

# Magnetic Mapping for the ${}^6\text{He}$ Experiment

## REU Final Presentation

Jessie Thwaites<sup>1</sup>  
Mentor: Alejandro García<sup>2</sup>

<sup>1</sup>College of Saint Benedict/Saint John's University

<sup>2</sup>CENPA, University of Washington

15 August 2018

# Outline

- 1 Motivation
- 2 Background
  - Weak Interaction
  - Helicity and Chirality
  - Fierz Interference
- 3 My Contribution
  - Gadget
  - Multipole Expansion
- 4 Discussion
- 5 Further Investigation

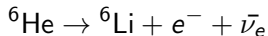
# Motivation

- Search for Beyond the Standard Model (BSM) physics through precision experiment
- predicted by other theories: supersymmetry, Grand Unified Theories

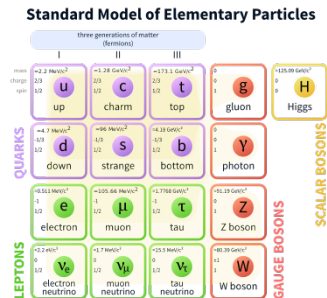


# Background - Weak Interaction

- Weak interaction - fundamental force
- responsible for  $\beta$  decay



- mediated by  $W^-$  boson
- new physics: interactions



# Background - Parity Violation

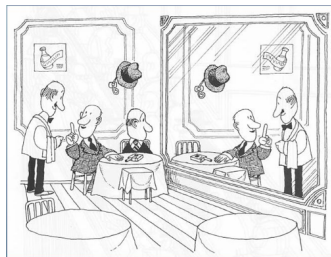
- *Parity* is the inversion of spatial coordinates

$$(ct, x, y, z) \rightarrow (ct, -x, -y, -z)$$

$$\hat{P}\vec{r} = -\vec{r}$$

$$\hat{P}\vec{L} = (-\vec{r}) \times (-\vec{p}) = \vec{r} \times \vec{p}$$

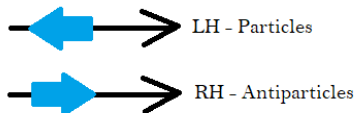
- Parity shows symmetry under the inversion of spatial coordinates
- with parity: expected both right- and left-handed particles
- Chien Sheng-Wu 1957 - left-handed particles only



# Helicity and Chirality

Helicity:

$$H = \frac{\vec{p} \cdot \vec{s}}{|\vec{p}||\vec{s}|} = \pm 1$$



Helicity *not* Lorentz invariant  
→ solution: define *Chirality*

$$e^L = \sqrt{\frac{1+\frac{p}{E}}{2}} e^{H=-1} + \sqrt{\frac{1-\frac{p}{E}}{2}} e^{H=+1}$$

$$e^R = \sqrt{\frac{1-\frac{p}{E}}{2}} e^{H=-1} + \sqrt{\frac{1+\frac{p}{E}}{2}} e^{H=+1}$$

$$e^R e^L = \sqrt{1 - \left(\frac{p}{E}\right)^2} = \frac{m}{E}$$

# Interaction Hamiltonian

Interaction Hamiltonian for  ${}^6\text{He}$  beta decay:

$$H_{int} = \bar{\psi}_f \gamma^\mu \gamma_5 \psi_i (2C_A e^{-L} \gamma_\mu \gamma_5 \nu_e^L) +$$

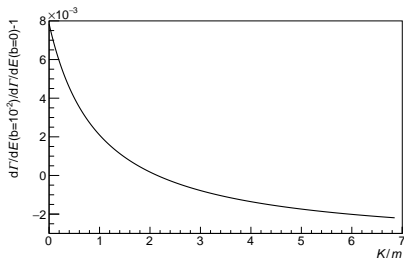
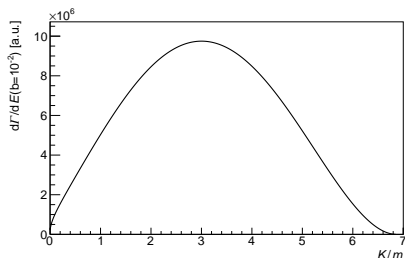
$$\bar{\psi}_f \sigma^{\mu\nu} \psi_i [(C_T - C'_T) e^{-L} \sigma_{\mu\nu} \nu_e^R + (C_T + C'_T) e^{-R} \sigma_{\mu\nu} \nu_e^L]$$

Search for tensor currents ( $\sigma_{\mu\nu}$ )

# Chirality-flipping - Fierz Interference

- terms that include RH & LH are chirality flipping
- show small distortions to spectrum

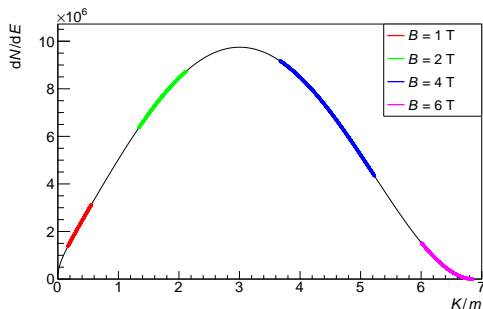
$$dW = dW_0 \left( 1 + a \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + b \frac{\Gamma m_e}{E_e} \right)$$
$$b \approx \frac{(C_T + C_T')}{C_A}$$





# Measuring the $\beta$ spectrum - CRES technique

- need precision measurements of the entire spectrum
- 6 GHz bandwidth, tune magnet
- Cyclotron Radiation Emission Spectroscopy (Project 8)



$$\omega_c = \frac{qBc^2}{E_e}$$

# *My Contribution*

## Magnetic Modeling

1. adapt NMR probe
2. multipole expansion
3. position mapping

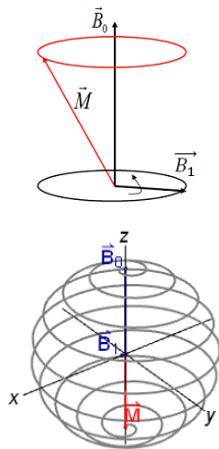
# The Gadget

Place the probe in the magnet at a particular location  $(\hat{r}, \hat{\theta}, \hat{z})$



# Nuclear Magnetic Resonance (NMR) Principles

- start with a sample in a magnetic field,  $B_0$
- perturb with a small oscillating field,  $B_1$
- at resonance, induces an energy transition by flipping magnetization
- produces a strong signal at this frequency - characteristic of magnetic field seen by nucleus
- use this magnitude measurement & fit to multipole expansion



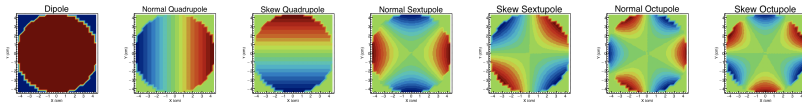
# Multipole Expansion

Laplace's Equation:

$$\nabla^2 \phi_m = 0$$

Solutions: Taylor Expansion with spherical harmonics:

$$\phi_m = \sum_{l=0}^{\infty} \sum_{m=-l}^l (a_l^m r^l + b_l^m r^{-(l+1)}) Y_l^m$$

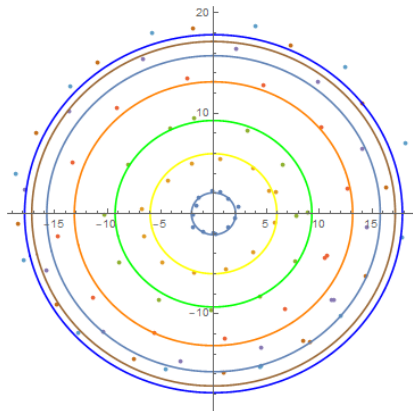


# Theodolite Mapping



- accurate position measurements for probe
- position accuracy impacts accuracy of Linear Least Squares fit in code

## Position mapping: $z=-20$ cm



- Mean  $(x,y)$  values for set  $r$
- colors show  $r$ -value
- Additional measurements:  $z=0$  and  $z=+20$  cm (not yet finished)

# Future Investigation

- Finish position mapping of magnet
- Automate gadget & Teslameter data collection process
- Improvements on multipole model



# Acknowledgements

- NSF and INT REU Program
- Dr. Alejandro Garcia and his group
- Deep, Gray, Cheryl and Linda



## References

- [1] A. Abragam. *Principles of Nuclear Magnetism*. Clarendon Press, 1961.
- [2] D. M. Asner, R. F. Bradley, L. de Viveiros, P. J. Doe, J. L. Fernandes, M. Fertl, E. C. Finn, J. A. Formaggio, D. Furse, A. M. Jones, J. N. Kofron, B. H. LaRoque, M. Leber, E. L. McBride, M. L. Miller, P. Mohanmurthy, B. Monreal, N. S. Oblath, R. G. H. Robertson, L. J. Rosenberg, G. Rybka, D. Rysewyk, M. G. Sternberg, J. R. Tedeschi, T. Thuemmler, B. A. VanDevender, and N. L. Woods (Project 8 Collaboration). Single-Electron Detection and Spectroscopy via Relativistic Cyclotron Radiation. *Phys. Rev. Lett.*, 114(16), Apr. 2015.
- [3] C. Boettcher. *Theory of Electric Polarization*. Elsevier Publishing Co., 1952.
- [4] M. Fertl, B. Graner, A. Garcia, M. Guigue, D. Hertzog, P. Kammel, A. Leredde, P. Mueller, N. S. Oblath, R. G. H. Robertson, G. Rybka, G. Savard, D. Stancil, H. E. Swanson, B. A. VanDevender, and A. Young. Detection of cyclotron radiation applied to searches for chirality-flipping interactions. *Not yet published*, 2018.
- [5] R. Hong, M. G. Sternberg, and A. Garcia. Helicity and nuclear beta decay correlations. *Am. J. Phys.*, 85(45), 2017.