

FUSION (& fission) BARRIERS

FROM SELF-CONSISTENT CALCULATIONS
AS A DF TEST

1. SHORT REVIEW OF FISSION BARRIERS
2. FUSION BARRIERS :
 - STATIC CALCULATIONS
 - PROBLEMS
 - RESULTS
3. CONCLUSIONS

Fission barriers: from (n, f) , (d, pf) , ...
 If those are impossible ($Z > 100$):

$$\sigma_{ER}^{A_1 + A_2 \rightarrow B}(E) \approx \pi \frac{\hbar^2}{2\mu E} \times$$

$$\sum_{l=0}^{\infty} \left\{ (2l+1) T(E, l) \right\} \times \left\{ \begin{array}{l} \text{fusion} \\ \text{barrier} \\ A_1 + A_2 \end{array} \right.$$

$$P_{CN}(A_1 + A_2 \rightarrow C; E, l) \times \left\{ \begin{array}{l} ? \end{array} \right.$$

$$P_{ER}(C \rightarrow B; E^*, l) \left\{ \begin{array}{l} \text{fission} \\ \text{barrier } C \\ \text{(statistical)} \\ \text{model} \end{array} \right.$$

$$\sigma_{\text{capture}}(E) = \pi \hbar^2 \sum_{l=0}^{\infty} (2l+1) T(E, l)$$

$$\sigma_{\text{fusion}}(E) = \pi \hbar^2 \sum_{l=0}^{\infty} (2l+1) T(E, l) P_{CN}(E, l)$$

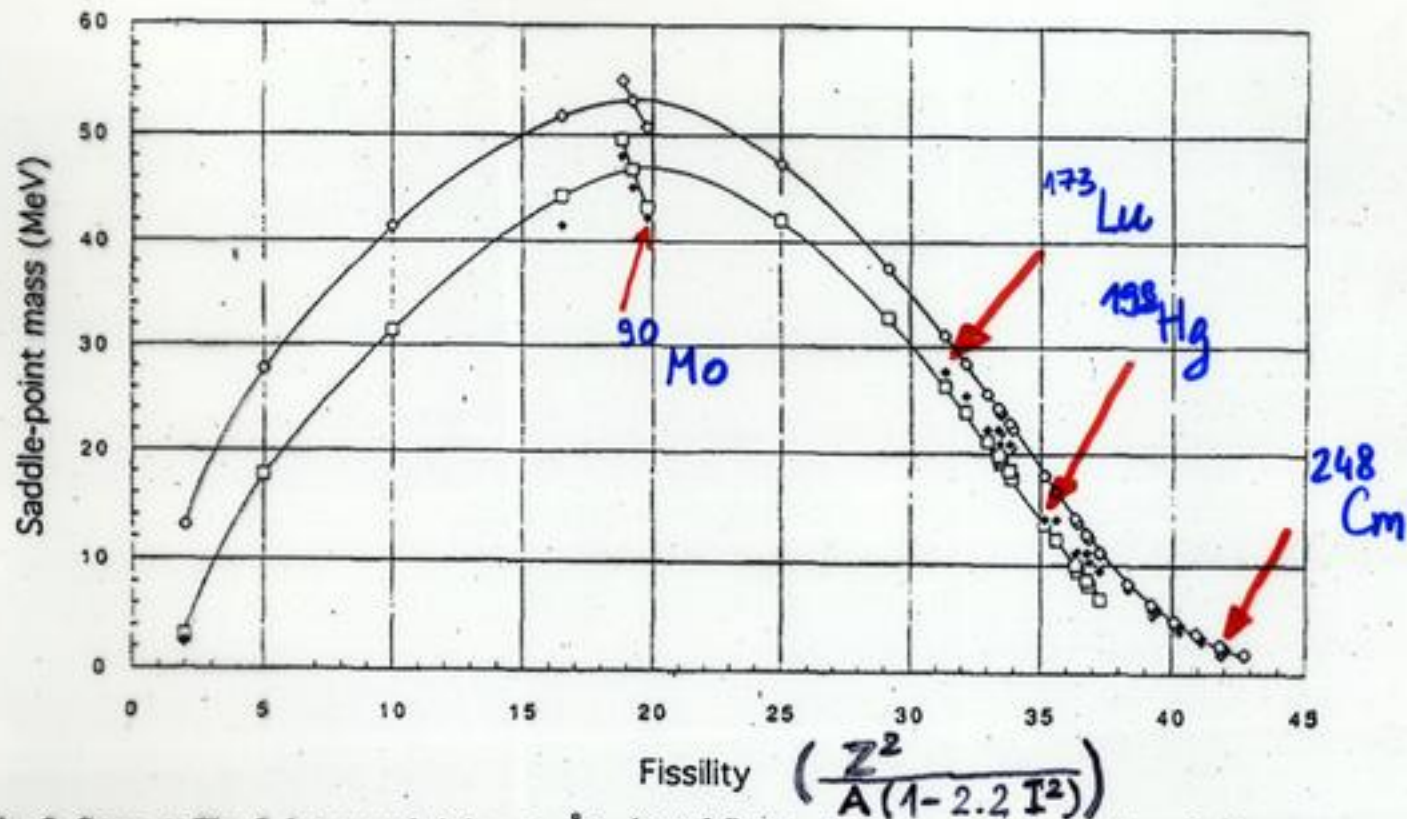


Fig. 3. Same as Fig. 2, but extended down to ^8Be (Ref. [5]). The four points around fissility 16–20 refer to ^{75}Br and $^{90,94,98}\text{Mo}$ (Ref. [9]).

(Fission barriers) ($\blacklozenge$) - measured
 (- G.S. Shell Correction) $\leftarrow$ "MACROSCOPIC" BARRIERS

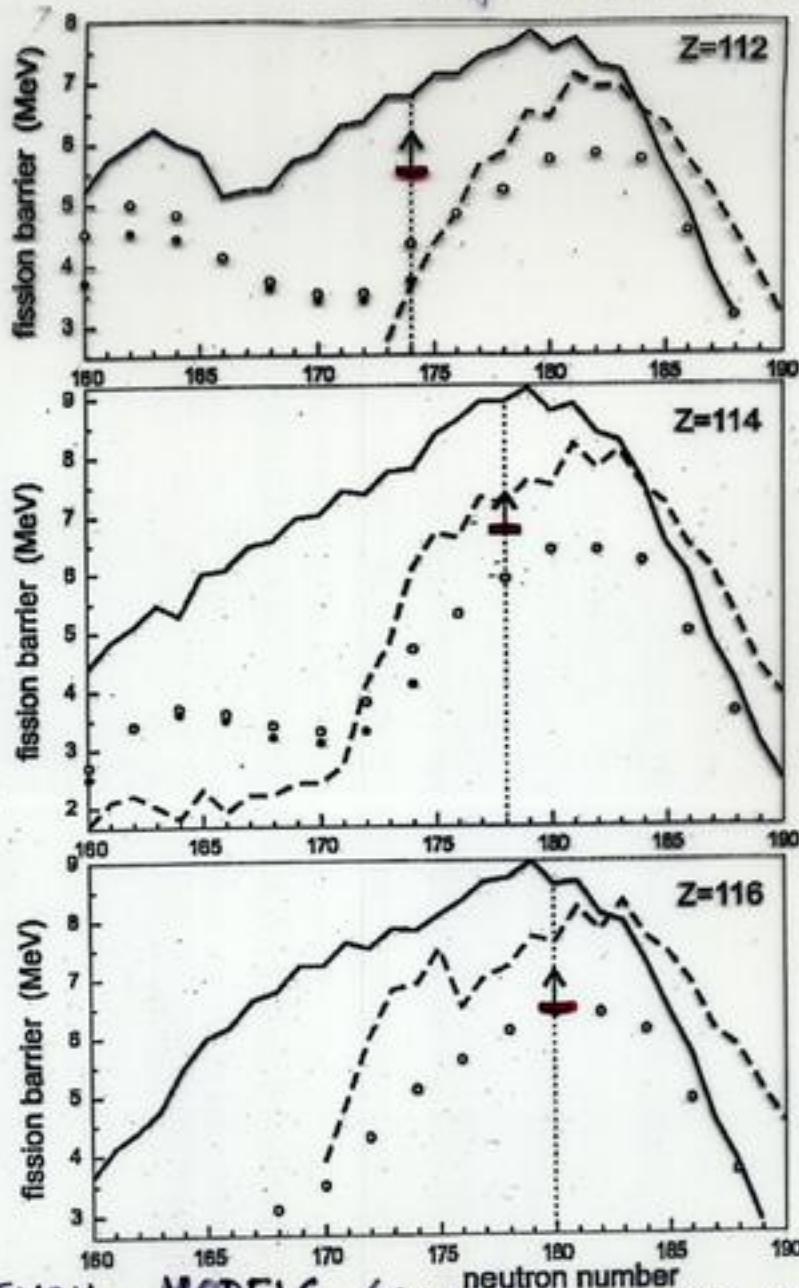
(W.D. Myers & W.J. Swiatecki, NPA 612, p. 249)

Experimental barriers for the heaviest nuclei

M.G. Itkis, Yu. Ts. Oganessian & V.I. Zagrebaev

Phys. Rev. C 65 044602

(2002)



VS PHENOM. MODELS (SMOOTH ENERGY+ SHELL CORR.)

— P. Möller et al., At. Data 59, 185 (1995)

---- A. Mamdouh et al., N.P.A 679, 337 (2001)

oooo R. Smolańczuk et. al.

* Results from Skyrme HF :
& relativistic MF

(T. Bürvenich et al., Phys. Rev. C 69, 014307, (2004))

	Expt.	MG3	SLy6
$^{286}_{112}$	5.5	3.38	6.06
$^{292}_{114}$	6.7	$^{(290)}_{3.56}$	$^{(290)}_{8.52}$
$^{296}_{116}$	6.5	$^{(294)}_{3.80}$	$^{(294)}_{9.59}$

← WITHOUT
NONAXIALITY
NO CORRECTIONS

Too large barriers for actinides.

* Skyrme Sk M* :

(L. Bonneau et al., Eur. Phys. J A 21, 381, (2004))

	exp.	B_A cal.	exp.	B_B cal.
$^{230}_{Th}$	6.1	4.9	6.5	4.4
$^{232}_{Th}$	5.8	5.5	6.2	4.1
$^{234}_{U}$	5.6	5.3	5.5	5.1
$^{236}_{U}$	5.6	6.2	5.6	4.6
$^{240}_{Pu}$	5.6	7.1	5.1	4.1
$^{252}_{Cf}$	5.3	7.1	3.5	2.9

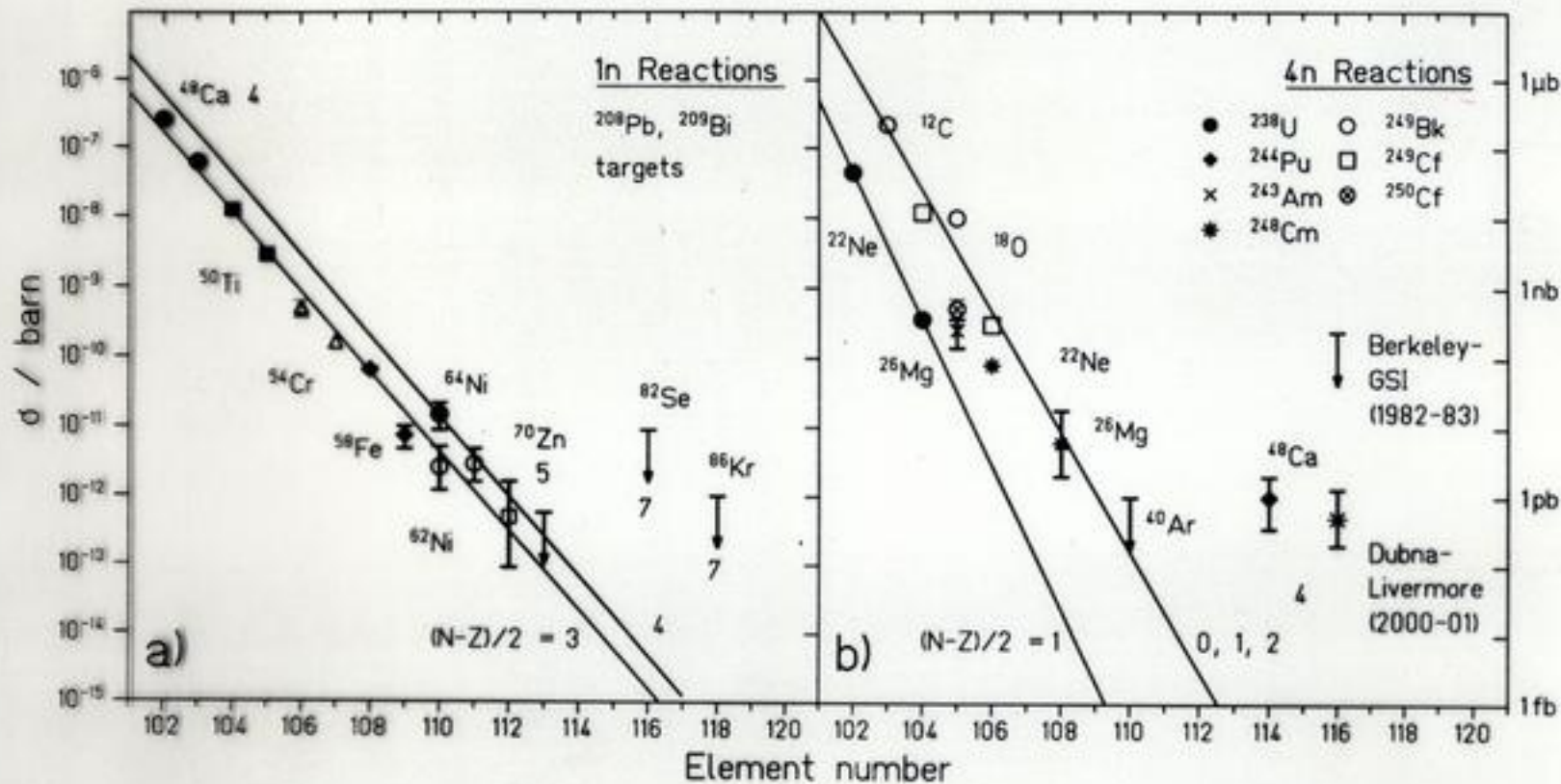
WITH
NONAXIALITY
&
ROT. CORRECTION
 $\left(-\frac{I^2}{2J}\right)$

(Probably too large barriers for superheavy)

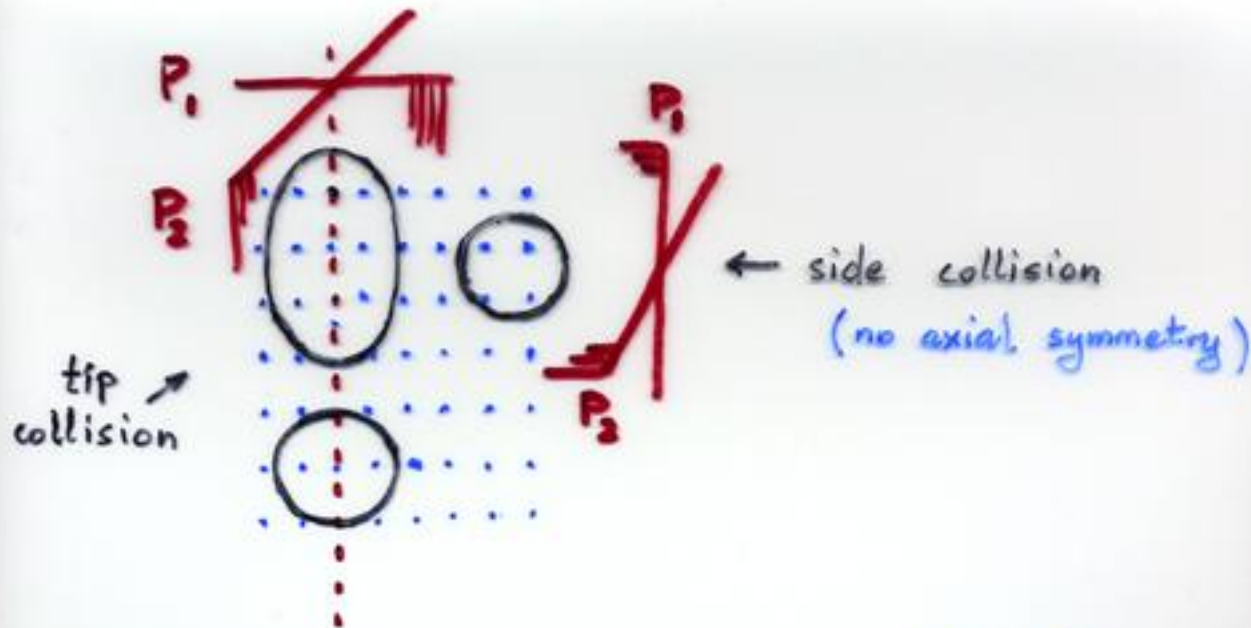
Nucleus-nucleus potentials at near-barrier energies from selfconsistent calculations.

i. Motivation

1. Definition of the static potential.
2. Important technical problems:
 - A. Specification of the entrance channel.
 - B. Question of the relative kinetic energy.
 - C. Continuous change of pairing in a system undergoing fusion or fission.
3. Examples of results and comparisons to data.
 - A) Barriers
 - B) Landscapes
4. Conclusions.



S. Hofmann (GSI)



static barrier : for $E_{1+2}(g.s.) \rightarrow Q$ value

$$V(R) = \overbrace{E_{1+2}(R) + B_1 + B_2}^{\text{for } E_{1+2}(g.s.) \rightarrow Q \text{ value}}$$

$\wedge$ $\vee$
 0 0

Within:
HF

To have $V=0$ at $R \rightarrow \infty$:

$$V \rightarrow V - E_{\text{kinetic relative}}$$

↓

$$\frac{A_2 \langle t_1 \rangle + A_1 \langle t_2 \rangle}{A_1 + A_2}$$

- We calculate V for $l=0$.
- We use Skyrme force SkM* (also SkP and SLy6)
- No pairing or δ pairing with cutoff

Fragments A_1 and A_2 ;

$$i=1,2 : \bar{P}_i = \left(\sum_{k \in i} \bar{P}_k \right) ; \quad \bar{P} = \bar{P}_1 + \bar{P}_2$$

$$\frac{\bar{P}_1^2}{A_1} + \frac{\bar{P}_2^2}{A_2} = \frac{A_2 \bar{P}_1^2 + A_1 \bar{P}_2^2}{A_1 + A_2} + \frac{\bar{P}^2}{A_1 + A_2} - \frac{\bar{P}_1 \cdot \bar{P}_2}{A_1 + A_2}$$

E_{cm} correction $\uparrow$ for 2 fragments

$E_{kinetic}$ relative

E_{cm} for a composed fragment

With the 2-body part :

$$E_{cm} = \left\langle \frac{\bar{P}^2}{A} \right\rangle = \begin{cases} 5.85 \text{ MeV} & \text{for } ^{208}\text{Pb} \\ 8.20 \text{ MeV} & \text{for } ^{48}\text{Ca} \\ 5.7 \text{ MeV} & \text{for } ^{256}\text{No} \end{cases}$$

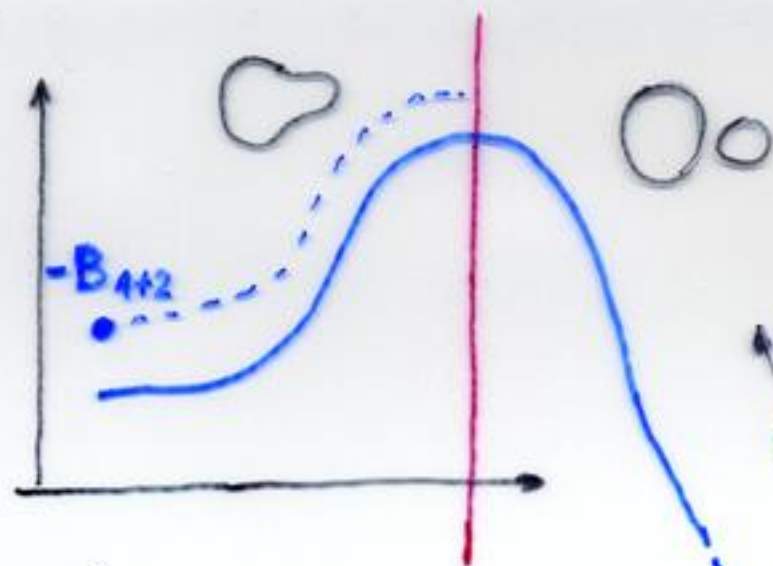
$$\rightarrow E_{cm}(^{208}\text{Pb}) + E_{cm}(^{48}\text{Ca}) - E_{cm}(^{256}\text{No}) \approx$$

$$\text{e.g. J.F. Banger & D. Gogney NPA333, 302(1980)} = \underline{8.3 \text{ MeV}}$$

By this amount one has to lower the barrier for separating fragments.

It should have effect on barriers for fission of the light nuclei.
(They are close to scission.)

$$\text{For SkM* : } E_{cm} \approx \langle \hat{t} \rangle_{\text{one body}} = 14-18 \text{ MeV}$$



Deformation energy I_{DEF}
of $(1+2)$ system

" I_{DEF} " for
1 & 2 separated

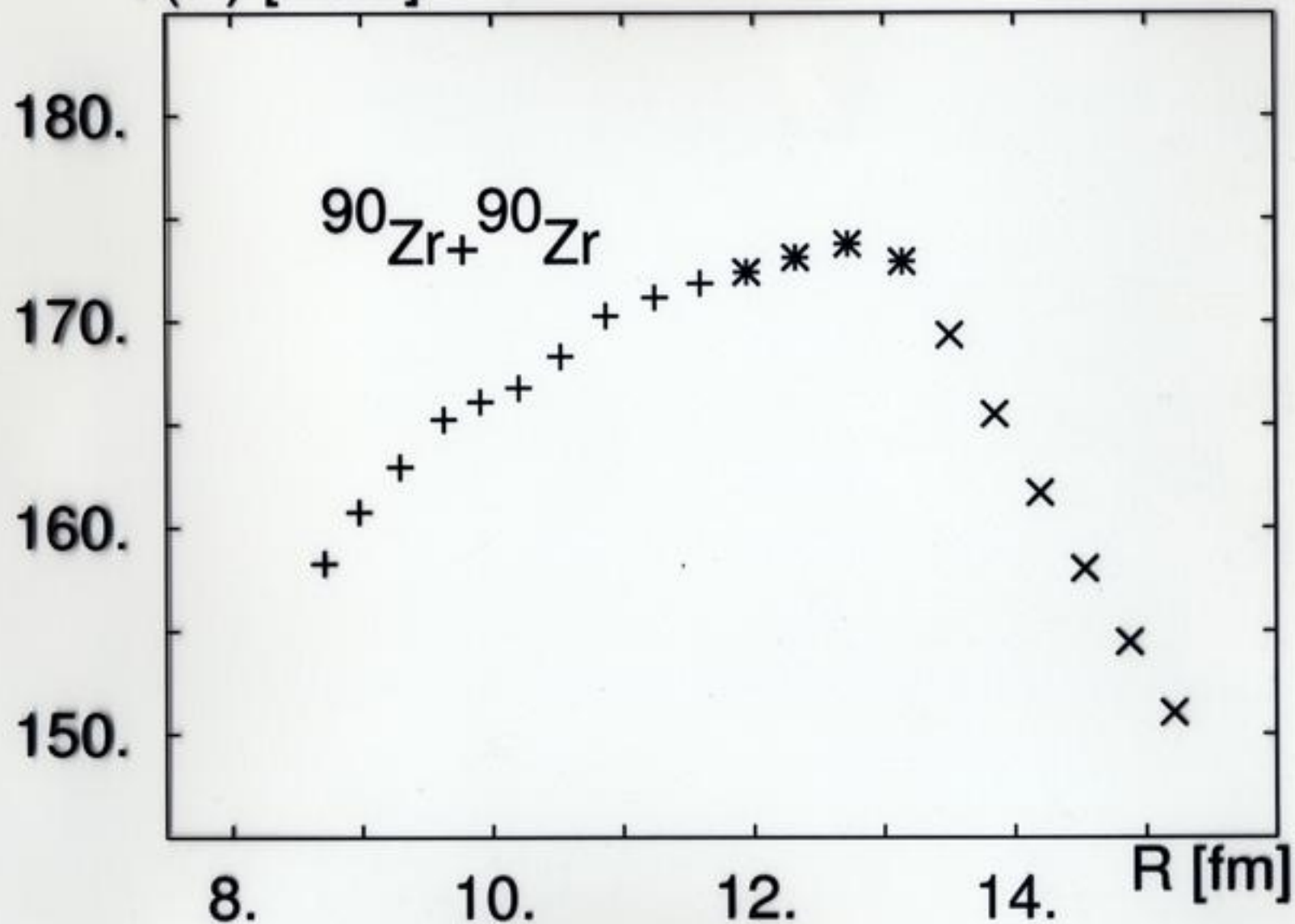
$-(B_1 + B_2)$

$$E^* - B_{1+2} = - (B_1 + B_2) + \underbrace{V_{fus} + E}_{E_{kin}(CM)}$$

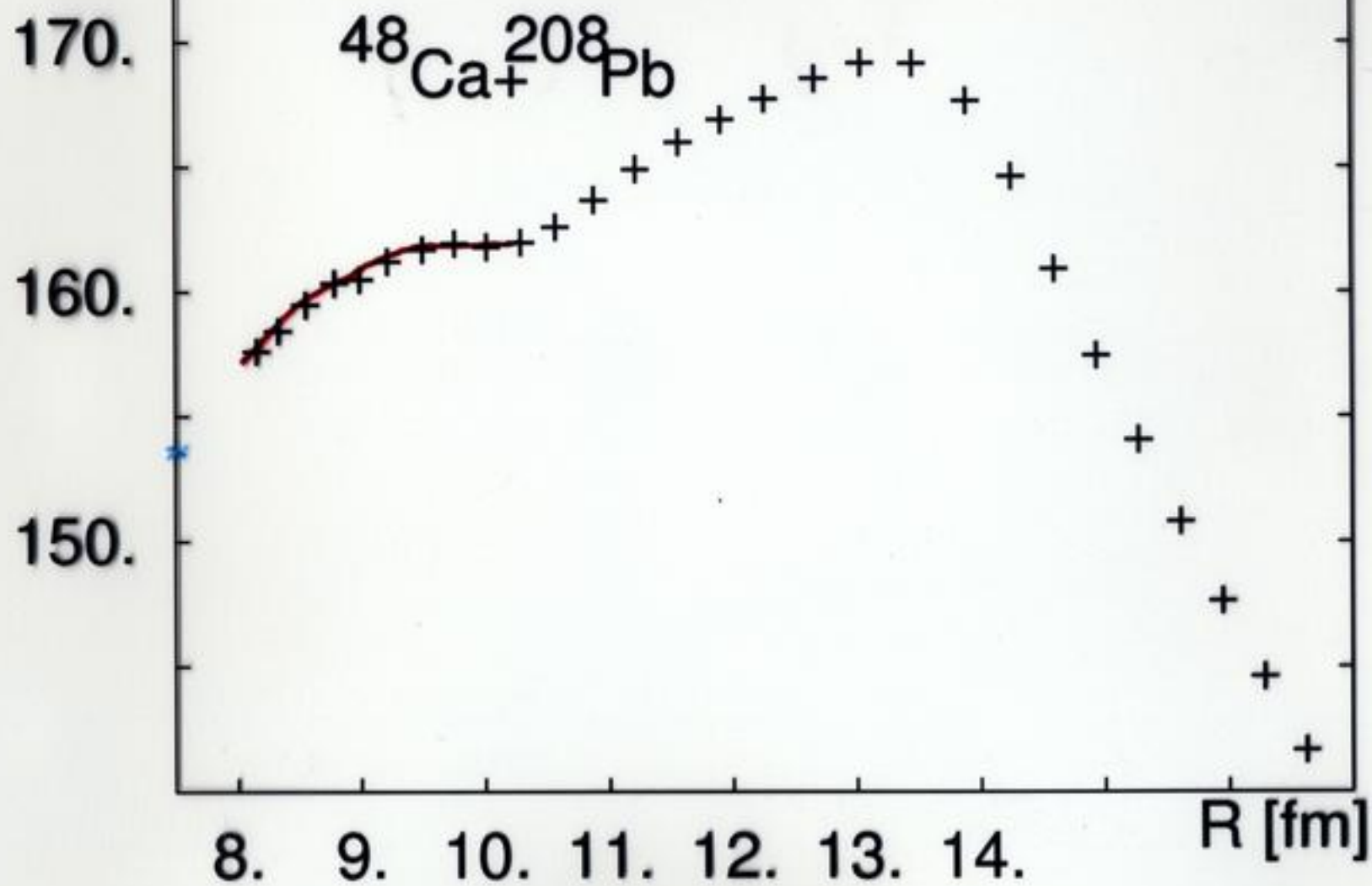
$$E_{min}^* = Q + V_{fus} \quad (\text{no tunneling})$$

SkM*, no pairing

$V(R)$ [MeV]



$V(R)$ [MeV]



^{256}No

$B_{\text{fis}} = 11.5 \text{ MeV}$
(9.5 NONAL)

[MeV]

-1865
-1870
-1875
-1880
-1885
-1890

40b
0

2

4

6

8

10

12

14

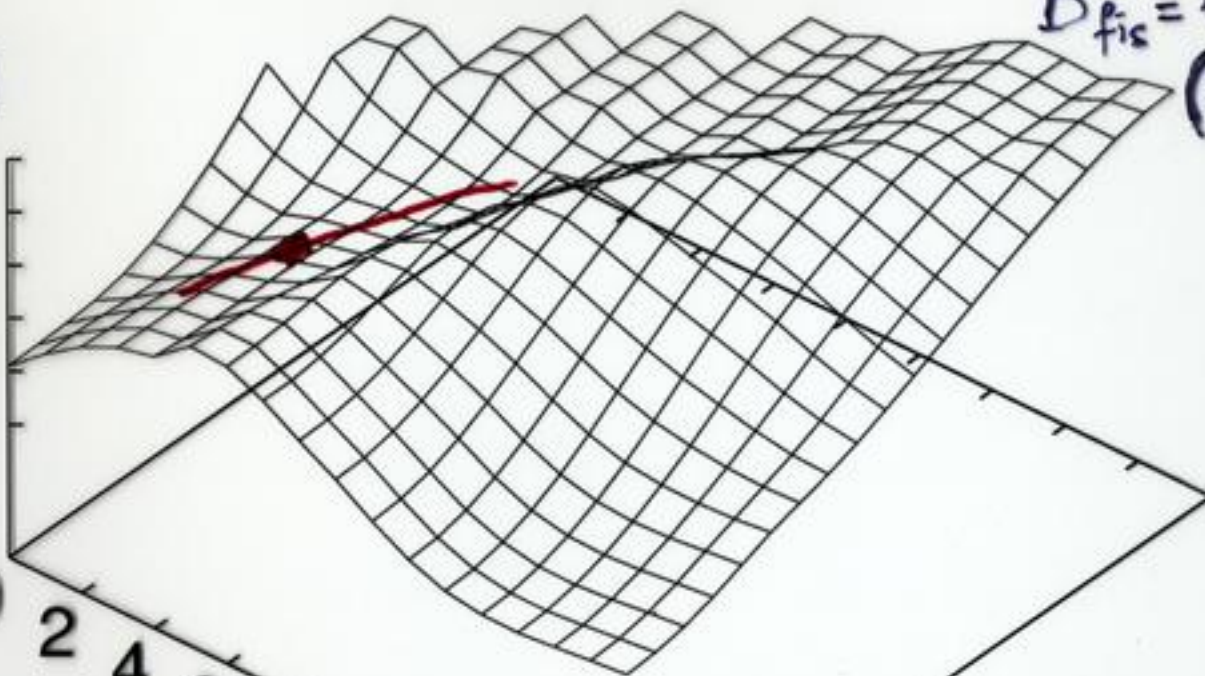
16

125b

Q

0

Q_{30}
 28×10^3
 fm^3



$V(R)$ [MeV]

↑ contact

200.

190.

180.

170.

160.

■ & ○: pairing
+, ×, *, □: no pairing
↑ frozen occupations

$^{48}\text{Ca} + ^{244}\text{Pu}$

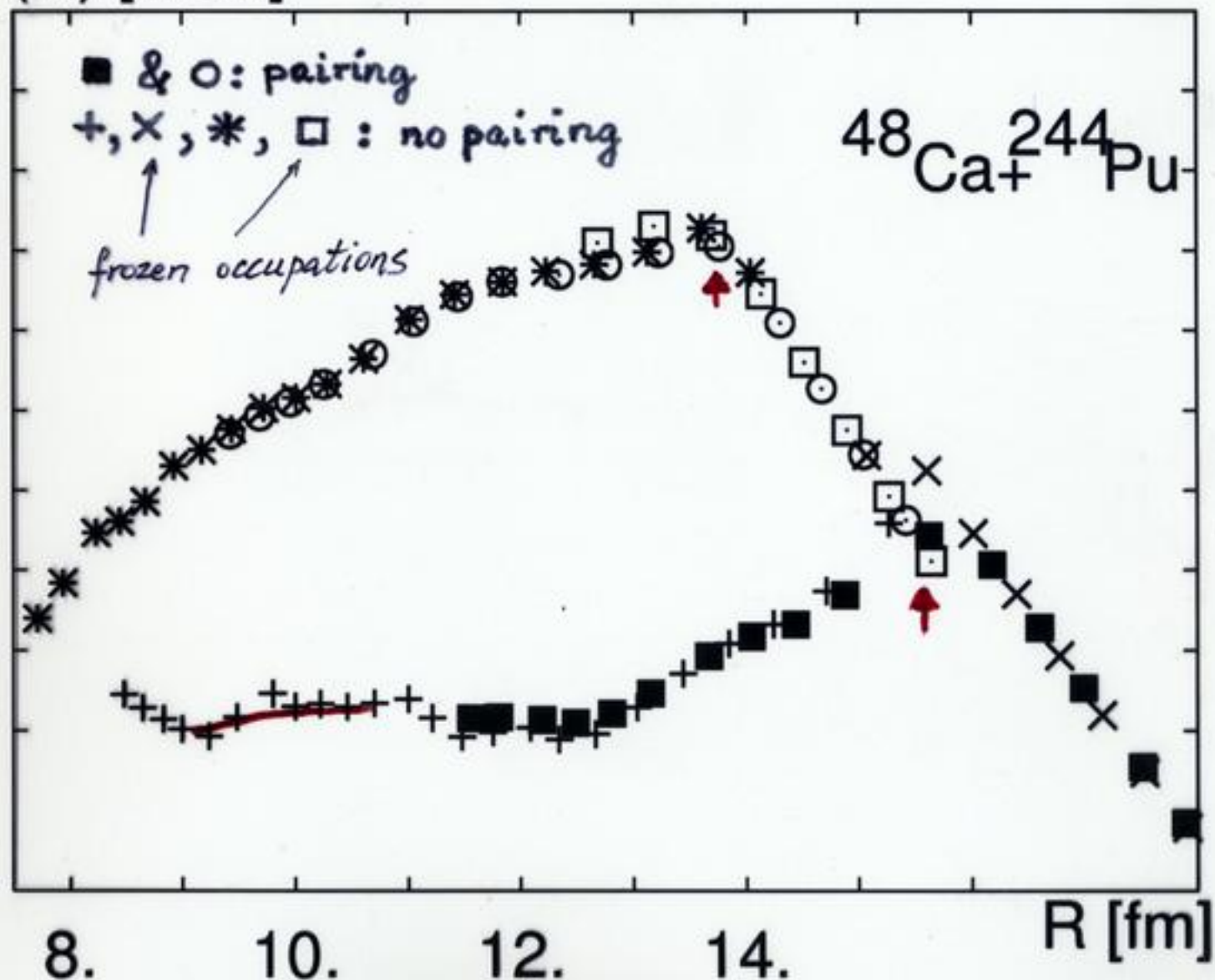
8.

10.

12.

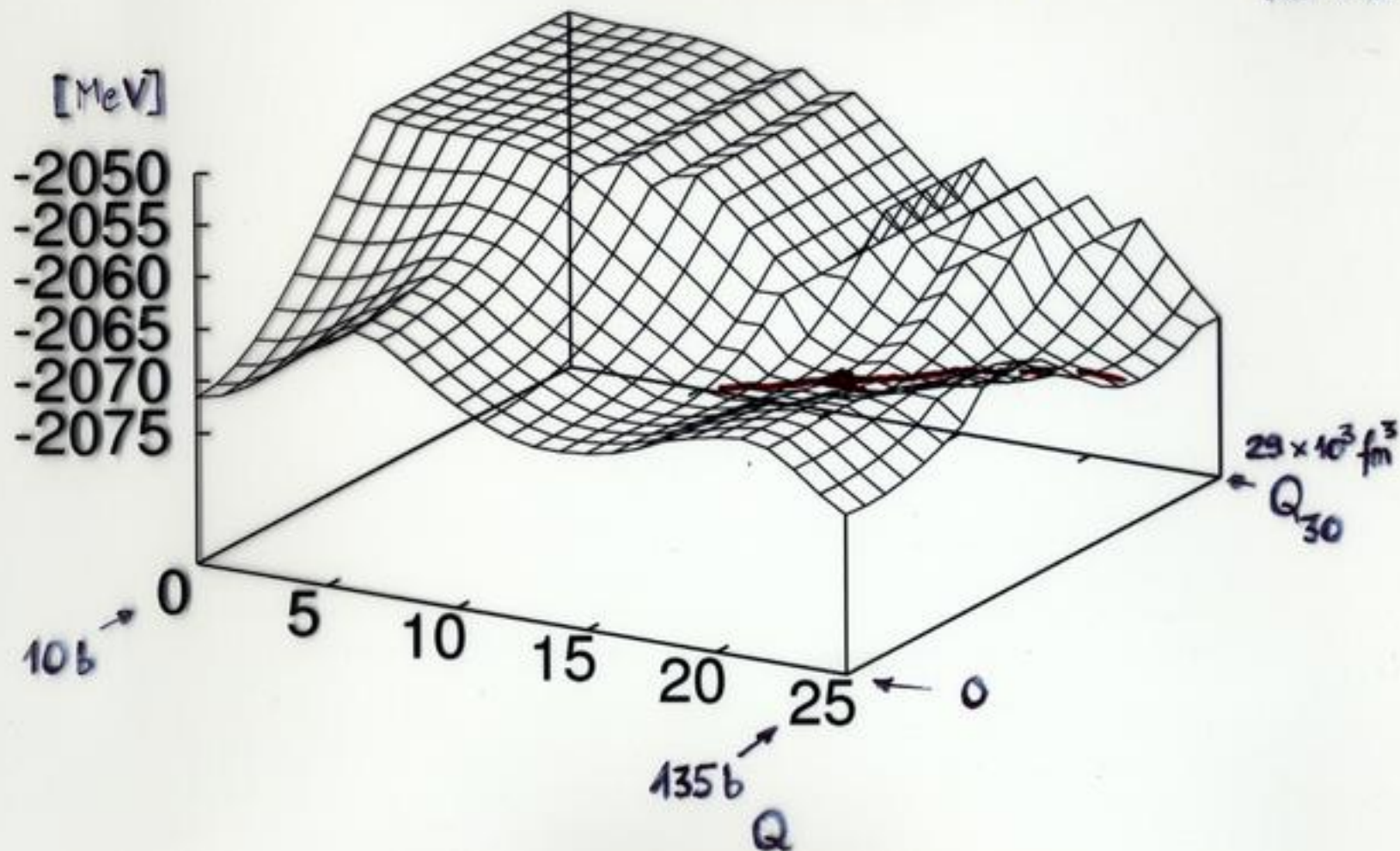
14.

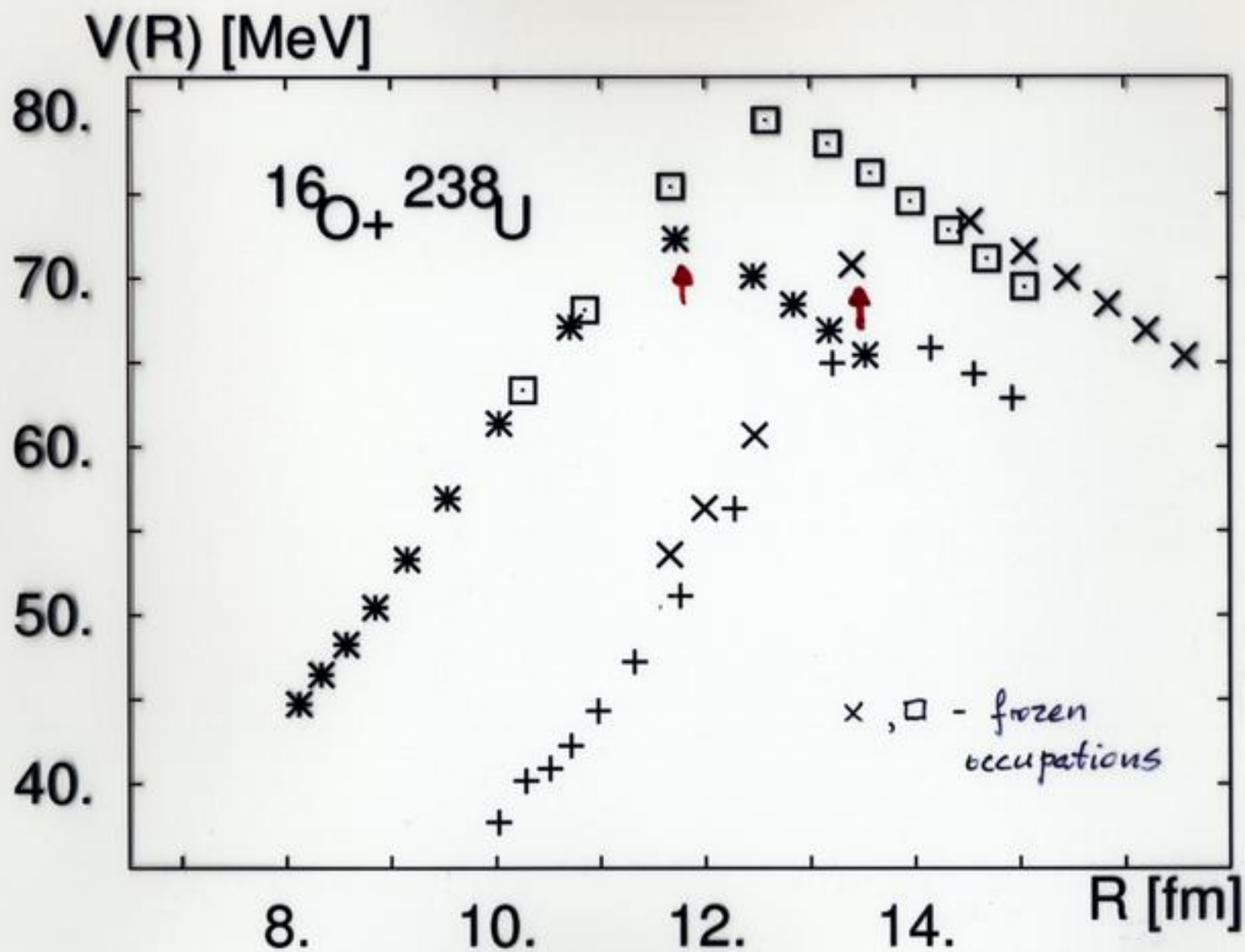
R [fm]



$^{292}_{114}$

$$B_{\text{fis}} = 9.1 \left(\rightarrow 25 \right) \text{ NON AX.}$$





System	Q	$Q_{th.err.}$	B_{cal}	B_{thre}	$E_{cm}(ER)$	B_{Bass}^{int}
$^{40}\text{Ca} + ^{40}\text{Ca}$	14.3	3.5	52	50.2 ± 0.2		52.5
$^{64}\text{Ni} + ^{64}\text{Ni}$	48.8		86.5	89.5 ± 0.3		94.5
$^{90}\text{Zr} + ^{40}\text{Ca}$	57.3	5	92	92.7 ± 0.6		97.7
$^{96}\text{Zr} + ^{40}\text{Ca}$	41.1	6	85	87.5 ± 0.3		96.6
$^{90}\text{Zr} + ^{90}\text{Zr}$	157.3	11	173.5	~ 175.85		181.0
$^{110}\text{Pd} + ^{32}\text{S}$	35.4	6	82.5(87.5)	80.4 ± 0.2		88.9
$^{110}\text{Pd} + ^{110}\text{Pd}$	199.7		199(220.5)	-	≥ 228	228.3
$^{182}\text{W} + ^{32}\text{S}$	84.9		123(133.5)	-	≥ 124	134.3
$^{154}\text{Sm} + ^{60}\text{Ni}$	147.6		166.5(184.5)	-	> 182	191.5
$^{238}\text{U} + ^{16}\text{O}$	38.3	5	73.5(79.5)	~ 71		82.9
$^{132}\text{Sn} + ^{64}\text{Ni}$	111.1	11	147	-	≥ 143	155.7
$^{132}\text{Sn} + ^{132}\text{Sn}$	260.8 *	25	254.5	-	-	257.4
$^{208}\text{Pb} + ^{48}\text{Ca}$	153.8	17	169	169 ± 2^C		176.1
$^{208}\text{Pb} + ^{64}\text{Ni}$	225.1		229	-	235.3-238.2	241.3
$^{208}\text{Pb} + ^{70}\text{Zn}$	244.9 *		240	-	257.2-259.1	256.3
$^{208}\text{Pb} + ^{82}\text{Ge}$	262.5 *		260.5	-	-	268.8
$^{238}\text{U} + ^{48}\text{Ca}$	160.8 *		167.5(188)	182 ± 2^C	192.2	193.8
$^{244}\text{Pu} + ^{48}\text{Ca}$	163.0 *	13	173(191.5)	-	194.5-202	197.3
$^{248}\text{Cm} + ^{48}\text{Ca}$	169.3 *		179.5(195.5)	-	199.7-205.1	201.0
$^{250}\text{Cf} + ^{48}\text{Ca}$	177.0 *		184(200.5)	-	-	205.1

B_{thre} : Phys. Rev. C 64, 024611 (2001)
 K. Siwek Wilczyńska & J. Wilczyński ; C - capture data

Conclusions

1. B^{fusion} calculated seem to be better than the Q values and masses; probable error cancellation.
2. $V(R)$ suggest fusion hindrance in tip collisions for heavier systems.
3. Energy landscapes provide additional hints for CN formation hindrance.
- ~ 4. Superheavy CN formation easier on deformed targets (projectiles).

Conclusions (general)

1. Barriers are important data for DFT
2. There are still problems with proper calculation of barriers.
3. Medium - heavy nuclei important (macroscopic effect)
4. Possible new terms pertaining to barriers:

$$-(\nabla \rho)^2 \tau \quad \xrightarrow{\text{to make it safe}} \quad \frac{M}{1 + C(\nabla \rho)^2} \tau$$

↓
surface peak
of the effective mass