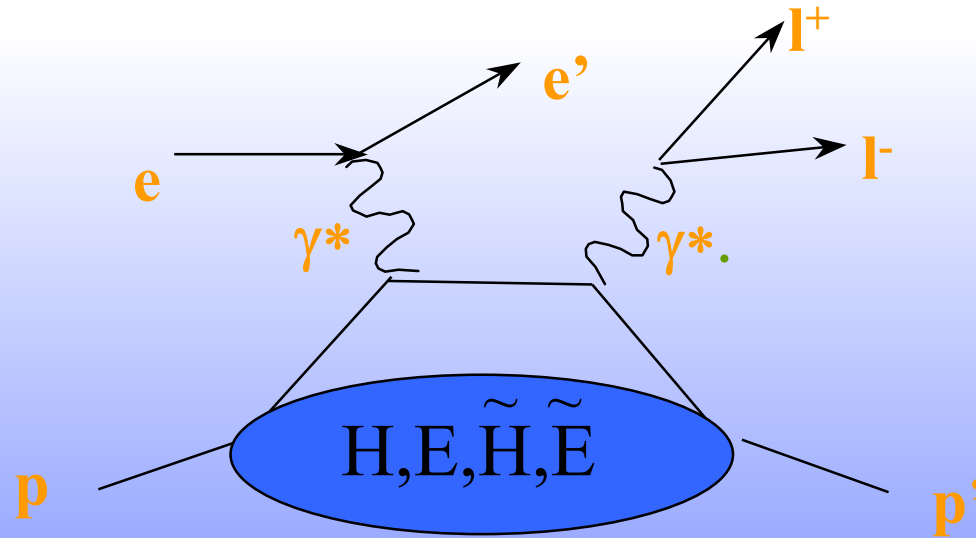


1/ DDVCS

(+ 2/ first study on the (x,t) correlations of the GPDs)



Seattle, 10/07/03
M. Guidal, IPN Orsay



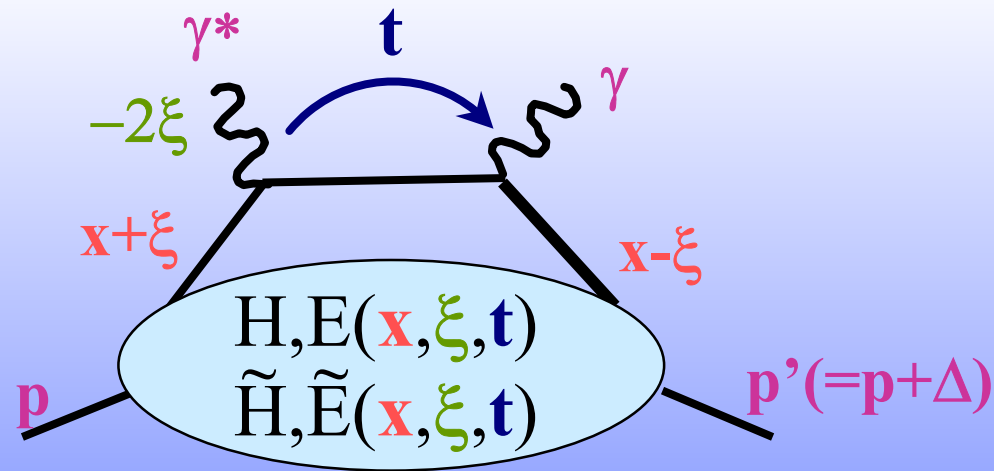
1/ DDVCS

(Double Deeply Virtual Compton Scattering)

**Direct access to GPDS
(no deconvolution)**

The handbag diagram

(Ji, Radyushkin, Mueller,...)



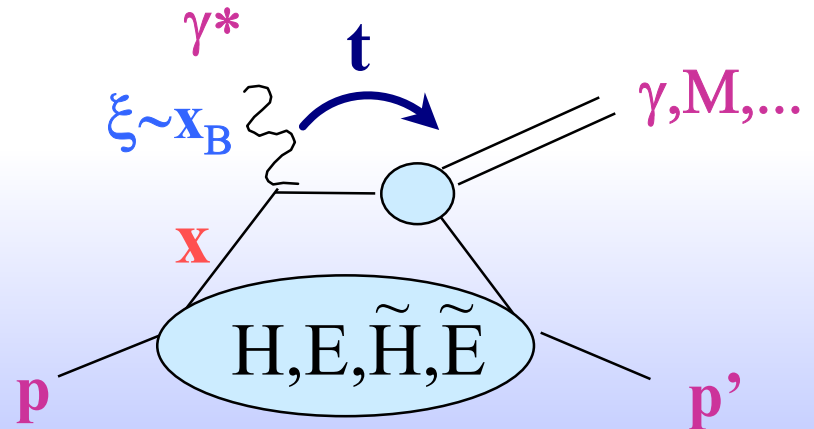
$$\Rightarrow \left\{ \gamma^- [\mathbf{H}^q(\mathbf{x}, \xi, t) \bar{N}(p') \gamma^+ N(p) + \mathbf{E}^q(\mathbf{x}, \xi, t) \bar{N}(p') i\sigma^{+\kappa} \frac{\underline{\Delta}_\kappa}{2M} N(p)] \right. \\ \left. + \gamma^5 \gamma^- [\tilde{\mathbf{H}}^q(\mathbf{x}, \xi, t) \bar{N}(p') \gamma^+ \gamma^5 N(p) + \tilde{\mathbf{E}}^q(\mathbf{x}, \xi, t) \bar{N}(p') \gamma^5 \frac{\underline{\Delta}^+}{2M} N(p)] \right\}$$

$H^q(\mathbf{x}, \xi, t, Q^2)$ but only ξ , t and Q^2 accessible experimentally

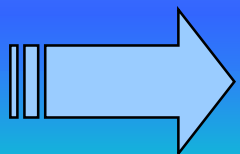
$$\xi = \frac{x_B/2}{1 - x_B/2} \quad t = (p - p')^2$$

$$Q^2 = -(e - e')^2$$

$$\mathbf{x} \neq x_B !$$



$$\frac{d\sigma}{dQ^2 dx_B dt} \sim \left| A \int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t, Q^2)}{\mathbf{x} - \xi + i\epsilon} d\mathbf{x} + B \int_{-1}^1 \frac{E^q(\mathbf{x}, \xi, t, Q^2)}{\mathbf{x} - \xi + i\epsilon} d\mathbf{x} + \dots \right|^2$$



$\mathbf{x}$: mute variable

Deconvolution needed !

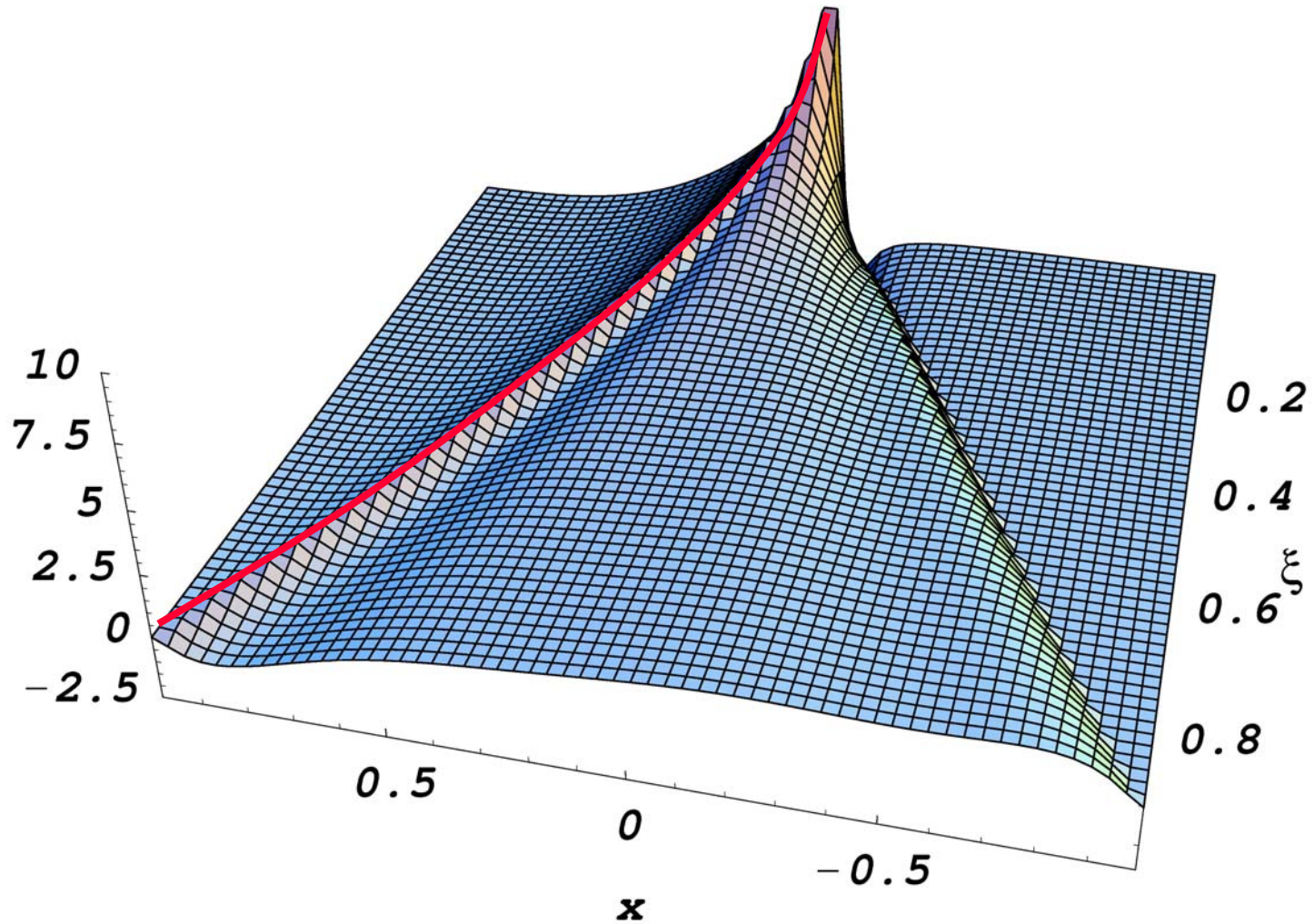
$H^q(\mathbf{x}, \xi, t)$ is *real* but amplitude is *complex*

$$\int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t)}{\mathbf{x} - \xi + i\varepsilon} d\mathbf{x} \quad \Rightarrow \quad \text{Differential cross section}$$

$$= \int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t)}{\mathbf{x} - \xi} d\mathbf{x} \quad \Rightarrow \quad \text{Real part} \\ \text{(charge asymmetry)}$$

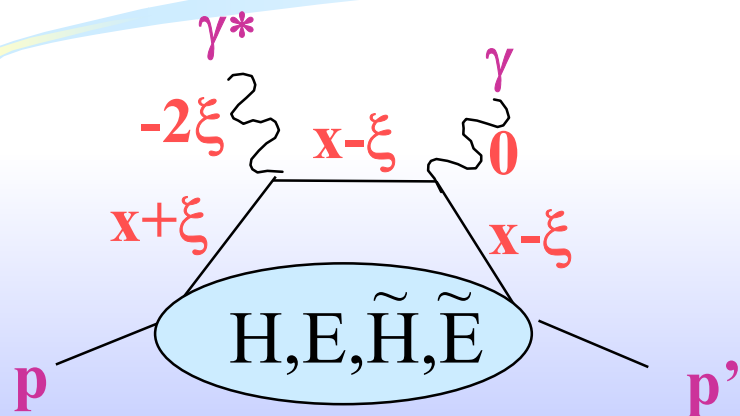
$$- i \pi \underbrace{\delta(\mathbf{x} - \xi) H^q(\mathbf{x}, \xi, t)}_{H^q(\xi, \xi, t)} d\mathbf{x} \quad \Rightarrow \quad \text{Imaginary part} \\ \text{(spin asymmetries)}$$

$$H^u(x, \xi, t=0)$$



(Goeke, Polyakov, Vanderhaeghen)

DVCS

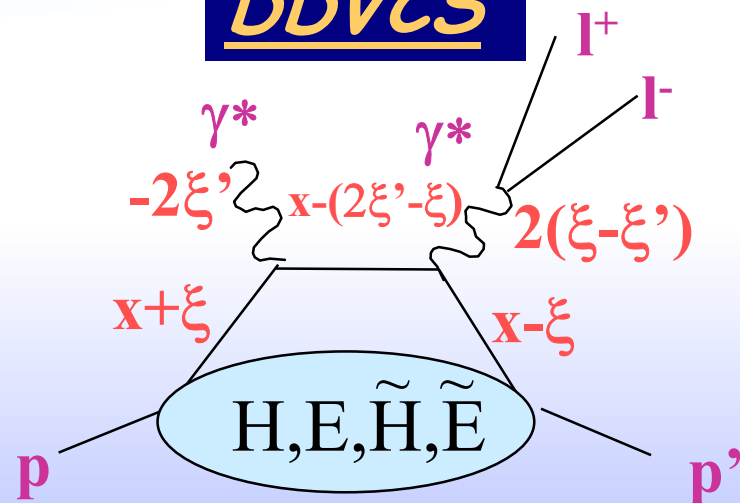


$$\sigma \sim \left| \int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t)}{\mathbf{x} - \xi + i\epsilon} d\mathbf{x} \right|^2$$

$$\text{Im} \sim H^q(\xi, \xi, t)$$

$$\text{Re} \sim \left| \int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t)}{\mathbf{x} - \xi} d\mathbf{x} \right|^2$$

DDVCS



$$\sigma \sim \left| \int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t)}{\mathbf{x} - (2\xi' - \xi) + i\epsilon} d\mathbf{x} \right|^2$$

$$\text{Im} \sim H^q(2\xi' - \xi, \xi, t)$$

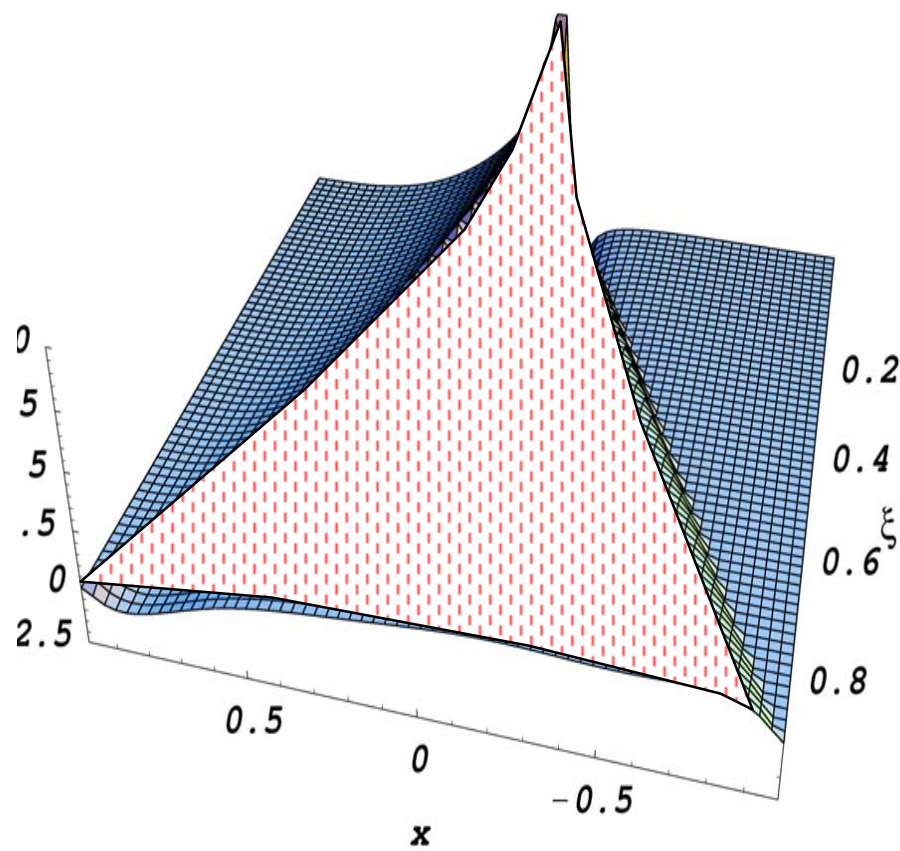
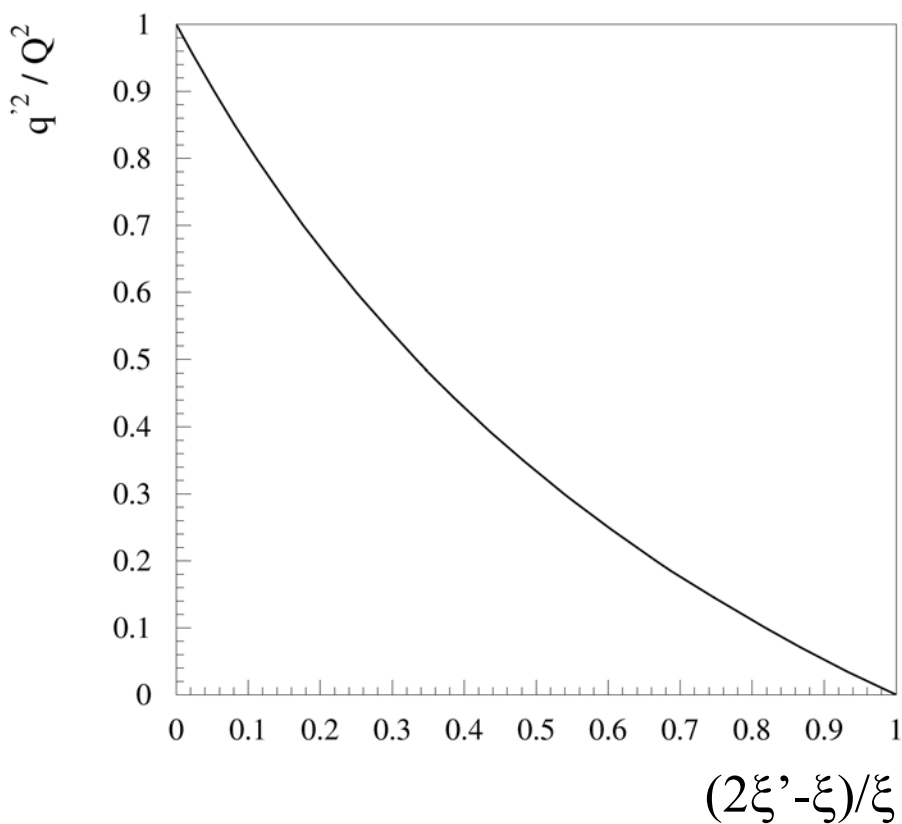
$$\text{Re} \sim \left| \int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t)}{\mathbf{x} - (2\xi' - \xi)} d\mathbf{x} \right|^2$$

$q'^2=0 \text{ GeV}^2$
 $q'^2=Q^2$
 $0 < 2\xi' - \xi < \xi$

Numerical example :

$Q^2=5 \text{ GeV}^2, q'^2=2 \text{ GeV}^2$
 $(2\xi' - \xi) = .43\xi$

SSA in $\gamma^* + p \rightarrow l^+ l^- + p$

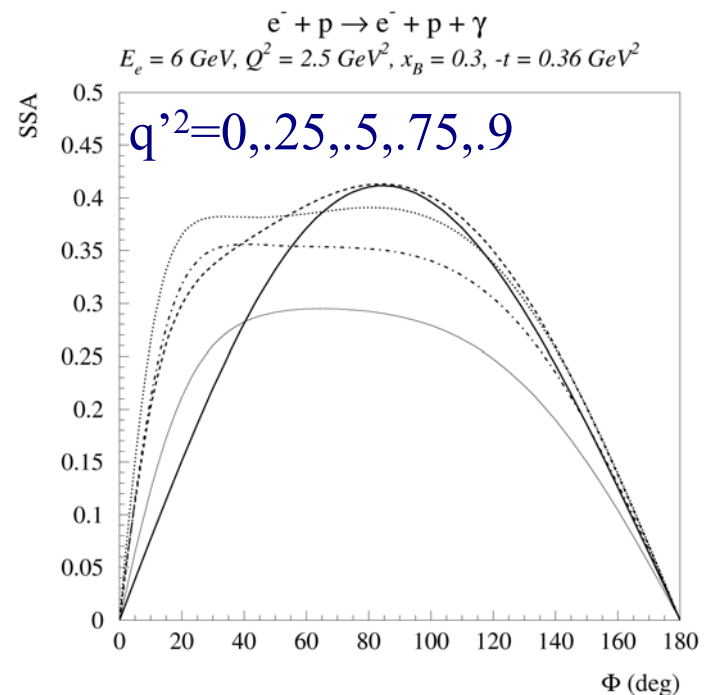
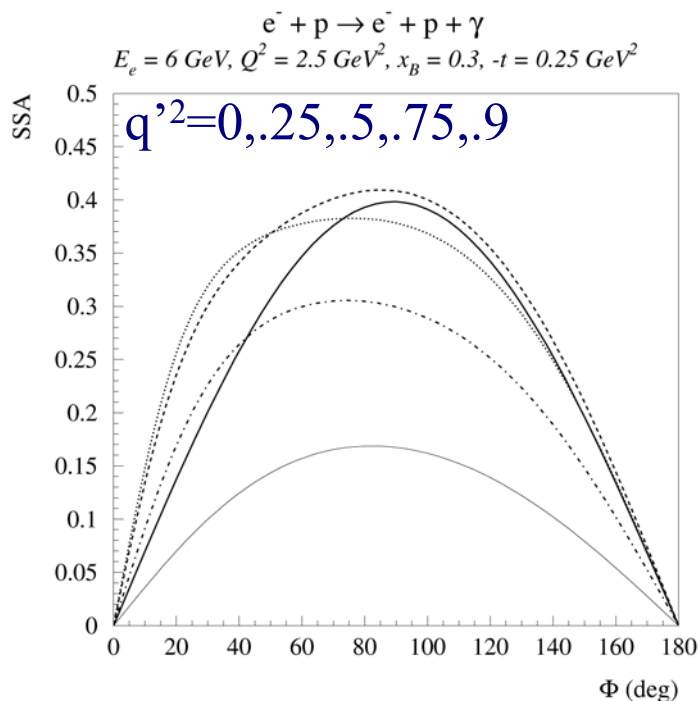
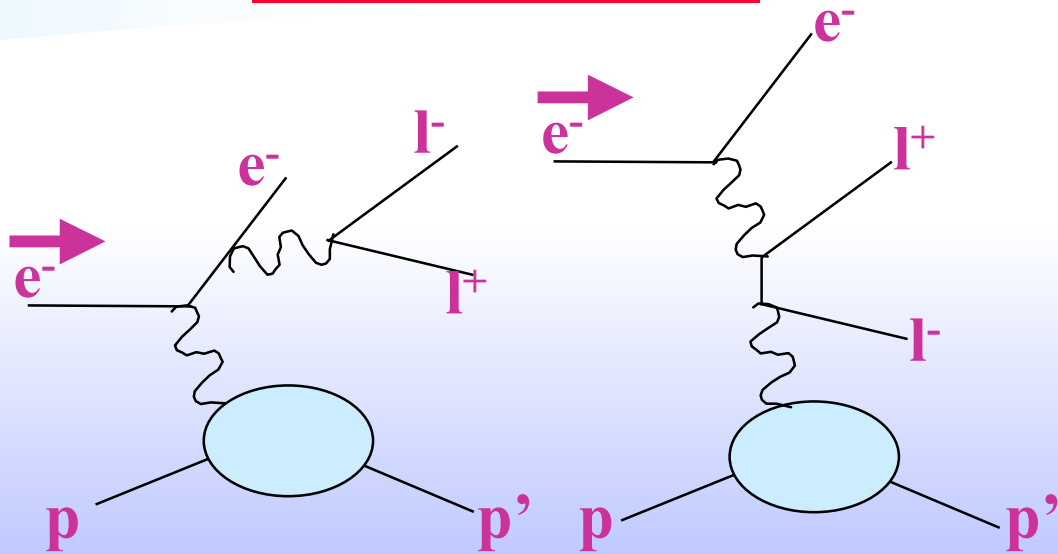
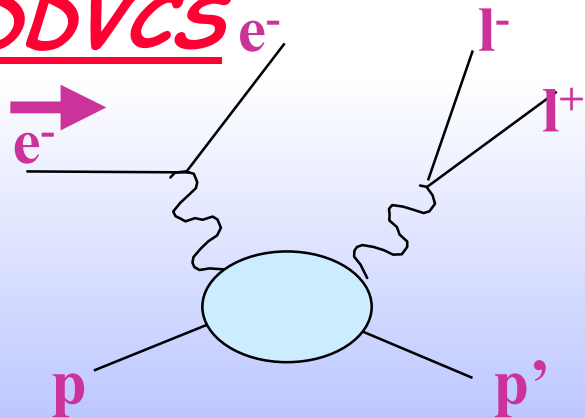


Beam Spin asymmetry for

ep $\Rightarrow$ ep γ^* $\hookrightarrow$ l+l-

Bethe-Heitler

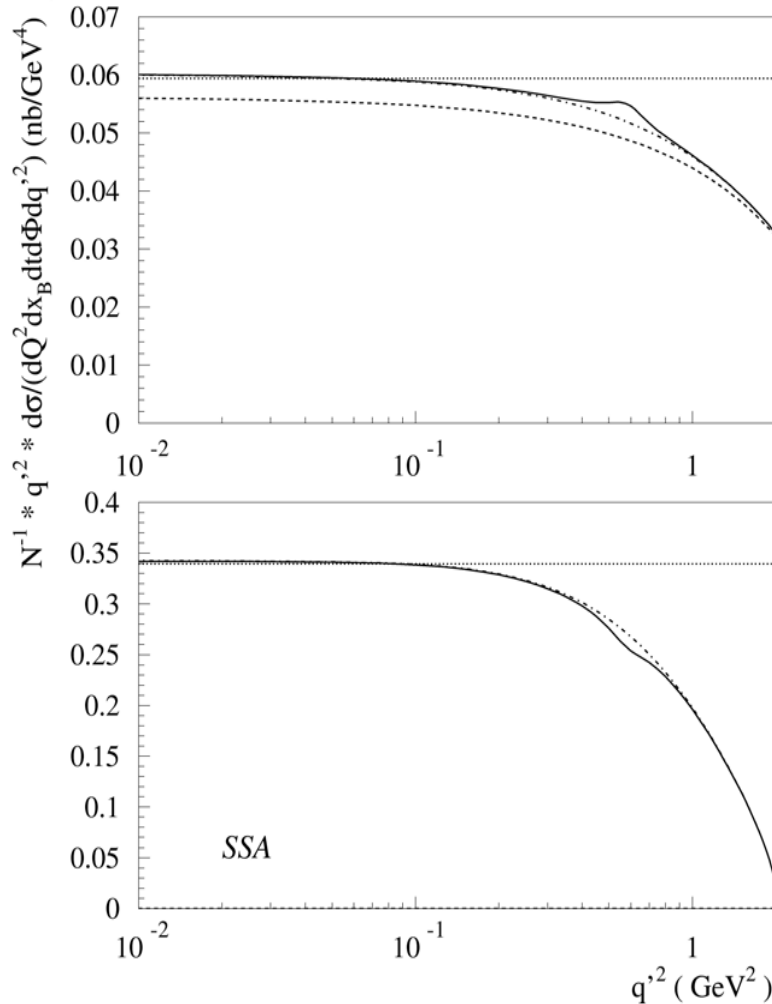
DDVCS



ρ influence

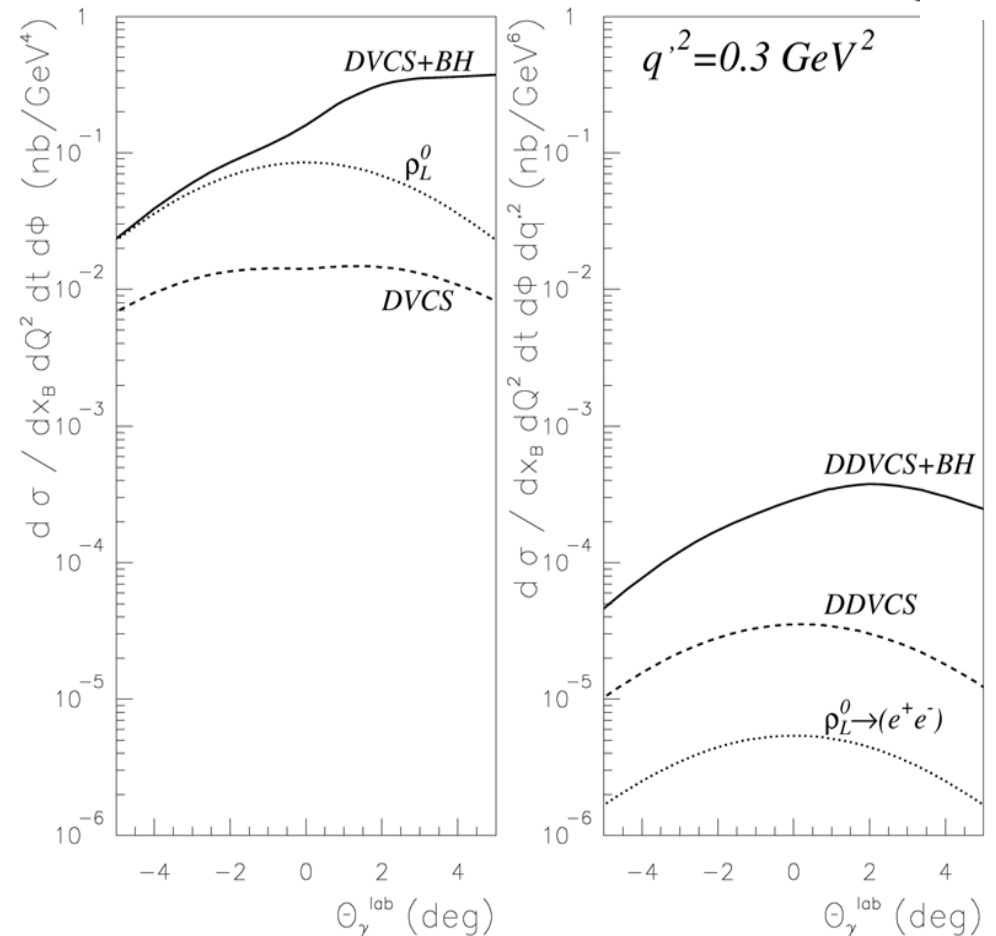
ep $\Rightarrow$ ep ρ $\hookrightarrow$ l^+l^-

$E_e = 11 \text{ GeV}, Q^2 = 4 \text{ GeV}^2, x_B = 0.25, t = -0.2 \text{ GeV}^2, \Phi = 90^\circ$



$E_e = 6 \text{ GeV}, Q^2 = 2.5 \text{ GeV}^2, x_B = 0.3, \Phi = 0 \text{ deg.}$

$e^- + p \rightarrow e^- + p + \gamma, \rho_L^0$ $e^- + p \rightarrow e^- + p + (\gamma, \rho_L^0)$

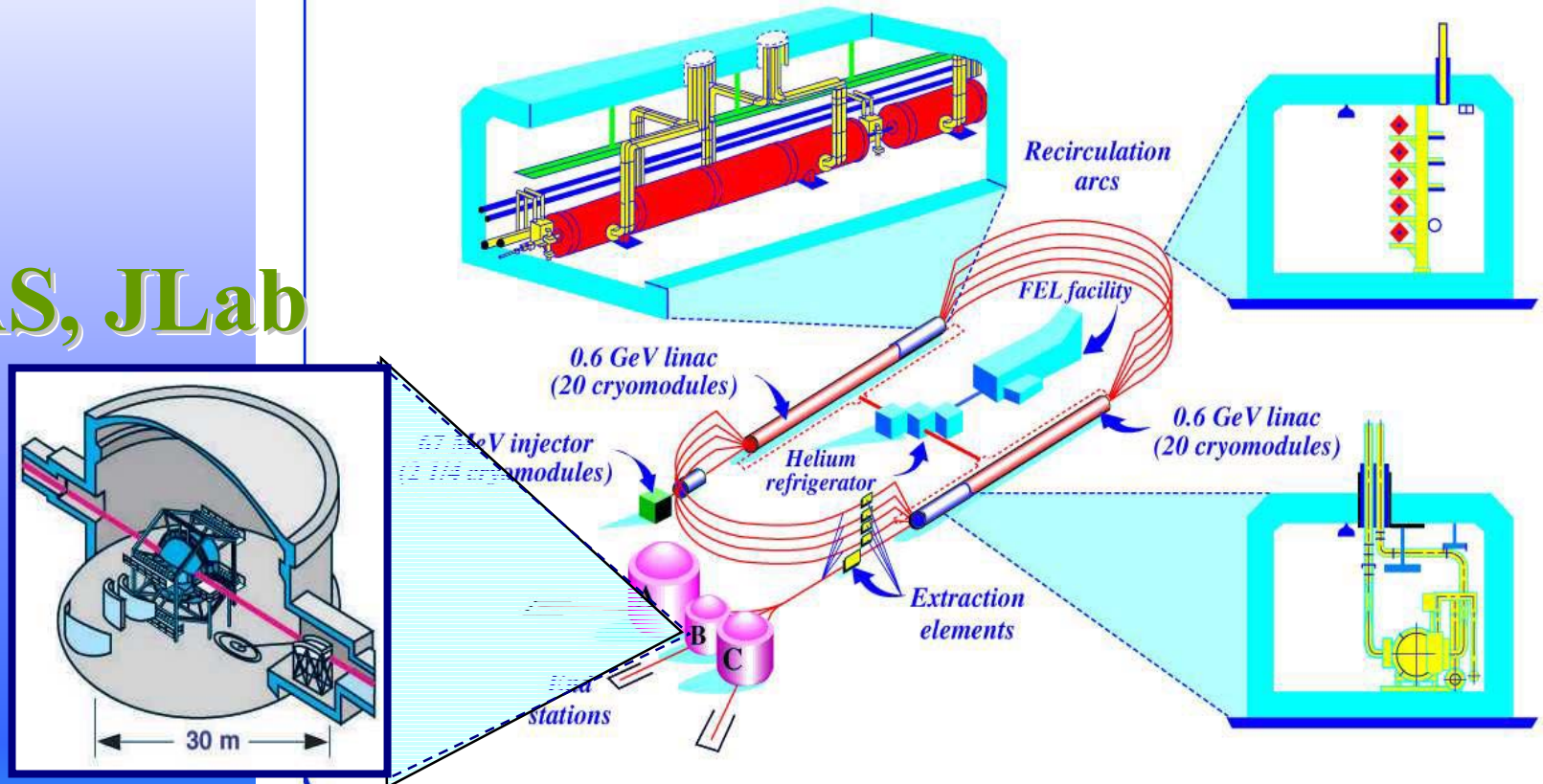


First experimental look

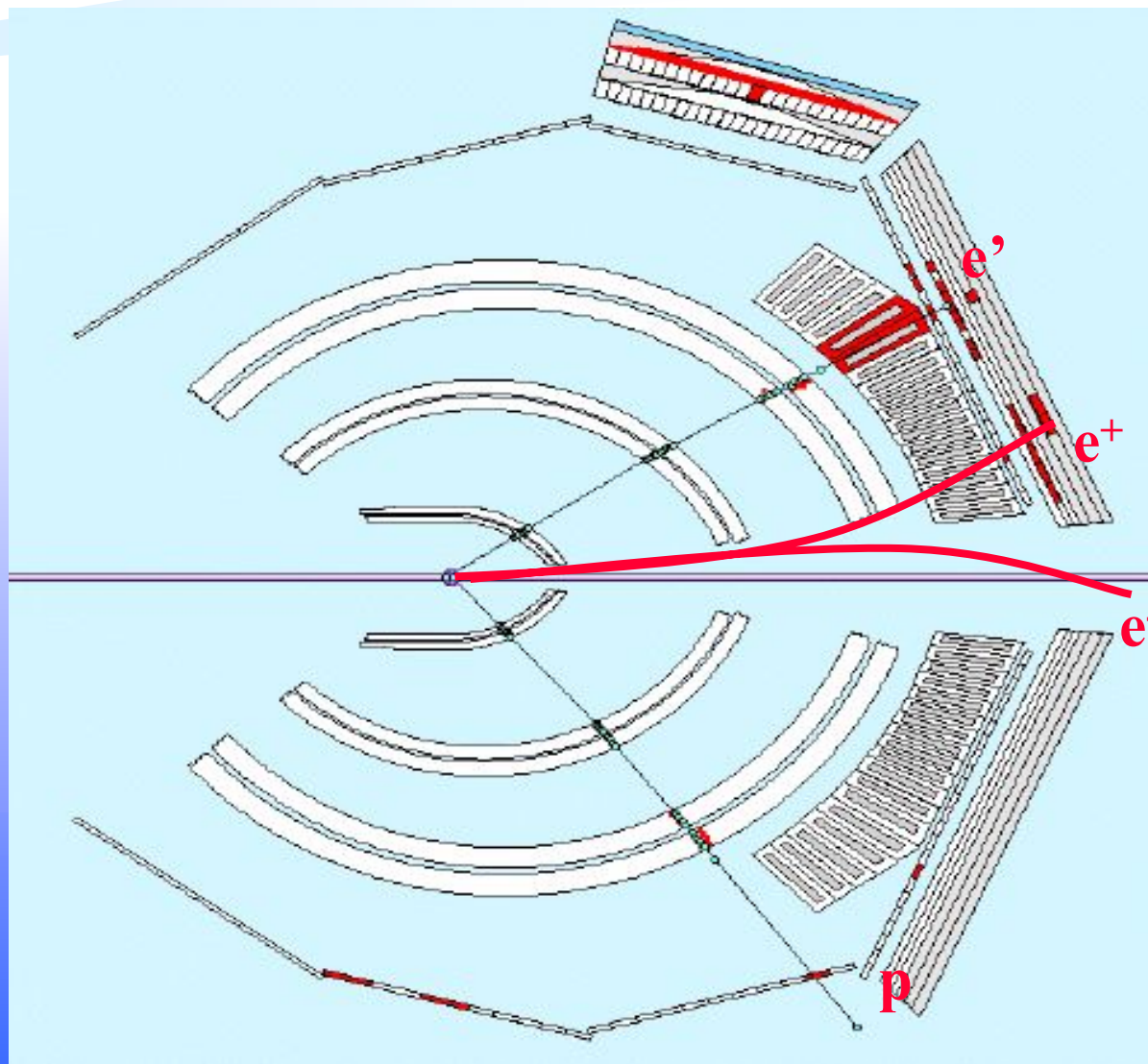
MACHINE CONFIGURATION



CLAS, JLab



Any
DDVCS
event in
CLAS ?

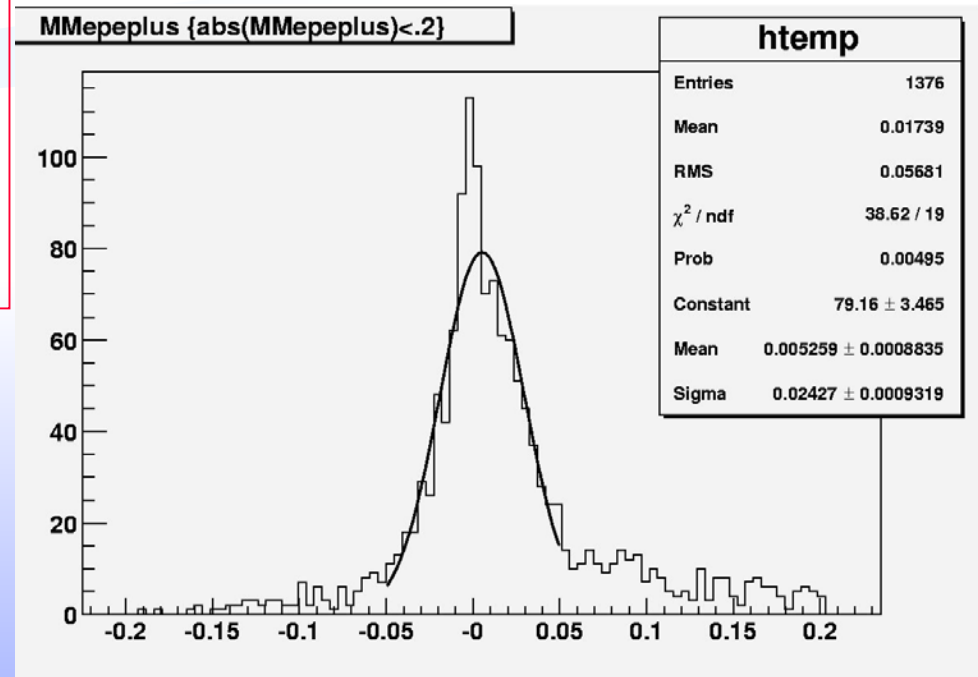


Detect e', e⁺ and p $\Rightarrow$ missing e⁻

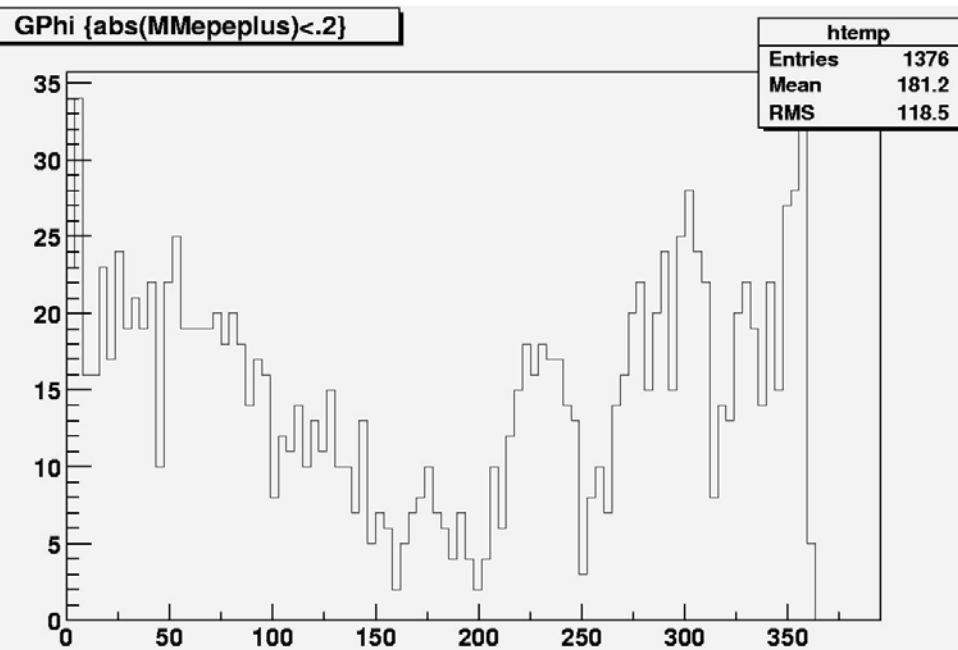
First experimental investigations

CLAS, 30 days beam time,
1/3 statistics, $E_e = 5.75$ GeV

Detect $e'pe^+$ $\Rightarrow$ missing e^-

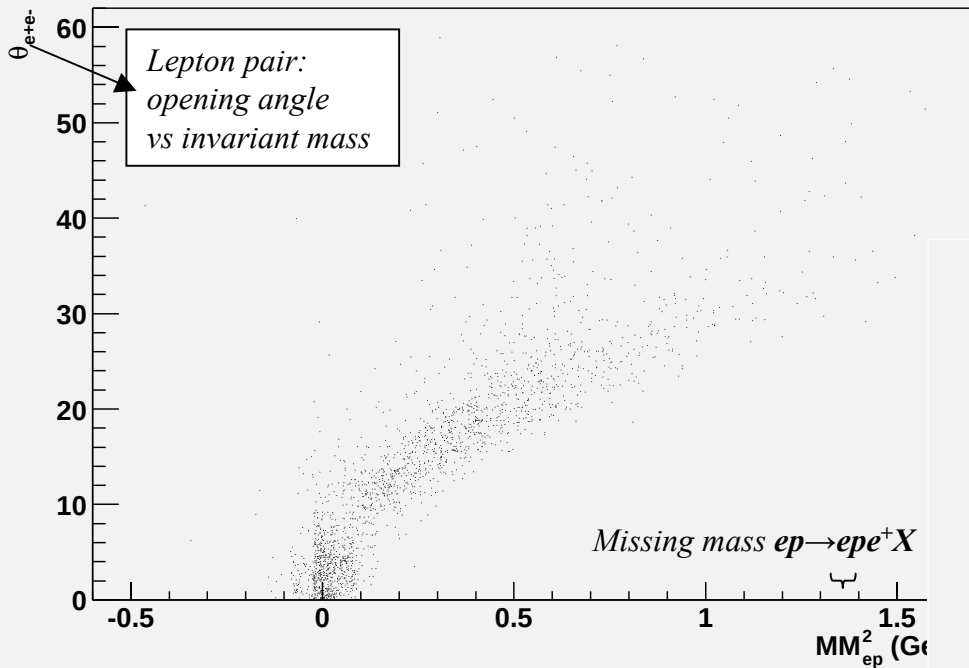


Missing Mass² ($e'pe^+ X$) (GeV²)



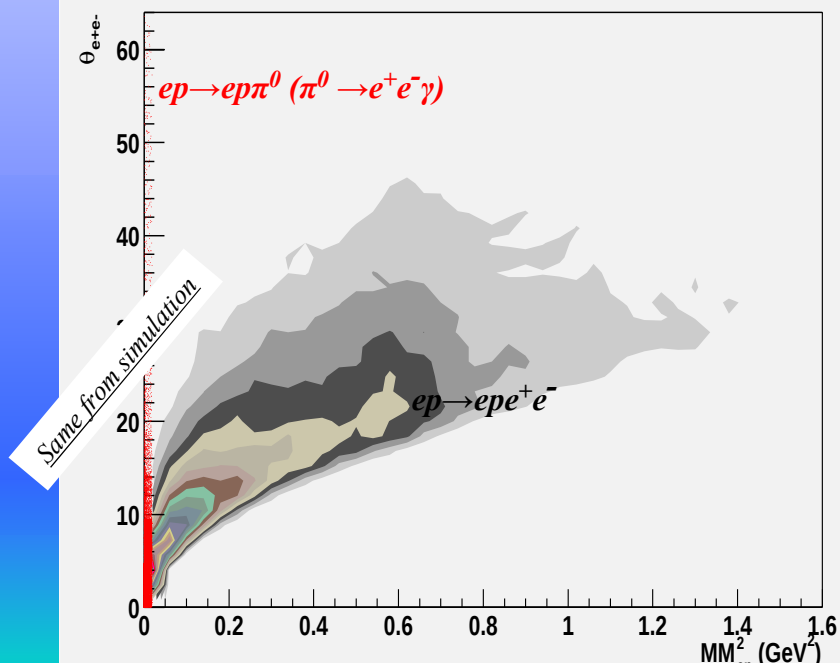
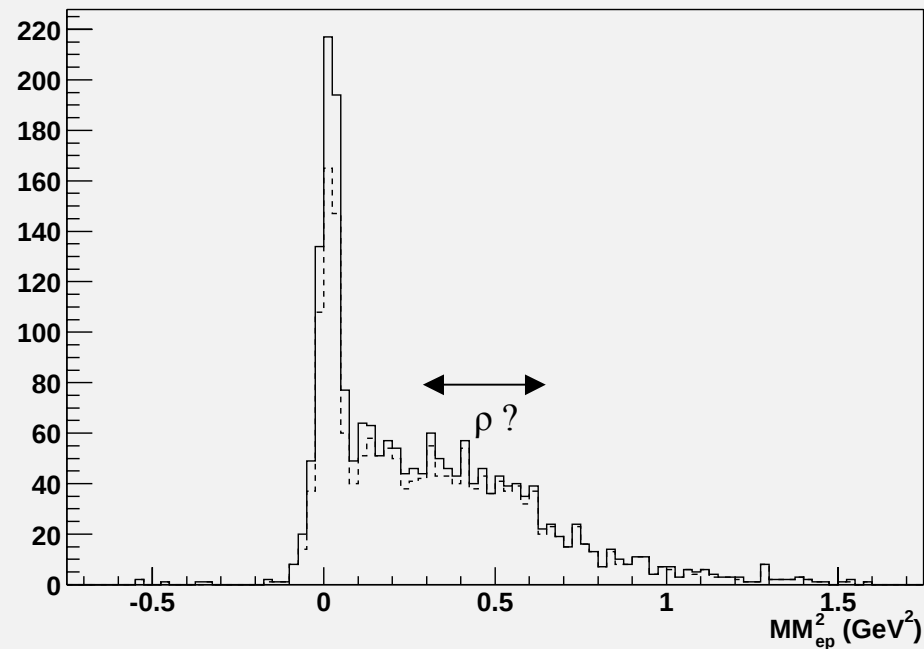
Analysis S. Morrow (Saclay)

Φ distribution



Distributions of counts

(not corrected from acceptance)



(q^2)

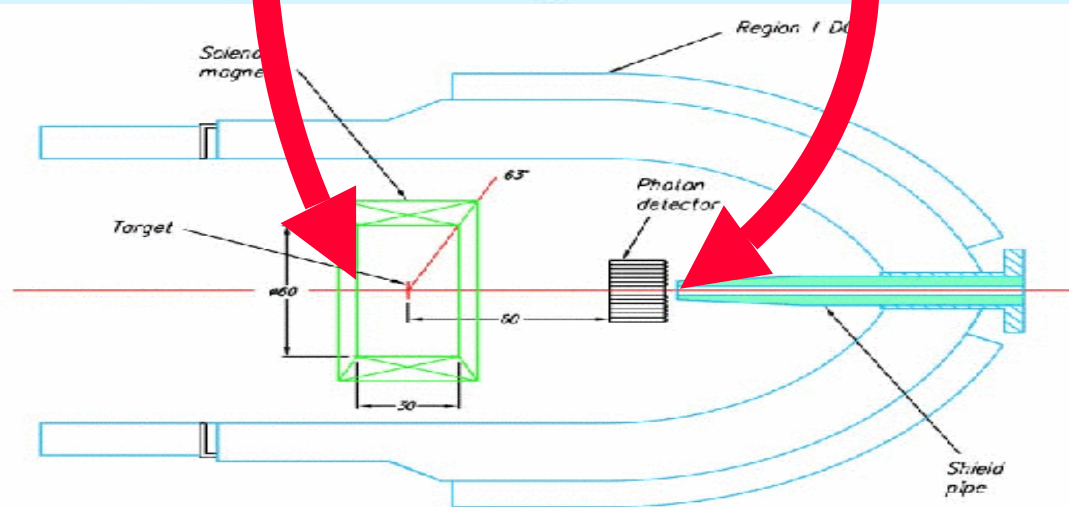
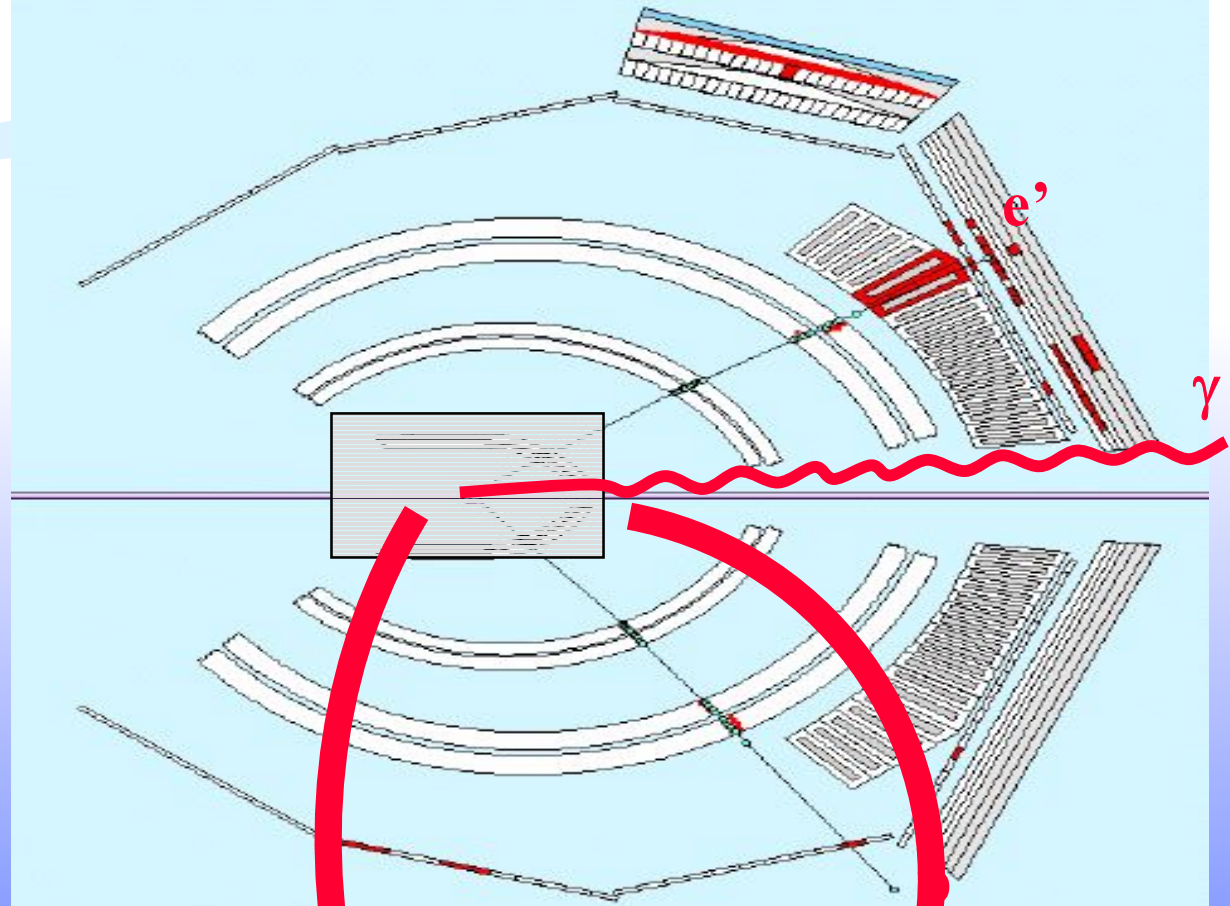
**Next step: extract
beam polarization asymmetry**

**Figures, courtesy of M. Garcon
& S. Morrow (Saclay)**

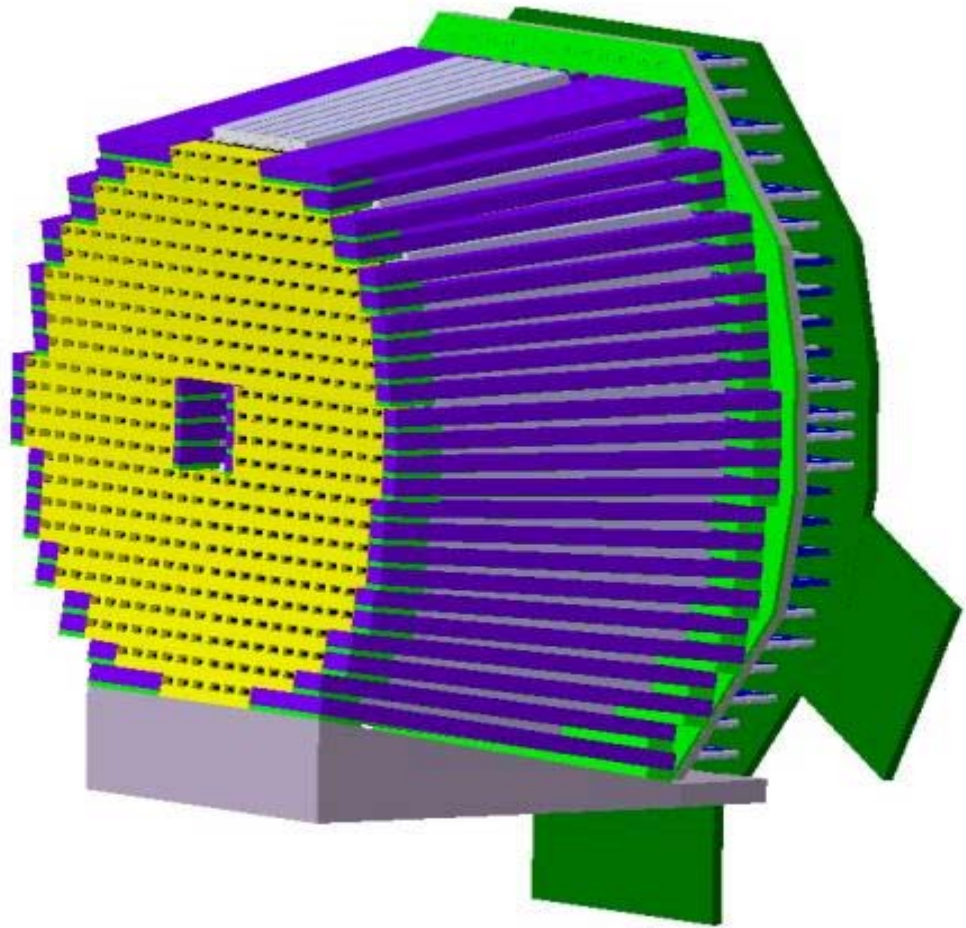
A typical
 $ep \Rightarrow ep\gamma$
event in
CLAS

Add EM
calorimeter
at forward
angles

Add solenoid
Moller shield
around target



**JLab/ITEP/
Orsay/Saclay/
UVA
collaboration**



ROSIE



Dynamical range : $50 \text{ MeV} < E_\gamma < 5 \text{ GeV}$ ($\sigma \sim 5\%/\sqrt{E_\gamma}$)

Counting rates $\sim 1 \text{ MHz}$

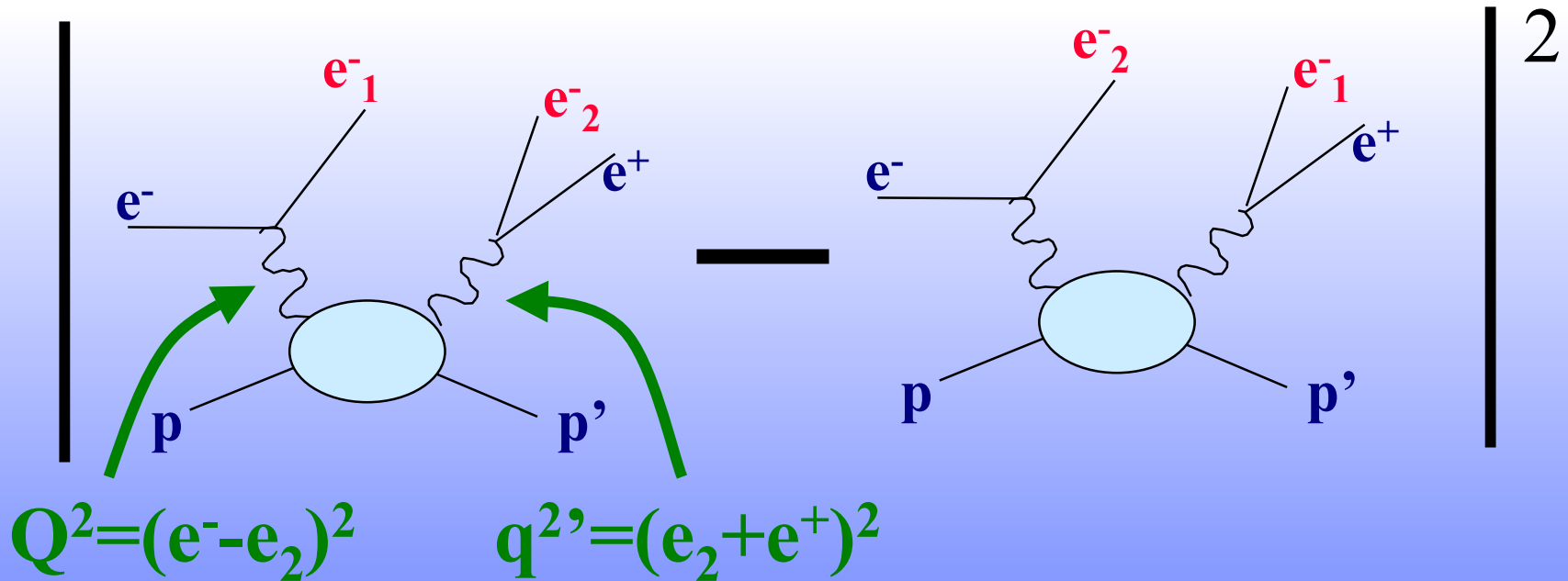
Magnetic field environment : $B \sim 1 \text{ T}$



$\sim 400 \text{ PbWO}_4$ crystals : $\sim 10 \times 10 \text{ mm}^2$, $l = 160 \text{ mm}$ (18λ 's)

Read-out : APDs + preamps

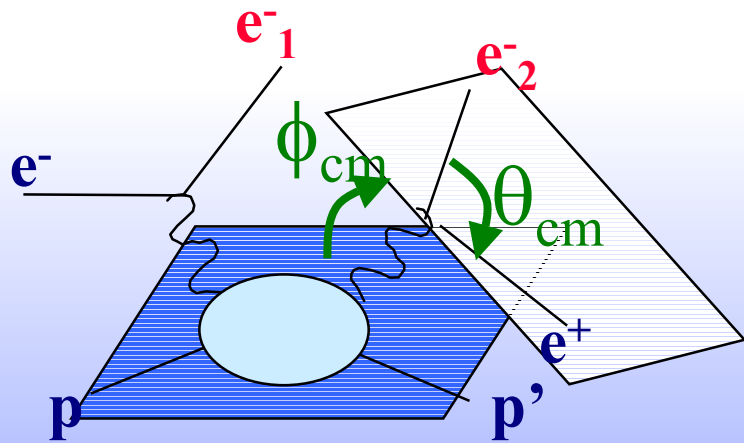
The particular case of e-/e+ pairs



1/ Theoretically, one has to anti-symmetrize

2/ Experimentally, ambiguity on defining Q^2 , $q^{2'}$, ...

A bit of kinematics



2 possibilities :

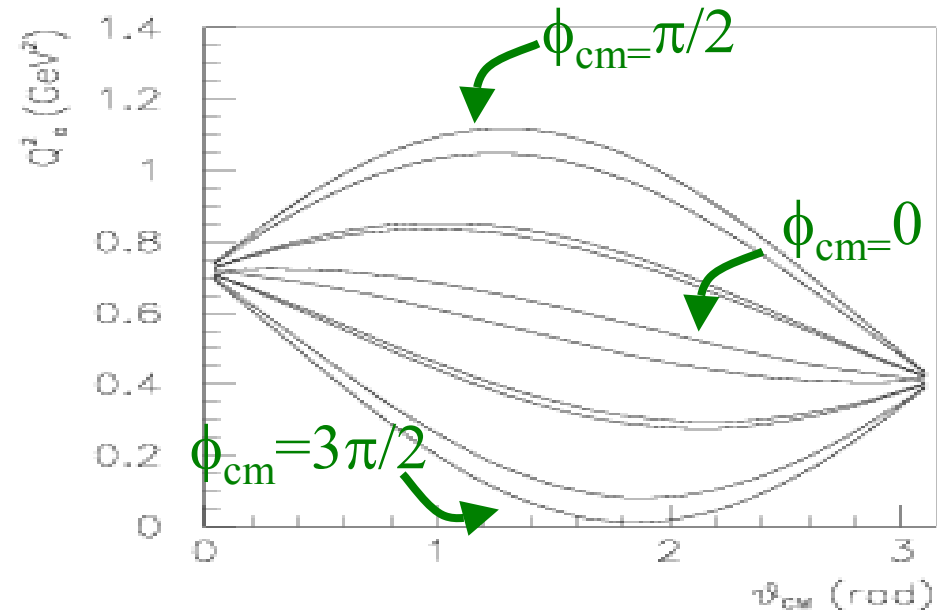
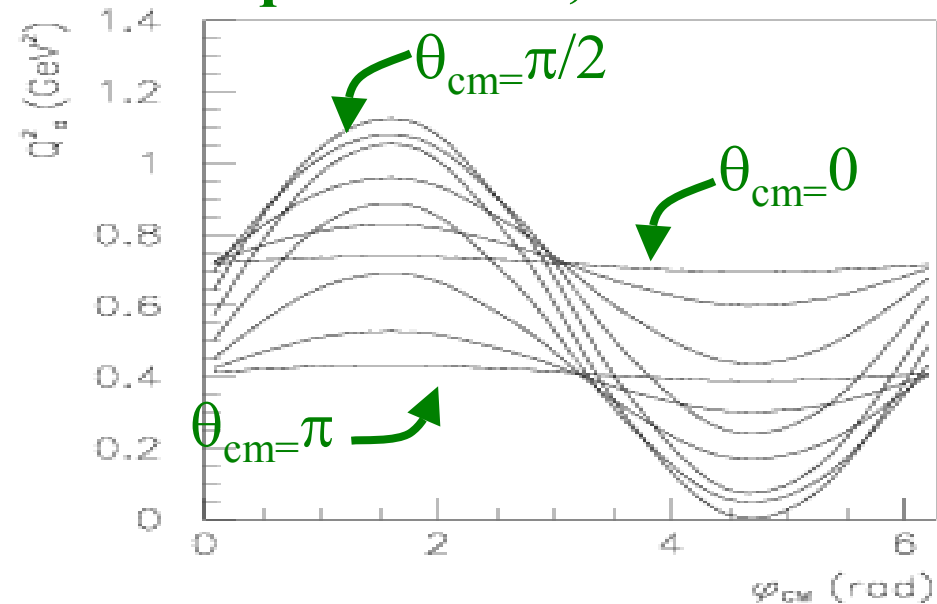
$$Q^2 = (e - e_1)^2$$

$$q'^2 = (e_2 + e^+)^2$$

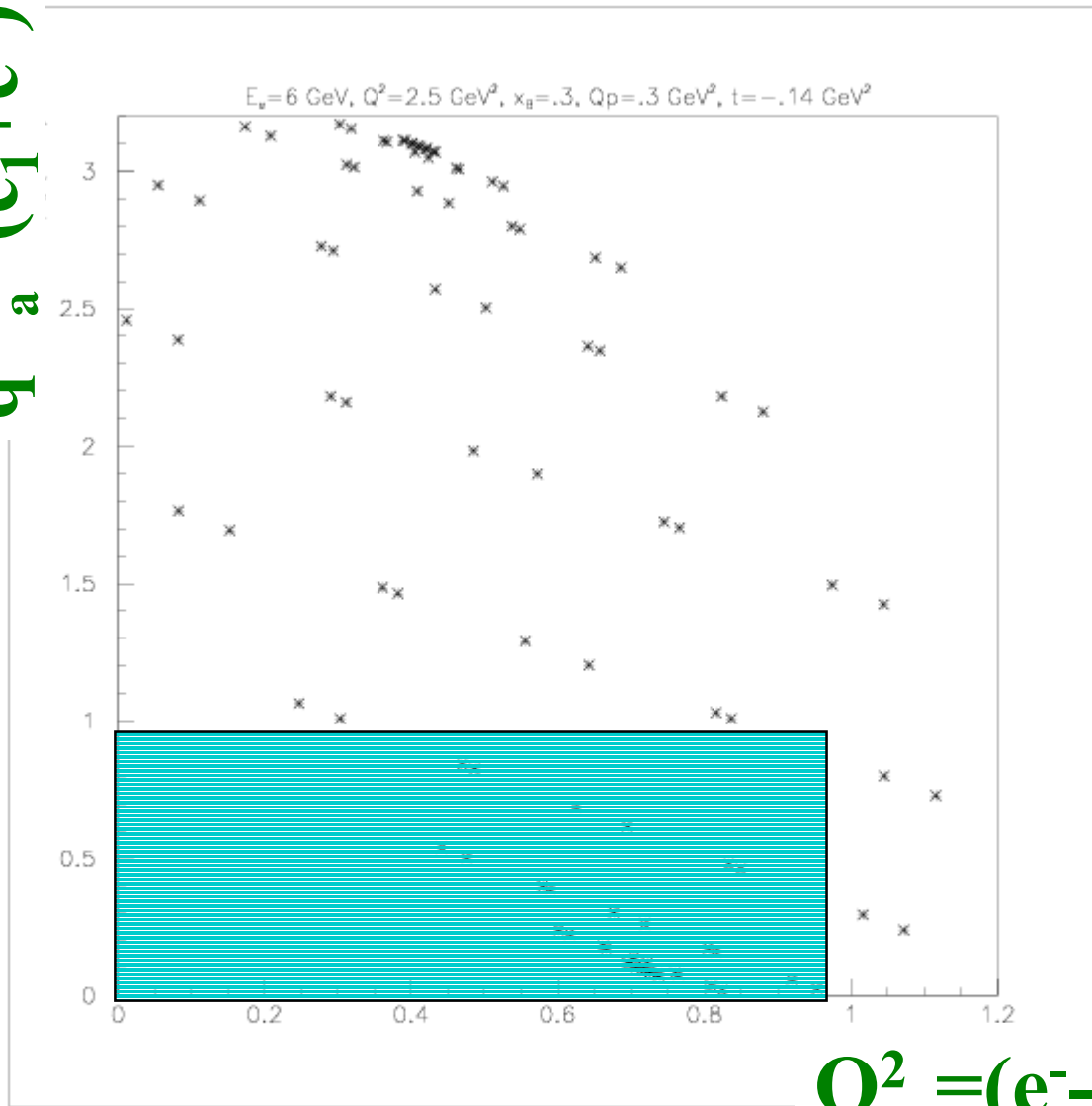
$$Q_a^2 = (e^- - e_1)^2$$

$$q_a'^2 = (e_1 + e^+)^2$$

$$E_e = 6 \text{ GeV}, Q^2 = 2.5 \text{ GeV}^2, q'^2 = .3 \text{ GeV}^2, t = -.14 \text{ GeV}^2$$



$$q_a'^2 = (e_1 + e^+)^2$$



At least, one virtuality $> 1 \text{ GeV}^2$



2/ Study on the (x,t) correlation of the GPDs

(in coll. with M. VdH & M. Polyakov)

Link between GPDs & FFs

$$F_1^q = \int_{-1}^1 H^q(x, \xi, t) dx$$

$$F_2^q = \int_{-1}^1 E^q(x, \xi, t) dx$$

Low t ($-t < 1 \text{ GeV}^2$) : **Regge** ansatz (Goeke, Poliakov, VdH)

$$F_1^u(t) = \int_0^1 u_v(x) 1/(x^{\alpha'_1 t}) dx \quad F_1^d(t) = \int_0^1 d_v(x) 1/(x^{\alpha'_2 t}) dx$$

$$\mathbf{F}_1^p = e_u F_1^u(t) + e_d F_1^d(t)$$

$$\mathbf{F}_1^n = e_u F_1^d(t) + e_d F_1^u(t)$$

Similarly $F_2^q(t) = \int_0^1 \kappa_v q_v(x) 1/(x^{\alpha'_2 t}) dx$

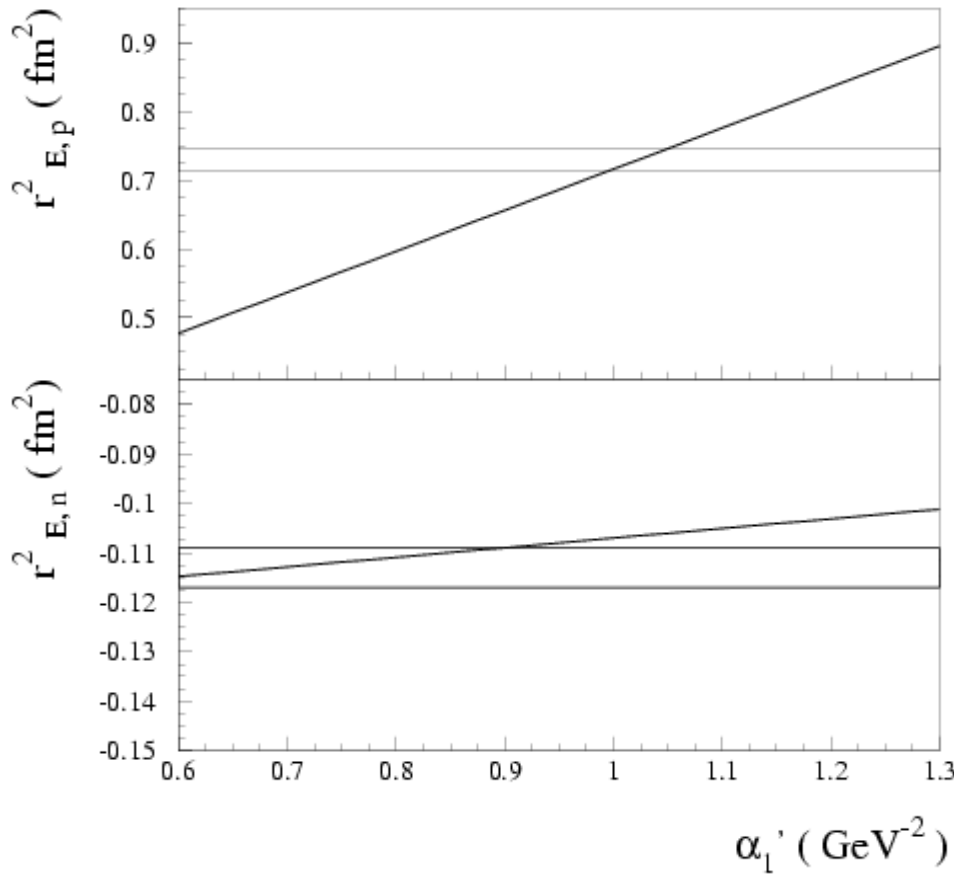
➡ 2 free parameters : α'_1, α'_2 (constrained by Regge)

➡ Fit 4 form factors : $G_{E,M}^{p,n}$

Proton & neutron electric charge radii

$$F_1^u = \int_0^1 u_v(x) 1/(x^{\alpha'_1}) dx \quad \Rightarrow \quad r_{1,p}^2 = -6\alpha'_1 \int_0^1 \ln x (e_u u_v + e_d d_v) dx$$

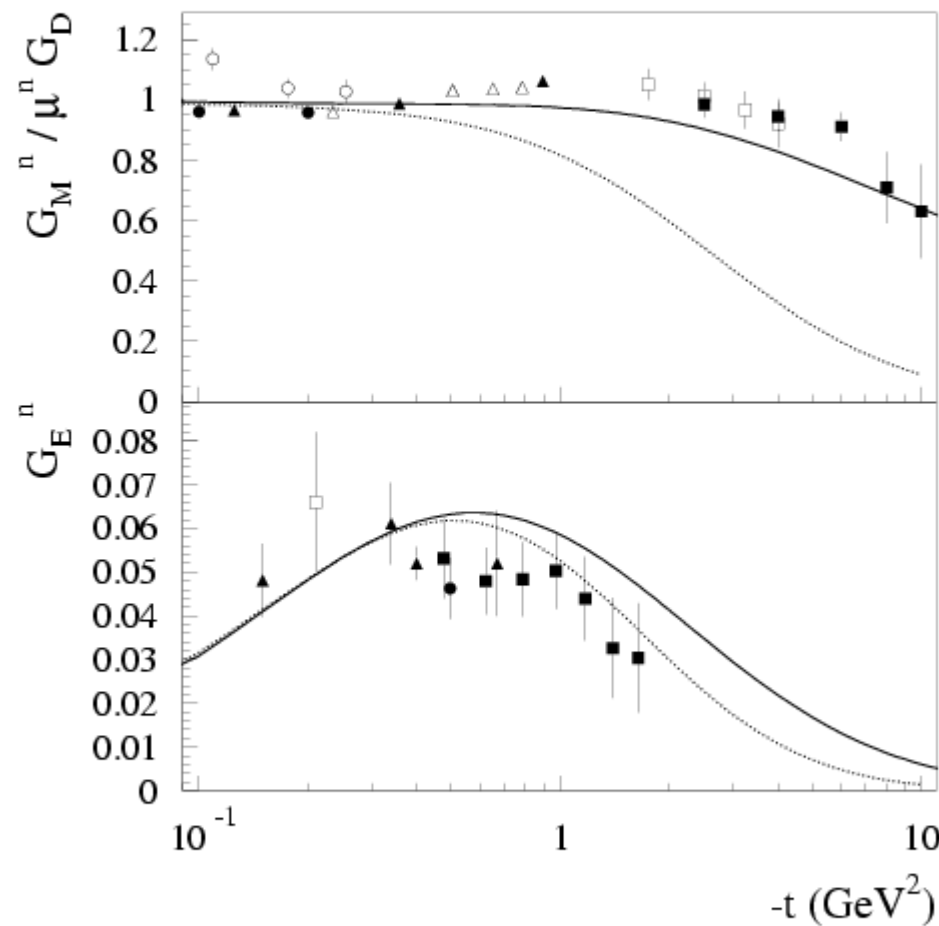
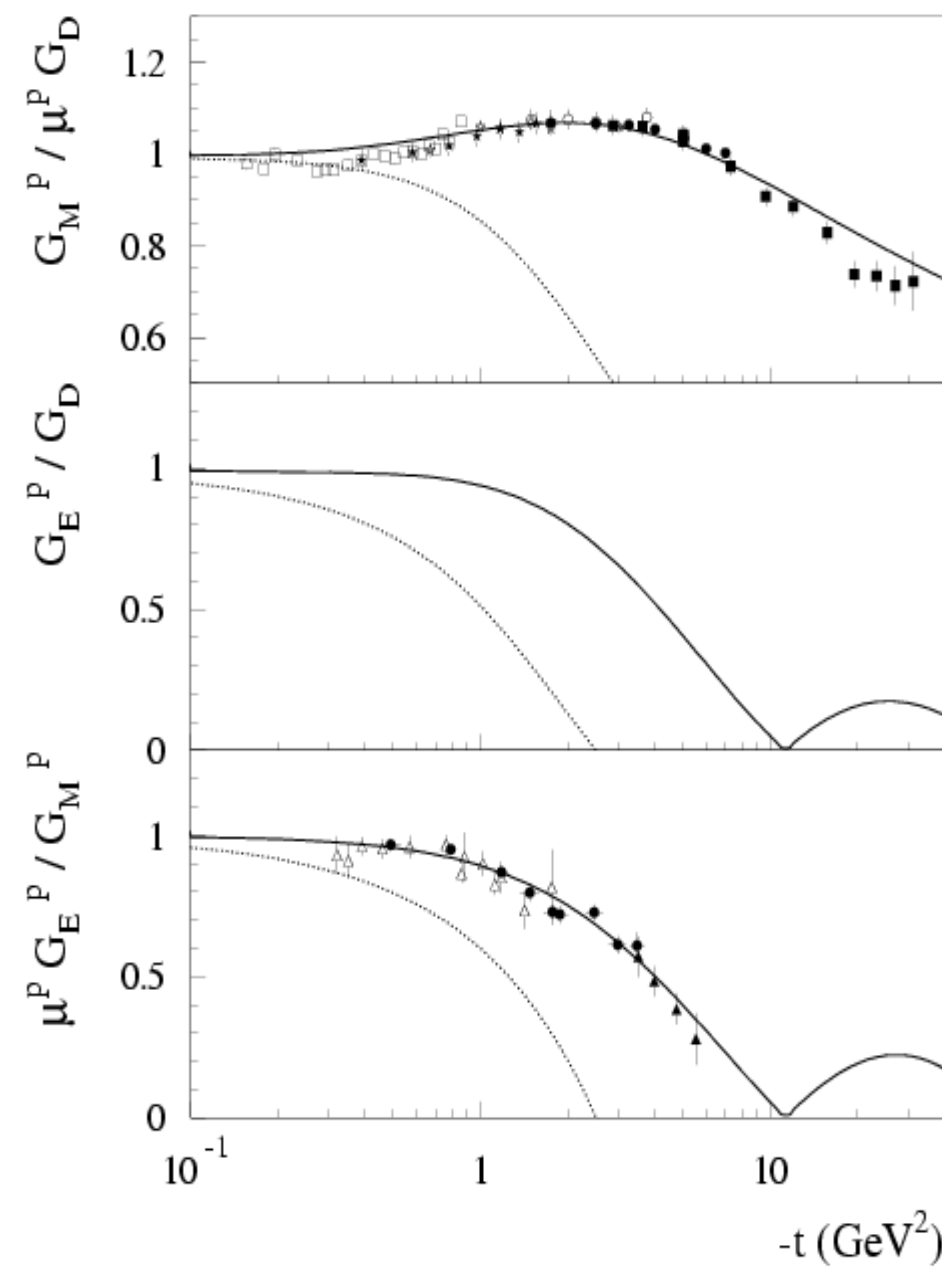
$$r_{E,N}^2 = r_{1,N}^2 + 3/2 \kappa_N / m_N^2$$



$$\Rightarrow \alpha'_1 \sim 1 \text{ GeV}^{-2}$$

PROTON electric and magnetic form factors

NEUTRON electric and magnetic form factors



Extending the t domain

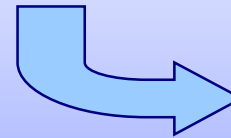
pQCD : $F_1(t) \sim 1/t^2$ at large t $(F_2 \sim 1/t^3)$

1/ Introduce non-linear Regge trajectories :

$$\alpha(t) = \alpha(0) + \alpha' 2T [1 - \sqrt{1 - t/T}]$$

(Brisudova, Burakovsky, Goldman)

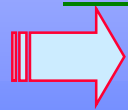
T : (free) non-linearity parameter



$$F_1(t) \sim 1/t^2$$

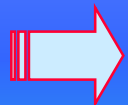
2/ a/ x-dependence of Eq is not constrained

b/ Large t power behavior is fixed by large x behavior



Large x behavior of E should be different from H

$$F_2^q(t) = \int_0^1 \kappa_v (1-x)^{\eta^q} q_v(x) / (x^{-\alpha'_2 t}) dx$$

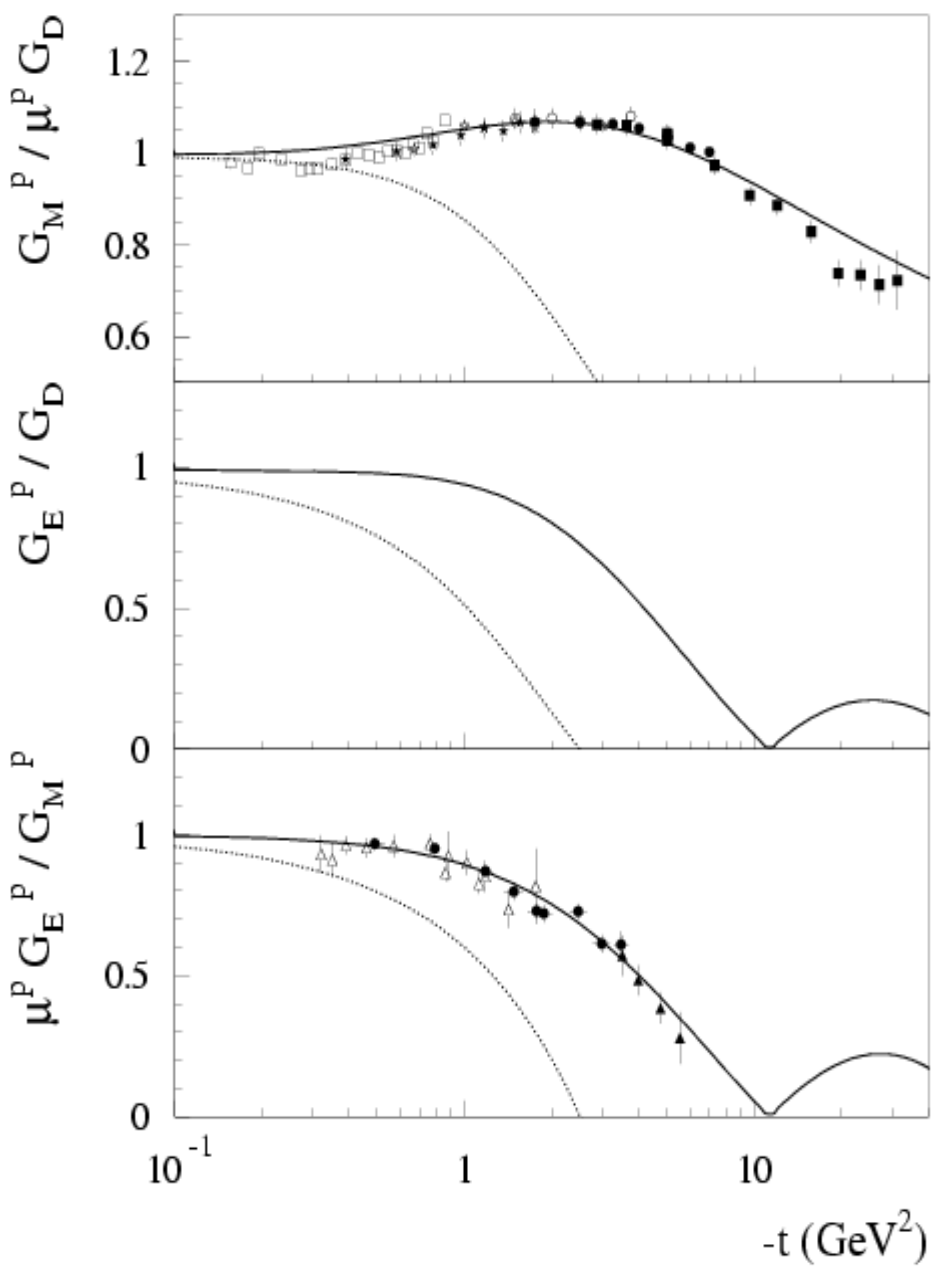


6 parameters : $\alpha'_1, \alpha'_2, \eta^u, \eta^d, T_1, T_2,$

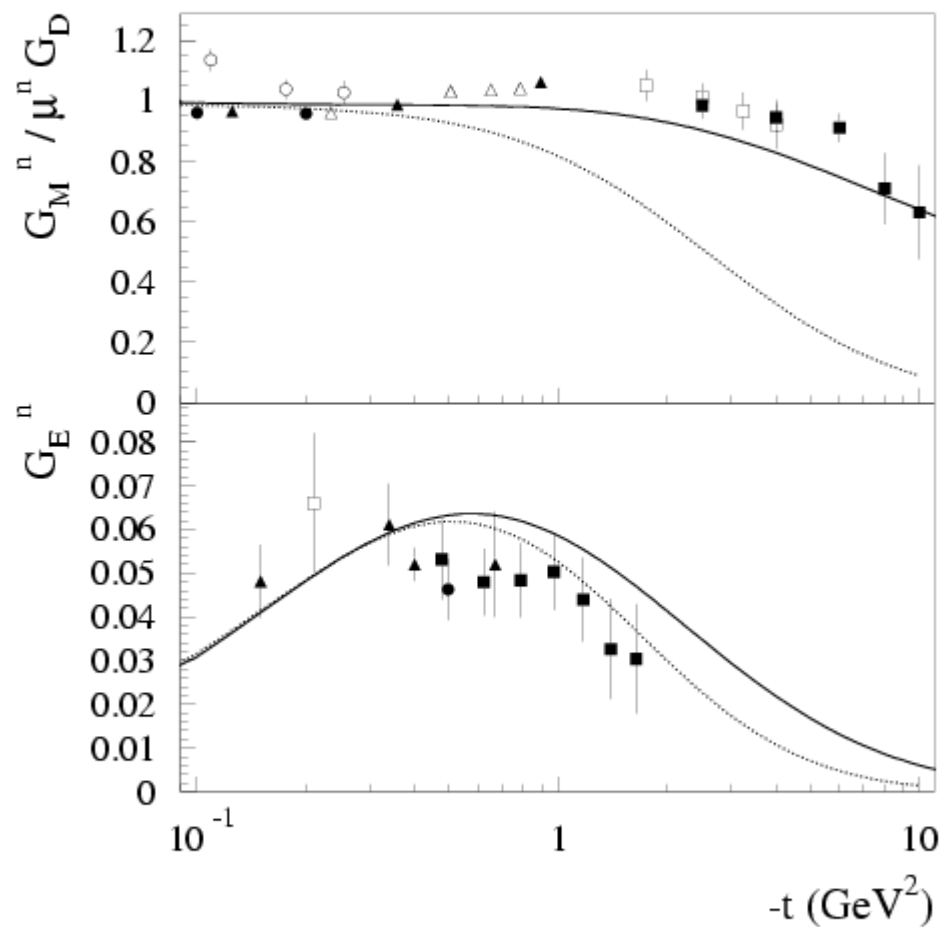


Fit 4 form factors : $G_{E,M}^{p,n}$ on whole t domain !

PROTON electric and magnetic form factors



NEUTRON electric and magnetic form factor



Nucleon strangeness : F_1^s

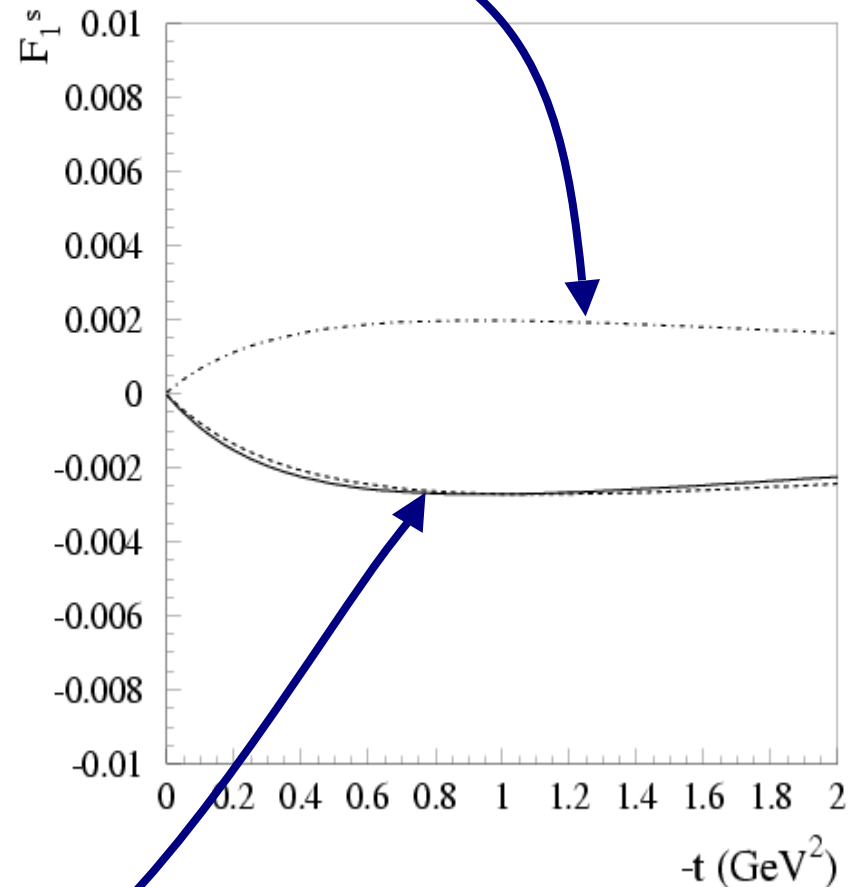
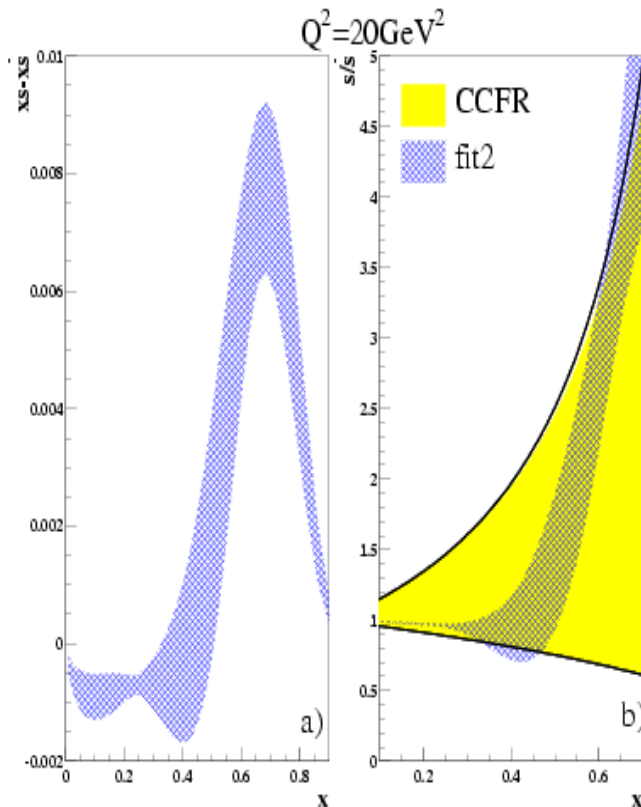
$$\int_{-1}^1 [s(x) - \bar{s}(x)] dx = 0$$

But : $F_1^s(t) = \int_{-1}^1 [s(x) - \bar{s}(x)] / (x^{\alpha' t}) dx \neq 0$

$s(x) - \bar{s}(x)$ distribution in the proton

NUCLEON STRANGENESS F_1 form factor

- extracted from $\nu, \bar{\nu}$ data
 - DIS fit performed by Barone, Pascaud, Zomer (2000)
- fit $s \neq \bar{s}$ (CDHS data) : $\langle xs \rangle - \langle x\bar{s} \rangle \simeq +2 \cdot 10^{-3}$



- fit based on $\nu, \bar{\nu}$ CCFR + NuTeV (2001) data :
 $\langle xs \rangle - \langle x\bar{s} \rangle \simeq -(2.7 \pm 1.3) \cdot 10^{-3}$

SUMMARY

1/DDVCS

- ➡ The (continuously) varying virtuality of the outgoing photon allows to “tune” the kinematical point (x, ξ, t) at which the GPDs are sampled
- ➡ Currently working out the anti-symmetrisation issues
- ➡ Experimental feasibility : maybe not so far away....

2/(x, t) dep. of GPDs

- ➡ α' should depend on Q^2 to match evolution of PDF/GPDs