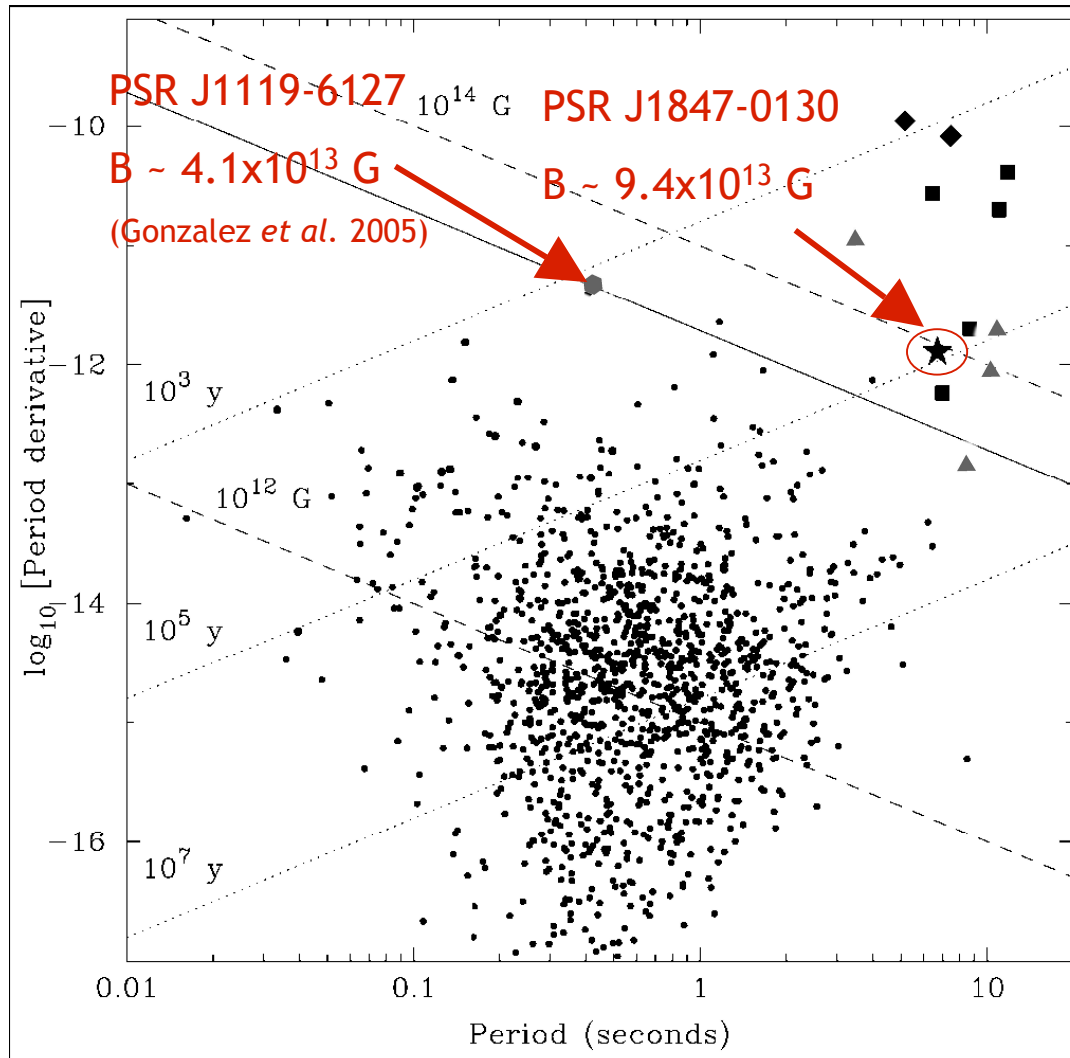
Compare the two:

$$B_p^2 \Omega^4 \propto \Omega \dot{\Omega}$$

Get the relations:  $P = 2\pi/\Omega$      $\dot{P} = -\dot{\Omega}/\Omega^2$

$$B \simeq 10^{12} \sqrt{P \dot{P}}_{-15} \text{ G}$$

## Relation P - dP/dt



(McLaughlin *et al.* ApJ 591: L135. 2003. "PSR J1847-0130: A Radio Pulsar with Magnetar Spin Characteristics.")

## HBPSR

("High Field Pulsars")

Critical quantum field:

$$B_{CR} \sim 4.4 \times 10^{13} G$$

Cyclotron energy = electron rest energy

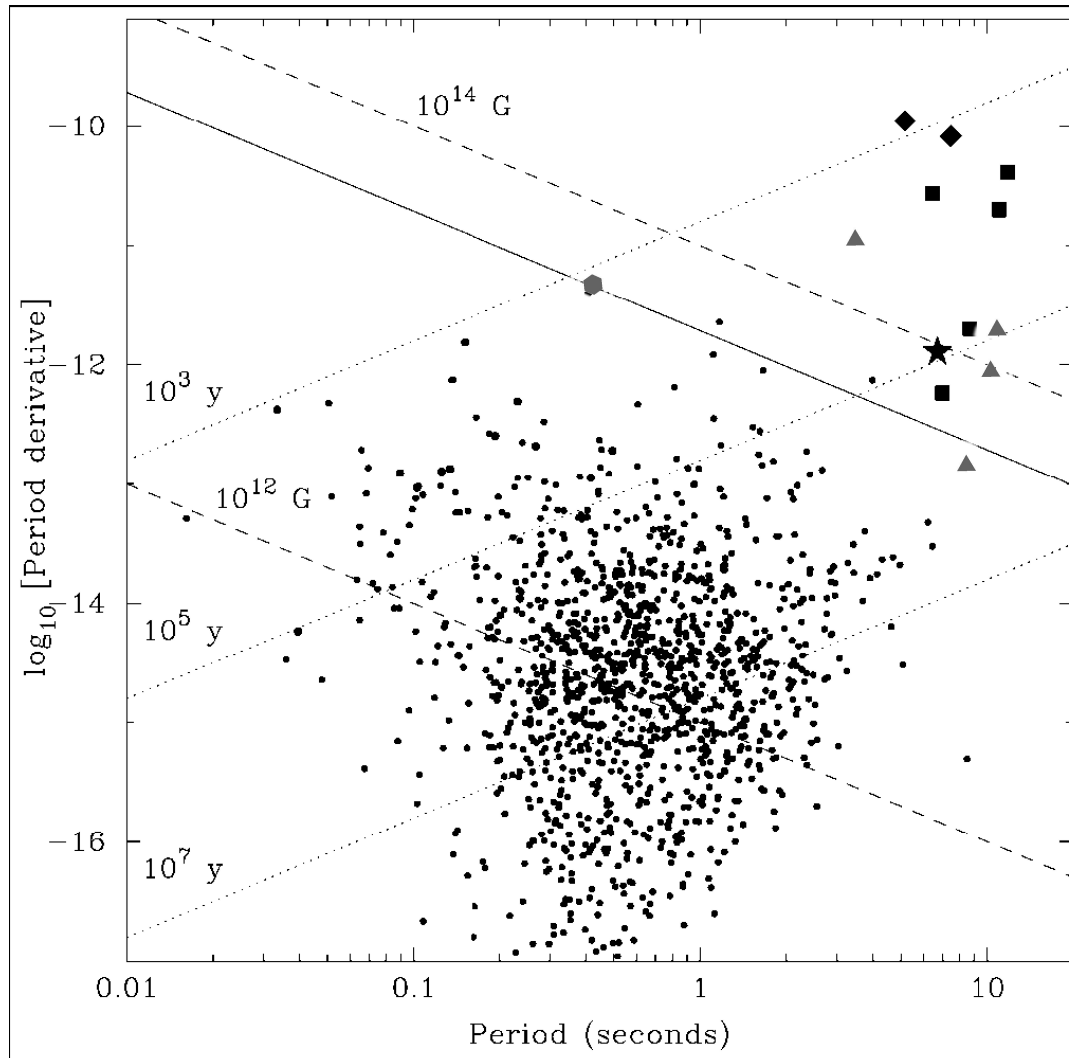
$B > B_{CR} \rightarrow$  "magnetic photon splitting" dominates "pair production"  $\rightarrow$  no emission in the radio

Before the Parkes Multibeam Pulsar Survey (1999):

Largest inferred  $B \sim 2.1 \times 10^{13} G$  for a radio pulsar.

AFTER:  $B \sim 1e13 - 1e14 G$

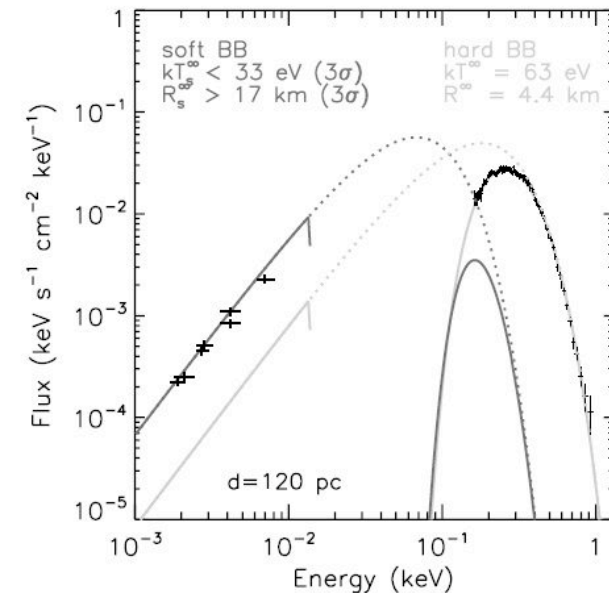
## Relation P - dP/dt



(McLaughlin *et al.* ApJ 591: L135. 2003. "PSR J1847-0130: A Radio Pulsar with Magnetar Spin Characteristics.")

## XDINS

("X-Ray Dim Isolated Neutron Stars")



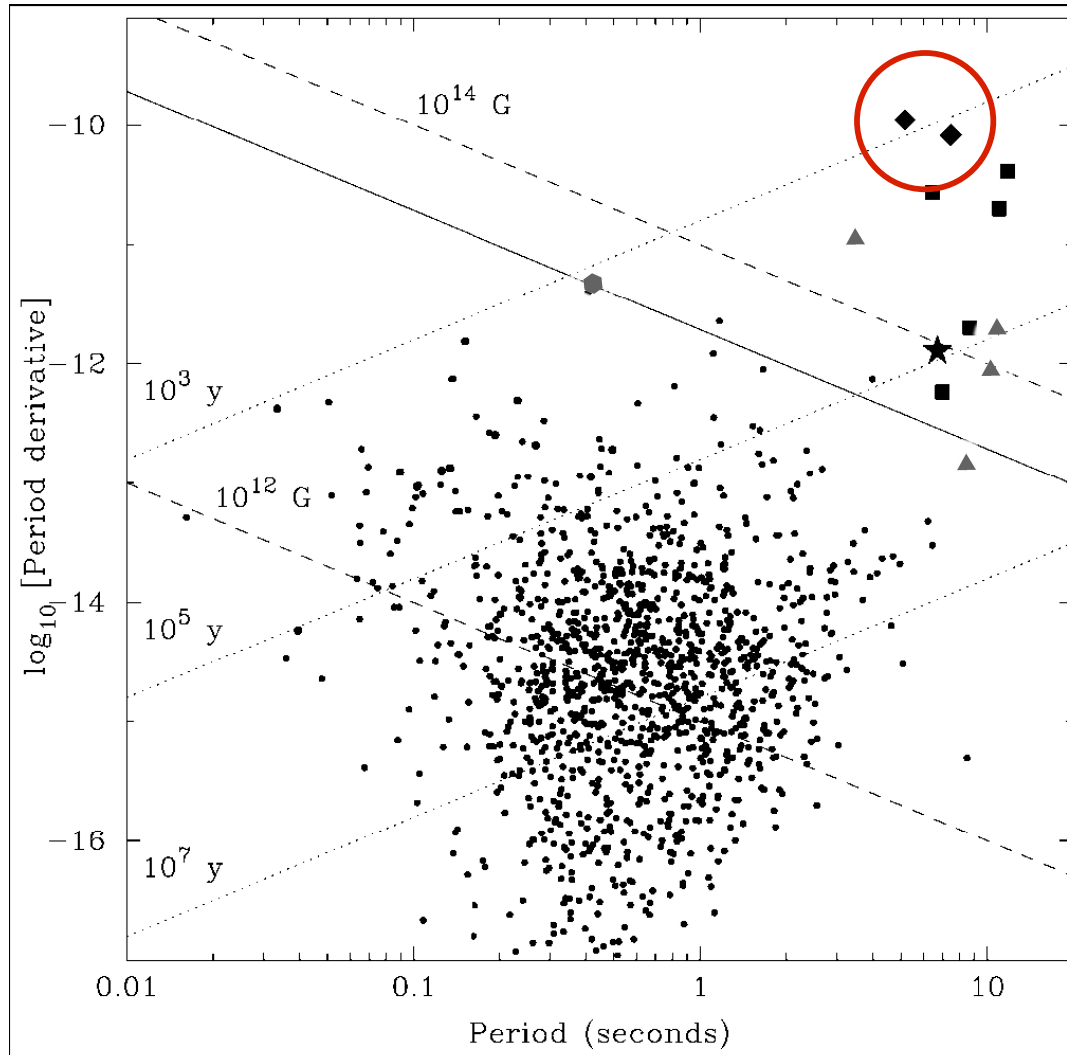
### General Characteristics:

- low, but persistent emission in x-rays,  $L_x \sim 10^{30}-10^{31} \text{ ergs}^{-1}$
- no emission in the radio
- Black Body with  $kT \sim 40-110 \text{ eV} \rightarrow r = 3 - 5 \text{ km}$
- broad absorption line  $\rightarrow$  proton cyclotron
- optical excess  $\rightarrow r > 10 \text{ km}$
- pulsations in 6 sources  $\rightarrow B \ 10^{13} - 10^{14} \text{ G}$
- $10^5 - 10^6$  years old
- close,  $d \sim 100 - 300 \text{ pc}$

## Relation P - dP/dt

## SGRs

("Soft Gamma-Ray Repeaters")



- short bursts (~100ms) en soft  $\gamma$  rays y x-rays with energies of  $\sim 10^{41}$  ergs and rise times of  $\sim 10$  ms

- 4 - (6?) in the Galactic and the LMC (1)

- optically thin Bremsstrahlung emission,  $kT \sim 20-50$  keV

- + power law with  $n \sim 2-3$  (quiescence)

- giant bursts,  $\sim 4 \times 10^{44}$  erg (3)

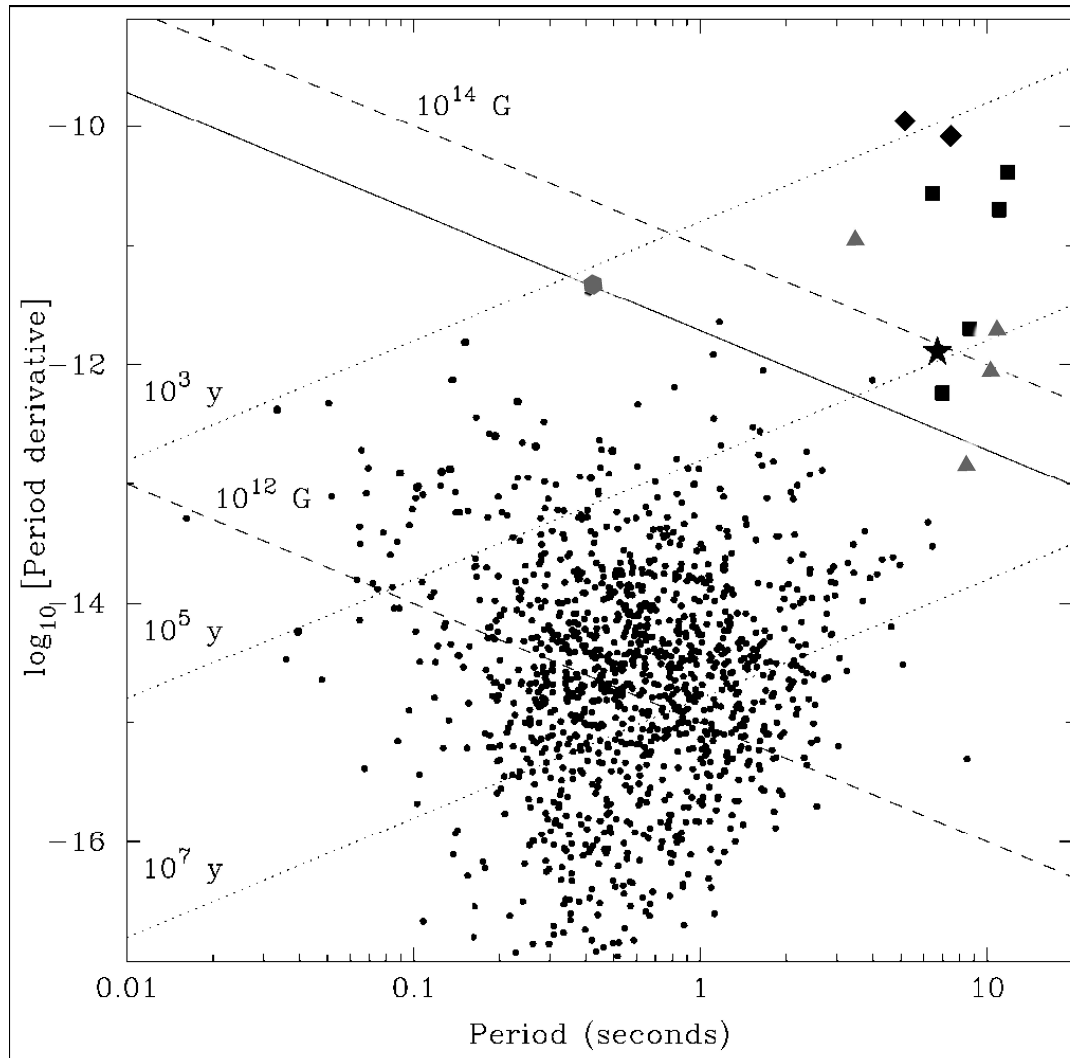
- 3 sources with pulsations in quiescence  $\rightarrow B \sim 10^{15}$  G

X-rays: surface origin

Bursts: crustal breaking and plasma excitation

(McLaughlin *et al.* ApJ 591: L135. 2003. "PSR J1847-0130: A Radio Pulsar with Magnetar Spin Characteristics.")

## Relation P - dP/dt



(McLaughlin *et al.* ApJ 591: L135. 2003. "PSR J1847-0130: A Radio Pulsar with Magnetar Spin Characteristics.")

## AXPs

### ("Anomalous X-Ray Pulsars")

- pulsations in x-rays,  $L_x \sim 10^{33} - 10^{35} \text{ ergs}^{-1}$ ,  $P \sim 6 - 12\text{s}$
- Soft x-ray spectrum with (i) Black Body  $kT \sim 0.4\text{keV}$  (ii) hard power law,  $n \sim 2.5 - 4$
- **Similar to the SGRs** : wide profiles and  $P - dP/dt$  in quiescence
- **Different to the SGRs**: softer spectrum, less noisy, lower  $B$ , association with SN
- Bursts in 2 cases but with a correlation with the rotation
- **"Anomalous"** - X-ray pulsars: NS accreting from a massive companion, fluctuations in the emission,  $L_x \sim 10^{37} - 10^{38} \text{ ergs}^{-1}$
- lack of Doppler shift  $\rightarrow$  no companion
- associations with SNRs  $\rightarrow$  young

# **Anisotropic Heat Transport: magnetic field effects in the crust**

Energy Balance:

$$C \frac{\partial T}{\partial t} = \text{Sources} - \text{Sinks} - \nabla \cdot \mathbf{F}$$

General relativistic effects + heat transport:

$$e^{\Phi} \mathbf{F} = -\hat{\kappa} \cdot \nabla (e^{\Phi} T)$$



# Anisotropic Heat Transport: magnetic field effects in the crust

Thermal conductivity of  
the electrons

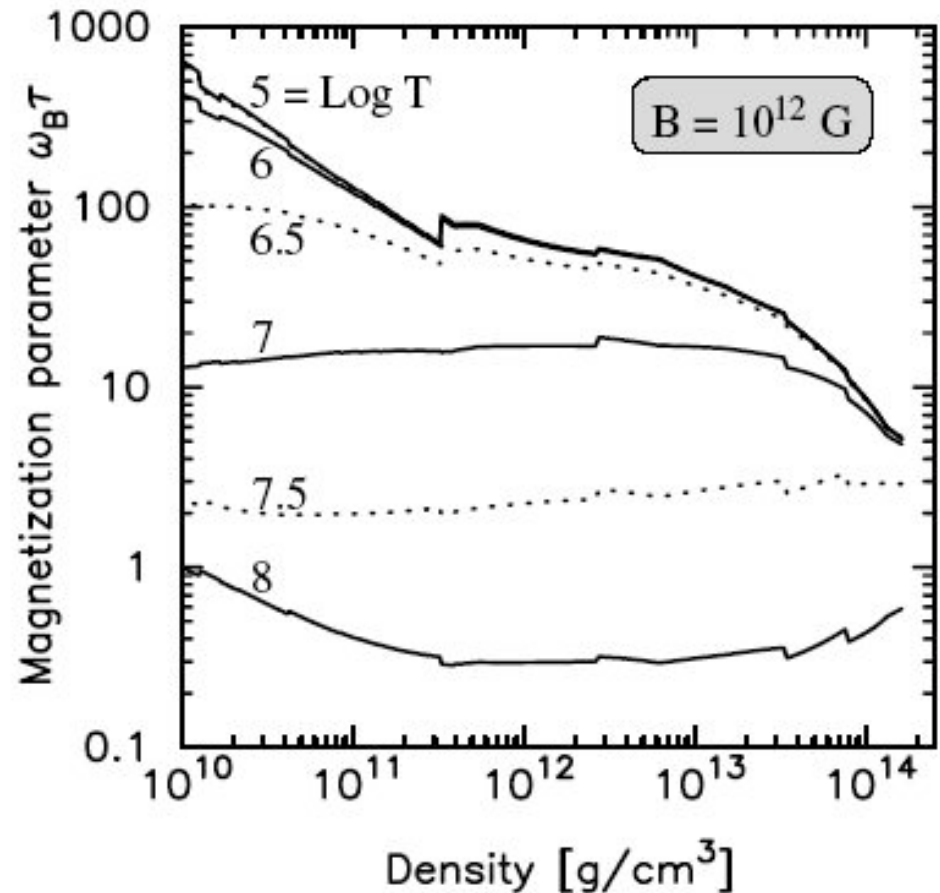
$$\vec{\kappa} = \begin{pmatrix} \kappa_{\parallel} & 0 & 0 \\ 0 & \kappa_{\perp} & \kappa_{\wedge} \\ 0 & -\kappa_{\wedge} & \kappa_{\perp} \end{pmatrix}$$

$$\kappa_{\parallel} = \kappa_0$$

$$\kappa_{\perp} = \frac{\kappa_0}{1 + (\omega_B \tau)^2}$$

$$\kappa_{\wedge} = \frac{\kappa_0 (\omega_B \tau)}{1 + (\omega_B \tau)^2}$$

Electron  
gyrofrequency  $\omega_B = \frac{eB}{m^*c}$



# Surface Temperature Distribution With Magnetic Field:

Only considering the effect of the magnetic field in the envelope:

$$T_s^4(\Theta_B) = T_s^4(\Theta_B = 0)\sin^2 \Theta_B + T_s^4(\Theta_B = 90)\cos^2 \Theta_B$$

**Greenstein & Hartke, 1983**

Best present version: Potekhin & Yakovlev, 2001

# Surface Temperature Distribution With Magnetic Field:

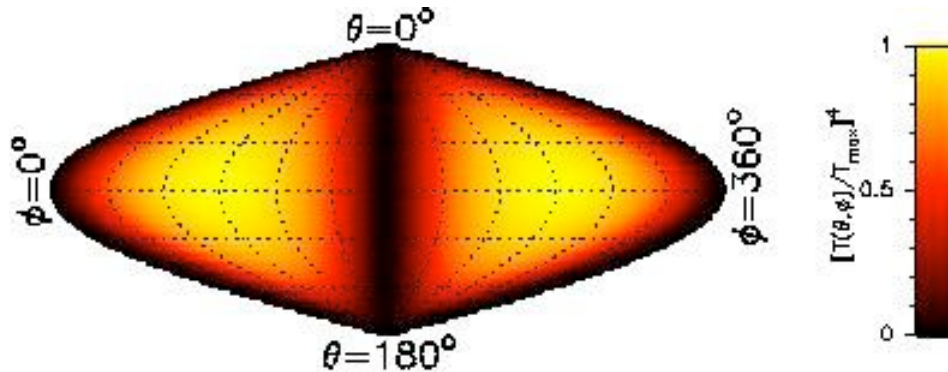
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Greenstein & Hartke, 1983

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Puro Campo Dipolar



# Surface Temperature Distribution With Magnetic Field:

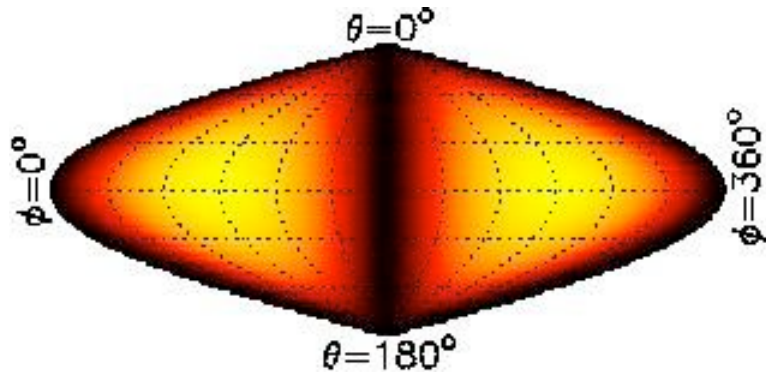
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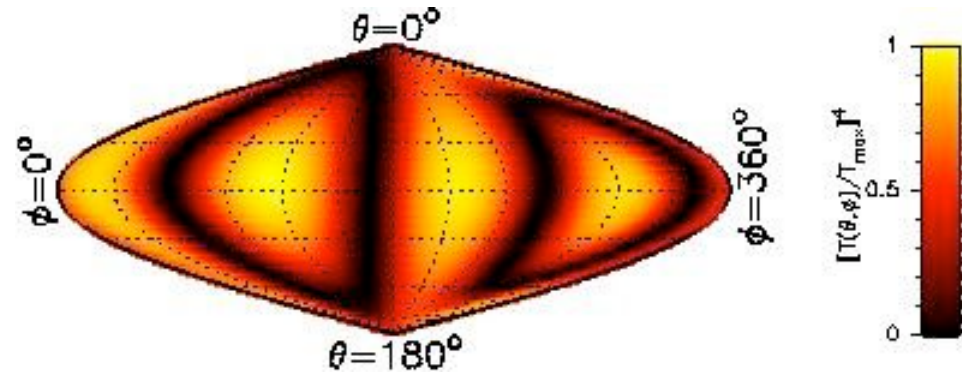
Greenstein & Hartke, 1983

Best present version: Potekhin & Yakovlev, 2001

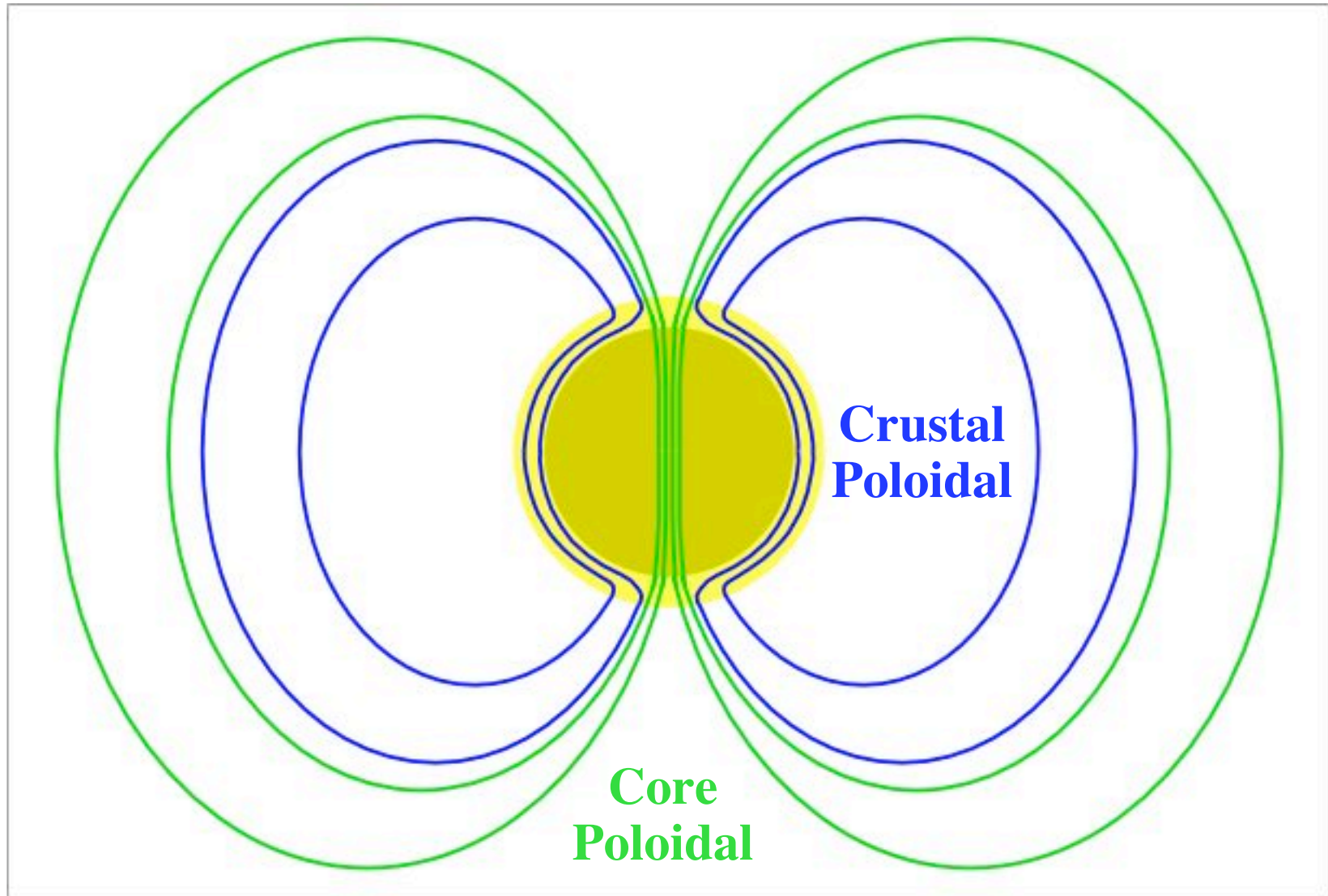
Purely Poloidal Dipolar



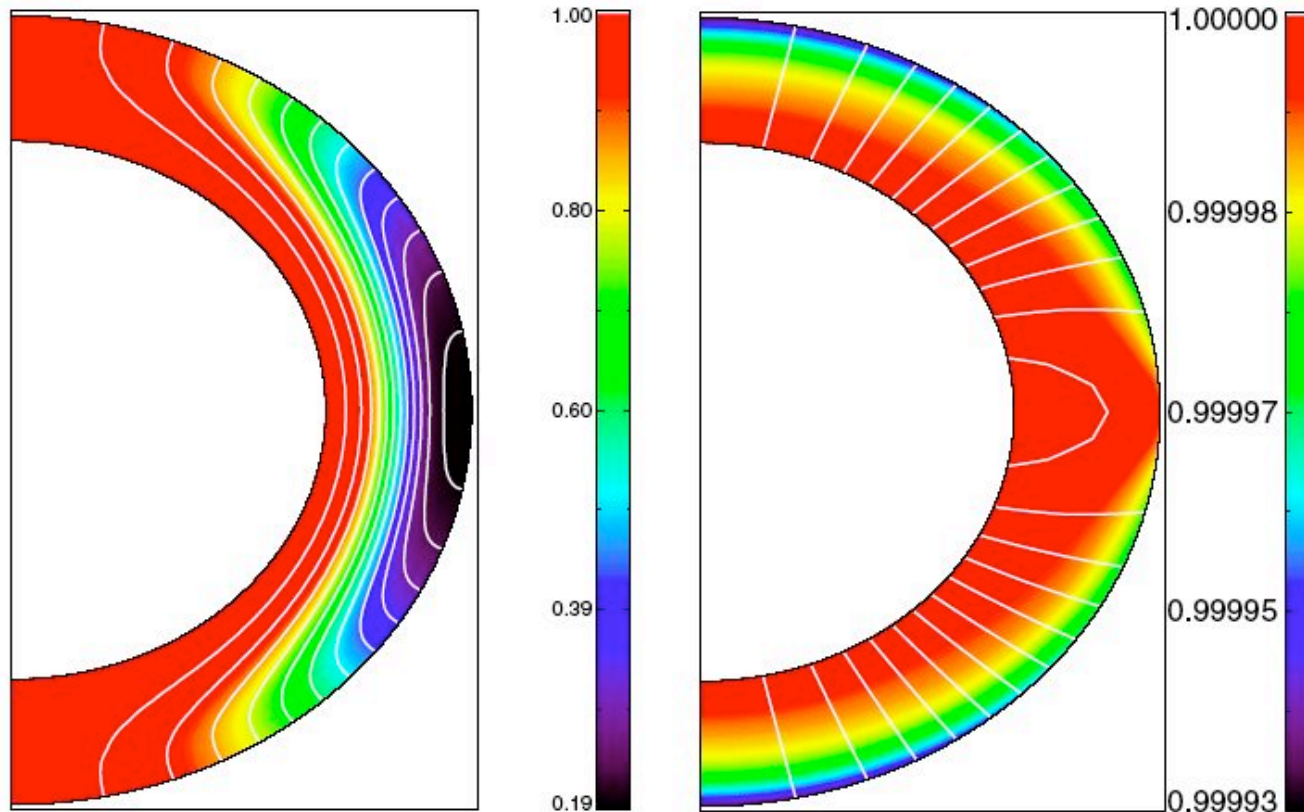
Poloidal Dipolar + Quadrupolar



# Dipolar Fields: Crust + Core Currents



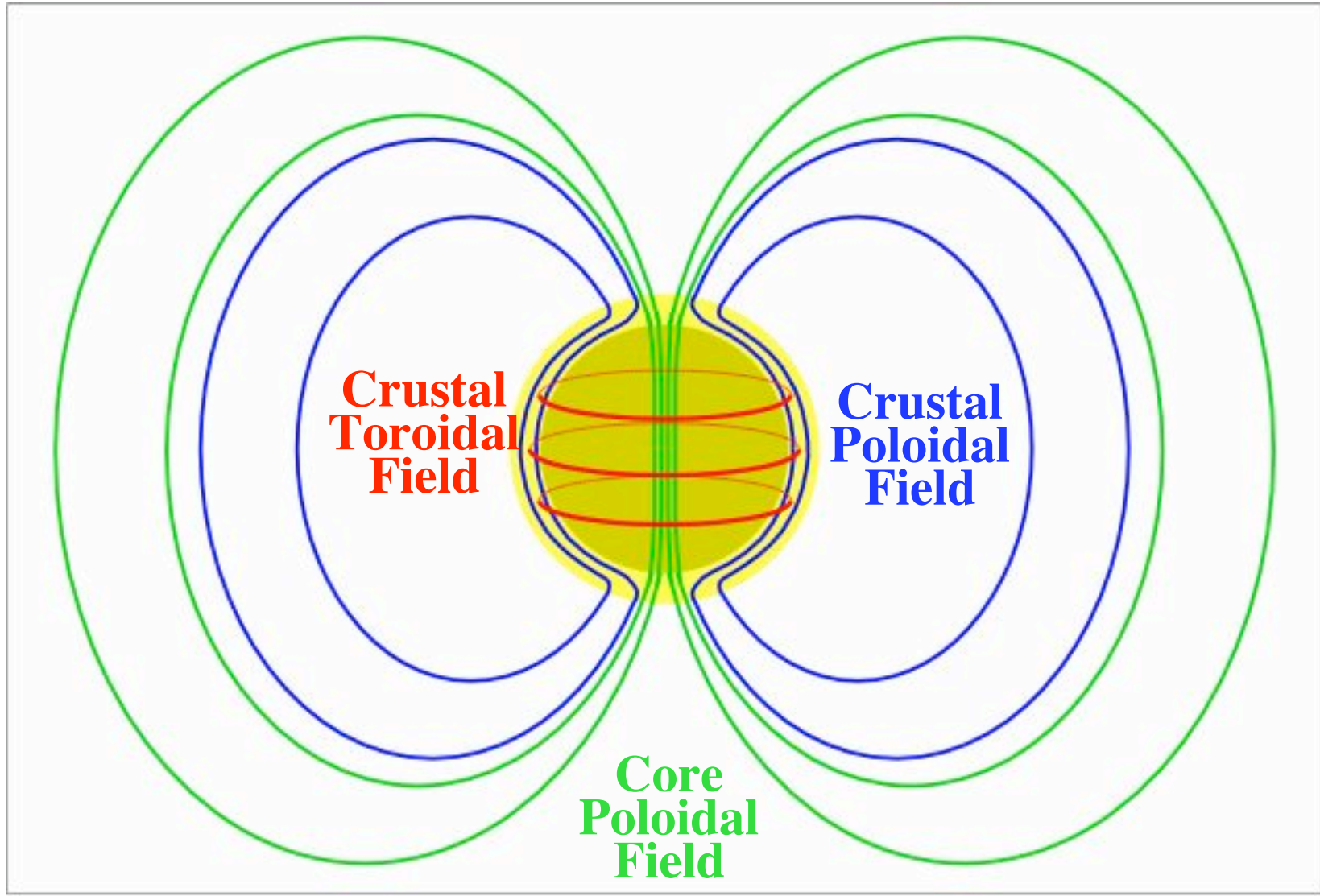
# Surface Temperature Distribution With Magnetic Field:



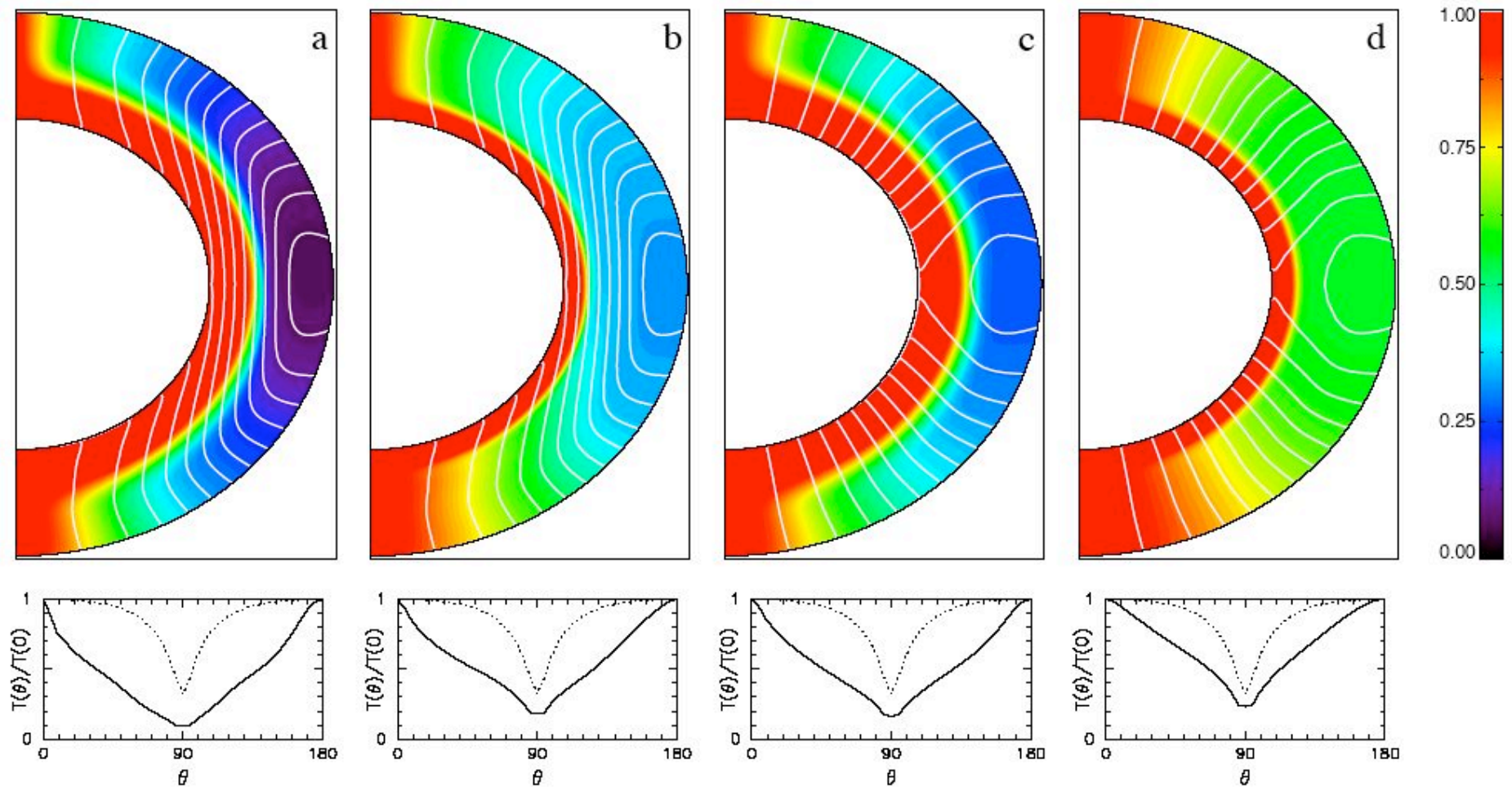
**Fig. 7.** Representation of both field lines and temperature distribution in the crust whose radial scale ( $r(\rho_n) \leq r \leq r(\rho_b)$ ) is stretched by a factor of 5, assuming  $B_0 = 3 \times 10^{12}$  G and  $T_{\text{core}} = 10^6$  K. Left panel corresponds to a crustal field, right panel to a star-centered core field. Bars show the temperature scales in units of  $T_{\text{core}}$ .



# Poloidal + Toroidal Components



# Surface Temperature Distribution With Magnetic Field:





# Surface Temperature Distribution With Magnetic Field:

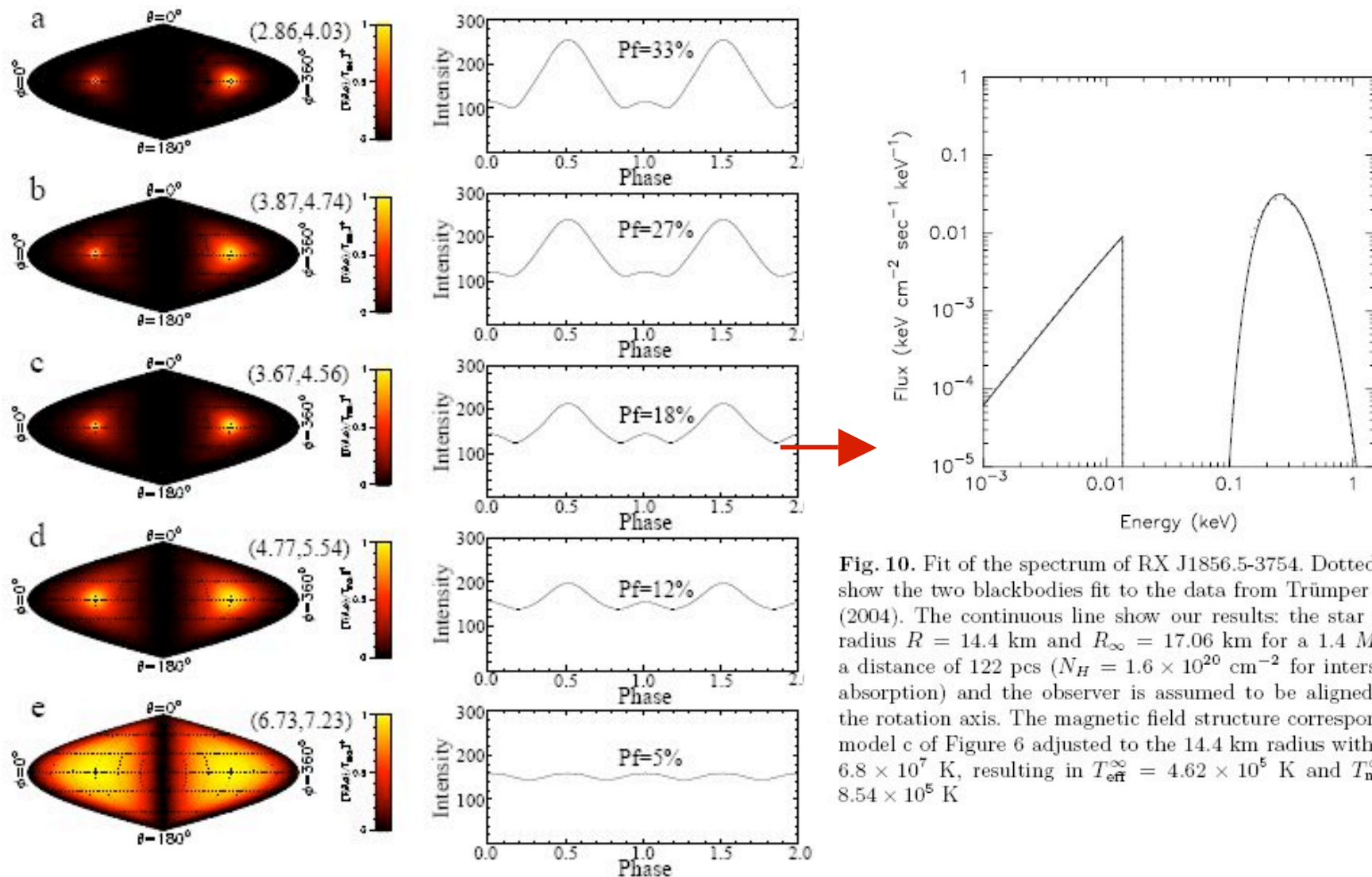
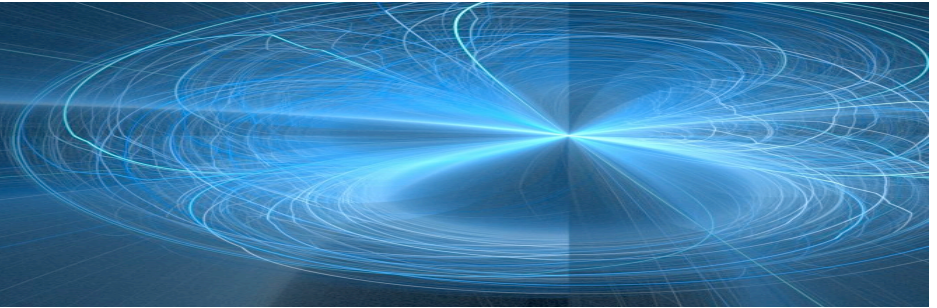
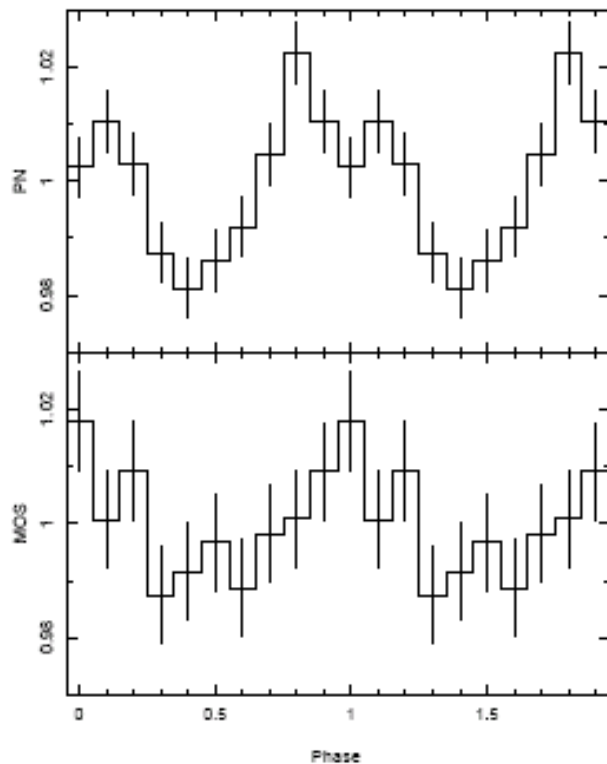


Fig. 10. Fit of the spectrum of RX J1856.5-3754. Dotted lines show the two blackbodies fit to the data from Trümper *et al.* (2004). The continuous line show our results: the star has a radius  $R = 14.4$  km and  $R_\infty = 17.06$  km for a  $1.4 M_\odot$ , at a distance of 122 pcs ( $N_H = 1.6 \times 10^{20}$  cm $^{-2}$  for interstellar absorption) and the observer is assumed to be aligned with the rotation axis. The magnetic field structure corresponds to model c of Figure 6 adjusted to the 14.4 km radius with  $T_b = 6.8 \times 10^7$  K, resulting in  $T_{\text{eff}}^\infty = 4.62 \times 10^5$  K and  $T_{\text{max}}^\infty = 8.54 \times 10^5$  K

# RX J1856.5-3754: new observations



**Observations:** *Tiengo & Mereghetti, 2007, ApJ 657:L101-L104, "XMM-Newton Discovery of 7s Pulsations in the Isolated Neutron Star RX J1856.5-3754."*



$$P = 7.05514 \pm 0.00007 \text{ s}$$

$$\dot{P} < 1.9 \times 10^{-12} \text{ s/s}$$

$$B < 1.2 \times 10^{14} \text{ G}$$

$$T > 6 \times 10^4 \text{ years}$$

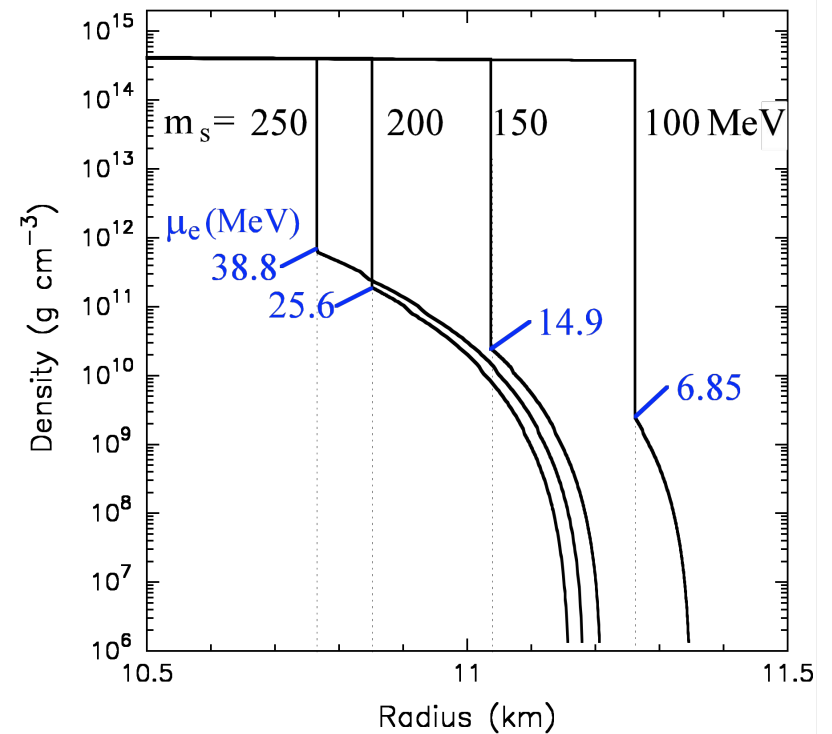
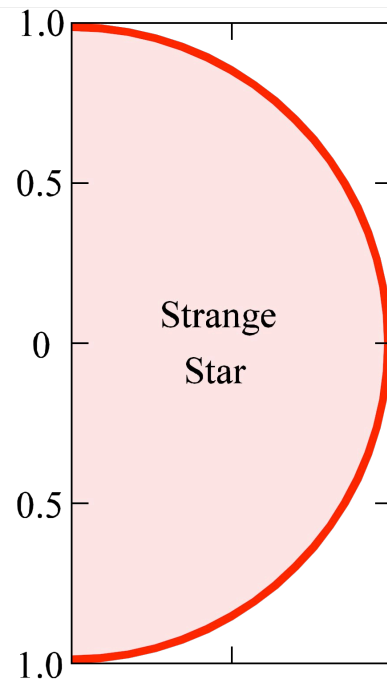
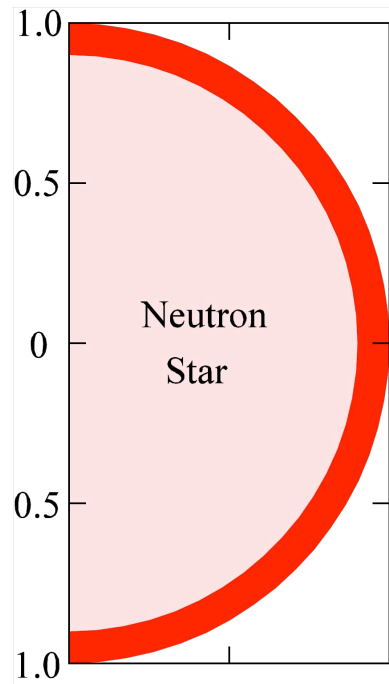
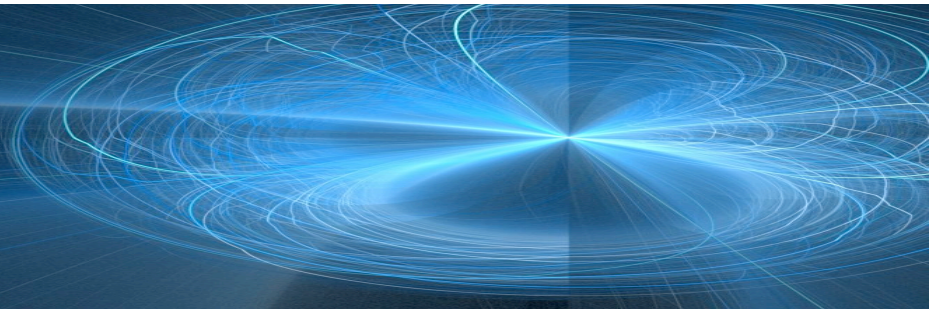
$$\text{PF} = 1.6\% \pm 0.2\%$$

$$\alpha = 90^\circ \rightarrow \text{PF} \sim 18\%$$

previous model

$$\alpha = 8^\circ \rightarrow \text{PF} \sim 1.5\%$$

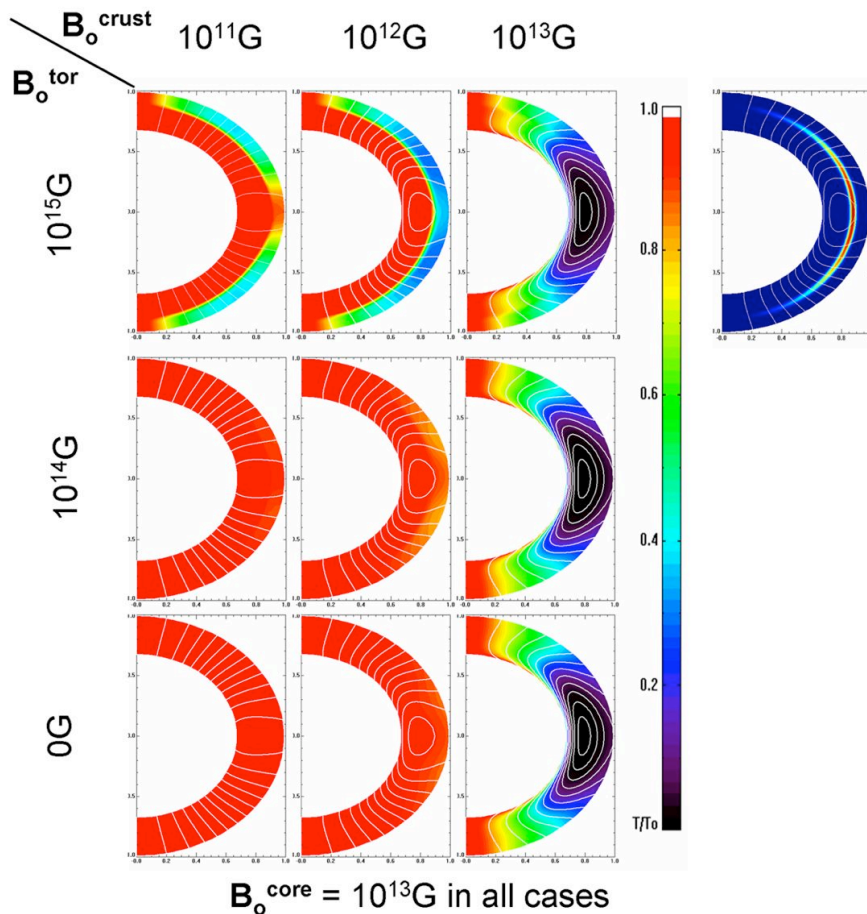
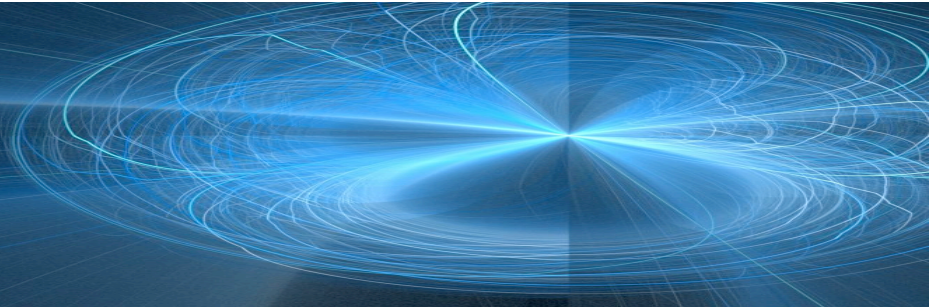
# RX J1856.5-3754: Quark Star?



(Henderson & Page. 2007. *Ap&SS.tmp*. "RX J1856.5-3754 as a Possible Strange Star Candidate.")



# RX J1856.5-3754: Quark Star?



$$B_{\text{tor}} = 1e15 \text{ G}$$

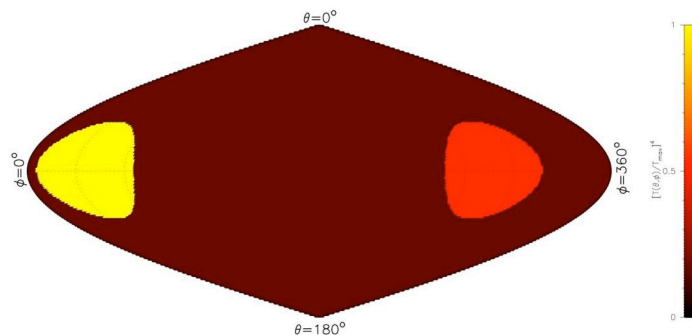
$$\Delta r = 250 \text{ m}$$

But the magnetic shear stress  
( $B_r B_\theta / 4\pi$ ) is too large for such a  
thin layer

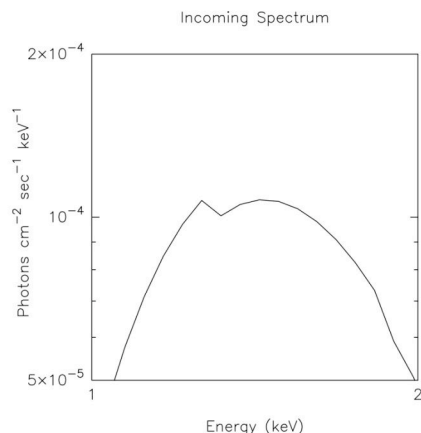
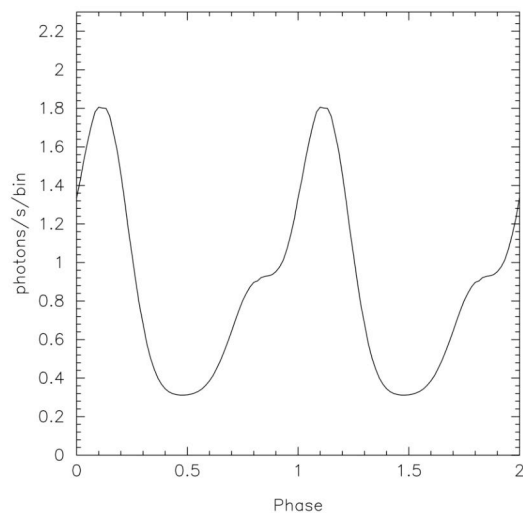
**→ NOT PROBABLE**

(Henderson & Page. 2007. *Ap&SS.tmp*. "RX J1856.5-3754 as a Possible Strange Star Candidate.")

# PSR J1119-6127: High Field Pulsar



PSPC detected Light Curves



## Model:

$T_1 = 3.6e6K$

$T_2 = 4.2e6K$

$T_s = 2.7e6K$

$\alpha = 90^\circ \rightarrow PF \sim 68\%$

## Observations:

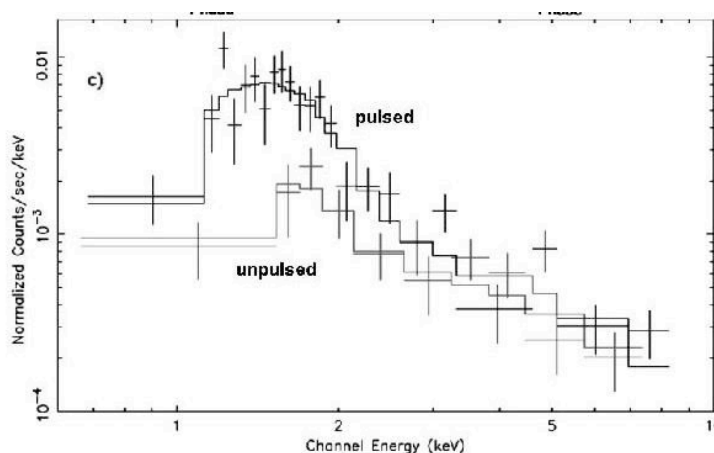
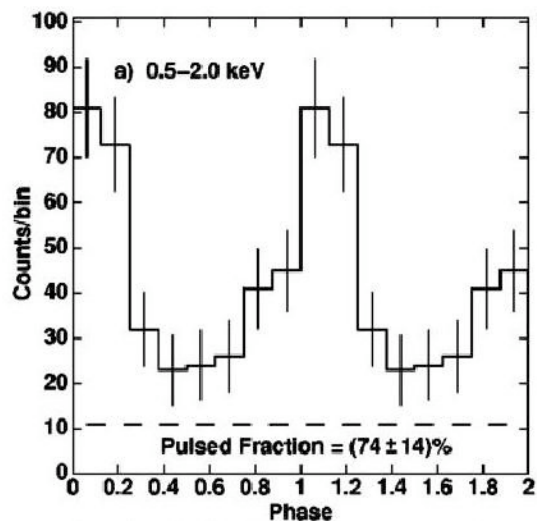
$P = 0.408s$

$t = 1700 \text{ years}$

$B = 4.1e13 \text{ G}$

$T_{bb,\infty} = 2.4e6 \text{ K}$

$PF = (74 \pm 14) \%$



(Gonzalez *et al.* Ap&SS tmp 2007. "PSR J1119-6127 and the X-Ray Emission from High Magnetic Field Radio Pulsars.")



