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UW Trapped Ion Lab

Quantum State Detection of a Barium-138 Ion in a Non-steady State Evolution

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Constructing a physical Qubit

Qubit: Most basic unit of information for Quantum Computing

Important Criteria for a physical qubit

- 1. Scalability
- 2. Long and Stable states
- 3. Measurement Capability

Barium Ion Qubit \rightarrow State Dependent Fluorescence

2-level atom interacting with External Field



Bare Hamiltonian

$$\widehat{H}_0 = E_1 |1\rangle \langle 1| + E_2 |2\rangle \langle 2| = \begin{bmatrix} E_1 & 0\\ 0 & E_2 \end{bmatrix} = \hbar \begin{bmatrix} \omega_1 & 0\\ 0 & \omega_2 \end{bmatrix}$$
$$= \hbar \begin{bmatrix} 0 & 0\\ 0 & \omega_0 \end{bmatrix} \quad (\omega_0 = \omega_2 - \omega_1)$$

Interaction Hamiltonian

$$\widehat{H}_{1}(t) = e\vec{r} \cdot \overrightarrow{E_{0}} \cos(\omega t) = \frac{\hbar}{2} \Omega(e^{i\omega t} |1\rangle \langle 2| + e^{-i\omega t} |2\rangle \langle 1|)$$

Rabi frequency:
$$\Omega = \frac{eE_{0}}{\hbar} \langle 1|\vec{r} \cdot \vec{e}_{rad} |2\rangle$$

Total Hamiltonian

Bare Hamiltonian

$$\widehat{H}_0 = \hbar \begin{bmatrix} 0 & 0 \\ 0 & \omega_0 \end{bmatrix} \quad (\omega_0 = \omega_2 - \omega_1)$$

$$\widehat{H} = \widehat{H}_0 + \widehat{H}_1 = \frac{\hbar}{2} \begin{bmatrix} 0 & \Omega e^{i\omega t} \\ \Omega e^{-i\omega t} & 2\omega_0 \end{bmatrix}$$

Rotating Frame Transformation

 $\widetilde{H} = \widehat{U}\widehat{H}\widehat{U}^{\dagger}$ $\widehat{U} = e^{i\omega t|2\rangle\langle 2|}$

$$\widetilde{H} = \frac{\hbar}{2} \begin{bmatrix} 0 & \Omega \\ \Omega & 2\Delta \end{bmatrix} \quad (\Delta = \omega - \omega_0)$$

Interaction Hamiltonian

$$\widehat{H}_{1}(t) = \frac{\hbar}{2} \Omega(e^{i\omega t} |1\rangle \langle 2| + e^{-i\omega t} |2\rangle \langle 1|)$$



Figure 1. Time evolution of 2-level atom interacting with an external resonant electric field

Spontaneous Decay

 $\begin{array}{c} |2\rangle \\ \hline \\ |1\rangle \end{array}$ Lifetime τ

Decay Rate $\Gamma = \tau^{-1}$

Collapse Operator $C = \sqrt{\Gamma} |1\rangle\langle 2|$



Figure 2. Change in time evolution of 2-level atom interacting with an external resonant electric field with increasing decay rate

State Detection of ¹³⁸Ba⁺ qubit



Coherent Dark States



Electron gets trapped in "dark states"

 $c_S \Omega_S = -c_D \Omega_D$

$$(|\psi\rangle = c_S |S\rangle + c_D |D\rangle + 0 |P\rangle)$$

Destructive Interference

Modeling 3 level system of ¹³⁸Ba⁺





Figure 4. Time evolution of a 3-level Ba ion reaching a steady dark state while both resonance lasers applied

Alternating laser pulses



Figure 5. Time evolution of 3-level Ba ion while two resonance lasers are alternating pulses

Optimizing Laser pulse intervals



Optimal Interval 493nm laser: 42.74 ns 650nm laser: 26.64 ns

Average probability in P state: 0.254

Figure 6. 3-level Ba ion's average p state probability while varying interval of laser pulses

Optimizing Laser pulse intervals



Figure 7. Time evolution of 3-level Ba ion while alternating two resonance pulses at optimal interval lengths identified by optimization algorithms

Zeeman Splitting



Selection Rule

Quantization Axis: direction along which magnetic field is aligned (z-axis)

Photon	Transition Rules	$\Delta m_i =$
j = 1	1. $\Delta l = \pm 1$	$\Delta m_i =$
$m_j = -1,0,1$	2. $\Delta m_j = -1,0,1$	$\Delta m_j =$

 $\Delta m_j = +1 : \sigma_+$ Transition $\Delta m_j = -1 : \sigma_-$ Transition $\Delta m_j = 0 : \pi$ Transition



Figure 8. Right-handed circularly polarized light (Image by Dave3457, Public Domain via Wikimedia Commons)

Electric field

- $\sigma_{\rm +}$ Right circular polarization
- σ_{-} Left circular polarization
- $\pi\,$ Linear Polarization along the quantization axis

Modeling 8 level system of ¹³⁸Ba⁺

 $S_{-1/2} = |0\rangle$ $S_{+1/2} = |1\rangle$ $P_{-1/2} = |2\rangle$ $P_{+1/2} = |3\rangle$ $D_{-3/2} = |4\rangle$ $D_{-1/2} = |5\rangle$ $D_{\pm 1/2} = |6\rangle$ $D_{+3/2} = |7\rangle$



 \vec{B} field is along z-axis

$$\hat{e}_{rad} = \begin{bmatrix} \sin \theta \\ 0 \\ \cos \theta \end{bmatrix}$$

z-component: drives π transition x-component: drives a linear combination of sigma+ and sigmatransitions

Optimizing Different Polarization Angle







Optimizing Laser Intervals



Figure 11. Time evolution of 8-level Ba ion while alternating two resonance pulses at optimal interval lengths identified by optimization algorithms

Coherent Dark state w/n D_{3/2} orbital



 \rightarrow Alternate polarization

Alternating Polarization of 650nm Laser



Figure 12. 8-level Ba ion time evolution for varying interval lengths of z-polarized laser pulses

Optimizing interval of polarized Laser pulses



Figure 13. Probability in p state for varying interval lengths of z-polarized laser pulses

within 80 ns of 650 nm laser pulse Optimal intervals z-polarized laser pulse: 44.10 ns x-polarized laser pulse: 35.90 ns

Average p state probability: 0.162

Optimal interval of polarized laser pulses



Figure 14. Time evolution of 8-level Ba ion while alternating differently polarized 650 nm laser pulses at optimal intervals



Future Work

- Study more theory to understand and reason the results
 - Coherent dark states
 - Solve Hamiltonian and Eigenstates
- Changing polarization
 - Distinguishing sigma+ and sigmatransitions
 - Elliptical polarization
- Coherent Bright States

Thank You, Questions?

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Back up: 8 level ¹³⁸Ba⁺ Hamiltonian

$$H = \begin{pmatrix} \Delta_g - u & 0 & \frac{\Omega_g}{\sqrt{3}} \cos \alpha & -\frac{\Omega_g}{\sqrt{3}} \sin \alpha & 0 & 0 & 0 & 0 \\ 0 & \Delta_g + u & -\frac{\Omega_g}{\sqrt{3}} \sin \alpha & -\frac{\Omega_g}{\sqrt{3}} \cos \alpha & 0 & 0 & 0 & 0 \\ \frac{\Omega_g}{\sqrt{3}} \cos \alpha & -\frac{\Omega_g}{\sqrt{3}} \sin \alpha & -\frac{1}{3}u & 0 & -\frac{\Omega_r}{2} \sin \alpha & -\frac{\Omega_r}{\sqrt{3}} \cos \alpha & \frac{\Omega_r}{2\sqrt{3}} \sin \alpha & 0 \\ -\frac{\Omega_g}{\sqrt{3}} \sin \alpha & -\frac{\Omega_g}{\sqrt{3}} \cos \alpha & 0 & \frac{1}{3}u & 0 & -\frac{\Omega_r}{2\sqrt{3}} \sin \alpha & -\frac{\Omega_r}{\sqrt{3}} \cos \alpha & \frac{\Omega_r}{2} \sin \alpha \\ 0 & 0 & -\frac{\Omega_r}{2} \sin \alpha & 0 & \Delta_r - \frac{6}{5}u & 0 & 0 & 0 \\ 0 & 0 & -\frac{\Omega_r}{\sqrt{3}} \cos \alpha & -\frac{\Omega_r}{2\sqrt{3}} \sin \alpha & 0 & \Delta_r - \frac{2}{5}u & 0 & 0 \\ 0 & 0 & \frac{\Omega_r}{2\sqrt{3}} \sin \alpha & -\frac{\Omega_r}{\sqrt{3}} \cos \alpha & 0 & 0 & \Delta_r + \frac{2}{5}u & 0 \\ 0 & 0 & 0 & \frac{\Omega_r}{2} \sin \alpha & 0 & 0 & 0 & \Delta_r + \frac{6}{5}u \end{pmatrix}$$

Energy shift $\Delta E = m_J g_J u$ $u = \mu_B \vec{B}$

 Δ detuning

Constants

result of angular integral (inner product) evaluating the coupling between the states $\langle i | e \vec{r} \cdot \vec{e}_{rad} | j \rangle$

Figure 15. Hamiltonian of 8-level Barium Ion system (adapted from Sosnova, 2020)