

Single Photon Blockade in Nanocavities with Weak Kerr Nonlinearity (Application)

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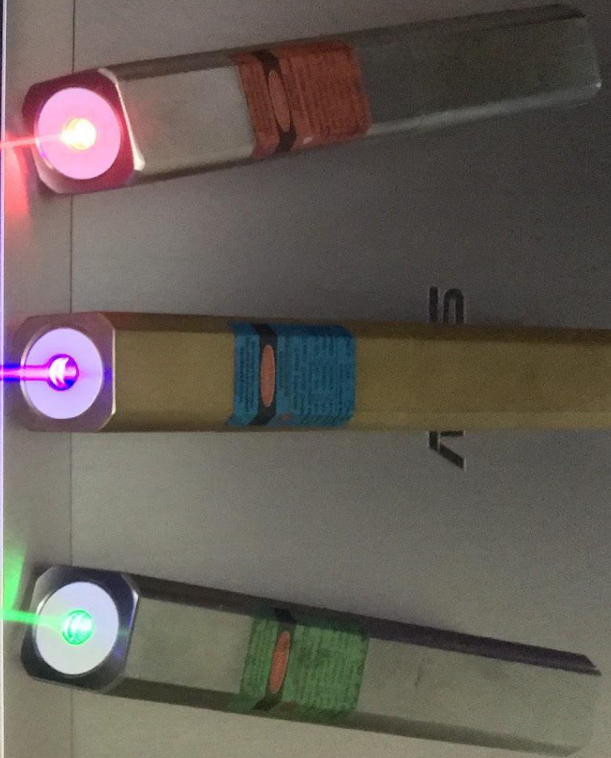
Outline

- Background
 - Cavities
 - Kerr Nonlinearity
 - Photon Blockade with nonlinear cavities
- Model for Si
 - Limitations on System
 - Calculating Nonlinear Coupling Strength (U) for Si
- Results
- Future Work
- Acknowledgements
- References

Background

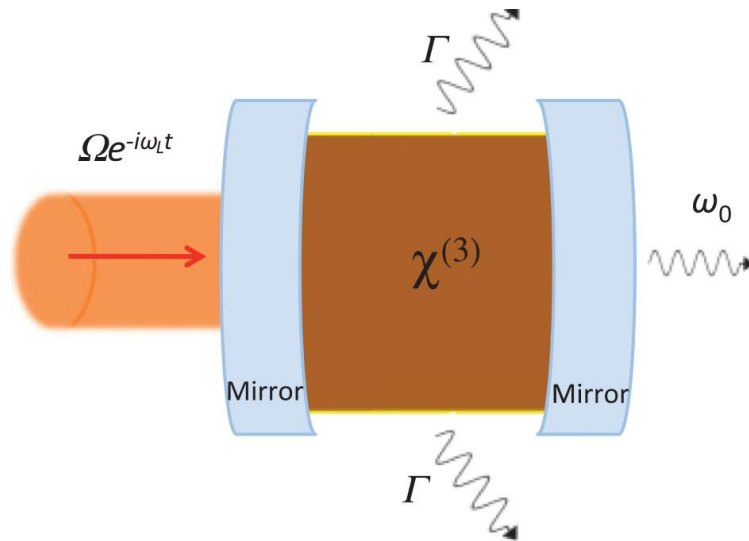
What tools exist to manipulate light?

- Lasers
- Cavities
- Non-linear materials
- Many more beyond the scope of this presentation



What are cavities?

- A resonator for E-M radiation
- Can trap photons



Maxwell's Equations in Matter



Where $\mathbf{D}$ is given by the following:

$$\mathbf{D} = \epsilon_0 \mathbf{E} + \mathbf{P}$$

In linear media,
we have the
following:

$$\mathbf{P} = \epsilon_0 \chi \mathbf{E}$$

$$\nabla \cdot \mathbf{D} = \rho$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

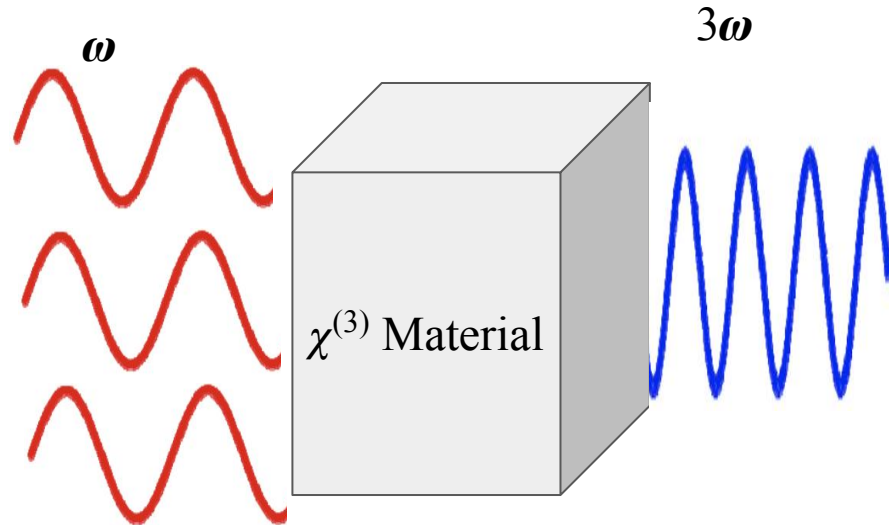
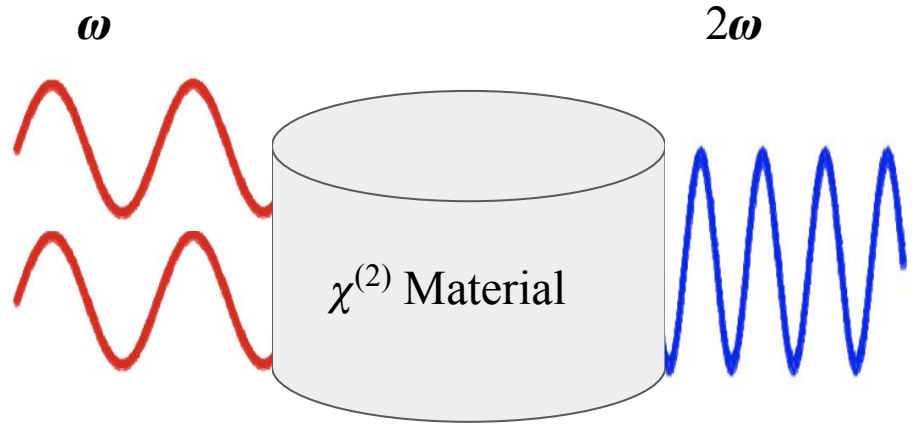
$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t}$$

Kerr Nonlinearity

The polarization can be generalized to...

$$\mathbf{P} = \epsilon_0[\chi\mathbf{E} + \chi^{(2)}\mathbf{E}^2 + \chi^{(3)}\mathbf{E}^3 + \dots]$$

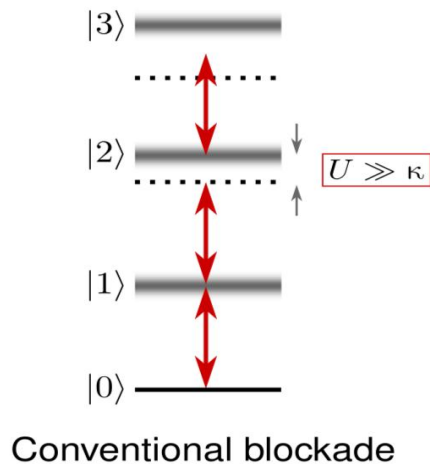
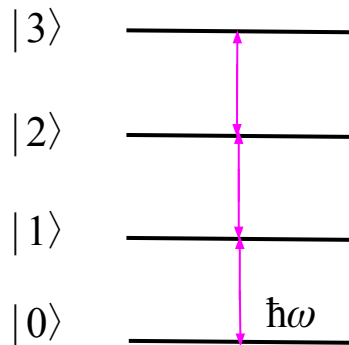
- The properties of the incident light are changed due to the material's response
- Can be applied to **cavities**, **quantum optics**, fiber optic systems, and more



Photon blockade with nonlinear cavities

Basic Ingredients:

- Nonlinear Coupling Strength (U)
- Source of light (laser)



Model for Si

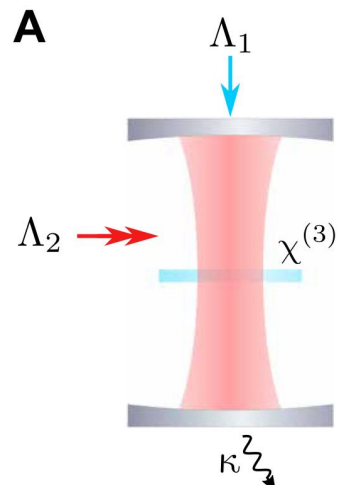
Overview for Simulation

- Used QuTIP to model a photon blockade with a Si nonlinear cavity

$$\frac{d}{dt}\hat{\rho} = -i[\hat{H}, \hat{\rho}] + \kappa\mathcal{D}[a]\hat{\rho}$$

Limitations on System

- Light can escape the cavity or cavity can absorb photons and can be modeled by the cavity decay rate (κ)
- Displacement errors



Calculating Nonlinear Coupling Strength (U) for Si

Parameters:

$$\chi^{(3)} = 0.45 \times 10^{-18} \frac{\text{m}^2}{\text{V}^2}$$

$$V_{\text{eff}} = 10^{-20} \text{ m}^3$$

$$\epsilon_r^2 = n^4 = (3.4)^4$$

$$\hbar\omega_0 = \frac{hc}{\lambda} = \frac{1240 \text{ nm eV}}{1550 \text{ nm}} = 0.8 \text{ eV}$$

Calculating U:

$$\begin{aligned} U &= \frac{3(\hbar\omega_0)^2}{4\epsilon_0 V_{\text{eff}}} \frac{\chi^{(3)}}{\epsilon_r^2} \\ &= 4.68 \times 10^{-28} \text{ J} \\ &= \frac{4.68 \times 10^{-28} \text{ J}}{10^6 \times 6.63 \times 10^{-34} \text{ Js}} \\ U &\approx 0.705 \text{ MHz} \end{aligned}$$

Results

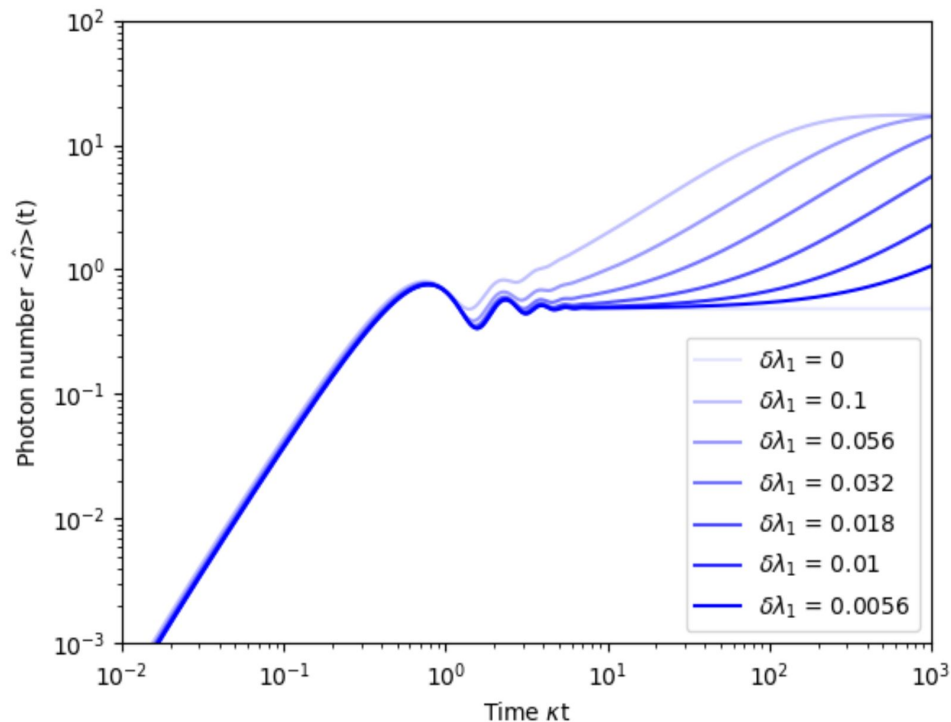
Simulation of Mismatched Drive Amplitude on Blockade Dynamics for Si

Drive Mismatch:

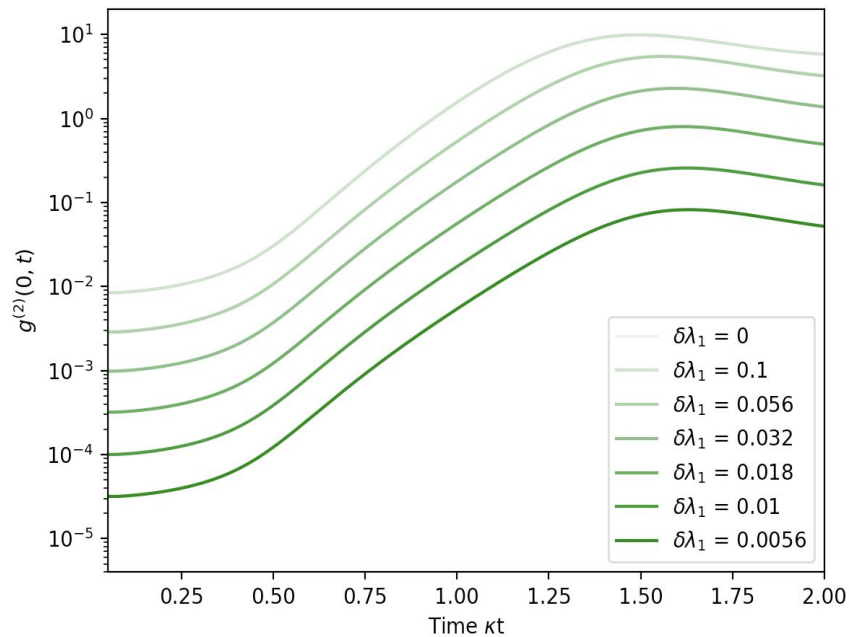
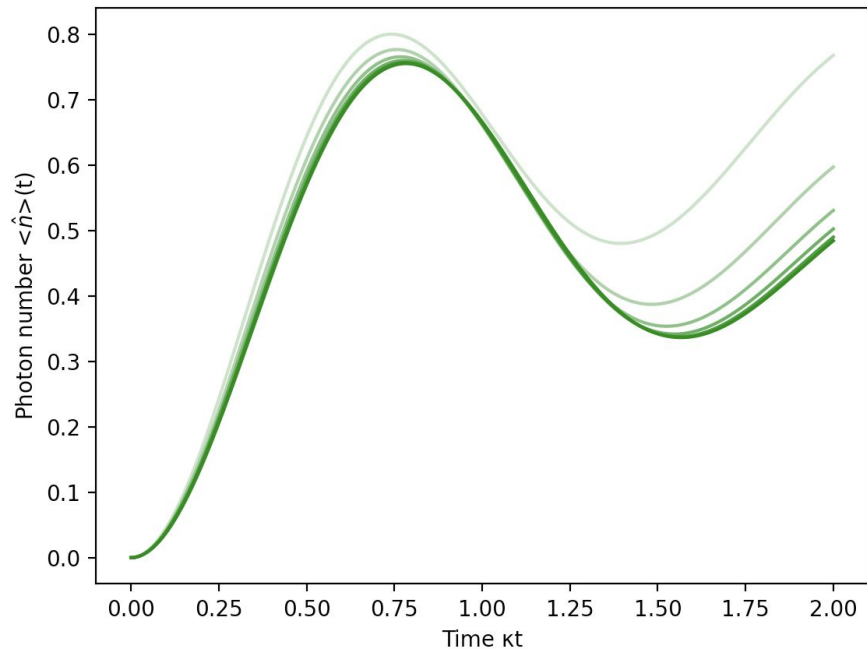
$$\tilde{\Lambda}_1 = -\tilde{\Lambda}_3(1 + \delta\lambda_1) = -\tilde{\Lambda}_3 r$$

Parameters used for simulation:

- $\kappa = 1$ MHz
- $U = 0.705$ MHz
- $N = 60$ states



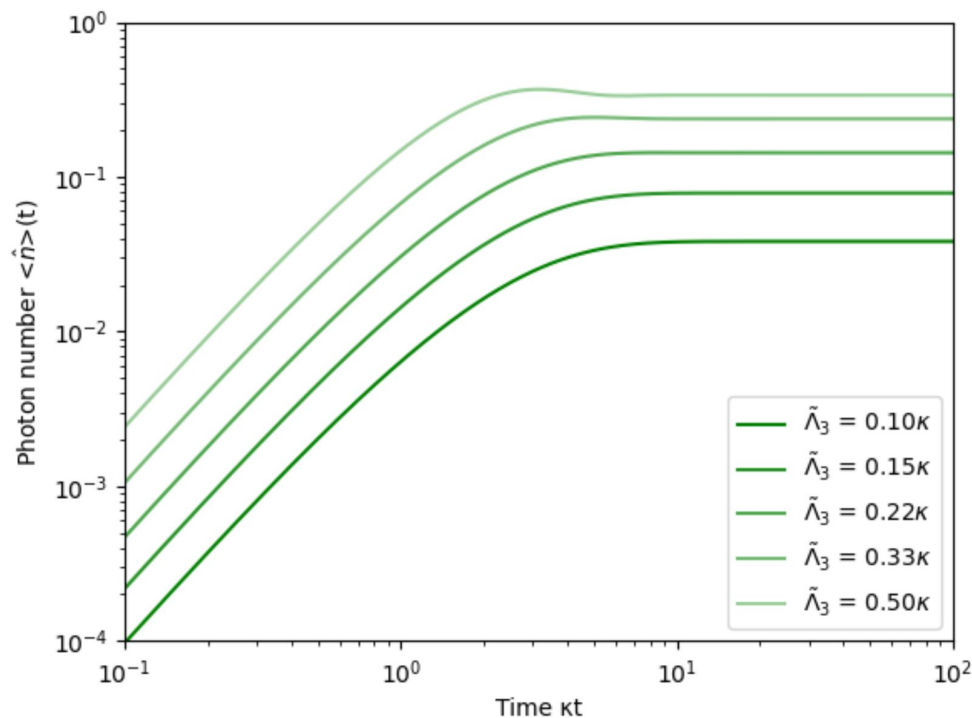
Simulation of Mismatched Drive Amplitude on Blockade Dynamics for Si cont.



Blockade Dynamics with Weak $\tilde{\Lambda}_3$ drive for Si

- Parameters used for simulation:

- $\kappa = 1$ MHz
- $U = 0.705$ MHz
- $N = 60$ states



Conclusion/Future Prospects

- Implement this in a lab setting
- Write paper discussing results



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References

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- [2] Sara Ferretti and Dario Gerace Phys. Rev. B **85**, 033303
- [3] M. Fox, *Quantum Optics: An Introduction* (Oxford University Press)