

Next Generation Radiative Neutron Decay Experiment

R.L. Cooper¹ T.E. Chupp¹ M.S. Dewey² T.R. Gentile²
H.P. Mumm² J.S. Nico² K.J. Coakley³ B.M. Fisher⁴
I. Kremsky⁴ F.E. Wietfeldt⁴ K.G. Kiriluk⁵ E.J. Beise⁵
H. Breuer⁵ J. Byrne⁶

¹University of Michigan

⁴Tulane University

²NIST, Gaithersburg, MD

⁵University of Maryland

³NIST, Boulder, CO

⁶University of Sussex

- 1 Experimental Developments
- 2 Correlation Coefficient a
- 3 Theoretical Review
- 4 Radiative Corrections
- 5 Summary

Goals for Run II

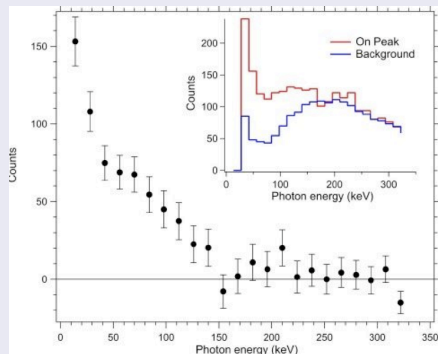
Goals

- 1% precision on branching ratio
- Measure energy spectrum

Obstacles

- Previous run systematics limited
- No response functions previously
- Inverse problem of extracting spectrum from convoluted data

Run I Spectrum

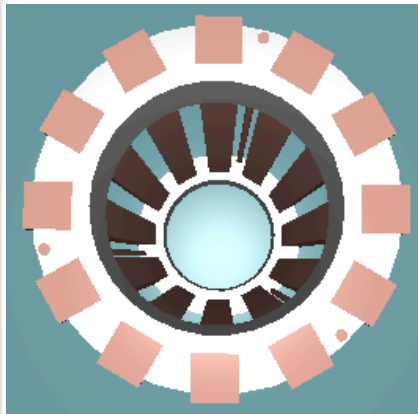


Source of Uncertainty	Correction (%)	Uncertainty (%)
Photon detector gain drift		6.0
Analysis cut efficiencies		5.0
Monte Carlo statistics		4.0
Photon efficiency/resolution	+3.0	3.0
Beam divergence/profile		3.0
Electron bremsstrahlung	-3.0	3.0
B field registration		2.0
Mirror potential registration		1.0
Electron backscattering		0.5
Electronic artifacts		0.5
Total	-0.0	10.4

New Hardware for Run II

Improvements

- 12-Element γ Detector
Higher statistics
Different sensitivity to correlated backgrounds
- Improved beam optics
“Active” area smaller than current beam
- Rigorous calibration routines
- Improved electronics
New Gage Octopus card
8 channels / card
Up to 125 MHz sampling
14-bit bipolar resolution
- Bare APD?



New Hardware for Run II

Improvements

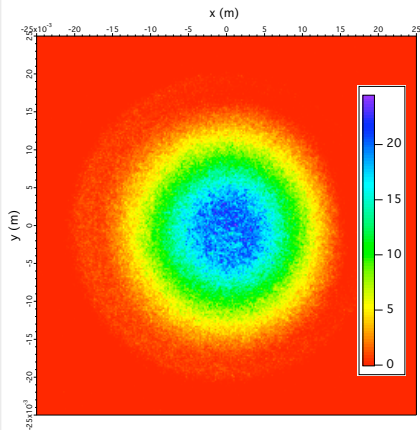
- 12-Element γ Detector
Higher statistics
Different sensitivity to correlated backgrounds
- Improved beam optics
“Active” area smaller than current beam
- Rigorous calibration routines
- Improved electronics
New Gage Octopus card
8 channels / card
Up to 125 MHz sampling
14-bit bipolar resolution
- Bare APD?



New Hardware for Run II

Improvements

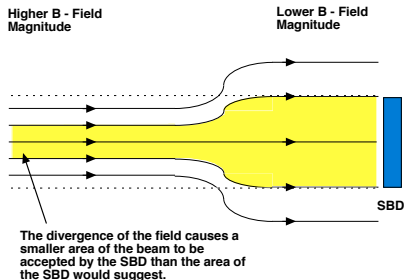
- 12-Element γ Detector
Higher statistics
Different sensitivity to correlated backgrounds
- Improved beam optics
“Active” area smaller than current beam
- Rigorous calibration routines
- Improved electronics
New Gage Octopus card
8 channels / card
Up to 125 MHz sampling
14-bit bipolar resolution
- Bare APD?



New Hardware for Run II

Improvements

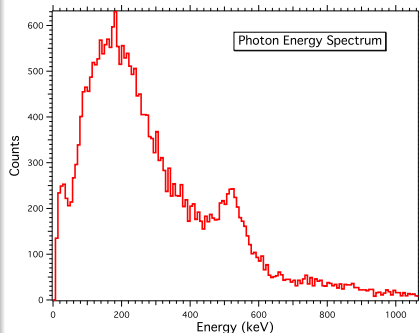
- 12-Element γ Detector
Higher statistics
Different sensitivity to correlated backgrounds
- Improved beam optics
“Active” area smaller than current beam
- Rigorous calibration routines
- Improved electronics
New Gage Octopus card
8 channels / card
Up to 125 MHz sampling
14-bit bipolar resolution
- Bare APD?



New Hardware for Run II

Improvements

- 12-Element γ Detector
Higher statistics
Different sensitivity to correlated backgrounds
- Improved beam optics
“Active” area smaller than current beam
- **Rigorous calibration routines**
- Improved electronics
New Gage Octopus card
8 channels / card
Up to 125 MHz sampling
14-bit bipolar resolution
- Bare APD?



New Hardware for Run II

Improvements

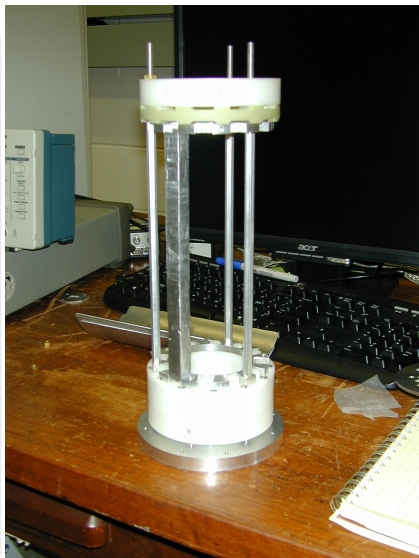
- 12-Element γ Detector
Higher statistics
Different sensitivity to correlated backgrounds
- Improved beam optics
“Active” area smaller than current beam
- Rigorous calibration routines
- Improved electronics
New Gage Octopus card
8 channels / card
Up to 125 MHz sampling
14-bit bipolar resolution
- Bare APD?



12-Element Detector

Nearly complete!

- 12 BGO crystals coupled to 12 APDs
- Requires 12 independent HV sources to individually adjust gains
- Each APD varies slightly
- 12 Preamp signals coupled to Gage Octopus cards
- Currently doing dewar tests
 - Temperature stability
 - Gain
 - Compton
 - Crosstalk noise / pickup



12-Element Detector

Nearly complete!

- 12 BGO crystals coupled to 12 APDs
- Requires 12 independent HV sources to individually adjust gains
- Each APD varies slightly
- 12 Preamp signals coupled to Gage Octopus cards
- Currently doing dewar tests
 - Temperature stability
 - Gain
 - Compton
 - Crosstalk noise / pickup



Dewar Tests

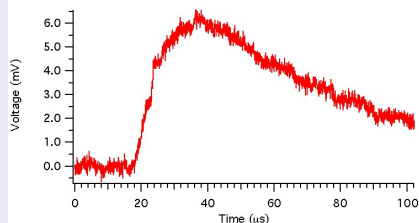
Current Work

- Test data being collected
- Learning about electronics
- Building DAQ
- Benchmarking APDs

Naive Analysis

- Adjust baseline
- Find peak channel
- Some small ripple
- Histogram these peaks
- **Operational**

Sample Trace



Stability Test

- Filled 5 hrs earlier
- Topped off 1 hr earlier
- Gaussian fit to histogram

Dewar Tests

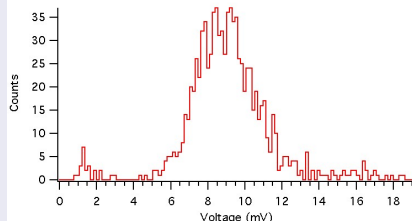
Current Work

- Test data being collected
- Learning about electronics
- Building DAQ
- Benchmarking APDs

Naive Analysis

- Adjust baseline
- Find peak channel
- Some small ripple
- Histogram these peaks
- **Operational**

Histogram



Stability Test

- Filled 5 hrs earlier
- Topped off 1 hr earlier
- Gaussian fit to histogram

Dewar Tests

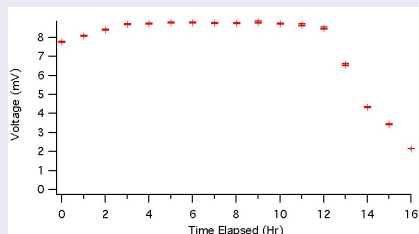
Current Work

- Test data being collected
- Learning about electronics
- Building DAQ
- Benchmarking APDs

Naive Analysis

- Adjust baseline
- Find peak channel
- Some small ripple
- Histogram these peaks
- **Operational**

Peak vs. Time

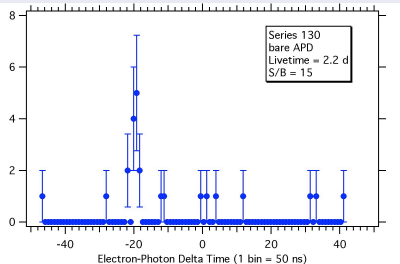


Stability Test

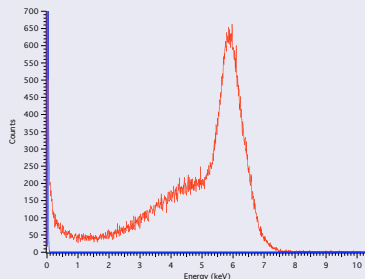
- Filled 5 hrs earlier
- Topped off 1 hr earlier
- Gaussian fit to histogram

Bare APD Photon Detector

$\Delta t_{e-\gamma}$ histogram



^{55}Fe 5.899 keV X-Ray



- Detects lower energy (100 eV threshold)
- Higher rate. BR [0.10-10 keV] $\approx 6.4 \times 10^{-3}$ (theory)

- High S/B in runs
- Small surface area
- Faster response time

Outline

- 1 Experimental Developments
- 2 Correlation Coefficient a**
- 3 Theoretical Review
- 4 Radiative Corrections
- 5 Summary

- Photon philosophy
Record first, ask questions later
- Many *ep* events collected with no energetic photon recorded
- Is there more information in our *ep* data?
- Over 10^7 total *ep* events recorded

- Unpolarized neutron decay rate (tree level)

$$\frac{d\Gamma}{dE_e d\Omega_e d\Omega_\nu} \propto p_e E_e (E_0 - E_e)^2 \left(1 + a \frac{p_e \cos \theta_{e\nu}}{E_e} \right)$$

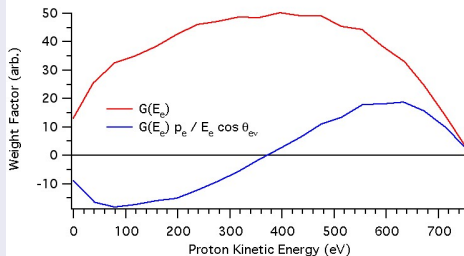
- Use Monte Carlo to integrate over all variables except E_p

$$\frac{d\Gamma}{dE_p} = f_1(E_p) + a \cdot f_a(E_p)$$

Proton Energy Dependence

- $f_a(E_p)$ term has strong proton energy dependence
- Experiment sensitive to proton energy can be made sensitive to a
- Electrostatic mirror does this in a very crude fashion

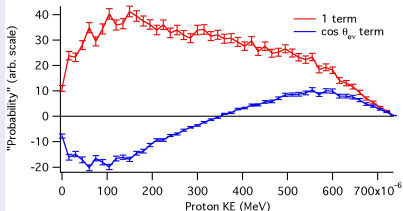
Dependence vs. Proton KE



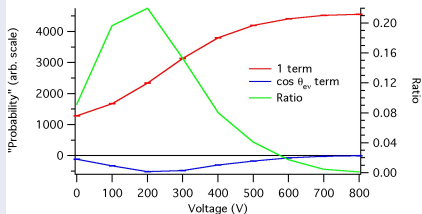
Phase Space Dependence

- Apparatus only sensitive to fraction of total available phase space
- Changes with mirror voltage
- Summing over proton energy yields contribution at particular voltage

0 V



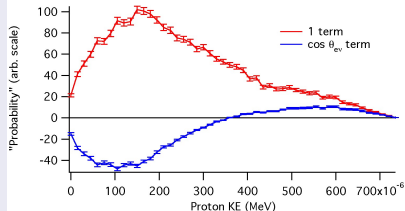
f_1 and f_a vs. Voltage



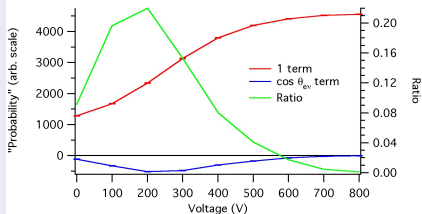
Phase Space Dependence

- Apparatus only sensitive to fraction of total available phase space
- Changes with mirror voltage
- Summing over proton energy yields contribution at particular voltage

200 V



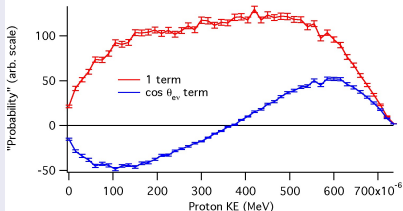
f_1 and f_a vs. Voltage



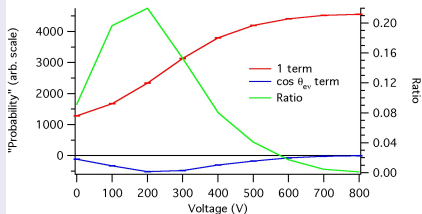
Phase Space Dependence

- Apparatus only sensitive to fraction of total available phase space
- Changes with mirror voltage
- Summing over proton energy yields contribution at particular voltage

800 V



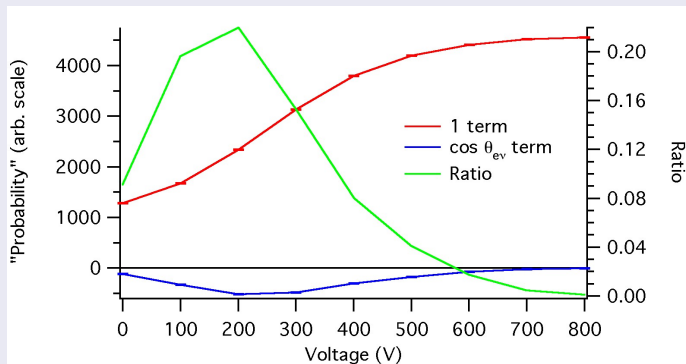
f_1 and f_a vs. Voltage



Weak Dependence

- Highest sensitivity $\approx 25\%$
- $a \approx 0.1$
- 2.5% sensitive at best
- $> 10^7$ ep events!

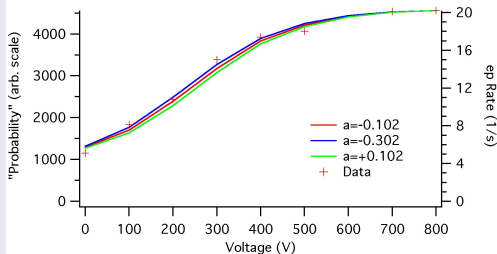
f_1 and f_a vs. Voltage



Preliminary Comparison to Data

- Current data doesn't constrain a
- Found run to run deviations
- Ratio method insensitive to deviations
- Illustrates low sensitivity
- A consistency check

Ratio vs. a



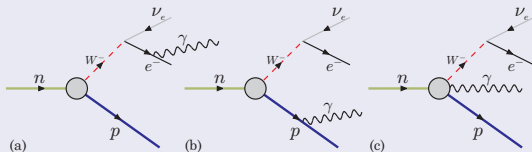
- More to come!

Outline

- 1 Experimental Developments
- 2 Correlation Coefficient a
- 3 Theoretical Review**
- 4 Radiative Corrections
- 5 Summary

Radiative Decay Matrix Element

Tree-level Feynman Diagrams



- (a), (b) QED calculable and (c) require HB χ PT EFT

$$\begin{aligned}
 \mathcal{M}_{\text{QED}} = & i \frac{eg_V}{\sqrt{2}} \left[\bar{u}_e(p_e) \frac{(2p_e \cdot \epsilon + \not{\epsilon} \not{p}_\gamma)}{2p_e \cdot p_\gamma} \gamma_\mu (1 - \gamma_5) v_{\bar{\nu}}(p_\nu) \right. \\
 & \times \bar{u}_p(p_p) \gamma^\mu (1 - \lambda \gamma_5) u_n(p_n) \\
 & - \bar{u}_e(p_e) \gamma_\mu (1 - \gamma_5) v_{\bar{\nu}}(p_\nu) \\
 & \left. \times \bar{u}_p(p_p) \frac{(2p_p \cdot \epsilon + \not{\epsilon} \not{p}_\gamma)}{2p_p \cdot p_\gamma} \gamma^\mu (1 - \lambda \gamma_5) u_n(p_n) \right]
 \end{aligned}$$

- Proton bremsstrahlung small contribution.
- Electron $\mathcal{O}(1)$
proton $\mathcal{O}(q/m_p)$
- Electron term only, is it correct? **NO**
- Use both, is this correct?
YES
- What's wrong with intuition?
NOTHING
- What's the resolution?

$$\frac{d\Gamma}{d^8X} = (1 + 3\lambda^2) \left[\frac{f_1(X)}{(p_e \cdot p_\gamma)^2} + \frac{f_2(X)}{(p_e \cdot p_\gamma)(p_p \cdot p_\gamma)} + \frac{f_3(X)}{(p_p \cdot p_\gamma)^2} \right. \\ \left. + a \left(\frac{f_1(X)}{(p_e \cdot p_\gamma)^2} + \frac{f_2(X)}{(p_e \cdot p_\gamma)(p_p \cdot p_\gamma)} + \frac{f_3(X)}{(p_p \cdot p_\gamma)^2} \right) \right]$$

where X is all the kinematic variables

- The **gauge invariant** trick

$$\sum_{\text{polarizations}} \epsilon_{\mu}^* \epsilon_{\nu} \rightarrow -g_{\mu\nu}$$

can only work with diagrams that are **gauge invariant**

- Electron diagram alone is NOT **gauge invariant**
- Electron diagram and proton diagram together are **gauge invariant** \Rightarrow Trick works
- To use only electron diagram \Rightarrow “**brute force**”
- Input ϵ_{μ} polarization explicitly
- “**Brute force**” on electron diagrams
= **gauge invariant** trick on both diagrams (tree level)
- $\mathcal{O}(1)$ proton contribution “illusory” \rightarrow cancels

Polarized Neutron Radiative Decay

- Calculation for unpolarized neutron
- Add polarization P by

$$u_n^s(p_n) \rightarrow \frac{1 + \gamma_5 P}{2} u_n^s(p_n)$$

- Decay rate is

$$\begin{aligned} \frac{d\Gamma}{d^8X} &= (1 + 3\lambda^2) [g_1(X) + ag_2(X) \\ &+ \mathbf{P} \cdot (Ag_3(X)\mathbf{p}_e + Bg_4(X)\mathbf{p}_\nu + Ag_5(X)\mathbf{k})] \end{aligned}$$

where a, A, B are familiar from non-radiative decay

- Photon - neutron polarization coefficient is A , not unexpected, electron bremsstrahlung and lowest order

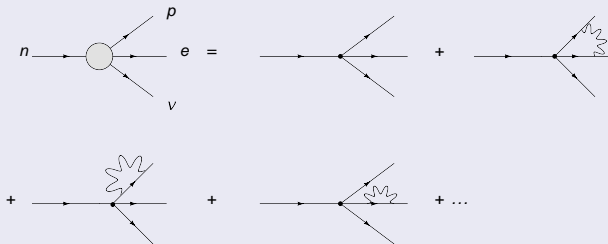
Outline

- 1 Experimental Developments
- 2 Correlation Coefficient a
- 3 Theoretical Review
- 4 Radiative Corrections**
- 5 Summary

Neutron Decay Vertex

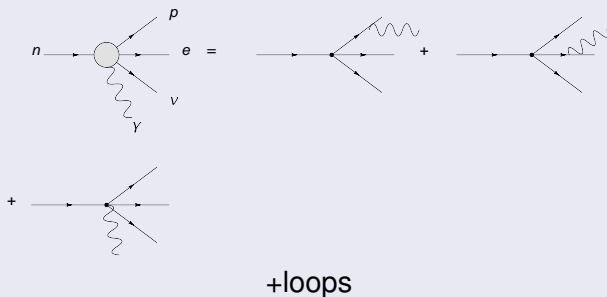
- Neutron decay begins with g_V^0 and g_A^0 at tree level
- Higher order loops correct g_V^0 and g_A^0
- Infrared divergences
- Bremsstrahlung diagrams needed

3-Body Final States



- Radiative decay experiment is just this subset
- With energy windows, hard / soft photon cutoff is explicit
- Cutoff can vary by design

4-Body (Bremsstrahlung) Final States



- Neutron decay is 3-body tree level diagram + loops with bremsstrahlung diagrams (with their subsequent loops) “incoherently” added to decay rate
- Expect $g_V^0 \rightarrow g_V$
- g_A hard to calculate, measure λ
- Radiative decay just a subset though!
- Why not $g_V^0 \rightarrow g_V'$ and measure λ' from only radiative decays?
- Energy dependent radiative corrections established in ${}^3\text{H}$ β -decay
S. Gardner et al., Phys. Lett. B **598**, 188 (2004)

Outline

- 1 Experimental Developments
- 2 Correlation Coefficient a
- 3 Theoretical Review
- 4 Radiative Corrections
- 5 Summary**

- Upgrade to new detector is underway
- Experiment is slightly sensitive to a , requires understanding systematics very well
- Provides more diagnostic checks
- Calculation confusion cleared up
- Calculation applied to polarized neutron system (tree level)
- Seeing vertex bremsstrahlung and measuring radiative corrections will likely require NLO calculations ($\text{HB}\chi\text{PT}$ and recoil order terms)