

National Nuclear Physics Summer School 2026
University of Washington, Seattle, June 29- July 11 2026

Low energy probes of physics beyond the Standard Model (3)

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University of Washington

Flow of the lectures

- The quest for new physics at the low-energy frontier: overview of *questions* and *probes*
- How does the precision / intensity frontier work?
 - Basics & example from history: the making of the Standard Model
 - ~~The Standard Model and its symmetries~~

- BSM effective field theory (EFT) framework
- “Zoom in” on selected low-energy probes: illustrate methods and impact
 - **Search for symmetry violation**
 - Neutrino mass and symmetries: Lepton Number ~~and Lepton Flavor~~ Violation

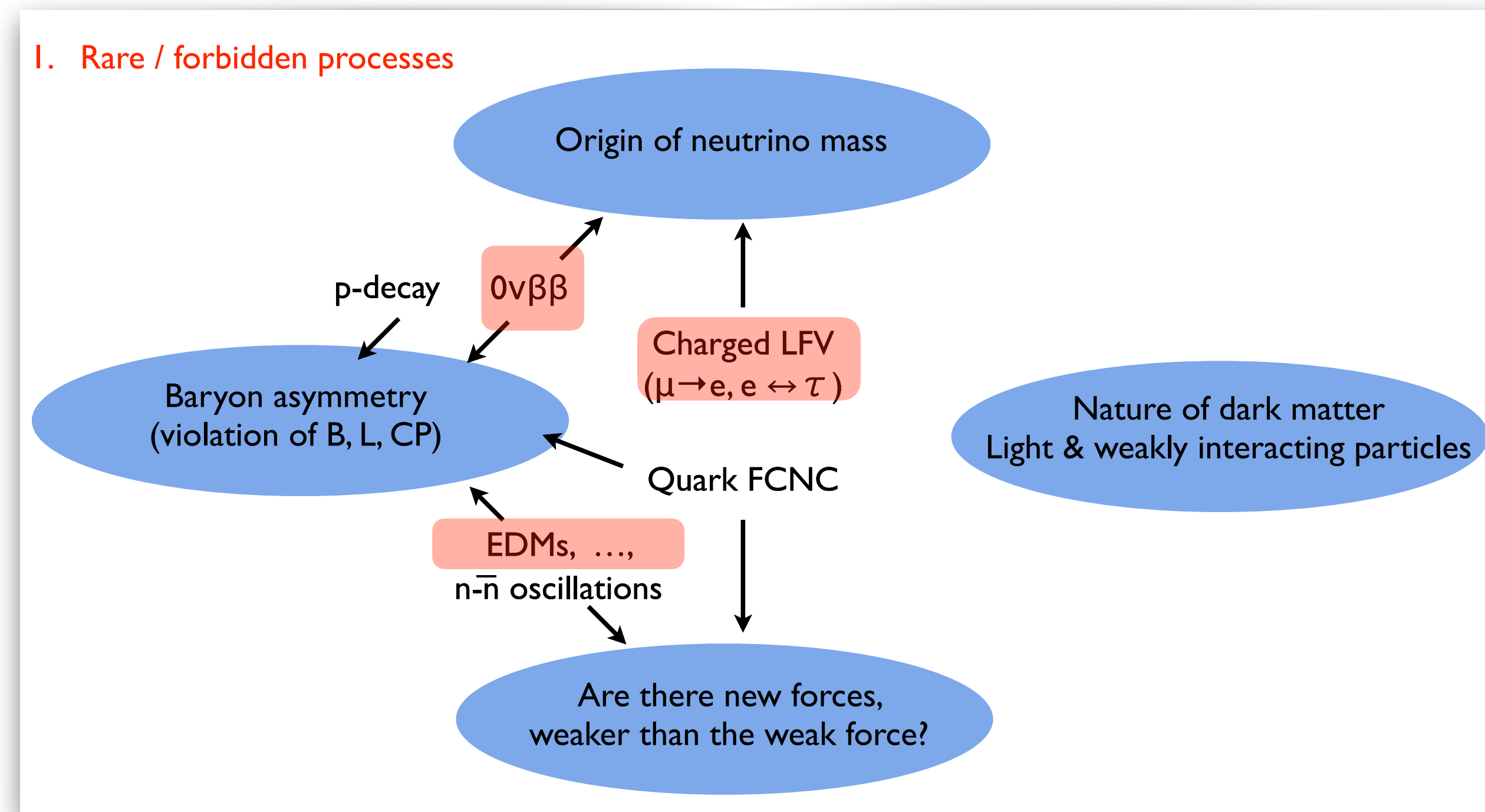
- CP-violation and permanent Electric Dipole Moments
- **Precision tests**
- Weak charged current (β decays), ~~neutral current (parity violating e scattering), muon g-2~~

Lecture 1

Lecture 2

Lecture 3

Rare / forbidden processes



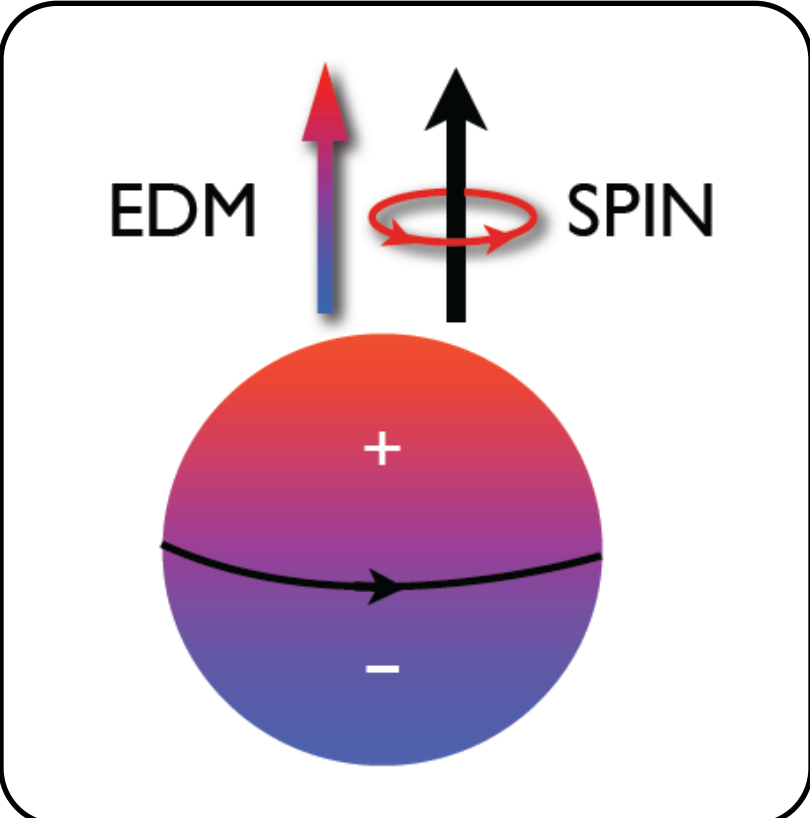
Discuss some theoretical aspects of EDMs

EDMs and symmetry breaking

- EDMs of *non-degenerate* systems violate P and T: $H = \vec{d} \cdot \vec{E}$

Classical picture →

Quantum level:
Wigner-Eckart theorem



The diagram shows a sphere with a vertical color gradient from red at the top to blue at the bottom. A red arrow labeled 'EDM' points upwards from the top of the sphere. A black arrow labeled 'SPIN' points upwards from the center of the sphere, with a red circular arrow around it indicating rotation. The top of the sphere is marked with a '+' sign and the bottom with a '-' sign.

$$\vec{d} = \sum_i q_i \vec{r}_i$$
$$\vec{d} = d \vec{J}$$

- CPT symmetry (holds for Lorentz-invariant quantum field theories) \Rightarrow nonzero EDMs signal also CP violation in the underlying theory

See Dave Kawall's lectures for experimental landscape and a lot more!

CP violation in the SM

$$\mathcal{L}_4^{CPV} = -\bar{\theta} \frac{g_s^2}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu} - \left(\frac{g_2}{2\sqrt{2}} W_\mu^+ \bar{u}_i \gamma^\mu (1 - \gamma_5) V_{ij} d_j + \text{h.c.} \right)$$

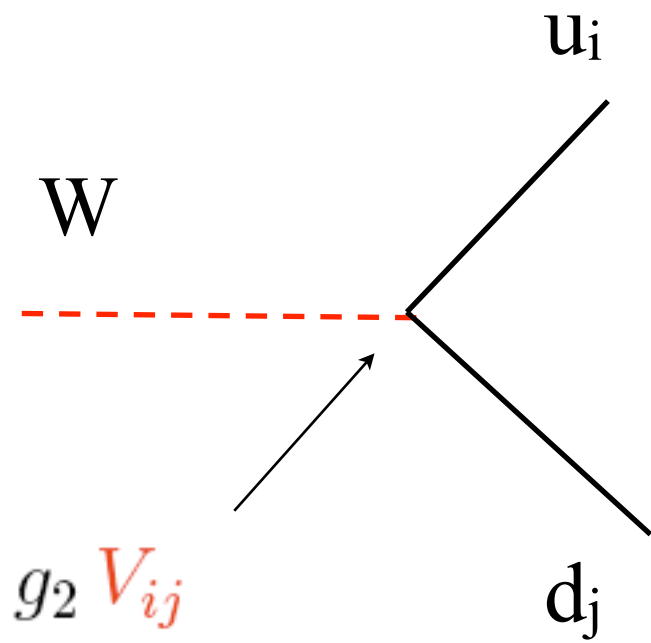
$\bar{\theta} = \theta - \text{ArgDet}(\mathcal{M}_q)$

‘QCD theta term’

$\sim \mathbf{B}_c \cdot \mathbf{E}_c$

$V_{CKM} = V_{u_L} V_{d_L}^\dagger$

Physically observable mismatch in the transformation of u_L and d_L needed to diagonalize quark masses



$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Cabibbo-Kobayashi-Maksawa (CKM) matrix

- CKM matrix is unitary:
 - 9 real parameters, but redefinition of quark phases reduces physical parameters to 4:
3 mixing angles and 1 phase

$$V_{ij} \rightarrow V_{ij} e^{i((\phi_d)_j - (\phi_u)_i)}$$

5 independent
parameters
(phase differences)

- Irreducible phase implies CP violation:

$$g_2 V_{ij} W_\mu^+ \bar{u}_L^i \gamma^\mu d_L^j + g_2 V_{ij}^* W_\mu^- \bar{d}_L^j \gamma^\mu u_L^i$$

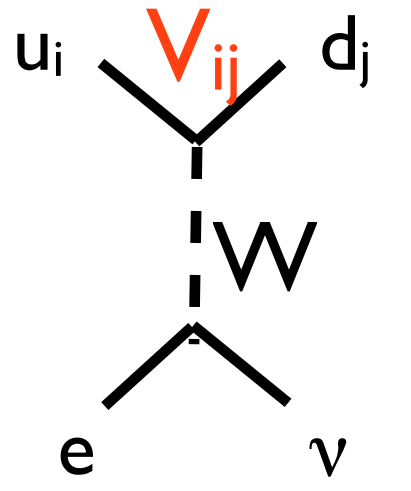
CP transformation

$$g_2 V_{ij} W_\mu^- \bar{d}_L^j \gamma^\mu u_L^i + g_2 V_{ij}^* W_\mu^+ \bar{u}_L^i \gamma^\mu d_L^j$$

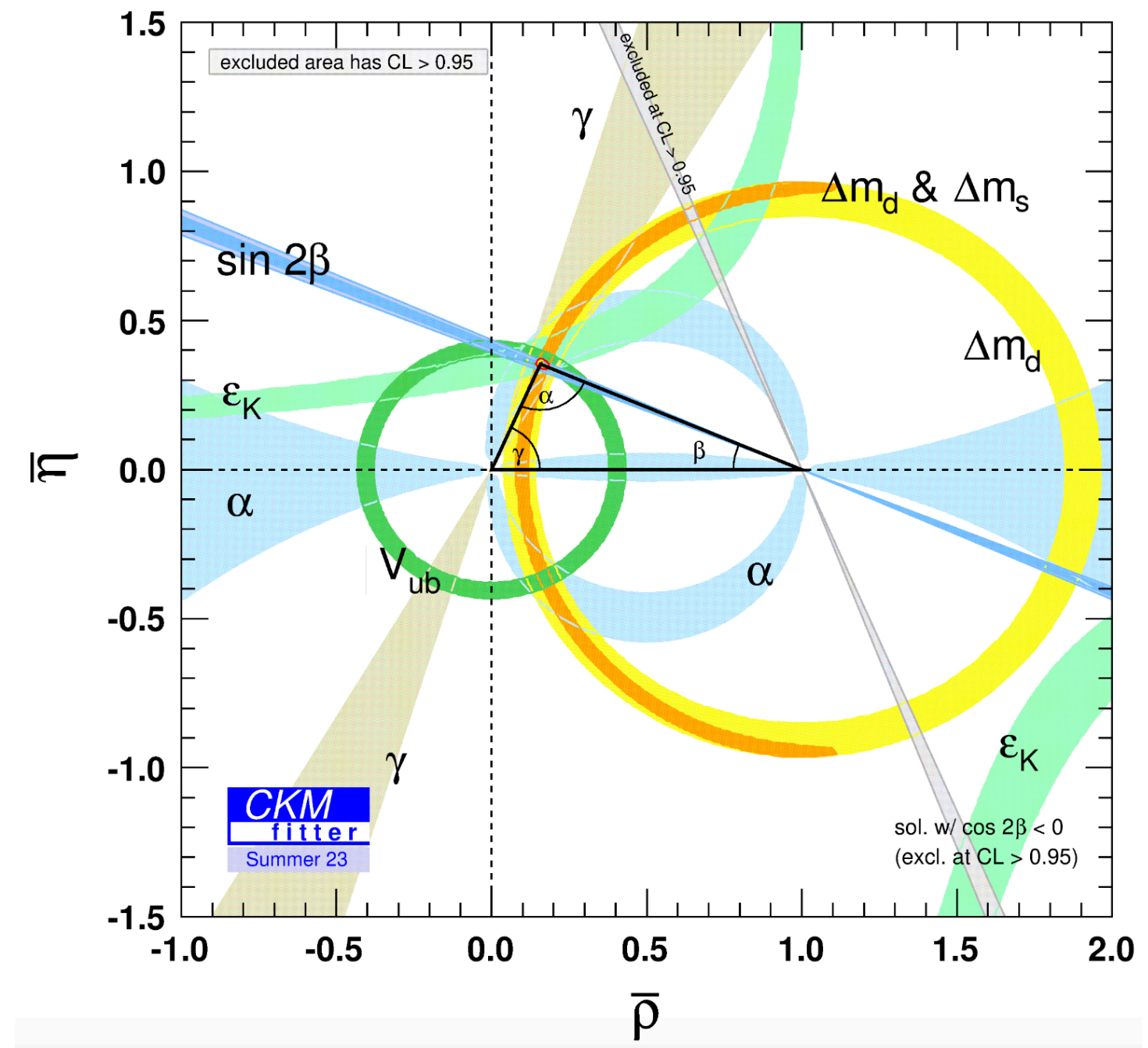
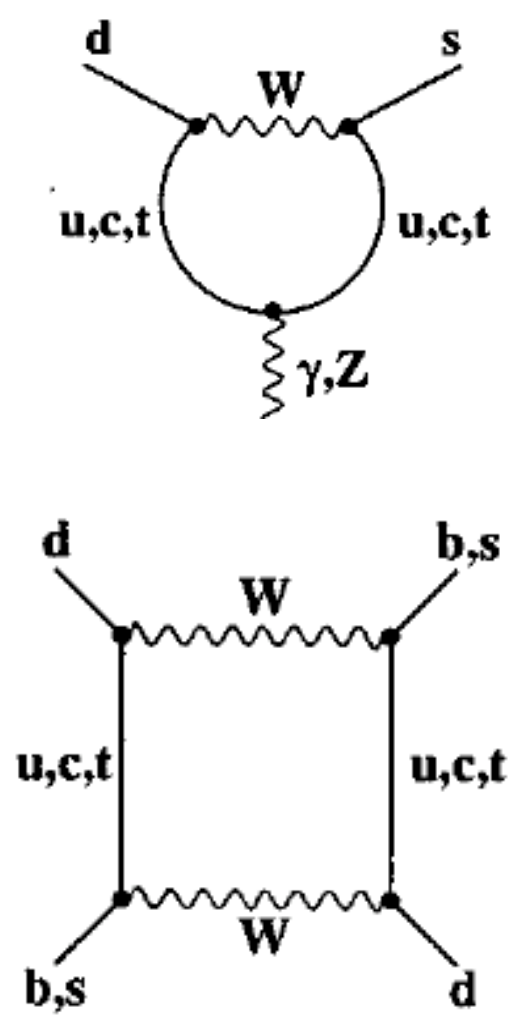
- Wolfenstein (1983) parameterization

Make explicit the hierarchical structure revealed by experiment:
 expand in $\lambda \approx V_{us} \approx 0.225$, with $\rho, \eta, A \sim O(1)$

$$V_{CKM} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$



- Status of the CKM matrix: quark flavor physics (including CPV) is well described by 3 mixing angles and a phase!



$$\bar{\rho} = \rho \left(1 - \frac{\lambda^2}{2}\right)$$

$$\bar{\eta} = \eta \left(1 - \frac{\lambda^2}{2}\right)$$

EDMs in the Standard Model?

$$\mathcal{L}_4^{CPV} = -\bar{\theta} \frac{g_s^2}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu} - \left(\frac{g_2}{2\sqrt{2}} W_\mu^+ \bar{u}_i \gamma^\mu (1 - \gamma_5) V_{ij} d_j + \text{h.c.} \right)$$

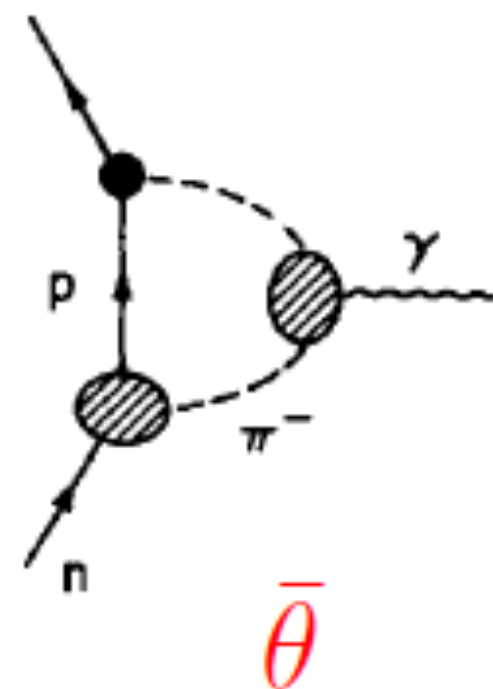
Axial transformation of
quark field

$$\sim \mathbf{B}_c \cdot \mathbf{E}_c$$

Baluni 1979
Crewther, Di Vecchia,
Veneziano, Witten 1979

$$-m_* \bar{\theta} \bar{q} i \gamma_5 q \sim \boldsymbol{\sigma} \cdot (\mathbf{p}_f - \mathbf{p}_i)$$

$$m_* = \frac{1}{\sum_i (1/m_i)} \simeq \frac{m_u m_d}{m_u + m_d}$$



$$d_n \sim \frac{m_*}{\Lambda_{\text{had}}^2} e \bar{\theta} \sim 10^{-17} \bar{\theta} \text{ e cm}$$

$$d_n < 3 \cdot 10^{-26} \text{ e cm}$$

$$\rightarrow |\bar{\theta}| < 10^{-9}$$

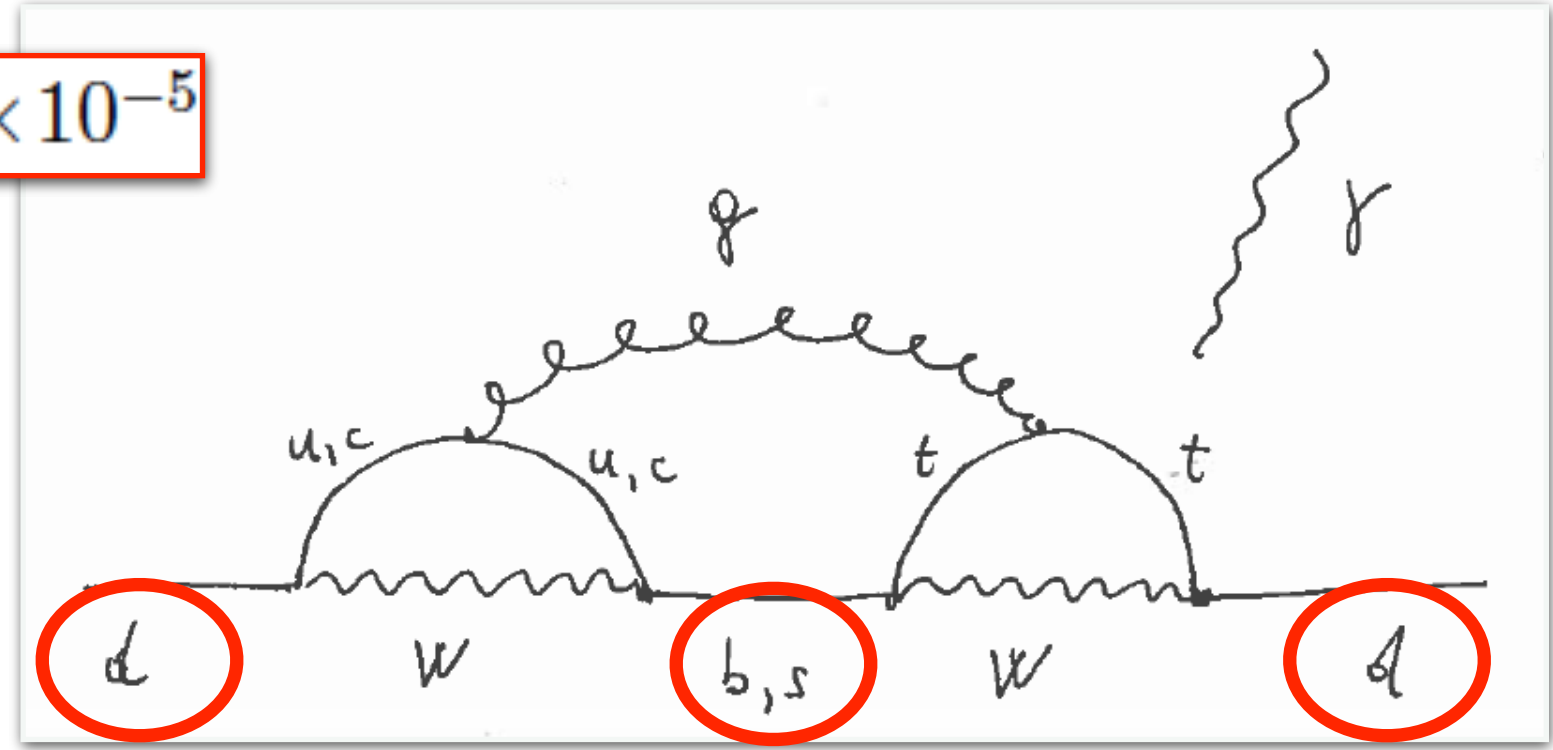
EDMs in the Standard Model?

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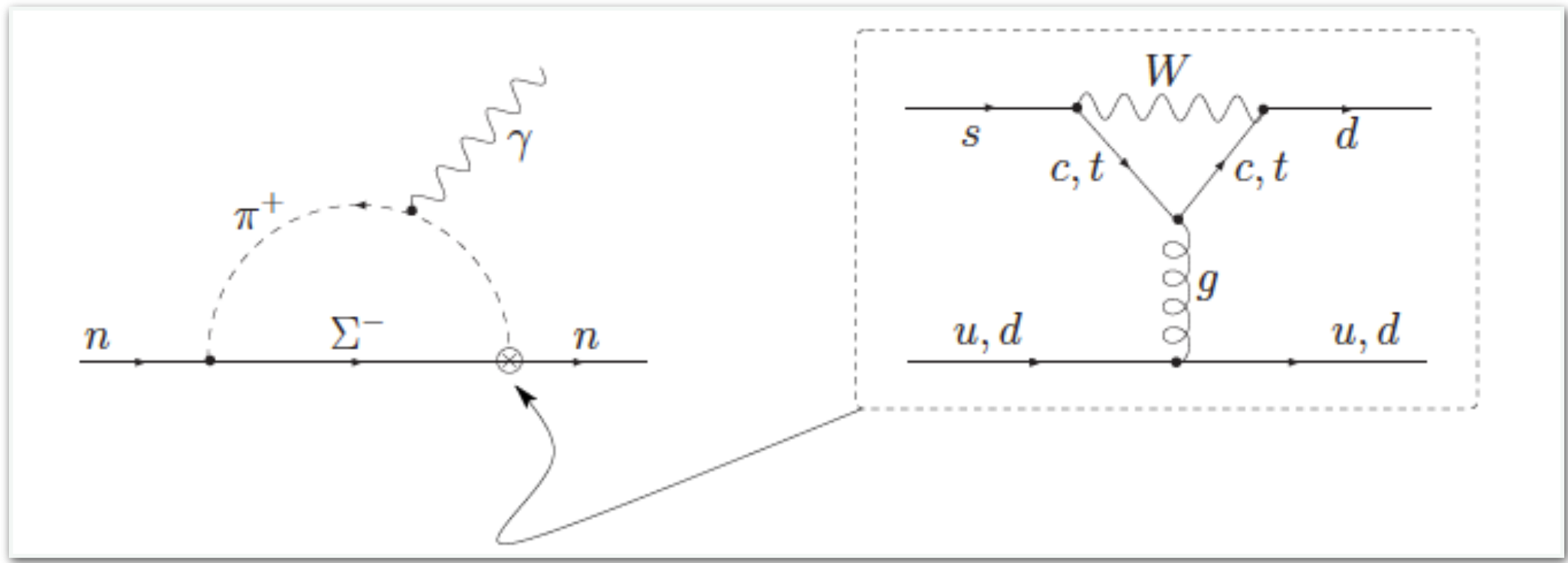
$$J_{CP} = \text{Im}(V_{tb} V_{td}^* V_{cd} V_{cb}^*) \simeq 3 \times 10^{-5}$$

$$d_q \sim 10^{-34} \text{ e cm}$$

$$d_e \sim 10^{-38} \text{ e cm}$$



Highly suppressed quark and lepton EDMs



Dominant contribution to nEDM

$$d_n \sim 10^{-31} \text{ e cm}$$

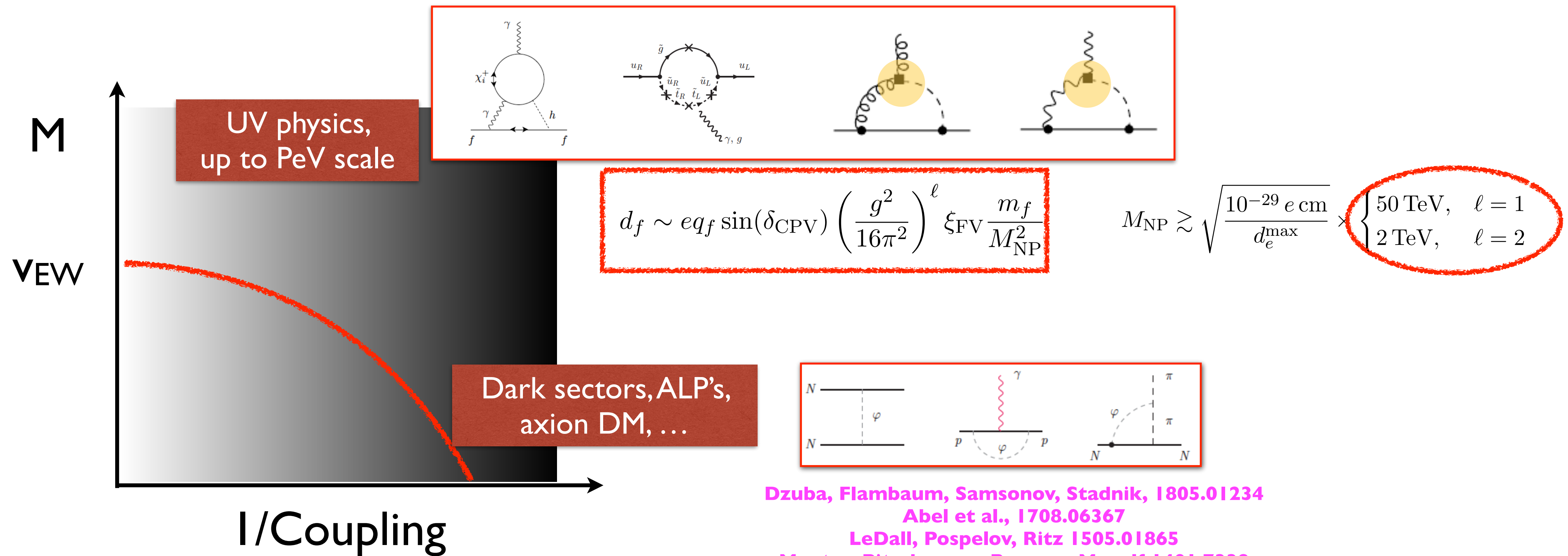
...
Pospelov-Ritz
hep-ph/0504231
C.Y. Seng 1411.1476

EDMs as probes of new physics

White paper 2203.08103 and refs therein

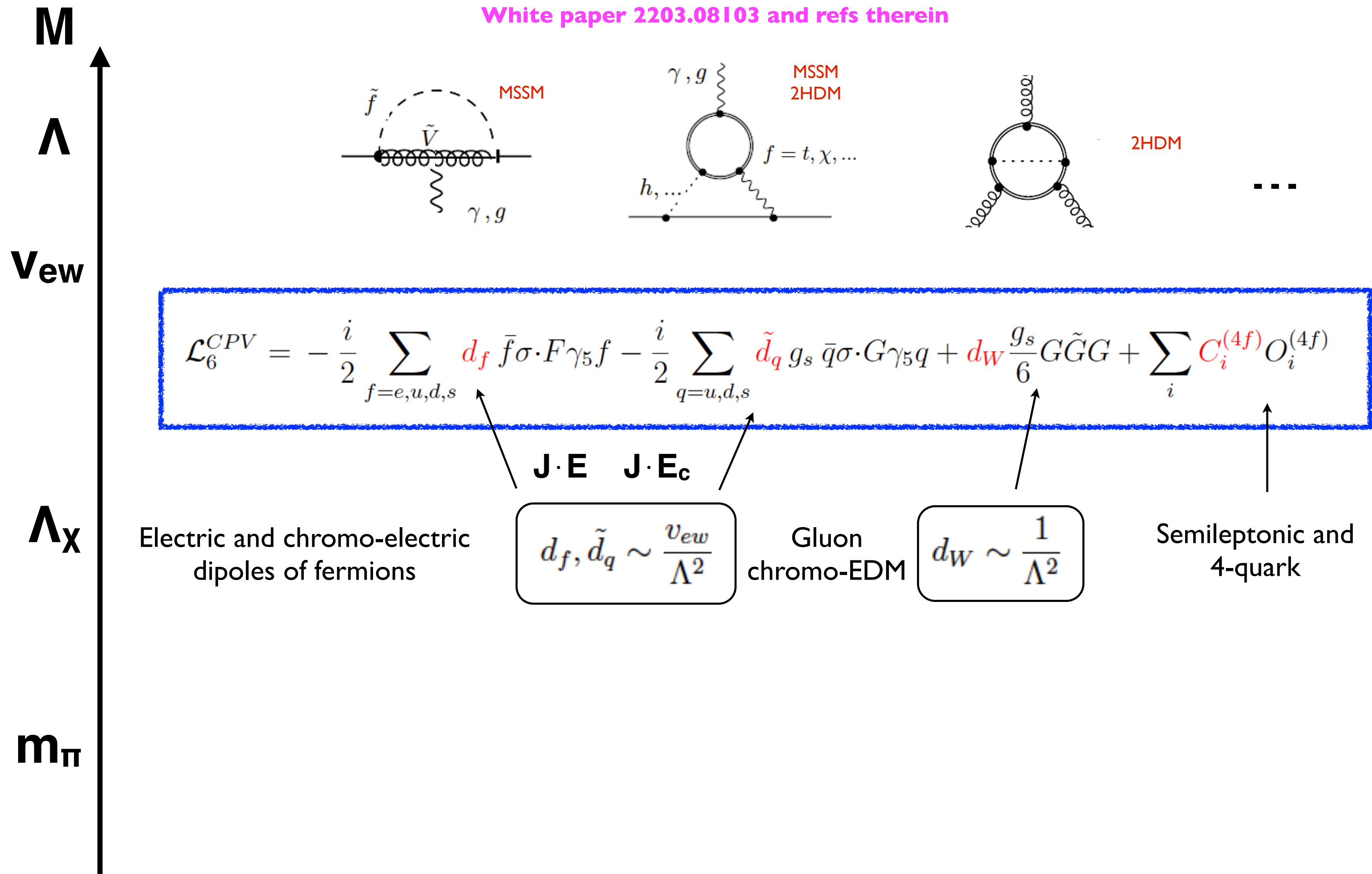
Chupp, Fierlinger, Ramsey-Musolf, Singh, 1710.02504

- Highly suppressed in Standard Model (CKM phase)
- A non-zero EDM would imply new physics or a tiny QCD θ -term (multiple measurements can disentangle the two)
- Sensitive to broad spectrum of new physics (Higgs sector, SUSY, ALPs...) & baryogenesis mechanisms



Connecting scales

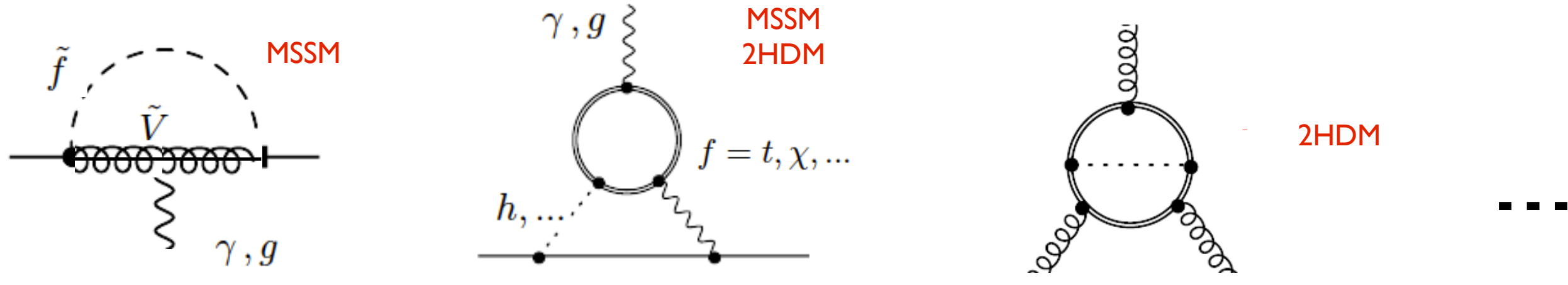
White paper 2203.08103 and refs therein



Connecting scales

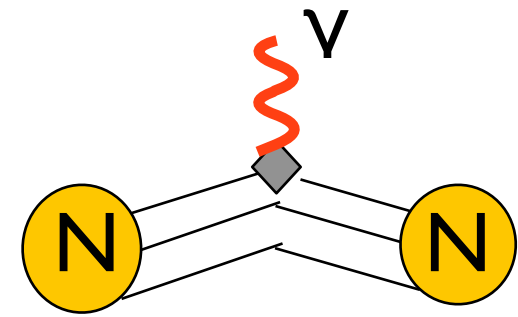
White paper 2203.08103 and refs therein

M
Λ
View
Λ_χ
m_π

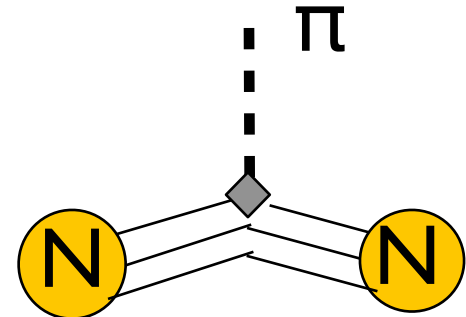


$$\mathcal{L}_6^{CPV} = -\frac{i}{2} \sum_{f=e,u,d,s} d_f \bar{f} \sigma \cdot F \gamma_5 f - \frac{i}{2} \sum_{q=u,d,s} \tilde{d}_q g_s \bar{q} \sigma \cdot G \gamma_5 q + d_W \frac{g_s}{6} G \tilde{G} G + \sum_i C_i^{(4f)} O_i^{(4f)}$$

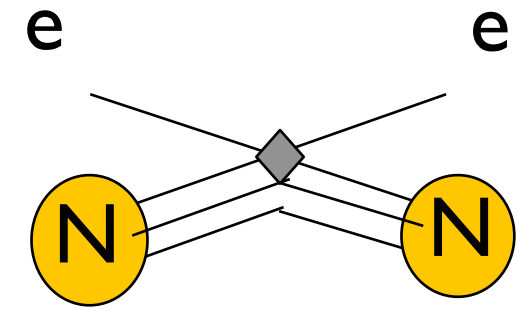
Electron and Nucleon EDMs



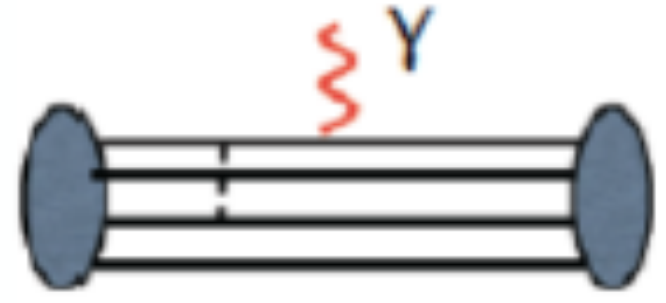
CP-odd πN couplings



Short-range 4N and 2N2e coupling



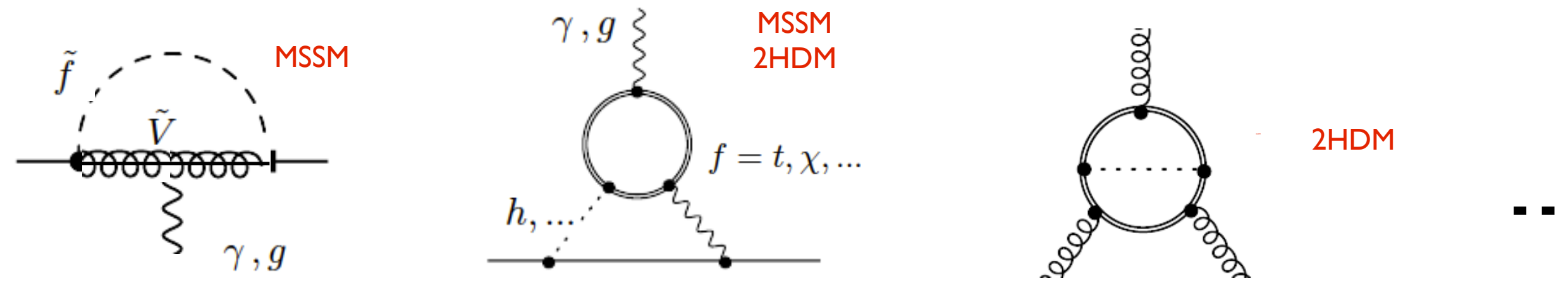
Chiral EFT analysis:
de Vries, Mereghetti, Timmermans, van Kolck, 1212.0990, ...



Connecting scales

White paper 2203.08103 and refs therein

M
Λ
View
Λ_x
m_π



$$\mathcal{L}_6^{CPV} = -\frac{i}{2} \sum_{f=e,u,d,s} d_f \bar{f} \sigma \cdot F \gamma_5 f - \frac{i}{2} \sum_{q=u,d,s} \tilde{d}_q g_s \bar{q} \sigma \cdot G \gamma_5 q + d_W \frac{g_s}{6} G \tilde{G} G + \sum_i C_i^{(4f)} O_i^{(4f)}$$

Lattice QCD QCD sum rules

$$d_n = -(1.5 \pm 0.7) \cdot 10^{-3} \bar{\theta} \text{ e fm} \quad \mu=2\text{GeV}$$

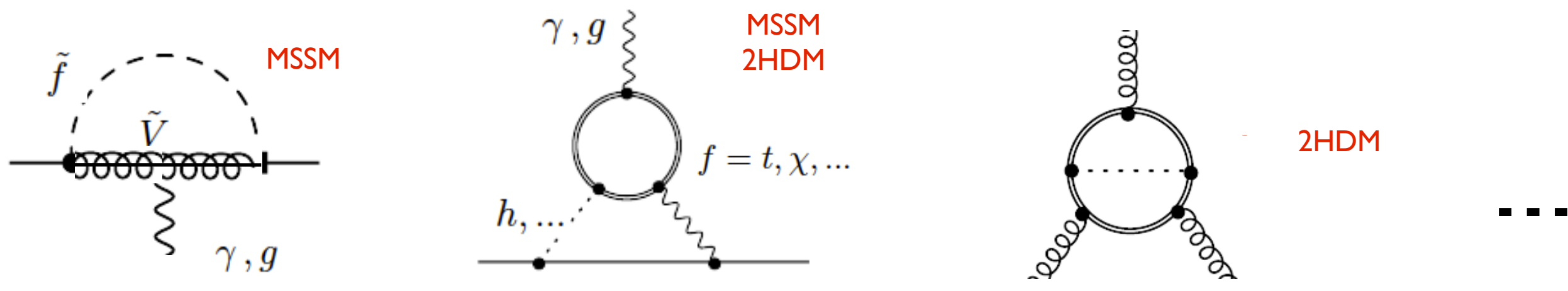
$$-(0.20 \pm 0.01) d_u + (0.78 \pm 0.03) d_d + (0.0027 \pm 0.016) d_s$$

$$-(0.55 \pm 0.28) e \tilde{d}_u - (1.1 \pm 0.55) e \tilde{d}_d + (50 \pm 40) \text{ MeV} e \tilde{d}_G$$

Connecting scales

M
Λ
View
Λ_x
m_π

White paper 2203.08103 and refs therein



$$\mathcal{L}_6^{CPV} = -\frac{i}{2} \sum_{f=e,u,d,s} d_f \bar{f} \sigma \cdot F \gamma_5 f - \frac{i}{2} \sum_{q=u,d,s} \tilde{d}_q g_s \bar{q} \sigma \cdot G \gamma_5 q + d_W \frac{g_s}{6} G \tilde{G} G + \sum_i C_i^{(4f)} O_i^{(4f)}$$

Lattice QCD QCD sum rules

$$\mathcal{L} = \bar{g}_0 \bar{N} \vec{\pi} \cdot \vec{\tau} N + \bar{g}_1 \bar{N} \pi_3 N$$

$$\bar{g}_0 = (5 \pm 10) (\tilde{d}_u + \tilde{d}_d) \text{ fm}^{-1} \quad , \quad \bar{g}_1 = (20_{-10}^{+40}) (\tilde{d}_u - \tilde{d}_d) \text{ fm}^{-1}$$

Pospelov-Ritz hep-ph/0504231 and refs therein

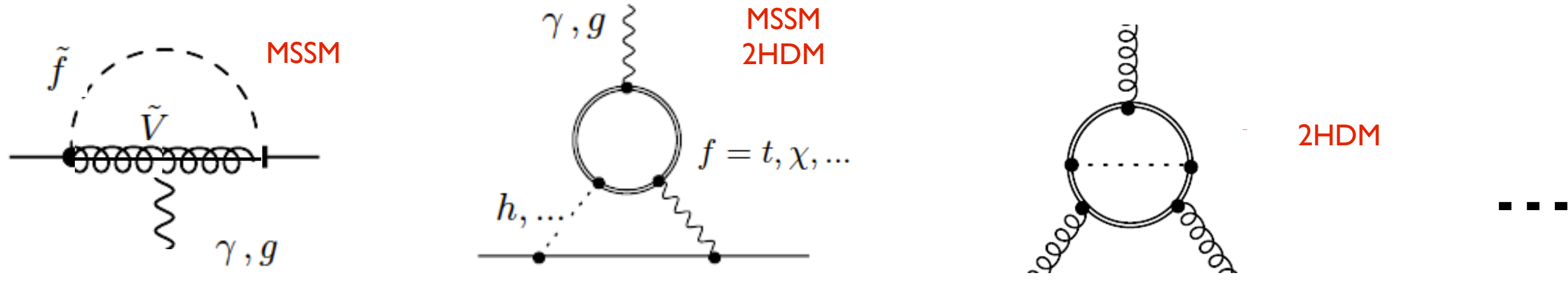
UNCERTAINTY SCOREBOARD:
Proton: same as neutron
Nuclei: worse

Opportunity for lattice QCD

Connecting scales

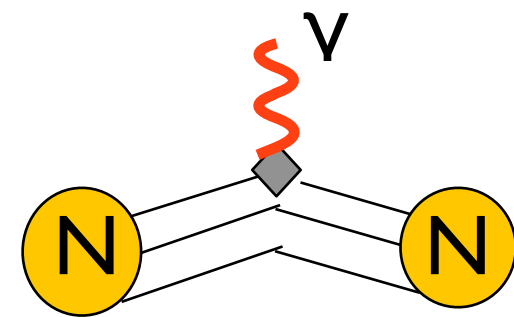
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M
Λ
View
Λ_χ
m_π

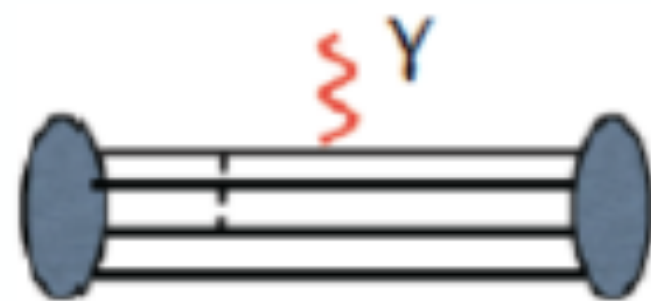
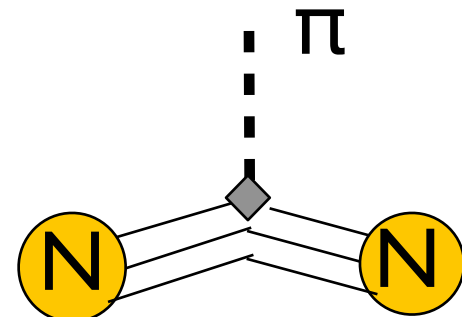


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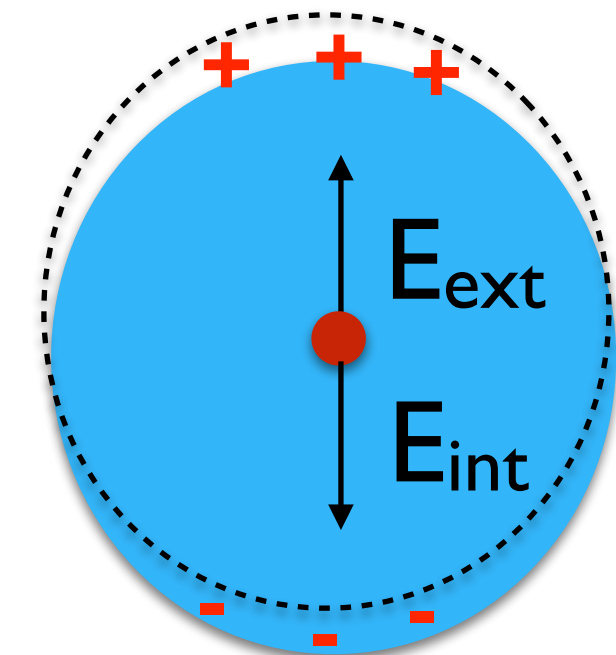
Electron and Nucleon EDMs



CP-odd πN couplings



At the atomic / molecular scale: work around Schiff screening
(finite size of nuclei and relativistic electron effects)
Diamagnetic atoms: O(100%) uncertainties
Paramagnetic atoms / molecules: O(10%) uncertainties



Summary: the “EDM matrix”

$i \in \{n, p, \dots, \text{ThO}, \dots, {}^{199}\text{Hg}\}$

Hadronic scale
effective couplings

(B)SM sources
of CP violation

$$d_i = \sum_j \alpha_{ij} \tilde{c}_j [\{c\}]$$

α_{ij}
Nuclear and atomic / molecular
matrix elements

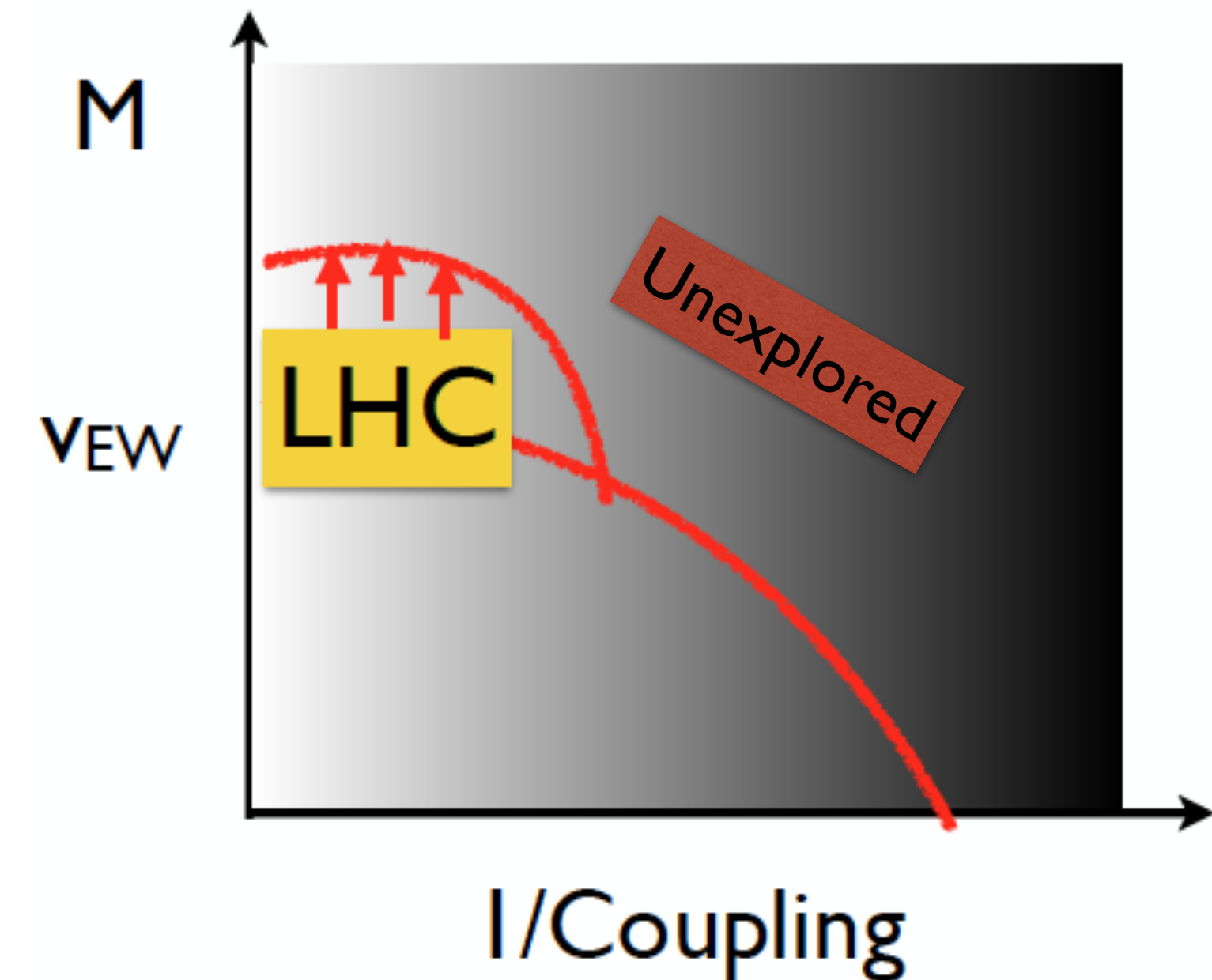
$$\tilde{c}_j = \sum_k \beta_{jk} c_k$$

β_{jk}
Hadronic matrix
elements

- To constrain & disentangle new CPV sources need multiple probes
- Many of the coefficients α_{ij} and β_{jk} are currently poorly known:
 - Need both α 's and β 's to connect EDMs to new physics [c_k 's]
 - Large uncertainties dilute constraining power: major challenge for theorists

EDMs in the LHC era

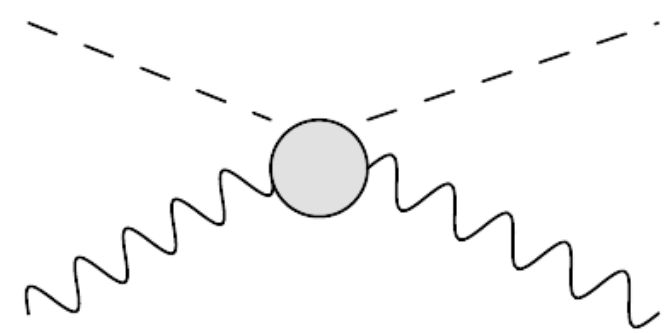
- LHC output so far:
 - Higgs boson @ 125 GeV
 - Everything else is quite heavier (or very light)
- *EDMs more relevant than ever:*
 - Strongest constraints of non-standard **CPV Higgs couplings**
 - One of few observables probing **PeV scale supersymmetry**
 - Strong constraints on **baryogenesis models**



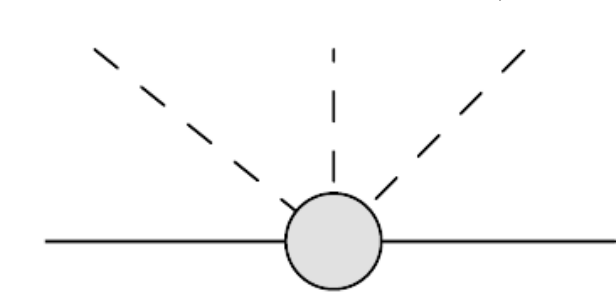
EDMs and CPV Higgs couplings

- Leading ($1/\Lambda^2$) CP-violating BSM interactions involving the Higgs:

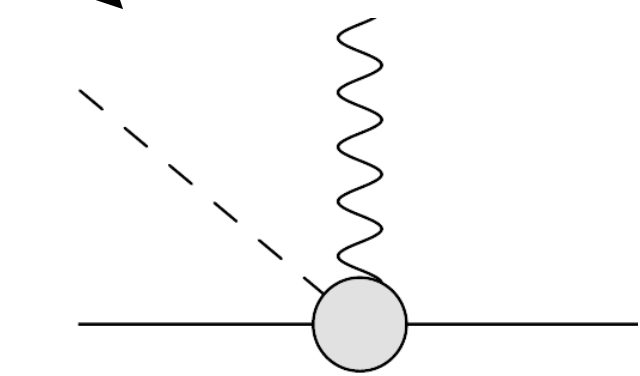
$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{SM} + \frac{C^{(5)}}{\Lambda} O^{(5)} + \sum_i \frac{C_i^{(6)}}{\Lambda^2} O_i^{(6)} + \dots$$



H-H-V- \tilde{V}
 $F_{\mu\nu} \tilde{F}^{\mu\nu} \sim \mathbf{E} \cdot \mathbf{B}$



H-q_L-q_R: pseudo-scalar
 Yukawa coupling $\sim \boldsymbol{\sigma} \cdot (\mathbf{p}_f - \mathbf{p}_i)$

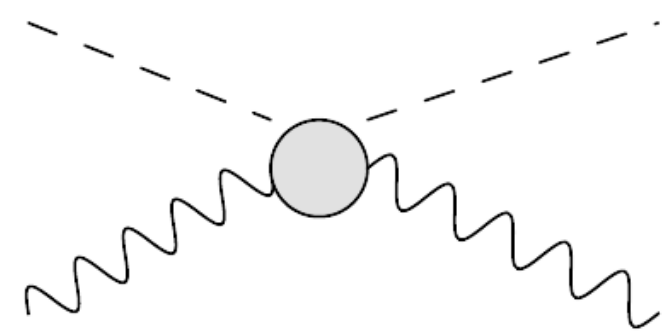


H-q_L-q_R-V: dipole $\sim \boldsymbol{\sigma} \cdot \mathbf{E}$
 $V = g, W^a, B$

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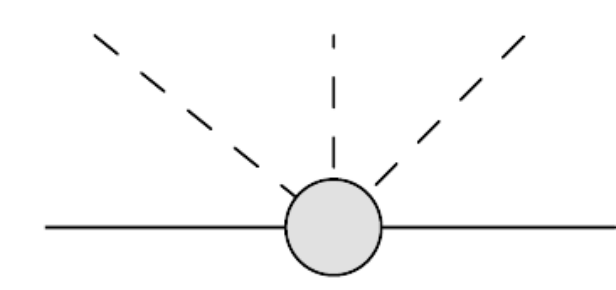
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H-H-V- \tilde{V}
 $F_{\mu\nu} \tilde{F}^{\mu\nu} \sim \mathbf{E} \cdot \mathbf{B}$

McKeen-Pospelov-Ritz
 1208.4597

VC, Crivellin, Dekens, de Vries,
 Hoferichter, Mereghetti, 1903.03625,
 Phys. Rev. Lett. 123, 051801 (2019)

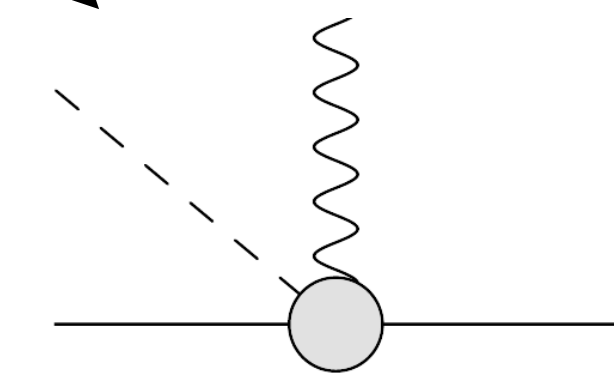


H-q_L-q_R: pseudo-scalar
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Brod Haisch Zupan 1310.1385

Chien-VC-Dekens-de Vries-Mereghetti,
 1510.00725

Brod-Stamou, 1812.12303

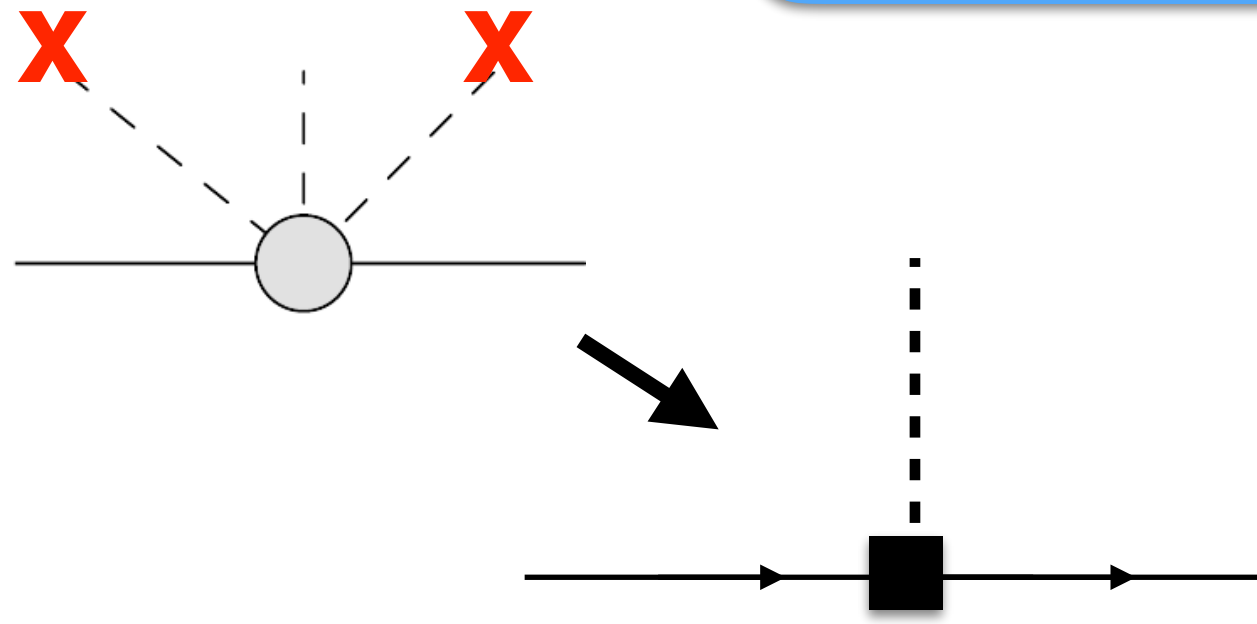


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VC-Dekens-de Vries-Mereghetti,
 1603.03049

Fuyuto & Ramsey-Musolf
 1706.08548

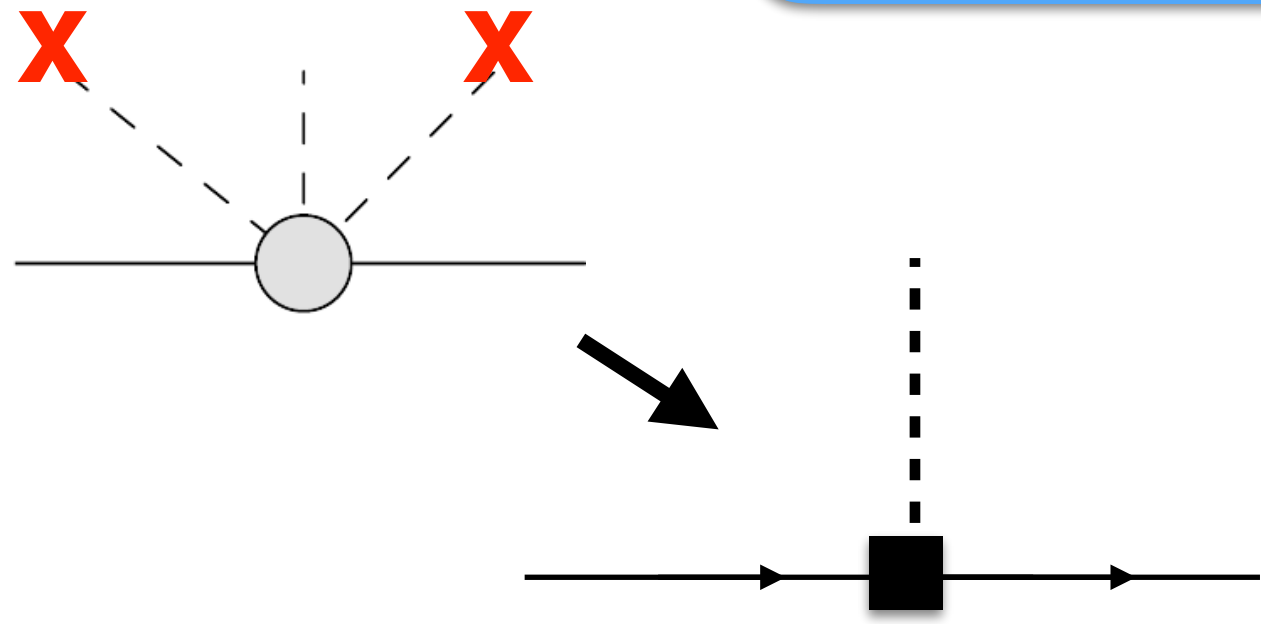
Yukawa couplings to quarks



$$\mathcal{L}_6^{CPV} \supset \sum_q v^2 \text{Im} Y'_q \bar{q} i \gamma_5 q h$$

Pseudo-scalar coupling
 $\boldsymbol{\sigma} \cdot (\mathbf{p}_f - \mathbf{p}_i)$ is zero in
the Standard Model

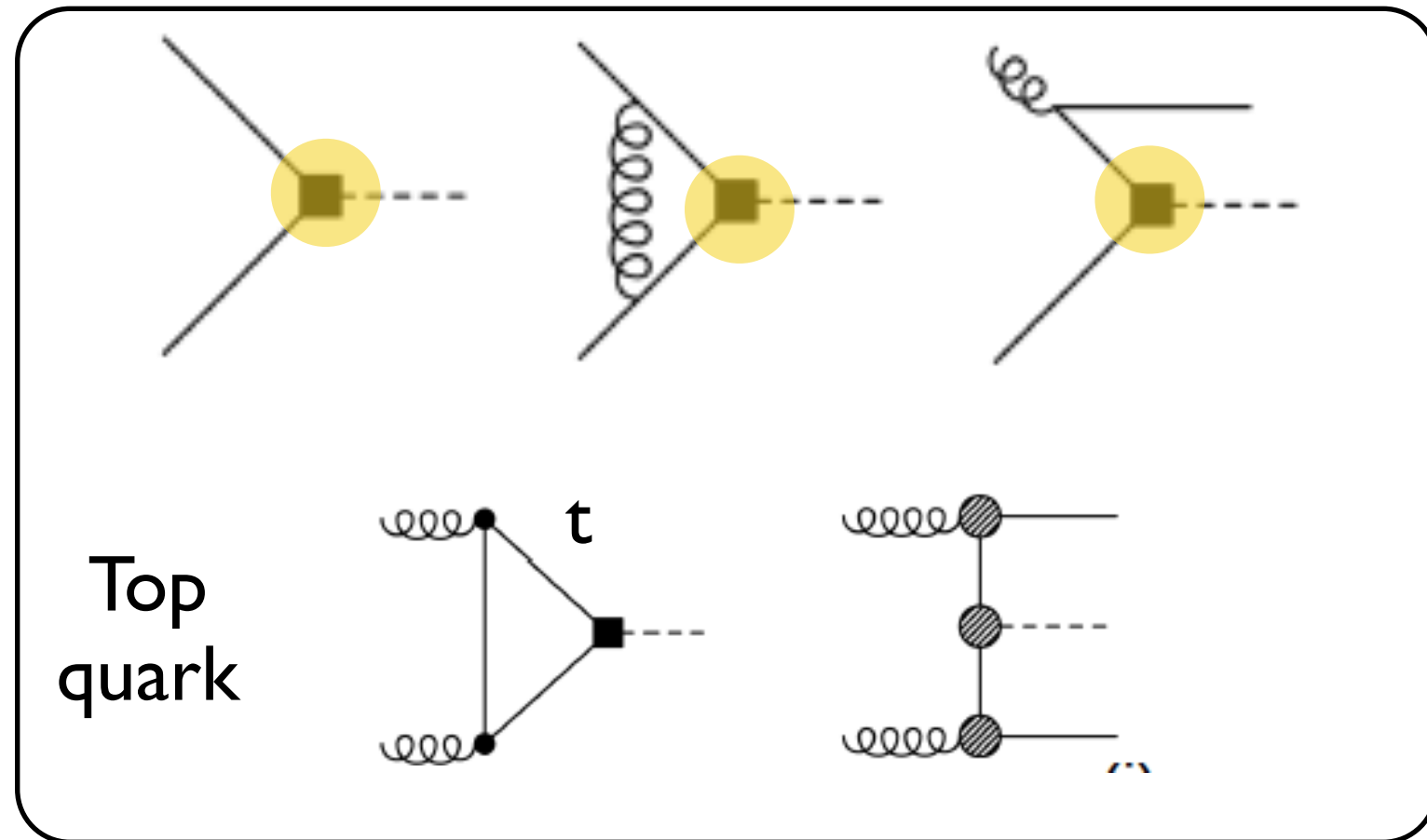
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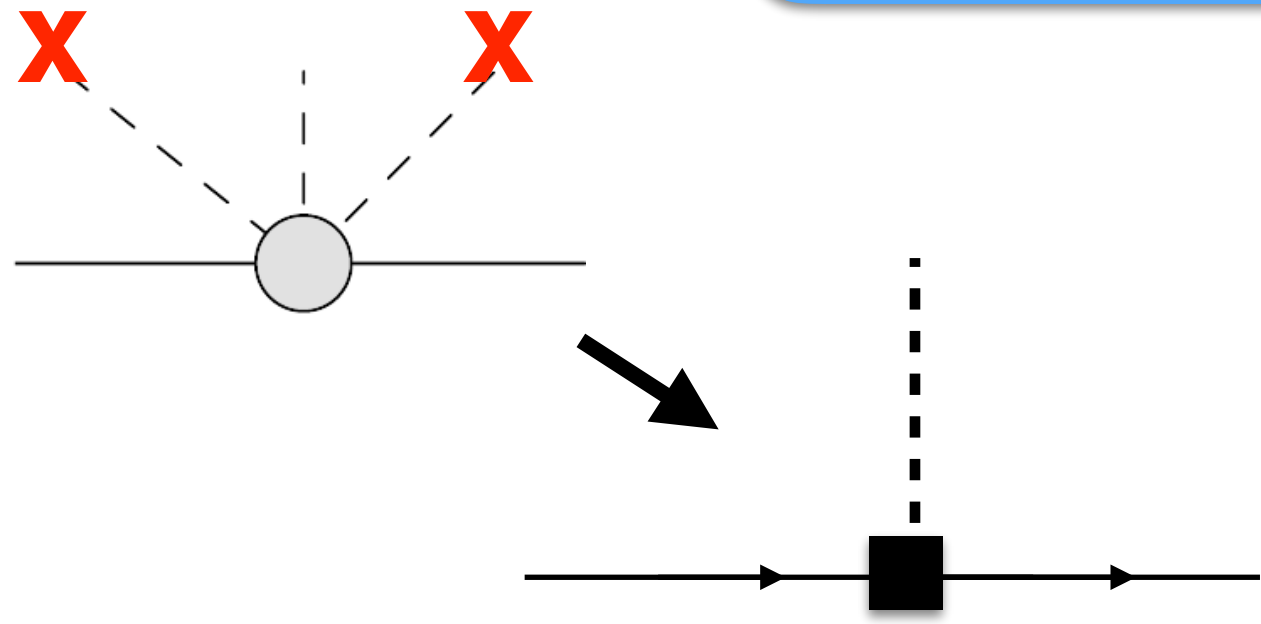
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Pseudo-scalar coupling $\sigma \cdot (\mathbf{p}_f - \mathbf{p}_i)$ is zero in the Standard Model

LHC: Higgs production & decay



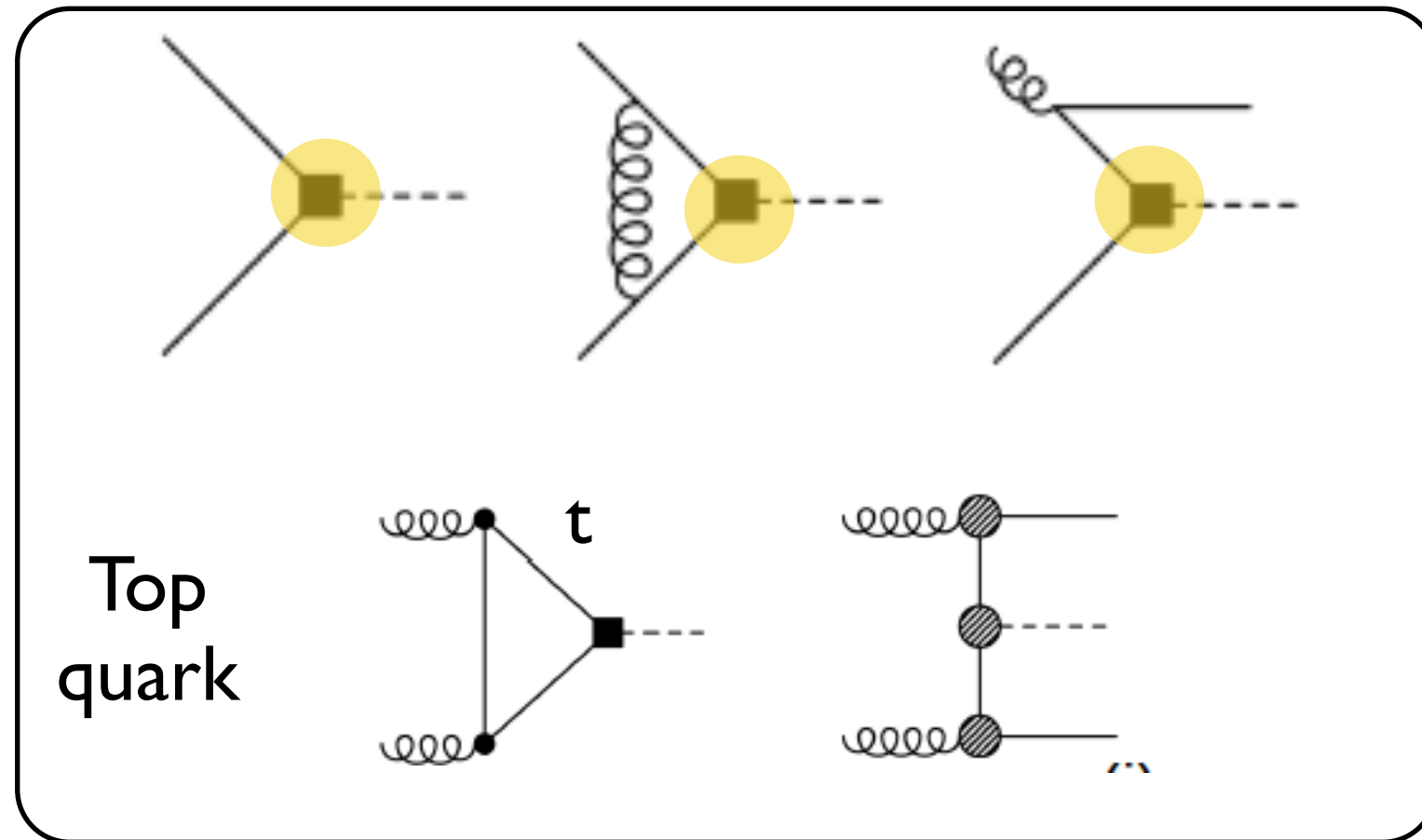
Yukawa couplings to quarks



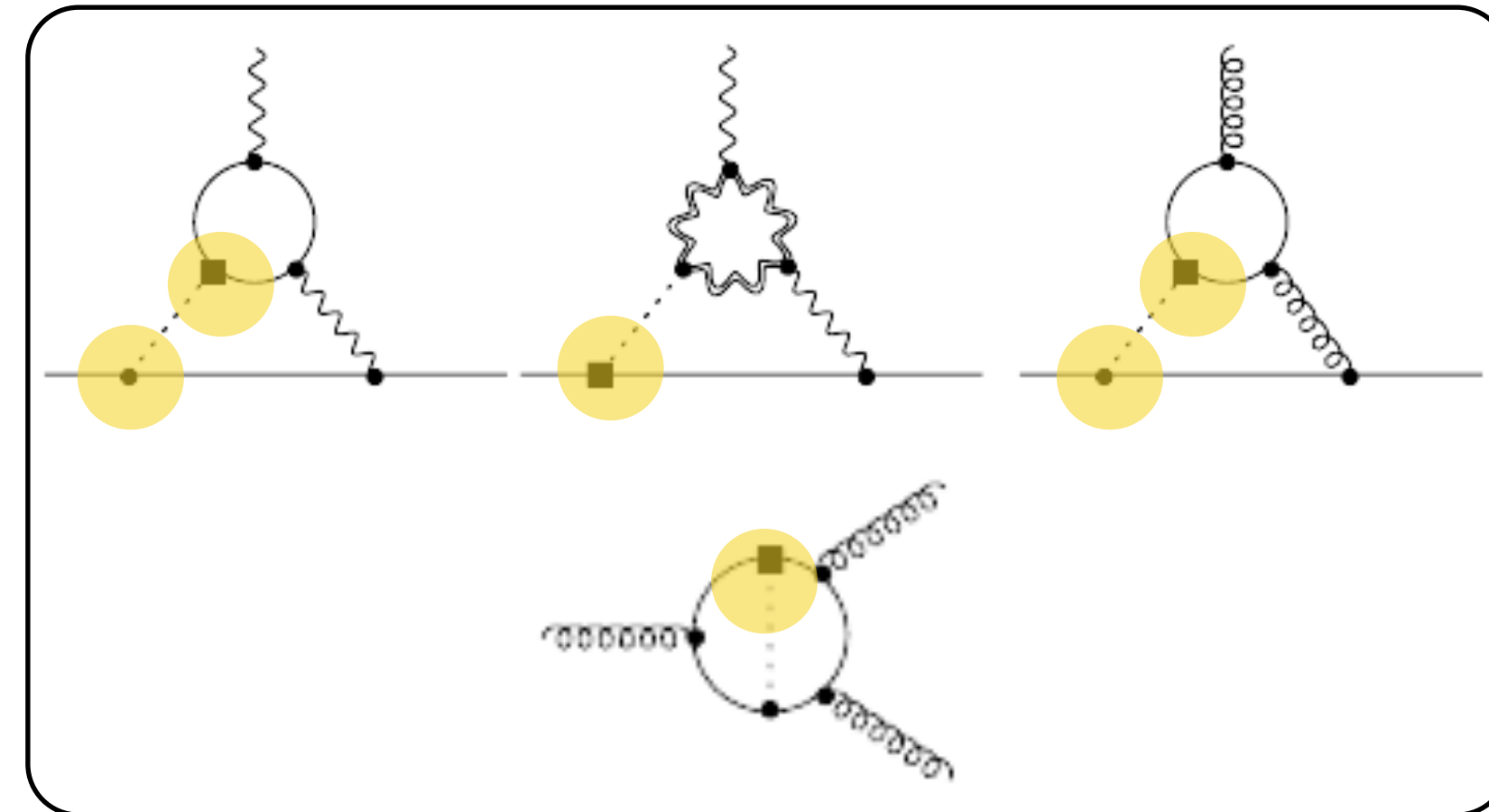
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Pseudo-scalar coupling $\sigma \cdot (\mathbf{p}_f - \mathbf{p}_i)$ is zero in the Standard Model

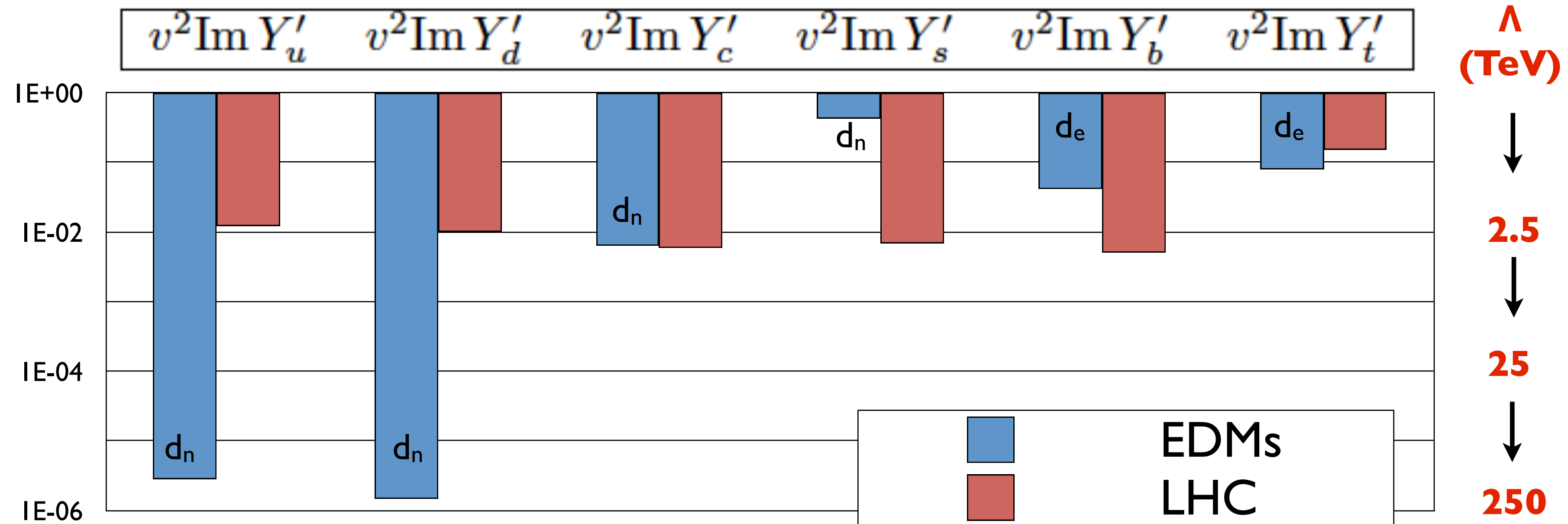
LHC: Higgs production & decay



Low Energy: induce electron, neutron, mercury EDM

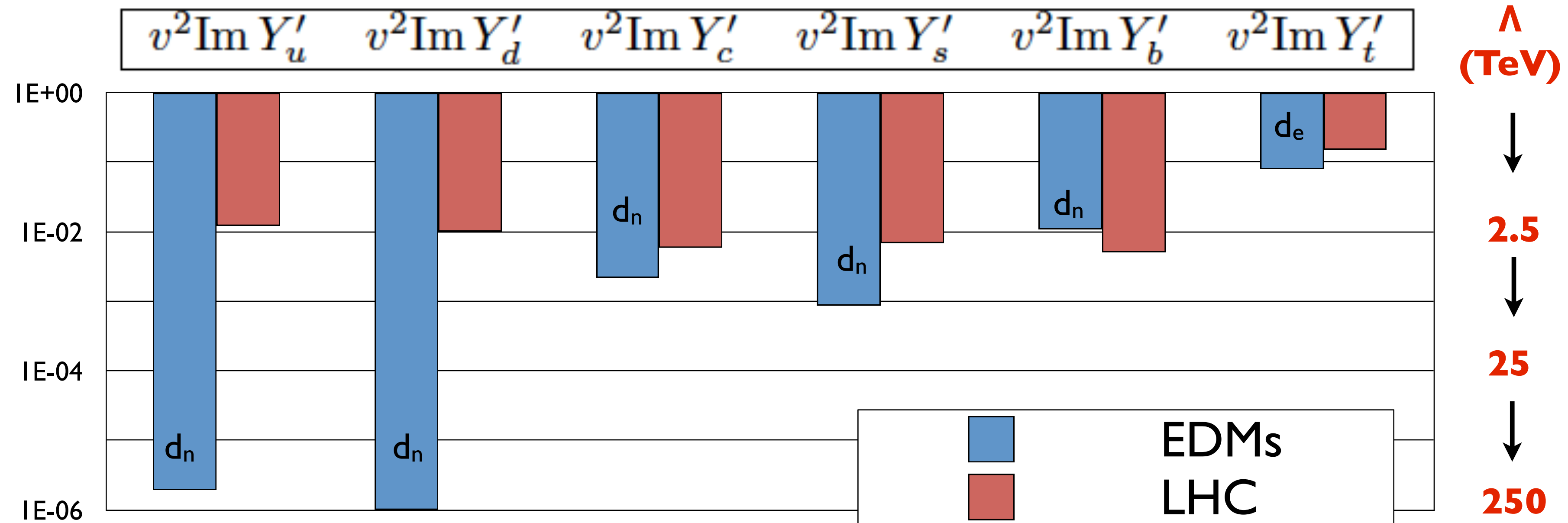


Yukawa couplings to quarks



- EDMs are teaching us something about the Higgs!
- Future: factor of 2 at LHC; EDM constraints scale linearly
- Uncertainty in matrix elements strongly dilutes EDM constraints

Yukawa couplings to quarks



- Much stronger impact of nEDM with reduced uncertainties, for example:

$$d_{n,p}[\tilde{d}_{u,d}]$$

25%

$$d_{n,p}[d_W]$$

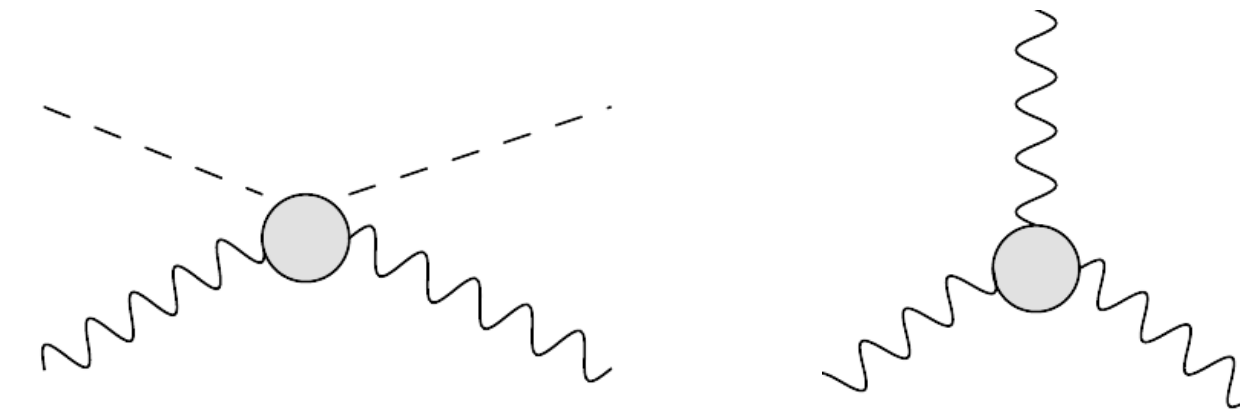
50%

Target for Lattice QCD

- Experiment at 5×10^{-27} e cm and improved matrix elements would make nEDM the strongest probe

Higgs-gauge CPV couplings

- Dominant sources of CPV (together with VVV) in so-called *universal theories*

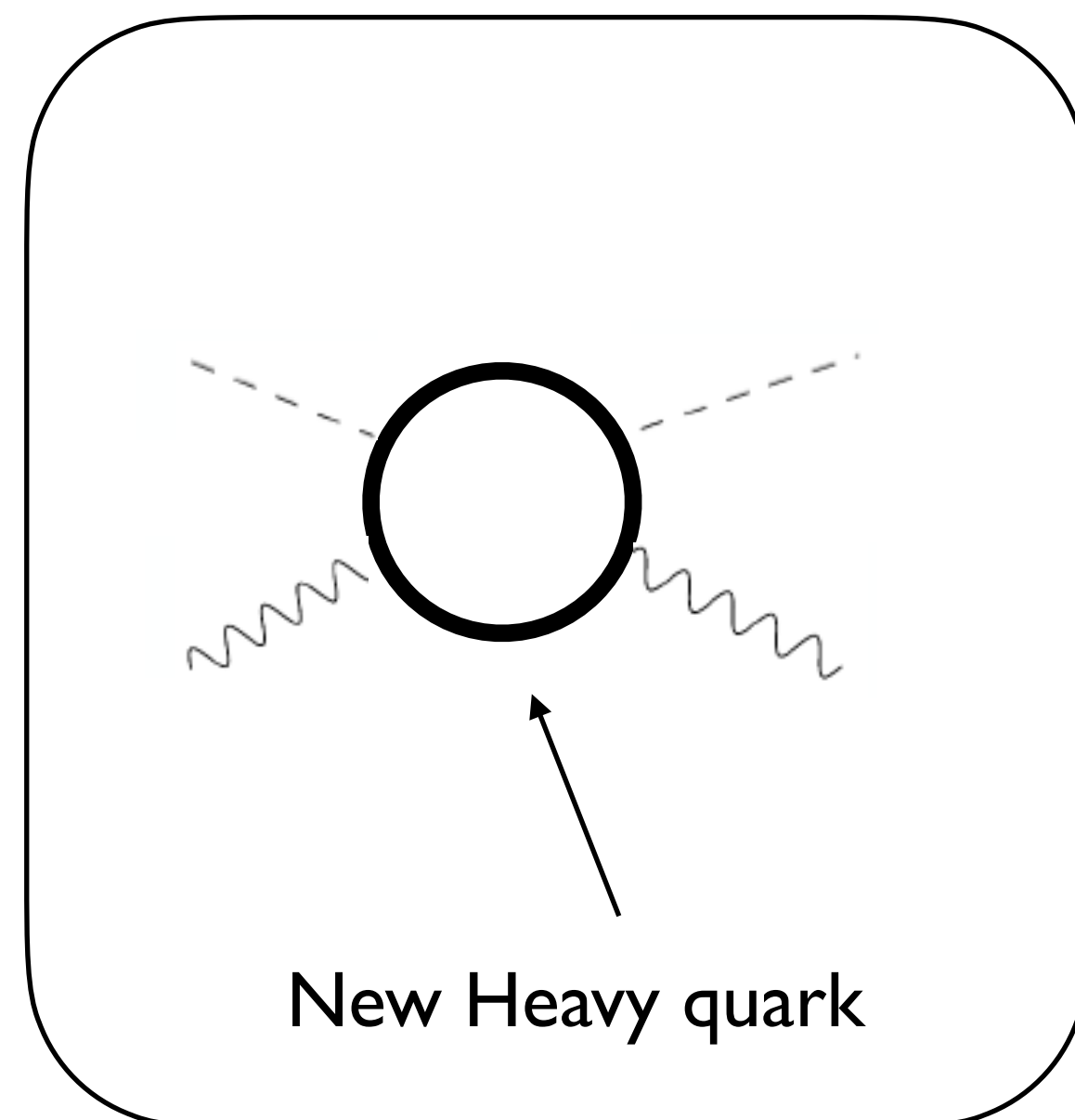


Peskin-Takeuchi, PRL 65, 964 (1990)

Barbieri-Pomarol-Rattazzi-Strumia hep-ph/0405040

Wells-Zhang, 1510.08462

Example



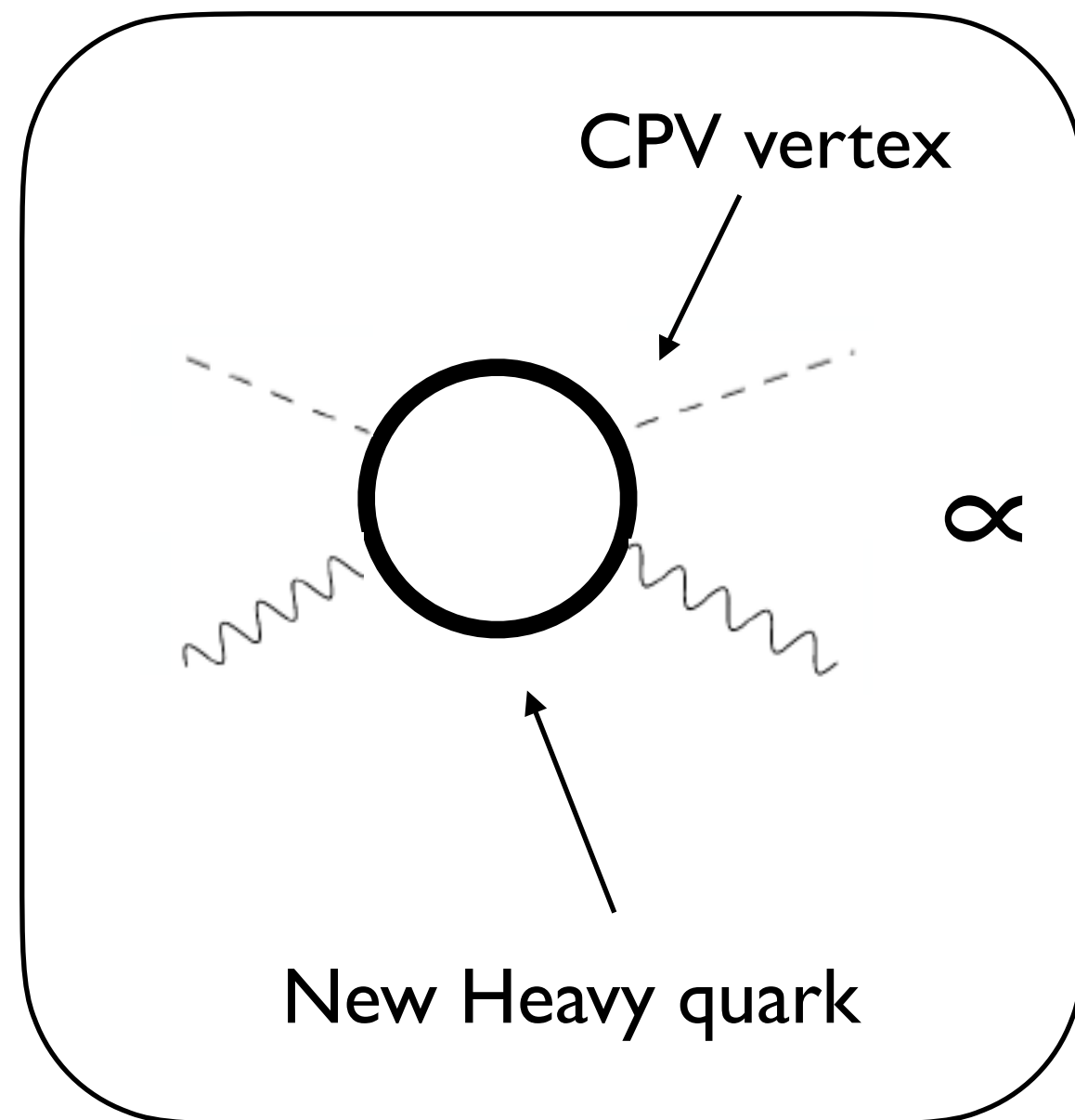
“Universal theories”

- New physics couples only to SM bosons (and to fermions through gauge currents)
- Consistent framework to analyze EW precision tests (oblique corrections, etc)
- Evade flavor constraints, scale can be low

Higgs-gauge CPV couplings

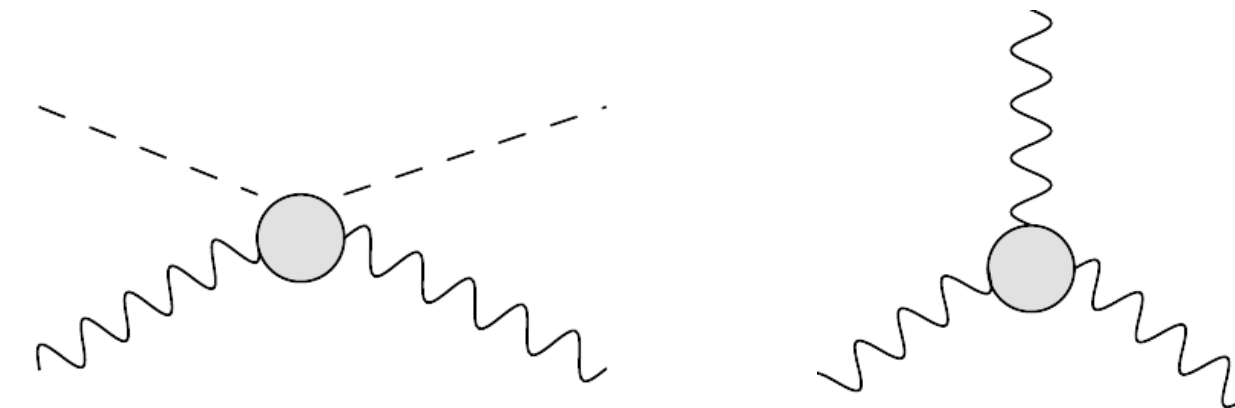
- Dominant sources of CPV (together with VVV) in so-called *universal theories*

Peskin-Takeuchi, PRL 65, 964 (1990)
 Barbieri-Pomarol-Rattazzi-Strumia hep-ph/0405040
 Wells-Zhang, 1510.08462



$$\propto F_{\mu\nu} \tilde{F}^{\mu\nu} \sim \mathbf{E} \cdot \mathbf{B}$$

Ferreira-Fuks-Sanz-Sengupta
 Eur. Phys. J. C (2017) 77:675



H-H-V- \tilde{V}

V-V- \tilde{V}

$$\uparrow v^2 C_{\varphi\tilde{B}}$$

$$\uparrow v^2 C_{\tilde{W}}$$

$$v^2 C_{\tilde{G}}$$

$$v^2 C_{\varphi\tilde{W}}$$

$$v^2 C_{\varphi\tilde{W}B}$$

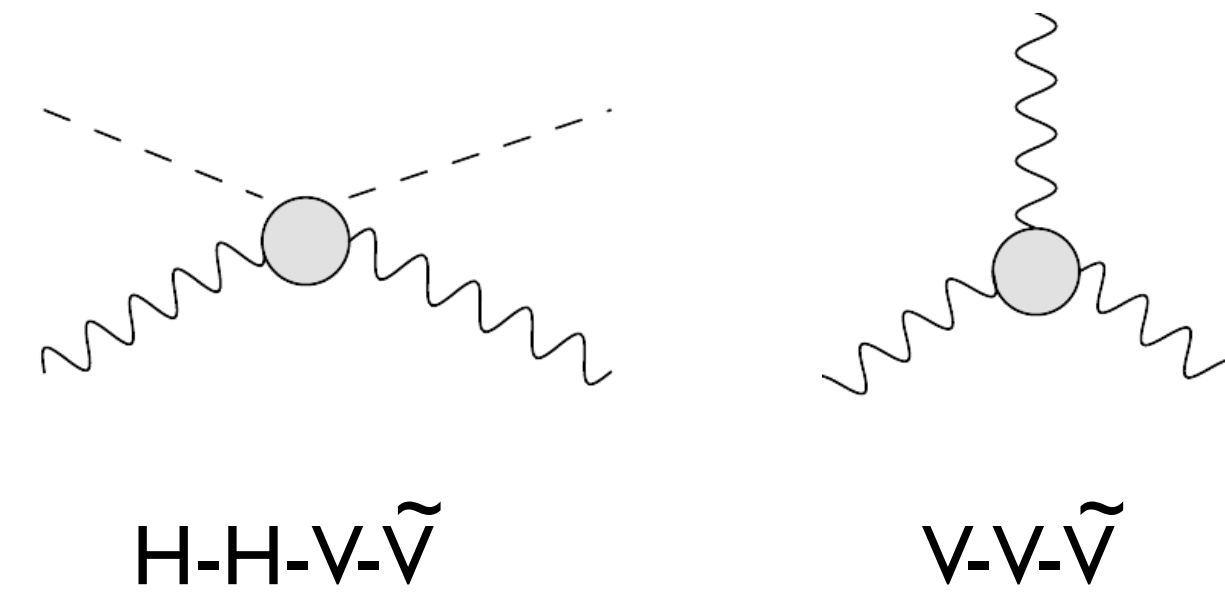
$$v^2 C_{\varphi\tilde{G}}$$

Six CPV couplings at $O(1/\Lambda^2)$

Higgs-gauge CPV couplings

- Dominant sources of CPV (together with VVV) in so-called *universal theories*

Peskin-Takeuchi, PRL 65, 964 (1990)
 Barbieri-Pomarol-Rattazzi-Strumia hep-ph/0405040
 Wells-Zhang, 1510.08462



- Induce CPV angular distributions in $pp \rightarrow h + 2 \text{ jets}, pp \rightarrow V + 2 \text{ jets}, \dots$



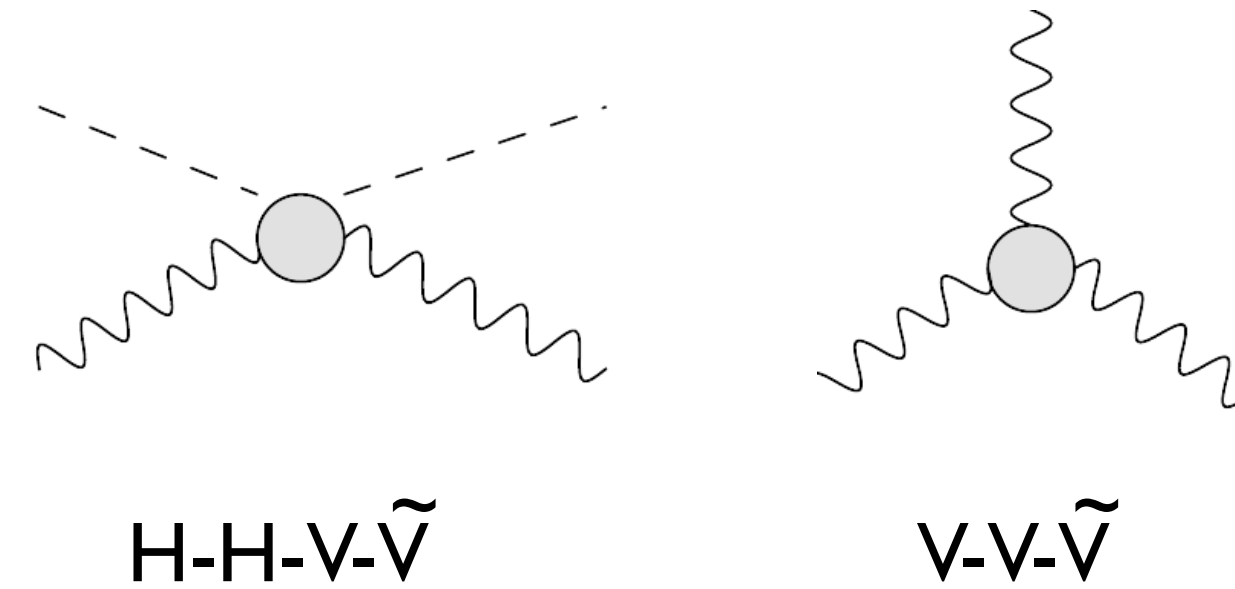
Angular distribution of the two jets ($\Delta\Phi_{jj}$) contains information about CP structure of the VVh vertex.

Triple products of momenta appear, e.g. $\mathbf{p} \cdot (\mathbf{q} \times \mathbf{k})$

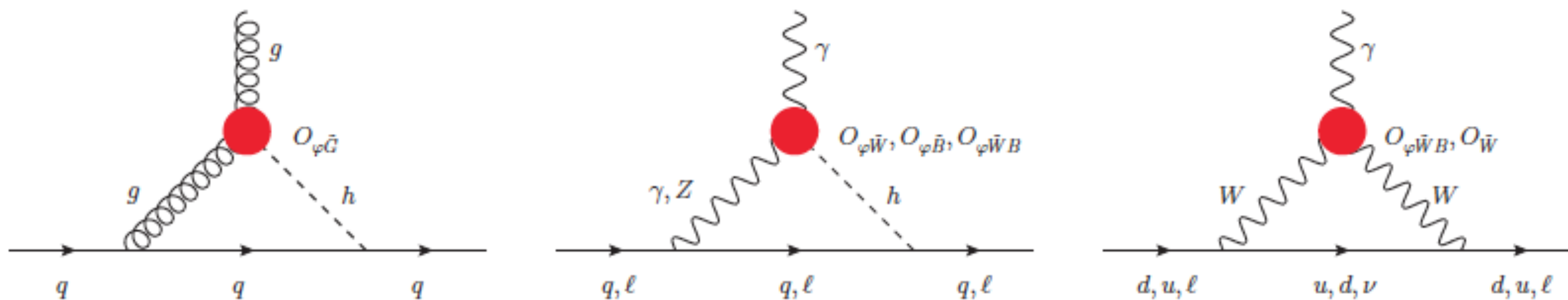
Higgs-gauge CPV couplings

- Dominant sources of CPV (together with VVV) in so-called *universal theories*

Peskin-Takeuchi, PRL 65, 964 (1990)
 Barbieri-Pomarol-Rattazzi-Strumia hep-ph/0405040
 Wells-Zhang, 1510.08462

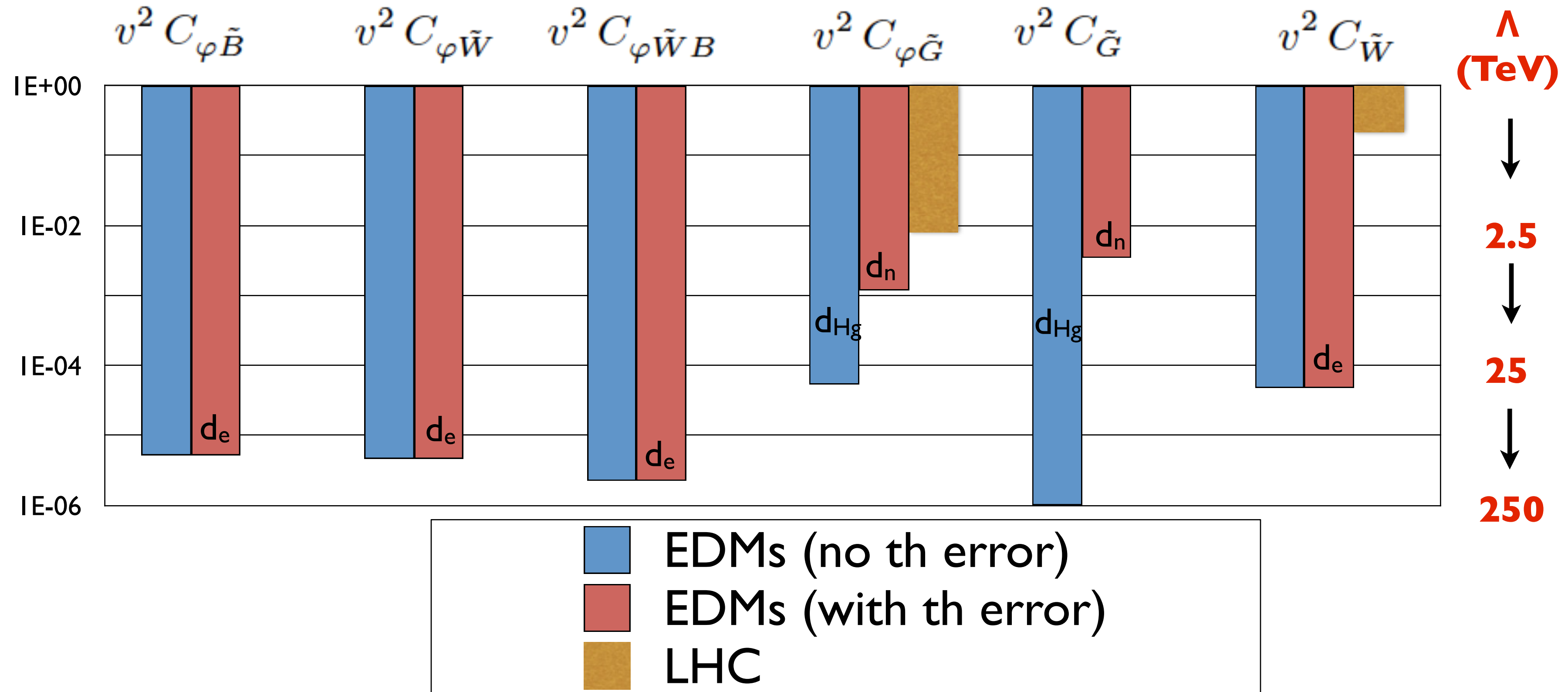


- Induce CPV angular distributions in $pp \rightarrow h + 2 \text{ jets}, pp \rightarrow V + 2 \text{ jets}, \dots$
- Induce light fermions (chromo)-EDMs at the 1-loop level



Higgs-gauge CPV couplings

- Current constraints, “turning on” one coupling at a time: EDMs vs LHC

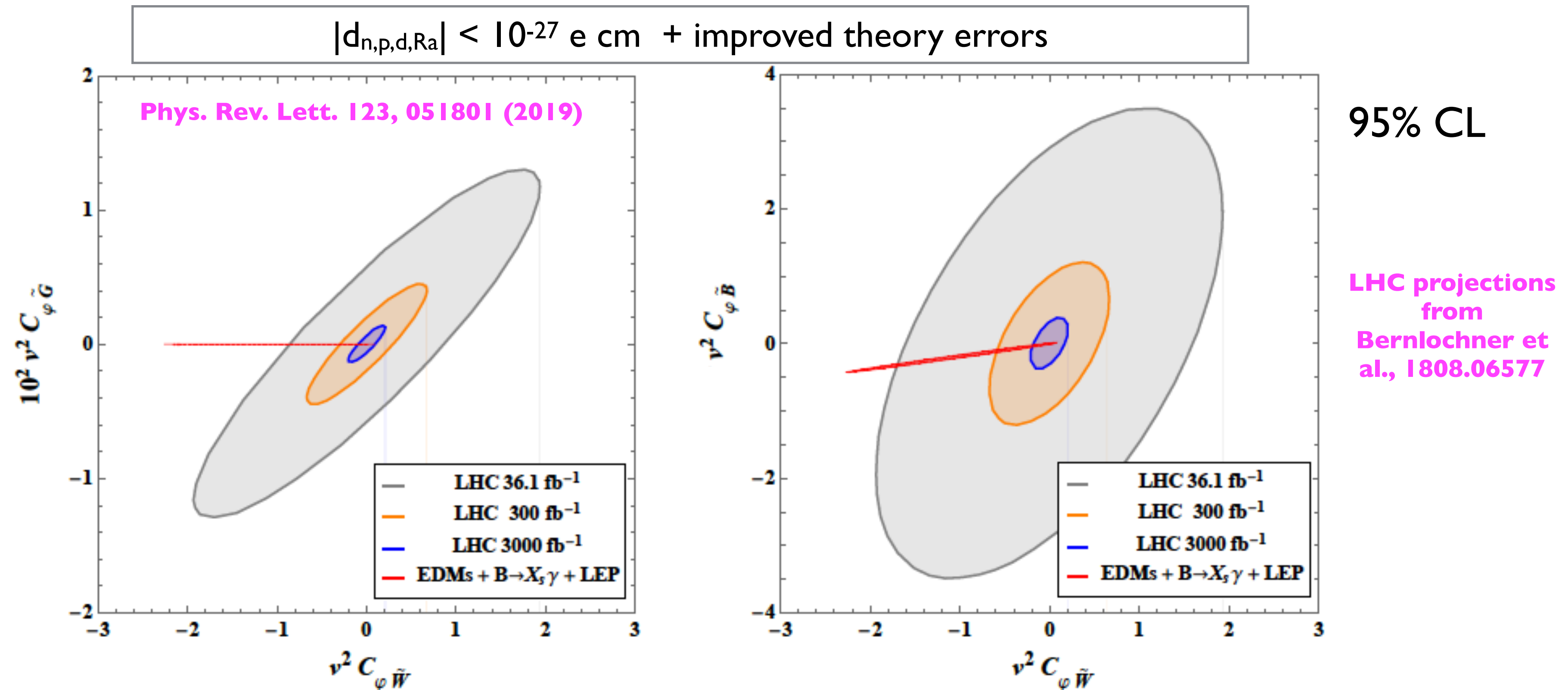


VC, A. Crivellin, W. Dekens, J. de Vries, M. Hoferichter, E. Mereghetti, 1903.03625, Phys. Rev. Lett. 123, 051801 (2019)

LHC limits from : ATLAS, 1703.04362 & Bernlochner et al., 1808.06577

Higgs-gauge CPV couplings

- Prospective constraints, turning on all couplings: low-energy vs LHC



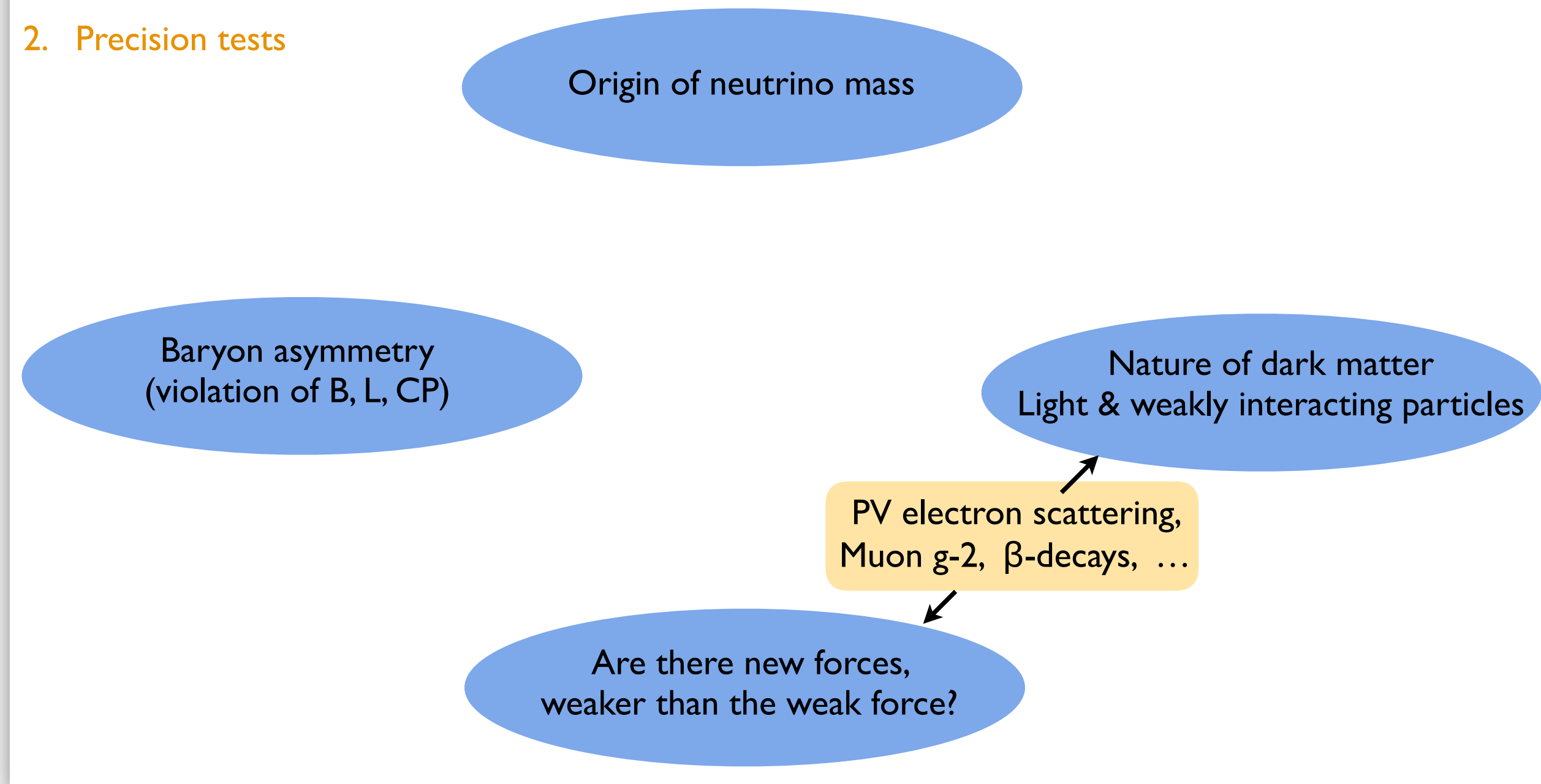
Low-energy measurements have far stronger constraining power → highly correlated allowed regions.
Distinctive pattern that could be probed at the high-luminosity LHC

Outlook on EDMs and CP violation

- Interpretation of null (for now) or positive EDM searches requires bridging scales: from BSM to hadronic, nuclear, atomic, molecular
 - Reducing theory uncertainties is essential
 - Lattice QCD can have big impact on hadronic matrix elements
 - Nuclear and atomic / molecular calculations
- EDMs are a powerful probe of new sources of CP violation
 - Stringent constraints on CPV couplings of the Higgs, much stronger than collider reach
 - More generally, **if new physics exists only at very high scale, EDMs may be among a handful of observables able to probe it**
 - Ongoing experimental searches in multiple systems, expect high sensitivity with radioactive molecules down the road

Precision tests

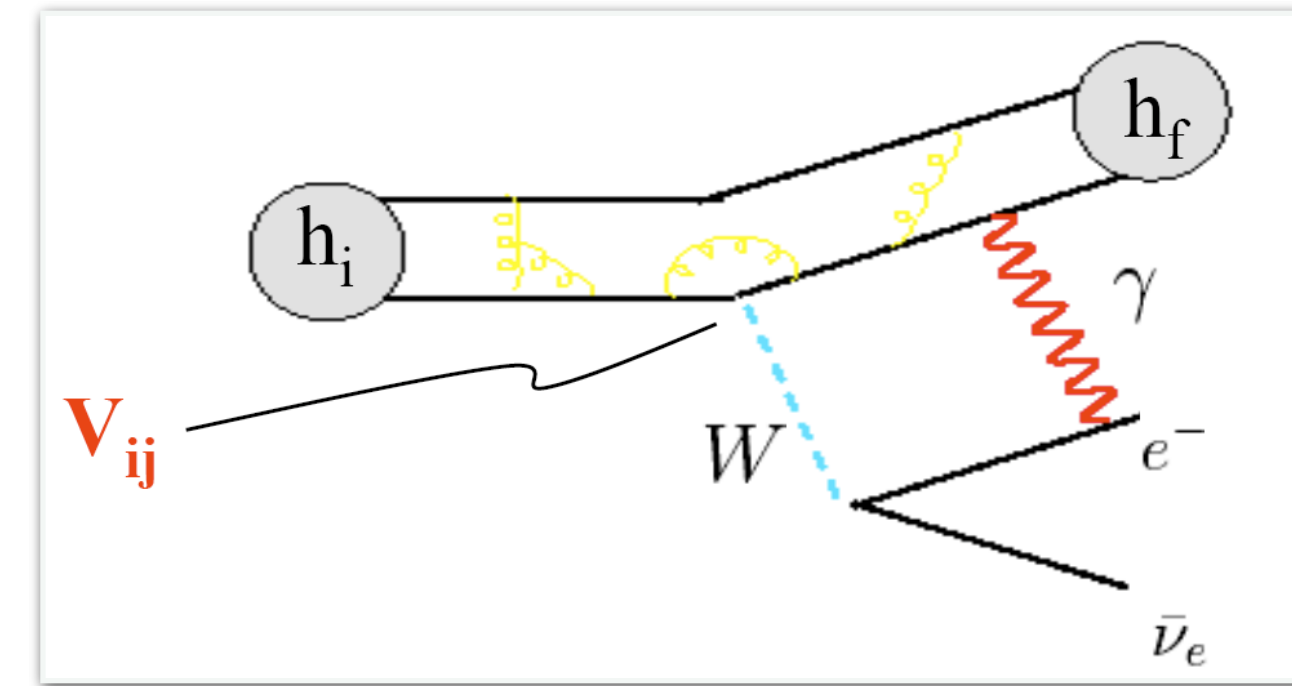
2. Precision tests



Will focus mostly on β decays

Precision tests

- **Beta decays** and **parity-violating electron scattering (PVES)** have played a central role in establishing the Standard Model



β decay

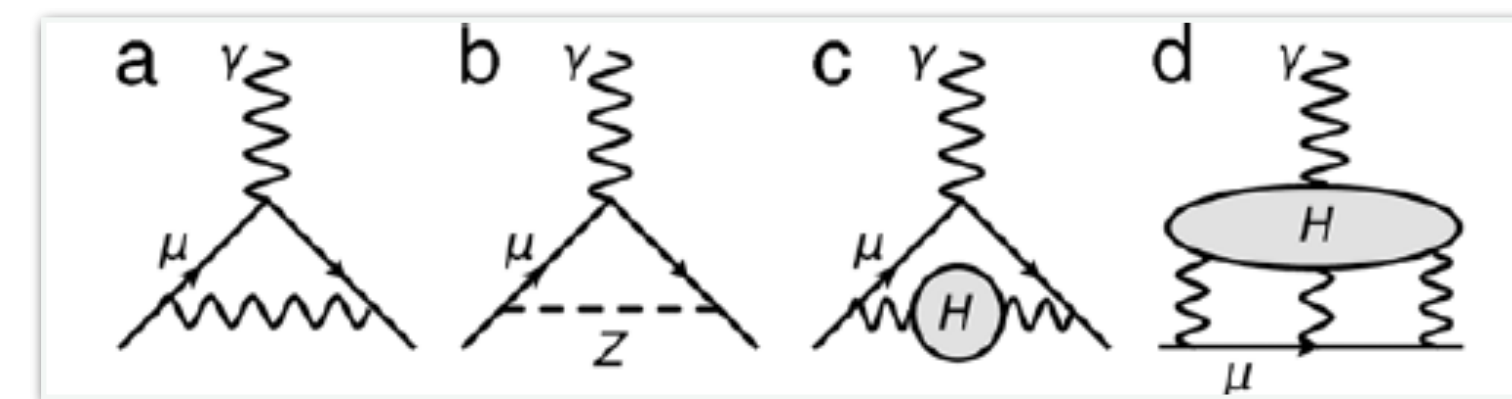
- Today, with precision approaching the 0.1% level or better (together with the **muon g-2** at the <ppm level!) they **probe quantum effects in the Standard Model at unprecedented levels**



Radiative corrections to electron scattering

- Broad sensitivity to new physics

See lectures by
D. Kawall



Representative diagrams for muon g-2

β decays in the SM and beyond

- In the SM, mediated by W exchange \Rightarrow only “V-A”; Cabibbo universality; lepton universality



$$G_F^{(\beta)} \sim G_F^{(\mu)} V_{ij} \sim 1/v^2 V_{ij}$$

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Cabibbo-Kobayashi-Maskawa

Cabibbo Universality

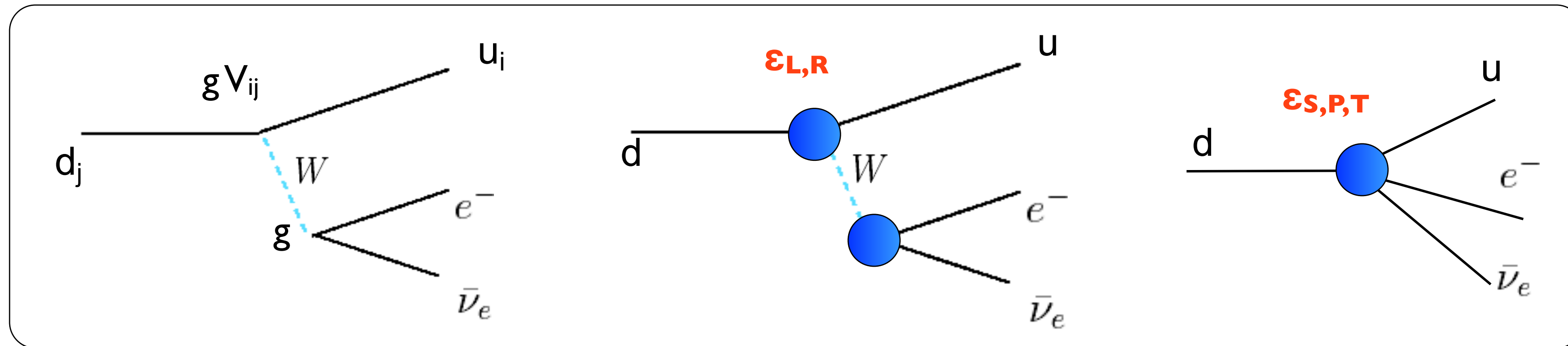
$$|V_{ud}|^2 + |V_{us}|^2 + \cancel{|V_{ub}|^2} = 1$$

$$[G_F]_e / [G_F]_\mu = 1$$

Lepton Flavor Universality (LFU)

β decays in the SM and beyond

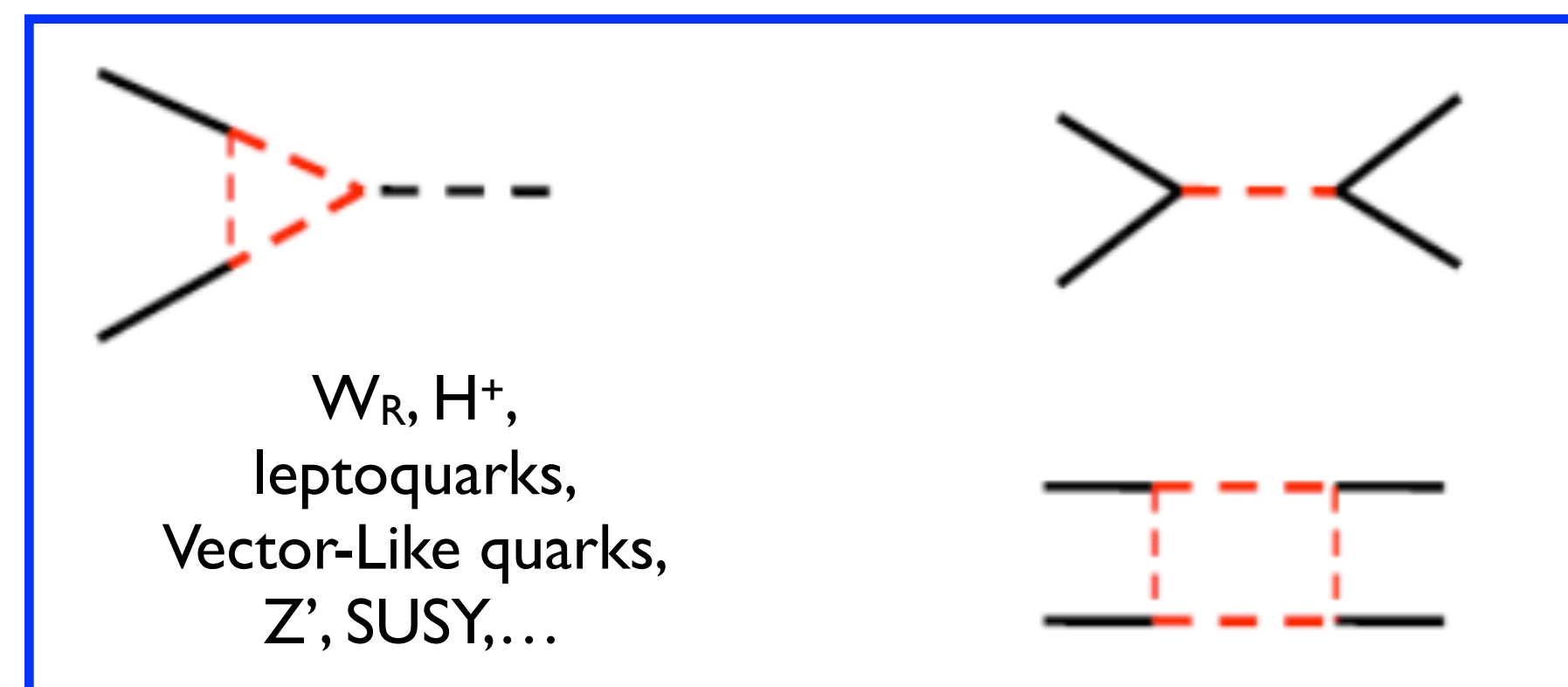
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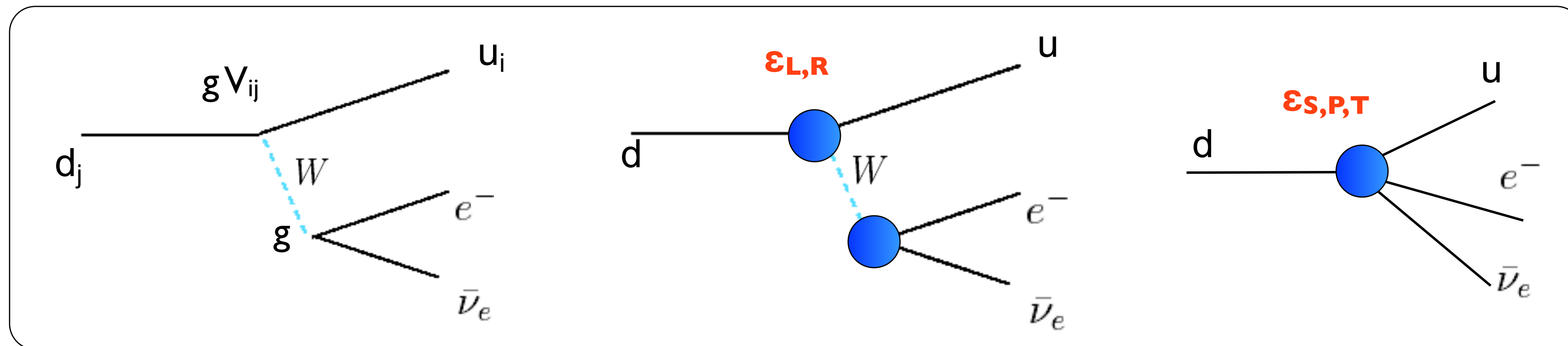
$$1/\Lambda^2$$

$$1/\Lambda^2$$



β decays in the SM and beyond

- In the SM, mediated by W exchange \Rightarrow only “V-A”; Cabibbo universality; lepton universality



$$G_F^{(\beta)} \sim G_F^{(\mu)} V_{ij} \sim 1/v^2 V_{ij}$$

$$1/\Lambda^2$$

$$1/\Lambda^2$$

$$E \ll \Lambda \quad \downarrow \quad \epsilon_\Gamma \sim \tilde{\epsilon}_\Gamma \sim (v/\Lambda)^2$$

$$\mathcal{L}_{\text{SM}} = \frac{G_F V_{ud}}{\sqrt{2}} \sum_{\Gamma} \left[\epsilon_\Gamma \bar{\ell} \Gamma \nu_L \cdot \bar{u} \Gamma d + \tilde{\epsilon}_\Gamma \bar{\ell} \Gamma \nu_R \cdot \bar{u} \Gamma d \right]$$

Ten effective couplings

$$\Gamma = L, R, S, P, T$$

- Precision of 0.1-0.01% probes $\Lambda > 10$ TeV. Several precision tests are possible....

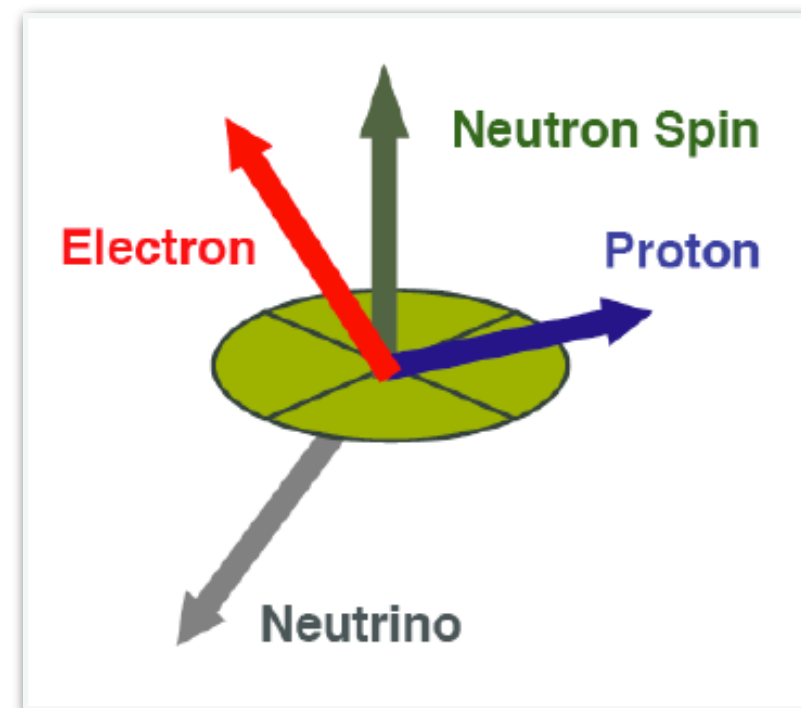
Searches for 'non V-A' currents

Measure differential decay distributions (mostly sensitive to $\varepsilon_{S,T}$)

$$d\Gamma \propto F(E_e) \left\{ 1 + b \frac{m_e}{E_e} + a \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + \langle \vec{J} \rangle \cdot \left[A \frac{\vec{p}_e}{E_e} + B \frac{\vec{p}_\nu}{E_\nu} + \dots \right] \right\}$$

Lee-Yang, 1956 Jackson-Treiman-Wyld 1957

b ($g_S \varepsilon_S, g_T \varepsilon_T$):
distortion of beta spectrum

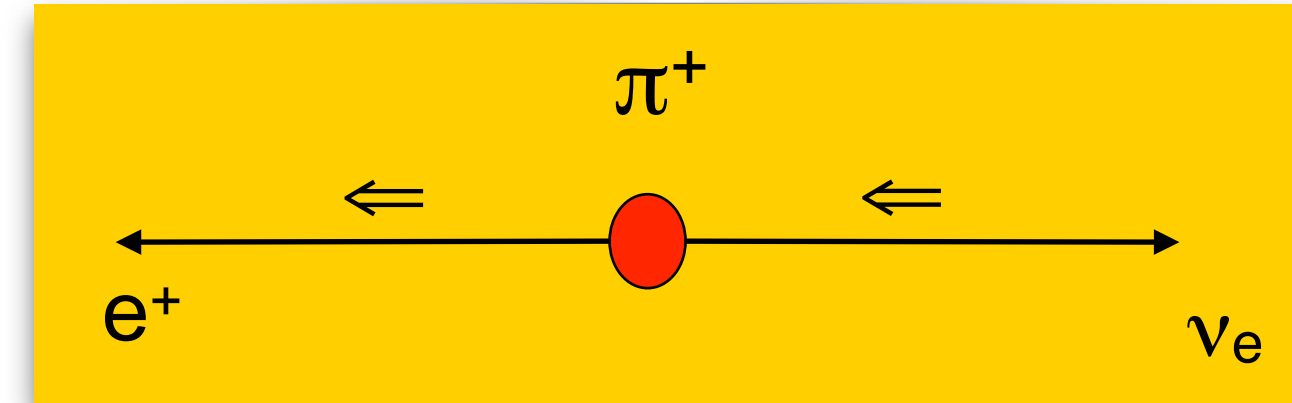


$a(g_A), A(g_A), B(g_A, g_A \varepsilon_A), \dots$
isolated via suitable experimental asymmetries

Bounds on $\varepsilon_{S,T}$ at the 0.1% level, $\Lambda \sim 5-10$ TeV

Lepton universality test with pions

- $R_{e/\mu} = \Gamma(\pi \rightarrow e\nu) / \Gamma(\pi \rightarrow \mu\nu)$ helicity suppressed the SM (V-A), zero if $m_e \rightarrow 0$



VC-Rosell 0707.3439

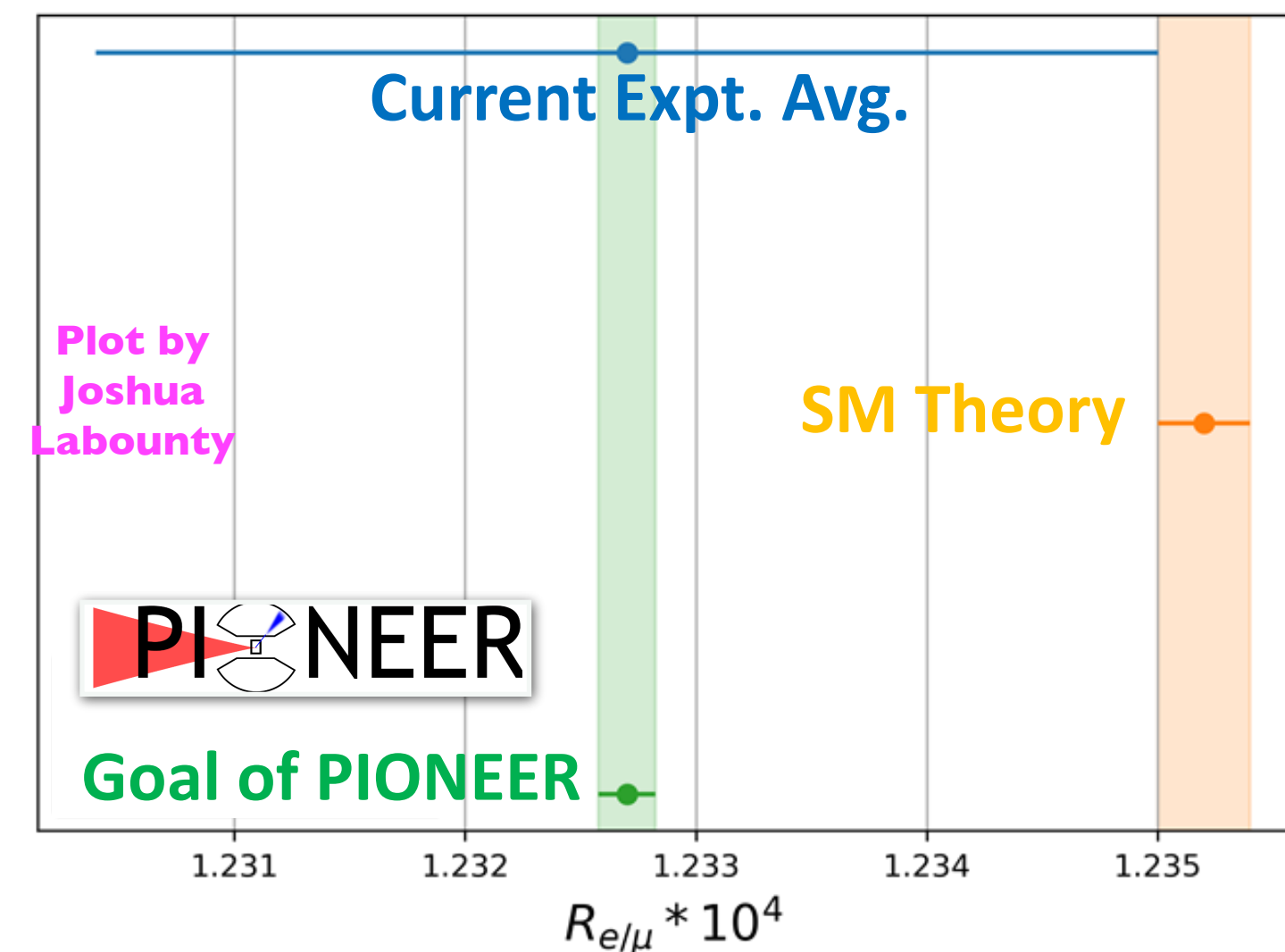
$$R_{e/\mu}(\text{SM}) = 1.23524(015) \times 10^{-4}$$

$$R_{e/\mu}(\text{Exp}) = 1.23270(230) \times 10^{-4}$$

PIENU Coll.

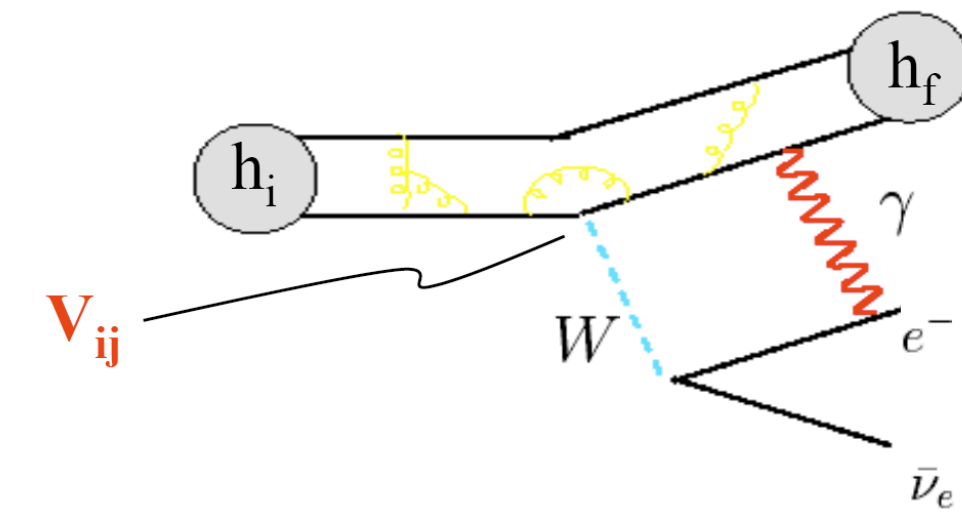
- $\sigma_{\text{exp}} \sim 15\sigma_{\text{th}} \Rightarrow$ pristine LFU test possible

- PIONEER @ PSI will match theoretical uncertainty. Order of magnitude gap — room for surprises! Will probe scales $\Lambda_A \sim 30 \text{ TeV}$ or $\Lambda_P \sim 1000 \text{ TeV}$ (helicity!)



Cabibbo universality test

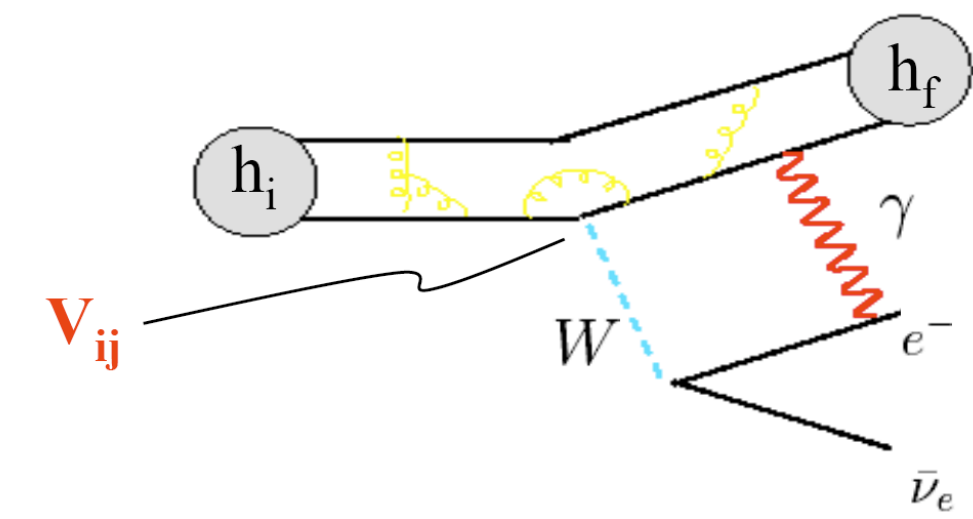
Extract $V_{us} = \sin\theta_C = \lambda$ and $V_{ud} = \cos\theta_C \simeq 1 - \lambda^2/2$
with *sub-percent precision* from decays involving hadrons
(currently $\delta\lambda/\lambda \sim 0.2\text{-}0.5\%$)



$$\Gamma = G_F^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \Delta_R) \times F_{\text{kin}}$$

Cabibbo universality test

Extract $V_{us} = \sin\theta_C = \lambda$ and $V_{ud} = \cos\theta_C \simeq 1 - \lambda^2/2$
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$$\Gamma = G_F^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \Delta_R) \times F_{\text{kin}}$$

Lifetimes,
BRs

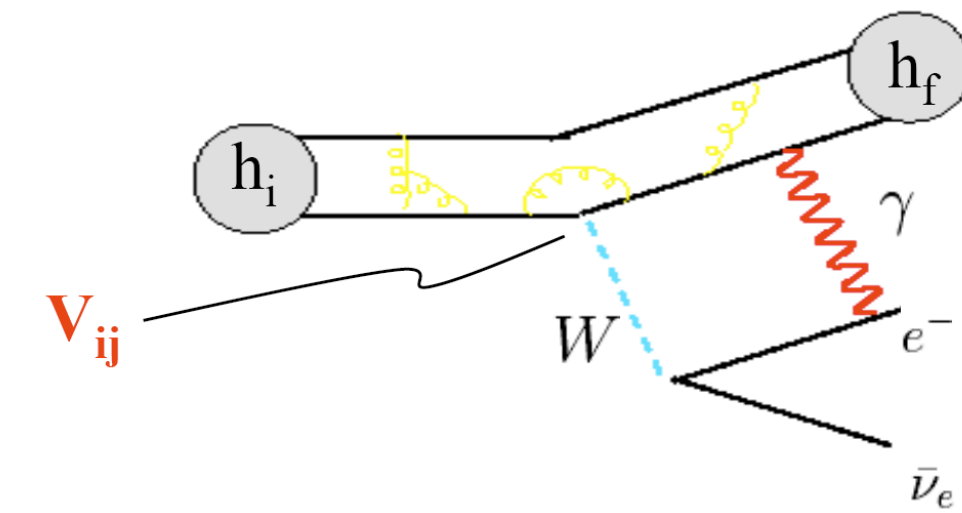
Muon
decay

Experimental input

Q-values, form
factors, ... →
phase space

Cabibbo universality test

Extract $V_{us}=\sin\theta_C=\lambda$ and $V_{ud}=\cos\theta_C \simeq 1 - \lambda^2/2$
with *sub-percent precision* from *decays involving hadrons*
(currently $\delta\lambda/\lambda \sim 0.2\text{-}0.5\%$)



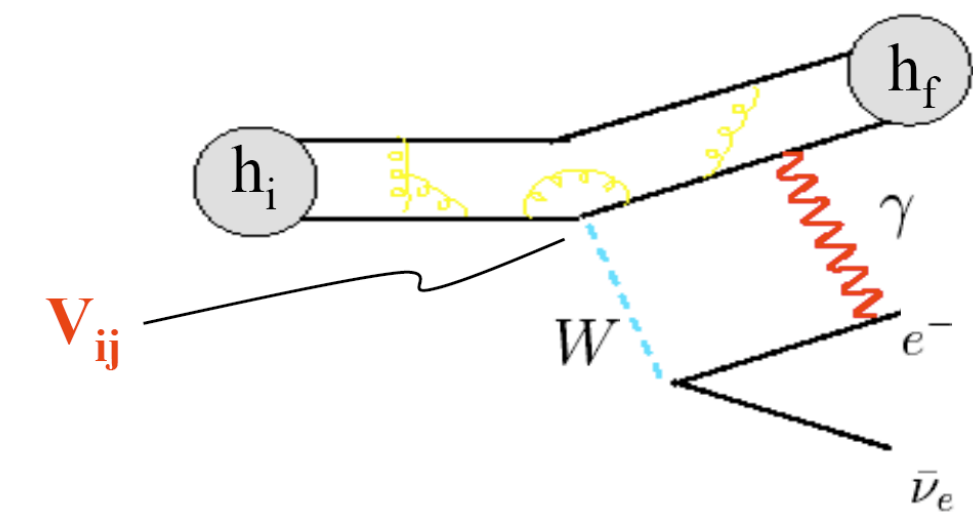
$$\Gamma = G_F^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \Delta_R) \times F_{\text{kin}}$$

Theory input

Hadronic / nuclear matrix elements of the weak V-A current,
including small corrections such as those induced by
electromagnetic radiative corrections $[(\alpha/\pi) \sim 2 \times 10^{-3}]$

Cabibbo universality test

Extract $V_{us} = \sin\theta_C = \lambda$ and $V_{ud} = \cos\theta_C \simeq 1 - \lambda^2/2$
 with *sub-percent precision* from decays involving hadrons
 (currently $\delta\lambda/\lambda \sim 0.2\text{-}0.5\%$)



$$\Gamma = G_F^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \Delta_R) \times F_{\text{kin}}$$

Channel-dependent effective
 CKM element
 (Contaminated by the BSM ε 's)

Unitarity test

$$\Delta_{\text{CKM}} \equiv |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right)$$

Paths to V_{ud} and V_{us}

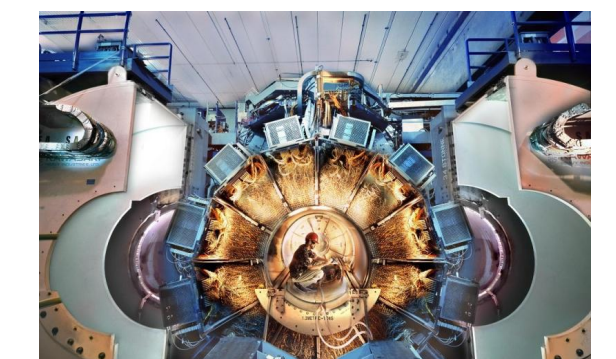
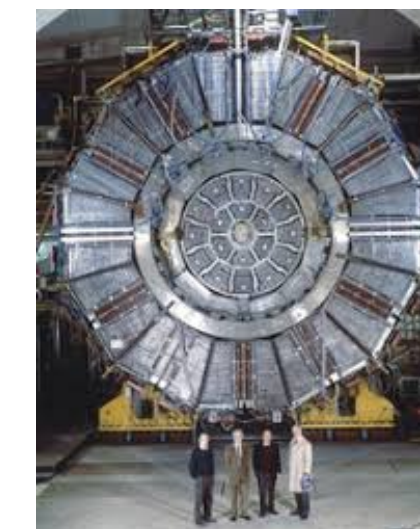
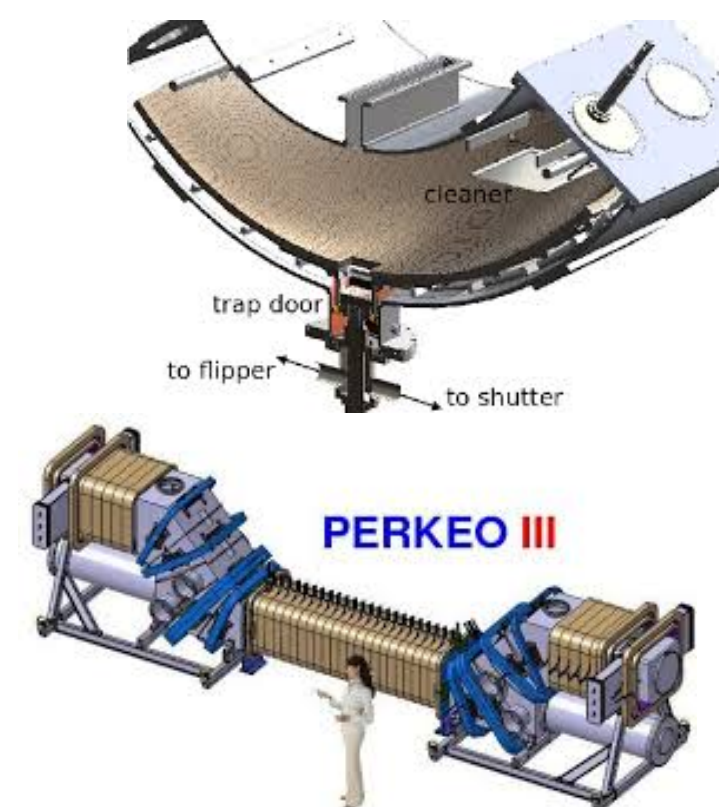
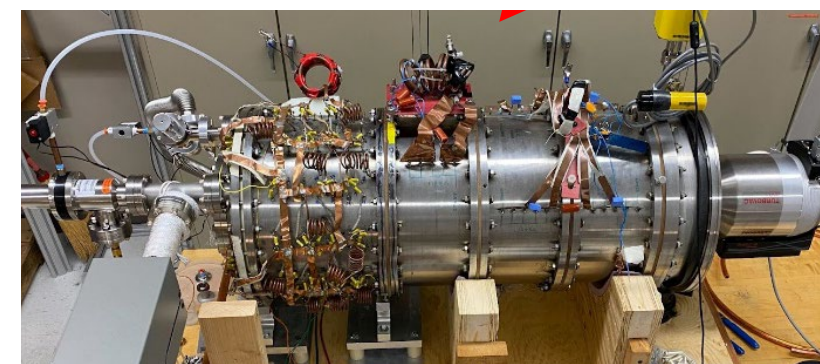
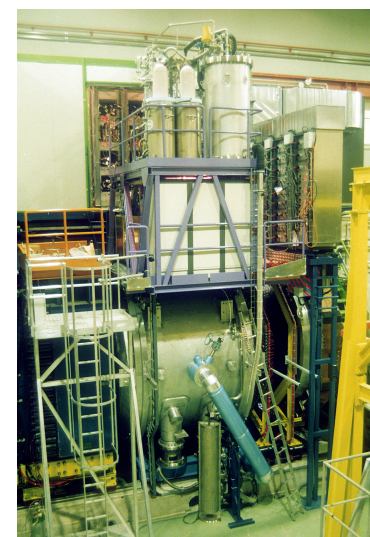
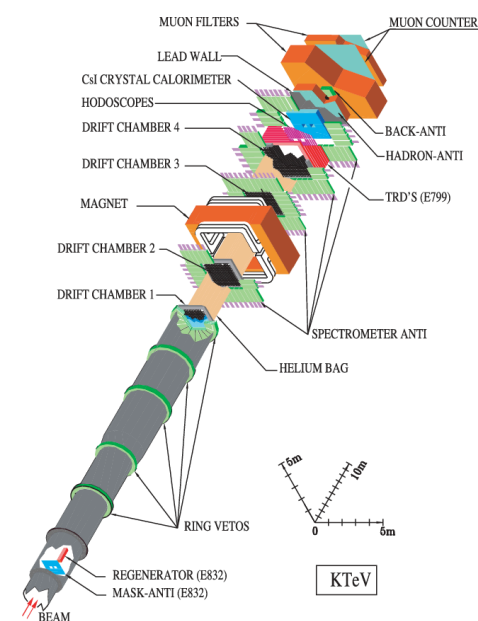
	Hadron decays			Lepton decays
V_{ud}	$\pi^\pm \rightarrow \pi^0 e \nu$ Nucl. $0^+ \rightarrow 0^+$	$n \rightarrow p e \nu$ Nucl. mirror decays	$\pi \rightarrow \mu \nu$	$\tau \rightarrow h_{NS} \nu$
V_{us}	$K \rightarrow \pi l \nu$	$\Lambda \rightarrow p e \nu, \dots$	$K \rightarrow \mu \nu$	$\tau \rightarrow h_S \nu$

Experimental input with sub-% precision from broad array of facilities and techniques

K, π , Hyperons:
Meson factories & fixed target experiments
(KLOE, KTeV, NA48, ...), with future
experiment possible at CERN and PSI

Nuclear beta decay experiments
Cold and Ultra Cold Neutron sources

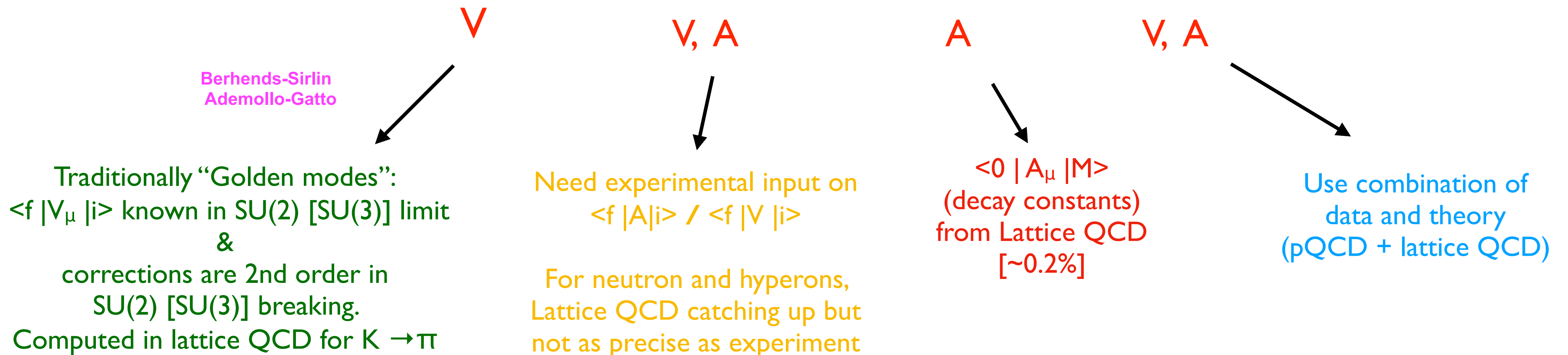
τ decays:
LEP (ALEPH, OPAL), Babar, Belle,
Belle-II, future tau-charm factory



Hadronic matrix elements

	Hadron decays			Lepton decays
V_{ud}	$\pi^\pm \rightarrow \pi^0 e \nu$ Nucl. $0^+ \rightarrow 0^+$	$n \rightarrow p e \nu$ Nucl. mirror decays	$\pi \rightarrow \mu \nu$	$\tau \rightarrow h_{NS} \nu$
V_{us}	$K \rightarrow \pi l \nu$	$\Lambda \rightarrow p e \nu, \dots$	$K \rightarrow \mu \nu$	$\tau \rightarrow h_S \nu$

Hadronic matrix elements: 'Vector - Axial' quark current



Radiative corrections

	Hadron decays			Lepton decays
V_{ud}	$\pi^\pm \rightarrow \pi^0 e \nu$ Nucl. $0^+ \rightarrow 0^+$	$n \rightarrow p e \nu$ Nucl. mirror decays	$\pi \rightarrow \mu \nu$	$\tau \rightarrow h_{NS} \nu$
V_{us}	$K \rightarrow \pi l \nu$	$\Lambda \rightarrow p e \nu, \dots$	$K \rightarrow \mu \nu$	$\tau \rightarrow h_S \nu$

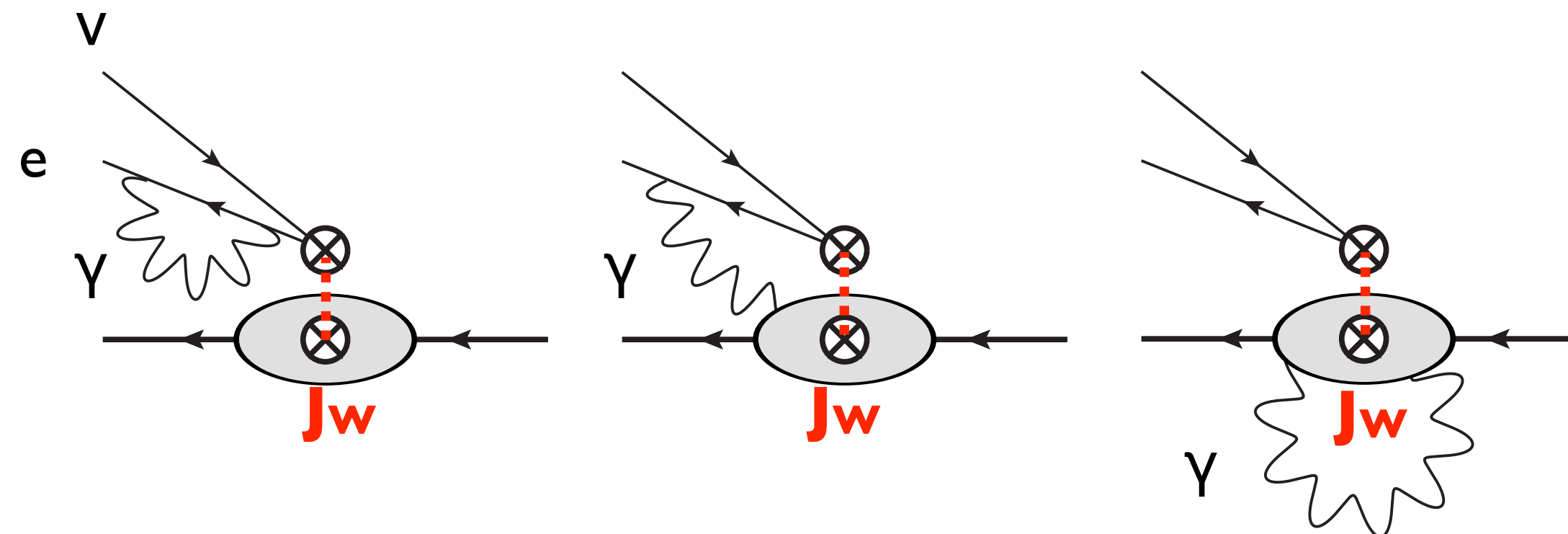
Electroweak radiative corrections

Mesons and neutron:
 well developed Effective Field Theory (EFT) framework, with non-perturbative input from lattice QCD and / or dispersive methods — systematically improvable

For leptonic K and π decays:
 full lattice QCD+QED available

Recent activity to assess nuclear structure uncertainties:
 Dispersive & EFT approaches to $O(G_F \alpha)$ recently developed.

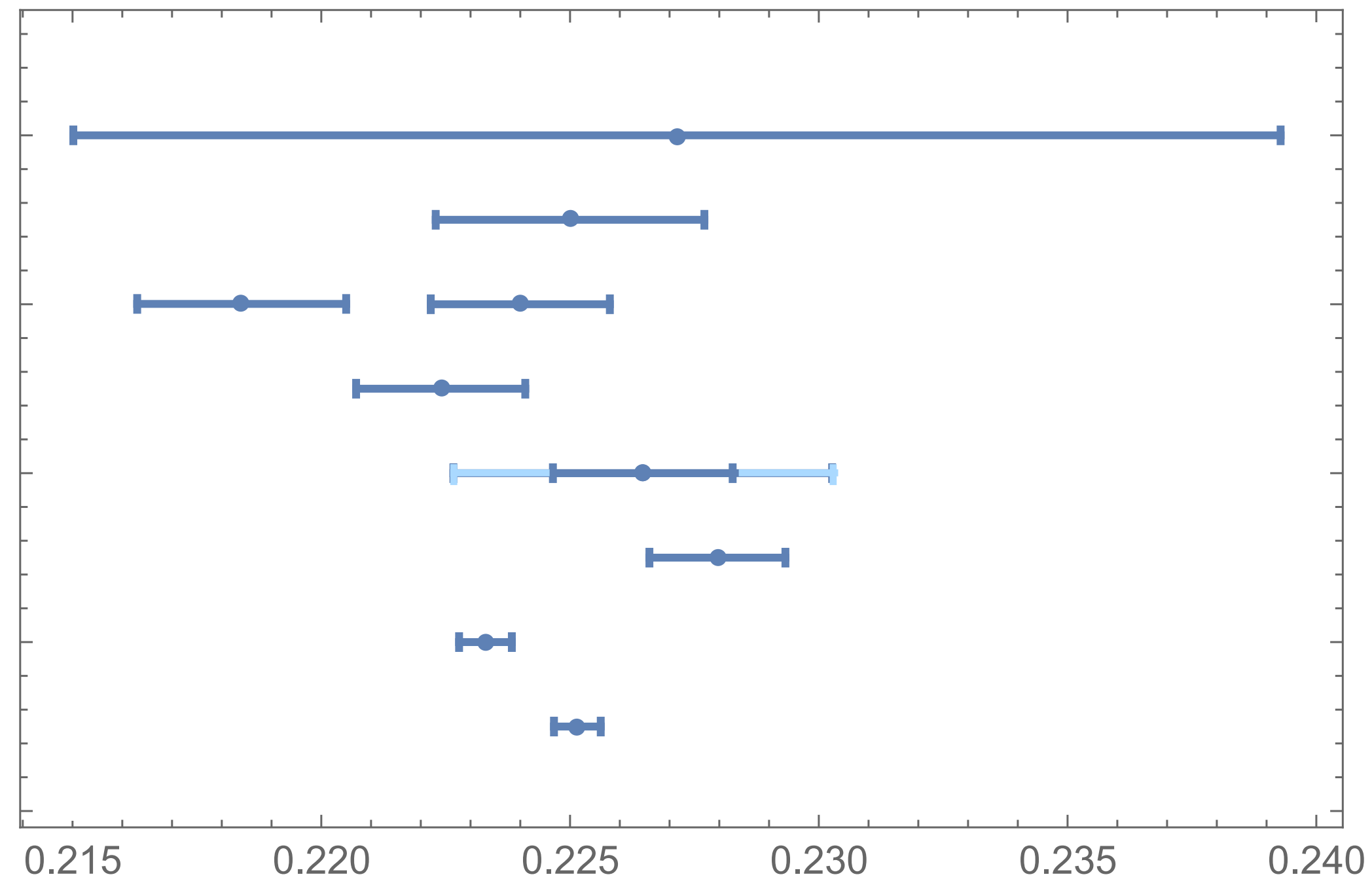
For exclusive channels, difficult to estimate the hadronic structure-dependent effects.
 Lattice QCD+QED?



The Cabibbo angle — global view

Convert V_{ud} to V_{us} via unitarity

$\pi^\pm \rightarrow \pi^0 e \nu$
 Hyperons
 τ inclusive
 τ exclusive
 $n \rightarrow p e \nu$
 $0^+ \rightarrow 0^+$
 $K \rightarrow \pi l \nu$
 $K \rightarrow \mu \nu / \pi \rightarrow \mu \nu$



V_{us}

Fractional uncertainty

Largest uncertainty

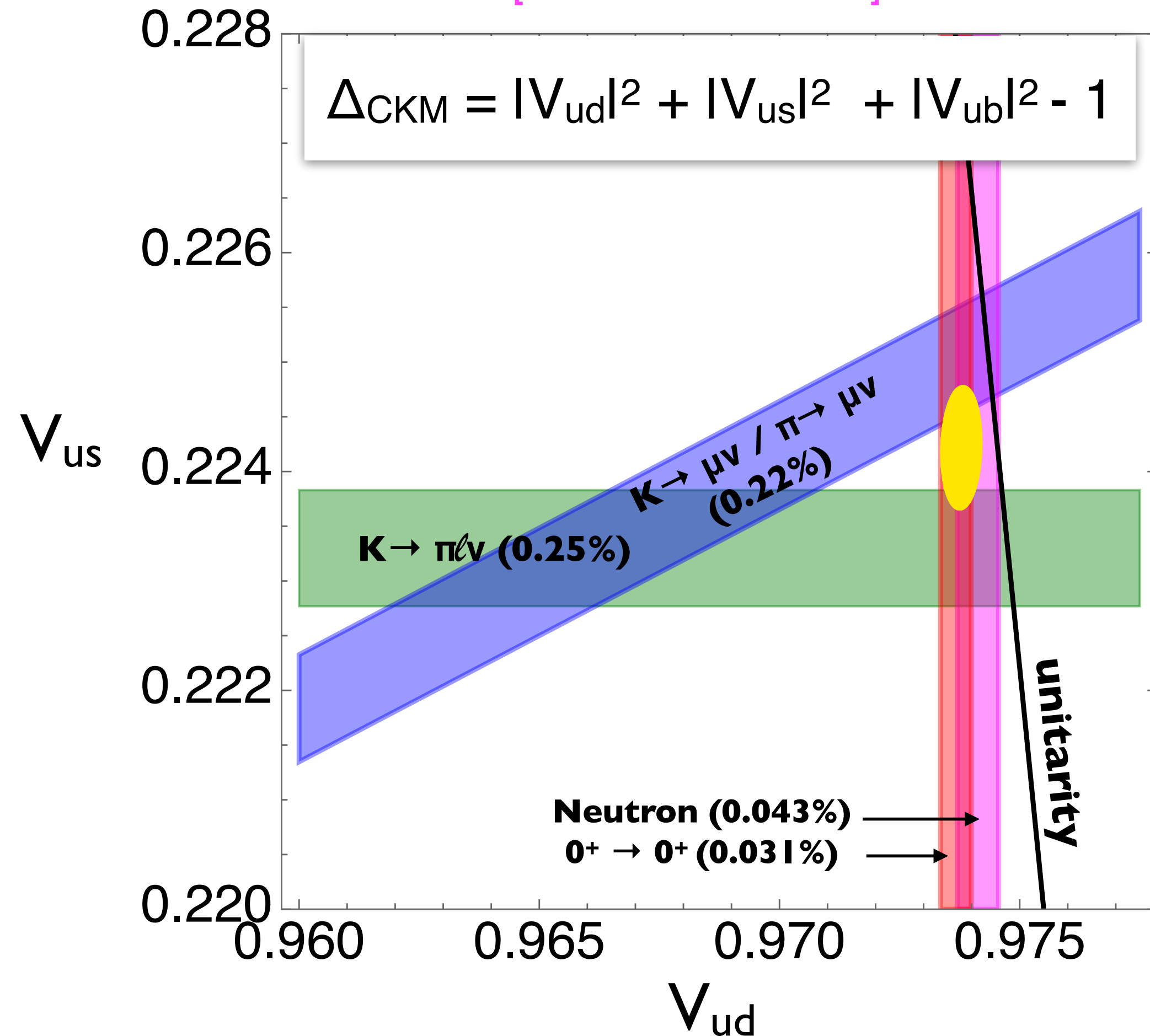
5.3%
 1.2% + ?
 0.8% + ?
 0.8% + ?
 0.8% (1.7%) (PDG)
 0.6% + ?
 0.24%
 0.21%

EXP
 EXP + TH
 EXP + TH
 EXP + TH
 EXP
 TH
 EXP + TH
 TH

Tension among the most precise determinations

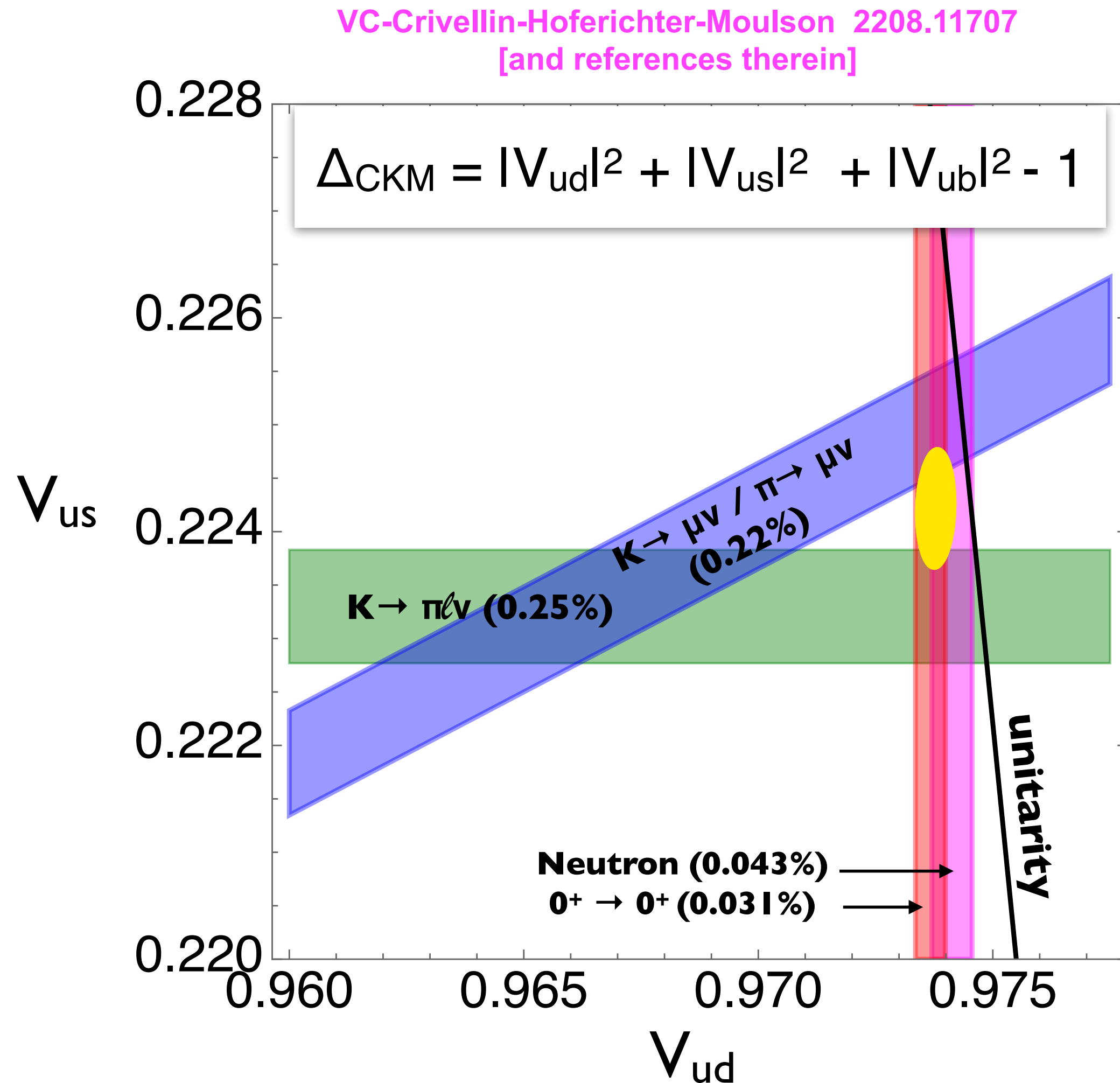
Tensions in the V_{ud} - V_{us} plane

VC-Crivellini-Hoferichter-Moulson 2208.11707
[and references therein]



- Bands don't intersect in the same region on the unitarity circle
- $\sim 3\sigma$ problem even in meson sector (Kl2 vs Kl3)
- $\sim 3\sigma$ effect in global fit ($\Delta_{\text{CKM}} = -1.48(53) \times 10^{-3}$)

Tensions in the V_{ud} - V_{us} plane

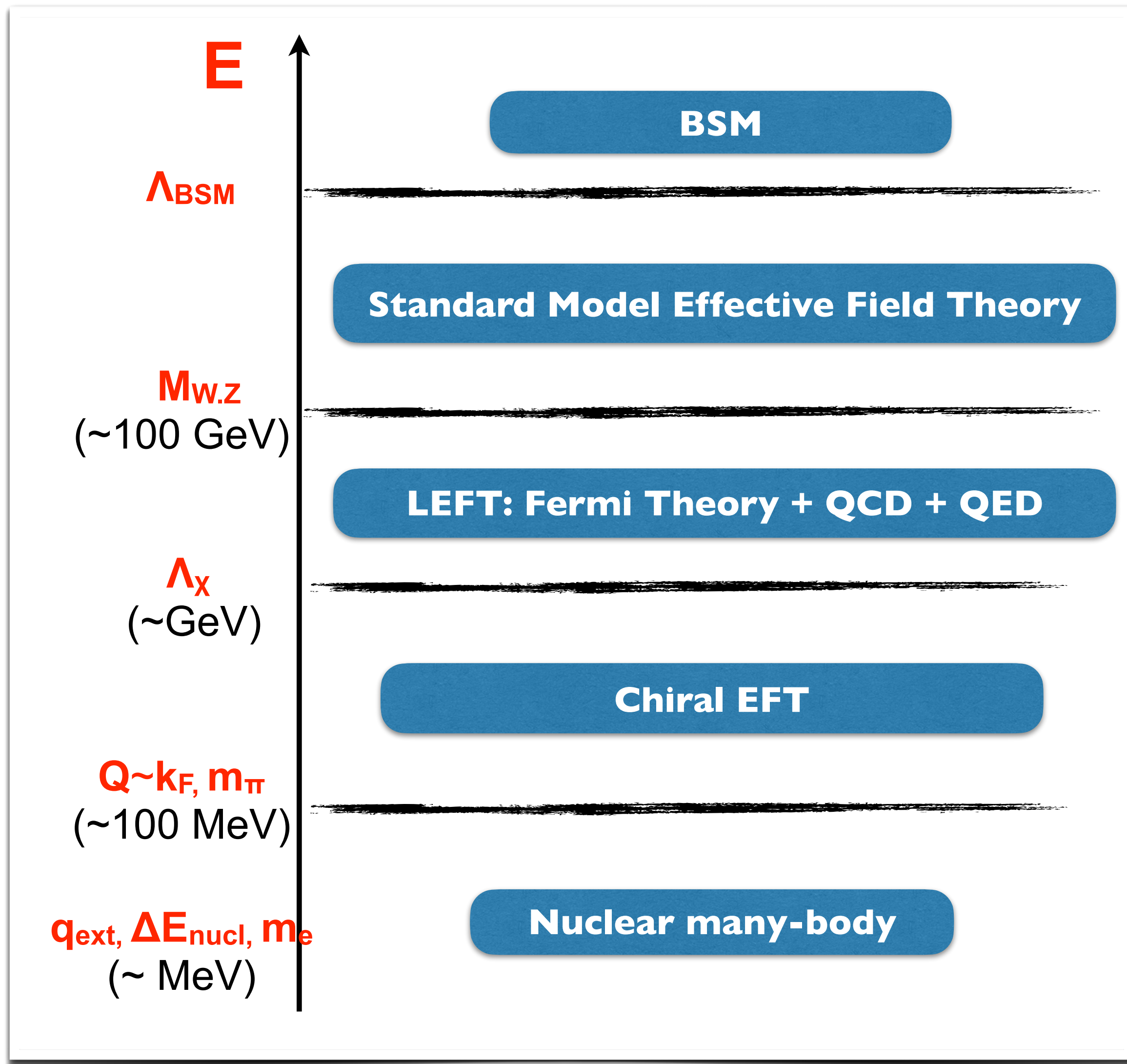


Cabibbo angle anomaly?

- **Needed / expected experimental scrutiny:**
 - neutron decay (will match nominal nuclear uncertainty)
 - pion beta decay (6x to 10x at PIONEER phases II, III)
 - new $K_{\mu 3}/K_{\mu 2}$ BR measurement at NA62
- **Theoretical scrutiny:**
 - Standard Model predictions with $\text{few} \times 10^{-4}$ precision!
 - Study possible BSM explanations that survive the constraints from other precision tests and the LHC

EFTs for β decays: from BSM to nuclei

Widely separated scales: $\Lambda_{\text{BSM}} \gg M_W \gg \Lambda_\chi \gg Q \sim k_F \sim m_\pi \gg m_e \sim q_{\text{ext}} \Rightarrow$ tower of EFTs



Single hadron (n or π)

VC, J. de Vries, L. Hayen, E. Mereghetti, A. Walker-Loud 2202.10439
 VC, W. Dekens, E. Mereghetti, O. Tomalak, 2306.03138
 Cao, Hill, Plestid, Vander Griend 2501.17916, 2508.05741
 M. Gorbahn, F. Moretti, S. Jaeger 2510.27648
 VC, M. Hoferichter, N. Valori, 2602.11253

Multi nucleons

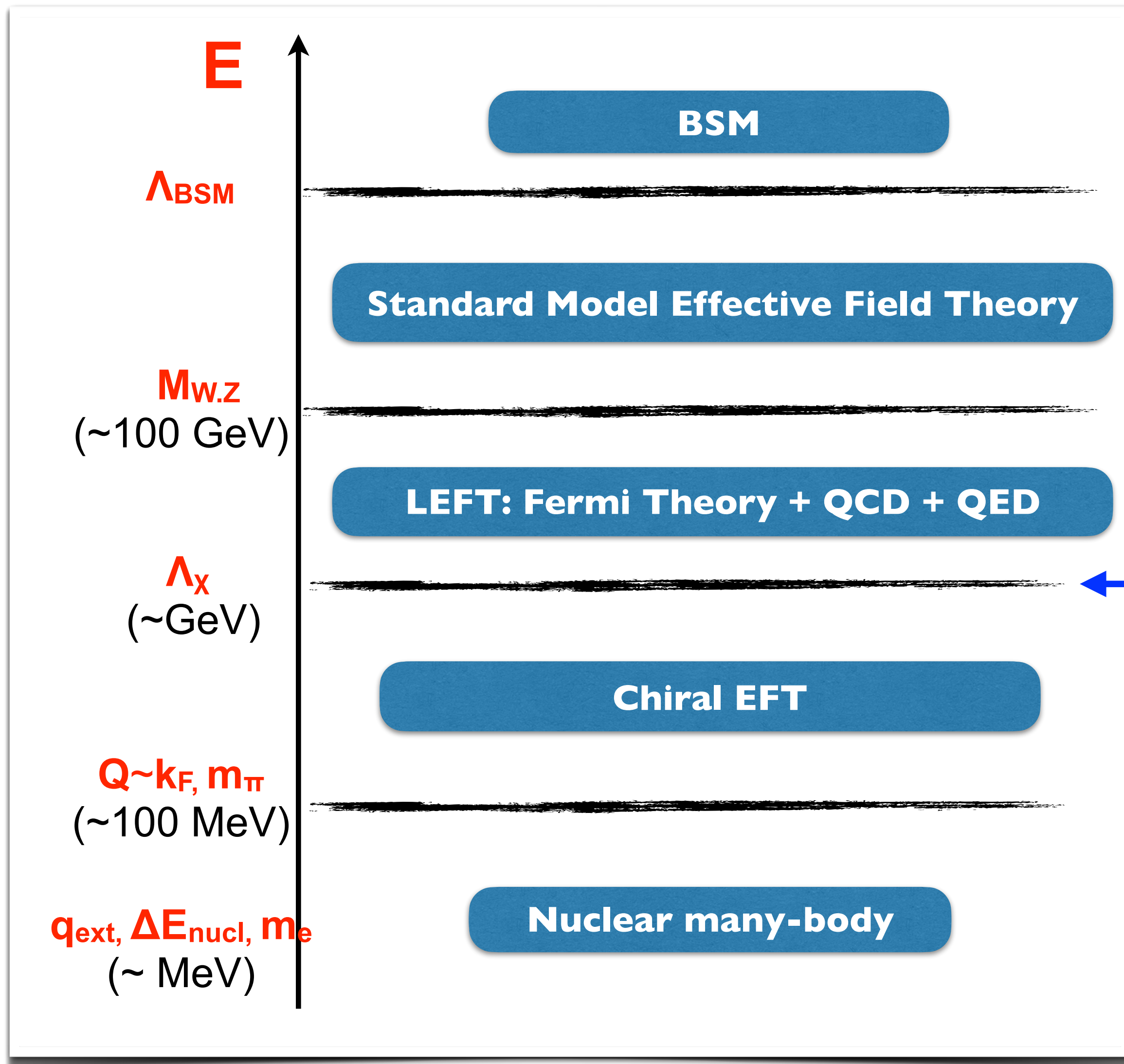
VC, W. Dekens,, J.de Vries, S. Gandolfi, M. Hoferichter, E. Mereghetti,
 2405.18469 & 2405.18464

Point-like nucleus

K. Borah, R. Hill, R. Plestid, 2309.07343, 2309.15929, 2402.13307
 Cao, Hill, Plestid, Vander Griend 2511.05446

EFTs for β decays: from BSM to nuclei

Widely separated scales: $\Lambda_{\text{BSM}} \gg M_W \gg \Lambda_\chi \gg Q \sim k_F \sim m_\pi \gg m_e \sim q_{\text{ext}} \Rightarrow$ tower of EFTs



The EFT expands amplitudes in ϵ 's and sums large logarithms $\sim \alpha^{n+m} (\ln(\epsilon))^n$

$$\epsilon_{\text{SMEFT}} = (m_W/\Lambda_{\text{BSM}})^2$$

$$\epsilon_W = (\Lambda_\chi/m_W)^2$$

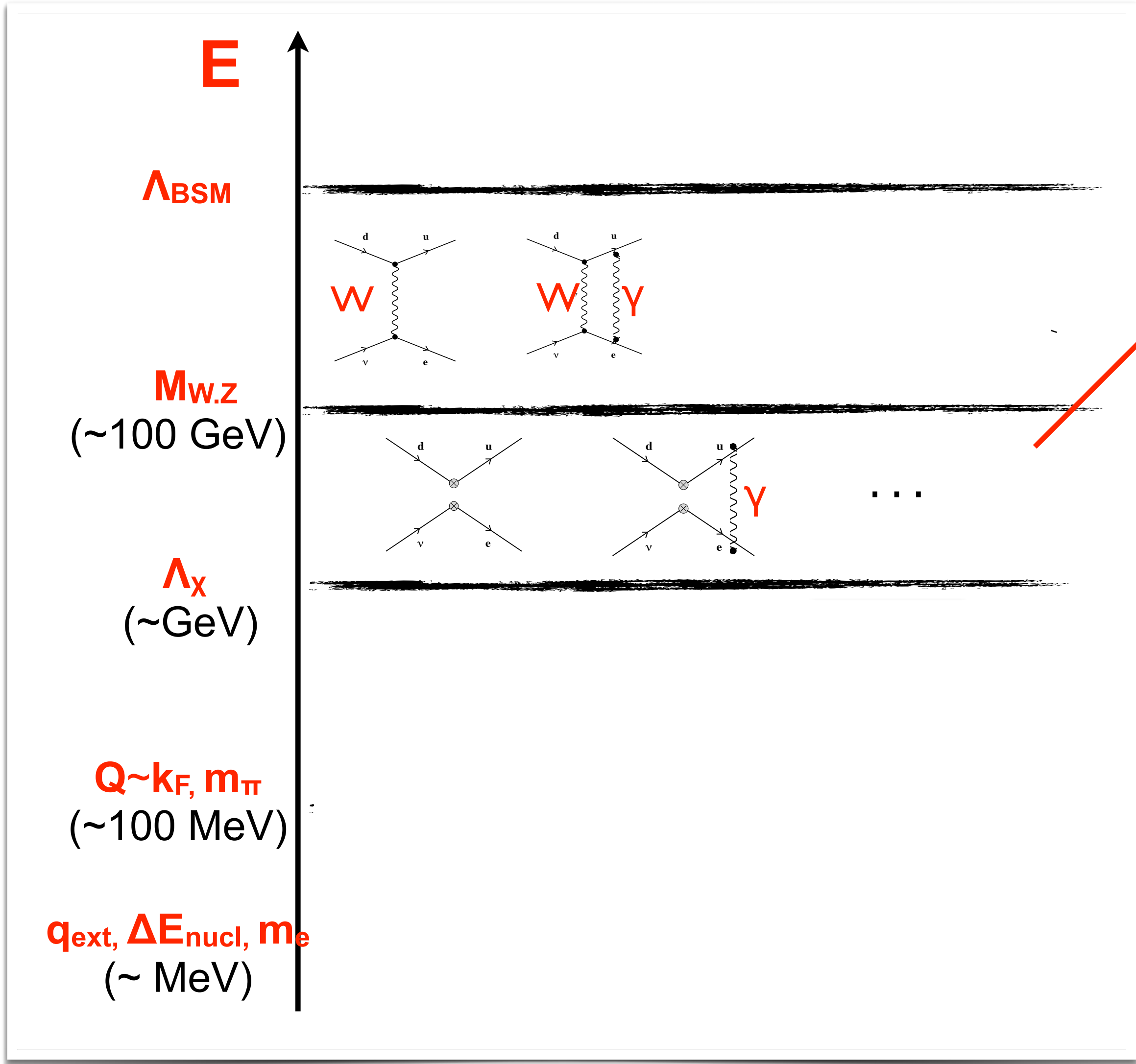
$$\epsilon_\chi = Q/\Lambda_\chi$$

$$\epsilon_\eta = q_{\text{ext}}/m_\pi$$

$$\epsilon_{\text{recoil}} = q_{\text{ext}}/\Lambda_\chi$$

Improving the SM prediction

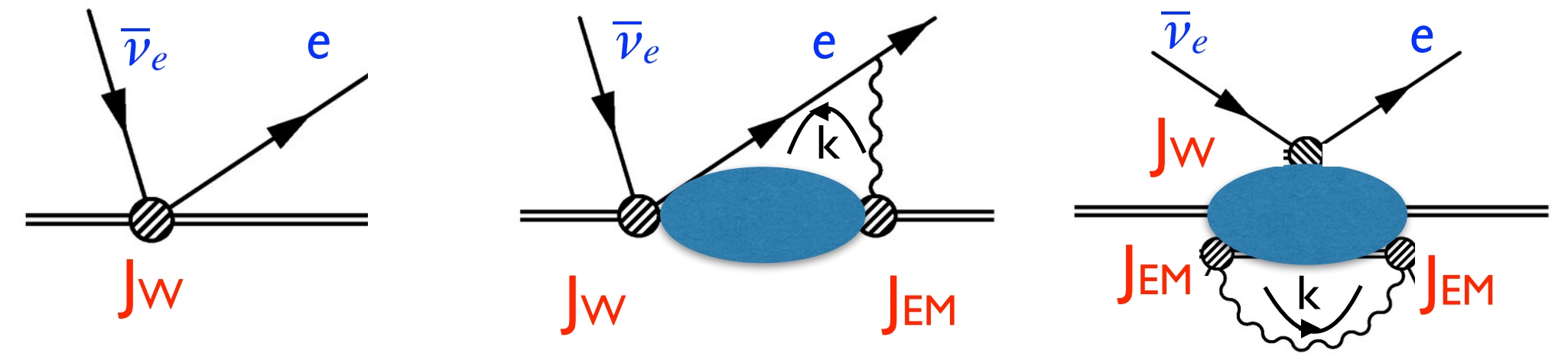
Widely separated scales: $\Lambda_{\text{BSM}} \gg M_W \gg \Lambda_\chi \gg Q \sim k_F \sim m_\pi \gg m_e \sim q_{\text{ext}} \Rightarrow$ tower of EFTs



$$\mathcal{L}_{\text{Fermi}} = -\frac{G_F}{\sqrt{2}} V_{ud} C_\beta(\mu) \bar{\ell} \gamma_\alpha (1 - \gamma_5) \nu_\ell \bar{u} \gamma^\alpha (1 - \gamma_5) d + \dots$$

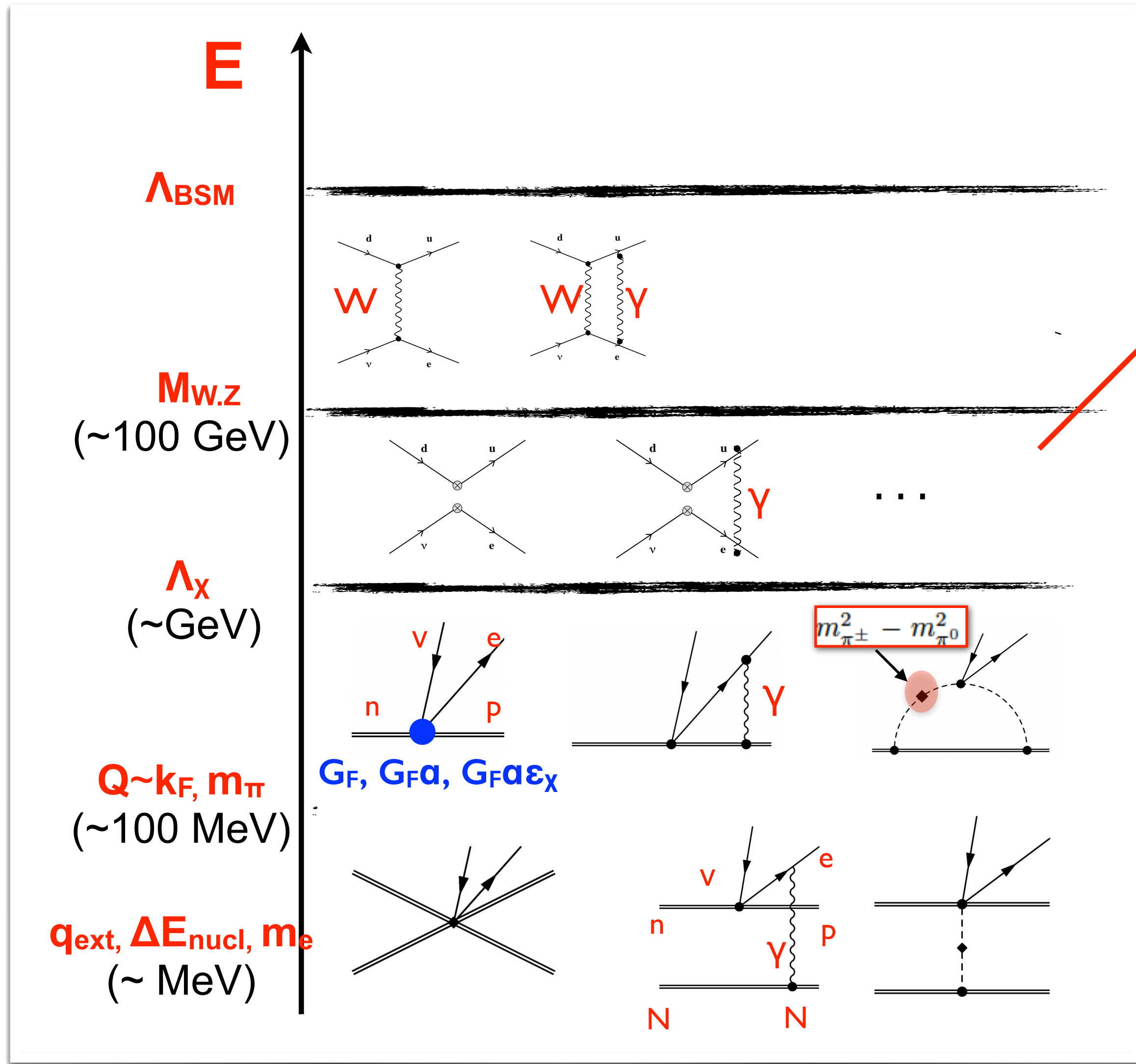
Matrix elements to $O(\alpha)$

$\langle f | \quad | i \rangle$



Improving the SM prediction

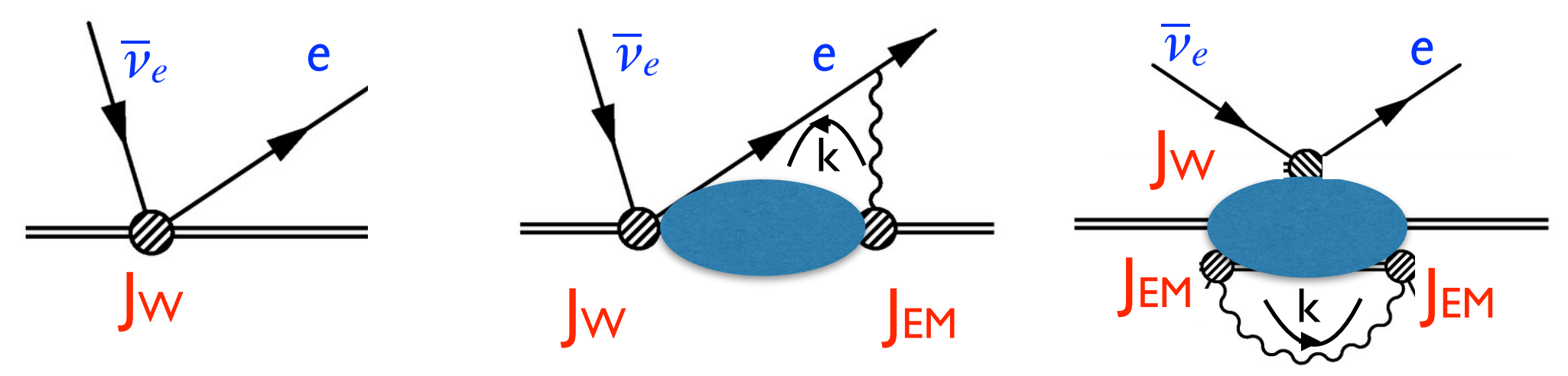
Widely separated scales: $\Lambda_{\text{BSM}} \gg M_W \gg \Lambda_\chi \gg Q \sim k_F \sim m_\pi \gg m_e \sim q_{\text{ext}} \Rightarrow$ tower of EFTs



$$\mathcal{L}_{\text{Fermi}} = -\frac{G_F}{\sqrt{2}} V_{ud} C_\beta(\mu) \bar{\ell} \gamma_\alpha (1 - \gamma_5) \nu_\ell \bar{u} \gamma^\alpha (1 - \gamma_5) d + \dots$$

Matrix elements to $O(a)$

$\langle f | \quad | i \rangle$

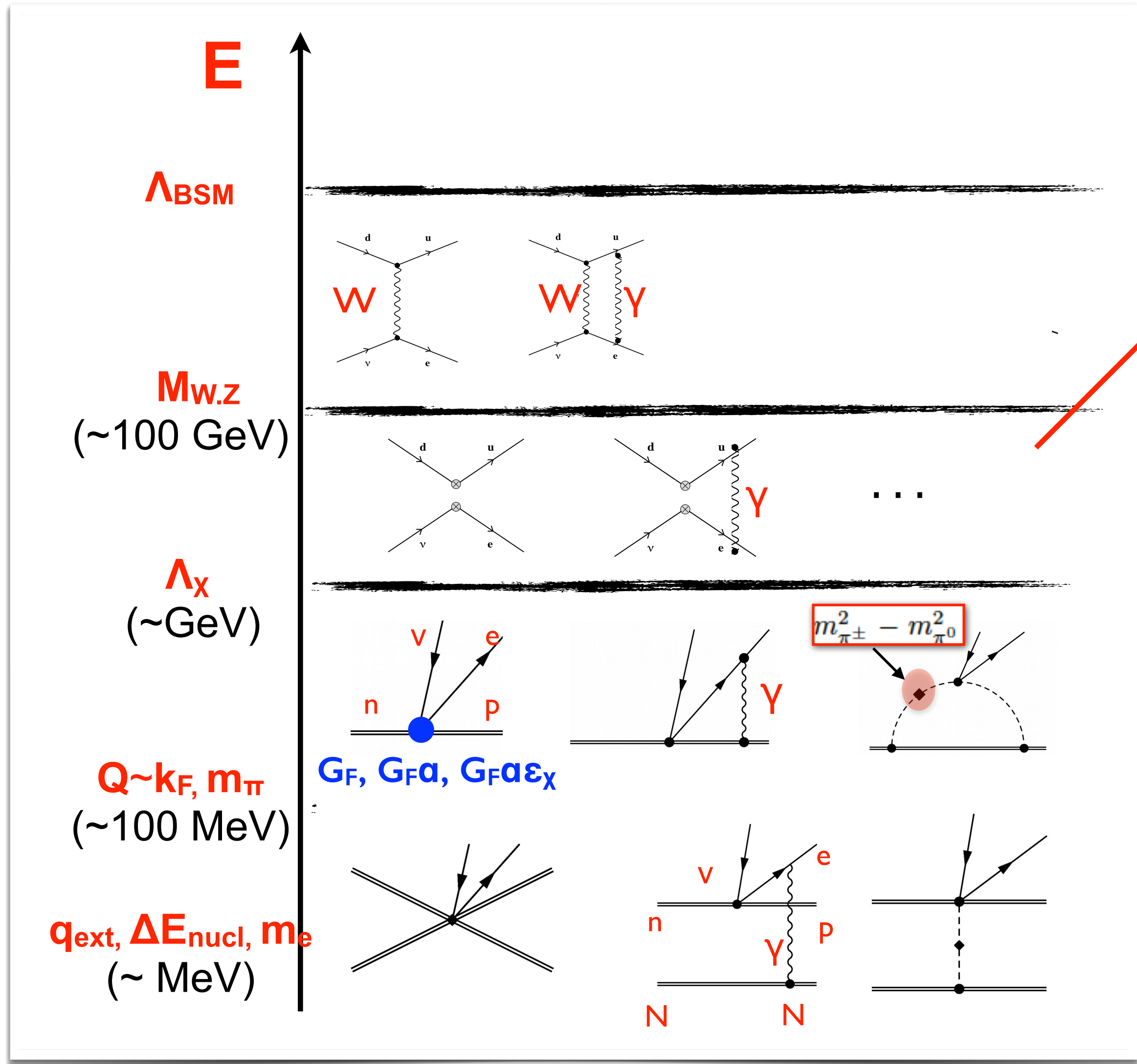


Contributions from photons of all virtualities — EFT captures them all

- Hard: $(k^0, |\mathbf{k}|) > \Lambda_\chi \sim m_N \sim \text{GeV}$
- Soft: $(k^0, |\mathbf{k}|) \sim Q \sim k_F \sim m_\pi$
- Potential: $(k^0, |\mathbf{k}|) \sim (Q^2/m_N, Q)$
- Ultrasoft: $(k^0, |\mathbf{k}|) \sim Q^2/m_N \ll k_F$

Improving the SM prediction

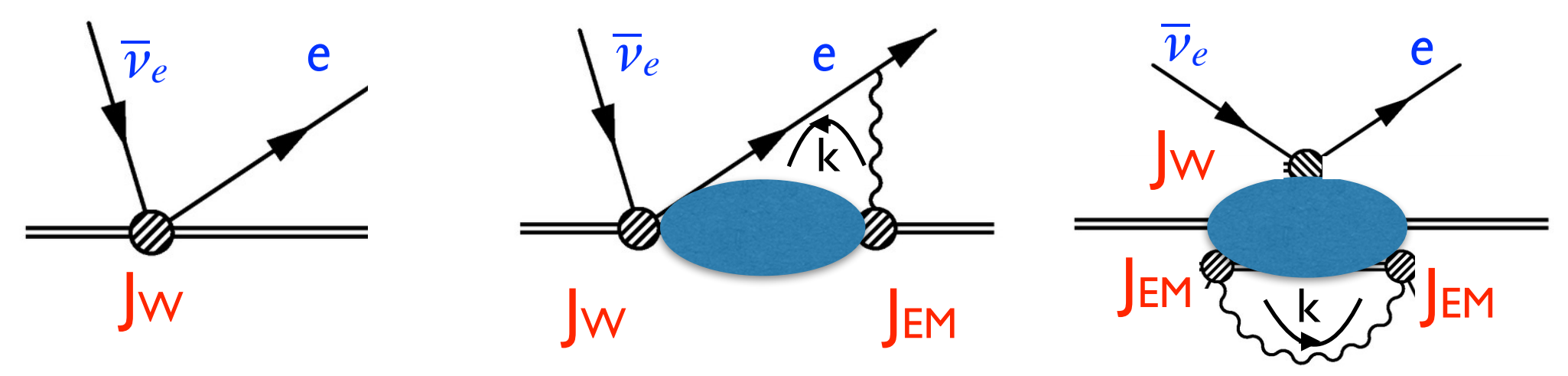
Widely separated scales: $\Lambda_{\text{BSM}} \gg M_W \gg \Lambda_\chi \gg Q \sim k_F \sim m_\pi \gg m_e \sim q_{\text{ext}} \Rightarrow$ tower of EFTs



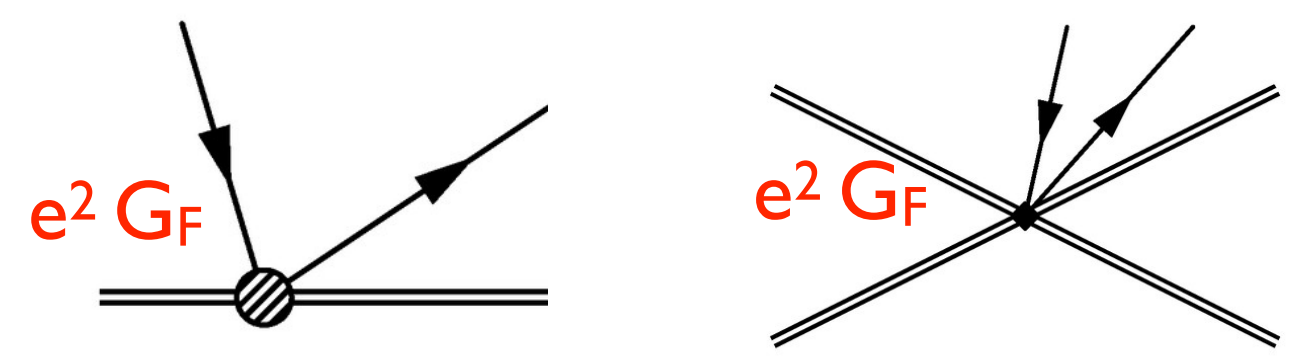
$$\mathcal{L}_{\text{Fermi}} = -\frac{G_F}{\sqrt{2}} V_{ud} C_\beta(\mu) \bar{\ell} \gamma_\alpha (1 - \gamma_5) \nu_\ell \bar{u} \gamma^\alpha (1 - \gamma_5) d + \dots$$

Matrix elements to $O(\alpha)$

$\langle f |$ $| i \rangle$

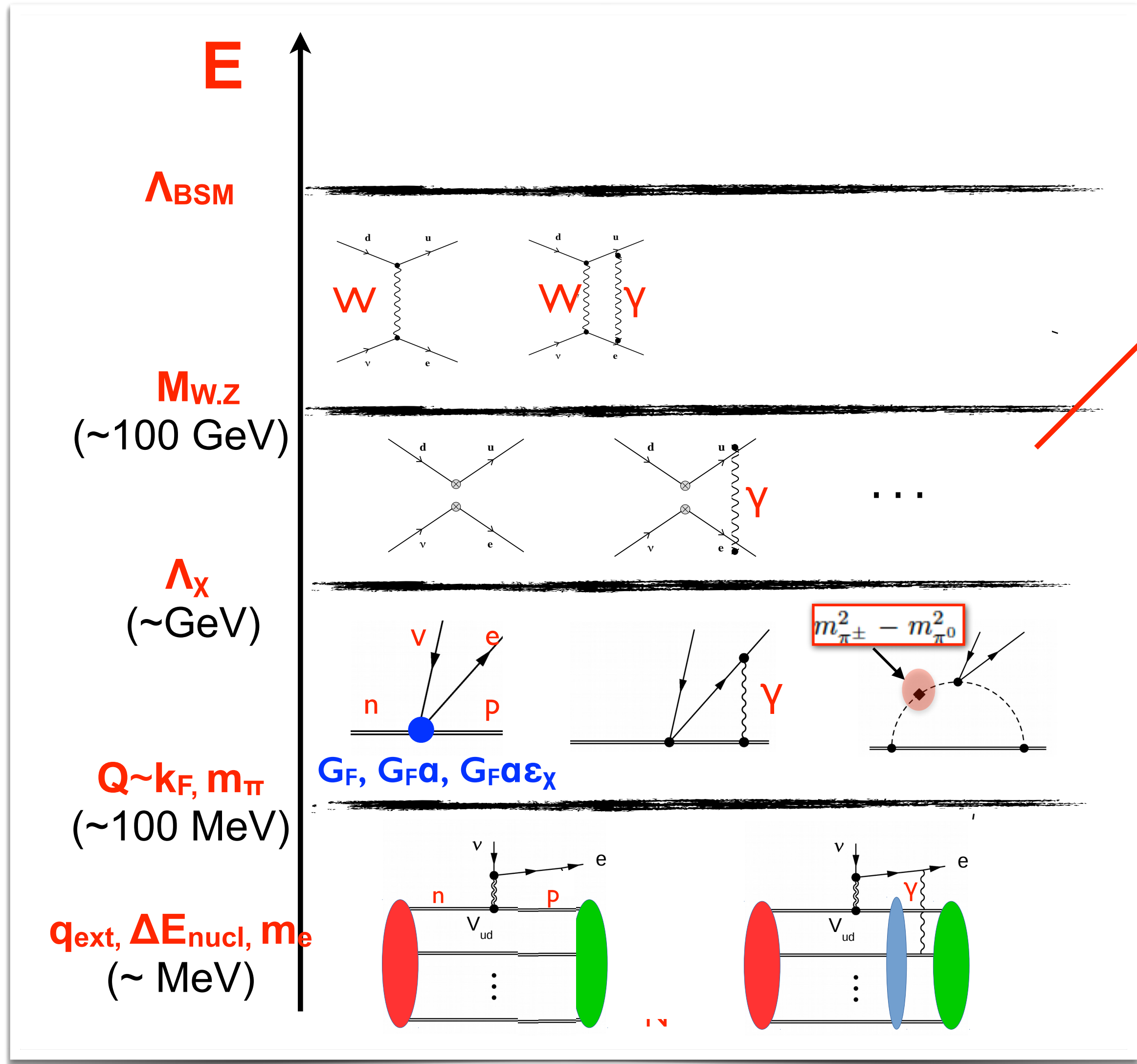


In particular, hard photons [$(k^0, |\mathbf{k}|) \gtrsim \Lambda_\chi \sim m_N \sim \text{GeV}$] leave behind local interactions at low energy



Improving the SM prediction

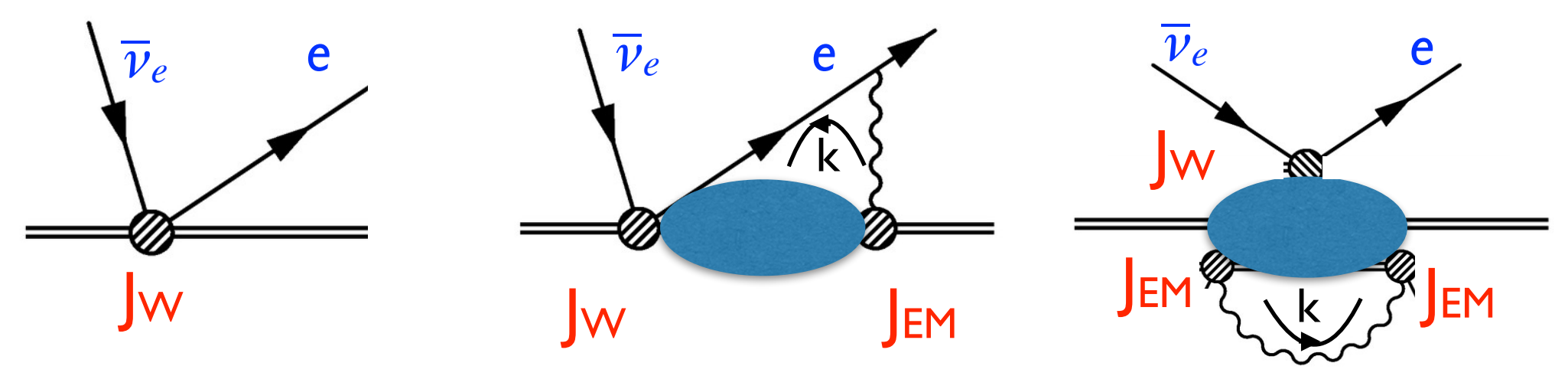
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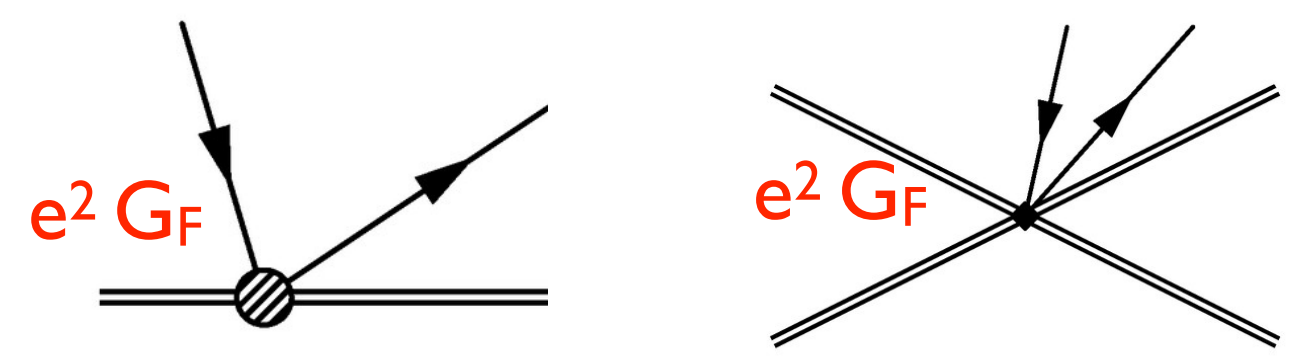
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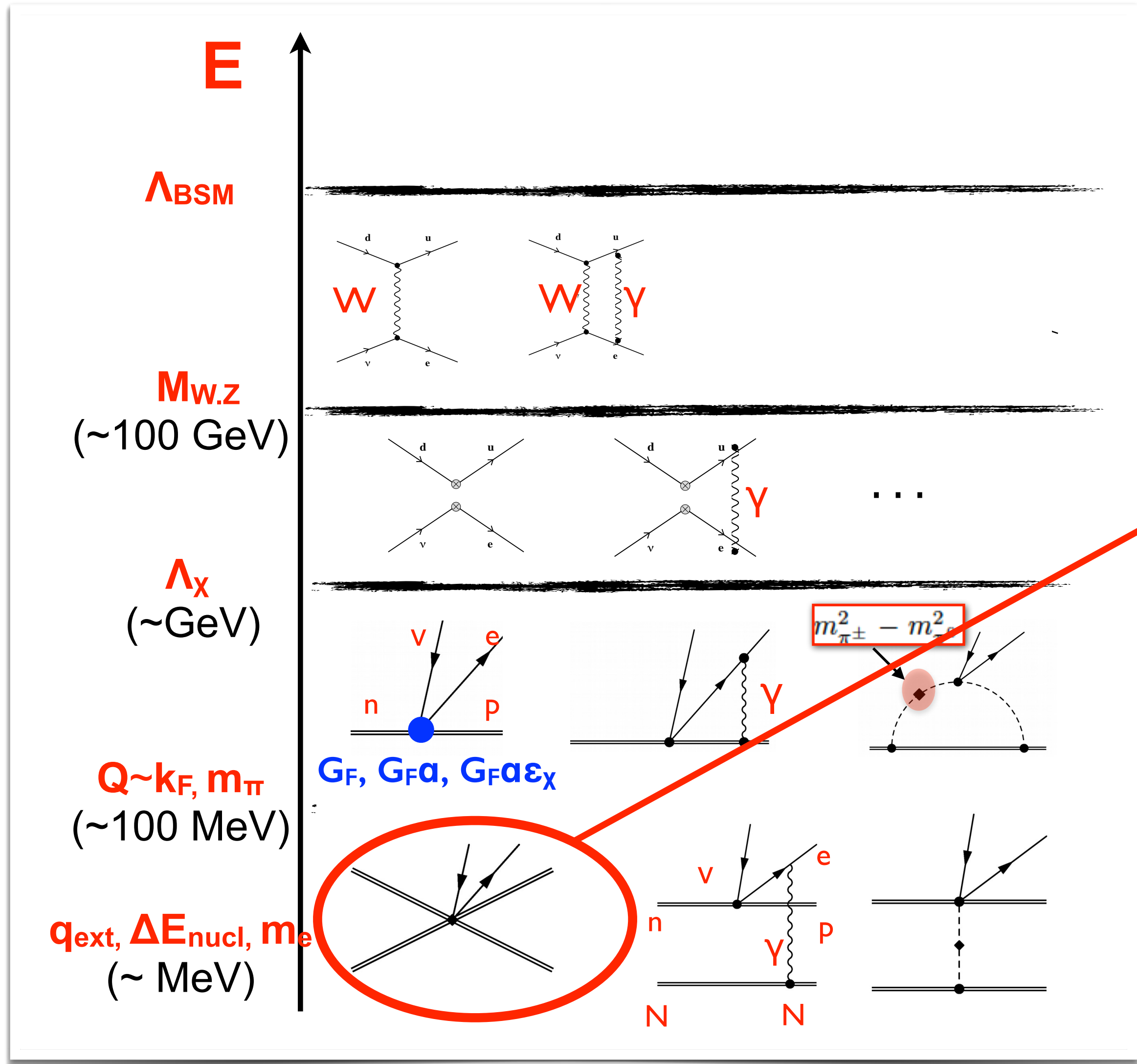


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Improving the SM prediction

Widely separated scales: $\Lambda_{\text{BSM}} \gg M_W \gg \Lambda_\chi \gg Q \sim k_F \sim m_\pi \gg m_e \sim q_{\text{ext}} \Rightarrow$ tower of EFTs



Multi nucleon

Hard photons induce $NN \rightarrow NN\gamma$ contacts \Rightarrow

$$\mathcal{L}_W^{2b} = -\sqrt{2}e^2 G_F V_{ud} \bar{e}_L \gamma_0 \nu_L \times$$

$$N^\dagger \tau^+ N \left(e^2 g_{V1}^{NN} N^\dagger N + e^2 g_{V2}^{NN} N^\dagger \tau^3 N \right)$$

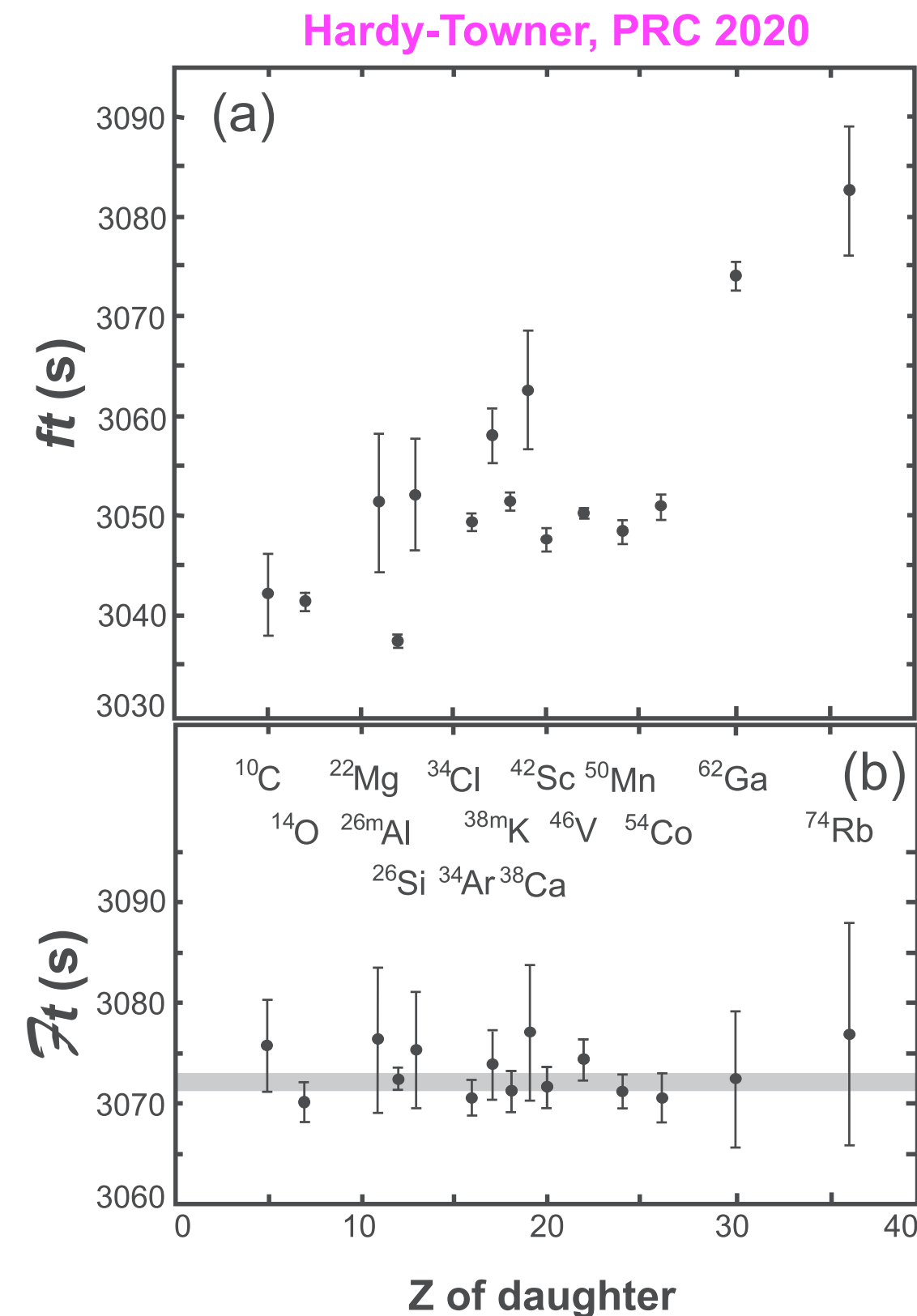
Renormalization $\Rightarrow g_{V1,V2}^{NN} \sim \frac{1}{F_\pi^2 \Lambda_\chi}$

Two body potentials of $\mathcal{O}(G_F a \epsilon_\chi)$ involves two currently unknown LECs!

Impact on V_{ud} and path forward

VC, W. Dekens,, J.de Vries, S. Gandolfi, M. Hoferichter, E. Mereghetti, 2405.18469, 2405.18464

- EFT has led to reduced uncertainties in the neutron and pion decay rate



- For nuclear decay, the EFT has identified new short-range corrections and (temporarily) increased the uncertainty

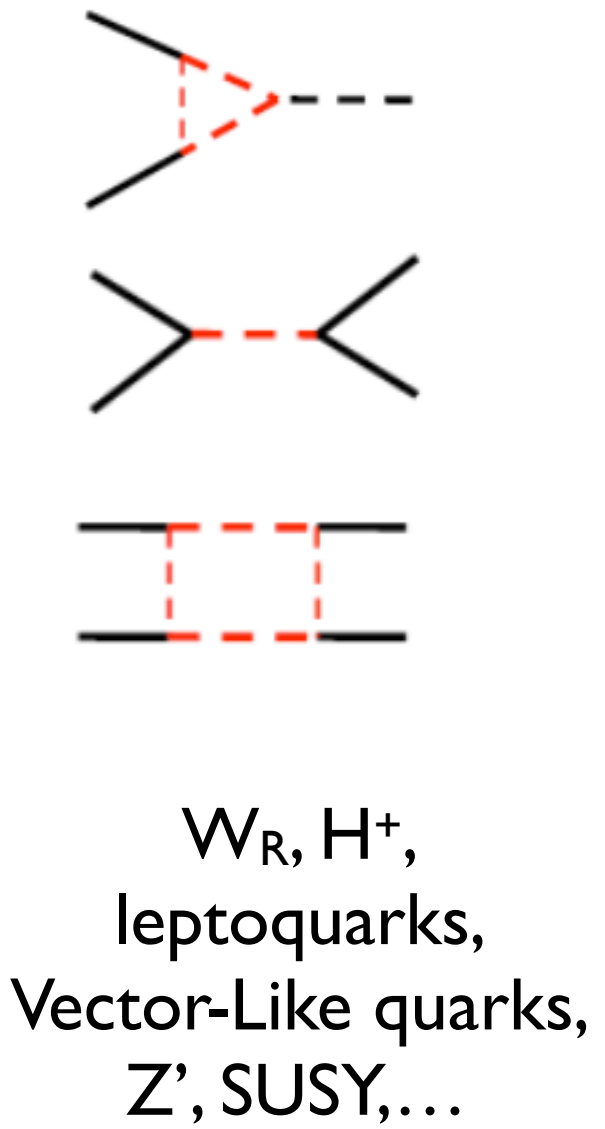
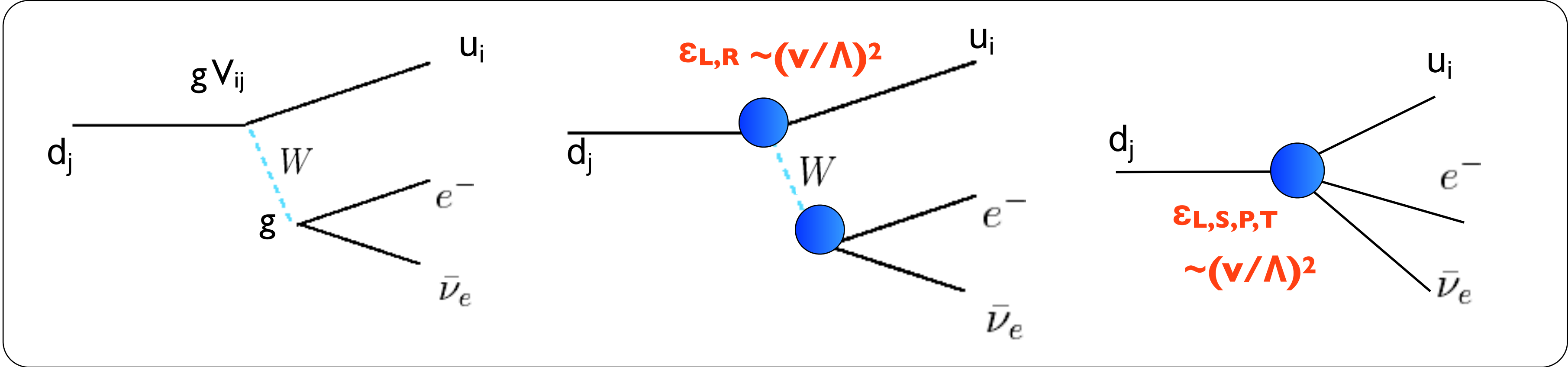
- Exploratory study in $^{14}\text{O} \rightarrow ^{14}\text{N}$ decay (with QMC) \Rightarrow
 δV_{ud} (nuclear structure) ~ 0.0003 |_{models} $\rightarrow 0.00052$ |_{EFT+QMC}

- LECs can be obtained by
 - Fitting data (along with V_{ud} and possibly BSM effective couplings) once NME calculations for several isotopes become available
 - Theory: dispersive analysis, Lattice QCD

Implications for new physics

Despite all the caveats, it is interesting to look at what we might learn if the 'Cabibbo Anomaly' survives!

Implications for new physics



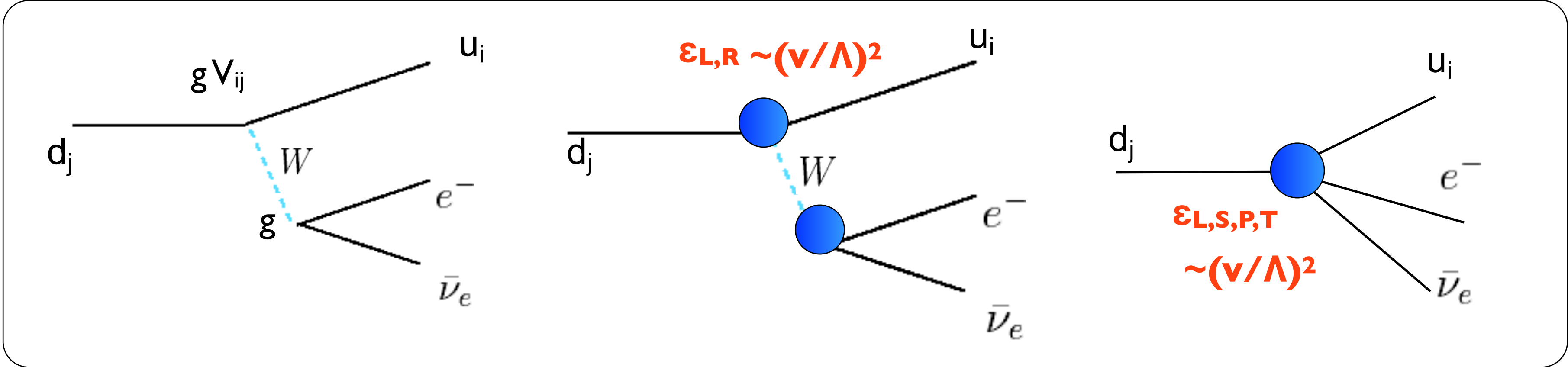
$E \sim \text{GeV}$ ↓

$$\mathcal{L}_{\text{SM}} - \frac{G_F V_{udj}}{\sqrt{2}} \sum_{\Gamma} \left[\epsilon_{\Gamma}^{(j)} \bar{\ell} \Gamma \nu_L \cdot \bar{u} \Gamma d_j + \tilde{\epsilon}_{\Gamma}^{(j)} \bar{\ell} \Gamma \nu_R \cdot \bar{u} \Gamma d \right]$$

$\Gamma = L, R, S, P, T$

BSM effects parameterized by 10(ud) + 10(us) effective couplings at $E \sim \text{GeV}$
 They map into vertex corrections and 4-Fermion interactions in SMEFT, above the EW scale

Implications for new physics



$W_R, H^+,$
 leptoquarks,
 Vector-Like quarks,
 $Z', SUSY, \dots$

$E \sim \text{GeV}$ ↓

$$\mathcal{L}_{\text{SM}} - \frac{G_F V_{udj}}{\sqrt{2}} \sum_{\Gamma} \left[\epsilon_{\Gamma}^{(j)} \bar{\ell} \Gamma \nu_L \cdot \bar{u} \Gamma d_j + \tilde{\epsilon}_{\Gamma}^{(j)} \bar{\ell} \Gamma \nu_R \cdot \bar{u} \Gamma d \right]$$

$\Gamma = L, R, S, P, T$

Δ_{CKM} tension confirmed: points to specific new physics

Δ_{CKM} tension removed: strong constraints, complementary to traditional ‘precision electroweak observables’

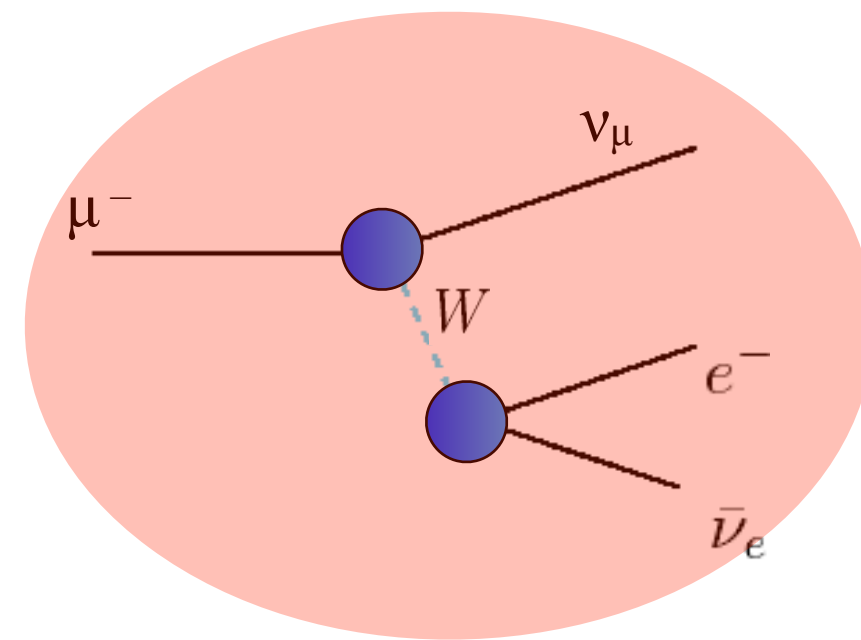
GeV-scale effective Lagrangian

VC, Gonzalez-Alonso, Jenkins 0908.1754, NPB

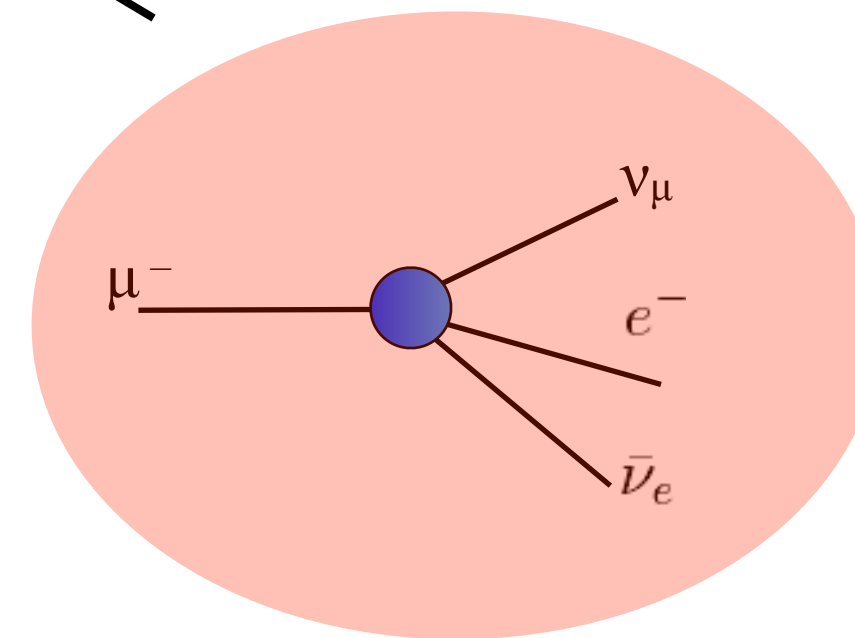
VC, Graesser, Gonzalez-Alonso 1210.4553, JHEP

Leptonic interactions

$$\mathcal{L}_{CC}^{(\mu)} = -\frac{G_F^{(0)}}{\sqrt{2}} \left(1 + \epsilon_L^{(\mu)}\right) \bar{e} \gamma^\rho (1 - \gamma_5) \nu_e \cdot \bar{\nu}_\mu \gamma_\rho (1 - \gamma_5) \mu + \dots$$



Vertex corrections



4-fermion contact interaction

GeV-scale effective Lagrangian

VC, Gonzalez-Alonso, Jenkins 0908.1754, NPB

VC, Graesser, Gonzalez-Alonso 1210.4553, JHEP

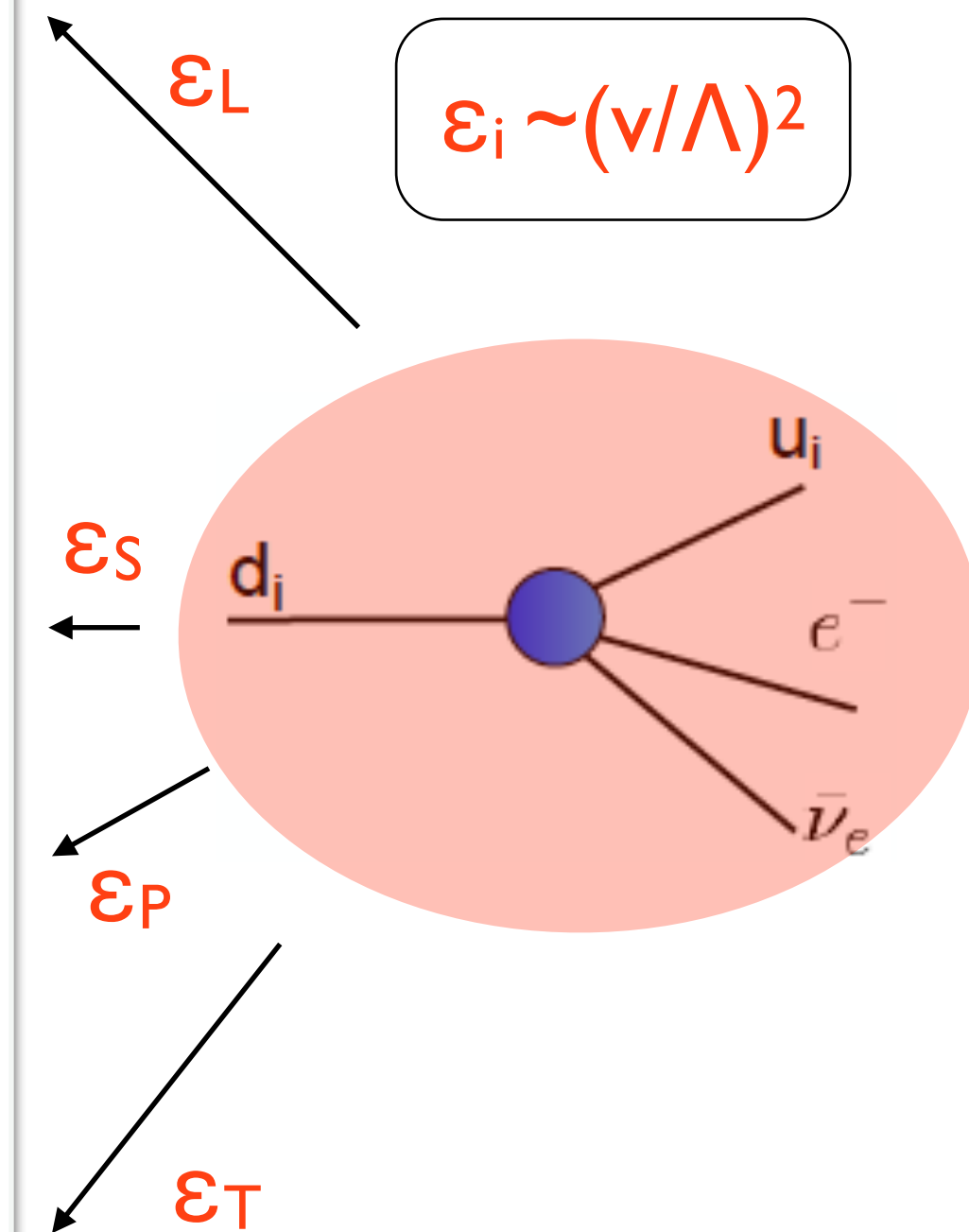
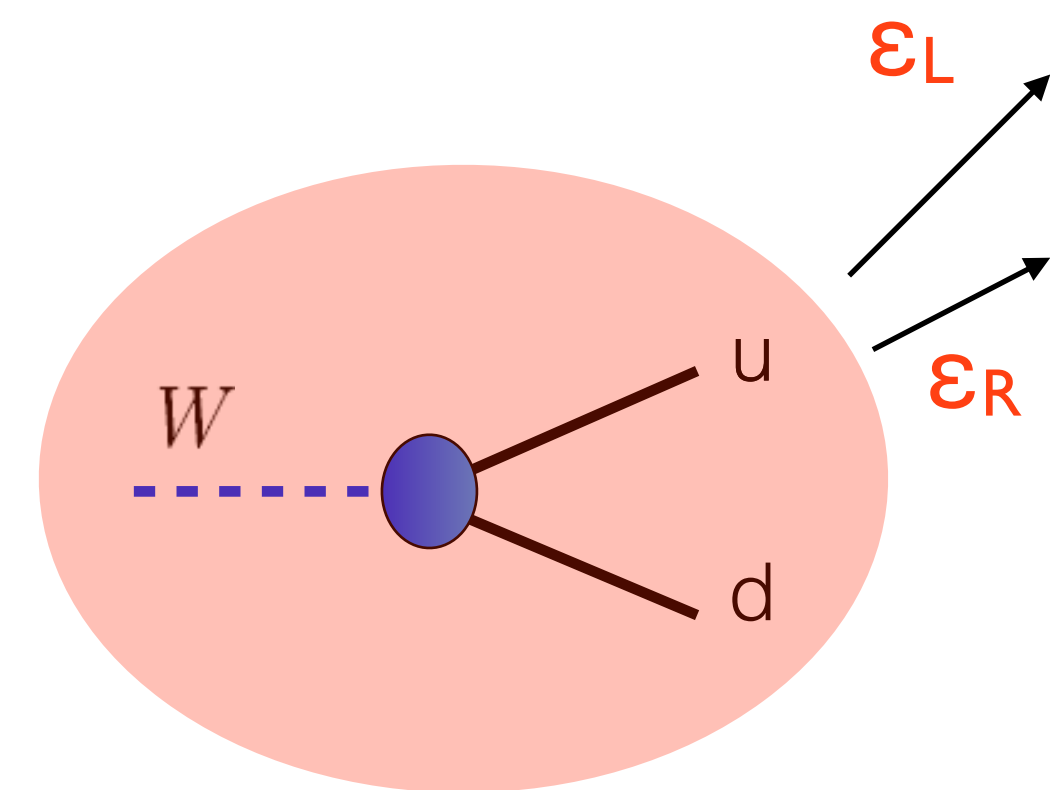
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Semi-leptonic interactions

$$\begin{aligned} \mathcal{L}_{CC} = & -\frac{G_F^{(0)} V_{ud}}{\sqrt{2}} \times \left[\left(\delta^{ab} + \epsilon_L^{ab} \right) \bar{e}_a \gamma_\mu (1 - \gamma_5) \nu_b \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d \right. \\ & + \epsilon_R^{ab} \bar{e}_a \gamma_\mu (1 - \gamma_5) \nu_b \cdot \bar{u} \gamma^\mu (1 + \gamma_5) d \\ & + \epsilon_S^{ab} \bar{e}_a (1 - \gamma_5) \nu_b \cdot \bar{u} d \\ & - \epsilon_P^{ab} \bar{e}_a (1 - \gamma_5) \nu_b \cdot \bar{u} \gamma_5 d \\ & \left. + \epsilon_T^{ab} \bar{e}_a \sigma_{\mu\nu} (1 - \gamma_5) \nu_b \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) d \right] + \text{h.c.} \end{aligned}$$

$$\epsilon_i \sim (v/\Lambda)^2$$



GeV-scale effective Lagrangian

VC, Gonzalez-Alonso, Jenkins 0908.1754, NPB

VC, Graesser, Gonzalez-Alonso 1210.4553, JHEP

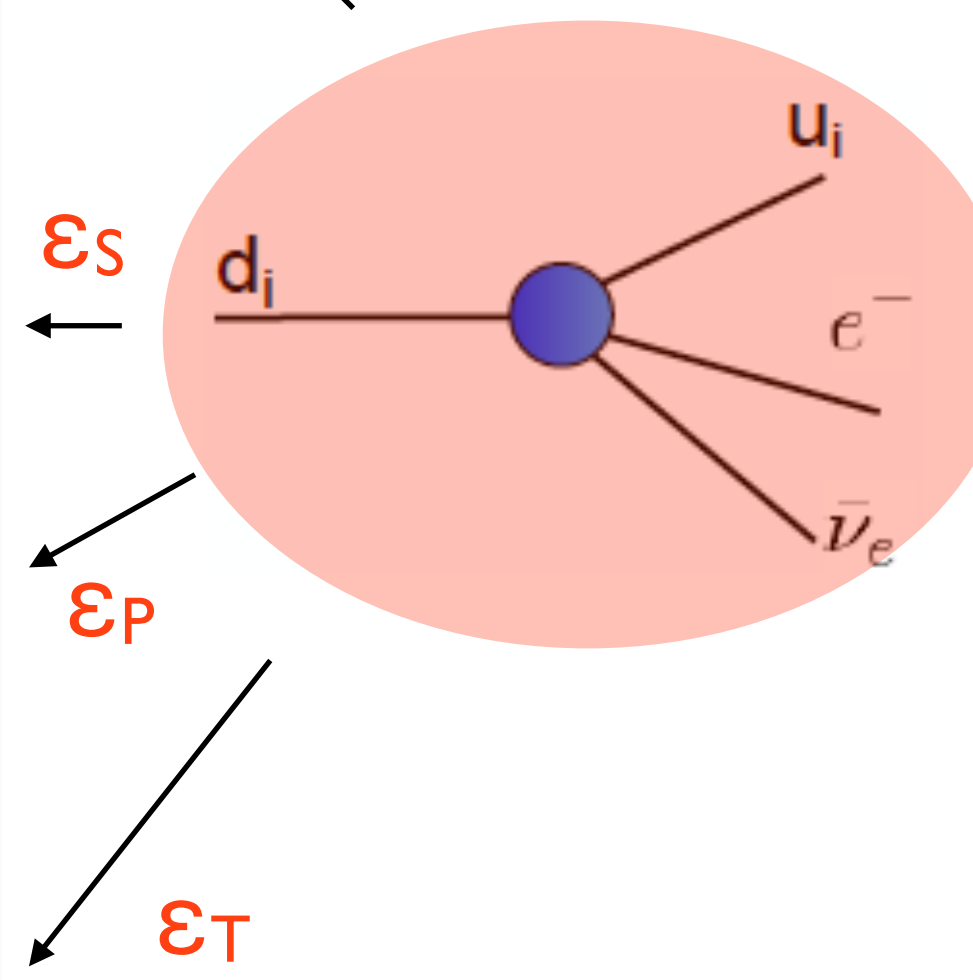
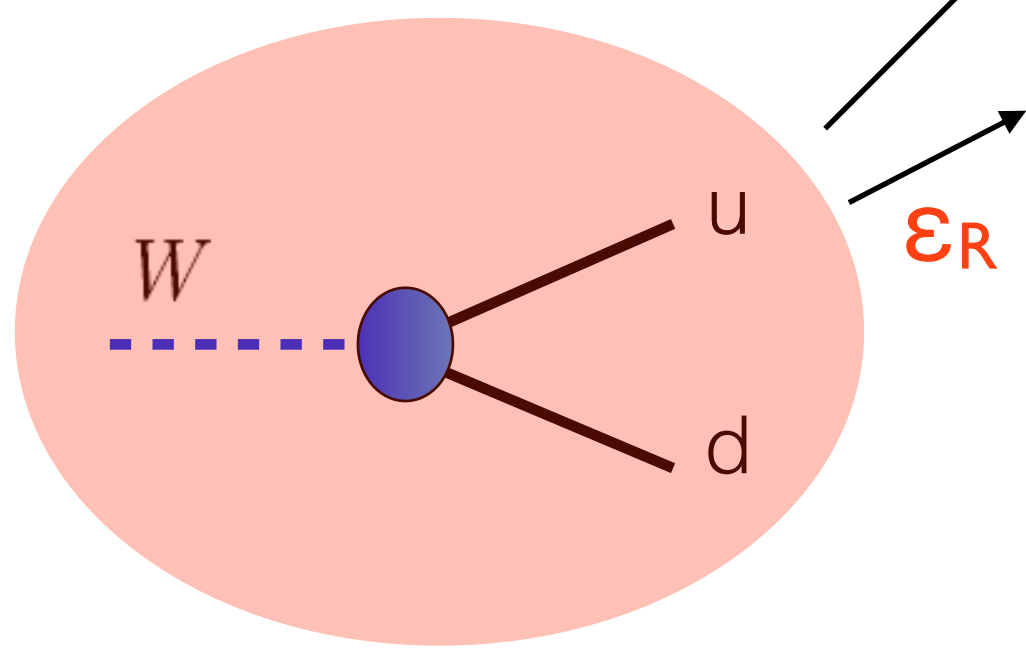
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$$\mathcal{L}_{CC}^{(\mu)} = -\frac{G_F^{(0)}}{\sqrt{2}} \left(1 + \epsilon_L^{(\mu)}\right) \bar{e} \gamma^\rho (1 - \gamma_5) \nu_e \cdot \bar{\nu}_\mu \gamma_\rho (1 - \gamma_5) \mu + \dots$$

Semi-leptonic interactions

$$\mathcal{L}_{CC} = -\frac{G_F^{(0)} V_{ud}}{\sqrt{2}} \times \left[\frac{G_F^{(\mu)} V_{ud}}{\sqrt{2}} (1 - \epsilon_L^{(\mu)}) \left(\delta^{ab} + \epsilon_L^{ab} \right) \bar{e}_a \gamma_\mu (1 - \gamma_5) \nu_b \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d \right. \\ + \epsilon_R^{ab} \bar{e}_a \gamma_\mu (1 - \gamma_5) \nu_b \cdot \bar{u} \gamma^\mu (1 + \gamma_5) d \\ + \epsilon_S^{ab} \bar{e}_a (1 - \gamma_5) \nu_b \cdot \bar{u} d \\ - \epsilon_P^{ab} \bar{e}_a (1 - \gamma_5) \nu_b \cdot \bar{u} \gamma_5 d \\ \left. + \epsilon_T^{ab} \bar{e}_a \sigma_{\mu\nu} (1 - \gamma_5) \nu_b \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) d \right] + \text{h.c.}$$

$$\epsilon_i \sim (v/\Lambda)^2$$



Corrections to V_{ud} and V_{us}

$$|\bar{V}_{ud}|_i^2 = |V_{ud}|^2 \left(1 + \sum_{\alpha} C_{i\alpha} \epsilon_{\alpha} \right)$$

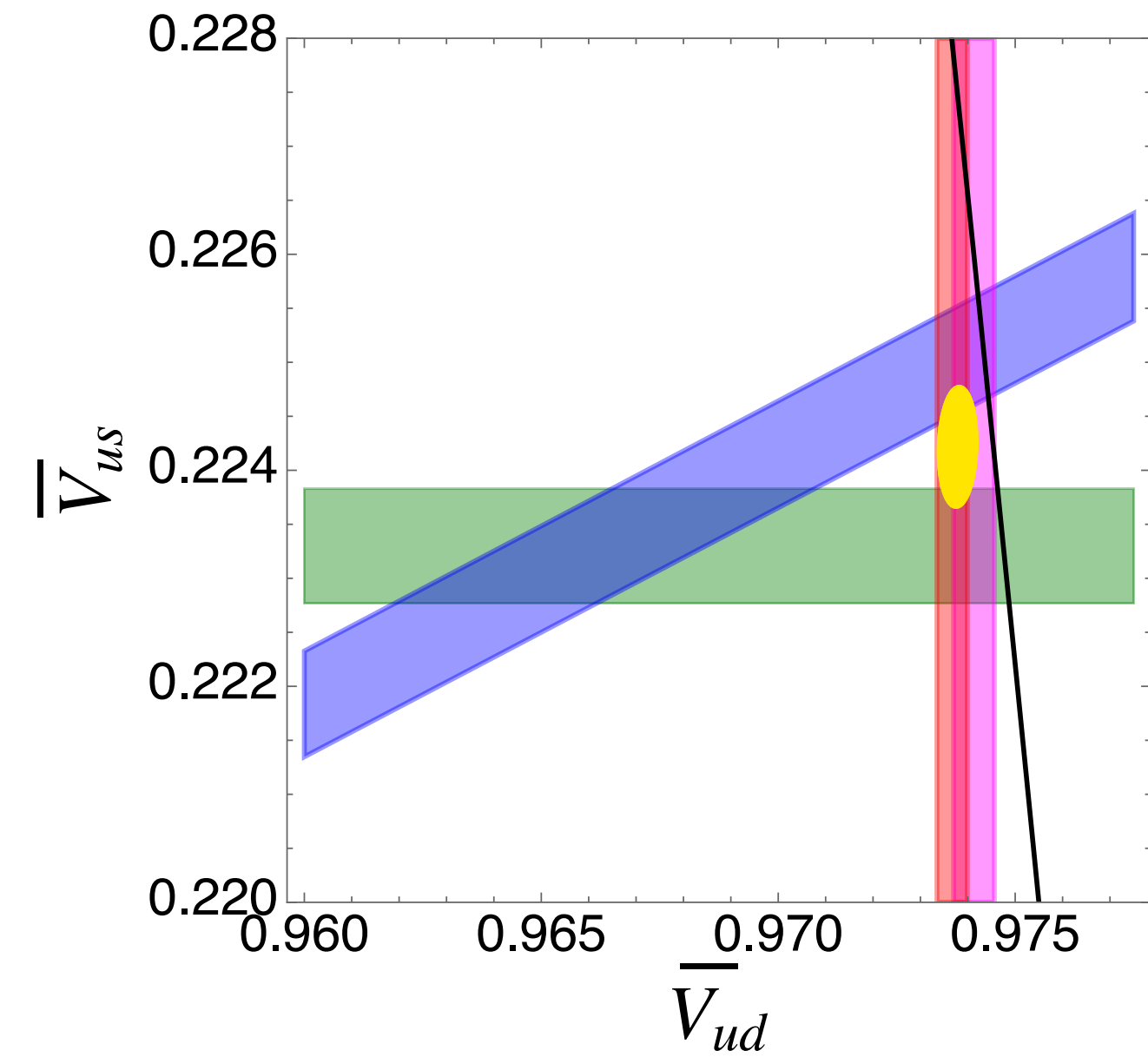
$$|\bar{V}_{us}|_j^2 = |V_{us}|^2 \left(1 + \sum_{\alpha} C_{j\alpha} \epsilon_{\alpha} \right)$$

Channel-dependent CKM elements extracted in the 'SM-like analysis'

Elements of the unitary CKM matrix

Known coefficients

BSM effective couplings



Find set of ϵ 's so that V_{ud} and V_{us} bands meet on the unitarity circle

Corrections to V_{ud} and V_{us}

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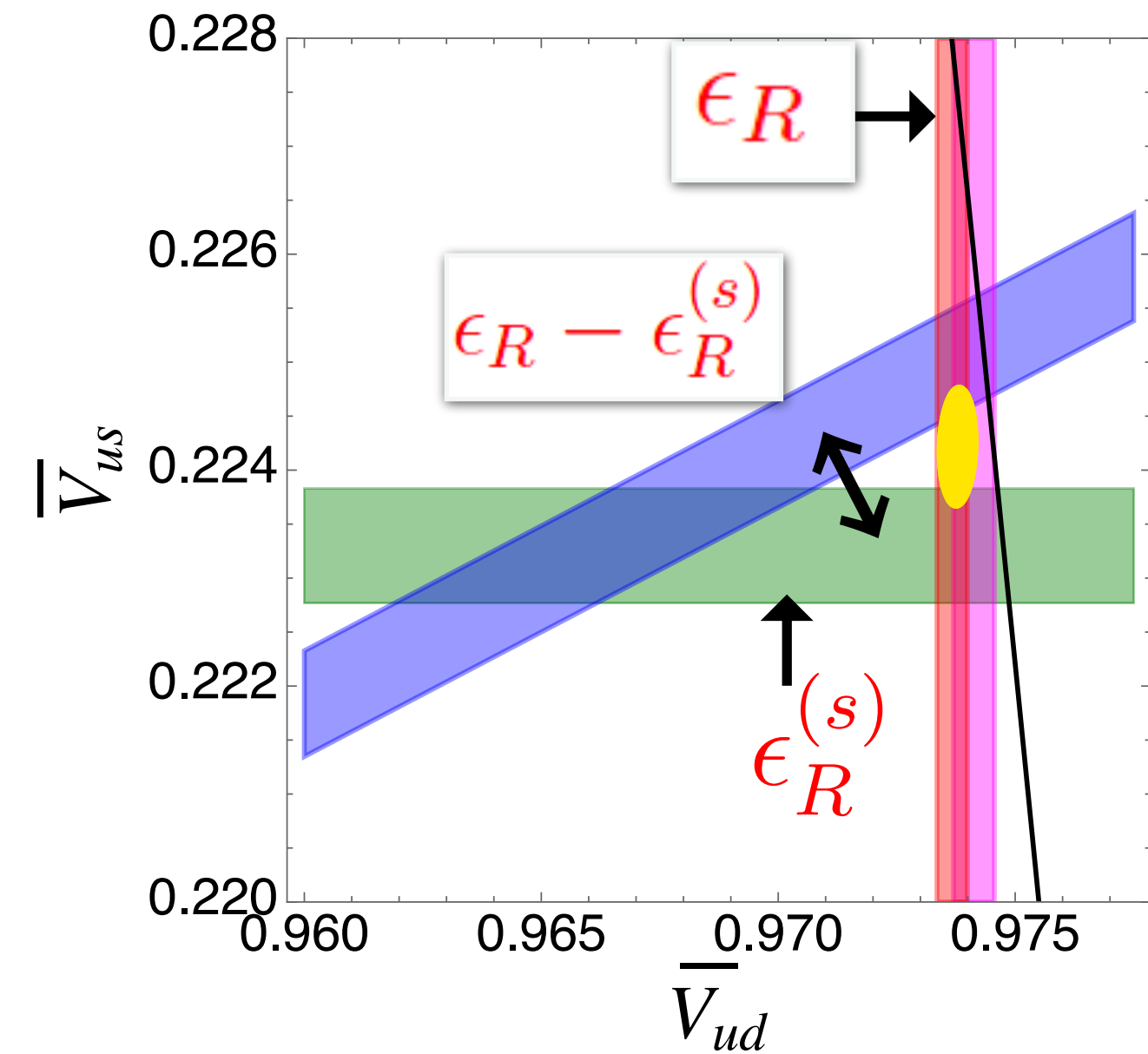
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Find set of ϵ 's so that V_{ud} and V_{us} bands meet on the unitarity circle

Simplest 'solution': right-handed (V+A) quark currents

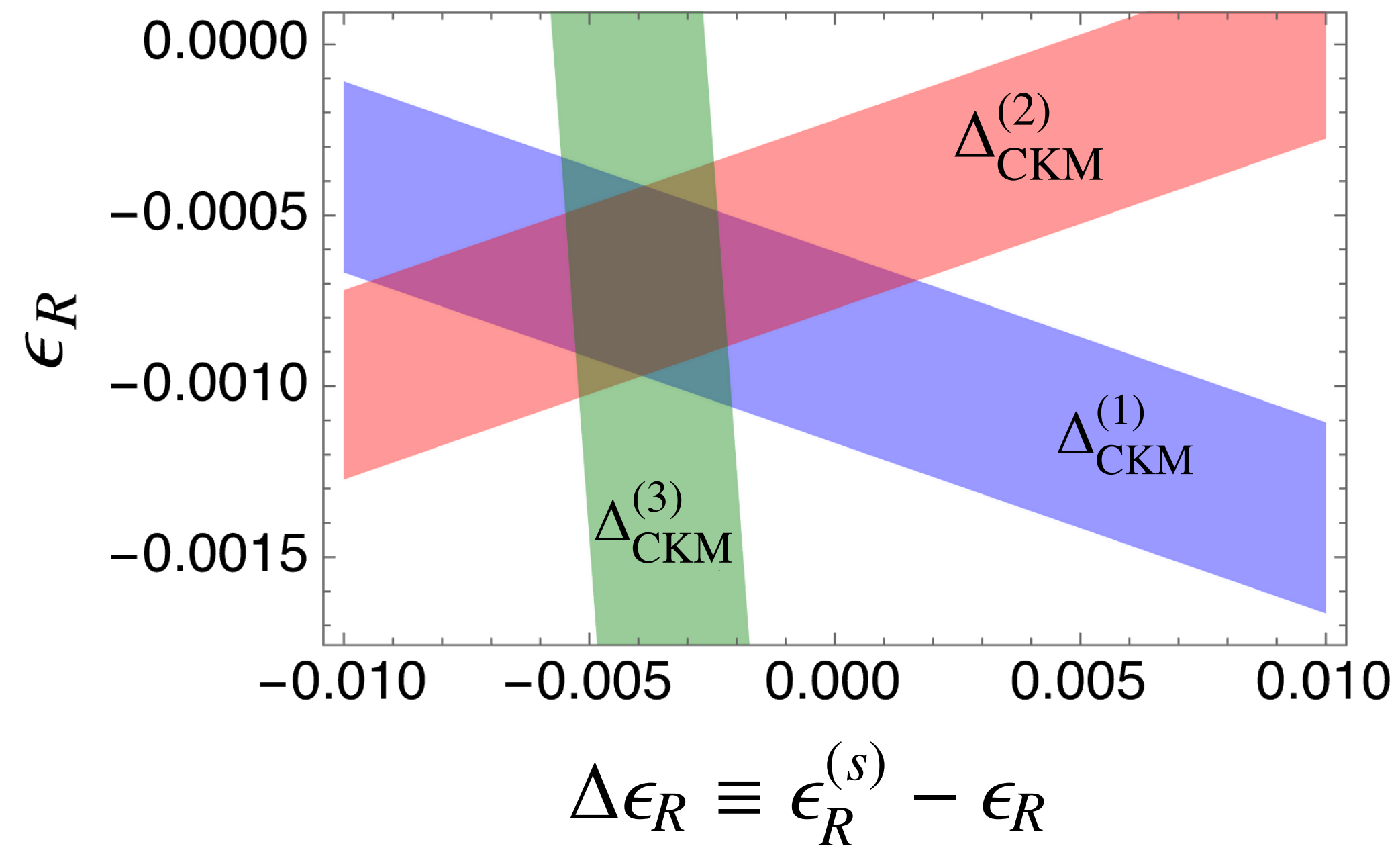
CKM elements from vector (axial) channels are shifted by $1 + \epsilon_R$ ($1 - \epsilon_R$).

V_{us}/V_{ud} , V_{ud} and V_{us} shift in correlated way, can resolve all tensions!

Alioli et al 1703.04751
Grossman-Passemar-Schacht 1911.07821
VC-Crivellin-Hoferichter-Moulson 2208.11707
VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong, 2311.00021

Unveiling R-handed quark currents?

VC-Crivellin-Hoferichter-Moulson 2208.11707



$$\begin{aligned}\Delta_{CKM}^{(1)} &= |V_{ud}^\beta|^2 + |V_{us}^{K\ell 3}|^2 - 1 \\ &= -1.76(56) \times 10^{-3} \\ \Delta_{CKM}^{(2)} &= |V_{ud}^\beta|^2 + |V_{us}^{K\ell 2/\pi\ell 2, \beta}|^2 - 1 \\ &= -0.98(58) \times 10^{-3} \\ \Delta_{CKM}^{(3)} &= |V_{ud}^{K\ell 2/\pi\ell 2, K\ell 3}|^2 + |V_{us}^{K\ell 3}|^2 - 1 \\ &= -1.64(63) \times 10^{-2}\end{aligned}$$



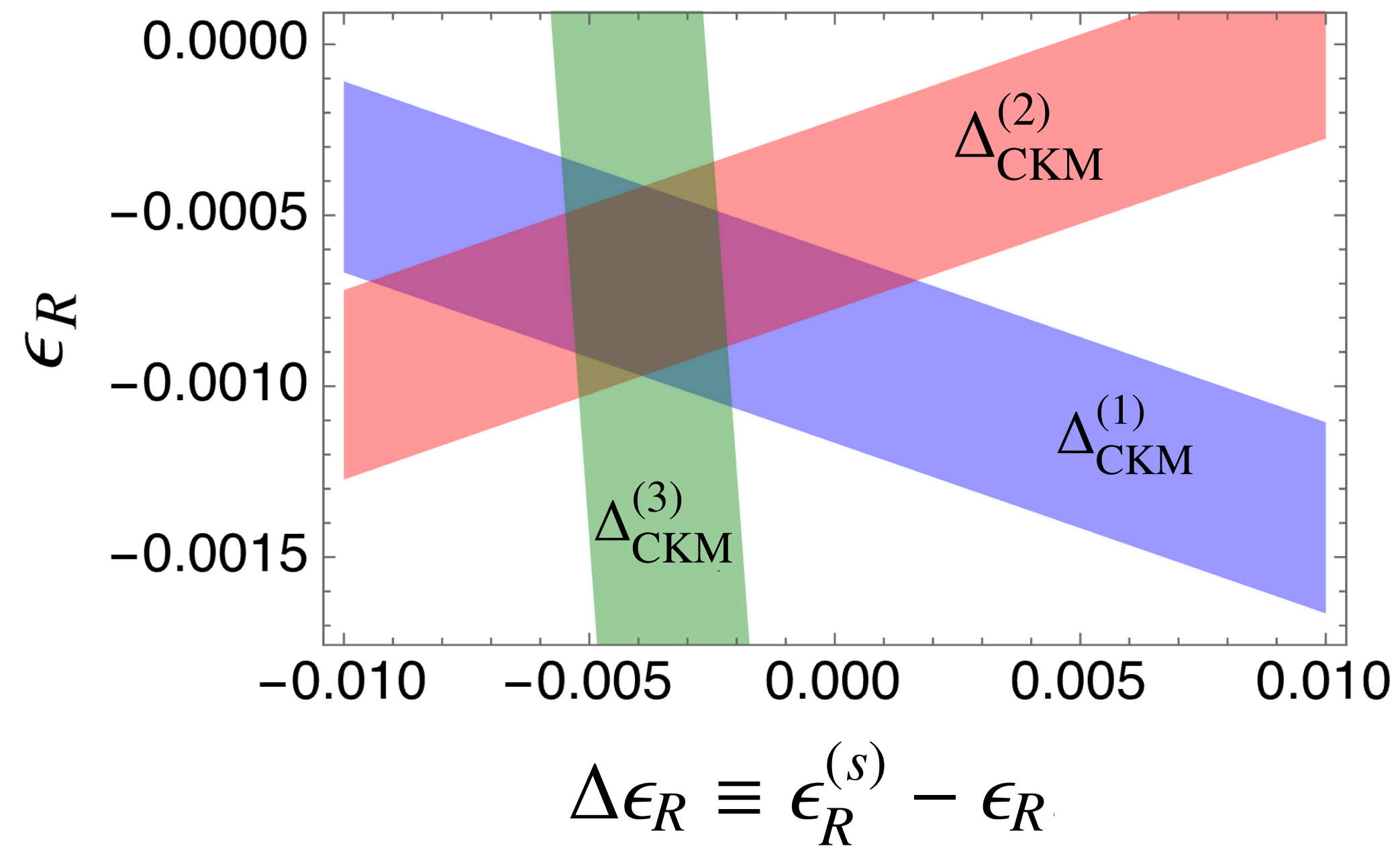
$$\begin{aligned}\epsilon_R &= -0.69(27) \times 10^{-3} \\ \Delta\epsilon_R &= -3.9(1.6) \times 10^{-3}\end{aligned}$$

$\Lambda_R \sim 5-10 \text{ TeV}$

- Preferred ranges are not in conflict with constraints from other low-E probes
- Does the R-handed current explanation survive after taking into account high energy data?

Unveiling R-handed quark currents?

VC-Crivellin-Hoferichter-Moulson 2208.11707



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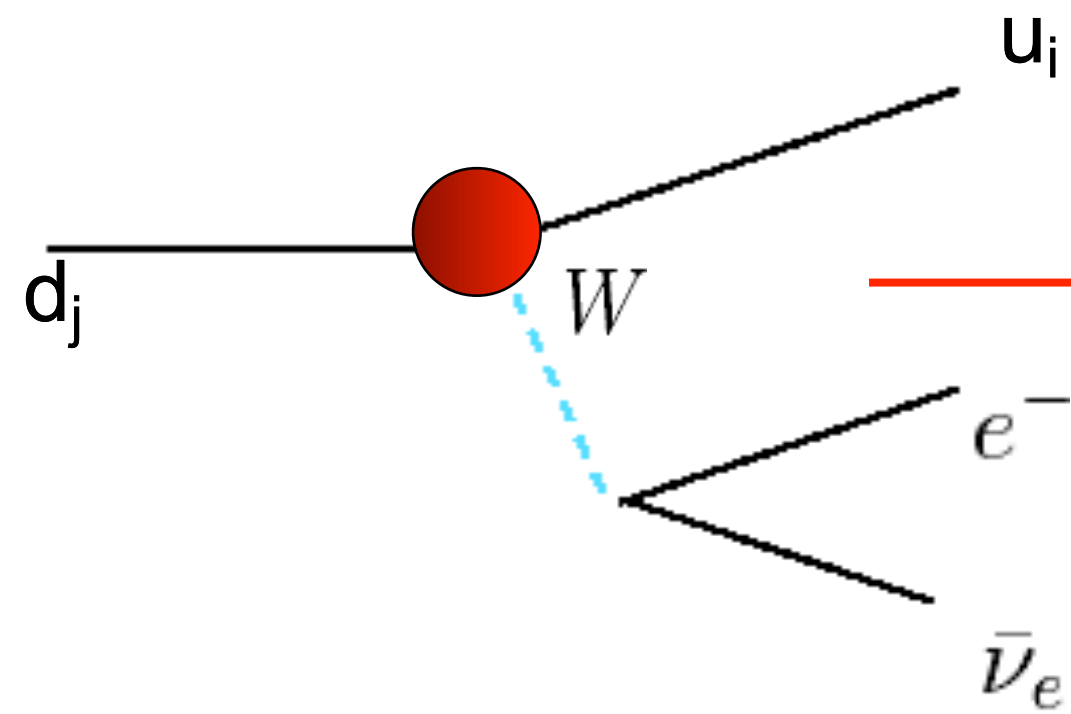
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- Preferred ranges are not in conflict with constraints from other low-E probes
- Does the R-handed current explanation survive after taking into account high energy data? Yes!

High scale origin of ϵ_R

- ϵ_R originates from SU(2)xU(1) invariant vertex corrections



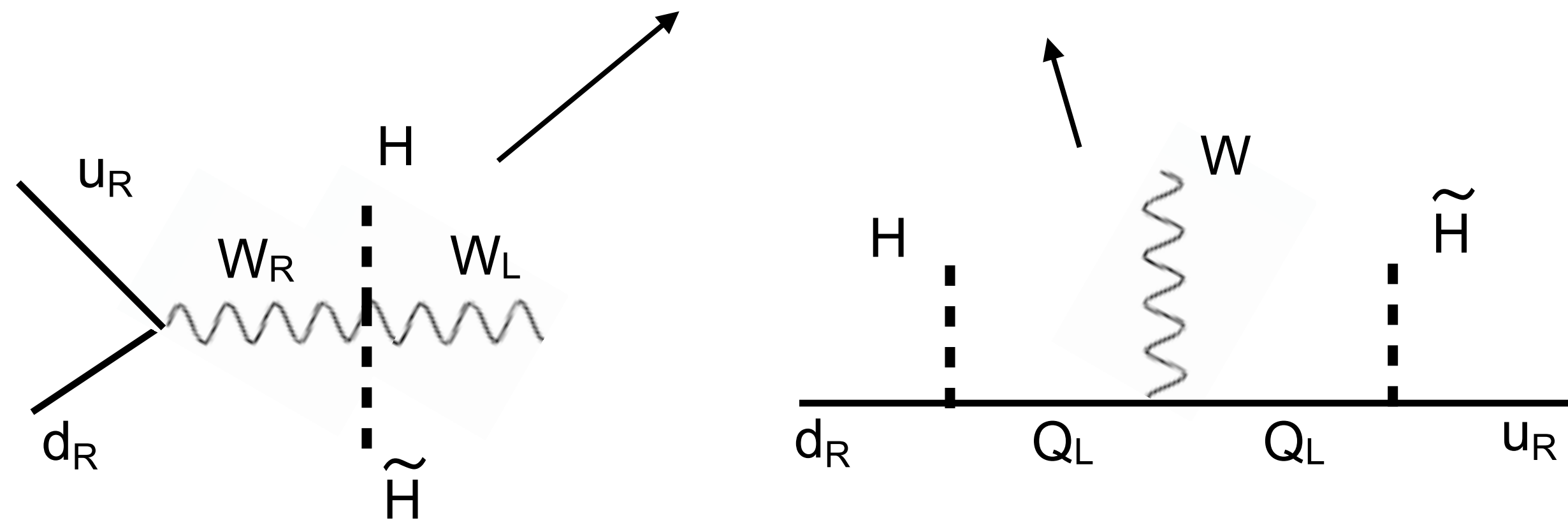
Building blocks

$$l^i = \begin{pmatrix} \nu_L^i \\ e_L^i \end{pmatrix} \quad q^i = \begin{pmatrix} u_L^i \\ d_L^i \end{pmatrix} \quad H = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix}$$

$$Q_{Hud} = i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$$

ϵ_R

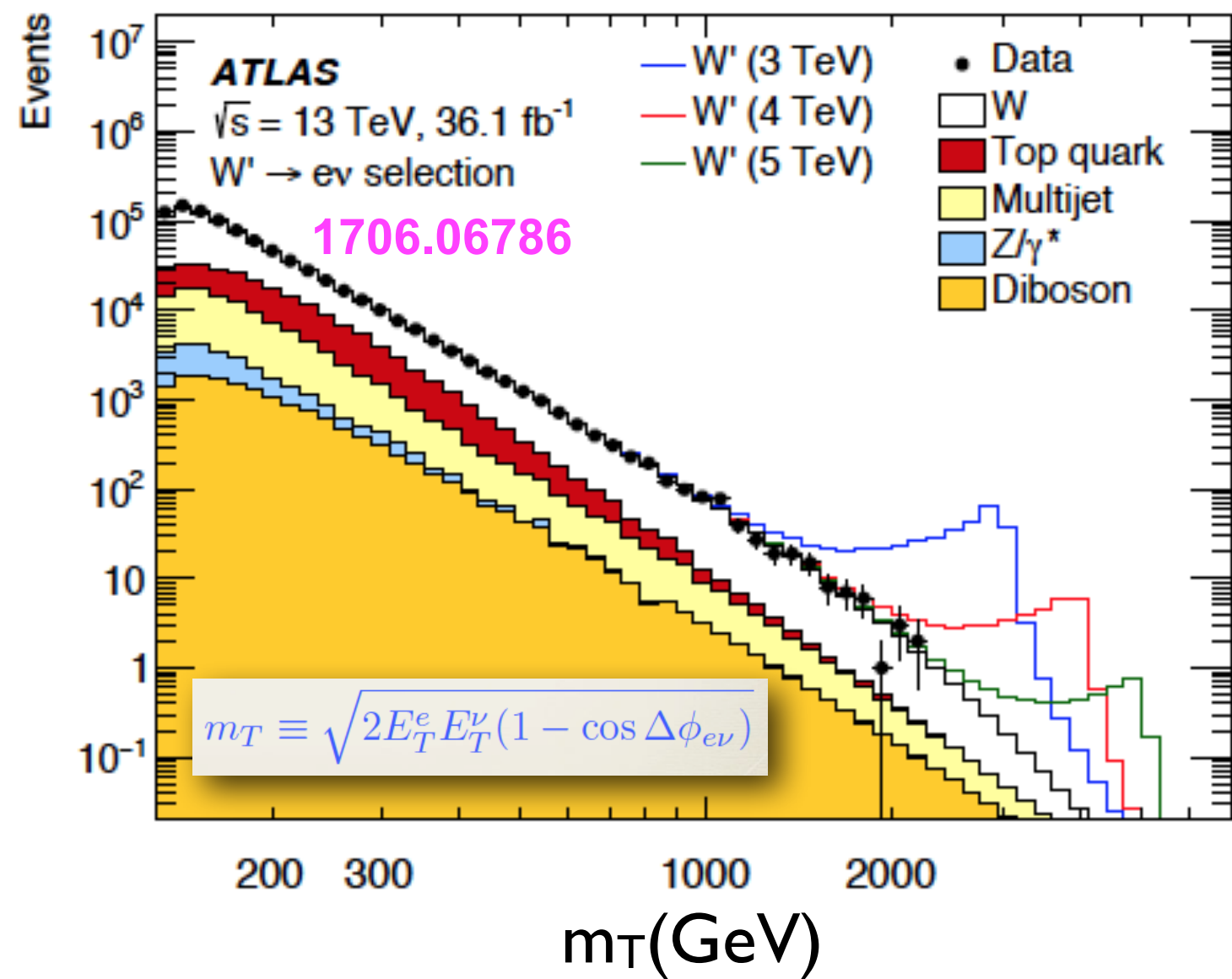
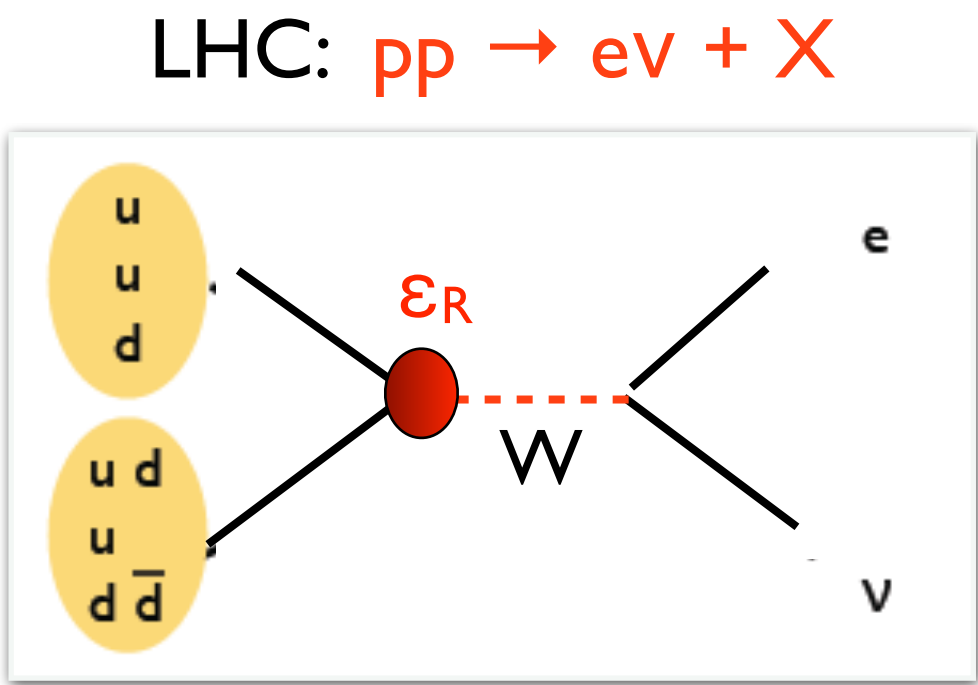
- Can be generated by W_L - W_R mixing in **Left-Right symmetric models** or by **exchange of vector-like quarks**



Belfatto-Bereziani 2103.05549. ...
Belfatto-Trifinopoulos 2302.14097

Collider constraints on ϵ_R are weak

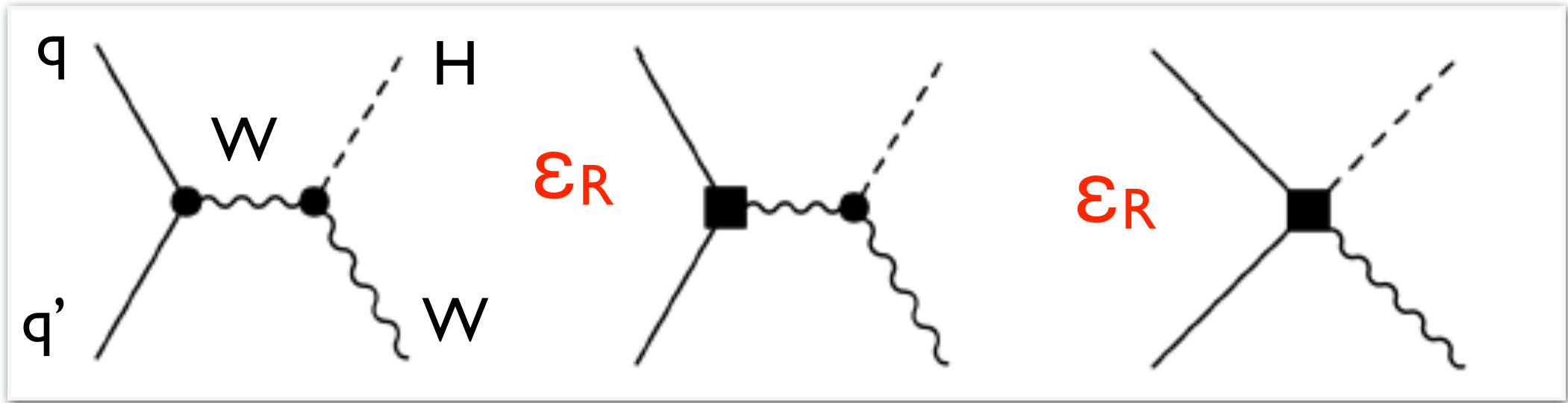
Contribute to $pp \rightarrow ev+X$ at the LHC



New contribution has same shape as the SM W exchange
 \rightarrow weak sensitivity

VC, Graesser, Gonzalez-Alonso 1210.4553
 Alioli-Dekens-Girard-Mereghetti 1804.07407
 Gupta et al. 1806.09006
 ...

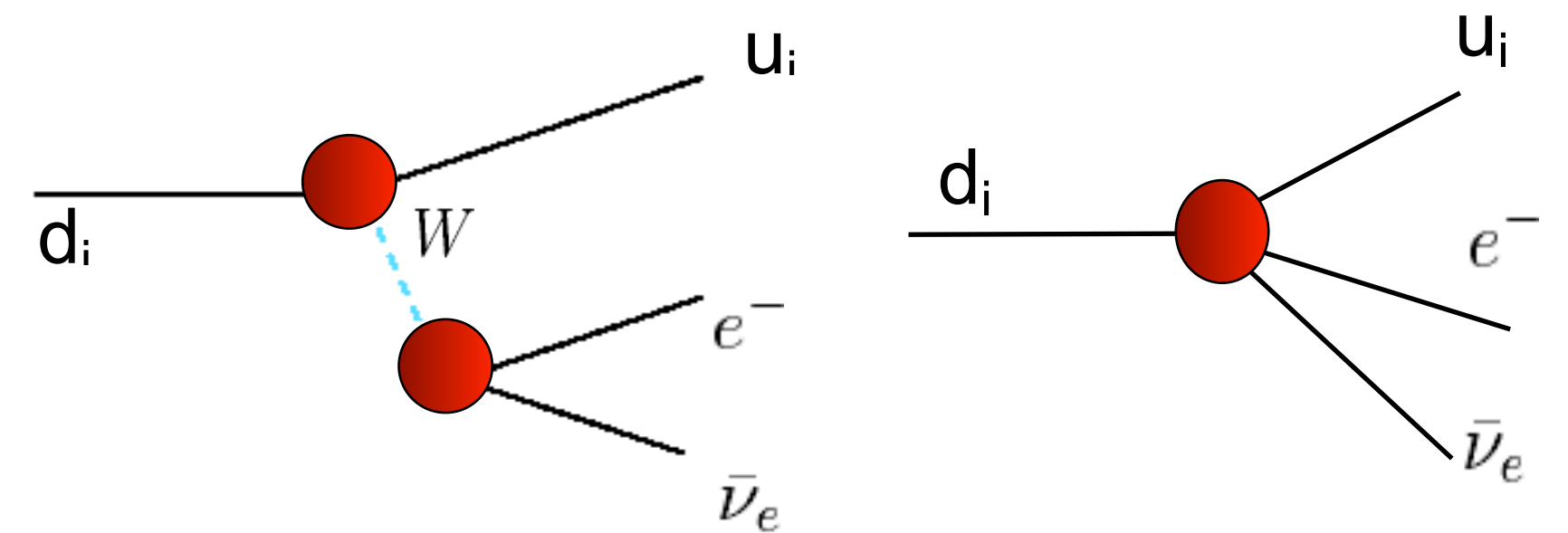
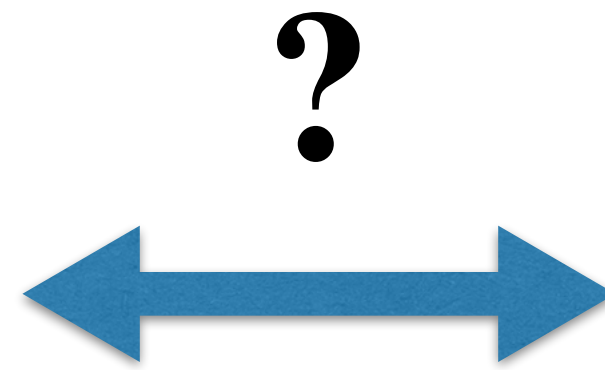
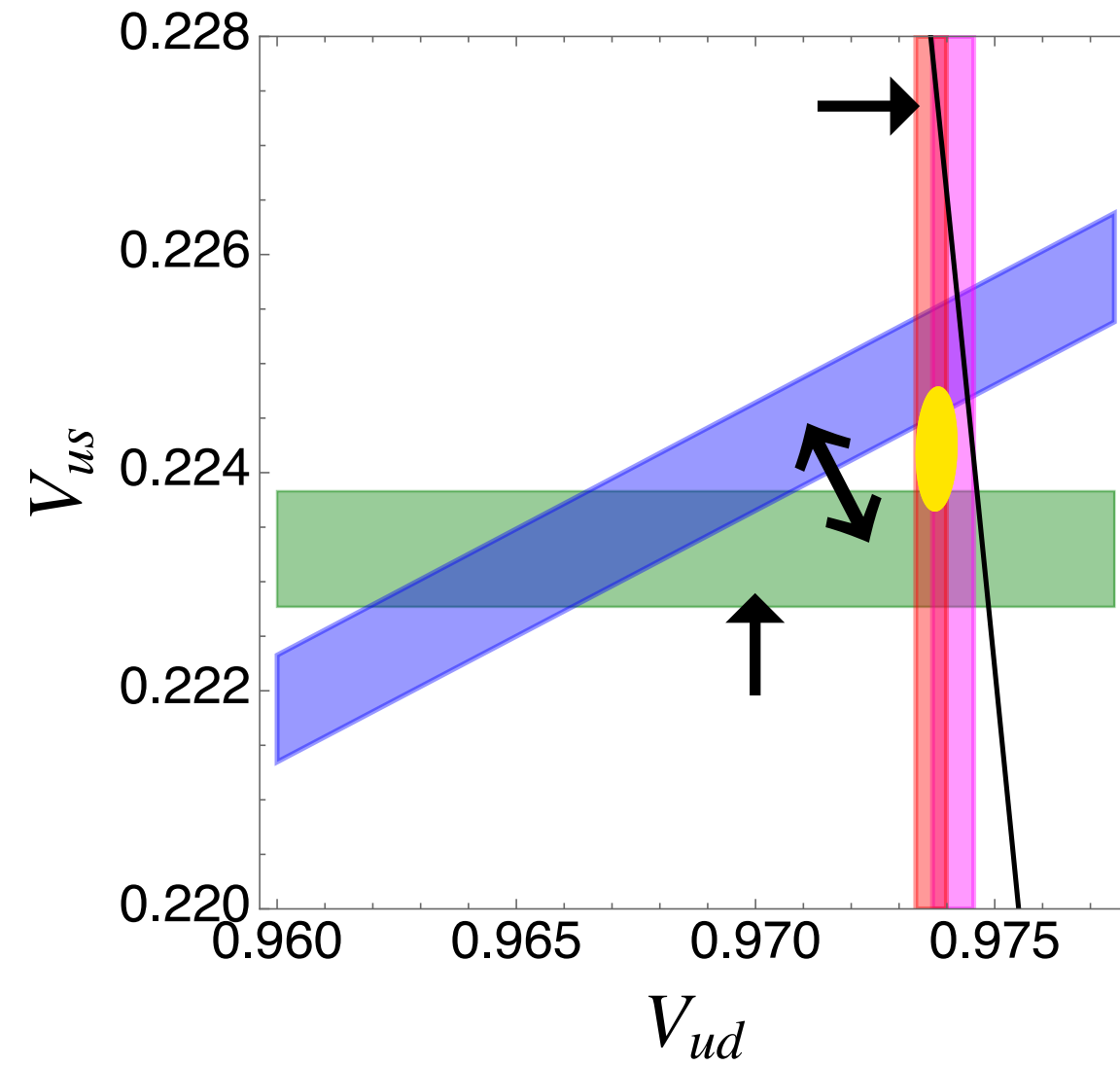
Contributes to associated Higgs + W production at the LHC



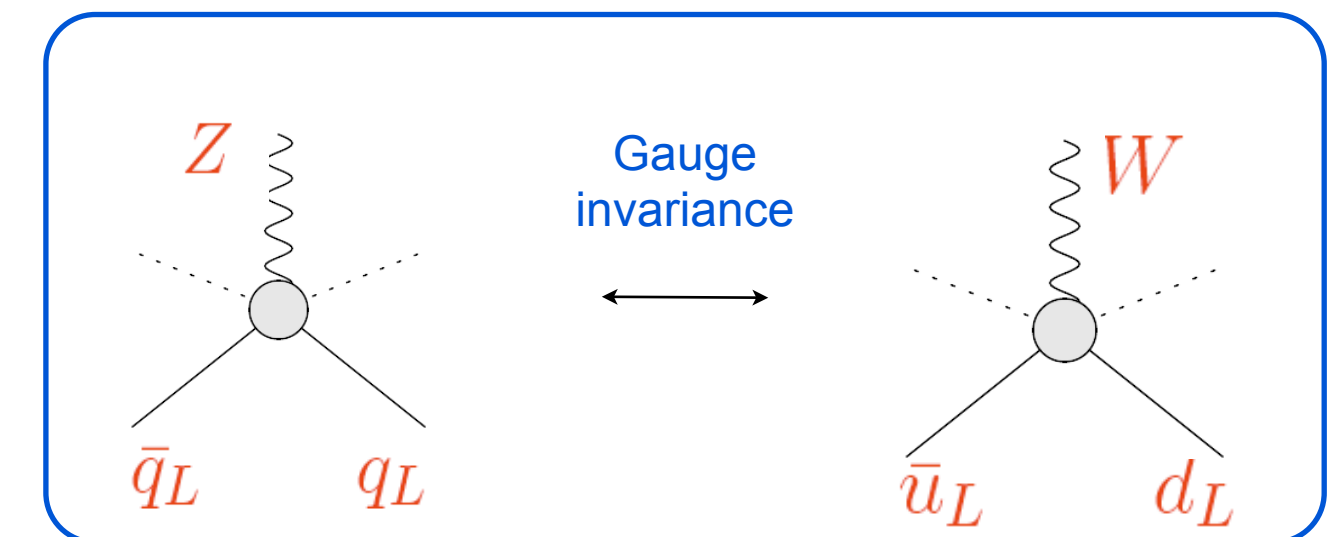
Current LHC results allow for $\epsilon_R \sim 5\%$

S. Alioli, VC, W. Dekens, J. de Vries, E. Mereghetti 1703.04751

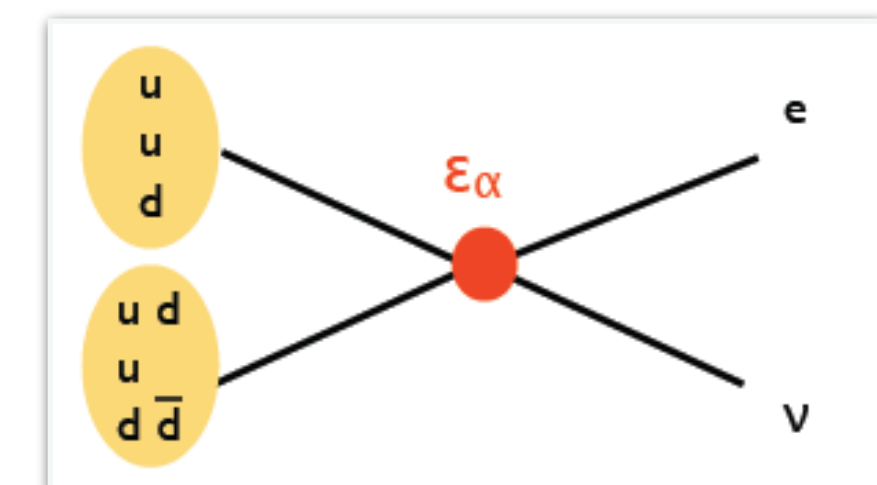
Broader perspective



Z-pole observables

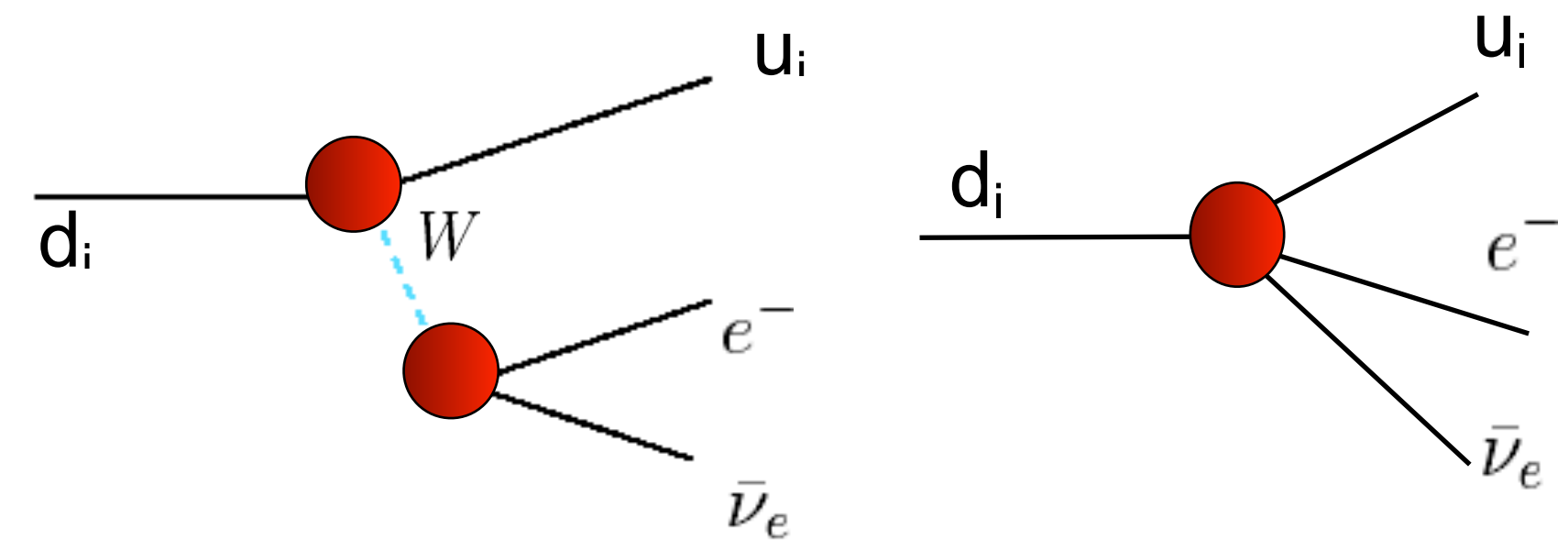
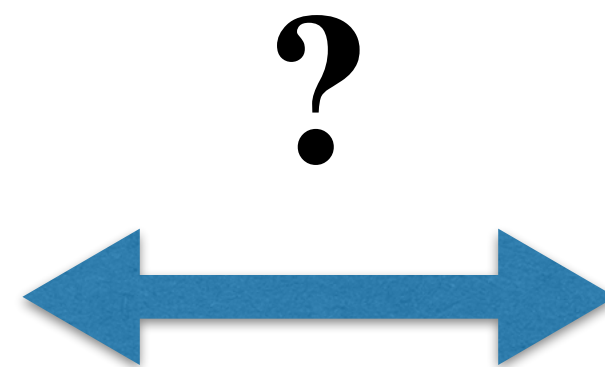
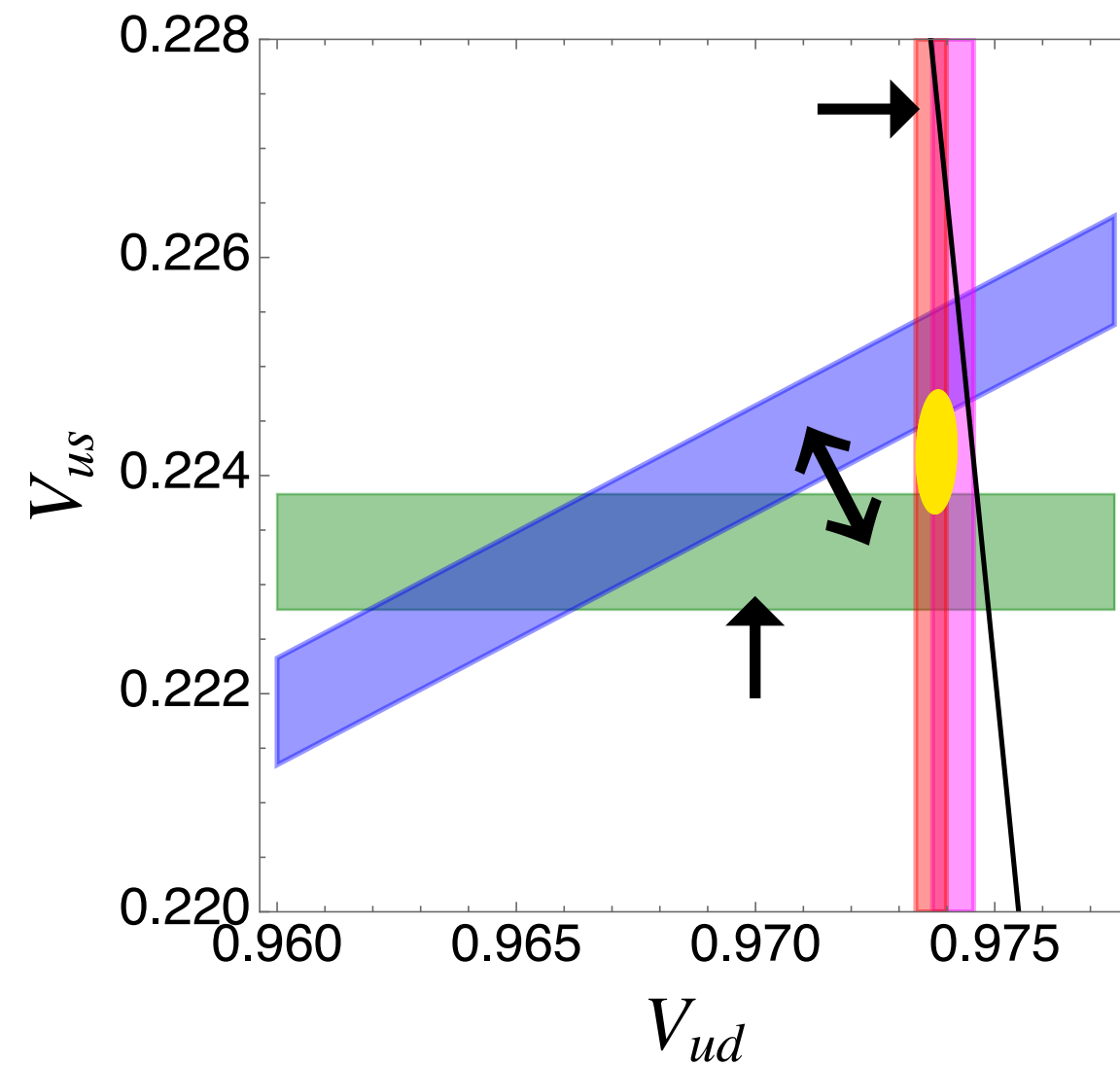


LHC: $pp \rightarrow e\nu + X$

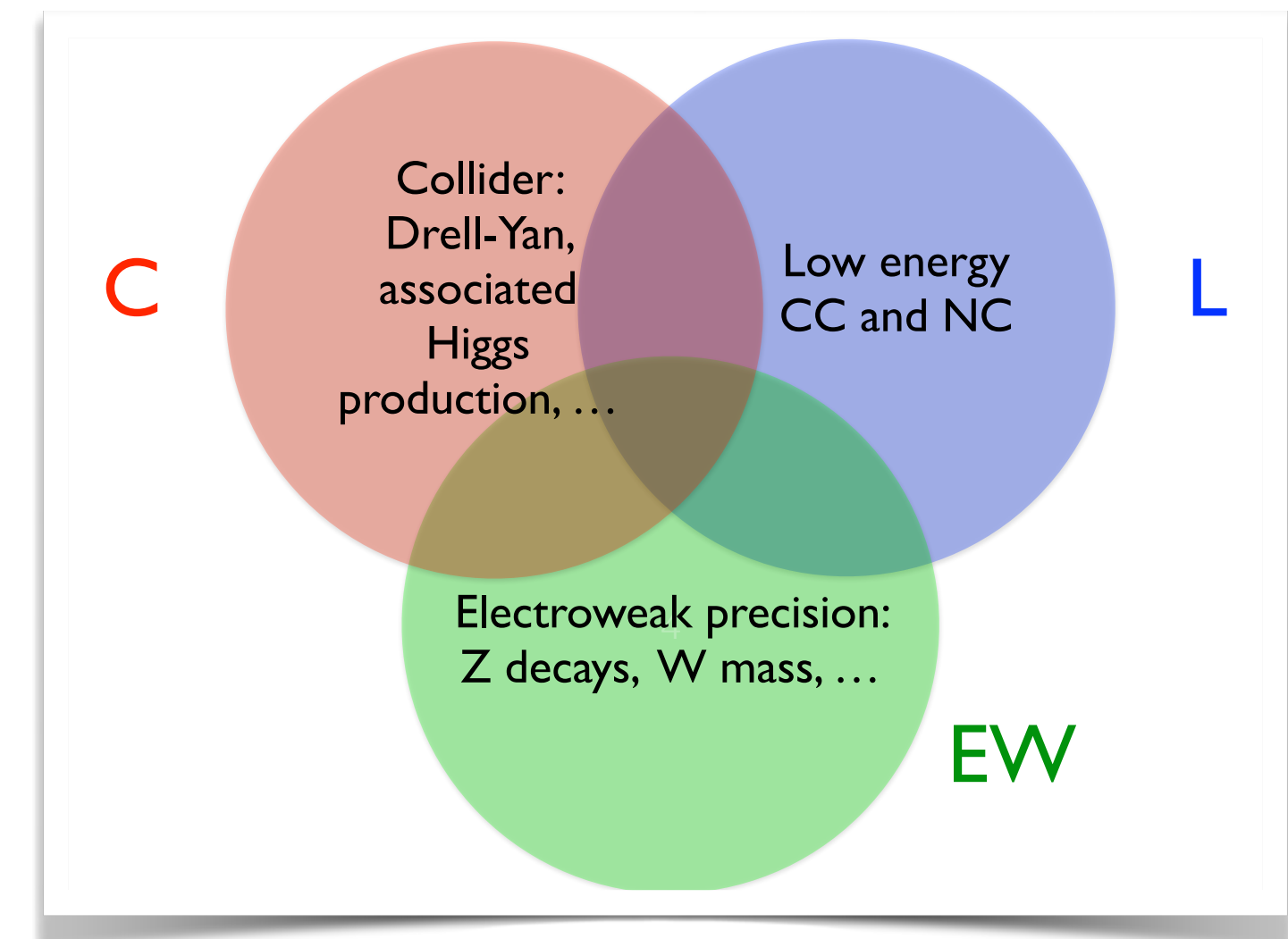


- New physics contributing to β decays also affects
 - Precision electroweak observables
 - Drell-Yan processes at colliders

Broader perspective



- New physics contributing to β decays also affects
 - Precision electroweak observables
 - Drell-Yan processes at colliders
- Need the ‘CLEW’ framework to analyze the impact of β decays on new physics (~ 40 operators)

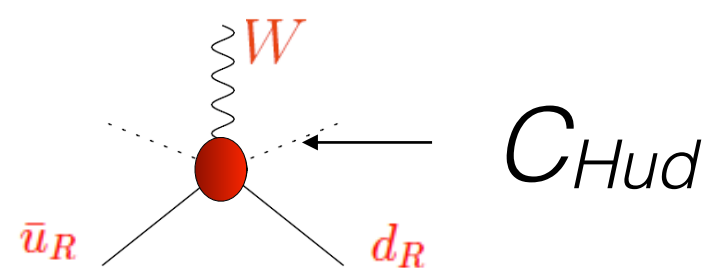


VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong, JHEP 03 (24) 33, arXiv: 2311.00021

A 'CLEWed' analysis

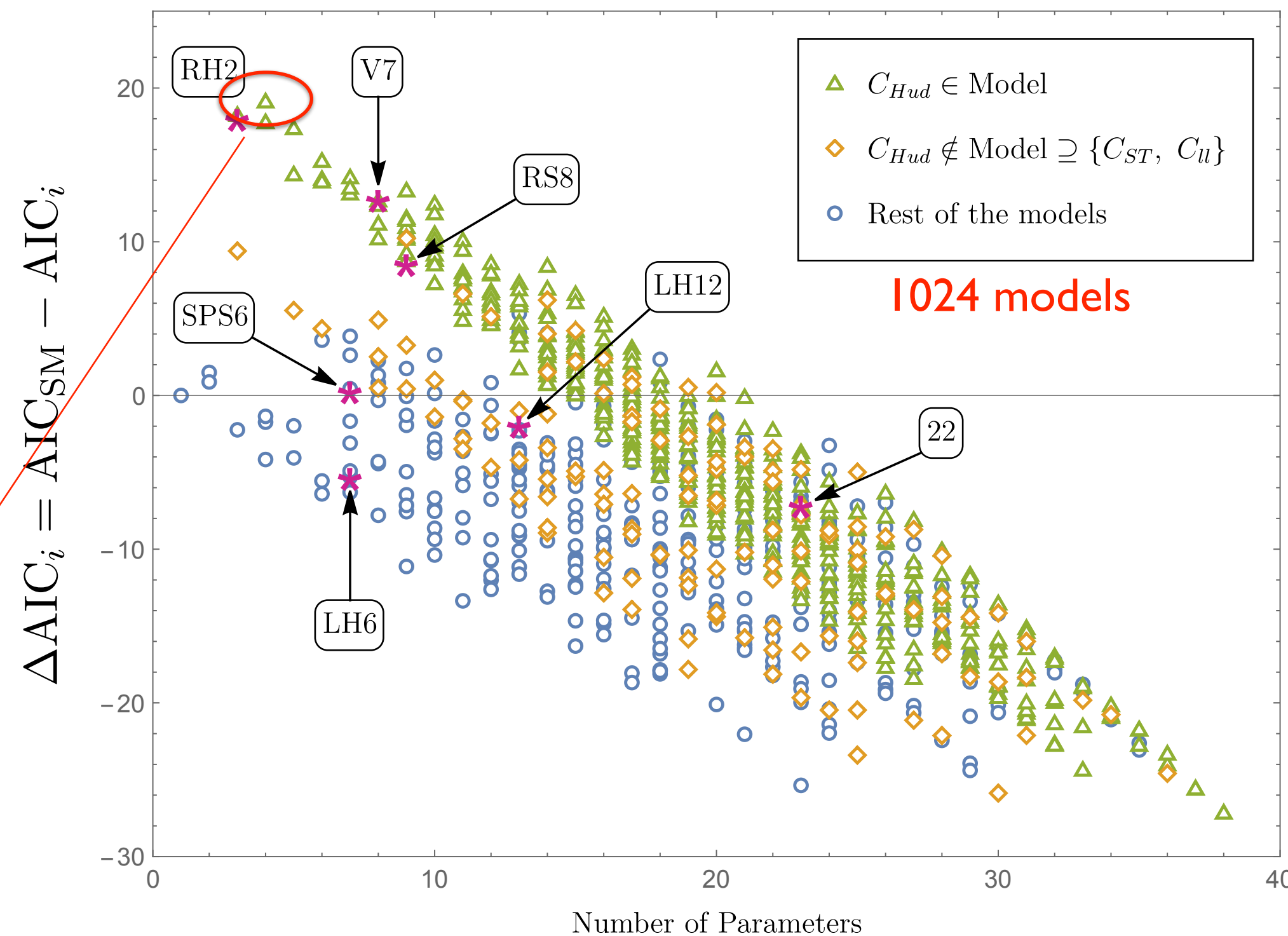
- Performed CLEW fit within SMEFT. Scanned model space by 'turning on' 10 classes of effective couplings

- Model selection? Akaike Information Criterion [$AIC = 2k - \ln(L)$] favors models with Right-Handed Charged Currents of quarks (V+A)



- Best fit to CLEW data: two RH CC vertex corrections and the S parameter

VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong,
JHEP 03 (24) 33, arXiv: 2311.00021



More favored models
↑
Standard Model
↓
Less favored models

CKM "anomaly" not ruled out by other data!
Unitarity test provides relevant input to unravel possible new physics.
Vector-like quark scenario is testable at the High-Luminosity LHC



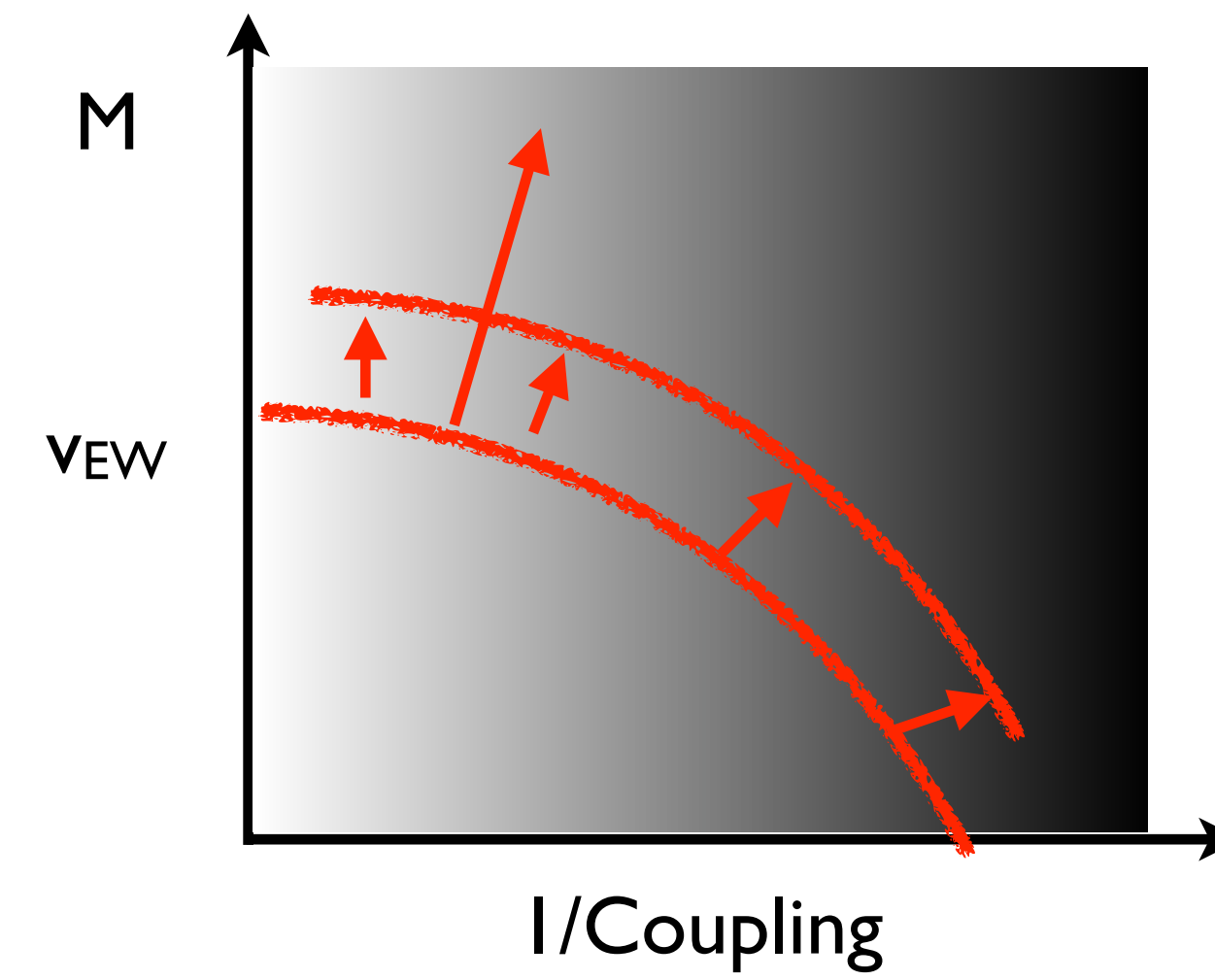
Precision beta decay outlook

- Current tensions in Cabibbo universality test could point to new physics at $\Lambda \sim \text{few TeV}$, with right-handed quark- W couplings a viable and testable culprit. However ...
- Both experimental and theoretical scrutiny is needed! Progress expected on several fronts:
 - **Experiment:** neutron, K , π , τ
 - **Theory:** lattice QCD+QED for neutron, K , π ; EFT+ 'ab-initio' methods for nuclei

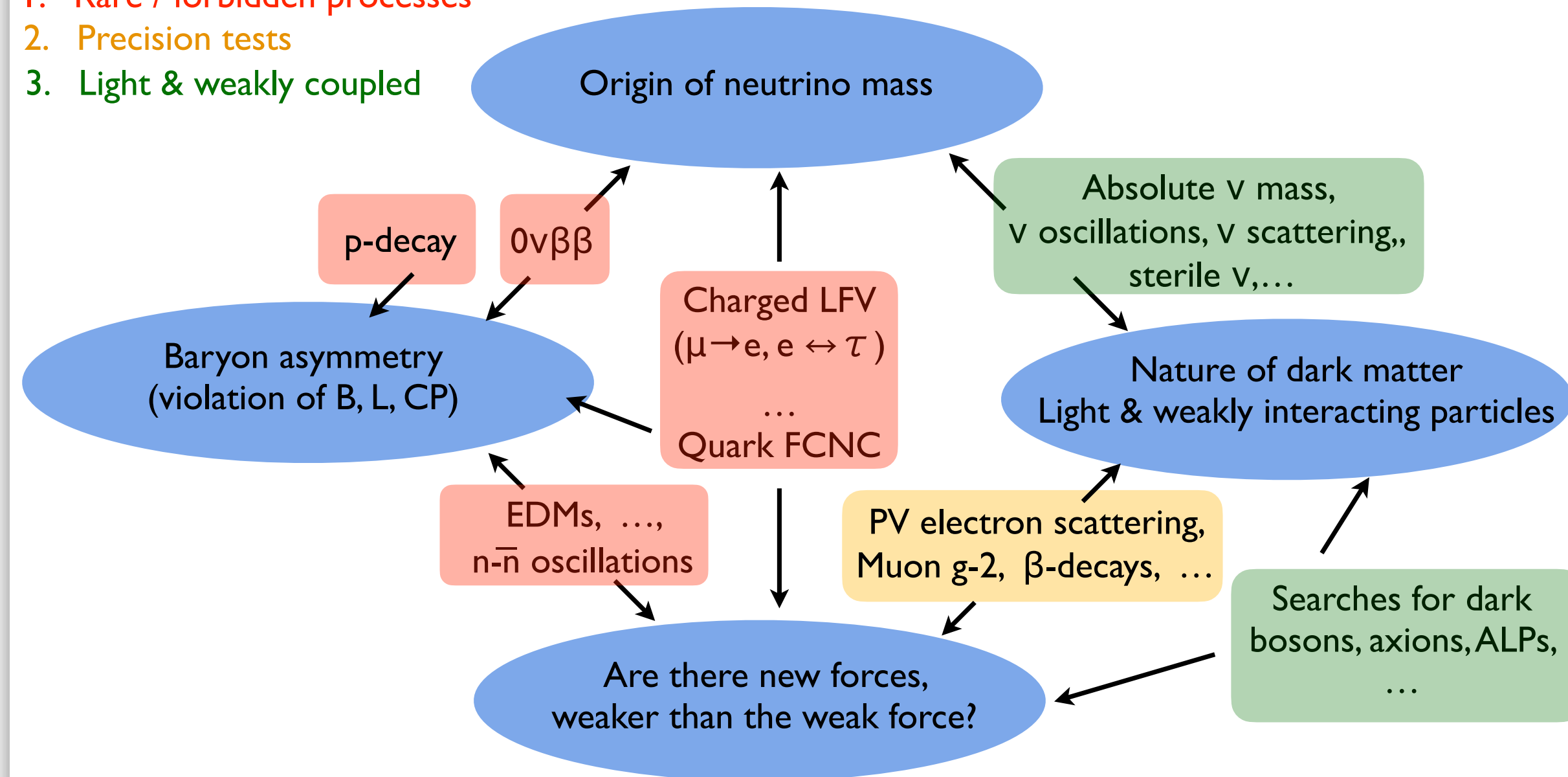
Active area of experimental and theoretical investigation

Concluding comments

- Vibrant experimental program at the low-energy Precision / Intensity Frontier is exploring uncharted territory in the search for new physics, in a complementary way to other frontiers



1. Rare / forbidden processes
2. Precision tests
3. Light & weakly coupled

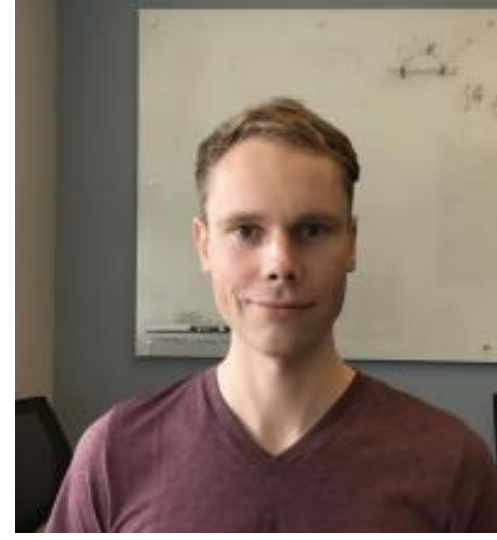


- The low-energy frontier probes BSM physics related to the ‘big questions’
- Theoretical challenges addressed by a combination of EFT, lattice QCD and other non-perturbative methods

Thanks to collaborators!



Maria Dawid



Wouter Dekens



Ayala Glick-Magid



Chien-Yeah Seng



Sasha Tomalak



Jordy de Vries



Stefano Gandolfi



Martin Hoferichter



Emanuele Mereghetti



Saori Pastore



Bira van Kolck



Andre' Walker-Loud

Thank you!



T. D. Lee in a drawing by
Bruno Touschek



Bruno Touschek
(1921-1978)

Backup

(Incomplete) List of acronyms

- ALPs: Axion-Like Particles
- BNV: Baryon Number Violation
- CC: (weak) charged current
- CP: Charge-Parity
- CPV: CP Violation
- EDM: Electric Dipole Moment
- EFT: Effective Field Theory
- FCNC: Flavor Changing Neutral Currents
- IR: infrared
- LEFT: Low Energy EFT (below the weak scale)
- LFV: Lepton Flavor Violation
- LNV: Lepton Number Violation
- NC: (weak) neutral current
- SM: Standard Model
- SMEFT: Standard Model EFT
- UV: ultraviolet

PVES on the weak mixing angle θ_W

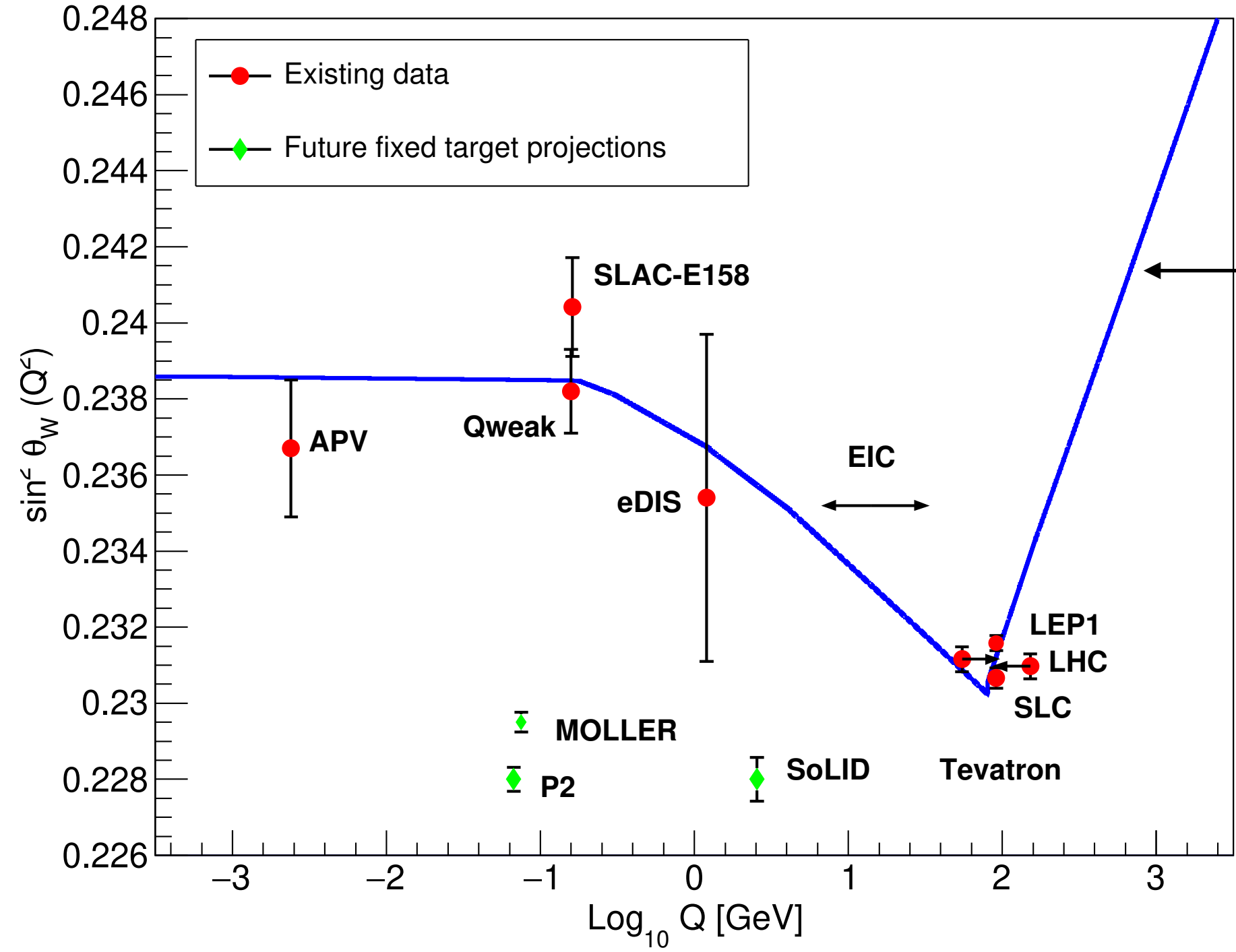
$A_{PV} = (\sigma_R - \sigma_L) / (\sigma_R + \sigma_L)$

↕

Generated by γ -Z interference

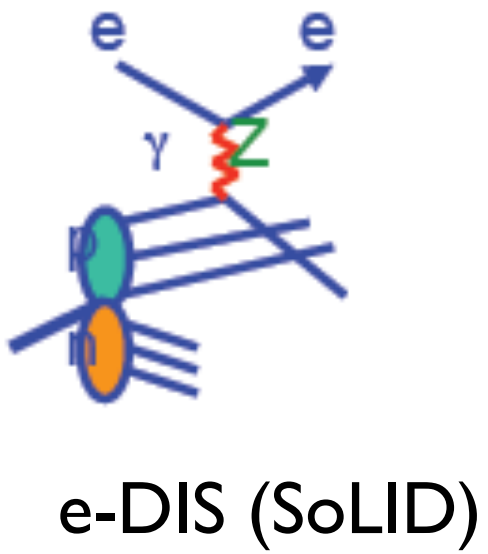
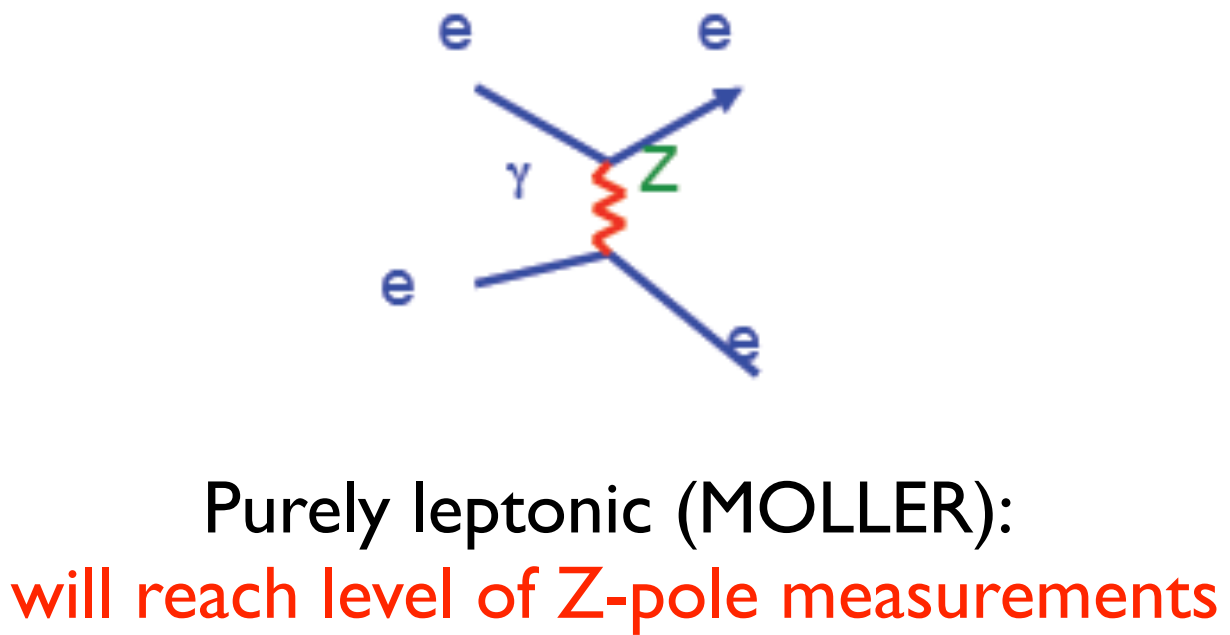
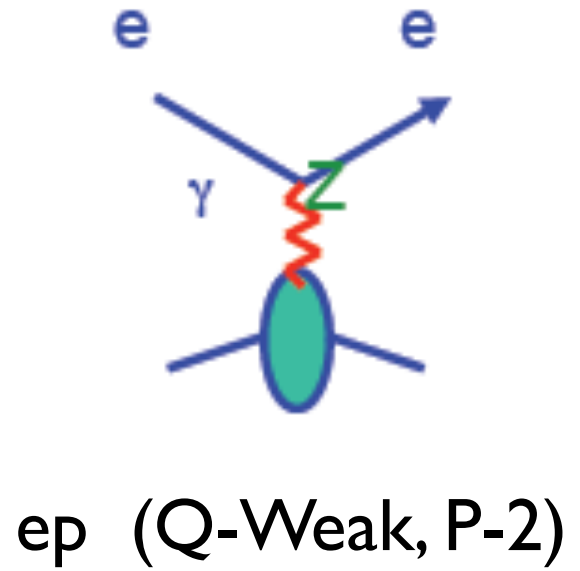
Access to
 $\theta_W = \text{ArcTan}(g_1/g_2)$

The diagrams show two interaction channels: a photon exchange (γ) and a Z boson exchange (Z). The Z boson exchange is further decomposed into its vector (V) and axial (A) components. The top diagram shows an electron-electron interaction, and the bottom diagram shows an electron-feynman (f) interaction.



SM prediction: relating EW measurements at $Q \sim 100$ GeV to low-energy

Erler & Ferro-Hernandez, 1712.09146 and references therein



PVES on the weak mixing angle θ_W

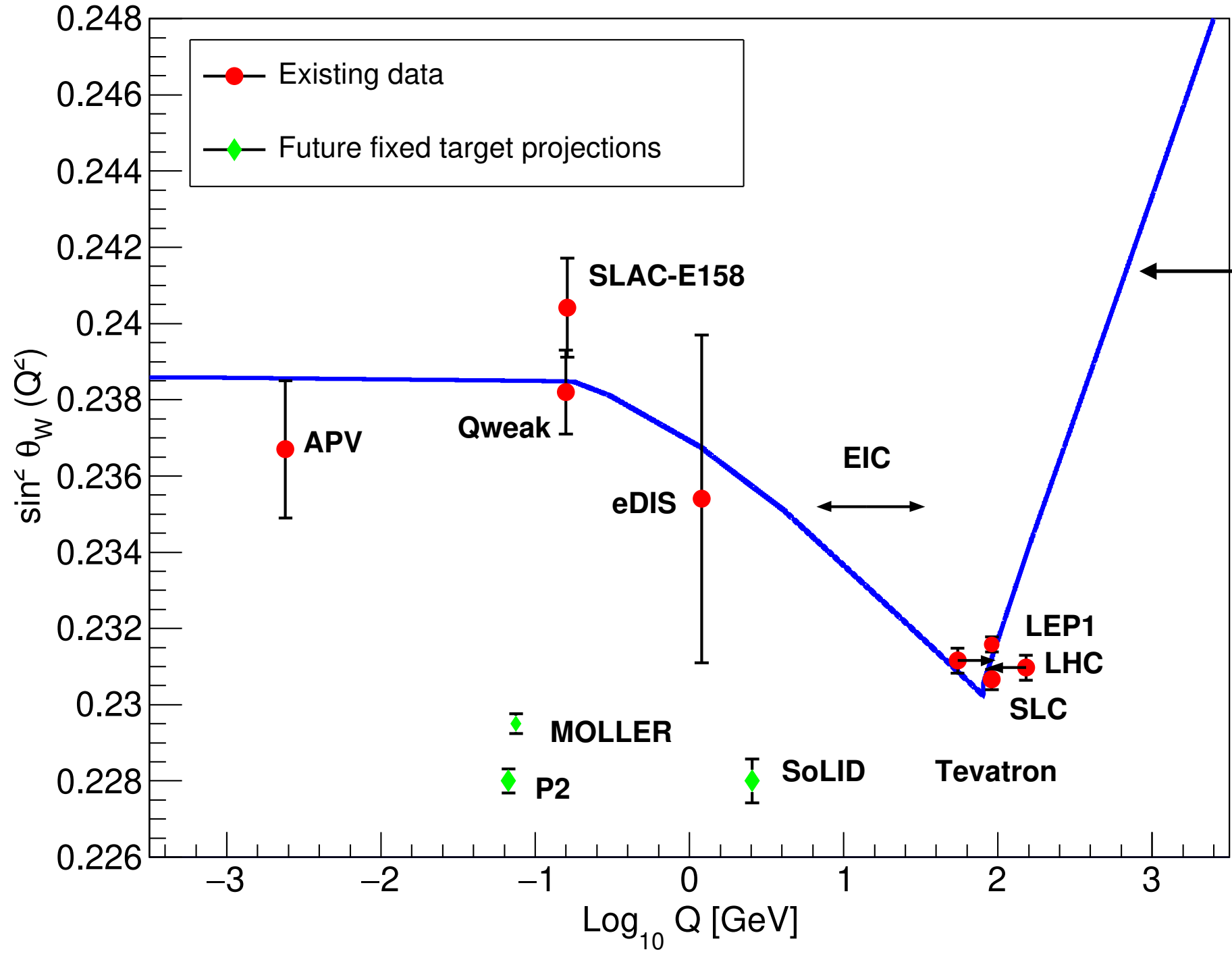
$A_{PV} = (\sigma_R - \sigma_L) / (\sigma_R + \sigma_L)$

↕

Generated by γ -Z interference

Access to $\theta_W = \text{ArcTan}(g_1/g_2)$

The diagrams show two interaction channels: $e e \rightarrow e e$ via γ exchange and $e f \rightarrow e f$ via Z exchange. The Z boson is shown with axial (A) and vector (V) couplings to the fermions.



SM prediction: relating EW measurements at $Q \sim 100$ GeV to low-energy

Erler & Ferro-Hernandez, 1712.09146 and references therein

Based on J. Erler et al. 1401.6199

$g_{AV}^{eq} \equiv 2g_A^e g_V^q$
 $g_{VA}^{eq} \equiv 2g_V^e g_A^q$
 $g_{AV}^{ee} \equiv 2g_A^e g_V^e$

vs $\frac{1}{(\Lambda_{AB}^{ij})^2}$

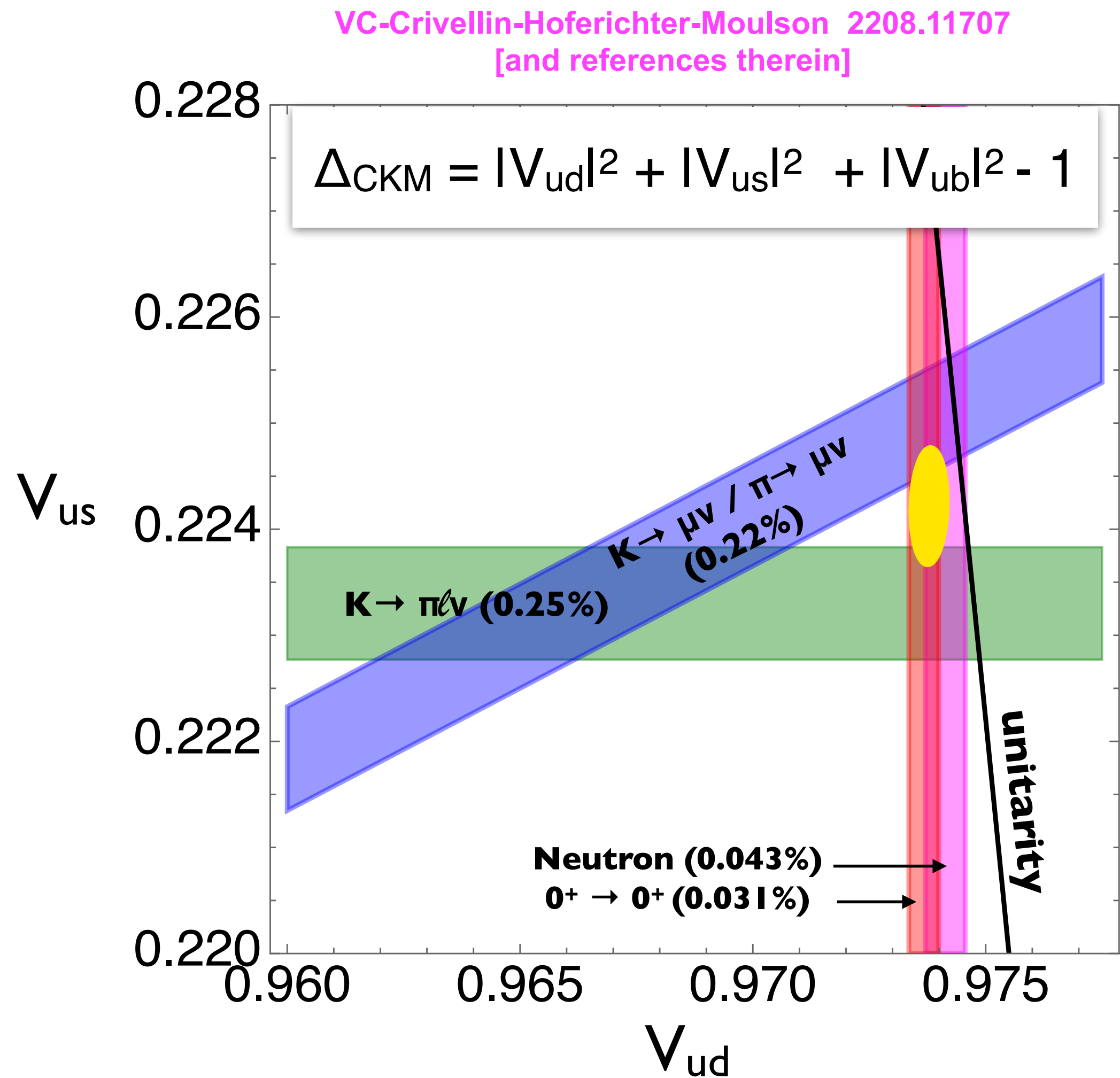
$\Lambda_{AV}^{eq} \sim 13$ TeV (P-2)

$\Lambda_{VA}^{eq} \sim 6$ TeV (SoLID)

$\Lambda_{AV}^{ee} \sim 11$ TeV (MOLLER)

Complementarity with LHC + sensitivity to low-scale new physics (Z', \dots)

Tensions in the V_{ud} - V_{us} plane



Neutron input:

$|V_{ud}|^2 \tau_n (1 + 3g_A^2)(1 + \Delta_{\text{RC}}) = 5099.3(3) \text{ s}$

Seng et al. 1807.10197, Czarnecki et al, 1907.06737
Shiells et al. 2012.01580
Hayen 2010.07262, Gorchtein-Seng 2106.09185

Feng, Gorchtein, Jin, Seng, ... 2308.16755

$V_{ud}^{n, \text{PDG}} = 0.97441(3)_f(13)_{\Delta_R}(82)_\lambda(28)_{\tau_n} [88]_{\text{total}}$

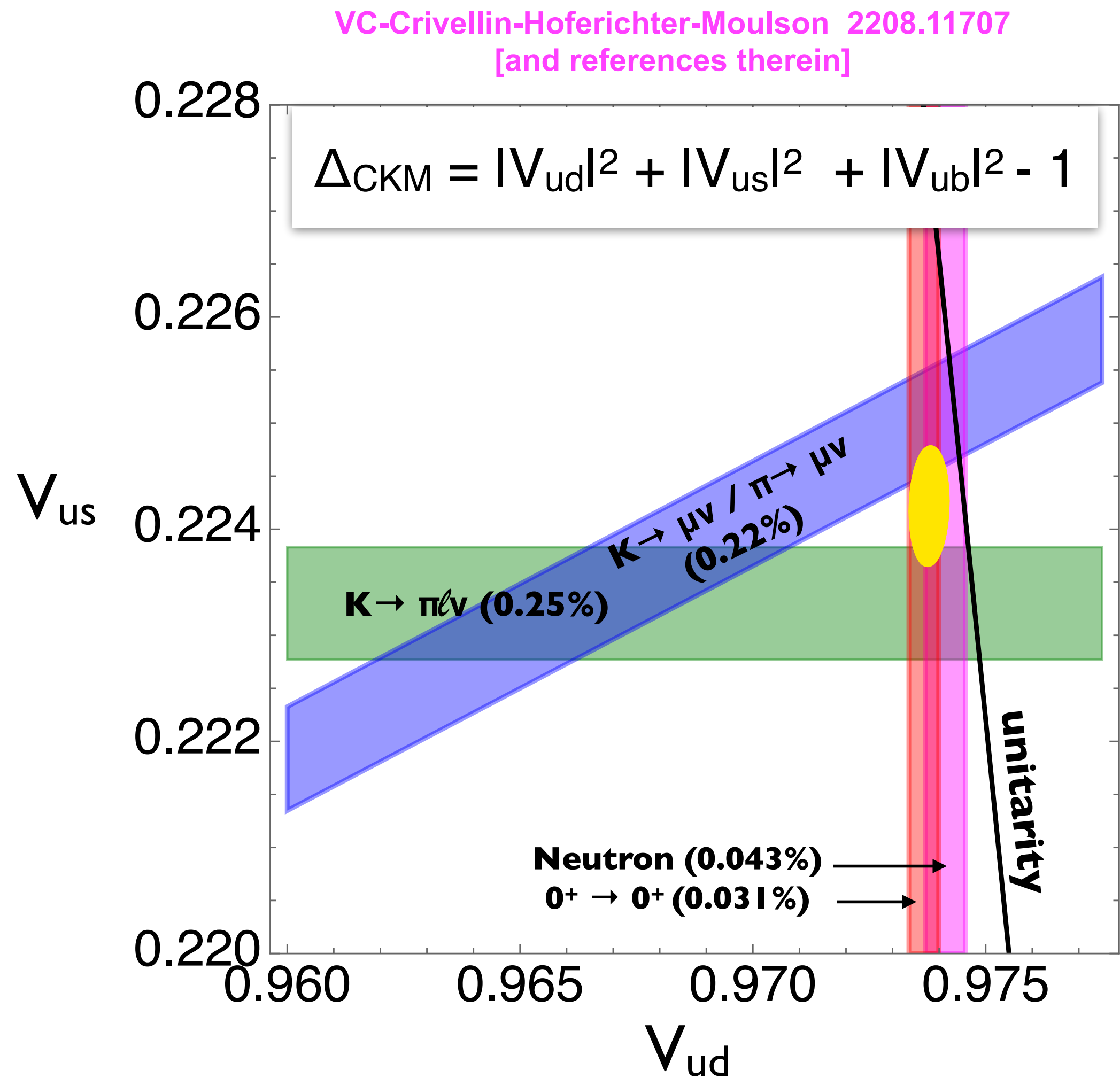
$V_{ud}^{n, \text{best}} = 0.97413(3)_f(13)_{\Delta_R}(35)_\lambda(20)_{\tau_n} [43]_{\text{total}}$

Maerkish et al,
1812.04666

$\lambda = g_A/g_V$

Gonzalez et al,
2106.10375

Tensions in the V_{ud} - V_{us} plane



$0^+ \rightarrow 0^+$ input

$$|V_{ud}|^2 = \frac{2984.432(3) s}{ft \left(1 + \delta'_R + \delta_{NS} - \delta_C + \Delta_R^V \right)}$$

Point-like nucleus
'outer corrections'

Single nucleon

$$V_{ud}^{0^+ \rightarrow 0^+} = 0.97367(11)_{\text{exp}}(13)_{\Delta_R^V}(27)_{NS}[32]_{\text{total}}$$

Hardy-Towner, PRC 2020
Gorchtein, Seng 2311.00044
review and references therein

Theoretical analysis of $R_{e/\mu}(\pi)$

$$P = (\pi, K) \quad R_{e/\mu}^{(P)} = \frac{m_e^2}{m_\mu^2} \left(\frac{m_P^2 - m_e^2}{m_P^2 - m_\mu^2} \right)^2 \times \left[1 + \Delta_{e^2 Q^0}^P + \Delta_{e^2 Q^2}^P + \Delta_{e^2 Q^4}^P + \dots + \Delta_{e^4 Q^0}^P + \dots \right]$$

- F_π drops in the e/μ ratio \rightarrow hadronic structure dependence appears only through EM corrections

- Organize calculation in EFT (ChPT):

$$Q \sim m_{\pi, K, \mu} / \Lambda_\chi \quad \Lambda_\chi \sim 4\pi F_\pi \sim 1.2 \text{ GeV}$$

- NLO correction \leftrightarrow point-like mesons (Kinoshita 59)



No contact (LEC):
contribution cancels
in the ratio!

$$\Delta_{e^2 Q^0}^\pi \sim -3\alpha/\pi \log m_\mu/m_e \sim -3.929\%$$

Use RGE to resum large IR logs (Marciano and Sirlin 1993)

$$\Delta_{e^4 Q^0}^{(\pi)} = 0.055(3)\%$$

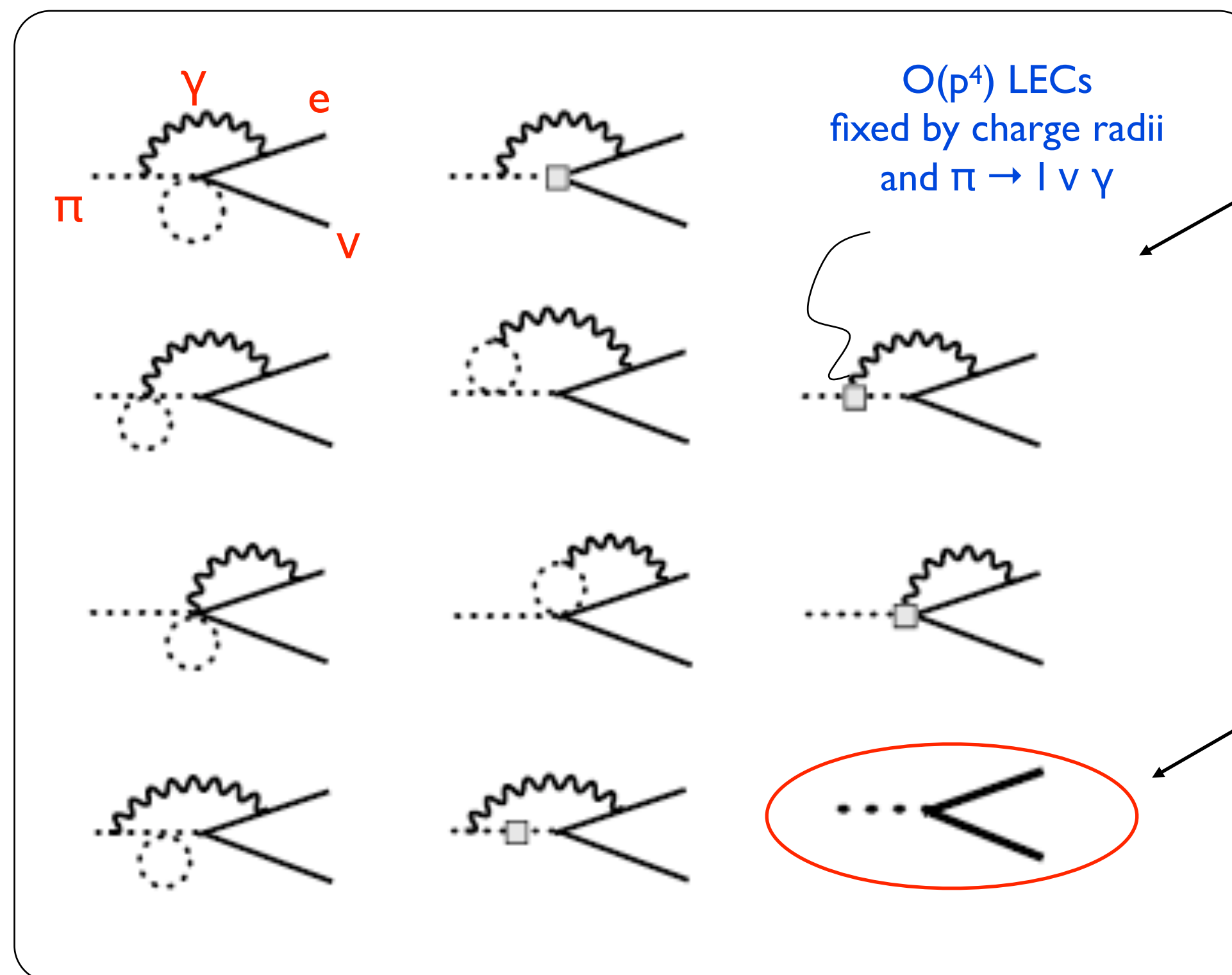
Theoretical analysis of $R_{e/\mu}(\pi)$

$$P = (\pi, K) \quad R_{e/\mu}^{(P)} = \frac{m_e^2}{m_\mu^2} \left(\frac{m_P^2 - m_e^2}{m_P^2 - m_\mu^2} \right)^2 \times \left[1 + \Delta_{e^2 Q^0}^P + \Delta_{e^2 Q^2}^P + \Delta_{e^2 Q^4}^P + \dots + \Delta_{e^4 Q^0}^P + \dots \right]$$

- Structure dependence appears at NNLO in ChPT!

$$\Delta_{e^2 Q^2}^\pi = 0.053(11)\%$$

$$\Delta_{e^2 Q^4}^\pi = 0.073(3)\%$$



1) One- and two-loop diagrams \Rightarrow
model-independent
single and double logs

2) $O(e^2 p^4)$ Low Energy Constant (LEC; estimated within large- N_c inspired resonance model (satisfying QCD s.d. constraints). Small contribution to final result, largest uncertainty

3) Str. Dep. Real photon emission, not helicity suppressed

Theoretical analysis of $R_{e/\mu}(\pi)$

$P = (\pi, K)$

$$R_{e/\mu}^{(P)} = \frac{m_e^2}{m_\mu^2} \left(\frac{m_P^2 - m_e^2}{m_P^2 - m_\mu^2} \right)^2 \times \left[1 + \Delta_{e^2 Q^0}^P + \Delta_{e^2 Q^2}^P + \Delta_{e^2 Q^4}^P + \dots + \Delta_{e^4 Q^0}^P + \dots \right]$$

Theory

$$R_{e/\mu}^{(\pi)} = 1.23524(015) \times 10^{-4}$$

Marciano-Sirlin, 1993, PRL →
VC-Rosell 0707.3439, PRL

Experiment

$$R_{e/\mu}^{(\pi)} = 1.23270(230) \times 10^{-4}$$

PIENU Coll., PRL 2015
PDG 2020

Theory result provides robust baseline for
new physics searches.

Might be further improved in the next
decade through lattice QCD+QED

