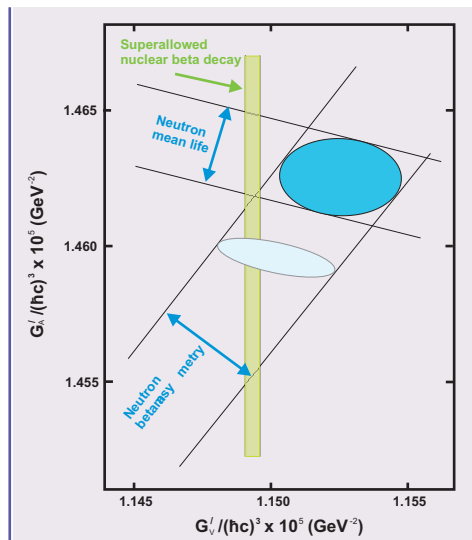
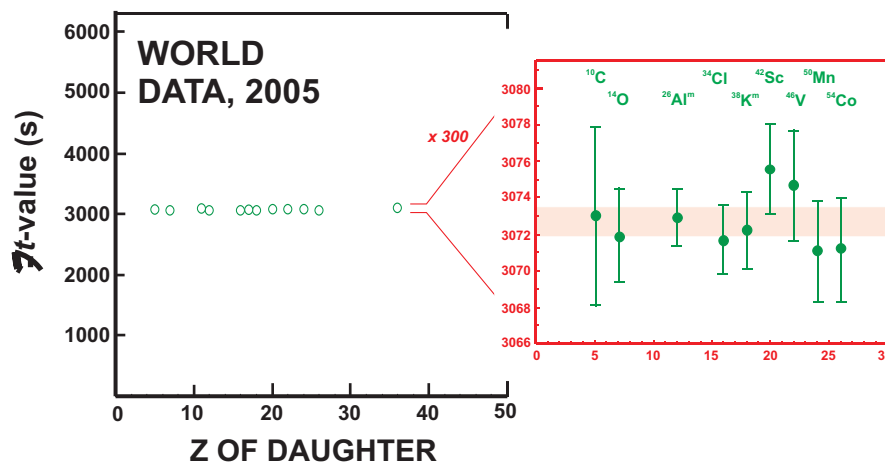


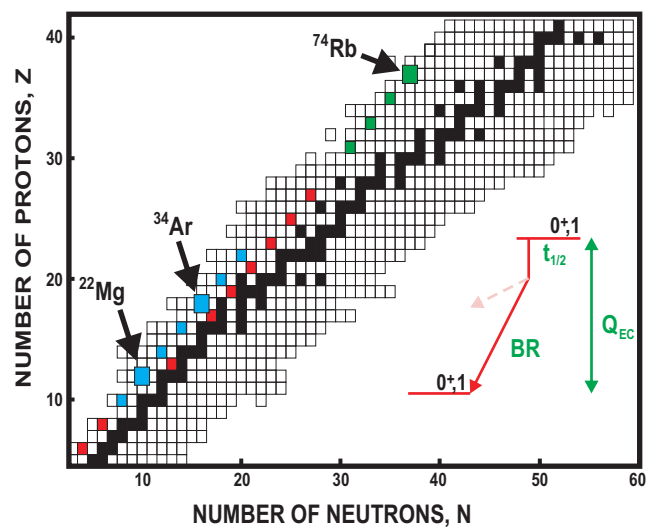
# SUPERALLOWED NUCLEAR BETA DECAY: RECENT RESULTS AND THEIR IMPACT ON $V_{ud}$

J.C. Hardy  
 Cyclotron Institute  
 Texas A&M University  
 U.S.A.

(with I.S. Towner)



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$



# SUPERALLOWED $0^+ \rightarrow 0^+$ BETA DECAY

## BASIC WEAK-DECAY EQUATION

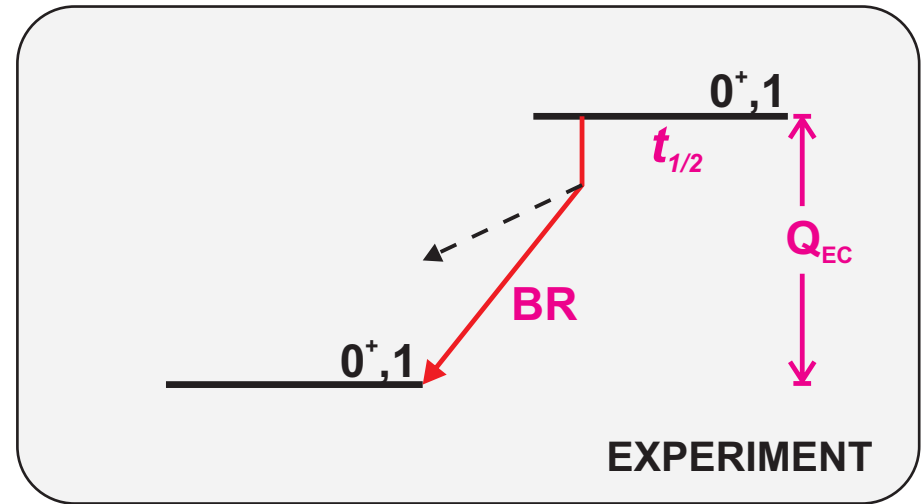
$$ft = \frac{K}{G_V^2 \langle \rangle^2}$$

$f$  = statistical rate function:  $f(Z, Q_{EC})$

$t$  = partial half-life =  $t_{1/2}/BR$

$G_V$  = vector coupling constant

$\langle \rangle$  = Fermi matrix element



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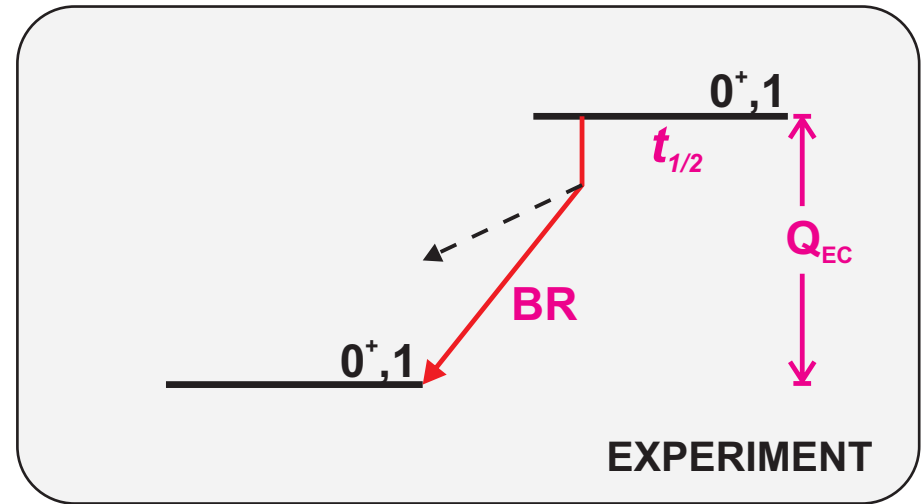
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## INCLUDING RADIATIVE CORRECTIONS

$$\mathcal{F}t = ft \left(1 + \frac{R}{C}\right) \left[1 - (C - NS)\right] = \frac{K}{2G_V^2 (1 + R)}$$

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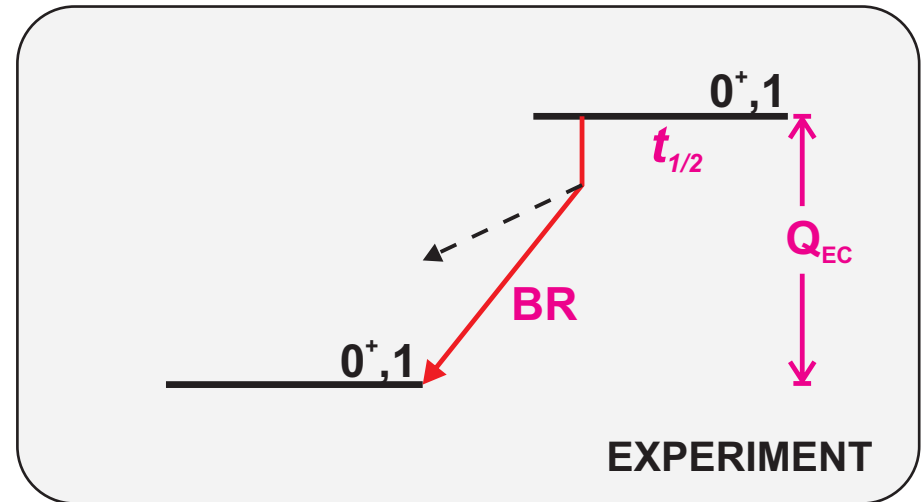
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## INCLUDING RADIATIVE CORRECTIONS

$$\mathcal{F}t = ft (1 + \overset{R}{\prime}) [1 - \overset{C}{\text{---}} \overset{NS}{\text{---}}] = \frac{K}{2G_V^2 (1 + \overset{R}{\text{---}})}$$

$f(Z, Q_{EC})$   
~1.5%

$f(\text{nuclear structure})$   
0.3-0.7%

$f(\text{interaction})$   
~2.4%

# WHAT CAN WE LEARN?

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FROM A SINGLE TRANSITION

Experimentally  
determine  $G_V^2 (1 + R)$

$$\mathcal{I}t = ft (1 + R) [1 - (C - NS)] = \frac{K}{2G_V^2 (1 + R)}$$

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Test Conservation of  
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$\mathcal{F}t$  values constant

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Obtain precise value of  $G_V^2(1 + R)$

Determine  $V_{ud}^2$

$$V_{ud}^2 = G_V^2/G^2$$



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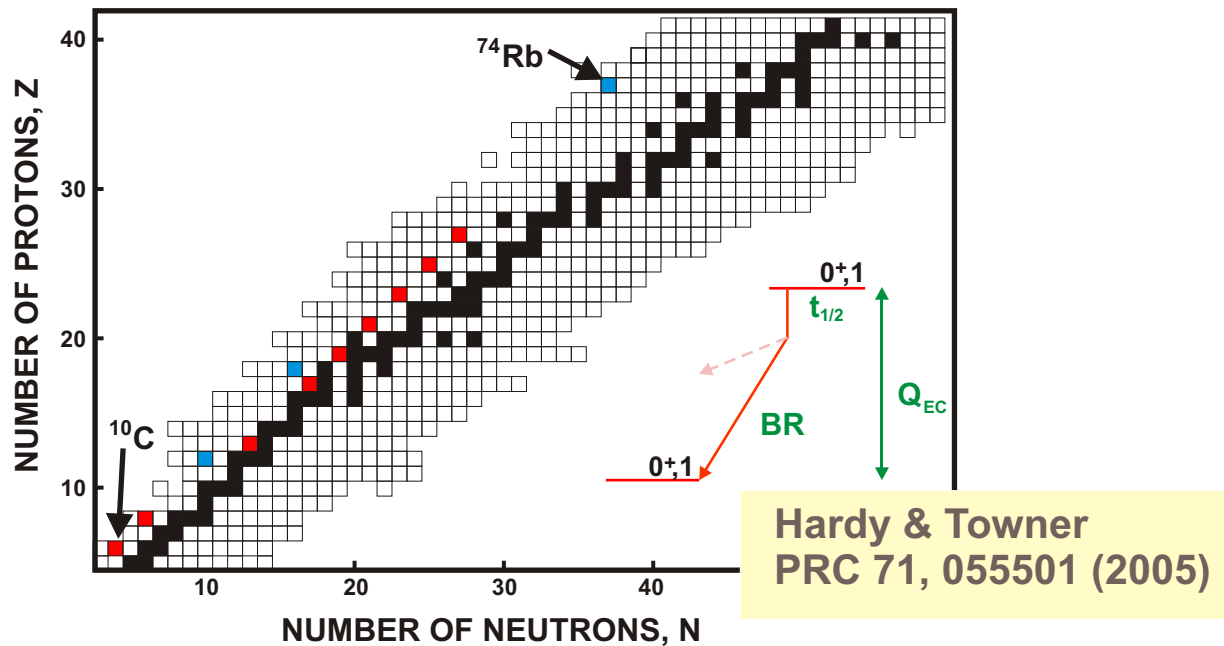
Determine  $V_{ud}^2$

$$V_{ud}^2 = G_V^2/G^2$$

Test CKM unitarity

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$$

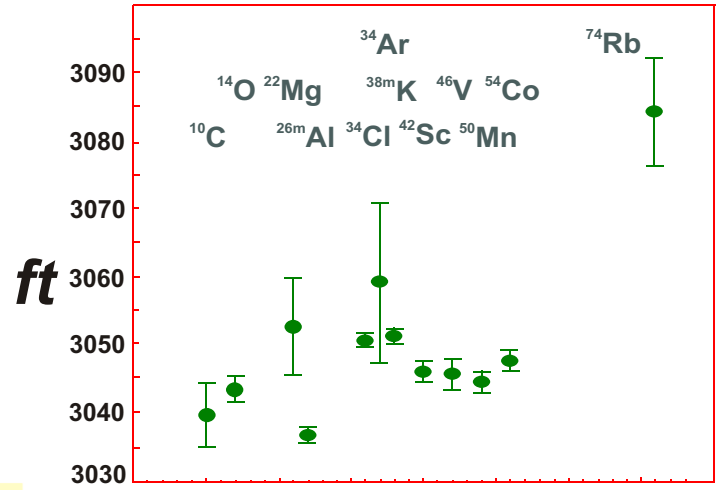
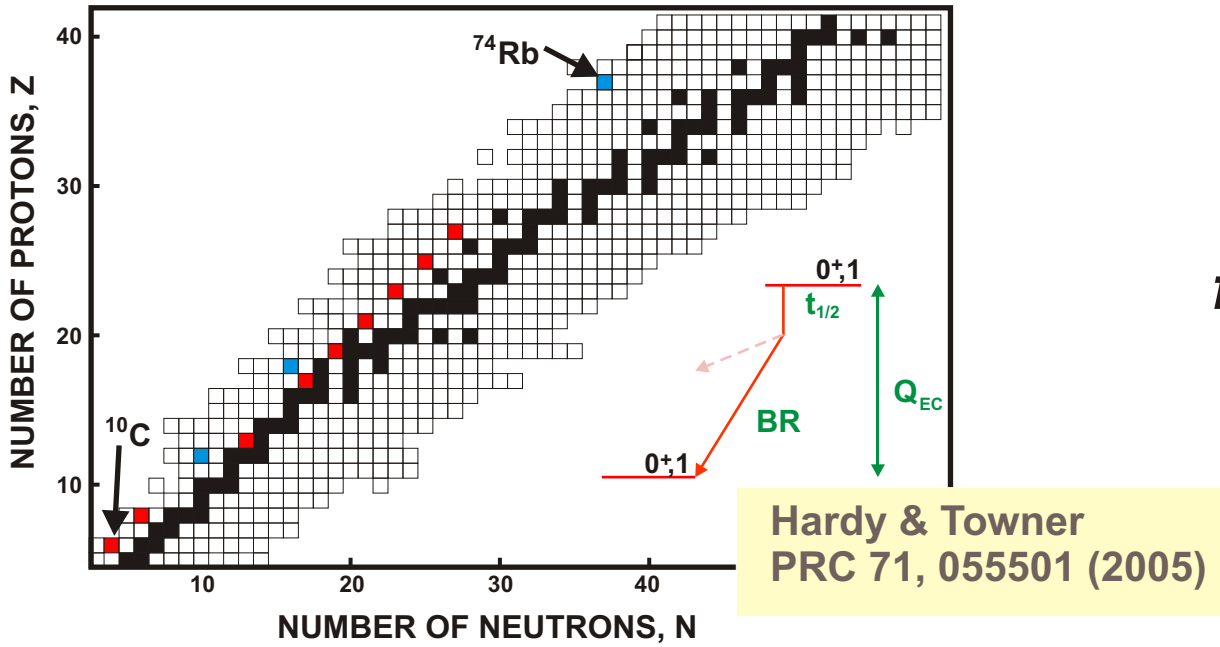
# WORLD DATA FOR $0^+ \rightarrow 0^+$ DECAY, 2005



- 9 cases with  $ft$ -values measured to **~0.1% precision**; 3 more cases with **<0.4% precision**.
- ~125 individual measurements with compatible precision

$$\overline{ft} = ft \left( 1 + \frac{R}{R'} \right) \left[ 1 - \left( \frac{C}{C'} - \frac{NS}{NS'} \right) \right] = \frac{K}{2G_V^2 \left( 1 + \frac{R}{R'} \right)}$$

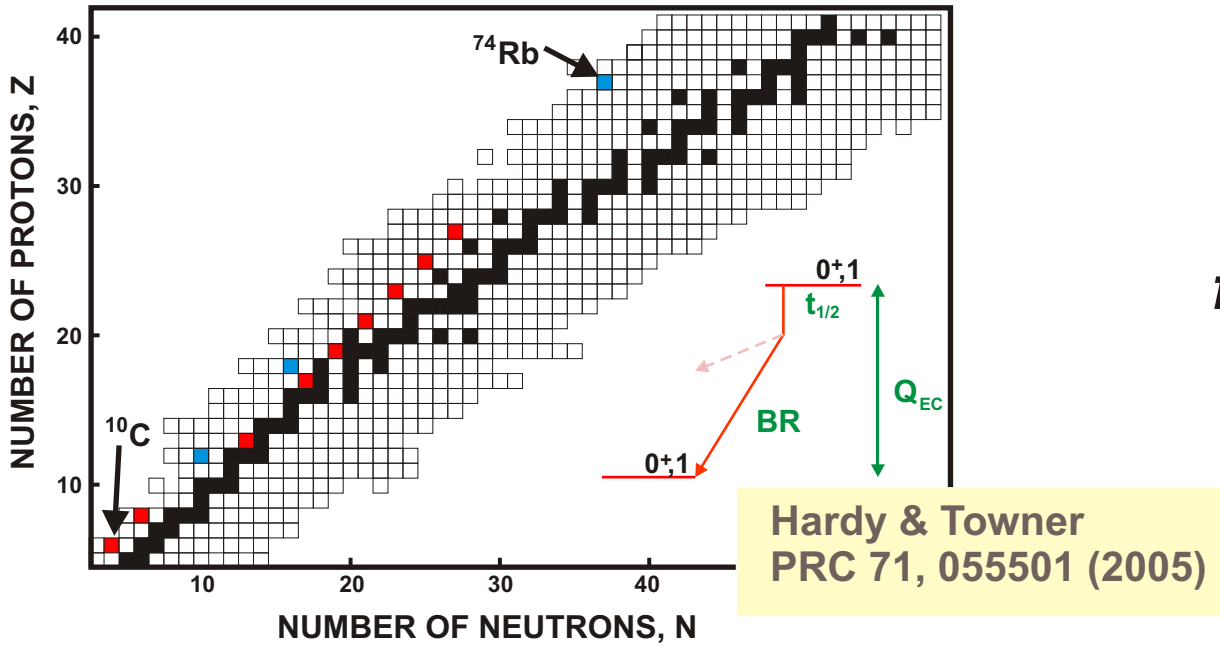
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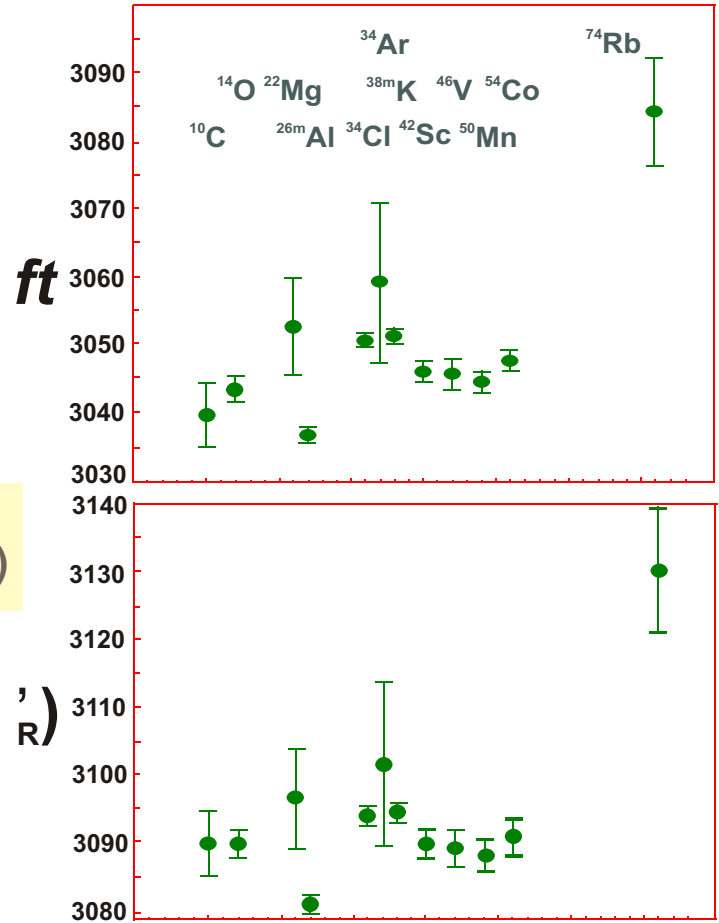
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$$\overline{ft} = ft (1 + \delta_R) [1 - (\delta_C - \delta_{NS})] = \frac{K}{2G_V^2 (1 + \delta_R)}$$

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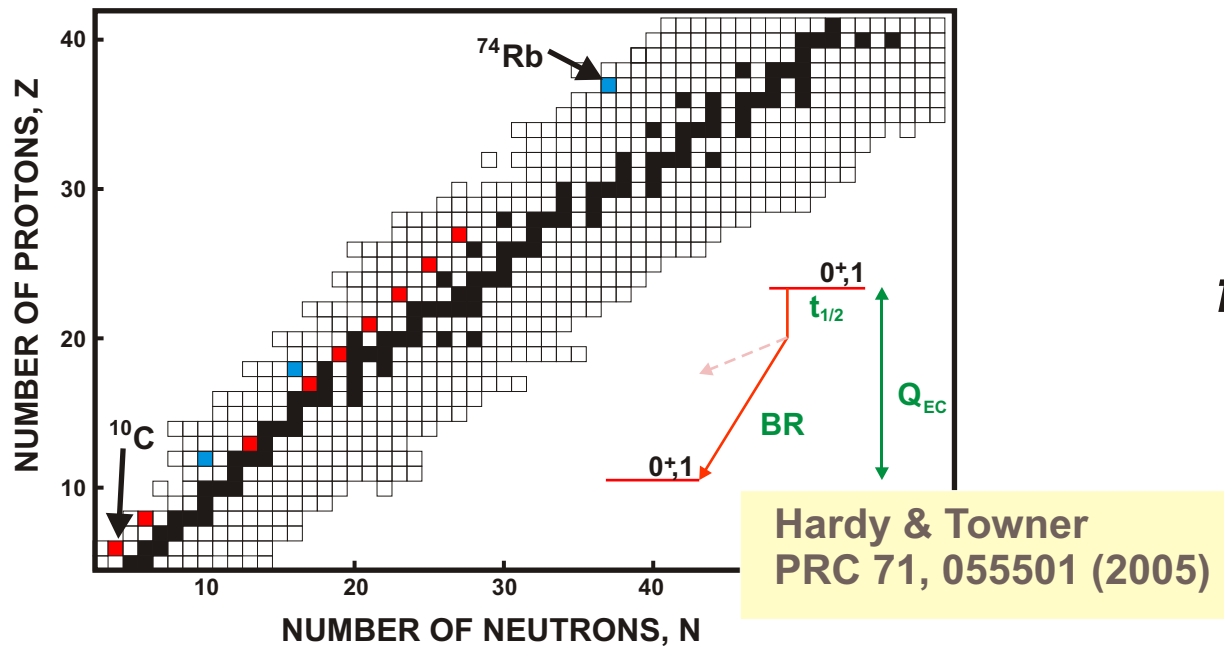
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$$ft (1 + \delta_R)$$

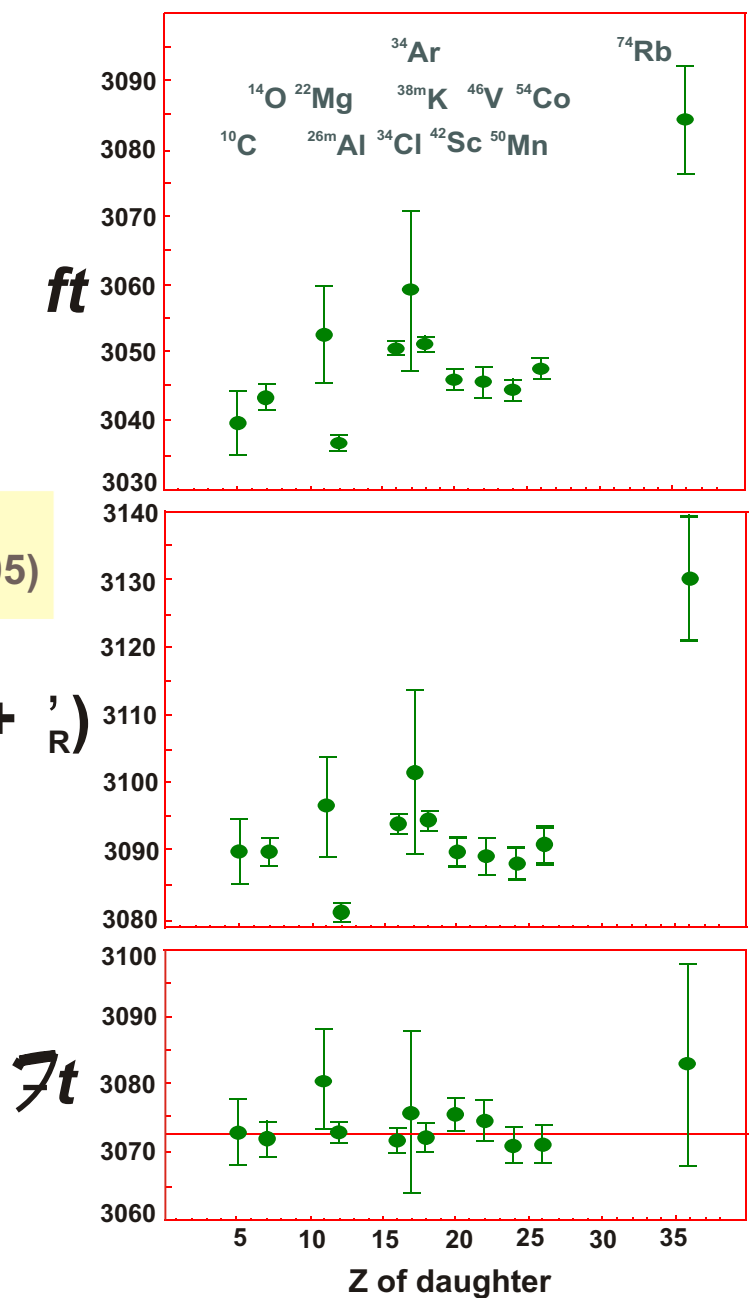
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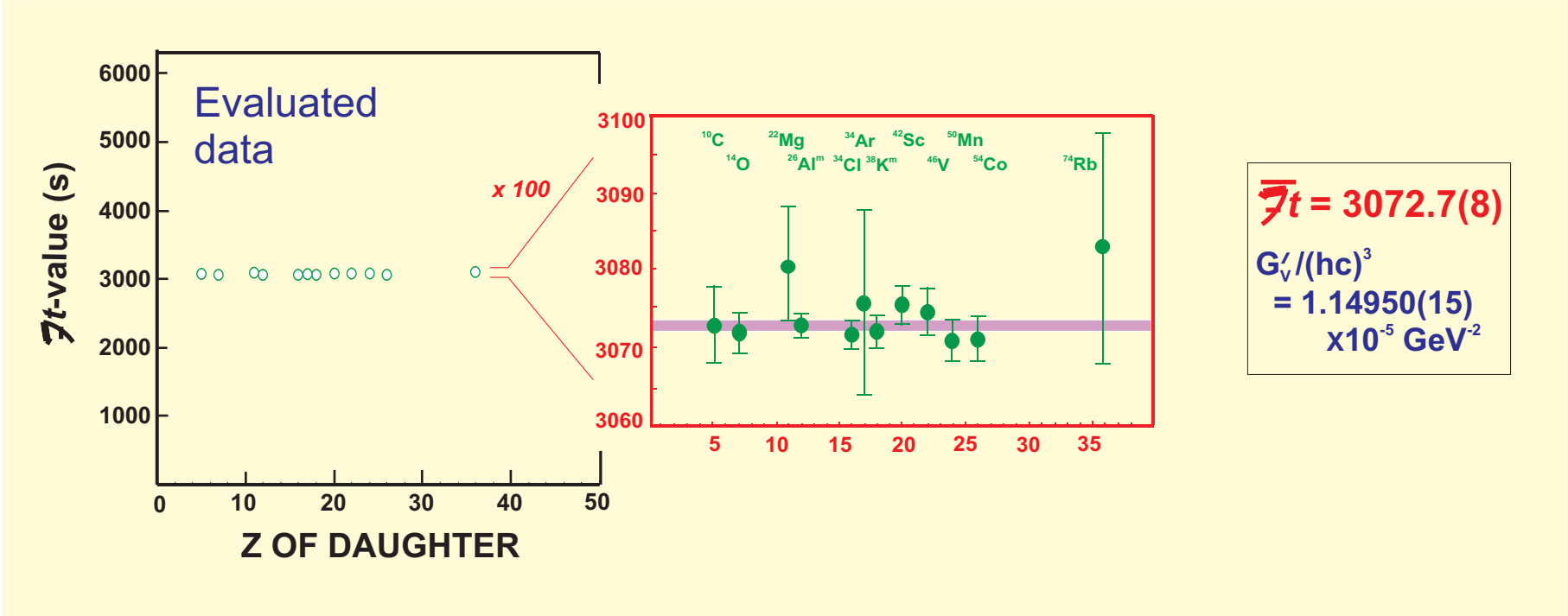
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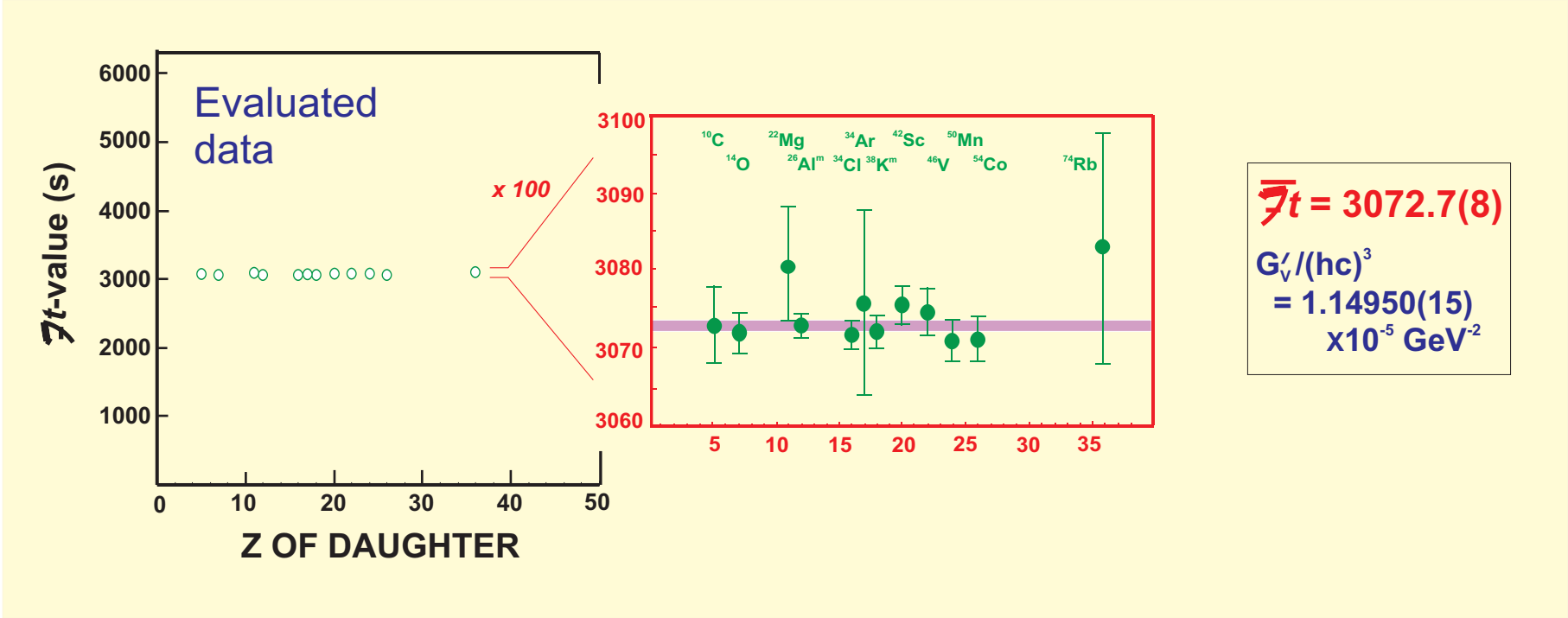


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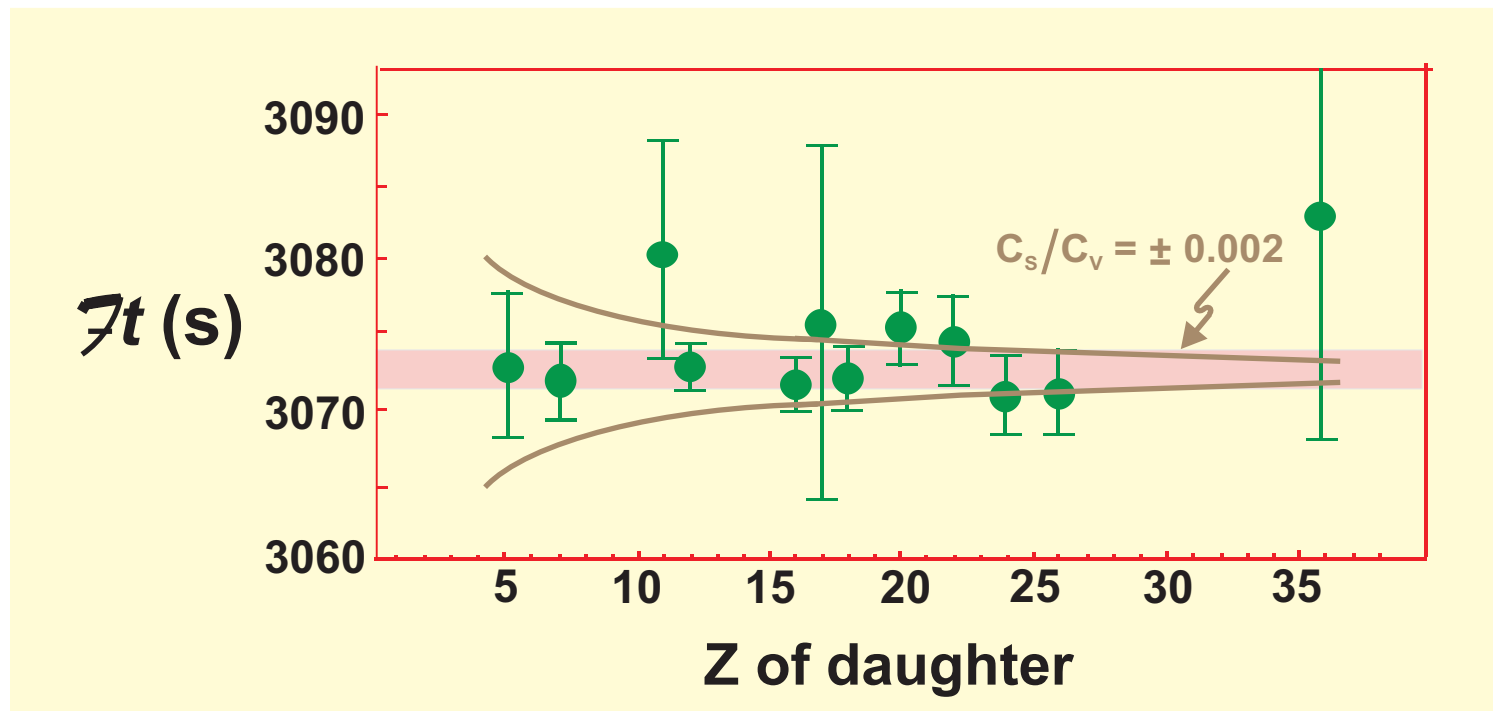
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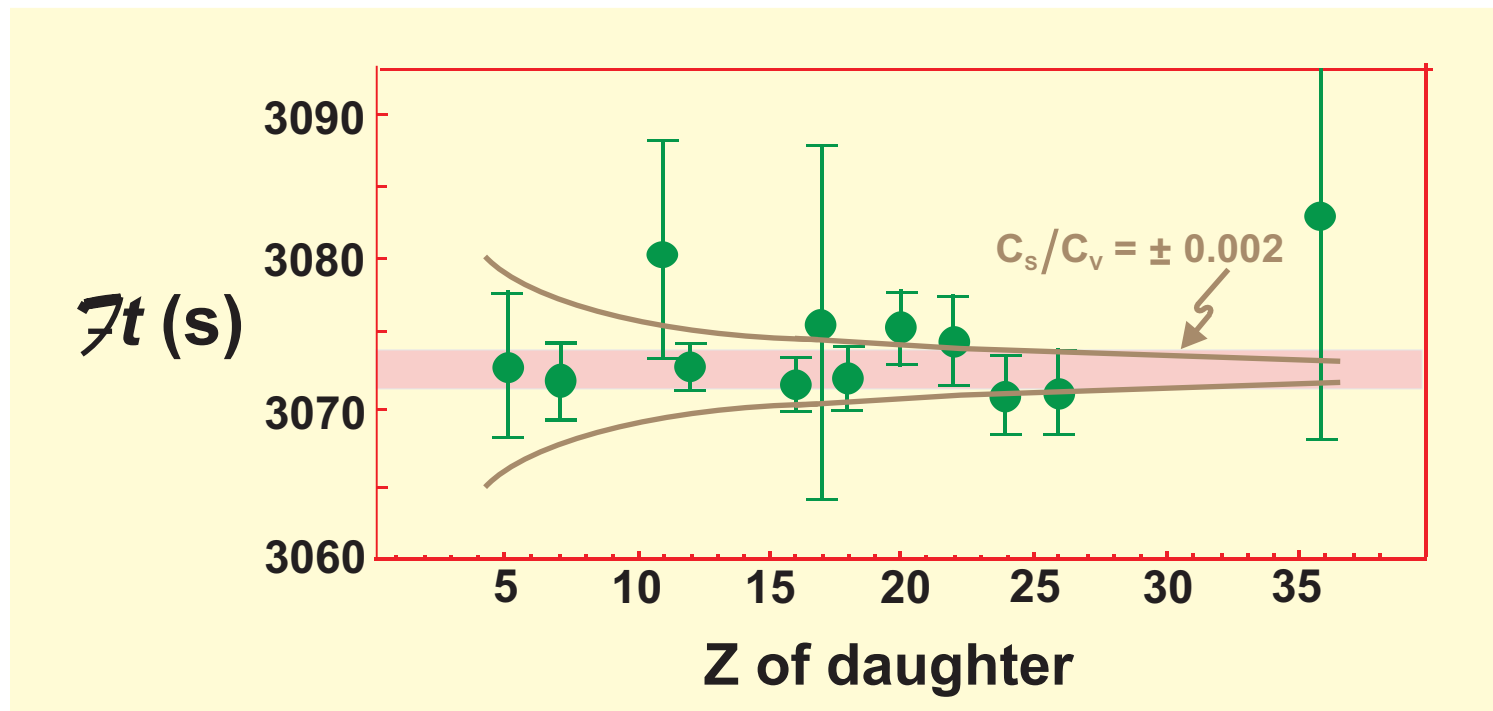
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Compare:

neutron  $V_{ud} = 0.9745 \pm 0.0018$

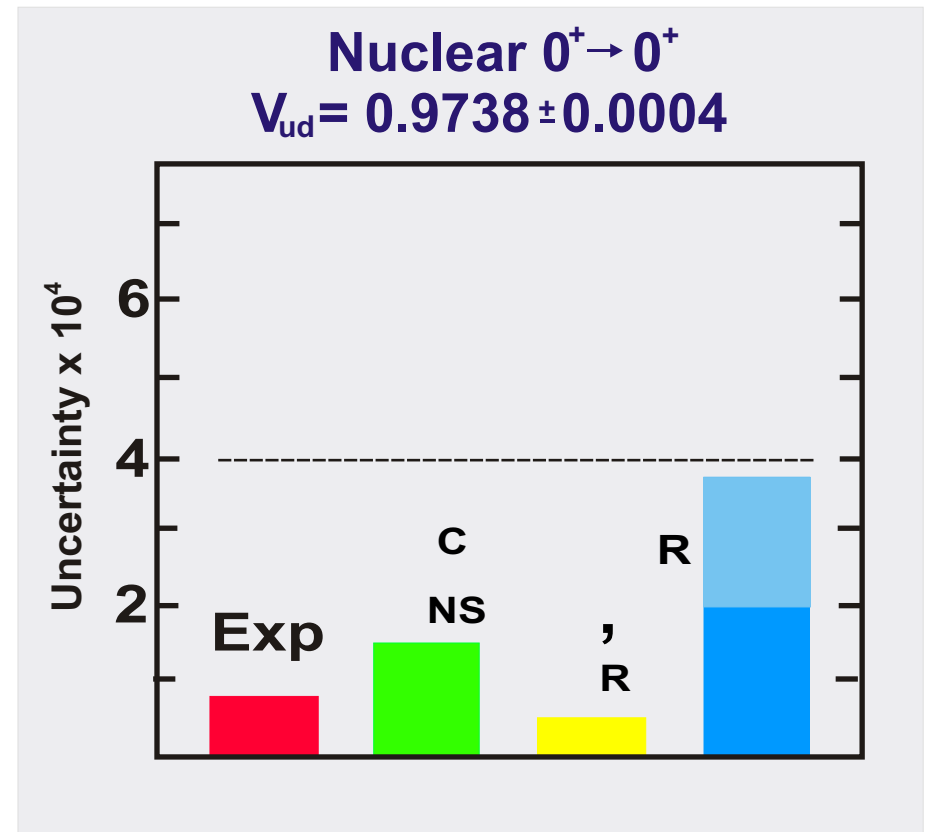
pion  $V_{ud} = 0.9751 \pm 0.0027$

# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS

- Goal is to tighten the window for new physics by reducing the uncertainty on  $V_{ud}$ .

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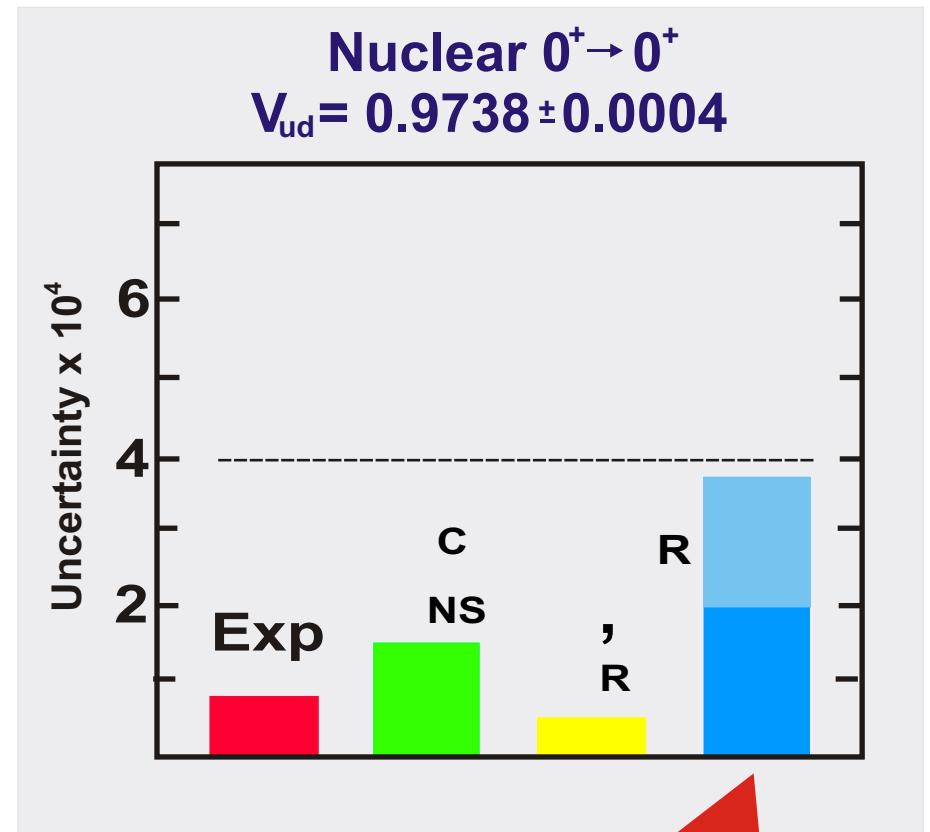




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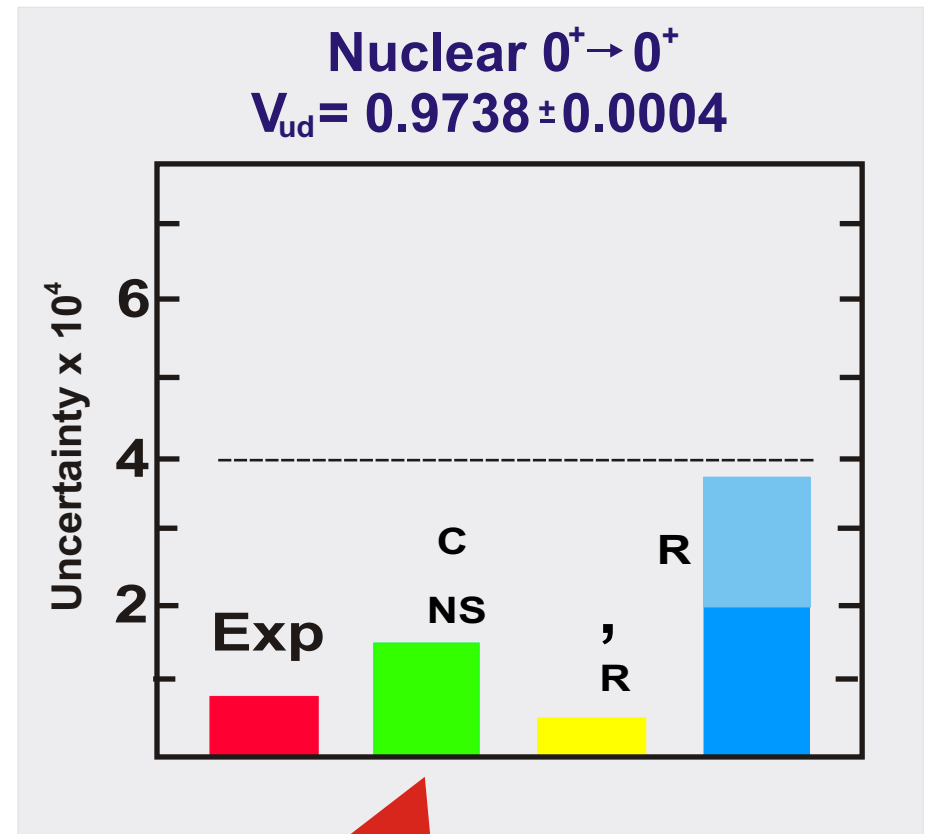
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Marciano & Sirlin  
PRL 96, 032002 (2006)



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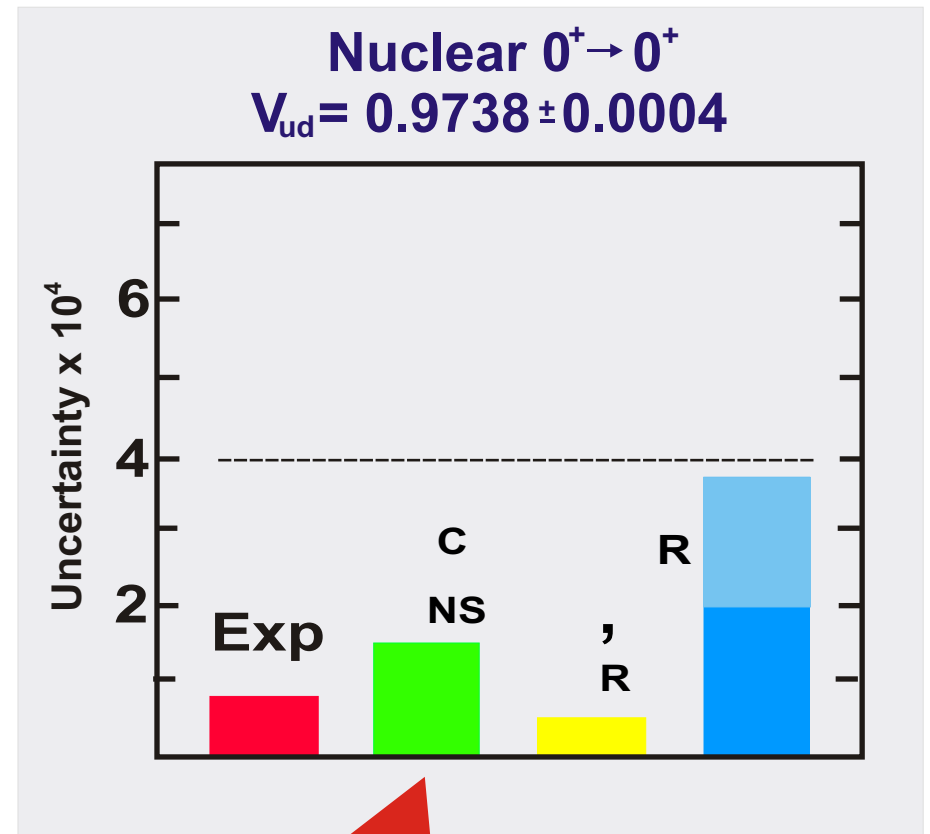
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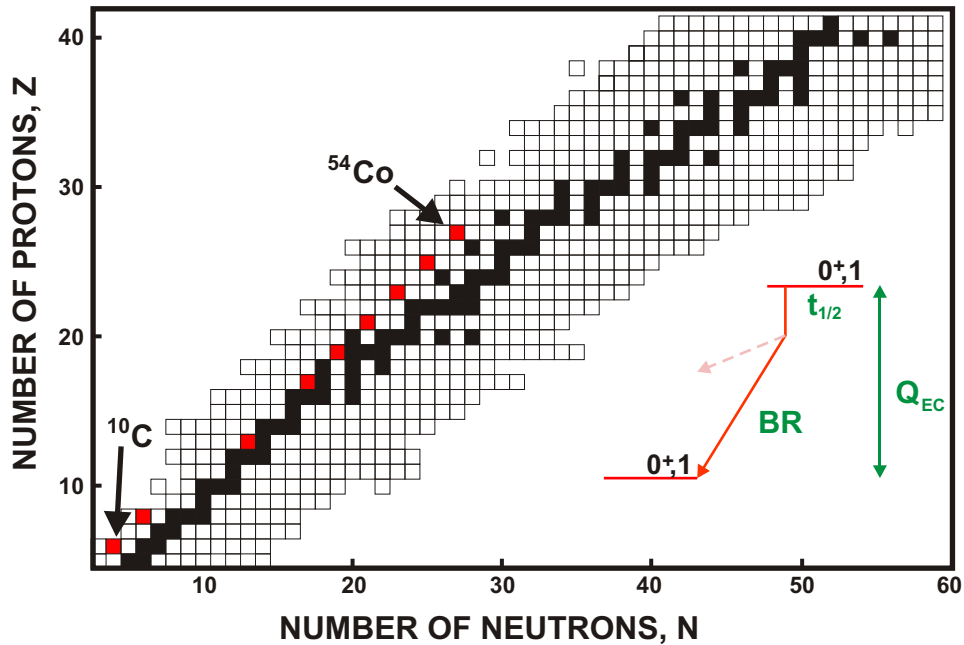
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Well known cases being improved and new cases explored.

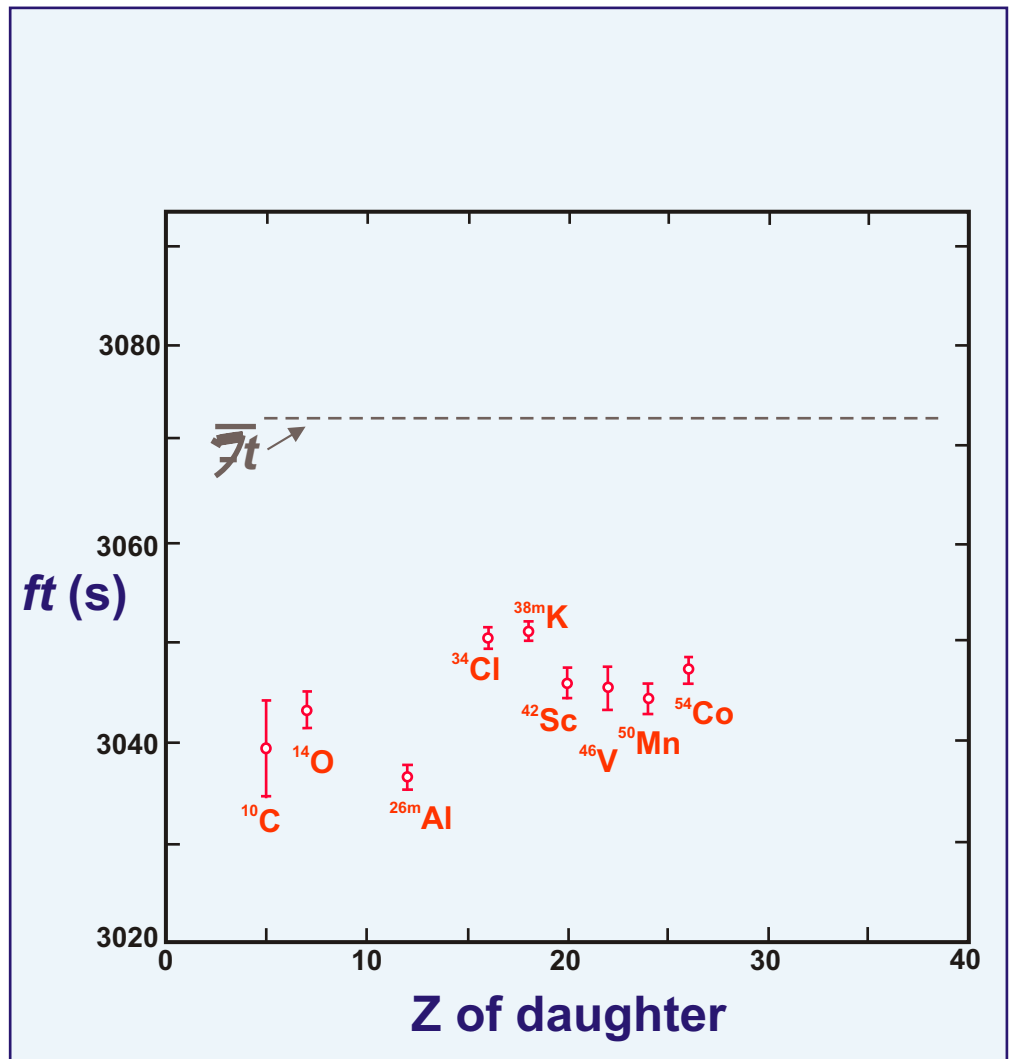


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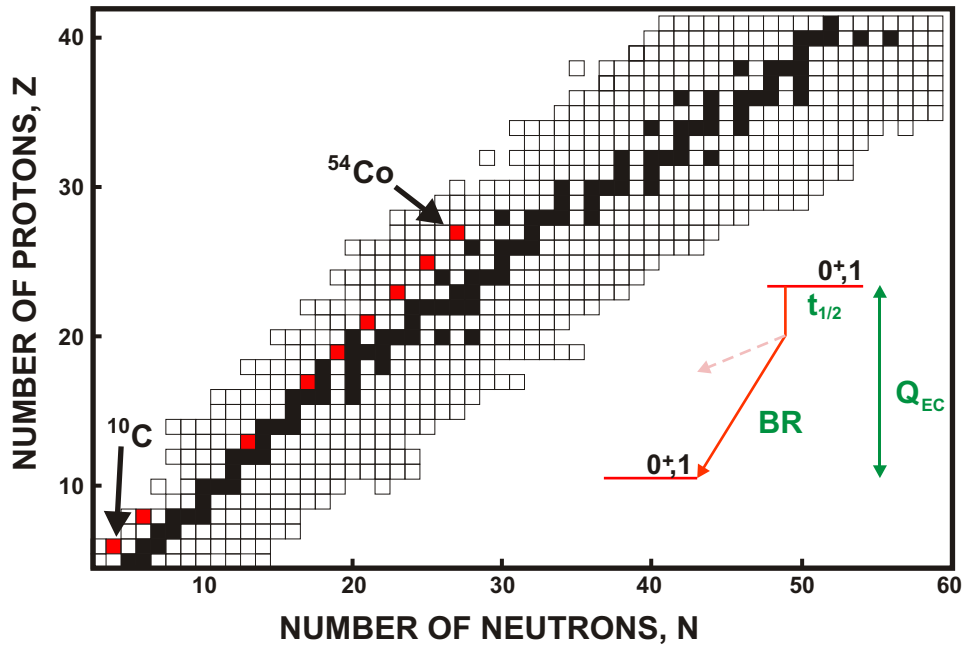


$$\overline{ft} = ft (1 + \frac{R}{R}) [1 - (C - NS)] = \frac{K}{2G_V^2 (1 + R)}$$

Strategy is to probe the nucleus-to-nucleus variation in  $C - NS$



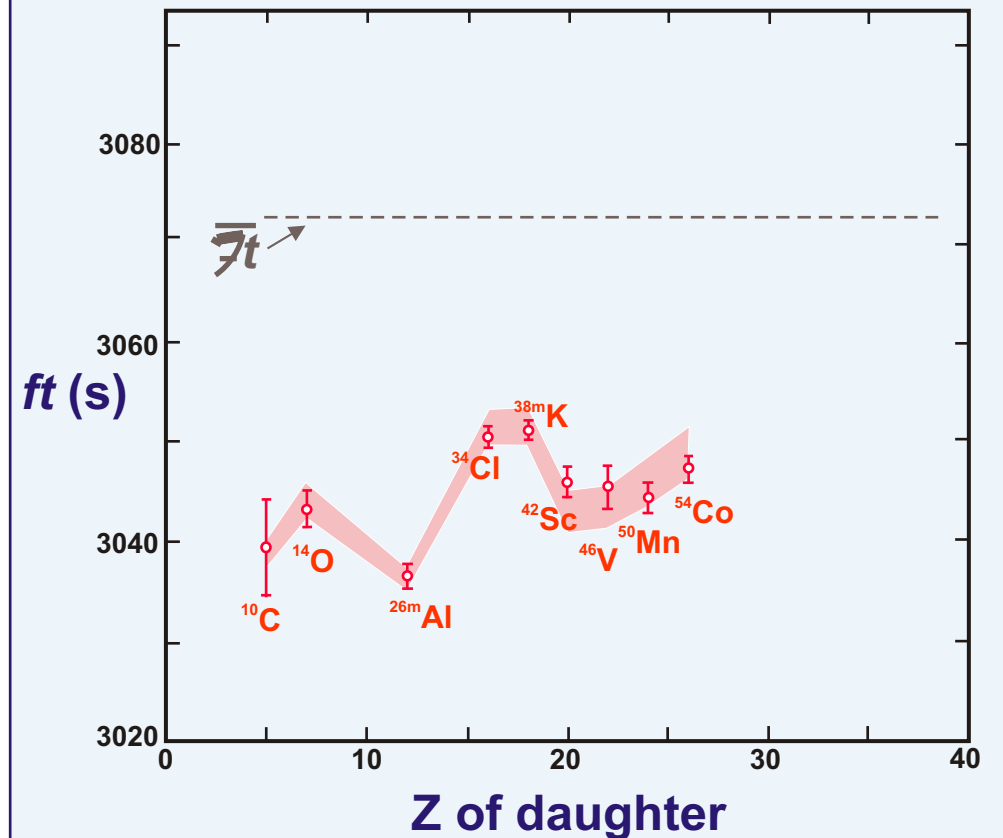
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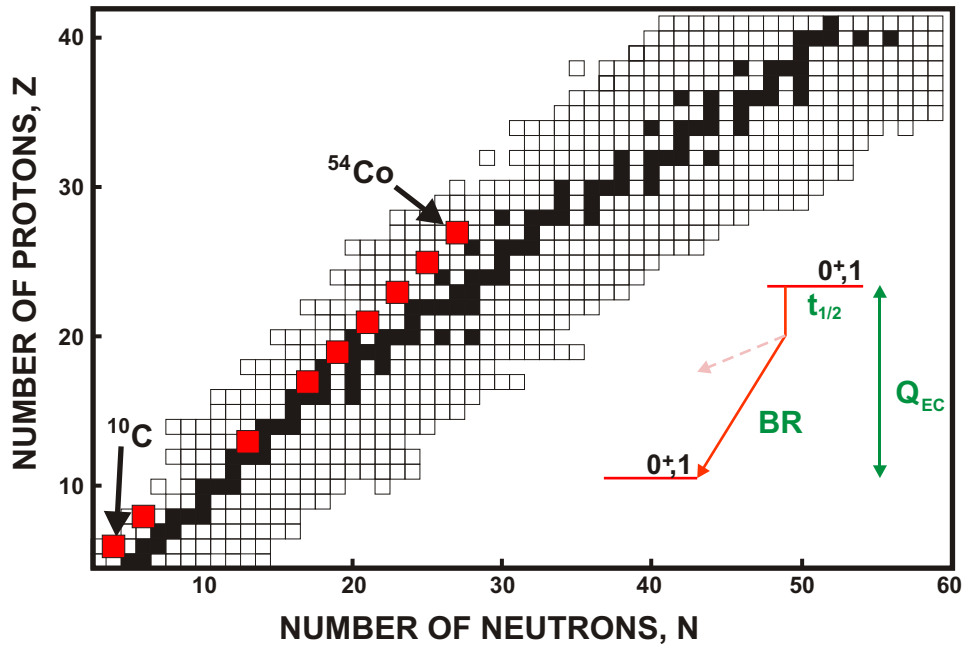
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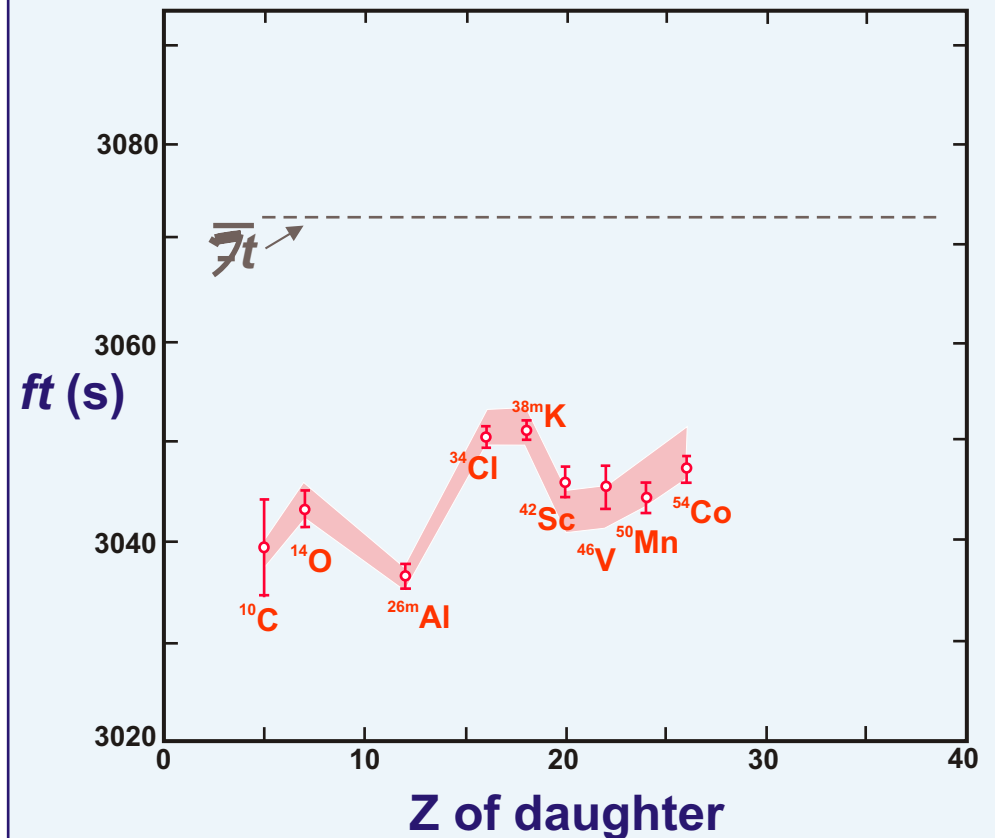
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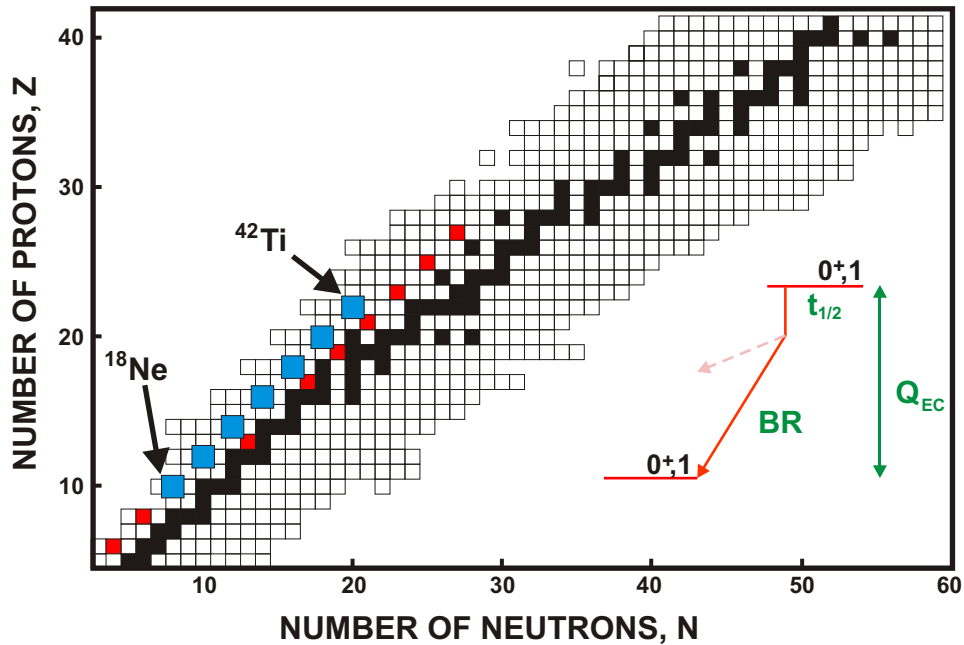
Increase measured precision  
on nine best  $ft$ -values

Strategy is to probe the  
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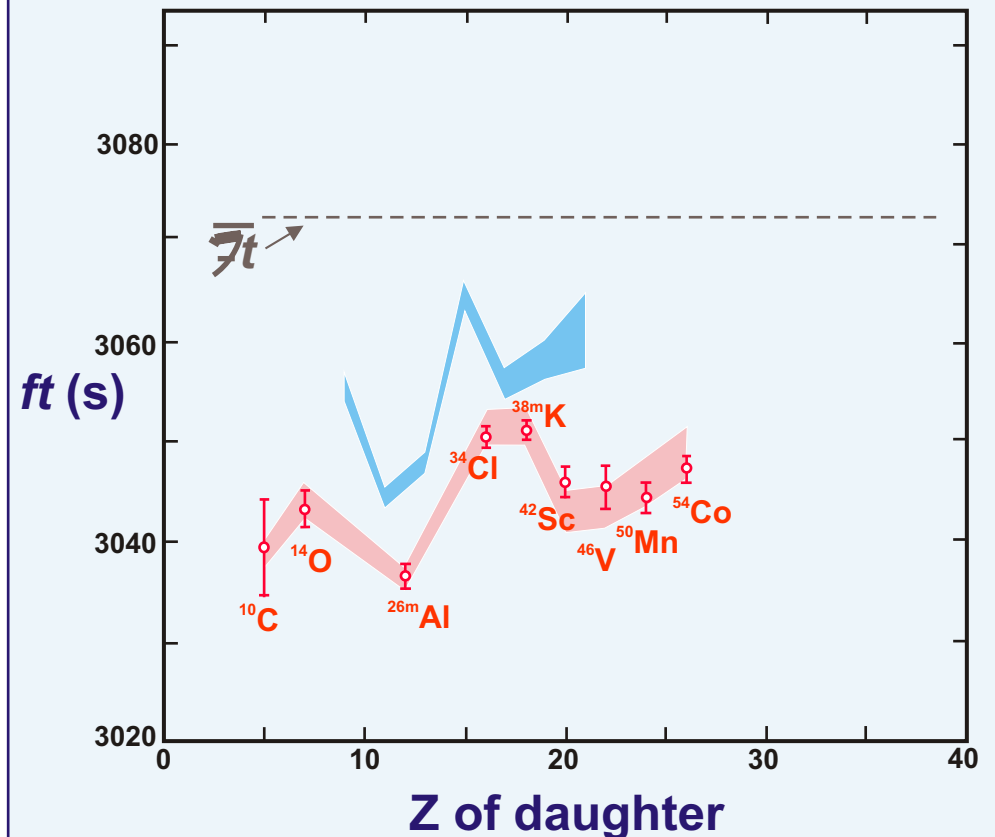


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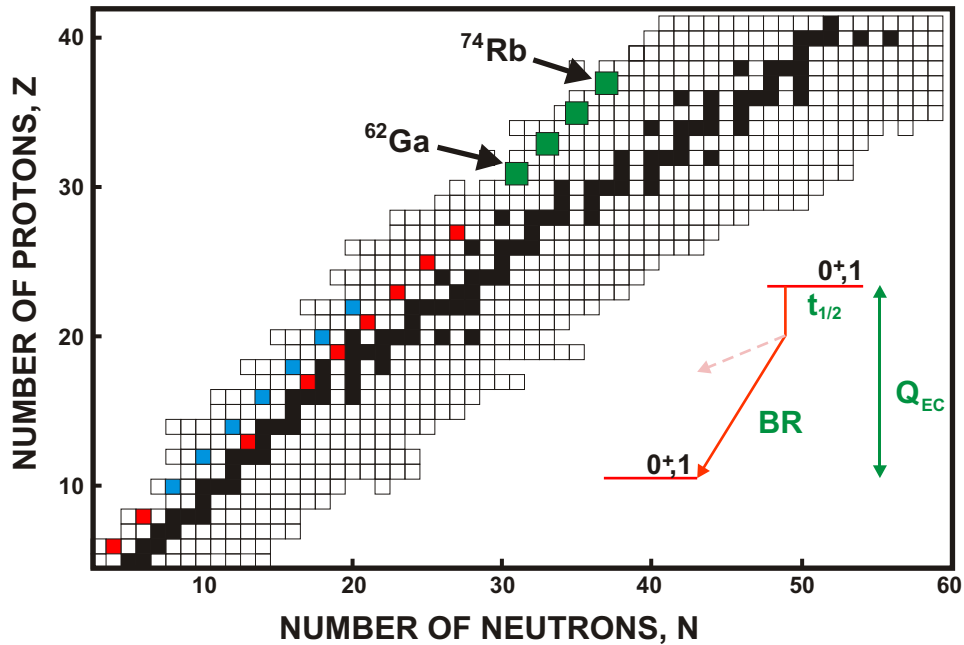
measure new  $0^+ \rightarrow 0^+$  decays  
with  $18 \leq A \leq 42$  ( $T_z = -1$ )

Strategy is to probe the  
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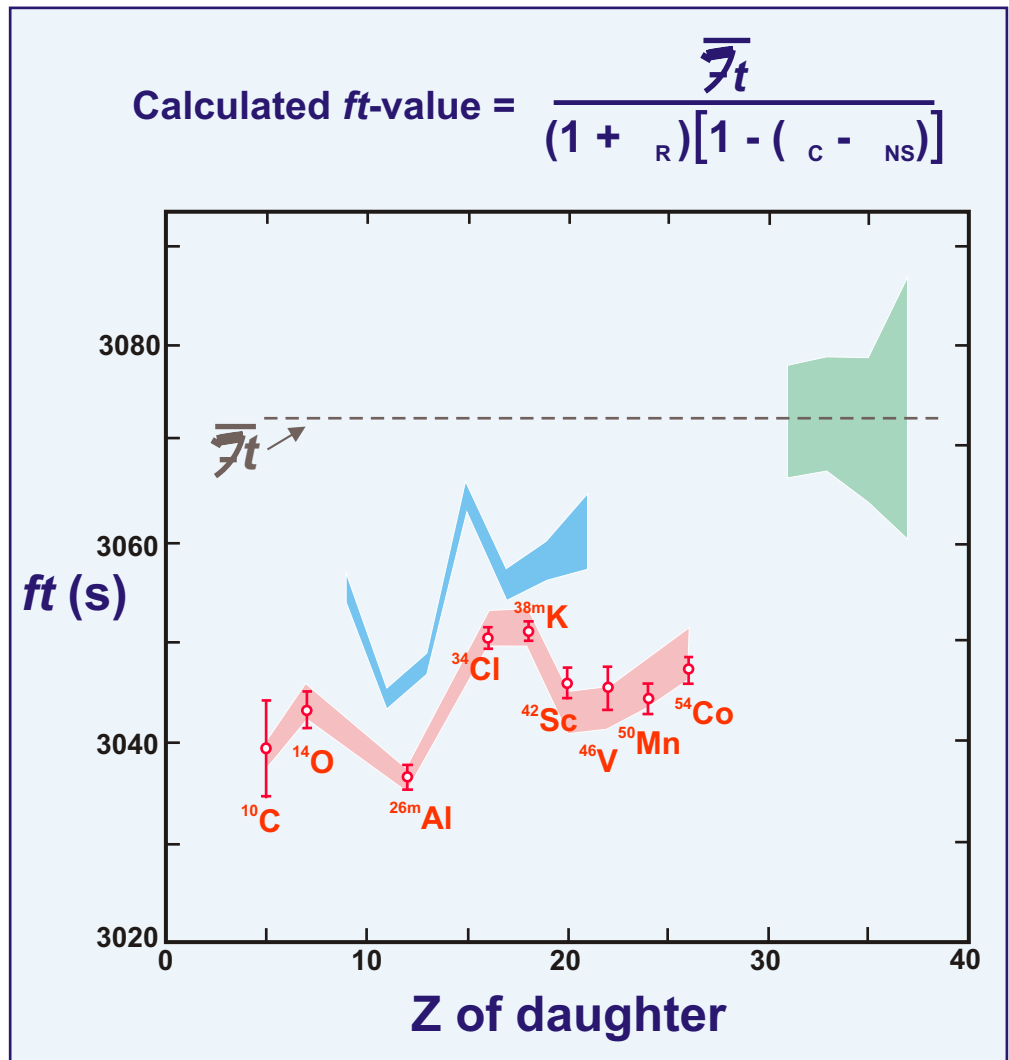


Strategy is to probe the nucleus-to-nucleus variation in  $C - NS$

Increase measured precision on nine best  $ft$ -values

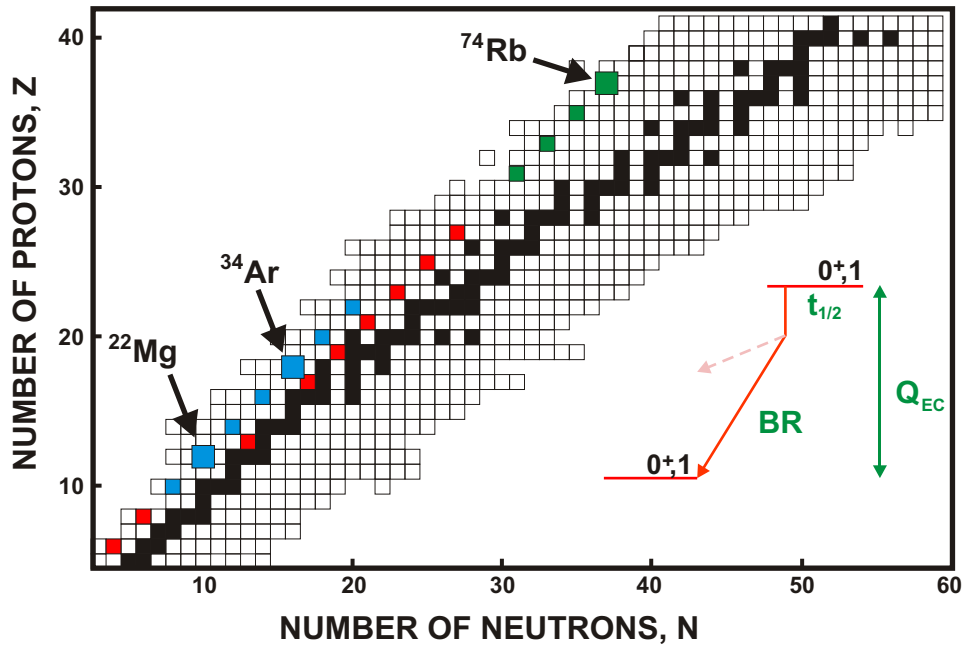
measure new  $0^+ \rightarrow 0^+$  decays with  $18 \leq A \leq 42$  ( $T_z = -1$ )

measure new  $0^+ \rightarrow 0^+$  decays with  $A \geq 62$  ( $T_z = 0$ )





# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS

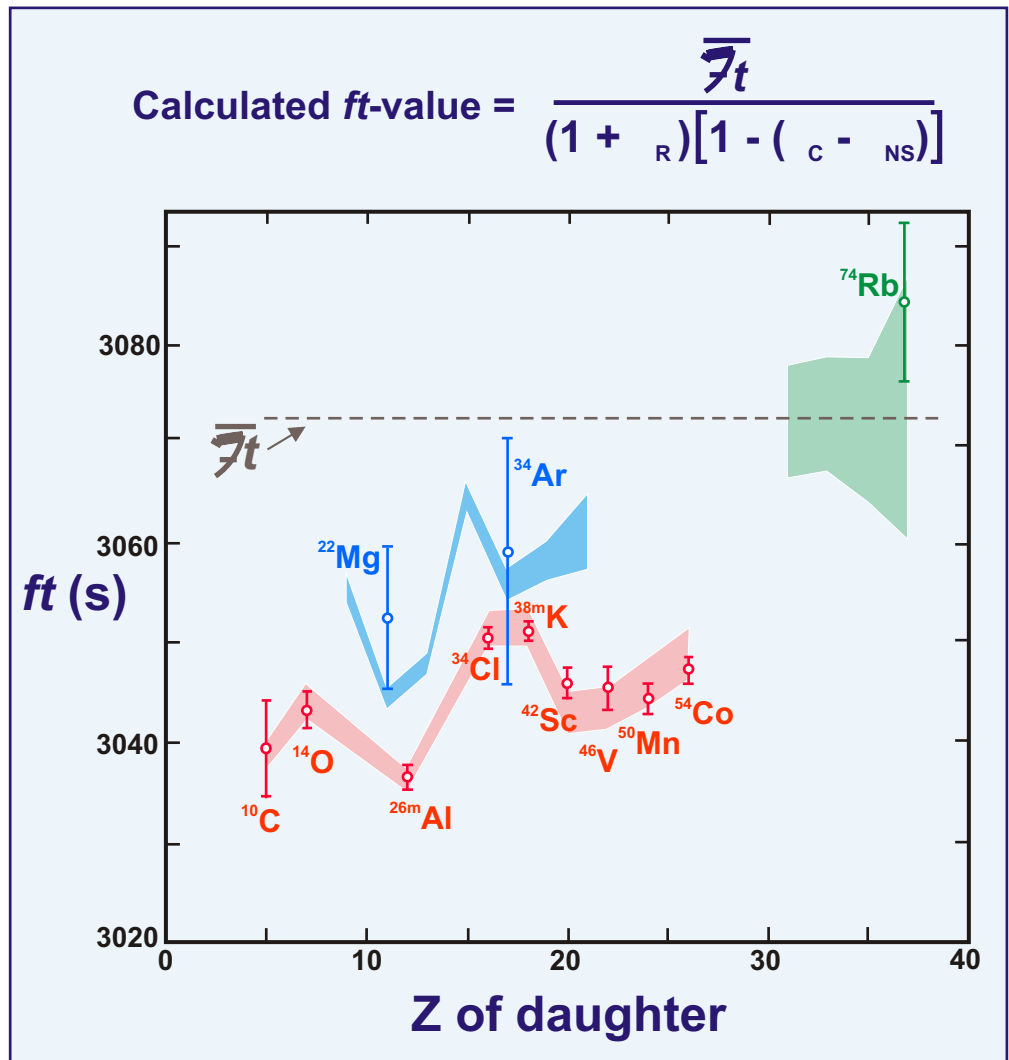


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Strategy is to probe the nucleus-to-nucleus variation in  $C - NS^*$



# RECENT OR CURRENT EXPERIMENTS

## $Q_{EC}$ values:

### Argonne (Canadian Penning trap)

$^{46}\text{V}$  Savard *et al.*, PRL 95, 102501 (2005)

$^{10}\text{C}$ ,  $^{14}\text{O}$ ,  $^{26}\text{Al}^m$ ,  $^{34}\text{Cl}$ ,  $^{42}\text{Sc}$

### Jyvaskyla (JYFLTRAP)

$^{62}\text{Ga}$  Eronen *et al.* PLB 636, 191 (2006)

$^{26}\text{Al}^m$ ,  $^{42}\text{Sc}$ ,  $^{46}\text{V}$  Eronen *et al.*,  
PRL 97, 232501 (2006)

$^{50}\text{Mn}$ ,  $^{54}\text{Co}$

### NSCL (LEBIT)

$^{38}\text{Ca}$  Bollen *et al.*, PRL 96, 152501 (2006)

### Munich Tandem

$^{46}\text{V}$  Faestermann *et al.*, Progress Report

### ISOLTRAP

$^{38}\text{Ca}$  George *et al.*, PRL 98, 162501 (2007)

## Half-lives:

### Auckland/Canberra

$^{50}\text{Mn}$  Barker & Byrne,  
PRC 73, 064306 (2006)

### LBNL

$^{14}\text{O}$  Burke *et al.*,  
PRC 74, 025501 (2006)

### Texas A&M

$^{34}\text{Cl}$ ,  $^{34}\text{Ar}$  Iacob *et al.*,  
PRC 74, 055502 (2006)

$^{10}\text{C}$ ,  $^{38}\text{Ca}$

## Branching ratios:

### TRIUMF

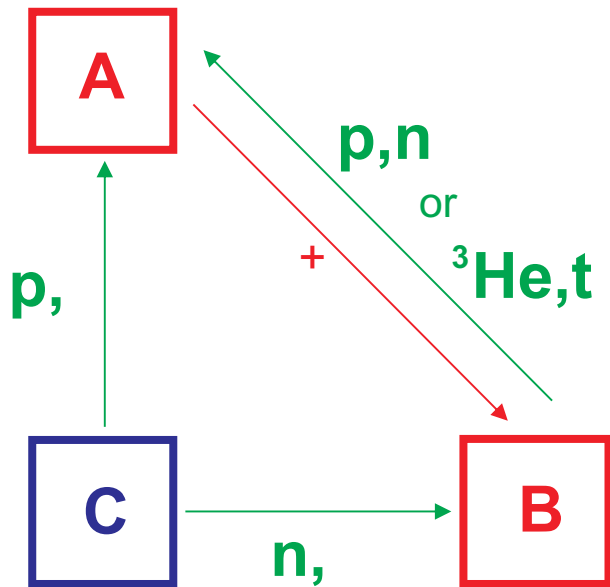
$^{62}\text{Ga}$  Hyland *et al.*,  
PRL 97, 102501 (2006)

### Texas A&M

$^{14}\text{O}$  Towner & Hardy,  
PRC 72, 055501 (2005)

$^{34}\text{Ar}$ ,  $^{38}\text{Ca}$

# METHODS USED FOR PRECISION MEASUREMENTS OF $Q_{EC}$



- $B(p,n)A$  threshold:  $p$  energy referred to standard volt.

$\pm 120$  eV

Auckland:

e.g. Phys. Rev. **C58** (1998) 821.

- $C(p, )A$  and  $C(n, )B$ ,  $Q$  value difference:  $p$  energy calibrated to known  $(p, )$ .

$\pm 100$ -200 eV

Oak Ridge/Utrecht:

e.g. Nucl. Phys. **A529** (1991) 39.

- $B(^3\text{He},t)A$  and  $B'(^3\text{He},t)A'$ ,  $Q_{EC}$  doublet: difference measured with voltmeter.

$\pm 130$ -200 eV

Chalk River:

e.g. Nucl. Phys. **A472** (1987) 419.

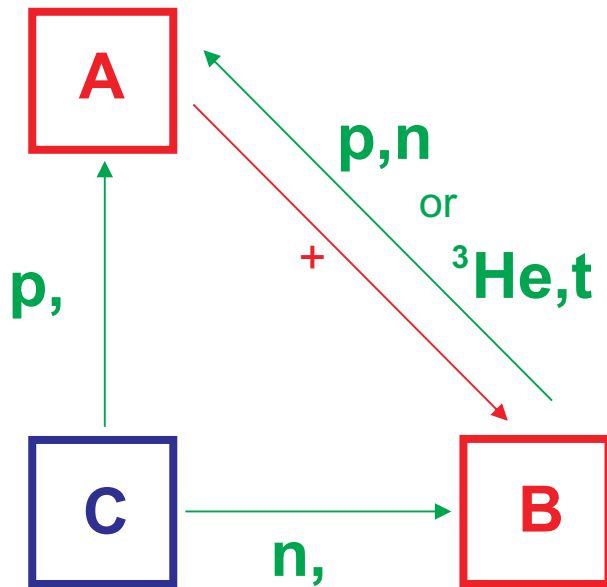
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$\pm 50$ -400 eV

e.g. Argonne (CPT):

Phys. Rev. Lett. **95** 102501 (2005).

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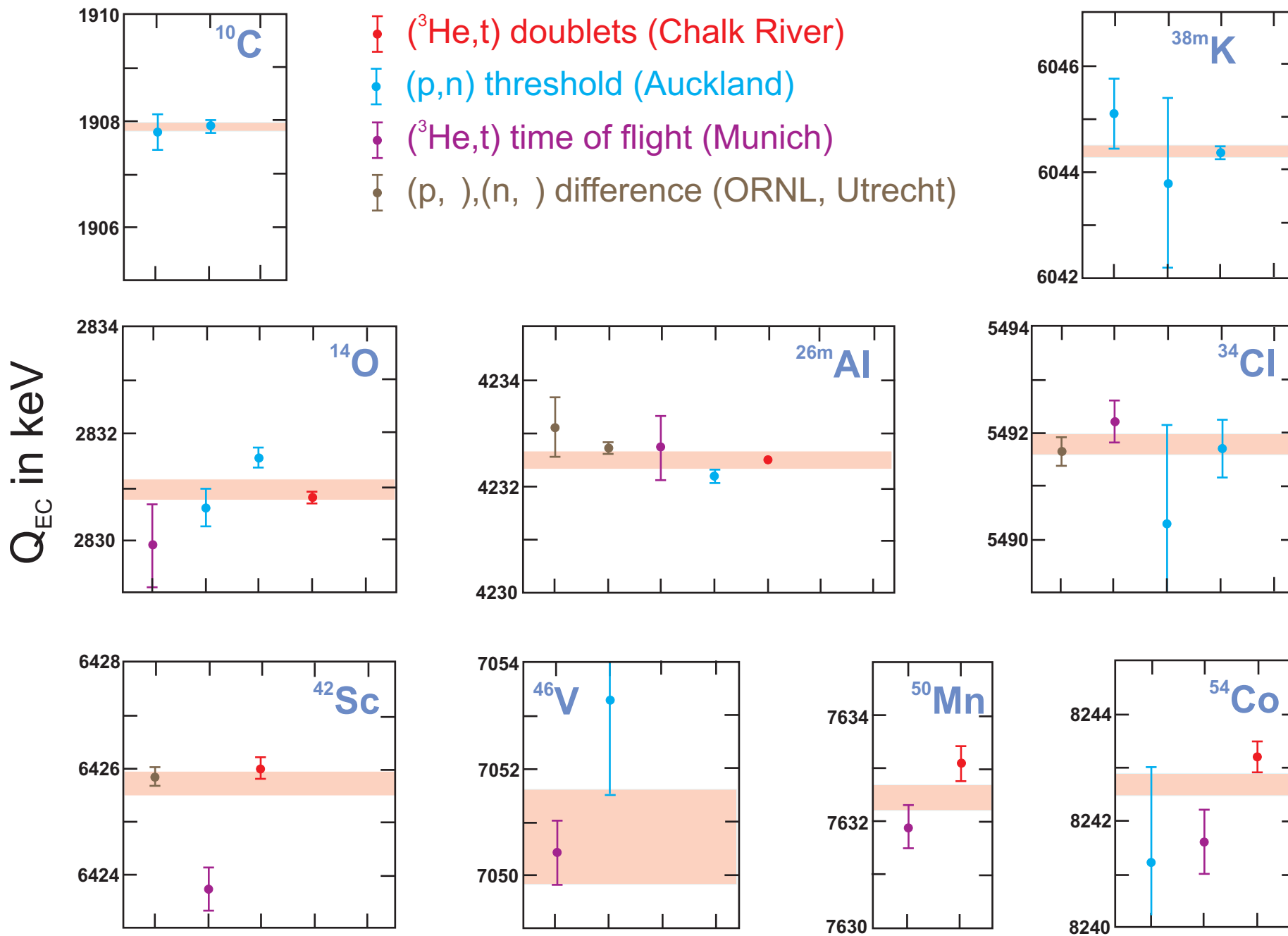
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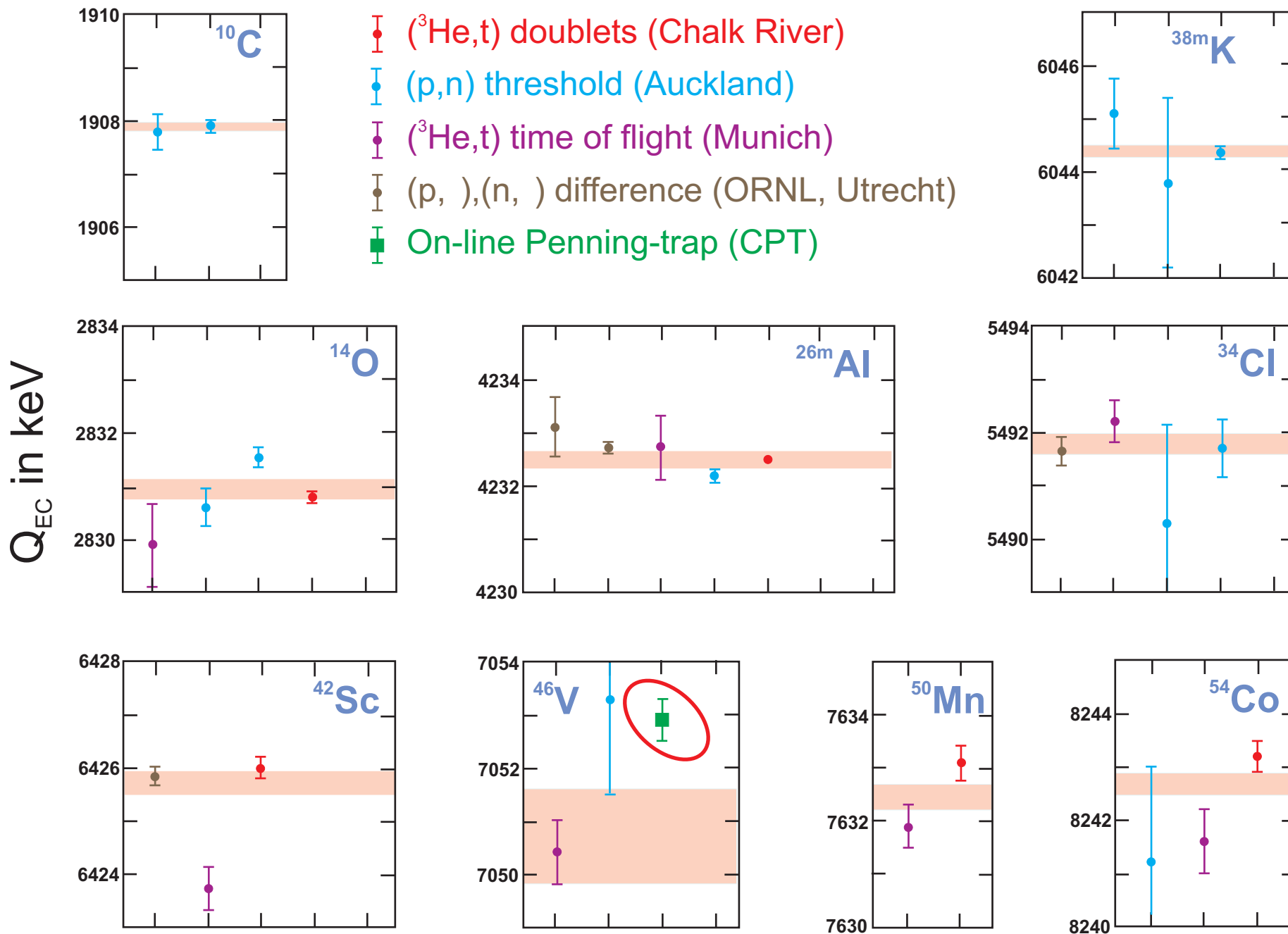
e.g. Argonne (CPT):

Phys. Rev. Lett. **95** 102501 (2005).

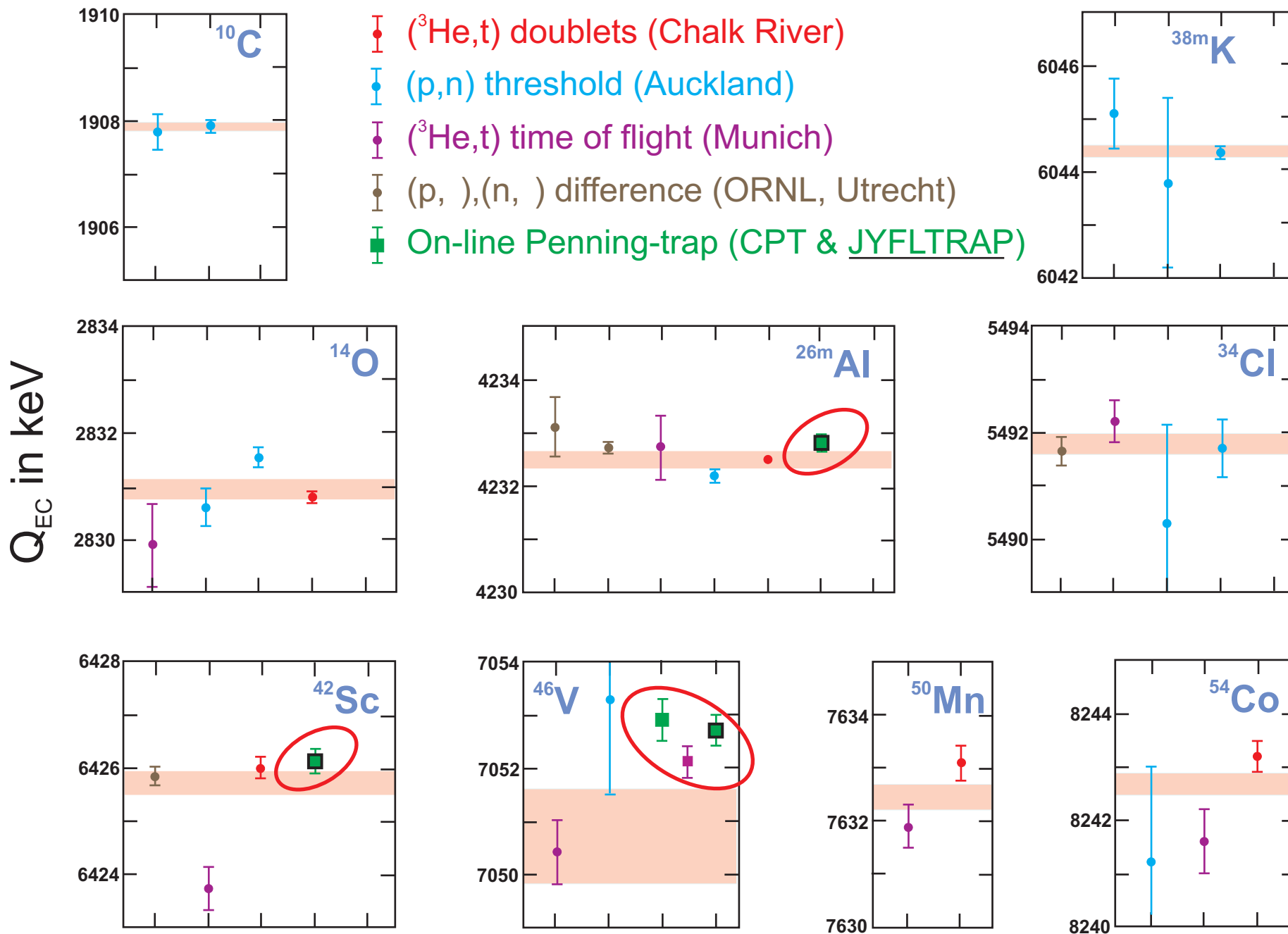
# $Q_{EC}$ FOR SUPERALLOWED TRANSITIONS (keV)



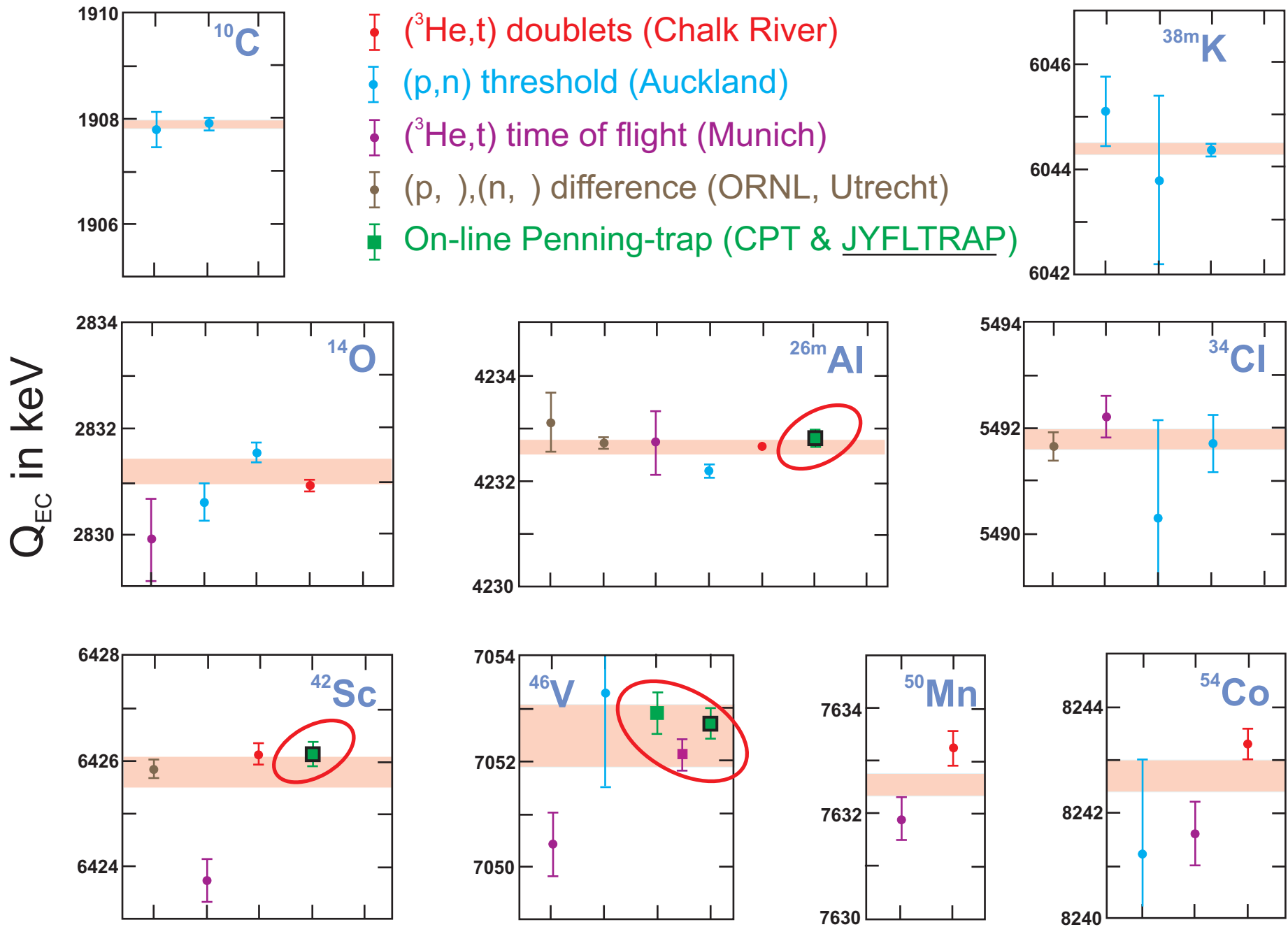
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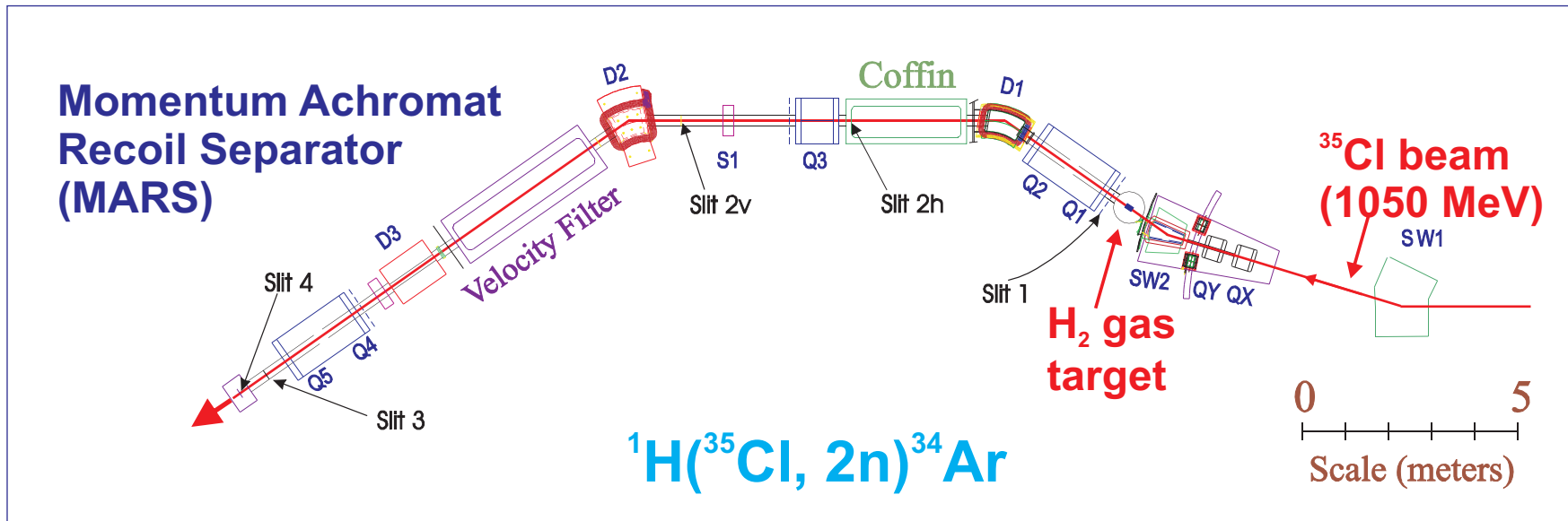


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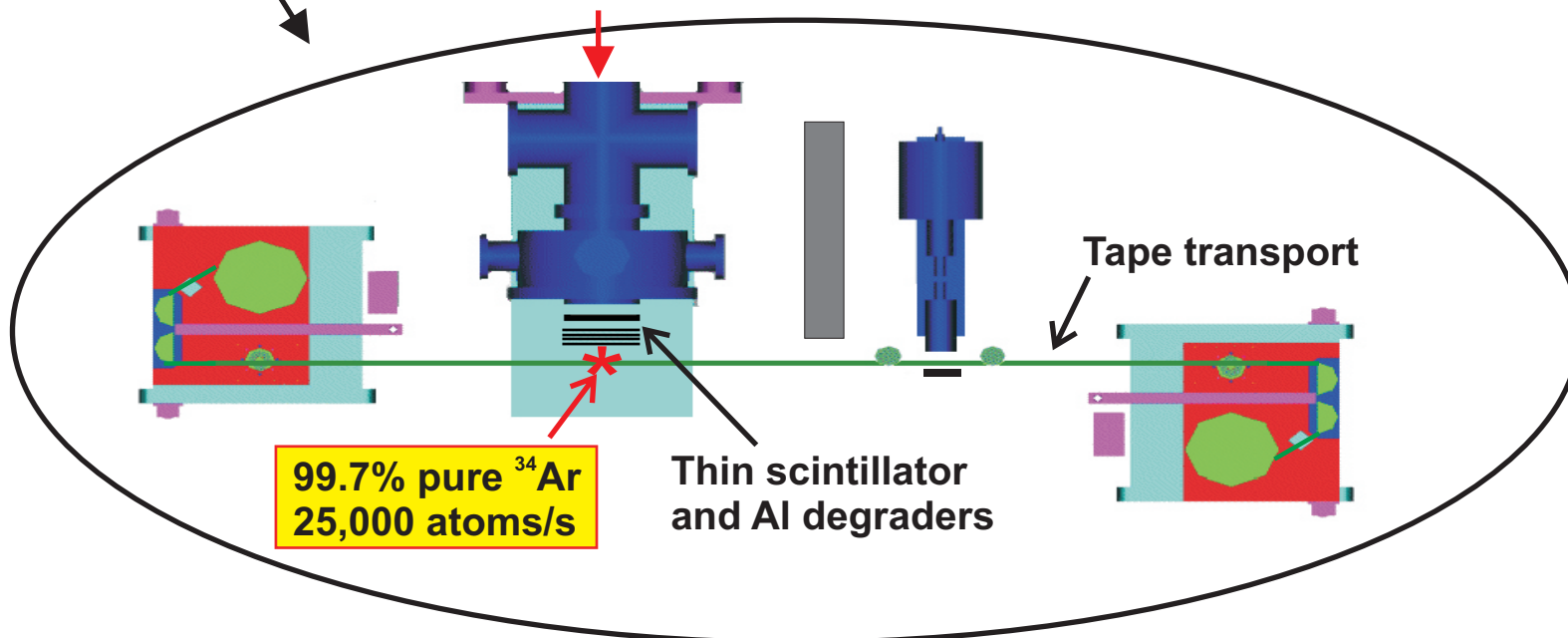
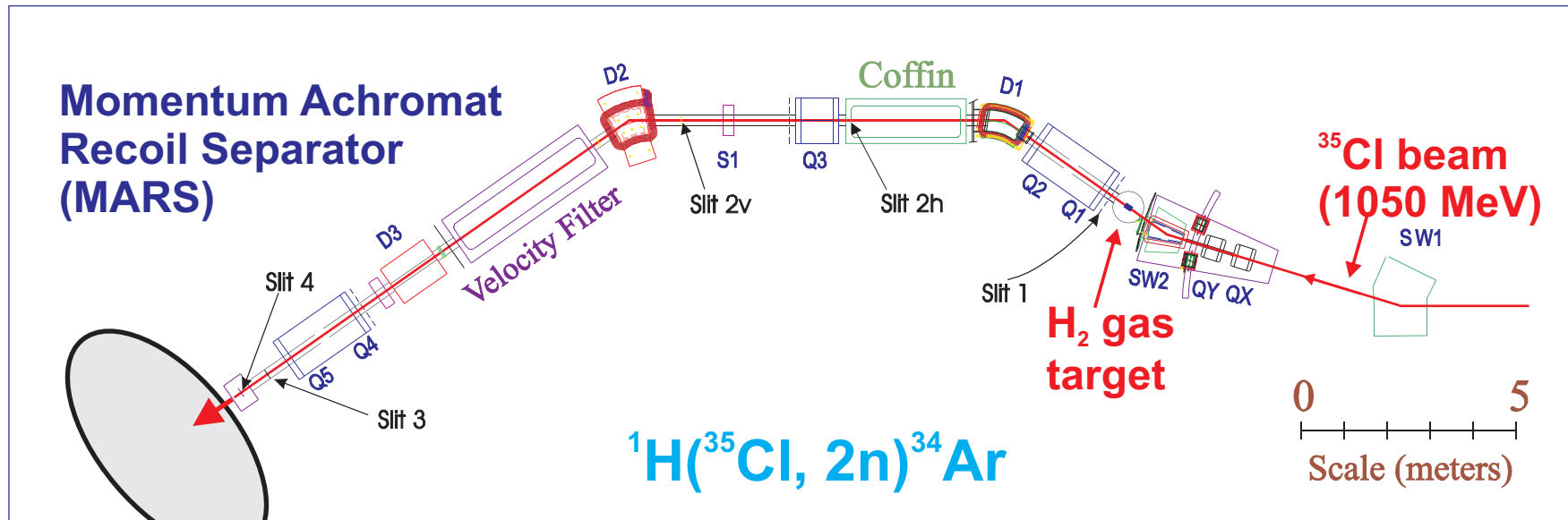




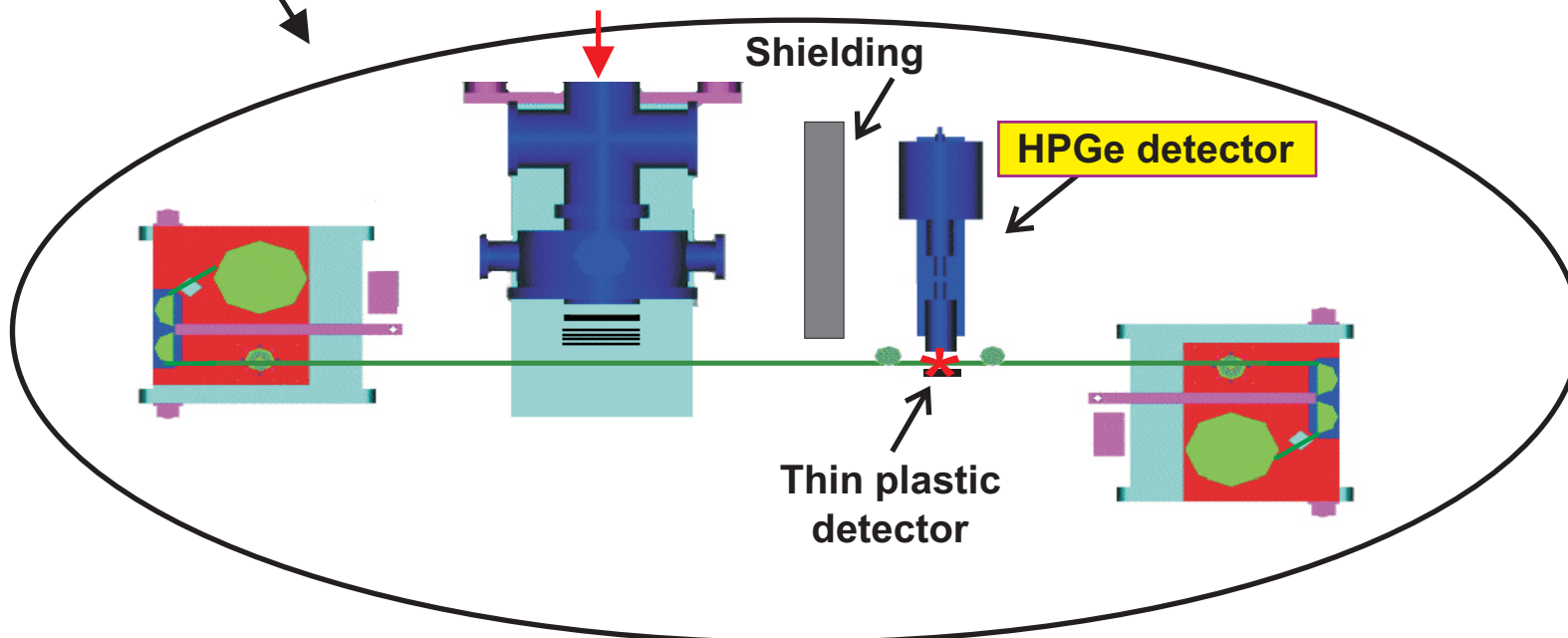
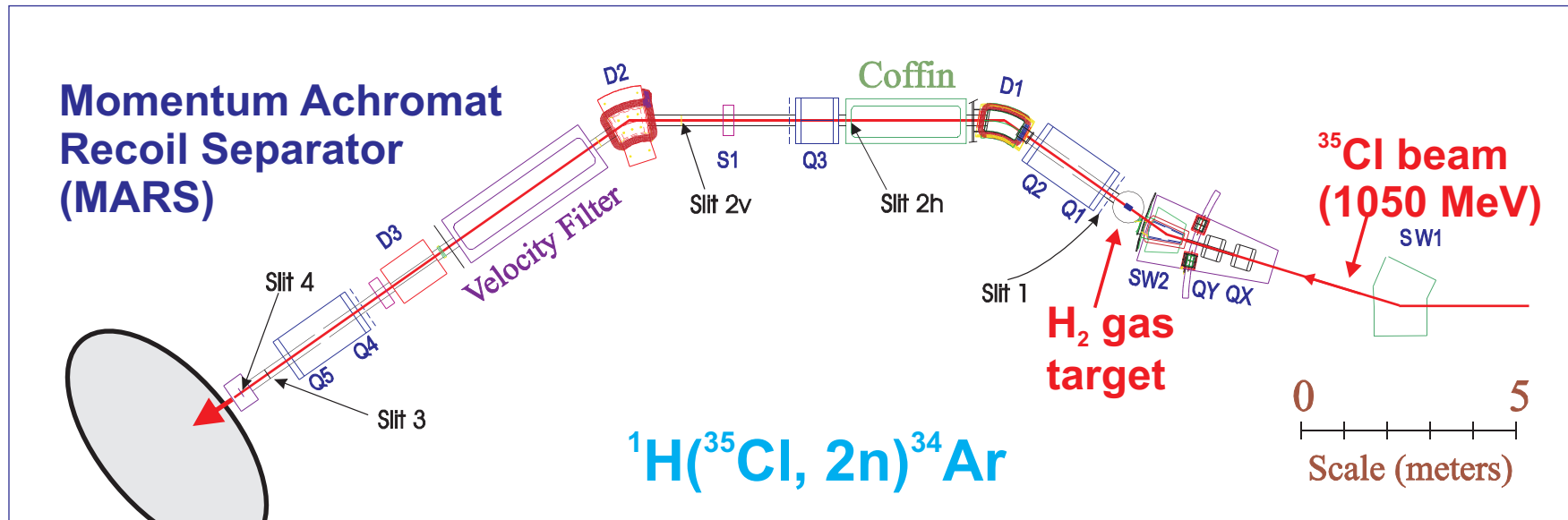
# PRECISION DECAY MEASUREMENTS AT TAMU



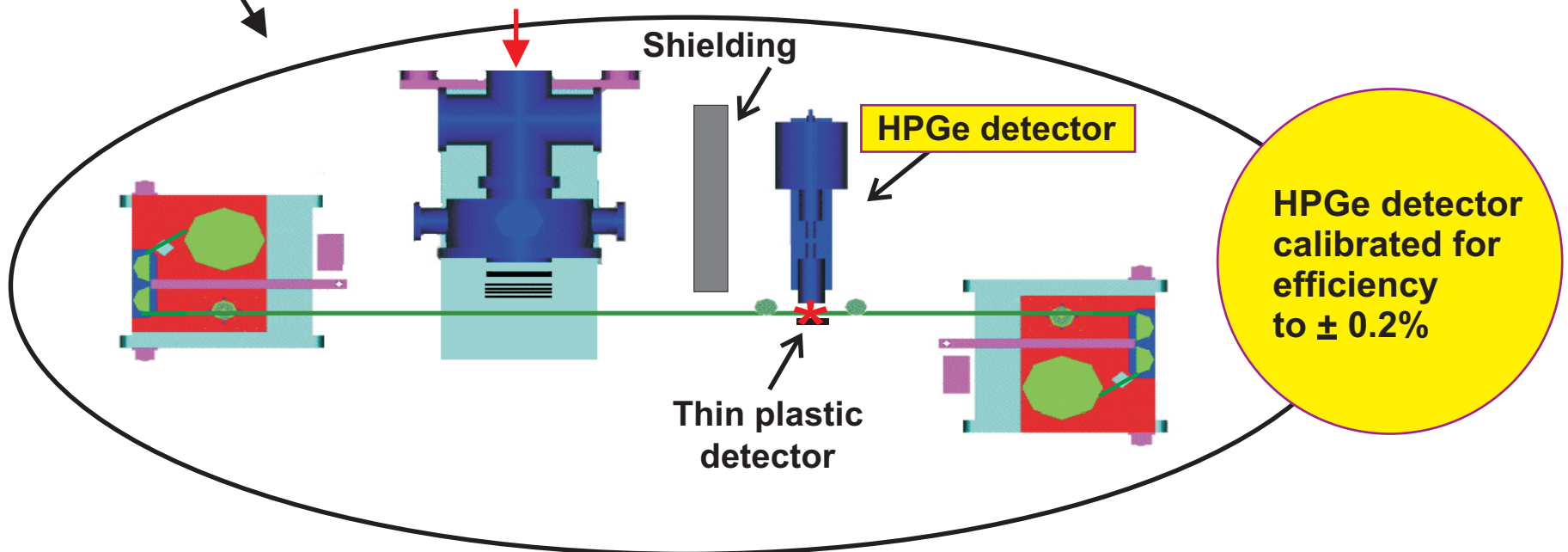
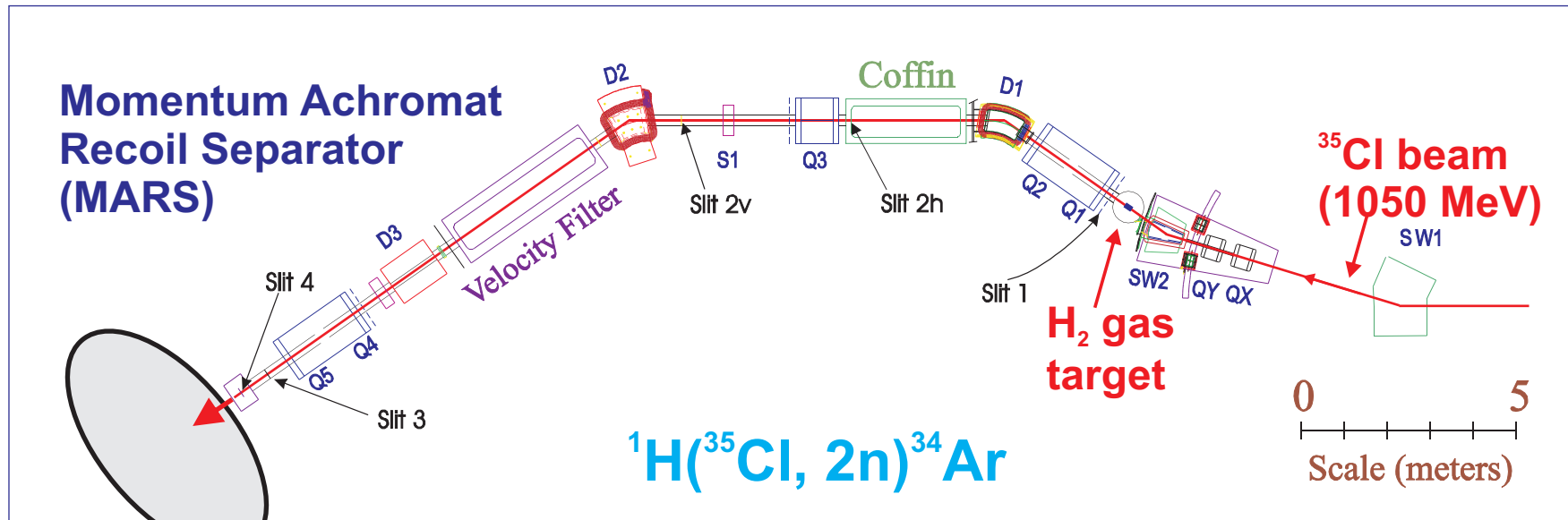
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# DETECTOR EFFICIENCY

$50 \text{ keV} < E < 1.4 \text{ MeV}$

Source measurements

vs

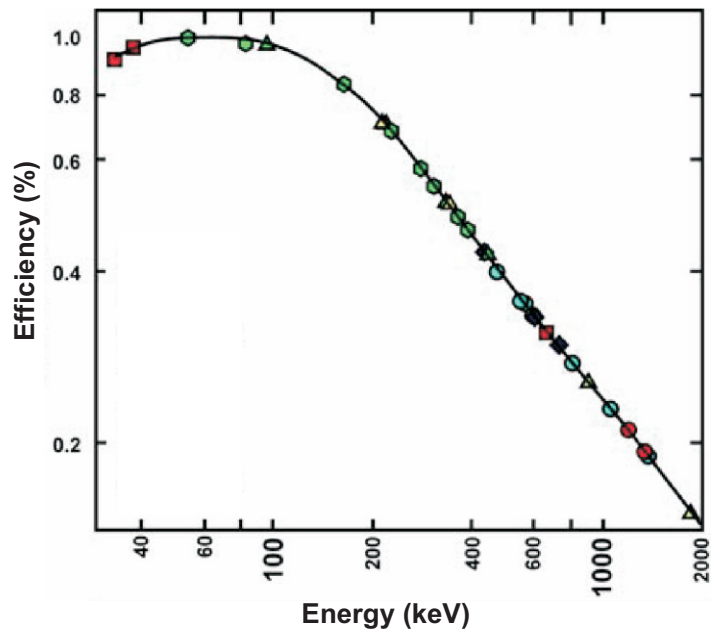
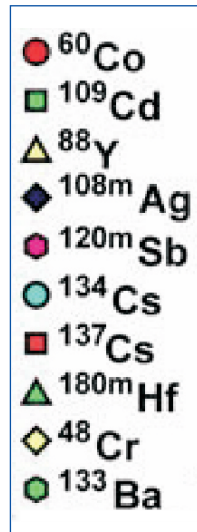
unscaled Monte Carlo  
calculations (CYLTRAN)

Physical properties and  
location of HPGe crystal  
measured precisely

10 sources recorded

4 key sources, 3 locally  
made, have pure cascades

$^{60}\text{Co}$  source from PTB with  
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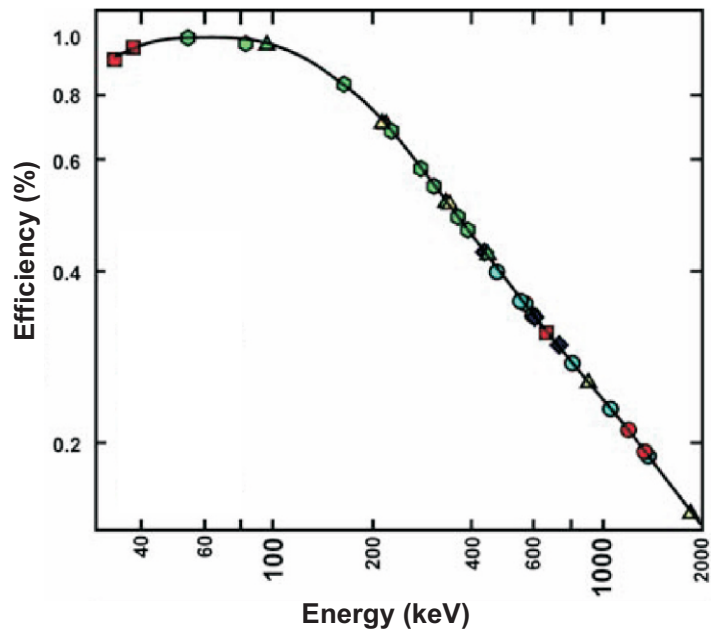
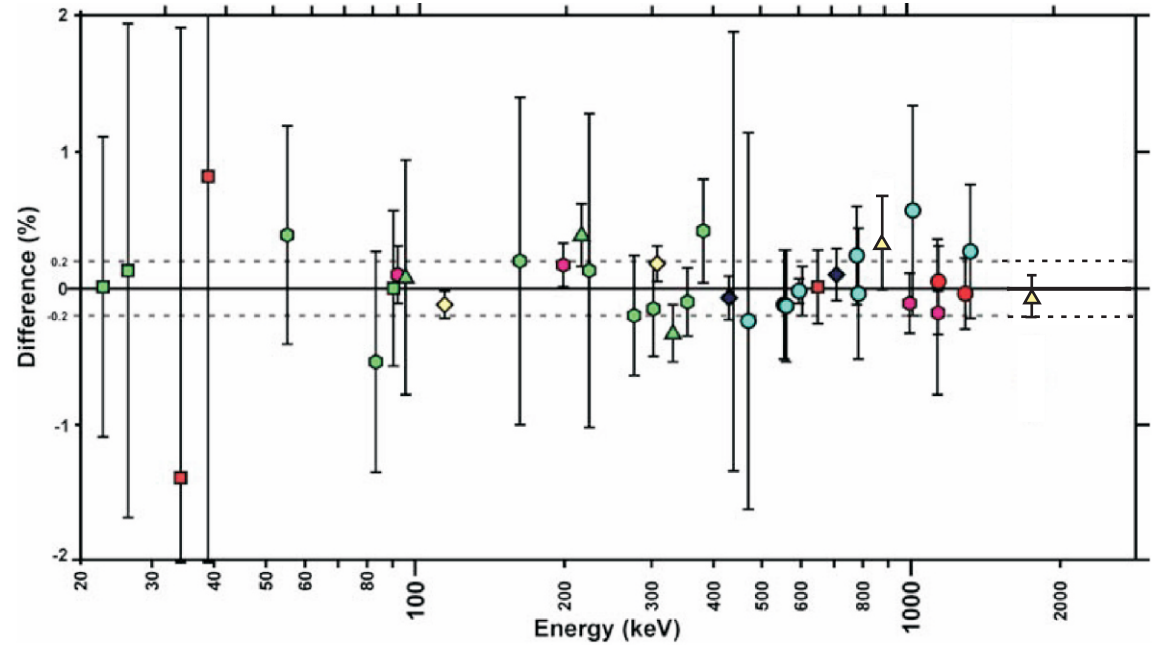
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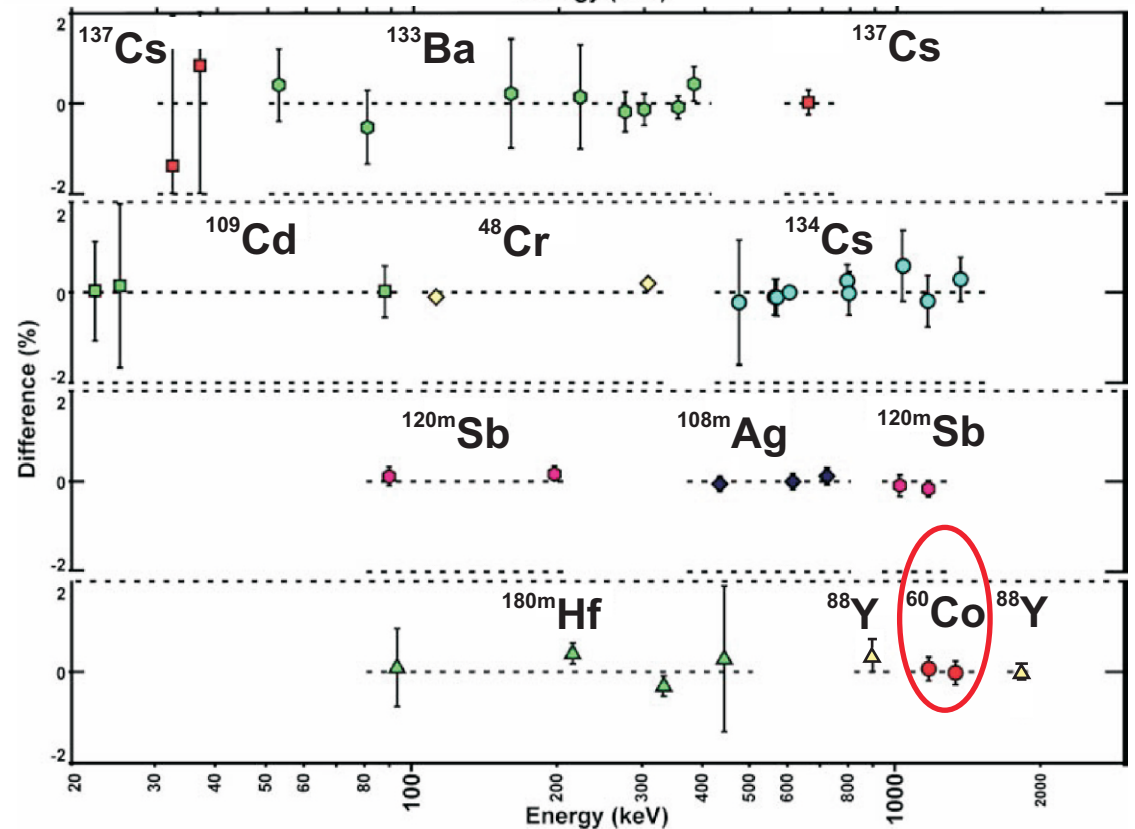
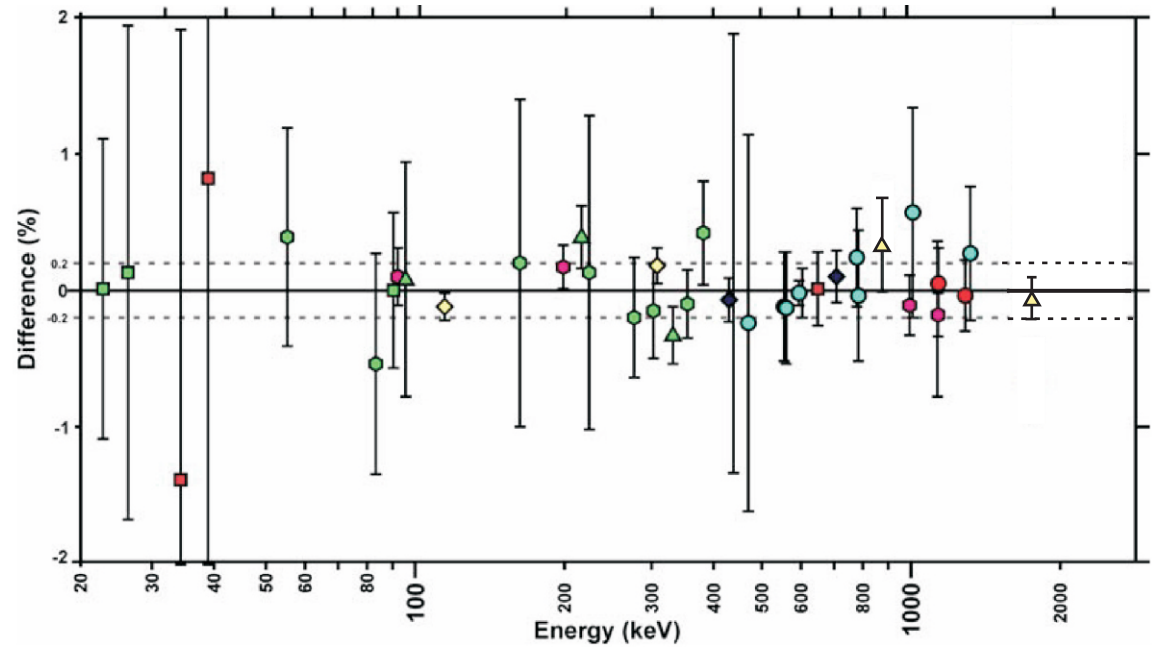
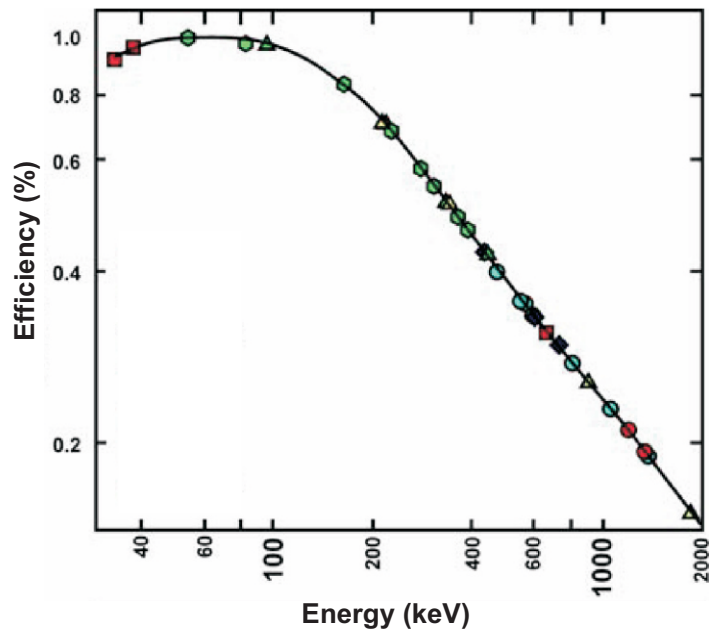
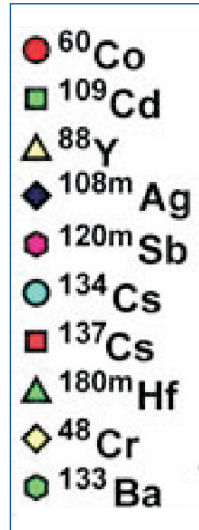
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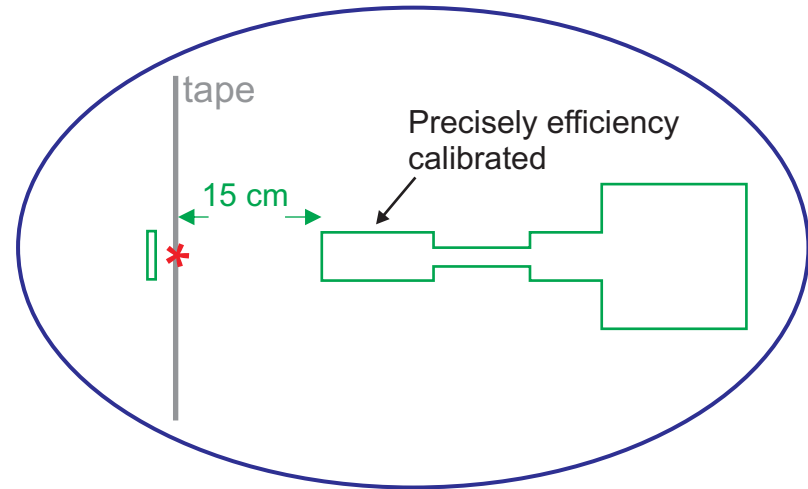
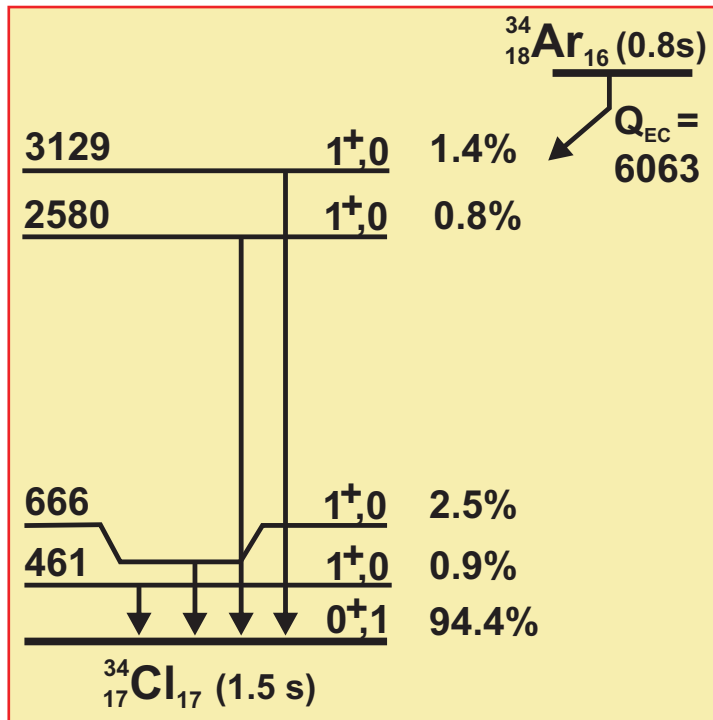
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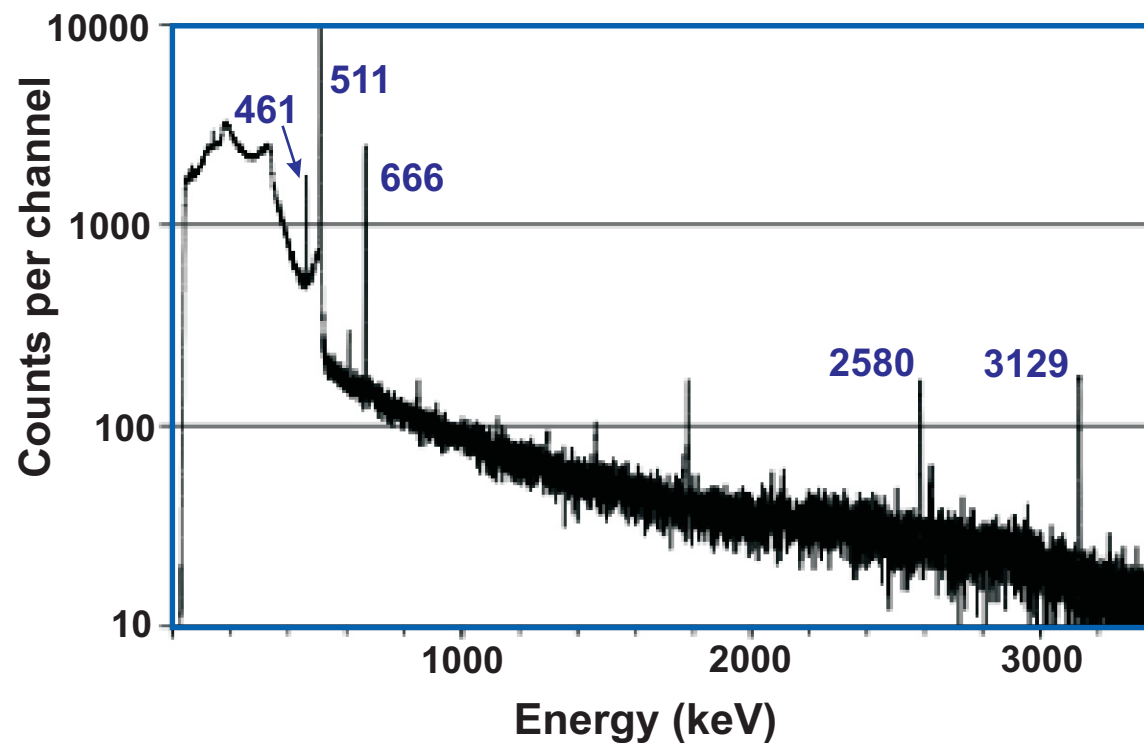
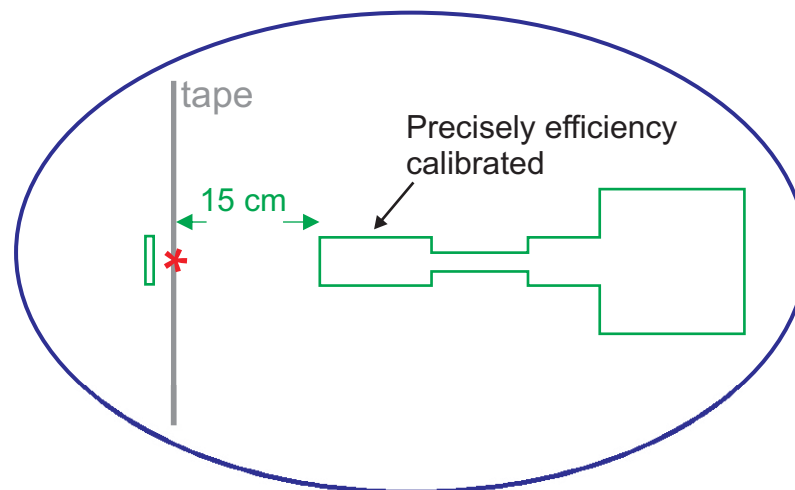
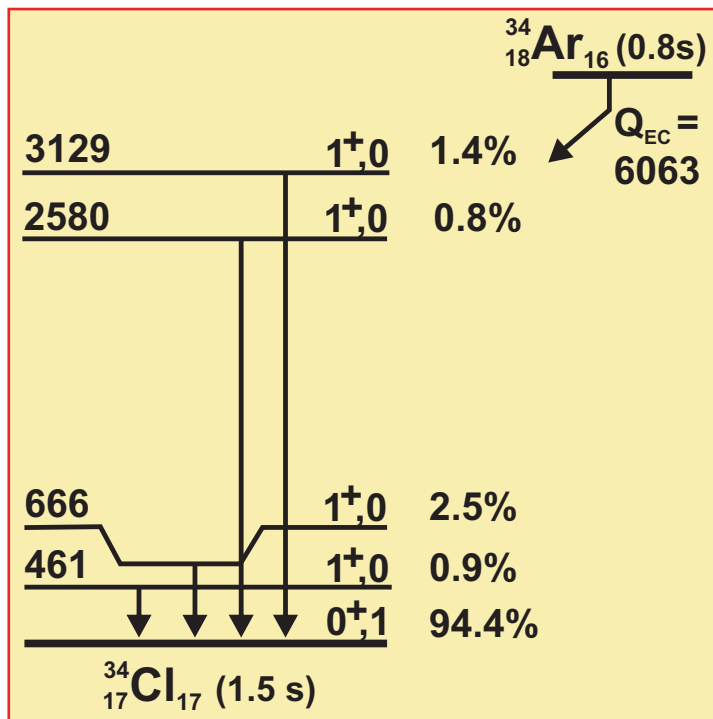


# BETA-DECAY BRANCHING OF $^{34}\text{Ar}$

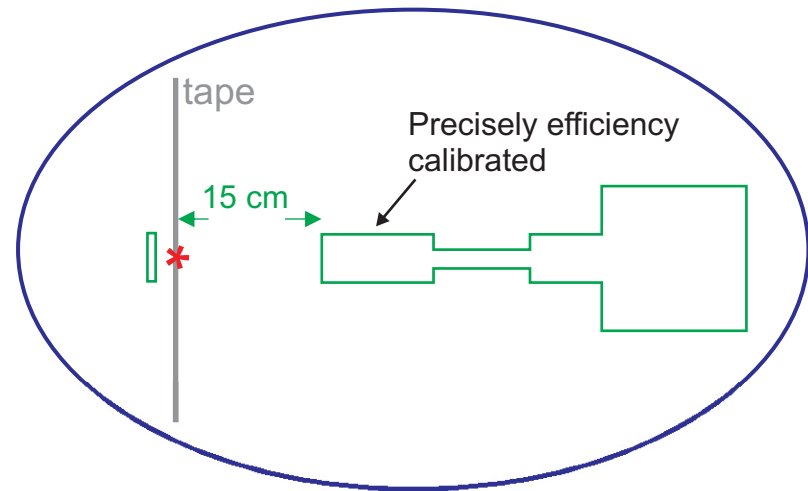
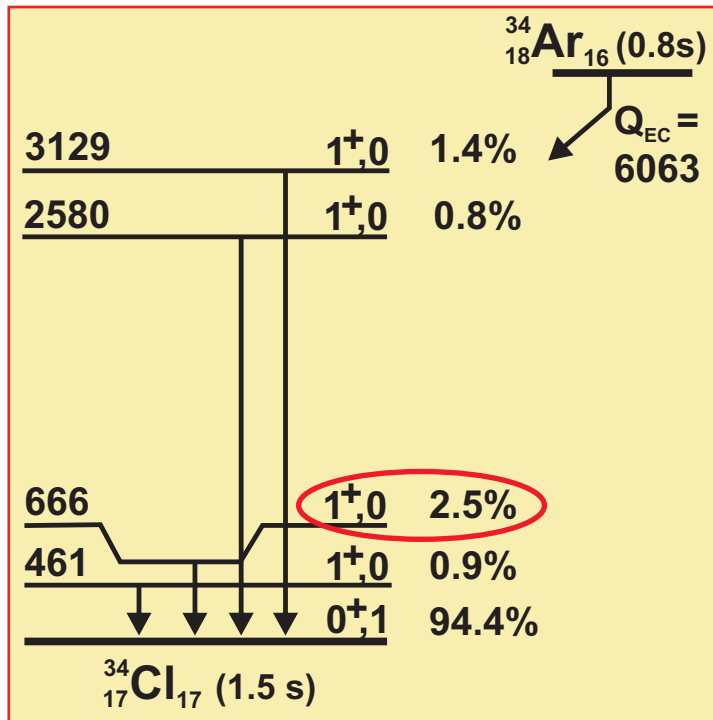




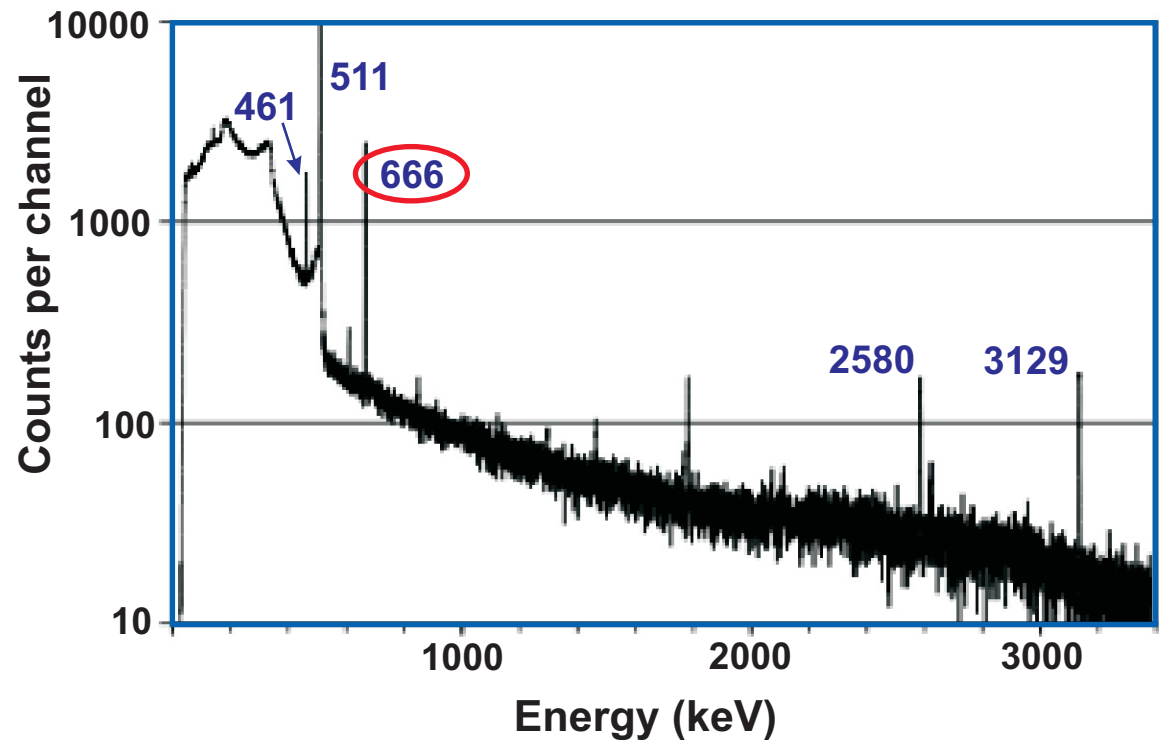
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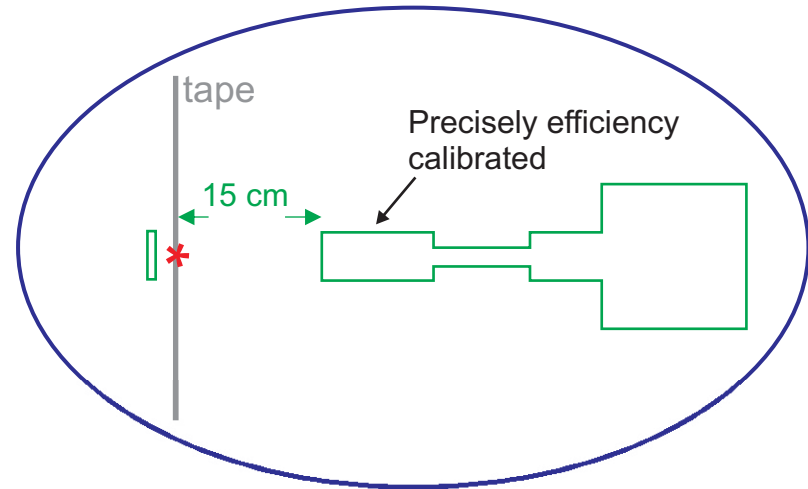
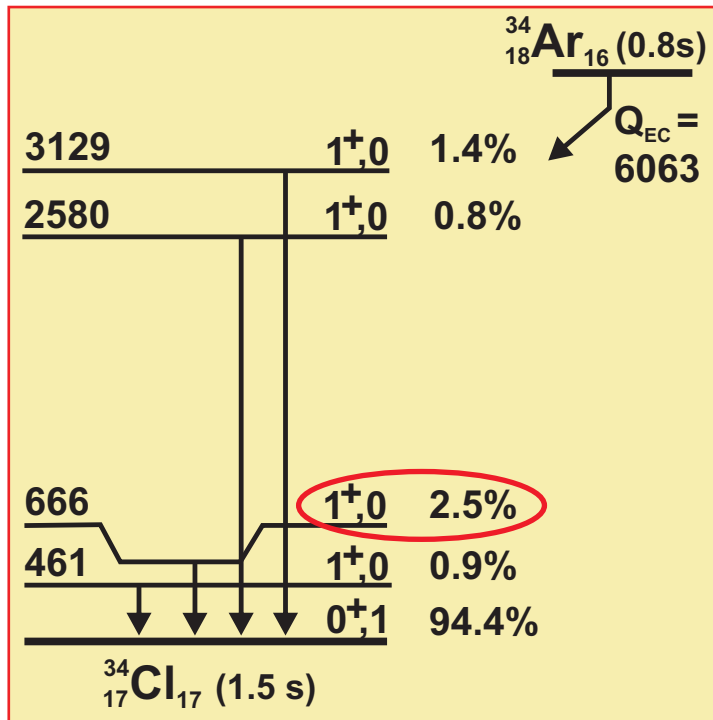
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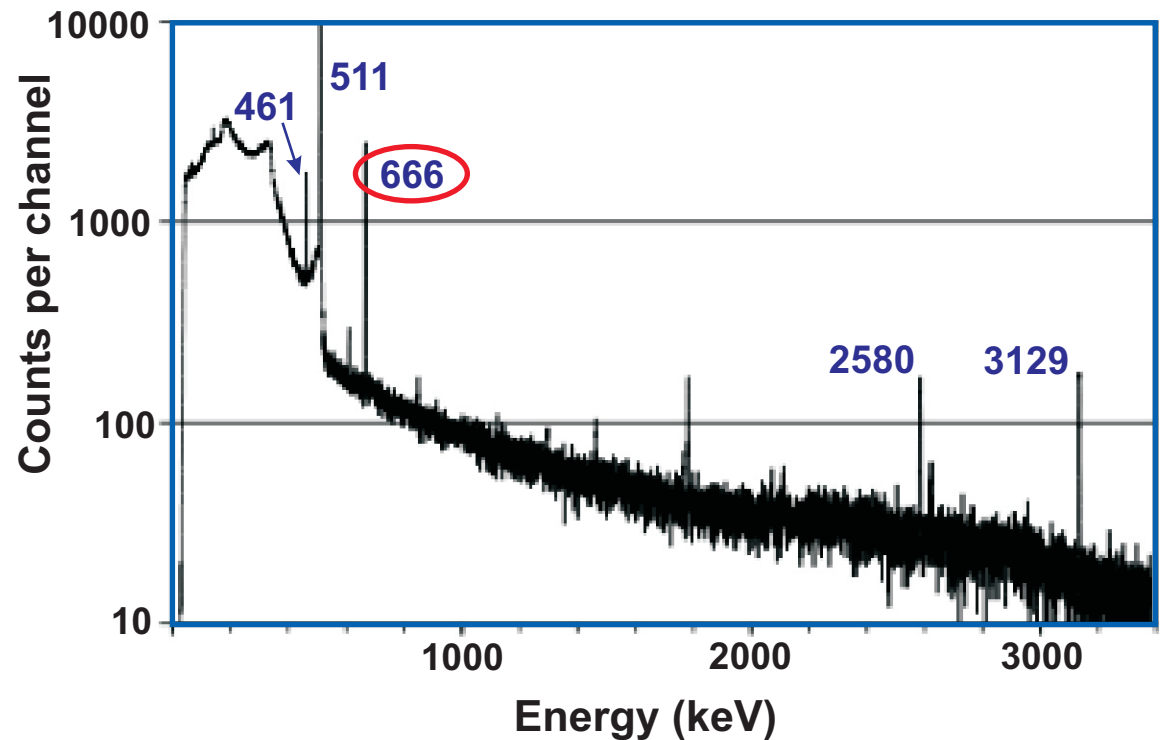
$$\frac{N_1}{N} = \frac{N_0 R_1}{N_0} \cdot 1$$



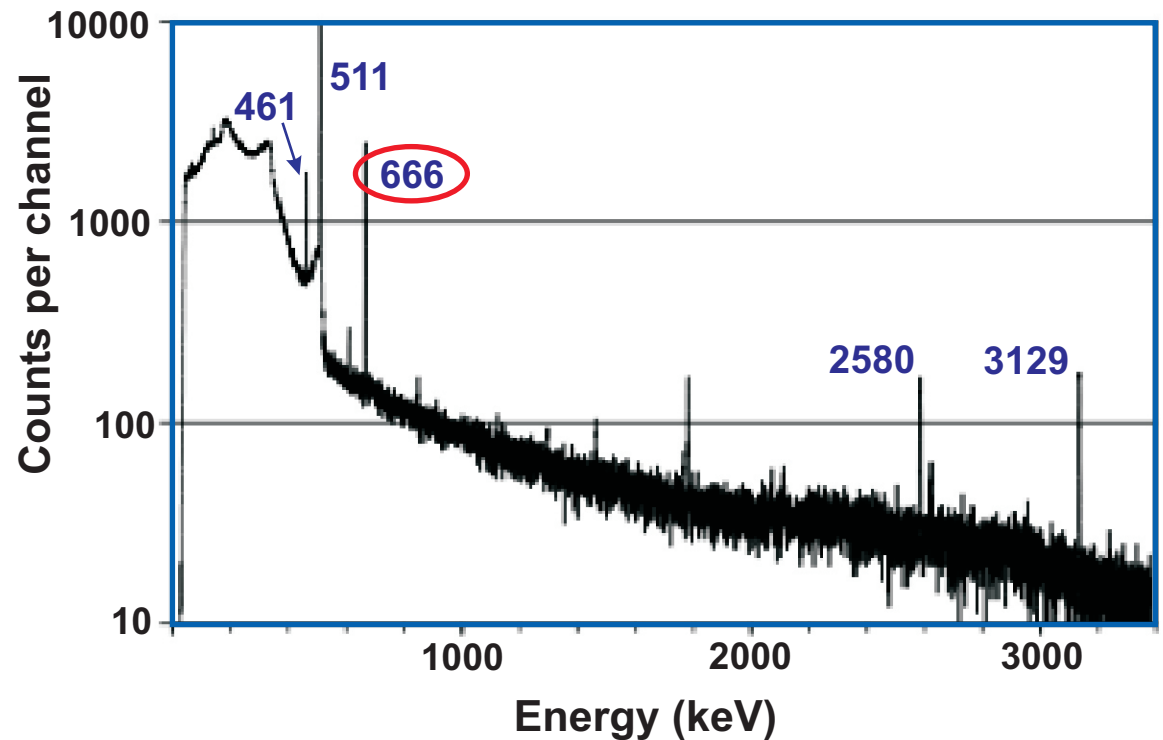
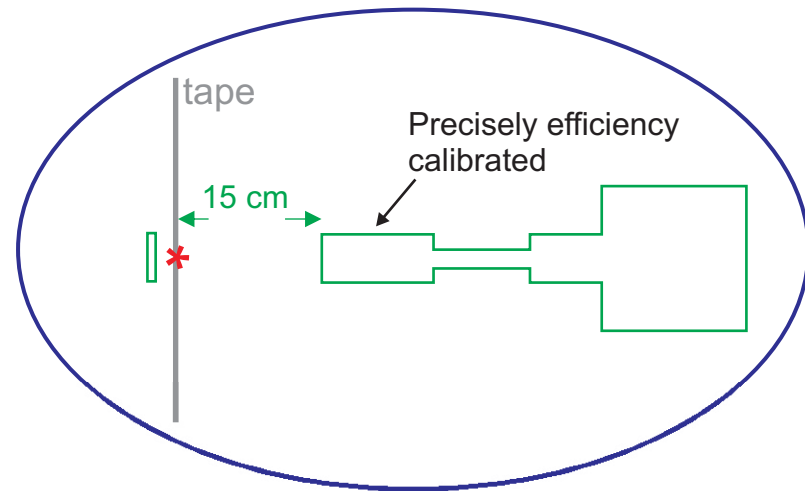
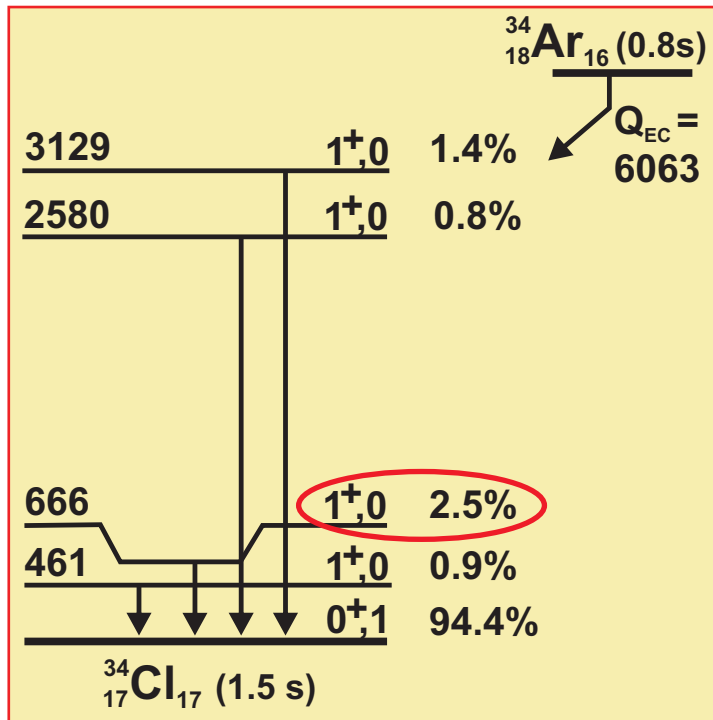
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$$\frac{N_1}{N} = \frac{N_0 R_1}{N_0}$$



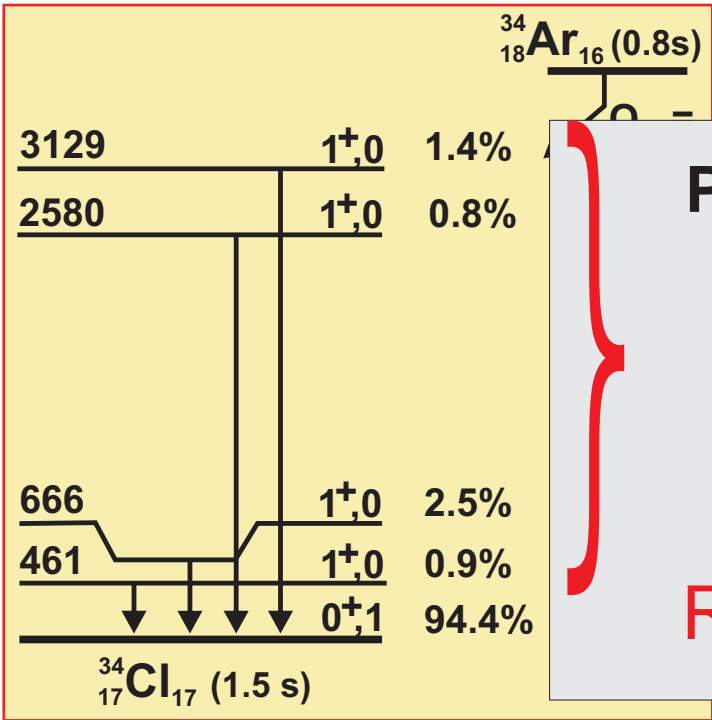
# BETA-DECAY BRANCHING OF $^{34}\text{Ar}$



$$\frac{N_1}{N} = \frac{N_0 R_1}{N_0}$$

$$R_1 = \frac{N_1}{N_0} k$$

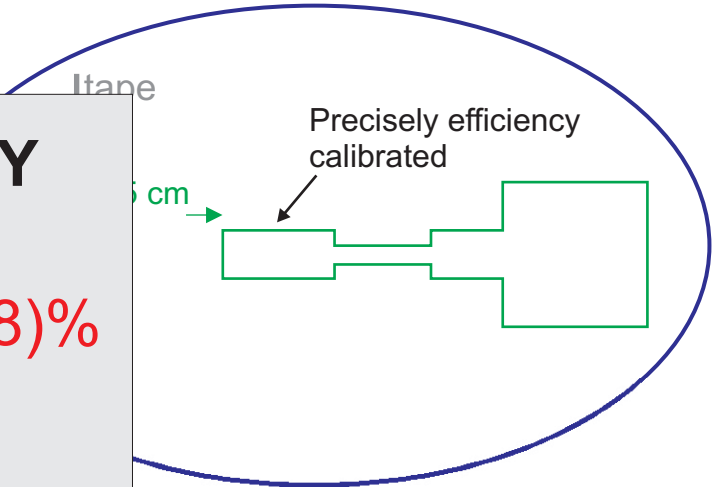
# BETA-DECAY BRANCHING OF $^{34}\text{Ar}$



PRELIMINARY

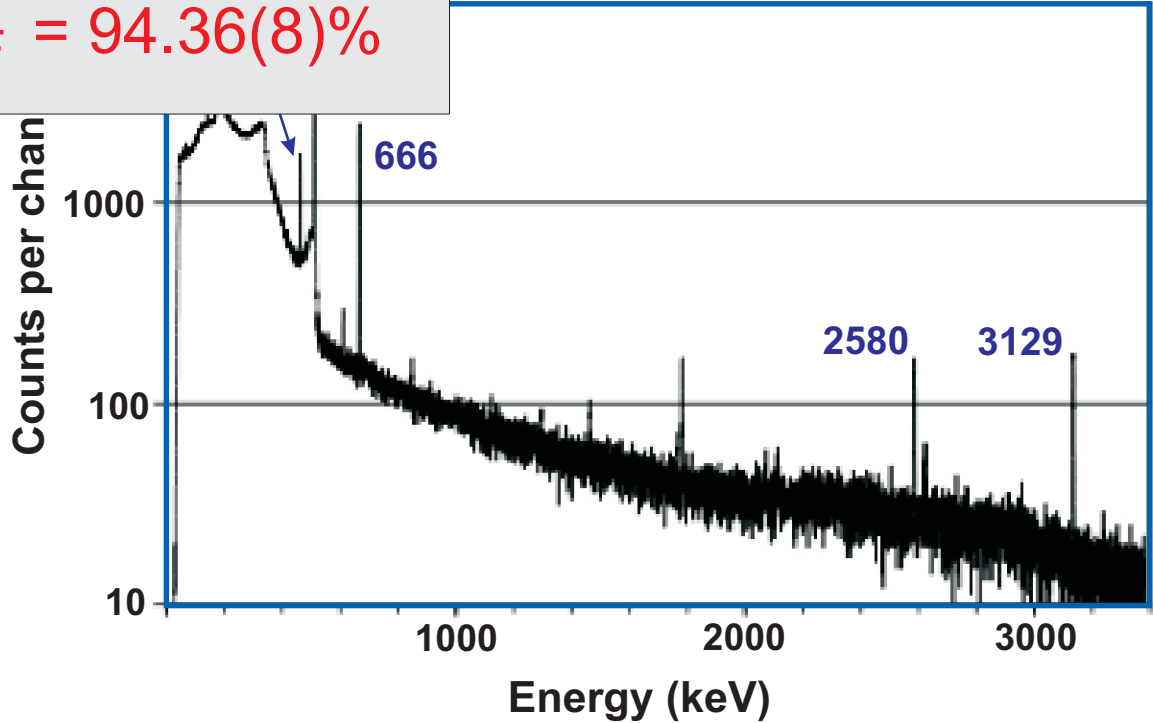
$R_{GT} = 5.64(8)\%$

$R_F = 94.36(8)\%$

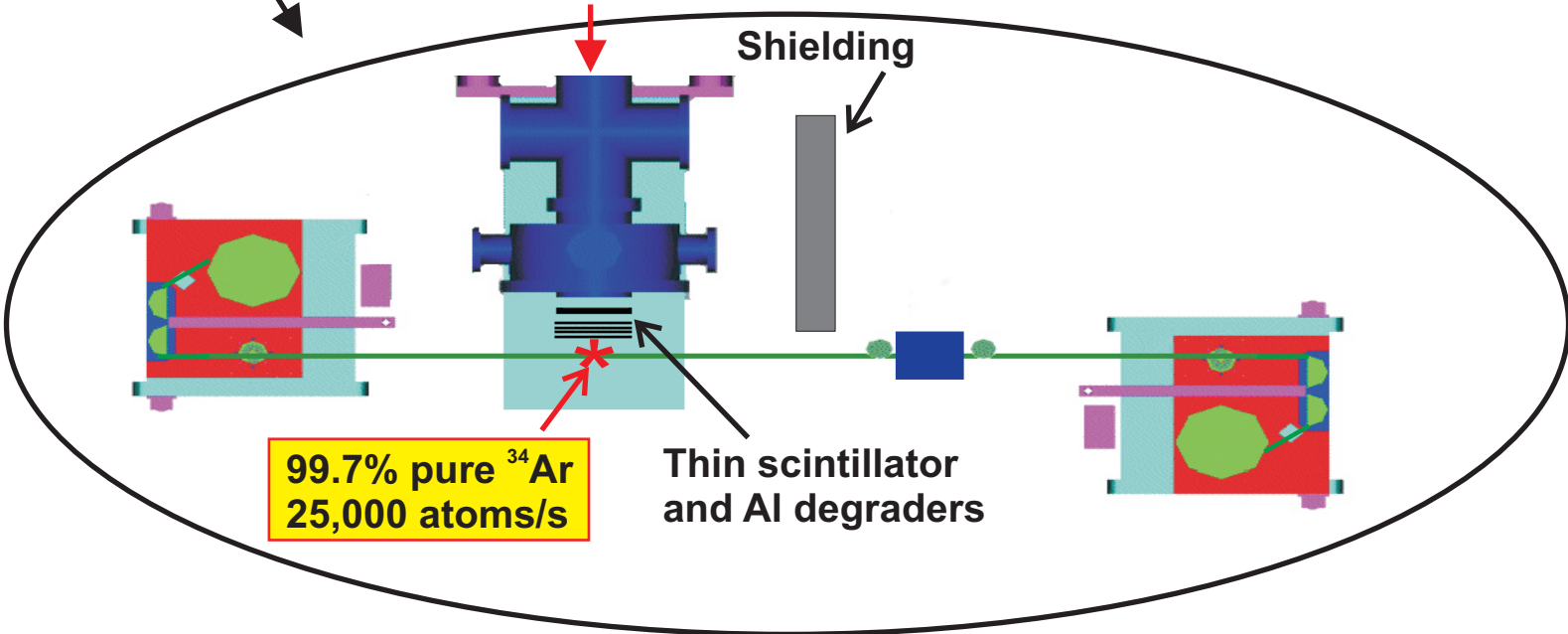
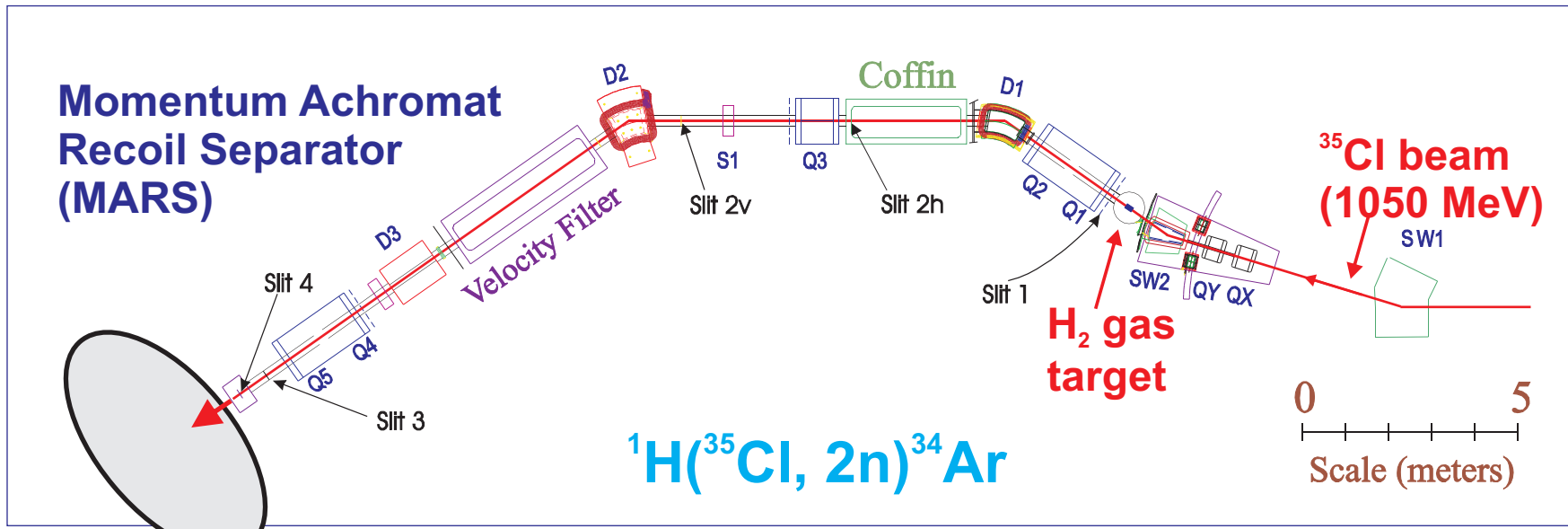


$$\frac{N_1}{N} = \frac{N_0 R_1}{N_0}$$

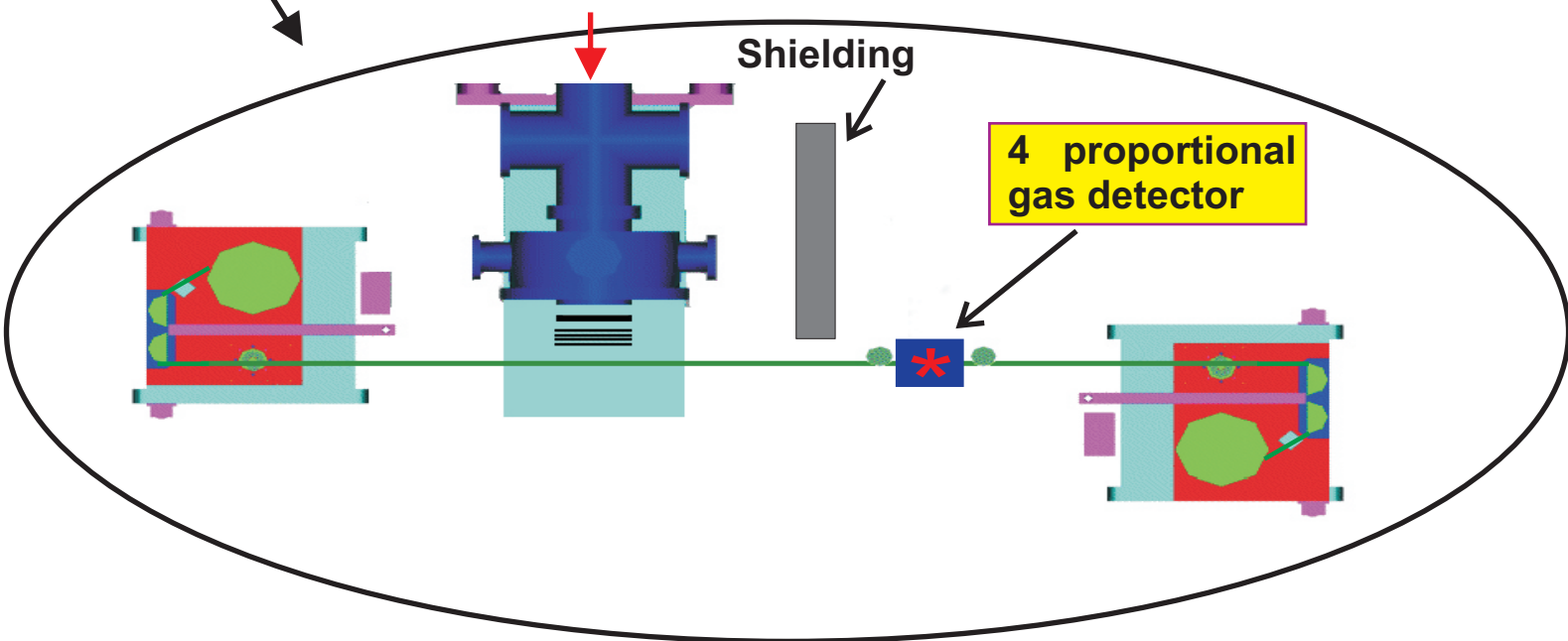
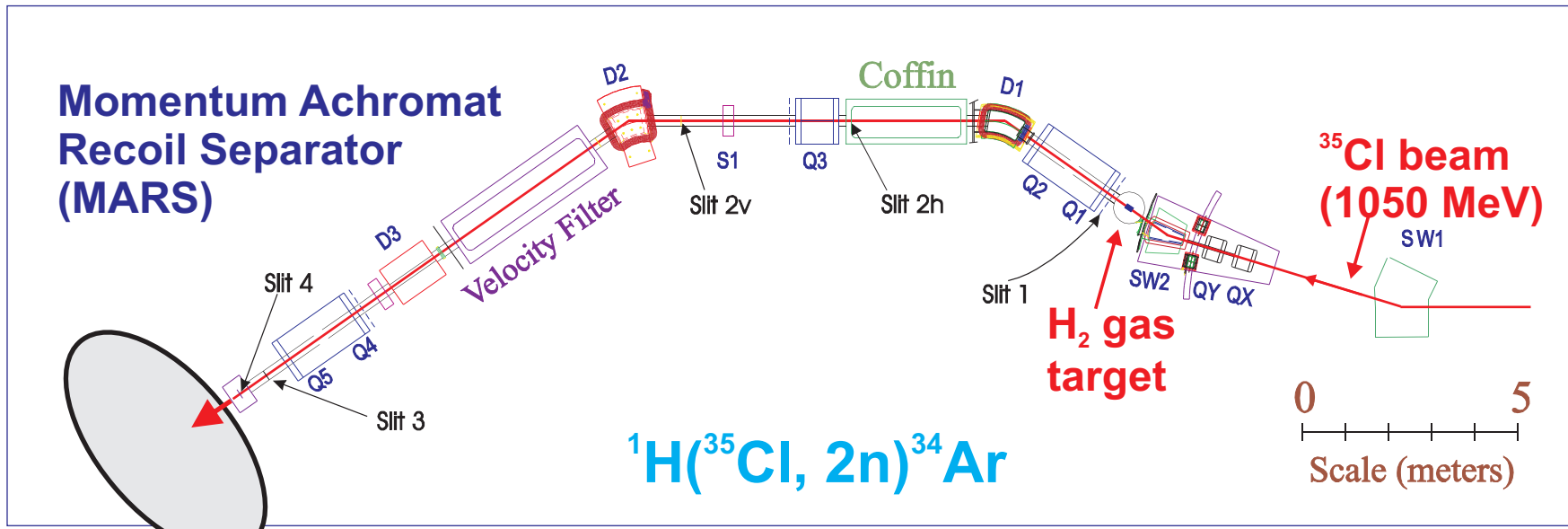
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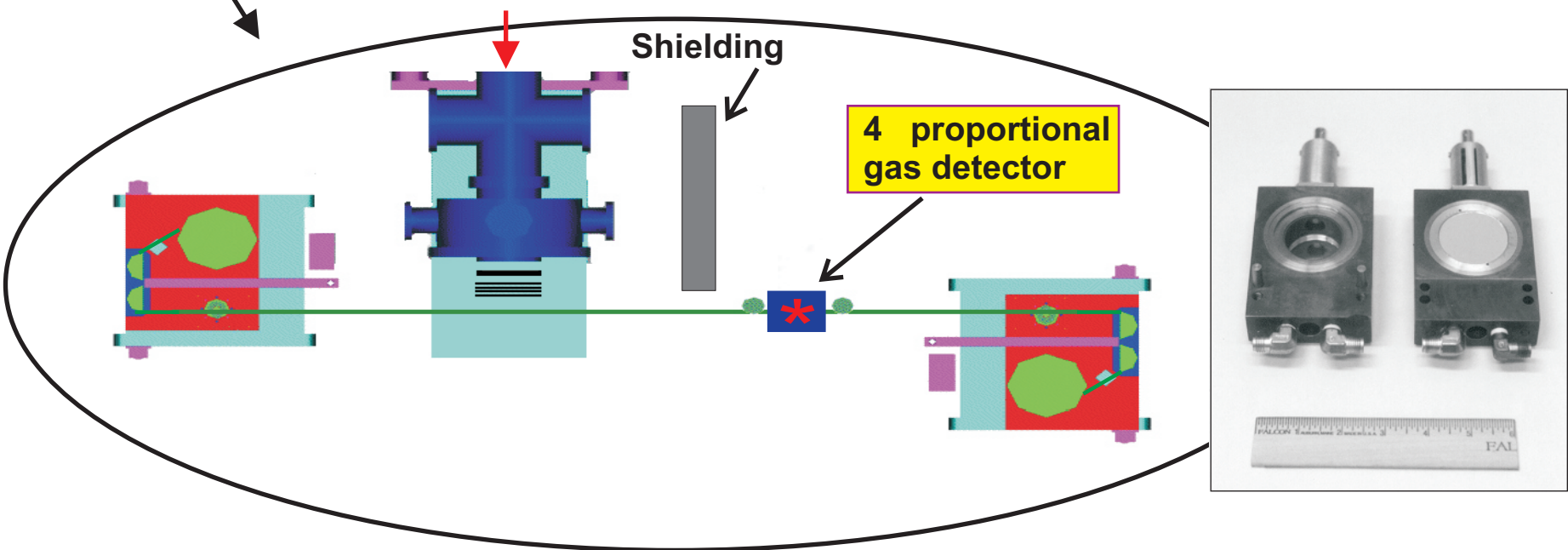
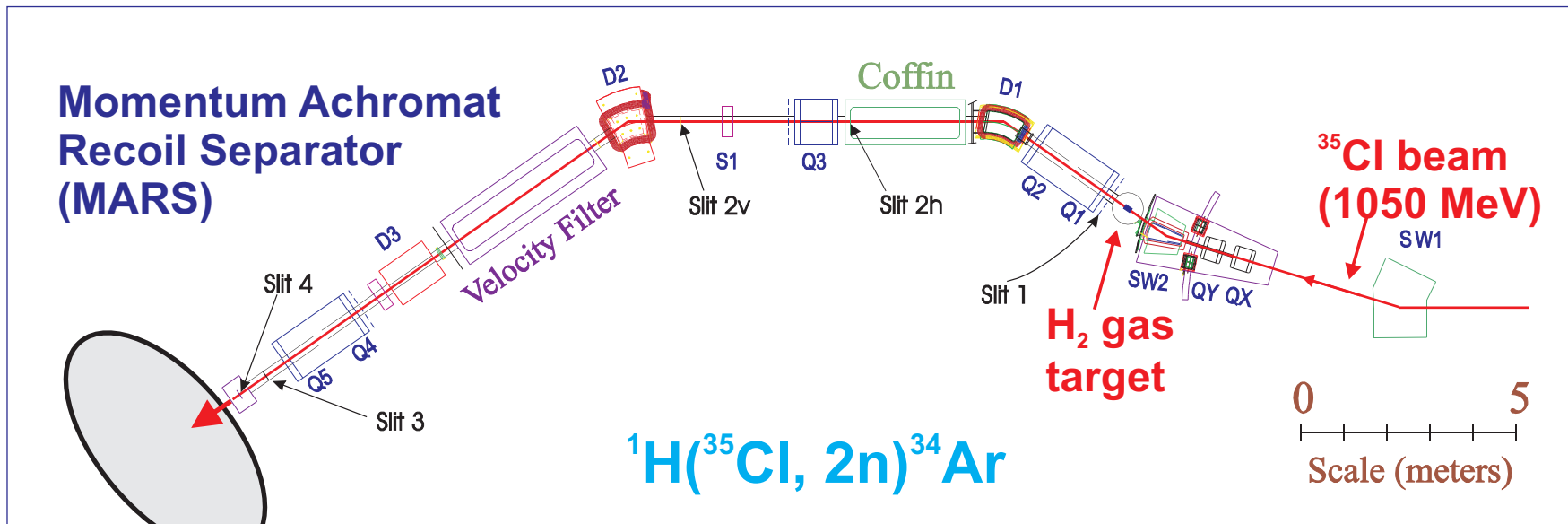
# PRECISION DECAY MEASUREMENTS AT TAMU



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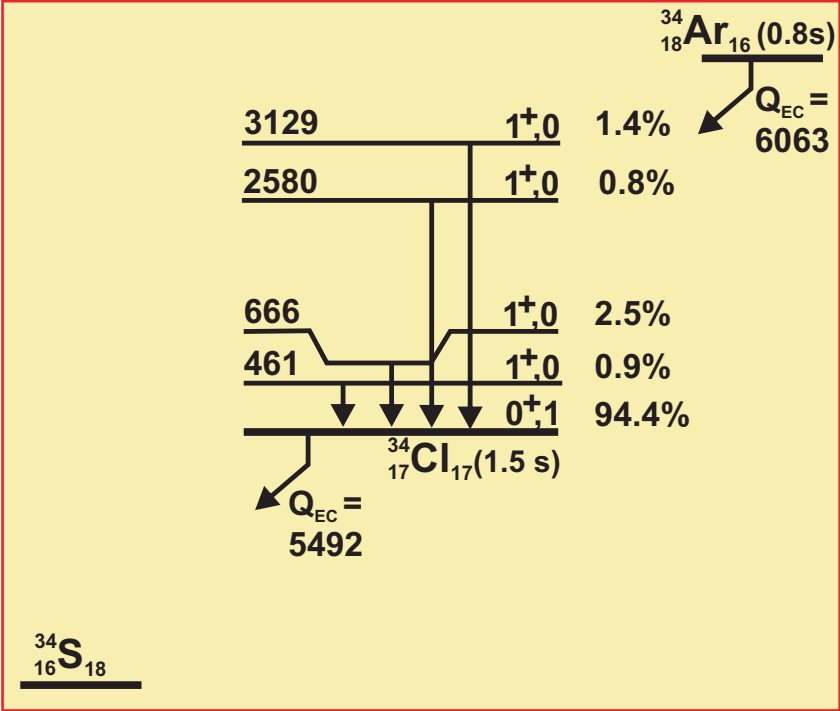


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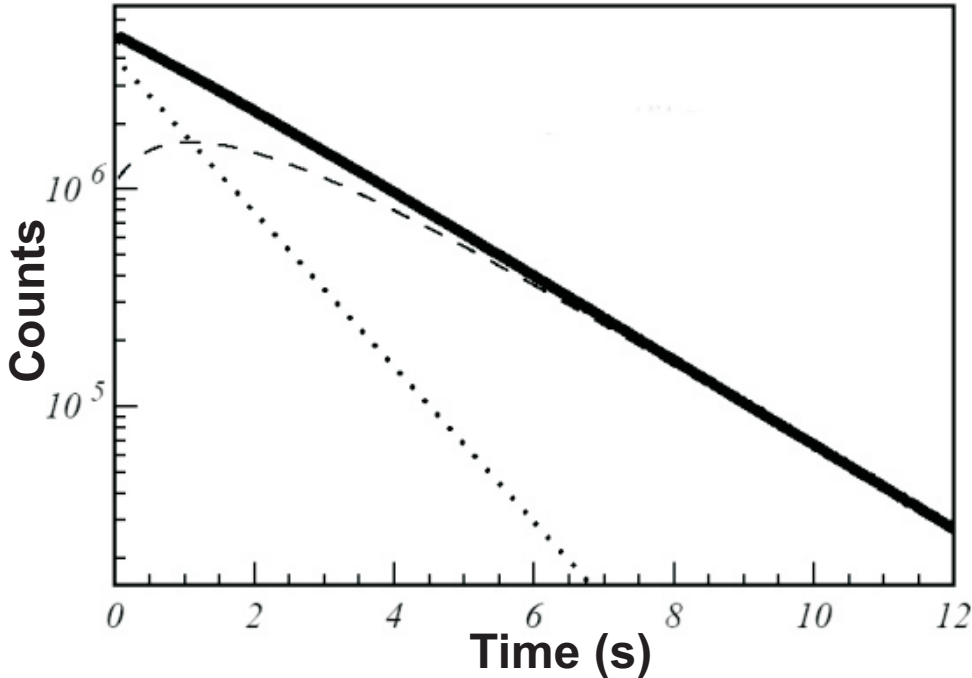
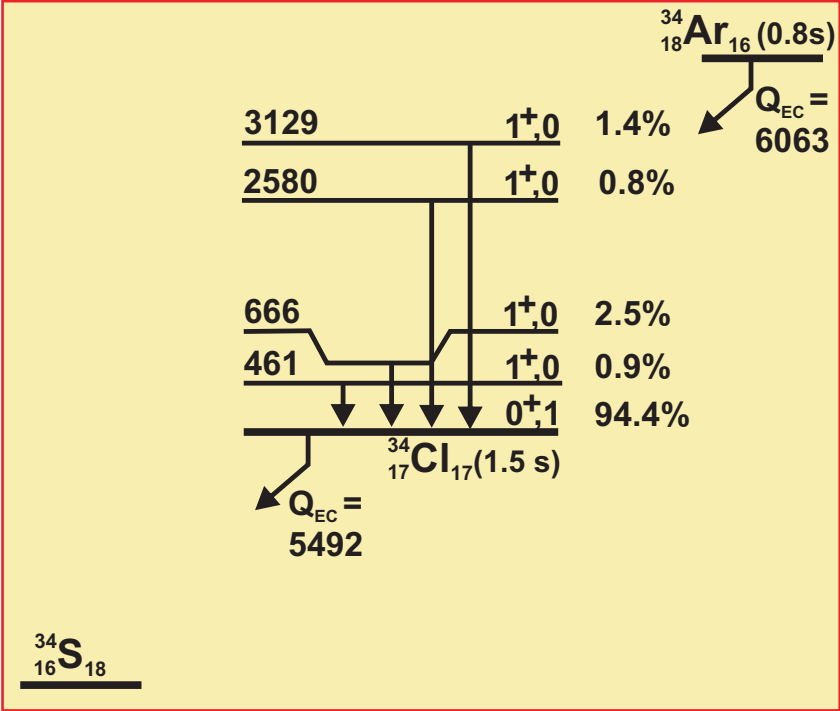




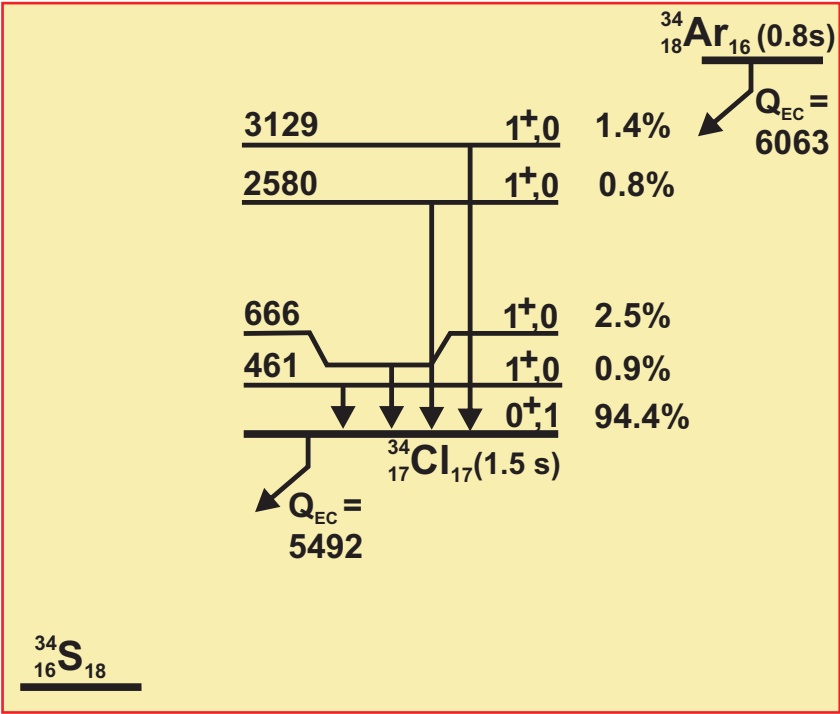
# HALF LIFE OF $^{34}\text{Ar}$



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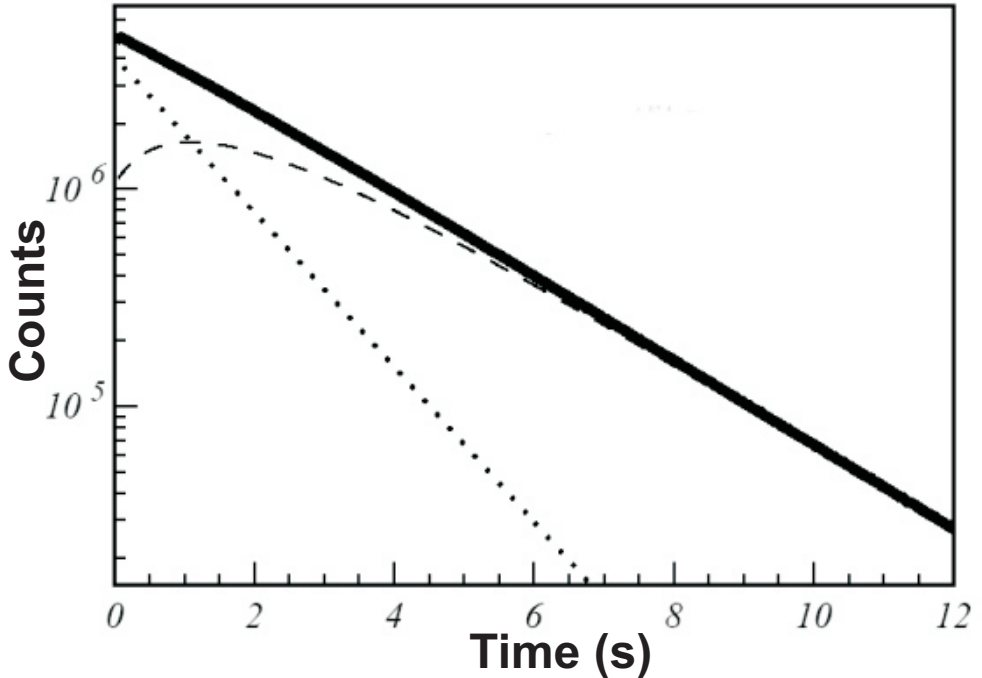


$$N_{\text{tot}} = C_1 e^{-\lambda_1 t} + C_2 e^{-\lambda_2 t}$$

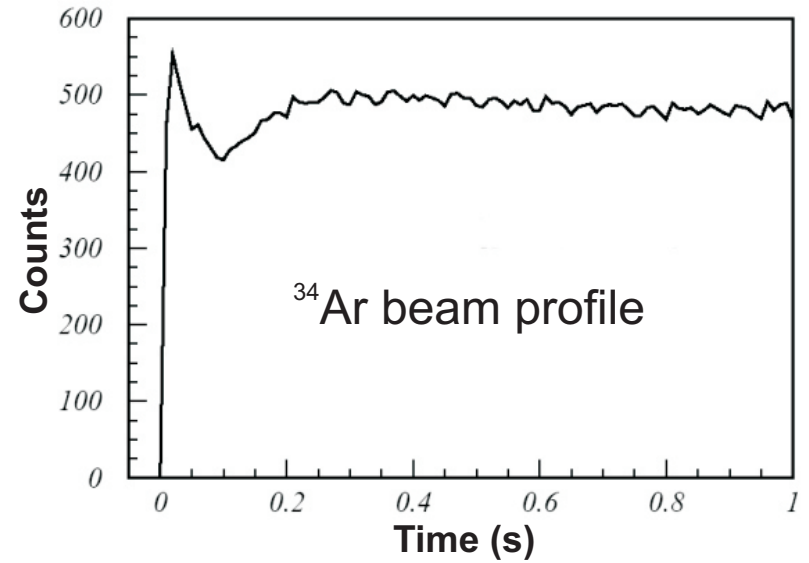
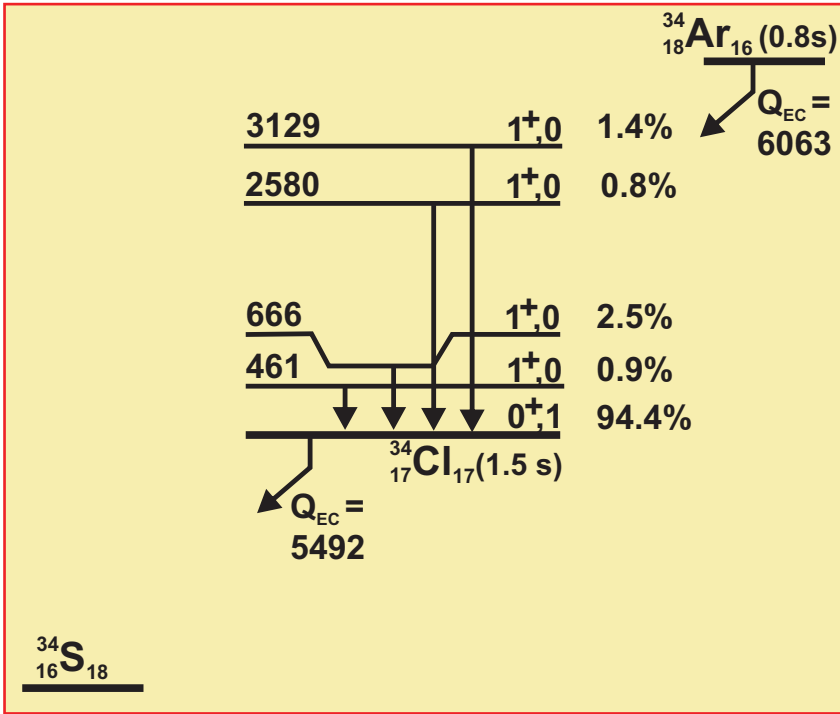
where

$$C_1 = N_1 \frac{\lambda_2 - \lambda_1}{\lambda_2 - \lambda_1}$$

$$C_2 = \left( N_2 - \frac{N_1 \lambda_1}{\lambda_2 - \lambda_1} \right) e^{-\lambda_1 t}$$



# HALF LIFE OF $^{34}\text{Ar}$

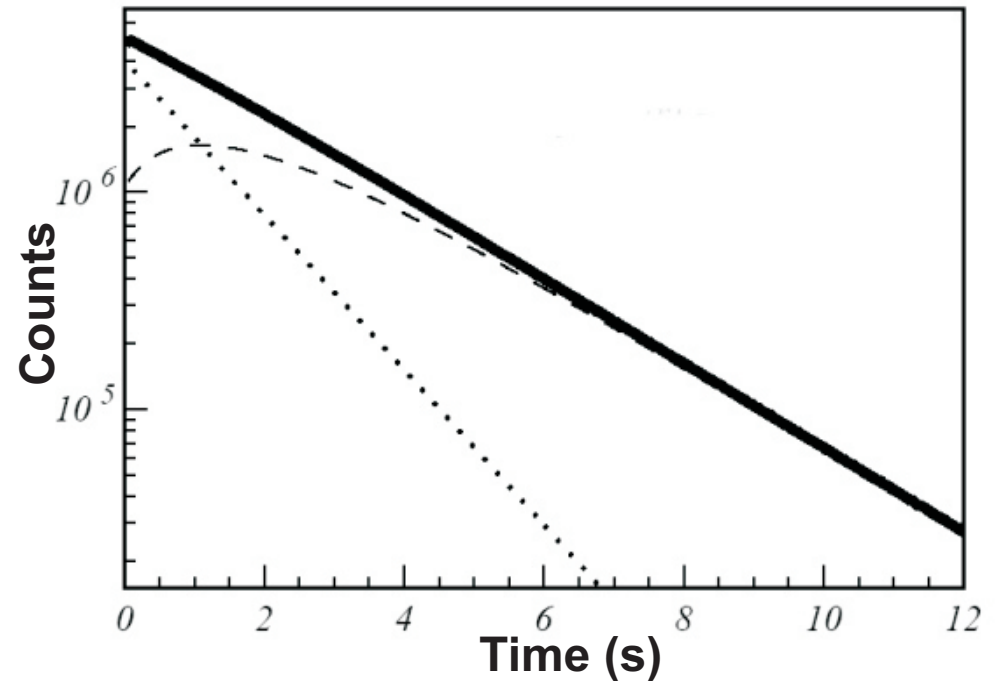


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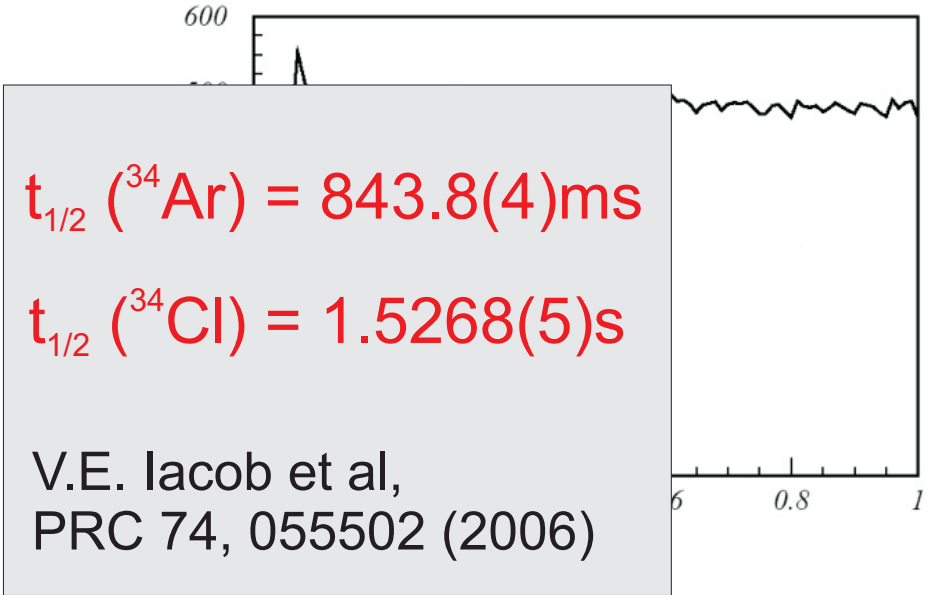
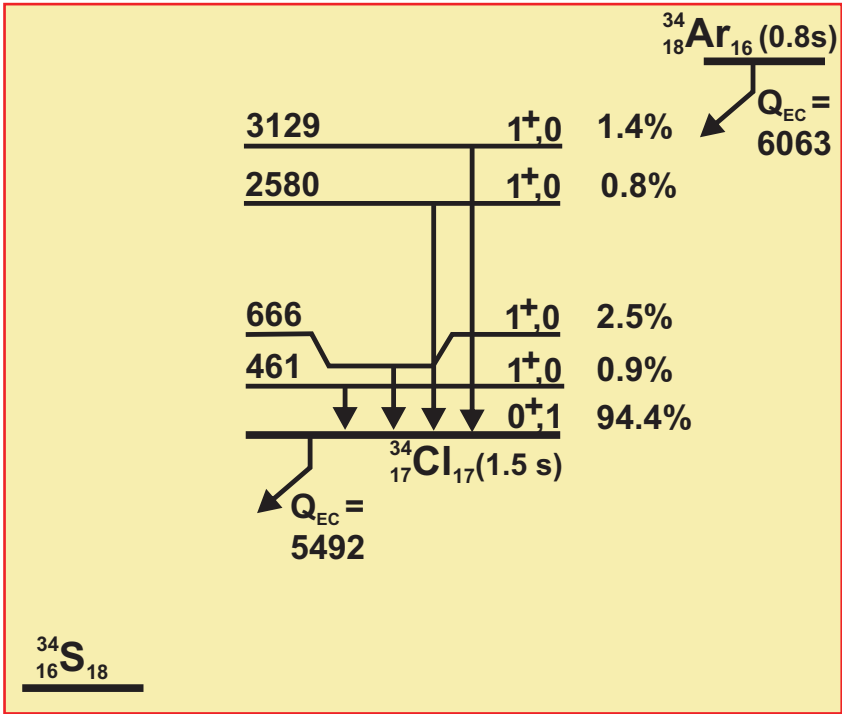
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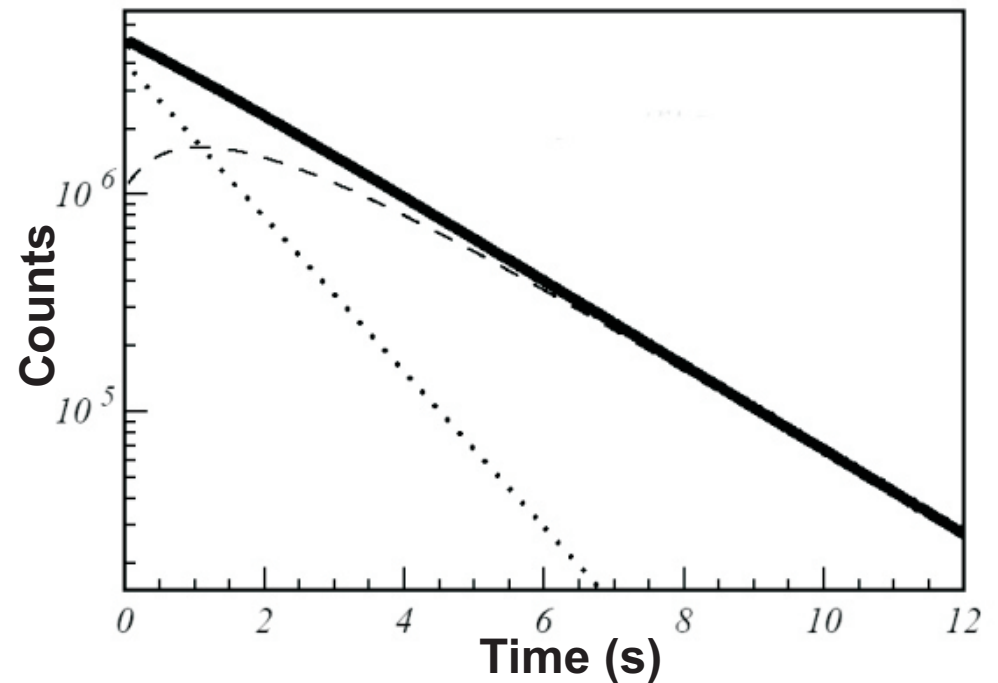


$$N_{\text{tot}} = C_1 e^{-t/\tau_1} + C_2 e^{-t/\tau_2}$$

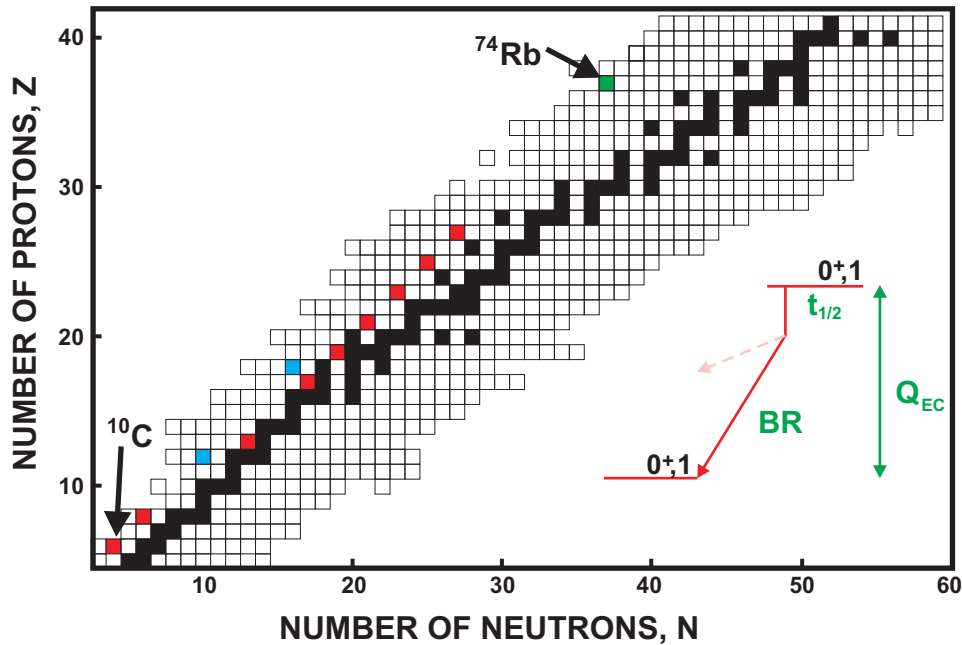
where

$$C_1 = N_1 \frac{2^{-t/\tau_2} - 1}{2^{-t/\tau_1} - 1}$$

$$C_2 = \left( N_2 - \frac{N_1}{2^{-t/\tau_1} - 1} \right) e^{-t/\tau_2}$$

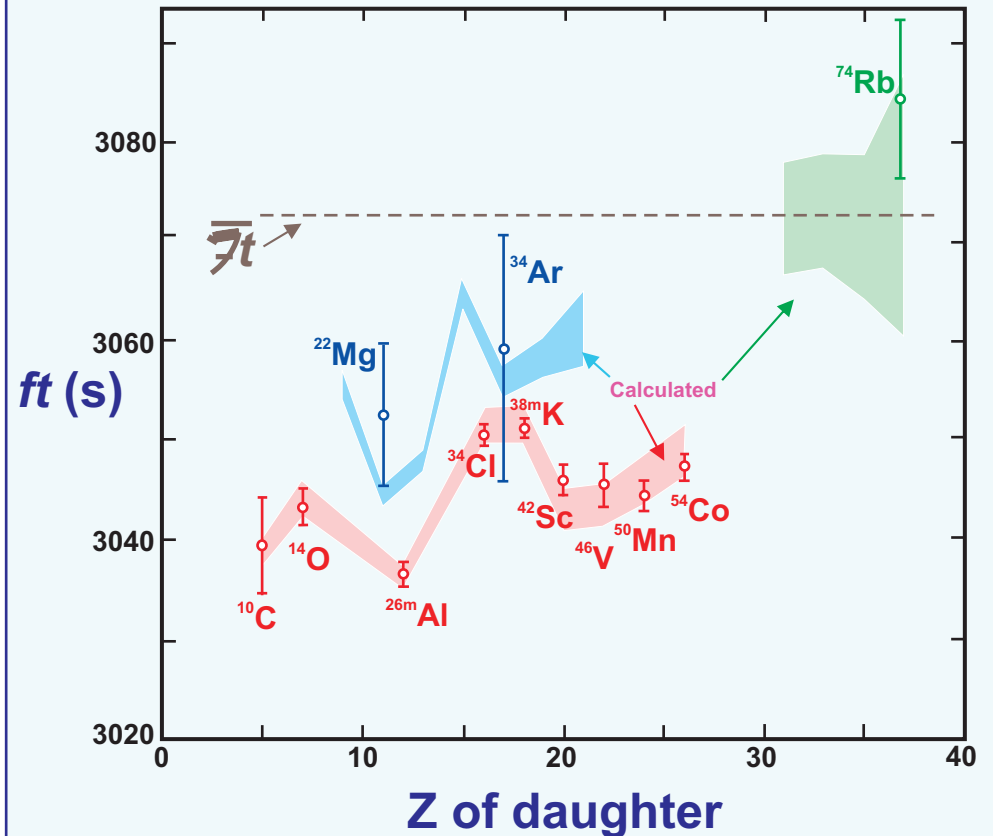


# STATUS OF RESULTS AS OF MAY 2007



Results of 2005 survey

$$\text{Calculated } ft\text{-value} = \frac{\overline{f}_t}{(1 + R)[1 - (C - NS)]}$$



What's new?

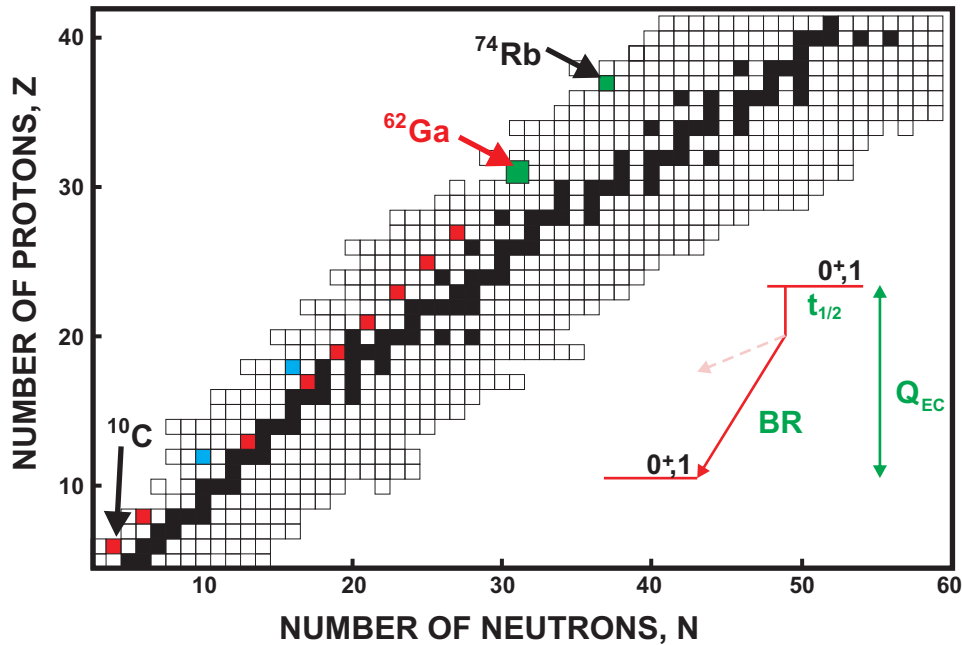
$^{62}\text{Ga}$ : new case added

$^{34}\text{Ar}$ : BR,  $t_{1/2}$  results improved

$^{46}\text{V}$ :  $Q_{\text{EC}}$  value improved

$^{10}\text{C} - ^{42}\text{Sc}$ :  $Q_{\text{EC}}$  values improved

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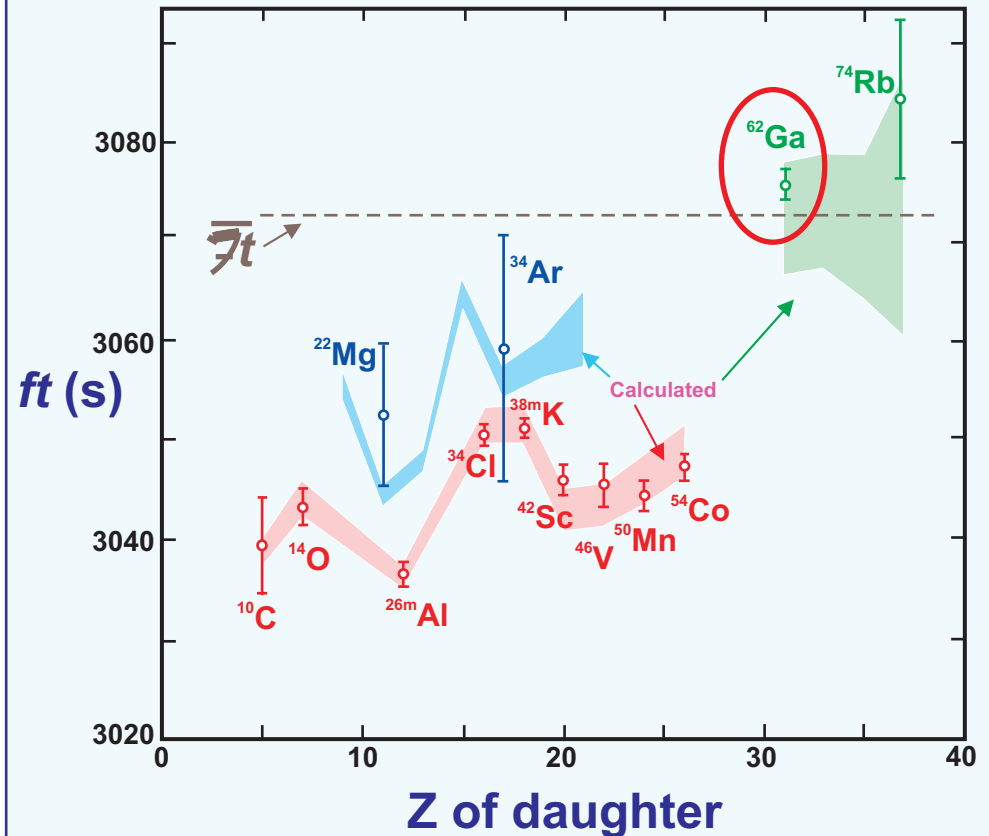


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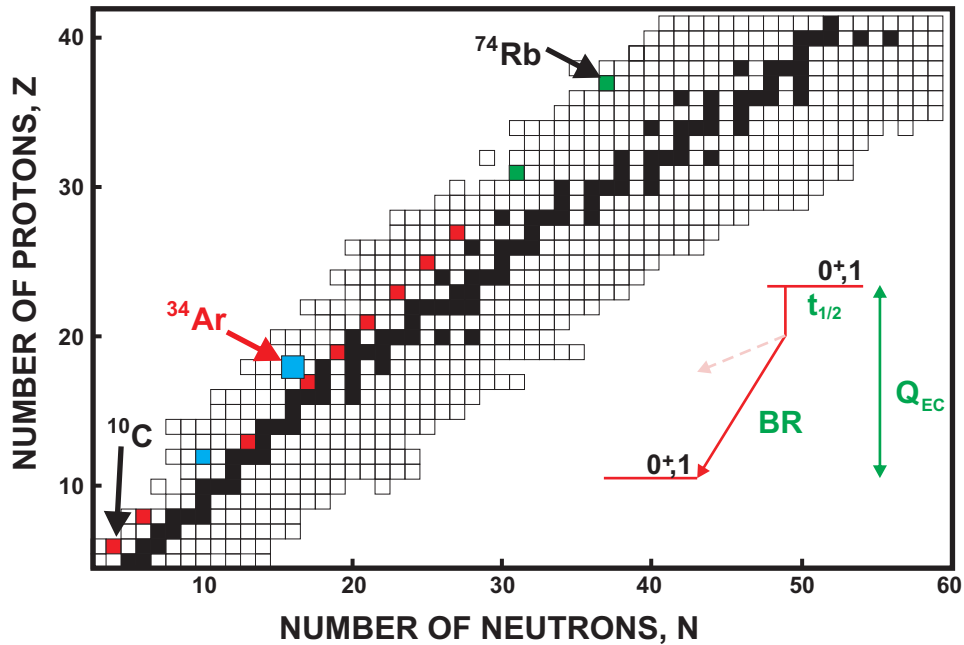
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Updated results

$$\text{Calculated } ft\text{-value} = \frac{\overline{f}_t}{(1 + R)[1 - (C - NS)]}$$



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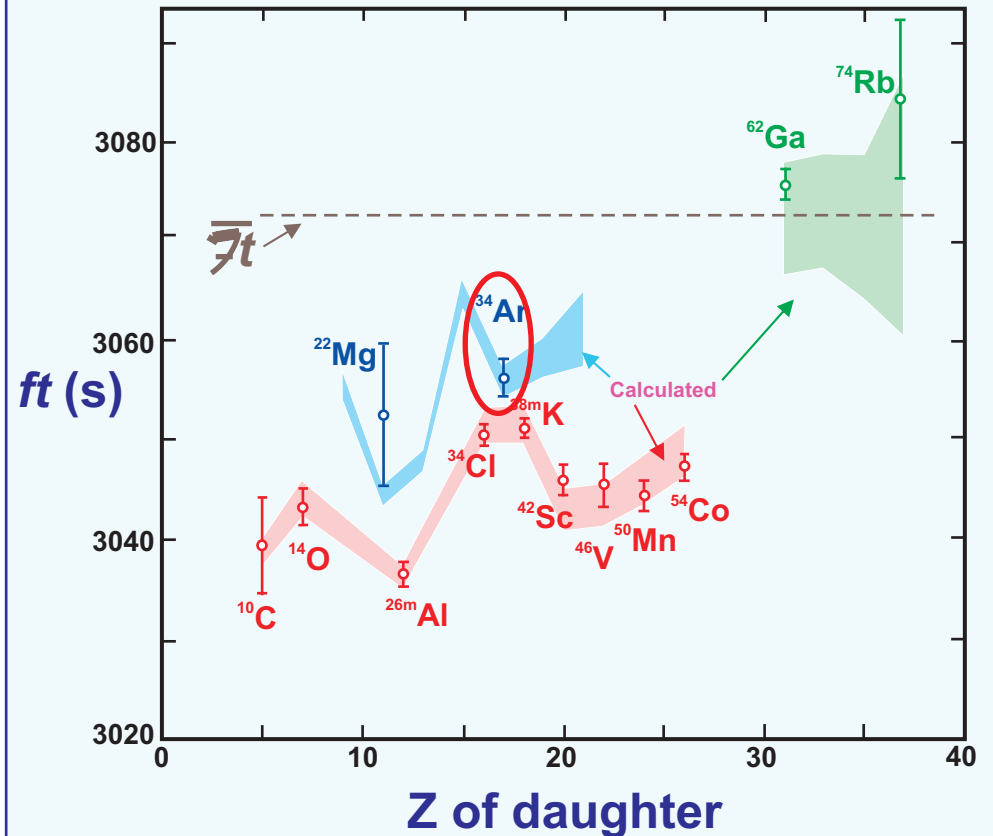


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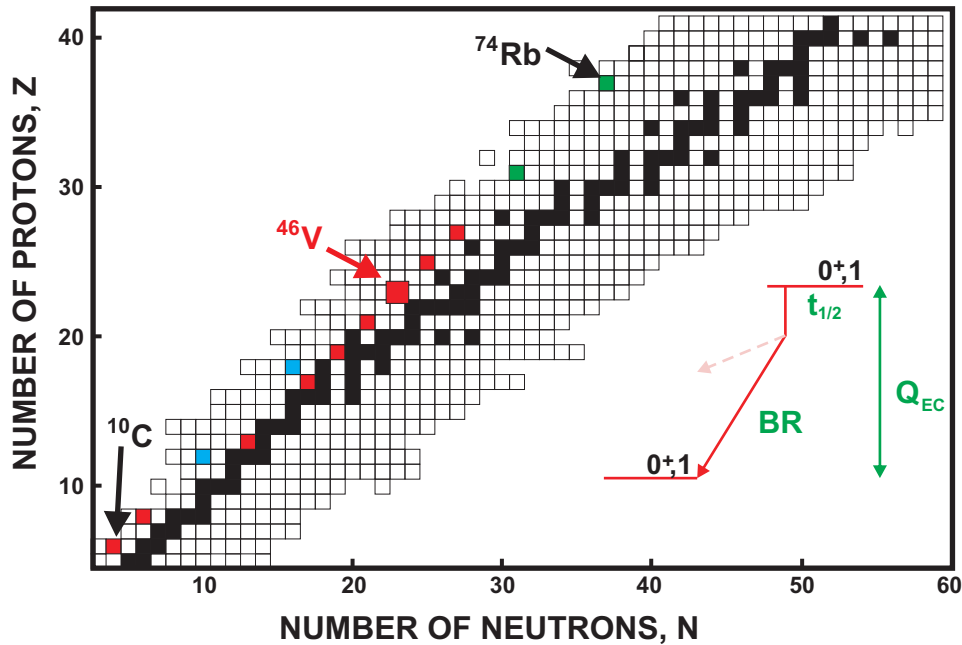
Updated results

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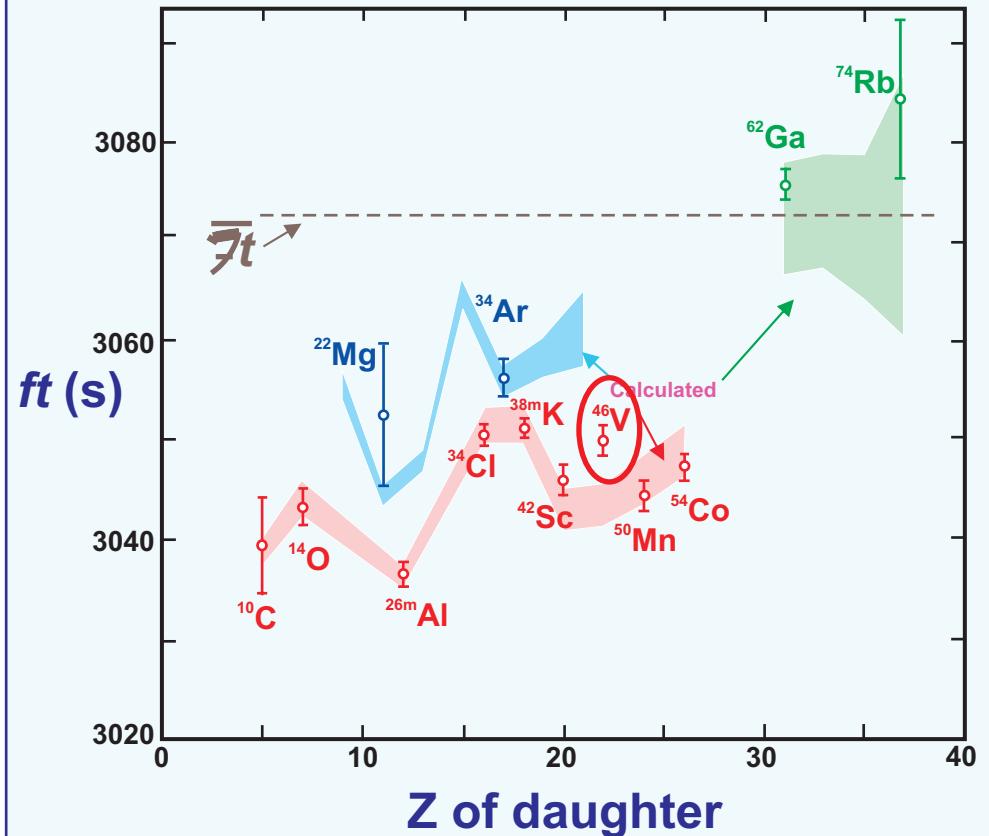


# STATUS OF RESULTS AS OF MAY 2007



Updated results

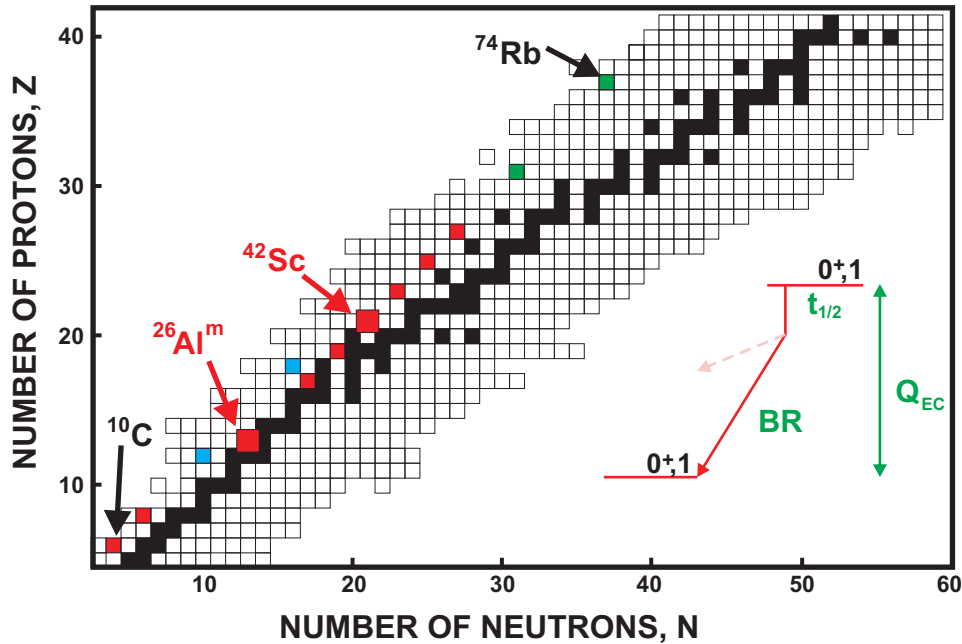
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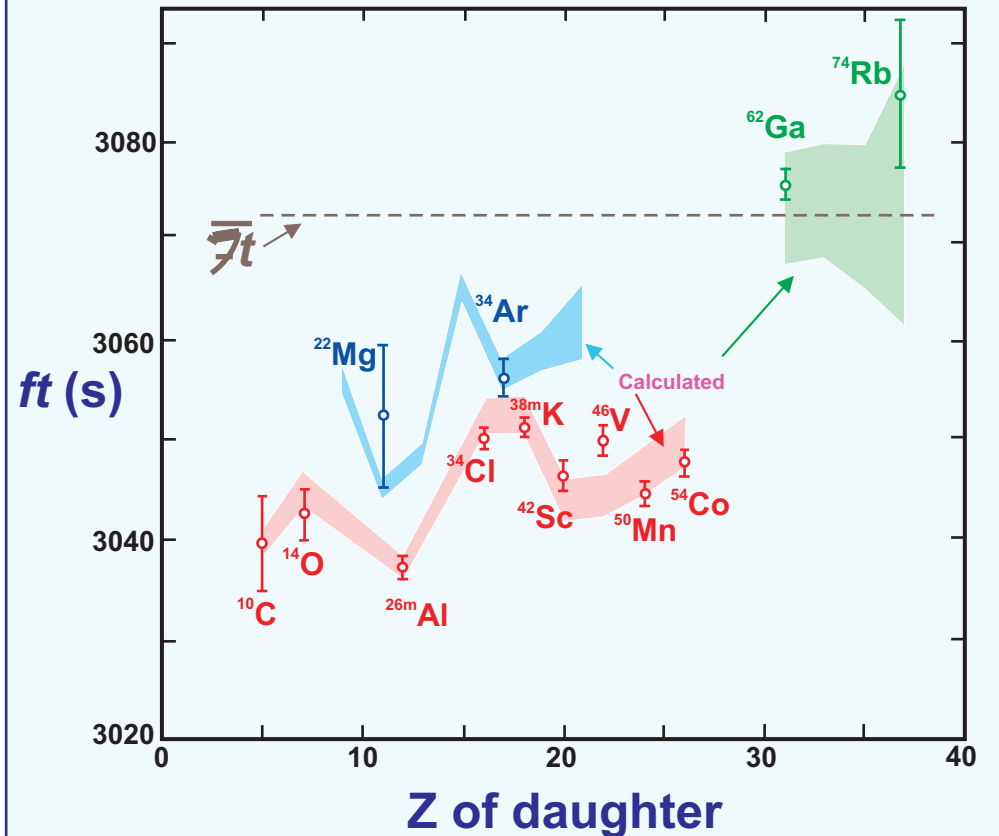


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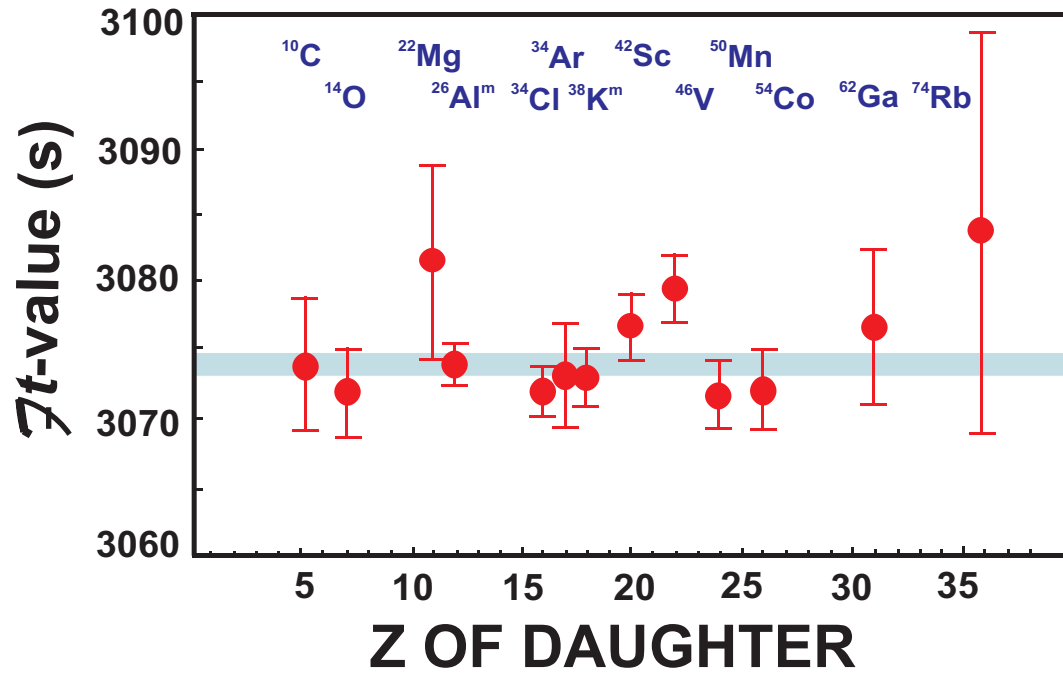
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Updated results + re-fit

$$\text{Calculated } ft\text{-value} = \frac{\overline{ft}}{(1 + R)[1 - (C - NS)]}$$



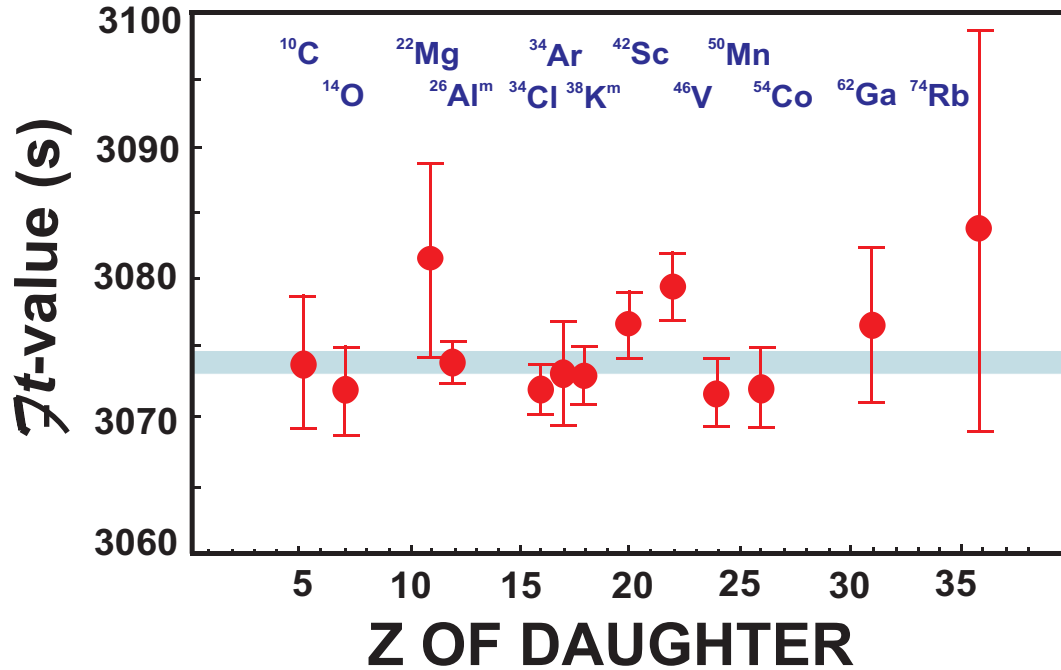
# THE BOTTOM LINE AS OF MAY 2007



$$\overline{Ft} = 3073.9(8)$$

$$V_{ud} = 0.97378(27)$$

# THE BOTTOM LINE AS OF MAY 2007



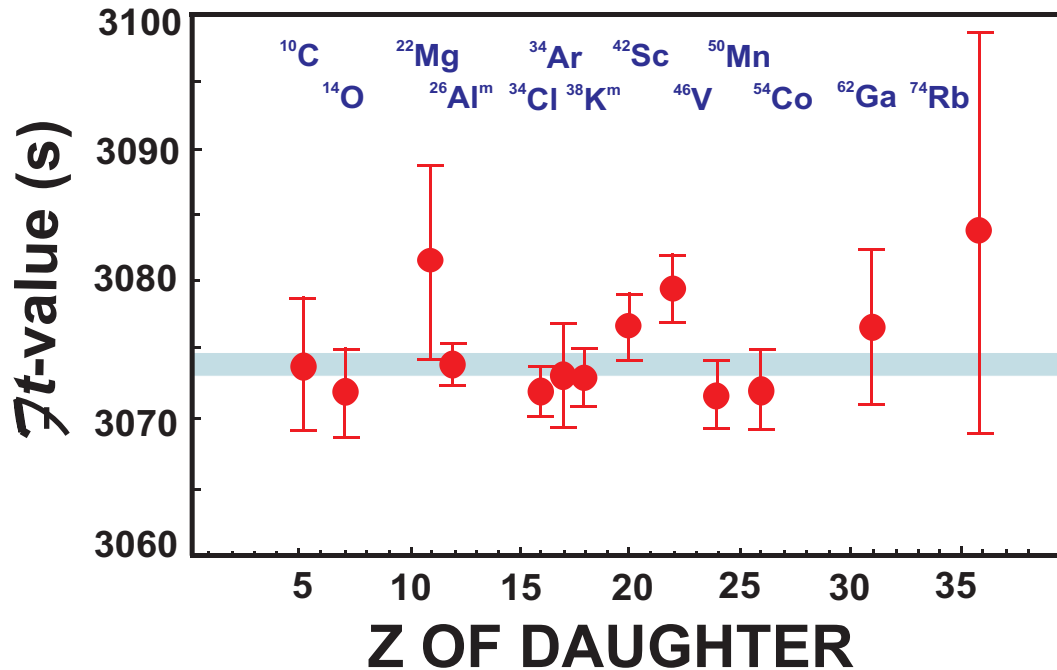
$$\overline{Ft} = 3073.9(8)$$

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2005 Review:

$$V_{ud} = 0.97380(40)$$

# THE BOTTOM LINE AS OF MAY 2007



$$\overline{T} = 3073.9(8)$$

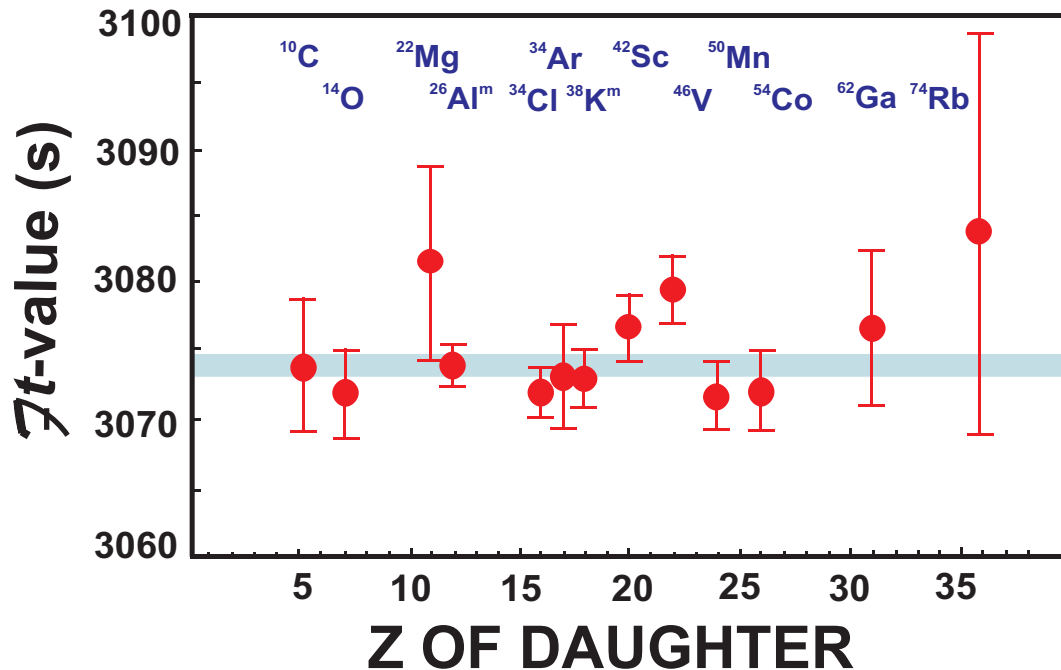
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Most of the reduction in the uncertainty on  $V_{ud}$  since 2005 comes from the improvement in the calculated radiative correction  $R^*$

# THE BOTTOM LINE AS OF MAY 2007



$$\overline{T} = 3073.9(8)$$

$$V_{ud} = 0.97378(27)$$

CKM UNITARITY:

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.9992(11)$$

$$0.9483(5)$$

$$0.0509(9)$$

$$<0.0001$$

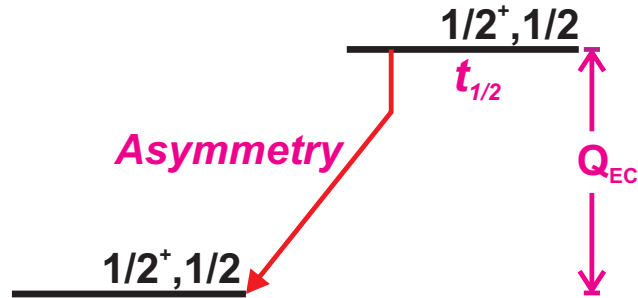
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# NEUTRON BETA DECAY

EXPERIMENTS



WEAK DECAY EQUATION

$$ft = \frac{K}{G_V^2 \langle \rangle^2 + G_A^2 \langle \rangle^2}$$

$$f = f(Q)$$

$$t = f(t_{1/2})$$

$G_{V,A}$  = coupling consts  
 $\langle \rangle$  = matrix elements

NEUTRON DECAY

$$ft = \frac{K}{G_V^2 (1 + 3^2)}$$

$$= G_A/G_V$$

RADIATIVE CORRECTIONS

$$t \rightarrow t(1 + R)$$

$$G_{V,A}^2 \rightarrow G_{V,A}^2 (1 + R) = G_{V,A}'^2$$

$$R = f(Q)$$

$$R = f(\text{interaction})$$

TO DETERMINE  $G_V$   
 TWO EXPERIMENTS  
 ARE REQUIRED:

Neutron lifetime  $\rightarrow G_V'^2 + 3G_A'^2$

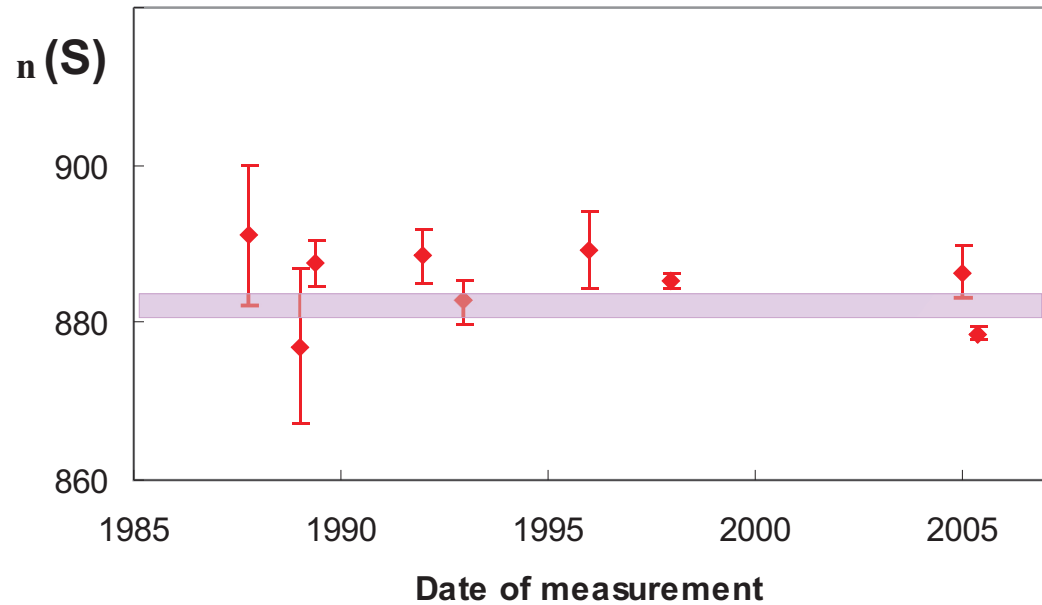
Beta-decay asymmetry  $\rightarrow G_A'/G_V'$

# NEUTRON DECAY DATA, 2006

## Mean life:

$$\tau_n = 882.0 \pm 1.3 \text{ s}$$

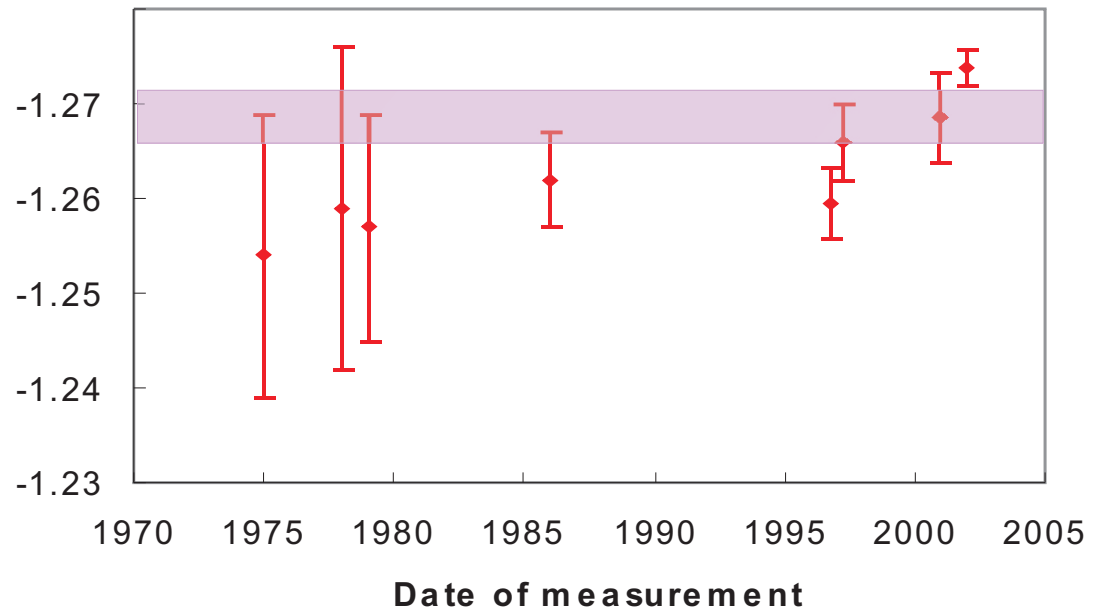
$$\chi^2/N = 5.4$$



## Beta asymmetry:

$$A_{\beta} = -1.2690 \pm 0.0028$$

$$\chi^2/N = 2.6$$





# NEUTRON DECAY DATA, 2006

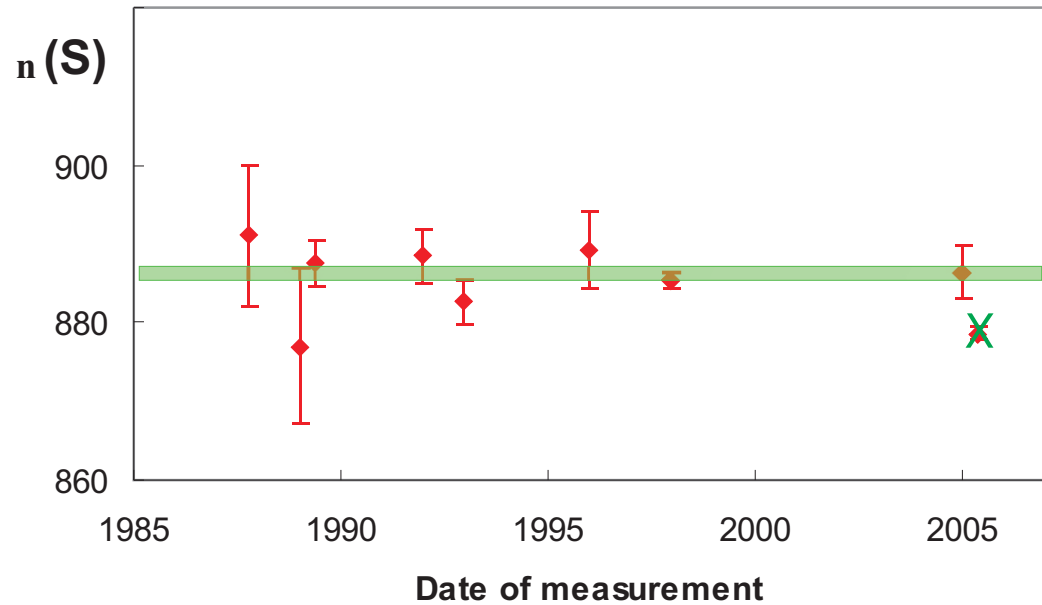
## Mean life:

$$\tau_n = 882.0 \pm 1.3 \text{ s}$$

$$\chi^2/N = 5.4$$

$$\tau_n = 885.6 \pm 0.8 \text{ s}$$

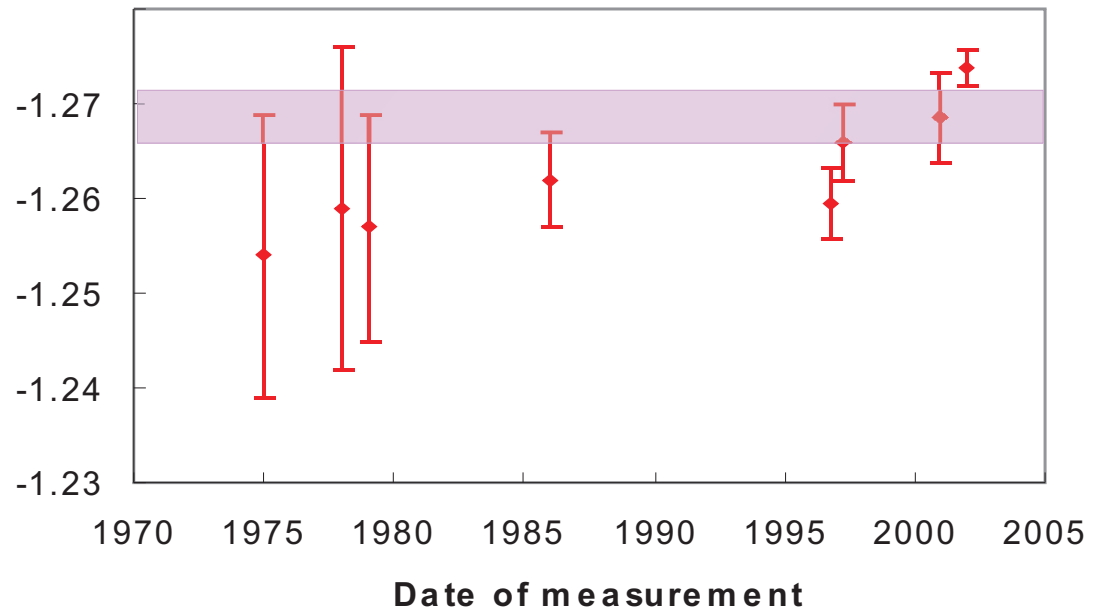
$$\chi^2/N = 0.5$$



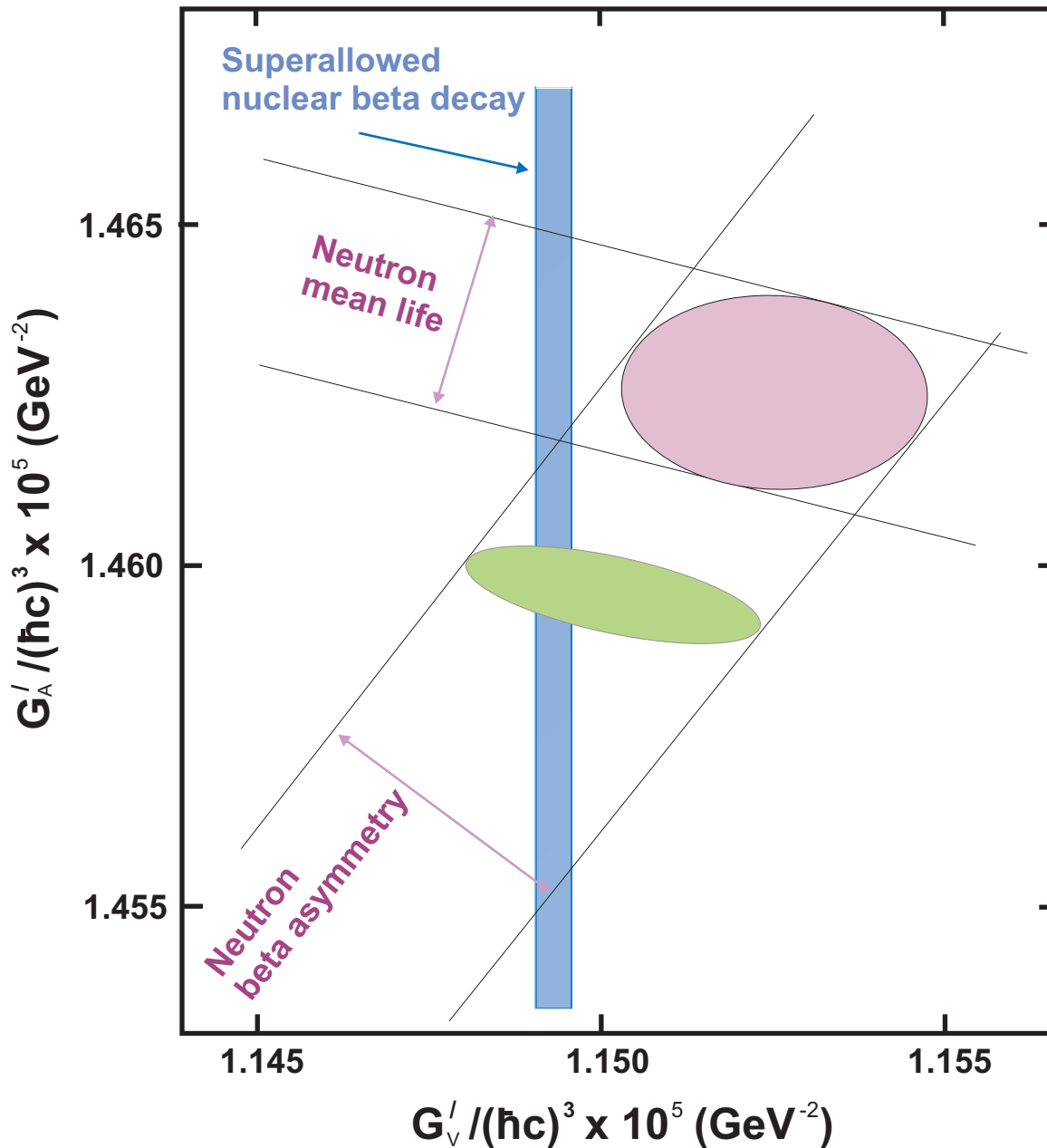
## Beta asymmetry:

$$A_{\beta} = -1.2690 \pm 0.0028$$

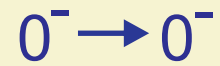
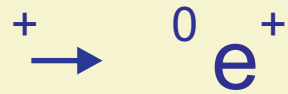
$$\chi^2/N = 2.6$$



# $G_A'$ , $G_V'$ FROM NEUTRON & NUCLEAR DECAY DATA



# PION BETA DECAY

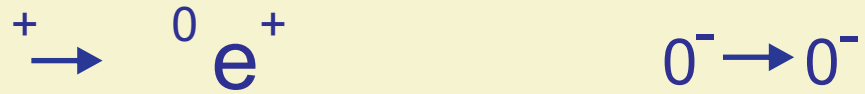


$$V_{ud}^2 = \frac{K}{2G_F^2 (1 + R)(1 + R)ft}$$

$$t = t_{1/2}/BR$$

$$BR \sim 10^{-8}$$

# PION BETA DECAY



$$V_{ud}^2 = \frac{K}{2G_F^2 (1 + R)(1 + R)ft}$$

$$t = t_{1/2}/BR$$

$$BR \sim 10^{-8}$$

## PIBETA experiment

D. Pocanic *et al.*,  
PRL **93**, 181803

$$\text{measured } \frac{BR({}^+ \rightarrow {}^0 e^+)}{BR({}^+ \rightarrow e^+)}$$

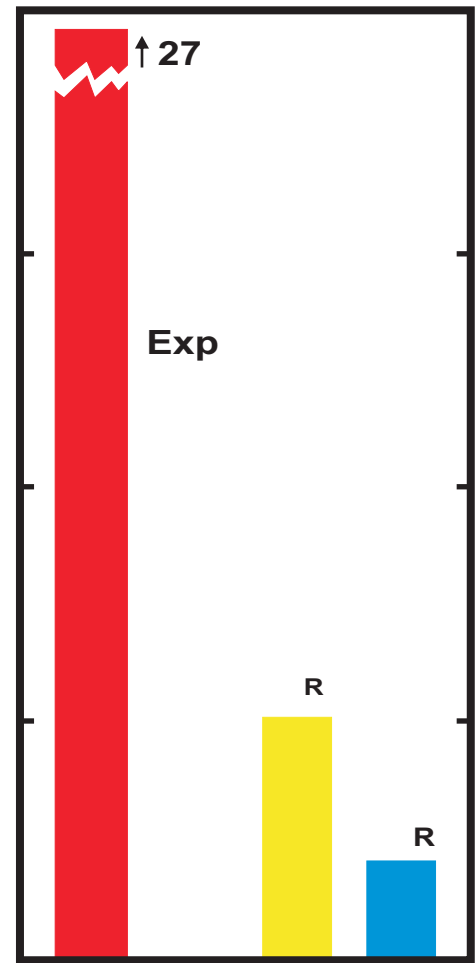
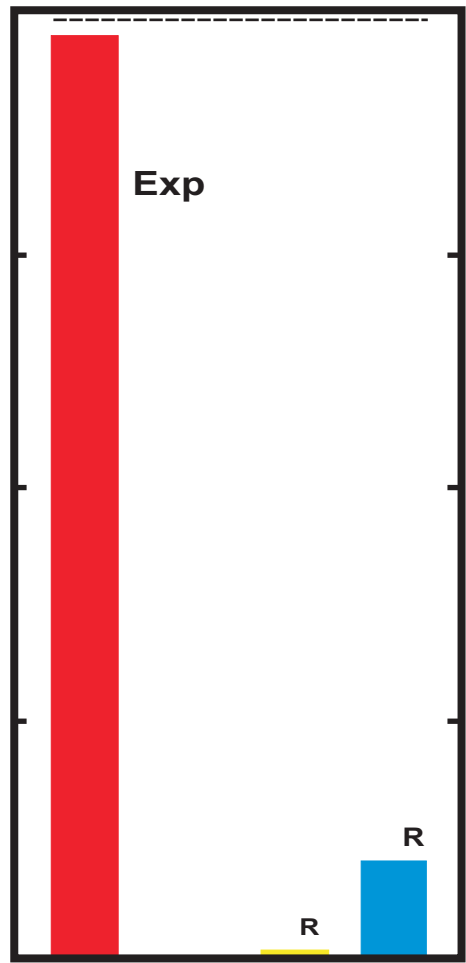
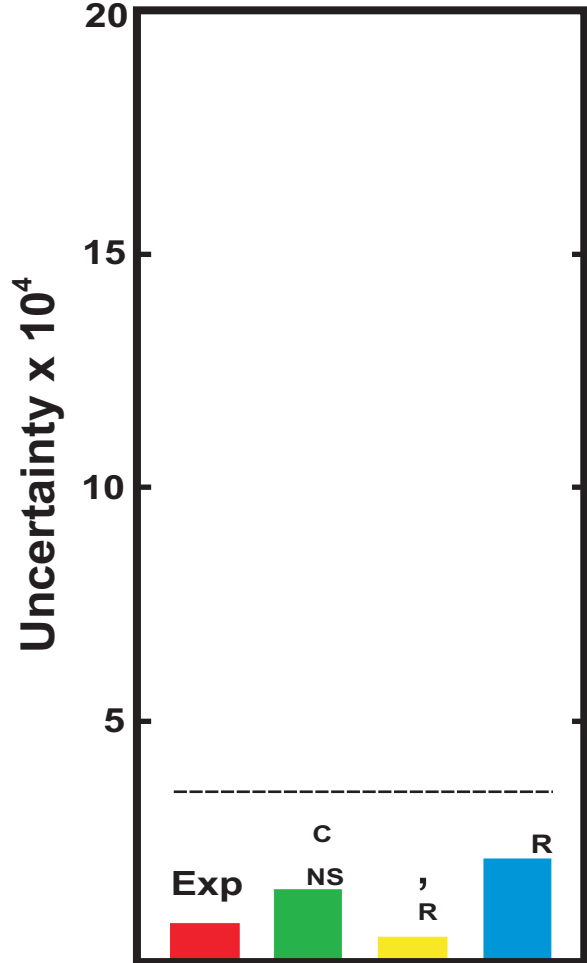
$$\begin{aligned} \text{result } V_{ud} &= 0.9732 \pm 0.0032 && \text{expt BR}_e \\ &= 0.9751 \pm 0.0027 && \text{theo BR}_e \end{aligned}$$

# CONTRIBUTIONS TO $V_{ud}$ UNCERTAINTY

**Nuclear  $0^+ \rightarrow 0^+$**   
 $V_{ud} = 0.9738 \pm 0.0003$

**Neutron**  
 $V_{ud} = 0.9745 \pm 0.0018$   
 (  $0.9765 \pm 0.0020$  )

**Pion beta decay**  
 $V_{ud} = 0.9751 \pm 0.0027$   
 (  $0.9732 \pm 0.0032$  )

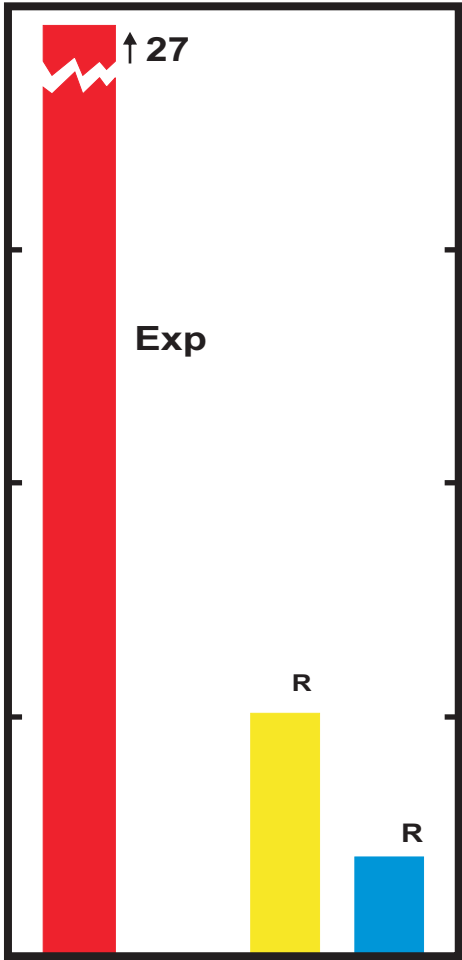
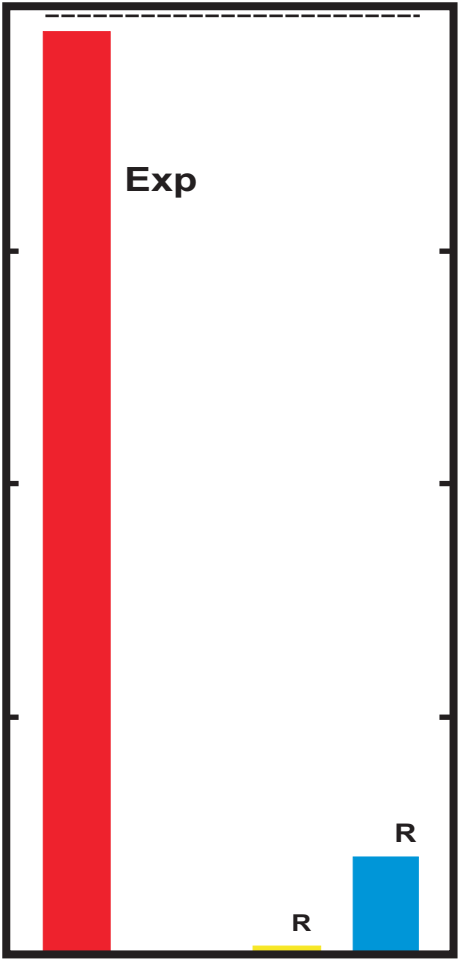
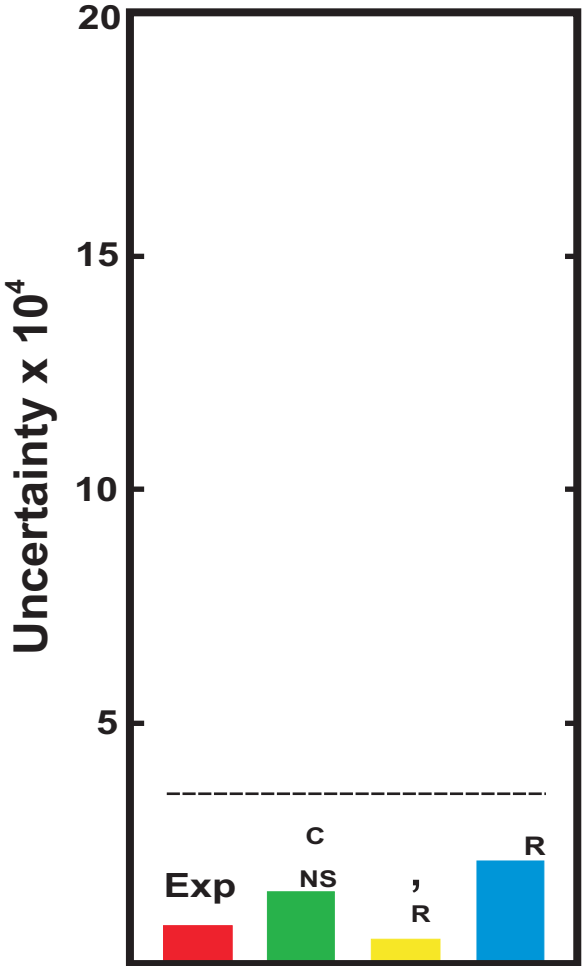


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 (0.9732  $\pm$  0.0032)



## SUMMARY

1. The 2005 superallowed  $\beta$ -decay survey yielded tight limits on new physics: CVC verified to 0.026%;  $|C_S/C_V| < 0.0013$ .
2. In the past two years, the nuclear result for  $V_{ud}$  has been considerably improved by both theory and experiment.
3. Neutron and pion decays still yield much less precise values for  $V_{ud}$ , limited by experimental uncertainties.
4. The superallowed  $\beta$  decay result for  $V_{ud}$  has been stable (with decreasing uncertainties) for decades.
5. Much nuclear activity is now focused on reducing  $V_{ud}$  uncertainty *via* tests of structure-dependent correction terms.
6. With one possible exception, nuclear results continue to support calculated structure-dependent correction terms.
7. CKM unitarity now verified to 0.1%. Uncertainty dominated by  $V_{us}$ , but  $V_{ud}$  will no doubt become critical again.
8. The value of  $V_{ud}$  can be improved further.